Effects of Anticipatory Control with Multiple User Classes

TRAIL Research School, Delft, November 2002

Authors

Ir. Henk Taale, Prof. dr. H.J. van Zuylen

Faculty of Civil Engineering and Geosciences, Delft University of Technology AVV Transport Research Centre

© 2002 by Ir. Henk Taale, Prof. dr. H.J. van Zuylen and TRAIL Research School

Abstract

1	Introduction	227
1.1	Problem description	227
1.2	Solutions Approaches	227
1.3	Research Aspects	228
1.4	Paper contents	229
2	Control Strategies	230
2.1	Webster	230
2.2	Smith's P ₀	231
2.3	Anticipatory Control	231
2.4	System Optimum Control	232
3	Algorithms	234
3.1	Traffic Modelling	234
3.2	Traffic Assignment	236
3.3	Solution Algorithms	237
4	Case Studies	240
4.1	Case description	240
4.2	Results	241
5	Conclusions and Further Research	243
Refere	ences	244



In this paper the integrated traffic control and traffic assignment problem is studied. This problem can be considered as a non-cooperative game in which the traffic authority, that controls the traffic signals, and the road users are the players, who use their own strategy and seek their own optimum. The game theoretical formulation leads to several different control strategies in which users' reactions to traffic control decisions are taken into account. Users' reactions can be the choice of route, departure time or even mode, but here only route choice is considered.

In this paper some of these control strategies for traffic signal control are described: Webster control, Smith's P_0 , Anticipatory Control and System Optimum Control. The first two control strategies are well known and described in the literature. The anticipatory control strategy can be formulated as a bi-level optimisation problem and this problem is solved using genetic algorithms. Also the system optimum solution can be found using genetic algorithms, simultaneously optimising route flows and green times.

In the paper the assignment method, together with the traffic model are formulated. In the assignment several user classes, each with its own perception of route costs, are defined and taken into account. For several simple example networks the traffic control methods are tested and it is shown that taking route choice into account is beneficial to the network performance. Further research will focus on the improvement of the traffic model used in the control optimisation, realistic networks and the problem of departure time choice.

Keywords

anticipatory traffic control, stochastic assignment, game theory, user classes



1.1 Problem description

Traffic control and traveller's behaviour are two processes that influence each other. The two processes have different 'actors' who may have different goals. The road manager will try to achieve a network optimum and will try to control traffic in such a way that this optimum is reached. Tools for controlling traffic are for example traffic signals, traffic information, ramp metering, etc. The optimum for the road manager can be minimum network delay or a preferential treatment for certain user groups, e.g. public transport or pedestrians (system optimum). The road users will search for their own optimum, e.g. the fastest or cheapest way to travel from A to B (user optimum). Decisions taken by the road manager in controlling traffic in a certain way have an influence on the possibilities for travellers to choose their preferred mode, route and time of departure, and vice versa. A change in traffic control may have the impact that traffic volumes change. If, for example, traffic control is modified such that congestion on a certain route disappears and delays on intersections decrease, traffic might be attracted from other links where congestion still exists or which are part of a longer route. This might have the consequence that queues, which originally disappeared, return. Delays may reappear at the original levels (Van Zuylen, 2001). The question is then whether there still is a net profit for the traffic system as a whole. The same question arises with respect to new traffic that may emerge as a consequence of shorter travel times, due to either elastic demand or induced demand. Another example is that public transport gets priority in intersection control. The delay for other road users may increase and thus force these road users to search for other routes, departure times or even transport modes in the network (Mordridge, 1997).

1.2 Solutions Approaches

If it is assumed that a modification in traffic control gives a change in travel behaviour, it is necessary to anticipate this change. If delays are optimised, it should be done for the traffic volumes that will be present after the introduction of the optimised traffic control and not for the traffic volumes that existed before the implementation. If the reaction of travellers is neglected in the optimisation of traffic control, the results may even be just opposite to the desired improvement. Mordridge shows that the improvement of the traffic condition for cars in a network with cars and public transport may cause a modal shift from public transport to the car, which at the end deteriorates the travel conditions for both modes (Mordridge, 1997).

Of course, it is possible to follow an interactive approach, where after each shift in traffic volumes the control scheme is adjusted until equilibrium has been reached, or one may use self-adjusting traffic control. However, it can be shown, for certain examples, that the process of the adjustment of traffic control, followed by a shift in traffic volumes, does not necessarily lead to a system optimum. It is even possible that the system oscillates between two or more states. This arises from the fact that the system optimum is not necessarily the same as the user optimum. The system optimum is good for the network as a whole, but can be disadvantageous for a part of the travellers in the network. The control problem is therefore to optimise traffic control in such a way that the system is at a certain, prescribed optimum, taking into

account the reaction of travellers. This is called the combined traffic assignment and control problem. More than 25 years this problem has been the subject of study. For an extensive overview one is referred to Taale and Van Zuylen (2001).

The reaction of users on traffic management measures has been included in many models that simulate the dynamics of traffic flows in networks. The shift of routes as response to travel times and traffic information is a standard feature of most dynamic traffic assignment models, some take also the shift in departure time into account. Very few give also an estimate of modal shifts, the shift in the demand-supply equilibrium and reallocation of activities. The optimisation of traffic control and traffic information, taking into account the response of travellers, is still less common. If one classifies the available literature, a distinction can be made between three different approaches to solve the combined assignment and control problem. The first is the iterative approach, which solves both problems separately and uses the outcome of one problem to serve as the input for the other problem. Most of the time this iterative process converges to a solution, although it cannot be proven that a unique solution exists. Van Zuylen and Taale (2000) showed for some examples that multiple solutions can exist and that some of them might be meta-stable. In game theoretical terms this can be considered a Cournot game, where the road manager and the road users are the two players who react on each other's moves, but don't have any knowledge about each other's behaviour. The second approach is the anticipatory optimisation approach. This approach still solves both problems one at the time, but in the optimisation of traffic control the reaction of the road users (e.g. route choice) is taken into account. In game theory this is called a Stackelberg game, where the road manager and the road users are two players and the road manager can anticipate the road users moves, because he has certain knowledge about their behaviour. The third approach solves both problems simultaneously and aims at a control policy that optimises globally, taking into account users' behaviour. Game theory calls this the monopoly game, where one player (in this case the road manager) can optimise the control with the assumption that the other player (the road users) obeys his directives. The game-theoretical approach is similar to the bi-level programming formulation, which is used to solve the combined optimisation problem in the more recent literature (Clegg et al, 2001 and Maher et al, 2001). The bi-level programming approach formulates the problem as two sub-problems and solves them simultaneously on two levels. Assumptions about the information known to the decision makers on the upper and lower level sub-problems determine which of the three approaches described above is used.

1.3 Research Aspects

From the literature it can be concluded that previous research was restricted to traffic signal control and route choice most of the time. Other aspects such as other traffic control measures and other travel choices (e.g. departure time) were rarely taken into account. In most references a static demand is assumed and the optimisation of the traffic control is restricted to green times only. The way in which delay is calculated varies: most of the time a delay formula (Webster's or TRANSYT) is used, but sometimes also simulation models, such as SATURN or DYNASMART. It must be emphasised that in most cases formulas are used that are not capable of handling oversaturated conditions and therefore lack practical relevance, because route choice in a network depends strongly on the network conditions and level of congestion. Other

In this paper the focus will be on the comparison of several control strategies for a number of small example networks. All cases have dynamic demand and cycle time optimisation is included in all control strategies. For the evaluation of the control strategies in the main loop the microscopic simulation model FLEXSYT-II- is used. The reader is referred to Taale and Middelham (1995) for more details. For the optimisation within some control strategies, a simple traffic model is used. The model propagates traffic through the network with some relations like the conservation of flow. It also calculates travel times, using specific delay functions.

The goal of the research is to determine the effects of anticipatory control for several small, artificial networks, in comparison with traditional control strategies. To make the route choice as realistic as possible, several user classes are defined, which differ in their route choice behaviour.

1.4 Paper contents

The paper is structured as follows. First, in chapter 2 the control strategies tested are described. In chapter 3 the traffic model and the traffic assignment method are specified and the solution algorithm is given. In the next chapter the example networks are sketched together with their characteristics and the results for all examples and all control strategies are given. Finally, conclusions are drawn and items for further research are briefly mentioned.

2 Control Strategies

Optimisation of traffic signal control is one of the oldest research fields in traffic engineering. The subject has drawn the attention of many researchers. In this paper several old and new control strategies are described and tested. The purpose is to study the interaction of these control strategies with route choice. Within all control strategies only the green times are varied between minimum and maximum values. The cycle time is not fixed, but is a result of the green times used. The results of all strategies are compared with the results of fixed-time control. The fixed-time control strategy is optimised for the demand of the busiest time period, using Webster's strategy, described in the next section.

2.1 Webster

Already in the fifties Webster published his famous report on the optimisation of fixed-time traffic control (Webster, 1958). In his work Webster did a theoretical analysis and carried out a lot of simulations to derive a formula for the average delay due to signal control. His formula for the average delay for a vehicle is:

$$d = \frac{C(1 - (g/C))^2}{2(1 - (g/C)x)} + \frac{x^2}{2q(1 - x)} - 0.65(\frac{C}{q^2})^{\frac{1}{3}}x^{2 + 5(g/C)}$$
(1)

where d is the average delay per vehicle in seconds, C decycle length in seconds, g the effective green time in seconds, x the degree of saturation defined as (q/s)*(g/C) (demand divided by the saturation flow and multiplied with the green fraction) and q the arrival rate in vehicles per second. In most applications of this formula the third term is omitted and replaced by a multiplication with 0.9. The formula then reads

$$d = 0.9\left(\frac{C(1 - (g/C))^2}{2(1 - (g/C)x)} + \frac{x^2}{2q(1 - x)}\right)$$
 (2)

Webster used these formulas to derive a general, optimal fixed-time control plan. He found that the general formulas for an optimal cycle time and the accompanying green times are

$$C = \frac{1.5L + 5}{1 - Y}, \text{ where L = lost time per cycle and } Y = \sum_{m} y_{m} = \sum_{m} \frac{q_{m}}{s_{m}}$$

$$g_{m} = \frac{y_{m}}{Y}(C - L)$$
(3)

It is known that other coefficients than 1.5 and 5 can give better results in other circumstances (Van Zuylen, 1980), but in this paper formula (3) is used to calculate new cycle times and new green times for every time period and every intersection for the flows entering that intersection. This means that the control plan changes due to changing route flows. In the algorithm used minimum and maximum hours for the

2.2 Smith's P₀

According to Smith three solution methods for the combined traffic assignment and control problem are possible: the iterative approach, the integrated approach and a generalisation of the iterative approach taking the control strategy into account (Smith, 1985). The control strategy P_0 is the result of this approach (Smith, 1980). Smith also showed that the P_0 control strategy complies with three conditions for equilibrium (flow, queues and control) and that using P_0 simplifies calculating a solution (Smith, 1987). It has capacity maximising properties, because it does not try to equalise the delays for every conflicting movement, but the product of delay and saturation flow.

The P_0 control strategy is implemented as a minimisation problem. For every intersection and every time period the product of delay and saturation flow for all conflicting movements is equalised and minimised. The saturation flow is given and the delay is estimated with the HCM 2000 delay formulas (TRB, 2000). In these formulas the average delay in seconds per vehicle is estimated with

$$d = d_1 + d_2 + d_3 \tag{4}$$

where

$$d_{1} = \frac{C(1 - g/C)^{2}}{2(1 - \min(1, x)(g/C))}$$

$$d_{2} = 900T_{f} \left((x - 1) + \sqrt{(x - 1)^{2} + \frac{8xKI}{QT_{f}}} \right)$$
(5)

The extra term d_3 is a term for additional delay due to non-zero queues at the start of the analysis period. With this term the time dependency is better, because the delay resulting from queues from the previous period are taken into account. In the formulas for d_1 and d_2 the variables are the same as before. Q the capacity of the signal controlled lanes in vehicles per hour (Q=sg/C, where s is the saturation flow in vehicles per hour), T_f the time interval in hours for which d is calculated and during which the arrival rate q is constant. The additional parameters K and I stand for a parameter for the given arrival and service distribution (e.g. 0.5 for fixed-time control) and a parameter for variance to mean ratio of arrivals from upstream signals (e.g. 1.0 for Poisson arrivals) respectively.

2.3 Anticipatory Control

The control strategies described above are reactive, meaning that they react on the current traffic conditions. It is also possible to anticipate on future traffic conditions, taking into account route choice. To that end, traffic assignment can be incorporated in the traffic control strategy. This can be formulated as a bi-level optimisation problem. In game theory this is called a Stackelberg game. The first two control strategies lead to a Cournot game. In the upper level problem the traffic manager tries to minimise the total travel costs

$$\min_{\mathbf{g}} Z_{\mathbf{g}} = \sum_{k} \sum_{o,d} \sum_{\mathbf{g} \in \mathbb{R}^{od}} (\mathbf{g}, \bar{\mathbf{f}}) \bar{f}_{k}^{rod}, \quad \mathbf{g} \in G$$
 (6)

In this formula is o an origin, d a destination, R^{od} the set of feasible routes between o and d, r a possible route, k the departure time interval, f_k^{rod} the route flow between o and d for route r departing during time interval k, c_k^{rod} the accompanying costs for this route flow (possibly travelling in more than one time interval) and G the set of feasible green times. The mark on the route flows f means that the route flows are in equilibrium, which is the solution to the lower level, dynamic traffic assignment problem (see paragraph on traffic assignment). So the road manager performs his optimisation for network flows that are constrained by the requirements of the user equilibrium.

To solve this problem, not an analytical, but a heuristic approach is used. Every feasible combination of green times can be seen as a point in the solution space G. To find the best combination, use is made of genetic algorithms. Genetic algorithms are part of the larger family of evolutionary algorithms. In general, evolutionary algorithms mimic the process of natural evolution, the driving process for the emergence of complex and well adapted organic structures, by applying variation and selection operators to a set of candidate solutions (population) for a given optimisation problem. In the past some simulation experiments with genetic algorithms have been carried out (see for example Foy et al, 1992; Hadi and Wallace, 1993 and 1994; Montana and Czerwinski, 1996; Clement and Anderson, 1997). From these experiments it can be concluded that using genetic algorithms to find optimal timing plans for intersections, which adapt to the actual traffic situation, is a promising idea. For the Dutch situation, with a lot of local, advanced vehicle actuated traffic signal control, the use of evolutionary algorithms to adapt the maximum green times (one of the important parameters of vehicle actuated control) according to the changing conditions was also studied with fairly good results (see Taale et al, 1998; Taale, 2000 and 2002).

For this paper a real valued genetic algorithm was used, implemented as a MATLAB® toolbox, which is named the Genetic Algorithms for Optimisation Toolbox (GAOT) (Houck et al, 1995). In the case of Anticipatory Control a member of the population (solution space) is a vector of green times of all intersections and time periods. Every member is evaluated using traffic assignment and simulation in an iterative way (see also figure 1). Because it takes a lot of time to iterate towards equilibrium, the number of iterations can be limited. This can be considered as predicting a few days ahead in a day-to-day route choice process. In the calculations described below, a choice of one day has been used. Predicting further ahead improves the final result, but not that much (Taale and Van Zuylen, 2003) The result of this process is a combination of green times that takes future traffic conditions, with respect to route choice, into account.

2.4 System Optimum Control

The system optimum control strategy is not really a practical one, but it is a kind of benchmark, useful to compare with other control strategies, because it represents the best that can be achieved if the traffic manager has total control. In some cases the road manager is able to impose route choice to the road users by regulations (one-way

$$\min_{\mathbf{g},\mathbf{f}} Z = \sum_{k} \sum_{o,d} \sum_{r \in R^{od}} c_k^{rod}(\mathbf{g},\mathbf{f}) f_k^{rod}, \quad \mathbf{g} \in G, \mathbf{f} \in F$$
 (7)

The flows don't have to be in equilibrium, but have to belong to the set of feasible route flows F. Again, genetic algorithms, implemented in the GAOT MATLAB® files, have been used to solve this optimisation problem. In this case a member of the population is a vector with route flows and green times for every time period. Genetic algorithms do not guarantee an optimal solution, but they will approach it fairly close, dependent on the number of generations and the size of the population. An advantage of genetic algorithms is that local optima are avoided; a disadvantage is the calculation time needed.

3 **Algorithms**

In the work described in this paper, a choice has been made to use simulation, both in the evaluation of control strategies as in the traffic assignment procedure, which is basically an iterative approach. The iterative approach is used, because of the possibility to handle different control types realistically and more reliable. Also, with simulation, the problems with the analytical description of the complex, non-linear behaviour of traffic flow is circumvented (Abdelfatah and Mahmassani, 1998 and 2001). In the traffic assignment procedure the microscopic simulation model FLEXSYT-II- is used (Taale and Middelham, 1995) and for the evaluation of the control strategies a simple, analytical model is used, which is described in the next paragraph. After that the traffic assignment and solution algorithms are described.

3.1 Traffic Modelling

The traffic model is a simple demand/capacity model that uses travel time functions to calculate link travel times. For that purpose the travel time functions described by Akçelik (1981 and 1991) and functions from the HCM 2000 (TRB, 2000) are used. These functions can be used for uncontrolled and controlled links. An advantage of the HCM 2000 formulas is that they take the initial queue into account. For uncontrolled links the travel time is estimated with

$$t = \frac{l}{v_{free}} + 0.25 \cdot T_f \left[(x - 1) + \sqrt{(x - 1)^2 + \frac{8 \cdot J_a \cdot x}{s \cdot T_f}} \right]$$
 (8)

where l is the link length, v_{free} is the free speed on that link, s the saturation flow, T_f the analysis period for which the arrival rate q is constant, x the degree of saturation (q/s) and J_a the so-called delay parameter. This parameter is dependent on the type of road and has a small value for motorways and larger values for arterials or secondary streets. For controlled links with no initial queue the travel time is estimated with

$$t = \frac{l}{v_{free}} + \frac{C(1 - g/C)^{2}}{2(1 - \min(1, x)\frac{g}{C})} + 900T_{f} \left[(x - 1) + \sqrt{(x - 1)^{2} + \frac{8 \cdot k \cdot I \cdot x}{Q \cdot T_{f}}} \right] \qquad x > 1$$

$$t = \frac{l}{v_{free}} + \frac{C(1 - g/C)^{2}}{2(1 - \min(1, x)\frac{g}{C})} \qquad x \le 1$$

$$(9)$$

where C is the cycle time in seconds, g the effective green time in seconds, Q the capacity of the signal controlled lanes in vehicles per hour (Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour <math>(Q=sg/C, where s is the capacity of the signal controlled lanes in vehicles per hour of the signal capacity of the signal capacity of the signal capasaturation flow in vehicles per hour) and x is the degree of saturation (x=q/Q). The additional parameters K and I stand for a parameter for the given arrival and service distribution (e.g. 0.5 for fixed-time control) and a parameter for variance to mean ratio of arrivals from upstream signals (e.g. 1.0 for Poisson arrivals) respectively.

If an initial queue is present an extra delay term d_3 (sec/veh) is added, which is

defined as

z - j

where W is the initial queue in the previous period (in vehicles), t the period (in hours) of unmet demand in T_f and u a delay parameter. Further details can be found in (TRB, 2000).

Input for the model is a network consisting of nodes and links, with their attributes. The nodes are described by their type (normal, origin node, destination node or controlled node) and their incoming and outgoing links. The links have attributes such as length, number of lanes, saturation flow and desired speed. Also different link types are distinguished: normal links, signal controlled links or metered links. Other input for the model is a set of general parameters, such as the number of time periods, the duration of these time periods and the length of the time step, which is used in the calculations. The length of the time step is maximised by the time a vehicle can travel the shortest link with free flow speed. Also origins and destinations have to be specified, including an OD table with the demands. Because a route based assignment is used, for every OD pair a set of feasible routes has to be specified. For the traffic model itself, the following algorithm is used:

Algorithm 1: Simple Traffic Model (T-Model)

Step 1: Initialise

- 1.1: determine general parameters, link and node attributes;
- 1.2: calculate incoming and outgoing saturation flows per node;
- 1.3: give every link an initial flow according to the demand.

Step 2: Main loop for every time step:

- 2.1: determine free flow travel time and capacity (depends on control) per link;
- 2.2: calculate travel time and delay per link with Akçelik travel time functions;
- 2.3: compute the outflow and the remaining space for every link, taking into account downstream queues;
- 2.4: for every node compute the inflows and outflows;
- 2.5: determine the inflows for every link;
- 2.6: calculate for every link the flows for the next time step.

Step 3: Route delays and travel times:

- 3.1: initialise variables;
- 3.2: calculate route delays and travel times per time step;
- 3.3: calculate route delays and travel times per time period;
- 3.4: calculate total time spent and total delay.

The T-Model is quit simple, but gives reasonable results and is very fast in calculations. Therefore, T-Model is used as the objective function in the genetic algorithms.

3.2 Traffic Assignment

The road user is assumed to obey the route-based discrete-time dynamic traffic equilibrium, which can be defined as:

For each origin-destination (OD) pair, the route travel costs for all users, travelling between a specific OD pair and departing during a specific time interval are equal, and less than (or equal to) the route travel costs which would be experienced (or perceived, in case of a stochastic assignment) by a single user on any unused feasible route (Chen 1999 and Bliemer, 2001).

In formulas this definition can be expressed as

$$(f_k^{rod} > 0 \Rightarrow c_k^{rod} = \pi_k^{rod}), \qquad \forall o, d, r \in \mathbb{R}^{od}, k$$
 where

$$\pi_k^{od} \equiv \min_{r \in \mathbb{R}^{od}} c_k^{od}, \qquad \forall o, d, k$$
 (12)

The traffic assignment problem can be formulated as a discrete time (finite dimensional) variational inequality problem: find an $\bar{f} \in \Omega$ such that

$$\sum_{o,d} \sum_{r \in \mathbb{R}^{od}} \sum_{k} c_k^{rod}(\mathbf{g}, \bar{\mathbf{f}}) (f_k^{rod} - \bar{f}_k^{rod}) \ge 0, \ \forall \mathbf{f} \in \Omega,$$
(13)

where Ω is defined as the set of all f satisfying the following constraints:

$$\sum_{r \in R^{od}} f_k^{rod} = q_k^{od}, \qquad \forall o, d, k,$$

$$f_k^{rod} \ge 0, \qquad \forall o, d, r \in R^{od}, k$$

$$(14)$$

 q_k^{od} is the demand between origin o and destination d for time interval k and R^{od} is the set of feasible routes between origin o and destination d. In a stochastic assignment the perceived route costs \hat{c}_k^{rod} can be represented by

$$\hat{c}_k^{rod} = c_k^{rod} + \varepsilon_k^{rod} \tag{15}$$

where c_k^{rod} are the real travel costs and \mathcal{E}_k^{rod} is the random component. If it is assumed that the random term is an independently and identically distributed Gumbel variate, than the multinomial logit model is obtained. Given actual travel costs, the route choice probabilities can then be described by (Sheffi, 1985 and Chen, 1999):

$$P_k^{rod} = \frac{\exp(-\theta c_k^{rod})}{\sum_{s \in R^{cd}} \exp(-\theta c_k^{sod})} \qquad \forall o, d, r \in R^{od}, k$$
 (16)

where θ is a parameter that reflects the degree of uncertainty in the travel time know-

information. In general there are three user types: habitual users, partially informed users and perfectly informed users. Habitual users always take the same route, irrespective of the information, e.g. if they don't have any alternative or no access to any information. Partially informed users know something about the conditions in the network due to their experience, but they are not completely informed like the perfectly informed users, who know all about the network condition for now and in the future. Perfectly informed users are the main assumption of the dynamic user equilibrium assignment.

A logit model describes the stochastic assignment with mixed user classes. In this paper the C-logit model, proposed by Cascetta *et al* (1996), is used. This logit model takes into account overlap in routes with the so-called commonality factor given, for route r of OD pair od per time period k, by

$$CF_{k}^{rod} = \beta \ln \left[\sum_{s \in R^{od}} \left(\frac{L_{rs}}{\sqrt{L_{r}L_{s}}} \right)^{\gamma} \right] \qquad \forall o, d, r \in R^{od}, k$$
 (17)

where L_r and L_s are the 'lengths' of routes r and s belonging to OD pair od. L_{rs} is the 'length' of the common links shared by routes r and s and β and γ are positive parameters. 'Length' can be the physical length or the 'length' determined by travel costs. In our case travel times are used. With this commonality factor and the known travel costs, the probability to choice path r, for OD pair od, time period k and user class u, and flow f for that user class are given by

$$P_{uk}^{rod} = \frac{\exp(-\theta_u c_k^{rod} - CF_k^{rod})}{\sum_{s \in R^{od}} \exp(-\theta_u c_k^{sod} - CF_k^{sod})}$$

$$f_k^{rod} = \sum_u P_{uk}^{rod} \xi_u q_k^{od} \qquad \forall o, d, r \in R^{od}, u, k$$

$$(18)$$

where ξ_u is the fraction of users belonging to class u.

3.3 Solution Algorithms

Using the control strategies, the traffic simulation model and the traffic assignment procedure described in the previous paragraphs, the solution algorithm for the combined dynamic control and assignment problem (DCAP), except for the system optimum control and assignment, is as follows:

Algorithm 2: Solution algorithm DCAP

Step 1: Initialise

1.1: initialise general parameters;

1.2: read network file with links, nodes, OD pairs, demands, routes and traffic signal control information;

1.3: determine initial green times $\mathbf{g}^{(0)}$ and cycle times $\mathbf{C}^{(0)}$;

- 1.4: initial assignment based on free flow travel times (or pre-specified) to calculate initial route flows $\mathbf{f}^{(0)}$ and link flows $\mathbf{u}^{(0)}$; 1.5: calculate initial route costs $\mathbf{c}^{(0)}$ and total delay $\mathrm{TD}^{(0)}$ using FLEXSYT;
- 1.6: set counter M=1.

Step 2: Main loop

- 2.1: determine necessary intersection information (minimum and maximum timings, etc.);
- 2.2: for all time periods and all intersections calculate new green times g^(M) and cycle times C^(M) with Webster, Smith's P₀ or Anticipatory Control;
 2.3: calculate route costs c^(M) and total delay TD^(M) using FLEXSYT;
 2.4: calculate new route flows f^(M) and link flows u^(M) using stochastic
- assignment (formulas (17) and (18);
- 2.5: calculate new δ_{M} with $\delta_{M} = a \cdot e^{-\eta M} + b/(M+1)$; 2.6: smooth route flows with $\mathbf{f}^{(M)} = \mathbf{f}^{(M-1)} + \delta_{M}(\mathbf{f}^{(M)} \mathbf{f}^{(M-1)})$;
- 2.7: round flows on integers and make them consistent with demand;
- 2.8: check convergence: if $\mathbf{f}^{(M)} = \mathbf{f}^{(M-1)}$ then stop, otherwise set M=M+1 and go to step 2.1.

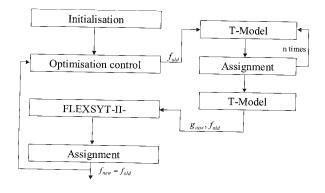
Step 3: Final touch:

- 3.1: calculate route costs $\mathbf{c}^{(M+1)}$ and total delay $TD^{(M+1)}$ using FLEXSYT;
- 3.2: determine simulation time.

In steps 2.6 and 2.7 the method of successive averages (MSA) is used to smooth the flows. The convergence of the MSA is slow, because the step size quickly becomes small and slowly decreases. Therefore, the step size δ_M is chosen in such a way that in the first few iterations the step size is larger than the size normally used (1/n), and smaller in the next iterations to speed up convergence. The necessary conditions

(Sheffi, 1985)
$$\sum_{i=1}^{\infty} \delta_i = \infty$$
 and $\sum_{i=1}^{\infty} \delta_i^2 < \infty$ are fulfilled for every choice of $a > 0$, $b > 0$,

a+b=1 and $\eta>0$. For this paper a=0.8, b=0.2 and $\eta=0.2$. For anticipatory control the algorithm is also sketched in figure 1. Note that in the anticipatory control strategies T-Model and the stochastic assignment are used frequently as an objective function, to evaluate the vector of green times. In the calculations for this paper, n was set to 1.



which uses a genetic algorithm to determine best green times and route flows simultaneously. This algorithm is:

Algorithm 3: Solution algorithm SOCAP

Step 1: Initialise

- 1.1: initialise general parameters;
- 1.2: read network file with links, nodes, OD pairs, demands, routes and traffic signal control information;
- 1.3: determine initial green times $\mathbf{g}^{(0)}$ and cycle times $\mathbf{C}^{(0)}$;
- 1.4: initial assignment based on free flow travel times (or pre-specified) to calculate initial route flows $\mathbf{f}^{(0)}$ and link flows $\mathbf{u}^{(0)}$;
- 1.5: calculate initial route costs $\mathbf{c}^{(0)}$ and total delay $\mathrm{TD}^{(0)}$ using FLEXSYT.

Step 2: Main loop:

- 2.1: determine necessary intersection information (minimum and maximum timings, etc.);
- 2.2: for all time periods calculate new green times $\mathbf{g}^{(1)}$, cycle times $\mathbf{C}^{(1)}$, route flows $\mathbf{f}^{(1)}$ and link flows $\mathbf{u}^{(1)}$.

Step 3: Final touch:

- 3.1: calculate route costs $\mathbf{c}^{(1)}$ and total delay $\mathbf{TD}^{(1)}$ using FLEXSYT;
- 3.2: determine simulation time.

In step 2.2 all variables all calculated in one round, using genetic algorithms. The outcome is evaluated in step 3 using FLEXSYT-II-.

4 Case Studies

4.1 Case description

The solution algorithms described were used to test the different control strategies for several small road networks, depicted in figure 2. The black dots represent signal-controlled intersections, the grey dots represent ramp metering locations.

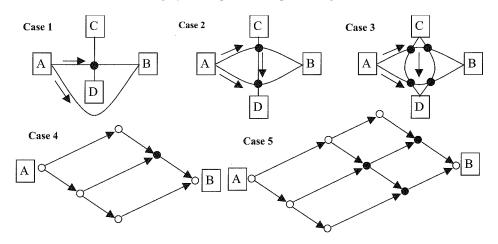


Figure 2: Several small road networks

The networks are hypothetical, but show a lot of variation in structure, demand and other characteristics. Due to the limit in size of the paper, not all characteristics (e.g. length and capacity of links) of the networks can be given. At this point it is sufficient to show that a variable demand is used. The number of time slices and the demand for all cases and OD pairs in shown in table 1.

Table 1	:	OD	demands	(veh/	hr)
---------	---	----	---------	-------	-----

	OD pair	Time period				
	(# routes)	1	2	3	4	5
Case 1	AB (2)	900	1900	1000	400	400
	CD (1)	400	800	400	300	300
Case 2	AB (2)	900	1900	1000	400	400
	CD (1)	400	1000	400	300	300
Case 3	AB (2)	1200	1900	1000	700	-
	CD (2)	400	1700	400	300	-
Case 4	AB (3)	2000	3500	2000	1500	-
Case 5	AB (6)	2000	3400	2000	1500	

assignment. For the control strategies the green times are allowed to vary between 7 and 40 seconds. The cycle time is not pre-fixed, but based on the green times and the intersection lost time, which is always 10 seconds.

Following Chen (1998) the parameters for the C-logit algorithm are chosen to be β = 1.0 and γ = 2.0. Three user classes are defined: class 1 are habitual users (10%), class 2 users (70%) have the perception parameters θ_2 = 1.0 and class 3 users (20%) have θ_3 = 3.0. These values were used for all cases. For case 1 extra runs were made with one user class with the perception parameter θ = 1.0.

For Anticipatory Control the number of generations for the GA is set to 60, with a population size of 25 and for the System Optimum Control the population size is set to 20 and 1500 generations should lead to a near optimal solution.

It is well known that different initial assignments can lead to different equilibria (Van Zuylen and Taale, 2000). For three cases (case 1, 4 and 5) the initial assignment was based on the free flow travel times. For cases 2 and 3 the distribution of the initial route flows was an extreme one: most of the traffic demand on one route and the rest on the other. The effects of other initial flows were not studied. All results, except the Webster control strategy for case 4 were obtained within 50 iterations. The exception took 52 iterations.

4.2 Results

The results for all cases and for all control strategies, in terms of the percentages of total delay of the equilibrium solution in comparison with fixed-time control (100%), are shown in figure 3.

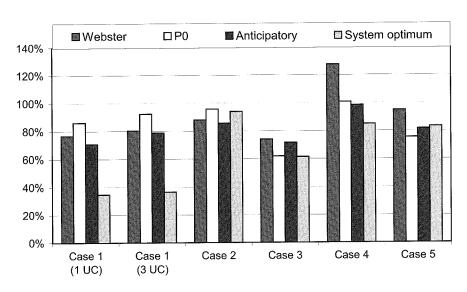


Figure 3: Percentages all control strategies in comparison with fixed-time control

The results show that for the cases 1, 2 and 4 Anticipatory Control is better than the traditional control strategies (Stackelberg game gives better results than Cournot

game). For the cases 3 and 5 P₀ is the best control strategy. Perhaps this strategy is good in symmetric networks, such as in cases 3 and 5. Another reason could be that for Anticipatory Control there are differences between the model used for the optimisation (T-Model) and the model used for the evaluation (FLEXSYT-II-). T-Model is a linear model that always gives consistent results in the sense that increasing flows lead to increasing travel times. FLEXSYT-II- is a stochastic model and therefore it is possible that increasing flows do not necessary lead to increasing travel times. This explains also that sometimes other results than expected are obtained: for case 2 the System Optimum Control is worse than Webster Control! If T-Model is used for both the optimisation and the evaluation, also for the cases 3 and 5 Anticipatory Control is better (Taale and Van Zuylen, 2003).

For case 4 it was difficult to beat the optimised fixed-time strategy. Only Anticipatory and System Optimum Control showed improvements. This is due to the fact that not all possible routes have control. The same is true for case 1, but there only two possible routes exist. Optimising the controlled intersection locally attracts traffic from the route without control and thus decreasing the performance. Anticipatory Control takes into account the route choice process and performs better.

In most cases System Optimum Control gave the best results. Of course, this control strategy will be difficult, if not impossible, to implement in real life, because it supposes complete cooperation of all road users, even when the decisions the road manager makes are not beneficial to them. In game theory this is called the monopoly game.

On average, for the example networks and initial assignments studied, Webster gave an improvement of 10%, P_0 gave an improvement of 15%, Anticipatory Control 19% and System Optimum Control 34%. The results for the last two strategies are biased due to the T-Model used for the optimisation.

The influence of the use of multiple user classes is not so large. Analysing the results in figure 3 for case 1 with one user class and three user classes, one can see that the relative differences are the same. Only the absolute values differ.

Fairly large improvements are possible if route choice is taken into account in the control strategy. For the examples studied, Anticipatory Control showed an improvement of 17% in comparison with optimised fixed-time control. In three out of five cases Anticipatory Control was better than the traditional control strategies. If not, the differences were due to the inconsistencies between the model used for the optimisation (T-Model) and for the evaluation (FLEXSYT-II-). Therefore, improvement of T-Model is needed.

From the traditional control strategies P_0 appeared to be the best, with an average improvement of 15%. Webster only gave an improvement of 10%, which is consistent with the results if T-Model is used for evaluation (Taale and Van Zuylen, 2003).

Further research will focus on the use and optimisation of vehicle-actuated control. VA control is the normal Dutch strategy for all intersections and will be studied in combination with anticipatory control, especially for more complex intersections. Other important research topics are the assumptions made for this paper. The question can be raised, what happens if the OD matrix is not known precisely or the assignment is not in equilibrium. Finally, the influence of departure time choice will be an interesting research field.

References

- Abdelfatah, A.S., H.S. Mahmassani (1998) System Optimal Time-Dependent Path Assignment and Signal Timing in a Traffic Network, paper for the *TRB 77th Annual Meeting*, Washington D.C.
- Abdelfatah, A.S., H.S. Mahmassani (2001) A Simulation-Based Signal Optimization Algorithm Within a Dynamic Traffic Assignment Framework, 2001 IEEE Intelligent Transportation Systems Conference Proceedings, Oakland (CA), pp. 430-435.
- Akçelik, R. (1981) *Traffic Signals: Capacity and Timing Analysis*, Research Report ARR No. 123, Australian Road Research Board.
- Akçelik, R. (1991) Travel time functions for transport planning purposes: Davidson's function, its time-dependent form and an alternative travel time function, on: *Australian Road Research* 21 (3), (Minor revisions: December 2000, pp. 49–59.
- Bliemer, M.C.J. (2001) Analytical dynamic traffic assignment with interacting user-classes, TRAIL PhD Thesis, Delft University Press, Delft.
- Cascetta, E., A. Nuzzolo, F. Russo, A. Vitetta (1996) A modified logit route choice model overcoming path overlapping problems: specification and some calibration results for interurban networks, in: J.-B. Lesort (ed.) *Proceedings of the 13th International Symposium on Transportation and Traffic Theory*, Lyon, France, pp. 697-711.
- Chen, H.-K. (1999) Dynamic travel choice models: a variational inequality approach, Springer, Heidelberg, Germany.
- Chen, O.J. (1998) *Integration of Dynamic Traffic Control and Assignment*, PhD Thesis, Massachusetts Institute of Technology, Boston, USA.
- Clegg, J., M. Smith, Y. Xiang, R. Yarrow (2001) Bilevel programming applied to optimising urban transportation, *Transportation Research Part B*, Vol. 35, No. 1, pp. 41-70.
- Clement, S., J. Anderson, (1997) Traffic Signal Timing Determination: the Cabal model, in: *Second International Conference on Genetic Algorithms in Engineering Systems*, Glasgow, United Kingdom, pp. 63-68.
- Foy, M.D., R.F. Benekohal, D.E. Goldberg (1992) Signal Timing Determination Using Genetic Algorithms, in: *Transportation Research Record 1365*, TRB, National Research Council, Washington D.C., pp. 108-115.
- Hadi, M.A., C.E. Wallace (1993) Hybrid genetic algorithm to optimize signal phasing and timing, in: *Transportation Research Record 1421*, TRB, National Research Council, Washington D.C., pp. 104-112.
- Hadi, M.A., C.E. Wallace (1994) Optimization of signal phasing and timing using Cauchy simulated annealing, in: *Transportation Research Record 1456*, TRB, National Research Council, Washington D.C., pp. 64-71.
- Houck, C.R., J.A. Joines, M.G. Kay (1995) A Genetic Algorithm for Function Optimization: A Matlab Implementation, NCSU-IE Technical Report 95-09, North Carolina State University.

flows, in: Transportation Research Part B, Vol. 35, No. 1, pp. 23-40.

Montana, D.J., S. Czerwinski (1996) Evolving control laws for a network of traffic signals, in: *Genetic Programming 1996*. The MIT Press, Cambridge, MA, pp. 333-338.

Mordridge, M.J.H. (1997) The self-defeating nature of urban road capacity policy; a review of theories, disputes and available evidence, in: *Transport Policy*, Vol. 4, No. 1, pp. 5–23.

Sheffi, Y. (1985) Urban Transportation Networks: Equilibrium Analysis with Mathematical Programming Methods, Prentice-Hall, Englewood Cliffs, NJ, USA.

Smith, M.J. (1980) A local traffic control policy which automatically maximises the over-all travel capacity of an urban road network, in: *Traffic Engineering + Control*, Volume 21, Number 6, pp. 298-302.

Smith, M.J. (1985) Traffic Signals in Assignment, in: *Transportation Research Part B*, Volume 19B, No. 2, pp. 155-160.

Smith, M.J. (1987) Traffic Control and Traffic Assignment in a Signal-Controlled Network with Queueing, in: N.H. Gartner and N.H.M. Wilson (eds.), in: *Transportation and Traffic Theory. Proceedings of the 10th International Symposium on Transportation and Traffic Theory*, Cambridge, Massachusetts, USA.

Taale, H. (1995) An algorithm for calculating the cycletime and greentimes for a signalized intersection, *Studies of the Faculty of Management Science*, University of Transport and Communications, Žilina, Slovakia, Volume 4, pp. 87-94.

Taale, H. (2000) Optimising Traffic Signal Control with Evolutionary Algorithms, paper for the 7th World Congress on Intelligent Transport Systems, Turin, Italy.

Taale, H. (2002) Comparing Methods to Optimise Vehicle Actuated Signal Control, in: *Proceedings of the Eleventh International Conference on Road Transport Information and Control*, IEE, London, UK, pp. 114-119.

Taale, H., F. Middelham (1995) Simulating Traffic and Traffic Control with FLEXSYT-II-, in: M. Snorek *et al* (eds.) *Modelling and Simulation 1995*, Society for Computer Simulation International, Istanbul, pp. 335-339.

Taale, H., H.J. Van Zuylen (2001) The Combined Traffic Assignment and Control Problem: An Overview of 25 Years of Research, paper for the 9th World Congress on Transport Research, Seoul, Korea.

Taale, H., H.J. Van Zuylen (2003) Effects of Anticipatory Control for Several Small Networks, paper submitted to the *Transportation Research Board 82nd Annual Meeting*, Washington D.C.

Taale, H., Th. Bäck, M. Preuß, A.E. Eiben, J.M. de Graaf, C.A. Schippers (1998) Optimizing Traffic Light Controllers by Means of Evolutionary Algorithms, in: *Proceedings of the EUFIT'98 Conference*, Aachen, Germany, pp. 1730-1734.

Transportation Research Board (2000) *Highway Capacity Manual*, Transportation Research Board, National Research Council, Washington D.C., USA.

Van Zuylen, H.J. (1980) A Delay Minimizing Traffic Assignment for (Nearly) Congested Road Networks, Verkeersakademie Tilburg, internal report.

Van Zuylen, H.J. (2001) The assessment of economic benefits of dynamic traffic management, paper for the 9th World Congress on Transport Research, Seoul, Korea.

Van Zuylen, H.J., H. Taale (2000) Traffic control and route choice: Conditions for Instability, in: M.G.H. Bell and C. Cassir (eds.) *Reliability of Transport Networks*, Research Studies Press Ltd, Baldock, United Kingdom, pp. 55-72.

Webster, F.V. (1958) *Traffic Signal Settings*, Road Research Technical Paper No. 39, Road Research Laboratory, London.