



**MSc Thesis in Geomatics**

# **Learning to Reconstruct Compact Building Models from Point Clouds**

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**Supervisors:**

Dr. Liangliang Nan

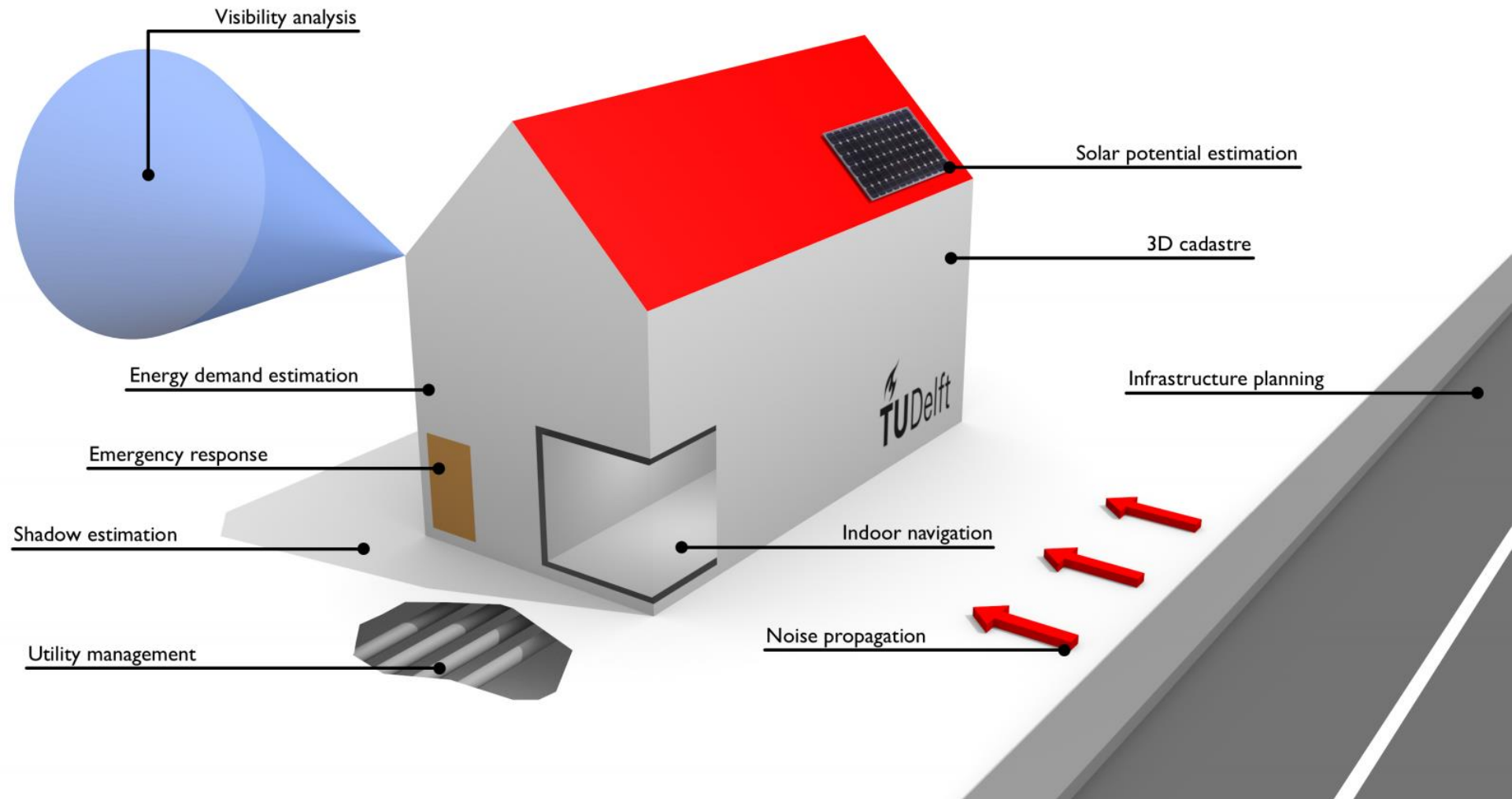
Dr. Seyran Khademi

**June 29, 2021**

- **Introduction**
- **Related work**
- **Methodology**
- **Datasets**
- **Results and discussion**
- **Conclusions**

- **Introduction**
- Related work
- Methodology
- Datasets
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# Introduction: 3D building models

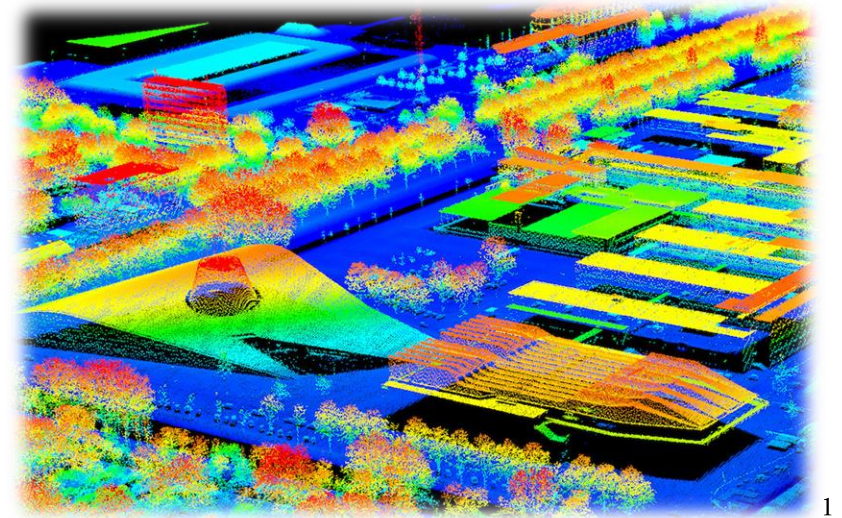


Applications of 3D building models [Biljecki et al., 2015]

# Introduction: Point clouds

## Acquisition of a point cloud

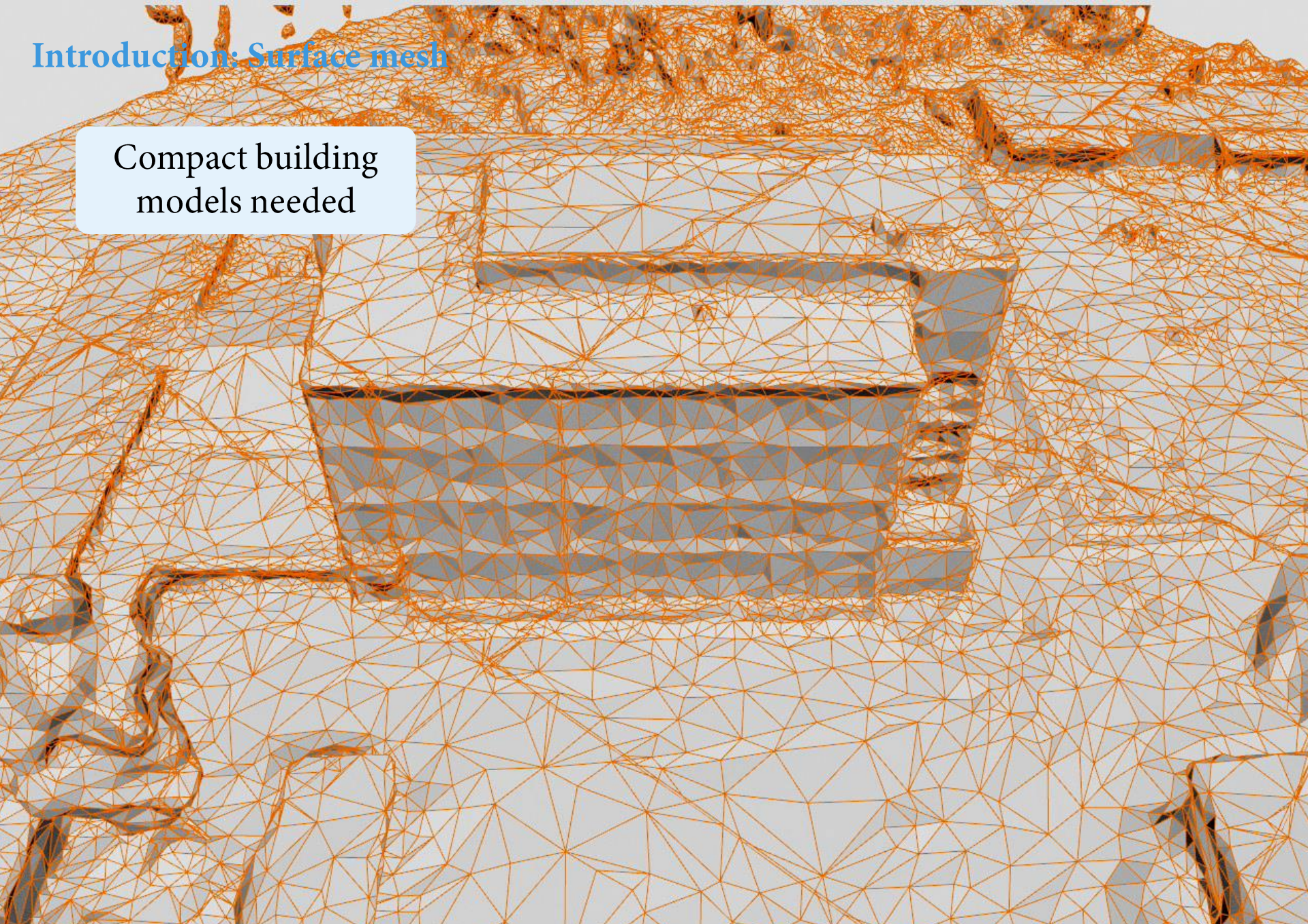
- Photogrammetry
- LiDAR (Light Detection and Ranging)



<sup>1</sup><https://www.tudelft.nl/bk/onderzoek/projecten/geoinformation-technology-governance>

## Introduction: Surface mesh

Compact building  
models needed



# Introduction: Piecewise planarity

## Piecewise-planar building models

- **Ubiquitous in the built environment**
- Capturing both geometry and topology with non-uniformity
- Compact, efficient with sparse sets of parameters

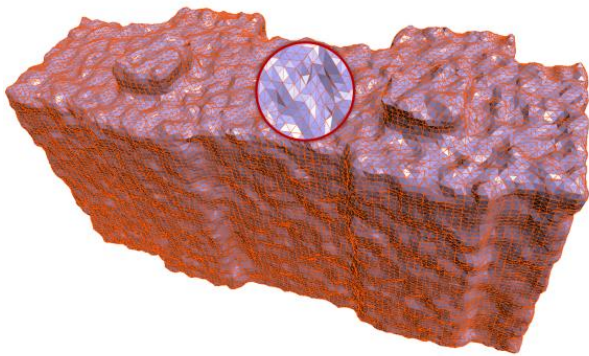


<sup>2</sup><https://www.tudelft.nl/bk/onderzoek/onderzoek-bij-bouwkunde/management-in-the-built-environment>

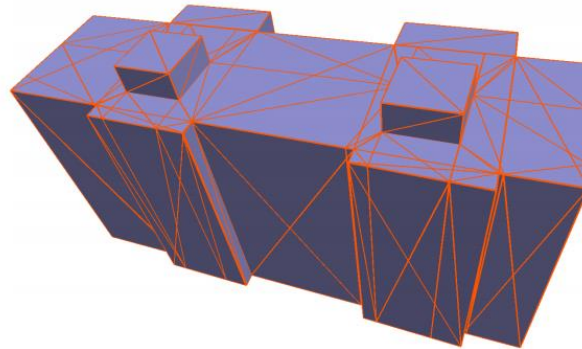
## Introduction: Piecewise planarity

### Piecewise-planar building models

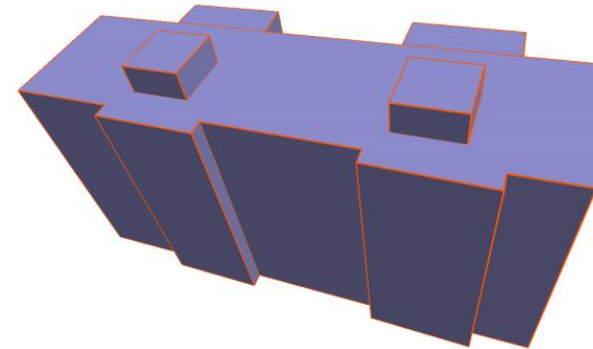
- Ubiquitous in the built environment
- **Capturing both geometry and topology with non-uniformity**
- **Compact, efficient with sparse sets of parameters**



Dense triangles (smooth)  
326,234 facets



Sparse triangles  
198 facets



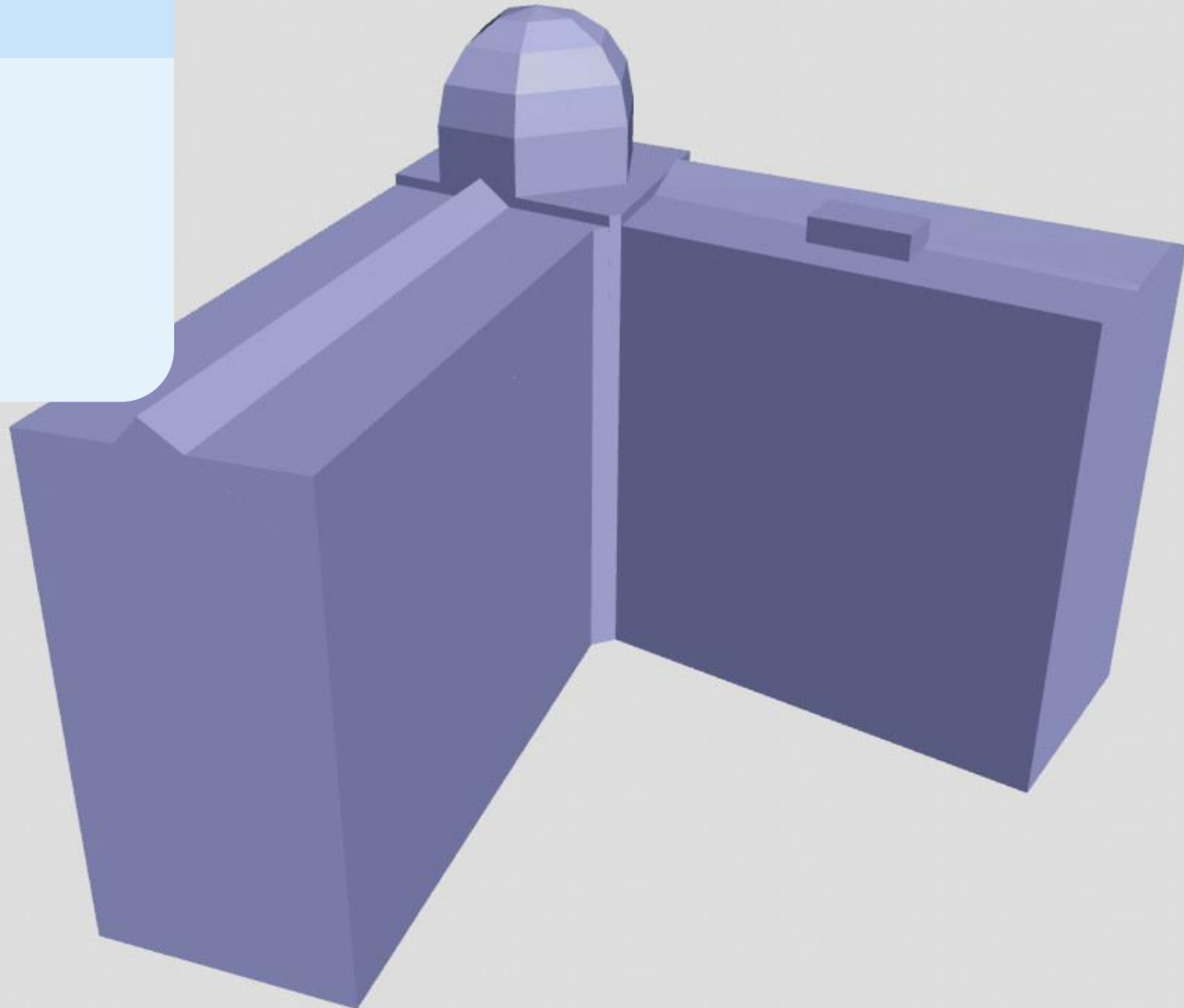
Sparse polygons  
61 facets



## Introduction: The *reconstruction* problem

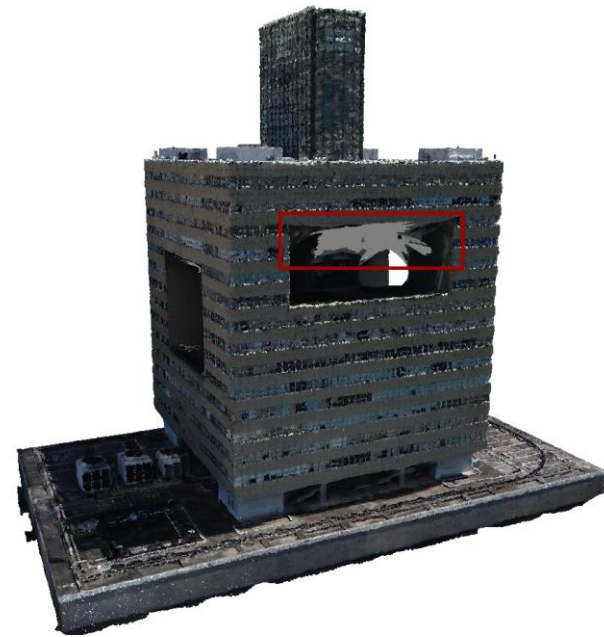
### The goal

- Compact
- Watertight
- Accurate
- Efficient

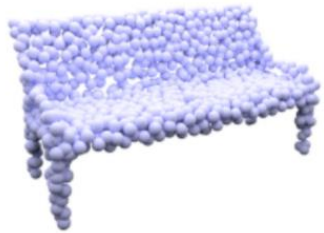
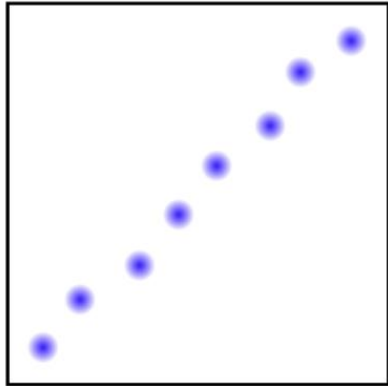


## Introduction: Challenges

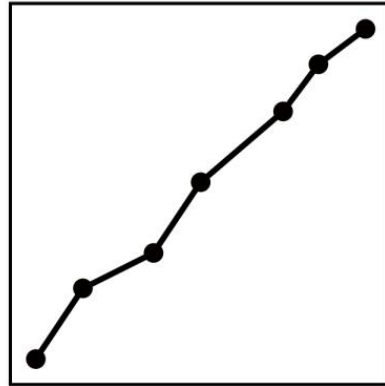
- Compactness, watertightness, efficiency
- **Limited input data quality**



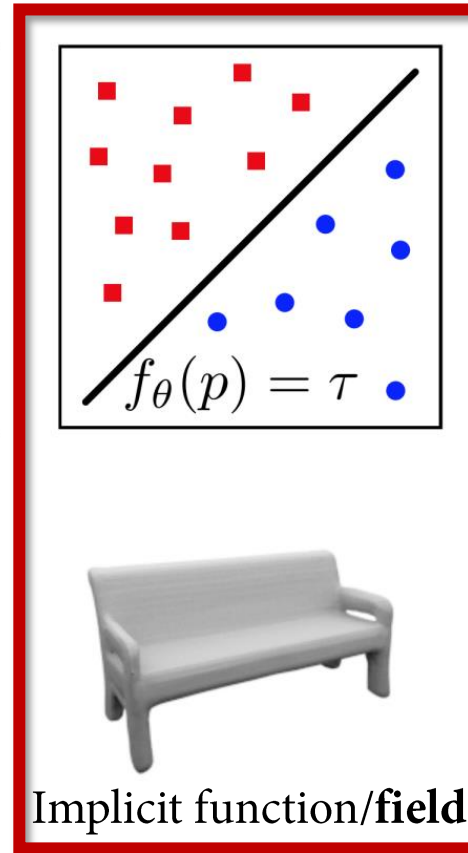
# Introduction: Inspiration and research question



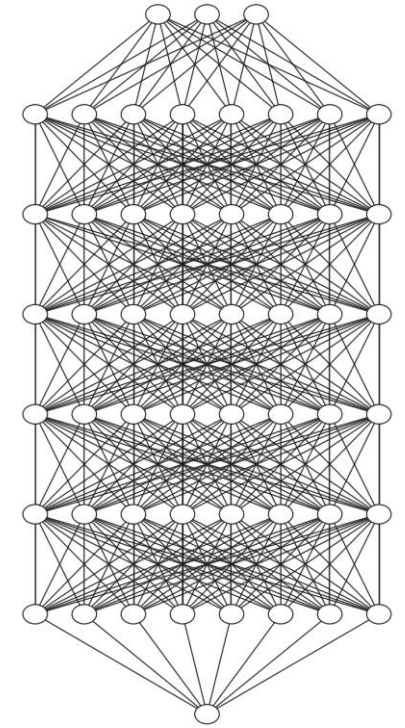
Point cloud



Surface mesh



Implicit function/field



Deep neural network

Shape representations [Mescheder et al., 2019]

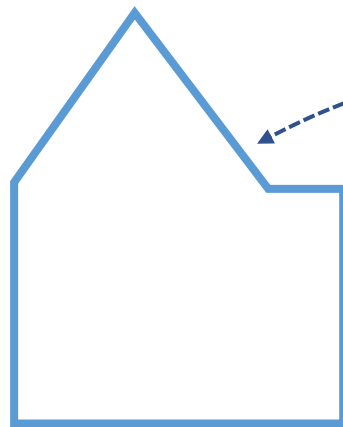
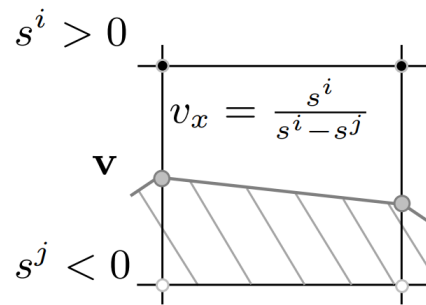
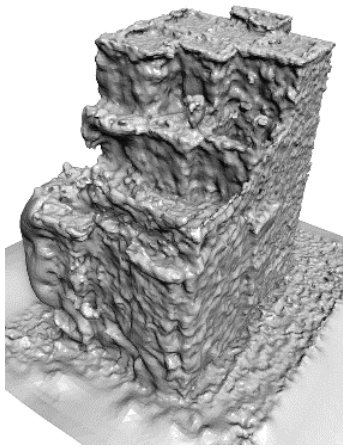
*How can deep implicit fields be used for compact building model reconstruction?*

- Introduction
- **Related work**
- Methodology
- Datasets
- Results and discussion
- Conclusions

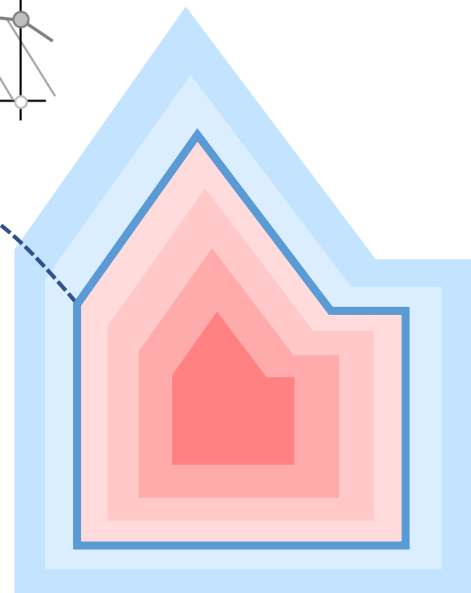
## Related work: Shape reconstruction (smooth)

- Poisson reconstruction [Kazhdan et al., 2006]
- Points2Surf [Erler et al., 2020]

**Massive triangles**



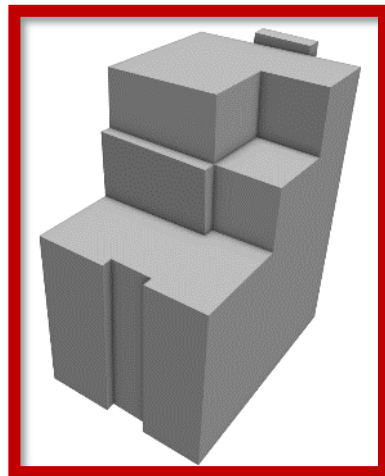
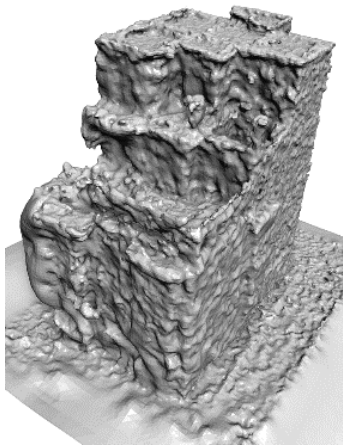
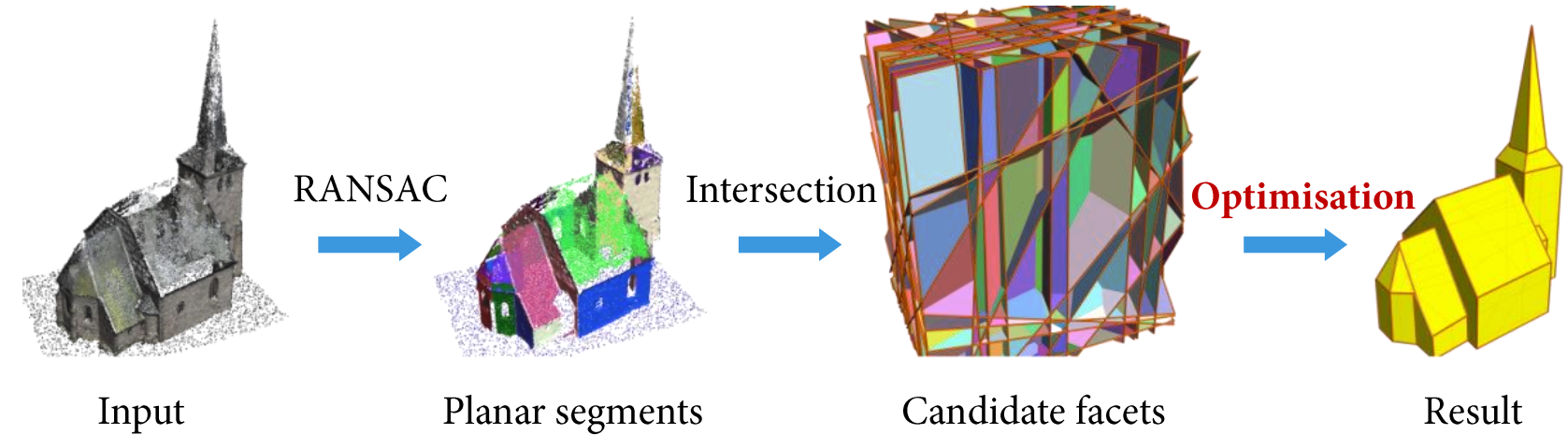
**Explicit  
(mesh)**



**Implicit**

## Related work: Shape reconstruction (piecewise-planar)

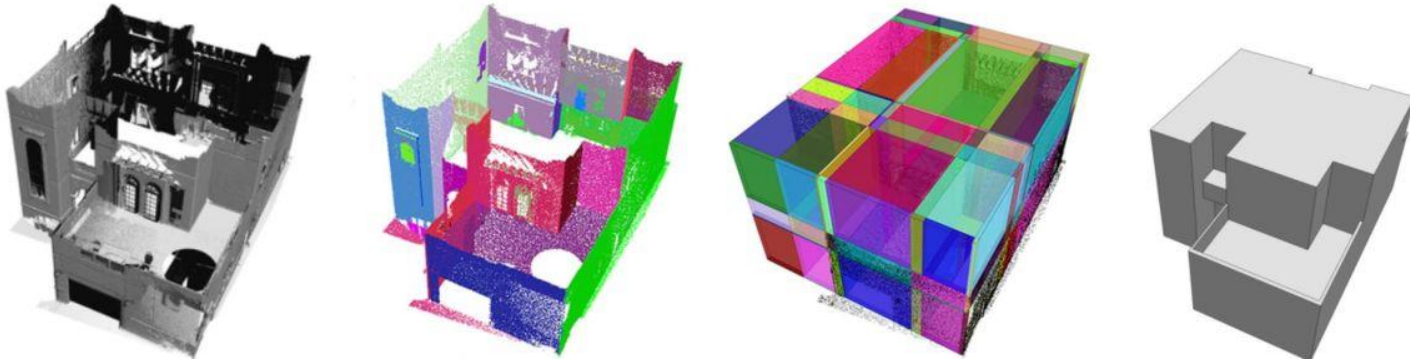
- PolyFit [Nan and Wonka, 2017]



**Scalability issue**  
**with its**  
**integer programming solver**

## Related work: Geometry simplification

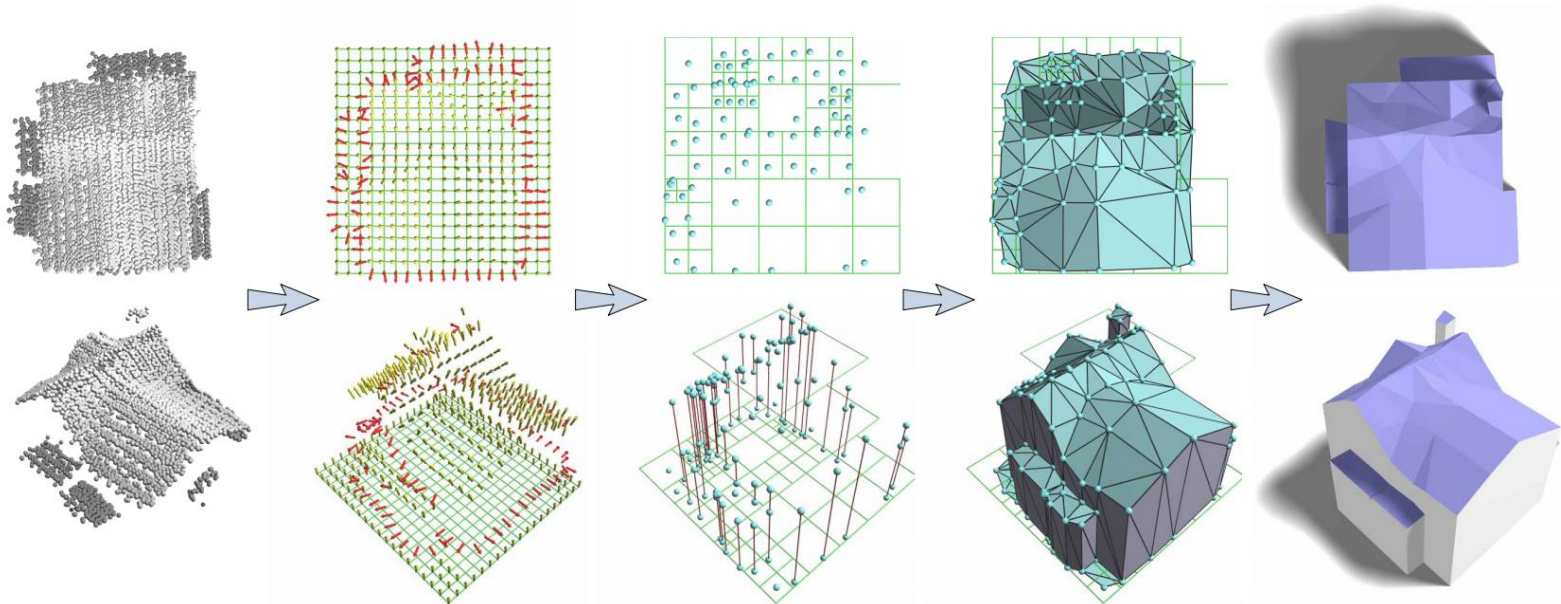
- **Manhattan-world reconstruction** [Li et al., 2016b]
- 2.5D Dual Contouring [Zhou and Neumann, 2010]



**Not generic with only boxes**

## Related work: Geometry simplification

- Manhattan-world reconstruction [Li et al., 2016b]
- **2.5D Dual Contouring** [Zhou and Neumann, 2010]

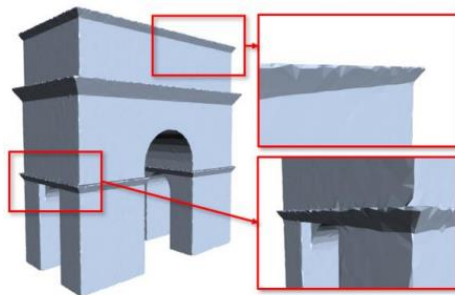


**Not generic with only 2.5D**

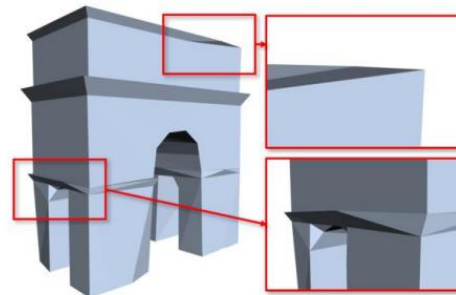


## Related work: Surface approximation

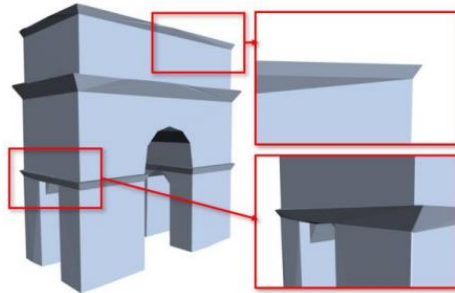
- Quadric error metrics (QEM) [Garland and Heckbert, 1997]
- Variational shape approximation (VSA) [Cohen-Steiner et al., 2004]
- Structure-aware mesh decimation (SAMD) [Salinas et al., 2015]



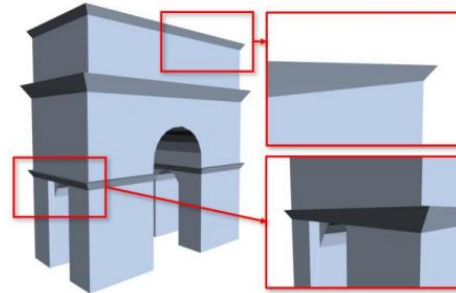
Input mesh  
(27,258 facets)



QEM  
(250 facets)



VSA  
(250 facets)



SAMD  
(250 facets)

**Dependent on  
input mesh**

[Bouzas et al., 2020]

## Related work: Summary

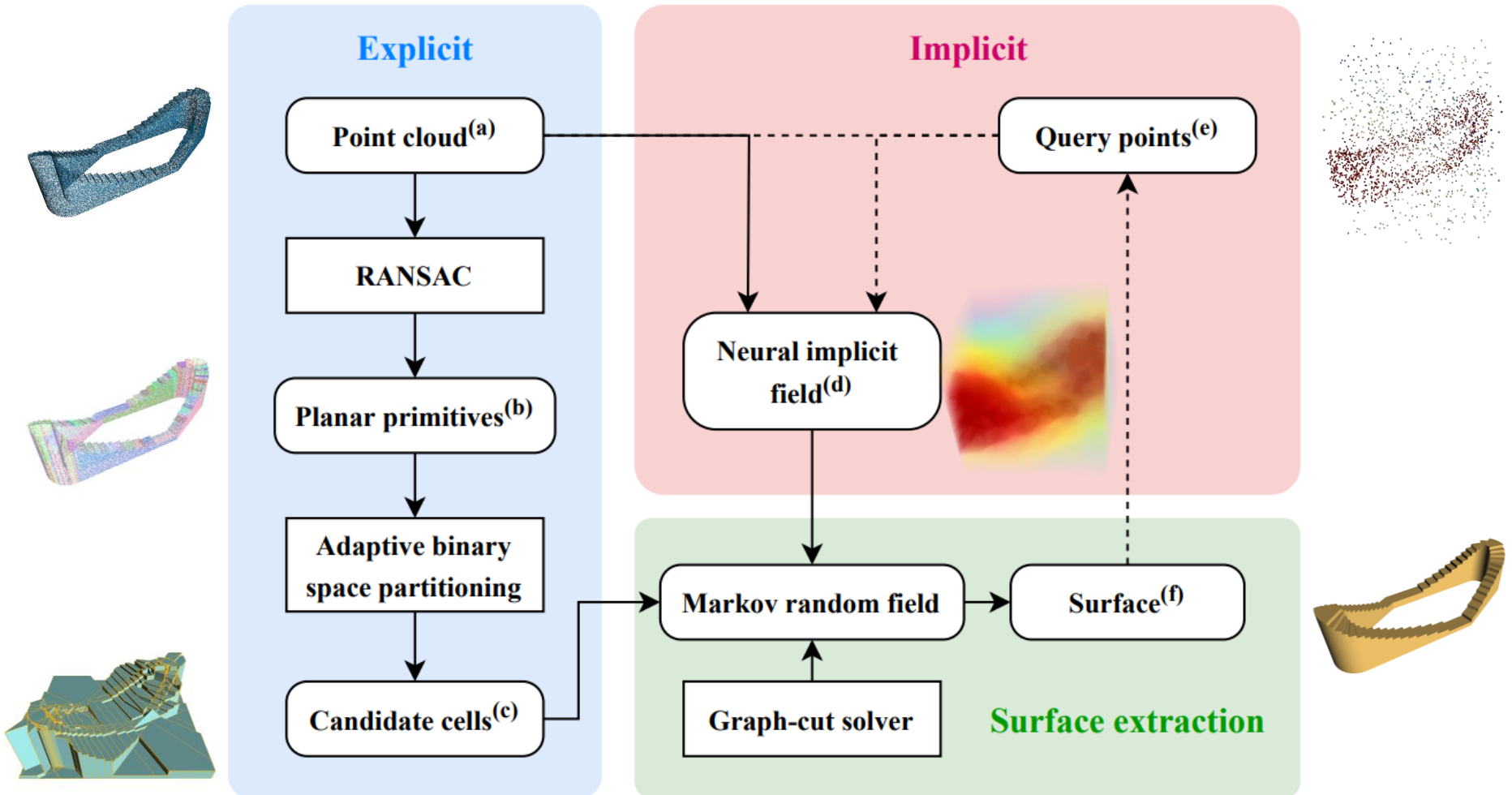
Related work	Characteristics				
	Name	Category	Compact	Watertight	Generic
Poisson [Kazhdan et al., 2006]	RC	✗	✗	✓	✓
Points2Surf [Erler et al., 2020]	RC	✗	✗	✓	✗
PolyFit [Nan and Wonka, 2017]	RC	✓	✓	✓	✗
QEM [Garland and Heckbert, 1997]	AP	✓	✗	✓	✗
SAMD [Salinas et al., 2015]	AP	✓	✗	✓	✗
VSA [Cohen-Steiner et al., 2004]	AP	✓	✗	✓	✗
Manhattan-world [Li et al., 2016b]	SP	✓	✓	✗	✓
2.5D DC [Zhou and Neumann, 2010]	SP	✗	✓	✗	✓
Ours	RC	✓	✓	✓	✓

Characteristics overview of related work<sup>3</sup>

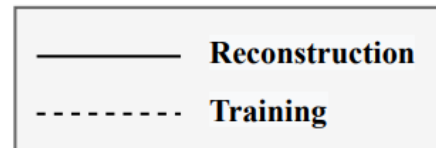
<sup>3</sup> Only methods in comparison through experiments (with official open-source code); See in the thesis a complete literature review

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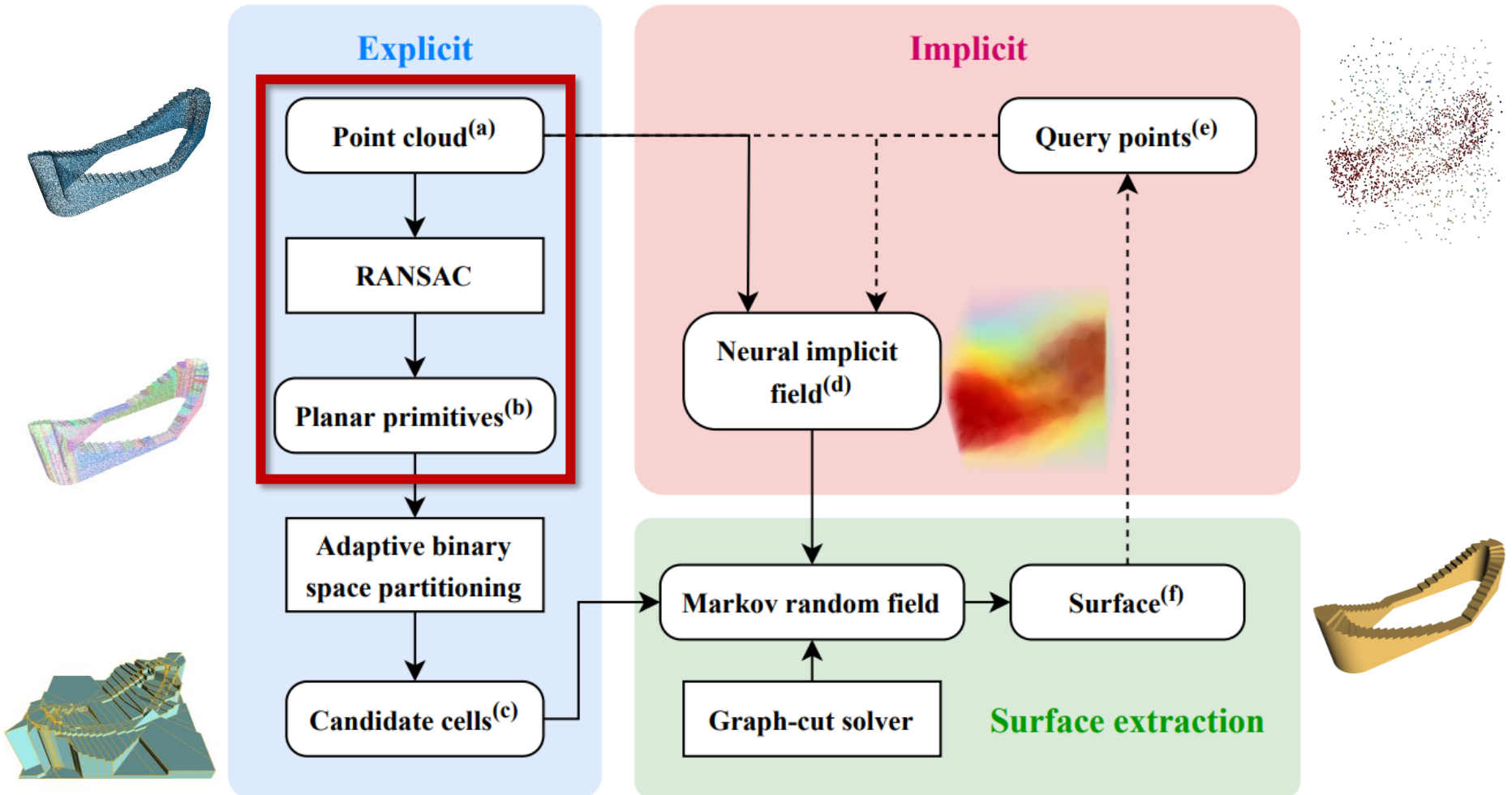
# Methodology: Overview



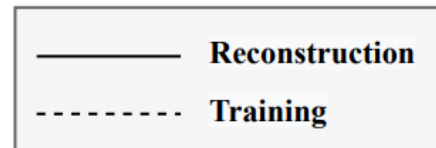
Overview of our framework



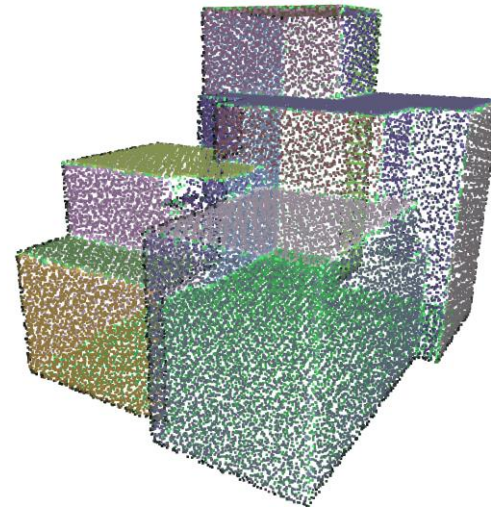
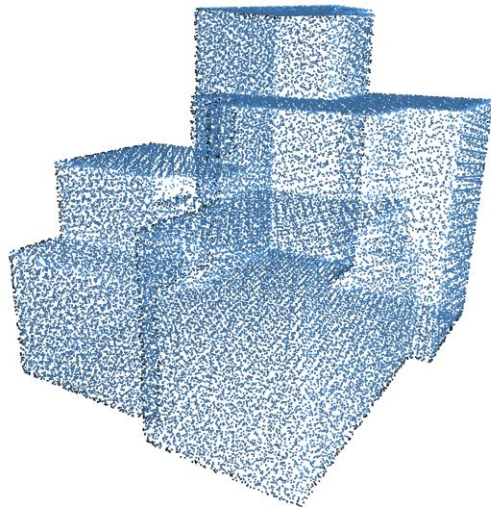
# Methodology: Overview



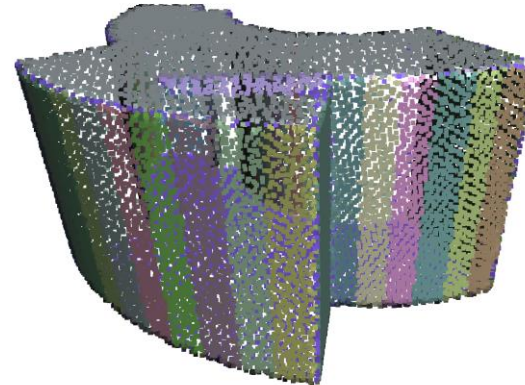
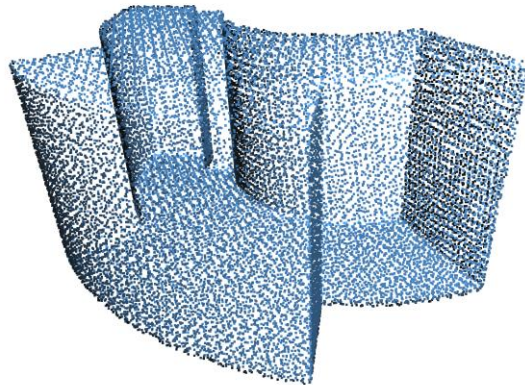
Overview of our framework



## Methodology: Adaptive binary space partitioning

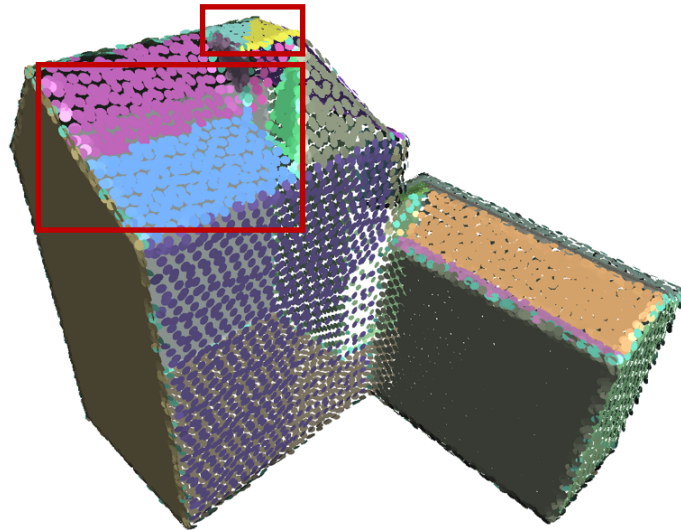


RANSAC

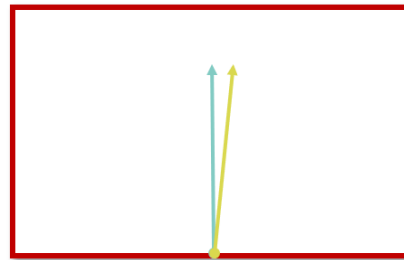


Planar primitive detection

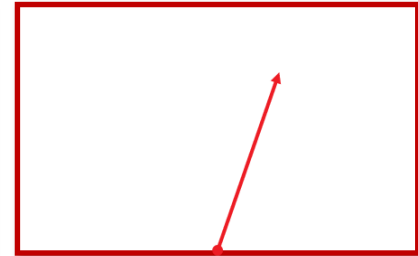
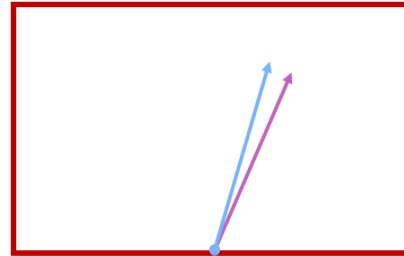
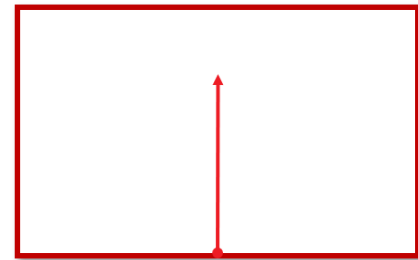
# Methodology: Adaptive binary space partitioning



Original

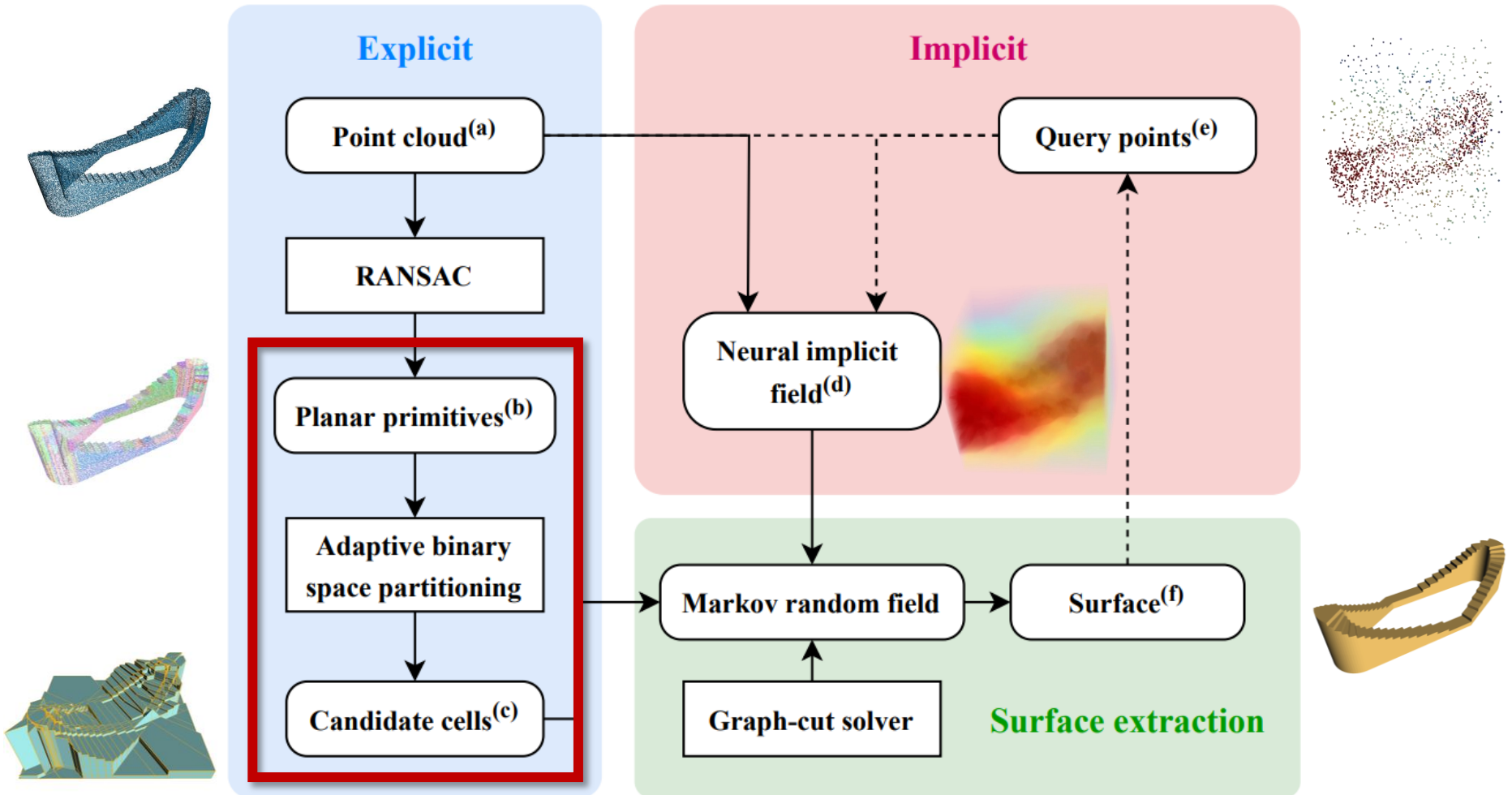


Refined

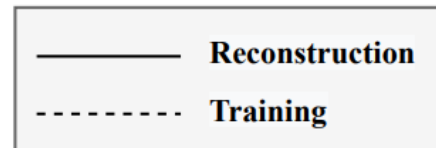


Planar primitive refinement

# Methodology: Overview

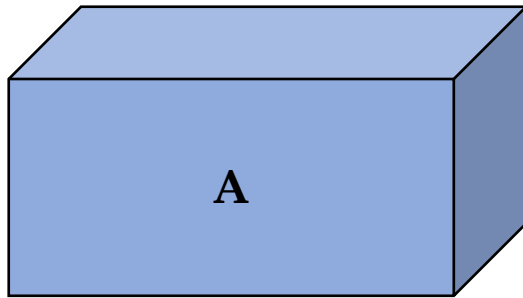


Overview of our framework

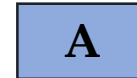




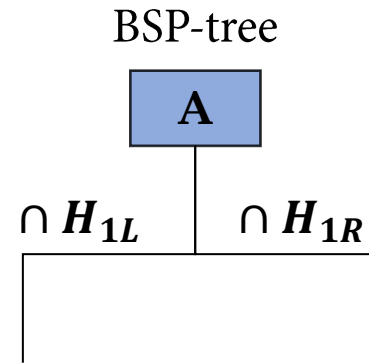
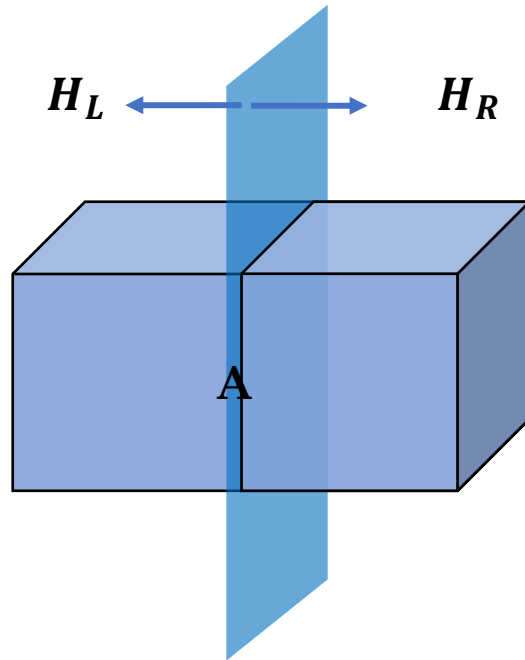
# Methodology: Adaptive binary space partitioning



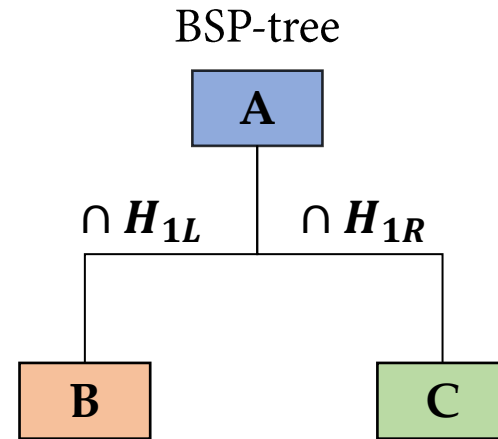
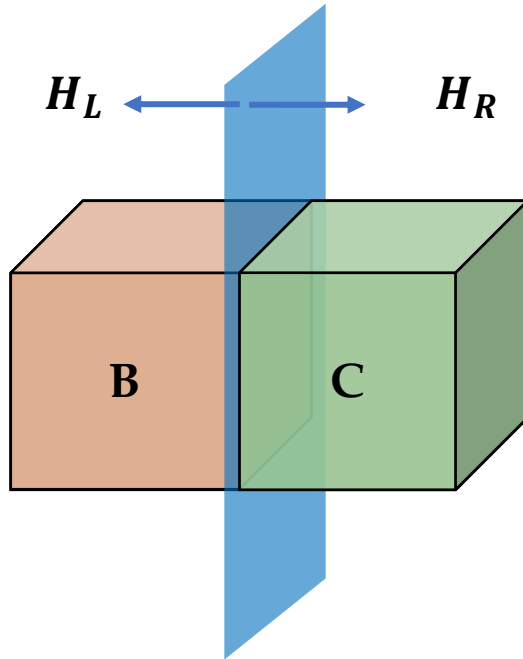
BSP-tree



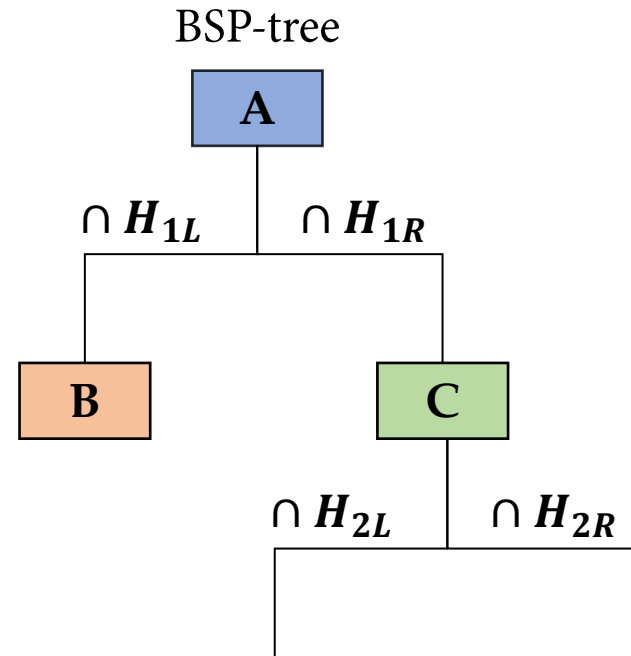
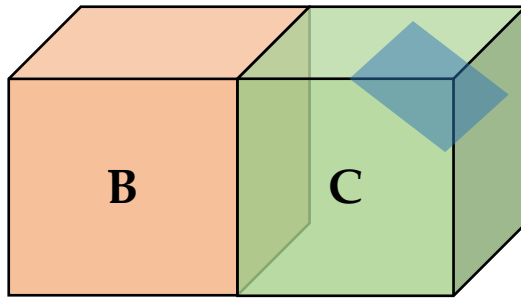
# Methodology: Adaptive binary space partitioning



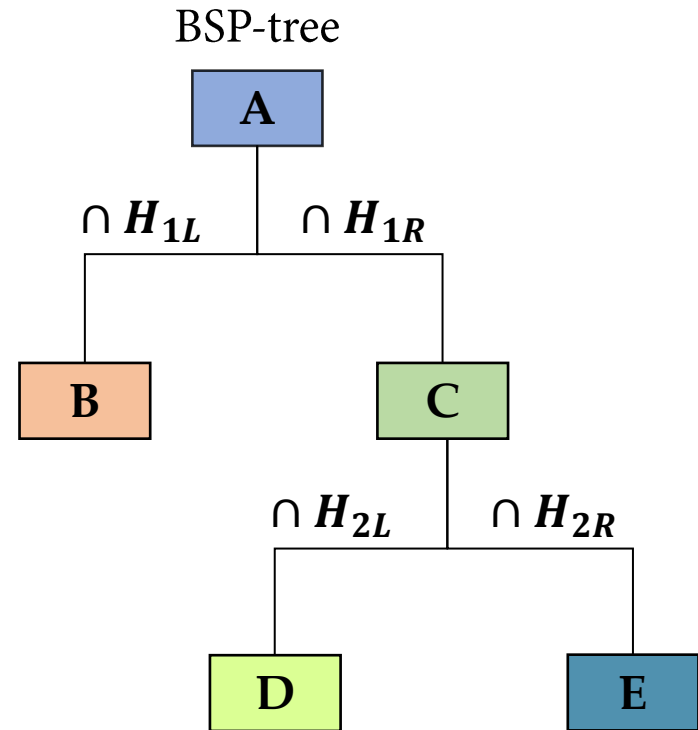
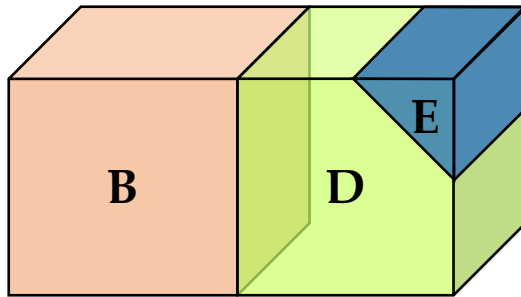
# Methodology: Adaptive binary space partitioning



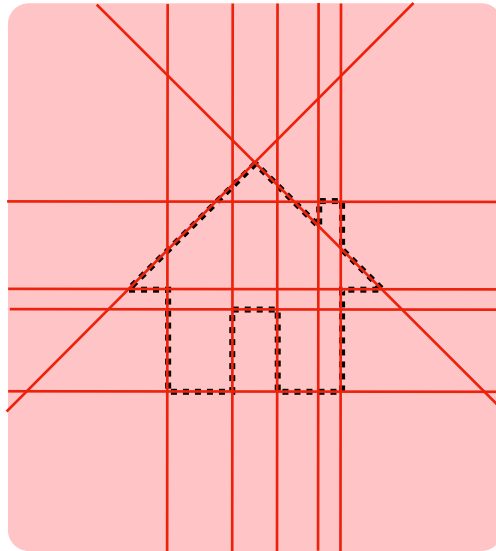
# Methodology: Adaptive binary space partitioning



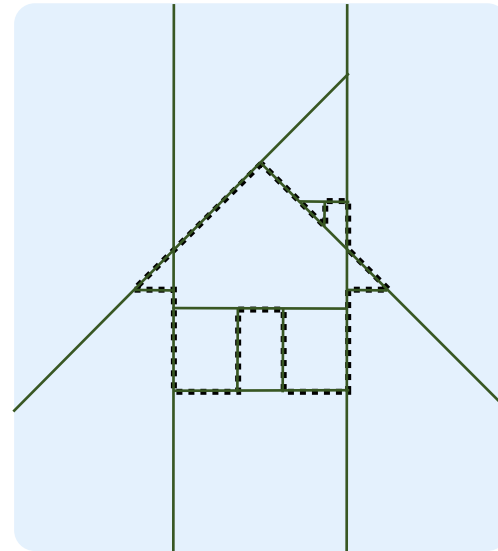
# Methodology: Adaptive binary space partitioning



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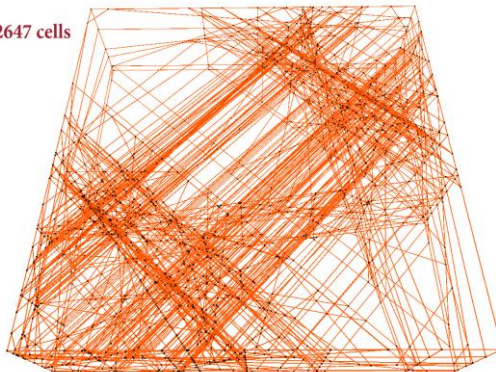


Exhaustive

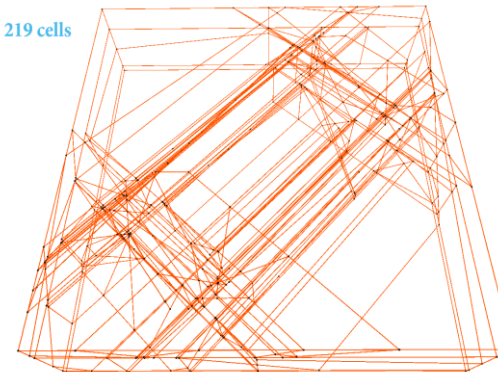


Adaptive

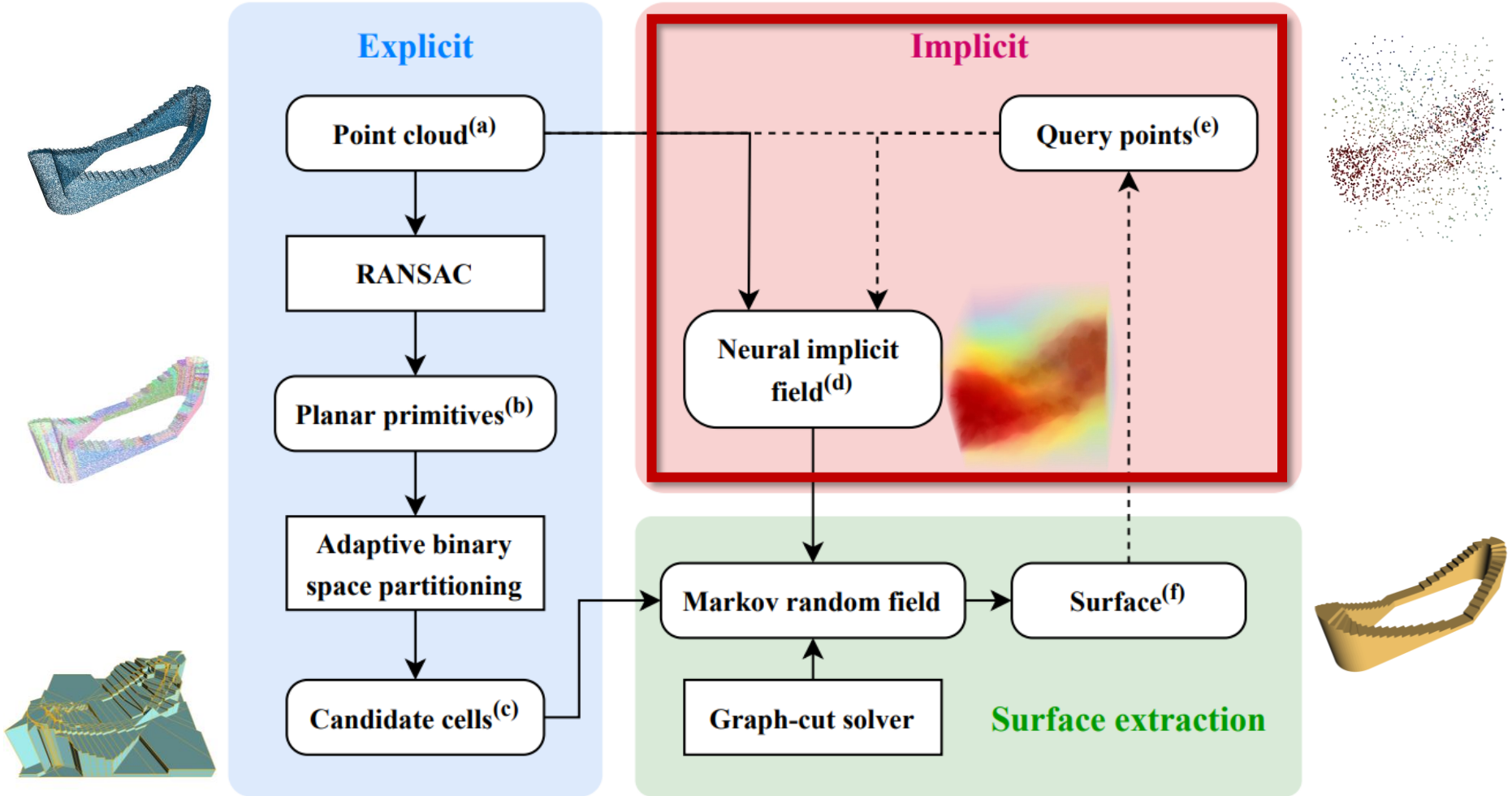
2647 cells



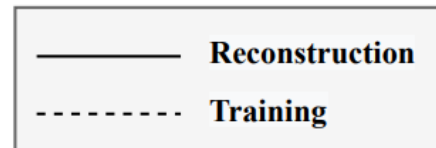
219 cells



# Methodology: Overview



Overview of our framework

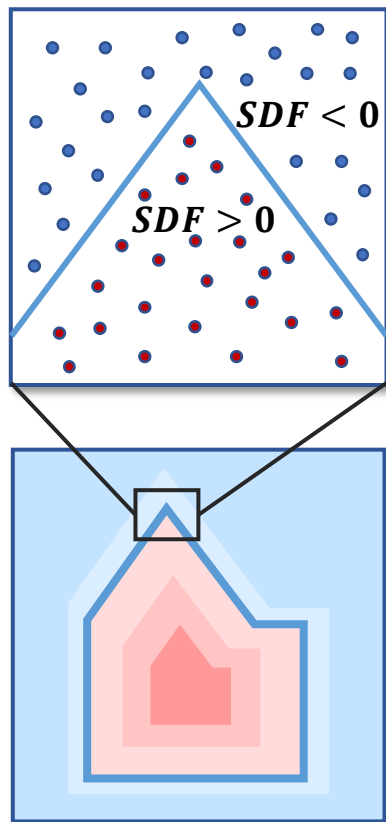


# Methodology: Occupancy learning in function space

Signed distance function

$$SDF(\mathbf{x}) = s : \mathbf{x} \in \mathbb{R}^3, s \in \mathbb{R}.$$

Surface at  $SDF(\cdot) = 0$





# Methodology: Occupancy learning in function space

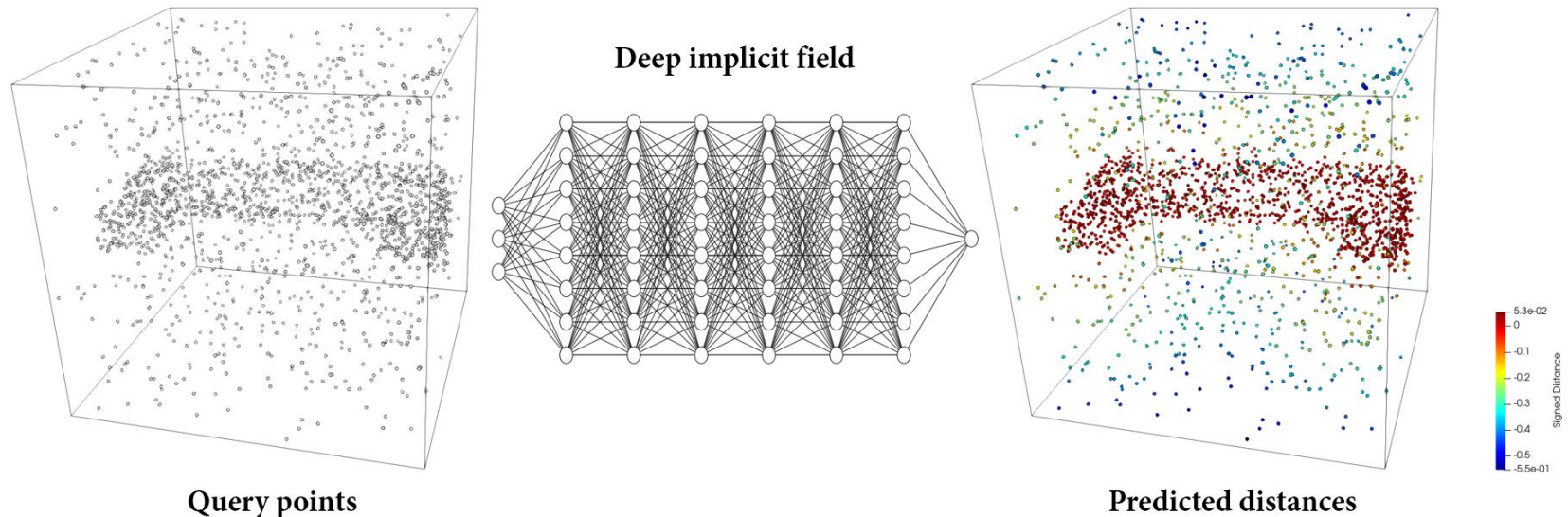
Signed distance function

$$SDF(\mathbf{x}) = s : \mathbf{x} \in \mathbb{R}^3, s \in \mathbb{R}.$$

Surface at  $SDF(\cdot) = 0$

$$SDF(\mathbf{x}) \approx \tilde{f}_P(\mathbf{x}) = s_\theta(\mathbf{x} \mid \mathbf{z}), \text{ with } \mathbf{z} = e_\varphi(P)$$

$P$ : point cloud  
 $\theta$ : NN parameters  
 $e$ : encoder

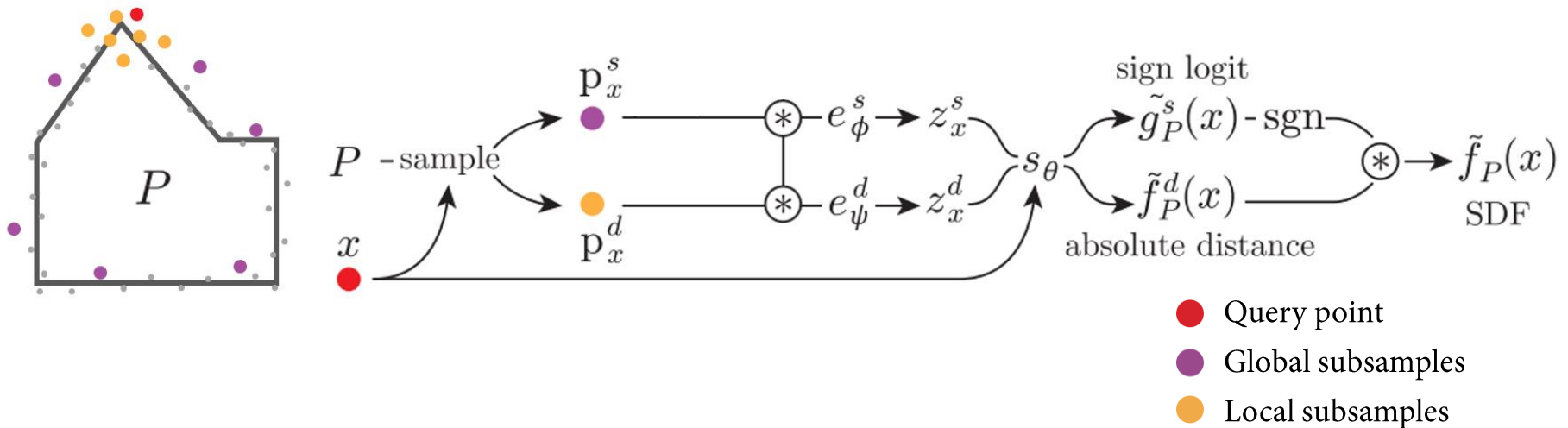


# Methodology: Occupancy learning in function space

Points2Surf neural network architecture [Erler et al., 2020]

$$SDF(\mathbf{x}) \approx \tilde{f}_P(\mathbf{x}) = s_\theta(\mathbf{x} \mid \mathbf{z}), \text{ with } \mathbf{z} = e_\varphi(P)$$

- $\tilde{f}_P^d(\mathbf{x}) = s_\theta^d(x \mid \mathbf{z}_x^d)$ , with  $\mathbf{z}_x^d = e_\psi^d(\mathbf{p}_x^d)$  Absolute distance
- $\tilde{f}_P^s(\mathbf{x}) = \text{sgn}(\tilde{g}_P^s(\mathbf{x})) = \text{sgn}(s_\theta^s(\mathbf{x} \mid \mathbf{z}_x^s))$ , with  $\mathbf{z}_x^s = e_\phi^s(\mathbf{p}_x^s)$  Sign

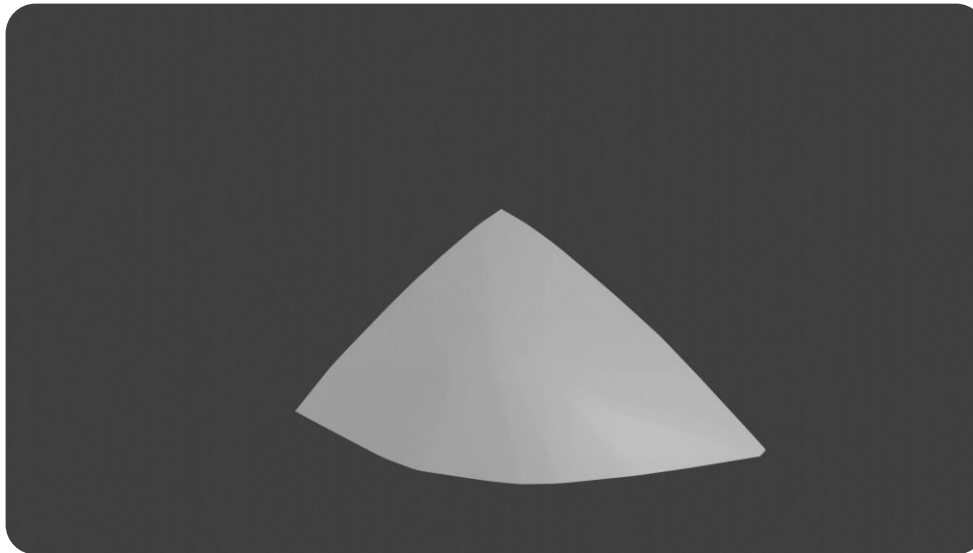


## Methodology: Occupancy learning in function space

Training with loss function

$$\sum_{(P,S) \in \mathcal{S}} \sum_{\mathbf{x} \in \mathcal{X}_S} \mathcal{L}^d(\mathbf{x}, P, S) + \mathcal{L}^s(\mathbf{x}, P, S)$$

- $\mathcal{L}^d(\mathbf{x}, P, S) = \left\| \tanh(|\tilde{f}_P^d(\mathbf{x})|) - \tanh(|d(\mathbf{x}, S)|) \right\|_2^2$  *Error of distance prediction*
- $\mathcal{L}^s(\mathbf{x}, P, S) = H(\sigma(\tilde{g}_P^s(\mathbf{x})), [f_S(\mathbf{x}) > 0])$  *Error of sign prediction*



Sanity check: overfitting one shape

*P: point cloud*  
*S: surface*  
*H: binary cross entropy*  
 *$\sigma$ : sigmoid*

# Methodology: Occupancy learning in function space

Signed distance voting

$$\bar{SD}^P = \frac{1}{P} \sum_{i \in P} SD_i^P$$

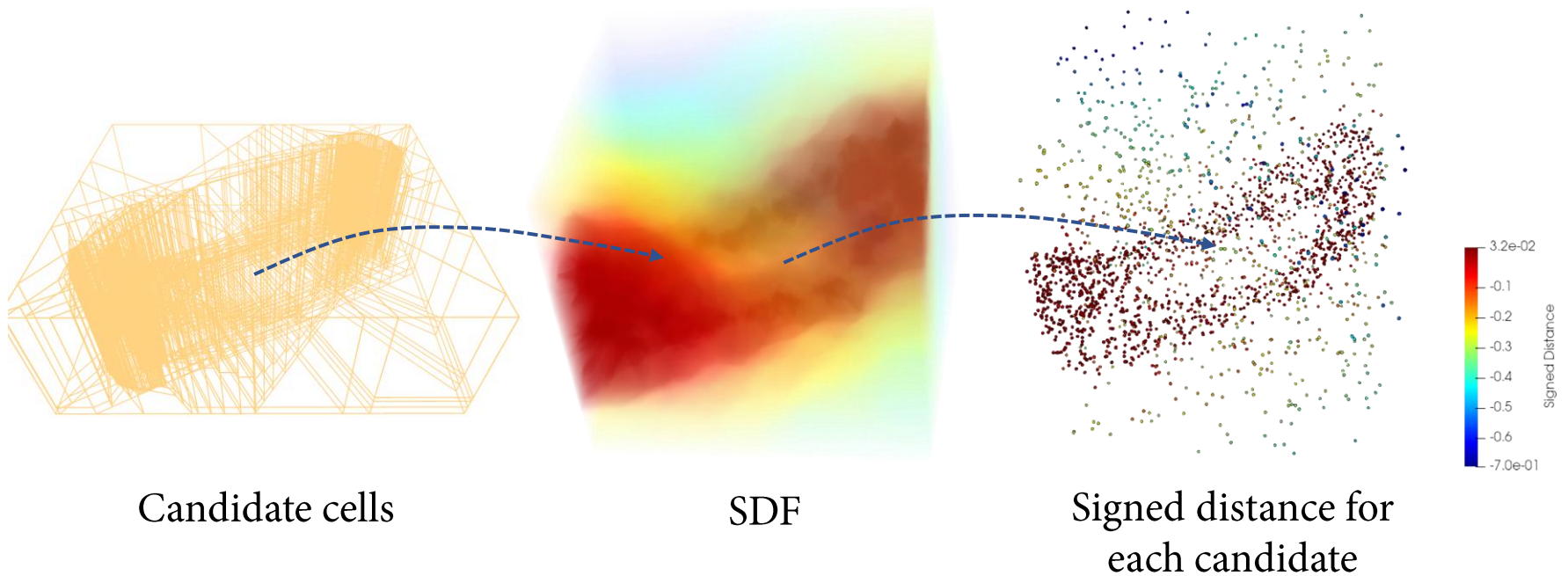


Point cloud

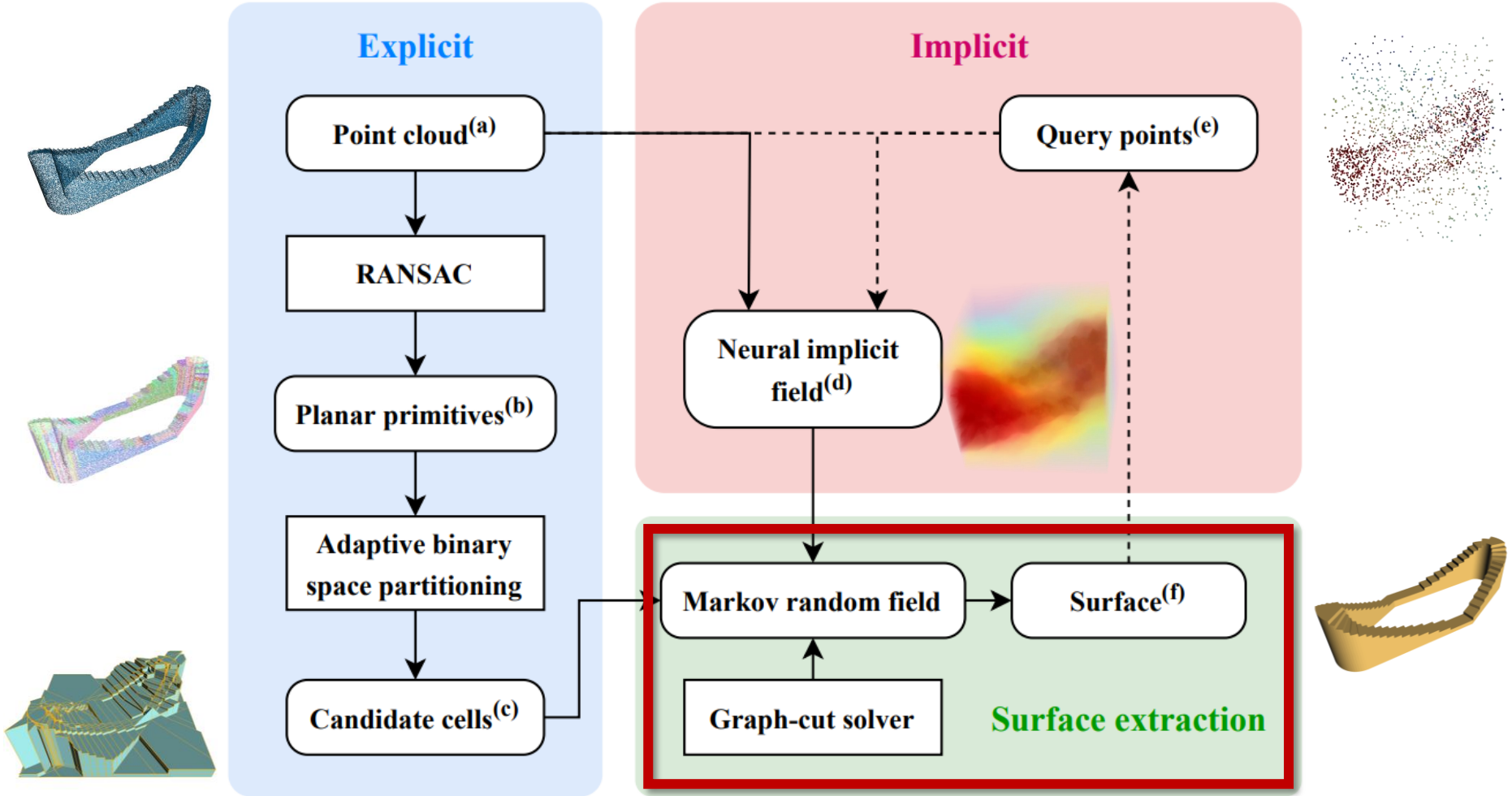
# Methodology: Occupancy learning in function space

## Signed distance voting

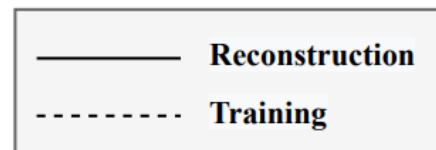
$$\bar{SD}^P = \frac{1}{P} \sum_{i \in P} SD_i^P$$



# Methodology: Overview



Overview of our framework

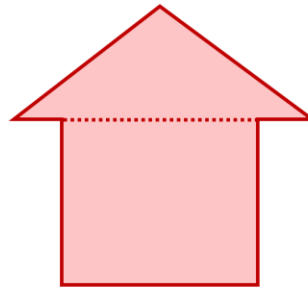
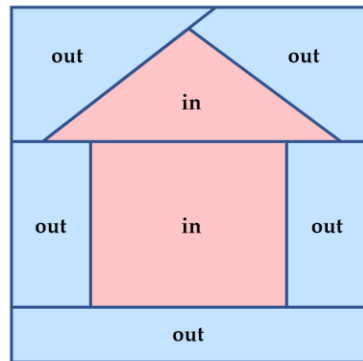


# Methodology: Surface extraction

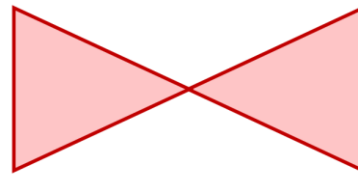
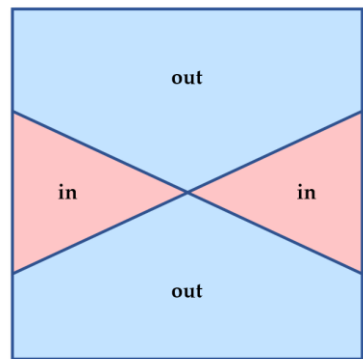
Energy formulation (Markov random field)

$$E(x) = D(x) + \lambda V(x)$$

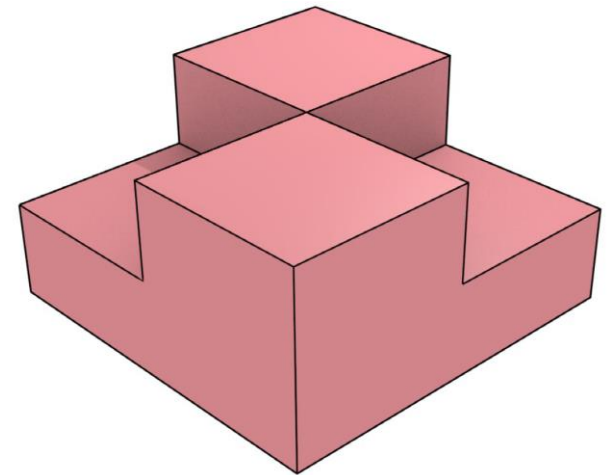
$$x_i = \{in, out\}$$



Manifold



Non-manifold



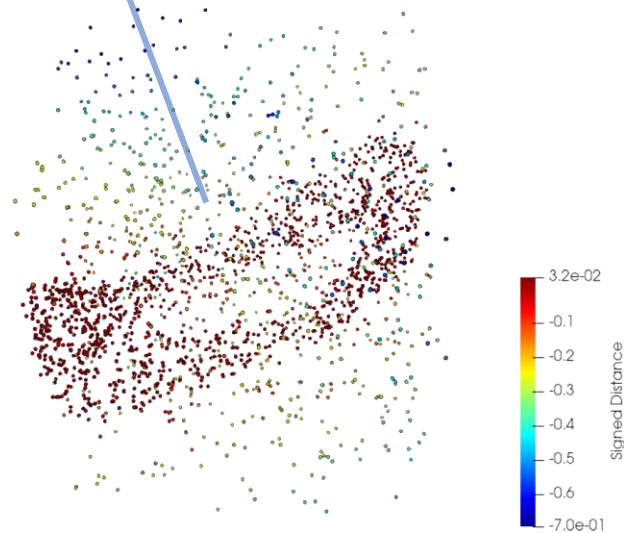
[Ohori, 2016]

## Methodology: Surface extraction

Fidelity term (unary potential)

$$D(X) = \frac{1}{|C|} \sum_{i \in C} d_i(C_i, x_i)$$

- $d_i(C_i, x_i) = |\text{probability}(C_i) - x_i|$
- $\text{probability}(C_i) = \text{sigmoid}(\text{SD}_i \cdot \text{volume}_i)$



Signed distance for  
each candidate

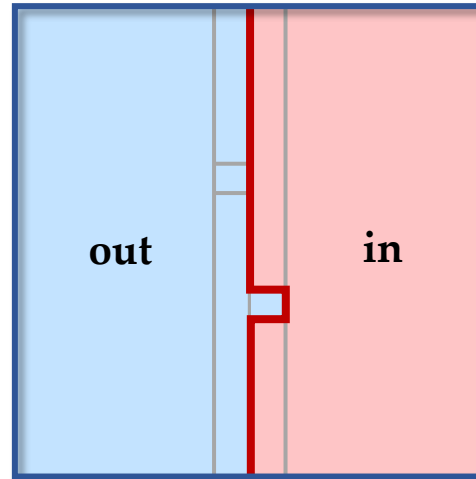
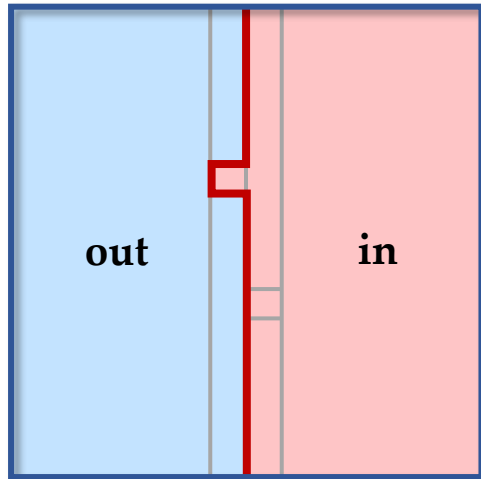


## Methodology: Surface extraction

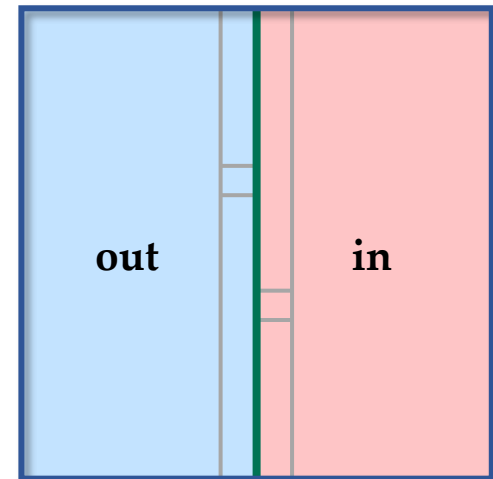
Complexity term (pairwise potential)

$$V(X) = \frac{1}{A} \sum_{\{i,j\} \in C} a_{ij} \cdot 1_{x_i \neq x_j}$$

- $\{i, j\} \in C$  represents pairs of adjacent polyhedra
- $a_{ij}$  denotes the shared area



Less zigzagging

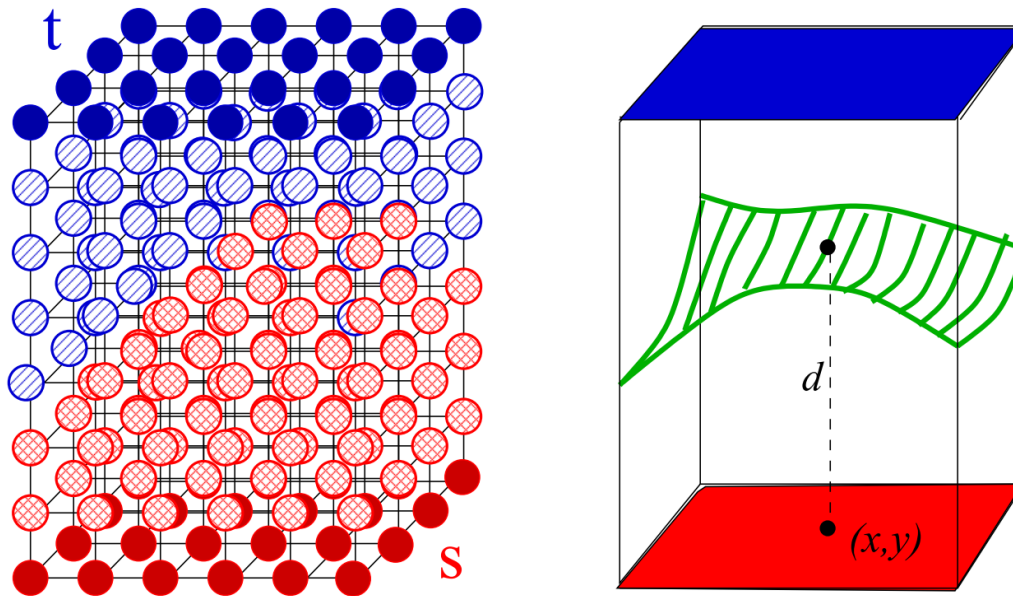


## Methodology: Surface extraction

Graph-cut solver for the Markov random field

$$E(x) = D(x) + \lambda V(x)$$

$$x_i = \{in, out\}$$



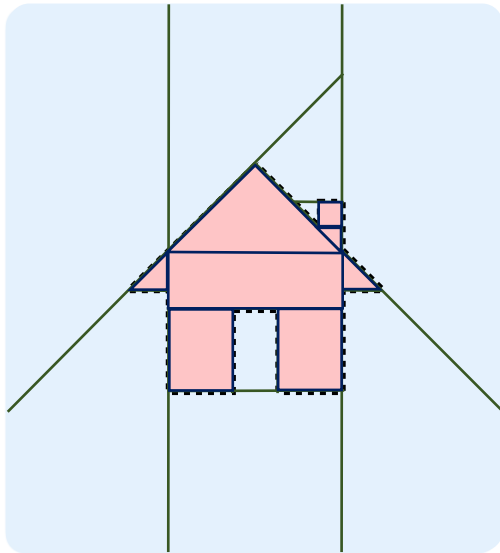
Graph cuts [Boykov and Funka-Lea, 2006]

## Methodology: Surface extraction

Graph-cut solver for the Markov random field

$$E(x) = D(x) + \lambda V(x)$$

$$x_i = \{in, out\}$$

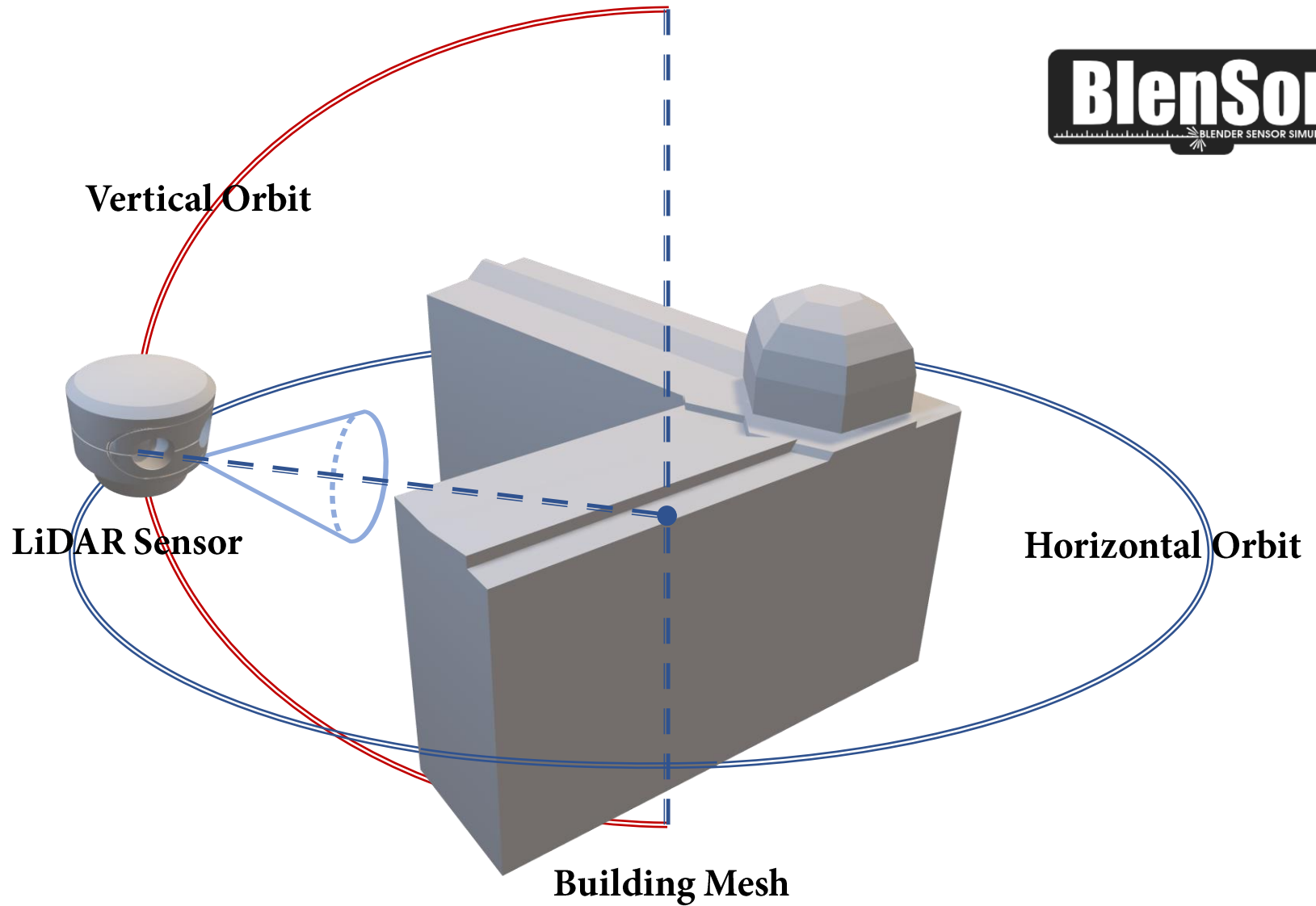


- Introduction
- Related work
- Methodology
- **Datasets**
- Results and discussion
- Conclusions

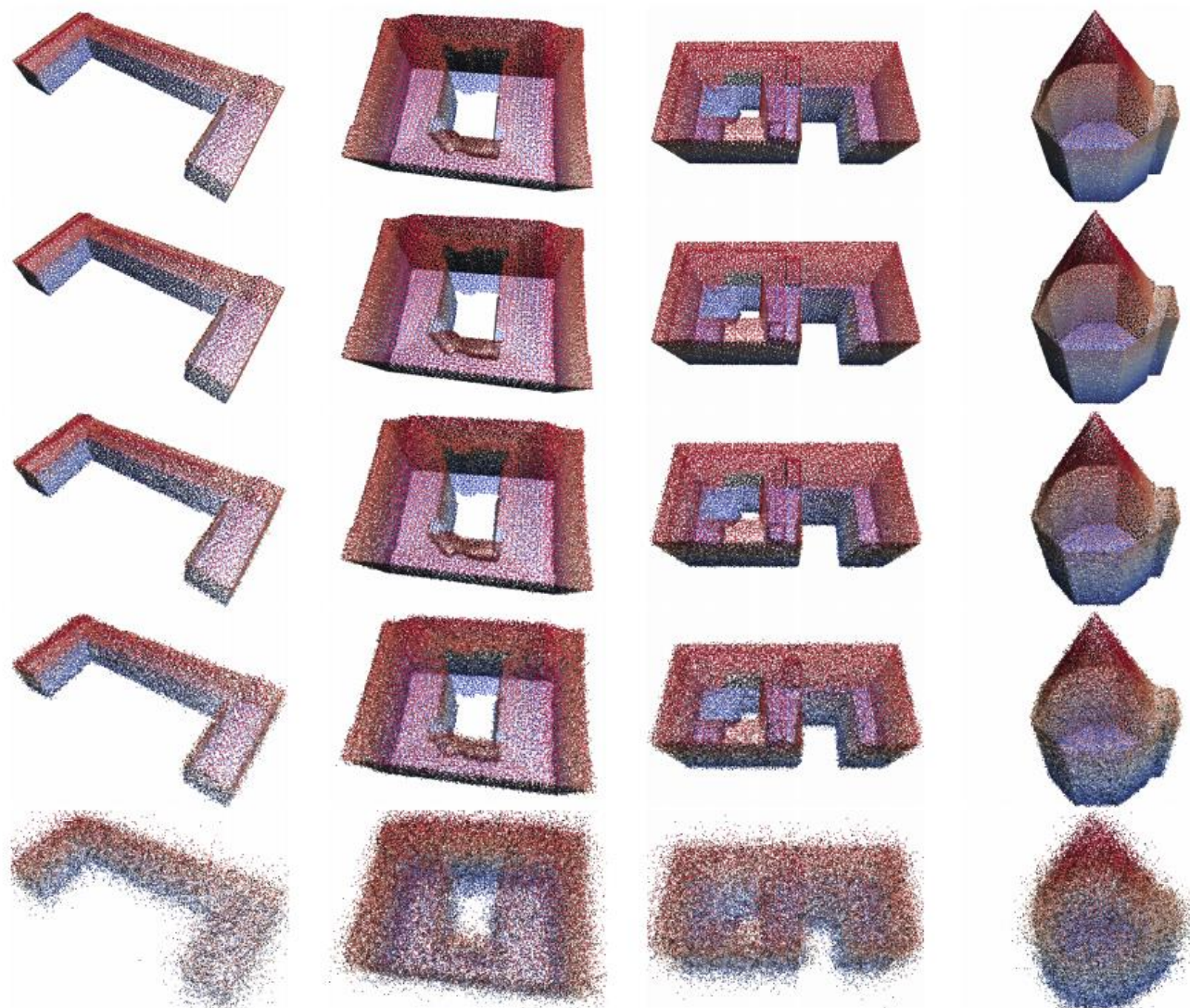
### Simulated LiDAR scanning from CityGML models

- Point clouds
- Surface -> Sampled query points with signed distance values

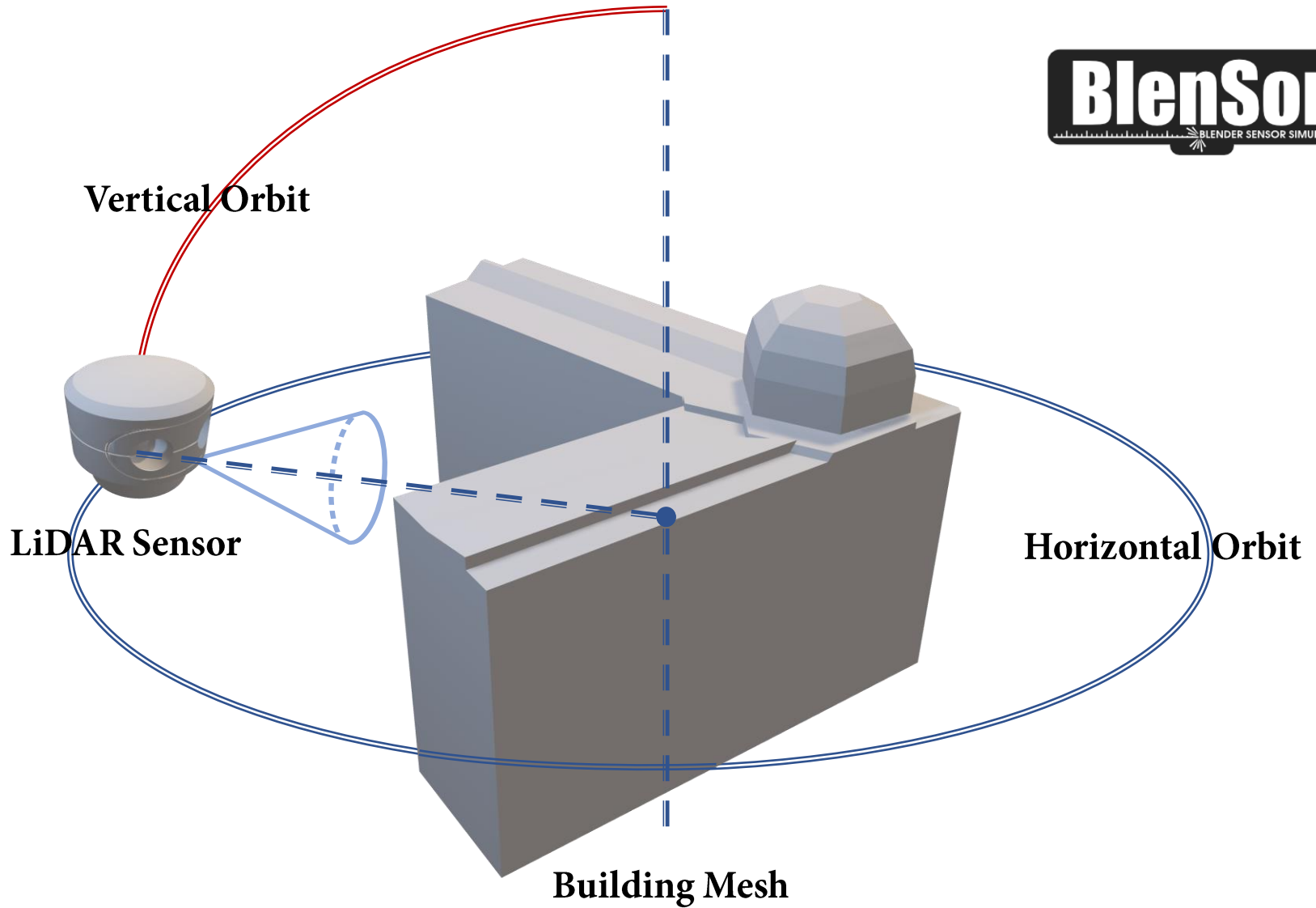




# Datasets: Helsinki full-view

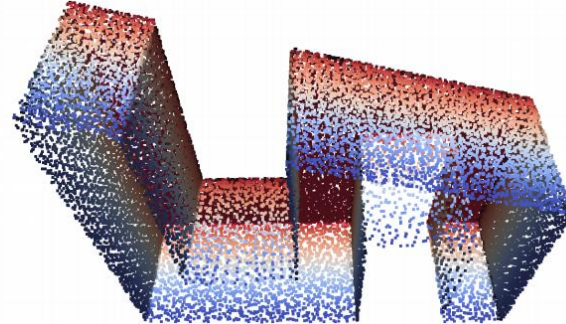
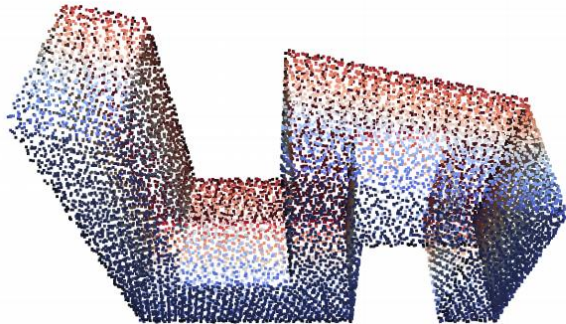
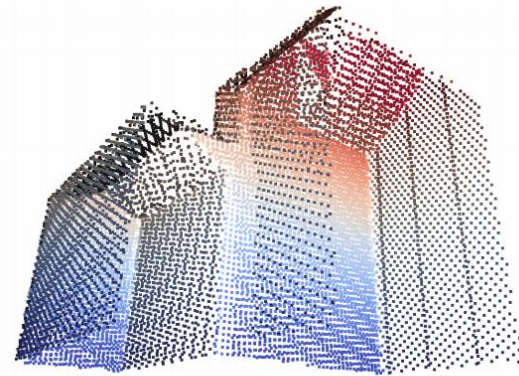
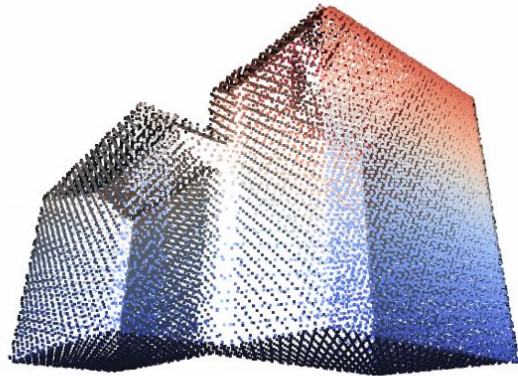


Gaussian Noise





## Datasets: *Helsinki*



*Helsinki full-view*

*Helsinki no-bottom*

## Datasets: *Shenzhen*



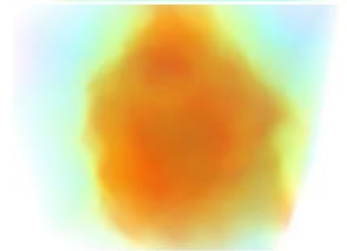
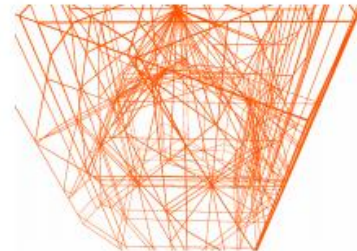
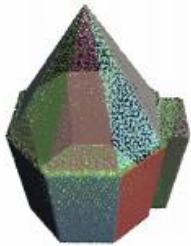
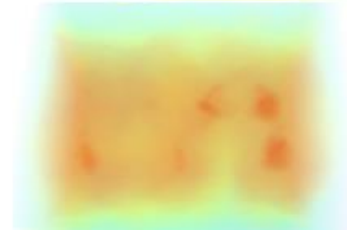
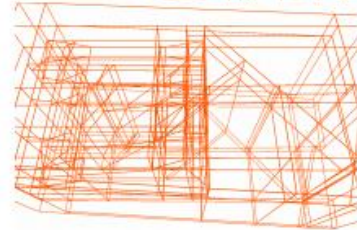
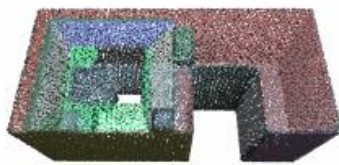
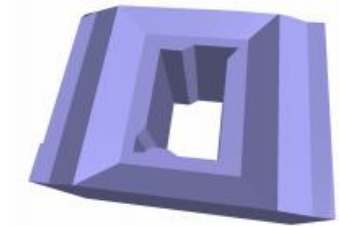
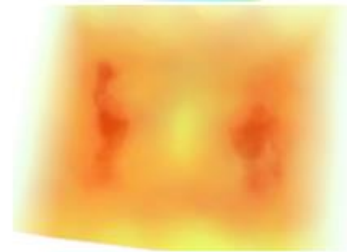
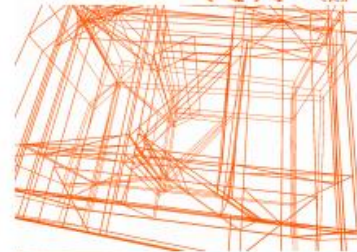
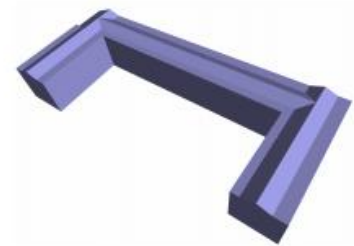
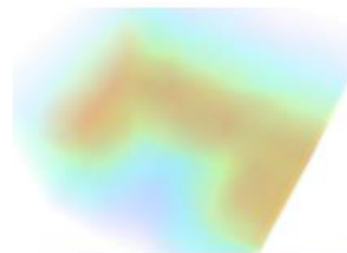
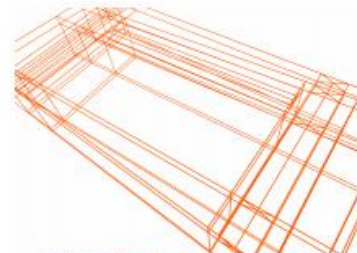
Data courtesy of Linfu Xie [[Xie et al., 2021](#)]

# Datasets

Name	Type	Perspective			Quantity	Usage
		Top	Bottom	Lateral		
<i>Helsinki full-view</i>	Simulated LiDAR	✓	✓	✓	768	Training + evaluation
<i>Helsinki no-bottom</i>	Simulated LiDAR	✓	✗	✓	768	Training + evaluation
<i>Shenzhen</i>	Real-world MVS	✓	✗	✓	6	Evaluation

- Introduction
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- Conclusions

# Results & discussion: *Helsinki* full-view



Point cloud

Candidate polyhedra

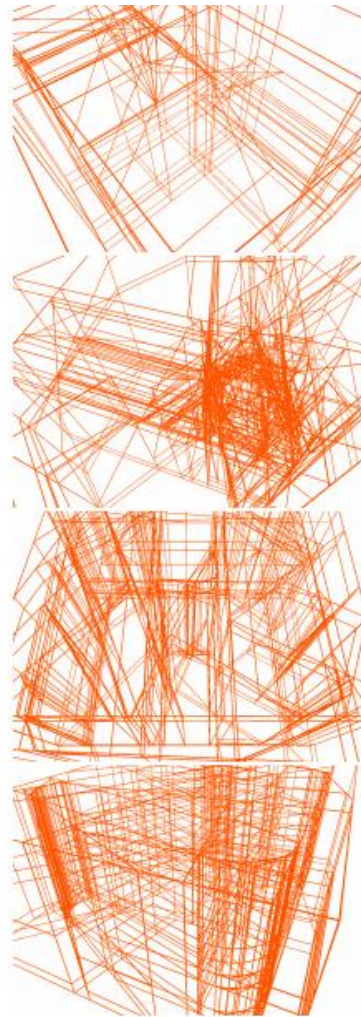
SDF

Reconstructed

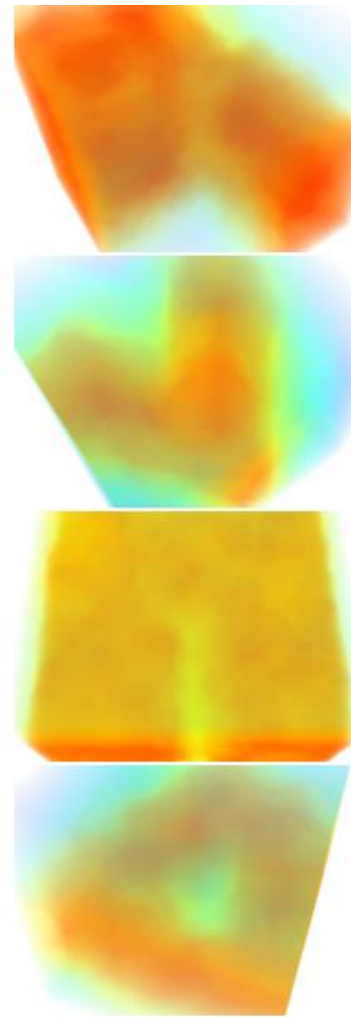
# Results & discussion: *Helsinki* full-view



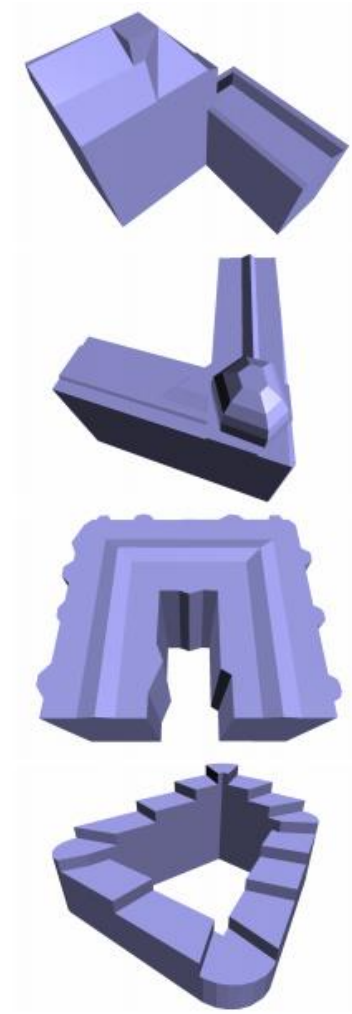
Point cloud



Candidate polyhedra

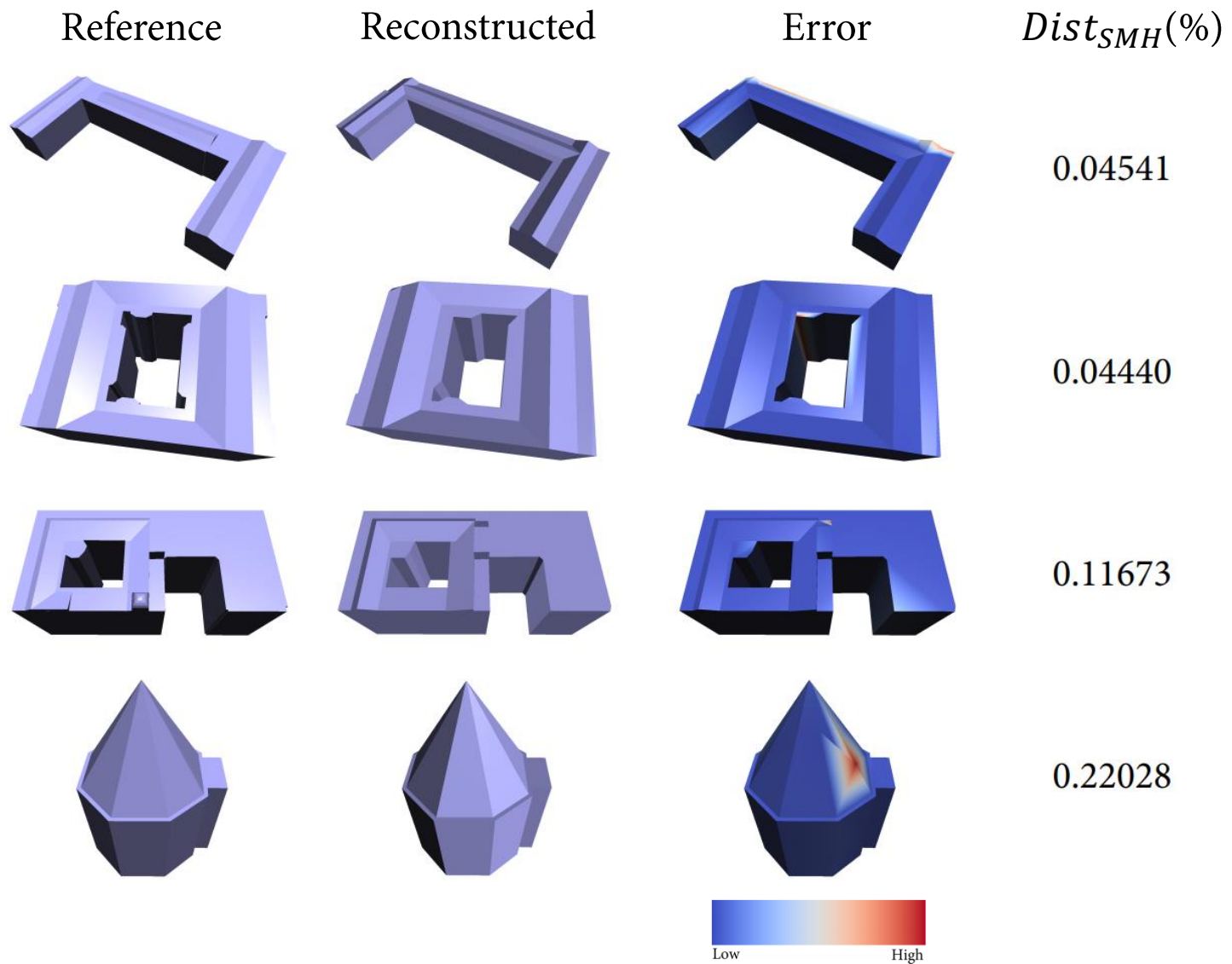


SDF

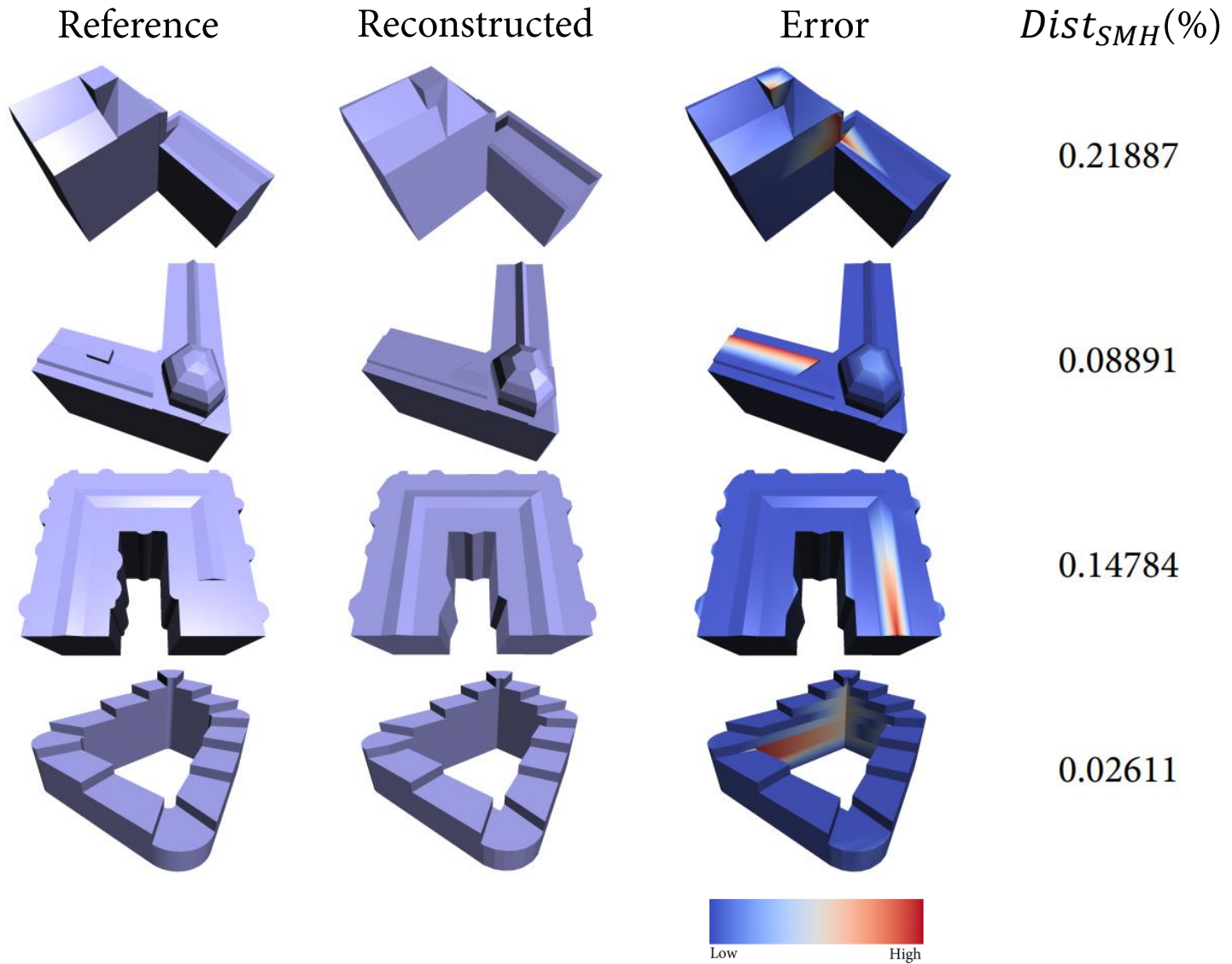


Reconstructed

# Results & discussion: *Helsinki full-view*

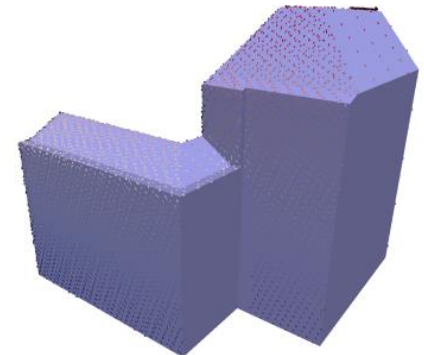
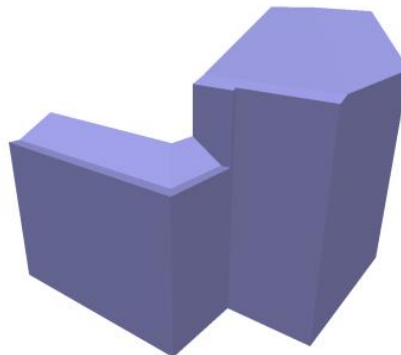
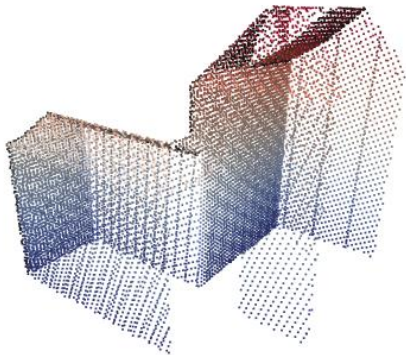
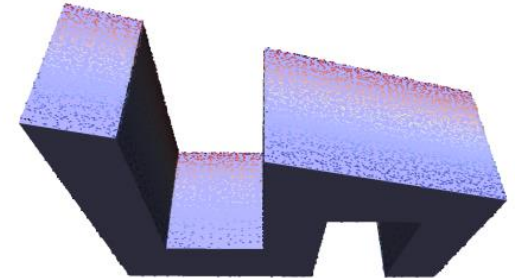
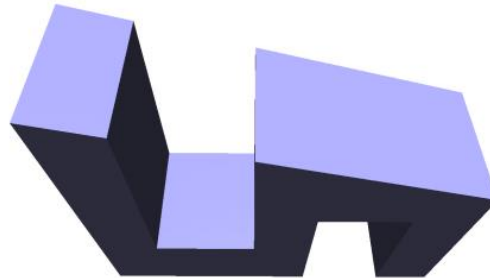
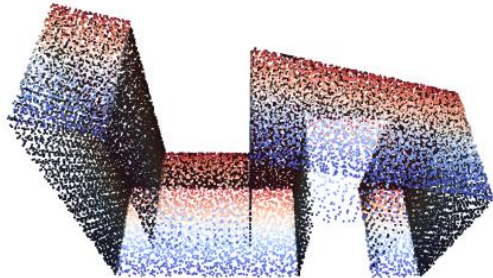


# Results & discussion: *Helsinki full-view*

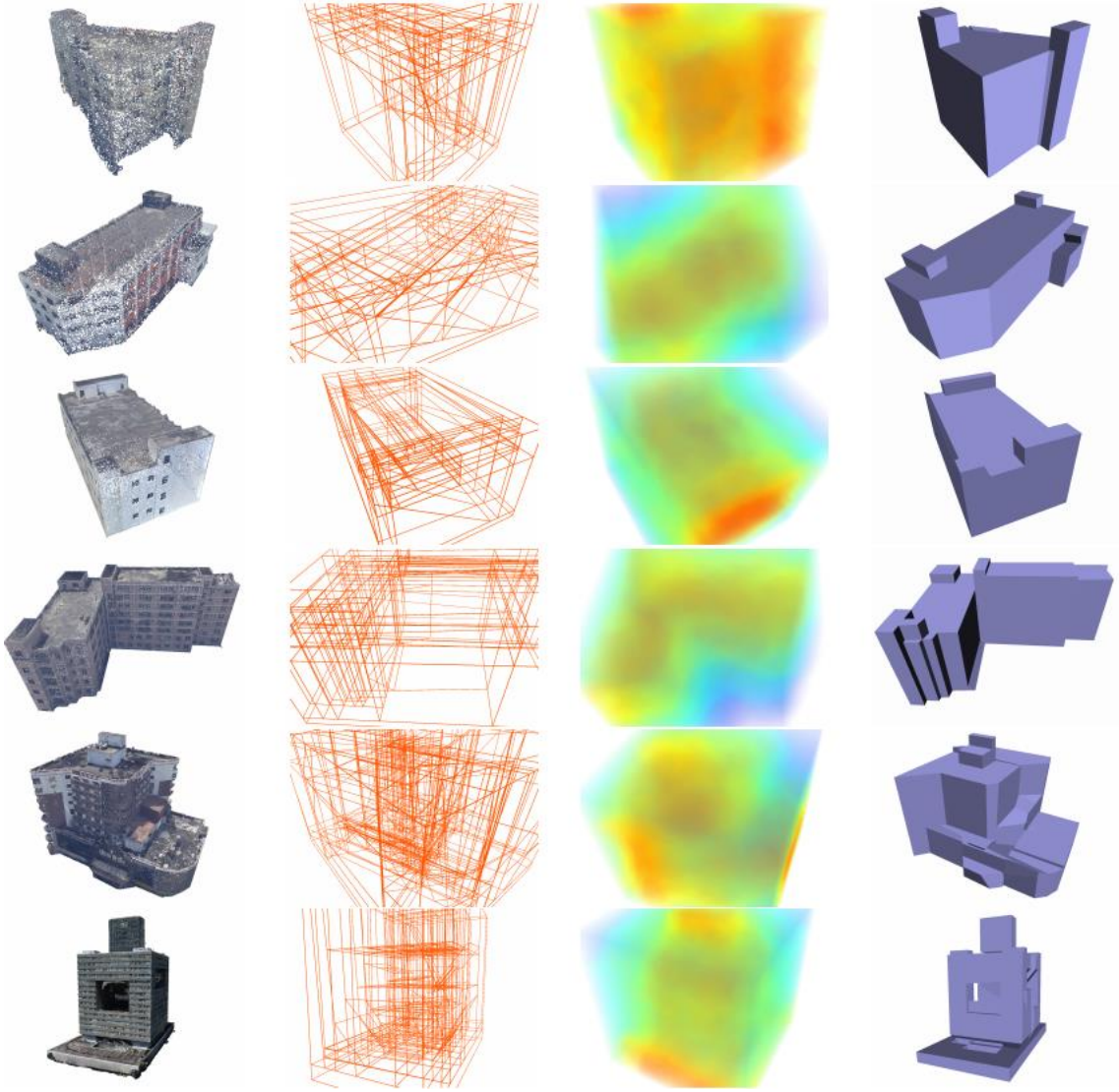
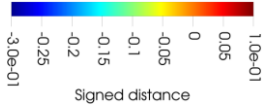




## Results & discussion: *Helsinki no-bottom*



# Results & discussion: *Shenzhen*



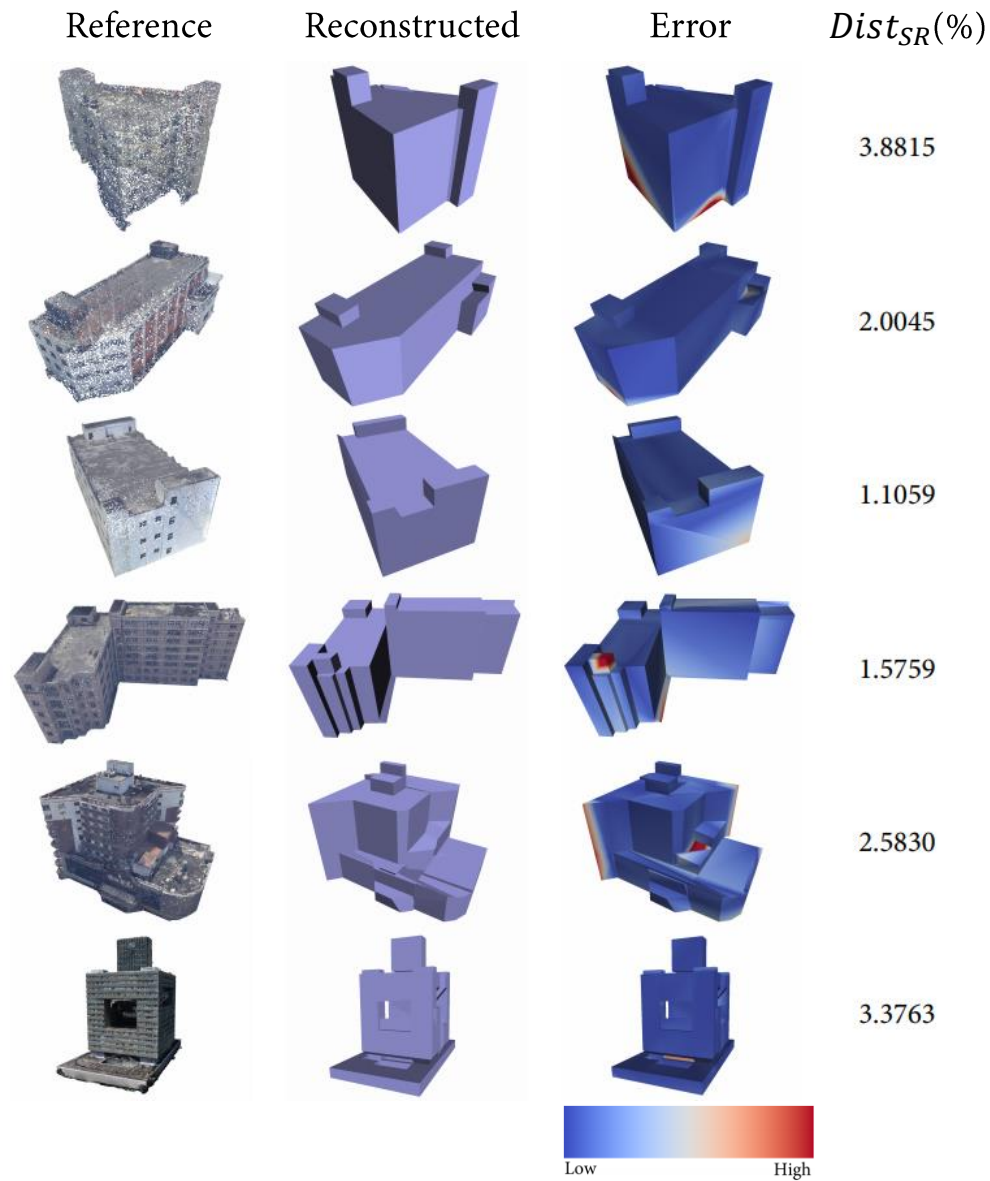
Point cloud

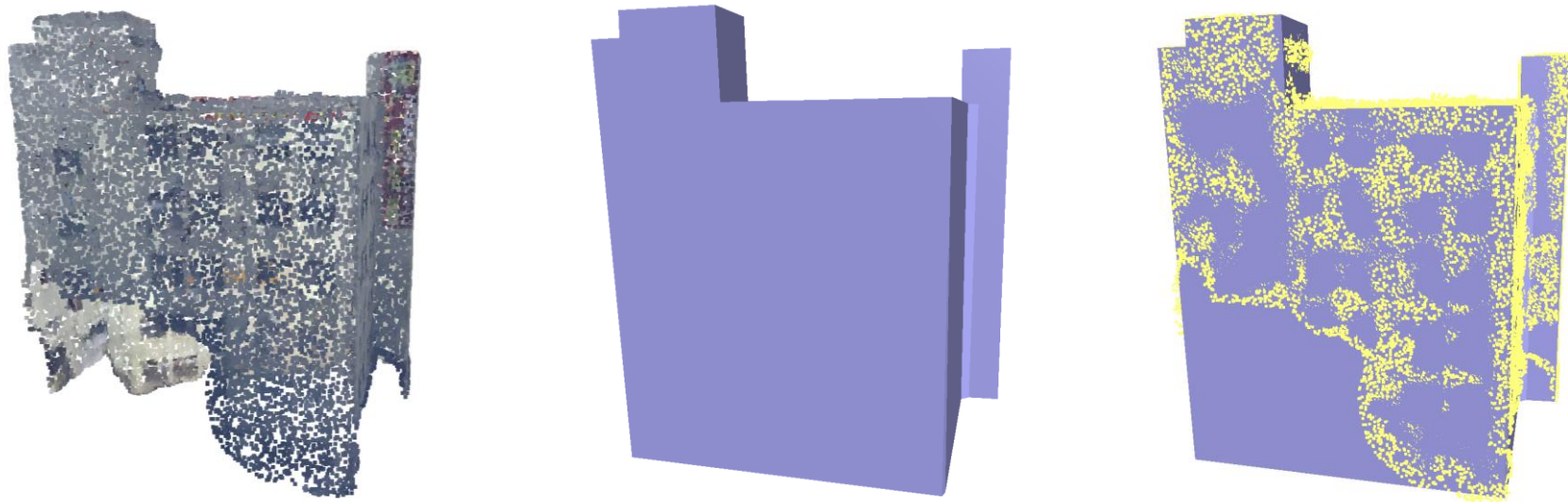
Candidate polyhedra

SDF

Reconstructed

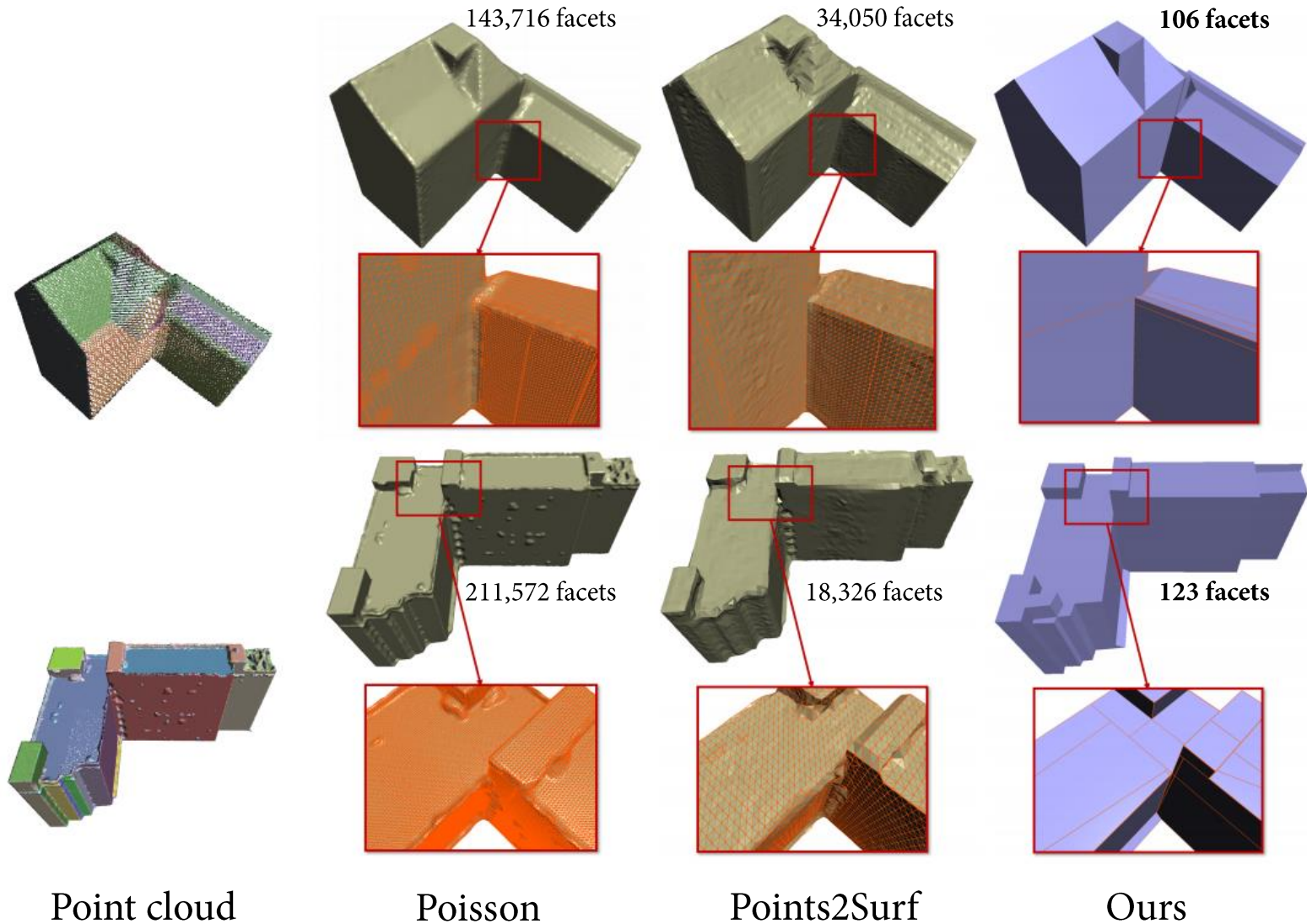
# Results & discussion: *Shenzhen*





Reconstruction from insufficient scans

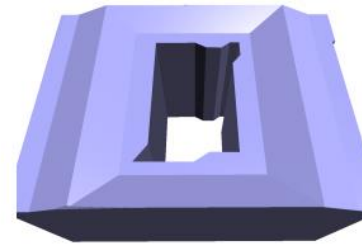
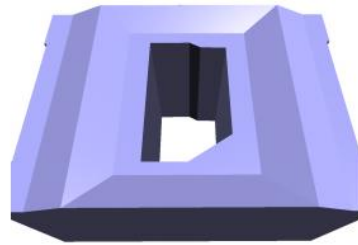
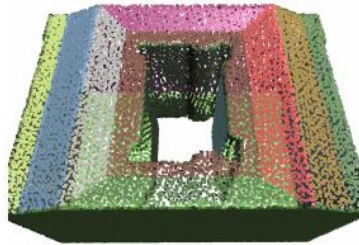
# Results & discussion: Comparison with smooth reconstruction



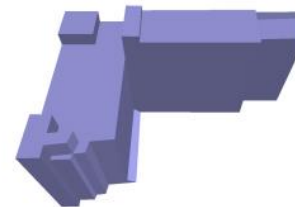
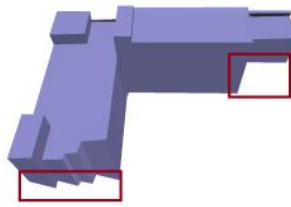
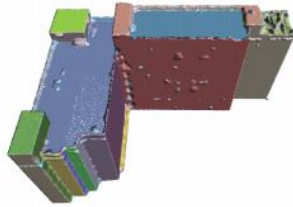
[Kazhdan et al., 2006] [Erler et al., 2020]

# Results & discussion: Comparison with piecewise-planar reconstruction

*Helsinki full-view*



*Shenzhen*

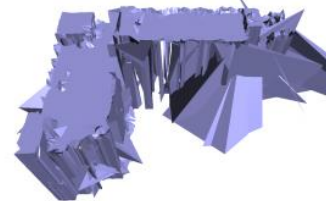
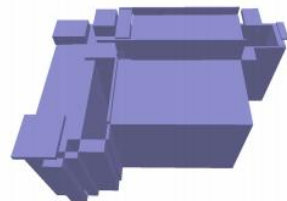
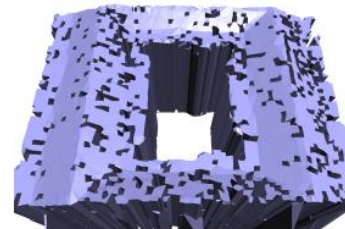
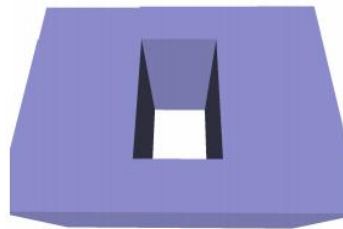


Point cloud

PolyFit

Ours

[Nan and Wonka, 2017]

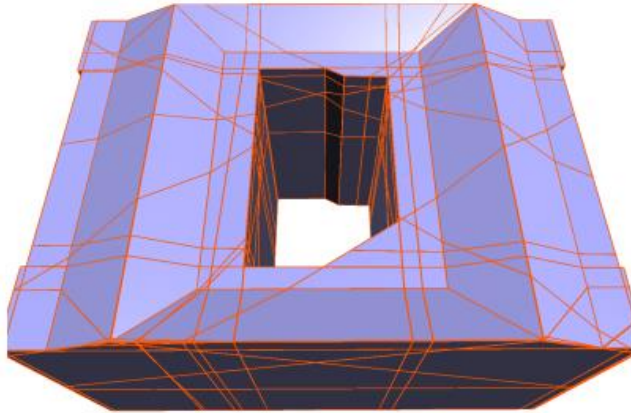


Manhattan-world  
[Li et al., 2016b]

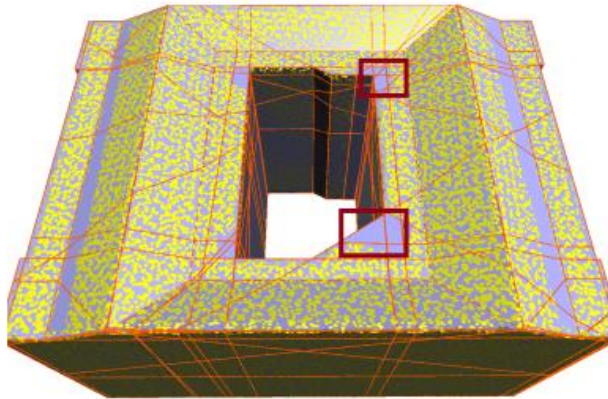
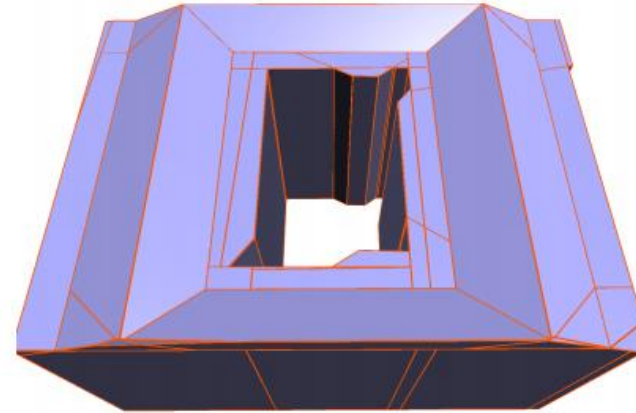
2.5D DC [Zhou and  
Neumann, 2010]

## Results & discussion: Comparison

643 facets

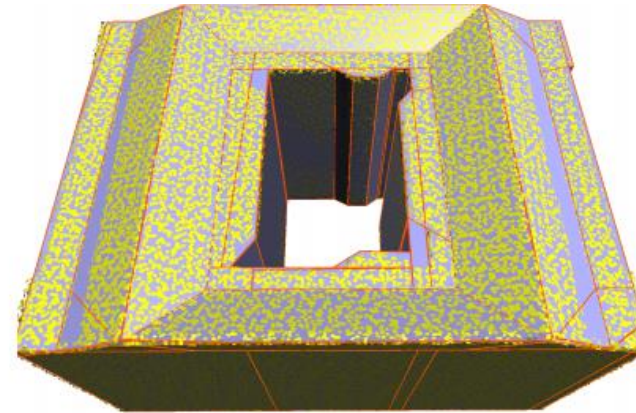


117 facets



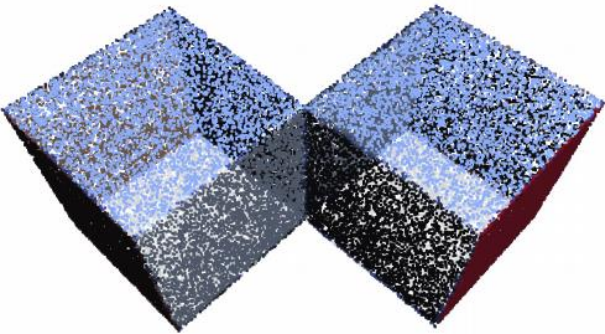
PolyFit

[Nan and Wonka, 2017]

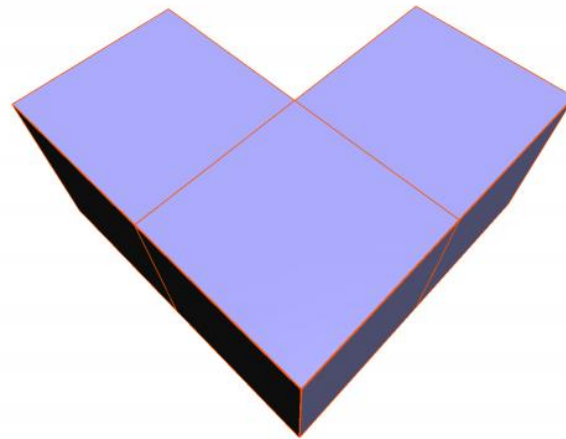


Ours

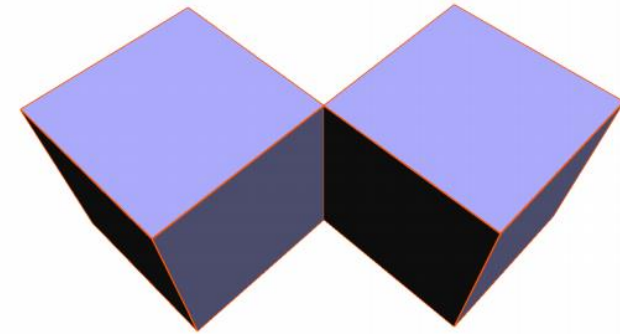
## Results & discussion: Comparison



Point cloud



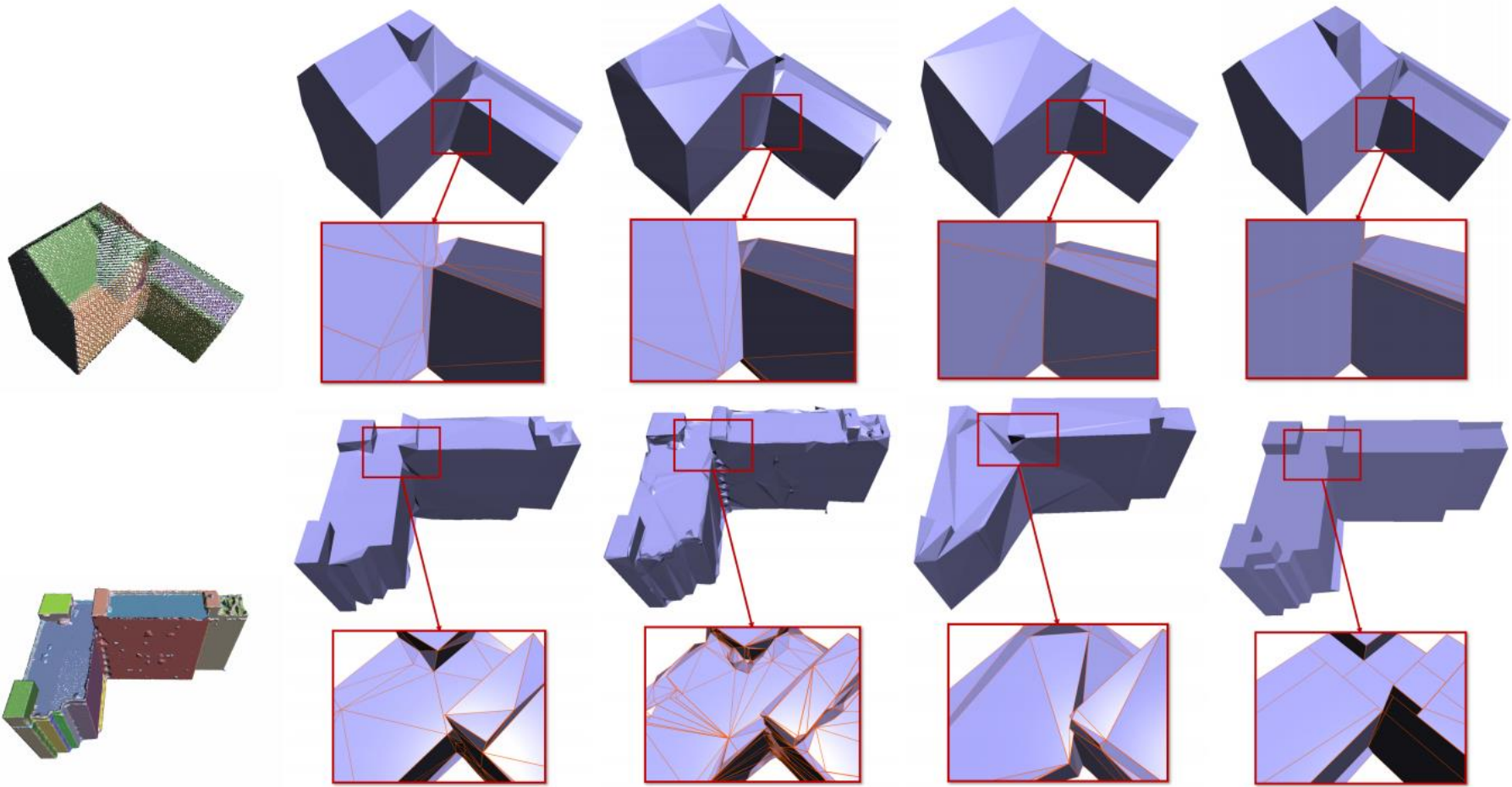
PolyFit  
[Nan and Wonka, 2017]



Ours



# Results & discussion: Comparison with surface approximation methods



Point cloud

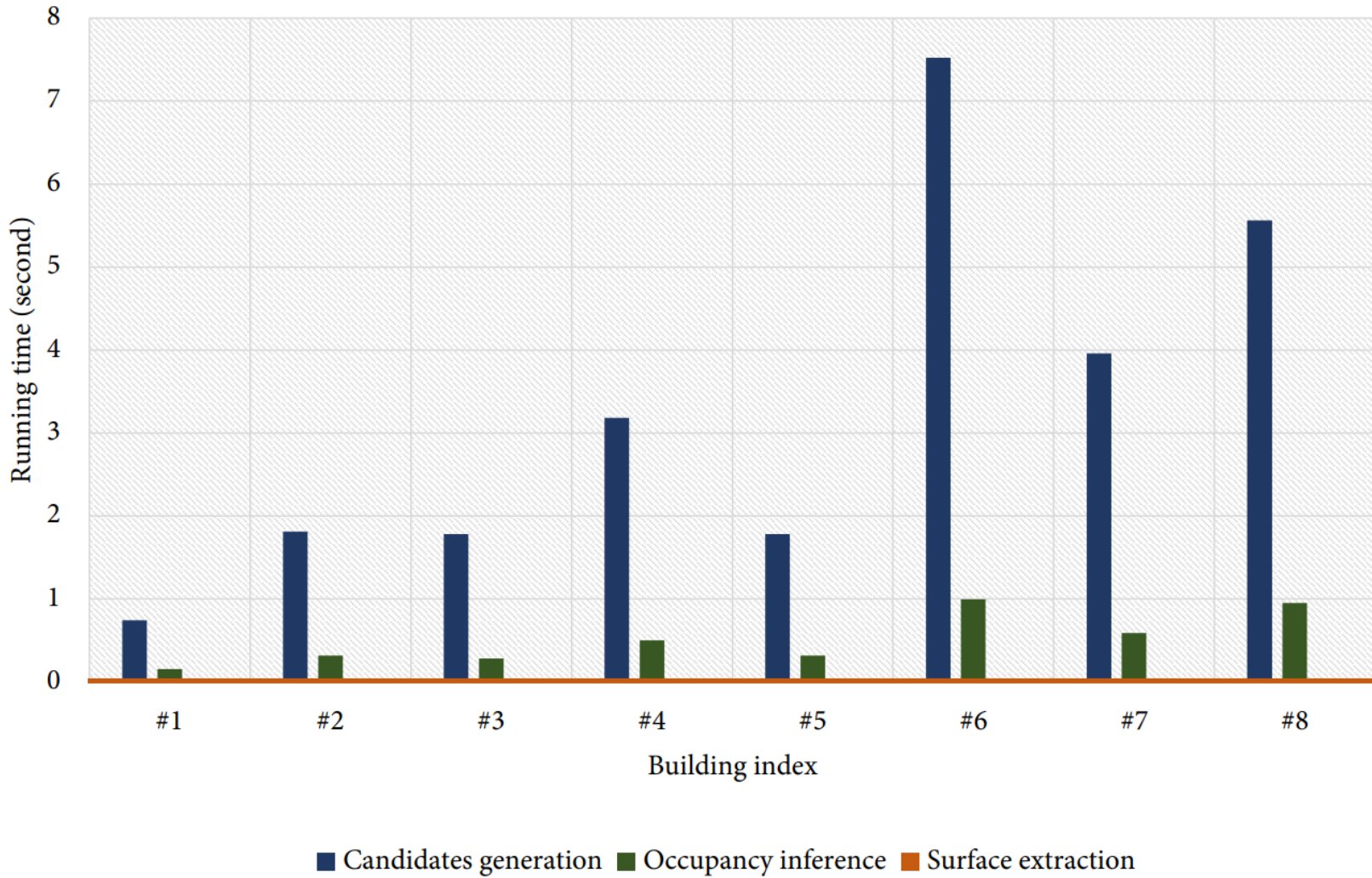
QEM [Garland and Heckbert, 1997]

SAMD [Salinas et al., 2015]

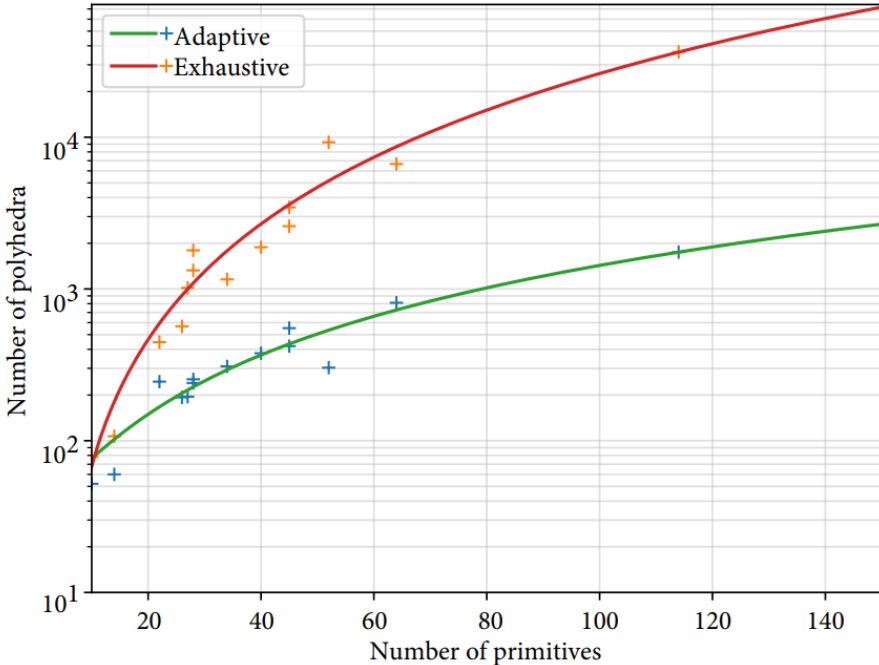
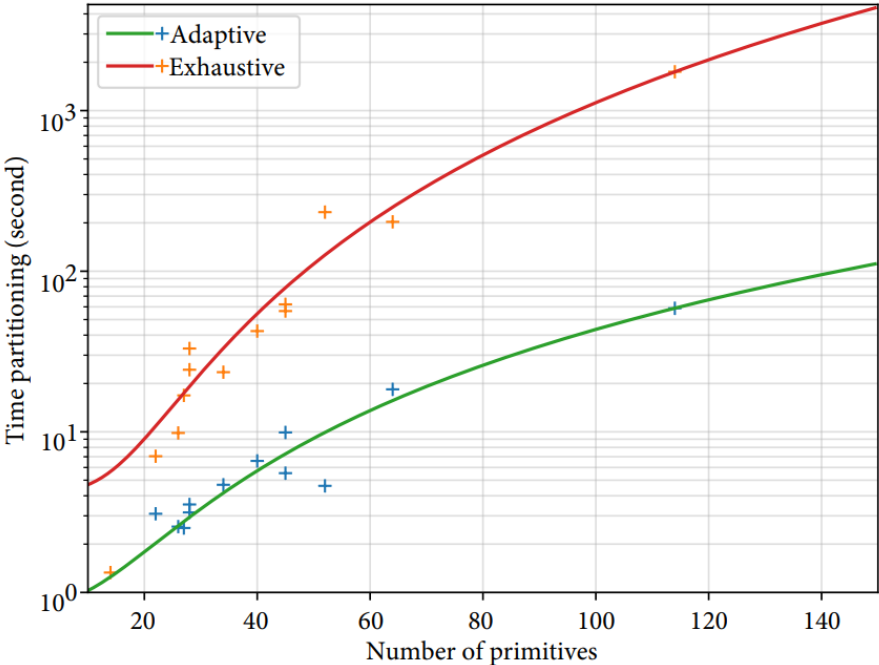
VSA [Cohen-Steiner et al., 2004]

Ours

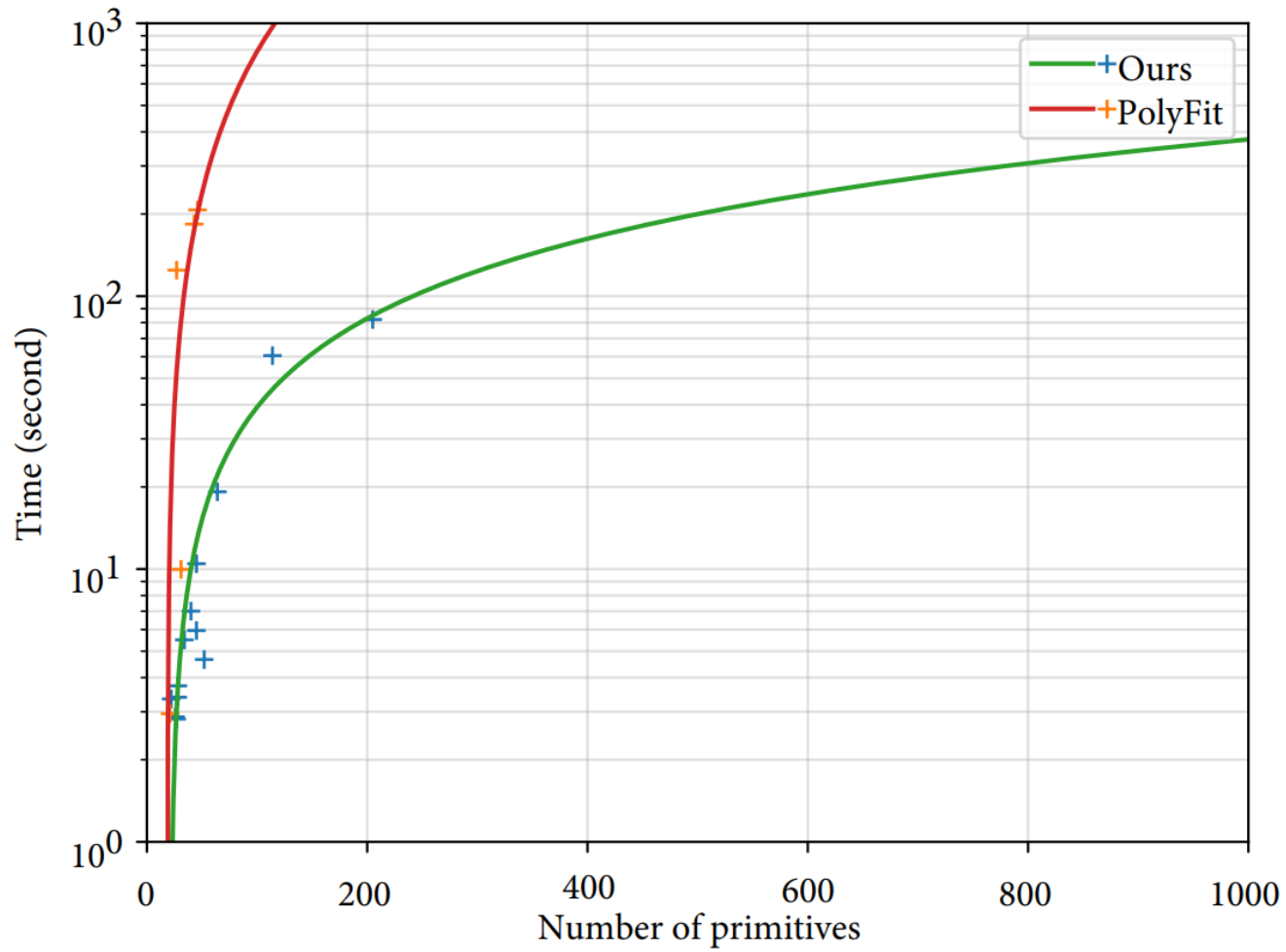
## Results & discussion: Efficiency



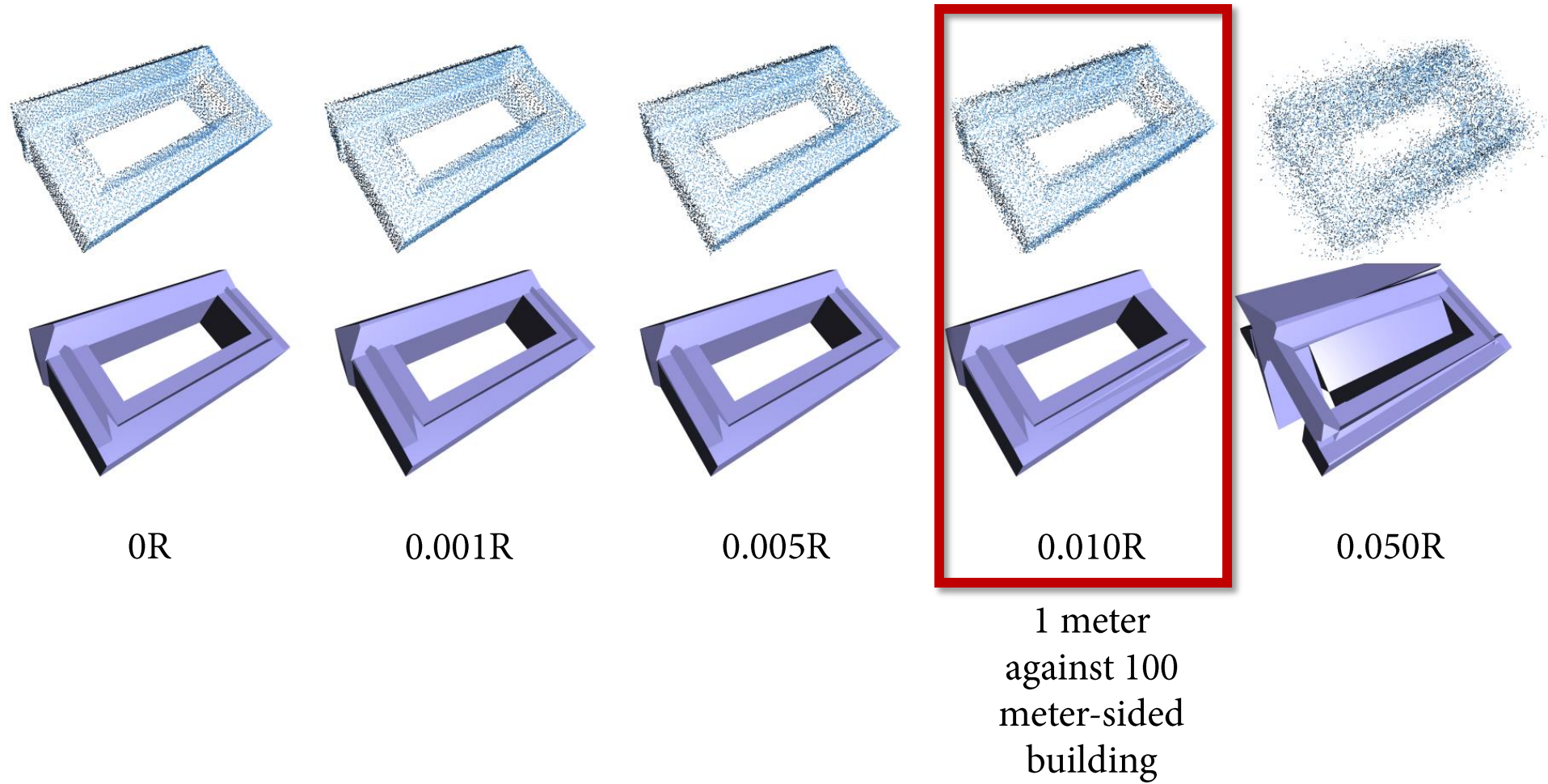
# Results & discussion: Efficiency



## Results & discussion: Scalability



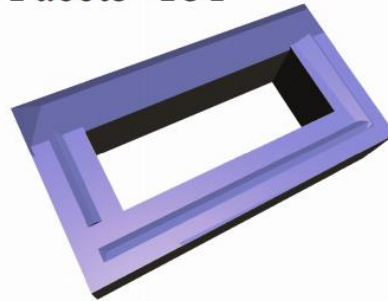
## Results & discussion: Robustness to noise



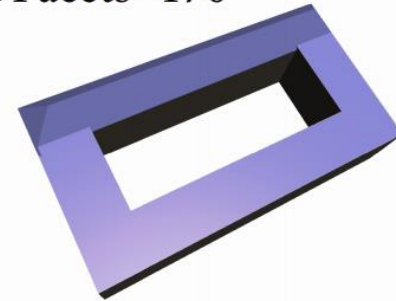
## Results & discussion: Impact of parameter $\lambda$

$$E(x) = D(x) + \lambda V(x)$$

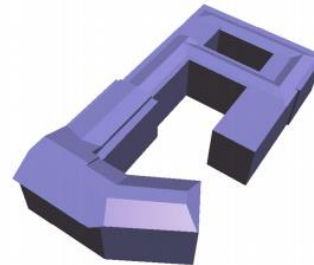
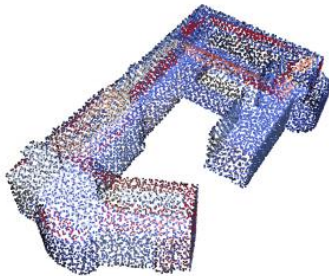
$Dist_{SMH}=0.04268$   
 $\#Facets=184$



$Dist_{SMH}=0.04324$   
 $\#Facets=170$



$Dist_{SMH}=0.07495$   
 $\#Facets=236$



$\lambda = 0.002$

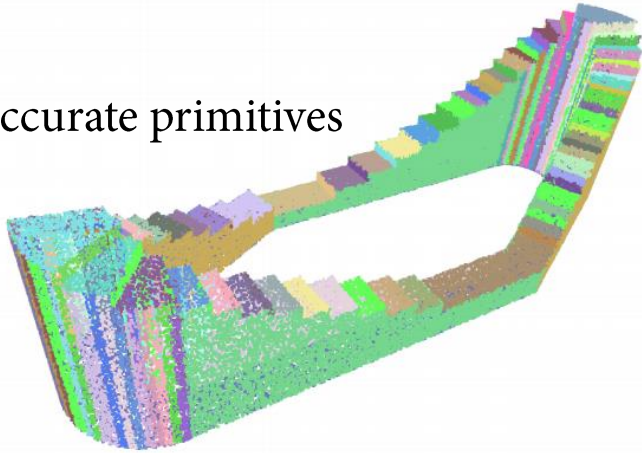
$Dist_{SMH}=0.07522$   
 $\#Facets=220$



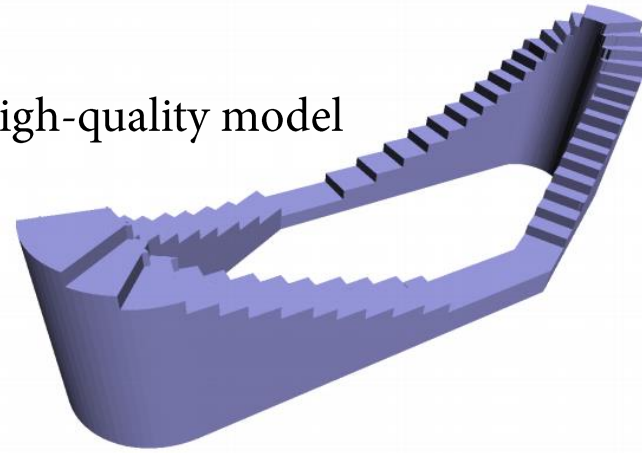
$\lambda = 0.01$

## Results & discussion: limitations

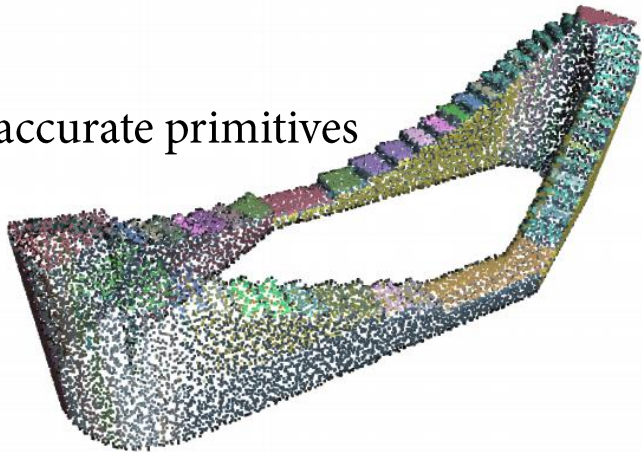
Accurate primitives



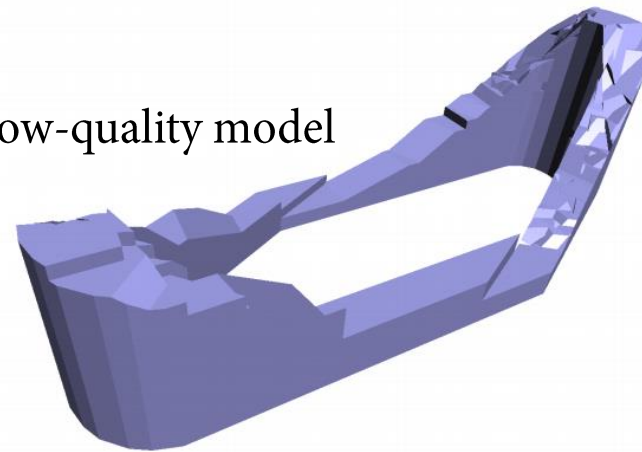
High-quality model



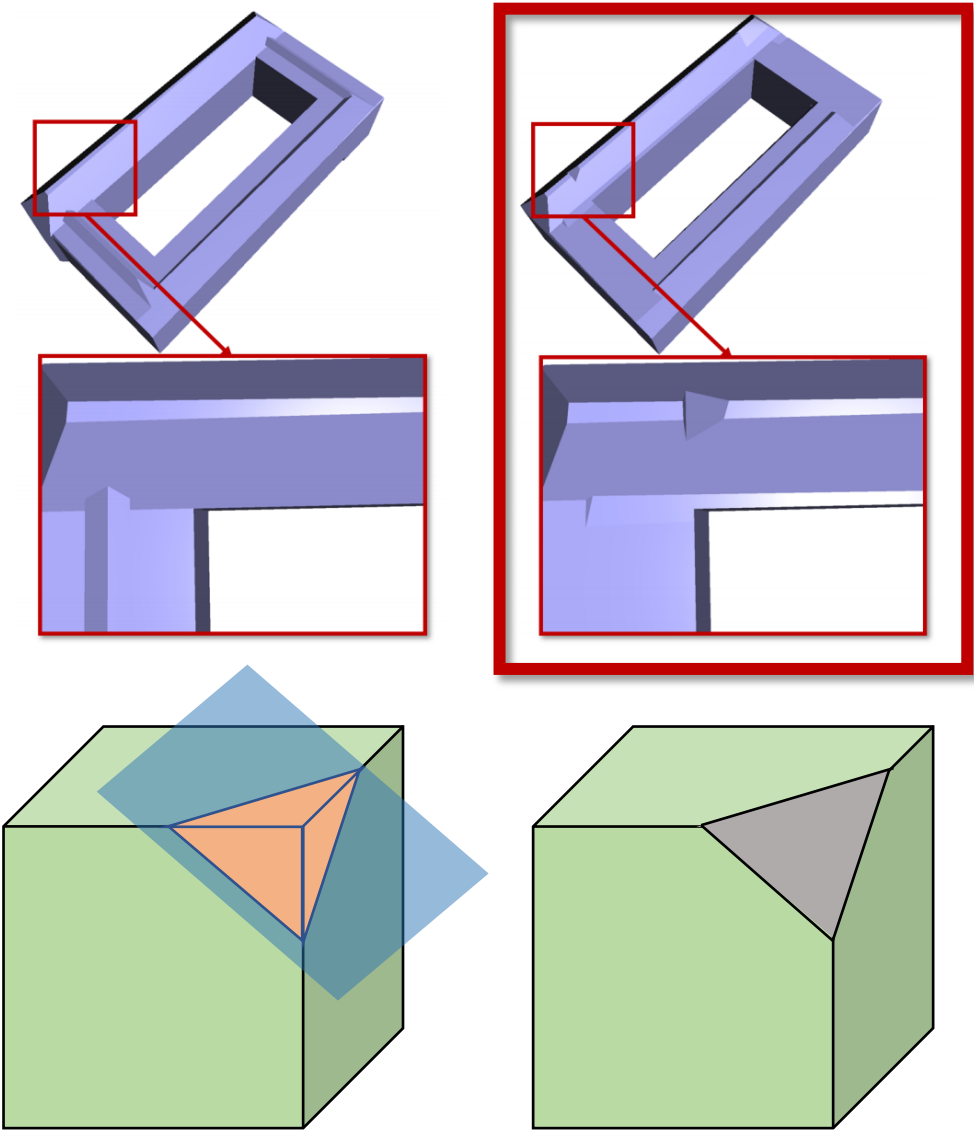
Inaccurate primitives



Low-quality model



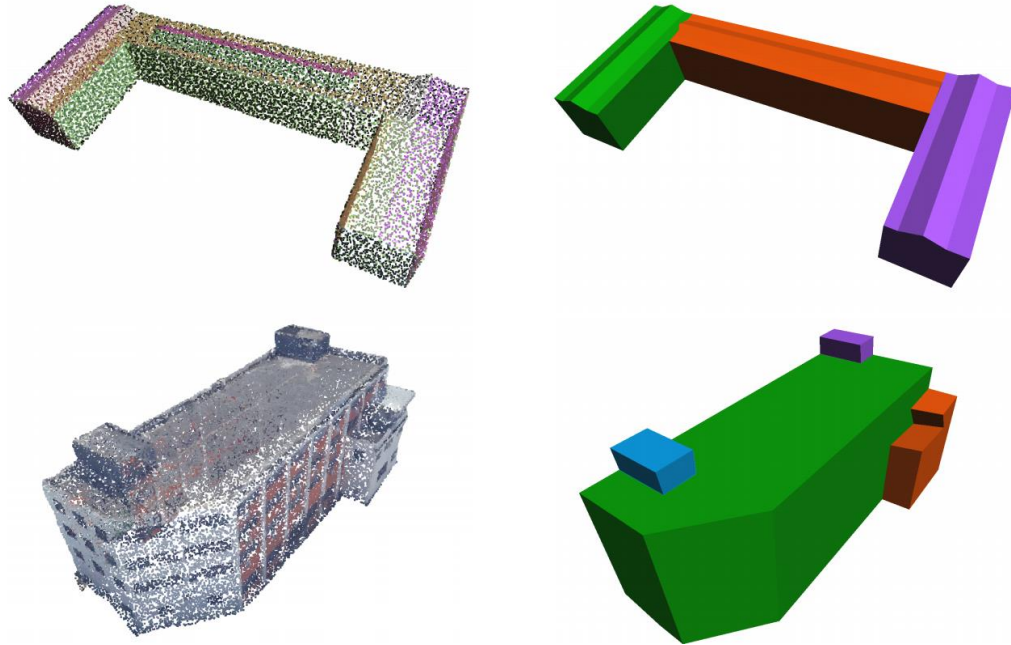
# Results & discussion: limitations



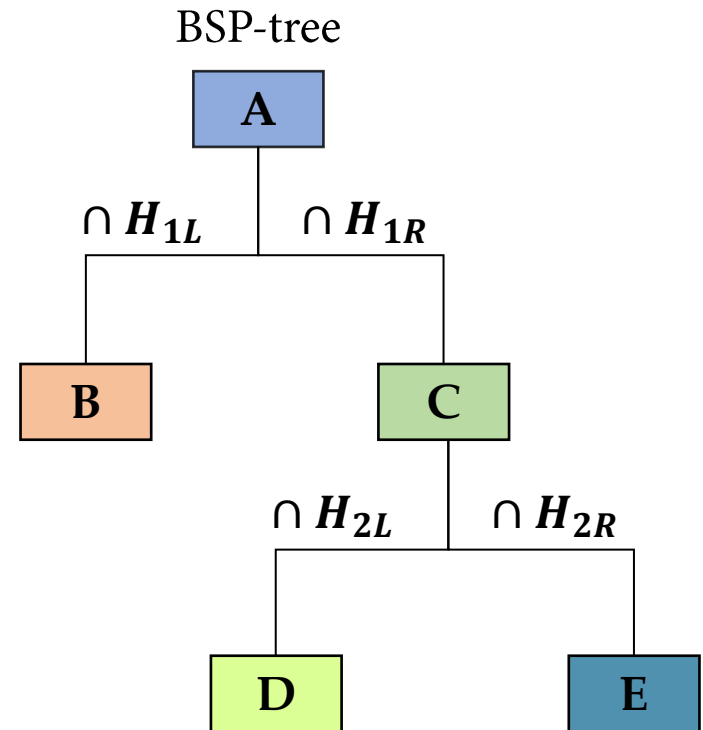
'Caved'  
artefact



# Results & discussion: Applications

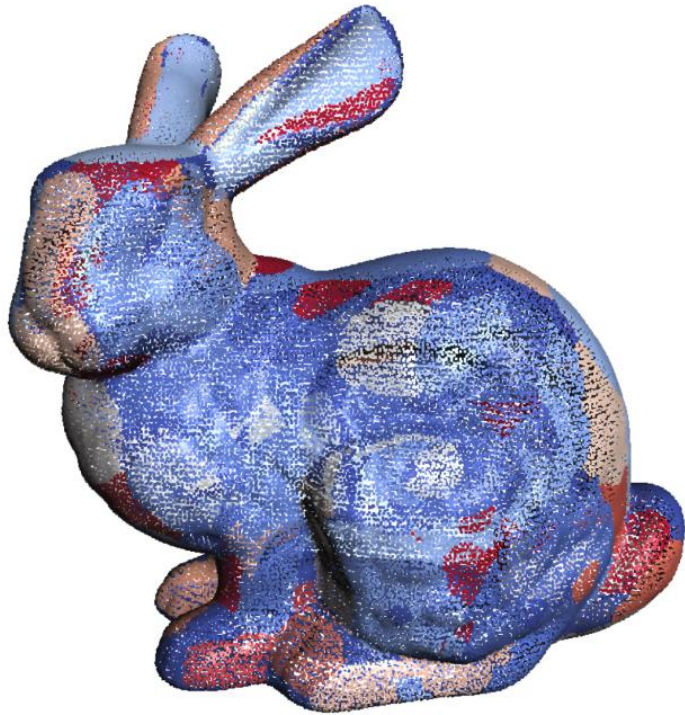


Building component analysis



## Results & discussion: Applications

- Compression
- Physical Simulation



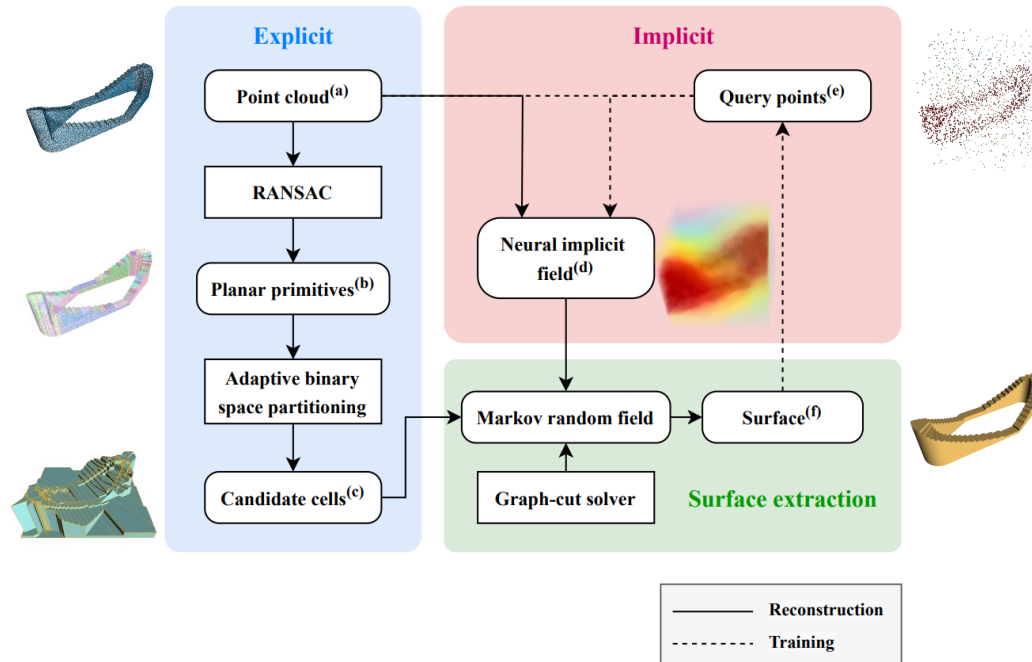
Generic shape reconstruction

- Introduction
- Related work
- Methodology
- Results and discussion
- **Conclusions**

# Conclusion: Research question revisited

*How can deep implicit fields be used for compact building model reconstruction?*

- Compactness and watertightness
- Generalisation
- Robustness
- Advantages & disadvantages



# Conclusion

## Contributions

- A learning-based framework to incorporate deep implicit fields into piecewise-planar urban building reconstruction
- An adaptive space partitioning strategy for cell complex construction
- An MRF formulation for efficient surface extraction
- Open synthetic building point cloud dataset

# Conclusion

## Future work

- End-to-end neural network architecture
- Extension to more general primitives
- .....

# Conclusion

## Source code

- <https://github.com/chenzhaiyu/absp>
- <https://github.com/chenzhaiyu/points2poly>

## Dissemination

- Thesis & Slides available at TU Delft Repositories
- ISPRS Journal manuscript in progress

## Learning to Reconstruct Compact Building Models from Point Clouds with Deep Implicit Fields

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### ABSTRACT

We present a novel framework for reconstructing compact, watertight, polygonal building models from point clouds. Our method comprises three components: (a) a cell complex is generated via adaptive space partitioning that provides a polyhedral embedding as the candidate set; (b) an implicit field is learnt by a deep neural network that facilitates building occupancy estimation; (c) a Markov random field is formulated for surface extraction via combinatorial optimisation. We extensively evaluate the proposed method in comparison with state-of-the-art methods in shape reconstruction, surface approximation and geometry simplification. Experimental results reveal that, with our neural-guided strategy, high-quality building models can be obtained with significant advantages over fidelity, compactness and computational efficiency. Our method shows robustness to noise and insufficient measurements, and generalise well directly from synthetic scans to real-world measurements.

### 1. Introduction

Three-dimensional (3D) building models play a pivotal role in shaping the digital twin of our world, and are facilitating various intelligent applications in urban planning (Herbert and Chen, 2015), solar potential analysis (Machete et al., 2018), environmental simulation (Stoter et al., 2020), etc. Recently, with the development of augmented and virtual reality applications, the demand for high-quality building modelling is growing rapidly (Blut and Blankenbach, 2021). Most reconstruction methods are dedicated to smooth surfaces represented as dense triangles, irrespective of piecewise planarity that exhibits in the built environment (Kazhdan et al., 2006; Erler et al., 2020). Simplification is therefore required as a follow-up procedure to convert the smooth surface into a compact one (Garland and Heckbert, 1997; Cohen-Steiner et al., 2004; Salinas et al., 2015; Bouzas et al., 2020). Although some works claim the possibility of reconstructing piecewise-planar shapes directly from point clouds, they suffer from serious scalability issues (Boulch et al., 2014; Mura et al., 2016; Nan and Wonka, 2017). In this work, we aim at efficiently reconstructing compact building surfaces directly from point clouds.

3D shapes are not confined to as explicit representations (e.g., point cloud, surface mesh, voxels), but can be encoded implicitly in a function space. A signed distance function (SDF), for instance, can describe an implicit field, where the surface of a shape is implicitly interpreted as zero-set of the SDF. A learnable indicator function of the SDF takes as input a query point and yields an indication on whether the

point belongs to the shape. The explicit geometry is then often extracted from the field via computational-expensive iso-surfacing (Mescheder et al., 2019). Compared with explicit expressions that are heterogeneously distributed, this homogeneous functional representation is particularly favourable for geometric machine learning. Especially recently, the scheme for learning in the function space has shown its competence in 3D geometric modelling (Park et al., 2019).

In this paper, we propose a novel framework for reconstructing compact, watertight, polygonal building meshes from point clouds by incorporating implicitly encoded function space with explicitly constructed geometry. The explicit geometry provides a polyhedral embedding as the candidate set, from which extraction of the building's surface is neural-guided by a learnt implicit field. We formulate a Markov random field (MRF) to introduce configurable surface complexity, and solve this optimisation problem using an efficient graph-cut solver. With our neural-guided strategy, we demonstrate that high-quality building models can be obtained with significant advantages over fidelity, compactness and computational efficiency against state-of-the-art methods in shape reconstruction, surface approximation and geometry simplification.

The main contributions of this paper are as follows:

- A learning-based framework for compact building model reconstruction. To the best of our knowledge, this is the first work where a deep implicit field is explored for building reconstruction. Our method shows significant performance and quality advantage over state-of-the-art methods for urban building reconstruction, especially for complex building models.
- An adaptive space partitioning solution for generating a cell complex of candidate polyhedra. Compared with the exhaustive baseline, our adaptive strategy can efficiently partition the space, minimising redundant

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**Thanks! Questions?**