A Two-Dimensional Weighting Function for a Driver Assistance System

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Abstract—Driver assistance systems that supply force feedback (FF) on the accelerator commonly use relative distance and velocity with respect to the closest lead vehicle in front of the own vehicle. This 1-D feedback might not accurately represent the situation and can cause unwanted step-shaped changes in the FFs during lateral maneuvers. To address these shortcomings, a 2-D system is proposed that calculates FF using a weighted average of the influences of lead vehicles. Offline simulations and an experiment in a driving simulator were performed to compare no feedback, 1-D systems, and the novel 2-D system during a car-following task with cut-in maneuvers. Results show that the 2-D feedback resulted in lower mean forces, lower response times to cut-in vehicles, and favorable subjective experiences as compared to the 1-D systems.

Index Terms—Accelerator, driver assistance, force feedback (FF), weighting function.

I. INTRODUCTION

CARRIVING is principally a visual task, with the view outside the car as the main source of information. When drivers allocate their attention elsewhere, e.g., inside the car to tune their radio, very little information remains about the driving situation, resulting in increased accident risk. Providing force feedback (FF) on the accelerator may help overcome this issue. Accelerator FF informs the driver of impending hazards, while preserving the driver’s control over the accelerator. Previous studies have shown that—when using appropriate FF algorithms—car-following tasks can be performed with equal precision but with less accelerator movement [1], [2]. Moreover, through analyzing electromyographic activity of relevant muscles and modeling the human neuromusculoskeletal system, it was shown that part of the driver’s control actions with the “haptic” gas pedal were performed by spinal reflexes, resulting in faster responses and a reduction of visual workload [2].

The FF systems described in [1] and [2] operate in one dimension only. Feedback is based on the longitudinal distance and relative speed with respect to one—i.e., the closest—vehicle within range of the (virtual) sensor system. One-dimensional feedback can induce unwanted effects when more than one vehicle is ahead of the own vehicle. Step-shaped changes in the FFs have been found to occur during lateral maneuvers, such as cut-ins. Unwanted reflexes, excessive wear of hardware, and timing problems associated with the balance between false alarms and missed detections are likely disadvantages of feedback discontinuities [1], [3].

One problem of 1-D feedback can easily be remedied. By applying a filter, for example, limiting the rate of change of feedback, these feedback discontinuities cannot occur anymore. However, in doing so, feedback is still 1-D, which might not accurately represent the driver’s perception of risk and could therefore lead to suboptimal driver comfort.

The goal of this paper is to develop and evaluate a solution for the limitations of 1-D feedback. A 2-D system is proposed that uses a weighted average of lead vehicles in calculating feedback. Indeed, the psychologically relevant aspects of car driving have often been represented in a 2-D fashion. Examples are the “field of safe travel” metaphor [4], a tube in which drivers operate [5], or a fan-shaped “committed zone” ahead of the own vehicle [6]. Two-dimensional potential-field methods have been proposed in the context of guiding vehicles [7]–[10]. We found these methods to be less suitable, however, because they either do not address the case of multiple vehicles or they superpose the influence of each vehicle, which leads to an overestimation of risk.

Our solution in calculating a weighted average can be interpreted as an intermediate solution between, on the one hand, the 1-D system that considers the lead vehicle having maximum importance, and on the other hand, existing 2-D systems that superpose the influences of all lead vehicles. In the following, our 2-D feedback system will be discussed and compared with some existing 1-D solutions.

II. FF SYSTEMS

Five FF solutions were evaluated: no feedback (NF), a 1-D system (1D), a rate-limited 1D system (1DR), a 2-D supersothing system (2DS), and the weighted 2-D system (2DW). These five systems are described as follows.

NF A normal accelerator without FF is used. The driver can only rely on visual information.

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1D FF is applied according to (1), shown at the bottom of the next page. This equation is based on [11] and has been developed to correctly correspond with a driver’s perception of risk. FF is a continuous function of the time headway (THW, in seconds), time-to-collision (TTC, in seconds), and throttle position ($\alpha$ in percent). In this paper, THW is defined as the distance from the front bumper of the own vehicle to the rear bumper of the lead vehicle divided by the speed of the own vehicle. TTC is defined as the distance from the front bumper of the own vehicle to the rear bumper of the lead vehicle divided by the relative speed between the lead vehicle and the own vehicle (defined as positive if the gap closes). For 1D, THW and TTC are considered with respect to only the nearest vehicle. FF is calculated for each lead vehicle and added together so that a resultant FF is obtained. 

1DR This is identical to 1D but, here, FF is rate-limited at 20 N/s. It can be considered a “quick-and-dirty” solution to prevent discontinuities in the FF. The limit of 20 N/s was considered subjectively comfortable during exploratory runs with experienced drivers in a driving simulator.

2DS Here, all vehicles within the 4-m-wide area in front of the own car contribute to FF when being visible from the center of the front bumper of the own vehicle. FF is calculated for each lead vehicle and added together so that a resultant FF is obtained.

2DW A weighted average of THW and 1/TTC is calculated. Here, a weighted THW and weighted 1/TTC (rather than THW and 1/TTC with respect to only the nearest vehicle) are used to calculate FF, still using (1). The remainder of this section will be devoted in describing how vehicles are weighted.

The weight that is assigned to a particular vehicle depends on the position of its rear bumper in an egocentric weight field. The weight field is shown in Fig. 1 and is described mathematically in (2)–(5), shown at the bottom of this page. In (2)–(5), the following notations are used.

1) $x$ is the longitudinal road-fixed coordinate, in meters.
2) $y$ is the lateral road-fixed coordinate, in meters.
3) $W(x, y)$ is the weight for a particular coordinate.
4) $x_b$ is the longitudinal boundary of the weight field, in meters.
5) $y_b$ is the lateral boundary of the weight field, in meters.
6) $\theta$ is the angle of a coordinate with respect to the front bumper.
7) $r$ is half the own-vehicle width (0.915 m, in our case).
8) $\rho$ ($= 0.5$) is a constant influencing the longitudinal weight distribution.
9) $V$ is the speed of the own vehicle, in meters per second.
10) $u$ is half the weight field width (2.0 m, in our case).
11) $s$ ($= 0.11/\text{s}$) and $t$ ($= 2.0 \text{ m/s}$) are constants that depend on the car dynamics and define the parabolic shape of the weight field.

$$FF = \begin{cases} 0, & \text{for } |y| < y_b, \ x \leq x_b, \ x \leq 0 \\ 0, & \text{for } |y| > y_b \\ 44.2, & \text{for } |y| \leq r \\ (9.66 + 0.077 \alpha) \cdot \left(\frac{1}{THW} + \frac{\rho}{TTC}\right)^{0.898}, & \text{otherwise} \end{cases}$$

$$W(x, y) = \begin{cases} 0, & \text{for } |y| \geq y_b, \ x \geq x_b, \ x \leq 0 \\ (x_b - x)^3 \cdot \cos(\theta), & \text{for } r < |y| < y_b \\ (x_b - x)^3, & \text{for } |y| \leq r \end{cases}$$

$$\theta = \frac{\pi}{2} \arctan \left(\frac{|y| - r}{x}\right)$$

$$x_b = 2.5 \cdot V$$

$$y_b(x) = \begin{cases} r + (s/V)x^2 + (t/V)x, & \text{for } r + (s/V)x^2 + (t/V)x < u \\ u, & \text{for } r + (s/V)x^2 + (t/V)x \geq u \end{cases}$$

Fig. 1. Weight field for a speed of 100 km/h. The center of the own vehicle’s front bumper is situated at (0,0). A linear grayscale is used (black corresponds to zero weight, and white corresponds to maximum weight at $x = 1 \text{ m}$).
Fig. 2. Weighting of vehicles. Weight is assigned to (parts of) rear bumpers in the weight field that are in the line of sight of the center of the own vehicle’s front bumper.

As shown in Fig. 2, parts of the rear bumpers of all vehicles in front, lying within the weight field and visible from the center of the own vehicle’s front bumper, are included.

The weight field is continuous within its boundaries and is zero beyond. Hence, the weight assigned to vehicles moving within, into, or out of the weight field is always continuous, thereby avoiding discontinuous step-shaped changes in the FF during lateral maneuvers of the vehicles in front or of the own vehicle.

The broadening boundaries in front of the own vehicle (for longitudinal distances smaller than 10 m) represent the contours of the reachable area. The width of the weight field was set at 4.0 m. When assuming that lane keeping of both the own vehicle and lead vehicles is a normally distributed process with an average corresponding to the lane center and a standard deviation of 0.30- and 3.6-m-wide lanes, this would result in a relatively low chance (5.3%) that weight is assigned to a part of a vehicle passing on another lane. It can be seen in (4) that the weight field elongates for higher velocities. Thus, the weight distribution between two lead vehicles remains constant when following with constant THW at varying speeds.

III. OFFLINE SIMULATIONS

Offline simulations were performed to test the five alternatives for FF introduced above. A cut-in maneuver was simulated, as shown in Fig. 3. The own vehicle followed a lead vehicle at a THW of 1.25 s, and a second lead vehicle cut-in from the left adjacent lane at a THW of 0.5 s. Its lateral motion was sinusoidal, with a lane change time of 6 s [12] and a lane change distance of 3.6 m. All lead vehicles had a length of 4.0 m and a width of 1.8 m.

First, an open-loop simulation was performed which assumed that the driver keeps the accelerator at a constant position. The results (FF versus time) are shown in Fig. 4. The FF was equal for each condition during the beginning and at the end of the cut-in, because the systems function identically when only one vehicle is visible from the own vehicle’s front bumper. For 1D, a sudden change in FF occurred at the moment the other lead vehicle became the closest vehicle within the 4-m-wide area. For 1DR, the change in feedback occurred at the same moment as with 1D, but the rate of change is limited to 20 N/s. 2DS induced a high amount of feedback when both vehicles were visible, an undesirable effect as the forces on the pedal may become too large. 2DS has therefore been discarded in the remainder of this paper. As with 1DR, the 2DW solution assured continuous feedback, i.e., no step-shaped changes were found. Feedback increased relatively late for 2DW as a result of the fact that it represents a weighted average of both lead vehicles. Mean FF was lowest for 2DW.

Second, a closed-loop simulation was performed using the same cut-in maneuver and feedback conditions as above (except for the 2DS). The driver was modeled as a linear controller with the goal to (visually) maintain a THW of 1.25 s and with a proportional control strategy (gain of 100, from weighted THW error in seconds to applied muscle force in newtons) and a time delay of 0.5 s. FF was modeled to only passively influence the position of the driver’s foot. The neuromuscular behavior of the foot was modeled as a mass (2.5 kg)-spring (200 Nm/rad)-damper (5 Nm · s/rad) system. The distance between the foot contact
point at the accelerator and its rotation point was 0.20 m. Throttle position, with a range of 20°, served as input to the longitudinal model of the own vehicle (mass of 1600 kg, maximum engine power of 148 kW). Initial speed was 100 km/h.

Results (throttle positions versus time since the start of the maneuver) are shown in Fig. 5. Around 2.0 s, the cut-in vehicle entered the 4-m-wide area, resulting in an immediate response for 1D followed by a small oscillation attributable to the springlike properties of the foot, indicating that a step-shaped increase of FF indeed may cause an unwanted response. The initial responses for 2DW and NF were the slowest because FF lagged behind or was absent. At approximately 7 s, the modeled driver depressed the accelerator to start following the cut-in vehicle.

IV. DRIVING-SIMULATOR EXPERIMENT

A driving-simulator experiment was performed to examine the actual human response to the feedback systems.

A. Method

Apparatus: The experiment was conducted in a fixed-base driving simulator, equipped with an actuated accelerator, a brake pedal, a steering wheel, and a digital dashboard display showing engine revolutions per minute and vehicle speed. The driving scene was projected on the laboratory wall, 2.9 m in front of the driver. The resolution of the projected image was 1024 × 768 pixels, and the size was 3.3 m × 2.4 m.

Subjects and Instructions: There were 14 subjects, 12 males and 2 females, aged 23 to 51, that participated. The mean duration of driver-license possession was 10.6 years, the mean self-estimated driving frequency per week was 4.4 h, and the mean driving frequency per week was 20 equal intervals. The questionnaire included the NASA Task Load Index (TLX) for assessing subjective workload [14] and four additional questions. All dependent measures were calculated for each run. Factor analysis was performed to cluster the measures into unique factors. This way, four useful factors were obtained. For each factor, two or three (intercorrelating) measures representing the factor were selected. Additionally, after each run, subjects were presented with questionnaires on a laptop computer. For each question, subjects could adjust a slider, which was divided into 20 equal intervals. The questionnaire included the NASA Task Load Index (TLX) for assessing subjective workload [14] and four additional questions. All dependent measures are shown in Table I. Subjects had the opportunity to comment on the answers to the four additional questions in textboxes.

B. Results

One data file (subject ten, 1D condition) was corrupted and excluded from the analysis. Table II shows the results of the dependent measures for the four accelerator systems.

Braking and Steering Activity: Individual differences were relatively large with respect to braking and steering activity. However, no significant differences were observed between the four feedback conditions.

Following Distance and Precision: No significant differences were found between 2DW and the other conditions.

Throttle Activity: No significant differences were found for throttle activity. Throttle activity was slightly higher for NF as expected from earlier research [1].

Forces: The means and standard deviations of FF were significantly lower for 2DW as compared to 1D and 1DR.
TABLE I
DEPENDENT MEASURES

<table>
<thead>
<tr>
<th>1. Braking and Steering Activity</th>
<th>SD BrakeForce (N)</th>
<th>35.5</th>
<th>31.6</th>
<th>35.6</th>
<th>32.7</th>
</tr>
</thead>
<tbody>
<tr>
<td>SD Steer (deg)</td>
<td>1.05</td>
<td>1.04</td>
<td>1.05</td>
<td>1.04</td>
<td></td>
</tr>
<tr>
<td>2. Following Distance and Precision</td>
<td>M THW (m)</td>
<td>1.37</td>
<td>1.53</td>
<td>1.49</td>
<td>1.48</td>
</tr>
<tr>
<td>SD THW (m)</td>
<td>0.48</td>
<td>0.55</td>
<td>0.52</td>
<td>0.49</td>
<td></td>
</tr>
<tr>
<td>3. Throttle Activity</td>
<td>SD Throttle (%)</td>
<td>25.6</td>
<td>24.5</td>
<td>24.5</td>
<td>24.5</td>
</tr>
<tr>
<td>SD RPM (RPM)</td>
<td>495</td>
<td>453</td>
<td>460</td>
<td>456</td>
<td></td>
</tr>
<tr>
<td>ThrottleReleased (%)</td>
<td>25.7</td>
<td>24.8</td>
<td>23.8</td>
<td>24.1</td>
<td></td>
</tr>
<tr>
<td>4. Forces</td>
<td>M FF</td>
<td>X</td>
<td>11.9</td>
<td>11.7</td>
<td>10.3</td>
</tr>
<tr>
<td>SD FF</td>
<td>X</td>
<td>6.7</td>
<td>5.4</td>
<td>4.3</td>
<td>*** <em>(1D,1DR)</em>*</td>
</tr>
<tr>
<td>5. Subjective Experience</td>
<td>TLX (5-100)</td>
<td>36</td>
<td>50</td>
<td>47</td>
<td>42</td>
</tr>
<tr>
<td>Safety (1-20)</td>
<td>9</td>
<td>8.5</td>
<td>10</td>
<td>12.5</td>
<td>** <em>(NF,1D)</em>*</td>
</tr>
<tr>
<td>Comfort (1-20)</td>
<td>9.5</td>
<td>7</td>
<td>6.5</td>
<td>13.0</td>
<td>** <em>(1D,1DR)</em>*</td>
</tr>
<tr>
<td>Pleasure (1-20)</td>
<td>11</td>
<td>7.5</td>
<td>8</td>
<td>11</td>
<td></td>
</tr>
<tr>
<td>Correspond (1-20)</td>
<td>1</td>
<td>7.5</td>
<td>11</td>
<td>15</td>
<td>*** <em>(NF)</em>*</td>
</tr>
</tbody>
</table>

Means of subjects were evaluated by a repeated measures analysis of variance (ANOVA). When equal variances could not be assumed, medians were evaluated by a Friedman test. *** p < 0.001, ** 0.01 ≤ p < 0.05. A Tukey-Kramer multiple comparison was performed to evaluate whether 2DW differed from other conditions at a 95% confidence level (shown between parentheses).

Subjective Experience: Subjective workload (TLX), safety, and comfort were more favorable for 2DW as compared to 1D, a significant effect. The correspondence between FF and visual information was rated highest for 2DW. Analysis of the written comments revealed that five of 14 subjects had reported that 2DW felt comfortable as compared to two subjects who reported this characteristic for the other conditions.

There are 11 subjects who drove with 1D that reported that they had received feedback that they could not explain or feedback from the wrong car, particularly from overtaking vehicles driving on the other lane. Three subjects reported the 1D feedback to be “aggressive” or “discontinuous.” NF yielded relatively low scores on the TLX and good scores on the subjective pleasure question. Four subjects reported to be satisfied at being in full control in the absence of any feedback. Five subjects reported to be annoyed at not being in full control when driving with FF.

The responses to cut-ins were analyzed in further detail because the conditions only differ from each other when multiple vehicles are considered. Fig. 6 shows the averaged throttle position of all cut-ins versus time since the start of the cut-in. Subjects released the accelerator soonest for 2DW. A repeated-measures analysis of variance (ANOVA) with Tukey–Kramer multiple comparison indicated that the mean throttle position at 2 s after the start of the cut-in was significantly lower for 2DW as compared to 1D ($p = 0.01$). Fig. 7 shows the averaged THW of all cut-ins. It can be seen that THW is lowest for NF and highest for 1D. The mean THW of 1DR and 2DW closely resemble. Fig. 8 shows the averaged FF. As could be expected from the simulations, FFs were lower and increased later for 2-DW as compared to 1D and 1DR.

V. CONCLUSION

In this paper, a 2-D FF system was proposed that calculates feedback using a weighted average of vehicles in front of the own vehicle. It provides a solution to what are considered the two main problems with conventional 1-D approaches. First, it eliminates the occurrence of discontinuous accelerator
movements that are caused by sudden changes of what the system considers to be the lead vehicle. Second, as it is based on a weighted contribution of all lead vehicles, depending on their relative risk, its behavior better matches the driver’s expectations. This research can be applied to also improve other 1-D systems, such as adaptive cruise control. It is recommended to investigate whether the concept of “risk weighting” in providing FF can be generalized to other applications, like teleoperation.

REFERENCES


Max Mulder received the M.Sc. and Ph.D. (cum laude) degrees in aerospace engineering from the Delft University of Technology, Delft, The Netherlands in 1992 and 1999, respectively. His Ph.D. dissertation focused on the cybernetics of tunnel-in-the-sky displays. He is currently an Associate Professor with the Department of Control and Simulation, Faculty of Aerospace Engineering, Delft University of Technology. His research interests include cybernetics and its use in modeling human perception and performance, and cognitive systems engineering and its application in the design of ecological human–machine interfaces.

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