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## **Unsupervised Feature Transfer for Batch Process Based on Geodesic Flow Kernel**

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Abstract: The problem of misalignment of the original measurement model is caused by nonlinear, time-varying characteristic of the batch process. In this paper, a method based on geodesic flow kernel (GFK) for feature transfer is proposed. By mapping data into the manifold space, the feature transfer from source domain to target domain is implemented. Distribution adaptation of real-time data and modeling data is performed to reduce the distribution difference between them. The historical data through distribution adaptation is used to establish a regression model to predict the real-time data, by which the unsupervised batch process soft sensor modeling is realized. The application of predicting the concentration of penicillin between different batches during the fermentation of penicillin demonstrated that the prediction accuracy of the model can be improved more effectively than the traditional soft sensor method.

Key words: Batch process, geodesic flow kernel, unsupervised, feature transfer, penicillin.

## **1** INTRODUCTION

At present, the difficulty in measuring key parameters during the batch process is mainly solved by multivariate statistical method based on measured data [1], such as Principal Component Analysis (PCA) and Partial Least Squares (PLS)-based algorithms [2,3]. However, when a large amount of process data is actually processed, there are often problems such as data drift [4], difficulties to obtain labels, and mismatch of the original model [5,6]. Multivariate statistical method is difficult to deal with such mixed dynamic characteristics.

Aiming at this problem, in [7], Artificial Neural Network (ANN) was applied to establish a soft sensor model of nonlinear process. However, its generalization ability cannot be guaranteed, so a well-trained model may lead to poor predictions of new observations. In [8], the author used Gaussian Mixture Regression (GMR) to establish multiple sub-models on historical data, and finally obtained the integrated regression model by weighting multiple sub-models according to the level of model output confidence. However, the output confidence of each sub-model is difficult to estimate for large structural risks. In [9,10], the author used the idea of Just-in-time learning (JITL), selecting the sample set that is most relevant to the current sample from the labeled historical data according to similarity metrics, and used machine learning methods to build a regression model to solve the problem of soft sensor for multiple working conditions. However, when the information of the current working condition is not included in historical data set, the established model cannot

adapt the data of the current working condition, causing the model misalignment.

Transfer learning [11,12,13] used existing knowledge to solve the target domain problem by mining the shared features between domains, which introduces new ideas for the above-mentioned multimode soft sensor. In [14], the author introduced the semi-supervised domain adapted ELM algorithm to the soft sensor field of chemical processes. By using the source domain and a small number of labeled samples in the target domain, a mathematical model was constructed to realize the soft sensor of melt index in the process of industrial polyethylene under multi-working conditions. In fact, the problem of untagged samples in the target domain is common in the actual production process, and the semi-supervised algorithm is no longer applicable.

Aiming at the problem of unlabeled target domain, manifold-based unsupervised transfer learning [15,16] has become a research hotspot. Manifold learning maps data to a reliable embedded projection to find the data representation in a low-dimensional subspace [17]. It can map different working condition data to different points on the potential continuous manifold space. Compared with Euclidean space, it can better reflect the inherent characteristics and rules between sample data of different working conditions. In [18], the author proposed an unsupervised transfer learning method based on geodesic flow for cross-domain image classification, mapping the target domain and source domain data to two points on the Grassmann manifold space [19]. In the direction of the geodesics at these two points, several intermediate points are selected and connected in order to realize the gradual domain transfer from the source domain to the target domain via the geodesic. In [20], the author further proposed a kernel method based on Grassmann manifold

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space, and realized the continuous transfer process from the source domain to the target domain by integrating an infinite number of subspaces. The results showed that compared with the Euclidean space, domain transfer in the manifold space can find the inherent rules of data between different domains.

In this paper, the feature transfer based on manifold space is introduced into the unsupervised soft sensor of batch process in the geodesic flow kernel method, and the model error caused by the large difference of data distribution in penicillin fermentation process is eliminated. The experimental results show that the soft sensor model has good availability and high measurement accuracy.

### 2 Proposed Method

#### 2.1 Subspace dimension measure

Suppose the source domain data  $X_s$  and the target domain data  $X_t$ . In order to improve the effect of feature transfer, the dimensionality of the subspace *d* needs to be determined to reduce the dimensionality of the data *D* in order to extract the main features .The protagonist concept is used [21], it can be defined as [20]:

$$\mathcal{D}(d) = 0.5[\sin\alpha_d + \sin\beta_d] \tag{1}$$

where  $\alpha_d$  denotes the *d*-th principal angle between the *PCA*<sub>S</sub> and *PCA*<sub>S+T</sub> and  $\beta_d$  between *PCA*<sub>T</sub> and *PCA*<sub>S+T</sub>. sin  $\alpha_d$  or sin  $\beta_d$  is called the minimum correlation distance[22]. The optimal dimension can be obtained by formula (2) [20]:

$$d^* = \min\left\{d \left| \mathcal{D}(d) = 1\right\}$$
(2)

#### 2.2 Construct geodesic flow

Let  $P_S, P_T \in \mathbb{R}^{D^*d}$  denote the two sets of basis of the subspaces for the source and target domains. Let  $R_S \in \mathbb{R}^{D^*(D-d)}$  denote the orthogonal complement to  $P_S$ , namely  $P_S^T P_S = 0$ . The geodesic flow is parameterized as  $\Phi: t \in [0,1] \rightarrow \Phi: t \in G(d,D)$ , under the constraints  $\Phi[0] = P_S, \Phi[1] = P_T$ . For other t [20]:

$$\Phi(t) = P_S U_1 \Gamma(t) - R_S U_2 \Sigma(t)$$
(3)

where  $U_1 \in \mathbb{R}^{d \times d}$  and  $U_2 \in \mathbb{R}^{(D-d) \times d}$  are orthonormal matrices. They are given by the following pair of SVDs [20]:

$$P_{S}^{T}P^{T} = U_{1}\Gamma(t)V^{T}, R_{S}^{T}P^{T} = -U_{2}\Sigma(t)V^{T}$$

$$\tag{4}$$

 $\Gamma$  and  $\Sigma$  are  $d \times d$  diagonal matrices. The diagonal elements are  $\cos \theta_i$  and  $\sin \theta_i$  for i = 1, 2, ..., d. Particularly,  $\theta_i$  are called the principal angles between  $P_S$  and  $P_T$ :

$$0 \le \theta_1 \le \theta_2 \le \dots \le \theta_d \le \pi / 2 \tag{5}$$

Moreover,  $\Gamma(t)$  and  $\Sigma(t)$  are diagonal matrices whose elements are  $\cos(t\theta_i)$  and  $\sin(t\theta_i)$  respectively.

#### 2.3 Compute geodesic flow kernel

Moving from the source domain to the target domain, the process of transfer from  $\Phi(0)$  to  $\Phi(1)$ , the new feature can be expressed as:

$$z = g(x) = \Phi(t)^T x$$
(6)

The geodesic flow kernel is defined as [20]:

$$\left\langle z_{i}^{\infty}, z_{j}^{\infty} \right\rangle = \int_{0}^{1} \left( \Phi\left(t\right)^{T} x_{i} \right)^{T} \left( \Phi\left(t\right)^{T} x_{j} \right) dt = x_{i}^{T} G x_{j}$$
(7)

where  $G \in \mathbb{R}^{D \times D}$  is a positive semidefinite matrix, it can be calculated by equation [20]:

$$G = \begin{bmatrix} P_{S}U_{1} R_{S}U_{2} \end{bmatrix} \begin{bmatrix} \Lambda_{1} & \Lambda_{2} \\ \Lambda_{2} & \Lambda_{3} \end{bmatrix} \begin{bmatrix} U_{1}^{T} R_{S}^{T} \\ U_{2}^{T} R_{S}^{T} \end{bmatrix}$$
(8)

where  $\Lambda_1, \Lambda_2, \Lambda_3$  are diagonal matrices, whose diagonal elements are:

$$\lambda_{1i} = 1 + \frac{\sin(2\theta_i)}{2\theta_i}, \lambda_{2i} = \frac{\cos(2\theta_i) - 1}{2\theta_i}, \lambda_{3i} = 1 - \frac{\sin(2\theta_i)}{2\theta_i}$$
(9)

A sample z that transfer the original sample features x along the geodesic direction can be obtained by:

$$z = \sqrt{G}x\tag{10}$$

Then the sample  $z_s$  mapped from  $x_s$  in the source domain can be obtained, so as  $z_t$  mapped from  $x_t$  in the target domain, and the existing labeled sample  $z_s$  can be modeled to predict the label of the sample  $z_t$ .

#### 2.4 Unsupervised feature transfer based on GFK

This paper takes into account the difference in data distribution after batch changes and the potential associations between different batches [23], and a soft sensor modeling method based on transfer learning is introduced. The transfer from the source batch to the target batch is completed by GFK. The purpose of predicting the concentration of penicillin is achieved. Figure 1 is the schematic diagram of the method.

Multi-batch soft sensor based on geodesic flow kernel combines pre-processed known batches of labeled (source domain) samples  $X_s$  and unknown batches of unlabeled (target domain) samples  $X_t$  into overall data set  $X = [X_s, X_t]$ . The optimal dimension  $d^*$  is obtained by  $PCA_{X_i}$  and  $PCA_{X_i}$ , and source and target datasets are embed in a Grassmann manifold.  $PCA_{X_t}$  and  $PCA_{X_t}$  are used as the subspace  $P_s$  and  $P_T$  in the GFK framework. Considering  $P_s$  and  $P_T$  as two points in the higher dimensional space, a geodesic flow is constructed between the two points, and then integrate an infinite number of subspaces along the flow  $\Phi(t)$ . Concretely, raw features are projected into these subspaces to form an infinite-dimensional feature vector. Inner products between these feature vectors define a kernel function that can be computed over the original feature space in closed-form.



Figure 1. Schematic of the method

Thus, through equations (7), the geodesic flow kernel is formed. The task of feature transfer from source domain to target domain is completed by the geodesic flow.

Finally, a soft sensor model is established using the adapted source domain sample and the source domain label to achieve prediction of the target domain label. The algorithm of proposed method is shown in Table 1.

Table 1. The proposed method algorithm

**Input**: the source domain sample  $X_s$ , the target domain sample  $X_t$ , the source domain label  $Y_s$ .

**Output**: the target domain label  $Y_t$ .

1: Data preprocessing.

2: Calculating the optimal dimension  $d^*$  according to equations (1) and (2).

3: Constructing the geodesic flow  $\Phi(t)$  by equation (3), getting the matrix *G* in the geodesic flow kernel according to equations (8) and (9), and obtaining the transferred data  $z_s$  and  $z_s$ , with equation (10).

4: Using  $z_s$  and the source domain label  $Y_s$  to train a PLSR soft sensor regression model f.

5: Getting the target domain label  $Y_t$  based on f and  $z_t$ .

## 3 Experiments

Penicillin is the first large-scale clinically purified antibiotic used in humans. The penicillin fermentation process is a typical biochemical reaction process. It is a metabolic activity of penicillin-producing bacteria to grow and synthesize antibiotics under appropriate fermentation conditions [24,25].

In this paper, penicillin concentration, which was often analyzed offline during penicillin fermentation, was selected as the target variable. Table 2 lists process variables with high correlation as inputs to the soft sensor. Samples were collected every 0.5 hours during a 400-hour fermentation process, thus 800 samples were obtained, and the first five batches were selected as five different working conditions for transfer.

No.	Variable description	unit
1	Culture time	h
2	Aeration rate	L/h
3	Agitator power	W
4	Substrate feed rate	L/h
5	Substrate feed temperature	K
6	Substrate concentration	g/L
7	Dissolved oxygen concentration	g/L
8	Biomass concentration	g/L
9	Culture volume	L
10	Carbon dioxide concentration	g/L
11	pH	-
12	Fermenter temperature	K
13	Generated heat	kcal
14	Acid flow rate	L/h
15	Base flow rate	L/h
16	Cold water flow rate	L/h
17	Hot water flow rate	L/h

Table 2. Input variables for penicillin fermentation process

In order to quantify the prediction performance of various methods, root mean square error (RMSE) is used as the evaluation standard for measurement accuracy. The calculation formula is as follows:

RMSE = 
$$\sqrt{\frac{1}{N} \sum_{i=1}^{N} (\hat{y}_i - y_i)^2}$$
 (11)

where  $\hat{y}_i$  and  $y_i$  represent the actual value and predicted value of the *i*-th sample, respectively, N is the number of test samples.

It is assumed that the known condition is the source domain and the condition to be measured is the target domain. In the experiment, PCA, PLS, ANN, GMR, JITL methods were used for comparison.

Figure 2 depicts the predicted result of penicillin concentration of each unsupervised method. It can be seen that under the same batch conditions, when the source batch and the target batch have a large difference in distribution, the accuracy of proposed method is higher compared with other methods. Figure 3 depicts the predicted result of GFK under the other batch conditions. The predicted value

2020 Chinese Control And Decision Conference (CCDC 2020)



can well track the measured value under all batch conditions, reflecting the advantages of proposed method. Table 3 describes the comparison result of penicillin concentrations predicted by different soft sensors under all batch conditions. The leftmost column " $n\rightarrow m$ " indicates the transfer from the nth batch to the mth batch. The last line represents the mean of RMSE of each algorithm. In order to compare the effects of different methods more intuitively, Figure 4 describes the evaluation accuracy of transfer to other batches when batches 1-5 are regarded as the source domain. Compared with the other prediction models, the proposed method achieved better predictive effect for the distribution adaptation of the source batch to the target batch by mapping the subspace to the manifold space for feature transfer.



Figure 4. The average transfer result of source batches 1-5

Table 3.	The com	parison o	f root mea	n square	error of	different	algorithms	in each	batch

Batch	РСА	PLS	ANN	JITL	GMR	GFK
1→2	0.0520	0.1392	0.0373	0.0568	0.0486	0.0469
1→3	0.0806	0.1871	0.1219	0.1205	0.0684	0.0552
1→4	0.1437	0.1869	0.1425	0.1564	0.1008	0.0686
1→5	0.3179	0.3603	0.1347	0.6369	0.1122	0.1078
2→1	0.0541	0.0836	0.0449	0.0536	0.0594	0.0441
2→3	0.1444	0.1247	0.0566	0.0701	0.0574	0.0347
2→4	0.1635	0.1862	0.1335	0.1131	0.1256	0.0949
2→5	0.3116	0.2553	0.1633	0.1874	0.1327	0.0997
3→1	0.0662	0.0672	0.0798	0.0815	0.0734	0.0526
3→2	0.0679	0.0568	0.0743	0.0569	0.0531	0.0335
3→4	0.2098	0.1711	0.1249	0.1104	0.1260	0.0992
3→5	0.4631	0.3321	0.1360	0.0921	0.1301	0.0893
4→1	0.1223	0.2196	0.0669	0.0821	0.0781	0.0664
4→2	0.1464	0.2563	0.1001	0.1126	0.1003	0.0971
4→3	0.1579	0.2721	0.1494	0.1216	0.1082	0.1060
4→5	0.2485	0.4444	0.1365	0.1121	0.0692	0.0506
5→1	0.0824	0.5533	0.1184	0.1047	0.0804	0.0755
5→2	0.0921	0.5949	0.1126	0.0989	0.0923	0.0551
5→3	0.1730	0.5637	0.1297	0.0963	0.0985	0.1067
5→4	0.0787	0.3935	0.0924	0.0769	0.0783	0.0515
Average	0.1588	0.2724	0.1078	0.1270	0.0897	0.0717

#### 4 Conclusion

In order to address the difficult problem of misalignment of the original measurement model is caused by complexity of the batch process. The unsupervised soft sensor for batch process based on geodesic flow kernel is used in this paper. According to utilizing common features between multiple batches and extracting similar knowledge structures to the target batch in the source batch, the performance of unsupervised soft sensor is improved. The concentration prediction during the multi-batch penicillin fermentation process is applied. The practicability and effectiveness of the model is illustrated by comparing experiments and cross experiments.

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