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# CHEMICAL REVIEWS

# Molecular Simulation of Hydrogen Systems: From Properties and Methods to Applications and Future Directions

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**ABSTRACT:** This extensive review highlights the central role of classical molecular simulation in advancing hydrogen ($H_2$) technologies. As the transition to a sustainable energy landscape is urgently needed, the optimization of $H_2$ processes, spanning production, purification, transportation, storage, safety, and utilization is essential. To this end, accurate prediction of thermodynamic, transport, structural, and interfacial properties is important for overcoming engineering challenges across the entire $H_2$ value chain. Experimental measurements, despite being the traditional way of obtaining these properties, can be limited by the distinctive nature of $H_2$, harsh operating conditions, safety constraints, and extensive parameter spaces. Free from such limitations, classical molecular simulations, in the general frameworks of Monte Carlo and Molecular Dynamics, provide an optimal balance between computational efficiency and accuracy, bridging the gap between quantum mechanical calculations and macro-scale modeling. This review also systematically covers molecular simulation methods and force fields for computing key properties of $H_2$ systems, such as phase and adsorption equilibria and transport coefficients. Beyond property prediction, we explore how molecular simulation reveals fundamental mechanisms governing hydrate formation and dissociation, membrane permeations, and $H_2$ embrittlement. When possible, data from multiple sources are compared and critically assessed, while effort is put on evaluating the force fields used and methodological approaches followed in the literature. Finally, this review aims at identifying research gaps and future opportunities, emphasizing emerging approaches, such as molecular simulation in the era of artificial intelligence.

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# 1. INTRODUCTION

## 1.1. Background and Motivation

Hydrogen ($H_2$) is a fundamental commodity in the chemical industry, serving as a building block of numerous products and processes in many different sectors. Characteristic examples are ammonia production, methanol synthesis, hydrocracking, steel and cement production, space exploration, and aerospace propulsion systems.[1−9] In the past decade, $H_2$ has gained significant attention as a clean energy carrier because it can be stored on the TWh scale.[10] $H_2$ can be produced via various methods, such as thermochemical processes, water electrolysis, direct solar water splitting, and geological and biological pathways.[11,12] Currently, the chemical industry primarily relies on fossil fuels to produce $H_2$, mostly without treatment of the emitted $CO_2$ (e.g., via natural hydrocarbon cracking, steam methane reforming, coal gasification or reforming processes).[1,13] This is the so-called grey $H_2$, which accounts for ca. 96% of the total $H_2$ supply. If the $CO_2$ emitted during $H_2$ production from fossil fuels is captured and stored, the result is the so-called blue $H_2$.[2] The transition to a sustainable energy landscape, with $H_2$ as an essential part, necessitates the efficient and economic production of the so-called green (i.e., via electrolysis of water using renewable energy sources) or low carbon $H_2$, in sharp contrast to $H_2$ produced from fossil sources.[14]

The European Union (EU) has reached the consensus that by 2030, 42% of the $H_2$ utilized in the industrial sector must be derived from renewable non-biological sources. This figure should increase to 60% by 2035. This decision is in alignment with the EU initiative "Fit for 55", which aims at a 55% reduction in greenhouse gas emissions by 2030. Thus, efforts focusing on scaling up the production and use of $H_2$ as a green energy carrier are becoming urgent in the context of chemical industry and mitigation of environmental impacts.[13,15−17] Such efforts, however, are hindered by technological challenges such as the high cost of green $H_2$ production,[16,18,19] the inefficient separation/purification methods of $H_2$ streams, the lack of safe transportation due to e.g., boil-off (the evaporation of liquid $H_2$ due to heat leakage into cryogenic storage tanks, causing continuous product loss[20]) and $H_2$ embrittlement,[17,21] the lack of commodity high-energy-density storage systems,[22,23] and the low efficiency, and often durability, of electrolyzers and fuel cells.[24] These challenges span the whole $H_2$ value chain, which in this review is going to be described by five different stages, i.e., $H_2$ production, purification, transport, storage, and utilization as shown in Fig. 1. Although, this categorization is not unique, it offers a practical view of the predominant $H_2$ technologies.

To overcome the engineering challenges in each stage of the $H_2$ value chain and to devise optimized processes that will allow for $H_2$ to play a central role in the energy mix of the future, accurate predictions of thermodynamic, transport, structural, mechanical, and electrochemical properties of $H_2$ systems are essential.[19,22,25,26] Such properties are phase equilibria and transport coefficients of gaseous mixtures and aqueous electrolyte solutions of $H_2$ (crucial for water electrolysis, fuel cells, deoxygenation, temperature/pressure swing adsorption), adsorption and absorption energies of $H_2$/adsorbents and storage capacities of different storage media (for physical storage), kinetic, structural and thermodynamic properties of hydrates (for physical storage and separations) and hydrides (chemical storage), electroosmotic drag coefficients in membranes (important for fuel cells and electrochemical compressors), interfacial tension and wettability (i.e., contact angles) of $H_2$/solid/liquid/gas systems (for subsurface storage), permeabilities of $H_2$ gas streams through nanoporous materials, membranes (separations of multicomponent $H_2$ streams) and geological media (subsurface storage), and phenomena such as $H_2$ embrittlement mechanisms in metals (safe transport in pipelines and storage in vessels). Aside from the plethora of required properties, the parameter space of
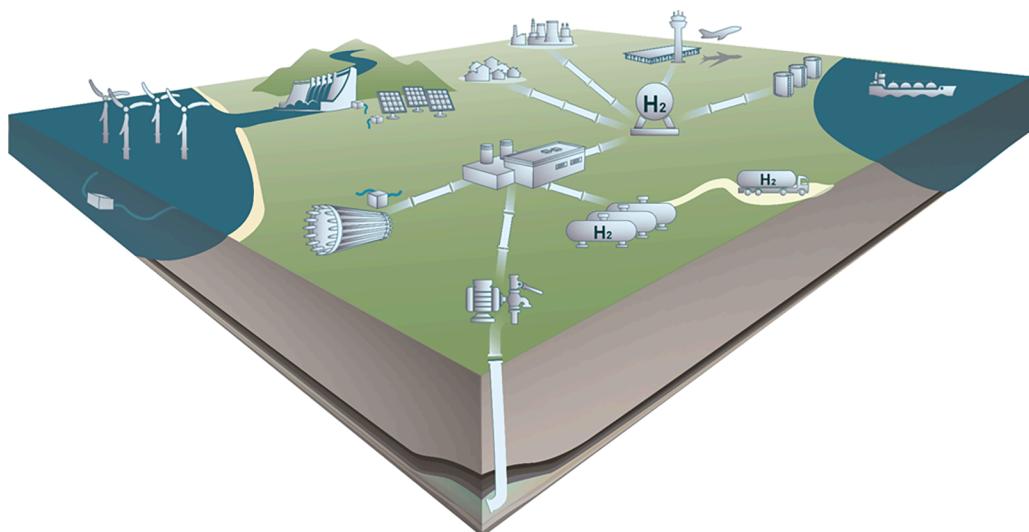
**Figure 1.** Schematic representation of a green hydrogen value chain spanning the production via water electrolysis using renewable energy sources, purification and compression of the hydrogen stream, storage in the liquid and gaseous form in tanks and in the subsurface, transportation via pipelines, trucks, and ships, and domestic and industrial utilization. Classical molecular simulation plays an important role as a reliable predictive tool for thermo-physical properties necessary for the design and optimization of the processes involved in all the stages in the hydrogen value chain.

temperatures, pressures, mixture compositions, and type of systems is extensive. This renders the total number of necessary physicochemical data extremely high, and therefore, makes data acquisition a challenging endeavor.

Traditionally, thermophysical properties are obtained via experimental measurements, often complemented by macro-scale modeling. Nevertheless, due to the numerous different systems, the extremely broad state-point space, and the harsh conditions involved (e.g., high temperatures and/or pressures, corrosive and/or dangerous species) in $H_2$ processes, experiments become costly, and often, not possible to perform at in-situ conditions due to the necessity for adherence to safety standards (e.g., Atmosphères Explosibles − ATEX) and Pressure Equipment Directive (PED) norms.[27,28] As a consequence, thermophysical data of $H_2$ systems remain scarce, especially at high pressures, temperatures, and electrolyte molalities (e.g., for alkaline/acidic electrolytes).[29,30] The lack of such datasets is particularly important because due to the low volumetric energy density of $H_2$ gas, high pressures (usually >200 bar) are necessary for many $H_2$ applications. Another experimental shortcoming is the limitation in spatial resolutions of the available experimental techniques, which makes the detection of atomic hydrogen in alloys challenging.[31] It is also important to note that experimental measurements alone, rarely guarantee deep insight into the fundamental physical and chemical mechanisms of the $H_2$ systems. Understanding these mechanisms at the molecular scale is paramount for overcoming engineering hurdles, optimizing processes and materials, and coming up with novel technologies. Complementary to experimental measurements, equation of state (EoS) modeling is a popular and efficient approach, mainly for predicting the phase behavior of single- or multi-component $H_2$ mixtures.[32−37] However, cubic EoS encounter difficulty in accurately predicting the phase diagrams of $H_2$ systems, while more advanced EoS such as the ones of SAFT, PC-SAFT, and Mie families, have been designed to mainly reproduce properties of long chain, polar, and hydrogen bonding molecules, and therefore, these models are not expected to have an improvement over simple cubic

EoS.[38−45] Moreover, EoS modeling alone cannot directly yield structural and transport properties of $H_2$ systems.

Due to these inherent limitations of experiments and EoS modeling, molecular simulation, performed in the general frameworks of Monte Carlo (MC) and Molecular Dynamics (MD), has emerged as an alternative powerful tool for computing thermophysical properties of $H_2$ systems at a wide parameter space range, and for providing unique insight into the molecular scale. Molecular simulations also guarantee safety and relatively low budget, since commodity computer clusters have become widely accessible. While performing molecular simulations to study $H_2$ systems and processes is a potent research route, it is not without limitations.[46−53] The first step in every molecular simulation is to choose the level of theory for simulating the material or system.[54] Options span accurate quantum-mechanical potentials derived from wave function or density-functional theory (DFT), classical fully atomistic potentials fitted to DFT or experimental data, united atom two-body potentials, and coarse-grained models.[51,55−58] The more detailed the model, the higher the accuracy, but the lower the computational efficiency. This means that although performing quantum mechanical simulations (e.g., DFT, Ab initio MD) will always yield the most precise results, such a modeling approach is only limited to small system sizes and time-scales. On the other side of the spectrum, although coarse-grained simulations (e.g., simulations using the Martini[59,60] potentials or dissipative particle dynamics - DPD[61]) allow access to much higher length- and time-scales, the computed properties can only serve as a qualitative measure, since the atomistic detail is omitted. Combining the best of both worlds, classical molecular simulation offers distinct advantages such as relatively high computational efficiency and accurate prediction of thermophysical proper-ties. In this sense, classical simulations play an important role in filling the gap between computationally intensive ab initio simulations and not-as-precise coarse-grained models or EoS. For these reasons, an extensive, but in some cases scattered, literature body of atomistic molecular simulations of $H_2$ systems is available to date. In this review, we attempt to

summarize these studies, and highlight the crucial role of molecular simulations, alongside experimental measurements, macro-scale modeling, and engineering approaches, in designing and refining $H_2$ technologies. Lately, tremendous efforts by researchers in academia and industry is put in blending Machine Learning (ML) (or even broader, Artificial Intelligence - AI) with molecular simulation techniques towards improving the predictive ability of models, and accelerate simulations and/or material screening. This upcoming paradigm shift in the way we perform molecular simulations, is also discussed in this review, focusing on the case of $H_2$ systems.

## 1.2. What to Expect from This Review and How to Read It

The scope of this review is to showcase the importance of classical molecular simulation studies in advancing technologies spanning the whole $H_2$ value chain (Fig. 1). The focus is on covering the most relevant properties of $H_2$ systems that can be computed with molecular simulation throughout the different aspects of the $H_2$ economy, i.e., we focus on properties important to $H_2$ production via water electrolysis, storage (e.g., in porous media, in hydrates, in the subsurface), $H_2$ compression for storage and mobility, membrane- and hydrate-based separations of $H_2$ streams, and $H_2$ embrittlement of metal pipelines. We provide a comparative assessment of the results of various properties of $H_2$ systems, obtained from different sources, while stretching the limitations and possible misalignment in the available literature.

An overview of the available simulation methods, and a critical discussion on most important concepts for computing $H_2$ properties is also provided. In more detail, we review different simulation techniques such as MC sampling methods for phase and adsorption equilibria, ways to compute hydrate three-phase (thermodynamic) equilibria, transport coefficients such as diffusivities, viscosities, and conductivities from MD simulations, kinetic MC simulations to obtain diffusion coefficients of $H_2$ in materials, and high-throughput screening of materials using classical simulation combined with ML. Another important contribution of this review is the comprehensive analysis of the advantages and limitations of the available force fields for different species involved in $H_2$ technologies (e.g., $H_2$, aqueous electrolytes, substrate materials, organic components).

Based on the thorough discussion of the different $H_2$ systems and properties, we also present an outlook for future research directions, especially in light of emerging approaches involving AI. When possible, we provide datasets of available properties of $H_2$ systems in tables and figures. These datasets can serve both as a reference point and as a motivation for future research. The raw data along with tables summarizing the availability of different properties (and corresponding ranges) can also serve as a bridge between industrial applications and academic research, e.g., to aid constructing engineering correlations, and as feed to process design tools.

In a nutshell, the goals of this review are the following:

- Inform the reader regarding the capabilities of molecular simulation for computing thermophysical properties central to the $H_2$ value chain.

- Provide an overview of the available literature and point the reader towards the appropriate molecular simulation studies relevant to various technologies across $H_2$ economy.

- Introduce the main molecular simulation methods and associated techniques for computing thermodynamic, transport, and interfacial properties of $H_2$ systems.

- Engage into a comprehensive discussion on the fundamental and engineering insights provided from molecular simulation of $H_2$ systems.

- Contribute tables and figures containing available thermophysical data compiled from different sources.

- Bring forth a pragmatic and useful outlook that will motivate and guide future research in the field, focusing on aspects that have not been sufficiently studied or require improvement.

This review aspires to cover a substantial part of literature on molecular simulation of $H_2$ systems. There are no restrictions on the years of literature (our literature review search covers studies until early 2025) or the type of systems considered. It is, however, important to note that we limit our attention only to classical molecular simulation, meaning that studies reporting quantum mechanical calculations are not discussed here (e.g., DFT, AIMD), except from some specific topics, for which the combination of DFT and classical molecular simulation is used as a norm. This choice was made due to the extremely high number of available studies using quantum mechanical approaches to study catalytic systems (e.g., $H_2$ evolution reactions) and surface reactions (e.g., $H_2$ storage on materials). In fact, these topics are already covered by several review articles. Nevertheless, to present a multi-scale perspective, the validity range and limitations of classical interaction potentials are discussed in detail, even for the cases where quantum effects of $H_2$ play a significant role. Similarly, studies using reactive force fields or methods (e.g., quantum MC and MD) are not discussed, except for a few cases which are rendered unique or complementary to the topics presented here (e.g., liquefaction, membranes).

Another topic that is not exhaustively discussed in this review is $H_2$ adsorption on all possible (two-dimensional) 2D and (three-dimensional) 3D (nano-)porous materials. Substantial research efforts have been focused on studying $H_2$ adsorption and separation using various materials, such as zeolites, metal organic frameworks (MOFs), covalent organic frameworks (COFs), graphene derivatives, borophane, boron nitride, and hydrides. Given the great number of available studies (in the order of thousands or more), we provide a focused overview primarily emphasizing recent advances in high-throughput screening using ML techniques. The permeation behavior of $H_2$ through polymeric matrices and minerals is covered up to an extensive degree, with the focus being on materials and processes relevant to storage in high–pressure tanks and the subsurface. Again, a thorough analysis of all available studies involving the interaction of $H_2$ with these families of materials is not feasible since a great number of polymeric and composite systems have been studied using molecular simulation to assess their performance as separation membranes. The latter application is discussed here, however, only with the purpose of providing an overview and a qualitative comparison between polymeric and other porous media for separations.

An area not discussed in this review is molecular modeling of $H_2$ interactions with plasma-facing materials (PFMs), a crucial research direction for realizing fusion energy as a sustainable power source.[62] At the atomistic scale, MD simulations have been performed by different research groups to reveal the mechanisms of $H_2$ trapping and intragranular blister formation

mainly in Tungsten (W) (i.e., the leading PFM material[63−65]) primarily using many-body (e.g., Brenner-type[66,67]), and recently also ML potentials.[62,64,68] Despite its importance for fusion materials research, the study of $H_2$-PFM lies outside the scope of the present review. For a comprehensive study on this topic, the reader is referred elsewhere.[63]

Given the extent and high density of information provided in this review, we have organized the manuscript in the following manner: In Section 2, the role of molecular simulation as a tool for predicting thermophysical properties, and for obtaining fundamental insight into each aspect of the $H_2$ value chain is elaborated upon. Section 2 also constitutes a comprehensive map of the review, containing a brief overview of the most important properties, relevant conditions, and methods regarding each $H_2$ technology considered, and referring the reader to the relevant sections in the rest of the manuscript, where more information and data are provided. Section 3 focuses on molecular simulation methods and models. Initially, an extensive discussion on the use, parameterization, and limitations of classical force fields used in MC and MD simulations is provided, followed by an outline of techniques that can be used in the frameworks of MD and MC to compute phase equilibria of gaseous and liquid mixtures of $H_2$, transport coefficients, wettability and interfacial tension, hydrate properties, gas permeabilities in materials, and quantities related to $H_2$ embrittlement. Section 4 constitutes a comprehensive review of available thermophysical properties of $H_2$ systems computed with molecular simulation. Examples of the data reviewed and discussed are two-component vapor-liquid equilibria (VLE) of $H_2$-$H_2O$, three-phase (hydrate) equilibria of $H_2$-$H_2O$, self- and mutual diffusivities, electro-osmotic drag coefficients in membranes, adsorption of $H_2$ onto materials, thermodynamic properties of wet compressed $H_2$, adsorption of $H_2$ onto rock formations, properties of hydrates (e.g., structural, kinetic, equilibria), liquid-vapor interfacial tensions of gas mixtures, high-throughput screening of materials for separations of $H_2$ containing streams, and $H_2$ embrittlement mechanisms. The discussion on the available literature also aims at identifying aspects that have not been sufficiently studied or discrepancies between different studies. Discussion on the role of AI and ML is also provided when applicable. Finally, in Section 5 a future outlook is compiled aiming to motivate new research in molecular simulations of $H_2$ systems.

## 2. ROLE OF MOLECULAR SIMULATION IN ADVANCING HYDROGEN TECHNOLOGIES: PROCESSES, PROPERTIES, AND RELEVANT CONDITIONS

In this section, we provide an overview of the role of molecular simulation in each stage of the $H_2$ value chain, i.e., production, purification, transport, storage, and utilization. The focus is on the important properties that can be computed with molecular simulation and the respective relevant conditions for each technology/application. Since many thermophysical properties are relevant to multiple applications and aspects in the $H_2$ value chain, this section serves as a comprehensive map for the rest of the review. To this purpose, every section below, aside from providing background information for different $H_2$ technologies, it also points the reader to the appropriate segment in Section 4, where the relevant properties are reviewed in detail.

### 2.1. Hydrogen Production, Compression, and Utilization in Electrochemical Systems

$H_2$ is commonly categorized based on the production pathway followed and the related emissions.[69,70] Grey $H_2$, the most prevalent form, is produced from natural gas via steam methane reforming. This process releases $CO_2$ into the atmosphere. The process for producing black and brown $H_2$ from coal emits both $CO_2$ and CO, and is considered the most harmful to the environment. When combined with $CO_2$ capture and sequestration, grey $H_2$ becomes blue $H_2$, where $CO_2$ emissions are partly avoided. Blue $H_2$ can act as a transitional stage between grey and green, enabling continued use of existing infrastructure during the transition. The production pathway via methane pyrolysis, yields the so-called turquoise $H_2$, which has solid carbon as a by-product. In this review, the focus is on green $H_2$ processes (production via water electrolysis using renewable sources). Nevertheless properties, and relevant methods to compute, e.g., phase equilibria, chemical reactions, and transport properties are equally applicable to the other $H_2$ production routes.

The design and wide use of efficient electrolysis systems capable of replacing fossil-based $H_2$ production with green $H_2$ signifies a crucial step towards the future energy landscape.[13] Achieving this necessitates the utilization of process modeling and precise understanding of the thermodynamic, electrochemical, and transport properties in various components of the electrolysers, including the balance of plant (BoP).[15,25,71−76] However, the cost competitiveness of green $H_2$ production poses a key challenge compared to fossil-based methods.[15] Fuel cells, which convert stored $H_2$ into electrical energy via the reverse process of electrolysis, complement the green $H_2$ energy cycle. Fuel cell technology shares fundamental electrochemical and thermodynamic principles with water electrolysis, where modeling membrane morphology, water management, and ion transport are key areas into which molecular simulations can provide valuable insights. Similarly, electrochemical $H_2$ compression (EHC),[77] an innovative method for compressing $H_2$ using electrochemical splitting and recombination of $H_2$, operates on comparable principles. The physical insights into these technologies derived from molecular simulations are examined collectively in this review due to their shared fundamental principles and similar $H_2$ mixtures involved.

EHC performs on similar electrochemical principles as a PEM fuel cell. The key difference is in the functions of the two devices, i.e., compressors are used to increase $H_2$ pressure e.g., for storage and transport, while PEM fuel cells generate electricity and water from $H_2$ and $O_2$, serving as a power source.[78] EHC requires optimal membrane hydration to maintain efficient charge transport through the membrane. This leads to a saturated $H_2$ stream at the outlet of the compressor. Proper water management is therefore essential to ensure optimal performance and longevity of the membrane. The presence of even low water content in $H_2$ introduces challenges for downstream of the EHC, for example the design of $H_2$ refueling stations, which must adhere to the standard limit of 5 ppm water content.[79,80] While minimizing humidity is critical for efficient $H_2$ refueling, increased humidity in the inlet gas of the fuel cell improves its performance. In fuel cells, a decrease in membrane humidity leads to an increase in ionic resistance and ohmic losses.[81] The application of molecular simulations becomes necessary in comprehending the inner workings of electrochemical compressors, wherein the
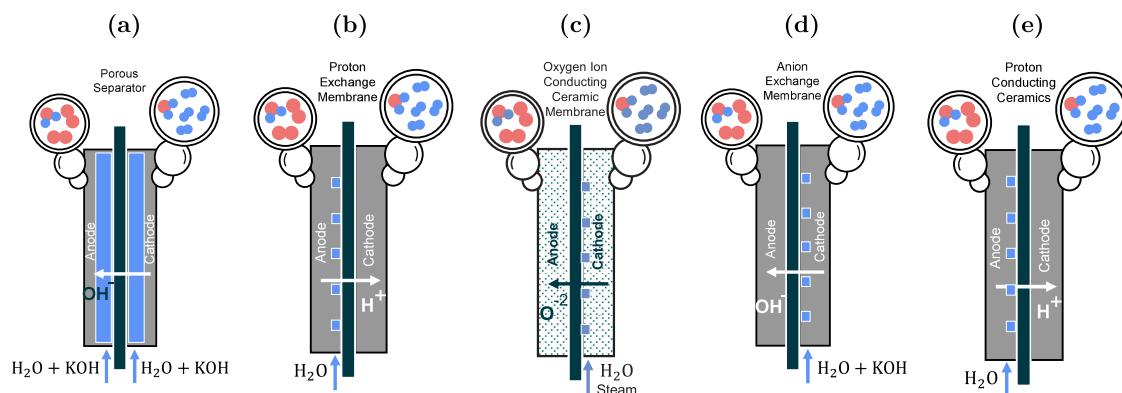
**Figure 2.** Schematic representations of different electrolyzer technologies for $H_2$ production: (a) alkaline water electrolysis, (b) proton-exchange membrane water electrolysis, (c) solid oxide electrolysis cell, (d) anion exchange water electrolysis, and (e) proton conducting ceramic electrolysis. To design, optimize, and obtain fundamental understanding of hydrogen production technologies, molecular simulation is used to compute properties, common to all electrolysis processes, e.g., solubilities of hydrogen, oxygen, and electrolytes, mass transport of these species to and from the electrodes, viscosity of the aqueous electrolytes, electrical conductivity, and electro-osmotic drag in the membranes.

fundamental mechanism involves the dissociation of $H_2$ molecules to protons on the anodic side, and the subsequent formation of $H_2$ on the cathodic side using electrical current.[77]

In the context of $H_2$ production (electrolysis), utilization (fuel cell), and electrochemical hydrogen compression (EHC), molecular simulation is important for property prediction to aid the process modeling of these electrochemical systems. Due to the shared electrochemical principles between these technologies, our focus of discussion is mainly on electrolyzers. Without delving into the details of the different available electrolyzer technologies, the following types of electrolysis are currently available[82] as shown in Fig. 2: alkaline water electrolysis (AWE), proton-exchange membrane water electrolysis (PEMWE), anion exchange water electrolysis (AEMWE), solid oxide electrolysis cell (SOEC), and proton conducting ceramic electrolysis (PCCEL).[82] Using molecular simulations to predict properties of and obtain physical insight into charge transport and phase behavior of electrolyte solutions is particularly relevant since such solutions are the common element in all these electrochemical systems. The range of relevant conditions and the solution compositions vary depending on the type of electrochemical system and operating mode, as discussed in more detail later on.

The high costs of green $H_2$ production are largely driven by elevated electricity prices and regulatory challenges.[15] While electricity costs are outside the scope of system design, efforts can focus on optimizing other factors impacting cost of green $H_2$ such as enhancing the efficiency and safety of electrolysis systems.[73,74,83,84] While the development of a cost-efficient electrolysis system also relies on factors such as the standardization of components, economies of scale, and efficient integration with renewable sources, these are not the focus of this review. Instead, we emphasize how molecular simulations can provide accurate thermodynamic and transport properties which are critical for optimizing green $H_2$ production and utilization in electrochemical systems to further drive cost reduction. Typical thermodynamic properties necessary for process modeling of water electrolysis are electrolyte densities, solubilities of gaseous species (e.g., $H_2$, $O_2$) in aqueous electrolyte solutions, surface tension of concentrated liquid electrolytes, and partial pressures of water vapor.[75,76] Thermodynamic and transport properties of aqueous potassium hydroxide (KOH), sodium hydroxide

(NaOH), and sodium chloride (NaCl) solutions are particularly relevant for electrolysis and fuel cells.[85−89] The dynamic viscosity of liquid electrolytes, mass transport expressed by the self- and mutual-diffusivities of all the species in the solution,[25,71,90,91] and ion transport in membranes are representative examples of important transport properties required for the process modeling of electrolyzer cells. These properties can be computed with molecular simulations using different methods. A detailed list of thermodynamic and transport properties of various $H_2$ systems relevant to electrochemical applications (i.e., production and utilization of $H_2$) computed via molecular simulations and reported in literature is provided in Table 1 along with the respective ranges of conditions (e.g., temperatures, pressures, hydration of membranes). For each system listed in Table 1, we also refer the reader to the relevant methodology and detailed discussion in Section 3 and Section 4.

Membrane electrode assemblies (MEAs) are critical components in electrochemical systems.[92] The membranes allow proton transport in acidic environments and hydroxide ion transport in alkaline environments while blocking the passage of gases, ensuring efficient charge transport and water management.[93] The conductivity of a polymer in a PEM/EHC is influenced by its crystallinity, equivalent weight, hydration level, side chain length, and morphology, making the optimization process complex and time-consuming due to the wide range of parameters involved. Effective water management in MEAs (hydration level) is essential, balancing electro-osmotic drag and back diffusion of water at different current densities. Electro-osmotic drag causes water to move across the membrane as protons migrate through the membrane under the influence of the imposed electric field.[92,94] Concurrently, back diffusion occurs due to the difference in water concentration between the cathodic and anodic compartments. Another related critical topic is understanding and mitigating degradation in MEAs. As an example, the contamination of ionomer membranes by e.g., $CO^{2+}$, $Na^+$, can significantly disrupt the morphology of the membrane, specifically blocking ion exchange sites. The presence of contamination can impair the flow of reactant gases in the catalyst layer. Additionally, it can hinder the diffusion of hydronium ions ($H_3O^+$) and water molecules, which are critical for maintaining proton conductivity and

**Table 1. Thermodynamic and Transport Properties Related to $H_2$ Production and Utilization in Electrochemical Systems Computed with Molecular Simulation in Different Studies[i]**

| Property | System[Method] | Conditions |
|---|---|---|
| Fugacity Coefficient | $H_2$-$H_2O$[a,110] | 264–323 K, 10–1000 bar |
| Chemical Potential | $H_2$-$H_2O$-KOH[a,111] | 298–423 K, 10–400 bar, 0–8 mol KOH/kg $H_2O$ |
|  | $H_2$-$H_2O$-NaCl[a,111] | 298–423 K, 10–400 bar, 0–6 mol NaCl/kg $H_2O$ |
| Solubility | $H_2$-$H_2O$[a,110] | 310–423 K, 10–1000 bar |
| Vapor-Liquid Equilibrium, Activity | $H_2$-$H_2O$[a,47] | 264.21–272.4 K, 100–1000 bar |
|  | $H_2$-$H_2O$[b,48] | 423, 477.59 K, 60.9–182.9 bar |
|  | $H_2$-$H_2O$-KOH[a,111] | 298–423 K, 10–400 bar, 0–8 mol KOH/kg $H_2O$ |
|  | $H_2$-$H_2O$-NaCl[a,111] | 298–423 K, 10–400 bar, 0–6 mol NaCl/kg $H_2O$ |
|  | $H_2$/$O_2$-$H_2O$-KOH[a,112] | 298–353 K, 1–100 bar, 0–8 mol KOH/kg $H_2O$ |
|  | $H_2$/$O_2$-$H_2O$-NaOH[a,112] | 298–353 K, 1–100 bar, 0–8 mol NaOH/kg $H_2O$ |
|  | $H_2$-$H_2O$-NaB(OH)$_4$[a,113] | 298–353 K, 1 bar, 0–5 mol NaB(OH)$_4$/kg $H_2O$ |
|  | $O_2$-$H_2O$, Nafion, Aquivion/Pt[d,114] | 353.15 K, 2.92 < λ < 13.83 |
| Joule-Thomson Coefficient | $H_2$-$H_2O$[c,47] | 323 K, 100–1000 bar |
| Thermal Expansivity Heat Capacity | $H_2$-$H_2O$[c,47] | 323 K, 100–1000 bar |
| Self-diffusion | Nafion, 3M, Hyflon[d,e93] | 300, 353 K, 5 < λ < 14 |
|  | Dry Nafion[d,115] | 150–600 K |
|  | Hydrated Nafion[d,f116] | 300 K, 3.44 < λ < 11.833 |
|  | Hydrated Nafion[d,117] | 300, 350 K, 3.5 < λ < 16 |
|  | $H_2$, $O_2$, Nafion[g,118,119] | 298 K, λ = 1 |
|  | $H_2$, $O_2$, $H_2O$, SPEEK[d,120,121] | 298–353 K, 4.9 < λ < 11.1 |
|  | $H_2O$, $H_3O^+$, Ph-SPEEK[d,122] | 300–400 K, 3.5 < λ < 40 |
|  | $H_2O$, $H_3O^+$, $CH_3OH$, Ph-SPEEK[d,123] | 360 K, 8 < λ < 28 |
|  | $H_3O^+$, PFSA type membranes[d,124] | 300 K, λ = 3 |
|  | $H_2O$, Nafion, Aquivion[d,125] | 298 K, 3 < λ < 18 |
|  | $H_2$-$H_2O$-KOH[a,112] | 298–353 K, 1–100 bar, 0–8 mol KOH/kg $H_2O$ |
|  | $H_2$-$H_2O$-NaOH[a,112] | 298–353 K, 1–100 bar, 0–8 mol NaOH/kg $H_2O$ |
|  | $O_2$-$H_2O$-KOH[a,112] | 298–353 K, 1–100 bar, 0–8 mol KOH/kg $H_2O$ |
|  | $O_2$-$H_2O$-NaOH[a,112] | 298–353 K, 1–100 bar, 0–8 mol NaOH/kg $H_2O$ |
|  | $H_2$-$H_2O$-NaB(OH)$_4$[a,113] | 298–353 K, 1 bar, 0–5 mol NaB(OH)$_4$/kg $H_2O$ |
| Electrical conductivity | $H_2O$-NaB(OH)$_4$[a,113] | 298–353 K, 1 bar, 0–5 mol NaB(OH)$_4$/kg $H_2O$ |
|  | Dry Nafion[d,115] | 150–600 K |
|  | $H_2$, $O_2$, Nafion[g,118,119] | 298 K, λ = 1 |
|  | $H_2O$, $H_3O^+$, Ph-SPEEK[d,122] | 300–400 K, 3.5 < λ < 40 |
|  | $H_2O$, $H_3O^+$, $CH_3OH$, Ph-SPEEK[d,123] | 360 K, 8 < λ < 28 |
|  | $H_3O^+$, PFSA type membranes[d,124] | 300 K, λ = 3 |
| Thermal Conductivity | $H_2O$, Nafion[d,126] | 300–350 K, 3 < λ < 20 |
| Electro-osmotic drag | $H_2O$, cylindrical pore of Nafion 117[d,127] | 298 K, < 7.65 λ < 20.9 |
|  | $H_2O$, Nafion 117[h,128] | 287.15–364.65 K, λ = 20 |
|  | $H_2O$, $H_3O^+$, Nafion[g,129] | 363 K, 4.25 < λ < 12.75 |
|  | $H_2O$, $H_3O^+$, Nafion[g,94] | 330–420 K, 5 < λ < 20 |
|  | $H_2O$, $H_3O^+$, Nafion[g,94] | 350 K, 1 < λ < 2 |

[a]Continuous fractional component Monte Carlo. [b]Monte Carlo. [c]Ensemble fluctuations. [d]Grand-equilibrium method; molecular dynamics. [e]Multistate empirical valence bond. [f]Reversible reference system propagator algorithms. [g]Molecular dynamics with reactive force fields. [h]Non-equilibrium molecular dynamics. [i]The superscripts in the table denote the simulation method used for each system. λ is the water content in the systems with membranes (see Eq. (31)). The table points the reader to the appropriate sections in this review where the relevant methods and discussion are provided. The relevant methods and in-depth discussions per property can be found in this review in the following sections: Fugacities, chemical potentials, solubilities, activities, and vapor-liquid equilibrium: Section 3.3.1 (methods), Sections 4.1.2.1, 4.1.2, and 4.1.1 (discussion). Joule-Thomson coefficient, thermal expansivity, and heat capacities: Section 3.3.4 (methods) and Section 4.1.4 (discussion). Diffusivities: Sections 3.2.4 and 3.2.3 (methods), and Section 4.1.5 and Section 4.1.7 (discussion). Electroosmotic drag: Section 3.2.12 (methods) and Section 4.1.6 (discussion).

hydration within the membrane. Such effects can be rigorously studied and understood via molecular simulations, which offer detailed insights into the structural and transport properties of ionomers under various contamination scenarios. To this purpose, molecular simulations are performed to model membrane morphologies, sorption, percolation, densities, glass transition temperatures, and ion transport.[92,94−101] The influence of these contributions can be isolated in molecular simulations which is challenging to achieve in experiments.[93] Classical MD simulations can capture the vehicular mechanism of charge transport, while reactive force fields and Ab-initio MD[102−105] can potentially capture the Grotthuss mechanism, since bond breaking and formation during the simulation is required.[93] Molecular simulations have also been used in the literature for modeling the membrane and ion transport within the membrane of electrochemical compressors.[92,97] Additionally, molecular simulations can be used to determine the water content in and the thermodynamic properties of the com-

pressed $H_2$ downstream of the electrochemical compressor.[47,106−110] Fig. 3 highlights various thermophysical properties which are crucial for the process design and optimization of two widely used electrochemical technologies (AWE and EHC) computed with molecular simulation.

## 2.2. Purification and Separation of Hydrogen Streams

**2.2.1. Separations with Membranes.** Membranes provide a potentially sustainable alternative to traditional separation methods of $H_2$ streams.[130−132] An important property of membranes is permeability ($P_i$). Membrane permeability quantifies the molecular-level transport of substances across thin barriers and differs significantly from other types of permeabilities reported in the literature, such as Darcy's permeability,[133] widely used in subsurface storage and porous media research. Membrane permeability is defined as $P_i = S_i D_i$, where $S_i$ is the solubility of species $i$ (which reflects its affinity with the membrane material) and $D_i$ is the diffusivity (which is a measure of the rate of molecular transport of the
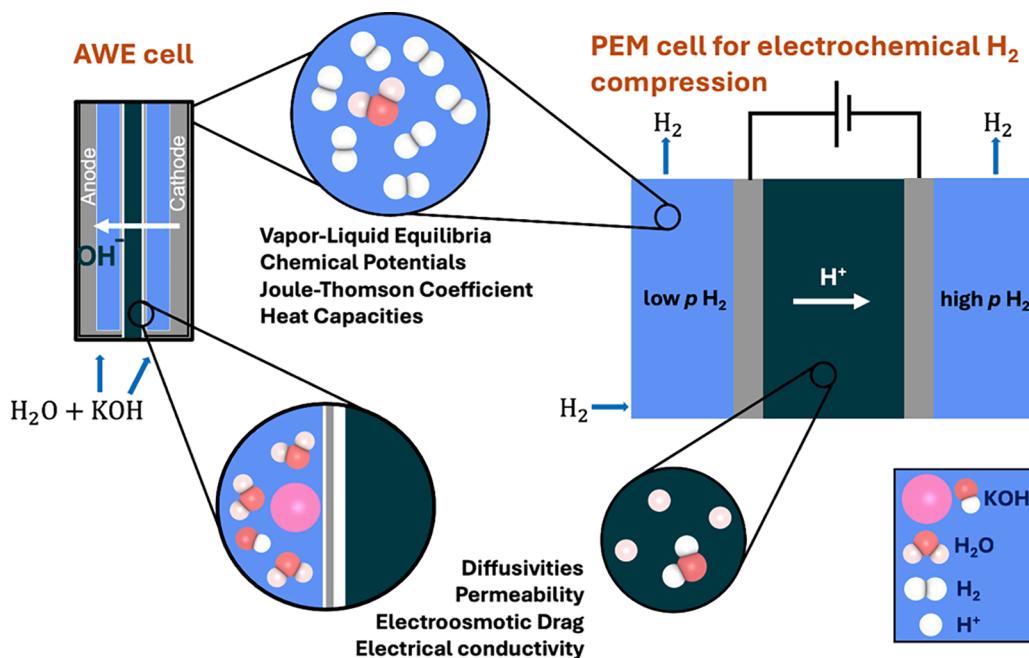
**Figure 3.** Schematic of alkaline water electrolysis and electrochemical $H_2$ compression in a proton exchange membrane cell highlighting areas where molecular simulations are crucial, e.g., electrical conductivity, electro-osmotic drag, heat capacity, Joule-Thomson coefficients, and vapor-liquid equilibrium.

species within the membrane). $P_i$ is commonly expressed in Barrer, a unit named after Richard L. Barrer,[134] a pioneer in membrane science. One Barrer represents the permeability of a membrane of 1 cm thickness that allows the passage of molecules occupying 1 $cm^3$ at standard temperature and pressure (STP: 273.15 K and 1 atm) per second through a 1 $cm^2$ of membrane area under a pressure difference of 1 cmHg. A related property, membrane permeance, measures the flux of a substance per unit driving force and membrane thickness. It is typically expressed in Gas Permeance Units (GPU), where 1 GPU corresponds to the permeance of a membrane that allows 1 $cm^3$ of gas (STP) to pass through 1 $cm^2$ under a pressure difference of 1 cmHg. Expressing permeability in GPU is convenient because the definition inherently accounts for membrane thickness, which can be useful when this parameter is unknown or varies between samples.

In membrane science, selectivity is expressed as the ratio of the permeabilities, $P_i/P_j$, of two species $i$ and $j$, as schematically shown in Fig. 4. While this ratio must be high enough to comply with the needs of a given process, at the same time a minimum permeability for the fast-permeating gas (e.g., $P_i$) should be ensured. Otherwise the overall process is regarded as of discouragingly low performance for industrial applications.

Polymeric membranes are extensively used in industrial-scale separations due to ease of fabrication, cost-effectiveness, and scalability. Polymeric membranes are classified into isotropic, which have a uniform composition and pore structure throughout their thickness, and anisotropic, which have varying pore structures and compositions across their cross-section.[135] Gas separation in polymeric membranes is driven by both solubility and diffusivity selectivity. While the well−known permeability/selectivity trade−off is fundamentally diffusion-dominated,[136] chemical modifications often improve performance by increasing solubility selectivity. For example, introducing polar or $CO_2$ − philic groups can enhance the uptake of condensable gases (e.g., $CO_2$, $CH_4$, $O_2$) and shift
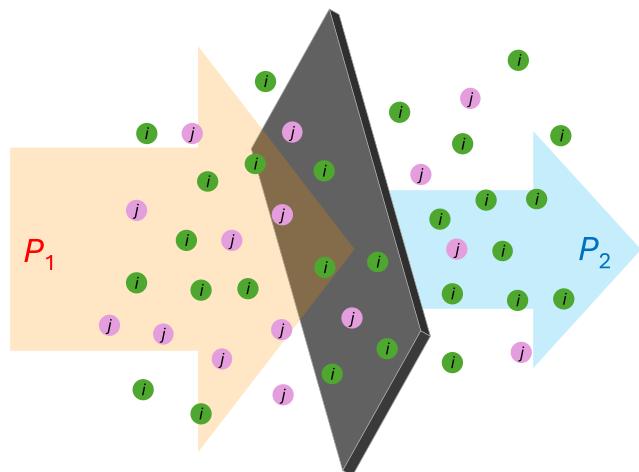


**Figure 4.** Schematic representation of a membrane separation process, showing the feed side of a mixture $i$ and $j$ at higher pressure ($P_1$), permeate at lower pressure ($P_2$) across the membrane.

materials upward relative to the Robeson limits. For $H_2$ − related separations, this has asymmetric consequences. Because $H_2$ is a non-condensable gas, and its solubility is difficult to increase, membranes aiming for high $H_2$ permeation selectivity ($H_2/CO_2$, $H_2/CH_4$) remain largely controlled by diffusion. In contrast, increasing the solubility of the heavier partner can substantially improve $CO_2/H_2$ or $CH_4/H_2$ selectivity, which explains why many polymer modifications benefit processes focused on capturing $CO_2$ or $CH_4$ from $H_2$ − rich streams but have limited impact on designing highly $H_2$ − selective membranes.

This observation creates a significant trade-off between permeability and selectivity, as it is shown in Fig. 5 where experimental results from the literature for separations of $H_2/CH_4$ (Fig. 5(a)) and $H_2/CO_2$ (Fig. 5(b)) mixtures with
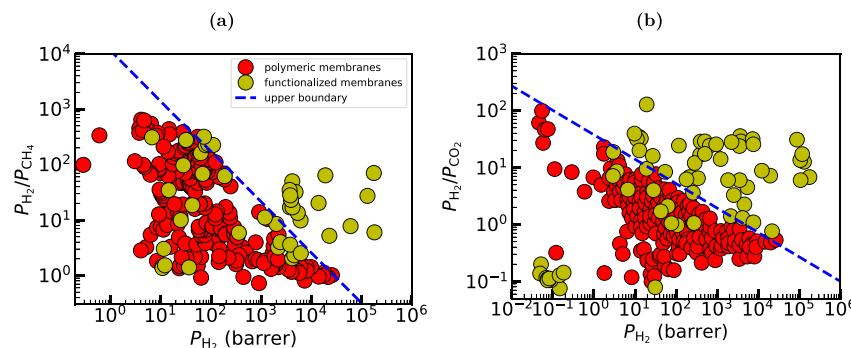
**Figure 5.** Representative performance assessment in the form of Robeson plots for (a) $H_2/CH_4$ and (b) $H_2/CO_2$, comparing experimental results on polymeric and functionalized nanoporous membranes (e.g., MOFs, COFs, zeolites, carbon-based, mixed matrix membranes). Polymeric membranes literature results taken from the seminal work of Robeson.[136] The data from literature for the functionalized materials were collected from an extended survey of the authors and can be found in Tables 15 and 16.
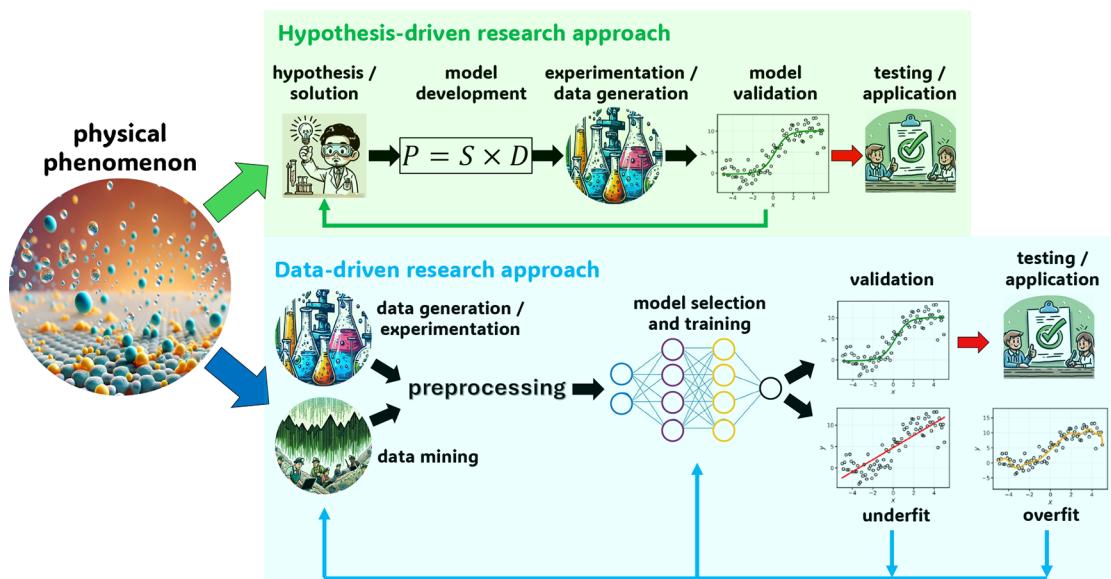


**Figure 6.** Schematic showing hypothesis (traditional) and data (modern)-driven research approaches. In the traditional route, a hypothesis is usually made in the beginning. Based on this hypothesis models are devised, and experiments are performed to test its validity. In the modern route, data are produced, analyzed, processed, and used to train machine-learning models. The outcomes of these models are validated and used to fine-tune the model. This approach is revolutionizing the study of $H_2$ processes involving porous materials. The figure is inspired from Fig. 2 of ref 150.

polymeric membranes are indicated with red color. This limitation hinders the widespread use of polymeric membranes for separations of $H_2$ streams, and has spurred research into exploring alternative materials that can overcome these intricacies.

Crystalline nanoporous materials have surfaced as a prominent class of candidates for addressing the drawbacks of polymeric membranes. These materials have high permeability and selectivity due to their unique structure. Nano-porous materials achieve separations of mixtures via primarily size and shape exclusion. This is due to the small, well-defined windows or apertures connecting internal cavities or narrow channels within the structures of the materials. The apertures act like molecular sieves, allowing smaller molecules to pass through while blocking larger ones.[137,138] The rigid structure of crystalline nanoporous materials provides more precise control over which molecules can pass, unlike polymeric membranes that typically rely on diffusion through flexible, less structured pathways.

While zeolites and activated carbons are widely used materials for $H_2$ gas separations in the industry,[139−143] due to the limited tunability of pore sizes of zeolites, attention has been directed towards exploring functionalized materials. The most prominent classes of such materials are MOFs (i.e., materials consisting of metal clusters linked with organic ligands)[144] and COFs (i.e., materials composed oranic molecules connected through covalent bonds).[145] Membranes can be made solely based on MOFs or COFs, or in a hybrid form by using polymers as a matrix and nanoporous materials as fillers, resulting in the so-called mixed-matrix membranes (MMMs).[146] One of the most fascinating features of MMMs is that they can be modified at the molecular level (by using e.g., different fillers, varying filler compositions, different polymer matrices) to tailor their macroscopic properties.[147]. This versatility opens an almost boundless array of possibilities for achieving desired separation results within the $H_2$ value chain.[148] This also becomes evident by the increased performance of functionalized membranes made of MOFs

**Table 2. Structure and Properties of the Three Most Common Types of Clathrate Hydrates in Nature[161]**

| hydrate structure | sI | | sII | | sH | | |
|---|---|---|---|---|---|---|---|
| crystal system | Primitive cubic | | Face-centered cubic | | Hexagonal | | |
| space group | $Pm3n$ | | $Fd3m$ | | $P6/mmm$ | | |
| cavity type (notation) | small (S) | large (L) | small (S) | large (L) | small (S) | medium (M) | large (L) |
| Description | $5^{12}$ | $5^{12}6^2$ | $5^{12}$ | $5^{12}6^4$ | $5^{12}$ | $4^35^66^3$ | $5^{12}6^8$ |
| cavity radius (Å) | 3.95 | 4.33 | 3.91 | 4.73 | 3.94 | 4.04 | 5.79 |
| cavities/unit cell, $n_{i,k}$ | 2 | 6 | 16 | 8 | 3 | 2 | 1 |
| H$_2$O/unit cell, $N_{w,k}$ | 46 | | 136 | | 34 | | |
| Unit cell formula | $2S \cdot 6L \cdot 46$ H$_2$O | | $16S \cdot 8L \cdot 136$ H$_2$O | | $3S \cdot 2M \cdot 1L \cdot 34$ H$_2$O | | |

and COFs, compared to the limited performance of pure polymeric membranes shown in Fig. 5.

Due to the virtually limitless ways of tailoring the separation performance of these materials through functionalization, achieving the desired results solely in the laboratory is a strenuous, time-consuming, and financially demanding process. Therefore, molecular simulation has emerged as a powerful computational tool for exploring modification-performance correlations and aiding the development of highly H$_2$-selective membranes.[149] MC and MD simulations are particularly valuable for computing properties related to performance metrics in membrane separations. Such properties are the solubilities, diffusivities, permeabilities, selectivities, and heats of adsorption of H$_2$ and other gases in the membranes. A brief but comprehensive review of the literature regarding these properties for pure H$_2$ and different mixtures (with e.g., CO$_2$, CH$_4$, N$_2$, He,) is provided in Section 4.6 for various materials (i.e., MOFs, COFs, MMMs, and zeolites). This discussion also covers properties such as the storage capacities, which are mainly useful for the design and evaluation of H$_2$ storage systems as briefly covered in Section 2.3.2. Relevant details on models and methods widely used to perform simulations of nanoporous materials and membranes are provided in Sections 3.1.4, 3.2.5, and 3.3.2.

With the advent of high performance computing, the execution of hundreds or even thousands of simulations is now feasible, allowing the exploration of wide design spaces of functionalized materials.[149] Assisted by ML techniques, these complex correlations become easier to uncover, as discussed in more detail in Sections 4.6.1 and 4.6.2. As shown in Fig. 6, ML leads to a paradigm shift in the development of separation membranes, enabling the transition from a hypothesis-driven approach, limited to trial-and-error, to a data-driven approach.[150−158]

In addition to membrane-based separations, large-scale H$_2$ purification is frequently carried out using adsorption processes such as pressure-swing adsorption (PSA) and temperature-swing adsorption (TSA). Both these processes rely on packed beds of porous adsorbents, often zeolites or activated carbons, and comprise the industrial state-of-the-art for H$_2$ recovery from complex mixtures. Although PSA/TSA operate on different principles than selective transport across membranes, both approaches benefit from molecular−scale insights into adsorption equilibria, energetics, and diffusion. Discussion on how high−throughput molecular simulations combined with ML approaches can be an important tool for selecting high−performing adsorbents for PSA and TSA processes is provided in Sections 4.6.1 and 4.6.2. For details relevant to PSA process design and optimization, the reader is referred to the studies of Park et al.[159] and Ribeiro et al.[160]

**2.2.2. Hydrate-Based Separations.** Clathrate hydrates, or simply hydrates, are crystalline, non-stoichiometric, inclusion compounds consisting of a hydrogen-bonded network of water molecules that form three dimensional cavities (cages) inside which guest molecules of appropriate size can be enclathrated (i.e., encaged).[161,162] The water molecules can self-assemble into forming cages under appropriate conditions (i.e., high pressures and/or low temperatures). The cages are further stabilized by weak van der Waals interactions between the water molecules in the lattice and the encaged guest molecules. The most common hydrate structures in nature are the sI, sII, and sH, which result from combinations of different numbers and types (i.e., pentagonal dodecahedron, $5^{12}$; tetrakaidecahedron, $5^{12}6^2$; hexacaidecahedron, $5^{12}6^4$; icosahedron, $5^{12}6^8$; irregular dodecahedron, $4^35^66^3$) of cages which form the unit cell of each hydrate structure. Table 2 shows the structural characteristics of the sI, sII, and sH hydrate structures.

Hydrates have attracted significant interest from the industry and academia due to their ability to selectively incorporate particular molecules of appropriate size in their crystal structure. This makes hydrates attractive candidates for a number of industrial applications, including the storage/transport of energy carriers such as H$_2$ and CH$_4$[163−166] and environmental gases such as CO$_2$,[167,168] gas mixture separations, water purification,[169] and desalination.[170] In particular, two industrial applications of hydrates are of significant importance within the H$_2$ value chain: (i) the storage (stationary or mobile applications) and transportation of H$_2$ inside hydrates[171,172] (i.e., hydrate slurries or solid hydrates in pellet form), and (ii) hydrate-based separation of the H$_2$/CO$_2$ binary gas mixture resulting from the so-called integrated coal gassification cycle (ICGC) plants, where the CO$_2$ is captured before fuel combustion (i.e., precombustion capture[173]). A hydrate-based separation of a gas mixture is the direct result of the selective incorporation of gas molecules from the mixture of appropriate size in the hydrate crystal structure.[174] Fig. 7 shows a cartoon representation of a single-stage hydrate-based separation for the general case of a gas mixture consisting of components A and B. The process works as follows: Initially, a gas mixture of A and B is in contact with water. The pressure and temperature conditions are tuned to induce hydrate formation, which is followed by separation of the solid hydrate phase and the subsequent hydrate dissociation. Two gas streams, an A-rich (i.e. the "unreacted" gas mixture which remained after hydrate formation), and a B-rich (i.e., resulting from hydrate dissociation), are produced, each of which has different compositions from the initial one. After implementing a number of hydrate formation/dissociation stages, gas streams having a certain degree of required purity are obtained. For extensive discussions on the
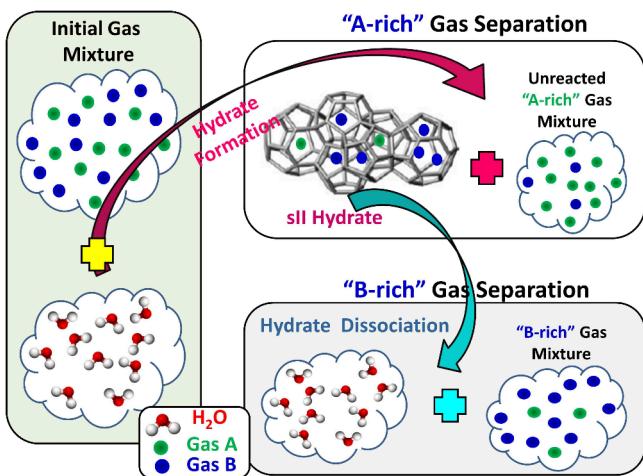
**Figure 7.** Schematic of a single-stage, hydrate-based, separation of a binary gas mixture "A + B", where A and B are the two gas components.



**Figure 8.** Pressure-equilibrium temperature diagram showing the three-phase equilibria curves for a hydrate-former with lower $(Q_1)$ and upper $(Q_2)$ quadruple points. Phase notation: H — hydrate; $L_w$ — liquid water; I — ice; V — vapor; $L_H$ — liquid hydrate-former.

experimental and computational aspects of hydrate-based $H_2$-mixture separations, the reader is referred to the review articles by Babu et al.,[173] Tsimpanogiannis et al.,[175] and Hassanpour-youzband et al.[176]

Molecular simulation is an important tool for computing various thermodynamic, transport, kinetic, and structural properties of interest to $H_2$ hydrate-related applications. Table 3 shows a number of such properties that can be

**Table 3. Important Thermophysical, Transport and Structural Properties for Pure or Mixed $H_2$ Hydrates**[a]

| Property | Methodology | Discussion |
|---|---|---|
| Phase $(p, T)$ equilibria | Section 3.2.14 | Section 4.8.1 |
| Structure | Section 3.2.15 | Section 4.8.3 |
| $H_2$ diffusivities | Section 3.2.3 | Section 4.8.8 |
| Kinetic rates | Section 3.2.15 | Section 4.8.2 |
| Promoter identification | | Section 4.8.7 |
| Storage capacities | Section 3.3.3 | Sections 4.8.5 and 4.8.4 |

[a]The reader is referred to the sections in this review where the respective methods (methodology) and review (Discussion) of the available literature are located.

obtained via MD and MC simulations. Table 3 also guides the reader to the corresponding sections in this review where particular properties and methods are further discussed for the case of pure or mixed $H_2$ hydrates. It should be noted that some of these properties can also be obtained by means of first principle calculations (e.g., DFT[177]). For detailed discussions on DFT-based calculations relevant to $H_2$ hydrates, the reader is referred elsewhere.[178−182]

Three-phase equilibria is among the most important thermodynamic properties for the design stages of hydrate-based processes. Fig. 8 shows a typical phase diagram of a hydrate-forming system that has a lower $(Q_1)$ and an upper $(Q_2)$ quadruple point. The solid lines indicate where the three-phases are at equilibrium, while the two stars indicate the quadruple points, i.e., where four-phase equilibria occurs. Certain hydrate-forming systems, such as $CH_4$, $N_2$, and Ar, exhibit only $Q_1$, while others, e.g., $CO_2$, $H_2S$, $C_2H_6$, $C_3H_8$, exhibit both $Q_1$ and $Q_2$. Experimental measurements, continuum scale modeling and molecular simulations can be
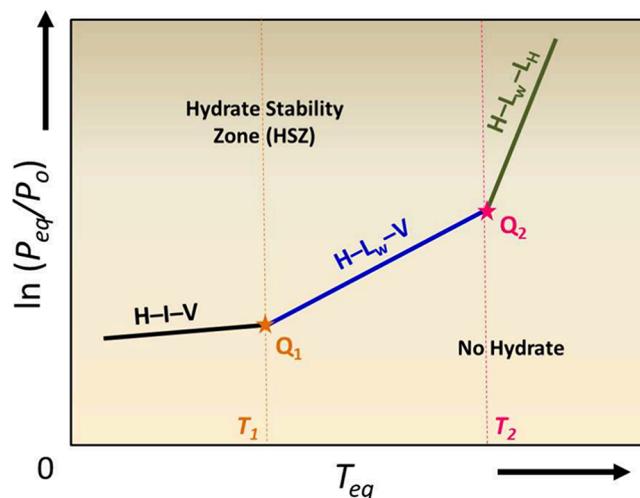
used for the estimation of hydrate phase equilibria. The vast majority of continuum scale modeling studies has been performed by an approach that couples van der Waals−Platteeuw statistical theory,[183] used for describing the solid solution, with an EoS that describes the vapor-liquid equilibria. The seminal work of Parrish and Prausnitz,[184] and the later modifications,[185,186] introduced to overcome some of the initial limitations of the theory, are capable of providing a satisfactory description of the phase equilibria for the most common hydrate systems. For a detailed review on this, the reader is referred to the study by Medeiros et al.[187]

The study of hydrate equilibria with MC and MD simulations can provide a deeper understanding of the related microscopic phenomena. Such molecular-scale methodologies can be used in a complementary role to the experimental and continuum-scale approaches to aid the design of new hydrate-related processes. Additional properties of interest reported in literature are the enthalpies of hydrate dissociation $(\Delta H^{dissoc})$, the enthalpies of enclathration $(\Delta H^{encl})$, isobaric heat capacities $(C_p)$, hydrate lattice expansivities, and separation efficiencies. Interestingly, no molecular simulation data regarding these properties are available for $H_2$ containing systems, despite the fact that these properties are essential for the design/optimization of industrial processes involving hydrate-based systems. This clearly shows that ample room is available for future computational studies of $H_2$-containing mixtures capable of forming hydrates.

**2.2.3. Separations Using Ionic Liquids.** As discussed earlier, membranes comprising polymeric and nanoporous materials can be used to efficiently separate $H_2$ streams under various conditions and for different applications. High selectivities and adsorption capacities, have also been reported using solvents based on ionic liquids (ILs) and deep eutectic solvents (DES). ILs are salts (comprising only ions) with melting temperatures orders of magnitude lower than common salts, e.g., NaCl. The melting $T$ of ILs is below 100 °C, and for some components (the so-called room temperature ILs) it can even be below ambient $T$. The broad liquid range, combined with other properties such as the negligible vapor pressures, thermal stability, and high degree of tunability, makes ILs an

interesting class of materials for a wide variety of processes. In addition, in the past 50 years ILs have been considered for use in industrial applications as an environmentally friendlier solvent compared to common organic components.

ILs have found application also in extraction (e.g., liquid-liquid) and separation (e.g., gas) processes, usually in the form of IL-supported membranes. For more details on ILs and their applicability the reader is referred elswhere.[188−191] To the best of our knowledge, no molecular simulation studies investigating relevant $H_2$/DES properties are available in literature. Contrary, studies on sorption, diffusivities, and interfacial properties of $H_2$ (and mixtures of $H_2$ with other gases) in ILs computed via MC and MD simulations are available. Nevertheless, the number of these studies is limited compared to e.g., $CO_2$/ILs or $CH_4$/ILs systems. Evidently, the main motivation for performing molecular simulations of $H_2$/ILs is the study of $CO_2$/$H_2$ separation, which is crucial for pre-combustion processes. Predicting properties for $H_2$ separations from $N_2$ and $CH_4$ are also common in the available molecular simulation literature owing to the importance of these mixtures for the design of carbon capture technologies. Since mixed-gas experiments are usually challenging to conduct, molecular simulations offer a compelling and efficient complementary method for predicting and understanding the absorption selectivities of IL/gas systems.

Based on our review of the available molecular simulation literature, $H_2$ appears to have very low solubilities in ILs compared to other gases, which increases with temperature (contrary to some experimental findings). $CO_2$/$H_2$ selectivity in ILs dramatically decreases with temperature, while, computations of $H_2$ diffusivities show that it diffuses up to 12 times faster than $CO_2$. The full review of this topic is provided in Section 4.5, along with details regarding discrepancies between simulations and experimental data. For relevant methods and models, the reader is referred to Sections 3.1.3, 3.2, and 3.3.1.

## 2.3. Hydrogen Storage

The high gravimetric energy density of $H_2$ (ca. 120 MJ/kg), nearly two and a half times higher than conventional fossil-based fuels such as methane, propane, diesel, and gasoline (see Fig. 9), makes it an attractive energy carrier. However, focusing solely on gravimetric energy density does not provide a complete picture regarding the widespread application of $H_2$, due to the storage challenges associated with its low volumetric density (ca. 0.010 MJ/L at 20 °C).[22,192] Typically, commercially compressed $H_2$ gas (CHG) is stored at pressures up to 700 bar. CHG at 300 bar has a density of 24 kg/m$^3$ at 15 °C, while at 700 bar and the same temperature, the density increases to 40 kg/m$^3$ as shown in Fig. 10.

Liquid $H_2$ (LH) at cryogenic temperatures has densities up to 70 kg/m$^3$. Subcooled liquid $H_2$ (SLH), which achieves a density of 62 kg/m$^3$ at -245 °C and 16 bar, is produced by slightly increasing the pressure of LH using state-of-the-art compression systems.[195,196] SLH storage faces challenges due to boil-off, estimated to last between 10 and 200 hours depending on the state of charge of the system.[195] Cryo-compressed $H_2$ (CCH), combining low temperatures with high pressures, and LH are other storage types, although the technology readiness level (TRL) for CCH remains low.[195]

Cost-effective, high energy density $H_2$ storage is a crucial part of the future sustainable energy landscape. The need to discover (at the material level) and design (at the system level)
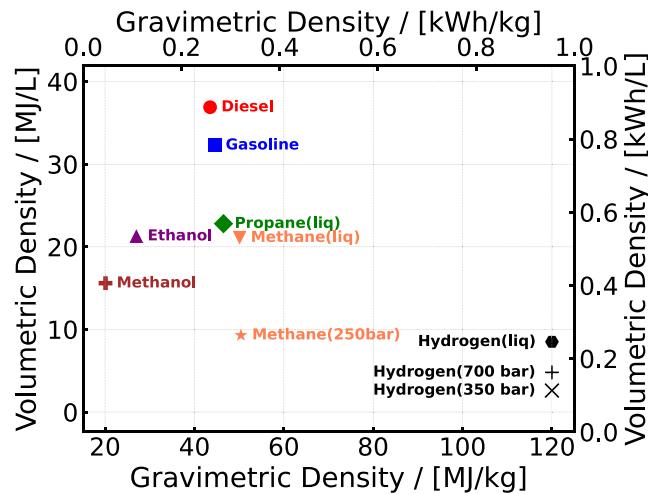


**Figure 9.** Gravimetric and volumetric energy densities of hydrogen compared to other fuels at ambient temperature. The data are extracted from refs 38 and 193.
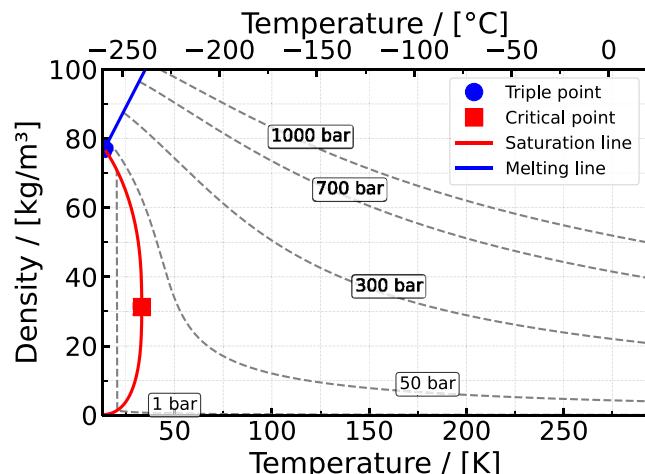


**Figure 10.** Hydrogen density - temperature diagram for different isobars. Data are taken from NIST.[194]

improved media for $H_2$ storage is specifically emphasized by the US Department of Energy (DOE).[22,197,198] Molecular simulations play a central role in addressing the material challenges and in modeling $H_2$ storage processes, especially under elevated pressures and temperatures (relevant to e.g., underground storage), providing unique insights into the physical-chemical mechanisms governing the behavior of the systems at hand. Such insights are almost impossible to achieve through experimental methods alone, which are limited by both safety, cost, and resolution constraints. To this end, the prediction of relevant thermophysical properties and insights obtained from molecular simulations can guide the design of more efficient $H_2$ storage systems.[77,199−201] This review focuses solely on classical molecular simulations related to three different types of storage, namely compressed $H_2$ for vehicular applications, storage in materials, and underground $H_2$ storage. It is important to note that this work does not extensively cover $H_2$ storage in materials, since this field is already well-documented in the literature, particularly regarding the vast array of nanoporous and 2D nano-materials. However, several key references to comprehensive reviews are provided on this topic for further reading.

**2.3.1. High Pressure Storage of Gaseous Hydrogen in Tanks.** The pathway to achieving a less carbon-intensive mobility sector relies on the use of battery electric vehicles (BEVs) and fuel cell electric vehicles (FCEVs). Usually, BEVs are most suitable for short-range commutes, while FCEVs are preferred for medium to long-haul applications.[193,195,202−206] Currently, CHG at 70 MPa and 35 MPa is used in light-duty vehicles, while an inlet pressure of up to 875 bar is required in on board $H_2$ storage tanks to refuel the FCEV within 3 to 4 minutes.[79,201,207−215]

In FCEVs of all types, e.g., trucks, light vehicles, buses, $H_2$ is stored at high pressures in different tanks of varying type and size. The main types of tanks are classified as I, II, III, IV, and V.[216,217] Type I tanks typically operate at a maximum pressure of 200 bar, with a gravimetric storage density of 0.01 to 0.02 $kg_{H_2}$/kg. Type II tanks, with a maximum pressure of 300 bar, reduce weight by 40% compared to type I tanks, but are still less efficient for $H_2$ storage due to a 50% increase in manufacturing costs.[216,217] Both types are unsuitable for mobility applications because of their low storage density. In contrast, type III and IV tanks, which operate between 450 and 700 bar, provide significantly higher $H_2$ storage capacity and are commonly used in fuel cell vehicles. Type IV tanks, in particular, are widely used due to their lightweight composite structure, capable of withstanding pressures up to 700 bar or higher.[216,217] Type V tanks, though still in development, are expected to offer even greater performance.[216,217]

Due to the high pressures in the tanks (e.g., 700 bar), $H_2$ gas experiences a strong driving force to escape. To mitigate this thermodynamic phenomenon, it is common that thermoplastic polymers and composite materials are used in the tanks as barrier materials (i.e., inner liners) that provide $H_2$ gas containment. To this purpose, developing polymers and composites with low inherent $H_2$ permeability is crucial. This requires extensive research involving a wide spectrum of materials tested under high pressures, which is not trivial to do with experiments alone. Molecular simulation can make a substantial contribution towards advancing $H_2$ storage systems under high pressures, which are essential for FCEVs.[218] The insights from molecular simulations allow for the understanding of $H_2$ interactions with the liner materials, which affect permeation resistance and gas barrier properties.[218] By studying these interactions at the nano-scale, molecular simulations help assess the suitability of polymeric and composite materials, thus, providing crucial insights into the performance and safety of $H_2$ storage systems. Molecular simulation studies in this field have mainly focused on studying $H_2$/polymer systems relevant to IV-type hydrogen tanks. The most common polymers in these tanks are polyamide-6 (PA6), polyethylene (PE) and high density polyethylene (HDPE), and composite materials such as graphene/PA6. Molecular simulation studies of synthetic rubbers, such as ethylene propylene diene monomer (EPDM), used mainly as sealing components (e.g., gaskets, hose liners, O-rings) in $H_2$ energy/storage infrastructure, are also available in the literature.

In Section 4.4 we provide a detailed review of the available molecular simulation literature reporting thermophysical properties of $H_2$/polymer (and composite) systems. These studies mainly report diffusivities (and diffusion mechanisms), solubilities (and sorption), permeabilities of $H_2$ in the solid phases, and polymer-specific properties such as the material fractional free volume (FFV), specific volume, and density.

Our analysis of the available literature revealed that there is a large data variability among the simulation studies. For example, the computed $H_2$ solubilities and permeabilities span three orders of magnitude across different studies, despite using the same (or similar) force fields and methods. In addition, we show that while molecular simulations capture experimental permeabilities qualitatively, quantitative differences exceed three orders of magnitude clearly indicating that there is ample room for improved predictions. For a description of the relevant molecular models and methods for computing the thermodynamic and transport properties of $H_2$/polymer systems, the reader is referred to Sections 3.1.4, 3.2.4, 3.2.5, 3.3.1, and 3.3.2.

**2.3.2. Storage in Materials.** To avoid working at high pressures (as discussed in Section 2.3.1) and/or at low temperatures (see Section 2.4.3), $H_2$ can be stored in solids and liquids.[22] Materials can store $H_2$ via physical (physisorption, i.e., via weak electrostatic or Van der Waals interactions) or chemical (chemisorption, i.e., via formation of chemical bonds) sorption.[23] Characteristic examples are intermetallic hydrides, where $H_2$ is physically absorbed within the interstitial space in the solid, or complex hydrides where covalent/ionic interactions between $H_2$ and adsorption cites drive the $H_2$ storage process.[193] Other families of relevant materials are the so-called Liquid Organic Hydrogen Carriers (LOHCs),[219] 2D materials (e.g., graphene, borophene),[220−222] and nanoporous materials such as MOFs and COFs (introduced in Section 2.2).

DOE has issued requirements for the design and production of new onboard automotive $H_2$ storage systems.[197,199] The most important requirements comprise $H_2$ gravimetric capacities of 6.5 wt.% or higher, volumetric capacities of 0.05 kg $H_2$/L or higher, and system costs of 266 $/kg $H_2$ or cheaper.[197] The adsorption energy of $H_2$ with the material should optimally range from -0.20 to -0.40 eV/$H_2$ to avoid under- or over-binding of the $H_2$ molecules with the storage medium.[223−226] A detailed description of the requirements including the minimum durability of the storage unit can be found in ref 197. It is noteworthy that no existing material has yet met all the requirements of DOE for onboard $H_2$ storage. This is a major motivation, driving research in both academia and industry to discover and fabricate new materials and catalysts for $H_2$ storage systems.[197]

Physisorption on porous materials such as MOFs and zeolites generally results in fast $H_2$ release and capture kinetics, but suffers from low gravimetric and volumetric $H_2$ capacities.[227,228] Chemisorption on materials such as metal hydrides, reaches larger $H_2$ capacities but the release of $H_2$ (i.e., the dehydrogenation reaction) is energy intensive and has slow kinetics.[229,230] To make $H_2$ economy feasible, discovering and using suitable and cost-effective materials with high $H_2$ capacities and fast release/capture kinetics are essential. 2D materials and porous structures, such as MOFs, are frequently studied for $H_2$ storage and separation (see also Section 2.2.1) due to their high surface-to-volume ratio and chemical tunability, which allows for optimizing adsorption capacities and efficiencies (see Section 2.2.1). The number of possible new materials that can be potentially synthesized and used for $H_2$ storage is virtually unlimited.[198]

Even when considering specific classes of nanoporous media, such as MOFs or zeolites, the number of materials that has been theoretically predicted to date reaches the order of mangnitudes of hundreds to millions. This combined with the

rapid rate that new families of materials are being discovered, synthesized, and considered for $H_2$ storage makes relying solely on experiments prohibitively costly and time-consuming.[231−235] Also, experimental measurements of $H_2$ systems require strict adherence to safety standards which involve protocols to prevent leaks, explosions, and contamination, especially at high-pressures.[197] To this end, atomistic molecular simulations have emerged as a robust and efficient approach to *in silico* screen extensive families of materials with respect to important properties governing $H_2$ storage. These properties include $H_2$ adsorption energies, gravimetric and volumetric storage capacities, and diffusion coefficients of $H_2$ in the materials.[51,236] This allows for early detection of unsuitable materials, either due to low storage capacities or material instability, but also for identifying key-performing media which can be further studied experimentally. Material properties such as the Young's modulus and thermal conductivity can also be predicted using molecular simulations[237,238] and used to evaluate potential $H_2$ storage systems. Considering the extensive body of literature on $H_2$ storage in 2D and 3D materials, and given the fact that this topic closely aligns with Section 2.2.1, in this review we present only a condensed discussion of $H_2$ sorption and storage in nanoporous media in Section 4.6. Focus is directed in the increasing coupling of AI techniques with classical molecular simulation to screen thousands of different materials Sections 4.6.1 and 4.6.2.

**2.3.3. Storage in Hydrates.** While gas hydrates have been known for more than 200 years, it was a common belief until recently that pure $H_2$ was not capable of stabilizing the hydrate structure due to the small size of the $H_2$ molecule. A major change in the dominant belief occurred in 1997, when Kuhs et al.[239] using neutron diffraction data of sII $N_2$ hydrates demonstrated experimentally that multiple occupancy of a hydrate cage was possible. The important study of Kuhs et al. was followed by a number of experimental studies that confirmed the possibility of multiple occupancies for $N_2$, $O_2$ and Ar (for more details the reader is referred to the relevant experimental studies discussed in the review by Tsimpanogiannis and Economou[240]). A few years later, MC studies confirmed the capability of molecular simulations to capture multiple occupancy phenomena. A detailed review of the relevant MC studies is presented in ref 240.

While experimental evidence of the existence of $H_2$ hydrates became available via a number of studies,[241−244] the interest in $H_2$ hydrates increased significantly only after Mao et al.[171] reported experimental measurements confirming the formation of pure $H_2$ hydrates at high pressures (i.e., 300 MPa at 280 K). At ambient pressure, pure $H_2$ hydrate was found to be stable at low temperatures (i.e., 150 K). Mao et al. performed energy-dispersive X-ray diffraction (EDXD) and neutron diffraction experiments to identify that $H_2$ hydrates are of type sII structure. Mao et al. also suggested that the $5^{12}$ (S-cages) could accommodate two $H_2$ molecules, while the $5^{12}6^4$ (L-cages) could accommodate up to four $H_2$ molecules. Such a configuration allows for a $H_2$ storage capacity equal to 5.0 wt.% $H_2$ on hydrates. This value is close to the US DOE target of 6.5 wt% and a volumetric density of 62 kg $H_2/m^3$ for $H_2$ storage in solid materials prior to 2001.[206] Fig. 11 shows a schematic of sII $H_2$ hydrate formation. Namely, when water and $H_2$ are brought together at appropriate pressure and temperature conditions, sII hydrate forms. This hydrate consists of two different types of cages (i.e., S-, and L-cage)
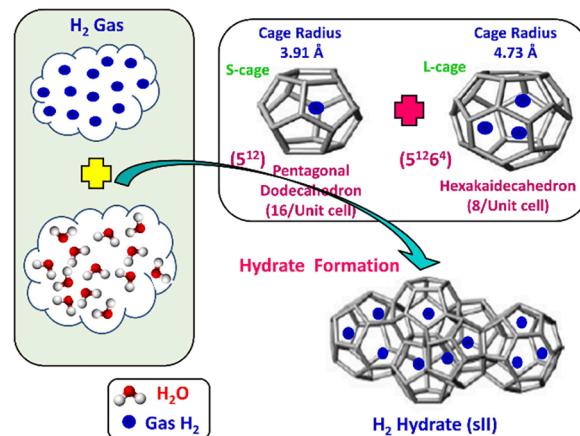


**Figure 11.** Schematic representation of $H_2$ hydrate (sII) formation. Sixteen pentagonal dodecahedron ($5^{12}$; S-cage) cages and eight hexacaidecahedron ($5^{12}6^4$; L-cage) cages combine in order to form a single unit cell of sII hydrate. The multiple occupancy of L-cages results in increasing the $H_2$ storage capacity of the hydrate.

as shown in the top right panel of Fig. 11. The possibility of multiple $H_2$ molecules occupying the L-cages (see bottom right panel of Fig. 11) results in a solid material with increased $H_2$ storage capacity compared to the case when all types of cages are occupied (at most) by a single $H_2$ molecule.

The high pressures (or the low temperatures) required for the formation of pure $H_2$ hydrates is a major limitation for the use of hydrates as $H_2$ storage materials for e.g., vehicular applications. Florusse et al.[245] reported experiments demonstrating that the high pressures ($\approx$ 2000 bar) required for the formation of pure $H_2$ hydrates can be significantly reduced (e.g., 50 bar at 280 K) by using tetrahydrofuran (THF) as hydrate "promoter" (i.e., a component that promotes hydrate formation at moderate pressure and temperature conditions compared to the pure case[246]). The use of a promoter, however, results in lower $H_2$ storage capacity due to the promoter occupying the L-type cages (see Table 2 for cage notation). Lee et al.[247] reported the possibility of increasing the $H_2$ storage capacity of the mixed $H_2$/THF hydrate by "tuning" the hydrate. Namely, using less than the stoichiometric amount of THF, therefore succeeding in having partial occupancy of the L-cages by $H_2$, instead of being occupied completely by THF. However, hydrate tuning has been highly debated in the literature due to the difficulty in experimentally reproducing the process (i.e., see the detailed discussions by Alavi and Ripmeester[177] and Papadimitriou et al.[248]). Furthermore, an extensive discussion on the experimental and computational aspects of $H_2$ storage in hydrates can be found in a series of review studies,[172,177,249−256] while an excellent discussion on the statistical mechanics theory behind the thermodynamic stability of hydrates is provided by Tanaka and Matsumoto.[257]

From the discussion presented here it becomes evident that we are interested in identifying properties (thermodynamic, transport, and structural) and condition that affect the $H_2$ storage capacity of pure or mixed $H_2$ hydrates. Such are the following: (i) three-phase equilibrium conditions (i.e., higher pressures result in higher cage occupancies, therefore higher storage capacities, as a result of the fact that hydrates are not stoichiometric materials. Namely, not all cages are required to be occupied for hydrate stability), (ii) $H_2$ diffusivity within the
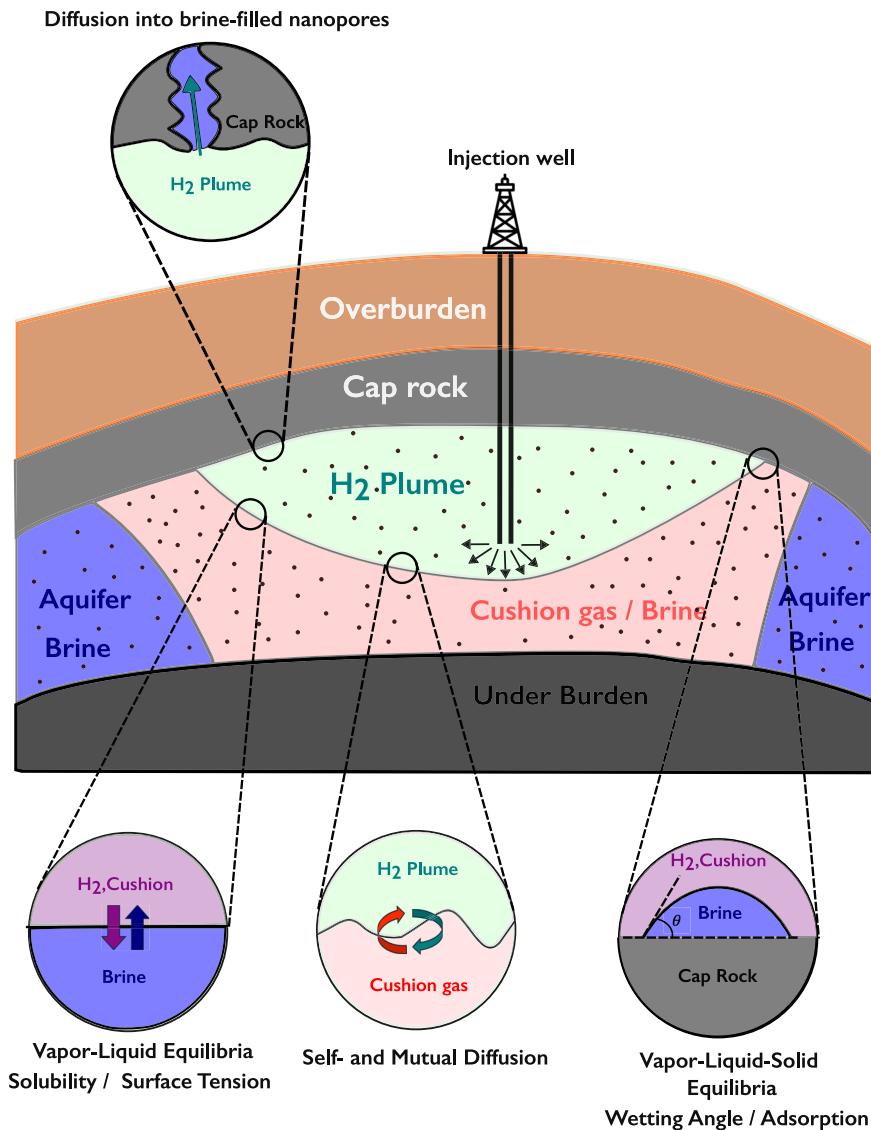
**Figure 12.** Schematic representation of key physical processes governing subsurface $H_2$ storage. We highlight areas where molecular simulations are crucial, e.g., the diffusion of $H_2$ into empty or brine-filled nanopores in the caprock, essential for assessing leakage risks, the dissolution of $H_2$-cushion gas mixtures into brines under reservoir conditions, where atomistic modeling enhances our understanding, the mixing of $H_2$ with cushion gas via molecular diffusion, potentially leading to contamination, and the three-phase contact angle between $H_2$-cushion gas mixtures, brine, and geological solids, determining the capillary pressure needed for hydrogen to invade brine.

hydrate crystal (i.e., $H_2$ can escape via diffusion from the hydrate solid structure, reducing the amount of $H_2$ stored in the hydrate), and (iii) hydrate lattice constants (i.e., the use of various promoters, having different sizes, can result in increasing the lattice constant, therefore, providing increased storage capacity).

**2.3.4. Subsurface Storage.** In 2021, the world energy consumption was estimated at 600 EJ.[258,259] This massive energy requirement highlights the need for extensive $H_2$ storage solutions. Given the limitations of surface storage facilities, e.g., holding the large volumes necessary for long-term energy storage, alternative solutions are explored. Geological formations, such as depleted reservoirs and salt caverns, offer storage capacities in the order of hundreds of gigawatt-hours, providing a feasible option for large-scale $H_2$ storage.[259−262]

Underground $H_2$ storage (UHS)[263,264] (also referred to as subsurface $H_2$ storage) involves injecting $H_2$ into geological formations where interactions with the surrounding gases, fluids, and solids occur. A cartoon representation of UHS is shown in Fig. 12. This process can include the use of a so-called cushion gas,[259−262] occupying up to 30% of the reservoir's volume, to maintain a minimum pressure and ensure mechanical stability. Brine (usually a mixture of water and sodium chloride) acts as a natural sealant preventing $H_2$ leakage into surrounding aquifers, maintaining the integrity and stability of the geological structure. Understanding the physical processes involved in subsurface $H_2$ storage is crucial for optimizing storage strategies and ensuring safety and efficiency. In past years, molecular simulation has been proven to be a necessary tool for investigating these processes at the molecular level, providing detailed insights into several key properties and physical mechanisms, while accessing state points and quantities which can be inaccessible without costly and complex experimental setups. For example, $H_2$ tends to form mixtures with other gases present in the reservoir, driven

**Table 4. Comprehensive List of Hydrogen Properties Relevant to Underground Storage (See Also Fig. 12), as Computed via MD Simulations[a]**

| Property | System | Condition | Property | System | Condition |
|---|---|---|---|---|---|
| $pVT$ | $H_2$ | 323-423 K, 5-50 MPa, 0-1 $x_{H_2}$ | | $H_2/CO_2$-NaCl Brine-Siloxane (Kaolinite) | 5−80 MPa, 303−343 K, 1.7 mol |
| | $H_2$-$CO_2$ | 323-423 K, 5-50 MPa, 0-1 $x_{H_2}$ | | $H_2/CO_2$-NaCl Brine-Talc | 15 MPa, 333 K, 3.4 mol |
| | $H_2$-$CH_4$ | 310-470 K, 15−30 MPa, 0-1 $x_{H_2}$ | | $H_2/CO_2$-KCl Brine-Talc | 15 MPa, 333 K, 0.13 mol |
| | $H_2$-$CO_2$ | 310-470 K, 15−30 MPa, 0-1 $x_{H_2}$ | | $H_2/CO_2$-NaCl Brine-Gibbsite (Kaolinite) | 15 MPa, 333 K, 3.4 mol |
| Self- and mutual-diffusivity | $H_2$-$CO_2$ | 323-423 K, 5-50 MPa, 0-1 $x_{H_2}$ | | $H_2/CO_2$-KCl Brine-Gibbsite (Kaolinite) | 15 MPa, 333 K, 0.13 mol |
| Thermodynamic factor | $H_2$-$CO_2$ | 323-423 K, 5-50 MPa, 0-1 $x_{H_2}$ | | $H_2/CH_4$-NaCl Brine-Siloxane (Kaolinite) | 5−80 MPa, 303−343 K, 1.7 mol |
| Interfacial tension | $H_2$-$H_2O$ | 0.1−160 MPa, 298−523 K, 0−5 mol | | $H_2/CH_4$-NaCl Brine-Talc | 15 MPa, 333 K, 3.4 mol |
| | $H_2$-NaCl Brine | 0.1−60 MPa, 298−523 K, 0−5 mol | | $H_2/CH_4$-KCl Brine-Talc | 15 MPa, 333 K, 0.13 mol |
| | $H_2$-$CaCl_2$ Brine | 1−30 MPa, 298−373 K, 0−5 mol | | $H_2/CH_4$-NaCl Brine-Gibbsite (Kaolinite) | 15 MPa, 333 K, 3.4 mol |
| | $H_2$-$MgCl_2$ Brine | 1−30 MPa, 298−373 K, 0−5 mol | | $H_2/CH_4$-KCl Brine-Gibbsite (Kaolinite) | 15 MPa, 333 K, 0.13 mol |
| | $H_2$-KCl Brine | 1−30 MPa, 298−373 K, 0−5 mol | Adsorption on clay-substrates | $CH_4/H_2/H_2O$-Na-Montmorillonite | 343 K / - |
| | $H_2$-$N_2$-$H_2O$ | 1−70 MPa, 300−343 K | | $H_2$-Kaolinite (Gibbsite and Siloxane) | 300 K / 1.0−50.7 MPa |
| | $H_2$-$CH_4$-$H_2O$ | 10−60 MPa, 323−388 K | | $H_2/CH_4$-Kerogen | 338 K / 0−27.6 MPa |
| | $H_2$-$CO_2$-NaCl Brine | 5−40 MPa, 298−373 K, 0−3 mol | | $H_2/CH_4$-Montmorillonite | 323 K / up to 11.15 MPa |
| Wetting angle | $H_2$-$H_2O$-Mica | 5 and 20 MPa, 300 and 323 K | | $H_2/CH_4/H_2O$-Montmorillonite | 323 K / up to 11.15 MPa |
| | $H_2$-$H_2O$-Gypsum | 5 and 20 MPa, 300 and 323 K | | $H_2/H_2O$-Kaolinite (Gibbsite and Siloxane) | 298.15 K / 0.1−10 MPa |
| | $H_2$-$H_2O$-Anhydrite | 5 and 20 MPa, 300 and 323 K | | $H_2/CH_4$-Hydroxylated Quartz | 323.15−423.15 K / 1−50 MPa |
| | $H_2$-$H_2O$-Halite | 5 and 20 MPa, 300 and 323 K | | $H_2/CO_2$-Hydroxylated Quartz | 323.15−423.15 K / 1−50 MPa |
| | $H_2$-$H_2O$-Silica (Q2 and Q4) | 5−60 MPa, 320 K | | $H_2/H_2O$-Hydroxylated Quartz | 323.15−423.15 K / 1−50 MPa |
| | $H_2$-$H_2O$-Silica (Q3/Q4) | 1−160 MPa, 298−523 K | | $H_2$-Kaolinite | 303.15−353.15 K / 0−18 MPa |
| | $H_2$-NaCl Brine-Quartz | 20 MPa, 333 K, 1.5−3.5 mol | | $H_2$-Illite | 303.15−353.15 K / 0−18 MPa |
| | $H_2$-NaCl Brine-Silica (Q2) | 0.1−150 MPa, 300−423 K, 0−5.4 mol | | $H_2$-Dolomite | 303.15−353.15 K / 0−18 MPa |
| | $H_2$-NaCl Brine-Humic Acid substrate (Q2) | 0.1 MPa, 300 K, 0.5 mol | | $H_2$-Quartz | 303.15−353.15 K / 0−18 MPa |
| | $H_2$-NaCl Brine-Siloxane with defects | 10 MPa, 323 K, 20 wt% | | $H_2$-Calcite | 303.15−353.15 K / 0−18 MPa |
| | $H_2$-NaCl Brine-Halite NaCl | 5−25 MPa, 300−400 K, 0−1 mol | | $H_2$-$SiO_2$ | 300 K / 10−30 MPa |
| | $H_2$-NaCl Brine-Quartz | 5−25 MPa, 300−400 K, 0−1 mol | | $H_2/CH_4$-$SiO_2$ | 300 K / 10−30 MPa |
| | $H_2$-NaCl Brine-Calcite | 5−25 MPa, 300−400 K, 0−1 mol | | $H_2/H_2O$-$SiO_2$ | 300 K / 10−30 MPa |
| | $H_2$-NaCl Brine-Montmorillonite | 5−25 MPa, 300−400 K, 0−1 mol | | $H_2/CH_4/H_2O$-$SiO_2$ | 300 K / 10−30 MPa |
| | $H_2$-KCl Brine-Silica (Q2) | 14−150 MPa, 323−423 K, 0−5.4 mol | | $H_2/CH_4/H_2O$-Kaolinite | 333.15 K / 30 MPa |
| | $H_2/CO_2$-$H_2O$-Calcite | 0.1−70 MPa, 298−373 K | | $H_2/CO_2/H_2O$-Kaolinite | 333.15 K / 30 MPa |
| | $H_2/CO_2$-$H_2O$-Quartz | 0.1−70 MPa, 298−373 K | | $H_2/CH_4$-Montmorillonite | 333 K / 15 MPa |
| | $H_2/CO_2$-$H_2O$-Silica | 10−30 MPa, 333−413 K | | $H_2/CO_2$-Montmorillonite | 333 K / 15 MPa |
| | $H_2/CO_2$-$H_2O$-Silica | 10−30 MPa, 333−413 K | | $H_2/CH_4$-Illite | 333 K / 15 MPa |
| | $H_2/CO_2$-$H_2O$-Graphene | 5−40 MPa, 292−343 K | | $H_2/CO_2$-Illite | 333 K / 15 MPa |
| | $H_2/CH_4$-$H_2O$-Calcite | 0.1−70 MPa, 293−373 K | | $H_2/H_2O$-Kaolinite (Gibbsite and Siloxane) | 298 K / 10 and 20 MPa |
| | $H_2/CH_4$-$H_2O$-Quartz | 0.1−70 MPa, 293−373 K | | $H_2$-Calcite | 298−350 K / 1−10 MPa |
| | $H_2/CH_4$-$H_2O$-Silica | 20 MPa, 373 K | | $H_2$-Hematite | 298−350 K / 1−10 MPa |
| | $H_2/CH_4$-$H_2O$-Graphene | 5−40 MPa, 292−343 K | | $H_2$-Quartz | 298−350 K / 1−10 MPa |
| | $H_2/N_2$-$H_2O$-Silica | 20 MPa, 373 K | | $H_2/CH_4$-Kaolinite | 333.15 K / 30−15−10 MPa |
| | | | | $H_2/CH_4$-Kerogen | 333.15 K / 30−15−10 MPa |
| | | | | $H_2$-Kerogen II-D | 333.15 K / 3−18 MPa |
| | | | | $H_2/CH_4$-Montmorillonite | 333.15 K / 3−18 MPa |
| | | | | $H_2/CO_2$-Montmorillonite | 333.15 K / 3−18 MPa |
| | | | | $H_2$-Kaolinite | 323−403 K / 1−50 MPa |
| | | | | $H_2/CH_4$-Kaolinite | 323−403 K / 1−50 MPa |
| | | | | $H_2/CO_2$-Kaolinite | 323−403 K / 1−50 MPa |

**Table 4. continued**

| Property | System | Condition |
|---|---|---|
| | H$_2$/CH$_4$-Quartz | 339–400 K / 1–50 MPa |
| | H$_2$/CH$_4$/H$_2$O-Quartz | 339–400 K / 1–50 MPa |
| | H$_2$-Kaolinite (Gibbsite and Siloxane) | 303–423 K / 1–30 MPa |
| | H$_2$/H$_2$O-Kaolinite | 318.15 K / 0.1–30 MPa |
| | CH$_4$/H$_2$O-Kaolinite | 318.15 K / 0.1–30 MPa |
| | H$_2$/CH$_4$/H$_2$O-Kaolinite | 318.15 K / 0.1–30 MPa |
| | H$_2$/H$_2$O-Pyrophyllite | 300 K / 0.1 MPa |
| | CO$_2$/H$_2$O-Pyrophyllite | 300 K / 0.1 MPa |
| | H$_2$/H$_2$O-Gibbsite | 300 K / 0.1 MPa |
| | CO$_2$/H$_2$O-Gibbsite | 300 K / 0.1 MPa |
| | H$_2$-Kerogen | 363.15 K / 0.1–50 MPa |
| | CH$_4$-Kerogen | 363.15 K / 0.1–50 MPa |
| | H$_2$/CH$_4$-Kerogen | 363.15 K / 0.1–50 MPa |
| | H$_2$-Na-Montmorillonite | 298–403 K / 1–50 MPa |
| | H$_2$/CO$_2$/H$_2$O-Na-Montmorillonite | 298–403 K / 1–50 MPa |
| | H$_2$/CH$_4$/H$_2$O-Na-Montmorillonite | 298–403 K / 1–50 MPa |
| | H$_2$/CO$_2$/Octane-Kaolinite (Gibbsite and Siloxane) | 300 K / 5.1–30.4 MPa |
| | H$_2$/OMCTS-MCM-41 Silica | 298 K / 0–1 MPa |
| | CO$_2$/OMCTS-MCM-41 Silica | 298 K / 0–1 MPa |
| | H$_2$-Montmorillonite | 333–413 K / 2–30 MPa |
| | H$_2$/H$_2$O-Montmorillonite | 333–413 K / 2–30 MPa |

| Property | System | Condition |
|---|---|---|
| | H$_2$/H$_2$O-Kaolinite | 310–410 K / 30 MPa |
| | H$_2$/NaCl Brine-Kaolinite | 310–410 K / 30 MPa |
| | H$_2$/MgCl$_2$ Brine-Kaolinite | 310–410 K / 30 MPa |
| | H$_2$-Calcium Silicate Hydrate | 300–370 K / 2.5–40 MPa |
| | H$_2$-Kerogen | 360 K / 3–41 MPa |
| | H$_2$/CH$_4$/H$_2$O-Illite | 326 K / 30.4 MPa |
| | H$_2$/CH$_4$/CO$_2$/H$_2$O-Illite | 326 K / 30.4 MPa |
| | H$_2$/CH$_4$/H$_2$O-Kerogen | 326 K / 30.4 MPa |
| | H$_2$/CH$_4$/CO$_2$/H$_2$O-Kerogen | 326 K / 30.4 MPa |
| | H$_2$/H$_2$O-Pyrophyllite | 368.15 K / 30 MPa |
| | H$_2$/H$_2$O-Montmorillonite | 368.15 K / 30 MPa |
| | H$_2$/H$_2$O-Beidellite | 368.15 K / 30 MPa |
| | H$_2$/H$_2$O-Calcite | 353 K / 20 MPa |

[a]For each property, the table contains the specific systems investigated and the conditions of the studies. The relevant methods and in-depth discussions per property can be found in this review in the following sections: pVT: Sections 3.2 and 3.3 (methods), Section 4.2 (discussion). Diffusivities and thermodynamic factors: Sections 3.2.3, 3.2.4, and 3.2.13 (methods), Section 4.2.5 (discussion). Interfacial tension: Section 3.2.16 (methods) and Section 4.9 (discussion). Wetting: Section 3.2.17 (methods) and Section 4.10 (discussion). Adsorption on clays: Section 3.3.2 (methods) and Section 4.7 (discussion).

by molecular diffusion (see Fig. 12) and hydrodynamic dispersion[265] caused by cyclic injection and production. The generalized Fick's law describes this multi-component diffusion, relating the mass flux of each component to the concentration gradients of the others, governed by the mutual diffusion coefficient.[266,267] These coefficients depend on thermodynamic state variables such as the pressure, temperature, and composition of the mixture. MD simulations can yield both accurate predictions of these coefficients, enhancing our understanding of the gas mixing behavior under various conditions relevant to subsurface H$_2$ storage.

H$_2$ and other gases in the reservoir interact with brine, leading to dissolution and exchange of molecules between the gas and liquid phases. The solubility of H$_2$ in the brine, which depends on factors such as pressure, temperature, and salinity, determines the mole fraction of dissolved H$_2$ and the moisture content in the gas phase at equilibrium (see Fig. 12). Accurate knowledge of these solubilities is critical for maintaining H$_2$ purity, and optimizing storage conditions. Molecular simulations offer a detailed view of these interactions, allowing for precise predictions of solubilities and the overall phase behavior. The interfacial tension between H$_2$ and brine significantly affects the stability and integrity of the storage system. The interfacial tension not only suppresses phase mixing, maintaining sharp gas-brine boundaries, and thus, reducing leakage,[259] but also promotes capillary trapping, in which H$_2$ becomes immobilized within brine-saturated pores on the grain scale. Although limiting phase mixing helps preserve the purity of stored H$_2$, capillary trapping within brine-filled pores diminishes the recoverable volume and thus hampers the effectiveness of underground hydrogen storage (UHS).[261] Because direct experimental measurements of such nanoscale forces are challenging, molecular simulations are indispensable for quantifying interfacial tension and elucidating the mechanisms of the H$_2$ brine interaction, thus guiding the design of safer and more efficient storage strategies.

Another property, important for UHS, is the contact angle between H$_2$, brine, and the solid geological matrix, which influences the wettability of the rock and the overall capillary pressure in the system (see Fig. 12). This, in turn, affects the storage capacity and retrievability of H$_2$. Molecular simulations can be performed to predict the wetting behavior and contact angles in these systems, offering insights into how to modify surface properties to improve storage performance. While atomistic simulations provide useful insight into inter- and intra-molecular forces, and capture the fundamental physics of the wetting phenomena, they cannot always provide accurate quantitative predictions. Therefore, coupling molecular simulations with higher scale modeling methods is essential for studying, and ultimately, improve UHS performance. Key transport and displacement processes unfold over pore networks that extend from millimeters to centimeters and feature tortuous throats and irregular geometries, length scales far beyond the reach of molecular dynamics because of the prohibitively large number of molecules needed for the simulations. To describe flow and capillary behavior in such media, one must therefore couple the interfacial properties (e.g., surface tension, contact angle, diffusion coefficients) computed from molecular simulations to mesoscale or continuum models, such as pore-network and lattice-Boltzmann frameworks, volume-of-fluid CFD solvers, or hybrid multiscale schemes. UHS is thus inherently multiscale, which means that only by integrating molecular-level data into coarser-scale simulations one can predict injectivity, storage capacity and H$_2$ retrievability relevant for UHS.

Understanding adsorption — the process by which gas molecules adhere to the surfaces of solids — is important for evaluating the feasibility and efficiency of UHS in geological formations. Adsorption can provide information related to the storage capacity, retention time, and potential leakage risks of H$_2$ within these formations, essential for ensuring both efficiency and safety.[268] Additionally, interactions between H$_2$

and swelling clays at grain contacts, involving adsorption and desorption, can induce clay swelling.[261] This swelling may lead to small normal and shear strains, resulting in stresses between individual grains. Over the lifespan of a $H_2$ storage complex, such stresses could contribute to mechanical fatigue and permanent deformation of the reservoir, leading to induced seismicity.[261] Therefore, sorption processes not only influence the retrievability of stored $H_2$ but also play a significant role in the long-term stability and safety of the storage site. The complexity of the subsurface environment, with its variations in pressure, temperature, mineral compositions, and complex pore morphologies, makes predicting adsorption behavior of $H_2$ an arduous task. Performing experimental measurements to study adsorption under these challenging conditions is fraught with practical challenges and risks, such as the high flammability of $H_2$ and the difficulty of replicating complex subsurface conditions in the laboratory. Molecular simulations have emerged as a powerful tool to overcome these challenges. Molecular simulations can accurately model the interactions between $H_2$ molecules and the diverse mineral surfaces found in geological formations, such as shale, quartz, and kerogen.[268] By replicating subsurface conditions, molecular simulations help predict the adsorption capacity and behavior of $H_2$, including its interaction with other gases like $CH_4$ and $CO_2$. The computed adsorption isotherms can then be used as input to reservoir-scale simulators to predict the transport of multicomponent $H_2$ mixtures, thus, helping in building predictive models for UHS.

From the short discussion above, it becomes apparent that molecular simulations are indispensable for advancing our understanding of subsurface $H_2$ storage systems. By providing detailed insights into gas-gas mixing, vapor-liquid equilibrium, interfacial tensions, and wetting behaviors, molecular simulations enable the optimization of storage strategies, ensuring safe, efficient, and long-term $H_2$ storage in geological formations. In an effort to build a sustainable energy future, taking full advantage of the power that molecular simulations offer will be crucial in overcoming the challenges associated with large-scale $H_2$ storage. To facilitate navigation, Table 4 provides a summary of key properties relevant to UHS, indicating the sections where relevant computational methods are explained and where the discussion of related articles can be found in this review.

## 2.4. Hydrogen Transport

**2.4.1. Transport in Polymer Pipelines.** $H_2$ economy presents new opportunities and challenges for pipeline systems. Currently, $H_2$ is mainly transported in compressed pressure vessels, tube trailers, and pipelines. Pipeline transport offers advantages due to high capacity, extensive inter-connectivity, geographic coverage, and relatively low operational costs. While over 5,000 km of $H_2$ pipelines exist globally, these are primarily constructed of various steel grades that face significant challenges from hydrogen embrittlement as discussed in more detail in Section 2.4.2. For this reason, polymer pipelines are considered a plausible solution for the transport of gaseous $H_2$ due to intrinsic advantages over traditional metallic infrastructures, such as corrosion resistance, flexibility, cost-effectiveness, and the ability to form robust joints through fusion techniques.[269] Among the numerous available polymeric materials, PE (and HDPE) is the predominant choice for gas distribution networks, comprising 90-95% of new installations in Europe and the United

States.[270] Despite their advantages, polymer pipelines face distinct challenges when transporting $H_2$. The most important drawback is the enhanced permeation rate of $H_2$ molecules through the polymer matrix, which can be up to five times higher than that of $CH_4$. The permeability is also heavily affected by the temperature and pressure conditions. Other disadvantages are the so-called blistering risk (i.e., $H_2$ absorbed by the polymer liner at high pressure cannot escape quickly enough during decompression, causing internal pressure buildup that creates blisters on the material), and various other possible material failure mechanisms which are outside the context of this review.[271] The semi-crystalline structure of PE consists of long polymeric chains with varying lengths and side branches. Pipeline performance is primarily determined by the base resin density, molecular weight of these chains, and their distribution. The viscoelastic properties of PE create complex creep and stress relaxation behaviors that make short-term tests inadequate for predicting long-term performance.

As with all aspects of $H_2$ technology discussed thus far, the safe and effective transport of $H_2$ through polymer pipelines requires deep understanding of material properties, manufacturing processes, and operational conditions. With the plans to expand $H_2$ infrastructure, developing polymer systems with enhanced barrier properties will be crucial for maintaining integrity and safety in transportation networks. Toward this goal, molecular simulation has become a widely used tool for studying $H_2$/polymer systems, as also discussed in Sections 2.2.1 and 2.3.1. As expected, the main body of the relevant molecular simulation literature focuses on PE/HDPE, which are the most adequate materials for pipelines. Nevertheless, $H_2$ interactions with other polymers such as ethylene-vinyl alcohol copolymer (EVOH) (a promising alternative to HDPE), poly(dimethylsiloxane) (PDMS), poly(chloro-p-xylene), polystyrene (PS), rubbery matrices, and polysaccharides have been studied via molecular simulation in a broader context spanning $H_2$ applications beyond transport in pipelines. The vast majority of these studies focus on the same properties (i.e., sorption, diffusion, and permeation), make use of similar methods (MC for computing sorption and MD for gas transport coefficients - see Section 3) and force fields (see Section 3.1.4). A representative selection of molecular simulation studies in this field is reviewed in Section 4.4.

**2.4.2. Hydrogen Embrittlement of Metallic Pipelines.** Numerous efforts for designing metallic pipelines such that they are compatible with $H_2$ are made by both the industry and scientific community. This is not a simple engineering task since the presence of atomic hydrogen (H) in metals (e.g., in steels used in existing natural gas pipelines) results in the deterioration of mechanical properties, such as strength and deformability. This phenomenon is known as hydrogen embrittlement (HE)[21,272−277] and can occur even at extremely low $H_2$ concentrations (in the order of 1 ppm). Therefore, HE poses a significant challenge to the safe transportation of gaseous $H_2$ via pipelines. The complexity behind understanding the fundamental mechanisms of HE lies in the fact that it requires an accurate description of the atomic H trapping and diffusion in the presence of different kinds of microstructural features. The diffusivity study, in particular, is crucial as the fact that the diffusible H causes embrittlement, is well established.[278,279] The minute amount of H present in a material, is attracted towards stress fields e.g., front of crack tip where it concentrates causing brittle fracture. Diffusion measurements e.g., permeation tests and Thermal Desorption

**Table 5. Thermophysical and Mechanical Properties Investigated in Relation to the Mechanisms Governing Hydrogen Embrittlement of Metals[a]**

| | | Relevant sections | |
|---|---|---|---|
| Properties | Materials | Methods | Discussion |
| H diffusion | bcc Fe; fcc Ni; bcc MoNbTaW; fcc FeMnCrCoNi | 3.2.7, 3.2.9, and 3.3.5 | 4.11.1, 4.11.6, and 4.11.7 |
| H trapping and H-mediated vacancy behavior | Carbides; oxides; bcc Fe; fcc Cu and Pd; bcc MoNbTaW; fcc CrCoNi, FeMnCrCoNi | 3.2.7 and 3.2.8 | 4.11.2, 4.11.6, and 4.11.7 |
| Dislocation nucleation and mobility | fcc Ag, Ni, Pd; bcc Fe; fcc FeNiCr and FeMnCrCoNi | 3.2.10 and 3.3.5 | 4.11.3, 4.11.6, and 4.11.7 |
| Crack propagation and GB decohesion | fcc Ni; bcc Fe; fcc CrCoNi, CoNiV, CoCrFeNi and FeMnCrCoNi | 3.2.7, 3.2.11, and 3.3.5 | 4.11.4 and 4.11.6 |
| Complex deformation behavior | fcc Ni; bcc Fe; hcp Mg | 3.2.7 and 3.3.5 | 4.11.5 |

[a]The sections that detail the methods and the subsequent discussion are indicated.[292]

Analysis (TDA),[280] have indicated that diffusible H can be trapped in microstructural features e.g., grain boundaries (GBs) and carbides. There is experimental evidence[281] that a material in service does not suffer from HE if the diffusible H can be controlled. This observation forms the basis of designing alloys with irreversible traps for immobilizing diffusible H.[281−283] Another effective way to reduce the amount of diffusible H in the material is by the usage of coatings, such as oxides and metallic alloys, which act as barriers against H thereby reducing the H uptake by the material.[283] The Slow Strain Rate Test (SSRT) performed within recent works[31,284] has shown that the stress-strain curves of H charged coated sample is similar to that of uncharged bare sample of X70 pipe steel. Most of the experimental techniques employed in the investigation of H in materials operate at the macro-scale and hence lack spatial resolution, thus, making the determination of H trapping sites difficult, especially when H is trapped in nano-sized precipitates. In this regard, Atom Probe Tomography (APT), which allows high spatial resolution, proves to be a reliable tool for nano-scale visualization of H distribution in steels.[285−288] Another useful experimental technique in this regard is the Small Angle Neutron Scattering (SANS).[289,290] The individual underlying mechanisms are, however, still hard to elucidate experimentally since the complexity of the steels implies combined effects.

HE in metallic pipelines is a multi-disciplinary phenomenon, involving chemical processes and mechanical deformation across a wide range of spatial and temporal scales.[291] At the chemical level, HE is initiated with $H_2$ adsorption and dissociation on metal surfaces, followed by atomic H diffusion into bulk lattices, vacancies, dislocation cores, and GBs. All involved processes, i.e., adsorption, absorption, desorption, and lattice diffusion, are governed by distinct thermodynamic and kinetic parameters, which strongly depend on the local microstructure. Concurrently, mechanical deformation involving crack propagation, GB decohesion, dislocation nucleation and motion, and vacancy formation interacts continuously with H diffusion, leading to coupled chemo-mechanical degradation.[292] Capturing these phenomena demands a hierarchical, multi-scale modeling approach: DFT simulations provide atomically accurate energetics and kinetics of H behavior at the sub-nanometer scale; MD simulations, with classical interatomic potentials, enable insights into defect-driven deformation processes at the nano-meter and nano-second scales; and Kinetic Monte Carlo (KMC) methods allow for the study of H diffusion and trapping processes over significantly longer, time-scales (i.e., milliseconds to seconds). Bridging

these methodologies offers a powerful and comprehensive framework to unravel the fundamental mechanisms underlying HE, enabling more accurate predictions and effective mitigation strategies for metallic structural components in H-rich environments. Table 5 summarises the key properties investigated in HE, and the metallic systems considered, while referring the reader to the sections where the relevant methods and discussion are presented in this review.

**2.4.3. Liquid Hydrogen.** As already discussed earlier in this review, the implementation of green $H_2$ is currently seriously hindered by the challenges related to transport and storage. Gaseous $H_2$ has an extremely low volumetric energy density, which can be increased if $H_2$ is liquefied. However, liquefaction is an expensive process that normally requires very low temperatures (ca. 20 K). The specific liquefaction energy is roughly equal to 15 kWh/kg, which corresponds to 1.5 Euros/kg if a realistic electricity price of 0.1 Euros/kWh is used.[293] The high energy consumption is a consequence of the low liquefaction temperatures that can only be attained by complex refrigeration cycles, and the unique behavior of $H_2$ at very low temperatures (the so-called quantum effects).[294] The molecules of $H_2$ can exist in two forms depending on the spins on the two H nuclei. If both spins are symmetric, i.e., in the same direction, the molecule is called ortho-$H_2$ (o-$H_2$) and when the spins are anti-symmetric, the molecule is referred to as para-$H_2$ (p-$H_2$). o-$H_2$ molecules have a higher energy state than the p-$H_2$ molecules. $H_2$ at room temperature contains 75% o-H2 and 25% p-H2, but the para-fraction is increased to almost 100% as the temperature is reduced to the liquefaction temperature of ca. 20 K. Due to the difference in the energy state of the spins, the ortho-to-para conversion is highly exothermic and releases a huge amount of heat during liquefaction. The released heat should be removed, which increases the cooling demand (energy requirement) of the refrigeration cycle. However, the heat release is not linear but increases exponentially with decreasing temperature. An interesting conclusion from this physics exercise is that it would be beneficial if $H_2$ could be liquefied at higher temperatures, because that would reduce the cooling demand as most of the energy is consumed at the lower temperatures (due to increased heat release). This sounds almost impossible, because the liquefaction of $H_2$ is governed by its pressure-temperature diagram (saturation line), which states that $H_2$ can be at the liquid state only in a temperature range of 14 K (triple point) to 33 K (critical point). Interestingly, a molecular simulation study in 2005 by Han et al.[295] showed that $H_2$ can be liquefied at 80 K if the liquefaction is performed under confinement in a carbon nanotube (CNT). This phenomenon was attributed to the

strong electrostatic interaction between the CNT and $H_2$ molecules, which induce local-ordering of the $H_2$ molecules and results in liquefaction. Note that such a finding does not necessarily violate thermodynamics, because the previously mentioned liquefaction temperature range of 14 to 33 K holds for bulk systems, which may be different for systems under confinement. However, the understanding of $H_2$ liquefaction under confinement is poorly studied and understood. To the best of our knowledge, no other theoretical or experimental studies to date were reported to verify the results of Han et al.[295] This showcases the power of molecular simulation not only as a predictive tool, complementary to experiments, but also as a vehicle for exploring new $H_2$ technologies. More details on this and a few other studies related to molecular simulation of liquid $H_2$ are provided in Section 4.3.

# 3. MOLECULAR SIMULATION METHODS FOR COMPUTING THERMOPHYSICAL PROPERTIES OF HYDROGEN SYSTEMS

In this section, we provide an overview of the most widely used methods and models for computing thermophysical properties of $H_2$ systems. Although a lot of ground related to thermodynamic, transport, interfacial, and structural properties, as well as physical mechanisms and force fields is covered here, a detailed discussion on statistical mechanics fundamentals, derivations of equations, and a full list of possible methods are out of the scope of this review. For such information, the reader is referred to relevant textbooks in the field of molecular simulation.[51,52,296−299]

## 3.1. Force Fields

To a great extent, the accuracy of classical molecular simulations, both MD and MC, relies on semi-empirical models, the so-called force fields, which describe the intra- and inter-molecular interactions between the atoms and molecules in the system. Thus, it is not surprising that rigorous effort has been put during the past five decades by numerous researchers to design "high-performance" force fields with varying complexity for almost all types of chemical species. "High-performance" entails that a force field is able to accurately reproduce as many experimentally measured thermophysical properties of a species as possible. Such a performance is usually tied to the strategy followed during the parameterization of the force field, e.g., the number and type of properties considered, the range of conditions, the functional forms used to approximate inter- and intra-molecular forces.

The main focus of force fields for important components, such as water, hydrocarbons, electrolytes, and bio-molecules, has been the replication of phase behavior, volumetric properties, structure, transport coefficients, and energies.[56,300−307] It is important to note that due to the fact that force fields are primarily fitted to experimental data, the abundance and accuracy of the available experimental data are crucial elements for accurate molecular simulations. Complementary, the significant attention put in performing MC and MD simulations for the prediction of many $H_2$ properties is a motivation for further experimental effort. In this review, we provide a brief discussion on force fields commonly used to perform molecular simulations of $H_2$ systems. The main focus is on the $H_2$ force fields, pure or in aqueous electrolyte solutions (important for electrochemical processes), systems involving $H_2$ and solid surfaces (important for storage), and organic components (important for separation applications).

Since this review paper mainly focuses on classical force fields, it is important to delineate the conditions under which quantum effects become significant and lead to noticeable deviations in the prediction of thermophysical properties using classical molecular simulations. The criteria discussed below serve as indicators for the onset of quantum mechanical contributions that should not be neglected. A commonly used criterion is based on the comparison between the thermal de Broglie wavelength and the characteristic interparticle spacing, approximated by mean nearest neighbor separation, $(V/N)^{\frac{1}{3}}$.[308] The de Broglie wavelength is given by

$$\Lambda = \left(\frac{h^2}{2\pi m k_B T}\right)^{1/2} \tag{1}$$

where $h$ is Planck's constant, $m$ is the particle mass, $k_B$ is the Boltzmann constant, and $T$ is the absolute temperature. Bartolomeu and Franco[308] report representative values for the ratio $\Lambda/(\frac{V}{N})^{\frac{1}{3}}$ as 0.36 at 100 K and 1000 bar, and 0.016 at 400 K and 1 bar. For liquid $H_2$, this ratio approaches 0.97, indicating that quantum effects are substantial and should be explicitly accounted for. A second criterion involves the comparison between the rotational temperature $\Theta_{rot}$ of molecular $H_2$ and the simulation temperature. Quantum effects in rotational degrees of freedom become significant when $\Theta_{rot}$ is comparable to or greater than the system temperature.[308] For molecular hydrogen, the rotational temperature is ca. 86 K, and is defined as

$$\Theta_{rot} = \frac{h^2}{8\pi^2 I k_B} \tag{2}$$

where $I$ is the moment of inertia of the molecule. If either of these criteria is fulfilled, classical simulations may yield inaccurate results. A way to mitigate this drawback is using the so-called quantum corrections (discussed in Section 3.1.1).

**3.1.1. Hydrogen.** Many different classical force fields have been developed for $H_2$, differing on the experimental/ab-initio parameters they are trained on, the functional form, and the number of interaction sites.[48,309−314] While the discussion we are presenting here does not aim to be exhaustive, it covers several of the most frequently used $H_2$ models in molecular simulation studies. Our goal is to highlight key parameter choices, point out inconsistencies and ambiguities that have emerged in the literature, and identify points of attention for researchers aiming to ensure consistency and reproducibility in the application of $H_2$ force fields. It is important to acknowledge the detailed assessment by Barraco et al.[309], who systematically compared eight Lennard-Jones (LJ)−based models in the gas phase, at conditions relevant to $H_2$ storage in tanks. To ensure cohesion and provide a self−contained overview, we also summarize relevant aspects of their findings in this review.

In classical simulations, the most popular functional form describing the pairwise attractive (van der Waals) and repulsive (Pauli's exclusion) forces is the 12-6 LJ potential ($U_{LJ}$)[51]

$$U_{LJ} = 4\epsilon_{ij}\left[\left(\frac{\sigma_{ij}}{r_{ij}}\right)^{12} - \left(\frac{\sigma_{ij}}{r_{ij}}\right)^6\right] \tag{3}$$

where $\epsilon_{ij}$ and $\sigma_{ij}$ are the so-called energy and size parameters, respectively, and $r_{ij}$ is the distance between species $i$ and $j$.

Although most $H_2$ force fields are based on the 12-6 LJ potential, the 9-6 LJ form has also been used e.g., in the IFF (9-6) force field[313] and the COMPASS force field of Yang et al.[315], Sun[316]. $H_2$ force fields using the 9-6 LJ potential have larger $\sigma_{ij}$ values than the 12-6 LJ to compensate for the reduced repulsive interactions.[309] The LJ potential can be considered as a special case of the more general Mie potential:

$$U(r) = \frac{n}{n-m}\left(\frac{n}{m}\right)^{\frac{m}{n-m}} \times \varepsilon\left[\left(\frac{\sigma_{ij}}{r_{ij}}\right)^n - \left(\frac{\sigma_{ij}}{r_{ij}}\right)^m\right]$$

(4)

By setting $n = 12$ and $m = 6$, one recovers the familiar 12-6 LJ potential, while $n = 9$ and $m = 6$ yields the softer-repulsion 9-6 LJ variant. Bartolomeu and Franco[308] proposed a single-site Mie potential, known as the SAFT-$\gamma$ Mie force field, using parameters previously optimized within the SAFT-VR Mie EoS framework.

To account for the electrostatic interactions, the most common approximation in $H_2$ force fields is Coulomb's law[51]

$$U_{Coul} = \frac{q_i q_j}{4\pi\epsilon_0 r_{ij}^2}$$

(5)

where $q_i$ is the charge of species $i$, and $\epsilon_0$ is the electric constant. Force fields that incorporate charges can be classified in two different categories, i.e., non-polarizable and polarizable. In non-polarizable force fields, $H_2$ is modelled using fixed point charges. Polarizable force fields account for the change in the charge distribution of a molecule depending on the environment.[314] Most of the $H_2$ models to date are non-polarizable.[309–311,313] For models with no intramolecular degrees of freedom, the total potential energy of the system follows from the summation of Eq. (3) and Eq. (5).[51,52] The combination of LJ and Coulombic potentials is not always sufficient to describe strong adsorption interactions of $H_2$ with materials.[317] In such cases, instead of the LJ, the Morse potential is used[318]

$$U_{Morse} = D_{ij}(1 - \exp[-\alpha(r_{ij} - r_{ij}^*)])$$

(6)

where $D_{ij}$ and $r_{ij}^*$ are the interaction and size parameters (analogous to $\epsilon_{ij}$ and $\sigma_{ij}$ for the LJ potential), respectively. Parameter $\alpha$ controls the width of the potential well. This extra fitting parameter of the Morse potential allows for better reproducibility of $H_2$ adsorption onto materials with exposed metal centers, such as MOFs.[317] Another functional form of intermolecular potentials of $H_2$ is the so-called Exp-6 (Buckingham). Although such models have been already derived more than 70 years ago (see for example the work of Mason and Rice[319]), they are scarcely used in molecular simulations of $H_2$ systems, and therefore, we do not discuss them further.

Fig. 13 shows a schematic representation of single-, two-, and three-site $H_2$ force fields. In single-site force fields, $H_2$ is assumed to have only one effective interaction site (united atom approach), which interacts with the surrounding molecules using only two-body attractive and repulsive forces.[309,320] The model by Vrabec and co-workers[48] (also referred to as Köster), with $\epsilon/k_B = 25.84$ K and $\sigma = 3.0366$ Å, was fitted to reproduce speed of sound and $PVT$ data in the 50-250 K range. In contrast, the potential by Buch[312] focuses on capturing orientational effects of $H_2$ at low temperatures (parameters: $\epsilon/k_B = 34.2$ K and $\sigma = 2.96$ Å). Hirschfelder et al.[321] proposed multiple sets of LJ parameters based on different datasets and methodologies: fitting to classical
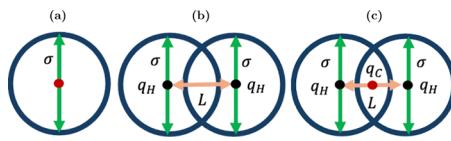


**Figure 13.** Schematic representations of (a) single-site, (b) two-site, and (c) three-site LJ-based $H_2$ force fields. The green arrows represent the $\sigma$ value of the LJ potential, the pink arrows represent the bond distance ($L$) of $H_2$, and $q_H$ and $q_C$ represent the charges on the H-atom and the center of mass of $H_2$, respectively. The force fields developed by Buch,[312] Köster et al.,[48] and Hirschfelder et al.[321] are examples of one-site force fields, in which the LJ site is located at the center of mass of $H_2$. The force fields developed by Cracknell[311] and Wang et al.[313] are examples of two-site force fields, in which the LJ sites are separated by a bond length $L$. The force fields by Cracknell[311] and Wang et al.[313] are non-polarizable and do not use charges (i.e., $q_H = 0$). The force field by Marx and Nielaba[310] is an example of a three-site $H_2$ force field, which accounts for the quadruple moment of $H_2$. Three-site LJ force fields can have up to three different LJ sites. This figure is based on the work of Barraco et al.[309]

viscosity data yields either $\epsilon/k_B = 33.3$ K, $\sigma = 2.968$ Å or $\epsilon/k_B = 38.0$ K, $\sigma = 2.915$ Å, while fitting to second virial coefficients produces $\epsilon/k_B = 37.0$ K, $\sigma = 2.928$ Å (quantum-based) and $\epsilon/k_B = 29.2$ K, $\sigma = 2.87$ Å (classical). The authors recommend using the viscosity-based fits for transport property calculations, and the virial-based parameters for thermodynamic modeling. In their review, Barraco et al.[309] refer to the parameter set $\epsilon/k_B = 37.0$ K and $\sigma = 2.928$ Å, derived from fits to the second virial coefficients. Rzepka et al.[322] and Ferrando and Ungerer[323] used the classically derived parameters from Hirschfelder's viscosity-based model, i.e., $\epsilon/k_B = 33.3$K and $\sigma = 2.97$ Å. Similarly, Caviedes and Cabria[324] adopted this parameter set in their study of $H_2$ storage capacities in slit-shaped pores, nanotubes, and torusenes. In contrast, Rahbari et al.[110] used the alternative viscosity-based parameterization by Hirschfelder, namely $\epsilon/k_B = 38.0$ K and $\sigma = 2.915$ Å. The specific rationale for selecting among the four parameter sets proposed by Hirschfelder is not necessarily explicitly addressed in these studies; however, in most cases, the choice appears to align with the focus and requirements of the respective application.

Two-site force fields, such as the IFF force field by Wang et al.[313], provide a more realistic representation of the structure of $H_2$ by including explicit interaction sites for each atom. This also allows for the inclusion of intra-molecular interactions, often represented by harmonic potentials, which capture the H-H bond vibrations. These vibrations are particularly important for accurately predicting spectroscopic properties such as Raman and IR spectra. However, this approach, due to the high-frequency nature of vibrational modes, requires the use of smaller MD integration time steps (typically <1 fs) to maintain numerical stability due to the high-frequency nature of vibrational modes. Despite their importance for vibration-dependent properties, the use of two-sites in the $H_2$ force fields has limited impact on the prediction of bulk thermodynamic and transport properties, such as self-diffusivities, $pVT$ relations, and physisorption of $H_2$, which are dominated by slower translational and rotational motions.[311] For many practical applications, the additional computational cost of resolving vibrations is unnecessary, and the use of simpler, rigid models (i.e., with a fixed bond length) is sufficient. Nevertheless, several two-site inter-molecular potentials have been

**Table 6. Overview of Selected Hydrogen Force Fields and Their Parameters**[a]

| Force Field | No. of Sites | Fitting Basis | $\epsilon/k_B$ | $\sigma/Å$ | $q_H/e$ | Q/DÅ | Temperature/ Pressure Range |
|---|---|---|---|---|---|---|---|
| Vrabec[48] | 1 | Speed of sound, PVT data, enthalpy of vaporization | 25.84 | 3.0366 | | | 50−250 K |
| Buch[312] | 1 | Potential energy, para-ortho $H_2$ clusters | 34.2 | 2.96 | | | Low T (34 K) |
| Hirschfelder (a)[321] | 1 | Viscosity (classical) | 33.3 | 2.968 | | | Not specified |
| Hirschfelder (b)[321] | 1 | Viscosity (classical) | 38.0 | 2.915 | | | Not specified |
| Hirschfelder (c)[321] | 1 | 2nd virial (quantum) | 37.0 | 2.928 | | | Not specified |
| Hirschfelder (d)[321] | 1 | 2nd virial (classical) | 29.2 | 2.87 | | | Not specified |
| Mondal[334] | 1 | | 9.56 | 3.14 | | | |
| Yang and Zhong[325] | 2 | PVT and self-diffusion | 10.0 | 2.72 | | | 80−300 K, up to 600 bar |
| Cracknell[311] | 2 | Adsorption energy, $Q_{st}$ in pores | 12.5 | 2.59 | | | 298 K |
| Yang | 2 | Bulk PVT fit | | | | | |
| Sun[331] | 3 | VLE near-critical region | 8.06 | 3.03 | 0.47 | | near critical region |
| SAFT-$\gamma$-Mie[308] | 2 | Heat capacity at constant pressure, speed of sound, PVT data | 18.355 | 3.1586 | | | |
| Marx and Nielaba[310] | 2+Q | Bond length, enthalpy of adsorption, isochoric heat capacity | 36.7 | 2.958 | | 0.6369 | Not specified |
| Bouanich[330] | 2+Q | 2nd virial coeff. fit | 11.2544 | 2.68259 | 0.1108 | | 98−773 K |
| TraPPE[331] | 2+Q | VLE near critical | 8.06 | 3.03 | 0.47 | | 33 K |
| Belof[332] | 3+Q | Ab initio, second virial coefficient, pressure-density relations | 8.8516 (COM), 4.0659 (outer) | 3.2293 (COM), 2.3406 (outer) | 0.3732 | | 50−500 K; 0−2000 atm |

[a]For extended discussion on the paremeters and consistency issues, the reader is referred to Section 3.1.1. $\epsilon$ and $\sigma$ are the LJ parameters (see Eq. (3)). Two- and three-site LJ force fields with a quadrupole are referred to as 2+Q and 3+Q, respectively.

developed to describe molecular $H_2$ based on different calibration targets. Yang and Zhong[325] proposed a $H_2$ model using parameters $\epsilon/k_B = 10$ K and $\sigma = 2.72$ Å, with a fixed bond length of 0.74 Å. This model was calibrated using experimental PVT data and self-diffusion coefficients of $H_2$ over a temperature range of 80−300 K and pressures up to 600 bar. Cracknell[311] proposed a two-site intermolecular potential for $H_2$ with $\epsilon/k_B = 12.5$ K, $\sigma = 2.59$ Å, and a fixed bond length of 0.74 Å. The LJ parameters were adjusted to reproduce $H_2$ adsorption behavior in graphitic slit pores, specifically targeting agreement with isosteric heats and adsorption isotherms obtained from earlier Path Integral Monte Carlo (PIMC) simulations.

The following models extend the two-site description of $H_2$ by incorporating electrostatic interactions via embedded quadrupoles, most commonly implemented through point-charge arrangements rather than explicit multipole sites. Most of the molecular simulation software packages do not support point multipole sites,[326] and thus, point charges are often preferred. Dipole moments can, in principle, be represented by a pair of closely spaced point charges ($+q$, $-q$), yielding a dipole moment $\mu_d = qd$. Similarly, three point charges ($+q$, $-2q$, $+q$) can be arranged to reproduce a quadrupole moment of the form $Q = 2qd^2$. Either the distance $d$ or the charge $q$ may be specified, and the choice of parameter is non-trivial.[326] In this review, most of the surveyed studies use point-charge models. In the case of the force field developed by Marx and Nielaba[310], some confusion has arisen regarding the specific charges used to reproduce the quadrupole moment, as noted by Barraco et al.[309] The parameters reported by Marx and Nielaba[310] are $\sigma = 2.958$ Å, $\epsilon/k_B = 36.7$ K, and a reduced quadrupole moment of $Q/((\pi\epsilon_0 k_B)^{1/2}=54.2$ in units of $(KÅ)^{1/2}$. While this quadrupole can be implemented directly via a point-multipole interaction, it may also be represented

using three point charges, if needed.[48] Köster et al.[48] refer to this value as $Q = 0.6369$ DÅ. Calculating the corresponding partial charge using the definition of the quadrupole yields $q/e = 0.120746$, as also reported by Barraco et al.[309], which is consistent with the original model.

Darkrim et al.[327] referenced a charge of $q = 0.615 \times 10^{-26}$ esu associated with quadrupole interactions between $H_2$ molecules. This appears to be a typographical or unit error. Interpreting this instead as $q = 0.615 \times 10^{-10}$ esu, an equivalent $q/e = 0.1280$ is obtained, which is close to the original charge of the force field.[309] Using the relation $Q = 2qd^2$ with $d = 0.741$ Å, the resulting quadrupole moment is $Q = 0.675$ DÅ, which is close to the value of 0.6369 DÅ reported by Köster et al.[48] In sharp contrast, using the originally stated[327] $q = 0.615 \times 10^{-26}$ esu underestimates the original quadrupole magnitude by several orders of magnitude. Ferrando and Ungerer[323] adopted the charge parameter of $q/e = 0.4664$ for the $H_2$ atom, which seems to deviate from the original force field by Marx, followed up by Darkrim. Similarly, Rahbari et al.[110] and Bartolomeu and Franco[308] adopted the LJ parameters from the Marx force field but used partial charges of $q = +0.468$ for $H_2$ and $-2q$ for the center of mass, which does not reproduce the quadrupole moment reported in Marx and Nielaba[328]. Another example of inconsistency appears in Li et al.[329] and Ferrando and Ungerer[323] who adopted the model by Darkrim et al.,[327] itself based on the Marx force field, and reported charges of $q = 0.4664$ for $H_2$ and $-2q$ for the center. It is unclear how this value was derived from the $q = 0.615 \times 10^{-26}$ esu cited in ref 327 as it does not reproduce the quadrupole originally reported by Marx and Nielaba. Bouanich[330] proposed another two-site $H_2$ LJ 12-6 potential with quadrupole having $\sigma = 2.68259$ Å, $\epsilon/k_B = 11.2544$ K with a fixed bond length of 0.7508 Å. The partial charge supplemented on $H_2$ sites is $q/e = 0.1108$ with a $-2q$ charge

in the center of mass. This force field was fitted using the experimental second-virial coefficients in the 98-773 K temperature range. Sun et al.[331] proposed a rigid three-site (H− M− H) potential for $H_2$ with LJ parameters $\sigma$ = 3.03 Å and $\epsilon/k_B$ = 8.06 K, and an intramolecular H-H distance of 0.741 Å. Partial charges of $q_H$ = +0.47 $e$ are placed on each H atom and a compensating charge of $q_M$ = −0.94 $e$ on the central M-site. The force field parameters were fitted using Monte Carlo simulations to reproduc experimental VLE data of $H_2$ near the critical temperature (ca. 33 K). Although it is not always possible to trace the complete history of how force field parameters have been used, adopted or modified, it is important to emphasize the need for careful comparison with original references and to explicitly report any deviations or assumptions made by subsequent authors.

Three-site force fields add further complexity by introducing an additional interaction site, typically placed at the geometric center of the molecule or representing a pseudo-atom. This approach enables a better representation of the electronic charge distribution within $H_2$, capturing dipole-induced interactions and quadrupole effects more accurately. These effects are particularly relevant in systems where electrostatic interactions play a significant role, such as in the study of $H_2$ interactions with polar surfaces or within electric fields. Although three-site models improve the accuracy of intermolecular interactions, there is a higher computational cost compared to one-site and two-site models. Belof et al.[332,333] parameterized both polarizable and non-polarizable potentials for $H_2$, derived from first-principles calculations. The non-polarizable LJ 12-6 potential incorporates three LJ interaction sites along with an embedded quadrupole moment. A fixed bond (with length of 0.742 Å) is used at the ends of which the masses are placed along with a charge of $q/e$ = 0.3732 each. The charge neutrality is conserved by the addition of a counter charge of $-2q$ at the center of mass. The LJ interaction site ($\epsilon/k_B$ = 8.8516 K and $\sigma$ = 3.2293 Å) is also placed at center of mass. Two other LJ sites ($\epsilon/k_B$ = 4.0659 K, $\sigma$ = 2.3406 Å, and $m$ = 0) are also placed 0.329 Å from the center of mass (on the same axis with the sites carrying the masses). The validation of this force field was based on second virial coefficient data for temperatures ranging from 50 to 500 K. The pressure density curves were validated for pressures between 0 and 20 MPa and 0 to 200 MPa, at 298.15 K and 77 K, respectively. For a comparative summary of the selected $H_2$ force fields discussed above, including parameter values, number of interaction sites, and fitting approaches, see Table 6.

As for bulk systems, choosing suitable force fields is a crucial step towards obtaining accurate results in classical molecular simulations of $H_2$ hydrates. A force field often used in hydrate studies is Silvera−Goldman[335] (SG). This model has both LJ and electrostatic interactions but uses a rather complex functional form which is not easy to implement in molecular simulation software. An attempt to resolve this drawback is through the approach proposed by Alavi et al.[336] where SG is replaced by a three-site LJ-based force field developed to reproduce the experimental quadrupole moment of $H_2$. In this model, the two H atoms bear negative point charges, while the positive charge is placed on a "dummy" atom located at the center of mass of the molecule (see Fig. 13c). This force field is the most popular in the field of hydrates, having been used in more than 60% of the MC and MD studies in literature. In the studies of Levesque et al.[337] and Gu et al.[338], $H_2$ was modeled using an one-site LJ model which takes into account the

quantum nature of $H_2$ via the Feynman−Hibbs (FH) correction[339]

$$U_{FH} = U_{LJ} + \frac{\beta\hbar}{24\mu}\left(\frac{d^2 U_{LJ}}{dr^2} + \frac{2}{r}\frac{dU_{LJ}}{dr}\right) + \cdots \tag{7}$$

where $\beta = 1/(k_B T)$ (where $k_B$ is the Boltzmann constant and $T$ is temperature), $\mu = m/2$ (where $m$ is the molecular mass of $H_2$), and $\hbar = h/(2\pi)$ (where $h$ is the Planck constant). For computational efficiency in molecular simulations of hydrates, instead of using Eq. (7), the corrected potential is replaced by an equivalent LJ potential with temperature-dependent $\sigma$ and $\epsilon$ parameters. This dependence is described using third degree polynomials. The use of higher order (e.g., quartic) terms in Eq. (7) has also been reported in literature.[340] However, such terms have been mostly ignored in hydrate studies. Figure 14 shows a comparison of different $H_2$ force fields used in studies of hydrate.
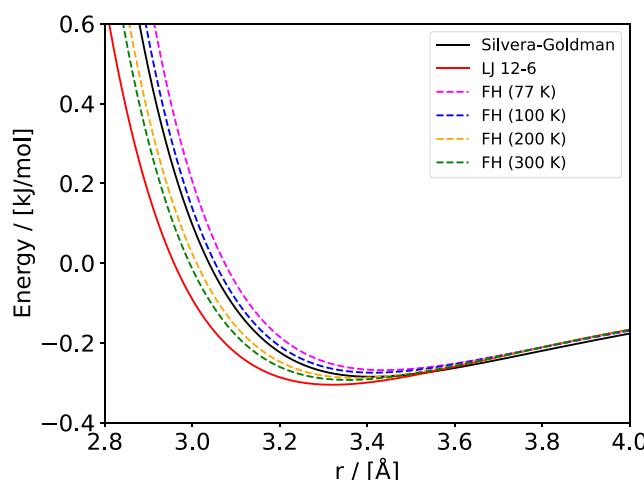


**Figure 14.** Comparison of different hydrogen potentials: Lennard-Jones (Eq. (3)), Feynman−Hibbs quantum effective potential (Eq. (7)) at different temperatures, and Silvera−Goldman force field. The data are taken from ref 341 (where more temperatures for the FH can be found).

Michalis et al.[342] in an effort to increase the accuracy of three-phase equilibrium calculations for the system $H_2/H_2O$ used a modification factor, $\chi$, to correct the Lorentz-Berthelot cross interaction energy parameter according to

$$\epsilon_{H(H_2)-O(H_2O)} = \chi\sqrt{\epsilon_{H(H_2)}\epsilon_{O(H_2O)}} \tag{8}$$

where $\epsilon_{H(H_2)}(H_2)$ and $\epsilon_{O(H_2O)}(H_2)$ are the LJ energy parameters of the H atom in $H_2$ and the oxygen atom in $H_2O$, respectively. The value of $\chi$ was obtained by minimizing the error in the calculation of aqueous $H_2$ solubility. Finally, a less used force field in hydrate studies is the one by Alavi et al.[343]. This model uses the anisotropic $H_2/D_2$ potential introduced by Wang[344], which was parametrized to account for quantum mechanical effects of $H_2$ motion at low temperatures (of order $\hbar^2$ in the second virial coefficient).

**3.1.2. Water.** Force fields for water are relevant for molecular modeling of processes such as hydrate formation, $H_2$ production (e.g., in alkaline electrolyzers), and $H_2$ storage (e.g., underground storage, where $H_2$ is in contact with aqueous NaCl solutions). Non-polarizable force fields with fixed point-charges are commonly used in molecular simulations of
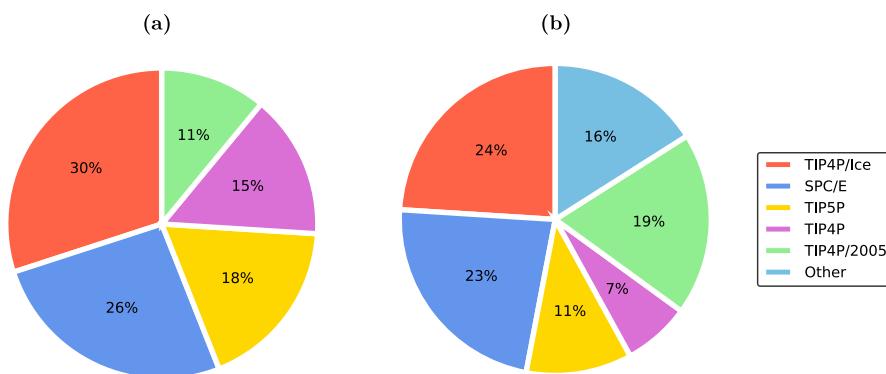
**Figure 15.** Overview of the relative popularity of the $H_2O$ force fields used in the $H_2$-hydrate literature of (a) MC and (b) MD studies. In panel (b), "Other" includes TIP3P (4%), TIP4P-FQ/Ice (2%), q-TIP4P/F (2%), SPC (2%), and other force fields. The statistics are based on the studies considered in this review.

aqueous electrolytes.[345−348] Non-polarizable force fields of water such as SPC/E[346] and TIP4P/2005[349] accurately capture thermophysical properties such as densities, radial distribution functions (RDFs), viscosities, and self-diffusivities of water. TIP4P/2005 which outperforms other fixed charged force fields in predicting densities and transport properties,[348] overestimates the vaporization enthalpy and underestimates the excess chemical potential of water.[110,345,350] At 323.15 K, the chemical potentials for the TIP4P/2005 water model deviate from the IAPWS empirical EoS[351,352] by ca. −500 K/$k_B$. The underestimation of the excess chemical potential of liquid water leads to severe underestimations of the saturated vapor pressure of water compared to experiments, and the solubilities of water in $H_2$ compared to experiments.[350] The TIP3P, TIP4P, TIP4P/$\mu$ (see the Supporting Information of ref 47 and Section 4.1.2.1), and the SPC water force fields significantly outperform the TIP4P/2005 force field for computing chemical potentials of liquid water.[110,345] A comparison of the predicting ability of the chemical potential in the liquid phase at $T$ = 323 K and pressures ranging between $P$ = 10 and $P$ = 1000 bar of different water force fields is provided in ref 110. The rigid, five-site TIP5P/Ew[353] water model has also been used in the literature to study high-pressure $H_2$ drying using zeolites.[143] Polarizable water force fields such as HBP,[354] BK3,[355] and AMOEBA[356] are on average ca. 3-5 times more computationally expensive compared to non-polarizable force fields (the newly developed polarizable force field of Xiong et al.[357] is an exception). Despite their improved accuracy for various properties of water, polarizable force fields have not gained the widespread popularity of non-polarizable force fields due to their increased computational cost and limited availability in open-source simulation software. For a relevant discussion, the reader is referred to study by Jiang et al.[354]

Already in 1987, Berendsen et al.[346] discussed that fitting non-polarizable force fields to the free energies of water (i.e., vaporization energies or excess chemical potentials) results in excluding the self-polarization energy of water. The inclusion of self-polarization energy results in accurate predictions for the transport properties of liquid water but at the cost of lower accuracy for the free energies of water. As such, not all thermodynamic and transport properties of aqueous systems can be described simultaneously using a single non-polarizable force field. Different water force fields can be chosen depending on the system or properties of interest. Force fields such as TIP4P/$\mu$, which are trained on free energies and

chemical potentials are more suitable than TIP4P/2005 for phase coexistence calculations, as accurate predictions for the chemical potentials of water is crucial for improving the prediction of vapor-liquid phase-coexistence compositions of $H_2O − H_2$ systems.[47] For computing transport properties of $H_2$ in liquid water, force fields such as TIP4P/2005 and SPC/E which are trained on liquid phase transport properties are more suitable, as accurate predictions for the viscosity of water ensures that drag forces that influence the transport of $H_2$ in water are accurately modeled.

Fig. 15 shows an overview of the relative popularity of the $H_2O$ force fields used in MC and MD studies of $H_2$-hydrate studies. As can be seen, the order of popularity in MC studies (Fig. 15(a)) is TIP4P/Ice,[358] SPC/E,[346] TIP5P,[359] TIP4P/2005,[349] and TIP4P,[360] while the respective order for MD studies (Fig. 15(b)) is TIP4P/Ice, SPC/E, TIP4P/2005, TIP5P, and TIP4P. In MD studies, various other force fields have also been used to a lesser extent, e.g., TIP3P,[300] SPC,[361] q-TIP4P/F,[362] TIP4P-FQ/Ice[363] While the vast majority of $H_2$-hydrate studies is performed with non-polarizable $H_2O$ force fields (which also ignore quantum effects), there are a few exceptions. Rick and Freeman[364] used the polarizable TIP4P-FQ/Ice $H_2O$,[363] which yields accurate predictions of the density and melting point of ice $I_h$. TIP4P-FQ/Ice is a reparameterization of the TIP4P-FQ model.[365] Cendagorta et al.[366] performed simulations for the quantum free energy profiles and rates of diffusion of $H_2$ and $D_2$ via the hexagonal face of two neighboring $5^{12}6^4$ hydrate cages considering the temperature range 8 K up to 200 K with q-TIP4P/F[362] $H_2O$, which is a modified version of TIP4P/2005. q-TIP4P/F is flexible and implicitly accounts for quantum effects.

During recent years, an increase in the use of TIP4P/Ice[358] $H_2O$ force field in MD studies of hydrates is observed. TIP4P/Ice is a rigid and non-polarizable model which was designed to accurately reproduce the melting temperature of hexagonal ice ($I_h$). García Fernández et al.[367] reported a melting temperature of $T_m$ = 270 ± 3 K. In a more recent study, Conde et al.[368] performed a systematic study to increase the accuracy of the direct phase coexistence approach (see Section 3.2.14), and recommended a value of $T_m$ = 269.8 ± 0.1 K for $I_h$. These calculations, therefore, show a clear under-prediction of the melting point of TIP4P/Ice by 3.35 K. Conde and Vega[369] argued that the accurate calculation of the melting temperature of hexagonal ice is essential for the accurate calculation of the three-phase coexistence temperature of hydrate systems using the phase coexistence approach.

**3.1.3. Ionic Species.** The presence of ions, such as $Na^+$, $K^+$, $Cl^-$, and $OH^-$, influences the thermophysical properties of water, which in turn affects the solubility, diffusivity, and phase behavior of $H_2$ in the system. Similarly to water, force fields for ions can be either non-polarizable or polarizable. Non-polarizable force fields of ions, such as Madrid-2019[370] and Joung-Cheatam,[371] assume fixed charges on the ions. Polarizable force fields for ions, such as the ones developed by Kiss and Baranyai[372] and Dočkal et al.[373], use more elaborate functional forms e.g., Gaussian charge distributions and the charge-on-spring model. In the "charge-on-spring" model a massless charge is attached to each ion by a harmonic spring. This allows the charge to move in response to the local electric field. As in the respective water force fields, the additional calculations required to determine the positions and forces on these charge-on-spring elements increase the complexity and the time requirements of the simulation (typically by a factor of 3-10).[372] Recent advances in polarizable force fields aimed at overcoming these limitations, striving to balance accuracy and efficiency.[357,373]

Until 2009, force fields of ions were primarily parameterized based on free hydration energies of salts and RDFs of ions and water (e.g., the location of the first peak and the number of water molecules in the first hydration layer).[371,374−377] A list of available ion force fields (until 2011) and the target properties, which are used for their validation is provided by Reif and Hünenberger[378]. The non-polarizable force field developed by Joung and Cheatham[371] for alkali (e.g., $Li^+$, $Na^+$, and $K^+$) and halide (e.g., $F^-$, $Cl^-$, and $Br^-$) ions is particularly popular in literature. The Joung-Cheatham[371] force field uses nominal charges (i.e., +1 [e] for $Na^+$ and −1 [e] for $Cl^-$) to model the electrostatic interactions of ions in the solution and can accurately predict the free hydration energies of ions in the aqueous solution along with the lattice energies (and constants) of the alkali halide salts in crystal form. Despite the success of the Joung-Cheatham force field for describing the free energies of ions, the dynamic properties (e.g., viscosities and self-diffusivities of ions and water) in concentrated salt solutions (i.e., beyond a molality of 1 mol salt / kg salt) cannot be accurately modeled with respect to experiments.

Since 2009, Leontyev and Stuchebrukhovhav have published several works using the concept of "scaled charges" for modeling ions in aqueous solutions.[379−382] Scaling down the charges of ions by a factor of 0.7-0.9 allows for accounting the dielectric screening of electrostatic charges in the aqueous medium.[370,381,383] Use of scaled charges has been shown to significantly improve the accuracy of predicting dynamical properties such viscosities, diffusion coefficients of water, and electrical conductivities for aqueous electrolyte solutions[112,113,370,384,385] at the cost of less accurate predictions for free hydration energies of salts. Several different force fields have been recently developed for modeling ions using scaled charges.[370,384] Madrid-2019, developed by Zeron et al.[370] in 2019, was parameterized based on the TIP4P/2005[349] water force field, and is particularly popular in literature of aqueous electrolytes due to its computational efficiency and accurate predictions of densities, RDFs, infinite dilution self-diffusivities of ions, and freezing point depression in aqueous electrolyte solutions. Madrid-2019 uses a charge scaling factor of 0.85 and has parameters for a wide array of ions such as $Li^+$, $Na^+$, $K^+$, $Cl^-$, and $SO_4^{2-}$), which are particularly important for $H_2$ applications. Despite its widespread use, Madrid-2019 force

field cannot accurately predict all properties (e.g., free hydration energies of salts and the transport properties of concentrated aqueous solutions). Recently, the Madrid-Transport[384] (with a charge scaling factor of 0.75) has been developed for aqueous NaCl and KCl solutions, which outperform the Madrid-2019[347] in predicting the transport properties (i.e., viscosities, self-diffusivities of ions, and electrical conductivities). However, this force field yields less accurate results for interfacial tensions and activities of water in aqueous electrolyte solutions.

Despite being scarce, molecular simulation data for properties of systems involving $H_2$ and more complex ionic species, such as ionic liquids (ILs), have been reported. In these studies, common force fields for ILs are the ones developed by Maginn and co-workers,[386−388] the General Amber force field (GAFF),[307] the Optimized Potentials for Liquid Simulations-All Atom (OPLS-AA) for ILs by Sambasivarao and Acevedo[389], and the model by Koller et al.[390]. Usually, the atomic point charges of the atoms of ILs are derived from quantum mechanical calculations using e.g., the Restrained Electrostatic Potential (RESP) method.[391] Similarly to the monovalent ions discussed earlier, a common practice in simulations of ionic systems such as ILs and DES is to scale the charges obtained from RESP (or other QM-based methods) to reduce the charge screening, and hence, improve force field accuracy. For more details on this approach, the reader is referred to refs 389 and 392−396 and the discussion in Section 4.1.2.

A wide variety of force fields for other ions, important for modeling $H_2$ processes, such as the Delft-Force field (for $OH^-$, $B(OH)_4^-$, and $BH_4^-$ ions),[113,397] have been developed recently. For a detailed overview of common ion models the reader is referred to the review by Nezbeda et al.[398] and refs 302, 370, and 385.

**3.1.4. Nanoporous Materials, Membranes, and Solid Substrates.** In the studies of $H_2$ separations or storage in nanoporous materials (e.g., MOFs, COFs, zeolites, CNTs), general force fields are mainly used. Among them, the Universal force field (UFF), developed in 1992 by Rappe et al.,[399] is designed to be applicable across the entire periodic table. UFF parameters are based on general rules that consider an element's hybridization and connectivity. Similarly, DREIDING by Mayo et al.[400] is a widely used generic force field aimed at predicting the structures and dynamics of organic, biological, and main-group inorganic molecules, making it a reasonable choice for polymer simulations. To better account for the wide structural space of specific functional materials families, more sophisticated approaches have been developed; QuickFF[401] is a force field para-metrization protocol for MOFs and other nanoporous materials that produces force field parameters from first-principles calculations. UFF4MOF[402] is an extension of UFF aiming at improved accuracy for MOFs. IntraZIF-FF[403] and ZIF-FF[404] are specialized force fields for ZIFs, capturing their flexibility and dynamic behavior.

For representing both crystalline and amorphous polymeric materials (e.g., in studies of barrier materials in $H_2$ tanks, and as membranes for separations and in electrochemical processes), the most common force fields are the condensed-phase optimized molecular potentials for atomistic simulation studios (COMPASS),[315,316,405] the polymer consistent force field (PCFF),[406] and OPLS.[360] These popular polymer force fields are combined with different $H_2$ models, such as the ones

discussed in detail in Section 3.1.1. It is also common that specially developed energy interaction parameters for the $H_2$[325,407] are used to study properties of $H_2$/polymer systems. It is noteworthy that despite being one of the most successful force fields for these systems, COMPASS is a proprietary model, part of the Direct Force Field software suite.[408] Other force fields used to model polymeric systems include the modified Adaptive Intermolecular Reactive Empirical Bond Order potential (AIREBO-M),[409] modified versions of the DREIDING force field (e.g., Mabuchi and Tokumasu[410]), and the model by Smith et al.[411]. Scarcely, the anisotropic united atom force field (AUA4)[412] is used to model polymeric materials.[413] It is important to note that many of these models, have also been used for zeolites and other nanoporous materials.

When computing the adsorption and storage capacities of $H_2$ in functionalized nanoporous materials, intramolecular interactions are often neglected.[198,317,414] Although MOFs are assumed to be rigid in most $H_2$ adsorption studies, it is important to note that the presence of gases, such as $CO_2$, in MOFs can induce swelling and phase transitions, which can result in changes to pore-sizes and adsorption properties.[415] To study these phenomena, flexible force fields are required. A review of flexible force fields for MOFs is provided by Heinen and Dubbeldam.[415] There is no general consensus as to which $H_2$ force field is most suitable for adsorption in MOFs.[414] For strong $H_2$ adsorption energies (especially for open metal and $H_2$ interactions), the Morse potential can be used to model the interatomic interactions between $H_2$ and the MOFs. The Morse potential has been shown to perform better than LJ in modeling stronger interatomic interactions.[317] Many studies in the literature underline the importance of quantum-corrections to classical potentials of $H_2$, with the most popular being the quasi-classical Feynmen-Hibbs correction[317] (see also Eq. (7) and Fig. 14). Without quantum corrections, the low temperature (below 70 K) adsorption capacity of $H_2$ can be over-predicted by ca. 20% as shown by Bobbitt and Snurr.[414] Although most $H_2$ force fields neglect the polarization of $H_2$ (primarily due to its small size), polarization can play an important role in $H_2$ adsorption especially when dealing with open metal adsorption sites. Polarization of $H_2$ significantly enhances the binding between $H_2$ and the adsorbent.[414] Thus, neglecting polarization by using non-polarizable $H_2$ force fields,[312] can result in inaccurate predictions of binding sites and capacities as shown by Franz et al.[416] In such cases, it is necessary to use polarizable force fields of $H_2$ or ab-initio simulations.[414,416] Getman et al.[317] and Bobbitt and Snurr[414] discuss in detail molecular simulations of $H_2$ adsorption on MOFs, and the use of appropriate force fields. In practice, researchers often need to make a compromise when choosing force fields, since the most accurate representation of adsorbate−organic group and adsorbate−metal interactions may not be equally well captured within a given model. While many studies adopt transferable force fields, others have introduced custom parameterizations in an effort to better capture the structural behavior of the frameworks of the porous media, particularly when new metals are present (see for example refs 417 and 418). Such refinements do not guarantee a universally improved adsorbate−framework description, but can enhance e.g., the accuracy of framework flexibility.

For guest gas molecules other than $H_2$ (e.g., $CO_2$, hydrocarbons), widely used force fields include the Transferable Potentials for Phase Equilibria (TraPPE), designed by Martin and Siepmann[301] to model phase equilibria of gases and hydrocarbons, emphasizing transferability and vapor-liquid coexistence properties, the Elementary Physical Model 2 (EPM2) by Harris and Yung[419] developed to accurately describe the phase behavior and thermodynamic properties of $CO_2$, making it suitable for gas adsorption studies, and OPLS.[360,420,421] In general, OPLS and GAFF[307] force fields are the most widely used force field for modeling hydrocarbons and guest molecules in porous materials.

MD studies related to $H_2$ storage in subsurface geological formations typically use classical force fields tailored to represent the structural and interaction properties of solids. Among these, CLAYFF (and its variations)[422−424] is the most prevalent, designed explicitly for layered minerals such as montmorillonite, kaolinite, pyrophyllite, beidellite, quartz, hematite, and calcium silicate hydrates. CLAYFF predominantly treats interactions through non-bonded potentials, capturing the essential physics of clays and related nanoporous materials with particular emphasis on hydration and surface interactions. UFF[399] is also frequently chosen to model inorganic solids such as kaolinite, illite, dolomite, quartz, and calcite, thanks to its wide applicability across the periodic table, and parametrization approach based on atomic hybridization and connectivity. The INTERFACE force field[425] extends popular biomolecular and organic force fields to accurately simulate inorganic oxide interfaces, as exemplified by its application to kaolinite. Other specialized force fields used in molecular simulations of $H_2$/substrate systems are the CVFF[426] and PCFF++[427] for modeling kerogen, OPLS[428] for graphene, and specialized models for silica-based meso-porous materials e.g., MCM-41.[429] Furthermore, force fields such as PCFF+[316,406,430] for $SiO_2$, and those specifically optimized for calcite (e.g., by Xiao et al.[431] and Raiteri et al.[432]), highlight the importance of targeted development of force fields to accurately capture specific structural, mechanical, or thermodynamic properties relevant to UHS.

**3.1.5. Metal-Hydrogen Systems.** Several classes of interatomic potentials have been developed to model metal−H interactions, including classical many−body methods such as the Embedded−Atom Method (EAM), its modified form (MEAM), Angular−Dependent Potentials (ADP), and Bond−Order Potentials (BOP), as well as modern machine−learning interatomic potentials (MLIPs). These methods represent a hierarchy of increasing complexity and accuracy in describing metal−H systems.

The EAM potential is a many−body framework that models metals by combining pairwise interactions with an embedding function representing the host electron density. Developed by Daw and Baskes,[433] EAM was groundbreaking in capturing metallic cohesion more accurately than simple pair potentials. Notably, the original work already addressed H in metals, employing EAM to study H interstitials, surface adsorption, and even the effect of H on Ni and Pd fracture.[434] This demonstrated the unique capability of EAM to model HE problems that pair potentials could not resolve. EAM potentials have been extensively parameterized for various metal−H systems, enabling detailed simulations of H trapping at defects and its weakening effect on metal bonds. Currently available EAM potentials for metal−H systems include Pd−Ag−H,[435] Al−Ni−H,[436] Fe−H,[437−439] Pd−H−He,[440] W−H−He,[441] Ni−H,[442] Pd−H,[440] W−H,[443] and Fe−Cr−Ni−H.[444] The MEAM potential extends the EAM framework by incorporating directional bonding effects, addressing a key

limitation of traditional EAM potentials. Developed by Baskes[445], MEAM was the first semi−empirical scheme able to treat fcc, bcc, hcp and diamond structures within one formalism, thereby capturing both metallic and covalent bonding. It has since been extended to second−nearest−neighbour (2NN−MEAM)[446] and multi-component versions and is now widely used for metal−H systems. Compared to EAM, the inclusion of angular terms in MEAM, provides enhanced accuracy in modeling HE phenomena across diverse metals, though at the cost of increased computational and parametric complexity. To date, MEAM potentials have been developed for various metal−H systems, including Al−H,[447] Al−V−H,[448] Fe−H,[449] Ni−H,[447] Ni−V−H,[448] V−H,[450] and Zr−H.[451]

ADPs offer a streamlined way to include directional bonding effects in metals, extending the EAM as a more tractable successor to MEAM. Introduced by Mishin et al.,[452] ADPs supplement the usual EAM energy with explicit dipole and quadrupole terms that penalize deviations from high-symmetry environments, capturing bond-angle dependence via analytic functions rather than the many−body screening routines of MEAM. These additional angular contributions span multiple coordination shells and employ smooth cutoffs for efficiency. Although initially parameterized for transition metals like bcc Fe and fcc Ni,[452] the same formalism has since been adapted successfully to a variety of alloys and metal−H systems. Currently available ADP parameterizations include Al−H,[453] Cr−Fe−H,[454] and Mg−H[455] systems.

BOPs derive from quantum mechanical principles, where bond strength depends explicitly on the local coordination environment. Unlike simpler approaches, BOPs incorporate multi−atom interactions (three− and four−body terms) that dynamically adjust bond energies based on atomic geometry.[456] This formulation provides superior description of directional bonding and bond-breaking/forming processes compared to ADP or MEAM, though at the expense of greater mathematical complexity. Developed initially for alloys and semiconductors,[457] BOP frameworks have been successfully extended to metal-H systems. Currently available BOP parameterizations for metal-H systems include Al-Cu-H[458] and Cu-H.[459]

MLIPs have emerged in the past decade as a transformative approach, leveraging data-driven models to achieve accuracy approaching that of DFT. The field was pioneered by Behler and Parrinello's neural network potential,[460] which demonstrated that high-dimensional neural networks could accurately reproduce DFT potential energy surfaces. Subsequent advances, including Gaussian approximation potential (GAP)[461] and moment tensor potential (MTP),[462] have broadened this methodology, enabling the modeling of complex multi-component systems through flexible functional forms. Unlike traditional empirical potentials, MLIPs are not constrained by predefined functional forms tied to specific theoretical frameworks (e.g., electron density or bond order). This allows MLIPs to achieve accuracies comparable to quantum-mechanics across diverse atomic environments. However, this comes at the cost of requiring extensive training data and reduced physical interpretability compared to conventional potentials.[463] For metal−H systems, MLIPs represent a significant breakthrough as they can simultaneously describe metallic, covalent, and even molecular interactions relevant to HE. Importantly, MLIPs serve as a unifying framework that can, in principle, replicate the behavior of EAM, MEAM, BOP, and other conventional potentials when trained on sufficient data, thereby bridging gaps between these established methodologies. With advancing computational power and algorithms, MLIPs are becoming indispensable tools for investigating HE across various metal systems with unprecedented detail. Successful applications include Pd-H,[464] Nb-H,[465] W-H,[465] Ti-H,[466] Fe-H,[467] and multi-component systems like Mo-Nb-Ta-W-H,[468] and Fe-Co-Ni-Cr-Mn-H.[469]

The landscape of interatomic potentials for metal-H systems reveals two fundamentally distinct modeling philosophies. Traditional approaches (EAM, MEAM, ADP, and BOP) employ compact functional forms grounded in physical principles, with parameters carefully optimized against experiments or DFT reference data. These models incorporate essential physics through distinct mechanisms: electron-density embedding in EAM, angular corrections in MEAM and ADP, and bond-order dependence in BOP. These fundamental physical principles serve as a safeguard, ensuring that even beyond their fitted regimes, the potentials typically maintain reasonable metallic or covalent behavior. In contrast, MLIPs forgo explicit physical constraints in favor of complex, high-dimensional functions with thousands of parameters trained on extensive DFT datasets.[463] While this flexibility enables remarkable accuracy across diverse structural and chemical environments when training data is comprehensive, it carries an inherent risk: configurations outside the training domain may produce unphysical predictions that empirical potentials would naturally avoid. Recent efforts to develop hybrid approaches, such as physics-informed neural network potentials, aim to bridge this divide by embedding physical constraints within ML architectures.[470] However, these methods currently remain limited in scope (e.g., to pure Al[471] and Ta[472] systems), and have not yet been successfully extended to metal-H applications.

When selecting interatomic potentials for HE studies, users must carefully balance two critical factors: (1) the accuracy for target phenomena, and (2) computational efficiency. For physics-based potentials (EAM, MEAM, ADP, BOP), accuracy depends on proper parameterization for specific applications, as demonstrated by Song and Curtin,[276] who refined Fe-H and Ni-H EAM potentials to better capture H-defect interactions, highlighting how even established models may require reparameterization for certain HE mechanisms. For MLIPs, accuracy is intrinsically linked to training data coverage; for instance, an MLIP trained only on bulk H diffusion[465] cannot reliably predict H-defect interactions[469] absent from its training set. Computational cost varies significantly across methods as shown in Table 7: relative to EAM, ADP and MEAM increase costs by ca. 3× and 7×, respectively, while BOP reaches ca. 13×.[473] Modern MLIPs (e.g., ACE, MTP16) further escalate costs to 20−66×,[474] though they offer near-DFT accuracy. Thus, the choice hinges on the priorities of the study: empirical potentials provide transferable, computationally efficient frameworks with inherent physical safeguards, whereas MLIPs deliver higher fidelity at greater computational expense, provided their training data adequately represents the relevant atomic configurations for HE.

## 3.2. Computation of Hydrogen Properties from Molecular Dynamics Simulations

The past two decades, MD simulations have been proven to be an invaluable tool for studying properties of $H_2$ systems. In brief, MD performs numerical integration of Newton's

**Table 7. Comparison of Computational Costs for Different Interatomic Potentials, Normalized Relative to EAM[a]**

| Force field | CPU cost relative to EAM (times) |
|---|---|
| EAM | 1 |
| ADP | 3 |
| MEAM | 7 |
| BOP | 13 |
| ACE | 20 |
| MTP16 | 66 |

[a]Performance data for EAM, ADP, MEAM, and BOP potentials are obtained from LAMMPS benchmark tests,[473] while results for ACE and MTP16 (where 16 denotes the MTP level) are sourced from Shuang et al.[474]

equations of motion to yield the positions of particles over time. Unlike MC simulations, which are limited to computing thermodynamic ensemble averages, MD simulations provide insight into both equilibrium and transport properties of a system. The interactions between atoms are determined based on the chosen force field (discussed in detail in Section 3.1). Typically, an MD simulation starts by initializing the positions and velocities of all particles in the simulation box, followed by an equilibration period to bring the system at thermodynamic equilibrium. Then, a production run, usually in the order of ns, is performed to sample the relevant properties. For all details regarding MD simulations the reader is referred to the relevant textbooks.[51,52,297]

The most common open source MD simulation packages for modeling $H_2$ systems are the Large-scale Atomic/Molecular Massively Parallel Simulator (LAMMPS)[475] and Groningen Machine for Chemical Simulations (GROMACS).[476,477] The modular structure of these simulation tools (and especially of LAMMPS), allows for extensions to the main code (e.g., via the creation of plugins) to accommodate new or advanced computations which are not part of the package (for example the information in ref 478). Nevertheless, other open-source MD software such as DLPOLY[479] and RASPA[480] is also used for modeling $H_2$ systems. Aside from the simulation packages, visualization software, such as VMD,[481] AVOGADRO,[482] iRaspa,[483] and OVITO,[484] is an indispensable tool for not only visualizing simulations but also computing properties and creating initial configurations. These tools are used to visualize both MD and MC simulations.

**3.2.1. Transport Properties: A Brief Introduction.** Both equilibrium (EMD)[51,52] and non-equilibrium molecular dynamics (NEMD)[52,485] simulations are naturally suited, and thus, widely used for computing transport coefficients. In NEMD, transport coefficients are calculated using[485]

$$\gamma = \lim_{X \to 0} \lim_{t \to \infty} \frac{J}{X} \tag{9}$$

where $\gamma$ is the transport coefficient (e.g., self-diffusion coefficient), $X$ is (usually) a fictitious field that drives a conjugate flux, $J$ (i.e., mass flux in case of self-diffusivity or momentum flux for the case of dynamic viscosity), and $t$ is the simulation time.[485] In EMD, transport coefficients can be computed either by using the Green Kubo (GK) or the Einstein relations.[51,485,486] Following the GK approach, transport coefficients are computed from integrals of time-correlation functions of dynamical variables, according to[52,299,487]

$$\gamma = \int_0^\infty \langle \dot{A}(t') \, \dot{A}(0) \rangle \mathrm{d}t' \tag{10}$$

where $\dot{A}$ is the corresponding dynamic variable and the angle brackets $\langle \cdots \rangle$ denote an ensemble average. The Einstein method follows[52]

$$\gamma = \langle (A(t) - A(0))^2 \rangle / 2t \tag{11}$$

which is a linear relation between time ($t$) and the mean-squared displacement (MSD) of the dynamical variable. Eq. (11) is valid at time-scales where the slope of MSD($t$) equals 1 in the logarithmic scale.[51,52] Using this as a criterion, one can specify the minimum simulation duration for computing transport coefficients using the Einstein method. Such a criterion is not present in the GK approach, where the tail of the time-correlation functions converges to zero regardless of how long the simulation is.[488,489] Thus, from a purely practical standpoint, the Einstein method is advantageous for computing transport properties. Nevertheless, both GK and Einstein methods should yield identical results.[490]

An advantage of using EMD over NEMD simulations is that a single simulation can be used to sample multiple different transport properties.[485,486] NEMD simulations often require multiple simulations at different field strengths (to extrapolate to 0 field) for each transport property.[94] An advantage of NEMD simulations is that, unlike EMD simulations, it can be used to simulate non-linear response behaviors such as the rheology of non-Newtonian fluids.[485] While EMD is well suited for studying spontaneous fluctuations in equilibrium, NEMD is particularly effective for investigating transport processes driven by external forces, such as electro-osmotic drag in polymer membranes. Since most of the systems reviewed in this work deal with aqueous Newtonian systems (such as alkaline electrolyte solutions), primarily EMD simulations are discussed in this work.

To compute transport properties using EMD in LAMMPS,[475] the OCTP plugin[491] or the PyLAT[492] post-processing tools can be used. In the OCTP plugin, Einstein relations are used in combination with the order-$n$ algorithm[51] as implemented by Dubbeldam et al.[493] PyLAT[492] uses a combination of GK (for dynamic viscosity and ionic conductivity), and Einstein relation (for self-diffusivity) expressions.

**3.2.2. Viscosity.** Computing viscosity, $\eta$, via EMD is generally preferred over NEMD because it uses spontaneous fluctuations in pressure of an unperturbed system avoiding introducing external fields or shear flows, which can potentially induce non-linear effects.[51,52,490] As mentioned earlier for all transport properties, $\eta$ in EMD can be computed by using either the GK approach or the Einstein relation.[490] The Einstein expression for $\eta$ is as follows

$$\eta = \lim_{t \to \infty} \frac{\mathrm{d}}{\mathrm{d}t} \left[ \frac{1}{20} \frac{V}{k_B T} \left\langle \sum_{\alpha\beta} \left( \int_0^t \mathrm{d}t' p_{\alpha\beta}^{\mathrm{Tr}}(t') \right)^2 \right\rangle \right] \tag{12}$$

where $t$ is time, $V$ is the volume of the simulation box, $k_B$ is the Boltzmann constant, $T$ is the temperature, and $\langle \cdots \rangle$ indicates an ensemble average. $p_{\alpha\beta}^{\mathrm{Tr}}$ are the components of the traceless pressure tensor calculated using

$$p_{\alpha\beta}^{\mathrm{Tr}} = \frac{p_{\alpha\beta} + p_{\beta\alpha}}{2} - \delta_{\alpha\beta} \left( \frac{1}{3} \sum_k p_{kk} \right) \tag{13}$$

where $\delta_{\alpha\beta}$ is the Kronecker delta. Eq. (12), allows viscosities to be computed directly from the slope of the MSD (term in the bracket) at long times.[490] This approach yields results identical with those obtained from the GK method, but avoids the complexity of fitting correlation functions, as discussed by Maginn et al.[490]

**3.2.3. Self-Diffusivity.** Self-diffusivity is the mass transport mechanism of a species driven by Brownian motion, occurring in the absence of chemical potential, temperature, or pressure gradients.[494] This review mainly deals with self-diffusivities in binary and multi-component gas/liquid mixtures containing $H_2$. In a multi-component mixture, the self-diffusivity can be calculated as follows

$$D_i^{\text{self,MD}} = \lim_{t\to\infty} \frac{d}{dt}\left[\frac{1}{2dN_i}\left\langle \sum_{j=1}^{N_i} (\mathbf{r}_{j,i}(t) - \mathbf{r}_{j,i}(0))^2 \right\rangle\right] \quad (14)$$

where $\mathbf{r}_{j,i}(t)$ is the position of the $j^{\text{th}}$ molecule of species $i$ at time $t$, $\langle \cdots \rangle$ denotes an ensemble average, and $d$ is the dimensionality of the system. Better statistical accuracy in the computation of $D_i^{\text{self,MD}}$ is achieved by considering the MSDs of all $N_i$ molecules in Eq. 14. At early times ($t \to 0$), a molecule exhibits ballistic motion with MSD scaling as $t^2$, while at long times ($t \to \infty$), the MSD scales linearly with $t$, indicating diffusive behavior, during which self-diffusivities are computed. It is important to note that although the slope of unity in the log-log plot of MSD as a function of time is a necessary condition for computing self-diffusivities (and other transport coefficients), it is not always sufficient. According to Maginn et al.[490], the square root of the MSD should be comparable or larger than the simulation box size length. This is a common practice ensuring that the diffusing molecule has explored a substantial part of the configurational space. A similar rule of thumb has been recently proposed by Kärger et al.[495] for diffusivity in nanoporous materials, where the square root of the MSD should be at least equal to one unit cell. This criterion ensures that the molecule is diffusing and not simply vibrating around its position.

Self-diffusivities computed in MD simulations suffer from finite-size effects which arise from spurious hydrodynamic interactions between the particles in the simulation box with their periodic images. These effects can be substantial, depending on the system size and type, and particularly prominent in dense systems, i.e., liquids or compressed gasses.[496] To mitigate finite-size effects, one should either perform MD simulations with large system sizes or use analytical corrections.[497−500] The most widely used correction term, the so-called Yeh-Hummer correction ($D^{\text{YH}}$), was derived in the pioneering studies of Dünweg and Kremer[497] and Yeh and Hummer.[498] The self-diffusivity at the thermodynamic limit can be obtained via the following expression

$$D_i^{\text{self}} = D_i^{\text{self,MD}} + D^{\text{YH}}(T, \eta, L) = D_i^{\text{self,MD}} + \frac{k_B T \xi}{6\pi\eta L} \quad (15)$$

where $D_i^{\text{self}}$ is the finite-size corrected self diffusivity of the $i^{\text{th}}$ species, $\xi$ is a dimensionless constant equal to 2.837298, and $L$ is the box length of a cubic simulation box. $\eta$ is the shear viscosity computed from MD simulations, which is shown to be independent of the size of the system.[496,498,501−503]

**3.2.4. Maxwell-Stefan and Fick (Mutual) Diffusivities.** Mutual diffusivities describe the collective diffusion of species which is commonly modeled using the MS (Maxwell-Stefan) and Fick frameworks. This review mainly focuses on mass transport phenomena in binary and multi-component gas/liquid mixtures containing $H_2$. The MS framework expresses diffusion in terms of chemical potential gradients, where the flux is driven by differences in the chemical potential, $\mu_i$, of each species and characterized by the MS diffusivity, Đ, an inverse-friction coefficient.[266,321] On the other hand, the Fickian approach uses concentration gradients, with flux governed by the Fick diffusivity, $D^{\text{Fick}}$.[266,504] Despite the different gradients considered, MS and Fick frameworks describe the same physical process, and are mathematically connected by the so-called thermodynamic factor, $\Gamma$, for diffusion, according to[505−509]

$$D^{\text{Fick}} = \Gamma Đ^{\text{MS}} \quad (16)$$

As discussed in more detail in Section 3.2.13, $\Gamma$ accounts for deviations from ideal behavior, and depends on the mixture's composition, pressure, and temperature.[510] While MS diffusivities are linked to chemical potentials, which are difficult to measure experimentally,[511] Fick diffusivities are more commonly reported due to their dependence on measurable concentration gradients.[266] Direct calculation of $D^{\text{Fick}}$ using non-equilibrium molecular dynamics simulations is possible, but impractical as it requires setting up systems with large concentration gradients, yielding inaccurate predictions of $D^{\text{Fick}}$ as discussed in the studies by Liu et al.,[506] Maginn et al.,[512] Tsige and Grest.[513,514]

In an $N-$ component mixture, there are $N(N-1)/2$ unique MS diffusivities which can be represented as a symmetric matrix. By performing EMD, the MS diffusivity, Đ, in binary mixtures are computed by first obtaining the Onsager coefficients $\Lambda_{ik}$ at zero total linear momentum.[505−507] $\Lambda_{ik}$ is computed from the cross-correlations of the molecular displacements of species $i$ and $k$[505−507,515]

$$\Lambda_{ik} = \lim_{t\to\infty} \frac{d}{dt}\left[\frac{1}{6N_{\text{tot}}}\left\langle \left(\sum_{l=1}^{N_i} (\mathbf{r}_{l,i}(t) - \mathbf{r}_{l,i}(0))\right) \right.\right.$$
$$\left.\left. \times \left(\sum_{m=1}^{N_k} (\mathbf{r}_{m,k}(t) - \mathbf{r}_{m,k}(0))\right)\right\rangle\right] \quad (17)$$

where $N_i$, $N_k N_{\text{tot}}$ are the number of molecules of type $i$ and $k$, and the total number of molecules in the system, respectively. $Đ^{\text{MS,MD}}$ for a binary mixture is then expressed as a linear combination of the Onsager coefficients,[505−507,515]

$$Đ^{\text{MS,MD}} = \frac{x_2}{x_1}\Lambda_{11} + \frac{x_1}{x_2}\Lambda_{22} - 2\Lambda_{12} \quad (18)$$

where $x_1$ and $x_2$ are the mole fractions of the components in the binary mixture.

As in the computation of self-diffusivities with EMD, finite-size effects are present also in MS diffusivities.[499,503] In a binary mixture, MS diffusivities can be corrected for finite-size effects using the term derived by Jamali et al.:[503]

$$Đ^{\text{MS}} - Đ^{\text{MS,MD}} = \frac{1}{\Gamma}\frac{k_B T \xi}{6\pi\eta L} = \frac{1}{\Gamma}D^{\text{YH}} \quad (19)$$

Fick diffusivities, $D^{\text{Fick,MD}}$, can be computed using Eq. (16). As shown by Jamali et al.,[516] extrapolation of $D^{\text{Fick,MD}}$ to its value at the thermodynamic limit follows from:

$$D^{\text{Fick}} - D^{\text{Fick,MD}} = D^{\text{YH}} \tag{20}$$

Eq. (20) shows that the finite-size correction to Fick diffusivities equals the Yeh-Hummer correction term for self-diffusivities (Eq. (15)). Corrections for an $N$-component system, were derived by Jamali et al.[500] In an $N$ component mixture, unlike $Đ^{\text{MS}}$, there are $(N-1)^2$ distinct Fick diffusivities where label order matters, i.e $D_{ij}^{\text{Fick}} \neq D_{ij}^{\text{Fick}}$. For a binary mixture, however, $D_{12}^{\text{Fick}} = D_{21}^{\text{Fick}} = D^{\text{Fick}}$.

The discussion above focuses on mass fluxes in a molar reference frame, where velocities are mole-fraction-weighted. Mass fluxes can also be evaluated using mass- or volume-averaged velocities, yielding different Fick diffusivities.[266,517] The benefits of each reference frame are discussed in detailed in Taylor and Krishna[266] (Section 3.1), Bird et al.[517] (Section 17.7), and in refs 508, 510, 518. Notably, for binary mixtures, Fick diffusivities remain identical across reference frames.[266,517] The discussion provided here is not exhaustive, but is meant to showcase the main approach for computing mutual diffusivities of $H_2$ mixtures using EMD. For detailed discussions on the MS and Fick frameworks in multi-component mixtures, the reader is referred to refs 266, 267, 500, and 519−526.

### 3.2.5. Diffusivity in Nanoporous Materials.
Diffusion inside nanoporous solids is studied extensively using experimental techniques such as frequency response methods, pulsed-field gradient NMR, and quasi-elastic neutron scattering.[527] These approaches define different, but closely related to each other types of diffusivities. Among these types, self-diffusivities in sorbents are convenient to compute via EMD using the methodology discussed in detail in Section 3.2.3. Transport diffusivity ($D_t(c)$, where $c$ is the concentration of the species in the material) is one of the most widely computed quantities to quantify the propagation of diffusing species in sorbents. $D_t(c)$ can be obtained using the following expression:

$$D_t(c) = D_0 \left( \frac{\partial \ln f}{\partial \ln c} \right)_T \tag{21}$$

The second term on the right-hand side in Eq. (21) is the thermodynamic factor, i.e., the derivative of the logarithm of the fugacity of the bulk phase ($f$) with respect to the logarithm of the concentration of the adsorbed phase.[528] Fugacities can be calculated via MC simulations (see Section 3.3). $T$ is temperature and $D_0$ is the so-called corrected diffusivity, which describes the displacement of the center of mass of the molecules propagating in the pores of the solid. Note that $D_0$ depends on $c$. Both self- and transport diffusivities, depend on the concentration or the guest loading. For a useful discussion on the subtle but critical differences between the measured and computed diffusivities, the approximations made in relating macroscopic and microscopic diffusion measurements, and the assumptions used in permeation models, the reader is referred to the work of Skoulidas and Sholl.[528]

Conventional MD faces challenges in accurately estimating diffusivity for orders of magnitude below $10^{-12}$ m$^2$/s[154,529] due to time-scale limitations. For this reason, other, non-conventional approaches are followed, that mostly fall under the category of enhanced sampling methods, addressing the problem as an activated process.[530] The most popular approach in the field is Transition State Theory (TST)[531] which can be coupled with umbrella sampling[532,533] to identify transition states of the propagation of $H_2$ gas molecules in the cages and apertures of the nanoporous material. Dynamically corrected TST (dcTST)[531,533,534] refines classical TST by

applying a transmission coefficient ($\kappa$) to account for the fact that overcoming the energy barrier of the aperture does not always result in a successful cage−to−cage crossing, i.e., some jumps fail to thermalize in the destination cage and re−cross the aperture. $\kappa$ (especially in the cases when it has a low value) can be efficiently computed following the approache of Ruiz-Montero et al.[530] Such effects can be even more pronounced when moving from rigid to flexible simulations (although $\kappa$ is also needed in simulations of rigid lattices[531,535]), since dynamic motions of groups located near the exit side of the aperture (e.g., rotating methyl groups in ZIFs or flexible linker tails) may intermittently obstruct or deflect the trajectory of the penetrating molecule. In dcTST, the diffusivity of $H_2$ is approached by tracking "hops" of $H_2$ molecules from cage to cage via crossing the framework's apertures. After many attempts, a successful aperture crossing will be achieved. The success rate is then translated to the diffusivity via the following expression

$$D_0 = \frac{1}{2n} k_{\text{EXIT}} l^2 \tag{22}$$

where $n$ is the dimensionality of diffusion (e.g., for 3D materials in which $H_2$ can diffuse in $x$, $y$, and $z$ dimensions, $n$ equals 3), $k_{\text{EXIT}}$ is the total exiting rate of a molecule from a cage to any of the adjacent ones, and $l$ is the distance between energy minima, which are the centers of cages. $k_{\text{EXIT}}$ is estimated by

$$k_{\text{EXIT}} = n_{\text{apert}} k_{\text{cross}} \tag{23}$$

where $n_{\text{apert}}$ is the number of available exiting apertures in a cage and $k_{\text{cross}}$ is the rate of successful crossings of a molecule (e.g., $H_2$) through a given aperture, given by[536]

$$k_{\text{crossing}} = \frac{1}{\sqrt{2\pi m}} P(\lambda^*) \tag{24}$$

where $m$ is the mass of the molecule, $\lambda$ is the reaction coordinate which can be regarded as a function of the Cartesian coordinates.[536] $P(\lambda^*)$ is the probability of finding the molecule in the dividing surface, which is an orthogonal plane at $\lambda = \lambda^*$ vertical to the reaction axis, close to the energy barrier (or at the point where free energy is maximized). For the cases discussed in this review the energy barrier corresponds to the aperture's center. $P(\lambda^*)$ depends on the free energy barrier and can be computed from

$$P(\lambda^*) = \sqrt{\frac{k_B T}{2\pi m}} \frac{\exp^{-\beta F(\lambda^*)}}{\int_{-\infty}^{\lambda^*} \exp^{-\beta F(\lambda^*)}} \tag{25}$$

where $F$ is the free energy, which can be computed by umbrella sampling.[51,52,532] $k_{\text{crossing}}$ (Eq. (24)) does not account for some seemingly successful jumps to a new cage, which end up again back to origin cage.[531] To account for this, a dynamic correction factor must be calculated, called correction factor ($\kappa$). Thus, the actual, crossing rate is

$$k_{\text{cross}}^{\text{dc}} = \kappa k_{\text{cross}} \tag{26}$$

Details on the umbrella sampling technique and the estimation of the correction factor $\kappa$ can be found in the work by Krokidas et al.[418]

### 3.2.6. Thermal Conductivity Using the WAVE Method.
Cheng and Frenkel[537] introduced the so-called WAVE method to calculate thermal conductivity of liquid $H_2$ (and

other systems) by analyzing density fluctuations rather than using the traditional GK method. According to the authors, this approach solves a significant limitation of GK methods when dealing with systems that have non-pairwise additive interactions (e.g., ML and DFT-derived potentials). The WAVE method uses Fourier components of density fields in the simulation cell, applies hydrodynamic theory that describes density fluctuations responsible for Rayleigh-Brillouin scattering, and uses the autocorrelation function of density waves to extract thermal conductivity. The width of the central Rayleigh peak in the power spectrum is proportional to thermal diffusivity (and thus thermal conductivity). In short, the scheme for computing thermal conductivity using the WAVE method involves the following elements: (i) Decomposing the density field into discrete Fourier components, (ii) analyzing the autocorrelation function or power spectrum of these components, (iii) fitting to hydrodynamic equations to extract conductivity $\lambda(k)$, and (iv) extrapolating $\lambda(k)$ to $k = 0$ to obtain the macroscopic thermal conductivity. Note that as stated by Cheng and Frenkel,[537] electronic effects are not accounted for since heat transfer in insulators occurs mainly due to the motion of nuclei (electrons are in the ground state and adiabatically follow the nuclei). The authors showed that the electronic contribution to the thermal conductivity of $H_2$ for the state points studied is negligible, i.e., ca. 0.002% of the computed value.

The method was validated with GK using a generalized LJ fluid over a wide range of temperature and density conditions (i.e., >20 different state points). The WAVE method only requires positional trajectories from MD simulations, making it usable as a post-processing step, there is no need to modify existing MD codes (classical or ab initio), while it works with any interaction potential, including many-body force fields, ML potentials, and DFT. According to the authors, the WAVE method eliminates the ambiguity in defining heat flux and atomic energy partitioning, and avoids potential issues with slowly decaying correlation functions in GK. Limitations of the WAVE method are the requirement of the system to be in the hydrodynamic regime (wavelengths larger than atomic dimensions), the possibility of large systematic errors due to extrapolations (although the statistical errors reported in ref 537) are small, and some discrepancies observed between GK and WAVE for bulk viscosity computations.

### 3.2.7. Identification of Hydrogen Segregation Sites at Defects.
The first task in studying H trapping and its interaction with defects is to identify the stable H segregation sites and the diffusion pathways that connect them. In perfect crystals, H occupies the classical tetrahedral (T) and octahedral (O) interstitials in bcc and fcc lattices respectively, and migrates along the minimum-energy paths between these sites as determined by Nudged Elastic Band (NEB) calculations. However, in highly distorted regions such as GBs or dislocation cores, these ideal sites no longer correspond directly to the actual trapping sites, making their identification non-trivial.

A broadly applicable strategy is the pure Voronoi-vertex sweep, i.e., one computes a full 3D Voronoi tessellation of the atomic network and treats every Voronoi vertex as a prospective H site. In fcc Ni, this automatically recovers all the T and O bulk interstices plus any irregular GB-specific voids;[538] in bcc Fe, the same vertex list captures all T sites but must be augmented by the midpoints of each Fe-Fe next-

nearest-neighbor bond to include the classical O sites before energy screening.[539]

By contrast, the polyhedral-centroid method first groups the GB region into its constituent convex packing units (e.g., tetrahedra, octahedra, pentagonal bipyramids, capped prisms) via a deltahedron-based tessellation, then places exactly one H candidate at the geometric center of each cell. This extra grouping step collapses thousands of raw vertices into a parsimonious set of physically meaningful "cages," each labeled by its polyhedral type and directly linked to local volume dilation, greatly enhancing interpretability and computational efficiency.[540,541]

Wang et al.[542] resort to a straightforward grid-scan of the GB region, placing H at regularly spaced points along and normal to the boundary and evaluating each binding energy. Although easy to implement, this brute-force line-grid approach is computationally intensive and its fixed spacing can overlook narrow or irregular traps, making it far less efficient and precise than geometry-driven methods like pure Voronoi sweeps or polyhedral-centroid tessellations.[542]

Having identified these distinct segregation sites, one can assemble the corresponding H-segregation energy spectrum for complex defect configurations, delineate the associated migration pathways, predict the equilibrium H distribution, and ultimately employ KMC simulations to model H diffusion.

### 3.2.8. Hydrogen Trapping and Interactions with Defects.
The energetics of H incorporation and trapping in a metal can be quantified in terms of two key quantities: (1) the solution energy and (2) the segregation (or trapping) energy. The energy to dissolve one H atom in the host crystal (relative to $H_2$ gas) is

$$E_{sol} = E_{host+H} - E_{host} - \frac{1}{2}E_{H_2} \tag{27}$$

where $E_{host+H}$ is the total energy of the supercell containing a single interstitial H atom, $E_{host}$ is the total energy of the pristine (defect-free) supercell, and $E_{H_2}$ is the total energy of an isolated $H_2$ molecule in vacuum. To assess the preference of H for a defect site versus a regular bulk interstitial, one evaluates

$$E_{seg} = (E_{defect+H} - E_{defect}) - (E_{bulk+H} - E_{bulk}) \tag{28}$$

A negative value of $E_{seg}$ indicates that H is energetically more stable at the defect site than in a bulk interstitial position.

Because the light mass of H gives rise to significant zero-point vibrational energy, one typically adds zero point energy (ZPE) corrections to the energies in the equations above. In practice, since the host and defect lattices contribute negligibly, the ZPE-corrected quantities reduce to[543,544]

$$E_{sol}^{ZPE} = E_{sol} + E_{host+H}^{ZPE} - \frac{1}{2}E_{H_2}^{ZPE} \tag{29}$$

and

$$E_{seg}^{ZPE} = E_{seg} + E_{defect+H}^{ZPE} - E_{host+H}^{ZPE} \tag{30}$$

where each $E^{ZPE}$ is the sum of $\frac{1}{2}\hbar\omega_i$ over the three H vibrational modes. All of these energies can be obtained from zero-temperature (static) calculations by first relaxing the relevant structures and then performing vibrational analyses on the H atoms. Energy minimization is typically carried out with conjugate-gradient (CG) or fast inertial relaxation engine

(FIRE) algorithms, either at the DFT level or using EAM or MLIP (see Section 3.1.5).

**3.2.9. Hydrogen Diffusion in Metals.** MD simulations provide a powerful approach for studying how H migrates through lattices in metals under realistic thermo-mechanical conditions. In a typical HE MD study, one integrates Newton's equations of motion for a large ensemble ($10^3$-$10^6$ atoms) using interatomic potentials parameterized to capture metal-H interactions, which range from EAM and MEAM to MLIP (see Section 3.1.5). H diffusion coefficients are then extracted from the MSD of H atoms via the Einstein relation (see Section 3.2.3). By performing simulations over a temperature range, one can obtain Arrhenius parameters (pre-exponential factor and activation energy). Periodic boundary conditions, a careful choice of time step, and sufficiently large simulation cells are crucial to minimize finite-size and sampling artifacts. Beyond pure lattice diffusion, MD naturally captures H trapping at microstructural features such as vacancies, dislocations, GBs, or free surfaces, enabling the observation of how these defects alter local diffusivity and cause transient trapping or "hopping" behavior.[538,545]

Path integral MD (PIMD), centroid MD (CMD) and ring-polymer MD (RPMD) represent three conceptually distinct ways to include nuclear quantum effects in atomistic simulations of H diffusion. In PIMD each H nucleus is replaced by a closed ring polymer of beads whose spring-bead system is thermostatted so as to sample the exact quantum canonical ensemble; because all beads move collectively, PIMD yields thermodynamic properties but does not correspond to real-time quantum dynamics. CMD and RPMD both build on the same ring-polymer framework but are tailored to approximate quantum dynamical observables: CMD propagates only the centroid (mean) position of each polymer under an adiabatic separation of internal modes, whereas RPMD evolves the full bead coordinates under Hamiltonian dynamics (with no thermostat on the real-time trajectories). Although the only formal differences among the three methods lie in the choice of fictitious bead masses and the thermostatting protocol, CMD and RPMD are based on different interpretations of how to extract time-correlation functions from the path-integral isomorphism. Both CMD and RPMD recover ordinary MD in the high-temperature limit, when the ring polymer collapses to a single point and quantum fluctuations become negligible.[465,546]

**3.2.10. Hydrogen-Mediated Dislocation Nucleation and Mobility.** Atomistic simulations, MD and transition-state calculations via the NEB method, offer powerful insight into how H modifies both the nucleation of dislocations at crack tips or free surfaces and the mobility of existing dislocations. H atoms must first be introduced at concentrations and lattice sites that mirror the intended service or experimental conditions. Equally critical is constructing a simulation cell that faithfully reproduces the target geometry, stress distribution and boundary conditions. For example, nanoindentation studies use MD to drive an indenter into a crystalline surface while monitoring the characteristic "pop-in" event in the load-displacement curve, which marks the onset of dislocation nucleation beneath the indenter[547] In a similar vein, constant-load compression of nanopillars with subsequent extended dynamic relaxation enables direct observation of dislocation emission from surfaces or edges under realistic loading rates and avoids artifacts associated with excessively high strain rates.[548,549] To probe H's effect on dislocation motion, MD

simulations can measure the critical resolved shear stress required to mobilize pre-existing dislocations in H-charged lattices.[550] In all cases it is essential to choose a sufficiently large simulation cell to eliminate spurious image interactions, apply thermostats and loading protocols that isolate the active deformation region, and select boundary constraints (fixed, free or periodic) that replicate experimental stress gradients. When these MD results are combined with climbing-image nudged elastic band (CI-NEB) calculations of the minimum-energy pathways for dislocation loop or half-loop formation, the integrated approach yields both activation energies and critical stress thresholds. Such insights are essential for quantifying how H alters the atomic mechanisms underlying fracture toughness and surface-driven plasticity.

**3.2.11. Hydrogen-Mediated Crack Propagation and Grain Boundary Decohesion.** One of the most critical aspects in the study of HE mechanisms is the coupled study of crack propagation and GB decohesion in the presence of H. In this process, H diffusion and mechanical deformation interact continuously, i.e., stress concentrations at a crack tip or along a GB attract H, which in turn weakens interatomic bonds and alters the local stress field, accelerating crack advance and promoting intergranular fracture.[551] Capturing this feedback loop requires chemo-mechanical models that combine H transport with fracture mechanics. Direct atomistic simulation of this coupling is particularly challenging because H diffusion is manifested on timescales (microseconds to seconds) far longer than typical MD loading rates (nanoseconds). As a result, most studies decouple diffusion and deformation by first establishing an equilibrium H distribution under a given stress field and then applying mechanical loading.

Two widely used strategies accomplish this without explicit H charging. In the Grand Canonical Monte Carlo (GCMC) method (see Section 3.3.2), H atoms are added or removed under a prescribed chemical potential (or gas pressure), allowing the system to reach equilibrium coverage at surfaces, GBs and crack-tip regions before loading begins.[552] Alternatively, insertion-relaxation protocols emulate H arrival by placing individual H atoms at interstitial sites dictated by the local elastic field of the crack tip, then relaxing the entire system via MD to permit real-time diffusion into favorable sites. Song and Curtin[276] used a self-consistent stochastic insertion algorithm which can be summarized as follows: At each step, the energy cost to add one more H at every empty interstitial is computed and translated into an equilibrium occupancy probability. Then randomly populate sites until no further H can be inserted at that stress intensity. Both approaches generate near-equilibrium H distributions around evolving crack tips without ever simulating $H_2$ molecules, enabling subsequent MD or CI-NEB studies of crack advance and GB decohesion under realistic H coverages.

By choosing an appropriate method for generating H distributions under varying loads, one can study HE under more realistic, coupled conditions. GCMC is typically performed before any mechanical loading to establish equilibrium H coverages at surfaces, GBs and crack tips. Once deformation begins, whether via dislocation emission, cleavage or crack advance, it proceeds at MD strain rates many orders of magnitude higher than H diffusion rates, so further redistribution of H is negligible on the simulation timescale.[553] The downside is that GCMC is computationally expensive, and therefore, impractical to run different simulations for each small loading increment. As a result, it cannot capture any

load-induced changes in H segregation. In contrast, self-consistent stochastic insertion algorithms rebuild the H distribution after each incremental increase in stress intensity. Although this still does not track H diffusion in real time, it captures the instantaneous interplay between evolving stress fields and H trapping at every load step, providing a practical compromise between physical fidelity and computational cost.[276]

### 3.2.12. Electroosmotic Drag Coefficient.
Electroosmotic drag (EOD) signifies the transport ratio of water to protons (H$^+$) in a membrane.[92] In hydrated membranes, H$^+$ are conveyed across the membrane in response to an electric field. H$^+$ do not migrate independently across the membrane; instead, they are stabilized as H$_3$O$^+$ or larger protonated clusters. Proton transport, therefore, occurs via the so-called proton hopping (Grotthuss mechanism)[554,555] and vehicular mechanism.[556] According to the vehicular mechanism, H$^+$ move between water molecules involving coordinated movement of H$_3$O$^+$ ions and water molecules. This differs from the Grotthuss mechanism, where protons hop through a chain of water molecules by breaking and forming hydrogen bonds. The combined effect of these two mechanisms results in the manifestation of ionic conductivity in hydrated membranes. EOD is influenced by the level of hydration ($\lambda$) which indicates how many water molecules are associated with each ion exchange site in the membrane. For a Nafion membrane, hydration is defined as

$$\lambda = \frac{N_{H_2O}}{N_{SO_3^-}} = \frac{N_{H_2O}}{N_{H_3O^+}} \tag{31}$$

where $N_{H_2O}$, and $N_{SO_3^-}$ are the numbers of water molecules and sulfonic acid groups in the membrane, respectively.

The EOD coefficient, $\xi_D$ is a measure of the number of water molecules transported alongside each proton within its solvation shell, and is defined as

$$\xi_D = \frac{j_{H_2O}}{j_{H^+}} \tag{32}$$

where $j_{H_2O}$ and $j_{H^+}$ are the fluxes of water molecules and protons, respectively. Note that $\xi_D$ is defined in the absence of concentration and/or pressure gradients, and at vanishing chemical potential gradients of water.[92,100,557,558] EOD coefficients are computed using NEMD, in which the driving force is imposed by an external electric field, **E**. The necessity for NEMD arises because the transport of water and ions are governed by both diffusion and the coupling of electrical and hydrodynamic forces. NEMD framework is therefore necessary, as the introduction of an electric field induces directional ion motion, which in turn influences water transport. In practice, the EOD coefficient is computed by applying external electric fields of varying magnitudes across one axis of the simulation box at a time and observing that ion velocities scale linearly with the field.[94] By analyzing the system's response to these external perturbations, the EOD can be extracted from the NEMD simulation in agreement with Eq. (32), from

$$\xi_D = \lim_{\mathbf{E} \to 0} \frac{j_{H_2O}}{j_{H^+}} \tag{33}$$

where each flux is obtained at vanishing **E**, ensuring the sampling occurs in the linear response regime. This definition is in alignment with the broader framework introduced in Eq. (9).

In a classical MD simulation, where proton hopping is absent, the flux of H$_3$O$^+$ perpendicular to one of the faces of the simulation box along the x, y, or z axis can be expressed as the product of the number of H$_3$O$^+$ and their average velocity along the respective axis, sampled during the production runs. Similarly, the flux of water molecules can be expressed as the product of the number of water molecules and their average velocity.[94] Consequently, Eq. (33) can be rewritten in terms of number density and velocity for the classical case where proton hopping does not occur

$$j_{H_3O^+} = N_{H_3O^+} \left\langle v_{H_3O^+} \right\rangle \tag{34}$$

where $j_{H_3O^+}$ is the flux of hydronium ions across the membrane. A similar expression applies to the molecular flux of water. Using the definition of $\lambda$ in Eq. (31), one can substitute $N_{H_2O} = \lambda N_{H_3O^+}$ into Eq. (33), leading to

$$\xi_D = \lim_{\mathbf{E} \to 0} \frac{j_{H_2O}}{j_{H_3O^+}} = \lambda \times \lim_{\mathbf{E} \to 0} \frac{\left\langle v_{H_2O} \right\rangle}{\left\langle v_{H_3O^+} \right\rangle} \tag{35}$$

Eq. (35) enables the direct computation of the EOD coefficient from MD simulations by tracking the velocities of water and H$_3$O$^+$ under an applied electric field. The EOD coefficient is determined by interpolating the average velocities as **E** approaches zero.[94] It is evident that Eq. (35) represents a specific case of the more general formulation given in Eq. (33).

It is important to note that $\xi_D$ can be computed using both classical simulations[94,127,559] and first principles MD of small systems.[129] The advantage of a first-principles simulation is that it captures the Grotthuss mechanism, in contrast to MD. Due to the fact that this mechanism becomes more dominant at higher water uptakes in the membrane, it is not a surprise that $\xi_D$ of water computed via classical MD is in good agreement with experimental data[560] at lower water uptakes[94]

### 3.2.13. Thermodynamic Factor for Diffusion.
The thermodynamic factor $\Gamma$ for diffusion links MS and Fick diffusivities via Eq. (16). For an $N$-component mixture, the thermodynamic factor matrix $\mathbf{\Gamma}$[266,510] is defined as

$$\Gamma_{ij} = \delta_{ij} + x_i \left( \frac{\partial \ln \gamma_i}{\partial x_j} \right)_{T, P, \Sigma} \tag{36}$$

where $x_i$ is the mole fraction, $\gamma_i$ the activity coefficient, $T$ the temperature, $P$ the pressure, and $\delta_{ij}$ the Kronecker delta. The constraint $\Sigma$ enforces that during the differentiation, $\{x_i\}$ of all species remain constant, except for the $n^{th}$ component, so that $\sum_{i=1}^{n} x_i = 1$[266,507,510]. The activity coefficient $\gamma_i$ is related to the chemical potential as follows[266,510]

$$\ln \gamma_i = \frac{\mu_i - \mu_i^o}{k_B T} - \ln x_i \tag{37}$$

where $\mu_i^o$ is the chemical potential of pure component $i$. For a binary mixture, Eq. (36) reduces to a single thermodynamic factor $\Gamma$. $\Gamma = 1$ denotes an ideal mixture, while negative values indicate phase separation. In general, $\mathbf{\Gamma}$ for an $N$-component mixture is not symmetric,[267,510] and for ideal mixtures ($\gamma_i = 1$), $\Gamma_{ij} = \delta_{ij}$. $\mathbf{\Gamma}$ can be computed via molecular simulation in various ways; via Kirkwood-Buff integrals (KBIs),[561−565,565−570]

simulations at the grand canonical (GC) ensemble,[571] and by using the Permuted Widom Test Particle Insertion (PWTPI) method.[572,573] Each approach has advantages and drawbacks. For example, KBIs yield thermodynamic factors without relying on activity coefficient models but require large system sizes to obtain accurate RDFs, especially for $n > 2$ components.[506,574] In contrast, PWTPI directly yields composition derivatives from a single simulation at a computational cost similar to WTPI,[51,575] but like WTPI and GC methods, it is inefficient at liquid-like densities due to the low probability of successful single-step particle insertions.[51] Recently, the CFCPWTPI method developed by Hulikal Chakrapani et al.[576] was used to compute thermodynamic factors for dense $CO_2$-$H_2$ mixtures using small systems (i.e., containing a few hundred molecules). Such innovations improve the feasibility and reliability of using molecular simulations to directly realize the theoretical definitions of thermodynamic factors.

### 3.2.14. Hydrate Phase Equilibria from the "Direct Phase Coexistence" Method.

The "direct phase coexistence" method[577] has extensively been used to calculate the phase equilibria of systems such as ice[367,368] and hydrates.[342,369,578−581] The different phases that are at equilibrium (e.g., solid hydrate (H)/ice (I), liquid water (W), gas (G)/vapor (V)) are brought in contact, and the evolution of the potential energy of the system is sampled via MD simulations at the $NPT$ ensemble. By performing a temperature scan (i.e., recording the potential of the system for each temperature considered) for any given, fixed pressure, the three-phase equilibrium temperature can be identified, as the average between the lowest value that hydrate dissociation occurs and the highest value that hydrate formation occurs. To increase the accuracy of the calculation, the equilibrium temperature should be the result of averaging multiple MD runs (replicas).

Fig. 16 is a schematic representation of the various steps of the "direct phase coexistence" approach. Typical configurations for the simulations, encountered in the literature, are the three-slab (WHG) or four-slab (WHWG) arrangement. A hydrate supercell ($K \times M \times N$) of the hydrate structure of interest is constructed by using $K$, $M$, and $N$ unit cells in the $x−$, $y−$, and $z−$ directions, respectively. The positions of the oxygen atoms within the unit cell of the sII hydrate can be obtained from Mak and McMullan,[582] while the corresponding positions for sI hydrates, from McMullan and Jeffrey.[583] The positions of the hydrogen atoms can be found by minimizing the energy of the system while fixing the oxygen atoms, resulting in a structure that respects the Bernal and Fowler[584] rules. Such an approach has been suggested[585] as an alternative to finding a configuration that has the minimum dipole moment. Takeuchi et al.[586] provided a detailed discussion for sI, sII, and sH hydrates. The authors used the TIP4P water model, and reported the coordinates of water molecules in the unit cell of hydrates that have nearly zero net dipole moment. The reported coordinates have been used in many molecular simulation studies, and have been further adapted for use with different water force fields.

All the centers of the cages can be filled with a single guest molecule (i.e., 100% (full) cage occupancy). Alternatively, experimental measurements or MC simulations can be used for cases of examining partial (i.e., lower than 100%) or multiple (i.e., higher than 100%) cage occupancy. A typical procedure followed during these simulations involves the following steps:
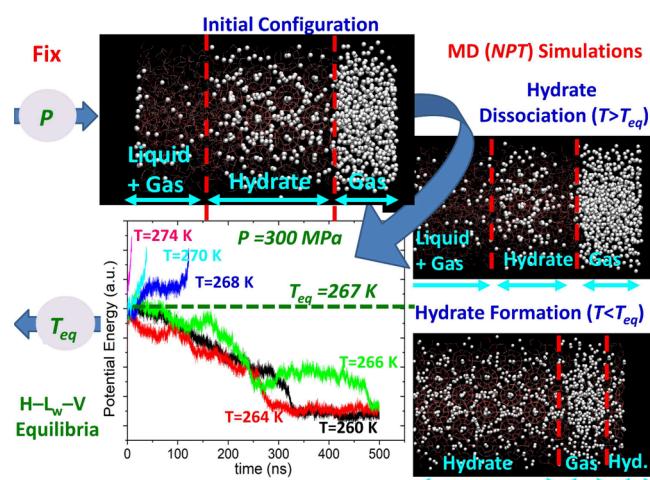


**Figure 16.** A schematic representation of the "direct phase coexistence" method. For a fixed $P$, an initial configuration (shown in the top left panel) consisting of three distinct slabs (i.e., (i) Liquid $H_2O$ + dissolved $H_2$, (ii) hydrate crystal, and (iii) gaseous $H_2$) is constructed to perform MD simulations ($NPT$ ensemble). The potential energy of the total system is recorded for various temperatures (shown in bottom left panel). For $T > T_{eq}$ (where $T_{eq}$ is the equilibrium temperature) the potential energy increases, and the hydrate dissociates (top right panel), while for $T < T_{eq}$ the potential energy decreases, and the hydrate phase grows (bottom right panel). For the shown $P$, $T_{eq} = 267$ K is identified as the average between the lowest value (268 K) at which hydrate dissociation occurs and the highest value (266 K) at which hydrate formation occurs.

Initially, each slab is equilibrated separately at each different pressure. Next, all different slabs are connected with a buffer distance, followed by energy minimization to avoid overlaps, while keeping the oxygen positions frozen. The connection of the slabs is achieved with their interfaces normal to the $x$-direction. During the equilibration of the water and $H_2$ slabs, their $y$ and $z$ dimensions are kept equal to the equilibrated $y$ and $z$ dimensions of the hydrate slab.

### 3.2.15. Hydrate Structure and Kinetics.

A number of methods have been reported for the calculation of the growth rate of hydrate crystals based on MD simulations. Such methods include: (i) the counting of the water molecules added to the hydrate phase,[587] (ii) plotting the potential energy as a function of time (until it reaches constant value) in order to estimate the growth time $\tau$. The growth rate, $u$, is then simply obtained by dividing the length of the grown hydrate, $\Delta L$, by $2\tau$ due to the fact that there are two interfaces growing under periodic boundary conditions,[588] and (iii) tracking of the position of the hydrate-liquid interface.[589,590] To identify the type of structure each water molecule belongs to, order parameters have been defined. The order parameters can describe the hydrogen bond network within the water. In particular, $F_3$ expresses deviations from the tetrahedral angle within the hydrogen bond network.[591] An angle $\theta$ can be defined between the oxygen atoms in a $B_i − A − B_j$ triad and then used to calculate $F_3$ through the equation

$$F_3 = \left\langle \left( \cos\theta |\cos\theta| + \cos^2\theta_t \right)^2 \right\rangle \tag{38}$$

where $\theta_t$ is the tetrahedral angle ($109.47°$). The angular brackets denote an average over all unique pairs $B_i$, $B_j$ and over all the designated central atoms $A$. Essentially, the order parameter probes oxygen atoms within the first solvation shell

of the central oxygen atom (i.e., less than 0.35 nm from oxygen A). $F_3$ will be close to zero for tetrahedrally coordinated water and larger than zero otherwise.[592]

For the analysis of hydrate crystals Rodger et al.[593] concluded that it would be useful to have an order parameter that can distinguish between the different tetrahedral networks adopted by water, and introduced a new, four-body order parameter ($F_{4\phi}$) based on the H-O−O-H torsion angle, $\phi$ for two adjacent water molecules; for these purposes the hydrogen atoms have been defined as the outer-most H in the water dimer. ($F_{4\phi}$) is defined as

$$F_{4\phi} = \langle \cos 3\phi \rangle \tag{39}$$

Therefore, by comparing the set of instantaneous order parameters for any specific water molecule with the distribution of parameters found within various stable phases (see Table 8), it is possible to identify the local phase to each

**Table 8. Order Parameters for Water Molecules in Various Phases**

| Phase | $F_3$ | $F_{4\phi}$ |
|---|---|---|
| Liquid | 0.1 | −0.04 |
| Hydrate | 0.01 | 0.7 |
| Ice | 0.01 | −0.4 |

water molecule, and thereby to determine both the hydrate content of a system and the extent to which the water molecules with hydrate local phase are clustered.

Alternatively, some studies considered the time evolution of the number of $5^{12}$ or $5^{12}6^4$ cages to track the hydrate growth rate. In particular, in two $H_2$-hydrate-related studies (i.e., $H_2$ + $CH_4$;[594] $H_2$ + THF[595]), the hydrate growth process was monitored with the face-saturated incomplete cage analysis method (FSICA).[596] By performing an analysis of the network topology formed by the hydrogen bonds of water molecules, FSICA can identify all of the face-saturated hydrate cages in the system, where face-saturation means that the edge formed between two water molecules is shared by at least two faces (water rings).[596] Zhang et al.[594] showed that the calculation of the growth rate, either using the evolution of the number of $5^{12}$ cages, or using the evolution of the number of $5^{12}6^4$ cages produce identical results for the hydrate crystal growth rate. The hydrate growth rate in these studies was calculated using the following equation:

$$R = \frac{N_{500ns} - N_{100ns}}{L_x L_y 400} \tag{40}$$

where $N_{100ns}$ and $N_{500ns}$ represent the number of $5^{12}$ cages in the system at 100 and 500 ns of simulation duration, respectively. $L_x$ and $L_y$ represent the $x −$ and $y −$ direction lengths of the system box, respectively. $\Delta t = 400$ is the time span between the two measurements.

**3.2.16. Interfacial Tension.** Let us consider a planar slab of fluid with a planar area $\mathcal{A} = L_\parallel^2$, in contact with a gas inside a simulation box with dimensions $L_\parallel$, $L_\parallel$, $L_\perp$ in the $x$, $y$, $z$ directions (box volume: $V = L_\parallel^2 \times L_\perp$), respectively. The thermodynamical definition of the interfacial tension of gas-liquid (or a liquid-liquid) interface in the canonical ($NVT$) ensemble is the change in the Helmholtz free-energy ($F$) of the system due to the change in the surface area of the interface[51,52,597]

$$\gamma = \left( \frac{\partial F(N, V, T)}{\partial \mathcal{A}} \right)_{N,V,T} \tag{41}$$

where the composition, volume, and temperature of the system are fixed. Interfacial tension in a system with fixed pressure, temperature, and composition is given by[51,52,597]

$$\gamma = \left( \frac{\partial G(N, p, T)}{\partial \mathcal{A}} \right)_{N,p,T} \tag{42}$$

where $G(N, p, T)$ is the Gibbs free energy of the system.

The mechanical definition of the surface tension using the microscopic pressure tensor for a planar fluid slab coexisting with a gas as proposed by Irving and Kirkwood is[597−599]

$$\gamma = \int_{-\infty}^{\infty} dz[p_\perp(z) - p_\parallel(z)] \tag{43}$$

where $p_\perp$ and $p_\parallel$ follow from

$$p_\perp = p_{zz} \tag{44}$$

and

$$p_\parallel = \frac{1}{2}(p_{xx} + p_{yy}) \tag{45}$$

The integrand of Eq. 43 is non-zero only in the vicinity of interface separating the two phases and zero otherwise.[51,52,597] As stated in the review by Ghoufi et al.[597], the definition of $\gamma$ from the thermodynamic route (Eq. (41)) and the mechanical route (Eq. (43)) are formally equivalent. It is important to note that Eq. (43) is valid for continuous pairwise-additive potentials.[51,52,597] It is readily shown that,

$$\int dz\, p_{\alpha\beta} = L_\perp \langle p_{\alpha\beta} \rangle \tag{46}$$

where

$$p_{\alpha\beta} = \rho k_B T(\mathbf{I})_{\alpha\beta} + \frac{1}{V} \left\langle \sum_{i=1}^{N-1} \sum_{j>i}^{N} (\mathbf{r}_{ij})_\alpha (\mathbf{f}_{ij})_\beta \right\rangle \tag{47}$$

where $\rho = N/V$ is density, $\mathbf{I}$ is the identity matrix, $\mathbf{r}_{ij}$ and $\mathbf{f}_{ij}$ are the separation vector and the intermolecular force between molecule $i$ and $j$, $\alpha$, $\beta = x$, $y$, $z$ and $\langle \cdots \rangle$ is the canonical (Boltzmann) average over the simulation run. Using Eq. (46) the interfacial tension in Eq. (43) can be rewritten as follows

$$\gamma = \frac{L_\perp}{2} \langle p_\perp - p_\parallel \rangle \tag{48}$$

where the factor 2 in the denominator signifies the presence of two interfaces. Equation 48 is also called the Kirkwood-Buff definition.[597,600]

**3.2.17. Solid Gas/Liquid Contact Angle.** Contact angles provide a quantitative measure of how a liquid, solid, and gas interact at their three-phase contact line.[52] As shown in Fig. 17, the contact angle is defined as the angle formed between the tangent to the liquid-gas interface and the solid surface at the point where they meet. Contact angle characterizes the wettability of the surface, i.e., small contact angles indicate a surface that is easily wetted, while large ones suggest poor wettability. By measuring contact angles, one can gain insights into surface chemistry, material properties, and fluid-solid interactions. Below, we describe how to compute contact angles for gas bubbles in MD simulations.
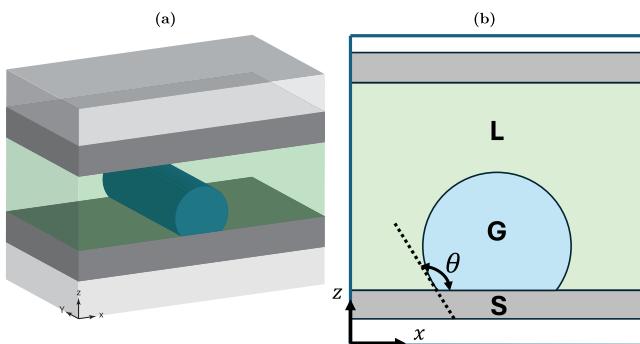
**Figure 17.** (a) A typical MD simulation setup for computing contact angles: A hydrogen nano-bubble (dark green) immersed in water/brine (transparent green), shaped cylindrically due to symmetry along the $y$-direction, is enclosed between solid surfaces (dark gray) at the top and bottom. The top wall serves as a piston (or barostat) to control gas-liquid pressure.[601,602] To prevent wall interactions across periodic boundaries, the simulation box length in the $z$-direction is (typically) several times longer than lateral dimensions.[602] The regions (in light gray) above the top wall and below the bottom wall are vacuum. (b) A cross section of the simulation box in the $x - z$ plane. The intersection between the solid surface (S), surface of the nanobubble (G) and the liquid medium (L) co-determines the contact angle $\theta$.

To compute contact angles, MD simulations are performed in the *NVT* ensemble adopting the setup shown in Fig. 17(a).[602−609] A cylindrical slab composed of $H_2$ gas spanning the $y -$ direction is surrounded by water while directly contacting a "solid" slab beneath it. Typically, a gas nanobubble spanning the $y -$ direction is chosen to avoid the effects of line tension on the contact angle. By eliminating effects of line tension on the contact angle, a comparison with experiments is possible. Introducing another solid slab positioned at a distance $w$ from the bottom slab confines the gas-liquid medium. Adjusting the distance $w$ allows for variation in the confining pressure, effectively serving as a barostat, as depicted in Fig. 17(a). The volumes between the lower surface of the lower solid slab and the upper surface of the upper solid slab are vacuum. To ensure that the slabs do not interact via the periodic boundary in the $z$-direction the top and bottom wall are positioned far from each other. Finally, the gas nanobubble is equilibrated for a duration of several ns, after which the contact angle can be computed.

To determine the contact angle, 2D $xz$ density maps (see Fig. 17(b)) are obtained by a binning procedure wherein the center-of-mass of the gas nanobubble in the simulation box are segregated into bins of a (typical) size of $0.5 \times 0.5$ Å$^2$, based on their position in the $xz$ plane. Density maps are averaged over several ns to obtain a smooth density profile. A non-linear regression is performed to fit the iso-density curve of the gas nanobubble to a circle, and its intersection with the position of the wall in the $z$ direction determines the contact angle, as shown in Fig. 17(b). For instance, the position of the wall in the $z$-direction is determined by averaging the positions of the outermost silica atoms if the wall is composed of silica as in the study by Chen and Xia.[605] The contact angle of a water droplet is the supplementary angle corresponding to the contact angle of the gas nanobubble, i.e., $\theta_{H_2O}=180$-$\theta$ in Fig. 17(b). A note of caution to the reader: in the absence of any pinning sites (or heterogeneities) the gas nanobubble tends to translate parallel to the wall, and its center of mass may vary with time. Thus,

when generating density maps, it is important to reposition the the gas nanobubble about its center of mass.

## 3.3. Computation of Hydrogen Properties Using Monte Carlo Simulations

The past decades, MC simulations have been evolved into a powerful tool for computing thermodynamic properties of reactive and non-reactive $H_2$ systems. Representative examples of such properties are phase coexistence, chemical reactions, solubilities (in gas, liquid, and solid phases), densities, and chemical potentials. As in MD simulations, the interactions between atoms and molecules are determined based on the chosen force fields. Unlike MD simulations, MC simulations use a stochastic algorithm. The concept of "trial-moves" is used in MC simulations to sample the phase-space. Examples of trial-moves are displacements and rotations of molecules, particle insertions (or deletions), volume changes, and changes in bond lengths.[51,52] Trials moves can be accepted (or rejected) based on a probability ($P_i$), which is often proportional to the probability of occurrence of the given micro-state (i.e., metropolis algorithm). Trial moves can also be more complex, such as identity swaps, where one particle type is replaced by another. The flexibility of MC methods is a significant advantage compared to MD. MC simulations typically involve thousands to millions of cycles, where each cycle consists of $N$ trial moves. The number of cycles needed depends on the property being studied, the size of the system, and the complexity of the force field. The properties listed in this section such as excess chemical potentials and solubilities can also be computed using MD. However, they are most commonly computed using MC simulations. For all details regarding MC simulations and statistical mechanics the reader is referred to the relevant textbooks.[51,52,296,298]

As for MD simulations, several high-quality open-source software packages have been developed through the years for performing MC simulations of $H_2$ (and other) systems. Prime examples are Towhee,[610] Cassandra, RASPA,[480] and BRICK-CFCMC,[611,612] however, the list of available codes is long. For a relevant discussion the reader is referred to ref 613. Visualization of MC simulations is an important feature allowing for both understanding of mechanisms and tracing of possible simulation errors. Examples of state-of-the-art visualization software for molecular simulations is discussed in Section 3.2.

Kinetic Monte Carlo (KMC) is a simulation technique that is used to model the time evolution of physical systems through stochastic processes, focusing on the dynamics and rates of transitions between states.[614,615] Unlike classical MC (described above), which primarily samples equilibrium configurations using acceptance probabilities based on energy differences, KMC explicitly tracks the temporal evolution of the system with transition rates, and associates time with each simulation step. KMC works by selecting transitions proportionally to their rates rather than attempting moves with uniform probability followed by accept/reject decisions, making it particularly well-suited for studying non-equilibrium processes and kinetic phenomena while classical MC excels at determining equilibrium thermodynamic properties. While MD simulations (see Section 3.2) are well-suited for studying fast processes such as the dislocation motion, they are limited in their ability to capture the long-timescale diffusion and segregation of $H_2$ in complex micro-structures. KMC methods complement MD by enabling the simulation of $H_2$ transport

over experimentally relevant timescales (up to seconds or longer) while maintaining atomic-level resolution. In this review, we briefly describe properties computed with KMC related to HE.

**3.3.1. Phase Equilibria of Hydrogen Systems.** Based on vapor-liquid equilibrium (VLE), the solubilities of $H_2$ in different liquid mixtures, densities, and equilibrium gas compositions can be determined. Equilibrium is established when the chemical potentials of both phases are equal. At this point, the densities of each phase become stable, fluctuating around well-defined values. To compute VLEs of $H_2$ mixtures from molecular simulations, different methods can be used.

*3.3.1.1. Gibbs Ensemble.* A common approach for computing the VLE of a system with MC simulations is the Gibbs Ensemble (GE) method introduced by Panagiotopoulos[616] in 1987. Unlike most MC and MD methods, GE considers two distinct simulation boxes (without any interface), each containing the gas or the liquid phase. GE enables the determination of phase coexistence properties of multicomponent systems from a single simulation. To achieve equilibrium, a sufficient number of MC trial moves are performed to generate random configurations within each phase, along with the random transfer of molecules between them.[51] To assess whether the chemical potentials of the two phases have equilibrated, test particle insertion methods[617] are often employed. When one of the phases has a high density (e.g., liquid water at room temperature), VLE computations can become inefficient. This is primarily due to the frequent rejection of molecular exchanges between the simulation boxes in conventional single-molecule trial insertion and removal moves. In such cases, the Continuous Fractional Component Gibbs Ensemble (CFCGE) approach (GE expanded with fractional molecules) can be used to facilitate the equilibration of phase compositions (i.e., sampling densities at equilibrium) while also enabling direct sampling of chemical potentials.[618] This approach will be discussed further in Section 3.3.1.4.

*3.3.1.2. Vapor−Liquid Equilibrium from Chemical Potentials.* Although GE and CFCGE methods provide a straightforward approach to compute the VLE of $H_2$ systems, the chemical potential of each phase (or species) can also be independently sampled in separate simulations to determine VLE compositions. Rahbari et al.[110] performed CFCGE simulations to compute the VLE of $H_2O − H_2$ systems at high pressures. At low $H_2$ concentrations, either a simulation box with a large number of molecules is required or extended simulation cycles to adequately sample the equilibrium composition in each phase. In such cases, separate simulations for each phase are recommended to determine the chemical potential for phase equilibrium.

Accurately computing chemical potentials is crucial for obtaining solubilities and VLEs of $H_2$ systems using molecular simulations. The chemical potential of $H_2$ in each phase can be expressed as

$$\mu_{H_2} = \underbrace{\mu_{H_2}^0(T) + k_B T \ln\left(\frac{\langle \rho_{H_2} \rangle}{\rho_0}\right)}_{\text{ideal gas part}: \mu_{H_2}^{id}} + \mu_{H_2}^{ex} \tag{49}$$

where $\mu_{H_2}^0(T)$ represents the reference chemical potential, incorporating intramolecular contributions such as rotation, vibration, translation, and bond dissociation energy. The

number density, $\rho_{H_2}$, is defined as the number of molecules per unit volume, with $\rho_0 = 1$ Å$^{-3}$ serving as a reference to ensure a dimensionless logarithm. $\mu_{H_2}^0(T)$ is relevant when chemical reactions (bond breaking/formation) are considered in the simulations. The first two terms in Eq. (49) correspond to the ideal gas contribution ($\mu_{H_2}^{id}$), while the final term represents the excess chemical potential ($\mu_{H_2}^{ex}$), which quantifies the difference in the Gibbs free energy associated with the addition of a molecule or species of type $i$ into an interacting molecular system compared to an ideal gas at the same temperature, pressure, and composition.[619] Different methods can be used to compute $\mu_{H_2}^{ex}$, and therefore, VLE and solubilities, in molecular simulations. Brief overviews of these methods are provided below.

*3.3.1.3. Widom Test Particle Insertion Method.* The Widom test particle insertion (WTPI) method, along with its adaptations, is widely used for computing $\mu_{H_2}^{ex}$ in both MC and MD simulations.[51,572,573,576,617,618,620−623] $\mu_{H_2}^{ex}$ is sampled using the WTPI method as

$$\mu_{H_2}^{ex} = -k_B T \ln \left\langle \exp[-\beta \Delta U_{H_2}^+] \right\rangle_{NVT} \tag{50}$$

where $\Delta U_{H_2}^+$ is the energy change of the system when a $H_2$ probe molecule (or any other species) is randomly inserted in the system. One should be aware that Eq. (50) faces challenges when simulating high-density systems or systems with a strong dependence on molecular orientation.[54,624,625] Variations of WTPI, in which the test particle is gradually inserted, are commonly used in expanded ensemble methods (in both MC and MD) to avoid the drawbacks of the single-step insertions.

*3.3.1.4. Continuous Fractional Component Monte Carlo.* The CFCMC[626,627] method is an adaptation of the expanded ensembles concept in MC simulations. A thorough review of this method is provided in.[618] In CFCMC, conventional ensembles such as *NPT*, *NVT*, GE or the reaction ensemble (RxMC), are expanded with a fractional molecule or a group of fractional molecules with scaled interactions. This leads to improving efficiency in cases where one phase has a high density or strong electrostatic interactions. Simultaneously, the excess chemical potentials of species in both phases are obtained. The interactions of the fractional molecules are scaled with a coupling parameter $\lambda \in [0, 1]$.[627−629] At $\lambda = 0$, the fractional molecule does not interact with the rest of the molecules in the system, while at $\lambda = 1$, the fractional molecule has fully scaled interactions. Staged insertions are performed during the simulation using random trial moves in $\lambda$ space by increasing or decreasing the value of $\lambda$. To improve sampling in $\lambda$ space (especially in dense systems, such as aqueous solutions), a biasing weight function is often applied[112,630] using the Wang-Landau algorithm.[631] Provided that sufficient sampling is performed at $\lambda = 0$ and $\lambda = 1$, $\mu_{H_2}^{ex}$ in the *NVT* or *NPT* ensemble follows from[627,632]

$$\mu_{H_2}^{ex} = -k_B T \ln\left(\frac{p(\lambda_{H_2} = 1)}{p(\lambda_{H_2} = 0)}\right) \tag{51}$$

where $k_B$ is the Boltzmann constant, and $T$ is the temperature in K. $p(\lambda_{H_2} = 1)$ and $p(\lambda_{H_2} = 0)$ are the probabilities of the coupling parameter $\lambda$ of $H_2$ fractional molecules being equal to 1 and 0, respectively.

Thermodynamic integration is an alternative method for computing excess chemical potentials in CFCMC simulations or in similar adaptations of expanded ensembles:[618]

$$\mu_{H_2}^{ex} = \int_0^1 \left\langle \frac{\partial U(\lambda_{H_2})}{\partial \lambda_{H_2}} \right\rangle d\lambda_{H_2} \tag{52}$$

In dense electrolyte solutions, performing random walks in the $\lambda$ space can become difficult because of the strong electrostatic interactions in the mixture.[612] In such cases, it is difficult to sufficiently sample the $\lambda$ space even using biasing weight functions constructed by the Wang-Landau algorithm. This is especially the case when computing $\mu^{ex}$ of ions, such as Na$^+$.[612] Thermodynamic integration can therefore be used in multiple simulations for fixed values of $\lambda \in [0, 1]$ to compute the excess chemical potentials.[612]

*3.3.1.5. Solubility of Hydrogen in the Liquid Phase.* The solubility of H$_2$ in the liquid phase can be computed based on the excess chemical potential of H$_2$ in the liquid phase. The ideal gas chemical potential of H$_2$ (and therefore the number density) in the liquid phase is obtained by imposing equal chemical potentials of H$_2$ in the gas phase and the liquid phase ($\mu_{H_{2(g)}} = \mu_{H_{2(l)}}$). The solubility of H$_2$ in the liquid phase follows from[47,110]

$$\frac{\langle \rho_{H_{2(l)}} \rangle}{\rho_0} = \exp\left[\frac{\mu_{H_{2(l)}}^{id} - \mu_{H_2}^0}{k_B T}\right] = \exp\left[\frac{\mu_{H_{2(g)}} - \mu_{H_{2(l)}}^{ex} - \mu_{H_2}^0}{k_B T}\right] \tag{53}$$

At low fugacities of H$_2$, the solubility of H$_2$ can also be computed using Henry coefficients ($H$):

$$\frac{\langle \rho_{H_{2(l)}} \rangle}{\rho_0} = \lim_{f_{H_2} \to 0} \frac{f_{H_2}}{H} \tag{54}$$

The Henry coefficient of H$_2$ can be computed directly based on $\mu_{H_{2(l)}}^{ex}$:

$$H = \rho_0 k_B T \exp\left[\frac{\mu_{H_{2(l)}}^{ex}}{k_B T}\right] \tag{55}$$

At sufficiently low H$_2$ densities, the ideal gas law can also be used (i.e., $f_{H_2} = P_{H_2} = \rho_{H_2} k_B T$). This significantly simplifies the computation of H$_2$ solubilities compared to Eq. (53), as no simulations are needed for the gas phase.

*3.3.1.6. Grand Equilibrium Method.* The grand equilibrium method computes VLE for multi-component systems by equilibrating the liquid phase in the *NPT* ensemble, where the chemical potential is sampled using Widom's test particle insertion method (explained in Section 3.3.1.3).[48] From the chemical potential, the Henry constant is calculated at infinite dilution. The chemical potential is then fitted as a function of pressure ($\mu(P)$) at constant temperature and mixture composition and approximated using a Taylor series expansion. This function is subsequently used in a pseudo-$\mu VT$ ensemble simulation of the vapor phase to sample the vapor pressure. Köster et al.[48] applied this method to compute VLE for H$_2$ multi-component systems.

*3.3.1.7. Fugacity Coefficient.* The fugacity coefficient of H$_2$ can be computed from the $\mu_{H_2}^{ex}$ or probability distribution of $\lambda$ (see Eq. (51)) in a mixture using

$$\phi_{H_2} = \frac{\exp\left[\frac{\mu_{H_2}^{ex}}{k_B T}\right]}{Z_{mix}} = \frac{1}{Z_{mix}} \times \frac{p(\lambda_{H_2} = 0)}{p(\lambda_{H_2} = 1)} \tag{56}$$

where $Z_{mix} = \frac{P\langle V \rangle}{N_t RT}$ is the compressibility factor of the mixture, and $N_t$ is the total number of moles in the mixture.

**3.3.2. Hydrogen Adsorption onto Nanoporous Materials.** The Grand Canonical Monte Carlo (GCMC) method (system at constant $\mu, V, T$) is widely used to study gas adsorption in nanoporous media such as polymers, MOFs, COFs, zeolites, and CNTs.[51,52,317] In GCMC, a simulation box with constant volume containing the adsorbent (e.g., solid) is used,[51,52] assuming contact with an infinite reservoir (not explicitly considered) that holds the adsorbate (e.g., H$_2$ or gas mixture) at a specified temperature, pressure, and composition. Gas molecules are randomly inserted and deleted (adsorbed/absorbed and desorbed) onto the material surface or in the pores. The chemical potential of each component in the reservoir (and therefore the solubility of the adsorbate), $\mu_i(p, T, x)$, can be computed using an EoS or WTPI method (see Section 3.3.1.3) in the *NPT* ensemble. This ensemble can also be extended with fractional H$_2$ molecules to compute solubility, phase coexistence, and equilibrium properties more efficiently, following the principles outlined in Section 3.3.1.4

An alternative way to compute the solubility coefficient is to use the WTPI method in MD trajectories of only the adsorbent (e.g., MOF, ZIF). The MD simulation generates representative host configurations (usually in the order of $10^3$ simulation snapshots). In each of these frames, a sole molecule of the gas under investigation is randomly inserted at various positions, to get adequate statistics on the conformations of the guest-host system, and at each insertion the energy of the system is calculated. An average over these different conformations yields $\mu_i^{ex}$ of the inserted species according to Eq. (50). The solubility, $S_i$, of component $i$ (e.g., H$_2$), can be then obtained from

$$S_i = \frac{22400 \text{ cm}^3 \text{ STP}}{\text{mol}} \frac{1}{RT} \exp\left(-\frac{\mu_i^{ex}}{RT}\right) \tag{57}$$

As already shown in Eq. (56) in Section 3.3.1.7, the excess chemical potential can lead to fugacity. This facilitates the production of adsorption isotherms, by linking the fugacity to the number of existing sorbed molecules.

**3.3.3. Hydrogen Adsorption and Separation of Gas Mixtures in Hydrates.** As discussed in the previous section, GCMC simulations are widely used to compute gas adsorption in solid nanoporous materials. Considering that gas hydrates have a fixed and well defined geometry, enables simulating their formation as a process of adsorption of H$_2$ gas inside a porous solid material (i.e., the different cages are considered as effective pores). Namely, the hydrate lattice is treated as a rigid porous solid substrate (i.e., H$_2$O molecules are fixed in their positions, not allowed to move) where an adsorption site can be positioned anywhere within a hydrate cage belonging to the hydrate lattice. To this end, MC simulations have been performed with either in-house or open-source software (e.g., MCCCS Towhee[610]). While studies using GCMC simulations consider H$_2$O molecules fixed in space, Brumby et al.[633] reported MC simulations in the GE (Section 3.3.1.1), allowing isotropic volume change moves (i.e., H$_2$O movement) in

addition to the regular MC moves, and reported good agreement with the counterpart GCMC studies.[248]

To determine the average occupancy $\theta$ (i.e., average number of $H_2$ molecules per cavity) for every cavity type, each $H_2$ molecule is assigned to the cavity center whose center is the closest. For a hydrate structure that contains $k$ types of cavities with $n_{i,k}$ cavities of type $i$ together with $N_w$ water molecules in a single unit cell, the gas ($H_2$) content, expressed as weight percentage (wt.%), is given by

$$(\text{wt. \%}) = \frac{MW_g \cdot \sum_{i=1}^{k} n_{i,k} \cdot \theta_i}{MW_g \cdot \sum_{i=1}^{k} n_i \cdot \theta_i + N_w \cdot MW_w} \times 100 \quad (58)$$

where $MW_g$ and $MW_w$ are the molecular weights of the guest gas (g) and water (w), respectively. In the more general case where a promoter (i.e., guest that contributes in hydrate formation under more favorable $P$ and $T$ conditions) is also present in the hydrate structure, the term $n_p \cdot \theta_p \cdot MW_p$ needs to be added to the denominator of Eq. (58), where it is assumed that the promoter has a molecular weight $MW_p$ and occupies the cavities of type $p$, with an average occupancy $\theta_p$. Usually it is assumed that all of the promoter-designated cavities are fully occupied by a single promoter molecule, therefore, $\theta_p = 1$.

The basic input for a GCMC run is the chemical potential of the adsorbate, which can be calculated via different methods. During the earlier hydrate-related MC studies, a simpler approach was utilized that was based either on (i) the use of general-purpose, cubic EoS,[634−637] which largely failed at computing the chemical potentials of $H_2$ at the conditions of interest for storage in hydrates since they were not developed using $H_2$ data, or (ii) on component-specific[638,639] EoS, which partially solved this problem. Later MC studies[248,341,640,641] used a more refined approach for the calculation of the chemical potential and the correlation of chemical potential to the pressure of the system. In particular, a series of MC simulations of bulk $H_2$ in the $NVT$ ensemble is performed from which the virial pressure is calculated. In a subsequent step, the excess chemical potential is calculated with WTPI[617] as explained in Section 3.3.1.3. The reference value of chemical potential, $\mu_0$, is calculated from an additional $NVT$ run where all interactions are set to zero. The chemical potential is, thus, calculated as a function of pressure, at a constant temperature. This approach is more reliable and self-consistent than using EoS, however, it requires additional computational resources. In this way, each run corresponds to a certain $H_2$ density and for this density the pressure and chemical potential are calculated from the appropriate equations. This procedure allows for the determination of the relation between pressure and chemical potential, while simultaneously, provides the EoS for $H_2$. Additional details regarding the methodology can be found in refs 248 and 641.

The separation of gas mixtures (e.g., $H_2/CH_4$ and $H_2/CO_2$) via hydrate formation is based on the principle that the different components of the gas mixture have a different distribution within the hydrate crystal compared to the original mixture composition. Therefore, a series of GCMC simulations can be performed at different $P$ and $T$ conditions to calculate the separation efficiency of the hydrate-based process. The simulation protocol is identical to the one described for the calculation of the hydrate gas storage capacities, applied however for the gas mixture, instead of the pure $H_2$ gas.

### 3.3.4. Heat Capacities, Thermal Expansivity, Joule−Thomson Coefficient, and Speed of Sound from Ensemble Fluctuations.

Thermal expansivity ($\alpha_P$), isothermal compressibility ($\beta_T$), isobaric heat capacity ($C_P$), isochoric heat capacity ($C_V$), and the Joule-Thomson coefficient $\mu_{JT}$ are derivative properties defined in classical thermodynamics as pressure or temperature derivatives.[571,642,643] These thermodynamic properties of $H_2$ gas or for multi-component $H_2$ systems at high pressures are computed using the so-called ensemble fluctuations in molecular simulations.[47,51] For the computation of heat capacity, ones needs to consider both the ideal and the residual contributions[644,645]

$$C_P(T, P) = \left(\frac{\partial \langle H \rangle}{\partial T}\right)_P = C_P^{id}(T) + C_P^{res}(T, P) \quad (59)$$

where

$$C_P^{res}(T, P) = \frac{1}{k_B T^2}[\langle U^{ext}\hat{H}\rangle - \langle U^{ext}\rangle\langle\hat{H}\rangle + P(\langle V\hat{H}\rangle - \langle V\rangle\langle\hat{H}\rangle)] - Nk_B \quad (60)$$

where $N$ is the number of molecules in the system. Eq. (60) is derived by using the enthalpy, $H$,[645]

$$H = H^{id} + H^{res} \Rightarrow$$
$$H = U^{int} + K + Nk_B T + U^{ext} + PV - Nk_B T \Rightarrow$$
$$H = \hat{H} + K \quad (61)$$

where $H^{id}$ and $H^{res}$ are the ideal and residual parts of $H$, and $K$ is the kinetic energy. $C_P^{id}$ can be obtained from thermodynamic reference tables[643,646] or quantum mechanical calculations.[53,647]

Thermal expansivity ($\alpha_P$) and isothermal compressibility ($\beta_T$) from ensemble fluctuations follow from

$$\alpha_P = \frac{1}{\langle V \rangle}\left(\frac{\partial \langle V \rangle}{\partial T}\right)_P = \frac{1}{k_B T^2 \langle V \rangle}(\langle V\hat{H}\rangle - \langle V\rangle\langle\hat{H}\rangle) \quad (62)$$

$$\beta_T = -\frac{1}{\langle V \rangle}\left(\frac{\partial V}{\partial P}\right)_T = -\frac{1}{k_B T \langle V \rangle}(\langle V^2\rangle - \langle V\rangle^2) \quad (63)$$

Having obtained $\alpha_P$ and $\beta_T$, one can also calculate the isochoric heat capacity from

$$C_V = C_P - \frac{T\langle V\rangle\alpha_P^2}{\beta_T} \quad (64)$$

The Joule−Thomson coefficient ($\mu_{JT}$) and speed of sound ($c_{sound}$) follow from

$$\mu_{JT} = \left(\frac{\partial T}{\partial P}\right)_H = -\left(\frac{\partial H}{\partial P}\right)_T \frac{1}{C_P} = \frac{1}{c_P}\left[T\left(\frac{\partial v}{\partial T}\right)_P - v\right] = \frac{v}{c_P}[T\alpha_P - 1] \quad (65)$$

and

$$c_{sound} = \sqrt{\frac{c_p}{c_V \times \beta_P \times \rho}} \quad (66)$$

where $c_P$, $c_V$ and $v$ are the specific heat capacities and the specific volume, respectively. In principle, the same fluctuation-based formulas and methods used to compute thermodynamic properties in MC simulations also apply to MD simulations performed in the same ensemble (e.g., see ref 308). Another example of using ensemble fluctuations in MD simulations is

the study by Rahbari et al.[94] where partial molar volumes and partial molar enthalpies of water in Nafion membranes were computed at different water uptakes.

It is noteworthy that for multi-component systems, the analytical expressions for thermodynamic derivatives based on fluctuations become increasingly complex. In such cases, using alternative methods such as the multiple linear regression are more practical and conceptually straightforward as shown by Rahbari et al.[648].

### 3.3.5. Hydrogen Diffusivity in Metals via Kinetic Monte Carlo.

KMC provides a framework for simulating H diffusion across experimentally relevant time scales (nanoseconds to seconds) while retaining atomistic resolution of individual hopping events.[649,650] The method is transferable across crystal structures. Here we illustrate with bcc and fcc lattices (such as Fe and Ni), though only the site topology and hop catalog require modification for other lattices. The simulation protocol begins by constructing a periodic supercell containing all symmetry-inequivalent interstitial sites (tetrahedral, octahedral) and defect traps (vacancies, dislocations, GBs). Each site $i$ is assigned a solution energy $E_i^{sol}$ from DFT or validated potentials. For each allowed transition $i \rightarrow j$, the CI-NEB calculations[651] are used to determine the saddle-point energy $E_{i \rightarrow j}^{\dagger}$, while harmonic transition-state theory yields the prefactor $\nu_{i \rightarrow j}$ (or a representative $\nu \approx 10^{13}$ s$^{-1}$ when phonon calculations are unavailable).[652] Symmetry operations reduce equivalent hops to a minimal set stored for reuse. The hop rate follows from

$$k_{i \rightarrow j} = \nu_{i \rightarrow j} \exp\left[-\frac{E_{i \rightarrow j}^{\dagger} - E_i}{k_B T}\right] \tag{67}$$

where $E_i = E_i^{sol} + E_i^{int} + E_i^{\sigma}$ combines solution, interaction (H-H or H-defect), and optional elastic terms. The residence-time algorithm proceeds by: (1) selecting events proportionally to their rates using $u_1 K$ ($u_1 \in (0, 1]$, $K = \sum_m k_m$), (2) advancing time by $\Delta t = -\ln u_2 / K$ ($u_2 \in (0, 1]$), (3) updating affected rates and heap structure, and (4) recording observables. The diffusivity is computed using the method described in Section 3.2.3, while trap statistics emerge from waiting-time distributions at defect sites.

A fundamental limitation of conventional KMC is its dependence on a predefined event catalog, in which all possible hops and their associated barriers must be known in advance. This requirement is tractable in pristine bcc or fcc lattices or for simple defects such as isolated vacancies, where diffusion pathways can be exhaustively enumerated. However, it becomes prohibitive in materials exhibiting a rich variety of local environments, such as H at complex GBs or dislocation cores, and is further exacerbated in chemically disordered systems like high-entropy alloys (see Section 4.11.6), where the combinatorial explosion of distinct atomic configurations yields effectively infinite diffusion paths and barrier values. Two strategies promise to remove this bottleneck. (i) On-the-fly KMC (for example using the kinetic Activation-Relaxation Technique) triggers a local saddle search whenever the system enters a new atomic environment, stores the resulting barrier under a topological fingerprint, and reuses it on subsequent visits.[653] (ii) Machine-learning-assisted KMC trains a surrogate model (neural network) on a modest set of barriers from DFT or highly accurate interatomic potentials, predicts activation energies from local descriptors during the run.[468,654] These adaptive workflows dispense with a static catalogue and make

KMC practical for H diffusion in chemically and structurally heterogeneous micro-structures.

GCMC (see Section 3.3.2), on the other hand, can be an efficient pre-equilibration method for multi-scale diffusion studies. GCMC "teleports" H atoms directly into deep traps such as vacancies, dislocation cores and GB sites, thereby establishing the equilibrium occupancy that ordinary diffusion would approach only after long KMC or MD times.[552] To generate KMC-ready H distributions one first fixes the external chemical potential $\mu_H$ (or the equivalent gas pressure) and builds a simulation cell, starting with a defect-free lattice to calibrate bulk solubility and later expanding it to include vacancies, dislocations, GBS or precipitates. A cavity-biased grand-canonical Monte Carlo (CB-GCMC) pre-equilibration then accelerates sampling: the lattice is scanned once to catalogue genuine interstitial cavities, after which each MC sweep attempts three move types, namely (i) small displacements of existing H atoms, accepted according to the Metropolis criterion; (ii) insertions of H atoms restricted to the pre-identified cavities; and (iii) deletions of cavity-hosted H atoms, with both insertion and deletion accepted or rejected by the grand-canonical rule. The thermodynamically consistent, trap-filled configurations produced by CB-GCMC can be used for subsequent MD simulations that target H-affected deformation such as crack propagation[553] and dislocation motion,[550] allowing those simulations to focus on the relevant kinetics rather than spending computational time on equilibration.

## 4. REVIEW OF THERMOPHYSICAL PROPERTIES OF HYDROGEN SYSTEMS COMPUTED WITH MOLECULAR SIMULATION

As discussed in Section 2, reliable thermophysical property predictions are essential for the design and optimization of all major $H_2$ processes, i.e., water electrolysis, compression, storage, transportation, liquefaction, and underground sequestration. The relevance of data derived from molecular simulations lies both in the ability to extract physical insight from molecular structures and interactions, and in the reduction of required experimental measurements under hazardous or challenging conditions, e.g., high pressures or toxic environments. To this extent, the use of molecular simulation in the process design of $H_2$ systems can greatly strengthen engineering workflows by providing reliable data on-demand. Here, we compile an extensive review of the available literature on classical molecular simulation of both pure $H_2$ and of $H_2$ systems involving other gases, liquids, and solids. Our discussion spans VLE of aqueous and non-aqueous $H_2$ solutions, electrolyte systems, thermophysical properties, transport coefficients, and interfacial phenomena. Due to the extended body of literature reporting properties of $H_2$ combined with porous and 2D materials (studied via both classical and quantum simulation methods), we limit the respective part of our review to mostly materials useful in UHS, hydrates, polymeric/composites, and metals. Nevertheless, a short overview of $H_2$/membrane/nanoporous systems is provided, espcecially in light of the new advancements in the field exploiting ML and AI approaches.

### 4.1. Thermodynamic and Transport Properties of Aqueous Hydrogen Solutions

#### 4.1.1. Vapor–Liquid Equilibrium, Fugacity, and Henry Coefficients of Aqueous Hydrogen Solutions.

**Table 9. Representative List of Phase Equilibrium Calculations of H$_2$-Containing Systems Using Molecular Simulations, Along with Relevant Details on Systems, Force Fields, Conditions, and Methods[a]**

| | | System Details | | Thermodynamic Conditions | | |
| Year | Study | System | Force Fields | Pressure | Temperature | Simulation Method |
|---|---|---|---|---|---|---|
| 1993 | Buch and Devlin[661] | H$_2$O(s), H$_2$(g) | Buch[661] | | 12 K | Diffusion MC, Path Integral MC |
| 1994 | Buch[312] | (para-D$_2$)$_3$(ortho-D$_2$)$_{10}$ and (para-D$_2$)$_{13}$ clusters | Buch[312] | | 1-3 K | Path Integral MC |
| 1998 | Rzepka et al.[322] | H$_2$(g), Carbon Slitpores, Carbon Nanotubes(s) | Rzepka (H$_2$) | 10-30 MPa | 50-600 K | GCMC |
| 1999 | Darkrim et al.[327] | N$_2$(g), H$_2$(g), Graphite(s) | Darkrim[327] | 0-600 MPa (N$_2$: 0-500 MPa, H$_2$: 0-60 MPa) | 77 and 293 K | GCMC |
| 2001 | Cracknell[311] | H$_2$(g), Graphitic Nanofibres (GNFs)(s) | Buch,[312] Cracknell[311] | 1-112 bar | 298 K | GCMC |
| 2005 | Urukova et al.[662] | CO$_2$(g), CO(g), H$_2$(g), [bmim][PF$_6$](l) | Cracknell[311] | Up to 9 MPa | 293 - 393 K | GE |
| 2007 | Ferrando et al.[323] | H$_2$(g), n-Alkanes(g), Iso-Alkanes(g), Alkenes(g), Cycloalkanes(g), Aromatics(g), Polyaromatics(g) | Hirschfelder,[321] Corresponding State, Darkrim,[327] Cracknell | 20.1-1200 bar | 160-664.1 K | GE |
| 2018 | Köster et al.[48] | H$_2$, N$_2$, H$_2$O, Ar, O$_2$ | Vrabec, Marx[310] | Up to 304.5 MPa | 83.15-625 K | NPT, $\mu$-VT |
| 2019 | Rahbari et al.[110] | H$_2$(g), H$_2$O(l) | Hirschfelder,[321] Buch,[312] Vrabec,[48] Cracknell,[311] Marx[310] | 10-1000 bar | 283-423 K | CFCMC |
| 2020 | Salehi et al.[663] | CO$_2$(g), H$_2$S(g), CH$_4$(g), CO(g), H$_2$(g), N$_2$(g), ChClU(l), ChClEg(l) | H$_2$ (Cracknell[311]), GAFF (ChClEg), OPLS (ChClEg) | 1 bar | 328 K | CFCMC |
| 2021 | Rahbari et al.[47] | H$_2$(g), H$_2$O(l), Ice Ih(s) | TIP3P, Modified TIP4P (TIP4P$\mu$); Marx,[310] Vrabec,[48] Cracknell,[311] Buch,[312] Hirschfelder (H$_2$) | 50-1000 bar (VLE: 100-1000 bar) | 264.21-423.15 K | CFCMC |
| 2021 | Liu et al.[664] | CO$_2$(g), SO$_2$(g), N$_2$(g), CH$_4$(g), H$_2$(g), Ionic Liquid(l) | Cracknell[311] OPLS-AA (ILs) | 1 bar | 300 K | NPT(MD)-GCMC |
| 2022 | Caviedes et al.[324] | H$_2$(g), Carbon nano-pores(s) | Rzepka (H$_2$(g)), Steele,[665] Tjatjopoulos[666] and Siderius-Gelb[667] potentials for pore interactions | 0.1-35 MPa | 298.15 K | GCMC |

[a]The data also contain non-aqueous systems for completeness.
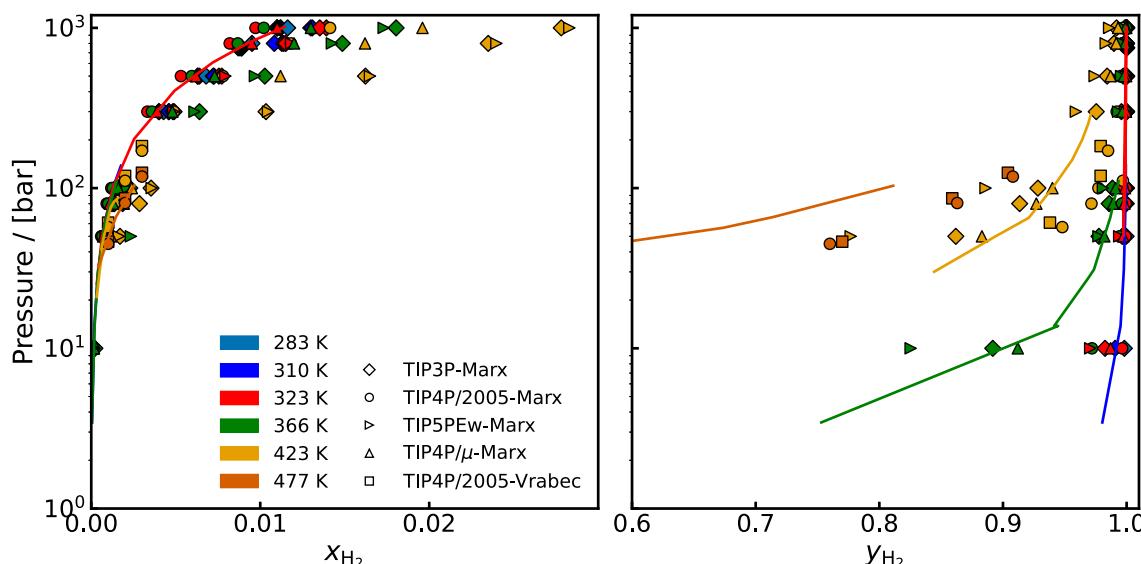
**Figure 18.** Isothermal phase diagram of the water-hydrogen system computed from molecular simulations, as reported in refs 47, 48, and 110. The solid lines represent experimental data. Simulation parameters and force field details are provided in refs 47, 48, and 110.
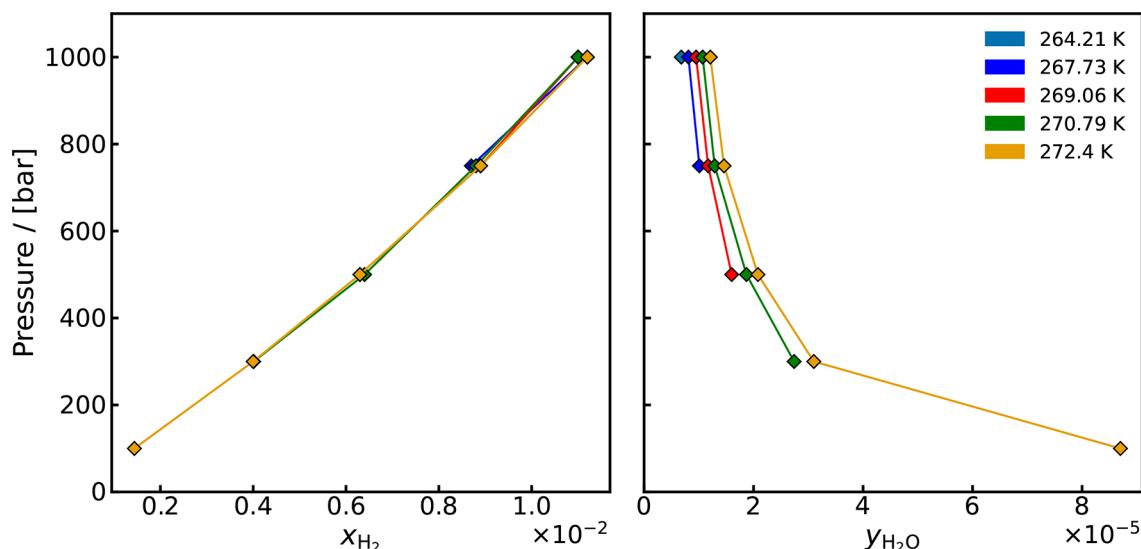


**Figure 19.** VLE of water hydrogen along the melting line of ice and higher pressures than the corresponding equilibrium pressure. The force field combination shown is TIP3P-Marx. The lines connecting the markers are drawn to guide the eye.

The knowledge of VLE of aqueous $H_2$ solutions is essential for the design and optimization of electrochemical systems and storage processes. In water electrolysis, the gas stream exiting the electrolyzer or separator tank typically consists of $H_2$ saturated with water vapor. Accurate determination of the partial pressure of water in $H_2$ is therefore critical for the design of downstream units such as knockout drums or dryers. Conversely, the solubility of $H_2$ in water or aqueous electrolyte solutions is necessary for modeling concentration gradients within the electrolyte phase, for instance when calculating gas crossover. An overview of representative molecular simulation studies reporting phase equilibria data of $H_2$ systems is provided in Table 9. The table includes both aqueous and non-aqueous systems (e.g., $H_2$-hydrocarbon systems) to provide the reader a view of the available literature.

Rahbari et al.[110] computed densities and fugacities of pure $H_2$, the VLE of $H_2$-water systems covering temperatures of 310, 323, 366, and 423 K, and pressures ranging from 10 to 1000 bar, and VLE at low temperatures along the melting line of ice $I_h$, corresponding to a temperature range of 264.21-272.4 K.[47] This low-temperature regime is particularly relevant for evaluating the thermodynamic behavior of $H_2$-water mixtures in refueling stations utilizing electrochemical compression. Several rigid, non-polarizable force fields were used in the CFCGE and CFC*NPT* ensembles (see Section 3.3.1.4). In the study by Köster et al.,[48] the Grand Equilibrium method (see methodology in Section 3.3.1.6) was used to calculate the VLE of binary $H_2$-water at 423 and 477.59 K for pressures in the range of 57 to 125 bar, as well as ternary mixtures of $N_2$-Ar-$H_2$ (which are discussed in Section 4.2). The solubilities of $H_2$-water systems at high pressures reported in refs 47, 48, and 110 are compiled in Fig. 18.

It is evident that experimental solubility data at elevated pressures remain limited. Available high-pressure solubility and VLE data have been compiled and reported in ref 110. For the gas phase, solubility measurements used for validation are in

the following pressure ranges: 50-300 bar at 423 K, 3.45-110 bar at 366 K, 50-1013 bar at 323 K (the widest pressure range), and 3.44-138 bar at 310 K. For the liquid phase, experimental solubility data span 20-87 bar at 423 K, 3-110 bar at 366 K, up to 1013 bar at 323 K, and 3.45-138 bar at 310 K. These data, as visualized in Fig. 18, serve as a benchmark for evaluating the performance of various force field combinations in reproducing VLE behavior across different thermodynamic conditions. The raw solubility data from molecular simulations, used in Fig. 18, are provided in the Supporting Information of refs 47, 48, and 110 for several $H_2$ models, including Hirschfelder,[321] Vrabec,[48] Buch,[312] the two-site model of Cracknell,[311] and the multi-site model of Marx.[310] Fig. 18 shows that the TIP3P and TIP4P/$\mu$ (see Section 4.1.2.1) water models, when combined with the Marx force field for $H_2$, yield the best agreement with experimental gas-phase solubility data. For the liquid phase, solubilities are most accurately captured using the TIP4P/$\mu$ combined with the Marx force field;[47] however, this comes at the cost of reduced accuracy in predicting liquid water densities compared to the TIP4P/2005 model. These findings underscore that while specific force field combinations can be tuned to yield accurate phase composition predictions, this often involves trade-offs with other thermophysical properties.

In ref 47, the TIP3P and TIP4P/2005 force fields were used to compute the VLE of the $H_2$-water system along the ice melting line and at elevated pressures. The results are presented in Fig. 19. TIP3P was selected in that study due to its superior performance in reproducing gas-phase compositions, as previously demonstrated by Rahbari et al.[110] Given the low solubility of water in $H_2$ at low temperatures, the mole fractions of water are plotted in Fig. 19 (right panel), rather than showing the $H_2$ mole fraction, which approaches unity under these conditions. This representation is particularly relevant for applications involving deep-freezing of $H_2$, such as at refueling stations, where accurate knowledge or prediction of water content at low temperatures is essential. No experimental data were found in published literature for the $H_2$-water system at such high pressures, highlighting the value of molecular simulation as a powerful predictive tool to estimate VLE behavior where experimental data are lacking. For this, appropriately validated force fields is a prerequisite.

A notable advantage of the CFCMC method for VLE calculations is that in addition to determining phase coexistence, it enables direct sampling of the excess chemical potentials of each component in both phases through random walks in $\lambda$ space. This facilitates the calculation of fugacity coefficients and Henry's law constants within the same simulation framework. The fugacity coefficients of pure $H_2$-calculated using the CFC$NPT$ ensemble-and fugacity coefficients of $H_2$ in the gas phase from VLE simulations using the CFCGE or CFC$NPT$ ensembles are presented in Fig. 20. As discussed earlier, fugacity coefficients and Henry's law constants are obtained inherently in these methods by introducing a fractional molecule and performing random walks in $\lambda$ space.

$H_2$ solubilities in the liquid phase obtained from the excess chemical potential, can be reported in form of Henry coefficient. The Henry coefficient (in units of bar) in ref 48 was computed using the following thermodynamic relation:

$$H = \rho k_B T \exp(\mu^{\text{inf}}/(k_B T)) \tag{68}$$
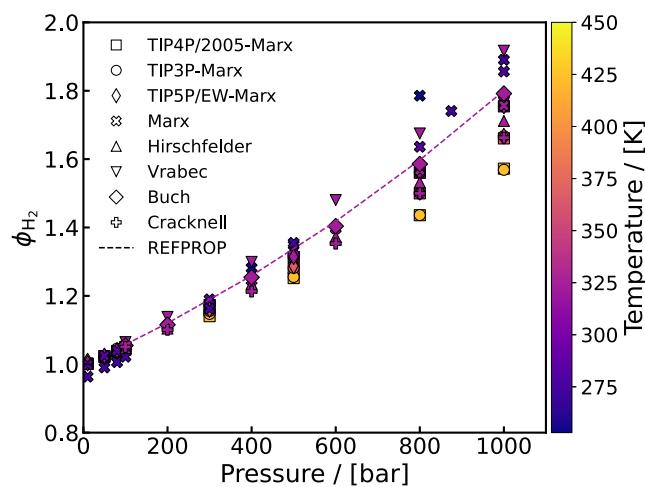


**Figure 20.** Fugacity coefficients of hydrogen computed for different force fields as a function of pressure. The data are obtained from legacy raw simulation data in refs 47 and 110 which have not been previously published, except for pure hydrogen at 323 K. As a reference, the fugacity coefficient of hydrogen at 323 K from REFPROP[352] is shown.

where $\mu^{\text{inf}}$ is the excess chemical potential at infinite dilution and $\rho$ is the saturated liquid density of the solvent. In the MD simulation study by Zhang et al.[655], the Henry constant is reported in units of bar$^{-1}$ and is calculated using

$$H_{\text{MD}} = \frac{\exp(-\mu^{\text{inf}}/(k_B T))}{\rho k_B T}. \tag{69}$$

Henry's law coefficients for $H_2$ in water reported by Köster et al.[48] were obtained over a broad temperature range of 280-625 K. These results exhibit the characteristic non-monotonic temperature dependence of $H_2$ solubility, with a clear maximum in the Henry's constant between 330 and 370 K, indicative of the low solubility of $H_2$ in water at intermediate temperatures. Zhang et al.[655] also calcualted the Henry coefficient of $H_2$ for different force fields of water and $H_2$ using MD simulations combined with the WTPI method (see Section 3.3.1.3).

Henry coefficients reported by Köster et al. and Zhang et al. are presented in Fig. 21. To ensure consistent units in the figure, the reported Henry coefficients by Zhang et al.[655] were converted to units of GPa. For completeness, the original correlation by the authors, valid at 273-433 K and 1 bar, is provided here as well:

$$H[\frac{x_{H_2}}{\text{bar}}] = 2.0369 \times 10^{-4} - 1.4628 \times 10^{-6}T$$
$$+ 3.6181 \times 10^{-9}T^2 - 2.8405 \times 10^{-12}T^3 \tag{70}$$

Experimental data compiled from refs 656 and 657 as cited by Zhang et al., are labeled as Exp. 1 in Fig. 21, while additional Henry coefficients reported by Zhang et al.[655], based on data from Alvarez,[658] are labeled as Exp. 2. The Exp. 1 dataset demonstrates internal consistency and excellent agreement with molecular simulation results. In contrast, the data from Alvarez significantly deviate from the other two sources, and are thus, distinguished as a separate experimental set, i.e., Exp. 2. Zhang et al. reported that the combination of TIP4P/2005 for water and the hydrogen model by Yang[325] yields excellent agreement with the Exp. 1 dataset. However, their reported
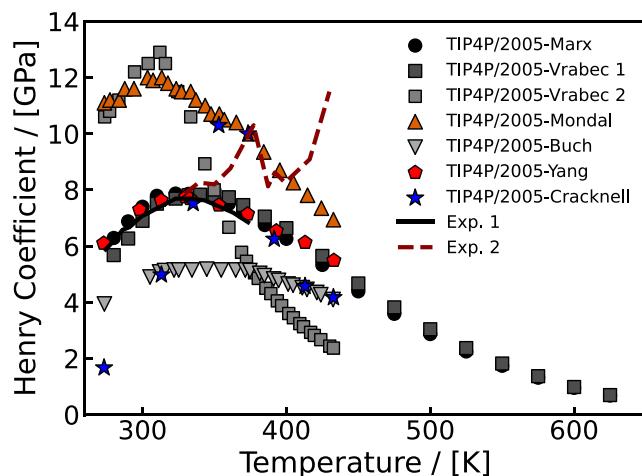
**Figure 21.** Henry coefficient of hydrogen in water as a function of temperature and pressure were compiled from refs 48 and 655. In ref 48, the Henry coefficients were calculated over a temperature range of 280-625 K. Zhang et al.[655] employed the TIP4P/2005 water model in combination with various hydrogen force fields, including those by Buch, Mondal, Yang, Cracknell, and Vrabec. To differentiate between the datasets corresponding to the TIP4P/2005-Vrabec force field combination, the results from Köster et al. are referred to as the first set, while those reported by Zhang et al. are designated as the second set. Exp. 1 are experimental data from refs 655−657 and Exp. 2 from refs 655 and 658.

Henry coefficients based on the TIP4P/2005-Vrabec force field combination show inconsistencies when compared to those by Köster et al., whose results align well with the experimental data. The $H_2$ force fields developed by Buch and Mondal reproduce the temperature dependence observed in the experimental data but systematically overpredict solubility across the entire temperature range. Nevertheless, both models are able to quantitatively capture the peak in the Henry coefficient between 300 and 350 K. Thermodynamic and structural properties of $H_2$ gas in bulk water computed via MC simulations have also been reported by Sabo et al.[659,660]

### 4.1.2. Vapor−Liquid Equilibrium of Aqueous Hydrogen Electrolyte Solutions. 
Obtaining accurate thermody-

namic properties of aqueous electrolyte solutions is considered one of the most challenging modeling problems in applied thermodynamics due to the complex interactions between the dissolved ions and the solvent.[668−671] Nevertheless, this is highly relevant for developing $H_2$ technologies, which often involve electrolytes, e.g., alkaline solutions in electrolysis cells. Typical salts encountered in $H_2$ applications are NaCl, NaOH, and KOH. For example, the solubility of $H_2$ in aqueous NaCl solutions is relevant for underground storage of $H_2$, and therefore, the prediction of accurate data at high temperatures (up to 500 K) and pressures (up to 1000 bar) is central.[630,672]

The reduction in the solubility of non-polar gasses in water in the presence of salts (ofter referred to as the salting-out effect) is a well-established phenomenon.[656,673,674] The salting-out effect of $H_2$ in aqueous solutions has also been studied using molecular simulations.[112,113,630,672,675] van Rooijen et al.,[630] Zhang et al.,[676] Kerkache et al.,[672] and Lopez-Lazaro et al.[675] computed the solubility of $H_2$ in concentrated NaCl solutions using MC simulations. Lopez-Lazaro et al.[675] and Zhang et al.[676] used the WTPI method to estimate the excess chemical potential of $H_2$ in aqueous NaCl solutions (from which $H_2$ solubilities can be computed as discussed in detail in Section 3.3.1). van Rooijen et al.[630] and Kerkache et al.[672] both performed CFCMC simulations to compute excess chemical potentials. As shown in Fig. 22(a), which is a compilation of solubility data from different studies, the $H_2$ solubilities computed using the WTPI[675] have error bars ca. 5 times larger than the solubilities computed using CFCMC calculations.[630,672] This showcases that the gradual insertion using the CFCMC method allows for much better sampling of the excess chemical potentials compared to the WTPI (particularly in the liquid phase). The marginal differences between the solubilities computed in the different studies can be almost solely attributed to the choice of force fields, as discussed thoroughly later on.

It has been shown that scaling down the partial charges of ions can improve the accuracy in predicting thermodynamic and transport properties in systems involving electrolytes.[347,394,395] This holds true also for aqueous $H_2$ electrolyte solutions, where the choice of scaled or un-scaled force fields
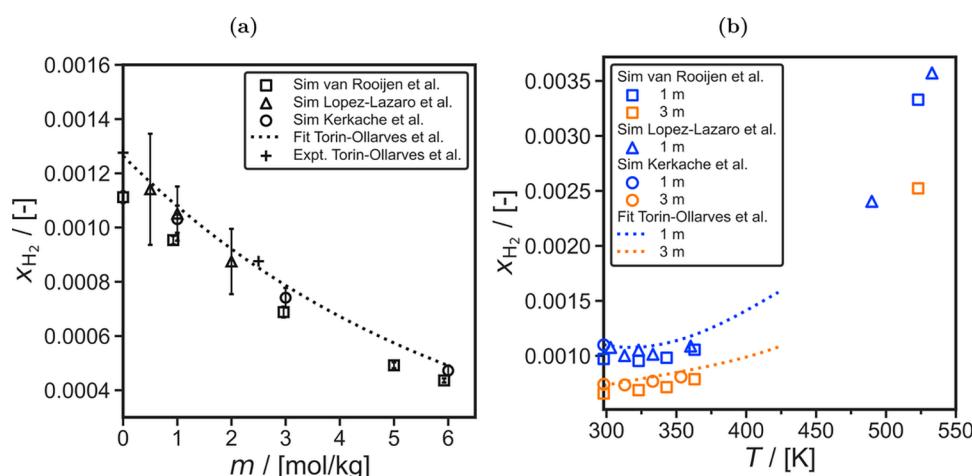


**Figure 22.** Solubilities of $H_2$ ($x_{H_2}$) in aqueous NaCl solutions at a $H_2$ fugacity of 100 bar at (a) 323 K as functions of salt molality $m$ (in units of mol salt / kg water), and (b) as functions of temperature $T$. The MC simulation data of van Rooijen et al.[630] and Lopez-Lazaro et al.[675] are shown. The MC data of Kerkache et al.[672] for solubilities of Marx $H_2$ in TIP4P/2005 water and Madrid-2019[347] NaCl with adjusted interaction parameters ($k_{ij}$ for $H_2$-$H_2O$) is also plotted. The experimental fit of Torin-Ollarves and Trusler[674] is shown for comparison.

plays a dominant role. van Rooijen et al.[630] combined Marx (for $H_2$), TIP4P/2005 (for water), and the Madrid-2019 NaCl force fields. Kerkache et al.[672] tested several different model combinations for $H_2O$ (i.e., TIP4P/2005, SPC/E, and TIP4P/EW), $H_2$ (i.e., Marx, Alavi, and Yang and Zhong), and NaCl (i.e., Madrid-2019, KBF, and OPLS). Madrid-2019 NaCl has scaled charges of +0.85 / -0.85 [e], while KBF and OPLS have charges of +1 / -1 [e]. Kerkache et al.[672] showed that NaCl force fields with un-scaled charges under-predict the solubilities of $H_2$ (thereby over-predicting the salting out effect), especially at higher salt molalities (≥ 4 mol salt / kg water). Lopez-Lazaro et al.[675] and Zhang et al.[676] also showed that the combination of Darkrim $H_2$ force field with TIP4P/2005 water, and OPLS, Joung-Cheatam, Smith, and Dang NaCl force fields (all having un-scaled charges) under-predict the solubility of $H_2$ in aqueous NaCl solutions by ca. 25%. Despite this, behavior of $H_2$ solubilities as a function of temperature is correctly predicted in refs 675 and 676. To accurately model the salting out of $H_2$ in aqueous NaCl solutions, Lopez-Lazaro et al.[675] adjusted the LB mixing rules for $Na^+$-$H_2$ and $Cl^-$-$H_2$. Madrid-2019 NaCl force field with scaled charges of +0.85 / -0.85 [e] was shown to perform accurately in predicting the salting out of $H_2$ in aqueous NaCl solutions without any further fitting of mixing rules as shown in Fig. 22 and discussed in refs 630 and 672.

Habibi et al.[112] computed the solubilities of $H_2$ and $O_2$ in aqueous KOH and NaOH solutions using the scaled charge force fields Madrid-Transport ($K^+$ and $Na^+$) and the DFF/$OH^-$ (developed in the same study). The authors performed CFCMC simulations at a temperature and pressure range of 298-353 K and 1-100 bar, respectively. The authors showed that thew newly developed DFF/$OH^-$ model accurately predicts densities and viscosities (5 to 20% deviations) of the aqueous NaOH and KOH solutions up to molalities of 8 mol/kg. The expected salting-out effect with increasing electrolyte concentration was also captured. Engineering equations were fitted using the simulation data for both solubilities and diffusivities of the gases in the aqueous solutions. It is important to note that the solubilities of $H_2$ in water are ca. 1 order of magnitude smaller at a concentration of 8 mol KOH / L solution compared to the solubilities of $H_2$ in pure water. Therefore, the choice of the salt force field is crucial when computing the solubility of $H_2$ in the aqueous phase. This is also the main motivation for heavily discussing the performance of force fields in this section.

Hulikal Chakrapani et al.[677] performed molecular simulations to compute the solubilities of $H_2$-$CO_2$ mixtures in aqueous NaCl solutions over a wide range of pressures (5-50 MPa), temperatures (323.15-423.15 K), and salinities (0-2 molal NaCl). TIP4P/$\mu$,[110] all-atom TraPPE,[678] and Marx[328] force fields were used for water, $CO_2$, and $H_2$, respectively. Using the CFCGE (see Section 3.3.1.1) method, solubilities of $H_2$, $CO_2$, and $H_2O$ were computed by equilibrating chemical potentials between the gas and liquid phases, with a fixed initial 1:1 $H_2$:$CO_2$ gas phase ratio. $CO_2$ solubility in aqueous NaCl solutions increased with pressure and temperature, but decreased with salinity due to the salting-out effect (well captured by the Setschenow equation[679]). The decline in solubility followed a consistent slope of approximately −0.21, independently of pressure and temperature. At low pressures (<10 MPa), $CO_2$ solubility rose linearly, transitioning to a non-linear behavior at higher pressures. Simulations matched

experiments within 5-10% at 423.15 K. Larger deviations were observed at lower temperatures.

In the study of Hulikal Chakrapani et al.[677] $H_2$, solubility increased with temperature across the range 323.15−423.15 K, at all pressures and salt concentrations. However, at a fixed pressure and temperature, the solubility of $H_2$ decreased with increasing salt concentration, exhibiting a Setschenow-type[679] slope of −0.11 to −0.19, corresponding to ca. 15% decrease in solubility per mole NaCl. The simulation results showed good agreement (within 5−10%) with experimental data at 323.15 K, though higher temperatures and pressures led to slight overestimations. In $CO_2 − H_2 − H_2O − NaCl$ systems, $CO_2$ solubility was shown to be lower than in $CO_2 − H_2O − NaCl$ (see Fig. 23a), whereas $H_2$ solubility increased (see Fig. 23b),
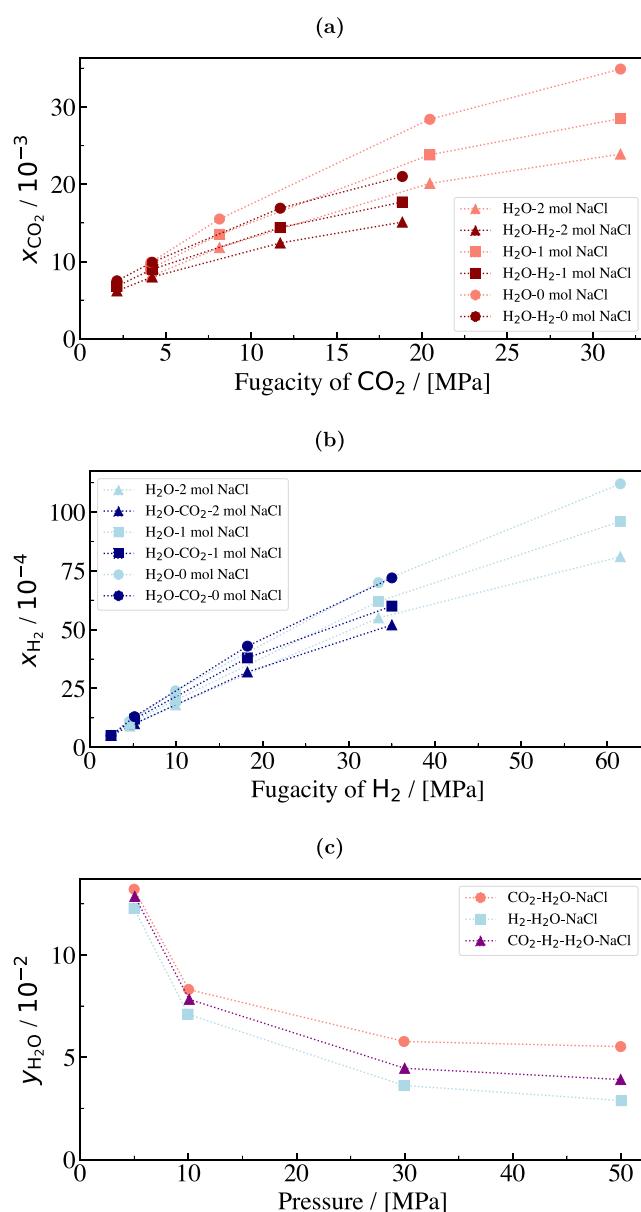


Figure 23. (a) The solubility of $CO_2$ in different aqueous NaCl solutions as a function of $CO_2$ fugacity. (b) The solubility of $H_2$ in different aqueous NaCl solutions as a function of $H_2$ fugacity. (c) The mole fraction of $H_2O$ in the gas phase as a function of pressure for different aqueous NaCl-$H_2$ mixtures. The lines connecting the markers are drawn to guide the eye.

suggesting a cooperative mechanism where $H_2$ promotes its own solubility while suppressing that of $CO_2$. Water content in the gas phase was computed to be between the values observed in the $CO_2$ and $H_2$ aqueous electrolyte systems (see Fig. 23c). At 423.15 K, water content decreased with pressure but showed little dependence on salt concentration. At 323.15 K, the water content remained nearly constant, while at 423.15 K it was found to be 20−40 times greater than the value at 323.15 K, when considered across all pressures.

The solubilities of $H_2$ in aqueous $NaB(OH)_4$ solutions were recently computed using CFCMC simulations at 298−363 K and 1 bar.[113] This electrolyte is relevant for applications related to hydrolysis of $NaBH_4$ solutions for $H_2$ storage. The presence of 5 mol $NaB(OH)_4$ / kg water is shown to significantly reduce both $H_2$ solubilities (by a factor of ca. 0.4) and the activities of water (by a factor 0.75). In a follow up work also focusing on $NaBH_4$ as a $H_2$ energy carrier, Postma et al.[680] developed a new force field (i.e., the DFF/$BH_4^-$, extending the DFF family) performed MD simulations to compute densities and viscosities of $NaBH_4$ (in the range 0 to 5 mol salt / kg water), $NaB(OH)_4$ (0 to 3 m), and 1 m NaOH aqueous solutions at 295 K. The predicted properties were within ca. 2% and 10% from the respective experimental data. The authors used the MD data to devise engineering correlations for densities, viscosities, and self-diffusivities for these systems which can be used as a fast model when data are required for e.g., $NaBH_4$ hydrolysis reactor design.

*4.1.2.1. Force Field Performance and the Effective Charge Surface Approach.* It is observed in the pervious section that obtaining accurate VLE data reequires careful selection of force field combinations for hydrogen and water. The results show that there is not a single combination of classical force fields that can predict all thermodynamic and transport properties accurately. An illustrative example is provided in Fig. 24,
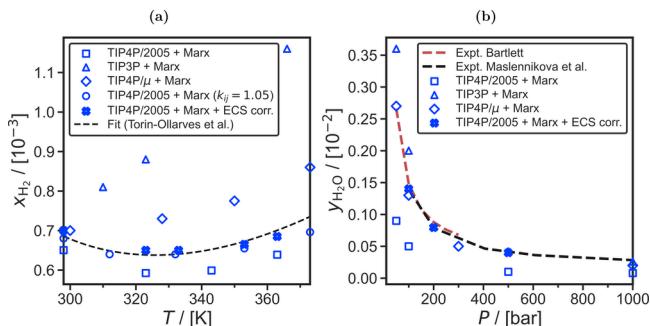


**Figure 24.** (a) Solubilities of $H_2$ (in units of mole fraction $x_{H_2}$) in liquid water at a $H_2$ fugacity of 50 bar as functions of temperature. (b) Solubilities of $H_2O$ (in units of mole fraction $y_{H_2O}$) in gaseous $H_2$ at 323 K as functions of total pressure. The MC data for $x_{H_2}$ and $y_{H_2O}$ for the combination of Marx[310] $H_2$ force field and TIP4P/2005 and TIP3P water is obtained from Rahbari et al.[46] The MC data for $x_{H_2}$ and $y_{H_2O}$ of Marx[310] $H_2$ and modified TIP4P (herein referred to as TIP4P/$\mu$) is obtained from refs 111 and 47, respectively. The MC data of Kerkache et al.[672] for solubilities of Marx $H_2$ in TIP4P/2005 with adjusted interaction parameters ($k_{ij}$ for $H_2$-$H_2O$) is also shown in (a). The MC data for Marx[310] and TIP4P/2005 water force field including the ECS free energy correction as introduced by Habibi et al.[350] is obtained from ref 111. The experimental fit of Torin-Ollarves and Trusler[674] for $x_{H_2}$ and the experimental data of Maslennikova et al.[681] and Bartlett[682] for $y_{H_2O}$ are shown for comparison.

aiming to show the differences in performance as a result of different force field parameterization. Figure 24 shows the solubilities of $H_2$ in liquid water and the solubilities of water in gaseous $H_2$ computed using MC simulations at 323 K and pressures from 10 to 1000 bar.

In ref 110 it is shown that the TIP3P water force field[300] combined with the Marx[310] force field results in accurate predictions for the equilibrium water content in the gas phase but cannot accurately predict the solubilities of $H_2$ in the liquid phase. The TIP4P/2005 water force field and the Marx[310] force field result in accurate predictions for the solubility of $H_2$ in water (and the variations with respect to temperature), but the water content in $H_2$ is under-predicted with respect to experiments (e.g., by a factor of 3 at 323 K).[110] The TIP3P water force field paramters are fitted on the vaporization energy of water, and can thereby correctly predict the experimental vapor pressure of water and the water content in the gas phase.[110,350] The TIP4P/2005[349] water force field parameters are trained on the liquid phase properties such as densities, temperature of maximum density, and transport properties (e.g., shear viscosities of water), and can thereby predict the solubilities of $H_2$ in water (and their temperature dependence) accurately with respect to experiments.[110]

In ref 47, a modified version of TIP4P/2005 (i.e., using the same geometry) was employed by scaling the atomic charges by a factor of 0.955, resulting in a dipole moment of 2.2 D. Subsequently, the Lennard-Jones energy parameter $\epsilon$ for oxygen was adjusted to 79.86 K to better match the chemical potential of liquid water. The TIP4P/$\mu$ accurately models the excess chemical potential of water (i.e., with respect to the ideal gas reference state), and results in accurate modeling of the water content in $H_2$. The solubilities of the Marx $H_2$ force field[310] in water at 298 K are also accurately modeled. However, the temperature dependence of $H_2$ solubilities in water are not accurately captured (no minimum is observed in $H_2$ solubilities at ca. 323 K similar to experiments[683]).

The reason why it is difficult to model the VLE of $H_2$ and water systems using non-polarizable water force fields can be traced back to the paper of Berendsen et al.[346] in 1987. Berendsen et al.[346] discussed that non-polarizable water force fields cannot capture both the experimental vaporization energy of water (required for modeling the vapor pressures of water) and the effective interactions that result in accurate predictions of densities (required for modeling the solubility of $H_2$ in water) and transport properties of water, due to "the missing term in effective pair potentials" (i.e., the title of the paper by Berendsen et al.[346]). Recently, Habibi et al.[350] developed a new method in which the TIP4P/2005 water force field is used to model the effective interactions in the liquid phase and an additional effective charge surface (ECS) is used to compute the excess chemical potential of water. The excess chemcial potential of water obtained using the ECS is used to compute a free energy correction for the free energies of TIP4P/2005 at different temperatures. Applying a free energy correction to the partition function of the isolated water molecules allows for accurately computing the excess chemical potentials of water, without compromising the liquid phase properties. As shown in Figure 24 and ref 111 this energy correction can be used to accurately predict both the equilibrium water content in the gas phase and the solubilities of $H_2$ in the liquid phase with respect to experiments. The simulations are performed at 298-423 K, 10-500 bar, 0-6 mol NaCl/kg water, and 0-8 mol KOH/kg water. As discussed in

ref 350 it is important not to model water vapor using non-polarizable water force fields trained on the liquid phase (e.g., TIP4P/2005 and TIP3P), as the second virial coefficients of water vapor (and thereby the excess chemical potentials of water in the gas phase) are not accurately modeled with respect to experiments.[684] It is advised to combine MC simulations with EoS, such that the MC simulations can be used to obtain the liquid phase chemical potentials and free energies and the EoS (such as the GERG-2008[685]) can be used to model $H_2O$-$H_2$ gaseous mixtures.

**4.1.3. Pressure−Volume−Temperature Computations.** Yang et al.[686] performed molecular simulations of aqueous $H_2/CO_2/H_2O$ systems to compute $pVT$ data and densities at conditions close to the supercritical regime, for which no prior experimental data were available. The motivation for this molecular simulation study is the application of supercritical water gasification of coal for energy production, a process in which $pVT$ properties are difficult to measure. The authors state that no experimental, theoretical, or simulation studies exist regarding the $pVT$ properties of $H_2O$-$H_2$-$CO_2$ mixtures in the near-critical and supercritical regions of water. They tested both the Cracknell and Buch force fields for hydrogen, but the results presented in the paper are based on the Cracknell force field. In their $H_2O$-$CO_2$ binary-mixture validation, the authors report that the absolute average error of the PR EoS and MD simulation is 15.09% and 0.66%, respectively. Thus, the adopted MD simulation model appears to have significantly better predictive accuracy than the PR EoS in near-critical and supercritical regions of water. However, for the $H_2O$-$H_2$ binary system, they note that no experimental research has investigated the $pVT$ properties of $H_2O$-$H_2$ mixtures under those conditions. Therefore, their MD results are only compared against Peng-Robinson calculations, with no direct experimental benchmark for $H_2O$-$H_2$ in the near-critical and supercritical regimes. The pressure calculations obtained for binary $H_2O$-$H_2$ and ternary $H_2O$-$H_2$-$CO_2$ mixtures are shown in Fig. 25. Temperatures vary from 673 to 973 K, and the mole fractions of hydrogen range from 0.05 to 0.20. The results obtained from MD simulations are potentially more accurate and can provide more insight than the PR EoS.

**4.1.4. Thermal Expansivity, Heat Capacity, Joule-Thomson Coefficient, and Speed of Sound of Aqueous Hydrogen Mixtures.** As discussed in Section 3.3.4, isothermal compressibility, thermal expansivity, heat capacity, speed of sound, and the Joule-Thomson coefficient are thermodynamic properties which can be computed from ensemble fluctuations in molecular simulations.[571,642,643] Alternatively, these properties can be calculated using the multiple linear regression method which have been shown to be mathematically equivalent.[648]

The study by Rahbari et al.[47], mainly motivated from electrochemical compression systems, focused on the effect of trace amounts of water on the thermodynamic properties of compressed $H_2$ using MD simulations. The authors computed thermal expansivity, heat capacity, Joule-Thomson coefficients, partial molar volumes and enthalpies and the VLE of pure $H_2$ and aqueous $H_2$ mixtures. The $H_2$-water data were obtained from a prior study by the authors[110] where equilibrium compositions were sampled at 366 - 423 K, and pressures up to 1000 bar. Importantly, the isothermal compressibility data were retrieved from the legacy simulation data in ref 47 and are presented in this review for the first time (Fig. 26 upper). TIP3P model was used for water, while a new force field, i.e.
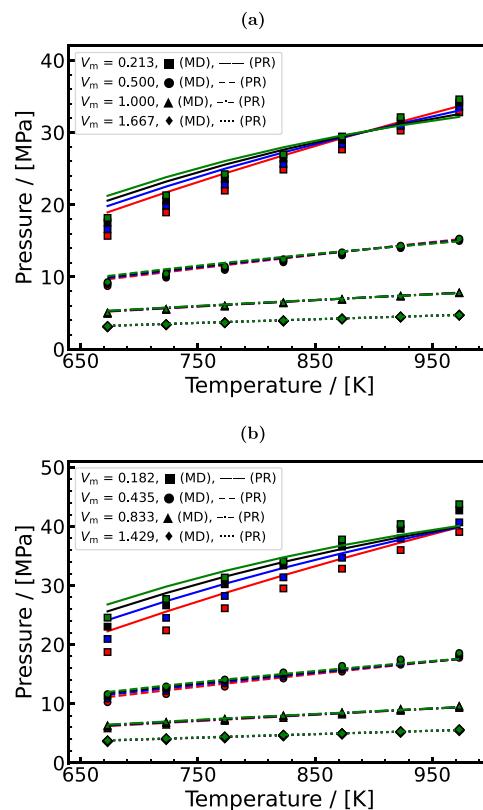


**Figure 25.** Pressure-temperature relation of (a) binary $H_2O$-$H_2$ mixtures and (b) ternary $H_2O$-$H_2$-$CO_2$ mixtures at different hydrogen mole fractions and molar volumes. MD simulation results are compared with predictions from the Peng-Robinson EoS. The different colors of the lines and markers correspond to different mole fractions of hydrogen (red: $x_{H_2}$=5%, blue: $x_{H_2}$=10%, black: $x_{H_2}$=15%, and green: $x_{H_2}$=20%).

TIP4P/$\mu$ was developed to yield improved solubilities (for more details the reader is referred to the Supporting Information of ref 47 and Section 3.1.2). $H_2$ was modelled with different force fields, with Marx showing the best overall performance. The molecular simulation results clearly indicated that at low pressures, the water content has significant influence on the thermodynamic properties of the $H_2/H_2O$ mixtures (i.e., a positive Joule-Thomson coefficient for $H_2O - H_2$ mixtures and a negative value for pure $H_2$ mixtures at 423 K and 50 bar).[47] The effects become less pronounced as pressure increases, and become negligible above 700 bar. All computed properties (for different force field combinations) are shown in Fig. 26 along with available data from NIST (REFPROP92[352]) for pure $H_2$. These results underline the importance of accounting for trace water content when modeling hydrogen systems for storage and energy applications.

Bartolomeu and Franco[308] developed a single-site force field for $H_2$ using the SAFT-$\gamma$ Mie potential, and validated it against existing LJ-type models (both 1-site and 2-site) for predicting thermophysical properties of supercritical $H_2$. Similarly to the study by Rahbari et al.,[47] the motivation of this study was high-pressure EHC applications. The authors reported both thermodynamic (i.e., densities, isochoric and isobaric heat capacities, thermal expansion coefficients, isothermal compressibilities, joule-Thomson coefficients, and speed of sound) and transport properties (i.e., diffusivities, viscosities, and thermal
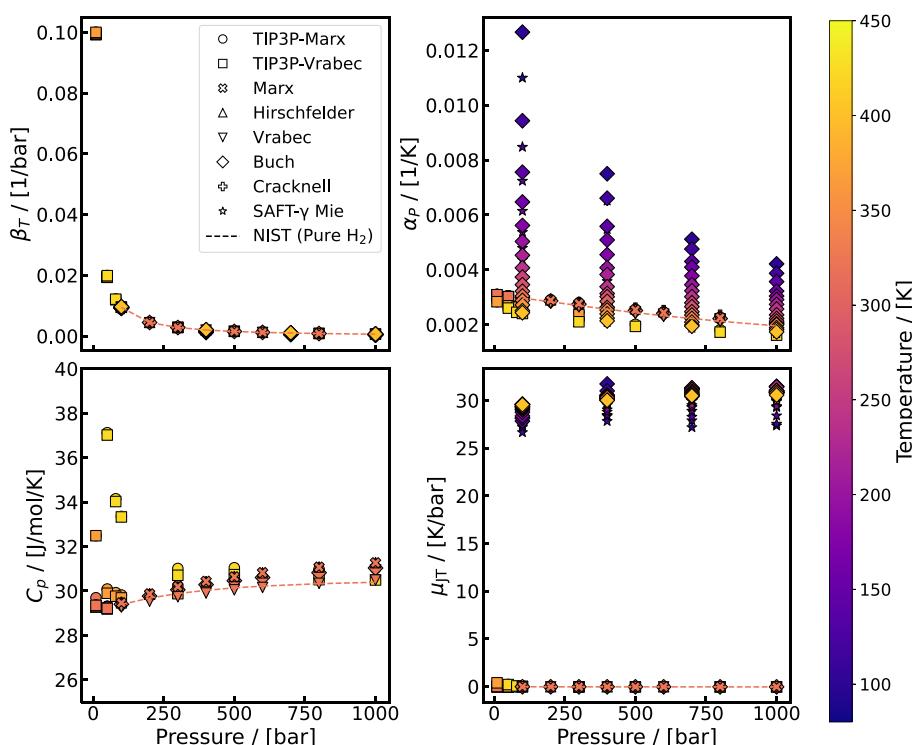
**Figure 26.** Comparison of different force fields in predicting the isothermal compressibility (top left), thermal expansivity (top right), isobaric heat capacity (bottom left), and Joule-Thomson coefficient (bottom right) of pure hydrogen in the gas phase over a pressure range of 10 to 1000 bar. Experimental data from NIST (REFPROP92[352]) are shown as lines. Raw simulation data are provided in the Supporting Information of ref 47. The error bars are smaller than the symbol size. For force field combinations with TIP3P, representing a gas phase saturated with water, the compositions at each temperature are directly taken from VLE simulations in ref 110 where the TIP3P force field was used for water and the Marx force field for hydrogen. The mole fraction of water in saturated hydrogen–water mixtures in the gas phase ranges from 0.004 to 0.138. Raw data from ref 308 were provided by the authors.

conductivities). The data from Bartolomeu and Franco[308] (provided to us by the authors) for the thermodynamic properties are shown in Fig. 26 and Fig. 27. This study emphasized that quantum effects are non-negligible at low temperatures, particularly when the de Broglie thermal wavelength approaches the inter-molecular distance or when the simulation temperature is below the rotational temperature of hydrogen (86 K). The authors observed that while a classical treatment may be acceptable for temperatures above 200 K, below this threshold, classical models increasingly deviate from experimental reference data. Among the tested models, the SAFT-γ Mie (which is a force field developed in the same study[308]) yielded the lowest average deviations, attributed to its softer repulsive potential and EoS-consistent parameterization, despite the absence of explicit quantum corrections.

### 4.1.5. Self-Diffusivity of Hydrogen in Aqueous Electrolyte Solutions.
As discussed in detail in Section 2.1, reliable data of $H_2$ diffusivities in the aqueous phase are essential for the design and optimization of $H_2$ electrochemical systems such as water electrolyzers and fuel cells.[71] The diffusion of $H_2$ in the aqueous phase influences the bubble formation and growth rates, which in turn influence the ohmic resistance of the aqueous electrolyte and reduces the active electrode area.[71] The self-diffusivity of $H_2$ is also a relevant property in supercritical water gasification for conversion of biomass to fuel gasses.[687] Obtaining self-diffusivities of $H_2$ (and other gasses) at high pressures and temperatures (e.g., supercritical conditions) requires cumbersome and expensive
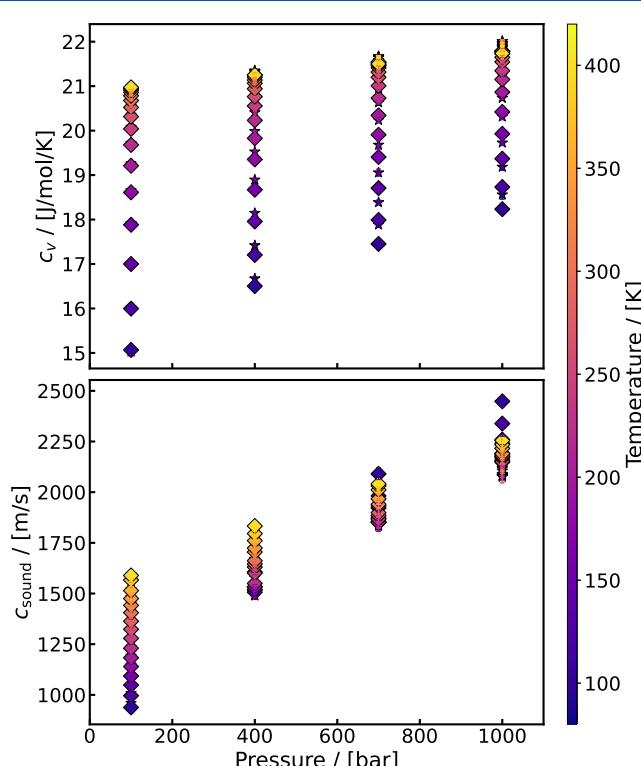


**Figure 27.** Isochoric heat capacity (top) and speed of sound (bottom) of supercritical hydrogen from ensemble fluctuations from MD simulations. Raw data from ref 308 was provided by the authors.

experiments. Thus, molecular simulations have been widely used for obtaining these data over a large temperature and pressure range.[688,689] The relevant methods are described in Section 3.2.

Fig. 28 shows the temperature and pressure conditions for which data (MD and experimental) of $H_2$ self-diffusion
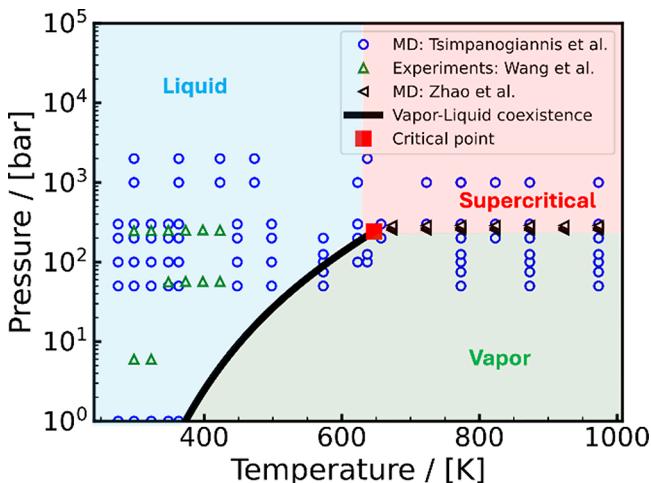


**Figure 28.** State points for which self-diffusivities of $H_2$ in water are available in literature. Experimental data ranges are from Wang et al.[690] which is the largest experimental dataset available. MD simulation data ranges are from the studies of Tsimpanogiannis et al.[688] and Zhao and Jin.[687]

coefficients in water are available.[687,688,690] The experimental dataset of Wang et al.[690] spans the most state points compared to the rest of the available experiments.[690] Additional experimental data at low pressures (0.1 MPa) have been collected and reported in ref 688. To the best of our knowledge, no experimentally measured self-diffusivities of $H_2$ in supercritical water are reported in open literature. Zhao and Jin[687] computed the diffusivity of $H_2$ in supercritical water while Tsimpanogiannis et al.[688] performed MD simulations to compute the diffusivities of $H_2$ and $O_2$ in water up to pressures of 2000 bar and 975 K. Kallikragas et al.[691] computed the diffusivity of $H_2$, $O_2$, OH radical, and $H_2O$ in liquid water at a temperature range of 298 - 973 K and water densities spanning 0.1 g cm$^{-3}$ to 1 g cm$^{-3}$. Since small gas molecules such as $H_2$ are sparsely soluble in liquid water (i.e., mole fractions of ca. $10^{-5}$ at 298 K and a $H_2$ pressure of 1 bar[112]), simulations of $H_2$ are often performed at near infinite dilution.[687,688,691] Therefore, to a great extent, the behavior of the solvent (e.g., density, viscosity) is the one dictating the diffusivity of the gas. This means that the choice of the water force field is crucial in these studies because the properties of the solvent need to be accurately modeled over a wide temperature and pressure range. Tsimpanogiannis et al.[688] and Zhao and Jin[687] used TIP4P/2005,[692] while Kallikragas et al.[691] used SPC/E. Both these water force fields perform well in modeling the density, viscosity, and self-diffusivity of liquid water.[345,348,692−694] As discussed in Section 3.1.2, TIP4P/2005 and SPC/E are rigid, non-polarizable force fields, ca. 3−10 times more computationally efficient than polarizable force fields.[354,355,695] The computational efficiency of non-polarizable force fields is a significant advantage compared to polarizable ones or quantum mechanical simulations (e.g., Born-Oppenheimer MD) for generating large datasets for transport properties of $H_2$ in

aqueous mixtures. Polarizable force fields have been used by Śmiechowski[314] (i.e., AMOEBA combined the $H_2$ force by Śmiechowski[314]) to compute the diffusion of $H_2$ and $H_2O$ in liquid water. However, these computations were carried out only at 298 K, and were not the main focus of the work by Śmiechowski[314] (i.e., calculation of Raman spectra for the hydrated $H_2$).[314]

To model $H_2$, Tsimpanogiannis et al.[688], used six different force fields for (i.e., Buch,[312] Marx,[310] Vrabec,[48] Cracknell,[311] Silvera-Goldman,[335] and Hirschfelder[321] $H_2$ force fields - see relevant discussion in Section 3.1.1). Depending on the $H_2$ model, the self-diffusivities varied by ca. 20−30%. Though this is a notable variation, it is comparable to the error of experimentally measured $H_2$ diffusivities found in literature.[348] The authors concluded that the Buch−TIP4P/2005 force field combination, performs the best, and proceeded in producing a wide range of data for $H_2$ and $O_2$ self-diffusivities in $H_2O$ as shown in the Arrhenius-type plot of Fig. 29. Based on these
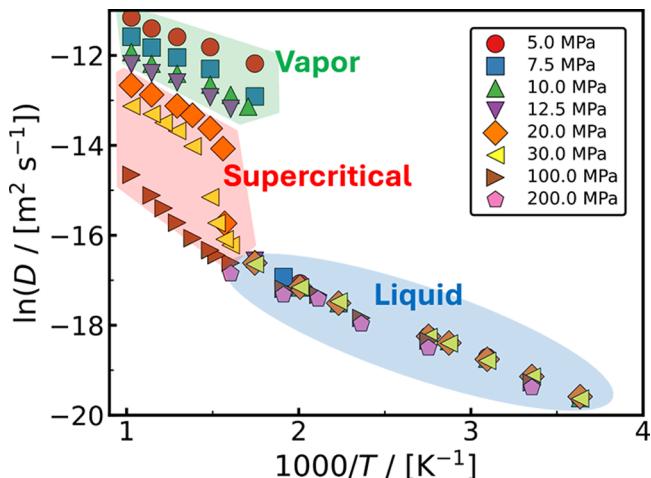


**Figure 29.** Arrhenius plot of the self-diffusion coefficients of $H_2$ in $H_2O$ computed by Tsimpanogiannis et al.[688] using the Buch[312]−TIP4P/2005[305] force fields. The computed diffusion coefficients are corrected for system-size effects.[498−500] The identified self-diffusivity patterns of the $H_2$ in $H_2O$, in the vapor, liquid, and supercritical regions are highlighted. Data were collected from ref 688.

data, Tsimpanogiannis et al.[688] developed engineering correlations for the regions shown in Fig. 29 corresponding to vapor, liquid, and supercritical conditions. In a follow-up study, Moultos and Tsimpanogiannis[696] revised the proposed correlation of the vapor region to increase the accuracy of predictions for the lower pressure and higher temperature regions.

Available data from experiments and MD simulations for the self-diffusivities of $H_2$ in liquid $H_2O$ have been considered to examine the validity of the Stokes-Einstein relation. Following the steps of Tsimpanogiannis et al.,[697] the analysis performed in ref 698 clearly indicates that the Stokes-Einstein relation is violated for both the experimental measurements and the MD simulation data. It is important to note that $H_2$ self-diffusivities computed from MD simulations are subject to finite-size effects[688] (see the relevant discussion in Section 3.2.3). The magnitude of these effects in the liquid phase depends on the temperature, number of molecules, and viscosity, as shown in Eq. (15).[498−500] The finite-size effects for diffusivities of $H_2$ in the aqueous phase are in the range 3-15% based on the studied

by Tsimpanogiannis et al.,[688] Habibi et al.,[112] and Śmiechowski.[314] Accounting for these effects is necessary to ensure the reproducibility of the MD data.

In a recent study Kerkache et al.,[699] investigated $H_2$ diffusivity in water and NaCl brine over a wide range of thermodynamic conditions, including temperatures from 298 to 473 K, pressures from 1 to 1000 bar, and salt molalities up to 6 mol salt/kg solvent, focusing on self-diffusion coefficients relevant to infinitely diluted $H_2$ in aqueous solutions; the study primarily addressed $H_2$-$H_2O$ and $H_2$-$H_2O$-NaCl systems. The results indicated that $H_2$ self-diffusion coefficients decrease with increasing salinity, for example from approximately $6.0 \times 10^{-9}$ m²/s in pure water to ca. $4.2 \times 10^{-9}$ m²/s at 6 mol/kg NaCl at 323 K and 200 bar, and increase with temperature and slightly decrease with pressure. No data on mutual diffusivities for $H_2$-$CH_4$ or $H_2$-$CO_2$ mixtures were provided. The physical mechanism underlying these findings is linked to the increasing structuring of the solvent and ions around the $H_2$ molecule, reflected by more negative two-body excess entropy values with higher salinity and pressure, leading to higher viscosity and thus lower diffusivity, while temperature weakens solvent structuring and enhances $H_2$ mobility. The solvent viscosity, accurately captured by the TIP4P/2005 water model combined with the Madrid-Transport salt force field, was found to be the dominant factor influencing $H_2$ diffusivity, consistent with the fractional Stokes-Einstein relation, having an exponent of ca. 0.83. The computed diffusion coefficients were compared qualitatively to limited experimental data available for $H_2$ diffusion in pure water and low salinity brine, showing good agreement in trends though experimental data remain sparse and uncertain at higher salinities and pressures. Finally, the study proposed both a fractional Stokes-Einstein model and an Arrhenius-type empirical correlation for $H_2$ self-diffusivity as functions of temperature, pressure, and NaCl molality, providing a reliable predictive framework for underground $H_2$ storage applications.

Molecular simulations have also been used to compute the diffusivity of $H_2$ in concentrated aqueous NaCl, NaOH, KOH, and $NaB(OH)_4$ solutions.[112,113,630,680] The data collected from literature are shown in Fig 30. These electrolyte solutions are primarily relevant for water electrolysis and $H_2$ storage (see
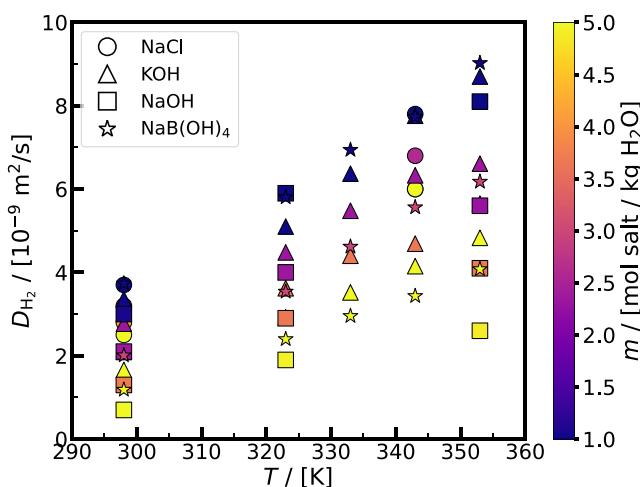
also Section 2.1). As in the simulations of $H_2$/water systems discussed earlier, it is important to choose salt/water force field combinations that can accurately model the densities and transport properties of the aqueous electrolyte solvents. For example, salt force fields that cannot capture the change in viscosity as a function of salt molality, it is expected that they also fail in modeling the diffusivity (and other properties) of $H_2$, ions, or water at different salt loadings.[630] Blazquez et al.[700] has shown that non-polarizable force fields of NaCl and KCl that correctly predict the density and viscosity of the aqueous solution can accurately describe the diffusion coefficients of Na⁺, K⁺, Cl⁻, and water. Similarly, Avula et al.[701] has shown that for predicting the anomalous increase in the water diffusivities in aqueous CsI solutions, the decrease in solution viscosities needs to be accurately captured. The data reported in the Supporting Information of van Rooijen et al.[630] show that the Madrid-2019 NaCl[370] force field overestimates the solution viscosities by ca. 20% at the solubility limit compared to Madrid-Transport,[384] and therefore, underestimates the diffusivities of $H_2$ in the aqueous solution.

### 4.1.6. Electroosmotic Drag Coefficient.

Din and Michaelides[127] computed EOD within a cylindrical pore examining both a flow of water molecules or ions, and the case of no macroscopic flow in the channel. The interactions between water molecules and wall atoms, and the interactions between hydrogen atoms (protons) and wall atoms were determined based on the work of Zhu and Robinson.[702] Din et al. established a linear connection between the EOD coefficient and water uptake. For $\lambda \in [7.65, 10.9, 12.2, 20.9]$, the EOD computed equals $[7.34, 10.5, 12.0, 19.6]$, respectively. These results are shown in Fig. 31. The overestimation of the EOD
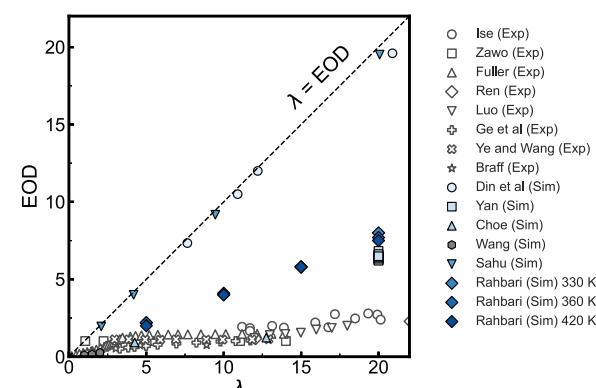


**Figure 31.** Electro-osmotic drag coefficients from MD simulations and experiments as a function of the hydration level, $\lambda$ (defined in Eq. (31)). The dashed line denotes the ideal case where EOD equals $\lambda$, serving as a reference. Data are compiled from refs 92, 94, 98, and 127−129.

possibly arises from the simplified pore model used in the simulations, which assumes uniform wall charge, straight cylindrical pores, and neglects structural complexity of the membrane. As a result, the simulations allowed for more water to be dragged by protons than what is observed in experiments with membranes. In addition, the proton hopping mechanism is missing from the model of the authors.

Yan et al.[128] performed atomistic MD simulations to compute the EOD coefficient with electric fields (up to 2 V/$\mu$m) for $\lambda = 20$. All-atom force-fields were used to model the hydrated PFSA oligomers, water molecules, and $H_3O^+$.[128,703]



**Figure 30.** Self-diffusivities of $H_2$ in aqueous NaCl, KOH, NaOH, and $NaB(OH)_4$ solutions at different temperatures and salt molalities at 1 bar. The data are collected from refs 112, 113, and 630.

**Table 10. Summary of Studies Calculating the EOD from Molecular Dynamics Simulations**

| | | System Details | | Thermodynamic Conditions | | |
|---|---|---|---|---|---|---|
| Year | Study | Phases | Force Fields | Electric Field V/Å | Temperature | Method |
| 1998 | Din et al[127] | Nafion(s), $H_2O$(l), $H^+$(aq) | SPC/E, $H^+$,[127] Wall atoms (Nafion) | 0.0592 to 0.3809 | 298 | NEMD |
| 2008 | Choe et al.[129] | Nafion(s), $H_2O$(l), $H_3O^+$(aq) | SPC/E, Nafion (Dreiding, UFF) | 0.05 | 363 | NEMD/Ab initio |
| 2008 | Yan et al.[128] | Nafion(s), $H_2O$(l), $H_3O^+$(aq) | TIP3P, $H^+$,[127] Nafion | 0.02 to 0.05 | 287.15-364.65 | NEMD |
| 2022 | Wang et al.[98] | Nafion(s), $H_2O$(l), $H^+$(aq) | SPC/E, Nafion (AMBER/GAFF) | 0.0001 to 0.0005 | 350 | NEMD |
| 2022 | Rahbari et al.[94] | Nafion(s), $H_2O$(l), $H_3O^+$(aq) | PCFF (Class II), COMPASS (partial charges) | 0.02, 0.05, 0.075, 0.100 | 330, 360, 420 | NEMD |
| 2025 | Sahu et al. | Nafion(s), $H_2O$(l), $H_3O^+$(aq), $Cu^+$, $Cu^{2+}$, $Cl^-$ | TIP4P/2005 ($H_2O$), DFT-derived charges (Nafion), LJ + Coulomb (ions), Nafion model from TURBOMOLE | 0.00, 0.02, 0.05, 0.075, 0.10 | 298 | NEMD (classical MD) |

Every backbone comprised four side chains terminated with sulfonic acid groups. The EOD coefficient was computed using two approaches: one based on average transport velocities, and the other on peak shifting velocities. Both methods yielded comparable results.[128] The EOD was computed over a temperature range of 287.15 K to 364.65 K, showing no significant temperature dependence. An average value of 6.41 was obtained. These values are notably higher than most experimental values as shown in Fig. 31. The authors attributed this overestimation to the absence of proton hopping in their model, which omits the dissociation of O-H bonds, and therefore, excluding a major transport mechanism. While the authors suggested a correction, the discussion was and not further supported by additional simulations or quantitative analysis. The proposed correction was, thus, a qualitative estimate rather than a rigorously derived result, limiting the strength of the comparison with experimental values.

Choe et al.[129] computed the EOD coefficient of water at $T = 363$ K for $\lambda$ values ranging from 4.25 to 12.75. Under a uniform electric field, the EOD coefficients were extracted from ab initio MD trajectories, yielding values of 0.92 and 1.23 for $\lambda = 4.25$ and $\lambda = 12.75$, respectively. These results are consistent with experimental measurements, as shown in Fig. 31. The model system comprised two Nafion monomers arranged around a central water cluster in a sandwich-like structure, with hydrophilic tails facing the water. The proton from the sulfonic acid end group was modeled as a hydronium ion. The Dreiding force field was used for intra-molecular interactions within Nafion, and UFF was applied for nonbonded interactions with water and hydronium (for more information on these force fields the reader is referred to Section 3.1.4). Classical MD simulations were first used to generate equilibrated configurations, which then served as initial states for AIMD. The authors attributed the nearly constant EOD across hydration levels to two opposing effects, i.e., the increased proton hopping at higher hydration, which tends to lower the drag, and the enhanced water mobility beyond the hydration shell, which tends to raise it. These effects largely offset each other, resulting in the observed invariance of the EOD with respect to water content. The study by Choe et al.[129] clearly demonstrates that combining ab initio calculations with classical MD enables a more accurate representation of the underlying transport physics (as also recently shown in ref 105). Although this review does not elaborate on QM methods, it is worth noting that such approaches are necessary for accurately predicting $H_2$ properties in electrochemical systems.

Rahbari et al.[94] computed the EOD coefficient for hydrated Nafion membranes at water contents $\lambda \in [5, 10, 15, 20]$ and temperatures between 330 and 420 K. The data reported in this study are shown in Fig. 31. The electric fields applied were in the range 0.05 to 0.10 V/Å while the velocity ratio of water to $H_3O^+$ ions was determined across different field strengths. PCFF and COMPASS force fields were used to model all interactions. This study showed that the average velocities of both species scaled linearly with the electric field, resulting in a constant velocity ratio and a linear dependence of EOD on hydration level. The EOD increased with $\lambda$, reaching up to 7.5 at $\lambda = 20$ and 420 K, while showing a slight decrease with temperature. As in the prior studies using classical force fields, proton hopping was not modeled, thus, limiting the accuracy of the computed EOD at high hydration. Nevertheless, the results at lower $\lambda$ aligned better with experiments as can be observed in Fig. 31.

Wang et al.[98] conducted classical MD simulations to compute the EOD in Nafion membranes with low hydration levels $\lambda = 1, 1.5$, and 2 at $T = 350$ K. The computed EOD coefficients were 0.098, 0.149, and 0.255, respectively. Electric fields ranging from 0.001 to 0.005 V/nm were applied, and EOD coefficients were determined from the average velocities of water and $H_3O^+$. The results are in excellent agreement with the linear model $EOD = \frac{2.5}{22}\lambda$, confirming the assumption made by Springer et al.[704] that EOD varies linearly with water content at low hydration. This finding is also in line with most experimental and simulation data at low water contents as shown in Fig. 31. Similarly to the prior classical studies, ss the hopping mechanism was not included, the calculated EOD reflects only vehicular proton transport.[94,556] The authors showed that EOD approaches zero as water content vanishes.

The linear increase of the EOD coefficient with hydration level, as predicted by classical MD simulation studies,[94,127] was also confirmed by Sahu and Ali.[705] Consistently with the prior studies, the approach did not include the Grotthuss mechanism (proton hoping). As a result, the computed EOD values were shown to overestimate experimental data, particularly in well-hydrated systems. This overestimation is further amplified by the use of high electric field strengths. The EOD values reported by Sahu et al. are shown in Fig. 31.

In summary, several studies have investigated the EOD in hydrated membranes using molecular simulations (see Table

10), providing valuable insights into the underlying transport mechanisms and associated limitations. Collectively, these studies show that while classical force fields can qualitatively reproduce trends in EOD, quantitatively accurate predictions, particularly at high hydration, require explicit modeling of proton hopping and a more realistic description of membrane nanostructure. It is also important to note that there remains considerable variability among experimental EOD measurements; however, a detailed discussion of experimental inconsistencies is beyond the scope of this review. Nevertheless, the major differences and systematic trends between simulation and experimental data can still be identified.

### 4.1.7. Reactive Systems and Membrane Properties Related to Hydrogen Research.

Despite the fact that in this review we primarily focus on the computation of thermophysical properties using classical molecular simulations, in many $H_2$ processes chemical, reactions cannot be ignored to obtain reliable predictions.[706] To this purpose, reactive MD and MC simulations allow for the study of chemical reactivity by explicitly modeling bond formation and breaking, providing a pathway towards understanding complex phenomena in $H_2$ (and many other) systems. These methods are particularly useful for studying the VLE of reactive systems, the internal workings of MEAs in fuel cells and electrolyzer cells, or any $H_2$ system where chemical reactions play a crucial role.[707−710] An important example in the context of $H_2$ systems is the application of reactive MD in modeling ion-exchange membranes, where proton hopping mechanisms, the lifetime of $H_3O^+$, and the dynamic behavior of reactive species in electrolyte environments are central mechanisms.[118] Unlike classical MD, which relies on predefined force fields (see Section 3.1), reactive MD uses techniques that allow for changes in molecular topology during the simulation. Reactive MD can be implemented within different modeling frameworks, including hybrid quantum-classical models, fully classical approaches, and quantum-based reactive force fields.[707,711]

The prediction of thermodynamic and transport properties of $H_2$, $H_3O^+$, and protons in MEAs (see Section 2.1) also requires the use of combined classical/reactive molecular modeling approaches. Relevant properties in such systems include ion diffusion, electrical conductivity, membrane structure, EOD, and thermal conductivity. As discussed in the previous section, accurate modeling of the membrane, serving as the medium for $H_2$ transport, is essential for understanding and optimizing system performance. Although a detailed analysis of MEAs lies outside the main scope of this review, selected membrane properties relevant to $H_2$ applications are discussed here to illustrate the depth of insight that can be obtained via molecular simulations.

The review by Arntsen et al.[93] explores the application of reactive MD simulations to study proton transport in polymers commonly used in fuel cells (Nafion 3M and Hyflon). The authors particularly highlight the Multistate Empirical Valence Bond (MS-EVB) method, which can capture the Grotthuss mechanism that classical non-reactive MD simulations fail to model. The application of MS-EVB simulations revealed an anti-correlation between vehicular and Grotthuss transport mechanisms. This anti-correlation was already hinted in Section 4.1.6 and Fig. 31 where our analysis of the collected simulation results revealed that excluding Grotthuss mechanism leads to overpredicting the EOD. The review by Arntsen et al.[93] demonstrates how $H^+$ conductivity computed from MS-

EVB simulations aligns more closely with experimental data,[93] showcasing the accuracy of the MS-EVB method. This study not only captured proton hopping, but also proposed a transport mechanism in which $H^+$ primarily pass between sulfonate groups, rather than diffusing through the bulk water region.

Awulachew and Nigussa[115] conducted MD simulations of MEAs encountered in fuel cells considering $Pd_3Ag$ electrodes as alternatives to Pt electrodes. Self-diffusion coefficients were computed using the Einstein approach (see Section 3.2.3) to determine $H^+$ conductivity, while coordination numbers were obtained from radial distribution functions. The conductivity values obtained were comparable to, but slightly higher than, those reported in the literature. A benchmark comparison was performed, and it was concluded that the combination of a Nafion membrane with a $Pd_3Ag$ electrode offers an efficient and cost-effective solution for MEAs. The authors discussed the influence of hydrogen bonding and temperature on $H^+$ mobility. The authors proposed that including interaction effects between $H^+$, the electrode, and the electrolyte improves the computation accuracy of $H^+$ conductivity. Cui et al.[116] performed classical MD simulations of hydrated Nafion membranes at hydration levels corresponding to $\lambda$ = 3.44, 5.42, 8.63, and 11.83. Water clustering and $H_3O^+$ diffusion were analyzed as functions of hydration. This study revealed that increasing water content promotes the formation of a connected aqueous network composed of interlinking water channels. Based on the molecular structure, the formation of Eigen-type ions is proposed as hydration increases. The authors attribute the low $H^+$ conductivity at low water contents to the disconnected morphology of the water network.

Venkatnathan et al.[117] performed MD simualtions to compute the density and diffusion coefficient of $H_3O^+$ in a nafion membrane at hydration levels $\lambda$ = 3.5, 6, 11, 16, and temperatures of 300 and 350 K. Consistently with the prior studies, diffusion coefficients were underestimated due to the lack of proton hoping in classical MD framework. The effects of hydration on the structure and vehicular transport of ions and the mobility of water molecules in Nafion membrane were discussed. The authors proposed that $H_3O^+$ ions do not merely act as passive charge carriers but actively shape the local structure of the hydrated Nafion membrane. At low hydration levels, participation of $H_3O^+$ in forming hydrogen bonds constrains the mobility of sulfonate, effectively affecting the morphology of the membrane. As hydration increases, these constraints are relaxed due to enhanced solvation, allowing sulfonate groups and $H_3O^+$ to become more spatially separated.

Hofmann et al.[118] performed reactive MD simulations to compute the diffusion and conductivity of oxygen and hydrogen ions in hydrated Nafion membranes at $\lambda$ = 6 and $\lambda$ = 12. The simulations indicated shorter $H_3O^+$ lifetimes at higher hydration levels. The authors proposed that the time−determining step for proton transfer is the formation of a precursor complex (Zundel-type) prior to rapid proton hopping. This study also showed that the conductivity significantly exceeds the value expected from self-diffusion alone, highlighting the role of collective proton motion. This is reflected in a reduced Haven ratio at higher hydration, indicating enhanced correlated transport and increased conductivity.

Brunello et al.[120] performed fully atomistic MD simulations to study the structure, sulfonate solvation, density, and water

**Table 11. Brief Overview of Mechanistic Insights Obtained from Molecular Simulation Studies of Hydrated Membranes Relevant to Hydrogen Systems**[a]

| Reference | Property Studied | Key Insights |
| --- | --- | --- |
| Flottat et al.[125] | Water diffusion in Nafion vs. Aquivion | Linear growth of water domains with hydration; earlier percolation in Aquivion; water volume fraction governs structure and dynamics |
| Awulachew and Nigussa[115] | Proton conductivity in MEAs with $Pd_3Ag$ electrodes | H-bonding enhances proton mobility; electrode-electrolyte interaction boosts conductivity; $Pd_3Ag$-Nafion outperforms Pt; simulation exceeds literature values |
| Cha[124] | Side chain length effect on $H_3O^+$ transport | Shorter side chains improve inter-chain mobility and ion conductivity; contradicts some experimental trends |
| Zhang et al.[95] | $H_3O^+$ and $H_2O$ diffusion in Nafion | $Na^+$, $Ca^{2+}$ disrupt water clusters; $Ca^{2+}$ has stronger binding and impact; reduced $H_3O^+$, $H_2O$ mobility |
| Arntsen et al.[93] | Review of proton transport in fuel cell membranes | MS-EVB captures Grotthuss mechanism; anti-correlation with vehicular transport; hopping occurs between sulfonates; matches experiments |
| Ozmaian and Naghdabadi[101] | Glass transition temperature of Nafion | Hydration lowers $T_g$ significantly; hydration gradients lead to heterogeneous degradation behavior |
| Brunello et al.[120] | Water transport in S-PEEK | Water content enhances phase segregation and water channel development; consistent with Nafion trends |
| Lins et al.[122] | Structure and transport in Ph-SPEEKK | Hydration increases sulfonate mobility and spacing; qualitative match with Nafion/SPEEK behavior |
| Hofmann et al.[118] | Proton transfer mechanisms | High $\lambda$ shortens $H_3O^+$ lifetime; precursor (Zundel-type) forms before hopping; collective effects increase conductivity |
| Venkatnathan et al.[117] | Density and diffusion in Nafion | $H_3O^+$ shapes local structure; low $\lambda$ restricts mobility via H-bonding with sulfonates |
| Cui et al.[116] | Water clustering and hydronium diffusion | Hydration enables channel formation; Eigen-ion structures proposed; disconnected morphology limits conductivity at low $\lambda$ |

[a]The table summarizes key findings on structure-transport relationships, ion coordination, and hydration-dependent phenomena in membrane electrode assemblies.

transport in hydrated sulfonated poly(ether ether ketone) (S-PEEK) at temperatures of 298 to 353 K, and $\lambda$ = 4.9 and 11.1. The simulations revealed that temperature has limited impact on sulfonate solvation and morphology, while water content significantly enhances nano-phase segregation and the development of water channels. Water diffusion increased with temperature and hydration, though activation energies remained similar, indicating a consistent diffusion mechanism. While explicit experimental validation is not provided, the authors point to qualitative consistencies with previous findings on membranes such as Nafion and Dendrion, suggesting physically plausible trends in structure and transport behavior.

Lins et al.[122] performed MD simulations of fully sulfonated Ph-SPEEKK to evaluate the influence of hydration level ($\lambda$ = 3.5, 6, 11, 16, 25, 40) on the internal structure of the membrane and $H^+$ transport. The authors computed diffusion coefficients for water and $H_3O^+$, as well as hydrogen bond statistics. In the absence of direct experimental data for Ph-SPEEKK, the pair correlation functions was used to assess sulfonate clustering, which revealed that higher hydration leads to greater sulfonate mobility and separation. While explicit validation was not deemed possible at the time of the publication, qualitative agreement with prior findings on SPEEK and Nafion was noted, particularly in hydration−dependent structural trends and the enhancement of diffusion at higher $\lambda$.

Ozmaian and Naghdabadi[101] computed the diffusion coefficient of water in hydrated Nafion with $\lambda$ = 14 at temperatures ranging from 100 to 600 K. The authors investigated the glass transition temperature ($T_g$) of hydrated Nafion to better understand its thermomechanical stability and performance limits, particularly for applications such as fuel cells and shape−memory devices. This study showed taht increasing hydration significantly lowers $T_g$; for example, at $\lambda$ = 20, $T_g$ = 230 K, while for $\lambda$ = 2, no clear transition is observed below 500 K. Overall, the simulations results show good consistency with experimental $T_g$ values (340 - 350 K). An important insight finding in this study was that membranes with hydration gradients may exhibit heterogeneous thermal and degradation behavior across their thickness, which is relevant for their operational durability.

Cha[124] performed MD simulations to investigate how the morphology of perfluorosulfonic acid (PFSA) membranes, specifically, the length of side chains, affects $H_3O^+$ conductivity in polymer electrolyte membranes (PEMs), which constitutes a key performance factor in fuel cells. The study was motivated by discrepancies between prior simulation and experimental studies, which reported conflicting results on whether shorter side-chains improve conductivity. To address this, Cha[124] developed tracked $H_3O^+$ pathways throughout the simulation. The findings showed that shorter side-chains increase the fraction of conductive $H_3O^+$, and enhance inter-chain ion movement, thus, improving ionic conductivity, contrary to some earlier experimental observations. Despite the motivation of this study, the discrepancies between the simulation and experimental results were not resolved, and follow-up research is proposed.

Flottat et al.[125] conducted MD simulations to elucidate why Aquivion (850 g/equiv) exhibits higher water diffusion than Nafion (850 g/equiv). Motivated by the fact that $H^+$ conductivity depends on the morphology of the hydrophilic water network (which itself is strongly influenced by hydration), the authors investigated how nanoscale structure governs transport properties. The simulations were shown to reproduce experimental trends for membrane density and water diffusion, while a linear increase in water domain size with hydration was obtained, in qualitative agreement with experimental measurements. A key finding was that the transition from isolated to percolated water networks occurs at a lower hydration level in Aquivion than in Nafion, potentially explaining improved diffusion/conductivity under dry conditions. The study also showed that structural and dynamic properties scale with water volume fraction, identifying it as a more fundamental parameter than hydration number.
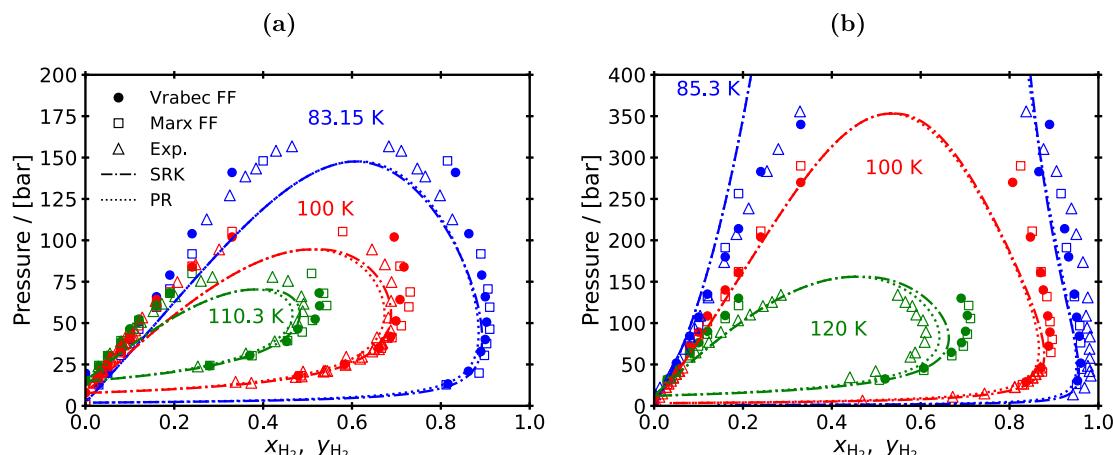
**Figure 32.** Comparison of molecular simulation results with experimental VLE data for the (a) $H_2$-$N_2$ and (b) $H_2$-Ar binary mixtures using the Vrabec and Marx hydrogen force fields, adapted from Köster et al.[48] The experimental data[712−714] are also presented in Köster et al.[48] The PR and SRK predictions are computed with the Open-Source Fluid Thermodynamics Toolkit Clapeyron.[715] The simulation results of $H_2$-Ar at 120 seem to deviate significantly from the experimental results, however, these measurements were performed at 122.73 K instead of 120 K.[714]

Zhang et al.[95] investigated the effects of $Na^+$ and $Ca^{2+}$ ions on the diffusion of $H_3O^+$ and water in Nafion 117 membranes using MD simulations. The study revealed that both cations significantly reduce $H_3O^+$ and water diffusivities by associating with sulfonic acid groups and disrupting water cluster connectivity, especially at $\lambda = 16$ and temperatures of 298 and 353 K. $Ca^{2+}$ appeared to have a stronger effect than $Na^+$ due to the higher charge and higher hydration degree, leading to stronger binding with sulfonic groups and greater disruption of water channels. Diffusion coefficients reported for all species confirm that $Na^+$ diffuses more rapidly than $Ca^{2+}$. The decline in $H_3O^+$ and $H_2O$ transport aligned with previous experimental and simulation findings. The computed diffusion of $Na^+$ was also shown to be in line with with the respective experiments.

This section highlighted how molecular simulations can be used to obtain deep mechanistic insights into the transport and thermodynamic behavior of $H_2$-related species in hydrated polymer membranes. By considering water content, temperature, ionomer morphology, and contaminant effects, molecular simulations not only provide a means of computation of diffusion coefficients and conductivities but also reveal nanoscale structural phenomena, such as water channel formation, sulfonate-cation interactions, and the role of hydration in enabling or restricting ionic transport. The representative studies reviewed above demonstrate the power of molecular simulations in studying experimentally inaccessible systems/ conditions, provided that accurate force fields and methods are used.

Table 11 provides a succinct summary of the key insights obtained from the relevant literature. While our focus here was mainly on transport properties which are relevant to $H_2$ applications, molecular simulations can also be used to study other membrane features such as thermal conductivity[126] or the impact of contamination on oxygen transport.[96] These topics lie outside the scope of this review but further illustrate the wide applicability of molecular simulation in membrane research.

## 4.2. Thermodynamic and Transport Properties of Nonaqueous Hydrogen Mixtures

### 4.2.1. Vapor-Liquid Equilibrium of Pure Hydrogen and Binary and Ternary Mixtures of Hydrogen with Argon, Nitrogen, and Carbon Dioxide. Köster et al.[48]

studied various thermophysical properties (including VLE, vapor and liquid densities, and residual enthalpy of vaporization) of binary $H_2$-$N_2$ mixtures using the grand equilibrium method (see Section 3.3.1.6). The simulations were conducted at $T = [83.15, 100, 110.3]$ K, with corresponding pressure ranges of $[(0.196−14.1), (0.794−10.20), (1.51−8)]$ MPa. To model $H_2$, the Vrabec[48] and Marx[310] force fields were used. The results, shown in Fig. 32a, demonstrate that the Vrabec model, which was fitted to $pVT$ and speed of sound data, is in good agreement with experimentally measured VLE data across the whole temperature range considered, outperforming Marx. Deviations are observed as pressure increases. Vapor pressures and saturated liquid densities are accurately captured, particularly at lower temperatures. The Vrabec force field is also shown to yield improved predictions of relative volatilities and residual enthalpies of vaporization compared to Peng– Robinson, SRK, and PC-SAFT EoS (for the PC-SAFT predictions the reader is referred to ref 48), which exhibit significant deviations from reference data in the critical and dense liquid regions. This force field also performs well in predicting homogeneous phase densities of equimolar $H_2$-$N_2$ mixtures under cryogenic and near-critical conditions, with mean absolute percentage errors below 1% in some cases.[48]

In the same study, Köster et al.[48] performed simulations also for $H_2$-Ar binary mixtures to compute the same properties (VLE, densities, and residual enthalpy of vaporization). For this binary mixture, the authors considered $T = [85.8, 100, 120]$ K, with corresponding pressure ranges of $[(0.090−34), (0.331−27), (1.220−15.6)]$ MPa for the Vrabec force field, and $[(0.088−25.644), (0.331−29), (1.220−14.3)]$ MPa for the Marx force field. As shown in Fig. 32b, molecular simulations using the Vrabec[48] force field, demonstrated good agreement with the available experimental VLE data. In particular, the saturated liquid compositions and vapor pressures at cryogenic conditions (90−120 K) are well captured. Although minor deviations were noted in the saturated vapor compositions at lower temperatures, the predictions from the molecular simulations remained within the scatter of the experimental data. Furthermore, in the homogeneous supercritical region, the computed compressibility factors matched experimental values with high accuracy, achieving mean absolute percentage errors below 1% for

pressures up to 9 MPa. These findings highlight the reliability of Vrabec force field in describing both phase behavior and volumetric properties of $H_2$-$N_2$ and $H_2$-Ar mixtures under sub- and super-critical conditions.

Raju et al.[716] computed the VLE of the $H_2$-$CO_2$ binary mixture using molecular simulations in the CFCGE ensemble (see Section 3.3.1.1). The authors compared the simulation results with data from the GERG-2008[685] EoS and available experiments. The results are illustrated in Fig. 33. Notably, the
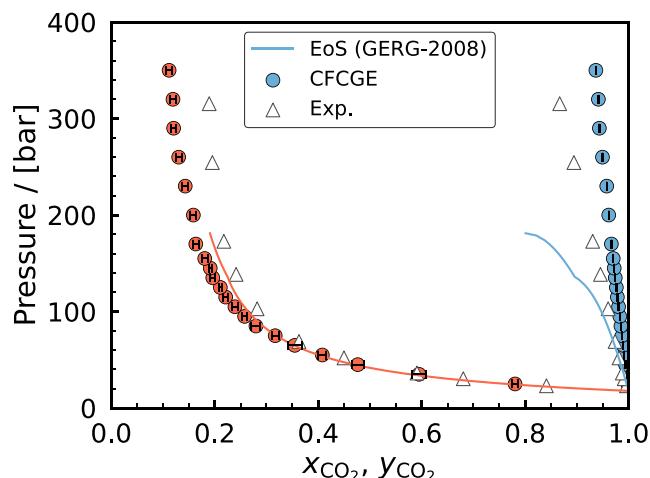


**Figure 33.** Vapor-liquid equilibrium data for the $CO_2$-$H_2$ binary mixture from molecular simulations[716] compared to GERG-2008[685] EoS predictions and experimental measurements.[717]

authors faced convergence issues with GERG-2008 at pressures exceeding 170 bar, as solid lines in Fig. 33 indicate. Moreover, the computed bubble points from GERG-2008 showed significant discrepancies from the experimental measurements. In contrast, the mole fractions obtained from molecular simulations exhibited good agreement with the experimental data by Tsang and Street,[717] with relative deviations remaining below 5% even at elevated pressures.

The VLE of the ternary $H_2$/Ar/$N_2$ system at 100 K was studied by Köster et al.[48] using the force field fitted in the same study. As shown in Fig. 34, the simulations accurately captured the vapor and liquid compositions for both pressures of 20 and 30 bar. A particularly large two-phase region is observed due to

the presence of $H_2$. The simulation results show excellent agreement with experimental data, while cubic EoS (SRK and PR) were shown to underestimate the extent of phase separation, and predicted narrower two-phase envelopes. Consistent with the accurate predictions for the binaries discussed earlier, Vrabec force field was also shown to perform well in predicting also the ternary phase behavior of these light gas mixtures.

### 4.2.2. Pressure−Volume−Temperature and Thermodynamic Factor Computations for Hydrogen, Methane, and Carbon Dioxide Mixtures.
Zhang et al.[718] performed MD simulations to compute the pressure of pure $H_2$, $CO_2$, $CH_4$, and their binary mixtures at various temperatures and molar volumes. The results, corresponding to a molar volume of $V_m = 0.143$ L mol$^{-1}$, are shown in Fig. 35. For pure-component simulations, the authors reported that the data from MD are in excellent agreement with predictions from GERG-2008 EoS and NIST. However, the reference provided by Zhang et al.[718] (ref 54) for the NIST database does not directly lead to the respective data. The molecular simulation data were subsequently used to parameterize new, computationally efficient analytical equations describing the $pVT$ behavior of $H_2$/$CO_2$/$CH_4$ mixtures at pressures up to 1720 bar and temperatures in the range of 310.9 to 470 K.

Zhang et al.[718] reported excellent agreement with available experimental data[719] at temperatures between 300 and 350 K, for 5 to 50% $H_2$ in $CH_4$ (see Fig. 36). Also, the $P\rho T$ MD data at 673.1 K are in excellent agreement with the available experiments[720] for the mixture 0.6992 $H_2$ + 0.3008 $CO_2$ as shown in Fig. 36. The authors proposed further developing analytical EoS for other binary or multicomponent gas mixtures using MD simulations, potentially augmented with machine learning.

In the recent studies by Hulikal Chakrapani et al.,[576,677] the Marx[310] force field was combined with TraPPE[721] to model the densities, Gibbs excess energies, and thermodynamic factors of $H_2$/$CO_2$ mixtures. For an extended collection of raw simulation data for these properties, but also viscosities, compressibility factors, and diffusivities, the reader is referred to the Supporting Information of refs 576 and 677. The authors presented a wide and reliable collection of simulation data spanning gaseous densities of $H_2$/$CO_2$ mixtures in the range of 298-423 K, 0-1 mole fraction of $H_2$, and for pressures up to 500 bar.[677] The thermodynamic factors of $H_2$/$CO_2$
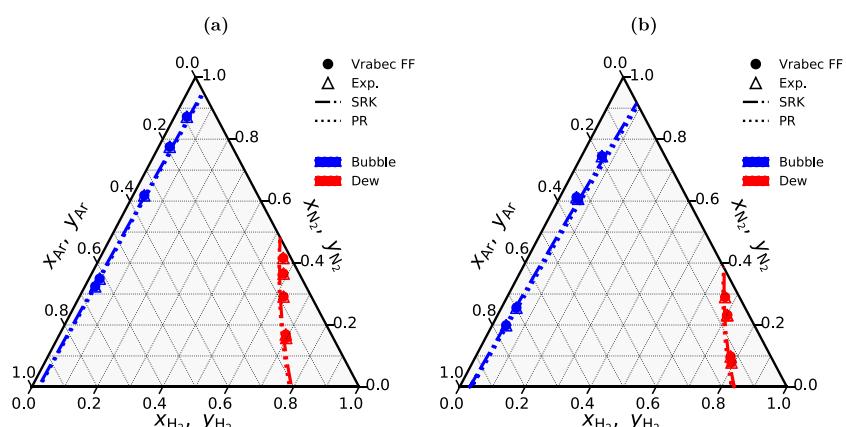


**Figure 34.** Ternary phase diagrams for the $H_2$/Ar/$N_2$ system at 100 K and (a) 20 bar or (b) 30 bar. The simulation data are collected from Köster et al.,[48] the experimental measurements from Xiao et al.,[712] and the SRK and PR EoS datapoints are computed with Clapeyron.[715]
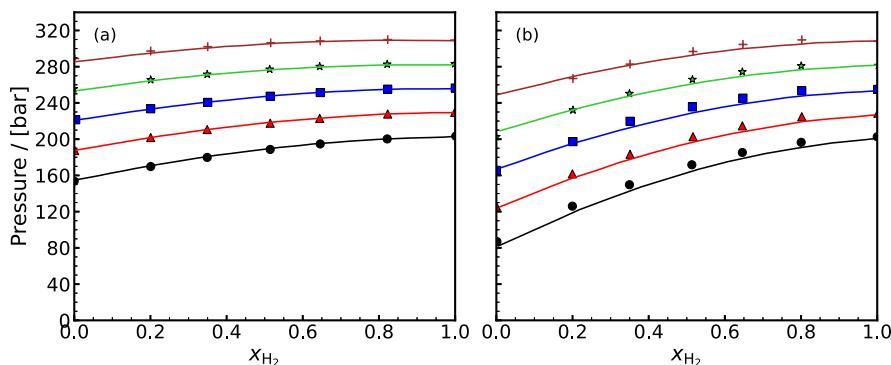
**Figure 35.** Pressure as a function of mole fraction of $H_2$ at different temperatures for (a) $H_2$-$CH_4$ and (b) $H_2$-$CO_2$ binary mixtures. EoS data are shown as lines (black: 310.9 K, red: 350 K, blue: 390 K, green: 430 K, brown: 470 K). Molecular simulation data are shown as symbols (black circles: 310.9 K, red triangles: 350 K, blue squares: 390 K, green stars: 430 K, brown crosses: 470 K).
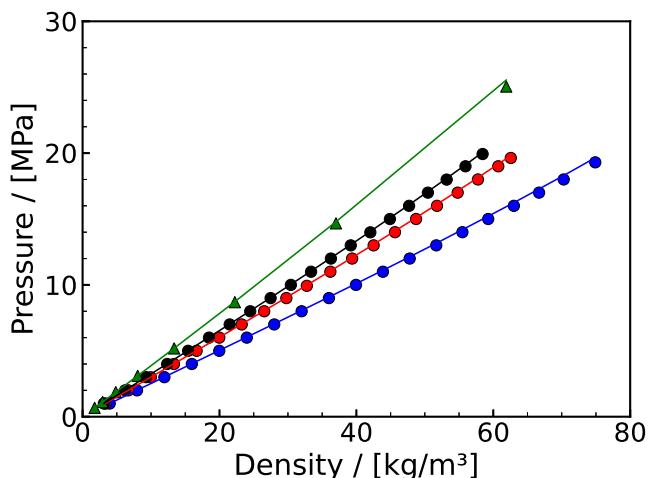


**Figure 36.** Pressure - density diagrams of an equimolar mixture of $H_2$ and $CH_4$ (black, red, and blue circles are molecular simulation data from ref 718. Black, red, and blue lines represent experimental data from ref 719). Additional comparisons for mixtures with $H_2$ mole fractions of 0.05 and 0.10 are provided in the Supporting Information of ref 718. Here, a $H_2$-$CH_4$ mixture with $H_2$ mole fraction of 0.6992 $H_2$ at 673.1 K is also shown (simulation data, represented as green triangles are from ref 718 and experimental data, shown as green line, are from ref 720).

systems were computed at 323 K (using CFCMC simulation - see Section 3.3.1.4), and were shown to have excellent agreement (within 3%) compared to values obtained using REFPROP.[352] Hulikal Chakrapani et al.[576] also showed that thermodynamic factors can be computed from simulations of small system sizes (of ca. 100 molecules) even for densely packed systems using the proposed method.

Barraco et al.[309] systematically compared eight classical LJ-based rigid molecular models of pure $H_2$ gas under thermodynamic conditions relevant to on−board $H_2$ storage in tanks. The selected temperatures (-50 °C to 90 °C) and pressures (50 to 2000 bar) reflect specifications provided by $H_2$ tank manufacturers, ensuring that the models are evaluated under realistic, high pressure, operating scenarios. A total of 600 MD simulations were conducted across twenty−five experimentally derived $H_2$ gas densities per temperature (-50 °C, 20 °C, and 90 °C). For each model, the study presented data for the $pVT$ and phase behavior, and self-diffusivities. The raw simulation data are available in the original work.[309] While all models exhibited nearly identical diffusion behavior, clear

differences emerged in reproducing phase behavior and solubility, especially at high densities. Among the force fields tested, the two-site model by Yang and Zhong[325] and the single-site model derived from Buch[312] performed most consistently across all conditions. For a detailed discussion on $H_2$ force fields see Section 3.1.1.

**4.2.3. Density, Thermal Expansivity, Heat Capacity, Joule-Thomson Coefficient, and Isothermal Compressibility of the Hydrogen-Light Gas Mixtures.** Raju et al.[716] performed MC and MD simulations to compute various thermodynamic properties of $CO_2$-rich mixtures with different gases ($N_2$, Ar, $CH_4$, and $H_2$) at mole fractions ranging from 0.01 to 0.10 (impurity level), exploring a broad spectrum of state points. The authors used well-known force fields previously validated for the pure components. For an extensive collection of raw simulation data and respective figures, the reader is referred to the main manuscript and Supporting Information of ref 716. To illustrate key trends without redundancy, here, we focus on the binary $CO_2$-$H_2$ system at a $H_2$ mole fraction of 0.05, comparing the data from molecular simulation with predictions from the GERG-2008 EoS obtained from REFPROP. Density predictions closely follow GERG-2008 EoS values as shown in Fig. 37. Under these conditions, the maximum relative deviation is approximately 4.4% in the MC simulation at 313 K and 60 bar, 4.3% in the
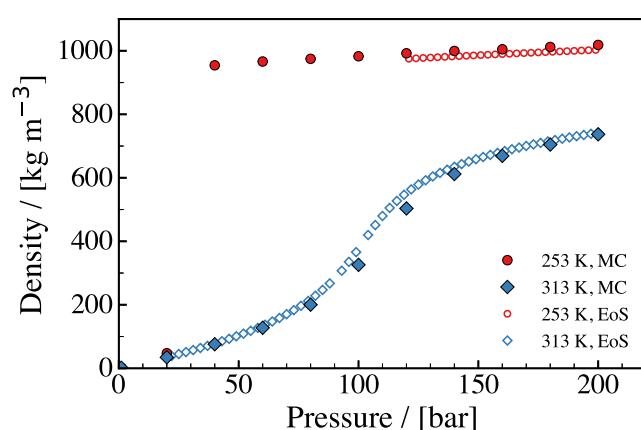


**Figure 37.** Density of $CO_2$-$H_2$ mixture as a function of pressure at a fixed $CO_2$ mole fraction of 0.05 for two temperatures. The EoS data are from GERG-2008 via REFPROP. Raw simulation data are provided in ref 716.
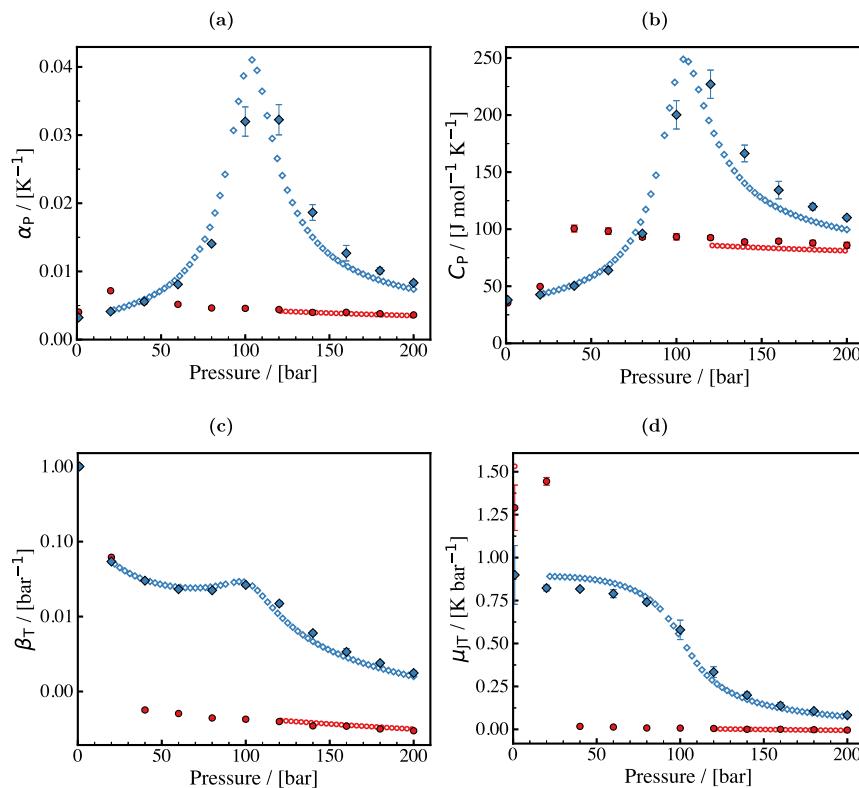
**Figure 38.** Thermodynamic properties of the $CO_2$-$H_2$ mixture at fixed $H_2$ mole fraction of 0.05: (a) Thermal-expansion coefficient, showing peaks near the saturation pressure at 313 K. (b) Isobaric heat capacity, which surges near saturation, showing increased sampling uncertainty. (c) Isothermal compressibility, also showing maxima at saturation. (d) Joule-Thomson coefficient. In all panels, MC simulation (ensemble-fluctuations) results are plotted with filled colored markers, and GERG-2008 EoS with white-filled markers. Red and blue colors represent 253 and 313 K, respectively.

MD simulation at 253 K and 80 bar, 2.1% in MC at 253 K and 40 bar, and 6.6% in MD at 313 K and 60 bar. Notably, in Fig. 37 the GERG-2008 EoS data are absent for 253 K (near the critical region), reflecting the known limitations of the EoS in that regime.

Raju et al.[716] also showed that $CO_2$-rich mixtures with $H_2$ gas as impurity, exhibit the largest reductions in thermal-expansion coefficients, isothermal compressibilities, isobaric heat capacities, and Joule-Thomson coefficients in the gas phase, followed, in decreasing order of effect, by $N_2$, Ar, and $CH_4$. Conversely, in the liquid and supercritical regions, $H_2$ impurities cause the greatest increases in these properties, again with $N_2$, Ar, and $CH_4$ having progressively smaller impacts. In contrast to these findings, the addition of $H_2$ raises gas phase speed of sound, but lowers this property in the liquid and supercritical phases. The respective data are shown in Fig. 38. As can be seen in Fig. 38(a), both the MC simulations and GERG-2008 EoS capture the pronounced maximum in the thermal-expansion coefficient of the $CO_2$-$H_2$ mixture at 313 K, as the pressure approaches saturation. At 253 K, the EoS fails to converge in the vicinity of the critical point (hence the missing data), whereas the MC simulations produce valid fluctuations, consistent with the absence of any phase split. The highest discrepancy between simulation and EoS occurs at approximately 120 bar and 313 K (very close to the saturation line of the mixture). Similar peaks are observed for the heat capacity (Fig. 38(b)) and the compressibility factor (Fig. 38(c)). For heat capacities near the saturation pressure, a sharp increase in both the EoS and MC results can be clearly observed. Due to the proximity to saturation, and the resulting

spontaneous density fluctuations, sampling becomes more computationally expensive, as reflected by the larger error bars. Therefore, the exact peak value cannot be predicted by MC simulations, unless prohibitively large system sizes are used. In ref 716, it is further concluded that the Joule-Thomson coefficient of $CO_2$ decreases in the presence of impurities. The JT coefficients for the $CO_2$-$H_2$ mixture are shown in Fig. 38(d).

**4.2.4. Self-Diffusivity of Hydrogen in Hydrocarbons.** The diffusivity of $H_2$ in hydrocarbons is a crucial property for industrial processes such as Fischer-Tropsch, coal liquefaction, hydrotreating, hydrogenation, liquid organic hydrogen carriers, and separation of gas mixtures. The diffusivities of $H_2$ in heavy alkanes can be used to evaluate the mass transfer limitations in chemical reactors, which operate in conditions ranging from 450−550 K and 20−80 bar.[722] As for the diffusivities of $H_2$ in aqueous solutions (see Section 4.1.5), experimental data of $H_2$/hydrocarbon systems at a wide range of relevant conditions are scarce. Therefore, analytical models, such as modified Stokes-Einstein relations, are used to estimate these diffusivities. To this end, MD simulations are used to predict both self- and mutual diffusion coefficients for different $H_2$/hydrocarbon mixtures.

Makrodimitri et al.[722] investigated the self-diffusivities of $H_2$, CO, and $H_2O$ in alkane mixtures with different chain lengths, ranging from $n$-$C_{12}$ to $n$-$C_{96}$. The TraPPE[301] and Hirschfelder[321] force fields were used to model the alkanes and $H_2$, respectively (see more details on these force fields in Section 3.1). The choice of force fields was based on the fact that TraPPE can accurately model the critical point, densities, and

melting temperatures for pure solutions and mixtures of alkanes over a wide temperature range, while the Hirschfelder model is simple (only LJ interactions) and accurate for pure $H_2$ gas properties. While TraPPE force field explicitly accounts for intramolecular interactions and the bond/angle/dihedral changes (modeled using harmonic potentials) for alkanes, for smaller molecules such as $H_2$, CO, and $H_2O$ intramolecular interactions and bond/angle changes are usually not considered as the vibrational and rotational relaxation times are significantly smaller than the time scales relevant for diffusion. Makrodimitri et al.[722] validated the diffusivities of $H_2$ and CO in pure $C_{12}$, $C_{16}$, and $C_{28}$ alkanes and obtained an agreement of ca. 10% compared to the respective experiments. MD simulations were then used to generate data for self-, Maxwell-Stefan, and Fickian diffusivities of $H_2$ alkane solutions. The self-diffusivities of $H_2$ in alkane solutions at constant temperatures and pressures were shown to decrease with the increase in the alkyl chain length. This is expected since large chain alkanes have high viscosities. The authors used SAFT EoS to compute thermodynamic factors and, thereby, the Fick diffusivities of $H_2$ and CO in $C_{12}$ and $C_{28}$ solutions at 473 K (see the method in Section 3.2.4).

Giraudet et al.[723] performed dynamic light scattering (DLS) experiments and MD simulations to measure/compute self- and mutual diffusivities of binary gas/$n$-alkane mixtures. The authors reported $H_2$ self-diffusivities in $C_6$ and $C_{10}$ for temperatures spanning 303−423 K (at pressures of ca. 40 and 10 bar for $C_6$ and $C_{10}$, respectively). The $H_2$ mole fractions in all mixtures were approaching infinite dilution. The Darkrim[327] and Hirschfelder[321] force fields were used to model $H_2$, while for the alkanes the L-OPLS[420] force field was used. As shown in Fig. 39, the agreement between computed



**Figure 39.** Diffusion coefficients of $H_2$ in different $n$-alkanes and 1-alcohols. Data sources: $n$-$C_6H_{14}$ MD and experimental data (expt),[723] $n$-$C_{10}H_{22}$ MD and expt,[723] alcohols,[725] MD data for $n$-$C_{12}H_{26}$ up to $n$-$C_{96}H_{194}$,[722] expt for these systems.[726,727] Details about the force fields are given in Section 4.2.4.

and experimentally measured diffusivities of $H_2$ in light alkanes is relatively high. Among the gases studied by Giraudet et al.,[723] $H_2$ showed distinctly higher diffusivities (e.g., compared to mixtures containing $N_2$ or CO), which follow an Arrhenius-like behavior. Consistent with other studies in literature, diffusivity decreased with increasing carbon chain length of the $n$-alkanes. The authors used the experimental and simulation data to develop semi-empirical correlations (based on the

model of Wilke and Chang[724]) with parameters being the temperature, solute and solvent molar masses, and the viscosity of the solvent.

In a consecutive study by the same research group following the same experimental technique (DLS) and simulation approach (methods and force fields), Wu et al.[725] reported $H_2$ self-diffusivities in 1-alcohols (i.e., $C_2H_6O$, 1-$C_6H_{14}O$, and 1-$C_{10}H_{22}O$) in the temperature range 303 - 423 K. As in their previous study,[723] the concentration of $H_2$ was close to the infinite dilution limit. The computed diffusivities are shown in Fig. 39 along with the respective experimental data. The temperature and alkyl chain dependence of $H_2$ diffusivity was the same as in the previous study, however, the value was lower compared to He diffusivity in the same solvents, despite the latter having a lower molar mass. The study showed that the fraction of hydrogen-bonded alcohol molecules was another factor affecting diffusivity. The fractions ranged from 0.99 at low temperatures to 0.68 at high temperatures for the different alcohol solvents, decreasing with increasing temperature and increasing alkyl chain length. The authors used the data to construct a semi-empirical model for fast estimations of the gas diffusivities in these alcohols. More MD and experimental data of transport and structural properties of $H_2$-hydrocarbon systems have been reported by Fröba and co-workers.[728−730]

By observing the different datasets collectively shown in Fig. 39, one can conclude that despite the different force fields and simulation protocols used in the different studies, the computed diffusivities show consistent trends, mainly dictated by the molecular weight of the hydrocarbon. Fig. 39 also reveals a lack of MD data for low/near-ambient temperature regimes for long $n$-alkanes, which can possibly be explained by the increased computational effort required to equilibrate and sample properties from these systems.

**4.2.5. Mutual Diffusivities of Hydrogen Mixtures.** Accurately computing the mutual diffusivities in $H_2$ mixtures is crucial for various applications including UHS and synthetic fuel production. Mutual diffusivities govern the rate of molecular mixing and mass transport in gas mixtures such as $H_2/CO_2$, impacting $H_2$ purity and storage efficiency in subsurface reservoirs. Additionally, $H_2$ diffusivity in aqueous environments (e.g., brines) affects $H_2$ losses due to dissolution and potential chemical reactions during UHS as discussed in Section 2.3.4. Since experimental data under relevant high-pressure and temperature conditions are not available or challenging to obtain, molecular simulations provide vital insights and reliable predictions of diffusion behavior, enabling better design and management of $H_2$ storage systems and related processes. Here, we review articles that report mutual- and self-diffusivities of $H_2$ binary mixtures with small gases using MD simulations. Contrary to self-diffusivities of aqueous systems, the data on mutual-diffusivities of $H_2$ mixtures are limited, practically corresponding to two studies, which are listed in Table 12.

Hulikal Chakrapani et al.[677] computed mutual (i.e., MS and Fick) diffusivities of binary gas mixtures of $H_2$ and $CO_2$, as well as their solubilities in NaCl brine, over pressures ranging from 5 to 50 MPa, temperatures from 323.15 to 423.15 K, $H_2$ mole fractions from 0 to 1, and salt concentrations up to 2 mol salt/kg of $H_2O$. MD simulations were used to compute transport properties, i.e., self-, MS, and Fick diffusivities (methods discussed in Sections 3.2.3 and 3.2.4), while GEMC simulations with the CFC method were conducted to obtain VLE and solubilities. MS diffusivities from MD exhibit

**Table 12. List of the MD Simulation Studies Investigating the Mutual Diffusivities of $H_2$-Gas Mixtures along with Information on the Force Fields and Thermodynamic Conditions**

| | System details | | Thermodynamic conditions | |
|---|---|---|---|---|
| Study | Components | Force field | $p/[MPa]$ | $T/[K]$ |
| Hulikal Chakrapani et al.[677] | $H_2$ | Marx[328] | 5−50 | 323.15−423.15 |
| | $CO_2$ | TraPPE[678] | | |
| Saric et al.[731] | $H_2$ | Vrabec[48] | 9 | 290−350 |
| | $CO_2$ | Merker et al.[732] | | |

significant deviations from the Darken relation,[509] which assumes ideal diffusing mixtures. For a $H_2$ mole fraction of ca. 0.7, Darken underestimates MS diffusivities by up to 30%, whereas deviations drop to about 5% at low or high $H_2$ concentrations. This underscores the non-ideal behavior of $H_2/CO_2$ mixtures, as also reflected in the thermodynamic factors, $\Gamma$, which quantify the non-ideality of mixtures (see Section 3.2.13). $\Gamma$ decreases with increasing pressure, and increases with temperature, spanning roughly 0.25 to 1 across the studied conditions. The deviation of $\Gamma$ from unity in the study by Hulikal Chakrapani et al.,[677] confirms strong non-ideal interactions affecting the MS-Fick relationship. The order of magnitude of Fick diffusivities, which are obtained by multiplying MS diffusivities with $\Gamma$, range from approximately $10^{-8}$ to $10^{-6}$ m$^2$/s, with higher values corresponding to lower pressures and elevated temperatures. At 5 MPa and 423.15 K, where mixtures approach ideal behavior, kinetic theory (using the Chapman-Enskog expression) predicts Fick diffusivities within 5% accuracy. However, at lower temperatures and higher pressures, especially in $CO_2$-rich mixtures, kinetic theory deviates by up to 75%. In contrast, $H_2$-rich mixtures retain agreement within about 15% even at 50 MPa, owing to their more ideal-gas-like behavior. To remedy kinetic theory's shortcomings at high pressures and low temperatures, the empirical Moggridge correlation is applied. This captures the liquid-like behavior of $CO_2$-rich mixtures and predicts MS, and thus Fick, diffusivities within 5 to 10% of computed values under such conditions. Yet, for $H_2$-rich mixtures and low pressures, Moggridge's correlation can err by up to 35%, making it less suitable in those regimes. The observed transport behavior stems from the transition between gas-like and dense-gas-like regimes, with self-diffusivities inversely proportional to mixture density. Molecular size differences also play a key role i.e., $H_2$ diffuses 2.5 to 6 times faster than $CO_2$, a discrepancy partially explained by the Stokes-Einstein relation. Comparisons with experimental data at near-atmospheric pressures (indirectly obtained by extrapolating the simulation data via the principle of corresponding states) show agreement within approximately 15%, thereby validating the molecular simulation approach. Although no single general fit function is proposed, established correlations (i.e., Chapman-Enskog kinetic theory, Fuller correlation, and Moggridge correlation) are assessed and recommended according to the relevant pressure, temperature, and composition regimes.

Saric et al.[731] performed MD simulations and EoS modeling to examine thermodynamic, transport, and structural properties of supercritical carbon dioxide (scCO$_2$) mixtures containing solutes such as $H_2$, $CH_4$, and various hydrocarbons, over temperatures from approximately 290 to 350 K, and

pressures in the range 9 - 12 MPa. The study focused on dilute compositions near the infinite-dilution limit (0.3-1.5 mol%). Here, the Widom region refers to the temperature span near the critical point where the fluid undergoes a continuous crossover from liquid-like to gas-like supercritical behavior. It is marked by pronounced maxima in thermodynamic response functions such as $c_p$, $\beta_T$, and $\alpha$, and corresponds to enhanced density fluctuations and structural changes. In this context, the temperature dependence of self-diffusion coefficients (also termed intra-diffusion coefficients) in $H_2/scCO_2$ mixtures was analyzed. These coefficients, representing species-specific Fickian self-diffusion, were derived from velocity autocorrelation functions in MD simulations, distinguishing them from MS diffusivities. Across the Widom region, self-diffusion coefficients exhibit a sigmoidal increase with temperature, rising by at least an order of magnitude between roughly 305 and 320 K at 9 MPa. Lighter molecules, such as $H_2$, diffuse significantly faster than e.g., hydrocarbons, with diffusivities increasing more steeply during the liquid-like to gas-like supercritical crossover. This sigmoidal behavior reflects the transition from a dense, liquid-like regime, dominated by strong intermolecular interactions and low diffusivity, to a low-density, gas-like regime where kinetic effects prevail and diffusivity is high. The crossover temperature aligns with maxima in $c_p$, $\beta_T$, and $\alpha$, and coincides with microscopic structural changes: a reduction in average coordination number and clustering effects quantified by Kirkwood-Buff integrals. Moreover, near the Widom line, the kinetic contribution to shear viscosity surpasses the configurational component, indicating a shift in molecular transport mechanisms. In the Widom region, simulation data exhibit increased scatter, reflecting the strong density fluctuations characteristic of critical phenomena. Finally, Saric et al.[731] proposed an empirical correlation for predicting the Widom line temperature as a function of pressure, solute mole fraction, and the critical properties of mixture components. Although this correlation yields only the thermodynamic crossover temperature, it enables indirect estimation of mutual diffusivity trends by pinpointing the temperature region where transport properties such as diffusivity change dramatically due to the liquid-to-gas transition in the supercritical phase. Consequently, knowledge of the Widom line location aids in anticipating the temperature range over which molecular transport properties vary strongly.

## 4.3. Hydrogen Liquefaction and Properties of Liquid Hydrogen Systems

Han et al.[295] investigated $H_2$ liquefaction on CNT surfaces by performing MD simulations using the reactive force field ReaxFF[707] to model $H_2$-CNT interactions. Although in this review we do not systematically discuss reactive systems, we cover this study for two reasons: (i) to the best of our knowledge, molecular simulations of $H_2$ liquefaction are extremely scarce, and (ii) the claim of the authors that the liquefaction of $H_2$ could be increased by introducing CNTs is both unique and could lead to significant advancements in $H_2$ transport and storage. The simulations compared $H_2$ interactions with different CNT systems (bundles, isolated CNTs, single- and multi-walled). The authors report that $H_2$ liquefaction occurred only on the CNT bundle (not on single CNTs) at 80 K and 100 bar. This phenomenon involves various mechanisms; deformation of the CNT bundle into oval shapes under pressure, charge transfer from low-curvature to

high-curvature regions of the deformed CNTs, development of charge polarization in the bundle, long-range electrostatic interactions between the polarized charges and $H_2$ molecules, and high local-ordering of $H_2$ gas leading to liquefaction. Single CNTs did not induce liquefaction because they deformed symmetrically under pressure, preventing charge polarization from developing. No chemisorption of $H_2$ was observed, only physisorption and liquefaction. Han et al.[295] suggest that $H_2$ gas could potentially be liquefied at temperatures higher than 80 K on more strongly polarized CNT bundles. This study provides insight into the previously unexplained linear increase in $H_2$ uptake with pressure observed by Ye et al.[733] and explains the discrepancy between the high storage capacity of CNT bundles versus the limited capacity of single CNTs.

Cheng and Frenkel[537] introduced the WAVE method and applied it to calculate the thermal conductivity of liquid $H_2$ and supercritical water (see the details of the method in Section 3.2.6). The $H_2$ system studied was highly compressed (33 GPa) at 2000 K. The authors used an ML-derived force field, for which they obtained a thermal conductivity of 5 W/mK. This value is on the same order of magnitude with the value for compressed gaseous $H_2$ at 1000 bar, obtained from the extrapolation of measurements. The authors note that nuclear quantum effects should probably be considered for more accurate results. For more details on these effects the reader is referred elsewhere.[734,735]

A series of studies, such as the ones by Lenosky et al.,[736] Collins et al.,[737] Holst et al.,[738] Tian et al.,[739] Redmer et al.[740] focused on computing properties of liquid $H_2$ mainly using quantum mechanical methods (e.g., ab initio MD, tight-binding electronic structure techniques, DFT). These studies report electrical conductivities, $pVT$ relations, hopping mechanisms and electronic transport coefficients, atomic/molecular $H_2$ properties, liquid-liquid phase transitions, shock-compressed $H_2$. Despite the wealth of physical insights and the useful data provided, a detailed analysis of these papers is not in the scope of this review, which focuses on classical molecular simulation of $H_2$ systems.

Liu et al.[741] performed MD simulations to study liquid $H_2$ nucleation and boiling on a flat aluminum heat conducting substrate. The authors used a simple LJ potential for $H_2$ molecules and an EAM potential for the wall. Bubble nucleation was studied in the temperature range of 100 - 200 K, while liquid $H_2$ was obtained at 20 K. The authors mention that their MD simulations revealed a complete bubble nucleation, growth, and merging process, while for the $H_2$ boiling process, nucleate, transition, and film boiling stages were obtained. Higher wall temperatures accelerated bubble growth rate and affected gas film growth rate more than bubble growth rate. Wall temperature was shown to have minimal effect on liquid layer thickness during nucleation. The contact angle computed was ca. 4.9 degrees. While the study by Liu et al.[741] provides some insight into interfacial $H_2$ properties, the methods used could raise concerns regarding the accuracy of the reported data and conclusions. The LJ potential used for $H_2$-$H_2$ interactions may be adequate for gaseous systems, however, since $H_2$ is a quantum fluid at low temperatures (such as the cryogenic temperature of 20 K used in the study), is highly unlikely to be accurate (techniques such as path-integral MD would be more appropriate). The authors mentioned that the potential validation was performed for density at 20 K and 1 bar, for which the result deviated only 1.37% from the NIST data (ca. 70 kg m$^{-3}$). While this seems

reasonable, density alone is insufficient to validate a model for complex phenomena such as boiling. The authors neither mention the use of quantum corrections nor of a more sophisticated force field which accounts for quantum effects. In addition, the cutoff distance for the interactions is not mentioned. The NEMD simulation performed to study the bubble nucleation was only 26 fs, which is extremely short for observing complete boiling phenomena.

## 4.4. Hydrogen Solubility, Diffusivity, and Permeability in Polymeric and Composite Materials

The role of molecular simulations the past 40 years in understanding gas sorption and permeation in polymers has been significant. Unlike inorganic materials, polymers experience structural alterations during these processes. Many studies successfully modeled barrier properties in various polymers (e.g., PET, PS, polyimides) and accurately predicted sorption mechanisms, temperature effects, and permeation values. Key qualitative findings include the sorption mechanisms below glass transition temperatures, accessible volume pockets influenced by polymer chemistry, and structural changes during sorption. Research also has been conducted to study mixed-gas penetrants and composite materials (such as MOF-polymers, zeolite-polymers), demonstrating that molecular simulations can reproduce experimental trends, and sometimes, even quantitative predictions of permeation properties.[742,743]

As discussed in Sections 2.2.1, 2.3.1 and 2.4.1, important $H_2$ technologies, such as storage in tanks, membrane separations, and gas transport via pipelines, may involve polymeric materials. To this purpose, MD and MC studies focusing on $H_2$ solubilities, diffusivities, and permeabilities in these materials are abundant in the literature. The study by Voyiatzis and Stroeks[407] presents a comprehensive investigation into the solubilities of $H_2$ and $O_2$ in two industrially significant polymers (e.g., as liner materials in high-pressure $H_2$ storage tanks): PA6 and HDPE. The authors used the free energy perturbation and fast-growth thermodynamic insertion methods, to predict $H_2$ solubilities in both the crystalline and amorphous phases of the polymers. These simulations were conducted in a temperature range of 300 - 360 K and at 700 bar pressure to study $H_2$ transport behavior under conditions relevant to storage in tanks. The crystalline phases of the PA6 and HDPE polymers consisted of 64 and 40 chains of infinite length, respectively. The crystal structure of PA6 in the simulation box is shown in Fig. 42(a). The amorphous phases comprised 10 PA6 molecules of 160 monomers, and 30 HDPE chains of 110 monomers. The study revealed that the crystalline phases of both PA6 and HDPE are completely impermeable barriers to both $H_2$ and $O_2$, despite the small size of these gases. The molecular simulations achieved semi-quantitative agreement with experimental solubility measurements. Discrepancies between predicted and experimental values were attributed primarily to the simulations' inability to fully account for the constraining effects that crystalline regions exert on adjacent amorphous polymer domains. The study also showed that despite $H_2$ being significantly smaller than $O_2$, it consistently exhibits lower solubility in both PA6 and HDPE. This is a rather counterintuitive finding, also shown in prior simulation and experimental studies, that can be explained based on the more favorable interactions of the $O_2$ with both polymer matrices compared to $H_2$. The findings by Voyiatzis and Stroeks[407] that $H_2$ migration occurs predominantly

through the amorphous regions, with crystalline domains acting as impermeable obstacles, and that intermolecular interactions between the gases and the polymer chains dominate solubility behavior over considerations of accessible volume distribution within the polymer, can be taken into consideration when designing gas barrier materials. The computed solubilities are shown in Fig. 40 and listed in Table 13.
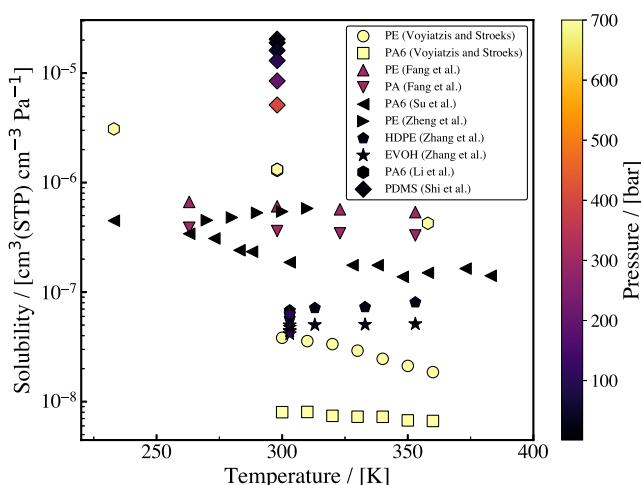


**Figure 40.** Solubilities of $H_2$ in different polymers computed via molecular simulations performed in different studies. The raw data and references are listed in Table 13 except for the solubility of $H_2$ in PDMS.[749]

Zhao et al.[744] performed all-atom MD simulations to study the mass of $H_2$ in PE, a liner material used in type IV storage tanks (see also Section 2.3.1). The study was performed at a wide pressure (up to 700 bar) and temperature (up to 400 K) range, and focused on different properties including tensile behavior, glass transition temperature, $H_2$ diffusion in various PE structures, and bubble formation during rapid depressurization. Several systems were considered, i.e., varied PE chain length and structure (branched and unbranched), reinforcement with graphene, the incorporation of small molecules as additives $(C_{20}H_{42})$, and various $H_2$ concentrations. The number of polymer chains in the systems studied varied from 1 to 16, having degrees of polymerization in the range of 500 to 2000. The authors showed that the presence of $H_2$ in PE matrices deteriorated tensile performance and decreased the glass transition temperature, compromising the structural integrity of the materials. Several structural factors affected $H_2$ diffusion in amorphous PE regions. In short, branches and side chains increased $H_2$ diffusivity by introducing more free volume below glass transition temperature, the chain length variation had minimal effect if chains were sufficiently long, polymer orientation improves barrier properties when aligned against the pressure drop direction, small molecules/additives (acting as plasticizers) increased diffusion rates, while graphene reinforcement has the opposite effect. During rapid depressurization, $H_2$ molecules aggregated into nano-sized bubbles within the polymer matrix. These bubbles formed in both exclusive and free volume regions, appearing and disappearing during pressure changes before stabilizing at low pressures. To study these bubbling effects, the authors introduced to the systems large number of $H_2$ molecules. A simulation snapshot showing a $H_2$ bubble comprising 1000 gas molecules in the

polymer is shown in Fig. 42(b). Similarly, for computing diffusivity, 100 $H_2$ molecules were used. It is important to comment here that such system sizes, which lead to phase separation (gas and polymer), make the control of the pressure of the system an arduous task for the barostat. Additionally, the introduction of rapid changes in pressures in MD simulations, bring the systems in a non-equilibrium state, during which equilibrium properties cannot be accurately sampled. Based on their findings, Zhao et al.[744] indicate that HDPE without branches and without small molecules as additives could deliver superior performance as a $H_2$ barrier, while graphene reinforcement should be oriented against the pressure drop direction. The computed solubilities are shown in Fig. 40 and listed in Table 13.

The permeation behavior of $H_2$ in PE and PA was also investigated by Fang and Ji[218]. Since the motivation of this study was also the high-pressure $H_2$ storage in IV-type tanks, the simulations were performed at representative for the application conditions, i.e., high pressure (300 bar) and at temperatures ranging from ca. 260 to 350 K. Contrary to Voyiatzis and Stroeks,[407] only amorphous phases were considered in this study. The authors state that the molecular weight of the PE cell was 3630, while the respective for PA was 3440. The respective polymerization degrees were 40 and 18. This study focused on several properties affecting $H_2$ permeation: FFV, and solubility, diffusion, and permeability coefficients. Qualitatively consistent with prior experiments and molecular simulation studies, Fang and Ji[218] showed that increasing temperature causes a decrease in solubilities and increase in diffusivities of $H_2$ in both polymers. FFV correlated positively with temperature, with PE showcasing an increase of FFV of ca. 50% (in the range 263-353 K) compared to ca. 33% of PA. A schematic representation of the FFV distribution in the PA matrix at 353 K is shown in Fig. 42(c). Permeability coefficients increased with increasing temperature, showing the dominant role of the diffusivity in the computation (see also Section 2.2.1). PE consistently exhibited higher solubilities and diffusivities than PA for all conditions considered. As a consequence, PA is stated to have superior $H_2$ permeability resistance, performing three to four times better than polyethylene in preventing $H_2$ permeation. The computed solubilities and permeabilities are shown in Fig. 40 and Fig. 41, and listed in Table 13 and Table 14, respectively. Despite simulations following the general trends of experimental data, quantitatively the simulation data overshoot the experiments by 1 to 2 orders of magnitude, clearly showing that either the simulation scheme and/or the force fields chosen have limited predictive ability. In a similar study, Li et al.[745] studied the barrier performance (via computing solubilities, diffusivities, and permeabilities) of graphene/PA6 composites, having the filler (graphene) composition as a parameter ranging from 3 to 7 wt%. Depending on the graphene content, the number of PA6 monomers varied from 8 to 60. The exact number of polymer chains used is not clearly mentioned, however, the unit cell dimensions for the different systems are provided. A configuration of a model graphene/PA6 system as obtained by the commercial software used by the authors is shown in Fig. 42(d). Similarly to the previous study, conditions relevant to $H_2$ storage at IV-type tanks were considered, i.e., 233 - 358 K and 1 - 700 bar. In this study, the properties were correlated to different graphene contents except from the different temperatures and pressures. Several insights, relevant to $H_2$ storage vessel design, were reported. Particularly, it was shown that the

**Table 13. Solubilities (S) of H$_2$ in PE/HDPE, PA6/PA, and EVOH Polymeric Matrices Computed in Different Studies[a]**

| Source | T | p | PE/HDPE | PA6/PA | EVOH |
|---|---|---|---|---|---|
| Voyiatzis and Stroeks[407] | 300 | 700 | $3.83 \times 10^{-8}$ | $8.01 \times 10^{-9}$ | |
| | 310 | 700 | $3.57 \times 10^{-8}$ | $8.05 \times 10^{-9}$ | |
| | 320 | 700 | $3.35 \times 10^{-8}$ | $7.42 \times 10^{-9}$ | |
| | 330 | 700 | $2.92 \times 10^{-8}$ | $7.28 \times 10^{-9}$ | |
| | 340 | 700 | $2.46 \times 10^{-8}$ | $7.27 \times 10^{-9}$ | |
| | 350 | 700 | $2.12 \times 10^{-8}$ | $6.74 \times 10^{-9}$ | |
| | 360 | 700 | $1.86 \times 10^{-8}$ | $6.66 \times 10^{-9}$ | |
| Fang and Ji[218] | 263 | 300 | $6.66 \times 10^{-7}$ | $3.87 \times 10^{-7}$ | |
| | 298 | 300 | $6.07 \times 10^{-7}$ | $3.61 \times 10^{-7}$ | |
| | 323 | 300 | $5.70 \times 10^{-7}$ | $3.44 \times 10^{-7}$ | |
| | 353 | 300 | $5.37 \times 10^{-7}$ | $3.29 \times 10^{-7}$ | |
| Su et al.[746] | 233 | 1 | | $4.49 \times 10^{-7}$ | |
| | 263 | 1 | | $3.41 \times 10^{-7}$ | |
| | 273 | 1 | | $3.09 \times 10^{-7}$ | |
| | 283 | 1 | | $2.41 \times 10^{-7}$ | |
| | 288 | 1 | | $2.34 \times 10^{-7}$ | |
| | 303 | 1 | | $1.87 \times 10^{-7}$ | |
| | 328 | 1 | | $1.76 \times 10^{-7}$ | |
| | 338 | 1 | | $1.76 \times 10^{-7}$ | |
| | 348 | 1 | | $1.38 \times 10^{-7}$ | |
| | 358 | 1 | | $1.50 \times 10^{-7}$ | |
| | 373 | 1 | | $1.64 \times 10^{-7}$ | |
| | 383 | 1 | | $1.41 \times 10^{-7}$ | |
| Li et al.[745] | 298 | 1 | | $1.32 \times 10^{-6}$ | |
| | 298 | 350 | | $1.31 \times 10^{-6}$ | |
| | 298 | 525 | | $1.29 \times 10^{-6}$ | |
| | 298 | 700 | | $1.32 \times 10^{-6}$ | |
| | 233 | 700 | | $3.09 \times 10^{-6}$ | |
| | 358 | 700 | | $4.25 \times 10^{-7}$ | |
| Zheng et al.[748] | 270 | 1 | $4.53 \times 10^{-7}$ | | |
| | 280 | 1 | $4.80 \times 10^{-7}$ | | |
| | 290 | 1 | $5.30 \times 10^{-7}$ | | |
| | 300 | 1 | $5.44 \times 10^{-7}$ | | |
| | 310 | 1 | $5.81 \times 10^{-7}$ | | |
| Zhang et al.[750] | 303 | 25 | $6.79 \times 10^{-8}$ | | $4.40 \times 10^{-8}$ |
| | 313 | 25 | $7.16 \times 10^{-8}$ | | $5.02 \times 10^{-8}$ |
| | 333 | 25 | $7.30 \times 10^{-8}$ | | $5.05 \times 10^{-8}$ |
| | 353 | 25 | $8.07 \times 10^{-8}$ | | $5.12 \times 10^{-8}$ |
| | 303 | 25 | $6.79 \times 10^{-8}$ | | $4.43 \times 10^{-8}$ |
| | 303 | 40 | $6.36 \times 10^{-8}$ | | $4.755 \times 10^{-8}$ |
| | 303 | 60 | $5.78 \times 10^{-8}$ | | $4.995 \times 10^{-8}$ |
| | 303 | 100 | $6.29 \times 10^{-8}$ | | $4.148 \times 10^{-8}$ |

[a]T is in units of K, p in bar, and S in cm$^3$(STP) cm$^{-3}$ Pa$^{-1}$.

5 wt% graphene/PA6 composite has the optimal barrier performance, achieving a 54.6% reduction in permeability coefficient compared to pure PA6 at ambient conditions. This substantial improvement indicates the effectiveness of graphene as a nanofiller for H$_2$ barrier applications. Li et al.[745] showed that temperature has a pronounced effect on H$_2$ diffusion, with the diffusion coefficient of 5 wt% graphene/PA6 increasing by 138% in the range 298 - 358 K at 70 MPa. The authors state that this finding highlights the importance of thermal management in storage vessel design. As in prior studies, H$_2$ diffusivity was shown to have a linear and inverse relationship with pressure for all materials. Pure PA6 consistently showed the highest diffusion coefficient, while the 4 wt% graphene/PA6 composite displayed the lowest. The addition of graphene was found to restrict polymer chain movement, and disrupt pore continuity within the polymer

matrix, creating a more tortuous path for H$_2$ molecules. FFV directly correlated with diffusion coefficients, providing a mechanistic explanation for the observed barrier improvements. The computed solubilities and permeabilities are shown in Fig. 40 and Fig. 41, and listed in Table 13 and Table 14, respectively.

H$_2$ permeability in PA6 was also studied via MD and MC simulations performed by Su et al.[746] Similarly to the studies discussed earlier, the authors highlight that H$_2$ permeation through these polymeric liners is almost inevitable, thus, understanding the behavior of H$_2$/PA systems under extreme conditions (233-358 K and 1-875 bar) is critical for evaluating long-term performance and safety of storage tanks. The authors claim that their work is the first comprehensive molecular-level investigation of H$_2$ permeation in PA6 under realistic service conditions. Given that Su et al.[746] performed
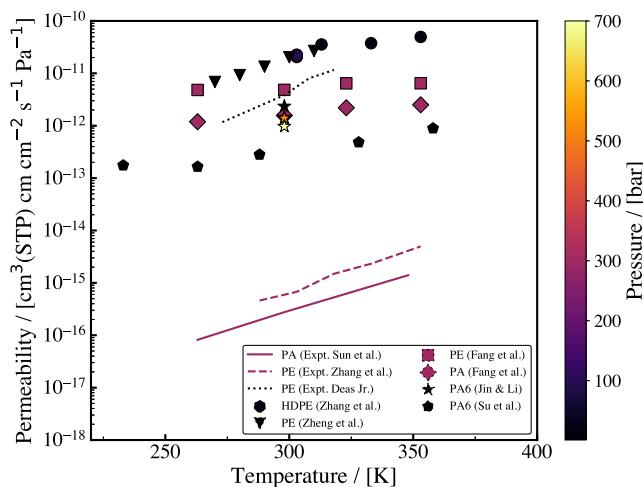
**Figure 41.** Permeabilities of $H_2$ in different polymers computed via molecular simulations performed in different studies. Three experimental datasets are shown for comparison (lines). The raw data and references are listed in Table 14.

**Table 14. Permeabilities ($P$) of $H_2$ in PE/HDPE and PA6/PA Computed in Different Studies[a]**

| Source | $T$ | $p$ | PA/PA6 | PE/HDPE |
|---|---|---|---|---|
| Fang and Ji[218] | 263 | 300 | $1.19 \times 10^{-12}$ | $4.82 \times 10^{-12}$ |
| | 298 | 300 | $1.57 \times 10^{-12}$ | $4.84 \times 10^{-12}$ |
| | 323 | 300 | $2.20 \times 10^{-12}$ | $6.43 \times 10^{-12}$ |
| | 353 | 300 | $2.51 \times 10^{-12}$ | $6.46 \times 10^{-12}$ |
| Li et al.[745] | 298 | 1 | $2.35 \times 10^{-12}$ | |
| | 298 | 350 | $1.44 \times 10^{-12}$ | |
| | 298 | 525 | $1.39 \times 10^{-12}$ | |
| | 298 | 700 | $9.70 \times 10^{-13}$ | |
| Su et al.[746] | 233 | 1 | $1.75 \times 10^{-13}$ | |
| | 263 | 1 | $1.65 \times 10^{-13}$ | |
| | 288 | 1 | $2.81 \times 10^{-13}$ | |
| | 328 | 1 | $4.83 \times 10^{-13}$ | |
| | 358 | 1 | $8.91 \times 10^{-13}$ | |
| Zheng et al.[748] | 270 | 1 | | $6.84 \times 10^{-12}$ |
| | 280 | 1 | | $9.24 \times 10^{-12}$ |
| | 290 | 1 | | $1.34 \times 10^{-11}$ |
| | 300 | 1 | | $2.03 \times 10^{-11}$ |
| | 310 | 1 | | $2.67 \times 10^{-11}$ |
| Zhang et al.[750] | 303 | 25 | | $2.16 \times 10^{-11}$ |
| | 313 | 25 | | $3.56 \times 10^{-11}$ |
| | 333 | 25 | | $3.76 \times 10^{-11}$ |
| | 353 | 25 | | $4.96 \times 10^{-11}$ |
| | 303 | 40 | | $2.26 \times 10^{-11}$ |
| | 303 | 60 | | $2.05 \times 10^{-11}$ |
| | 303 | 100 | | $2.24 \times 10^{-11}$ |
| Experimental data by Deas-Jr et al.[751] | 273 | 1 | | $1.17 \times 10^{-12}$ |
| | 298 | 1 | | $3.84 \times 10^{-12}$ |
| | 308 | 1 | | $8.04 \times 10^{-12}$ |
| | 318 | 1 | | $1.16 \times 10^{-11}$ |
| Experimental data by Na Zhang et al.[752] | 288 | 300 | | $4.60 \times 10^{-16}$ |
| | 303 | 300 | | $6.75 \times 10^{-16}$ |
| | 318 | 300 | | $1.49 \times 10^{-15}$ |
| | 333 | 300 | | $2.32 \times 10^{-15}$ |
| | 353 | 300 | | $4.97 \times 10^{-15}$ |
| Experimental data by Sun et al.[753] | 263 | 300 | $8.18 \times 10^{-17}$ | |
| | 298 | 300 | $2.76 \times 10^{-16}$ | |
| | 348 | 300 | $1.40 \times 10^{-15}$ | |

[a]Three experimental datasets are provided for comparison. $T$ is in units of K, $p$ in bar, and $P$ in $\text{cm}^3(\text{STP})$ cm $\text{cm}^{-2}$ $\text{s}^{-1}$ $\text{Pa}^{-1}$.

simulations up to 875 bar, and that correction factors are applied to the results, their claim may be partially justified. However, it is important to comment here that this study uses conventional methods and tools to compute properties that have also been presented earlier for both PA and other polymeric matrices. In more detail, the authors primarily perform GCMC simulations to compute $H_2$ solubilities, MD simulations to calculate diffusion coefficients, while they apply corrections to account for polymer crystallinity (30%). The corrections used for the solubilities and diffusivites are functions of the volume fractions of the amorphous and crystalline regions, which have been used also in earlier studies.[413,747] In this study, 4 polymer chains comprising 200 monomers, were used. Su et al.[746] discuss the dependence of solubitlies, FFVs, and diffusivities on temperature, which exhibit complex patterns with multiple Arrhenius regions, particularly at ca. PA6's glass transition temperature. The computed solubilities and permeabilities are shown in Fig. 40 and Fig. 41, and listed in Table 13 and Table 14, respectively. The study identified a "hopping" mechanism for $H_2$ diffusion in PA6, according to which $H_2$ molecules vibrate within the free volume pores for extended periods with a sudden hop happens to adjacent pores when the thermal motion of the polymer chains creates temporary channels. The simulation trajectory of a $H_2$ molecule in PA6, indicating the hopping transport mechanism, is shown in Fig. 42(e). Please note that this $H_2$ hopping mechanism should not be confused with the proton hopping mechanism discussed in e.g., Sections 3.2.12, and 4.1.6. As a conclusive remark, this study showcases that molecular simulations play a crucial role for understanding complex $H_2$ phenomena at elevated conditions. For example, the identification of multiple Arrhenius regions in the behavior of sorption and diffusivity can lead to improved predictive models for permeation behavior.

Motivated by the use of polymers as building or supporting materials in pipelines, Memari et al.[413] performed experiments and molecular simulations to study the solubility of $CH_4+CO_2$ and $CH_4+H_2$ mixtures in semicrystalline PE below its melting temperature. MC simulations in the osmotic ensemble were performed using PE chains of 70 carbon atoms each. To the best of our knowledge, this is the only $H_2$/PE study which uses

an anisotropic potential to model the hydrocarbon (AUA4[412]). Interestingly, the force field used for $H_2$ was developed by Darkrim et al.[327] to study the physisorption of $H_2$ and $N_2$ on graphite basal planes. Memari et al.[413] performed the MC simulations at 313 K and two pressures (6 and 21 bar), while a high-pressure ($700\pm100$ bar) was also examined to mimic the effect of crystallinity of the permeable zones due to the increase in the density of the polymer matrix as stated by the authors. The simulation results for the concentration of $H_2$ in PE were shown to be a factor of 2 higher than the respective experimental data. The agreement with experiments for both gas mixtures is significantly better at the high-pressure, while the solubility selectivity $S_{CH_4/SH_2}=54$ is in agreement with predictive correlations.

Zheng et al.,[748] also motivated by the application of PE as pipeline material, conducted MD and GCMC simulations to predict solubilities, diffusivities, and permeabilities of $H_2$ in this polymer. The temperatures and pressures considered were in the range 270 - 310 K and 1 - 70 bar, respectively, in an effort

**Table 15. Experimentally Measured $H_2/CH_4$ Permeabilities Gathered from Different Literature Sources[a]**

| Membrane | $P_{H_2}$ (Barrer) | $P_{H_2}/P_{CH_4}$ |
|---|---|---|
| ZIF-8[812] | $1.38 \times 10^4$ | 20.3 |
| ZIF-8[813] | $1.25 \times 10^4$ | 16.2 |
| ZIF-22[814] | $2.27 \times 10^4$ | 5.2 |
| LTA[815] | $3.76 \times 10^3$ | 3.6 |
| HKUST-1[816] | $1.79 \times 10^5$ | 6 |
| ZIF-7[817] | 358 | 5.9 |
| P84/ND[818] | 6.7 | 310 |
| Matrimid/ZIF-11 (10%)[819] | 28.11 | 97 |
| 6FDA-TTM/Si-H (5%)[820] | 62.6 | 160.5 |
| MWCNT@GONRs (2%)[821] | 42.5 | 18.5 |
| PLA[822] | 25 | 10 |
| Hyflon AD60X[823] | 187 | 62 |
| ZIF-8/6FDA-durene[824] | $4.2 \times 10^3$ | 17 |
| Matrimid-ZIF-8[825] | 64 | 137 |
| MMM-ZIF-8[826] | 27.1 | 123.2 |
| MMM- UiO-66[826] | 64.4 | 153.3 |
| JUC-160[827] | $2 \times 10^3$ | 8.5 |
| MEFMEQ mixture[828] | $3.7 \times 10^3$ | 7 |
| MEFMEQ single components[828] | $4.8 \times 10^3$ | 21 |
| ZIF-8 mixture[828] | $6 \times 10^3$ | 9.8 |
| ZIF-8 single components[828] | $5.3 \times 10^3$ | 13.4 |
| MOF-5 mixture[828] | $4.1 \times 10^3$ | 2 |
| MOF-5 single components[828] | $4.6 \times 10^3$ | 2.3 |
| Cu-BTC mixture[828] | $2.2 \times 10^3$ | 3.2 |
| Cu-BTC single components[828] | $2.4 \times 10^3$ | 4 |
| ZIF-7[829] | 15.4 | 35.8 |
| ZIF-62 glass[830] | $4.2 \times 10^3$ | 50 |
| NH2 − MIL−53[831] | $1.3 \times 10^5$ | 27.3 |
| ZIF-90[832] | $1.7 \times 10^5$ | 70.5 |
| Ni$_2$(L-asp)$_2$(bipy)[833] | $6 \times 10^4$ | 7.77 |
| ZIF-7[829] | 14.4 | 34.6 |
| MOF-5[834] | $1.89 \times 10^5$ | 64 |
| SIM-1[835] | $6.1 \times 10^3$ | 2.52 |
| Sod-ZMOF-1[836] | 36.5 | 1.4 |
| PSM-MOF[837] | $1.18 \times 10^3$ | 11.1 |
| Pebax ZIF-67 NP[838] | 10.7 | 1.444 |
| Pebax ZIF-67 MP[838] | 10.8 | 1.367 |
| Pebax Zif-67 NS[838] | 12.1 | 1.528 |
| Pebax 1675/CuNi[839] | 11.5 | 3.026 |
| PEEK-WC/CuNi[839] | 68.01 | 68.01 |
| 6FDA-BI[840] | 33.4 | 278.2 |
| P/Zn[813,840] | 31.8 | 278 |
| 6FDA-BI/20%ZIF-8[840] | 78.5 | 223.9 |
| 6FDA-BI/20%ZIF-8 0.004 Zn[813,840] | 88.2 | 233.4 |
| 6FDA-BI/20%ZIF-8 0.007 Zn[813,840] | 110.1 | 225.2 |
| 6FDA-BI/20%ZIF-8 0.01 Zn[813,840] | 72.3 | 318.3 |
| ZIF-67-in-TpPA-1[841] | $3.67 \times 10^3$ | 34.9 |
| ZIF-8-in-TpPA-1[841] | $3.92 \times 10^3$ | 23.1 |
| ZIF-67-in-TpBD[841] | $3.77 \times 10^3$ | 27.9 |

[a]The data are used in Fig. 5(a) and Fig. 48(a).

to match common operating conditions for urban PE pipelines. The authors used five PE chains each one with a degree of polymerization of 500 (corresponding to $C_{1000}H_{2002}$) to build an amorphous polymer phase. A molecular representation of the PE in the simulation box is shown in Fig. 42(f). In line with the similar studies reviewed earlier, solubilities, diffusivities, and permeabilities increased with temperature, while pressure was shown to have a negligible effect. The computed

solubilities and permeabilities are shown in Fig. 40 and Fig. 41, and listed in Table 13 and Table 14, respectively. As in the study by Su et al.,[746] the gas is shown to obey the hopping transport mechanism. The free volume increases with temperature, therefore, enhancing $H_2$ diffusivity. The computed permeabilities were shown to systematically over-predict the experimental data by 5 to 6 times in the whole temperature range considered, clearly indicating that there is room for improved predictions using molecular simulations. This can be achieved by either using more accurate combination of force fields and/or by fine-tuning the polymer chain characteristics (e.g., molecular weight, number of chains, degree of crystallinity).

Recently, $H_2$ permeation through HDPE and EVOH was studied by Zhang et al.[750] at conditions relevant to gas transport in polymer pipelines, i.e., 30 °C to 80 °C (303.15 - 353.15 K) and 25 - 100 bar. The authors constructed systems containing 12 HDPE (or EVOH) chains but the degree of polymerization or the molecular weight of the polymer chains is not mentioned. The representativeness of the model was validated by comparing the density of the simulation box containing the polymer matrix with experimental values. Similarly to all the previous studies discussed in this section, temperature was shown to have a strong effect on $H_2$ properties. In particular, as temperature increased from 30 °C to 80 °C, the solubility, diffusion, and permeability coefficients of $H_2$ in HDPE increased by 18.7%, 92.9%, and 129.0%, respectively. In EVOH, these coefficients increased by 15.9%, 81.6%, and 112.7%. EVOH exhibited superior $H_2$ barrier properties compared to HDPE due to the hydroxyl groups in EVOH forming strong hydrogen bonds that impede $H_2$ movement. The computed solubilities and permeabilities are shown in Fig. 40 and Fig. 41, and listed in Table 13 and Table 14, respectively. Zhang et al.[750] showed that the $H_2$ permeation mechanism involves two processes: adsorption, where the gas molecules aggregate in low-potential-energy regions; and diffusion, where $H_2$ molecules vibrate within confined spaces before occasionally transitioning between holes. Comparisons of the simulation data with experimental measurements of $H_2$ permeability in HDPE are provided, showing an agreement within 7.24% difference.

Except from the study of common thermoplastics such as PE and PA used mainly as liner materials in tanks and pipelines, the sorption and diffusivity of $H_2$ in poly(chloro-p-xylene)[754] (the simulation box containing the polymer is shown in Fig. 42(g)), PDMS Shi et al.,[749] and in rubbery polymers[755−757] have been reported in the literature. Stalker et al.[758] performed simulations of different cellulose configurations, i.e., purely crystalline (which showed no $H_2$ sorption), slit pore structures with varying inter-layer spacings (4.67-7.67 Å), amorphous phase, and "pinned" structures with fixed glycosidic oxygens. A molecular simulation snapshot of the slit pore configuration is shown in Fig. 42(h). $H_2$ molecules within the narrow slit pores were shown to occupy discreet positions, being trapped in the empty spaces between the cellulose layers. The authors showed that in the case of wide slit pores, this behavior is not obeyed, and $H_2$ has more freedom to move in between the polymer layers. While pure crystalline cellulose was found to be not suitable for $H_2$ storage, the modified structures showed potential at experimentally accessible pressures (<100 bar), suggesting that engineered cellulose-based materials could be a viable option. Yi et al.[759] performed MD simulations investigating the diffusion of $H_2$ and its isotopes; deuterium

**Table 16. Experimentally Measured $H_2/CO_2$ Permeabilities Gathered from Different Literature Sources[a]**

| Membrane | $P_{H_2}$ (Barrer) | $P_{H_2}/P_{CO_2}$ | Membrane | $P_{H_2}$ (Barrer) | $P_{H_2}/P_{CO_2}$ |
|---|---|---|---|---|---|
| UiO-66-NH2[842] | 213.2 | 6.8 | ZIF-8-in-TpPA-1[841] | 3772.04 | 28.73 |
| PEI/PVP-UiO-66-NH2[843] | 31 | 0.0787 | ZIF-67-in-TpBD-1[841] | 3490.05 | 23.85 |
| Matrimid/EDA/ZIF-90[844] | 19 | 9.5 | HKUST-1[816] | 176844 | 6.8 |
| PPO/Silica[845] | 257.23 | 3.6 | ZIF-7[852] | 54.2 | 8.4 |
| PI/NH2-MIL-53[846] | 384.1 | 16.7 | ZIF-7[814] | 340.8 | 6.48 |
| PI/ZIF-8/EDA[847] | 283.5 | 12 | ZIF-22[853] | 19572 | 7.2 |
| PIL/IL/MIL-53[848] | 0.14778 | 0.07519 | ZIF-8[854] | 3536.4 | 6 |
| PIL/IL/ZIF-8[848] | 0.0514 | 0.2 | NH2-MIL-53 (Al)[855] | 87750 | 30.9 |
| PEBAX-0H[849] | 0.04879 | 0.13769 | ZIF-8[856] | 2534.8 | 3.28 |
| PEBAX-2H[849] | 0.06889 | 0.11563 | Amine-Mg-MOF-74[857] | 2240 | 28 |
| PEBAX-4H[849] | 0.07507 | 0.11055 | MIL-96 (Al)[858] | 12260.8 | 8.8 |
| PEBAX-8H[849] | 0.08876 | 0.10430 | Zn_2(Bim)3[859] | 19.187 | 128.4 |
| PEBAX-12H[849] | 0.0808 | 0.10892 | PIM-EA-TB[860] | 7620.1 | 1.09 |
| PEBAX-24H[849] | 0.07652 | 0.10732 | PIM-SBI-TB[860] | 21697.4 | 0.76 |
| Glass ZIF-62[830] | 4597 | 2.25 | mPBO[861] | 178.5 | 6.2 |
| P84/ND[818] | 6.7 | 4.1 | PHBOA (8:2)[862] | 0 | 8 |
| Matrimid/ZIF-1 (10%)[819] | 28.11 | 4 | PBI[863,864] | 12.8 | 20 |
| 6FDA-TTM/Si-H (5%)[820] | 62.6 | 2.1 | PBI[865] | 3.6 | 8.6 |
| PI/MWCNT@GONRs (2%)[821] | 42.5 | 1.7 | PBI[866] | 2.9 | 7.1 |
| 6FDA-DAM-ZIF-11 (10%)[819] | 106.7 | 0.97 | PBI[867] | 27 | 16 |
| 6FDA-DAM-ZIF-11 (20%)[819] | 272.45 | 1.06 | BILP-101x (400 nm)[868] | 9.68 | 39.5 |
| 6FDA-DAM-ZIF-11 (30%)[819] | 76.76 | 1.05 | NUS-2@PBI[869] | 2.95 | 18.78 |
| P100G0[850] | 0.07465 | 0.10417 | [COF-300]- [Zn2(bdc)2(dabco)][870] | 130368 | 12.6 |
| P100G2[850] | 0.08241 | 0.11236 | [COF-300]- [ZIF-8][870] | 105520 | 13.5 |
| P100G5[850] | 0.14525 | 0.12821 | COF-300[870] | 107520 | 6 |
| P100G8[850] | 0.18277 | 0.14286 | COF-LZU1[871] | 1842.1 | 6 |
| ZIF-8[851] | 5411 | 4.5 | ACOF-1[871] | 1211.34 | 14.1 |
| CL 6FDA-durene[824] | 116.7 | 24.3 | COF-LZU1-ACOF-1[871] | 660.2 | 24.2 |
| 33 MMM[824] | 2137 | 1.4 | CTF-1[872] | 501 | 17.4 |
| 50 MMM[824] | 4157 | 1.3 | TpPa-1-30/GO-10[873] | 943.47 | 25.57 |
| CL 33 MMM[824] | 394.5 | 28.6 | [COF-300]- [UiO-66][874] | 117310 | 17.2 |
| CL 50 MMM[824] | 501 | 28.8 | COF-LZU1[875] | 7309.6 | 31.6 |
| CL skin alone on 33 MMM[824] | 12.5 | 34.6 | TFB-BD[875] | 7604.4 | 25.6 |
| CL skin alone on 50 MMM[824] | 13.9 | 32.4 | | | |
| CL skin alone on 6FDA-durene[824] | 11.1 | 31.7 | | | |
| ZIF-67-in-TpPA-1[841] | 3618.75 | 35.71 | | | |

[a]The data are used in Fig. 5(b) and Fig. 48(b).

($^2$H) and tritium ($^3$H) in PS under normal temperature (298 K) and pressure (1 atm). The research is motivated by the use of PS as a target material in Inertial Confinement Fusion (ICF), where understanding gas diffusion is critical for maintaining $^2$H-$^3$H mixtures within the targets. The authors studied PS models with varying degrees of polymerization (i.e., 60, 120, 180, and 240). Interestingly, the PCFF[406] was used for all species in this study, including $H_2$ and the isotopes. Diffusion coefficients were shown to decrease with increasing isotope mass ($H_2 > {}^2H > {}^3H$), and decrease with increasing polymer molecular weight. FFV correlates with diffusion behavior, with higher free volume leading to higher diffusion rates. The novel aspect of this study is the investigation of the isotopes diffusion coefficients in PS, which is particularly valuable for ICF research. These gases had not been previously studied in this context despite their importance in fusion applications. The work also establishes relationships between molecular weight, free volume, cohesive energy density, and diffusion behavior that could guide the development of improved target materials with reduced gas permeability. To the best of our knowledge, studies of $H_2$ permeation in polymers using coarse-grained approaches are limited (e.g., see Zhao et al.[760]) and out of this review.

Synthetic thermoset polymers which are primarily used as components in auxiliary equipment (e.g., gaskets, sealing rings) in $H_2$ storage infrastructure, with most notable the EPDM rubber, have been studied via molecular simulation. Wilson and Frischknecht[761] used an MC−based method to create a model of cross−linked EPDM. Subsequently, MD simulations using LAMMPS[762] were performed to study the rubber's behavior when filled with high $H_2$ at near−ambient temperature. The OPLS-AA[428] force field was used for all species. The authors computed $H_2$ solubilities (as a function of cross−link density) and diffusivities (as a function of the gas concentration). The reported data are in−line with previous simulations and experiments. The authors showed that rapid $H_2$ depressurization caused system volume to increase, and $H_2$ − accessible free volume to expand (with effects being more pronounced at high $H_2$ concentrations). Higher cross-link density increased $H_2$ − accessible free volume but reduced volume changes during decompression, and produced fewer large pores post−decompression. These findings indicate that higher cross−linking densities might help prevent cavitation in EPDM, though the additional free volume from cross−links could create potential cavitation initiation sites. The authors recommend experimental investigation of crosslinking density
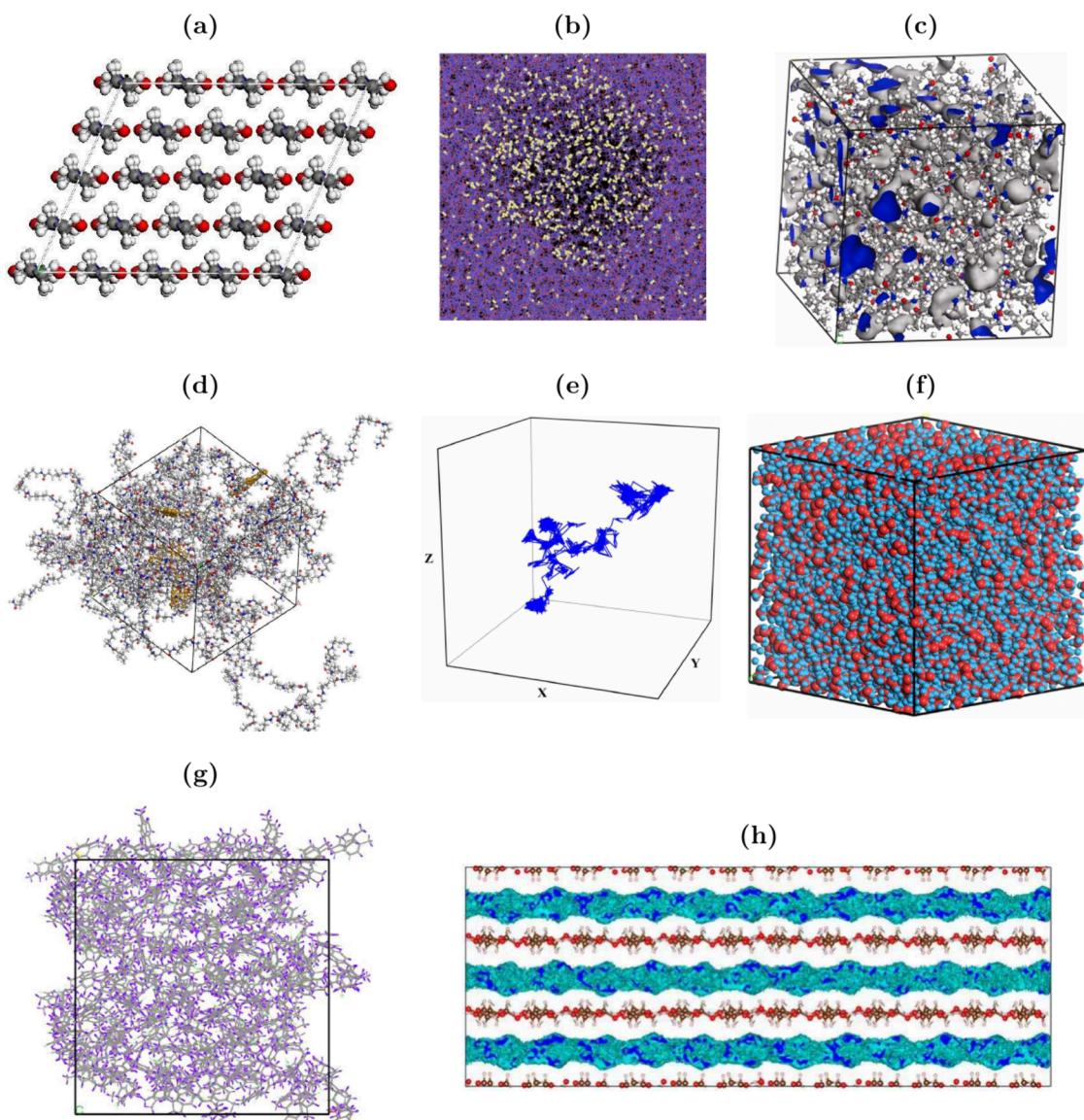
**Figure 42.** Simulation snapshots and molecular representations collected from different studies of H$_2$/polymer systems: (a) PA6 crystal structure shown in the x-y plane, (b) H$_2$ gas bubble in PE. H$_2$ molecules are shown in yellow; PE is shown in blue (C atoms) and the (H atoms), (c) free volume distribution in PA at 353 K, (d) a model graphene-modified PA6 system. Graphene atoms are shown in yellow, (e) the trajectory of a H$_2$ molecule in amorphous PA6 328 K and 0.1 MPa, (f) amorphous PE matrix. Carbon atoms are shown in blue and hydrogen atoms in red, (g) amorphous poly(chloro-p-xylylene) matrix, (h) H$_2$ sorption sites in a cellulose slit pore. [Panel (a) is reprinted with permission from Voyiatzis and Stroeks, Phys. Chem. B 2022, 126, 32, 6102-6111. Copyright 2022, American Chemical Society. Panel (b) is reprinted from International Journal of Hydrogen Energy, Vol 47, Jiawei Zhao et al., Molecular dynamics simulation of H$_2$ in amorphous polyethylene system: H$_2$ diffusion in various PE matrices and bubbling during rapid depressurization, 39572−39585, Copyright (2022), with permission from Elsevier. Panel (c) is reprinted from Materials Today Communications, Vol 35, Qing Fang, Dongmei Ji, Molecular simulation of hydrogen permeation behavior in liner polymer materials of Type IV hydrogen storage vessels, 106302, Copyright (2023), with permission from Elsevier. Panel (d) is reprinted from Li et al.,[745] open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY 4.0) license. Panel (e) is reprinted from International Journal of Hydrogen Energy, Vol 50, Part D, Ying Su et al., Hydrogen permeability of polyamide 6 as the liner material of Type IV hydrogen storage tanks: A molecular dynamics investigation, 1598-1606, Copyright (2024), with permission from Elsevier. Panel (f) is reprinted from Journal of Molecular Liquids, Vol 368, Part B, Dukui Zheng et al., Molecular dynamics investigations into the hydrogen permeation mechanism of polyethylene pipeline material, 120773, Copyright (2022), with permission from Elsevier. Panel (g) is reprinted from Computational Materials Science, Vol 49, Chunhai Lu et al., A molecular modeling study on small molecule gas transportation in poly (chloro-p-xylylene), S65-S69, Copyright (2010), with permission from Elsevier. Panel (f) is from Molecular simulation of hydrogen storage and transport in cellulose Molecular simulation of hydrogen storage and transport in cellulose, Stalker et al., Molecular Simulation, Vol 47, 170−179, Copyright (2010), reprinted by permission of the publisher (Taylor & Francis Ltd, http://www.tandfonline.com).]

effects on high−pressure H$_2$ − induced EPDM failure as a potential future research direction. In a complementary study by the same research group, Brownell et al.[763] performed all−atom classical MD simulations to examine how compositional changes affect gas diffusion in EPDM, in an effort to guide material design to rubbers less prone to H$_2$ − induced failure. The simulations revealed anomalous, sub-diffusive H$_2$ transport. Two distinct gas groups were identified: high−mobility

gas and low—mobility gas constrained by polymer interactions. Lower temperatures increased gas localization in the low—mobility group, creating necessary conditions for cavitation damage. At reduced temperatures, higher cross—link density enhanced $H_2$ mobility and decreased trapped $H_2$ fraction, suggesting increased cross—linking may minimize cavitation precursors. The authors applied a two—state kinetic model to determine energy requirements for transitions between mobility states.

Recently, Wilson et al.[764] expanded prior studies of EPDM by studying a composite material which incorporates silica into the rubber. The motivation is that elastomers with nano-sized fillers such as silica or carbon black achieve improved mechanical properties. Filler dispersion and filler-polymer interfacial strength are crucial factors in this enhancement. Interfacial strength is vital for component durability in pressurized gas sealing applications e.g., O-rings, where poor filler-polymer binding can create internal void formations. To understand fundamental mechanisms behind pressurized $H_2$-induced elastomer failure, the authors performed MD simulations to examine $H_2$ over-saturation effects on filler-polymer interaction strength. Consistently with their prior studies, the OPLS-AA[428] force field was used to model the polymer, while the parameters by[765] were for the silica surface. The authors systematically investigated the interface between EPDM and silica across varying $H_2$ gas concentrations, cross-link densities, and surface chemistries. The simulations showed that high $H_2$ concentrations (1000 $H_2$ molecules) caused significant interfacial failures, including hole formation and complete debonding, while lower concentrations (up to 750 $H_2$ molecules) did not cause debonding. $H_2$ preferentially accumulated at silica-EPDM interfaces, creating concentration gradients that persisted after decompression. Higher $H_2$ concentrations reduced adhesive strength between silica and EPDM, with surface hydroxylation and crosslink density influencing the debonding behavior. The results suggest that dissolved high-pressure $H_2$ can compromise silica-EPDM interfaces, potentially leading to bubble formation and cavitation-induced failure in $H_2$ environments.

As shown in Figs. 40 and 41, and the Tables 13 and 14, the simulation data reported in literature regarding $H_2$ solubilities and permeabilities in different polymeric matrices significantly vary. The computed solubilities and permeabilities collected from different authors span three orders of magnitude. While this is expected up to a degree due to the different pressures and temperatures considered, the fact that most of the studies use the same force fields (primarily COMPASS[316] and PCFF[406]) and similar methods, makes the discrepancies shown in Figs. 40 and 41 interesting. Despite the common elements in these studies, different $H_2$ force fields, system sizes, polymer chain lengths, and simulation schemes (e.g., for equilibration and production runs) are used, leading to diverging results. Another striking outcome after reviewing these datasets is that while all simulations seem to be able to capture the experimental permeability trend (i.e., qualitative agreement), the quantititative difference is more than three orders of magnitudes as shown in Fig. 41. This finding alone is a strong indication that there is still ground to cover for producing accurate predictions for $H_2$/polymer systems using molecular simulation. It is also important to mention here that caution should be exercised when interpreting computed results for solubilities and permeabilities due to the inherent difficulties in these simulations having to do with slow

dynamics, generic force fields, and computationally demanding systems. Another interesting point is that although we do not show here the collected data on computed diffusivities (which are used to compute permeabilities), none of the studies apply corrections to account for finite size effects.[498−500] It is not clear how big such effects are for the $H_2$/polymer systems, however, no investigation has been performed to shed light on this.

## 4.5. Hydrogen Solubility, Diffusivity, Permeability, and Interfacial Properties in Ionic Liquids

Separation of gases using ILs has been an active field in the molecular simulation community the past 20 years. Due to the ever increasing interest in developing carbon capture technologies for environmental and industrial purposes,[766] the vast majority of the ILs simulation studies have focused on both pure and mixtures of $CO_2$, with a lot of effort put on scrutinizing the diverse families of ILs. Following the same route, various thermodynamic and transport properties of $H_2$/ILs computed via MC and MD simulations have been reported to date. Shi et al.,[767] motivated by the carbon capture potential of the so-called supported IL membranes, performed molecular simulations to study the solubility, diffusivity, permeability, and partial molar properties of pure $H_2$, $CO_2$, and Ar, and their mixtures in 1-$n$-hexyl-3-methylimidazolium bis-(trifluoromethylsulfonyl)amide ([hmim][Tf$_2$N]). Molecular representations of the ions of these ILs are shown in Fig. 43. Two different $H_2$ force fields were compared: Buch[312] and Cracknell[311] (see Section 3.1.1). Notably, while the original Cracknell model is rigid, the authors implemented a flexible version to make it compatible with their hybrid MC method which involves a time reversible integrator (the authors explicitly note that traditional constraint dynamics methods for rigid molecules are time reversible, and thus, the original rigid $H_2$ could not be used in their scheme). Also, the effect of polarizability of $H_2$ on solubility was investigated, but it was shown to be negligible. The simulations were performed in a temperature range of 313−573 K and for pressures 1−500 bar for pure $H_2$, and 50−300 bar for mixed gas systems. The simulations showed that $H_2$ solubility in the IL increased with temperature, contradicting some prior experimental studies. Both force fields gave similar results for thermodynamic properties, though the Cracknell model showed better agreement with experimental data, particularly at high pressures. The molar volume of the ionic liquid was found to be the primary determinant of $H_2$ solubility, with a clear linear relationship between the Henry coefficient and molar volume. Based on an energy analysis, the interactions between $H_2$ and IL were shown to be ca. three to six times weaker than the interactions of the other gases with the IL. The selectivity of $CO_2$ over $H_2$ decreased from ca. 30 at 313 K to ca. 3 at 573 K. The authors showed that $H_2$ diffuses 5−12 times faster than $CO_2$, while the permeability of $H_2$ was 2.3−3.5 times larger than experiments. Shi et al.[767] highlight substantial differences in experimentally measured $H_2$ solubilities between research groups. These discrepancies (some showing solubility increasing with temperature, others showing the opposite) indicate difficulties in measuring solubility for such poorly soluble gases. The paper reports negative volume expansion when $H_2$ dissolves in the ionic liquid at high pressures, suggesting a compression effect. This is somewhat counter-intuitive but can be explained by the high pressures required for appreciable $H_2$ solubility. The authors conclude that good
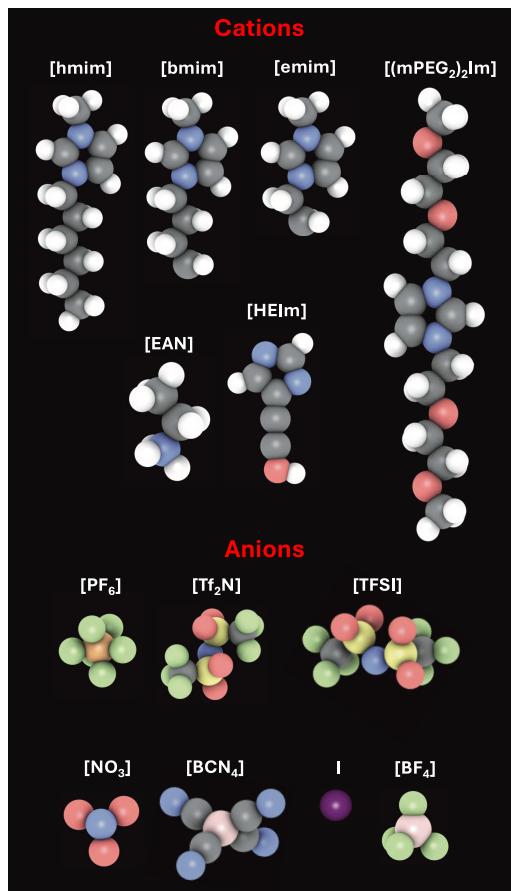
**Figure 43.** Molecular representations of the cations and anions of the ionic liquids studied in the papers reviewed here (iRaspa[483] visualization software was used). Color code for the atoms: gray: carbon, white: hydrogen, blue: nitrogen, red: oxygen, green: fluorine, dark yellow: phosphorous, yellow: sulfur, pink: boron, purple: iodine.

IL candidates for $CO_2/H_2$ separation should have low molar volumes (to reduce $H_2$ solubility) while maintaining high $CO_2$ solubility through strong interactions. This somewhat contradicts the observation that molar volume is positively correlated with gas solubility in general.

In a follow-up study, Shi and Sorescu[768] investigated how confining [hmim][Tf2N] IL in (20,20 and 9,9) CNTs (composite material) affects gas sorption properties. The authors used the same flexible version of Cracknell model.[767] The simulations were performed at temperatures up to 573 K and pressures up to 400 bar. It was shown that $H_2$ diffuses ca. 1.5 times faster than $CO_2$ in the composite material. In contrast, $H_2$ diffuses almost 10 times faster than $CO_2$ in both CNT and bulk IL. At 313 K, $H_2$ in the (20,20) CNT was shown to diffuse ca. 4900 times faster than in the composite material. CNT showed the highest $H_2$ sorption, followed by composite material and the bulk IL. For increasing temperature $H_2$ sorption: (i) increased in [hmim][Tf2N], (iii) decreased in CNT, and (iii) and remained almost unaffected in the composite material, which exhibited higher $CO_2/H_2$ sorption selectivity than both IL and CNT ( $S_{CO_2/H_2}$ = 15.0 ± 1.0, 39 ± 2, and 79 ± 2 for CNT, IL, and the composite, respectively). The authors suggest that the composite material would be superior to both IL and CNT for the $CO_2/H_2$ separation.

Singh et al.[391] presented a MC simulation study of the solubility of $CO_2$, $H_2$, and their mixtures in ILs 1-alkyl-3-methylimidazolium bis(trifluoromethanesulfonyl)amide ([$C_n$mim] [Tf2N], n = 4, 6). Molecular representations of the ions of these ILs are shown in Fig. 43. The motivation was the $CO_2/H_2$ separation in pre-combustion processes, for which understanding $S_{CO_2/H_2}$ in high-pressure/temperature gas mixtures is crucial. The authors have implemented advanced sampling algorithms (e.g., cavity-biased, configurational-biased, and "slow-growth" - for more details on these techniques, the reader is referred to the refs within Singh et al.[391]) to overcome the inherent difficulties in MC simulations of dense and complex systems, such as ILs. Simulations were performed at 333, 413, and 573 K, and pressures up to 300 and 80 bar for pure $H_2$ and mixtures, respectively. It was shown that $H_2$ solubility in ILs slightly increases with temperature (positive enthalpy of absorption), while the volume change upon $H_2$ absorption were negligible (e.g., <1% at 300 bar). $S_{CO_2/H_2}$ was shown to decrease significantly with temperature (from 40-60 at 333 K to 3-4 at 573 K). Interestingly, this study contradicts previous experimental findings by that suggested that $CO_2$ enhances $H_2$ solubility at high pressures. The work concludes that $CO_2$ and $H_2$ are absorbed almost ideally in these ILs, with no significant interactions between the two gases in the liquid phase at the studied conditions.

Ramdin et al.[769] performed MC simulations to predict the solubility of various pre-combustion gases including $H_2$ in 1-butyl-3-methylimidazolium bis(trifluoromethylsulfonyl)imide [bmim][Tf2N] (note that [bmim] is a different notation for the [$C_4$mim] cation, where b stands for butyl). Cracknell[311] force field was used to model $H_2$ and the model by Liu and Maginn[770] for the IL. The simulations were performed at 333.15 K and pressures up to 150 bar. The authors showed that $H_2$ has the lowest solubility among all studied gases ($H_2$S > $CO_2$ > $CH_4$ > CO > $N_2$ > $H_2$). Simulations under-predicted the $H_2$ solubility compared to experiments with the difference being 23-33.0%. The computed $S_{CO_2/H_2}$ was reported to be 38.3, while the experimental is 30.4. This value is close to the commercial solvent Selexol which as a respective selectivity of 25. This may indicate that the IL might not offer significant advantages despite its higher cost. This study showcases that despite the quantitative discrepancies between MC simulation and experiment, one should also keep in mind that solubilities of $H_2$ in ILs are difficult to measure experimentally with uncertainties being as high as 50%.

In their MC study, Wittich and Deiters[771] examined how the choice of simulation box geometry (cubic and orthorhombic) affects $H_2$ solubilities in ILs computed. The IL studied was 1-n-butyl-3-methyl-imidazolium hexafluorophosphate ([bmim]-[$PF_6$]) for temperatures ranging from 313 to 373 K at atmospheric pressure. Molecular representations of the ions of this IL are shown in Fig. 43. Similarly to the IL studies discussed earlier, the Cracknell[311] force field was used to model $H_2$, while the united-atom model by Shah and Maginn[772] was used for [bmim][$PF_6$]. The cubic simulation box was shown to yield Henry's constant values closer to experimental results for $H_2$, but still overestimated the experimental data by 14-57%. The authors observed that simulation box geometry significantly affects diffusivity, with the orthorhombic box showing faster diffusion rates. The authors mention that system size effects are present but could not fully investigate them due to computational constraints.

Despite this study suggested that for some properties, such as Henry's constants, the orthorhombic box may better represent the system by allowing more configurational freedom, this did not hold true for the case of $H_2$.

Klein et al.[773] performed DLS experiments and MD simulations to measure/compute the diffusivities (thermal and fick) of binary mixtures of [emim] / [hmim] / [C$_{10}$mim] [NTf$_2$] with $H_2$, He, $N_2$, $CO_2$, and Kr. This work is part of a large number of studies by the research group focusing on thermodynamic and transport properties of gas/liquid mixtures spanning alkanes, alcohols, and ILs. The temperature and pressure ranges covered were 298 - 423 K and 1 - 65 bar, respectively. The authors used various combinations of force fields (details are provided within ref 773) to identify suitable models for predicting densities, viscosities, and diffusivities. Klein et al.[773] reported self- (mentioned as thermal) and fick (component $D_{11}$) diffusion coefficients. For the whole temperature and pressure ranges, the computed diffusivities were in relatively close agreement (within 12%) with the experiments. The self-diffusivities of $H_2$ in [emim][NTf$_2$] ranged from 2.54 to $6.45 \times 10^{-9}$ m s$^{-1}$ for temperatures 298 to 348 K. For the same temperature range, the respective values for self-diffusivity of $H_2$ in [hmim][NTf$_2$] and [C$_{10}$mim]-[NTf$_2$] were similar (deviations of lower than 10% between the different solvents). Unlike in $n$-alkanes, the diffusivities of the gasses in the ILs were not significantly affected by the viscosity of the solvents.

Recently, Zhai et al.[774] investigated how $H_2$ affects both bulk (viscosity) and interfacial properties (surface tension) of three imidazolium-based ILs using both experiments and MD simulations. The ILs studied were the hydrophobic 1-ethyl-3-methylimidazolium bis(trifluoromethanesulfonyl) imide ([C$_2$C$_1$Im][NTf$_2$], also commonly abbreviated to [emim] [NTf$_2$] since e refers to the ethyl group) and 1-methyl-3-octylimidazolium hexafluorophosphate ([C$_8$C$_1$Im][PF$_6$]) as well as the hydrophilic 1,3-bis(2-(2-ethoxyethoxy)ethyl) imidazolium iodide ([(mPEG$_2$)$_2$Im]I). Molecular representations of the ions of these ILs are shown in Fig. 43. To model the ILs, the authors used the force fields by Kelkar and Maginn[388] and Seidl et al.[775] with optimized partial charges. For $H_2$ the IFF[313] model was used. The conditions examined where 303-393 K and 1 - 310 bar. The authors showed that $H_2$ has low solubility in all three ILs, with maximum values (in mole fraction units) of $\chi_{H2}$ = 0.092 for [C$_2$C$_1$Im][NTf$_2$] at 270 bar and 353 K and $\chi_{H2}$ = 0.041 for [(mPEG$_2$)$_2$Im]I at 310 bar and 393 K. It was shown that $H_2$ solubility is ca. 3.5 times higher in the hydrophobic [C$_2$C$_1$Im][NTf$_2$] than in the hydrophilic [(mPEG$_2$)$_2$Im]I at 353 K. Notably, $H_2$ appeared to only occupy existing voids in the IL rather than creating additional volume It was also shown that $H_2$ has no significant effect on the viscosities of ILs for pressures up to 80 bar. Nevertheless, the IL force fields overestimate the viscosity by a factor of 2-2.5 compared to experiments, though they capture the qualitative behavior. MD simulations revealed two counterbalancing effects, i.e., increased pressure compresses the liquid (increasing viscosity) while dissolved $H_2$ has a plasticizing effect (decreasing viscosity). Pressures had a small effect on the gas/liquid surface tension (ca. 6% decrease at 80 bar) which is due to the weak enrichment of the IL-gas interface with $H_2$. Overall, the effect of $H_2$ on the IL properties investigated is similar to what has been observed for non-electrolytic organic solvents.

Sharing the motivation with the studies discussed earlier, Rivera-Pousa et al.[776] studied $H_2$ absorption in the following protic and aprotic ILs: [EAN][NO$_3$], [HEIm][NO$_3$], [HEIm] [TFSI], [EMIm] [B(CN)$_4$], [EMIm][TFSI], [EMIm][NO$_3$], [EMIm] [BF$_4$], and a series of [C$_n$MIm][BF$_4$] with varying alkyl chain lengths ($n$ = 2, 4, 6, 8, 10, 12). Molecular representations of the ions of these ILs are shown in Fig. 43. The authors focused on high temperatures (550 K) and pressures (50 bar) because these conditions are relevant for processes such as Fischer-Tropsch synthesis. It was shown that $H_2$ solubility increased with alkyl chain length in cations. Also, $H_2$ molecules showed weak interactions with the ILs, while they preferentially occupied the apolar domains of the ILs. However, in ILs with nitrate anions, $H_2$ also occupied polar regions. Another finding was that the structure of ILs was almost insensitive to the presence of $H_2$, while free volume and cavity formation appear to be the most important factors affecting solubility. Interestingly, in this study unscaled charges for ions were used instead of scaled charges that are typically used to prevent sluggish dynamics (see also Section 3.1.3). The study revealed that even though nitrate-based ILs show the most favorable solvation enthalpies, they have the lowest $H_2$ solubility due to limited available void space.

## 4.6. Hydrogen Sorption and Diffusivity in Metal- and Covalent-Organic Frameworks and Zeolites

Molecular simulations play a central role in the pursuit of understanding the mechanisms underlying sorption, diffusion, and permeability of $H_2$, and the selectivity of $H_2$ mixtures in nanoporous media such as MOFs and COFs. For this reason, an extensive literature body is available, making the detailed review of this area here not feasible. Nevertheless, we provide a short overview of important, relevant, and relatively recent studies to showcase the range of applicability of MC and MD simulations in studying $H_2$ sorption phenomena, especially in light of AI and ML approaches.

As discussed in detail in Section 2.2, accurate modeling of separations of $H_2$/gas mixtures requires accounting for both sorption and diffusion of the species involved, as membrane permeability is determined by both these phenomena. Early simulation studies focused on such properties in MOFs,[777,778] particularly focusing on separations of $H_2$ from $CO_2$ and $CH_4$. Keskin and Sholl[130] performed GCMC and MD simulations to compute both sorption and diffusion of $H_2$, $CO_2$, $CH_4$, and $N_2$ in MOF-5. Wu et al.[779] developed a modified force-field for ZIF-8, enabling simulations of $H_2$ sorption and diffusion alongside other gases. In 2012, Keskin[780] reported simulation results for sorption, diffusion, gas permeability, and membrane selectivity of $H_2$ over $CH_4$, focusing on COFs. The authors demonstrated the superior performance of COF-6 compared to zeolites and MOFs. Krokidas et al.[418] explored the potential of functionalization of MOFs to design novel structures for membranes, offering unprecedented $H_2$/$CH_4$ separation efficiency.

Song and No[781] used GCMC calculations to study the influence of available volume, surface area, cation types (e.g., Mg, Mn, and Ca), and pre-adsorbed benzene on the $H_2$ capacity of zeolites. Song and No[781] showed that the available volume and surface area per mass of zeolite are the two parameters having the strongest correlation with $H_2$ storage capacities, and that pre-adsorbed benzene can significantly decrease $H_2$ storage capacity by lowering the available volume in the zeolite structure. Deeg et al.[782] investigated $H_2$
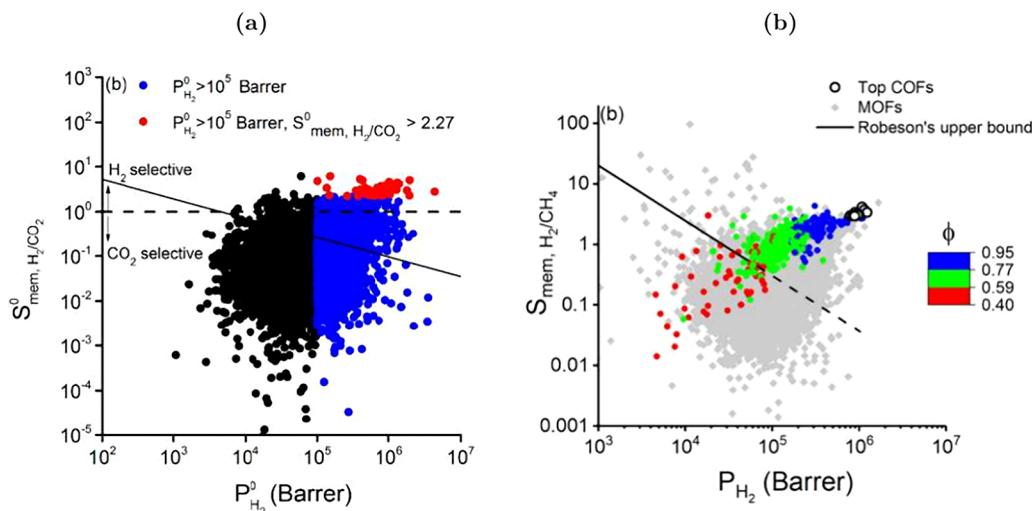
**Figure 44.** Robeson plots of (a) $H_2/CO_2$ membrane selectivities as a function of $H_2$ permeability for the MOFs studied by Avci et al.,[787] and (b) the high-performing $CH_4/H_2$ COFs, highlighting the importance of porosity, $\phi$, as a driving characteristic of separation performance.[789] [Panel (a) is reprinted from Avci et al.,[787] ACS Applied Materials & Interfaces, Vol 12, 41567−41579. Copyright 2020, American Chemical Society. Panel (b) is reprinted from ref 789. Industrial & Engineering Chemistry Research, Vol 60, 12999−13012. Copyright 2020, American Chemical Society (this publication is licensed under CC-BY-NC-ND 4.0)].

adsorption in two all-silica zeolites (i.e., ITQ-29 and MFI) at cryogenic temperatures using molecular simulations. This study revealed that a single-site $H_2$ force field with an uncharged LJ center can best reproduce experimental adsorption isotherms, while small adjustments to LJ parameters can significantly improved accuracy. It was also shown that in ITQ-29, $H_2$ preferentially adsorbs onto sodalite cages at low temperatures, creating a unique temperature-dependent pattern in heats of adsorption. In MFI, adsorption occured in sinusoidal channels at low temperatures.[782] The authors also incorporated quantum effects via the Feynman-Hibbs potential (see Section 3.1.1), demonstrating the importance of considering the quantum nature of $H_2$ to accurately model adsorption, especially at very low temperatures (i.e., 25 K). Extensive reviews of molecular simulations of $H_2$ adsorption on functionalized nanoporous materials are provided by Getman et al.[317] and Bobbitt and Snurr.[414]

Simulations have also played a crucial role in advancing the study of MMMs, effectively combining the cost-effective and scalable attributes of polymers with the high-performance capabilities of MOFs/COFs as fillers. Yilmaz and Keskin[783] explored diverse combinations of MOFs and polymers for $H_2/CH_4$ and $H_2/CO_2$ separations, towards the development of high-performing MMMs. The computed gas selectivity and permeability were compared with experimental data, showing good agreement. The authors also proposed new MOF-based MMMs exhibiting high performance for specific gas separations.

**4.6.1. High-Throughput Screening Simulations.** So far in this review, insights into $H_2$ separation mechanisms obtained solely from molecular simulations have been discussed. Nevertheless, the growing availability of structural databases and computational resources enabled a shift towards large-scale, high-throughput screening studies. This approach, comprising massive numbers of simulations, allows for the systematic evaluation of thousands of candidate materials, offering a data-driven perspective on separation performance. Early efforts focused on extracting simple structure-property relations from these datasets, often using visual/manual

inspection of simulation results or heuristic approaches based on intuitive structural descriptors such as pore size or surface area.[784] In recent years, however, the adoption of ML and AI has allowed for a more powerful and automated analysis of such relationships, enabling faster and more accurate prediction of material performance across vast chemical spaces. Such data-intensive approaches are efficient since the different structures comprising each family of nanoporous materials are in the order of hundreds of thousands. For example, ca. 100000 different MOF structures have been reported in literature, and more than half a million other MOF structures have been predicted to date.[785]

In the past decade, the significant advancements in high-performance computing have enabled researchers to conduct large-scale screening simulation studies, allowing for the evaluation of numerous material structures in terms of separation performance.[786] For instance, Avci et al.[787] performed high-throughput computational screening on a comprehensive subset of MOFs of the CSD database,[788] exploring the $CO_2$ capture and $H_2$ purification potential of 10221 MOFs. These simulations revealed the best-performing materials for PSA, vacuum swing adsorption (VSA), and TSA processes, outperforming commercial zeolites and previously studied MOFs in terms of $CO_2/H_2$ selectivity (see Fig. 44a).

Similarly, Altintas et al.[790] focused on the comparison of two widely used computation-ready MOF databases, i.e., CoRE[791] and CSDSS.[792] The authors id entified 3490 common MOFs in these databases and conducted simulations to compute their $CH_4$ and $H_2$ uptakes. The study also highlighted 'problematic' MOFs exhibiting different gas uptakes depending on the database used, leading to significant variations in ranking and material selection. Aksu et al.[793] focused on COFs for $CO_2/H_2$ separation using a high-throughput computational screening approach on the CoRE COF.[794] This study covered 288 experimentally synthesized COFs, providing valuable insight into the performance of COFs as adsorbents and membranes for pre-combustion $CO_2$ capture. Notably, many COFs outperformed traditional zeolites in terms of $CO_2$ selectivity and working capacities. The structural analysis revealed that

COFs with specific pore sizes and porosities are potential adsorbents for selective $CO_2/H_2$ separation. Aksu et al.[149] extended the screening to a database of hypothetical COFs (hypoCOF). Through an extensive series of molecular simulations, the authors identified top-performing hypoCOFs as adsorbents and membranes for $CO_2$ capture and $H_2$ purification. The findings of this study indicated higher $CO_2$ selectivities and working capacities compared to experimentally synthesized COFs under specific conditions. The study also emphasized the importance of hydrogen bonding between $CO_2$ and functional groups of linkers for $CO_2$ selectivity in hypoCOFs. Altundal et al.[789] explored the separation potential of COFs for $CH_4$ purification from gases such as $H_2$, $N_2$, and $C_2H_6$. By combining GCMC and MD simulations, they assessed adsorption and membrane-based separation performances of 572 COFs. The results demonstrated that COFs have the potential to outperform conventional adsorbents in $H_2$/$CH_4$ separations. Additionally, this study identified structural features related to high selectivities and permeabilities, offering a basis for designing COFs with exceptional $CH_4$ separation performance. For example, Fig. 44b shows that higher porosity values, $\phi$, result to higher separation performance. Avci et al.[795] investigated the influence of metal exchange in MOFs on $CO_2/H_2$ and $CO_2/CH_4$ separation performances. By exchanging Zn nodes with different metals, they obtained 32 metal-exchanged MOFs (M-MOFs), and showed that the exchange of Zn with V and Cr significantly improved $CO_2$ uptakes and adsorption selectivities. These molecular-level insights can provide a valuable guide for designing MOFs with enhanced $CO_2$ separation efficiency.

Zeolites, are another class of porous media similar to MOFs and COFs in many aspects. Zeolites are crystalline aluminosilicate materials characterized by a well-defined, micro-porous structure composed of interconnected channels and cages. These materials have long been studied for applications in gas storage and separation because of their inherent thermal and chemical stability. Despite their attractive structural features, the storage capacities of $H_2$ in unmodified zeolites (e.g., without structural modifications and doping with metals or other additives) are unsatisfactory (i.e., ca. 0.2-1.1 wt % $H_2$).[796] Molecular simulations are used in the literature to identify critical features that can enhance $H_2$ storage capacities and to design new zeolite structures suitable for $H_2$ storage applications.[781,782,797,798] Manda et al.[797] explored the $H_2$ storage capacities of 233 zeolites using GCMC simulations combined with ML. An impressive $H_2$ storage capacity of 4.8 wt% $H_2$ was reported in the Linde Type A structure, attributed to the low mass of the zeolite and the large gravimetric and volumetric surface area.[797] For a more detailed discussion of $H_2$ storage in zeolites the reader is referred elsewhere.[796,797,799]

**4.6.2. Artificial Intelligence and Machine Learning to Accelerate Material Screening.** Building on the advancements of high-throughput screening and the increasing availability of structure databases, such as the aforementioned CoreMOF,[800] hypoCOF,[801] CoRE COF,[802] as well as, the Inorganic Crystal Structure Database (ICSC),[803] Crystallographic Open Database (COD),[804] and the Cambridge Structural Database (CSD),[805] the scientific community has witnessed a flourishing interest in the utilization of AI and ML as a powerful approach for screening and designing $H_2$-related processes involving MOFs and COFs. Particularly in the context of functionalized, nanoporous solids, these techniques offer a remarkable opportunity to explore and comprehend

intricate structure-property correlations.[806] Ahmed et al.[198] evaluated the $H_2$ storage capacities of ca. 20000 different MOF structures using MC simulations (results are shown in Fig. 45). The authors, then, used the data to train a ML model, which was used to screen nearly half a million different MOF structures.
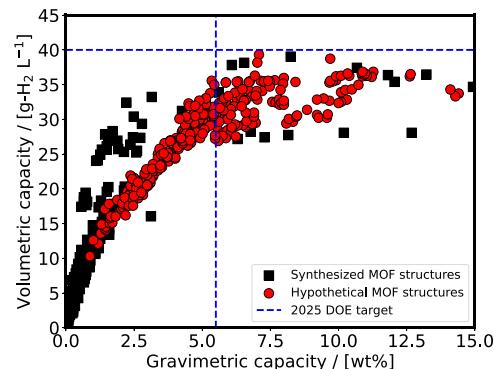


**Figure 45.** Volumetric and gravimetric capacities of $H_2$ for different MOFs computed with using GCMC simulations.[198] The volumetric and gravimetric capacities are computed at 77 K for a pressure swing of 100 bar to 5 bar. Various MOF structure databases were utilized for the GCMC simulations conducted by Ahmed et al.,[198] including databases containing synthesized MOF structures as well as databases of hypothetical MOF structures. The data for this plot is obtained from the work of Ahmed et al.[198]

Recently, Chen et al.[151] presented empirical-Morse force fields based on ab-initio calculations for interactions of $H_2$ with Mg-alkoxides. The empirical force fields are then used to perform high-throughput GCMC simulations of ca. 3000 metal-alkoxide functionalized COF structures, and to develop ML models to predict $H_2$ capacities.[151] Bucior et al.[807] developed a data-driven approach using sparse regression models to predict gas adsorption in MOFs, enabling rapid exploration of large databases and identification of top-performing candidates like MFU-4l. Similarly, Dureckova et al.[808] used ML to construct quantitative structurerelationship (QSPR) models for $CO_2$ working capacities and $CO_2/H_2$ selectivities in MOFs. Their work demonstrated that ML can accurately predict the performance of MOFs, even in topologically diverse databases, while significantly accelerating the screening process. Yang et al.[809] utilized ML algorithms, such as decision trees and random forests, to predict the separation performance of computational-ready MOF membranes for $H_2$-related separations, such as $H_2/CO_2$, $H_2/CH_4$, $H_2/N_2$ and $He/H_2$. By analyzing structural feature descriptors and principal components, the authors successfully identified the best-performing MOFs for each binary gas mixture.

Shi et al.[810] summarized recent progress in ML-assisted high-throughput computational screening of MOFs, including applications in $CH_4$ storage, $H_2$ storage, and $CO_2$ separations. The authors showed that the use of ML models improved the screening speed by several orders of magnitude and facilitated the identification of high-performance materials. Bai et al.[811] explored the application of high-throughput computational screening and ML for evaluating the $H_2$ separation performances of COF membranes. Their models efficiently predicted permeability and selectivity, enabling the identification of top-performing COFs for $H_2$ separation. Fig. 46 shows the
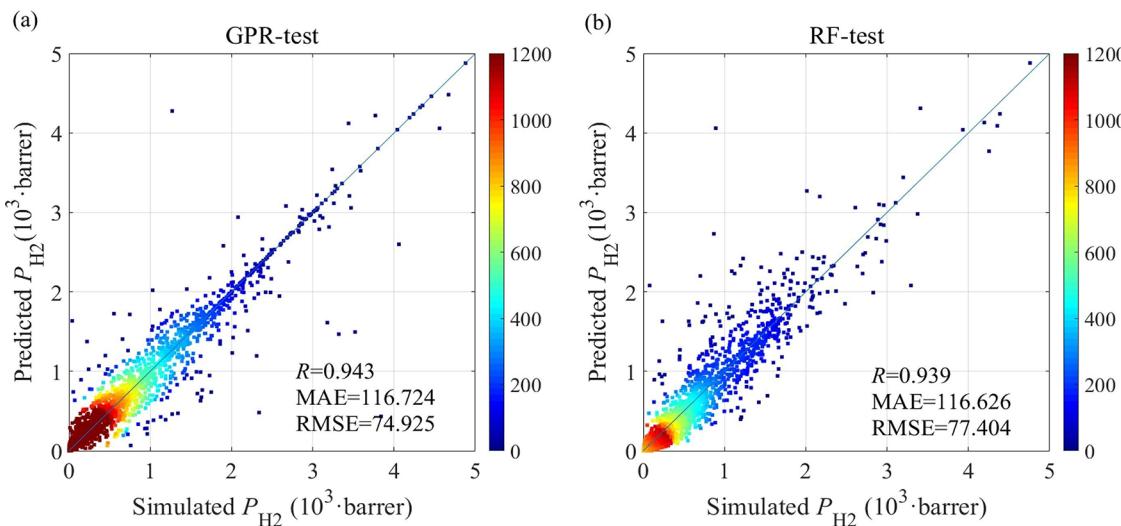
**Figure 46.** Predictions compared with the data of the test set (simulations) for $P_{H_2}$ made with (a) GP and (b) with RF, from the work of Bai et al.[811] [The figure is reprinted from Chemical Engineering Journal, Vol 446, Xiangning Bai et al., Machine−Learning−Assisted High−Throughput computational screening of Metal−Organic framework membranes for hydrogen separation, Copyright (2022), with permission from Elsevier].

performance of Gaussian Processes (GP) and Random Forest (RF) regression models in predicting the permeability of TMSP of $H_2$, in the form of parity plots (i.e., predictions vs simulation results). Aksu and Keskin[153] introduced a high-throughput computational screening approach combined with ML for assessing synthesized and hypothetical COFs for $CH_4$/$H_2$ separation. By developing ML models based on simulation results on 7700 COFs of the 69800 in total in their dataset, these authors accurately predicted the adsorption properties of hypothetical COFs and identified the top-10 performing COFs in VSA and PSA processes as shown in Fig. 47.
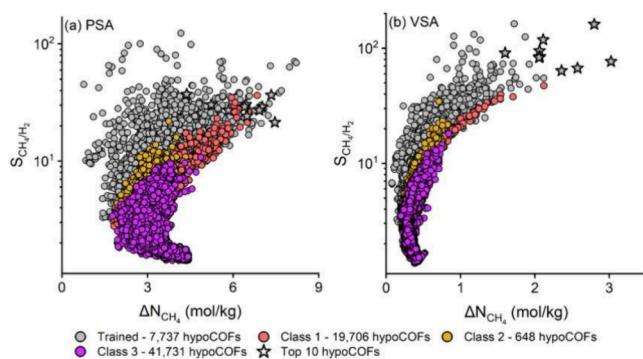


**Figure 47.** ML predictions of $CH_4$/$H_2$ performance for (a) PSA and (b) VSA processes. [The figure is reprinted from Journal of Materials Chemistry A, Aksu and Keskin,[153] Advancing $CH_4$/$H_2$ separation with covalent organic frameworks by combining molecular simulations and machine learning (This article is licensed under a Creative Commons Attribution-NonCommercial 3.0 Unported Licence - CC BY-NC 3.0)].

As a concluding remark, it is important to highlight that the design of materials for $H_2$-gas separations, with molecular simulation as the enabling tool, can pave the way for membranes with unprecedented performance. Fig. 48 illustrates this potential by comparing predicted materials from simulations with state-of-the-art synthesized membranes. These Robeson plots show that *in silico* designed nanoporous materials, such as MOFs and COFs, not only outperform

conventional polymer membranes but also exceed the performance of previously studied functionalized porous materials. Notably, many of the predicted structures lie beyond the traditional upper bounds for both $H_2$/$CH_4$ and $H_2$/$CO_2$ separations, demonstrating that simulation-guided design can expand the accessible membrane performance space. Table 17 provides a list of the available simulation data from high-throughput screenings and ML studies in literature. We provide data for the diffusivity, permeability, and sorption of $H_2$ mixtures on various functionalized nanoporous materials. It is important to note that most computational studies of MOF/COF membranes assume defect-free, perfectly crystalline, and rigid structures. While this practice is useful for identifying intrinsic transport limits, it represents a highly idealized model which may differ significantly from real, defect-containing, and flexible membranes.

## 4.7. Adsorption and Diffusivity of Hydrogen in Clay-Rich Reservoirs

Here, we summarize the findings from MD and GCMC studies (also see Table 18) to clarify how the insights presented for mechanisms such as adsorption, solubility, diffusivity, and intercalation processes influence the efficiency of UHS. We first discuss competitive adsorption on rock surfaces, then discuss $H_2$ solubility in confined water, pore-scale transport dynamics, and intercalation within layered geological structures. Researchers frequently use substrates such as kaolinite and graphite in $H_2$ storage studies due to their distinct yet complementary properties, enabling systematic exploration of adsorption and diffusion at the molecular scale. Kaolinite, an abundant clay mineral characterized by a 1:1 layered structure, exhibits two distinct surfaces (hydroxylated (gibbsite) and siloxane) resulting in varying $H_2$−solid interactions. These properties make kaolinite ideal for modeling the heterogeneous pore surfaces found in subsurface reservoirs.[877] Conversely, graphite and its derivative graphene offer high chemical stability, low mass, and a well-defined 2D structure, serving as proxies for organic-rich fractions commonly found in shale formations.[878,879] The utilization of these representative substrates enables the systematic evaluation of how pore size, temperature, and pressure influence adsorption and diffusion,
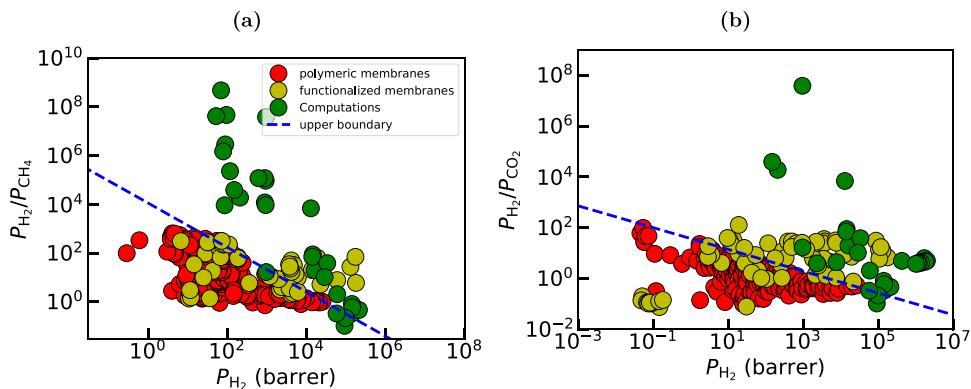
**Figure 48.** Robeson plots of (a) $H_2/CH_4$ and (b) $H_2/CO_2$ separation depict the impact of computational-empowered design. Functionalized nanoporous materials engineered through simulations surpass the current, experimentally measured polymers and functionalized nanoporous materials, showcasing unprecedented gas separation performance. The literature results on polymeric membranes are taken from the seminal work of Robeson.[136] The experimental and computational data for functionalized materials are collected from an extended survey of the authors, and are listed in Tables 15, 16, and 17.

which are key properties for assessing UHS viability. Additionally, the well-characterized nature of materials such as kaolinite and graphite facilitates the validation of molecular simulations against experimental data, thereby refining theoretical models. The distribution of substrates adopted in the reviewed studies is summarized in Fig. 49.

**4.7.1. Competitive Adsorption on Organic and Inorganic Substrates.** For applications pertaining to subsurface storage like UHS, $H_2$ must stick to rock surfaces effectively but remain easy to retrieve, often competing with cushion gases like $CH_4$ and $CO_2$. We review articles studying the adsorption of gas mixtures in organic and inorganic nanopores. Ho et al.[880] performed molecular simulations to study the adsorption and diffusion of $H_2$ and $CH_4$ in shale systems, with a particular focus on kerogen. The study demonstrates that $CH_4$ exhibits a substantially higher excess adsorption than $H_2$ over the entire pressure range, with the total $CH_4$ uptake reaching approximately 3.3 mmol/g at a $CH_4$ pressure of ca. 100 bar. Moreover, the computed interaction energies indicate that kerogen has a much stronger affinity for $CH_4$ (with a minimum interaction energy of ca. -4.3 kcal/mol) compared to $H_2$ (ca. -1.8 kcal/mol), which explains the preferential adsorption of $CH_4$. When simulating a competitive 1:1 $CH_4$:$H_2$ mixture, the kerogen selectivity for $CH_4$ is found to be more than 10 to 25 times higher than that for $H_2$, corroborating existing literature and experimental insights. The simulations further reveal that under conditions of low residual $CH_4$ partial pressure, up to 30−35% of adsorbed $CH_4$ desorbs upon $H_2$ injection. The overall $H_2$ uptake in kerogen is of the same order of magnitude as that observed in coal, reinforcing the broader relevance of the results. The MD simulations also predicted that the diffusion coefficient of $H_2$ in the kerogen matrix is approximately $20-40 \times 10^{-9}$ $m^2/s$, which is approximately one order of magnitude higher than that for $CH_4$ and $CO_2$, in agreement with comparative studies. These simulation results effectively complement their NMR experiments, which have independently observed distinct signatures for free versus adsorbed $H_2$ in shale. Overall, the study provides a molecular-level understanding of the competitive adsorption phenomena, highlighting that the dominance of $CH_4$-kerogen interactions must be considered when designing $H_2$ geological storage projects.

Zhang et al.[881] performed GCMC simulations to explore $H_2$ adsorption in shale nano-pores for both organic (kerogen) and inorganic (montmorillonite, MMT) substrates at 333.15 K and pressures up to 180 bar, finding that pure $H_2$ exhibits nearly twice the excess adsorption on kerogen relative to MMT (yielding a higher absolute storage capacity) while recovery efficiency − defined as the percentage of gas retrieved when pressure is reduced from 180 bar to 3 bar − remains similar between the substrates. In competitive adsorption tests with equimolar mixtures of $CH_4$ and $H_2$, $CH_4$ preferentially adsorbs on kerogen (with selectivity values above one) and, although $CH_4$ still adsorbs more strongly in MMT, overlapping adsorption layers result in a smaller competitive difference; additionally, the presence of cushion gases dramatically reduces $H_2$ storage capacity (by about 50% in 5 nm pores and up to 80% in 2 nm pores) due to $H_2$ dilution and competitive displacement, with the effect intensifying as pore size decreases and $CO_2$ proving more effective than $CH_4$ (yielding $CO_2/H_2$ selectivity values up to 18 in 2 nm pores), thereby underscoring how pore size, substrate type, and specific gas interactions govern adsorption and recovery, which is critical for optimizing UHS processes.

Kahzadvand et al.[882] investigated the partitioning behavior of a $H_2$ and cushion gas ($CO_2$ or $CH_4$) mixture within clay mineral pores to assess caprock integrity during UHS. Using advanced non-equilibrium molecular simulations at 333 K and 150 bar, this study provided molecular-level insights by using constant reservoir composition MD (CRC-MD) which dynamically maintains fixed fluid compositions in designated regions, thereby overcoming limitations such as feed depletion and composition control seen in traditional methods. The results reveal that pores narrower than 0.5 nm are impermeable to both $H_2$ and cushion gases, while $H_2$, owing to its superior rotational degrees of freedom, begins to penetrate at pore widths between 0.5 and 0.6 nm, with a notable increase in number density observed at these dimensions. In contrast, cushion gases, particularly $CO_2$, exhibit a stronger affinity for the clay surfaces and edges, dominating pore occupancy in interlayer spaces up to approximately 2 nm. Quantitatively, the simulations show that in montmorillonite and illite pores, the mole fraction of $CO_2$ initially exceeds that of $H_2$ at 0.6 nm for $CO_2/H_2$ mixtures, with parity reached only at larger pore sizes (around 5 nm in montmorillonite and 7 nm in illite). For $H_2$/

**Table 17. Sorption, Diffusivity, and Permeability Data Collected from Molecular Simulation Studies of Pure H$_2$ and H$_2$ Mixtures in Different Functionalized Nanoporous Materials**

| Study | Material | Sorption Selectivity | | Diffusion Selectivity | | $D_{H_2}(10^{-10}m^2/s)$ | Permeability Selectivity | | $P_{H_2}$ (barrer) |
|---|---|---|---|---|---|---|---|---|---|
| | | $CH_4/H_2$ | $CO_2/H_2$ | $H_2/CH_4$ | $H_2/CO_2$ | | $H_2/CH_4$ | $H_2/CO_2$ | |
| Yang et al.[876] | MOF-5 | 5 | | | | | | | |
| Liu et al.[778] | Cu-BTC | 10 | | | | | | | |
| | IRMOF-9 | 13.51 | | | | | | | |
| | IRMOF-10 | 3.48 | | | | | | | |
| | IRMOF-11 | 18.53 | | | | | | | |
| | IRMOF-12 | 6.31 | | | | | | | |
| | IRMOF-13 | 17.15 | | | | | | | |
| | IRMOF-14 | 5.3 | | | | | | | |
| Wu et al.[779] | ZIF-8 | | | 571.43 | 41.67 | 2.28 | | | |
| Keskin[780] | COF-5 | 9.894 | | 6.06 | | | 0.612 | | |
| | COF-6 | 17.223 | | 4.785 | | | 0.272 | | |
| | COF-10 | 4.741 | | 7.09 | | | 1.484 | | |
| Krokidas et al.[418] | ZIF-8 | 14.1 | 21.8 | 277.8 | 33.3 | $1.6 \times 10^{-8}$ | 20 | 1.49 | $1.62 \times 10^4$ |
| | ZIF-67 | 14.1 | 24.1 | $2 \times 10^{-3}$ | 9.1 | $8.7 \times 10^{-9}$ | 16.67 | 0.09 | $9.66 \times 10^2$ |
| | BeIF-1 | 28.9 | 49.1 | $1.1 \times 10^9$ | 45.5 | $9.4 \times 10^{-10}$ | $3.85 \times 10^7$ | 0.62 | $9.55 \times 10^2$ |
| | ZIF-7-8 | 23.7 | 47.4 | $4.81 \times 10^5$ | 238.1 | $2.4 \times 10^{-10}$ | $1.9 \times 10^4$ | 3.15 | $2.1 \times 10^2$ |
| | Co-ZIF-7-8 | 25.1 | 49.1 | $9.43 \times 10^5$ | 90.9 | $1.7 \times 10^{-10}$ | $3.9 \times 10^4$ | 3.49 | $1.5 \times 10^2$ |
| Yilmaz et al.[783] | ZIF-2 | | | 2.48 | 11.7 | $6.20 \times 10^{-8}$ | 0.104 | 0.175 | $9.21 \times 10^4$ |
| | ZIF-3 | | | 7.33 | 73.3 | $1.10 \times 10^{-7}$ | 0.343 | 0.987 | $1.49 \times 10^5$ |
| | ZIF-10 | | | 5.71 | 13.3 | $1.60 \times 10^{-7}$ | 0.465 | 0.409 | $2.13 \times 10^5$ |
| | ZIF-11 | | | 9.23 | 17.1 | $1.20 \times 10^{-7}$ | 0.812 | 0.598 | $1.41 \times 10^5$ |
| | ZIF-12 | | | $1.86 \times 10^3$ | 15.3 | $1.10 \times 10^{-8}$ | 88.3 | 0.251 | $1.45 \times 10^4$ |
| | ZIF-60 | | | $1.45 \times 10^{11}$ | $2.16 \times 10^9$ | 1.1 | 70.4 | 0.460 | $1.41 \times 10^4$ |
| | ZIF-65 | | | 6.32 | 23.1 | $1.20 \times 10^{-7}$ | 0.593 | 0.658 | $1.45 \times 10^5$ |
| | ZIF-67 | | | $5.32 \times 10^2$ | $8.25 \times 10^2$ | $3.30 \times 10^{-8}$ | 38.7 | 11.6 | $3.37 \times 10^4$ |
| | ZIF-69 | | | $1.29 \times 10^5$ | 22.9 | $1.10 \times 10^{-8}$ | $6.9 \times 10^3$ | 0.409 | $1.30 \times 10^4$ |
| | ZIF-78 | | | 54.5 | $1.13 \times 10^2$ | $5.40 \times 10^{-8}$ | 2.05 | 1.67 | $6.02 \times 10^4$ |
| | ZIF-79 | | | $2.89 \times 10^2$ | $2.00 \times 10^2$ | $2.80 \times 10^{-8}$ | 10.4 | 2.02 | $2.88 \times 10^4$ |
| | ZIF-81 | | | 7.00 | 91.3 | $8.40 \times 10^{-8}$ | 0.214 | 1.34 | $9.93 \times 10^4$ |
| | ZIF-90 | | | 9.00 | $2.84 \times 10^2$ | $5.40 \times 10^{-8}$ | 0.333 | 4.03 | $5.80 \times 10^4$ |
| Avci et al.[787] | FOTNIN | | 12 | | 76.05 | $1.35 \times 10^{-6}$ | | 6.34 | $1.67 \times 10^6$ |
| | BAZGAM | | 3.47 | | 17.42 | $1.51 \times 10^{-6}$ | | 5.02 | $1.97 \times 10^6$ |
| | PESSUE | | 3.93 | | 19.42 | $3.86 \times 10^{-7}$ | | 4.94 | $4.26 \times 10^5$ |
| | XANLIJ | | 2.95 | | 13.55 | $8.39 \times 10^{-7}$ | | 4.59 | $1.83 \times 10^6$ |
| | AVAJUE02 | | 4.1 | | 18.06 | $1.01 \times 10^{-6}$ | | 4.4 | $1.33 \times 10^6$ |
| | XAHQAA | | 4.52 | | 18.84 | $1.06 \times 10^{-6}$ | | 4.17 | $1.40 \times 10^6$ |
| | KAZSIQ | | 7.25 | | 29.82 | $9.08 \times 10^{-7}$ | | 4.11 | $1.21 \times 10^6$ |
| | CEFNOT | | 5.25 | | 20.94 | $8.67 \times 10^{-7}$ | | 3.99 | $1.15 \times 10^6$ |
| | XAHPUT | | 4.72 | | 18.47 | $8.83 \times 10^{-7}$ | | 3.91 | $1.16 \times 10^6$ |
| | NIBJAK | | 4.78 | | 18.17 | $7.65 \times 10^{-7}$ | | 3.8 | $1.02 \times 10^6$ |
| Aksu et al.[793] | PE-COF-I (for PSA) | | 368.2 | | | | | | |
| | NPN-2 (for PTSA) | | 2196.1 | | | | | | |
| | NPN-2 (VSA) | | 566.3 | | | | | | |
| | NPN-1 (TSA) | | 856.8 | | | | | | |
| | NPN-1 (VTSA) | | 936 | | | | | | |
| Aksu et al.[149] | linker99_C_linker100_C_pts (PSA) | | 229 | | | | | | |
| | linker92_C_linker92_C_bpi (VSA) | | 336 | | | | | | |
| | linker103_CH_linker89_N_unh (membrane) | | 0.49 | | 12.5 | | | 6.14 | |
| | linker91_CH_linker95_N_bod | | 0.67 | | 9 | | | 6.04 | |
| Altundal et al.[789] | CTF-FUM (VSA) | 102.7 | | | | | | | |
| | COF-303 | 21.84 | | | | | | | |
| Yang et al.[809] | TUMGOX | | | | | | $1.2 \times 10^4$ | 4.39 | $8.9 \times 10^2$ ($H_2/CH_4$) |

**Table 17. continued**

| Study | Material | Sorption Selectivity | | Diffusion Selectivity | | $D_{H_2}(10^{-10} m^2/s)$ | Permeability Selectivity | | $P_{H_2}$ (barrer) |
|---|---|---|---|---|---|---|---|---|---|
| | | $CH_4/H_2$ | $CO_2/H_2$ | $H_2/CH_4$ | $H_2/CO_2$ | | $H_2/CH_4$ | $H_2/CO_2$ | |
| | HEDCEA | | | | | | $9.4 \times 10^3$ | 3.95 | $7.75 \times 10^3$ ($H_2/CO_2$) $9.35 \times 10^2$ ($H_2/CH_4$) $2.35 \times 10^3$ ($H_2/CO_2$) |
| Bai et al.[811] | IDAZEU | | | | | | $9.4 \times 10^4$ | | 935.42 |
| | WENSIS | | | | | | $1.2 \times 10^5$ | | 890.06 |
| | YAFGAP | | | | | | $1.2 \times 10^5$ | | 614.29 |
| | BEVQUP | | | | | | $4.7 \times 10^7$ | | 95.68 |
| | BEVQID | | | | | | $2.3 \times 10^5$ | | 117.45 |
| | JASNEX | | | | | | $2.9 \times 10^6$ | | 88.9 |
| | NIRDEX | | | | | | $1.5 \times 10^6$ | | 78.75 |
| | HIWXER | | | | | | $4.2 \times 10^7$ | | 52.27 |
| | NAXKOO01 | | | | | | $9.2 \times 10^3$ | | 85.78 |
| | EMANAH | | | | | | $4.8 \times 10^8$ | | 69.68 |

$CH_4$ systems, $CH_4$ fails to penetrate below 0.6 nm, highlighting a selective permeation linked to molecular size, while at 1 nm, $CH_4$ occupancy peaks with relative ratios of about 0.6:0.4 compared to $H_2$, before declining at larger pore sizes. The study underscores that the effectiveness of cushion gas in inhibiting $H_2$ leakage is strongly dependent on pore thickness and clay surface charge, with $CO_2$ showing higher adsorption owing to electrostatic interactions with negatively charged sites and exchangeable cations. Furthermore, the detailed analysis via 2D density maps illustrates that gas molecules accumulate preferentially in the mid-interlayer region and near the clay edges, which correlates well with experimental observations and prior simulation studies. New physics uncovered include the dynamic interplay between rotational freedom of $H_2$ and the surface affinity of cushion gases, leading to qualitatively different partitioning behaviors in nano-pores (pore sizes < 2 nm) versus meso-pores (pore sizes > 2 nm). The CRC-MD approach thus not only clarifies the penetration thresholds (e.g., 0.5, 0.6, and 2 nm) but also reveals that for pore sizes larger than 4 nm, the gas composition approaches bulk behavior. Overall, this work provides a comprehensive molecular explanation for the dual role of cushion gases as both pressure maintenance agents and leakage barriers in $H_2$ geo-storage applications.

Muther and Dahagi[883] performed a study of $H_2$ adsorption on kaolinite using GCMC simulations to elucidate adsorption mechanisms under varying geological conditions. The study validates its simulation setup by comparing the computed $CO_2$ adsorption isotherms with experimental measurements taken at 298.15 K and pressures ranging from 0.2 to 1 bar, thereby establishing a robust basis for subsequent simulations. The results show that under high-pressure (10−500 bar) and elevated temperature (323−403 K) conditions, pure $H_2$ adsorption on kaolinite ranges from 0.0494 to 2.237 mol/kg; specifically, $H_2$ uptake increases with pressure and decreases with temperature. When $H_2$ is mixed with $CO_2$ or $CH_4$, the simulations reveal that introducing 10−50 mol% of these gases significantly reduces $H_2$ uptake because the available adsorption sites on the kaolinite are increasingly occupied by $CO_2$ or $CH_4$ molecules. In particular, the simulations indicate that, when present, $CO_2$ displaces $H_2$ more effectively than $CH_4$−as evidenced by lower $H_2$ density peaks-suggesting that

the kaolinite surface exhibits a stronger affinity for $CO_2$. Furthermore, the RDFs confirm that among the atoms in the kaolinite structure, silicon atoms contribute slightly more to the $H_2$ adsorption process than do $H_2$, oxygen, or aluminum atoms. Overall, the quantitative insights obtained-such as the observed linear decrease in the Henry coefficient with increasing temperature-are in good agreement with previous simulation and experimental studies on gas adsorption in clay minerals, and can help guide strategies for underground $H_2$ storage. The study also demonstrates that the desorption curves closely mirror the adsorption behavior, confirming efficient $H_2$ recovery without hysteresis effects.

Muther and Dahaghi[884] performed GCMC simulations to compute the adsorption of $H_2$ on hydroxylated quartz (i.e., a representative geological mineral) across a wide range of pressures and temperatures. The study utilizes a molecular-scale quartz structure that has been hydroxylated to mimic natural subsurface conditions. The simulations explore the response of $H_2$ in both pure and mixed gas systems. The results show that $H_2$ uptake increases linearly with pressure, while high temperatures (up to 403 K) reduce adsorption since elevated temperatures weaken the mineral's affinity for $H_2$ by increasing the kinetic energy of the molecules, reducing the stability of $H_2$ retention on the quartz surface. To quantify the mineral's affinity for $H_2$, Henry coefficients were calculated, which were shown to consistently decrease with rising temperature, indicating that adsorption is less favorable when kinetic energy is higher; this decline is accompanied by higher binding energies between $H_2$ and the quartz surface, reinforcing the observation that elevated temperatures reduce adsorption effectiveness. In mixed gas systems, the presence of $CO_2$ and $CH_4$ further displaces $H_2$, with $H_2$ uptake reduced to as low as 1.28 mol/kg in a 50:50 gas mixture, mirroring trends observed in other porous materials such as MOFs and zeolites, and the addition of a thin water film (ca. 1 wt%) further reduces $H_2$ adsorption by ca. 3% due to water molecules preferentially occupying the adsorption sites on the hydroxylated quartz surface, highlighting the crucial role of surface hydroxyl groups in mediating gas interactions. Overall, the study emphasizes that both conditions (i.e., pressure and temperature) and compositional factors (e.g., presence of $CO_2$, $CH_4$, and water) are critical in controlling $H_2$ adsorption on

**Table 18. Overview of the Literature on H$_2$ Adsorption in Geological Substrates**[a]

| Author | Materials/Force Fields | Method | T [K]/P [MPa] | Pore Size [nm] | Mixture(s) |
|---|---|---|---|---|---|
| Wang et al.[905] | Na-Montmorillonite (CLAYFF)[422,423] | EMD and NEMD | 343 K /Not mentioned | 3.7–8.2 | CH$_4$, H$_2$, H$_2$O |
| | H$_2$ (Cracknell Two-site)[311] | | | | |
| | CH$_4$ (TraPPE-UA)[301] | | | | |
| | H$_2$O (SPC/E)[346] | | | | |
| Oliver et al.[879] | Kaolinite - Gib.[1] and Sil.[2] (CLAYFF)[422,423] | EMD | 300 K / 1.0-50.7 MPa | 1–20 | H$_2$ |
| | Graphene (OPLS)[428] | | | | |
| | H$_2$ (Michels Single site)[924] | | | | |
| Ho et al.[880] | Kerogen (CVFF)[426] | GCMC | 338 K / 0–27.6 MPa | Disordered | H$_2$ and CH$_4$ |
| | H$_2$ (Buch Single site)[312] | | | | |
| | CH$_4$ (TraPPE-UA)[301] | | | | |
| Ho et al.[921] | Montmorillonite (CLAYFF)[422,423] | GCMC | 323 K / upto 11.15 MPa | n/a | H$_2$ and CH$_4$ |
| | H$_2$ (Darkrim Three-site)[327] | | | | H$_2$, CH$_4$ and H$_2$O |
| | H$_2$O (SPC/E)[346] | | | | |
| Zhang et al.[889] | Kaolinite − Gib. and Sil. (CLAYFF)[422,423] | GCMC | 298.15 K / 0.1–10 MPa | 5–200 | H$_2$ and H$_2$O |
| | H$_2$ (Cracknell Two-site)[311] | | | | |
| | CH$_4$ (TraPPE)[925] | | | | H$_2$ and CH$_4$ |
| | H$_2$O (SPC/E)[346] | | | | |
| Muther et al.[884] | Hydroxylated Quartz (CLAYFF)[422,423] | GCMC | 323.15−423.15 K / 1−50 MPa | 3 | H$_2$ and CH$_4$ |
| | H$_2$ (Darkrim Three-site)[327] | | | | H$_2$ and CO$_2$ |
| | CH$_{TraPPE}$[301] | | | | H$_2$ and H$_2$O |
| | CO$_2$ (EPM2)[419] | | | | |
| Zhao et al.[886] | Kaolinite (UFF)[399] | GCMC and MD | 303.15−353.15 K / 0−18 MPa | 0.3−0.4 | H$_2$ |
| | Illite (UFF)[399] | | | | |
| | Dolomite (UFF)[399] | | | | |
| | Quartz (UFF)[399] | | | | |
| | Calcite (UFF)[399] | | | | |
| | H$_2$ (UFF Two-site)[399] | | | | |
| Liu et al.[923] | SiO$_2$ (PCFF+)[316,406,430] | MD and MD−MC | 300 K / 10−30 MPa | 0.5−1.4 | H$_2$ |
| | H$_2$ (PCFF+)[316,406,430] | | | | H$_2$ and CH$_4$ |
| | CH$_4$ (PCFF+)[316,406,430] | | | | H$_2$ and H$_2$O |
| | H$_2$O (PCFF+)[316,406,430] | | | | H$_2$, CH$_4$ and H$_2$O |
| Li et al.[329] | Kaolinite[422,423] | MD | 333.15 K / 30 MPa | 0.6 | H$_2$, CH$_4$, and H$_2$O |
| | H$_2$ (Three-site Darkrim)[327] | | | | H$_2$, CO$_2$, and H$_2$O |
| | CH$_4$ (TraPPE)[925] | | | | |
| | CO$_2$ (TraPPE)[678] | | | | |
| Kahzadvand et al.[882] | Montmorillonite and Illite (CLAYFF)[422,423] | MD | 333 K / 15 MPa | 0.4−7 | H$_2$ and CH$_4$ |
| | H$_2$ (Three-site Marx)[328] | | | | H$_2$ and CO$_2$ |
| | H$_2$O (SPC/E)[346] | | | | |
| Bui et al.[895] | Kaolinite − Gib. and Siloxane (CLAYFF)[422,423] | MD | 298 K / 10 and 20 MPa | 1 and 2 | H$_2$ and H$_2$O |
| | H$_2$ (Single-site Buch)[312] | | | | |
| | H$_2$O (SPC/E)[346] | | | | |
| Zheng et al.[878] | Calcite (Xiao)[431] | MD | 298−350 K / 1−10 MPa | 2 and 20 | H$_2$ |
| | Hematite (modified CLAYFF)[424] | | | | |
| | Quartz (CLAYFF)[422] | | | | |
| | H$_2$ (Three-site Alavi)[336] | | | | |
| Xie et al.[887] | Kaolinite[423] and Kerogen (CVFF)[426] | MD | 333.15 K / 30−15−10 MPa | 2 and 5 | H$_2$ and CH$_4$ |
| | H$_2$[313] | | | | |
| | CH$_4$ (TraPPE)[301] | | | | |
| Zhang et al.[881] | Kerogen II-D (CVFF)[426] | GCMC | 333.15 K / 3−18 MPa | 2 and 5 | H$_2$ |
| | Montmorillonite (CLAYFF)[422,423] | | | | H$_2$ and CH$_4$ |
| | H$_2$ (Single-site Buch)[312] | | | | |
| | CH$_4$ (TraPPE)[301] | | | | H$_2$ and CO$_2$ |
| | CO$_2$ (Fully Flexible)[926] | | | | |
| Muther and Dahagi[883] | Kaolinite (CLAYFF)[422,423] | GCMC | 323−403 K / 1−50 MPa | 3 | H$_2$ |
| | H$_2$ (Three-site Darkrim)[327] | | | | H$_2$ and CH$_4$ |
| | CH$_4$ (TraPPE)[301] | | | | H$_2$ and CO$_2$ |

**Table 18. continued**

| Author | Materials/Force Fields | Method | $T$ [K]/$P$ [MPa] | Pore Size [nm] | Mixture(s) |
|---|---|---|---|---|---|
| Chen et al.[885] | $CO_2$ (EPM2)[419] Quartz (CLAYFF)[422,423] $H_2$ (Single-site Michels)[924] $CH_4$ (TraPPE-UA)[301] $H_2O$ (TIP4P)[300] | GCMC and MD | 339−400 K / 1−50 MPa | 2, 4, and 10 | $H_2$ and $CH_4$ $H_2$, $CH_4$, and $H_2O$ |
| Shang et al.[877] | Kaolinite : Gib. and Sil. (CLAYFF)[422,423] $H_2$ (Three-site Darkrim)[327] | GCMC and MD | 303−423 K / 1−30 MPa | 1−20 | $H_2$ |
| Zhang et al.[896] | Kaolinite (CLAYFF)[422,423] $H_2$ (Two-site Cracknell)[311] $CH_4$ (TraPPE)[925] | GCMC | 318.15 K / 0.1−30 MPa | 0.5−2 | $H_2$ and $H_2O$ $CH_4$ and $H_2O$ $H_2$, $CH_4$, and $H_2O$ |
| Choudhary and Ho[898] | Pyrophyllite, Gibbsite (CLAYFF)[422,423] $H_2$ (Three-site Darkrim)[327] $CO_2$ (TraPPE)[678] $H_2O$ (SPC/E)[346] | MD | 300 K / 0.1 MPa | 1.326 and 1.626 | $H_2$ and $H_2O$ $CO_2$ and $H_2O$ |
| Babaei et al.[888] | Kerogen (CVFF)[426] $H_2$ (Single-site Buch)[312] $CH_4$ (TraPPE-UA)[301] | GCMC and MD | 363.15 K / 0.1−50 MPa | Disordered | $H_2$ $CH_4$ $H_2$ and $CH_4$ |
| Muther and Dahagi[922] | Na-Montmorillonite (CLAYFF)[422,423] $H_2$ (Three-site Darkrim)[327] $CO_2$ (Cygan Flexible)[927] $CH_4$ (TraPPE-UA)[301] $H_2O$ (Not mentioned) | GCMC and MD | 298-403 K / 1−50 MPa | 1.26−1.55 | $H_2$ $H_2$, $CO_2$, and $H_2O$ $H_2$, $CH_4$, and $H_2O$ |
| Choudhary and Ho[897] | Kaolinite : Gib. and Sil. (CLAYFF)[422,423] $H_2$ (Two-site IFF)[313] $CO_2$ (TraPPE)[678] $C_8H_{18}$ (OPLS all-atom)[428] | MD | 300 K / 5.1−30.4 MPa | n/a | $H_2$, $CO_2$ and Octane |
| Ho et al.[894] | MCM-41 Silica (Customized)[429] $H_2$ (Single-site)[894,928] $CO_2$ (EPM)[419] OMCTS (Customized)[928] | GCMC | 298 K / 0−1 MPa | 3.4 (Cylindrical) | $H_2$ and OMCTS $CO_2$ and OMCTS |
| Liu et al.[906] | MMT (CLAYFF)[422,423] $H_2$ (Single-site Hirschfelder)[321] $H_2O$ (SPC/E)[346] | MD | 333-413 K / 2−30 MPa | 3-40 | $H_2$ $H_2$ and $H_2O$ |
| Mashhadzadeh et al.[899] | Kaolinite (INTERFACE)[425] $H_2$ (Two-site Yang)[325] $H_2O$ (SPC/E)[346] $Na^+$,[371] $Cl^-$,[929] $Mg^{2+}$ [929] [1−5 M] | MD | 310−410 K / 30 MPa | 1−10 | $H_2$ and $H_2O$ $H_2$ and NaCl Brine $H_2$ and $MgCl_2$ Brine |
| Hubao et al.[907] | Calcium Silicate Hydrate (CLAYFF)[425] $H_2$ (Single-site Hirschfelder)[321] | MD and GCMC | 300−370 K / 2.5−40 MPa | 2.5−40 | $H_2$ |
| Raza et al.[908] | Kerogen (PCFF++)[427] $H_2$ (Single-site Waldman)[930] | MD and GCMC | 360 K / 3−41 MPa | 0.5 and 2 | $H_2$ |
| Kim et al.[909] | Illite (CLAYFF)[422,423] and Kerogen (CVFF)[426] $H_2$ (Two-site Wang)[313] $CH_4$ (OPLS)[428] $CO_2$ (Not mentioned) $H_2O$ (SPC/E)[346] | MD | 326 K / 30.4 MPa | n/a | $H_2$, $CH_4$, and $H_2O$ $H_2$, $CH_4$, $CO_2$, and $H_2O$ |
| Ghasemi et al.[910] | Pyrophillite (CLAYFF)[422,423] Montmorillonite (CLAYFF)[422,423] Beidellite (CLAYFF)[422,423] $H_2$ (Two-site Yang)[325] $H_2O$ (SPC/E)[346] | MD | 368.15 K / 30 MPa | 1−8 | $H_2$ and $H_2O$ |
| Li et al.[931] | Calcite[432] $H_2$ (Single-site Hirschfelder)[321] $H_2O$ (SPC/E)[346] $Na^+$, $Cl^-$ [374] | MD | 353 K / 20 MPa | 8 | $H_2$ and $H_2O$ |

**Table 18. continued**

| Author | Materials/Force Fields | Method | $T$ [K]/$P$ [MPa] | Pore Size [nm] | Mixture(s) |
|---|---|---|---|---|---|
| | $Mg^{2+}$,[932] $SO_4^{-2\ b\ 933}$ | | | | |

$^a$Gibbsite surfaces have a -OH group : Hydrophilic $^b$Siloxane surfaces have an Si-O-Si group : Hydrophobic
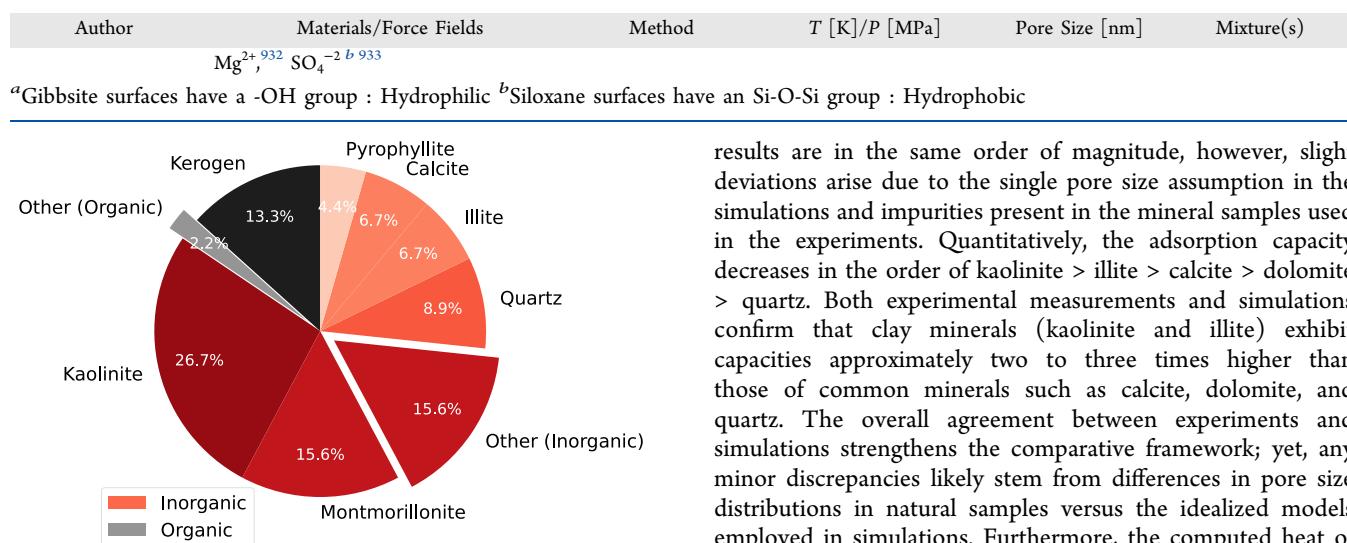


**Figure 49.** The substrates considered in the molecular simulation studies reviewed in this section. The sectors in shades of red and black represent inorganic and organic materials, respectively.

hydroxylated quartz, with the interplay between these factors ultimately determining the storage capacity and stability of $H_2$ geo-storage systems. Similarly, Chen et al.[885] used GCMC simulations to study the adsorption of $CH_4$–$H_2$ mixtures under conditions representative of shale gas reservoirs. A base-case scenario was set in a 4-nm slit pore at 370 K and 300 bar (in the paper, units of Fahrenheit and psi were used), while simulation conditions spanned temperatures of 339 - 400 K, and pressures up to 500 bar. It is important to note that experimental data are available only for pure $CH_4$ adsorption; the computed excess adsorption capacities and adsorbed phase densities $CH_4$ agree with these experiments within a deviation of 3%. The outcomes revealed that when the mole fraction of $CH_4$ is high ($\geq$50%), $CH_4$ is preferentially adsorbed on both graphite and quartz surfaces, forming an adsorption layer close to the solid boundary, while $H_2$ is predominantly distributed in the free phase within the pore. However, when the mole fraction of $CH_4$ is low (e.g., 20%), the behavior changes: in the graphite layer, the fewer $CH_4$ molecules present leave sufficient space for $H_2$ to form its own adsorption layer at the surface. A similar trend is observed for the quartz surface, although the density of the $H_2$ adsorption layer is notably lower compared to that in the graphite system. When water is present in the system (modeled with TIP4P), water molecules strongly interact with the solid surfaces, particularly with the carbon atoms of the graphite layer and the hydroxylated (100) face of quartz, which further suppresses $CH_4$ adsorption. This suppression reinforces the free distribution of $H_2$, with water forming its own distinct adsorption layer and having small direct effect on the behavior of $H_2$ molecules.

Zhao et al.[886] evaluated the feasibility of using depleted shale gas reservoirs for UHS by combining experiments with molecular simulations. A major finding was that $H_2$ adsorption is well described by the Langmuir isotherm over temperatures ranging from 303.15 K to 353.15 K and pressures up to 180 bar, which indicates that only a single layer of $H_2$ molecules is adsorbed on the mineral surfaces. It is noteworthy that the Langmuir fit was applied separately to experimental excess adsorption isotherms as well as simulation data. Both sets of

results are in the same order of magnitude, however, slight deviations arise due to the single pore size assumption in the simulations and impurities present in the mineral samples used in the experiments. Quantitatively, the adsorption capacity decreases in the order of kaolinite > illite > calcite > dolomite > quartz. Both experimental measurements and simulations confirm that clay minerals (kaolinite and illite) exhibit capacities approximately two to three times higher than those of common minerals such as calcite, dolomite, and quartz. The overall agreement between experiments and simulations strengthens the comparative framework; yet, any minor discrepancies likely stem from differences in pore size distributions in natural samples versus the idealized models employed in simulations. Furthermore, the computed heat of adsorption was in the range of ca. 9−26 kJ/mol. This range, which lies well below the threshold for chemical adsorption, confirms that the process is dominated by physisorption. Additionally, $H_2$ diffusion coefficients were computed from MD simulations. It was shown that $H_2$ has the lowest diffusion coefficient in illite (ca. $0.018 \times 10^{-9}$ m$^2$/s) and the highest in dolomite (ca. $25.83 \times 10^{-9}$ m$^2$/s). This variation is attributed to the hindering effect of interlayer cations in illite and a relatively more open nano-pore structure in dolomite, which facilitates faster molecular movement. Overall, while the qualitative agreement between experiment and simulation confirms the potential of shale inorganic minerals for $H_2$ storage, the significant quantitative deviations emphasize the need for further refinement in pore structure modeling, and a more detailed study of additional factors (e.g., organic matter, residual gases, water).

In a similar study, Xie et al.[887] investigated the feasibility of UHS in depleted shale gas reservoirs by performing MD simulations that capture the complete huff-n-puff process. In that work, the simulation conditions mimic reservoir settings (333.15 K and pressures varying from 300 down to 100 bar). The simulations were designed to mimic a reservoir's operational cycle by first reducing pressure from 300 to 150 bar to trigger $CH_4$ desorption (the *huff* stage), then injecting $H_2$ until a desired composition is achieved, and finally further lowering the pressure to 100 bar (the *puff* stage) to mobilize the stored $H_2$. Recovery efficiency is quantified by comparing the computed $H_2$ densities before and after the final pressure drop. This cyclic injection and production strategy is designed to maximize storage efficiency while enabling later retrieval of $H_2$. The study compares two types of nano-pore models. The organic nano-pores are modeled using a type II-D kerogen representation derived from previous studies (i.e., a realistic representation of organic matter in shale), while the inorganic nano-pores are represented by kaolinite-based models of clay minerals. The adsorption capacities in these nano-pores are quantified by analyzing the ensemble-averaged density profiles and the distribution of gas molecules (both $H_2$ and $CH_4$) along the pore dimensions. In practice, the adsorption capacity is measured in terms of apparent adsorption isotherms and the average density computed from simulation snapshots at equilibrium. Furthermore, the simulations revealed that for the reservoir conditions studied, the organic pores show a
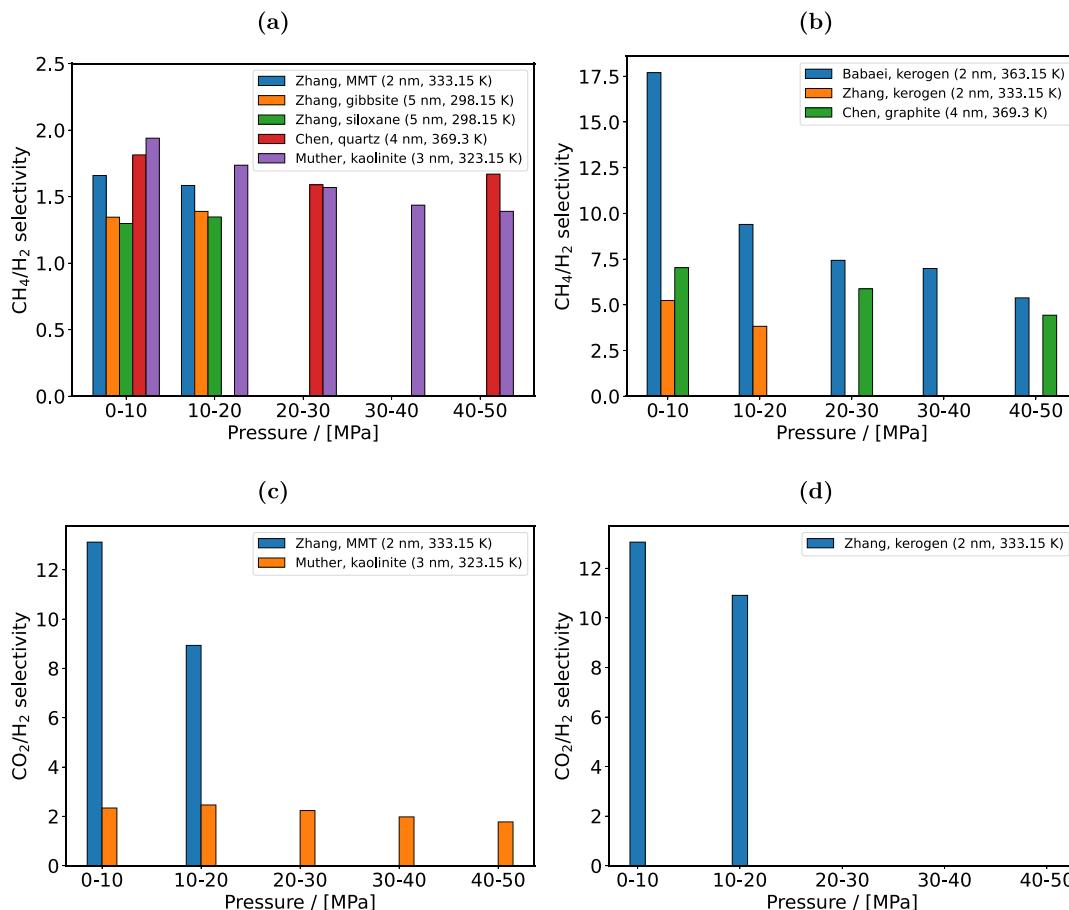
**Figure 50.** Comparison of $CH_4/H_2$ selectivities gathered from the literature for (a) inorganic and (b) organic pores. Comparison of $CO_2/H_2$ selectivities gathered from the literature for (c) inorganic and (d) organic pores. The data are taken from Zhang et al.,[881] Chen et al.,[885] Babaei et al.,[888] and Muther and Dahagi.[883] Each bar represents the mean selectivity within pressure bins of 10 MPa (0-10, 10-20, 20-30, 30-40, 40-50 MPa), calculated from data points in the corresponding pressure range. The legend indicates the study and, where applicable, the pore width (e.g., 2 nm) and temperature. Pressure values were converted from psi to MPa where necessary, and selectivity was inverted for studies where $H_2$/gas was originally reported. This figure illustrates the variation in selectivity across different geological materials and gas mixtures, highlighting the impact of pore type and pressure on adsorption behavior.

unique density profile for $H_2$ where the first adsorption peak is lower than the second. This behavior is opposite in inorganic pores, which can be attributed to competitive adsorption with $CH_4$, which strongly adheres to the organic surface. Density profile analysis clearly corroborated these findings across the different pressure points studied. The simulation results were further validated by comparing the computed bulk densities of pure and binary gas mixtures with NIST data. In the huff-n-puff cycle, recovery efficiency was determined by monitoring the change in the average density of $H_2$ before and after the puff stage; for example, recovery efficiencies were found to be 49.9% in organic meso-pores and 40.0% in organic micro-pores, in contrast with higher recovery values in inorganic pores (70.0% in meso-pores and 63.3% in micr-opores). These percentages are calculated as the ratio of the recovered $H_2$ (measured as the drop in average density) to the initial injected $H_2$ density.

Babaei et al.[888] followed a hybrid GCMC/MD approach at 363.15 K and pressures up to 500 bar to investigate the adsorption and diffusion of $H_2$, $CH_4$, and their mixtures in type II-D kerogen, wherein realistic pore size distributions are generated through the incorporation of dummy particles. In this framework, the inherent heterogeneity of the kerogen matrix is captured via three distinct models (Model 1, Model 2,

and Model 3) constructed by embedding dummy particles with diameters of 0 nm, 1 nm, and 2 nm, respectively, to represent incremental variations in pore structure. Two computational frameworks were established to quantify adsorption-induced deformation. The "Lagrangian approach" referenced the system to its pre-adsorption state under fixed thermodynamic conditions, maintaining a constant accessible volume as a baseline, whereas the "Eulerian approach" was used to compare the system with and without adsorption under identical mechanical conditions, rendering the pore structure pressure dependent and more sensitive to deformation at high pressures. This detailed representation was critical as variations in pore size not only affect the accessibility of adsorption sites but also determine the extent of swelling induced by gas adsorption, a key factor influencing both the storage capacity and mechanical integrity of the matrix. In the case of $CH_4$ adsorption, the results indicated that the flexible kerogen models exhibited 1.4, 1.6, and 1.3 times higher adsorption in Models 1, 2, and 3, respectively, compared to their rigid counterparts. The corresponding volumetric strain (a measure of matrix expansion) ranged from 3.25% to 4.54% using the Lagrangian approach, and from 2.97% to 5.92% with the Eulerian approach at high pressures. For $H_2$ adsorption, however, the kerogen showed negligible deformation overall

with the matrix experiencing either slight swelling or even contraction depending on the pore size distribution, an outcome attributed to the $H_2$'s small molecular size and weak adsorption affinity, combined with capillary effects and pore geometry variations. Moreover, the study revealed that $H_2$ diffuses roughly one order of magnitude faster than $CH_4$ ($6.87 \times 10^{-9}$ m$^2$/s for $H_2$ compared to $0.30 \times 10^{-9}$ m$^2$/s for $CH_4$ at 5 MPa). Although $CH_4$ was preferentially adsorbed, as evidenced by a selectivity greater than 1 across all pressures, this selectivity decreases with increasing pressure due to the saturation of adsorption sites, thereby reducing the differences between the two gases. Zhang et al.[889] used GCMC simulations to investigate the adsorption behavior of $H_2$/$CH_4$ mixtures in two types of kaolinite nano-pores, namely, the hydrophilic gibbsite and the hydrophobic siloxane pores, with pore sizes ranging from 5 to 200 nm, at 298.15 K and pressures between 1 and 100 bar. Under dry conditions, the study demonstrated that increasing the bulk $H_2$ mole fraction leads to an increased storage density for $H_2$, with its adsorption varying linearly with pressure, and a corresponding decrease in $CH_4$ density. Notably, when the injected mixture contained less than 20% $H_2$, the adsorption process selectively favors $H_2$. For instance, an injection mixture of 5% $H_2$ and 95% $CH_4$ yielded a $H_2$/$CH_4$ selectivity of approximately 2. Although both nano-pore types exhibit enhanced $H_2$ selectivity under low $H_2$ injection fractions, the surface chemistry plays a critical role: in gibbsite pores, strong interactions between $CH_4$ molecules and the pore surface result in higher $CH_4$ densities at low $H_2$ fractions, whereas in siloxane pores the overall $CH_4$ capacity is slightly lower, thereby improving the relative selectivity for $H_2$. In terms of pore size effects, the absolute density of $H_2$ remains nearly independent of the pore size because most stored $H_2$ is concentrated in the middle of the pore; however, the relative selectivity, defined as the ratio of the adsorbed $H_2$ to $CH_4$, increases in larger pores (particularly those exceeding 100 nm) due to improved enrichment of $H_2$. The presence of moisture reduces the adsorption densities of both gases in the mixed-gas scenario. In hydrophilic (gibbsite) nano-pores, water molecules are strongly attracted to the surface via hydrogen-bonding, forming a thin film along the walls, whereas in hydrophobic (siloxane) pores, water tends to form clusters that span across the pore, reducing the available free volume. Under moist conditions, for example at a water concentration of 0.2 g/cm$^3$ and a bulk $H_2$ mole fraction of 20%, the gibbsite pores are more favorable for $H_2$ storage than their siloxane counterparts. Although both pore types exhibit reduced overall adsorption densities in the presence of water, the effective storage volume in siloxane pores is more significantly diminished due to the water clusters, which adversely affect the selective adsorption of $H_2$.

A cross-comparison of these studies reveals several common quantitative trends. Muther and Dahaghi[883,884] reported that with increasing temperature, $H_2$ molecules possess greater kinetic energy, which they argued weakens attractive interactions with the adsorbent surface, thereby reducing adsorption capacity. While this reflects the interpretation of these authors, a more physically consistent explanation is that the release of $H_2$ at higher temperatures arises from the increasing dominance of entropic effects, rather than from the weakening of enthalpic attractions. It should also be noted that GCMC simulations, by construction, do not capture kinetic energy and kinetic effects. Thus, the observed reduction in adsorption with temperature in GCMC results should not be

attributed to the reduced molecular kinetic energy of $H_2$ molecules.

Shifting our focus on the adsorption of $CH_4$/$H_2$ and $CO_2$/$H_2$ on organic and inorganic pores, we compiled Fig. 50 which shows selectivities for these mixtures collected from different simulation studies. Given the potential sensitivity of selectivities to pore size[890] and temperature, the values are selected such that the data can be compared without significant biases introduced from varying thermodynamic conditions. From Fig. 50(a) and (b), it is clear that the selectivity of $CH_4$ over $H_2$ remains above one in both organic and inorganic pores. However, the magnitude of this selectivity differs substantially: organic nano-pores (e.g., kerogen) often exhibit values an order of magnitude larger than their inorganic counterparts. Organic nano-pores show higher $CH_4$ selectivity because their heterogeneous surfaces provide stronger van der Waals interactions, promoting the formation of saturated, well-defined $CH_4$ adsorption layers that preclude extensive $H_2$ binding.[881,891] The stronger van der Waals interactions between $CH_4$ and carbon, compared to $H_2$ and carbon, arise from differences in the LJ potential parameters, specifically the well-depth. For instance, Kumar et al.[892] illustrated these differences clearly in their interaction profiles (Figure 2 in ref 892), showing that the well-depth for $CH_4$-carbon interactions is approximately eight times deeper than that for $H_2$-carbon interactions. This deeper potential well for $CH_4$ reflects its larger molecular size and greater polarizability,[893] both of which enhance dispersion forces relative to $H_2$. In contrast, inorganic minerals, with their lower $CH_4$ affinity and more uniform surfaces, result in less saturation and greater availability of sites for $H_2$, thus, reducing $CH_4$ selectivity.

As shown in Fig. 50(a) and (c), $S_{CO_2/H_2}$ selectivities are significantly higher than $S_{CH_4/H_2}$ indicating a strong preferential adsorption of $CO_2$ over $CH_4$[890] in inorganic pores. This strong adsorption can be attributed to the strong quadrupole moment and polarizability[890] of $CO_2$. This substantial preference for $CO_2$ compared to $CH_4$/$H_2$ systems can have significant practical implications. For instance, in underground storage, the intentional use of $CO_2$ as a cushion gas would result in its retention on pore surfaces, leaving $H_2$ predominantly in the free (mobile) phase, which is advantageous for recovery and purity. For organic pores, the comparison between Fig. 50(b) and (d) suggests that $S_{CO_2/H_2}$ reported by Zhang et al.[881] generally exceeds $S_{CH_4/H_2}$, except in the data from Babaei et al.,[888] who studied adsorption in disordered pores, leading to a pore size distribution rather than a single pore size (as in slit-pore studies).

The studies reviewed earlier suggest that beyond surface chemistry and cushion gases, pore size, pressure, and temperature all significantly impact gas/$H_2$ selectivities. Zhang et al.[890] demonstrated that $S_{CO_2/H_2}$ in Na-Montmorillonite pores vary by a factor of 3 to 4 when pore size increases from 2 to 5 nm. In sharp contrast, $S_{CH_4/H_2}$ in the disordered kerogen pores studied by Babaei et al.[888] hardly show any change despite an increase in mean pore size from 0.4 nm (Model 1) to 2 nm (Model 3). The authors attributed this invariance to the particularly strong $CH_4$-kerogen interactions overshadowing pore size effects.[888] Another commonly observed behavior across the reviewed studies is the decrease in selectivities with increasing pressure due to the saturation of

binding sites. There has not been a systematic investigation of the role of temperature in gas selectivity.

The presence of water films typically reduces $H_2$ adsorption by 3 to 40%, whereas cushion gases like $CO_2$ and $CH_4$ form robust adsorption layers, potentially decreasing $H_2$ capacity by up to 30%. $H_2$ interaction energies in pure systems range from approximately −1.5 to −2.0 kcal/mol, while competing gases exhibit stronger binding (e.g., $CH_4$ at −4.3 kcal/mol). Smaller pore sizes show up to 40% higher adsorption, and the maturity of organic content (kerogen) further modulates these effects. Together, these quantitative findings provide a road-map for understanding and optimizing competitive adsorption and storage performance in geological formations.

### 4.7.2. Solubility of Hydrogen under Confinement.
Solubility under confinement is a crucial topic with direct implications for UHS and other applications. As highlighted by Ho et al.,[894] the confined environment in nano-pores - whether circular, as in some studies, or flat-walled, as in others - not only enhances gas solubility through mechanisms such as cavity formation and solvent layering, but also alters gas diffusion and clustering behavior. The studies focusing on this topic use a variety of molecular models. For example, Ho et al.[894] studied circular pore systems to mimic realistic confined environments, whereas Bui et al.[895] used flat-wall, slit-shaped nano-pore models that represent kaolinite or other clay minerals. Such differences in the molecular systems used allow for a rigorous comparison of how pore geometry and surface chemistry control gas uptake phenomena. A detailed information of the thermodynamic conditions, pore sizes, materials, and the force fields used in the different studies are tabulated in Table 18.

Ho et al.[894] investigated gas uptake in a model meso-porous system where a solvent is confined within well-defined pores, providing a basis for understanding how nano-confinement affects gas-solvent interactions. The paper identifies two distinct mechanisms for over-solubility. For gases that interact strongly with the solid surface (e.g., $CO_2$ on silica), there is an adsorption-driven uptake, while for gases with weak gas/solid interactions (such as $H_2$), the predominant mechanism is an enhanced solubility due to the formation of low-density regions arising from solvent layering. For instance, the work explains that when only a single layer of solvent is present inside a meso-pore, adsorption at the gas/liquid interface contributes additionally to the gas uptake. Although no numerical values are provided in this study, the mechanism establishes the baseline for comparison with more detailed quantitative studies in later works, such as Bui et al.[895] The study by Zhang et al.[896] examined $H_2$ dissolution in water-saturated caprock nano-pores mimicking natural sealing layers. Nano-confinement in these pores was shown to enhance $H_2$ solubility by up to 27 times relative to bulk water. For example, Zhang et al.[896] report that in pores with an optimal width of 0.55 nm, the dissolved $H_2$ density reaches 5.614 kmol/m$^3$ at 318.15 K and 300 bar, corresponding to an enhancement factor of about 27.4 times the bulk value.

In the context of UHS, Bui et al.[895] studied $H_2$ solubility in water confined within kaolinite nano-pores. Two distinct pore widths were considered: 20 Å and 10 Å. For the 20 Å wide pore, the study reports that under pressures of 100 and 200 bar, $H_2$ solubility is enhanced by approximately 2.5 times compared to bulk water as shown in Fig. 51. Strikingly, in the 10 Å pore, the solubility is significantly enhanced to nearly 25 times that of the bulk (see Fig. 51). These numbers are
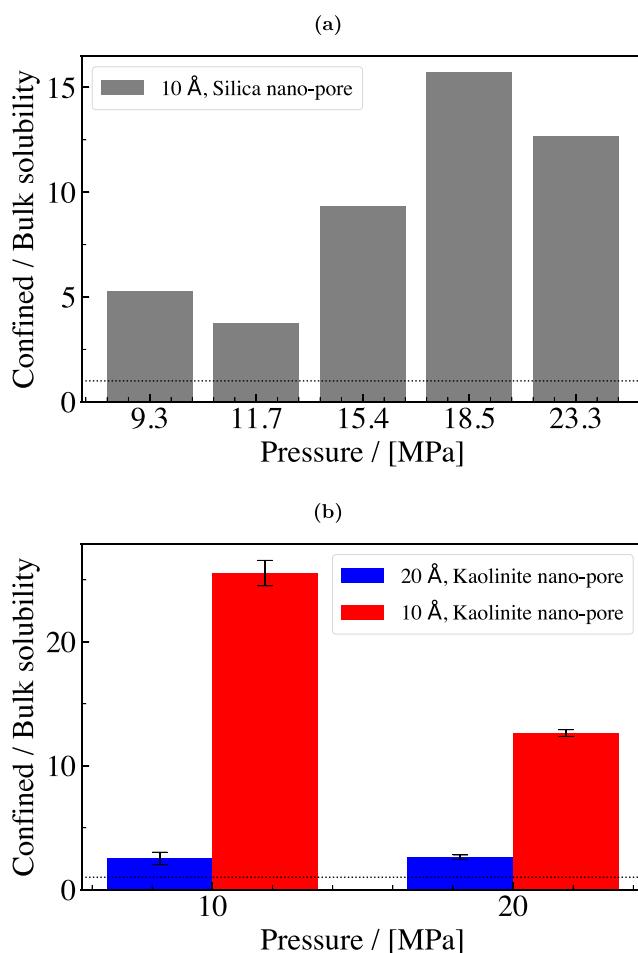


**Figure 51.** Enhancement of solubility under confinement: Ratio of gas solubility in confined water and bulk water for (a) $CH_4$ and (b) $H_2$. $H_2$ solubilities are taken from Bui et al.[895] and $CH_4$ solubilities are taken from Phan et al.[900] and Sakamaki et al.[904] The nano-pores are made of Kaolinite in the study by Bui et al.[895] (see Table 18) and Silica in Phan et al.[900] The dotted line serves as a reference where bulk solubility equals confined solubilities.

supported by detailed water density profiles that reveal pronounced hydration layers; $H_2$ preferentially accumulates in regions of low water density near the hydrophobic siloxane surface, whereas the hydrophilic gibbsite side shows a dense water layer that excludes $H_2$. The enhancement is attributed to pronounced water density fluctuations that generate regions of low solvent density where $H_2$ preferentially dissolves. Interestingly, while the confinement retards water diffusion, $H_2$ diffusion is enhanced due to these fluctuations. The study clearly links the molecular-scale structuring of water under confinement to the observed over-solubility of $H_2$.

The work by Choudhary and Ho[897] explores a hybrid system designed to mimic depleted oil reservoirs, where oil, gas, and kaolinite interact. The study demonstrates that $H_2$ dissolves more readily in oil than in water, owing to weaker $H_2$-oil interactions compared with $H_2$ - water interactions. Quantitatively, the simulation results indicate that the addition of as little as 5% $CO_2$ (in mole fraction units) can reduce $H_2$ dissolution in oil by approximately 15% because of the resulting decrease in interfacial tension. $H_2$ adsorption is weak and similar on both hydrophilic and hydrophobic faces, whereas it is $CO_2$ that exhibits a strong preference for the

hydrophilic side. These detailed quantitative observations (e.g., the reduction percentage and the role of specific surface terminations) provide a link of the molecular-level interactions with the overall gas uptake behavior. Choudhary and Ho[898] focused on gas clustering within hydrated nano-pores with contrasting surface chemistries. It shows that over-solubility can emerge either through adsorption at the liquid/solid interface or by gas molecules migrating into low-density regions formed by solvent structuring. For example, in hydrophobic nano-pores (represented by pyrophyllite with siloxane rings), $CO_2$ exhibits a much stronger tendency to form stable dimers and larger clusters due to its higher quadrupole moment ($14.2 \times 10^{-40}$ C m$^2$) compared to $H_2$ ($1.7 \times 10^{-40}$ C m$^2$); as a result, while $CO_2$ tends to exit the pore as clusters, $H_2$, with its lower polarizability ($0.80 \times 10^{-24}$ cm$^3$), shows a lesser degree of clustering. Such molecular insights, supported by free energy calculations, are crucial for understanding how nano-pore dimensions and surface chemistry jointly control the aggregation processes within confined media.

The investigation by Mashhadzadeh and Faroughi[899] used atomistic simulations to study the behavior of dilute $H_2$ in water-saturated kaolinite-a mineral representative of clay-rich caprocks. Their results indicate that as the pore size decreases, for example from 100 Å down to 10−15 Å, dense layers of water and $H_2$ form near the clay surface. These structured arrangements lead to a reduction of the $H_2$ self-diffusion coefficient compared to the bulk phase, even as local $H_2$ concentrations are elevated. The study further identifies that the presence of divalent ions (with larger hydration shells), such as $Mg^{2+}$, decreases $H_2$ mobility more significantly than monovalent ions. These findings offer useful insights into the interplay between nano-scale confinement, salinity, and molecular diffusion.

All studies discussed in this section converge to the notion that both nano-confinement and surface/interface phenomena, ranging from cavity formation, solvent layering, and density fluctuations to specific interaction strengths, are vital in enhancing $H_2$ solubility (or over-solubility) in confined media. Concrete examples, showcasing the particular nature of confined $H_2$ are the studies by Zhang et al.,[896] where it was shown that a pore width of 5.5 Å at 318.15 K and 300 bar yields a $H_2$ solubility enhancement of nearly 27 times relative to bulk, and by Bui et al.,[895] where it was reported that kaolinite nano-pores with a width of 10 Å result in a 25-fold enhancement of hydrogen solubility at pressures of 100−200 bar. In the molecular simulation studies reviewed here, the differences in interfacial behavior were also highlighted, i.e., hydrophobic surfaces such as siloxane and pyrophyllite, foster the formation of gas clusters[898] and low-density solvent regions, whereas hydrophilic surfaces, such as gibbsite and kaolinite, tend to form dense water layers that limit gas uptake. The study addressing oil−clay−gas interactions by Choudhary and Ho[897] underscores the role of interfacial tension and mineral surface properties in modulating gas uptake in hybrid systems. It is also important to emphasize that this confinement-induced over-solubility is not unique to $H_2$. Similar trends have been reported for other gases, such as $CH_4$ and $CO_2$, across a range of systems spanning protein−water and gas−water in industrial catalysis. As reported in the literature, $CH_4$ solubility in confined water has been reported to be enhanced by up to 50 times relative to its bulk value.[900] Likewise, $CO_2$ over-solubility in confined solvents has been

well documented in studies where confinement and the nature of the solid surface (e.g., hydrophobic and hydrophilic terminations) significantly alter the adsorption−desorption equilibrium.[898]

The influence of confinement on gas solubility is not limited to simple gas−solvent systems. Similar mechanisms-often linked to water density fluctuations, cavity formation, and local solvent structuring-also manifest in more complex media, such as those involving protein - water interactions. Reviews on protein hydration, such as the work by Ball,[901] as well as studies on hydrophobic effects and water density fluctuations discussed by Rego and Patel[902] and Jamadagni et al.,[903] provide additional evidence that enhanced gas uptake under nano-confinement is a universal phenomenon, governed by a delicate balance between solvent layering, cavity formation, and specific gas−solid and gas−solvent interaction strengths.

### 4.7.3. Diffusivity of Hydrogen under Confinement.

Understanding mass transport mechanisms of $H_2$ in geological environments is essential for evaluating both the feasibility and efficiency for a variety of applications such as UHS. This section reviews recent studies using MD simulations to investigate $H_2$ transport in nano-pores inspired by geological systems. In the study by Wang et al.,[905] EMD simulations were first used to reveal the behavior of fluid mixtures in Na-montmorillonite nano-pores, showing that water preferentially adsorbs onto the clay surfaces forming water films. At a water content of 10%, both $H_2$ and $CH_4$ form two distinct adsorption layers in smaller pores. As water content increases, the water film thickens by 2−3 times, driving the gas molecules into the bulk region, while the calculated selectivity coefficients for $H_2$/$CH_4$ (ranging from 0.70 to 0.76) indicate that the cushion gas ($CH_4$) effectively reduces $H_2$ loss. In contrast, NEMD simulations captured the dynamic transport behavior under applied pressure gradients, where elevated pressures induce the desorption of water molecules near the pore walls, thereby enhancing the accumulation and mobility of $H_2$. The self-diffusion coefficient of $H_2$ was observed to decrease by up to 53% when water content increases from 10% to 30%, with the ratio of $H_2$ to $CH_4$ diffusion coefficients decreasing from 2.2 to 1.7. Under high pressure gradients, a notable desorption of water molecules is observed near the pore walls that enhances the accumulation and mobility of $H_2$ in these regions, a phenomenon that is consistent with recent experimental trends in enhanced multiphase flow through nanoporous media.

The study by Oliver et al.[879] reported MD simulations of $H_2$ transport in nanoporous media, focusing on both organic (graphene) and inorganic (kaolinite) slit pores under subsurface conditions. The authors investigated how $H_2$ diffusion is influenced by surface chemistry and pore size (ranging from 2 to 20 nm), and pressure (from 20 to 500 bar). Notably, $H_2$ adsorption occured as a monolayer (3 Å thick) on both materials, though graphene exhibited ca. 35% higher surface density than kaolinite. Despite the stronger gas−solid interaction in the case of graphene, the self-diffusion coefficients (in the order of $10^{-6}$ m$^2$/s) were higher in graphene than in kaolinite at low pressures. This finding, supported also by the density profiles, collision times (with graphene's collision time being approximately 2 ps longer at 20 atm), and lateral velocity autocorrelation functions that reveal more frequent wall-mediated collisions on the rougher kaolinite surface. Both materials demonstrated an exponential decrease in $H_2$ self-diffusion coefficients with increasing pressure. However, at high pressures (beyond 50-100 atm),

the impact of surface chemistry diminishes as gas−gas collisions begin to dominate, leading their transport properties to converge.

Zheng et al.[878] studied the mechanisms of $H_2$ diffusion in geological slit pores made of calcite, hematite, and quartz, focusing on the effects of temperature, pressure, pore size (confinement), and surface chemistry. The study demonstrated that for all three minerals, the $H_2$ self−diffusion coefficient increases with temperature in the range of 298 to 350 K, and in 20 nm slit pores at 100 bar the diffusion follows a bulk regime with the relation $D \propto T^{1.5}$ (supported by linear trends in the ln−ln plots with slopes equal to ca. 1.5). In contrast, increasing the pressure from 10 to 100 bar, consistently reduces the diffusion coefficient across all minerals, following a power law with fitted exponents ranging from −0.825 to −0.964, which is corroborated by analyses of normalized interaction energies and density profiles showing enhanced adsorption at higher pressures. When the pore aperture is reduced from 20 nm to 2 nm, the diffusion coefficient decreases substantially due to stronger wall-gas interactions, resulting in a shift from bulk to transition or even surface diffusion regimes. The study showed that surface roughness enhances $H_2$ diffusion in larger pores by effectively enlarging the pore space while it decreases diffusion in smaller pores due to stronger adsorption. These conclusions were corroborated by comparisons of decay times from velocity autocorrelation functions and 2D density distributions. In a related work, Shang et al.[877] performed simulations to compute the $H_2$ diffusion and adsorption in confined kaolinite slits using a hybrid MD−GCMC approach. Similarly to the studies reviewed so far, the focus of this work was also on how variations in pore size, temperature, pressure, and surface mineralogy affect $H_2$ properties. This study showed that when the pore size exceeds 5 nm, $H_2$ is predominantly located in the bulk phase with minimal adsorption losses, whereas for pores below 5 nm, a rapid decrease in both excess adsorption and diffusion coefficient due to enhanced gas−solid interactions is observed. Increasing temperature from 303 to 423 K reduced the adsorption capacity but concomitantly increased the $H_2$ diffusion coefficient, following a power law relationship, with corresponding changes in both the density profiles and the gas−solid interaction energy. Meanwhile, elevating pressure from 10 to 300 bar enhanced the storage capacity while diminishing the mobility of $H_2$, as supported by the observed rise in adsorption peak densities and the inverse trend in diffusion coefficients. In terms of surface chemistry, the study by Shang et al.[877] revealed that the positively charged gibbsite surface promotes $H_2$ adsorption compared to the negatively charged siloxane surface.

Liu et al.[906] conducted MD simulations to investigate the diffusion of $H_2$ confined in montmorillonite nano-pores, with the motivation being assessing its leakage risk in geological storage settings. The study systematically examined the dependence of the self−diffusion coefficient (which were shown to be on the order of $10^{-8}$ $m^2$/s) on temperature (333−413 K), pressure (20−300 bar), and pore size (with slit apertures ranging from 3 to 40 nm). It was observed that diffusivity increases moderately with temperature and pore size, yet decreases with higher pressures. For example, in an 8 nm slit, the diffusivity increased from approximately 8.08 × $10^{-8}$ $m^2$/s at 353 K to 10.03 × $10^{-8}$ $m^2$/s at 413 K, while an increase in the pressure from 2 to 300 bar led to a reduction from nearly 10 × $10^{-8}$ $m^2$/s to 7.5 × $10^{-8}$ $m^2$/s. The authors further demonstrated anisotropic diffusion by resolving local

diffusion coefficients into components parallel and perpendicular to the clay surfaces, with density profile analyses revealing a single adsorption layer at ca. 2.8 Å from the surface. In addition, trends in $H_2$ diffusion under varying moisture content and brine salinity were explored. As the average water density increases in a 3 nm slit from 0.568 to 0.758 $g/cm^3$, the self−diffusion coefficient steeply decreases from 8.27 × $10^{-8}$ to 4.25 × $10^{-8}$ $m^2$/s. While variations in salinity up to 8 wt% yield minor changes, at 12 wt% the diffusivity drops further (e.g., from 8.67 × $10^{-8}$ to 7.21 × $10^{-8}$ $m^2$/s) due to the formation of brine droplets that hinder gas motion. Although similar trends in diffusion modulation have been reported for other fluids such as $CH_4$, $CO_2$, octane, and nonadecane, the study implied that the relatively moderate fluid−solid interactions of $H_2$ render its pore−size sensitivity less pronounced than that of the other materials.

Using MD simulations, Mashhadzadeh and Faroughi[899] computed $H_2$ diffusion in water-saturated kaolinite nano-pores under conditions relevant to UHS. The study explored how variations in pore size (ranging from 10 to 100 Å), temperature (from 310 to 410 K), and ionic composition (salinities of 1 to 5 M, and the use of monovalent $Na^+$ versus divalent $Mg^{2+}$ ions) affect the diffusion of $H_2$ under a fixed pressure of 300 bar. It was shown that reducing pore size leads to denser $H_2$ and water layers at the kaolinite surface, and consequently, to a significant reduction in $H_2$ diffusivity. $H_2$ diffusivities dropped from ca. 7.8 × $10^{-9}$ $m^2$/s at a confinement distance of 60 Å to ca. 2.5 × $10^{-9}$ $m^2$/s at 10 Å. Similarly, the study demonstrated that higher temperatures promote increased $H_2$ mobility, with diffusion coefficients increasing from apporximately 4.49 × $10^{-9}$ $m^2$/s at 310 K to 9.27 × $10^{-9}$ $m^2$/s at 410 K. The presence of divalent ions such as $Mg^{2+}$ further restricts $H_2$ motion compared to monovalent ions ($Na^+$) due to their larger hydration shells and stronger electrostatic interactions. Overall, these findings underscored the critical roles of pore size, surface chemistry, temperature, and salinity in controlling $H_2$ transport in confined systems, which are important implications for UHS technologies.

Hubao et al.[907] investigated the diffusion and distribution of $H_2$ in confined calcium silicate hydrate (C-S-H) nano-pores using MD simulations, covering a wide range of conditions, namely temperatures ranging from 300 to 370 K, pressures from 25 to 400 bar, and pore sizes spanning 2.5−40 nm. The study revealed that $H_2$ molecules tend to accumulate near the C-S-H walls, forming a high-density adsorption layer. The diffusion of $H_2$ was shown to be strongly anisotropic, with diffusion parallel to the walls being significantly faster than in the perpendicular direction. Furthermore, increasing pressure notably elevates the density and suppresses the overall diffusion coefficient, whereas higher temperatures reduce the density and enhance mobility. Although similar observations have been already made, for confined fluids, $H_2$ exhibits a distinct single adsorption layer due to its relatively weak interactions with the surface compared to materials like water and $CO_2$, for which multi-layer adsorption is often reported. Finally, the work demonstrated that as the pore size increases beyond a critical threshold (ca. 20 nm), the confined diffusion gradually approaches that of the bulk phase.

Raza et al.[908] reported self−diffusivities of $H_2$ in organic-rich shale, focusing on how $H_2$ transport behavior changes with pore confinement, pressure, and indirectly with surface chemistry via kerogen type. The study considers two representative kerogen types (II-A, representing immature

organic matter, and II-C, representing mature organic matter) with slit pore sizes of 0.5 and 2 nm. The temperature was constant at 360 K while pressures ranged from 30 to 400 bar. The findings indicated that the dominant transport mechanism is "transitional diffusion," characterized by Knudsen numbers between 0.64 and 9.72, where $H_2$ diffusion is a balanced interplay between slip flow and molecular diffusion. Across both kerogen types, a clear trend emerges where $H_2$ diffusivity declines with increasing pressure, and, importantly, larger pores (2 nm) consistently yield higher self-diffusion coefficients (ranging from ca. 0.004 to 0.02 cm²/s for type II-A and 0.0037 to 0.019 cm²/s for type II-C) compared to the 0.5 nm pores. For a fixed nano-pore size, the thermal maturity of the kerogen does not have a discernible impact on $H_2$ diffusivity even though type II-A tends to retain greater $H_2$ density due to stronger adsorption effects. Finally, the diffusion data were successfully regressed to a power-law model with coefficients of determination ($R^2$) being in the range 79−98%, providing a continuous description of the diffusivity−pressure relationship. Note that while the study explores variations with pore size and pressure in depth, the temperature was kept constant and specific variations in surface chemical properties beyond the kerogen type were not explicitly considered.

Kim et al.[909] also studied the $H_2$ diffusion within nanoporous shale caprocks. The simulations considered both binary ($H_2/CH_4$) and ternary ($H_2/CH_4/CO_2$) gas mixtures confined by three distinct pore types i.e., organic pores formed by kerogen, inorganic pores formed by clay, and mixed−wet pores composed of both kerogen and clay. The simulations were carried out at 300 atm and 326 K, focusing on diffusive transport in two directions: perpendicular ($x$ direction) to the pore faces (which, due to periodic boundary conditions, includes diffusion through the kerogen matrix) and parallel ($yz$ direction) to the pore surfaces. Graham's law states that the rate of gas diffusion varies inversely with the square root of its molecular weight (i.e., lighter gases diffuse faster than heavier ones). However, while the expectation is that $H_2$ (having very low molecular weight) should diffuse much more rapidly than $CH_4$ and $CO_2$, the results by Kim et al.[909] showed that the differences are moderated by additional factors such as surface affinity, adsorption by water and ions, and restrictions imposed by the available pore space. In fact, $H_2$ exhibits a self-diffusivity in the order of $10^{-7}$ m²/s in the parallel direction in clay and mixed-wet pores, whereas diffusion through kerogen is reduced by 2−3 orders of magnitude owing to its much smaller pore sizes (ca. 1 to 10 nm). These findings illustrate that, beyond the influence of molecular weight, the interplay between adsorption phenomena and pore geometry is critical for understanding $H_2$ diffusivity in geologic media.

Ghasemi et al.[910] also performed MD simulations to investigate $H_2$ diffusion in confined, water−saturated clay minerals, which is a representative caprock system for UHS. The authors systematically explored the effects of pore size, surface chemistry, and interlayer cations under conditions of 368.15 K and 300 bar. The study examined five clay mineral types, namely pyrophyllite (uncharged), Na- and Ca-montmorillonite, and Na- and Ca-beidellite (both negatively charged with different charge distributions), providing insight into how $H_2$ mobility is affected confinement in the pores. For the charged clays, a critical pore size of ca. 2 nm was observed for which a substantial increase in the $H_2$ diffusion coefficient occurred (increase of up to 24.06% relative to bulk water), while for pyrophyllite the diffusion coefficient increased

monotonically with pore expansion, indicating that is not affected by surface charge. The study also showed that the distribution of negative charges (concentrated in the octahedral layer of montmorillonite versus the tetrahedral sheets in beidellite) significantly influences the positioning of $H_2$ molecules relative to the clay surfaces, thereby affecting diffusion, whereas the effect of inter-layer cations (with $Na^+$ allowing slightly higher mobility compared to $Ca^{2+}$ due to their closer association with the clay surface and smaller hydration shell) is comparatively less pronounced. By using the Einstein relation to analyze molecular trajectories, the authors corroborated that confined $H_2$ diffusion is markedly different from that in bulk water and converges toward bulk behavior as pore size increases beyond 2 nm, with the diffusion coefficient for some clays approaching that in bulk water (ca. 13.07 × $10^{-9}$ m²/s) at larger spacings (up to 8 nm).

A common oversight observed in many of the studies discussed above relates to the subtlety involved in diffusion parallel to interfaces. Determining diffusion coefficients of gases and liquids confined within cavities or at inhomogeneous interfaces, such as air-water or water-solid boundaries, presents unique challenges.[911−913] In confinement, traditional methods like the Einstein or Kubo relations (see Section 3.2.1) become insufficient. For confined liquids, the MSD is inherently limited by the size of the confinement, making it difficult to clearly define a diffusion coefficient. For systems with inhomogeneous regions, particles typically spend a finite duration within a specific area before exploring others (see also the discussion on $H_2$ diffusivity in polymers in Section 4.4). Consequently, the diffusion coefficient will vary across regions, and the MSD computed for particles initially localized in a particular region will only exhibit linear behavior after sufficient time has elapsed, allowing particles to sample all available regions. Ultimately, the slope of this long-term linear behavior represents an averaged diffusion coefficient across the entire system.

Berne and co-workers developed a methodology to quantify position-dependent diffusion coefficients in interfacial or confined fluids, where conventional MSD or GK approaches fail.[914] The method is based on the anisotropic Smoluchowski equation, which describes molecular diffusion in systems with an inhomogeneous density profile arising from the influence of the solid-liquid or liquid-vapor interface. This spatial variation in density can be expressed as a potential of mean force that enters the Smoluchowski formulation, allowing diffusion to be resolved into diffusivities parallel and perpendicular to the interface. For the parallel component, MD trajectories are analyzed within each layer while imposing virtual absorbing boundaries. The mean lateral displacement of molecules that remain within a layer yields the local in-plane diffusivity. For the perpendicular component, where the location of a molecule from the solid-liquid or liquid-vapor interface strongly affects molecular motion, Langevin dynamics simulations are performed in parallel with MD using the same potential of mean force and boundary conditions. The friction parameter in the Langevin model is adjusted until the survival probability matches that from MD, from which the perpendicular diffusivity is inferred. For layers located well within the bulk phase, where the density is uniform and unaffected by interfacial gradients, the perpendicular diffusivity is readily obtained from the exponential decay of the molecular survival probability within that region. Although accurate and physically motivated, this dual-simulation approach can be
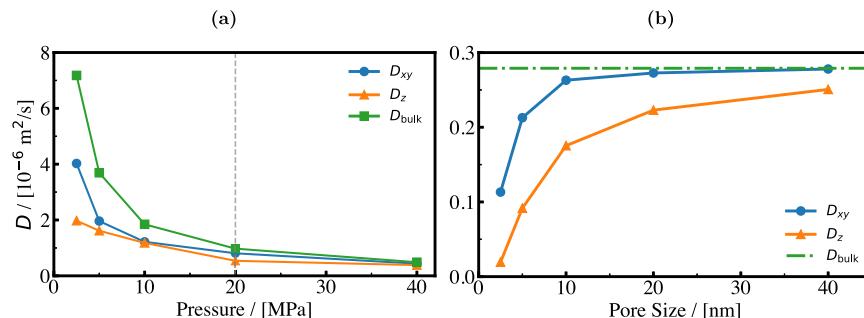
**Figure 52.** Self-diffusion coefficients of hydrogen in calcium silicate hydrate (C-S-H) pores computed with MD simulations. (a) Lateral ($D_{xy}$, blue circles), perpendicular ($D_z$, orange triangles), and bulk ($D_{bulk}$, green squares) diffusion coefficients as a function of pressure at a fixed pore size of 5 nm and temperature of 340 K. A vertical dashed line indicates 20 MPa, corresponding to the conditions in (b). (b) Lateral ($D_{xy}$, blue circles), perpendicular ($D_z$, orange triangles), and bulk ($D_{bulk}$, green dash-dotted line) diffusion coefficients versus pore size at a fixed pressure of 20 MPa and temperature of 340 K. All data in the plots are taken from Hubao et al.[907]

cumbersome since Langevin dynamics must be solved alongside MD for each spatial region, motivating later efforts toward simpler alternatives for evaluating perpendicular diffusivities.

Of relevance in this context is the work of Mercier Franco et al.,[911] who proposed an analytical alternative to the dual-simulation approach. In their method, the potential of mean force associated with regions of non-uniform density is linearized, allowing the anisotropic Smoluchowski equation to be solved analytically for the perpendicular diffusivity. In this framework, the perpendicular diffusivity is inversely proportional to the molecular residence time, defined as the time integral of the survival probability, within a given layer. Hence, layers where molecules remain trapped for longer times exhibit lower perpendicular diffusivities. The predicted diffusivities for water near the liquid-vapor interface agree closely with those obtained by Liu et al.,[914] validating the underlying approximation. This methodology was later extended by Spera et al.[915] to methane-ethane mixtures confined in calcite nanopores, where steep density gradients arise near the walls. Their study demonstrated that the perpendicular diffusivity in the first adsorbed layer is highly sensitive to the precise definition of the interfacial boundary, highlighting the importance of accurately identifying the starting point of the adsorbed layer. In all such cases, the perpendicular diffusivity remains consistently smaller than the corresponding parallel component. An alternative approach was proposed by Předota et al.,[916] who directly computed spatially resolved diffusivities from molecular dynamics trajectories by tracking mean-square displacements within bins parallel to the interface. To minimize artefacts from molecules crossing between bins, half of the squared displacement was apportioned to the initial and terminal bins, and diffusivities were extracted from the linear regime of the mean-square displacement over intermediate timescales. This pragmatic treatment yields well-behaved perpendicular diffusivities even in finite slab geometries and provides a numerically efficient alternative to dual-simulation or analytical methods.

The methodology proposed by Berne and colleagues (and modifications of this methodology) has successfully been applied in multiple contexts, including the diffusion of water confined within clay materials,[917−919] and more recently in H$_2$ storage studies. For instance, Bui et al.[895] used this method to computed water diffusion parallel to surfaces at various spatial locations, close to hydrophobic and hydrophilic surfaces, and

within the bulk region. Among recent hydrogen diffusion studies, only Liu et al.[906] and Hubao et al.[907] explicitly considered diffusivities within distinct layers, while other studies[877−879,899,905,908−910] did not follow this layered approach.

Considering these insights, we proceed by examining how the wall-parallel ($D_{xy}$ - lateral) and wall-normal ($D_z$ - perpendicular) diffusivities vary with pressure and pore size. Initially, we focus on the results from Liu et al.,[906] since[906] do not explicitly address these diffusion dependencies. In Fig. 52(a), both $D_{xy}$ and $D_z$ decrease with increasing pressure, approaching $D_{bulk}$. This trend signifies reduced confinement effects at higher pressures, where H$_2$-H$_2$ collisions dominate over pore wall interactions. Under all conditions considered, $D_{xy}$ remains significantly higher than $D_z$, clearly demonstrating anisotropic diffusion due to confinement by the nano-pore walls. At low pressures, diffusion within nano-pores strongly deviates from bulk values due to prominent wall interactions. H$_2$ molecules become adsorbed on the C-S-H surfaces, significantly restricting mobility, particularly perpendicular to the walls. With increasing pressure, the nano-pores become densely populated, and molecular collisions dominate diffusion behavior, diminishing confinement effects. Consequently, diffusivities (especially the lateral component - $D_{xy}$) approach bulk-phase values. Fig. 52(b) shows that at larger pore sizes (20−40 nm), $D_{xy}$ approaches bulk values faster than $D_z$, indicating stronger confinement effects in the perpendicular direction. Overall, larger pore sizes enhance diffusion rates and reduce anisotropy. Liu et al.[906] reported similar anisotropic diffusion behavior in nanoporous montmorillonite, where lateral mobility closely matches bulk-phase diffusion even near surfaces, while perpendicular diffusion is significantly hindered due to confinement and boundary interactions. Lastly, as emphasized by Ghasemi et al.,[910] it is essential to account for hydrodynamic finite-size corrections when evaluating self-diffusivities in confined environments,[499] a point initially highlighted by Rotenberg and colleagues.[920] Among the reviewed studies, only Ghasemi et al.[910] explicitly considered these corrections, reporting a mere 2% impact of confinement on H$_2$ self-diffusivities. We conclude by urging future studies to consider both anisotropic diffusivities and finite-size hydrodynamic effects when reporting self- or mutual diffusivities of H$_2$ mixtures under confinement.

**4.7.4. Hydrogen Intercalation and Leakage in Geological Nanopores.** The behavior of H$_2$ within geological nano-pores is highly affected by two complementary but

distinct phenomena: (1) intercalation of $H_2$ into hydrated clay nano-pores, and (2) $H_2$ leakage through nano-pore defects and cracks. While intercalation studies primarily explore how $H_2$ molecules enter and remain within clay layers, leakage studies focus on identifying mechanisms by which $H_2$ may escape from these geological barriers. In this section, we first address recent advances in the energetics and molecular interactions governing $H_2$ intercalation, followed by a discussion of factors influencing $H_2$ leakage from nanoporous caprocks.

Ho et al.[921] investigated $H_2$ intercalation mechanisms in hydrated montmorillonite clay, relevant to $H_2$ geological storage. Using meta-dynamics/MD simulations, the authors showed that dissolving $H_2$ in bulk water is highly unfavorable (2.3 kcal/mol). Within clay interlayers (with spacings of 12.5 Å and 15 Å), $H_2$ intercalation remains thermodynamically challenging, though slightly less so in hydrophobic regions near siloxane ring centers due to their lower local charge density. In contrast, regions with higher charge density from isomorphic substitutions (e.g., Mg replacing Al) and interlayer cations strongly repel $H_2$ intercalation. Compared to $H_2$, $CO_2$ demonstrated significantly more favorable energetics, indicating that the limited polarizability and quadrupole moment of $H_2$ severely restricts its interactions within these environments. Muther and Dahaghi[922] extended this analysis by studying $H_2$ intercalation in hydrated sodium montmorillonite (Na-MMT) clay under realistic geological conditions (1−50 MPa, 298−403 K). They observed similarly low $H_2$ intercalation mole fractions (approximately $1.569 \times 10^{-6}$ to 0.0119), attributed to the limited solubility of $H_2$ in water, and its weak interactions with clay surfaces. Crucially, intercalation is significantly influenced by the hydration state, with increased uptake generally occurring during the transition from monolayer (1W, ∼12.5 Å) to bilayer hydration (2W, ∼15.5 Å), although slight decreases may result from water filling interlayer spaces. Competitive adsorption with $CO_2$ and $CH_4$ further reduces $H_2$ uptake (by ca. 32% and 52%, respectively), highlighting complex interactions among gases that limit $H_2$ storage potential but simultaneously mitigate risks to caprock integrity.

Li et al.[329] studied $H_2$ leakage through nano-cracks in kaolinite caprocks using MD simulations. The focus was on $H_2$ near hydrophilic gibbsite and hydrophobic siloxane surfaces at 333.15 K and 30 MPa, varying water content and cushion gas compositions. On gibbsite surfaces, increasing water content significantly reduces $H_2$ leakage—from nearly complete leakage at low water content to below 5% when water is sufficient to form dense adsorption layers. On siloxane surfaces, water distribution is less uniform, leading to variable $H_2$ retention efficiency. For $CO_2$, stronger adsorption in gibbsite and kaolinite aquifers enhances its collaboration with $H_2O$ to effectively block cracks. For $CH_4$, while it helps plug $H_2$ leakage on hydrophilic gibbsite by hindering entry, its role is minimal on siloxane surfaces, where the non-uniform distribution of $H_2O$ governs leakage control. These findings emphasize surface chemistry, water content, and gas composition as critical factors for leakage prevention. Liu et al.[923] further explored $H_2$ leakage through nanoporous shale caprock using MD and MC simulations. The authors highlighted that $H_2$, due to the small molecular size (less than 1 Å), easily leaks through nano-pores, whereas larger molecules such as $CH_4$ create stable adsorption layers, reducing $H_2$ contact with rock surfaces. Water further reinforces caprock integrity by forming clusters through $H_2$ bonding, enhancing the sealing effect in combination with

$CH_4$. Leakage increases with pore size, significantly intensifying beyond approximately 10.5 Å. Higher pressures accelerate leakage through distinct stages of blockage, partial penetration, and eventual breakthrough. Additionally, elevated temperatures weaken water clusters by disrupting $H_2$ bonds, thereby increasing $H_2$ leakage. This study underscores the critical interplay between pore geometry, surface chemistry, and environmental conditions in governing $H_2$ leakage dynamics.

In summary, these studies collectively illuminate the complexities underlying $H_2$ behavior in nanoporous geological formations. The low affinity of $H_2$ for water and clay surfaces poses intrinsic barriers to efficient intercalation, while nano-pore surface chemistry, water content, gas composition, and operating conditions decisively influence leakage pathways. These insights from molecular simulations can significantly contribute to strategies for safer and more efficient UHS.

## 4.8. Hydrogen in Pure and Mixed Hydrates

### 4.8.1. Hydrate−Liquid−Vapor Three-Phase Equilibria of Aqueous Hydrogen Solutions.
Frankcombe and Kroes[934] performed MD simulations using 2D, sII clathrate hydrate slabs with an occupancy equal to (1S + 4L) $H_2$, in contact with a slab of $H_2$ gas at a pressure of 1500 bar. The authors used different water force fields (SPC/E, TIP3P, TIP4P, TIP4P/2005, TIP4P/Ice, and TIP5P) to compare the predicted stability of the $H_2$ hydrate in the simulation with the respective experimental data, and concluded that TIP5P yielded the best temperature−pressure stability prediction for the hydrate, predicting a decomposition temperature in the range 245−265 K. It should be noted, however, that this conclusion was the result of a single MD simulation, instead of using multiple replicas as discussed in detail in refs 369 and 578.

The first attempt to calculate the three-phase ($H − L_w − V$) equilibria (see Fig. 8 for notation) for the binary $H_2 −$ water system using the "direct phase coexistence" approach was reported by Luis et al.[935] The authors used TIP4P/Ice and the $H_2$ force filed proposed by Alavi et al.[336] (see details in Section 3.1), and reported predictions that were underestimating the three-phase equilibrium temperature by ca. 16−20 K. In a subsequent study, Luis et al.[936] examined the effects of externally-applied static electric fields on the stability of $H_2$ hydrates. The authors concluded that hydrate crystallization is prevented with a certain magnitude of electrical field, which depends on the pressure of the system. Namely, as the pressure increases, an electrical field of lower intensity is needed to inhibit crystallization.

Michalis et al.[342] performed simulations with a modified "direct phase coexistence" approach and reported a significant improvement (i.e., by 10.5 K) in the calculation of the three-phase equilibria temperatures for the pressure range 100−300 MPa compared to the earlier study of Luis et al.[935] The improvement was the direct result of implementing two modifications in the treatment of the $H_2$ force-field. Namely, (i) the use of $H_2$ LJ parameters that are a function of temperature, and (ii) the water−$H_2$ guest energy interaction parameters were optimized further by using the Lorentz-Berthelot combining rules, accounting for the improved description of the solubility of $H_2$ in water (i.e., Eq. (8) discussed in Section 3.1.1). While the simulations by Michalis et al.[342] currently provide the most accurate description of the $H − L_w − V$ equilibrium temperature for the binary $H_2 −$ water system, using the "direct phase coexistence" approach, there is

still room for improvements. In particular, there is still an under-prediction of the three-phase equilibrium temperature of the pure $H_2$ hydrate by a $\Delta T$ that is higher than the value of 3.35 K, that the TIP4P/Ice water model under-predicts the melting point of ice $I_h$. This is clearly shown in Fig. 53 which is
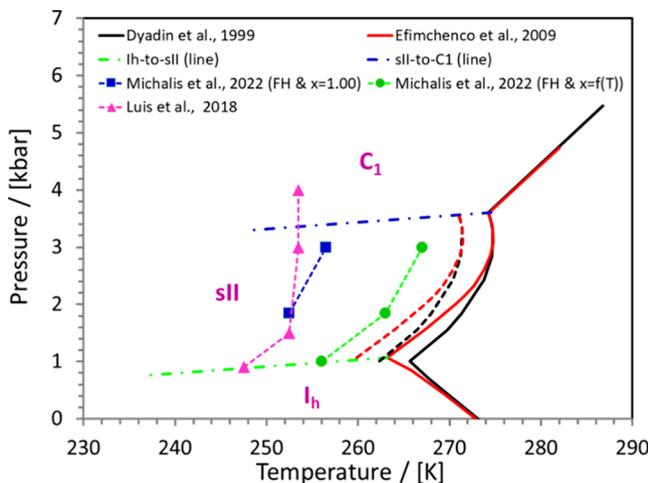


**Figure 53.** Experimental values (denoted with lines) and MD data from Michalis et al.[342] [blue squares: Feynman−Hibbs (FH) and $\chi$ = 1.00; green circles: FH and $\chi = f(T)$] and from Luis et al.[935] (magenta triangles) for the three-phase coexistence temperature of the hydrogen hydrate system. The two dashed lines denote the MD-expected phase equilibrium lines corresponding to the experimental data of Dyadin et al.[244] (black line) and Efimchenko et al.[937] (red line). The MD-expected values presented in the figure are defined as $T_{\text{Eq,expected}} = T_{\text{Eq,exp}} - 3.35$ K, where $T_{\text{Eq, exp}}$ is the experimental three-phase equilibrium temperature. Data extracted from ref 342.

constructed with data from ref 342. Another important observation made by Michalis et al.[342], that needs future experimental/computational investigation, is the reported discrepancy between the experimental data for the three-phase equilibrium conditions for the binary $H_2$ − water system of Dyadin et al.[244] and Efimchenko et al.,[937] especially at temperatures lower than 268 K (see Fig. 53).

Kang et al.[938] used the "phase coexistence" approach to calculate the three phase equilibria for the mixed $H_2$ + THF (5.56 mole% THF) hydrate at 100, 250, and 400 bar. The authors considered two different cases for the LJ parameters between the centers of the mass of $H_2$ and the oxygen of $H_2O$. Namely, the first case used LJ parameters based on ab initio calculations, while the second used the classical Lorentz-Berthelot mixing rule. As shown in Fig. 54 the ab initio-based parameters produce better agreement with the experimental measurements.

### 4.8.2. Kinetics of Hydrate Growth/Decomposition.
Zhang et al.[594] studied the growth of mixed $H_2$ + $CH_4$ hydrate with MD simulations, motivated by the high energy density of the particular gas mixture. The authors reported that the growth mechanism of the mixed hydrate is controlled by the solubility and diffusivity of the guest molecules. The complex interplay of diffusivity and solubility with the increasing temperature results in a growth rate and cage occupancy maximum at 250 K and a pressure equal to 50 MPa. Therefore, by an appropriate selection of $P$, $T$ conditions certain storage capacities can be achieved. In a similar study Tian and Zhang[595] studied the mixed $H_2$ + THF hydrate with MD simulations and reported growth rates at (i) 50 MPa and
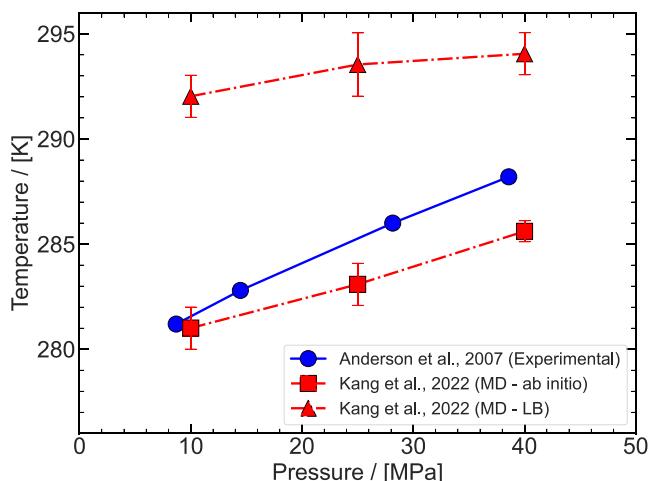


**Figure 54.** Phase equilibria $(H-L_w - V)$ of $H_2$ + THF hydrates. Blue circles denote experimental measurements (5.56 mole% THF) by Anderson et al.[939] Red symbols denote the MD "phase coexistence" simulation values of Kang et al.[938] Lines connecting the symbols are guides to the eye only.

temperatures in the range 230−270 K, and (ii) at 250 K and pressures in the range 20−110 MPa, reporting a maximum cage occupancy maximum at 260 K and a pressure equal to 50 MPa. The computed $H_2$ storage capacity was shown to be correlated with the trend of the growth rate. Fig. 55a shows the hydrate growth rates computed with MD as a function of $T$ (at $P$ = 50 MPa), while Fig. 55b shows the calculated hydrate growth rates as a function of $P$ (at $T$ = 250 K) for the cases of $H_2$ + $CH_4$ (Zhang et al.[594]) and $H_2$ + THF (Tian and Zhang[595]) mixed hydrates. Tian and Zhang[595] observed that in MD simulations at 50 MPa, the mixed $H_2$ + THF hydrate growth rates exhibit a maximum at 260 K, which is close to the temperature conditions of the maximum growth rates of pure THF hydrate. For temperatures above 260 K, a dramatic decrease is observed in the growth rate (see Fig. 55a). Notice that for the case of $H_2$ + $CH_4$ the maximum is obtained at 250 K. Contrary, as shown in Fig. 55b, a practically negligible dependence on pressure is observed (for constant $T$ = 250 K) for the growth rates of the mixed $H_2$ + THF hydrate. However, for the case of $H_2$ + $CH_4$, Zhang et al.[594] reported an increase of almost 300% in the growth rate for the pressure range 20−110 MPa.

While the studies of Zhang et al.[594] and Tian and Zhang[595] reported hydrate growth rates in units of $[nm^{-2} \, ns^{-1}]$, other MD studies report growth rates in units of [cages/ns]. Such are the studies by Kang et al.[938] for $H_2$ + THF mixed hydrate, and Hu et al.[940] for $H_2$ + $CH_4$ mixed hydrate. The combined results of the two studies are shown in Fig. 56, where the hydrate growth rate is plotted as a function of the THF (or $CH_4$) concentration in units of [mol%]. From Fig. 56 it becomes evident that as the concentration of THF (or $CH_4$) increases towards the stoichiometric value, hydrate formation rate decreases in both cases of mixed hydrates. Furthermore, similar to the conclusion reported by Tian and Zhang,[595] a negligible effect of pressure on the growth rate can be seen in the MD simulations of Kang et al.,[938] for the case of $H_2$ + THF mixed hydrates.

Ghaani and English[941] performed both equilibrium and non-equilibrium MD simulations to study thermal-driven decomposition of mixed $H_2$ + propane planar clathrate crystals with
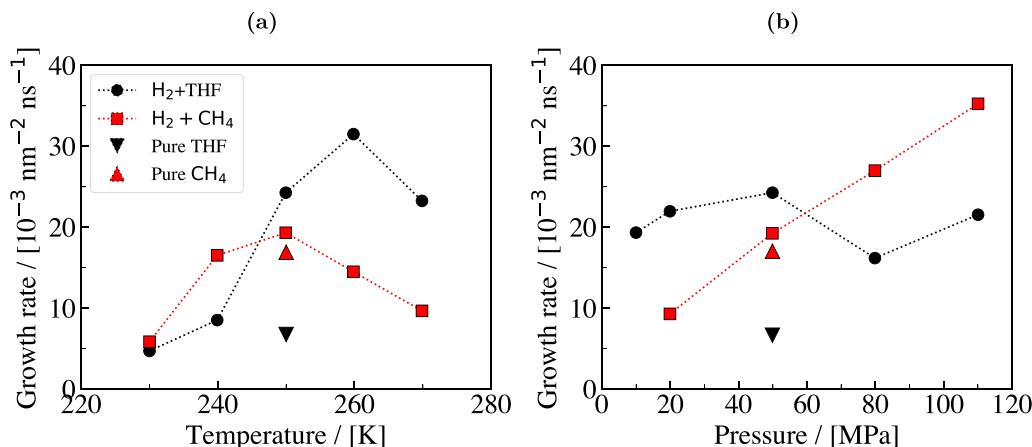
**Figure 55.** Comparison of computed growth rates of $H_2$ + THF (black symbols − Tian and Zhang[595]) and $H_2$ + $CH_4$ (red symbols − Zhang et al.[594]) binary hydrates: (a) growth rate as a function of temperature at 50 MPa and (b) growth rate as a function of pressure at 250 K. The triangles represent the growth rates of pure THF and $CH_4$ hydrates, respectively. Lines are drawn to guide the eye. The data are taken from ref 595.
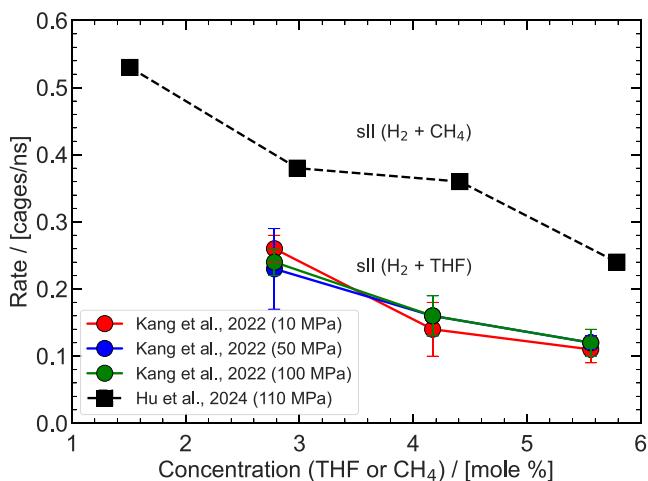


**Figure 56.** Hydrate growth rate as a function of THF (or $CH_4$) concentartion. Comparison of growth rates of $H_2$ + THF (red symbols − Kang et al.[938]) and $H_2$ + $CH_4$ (green symbols − Hu et al.[940]) binary hydrates computed with MD simulations. Lines are drawn to guide eye.

liquid water at 260−320 K. The authors concluded that the different surface-cavity terminations result in substantial differences in initial break-up rates. In a subsequent study, Ghaani et al.[942] used non-equilibrium MD simulations to study the $H_2$ release and uptake from/into propane planar clathrate surfaces a temperatures ranging from 180 to 273 K.[943] reported experimental measurements and MD simulations of the mixed sII $H_2$ + propane hydrate dissociation by heating or depressurization, and concluded that (i) $H_2$ release from the hydrate crystal was much faster than that of propane, with experiments and simulations being in agreement, and (ii) simulations showed that hydrate dissociation induced by depressurization was slower than the case induced by heating, an observation which contradicts the experimental measurements reported in the same study. The authors tracked the number of $H_2$ and propane molecules in the aqueous and hydrate phases. Only complete cages were considered for the counting of $H_2$ and propane molecules in the hydrate crystal. They also tracked the number of hydrogen bonds and the potential energy. The number of hydrogen bonds was closely

associated with the degree of crystallization of water molecules, reflecting, thus, the kinetics of hydrate dissociation.

### 4.8.3. Structural and Other Properties of Hydrates.

Wang et al.[180] combined QM calculations with classical MD to compute average structure and vibrational spectra of $H_2$ in pure sII $H_2$ clathrate. The authors reported that the $H_2$ molecules in the L cages and the singly-occupied S cages are stretched, and the vibrational mode is softened and uncoupled. Contrary, in the case of doubly-occupied S cages, the $H_2$ molecules were shown to be slightly compressed, with the vibrational frequencies being close or above that of the free gas. Furthermore, a strong vibrational coupling was observed as a result of the short intermolecular distance between the two $H_2$ in the S cages.

Gorman et al.[944] performed MD simulations to investigate the dynamical and energy-related properties in sII pure $H_2$ and mixed $H_2$ + THF hydrates at 30 and 200 K (also at intermediate temperatures) and 0.05 kbar, using SPC/E and TIP4P/2005 water models. The study ignored the quantum effects which are expected to be important at temperatures below 150 K. Mondal et al.[334] performed MD simulations to calculate binding energies and radial distribution functions for various cases of occupancies of the sI pure $H_2$ hydrate, using the SPC/E water model. By observing the radial distribution functions of $H_2$ loaded hydrates, the authors concluded that within the time-scale considered (200 fs), the $H_2$ hydrate cages are not ruptured. In a later study,[945] also performed MD simulations on structure and dynamics of high-pressure ices and filled ices, using TIP4P and TIP5P water models. This study focused on the rotational motions of both $H_2O$ and $H_2$ molecules in the filled-ice $C_2$ in addition to those in ice VII.

Rick and Freeman[364] used three water models (SPC/E, TIP4P/Ice, and TIP4P-FQ/Ice) to predict dielectric constants, the proton order parameters, and the molecular volumes for pure Ar and $H_2$ clathrate systems. The conclusion provided was that the dielectric response arises only from the water molecules as a result of the fact that the guest molecules do not have a dipole moment. English et al.[946] performed equilibrium MD simulations to investigate thermal conduction mechanisms via the GK approach (see Section 3.2.1) for sII pure $H_2$ hydrate, at 0.05 kbar and temperatures in the range 30−250 K. The authors considered the TIP4P water model, and assumed single or double occupancy of the $5^{12}$ cages and quadruple

occupancy of the $5^{12}6^4$ cages. Consistent with prior literature, in this study it was pointed out that for temperatures of ca. 150 K and below, it is expected that classical MD will not accurately capture the quantum nature of $H_2$ motion. Zhao et al.[947] performed MD simulation, as well as DFT and AIMD simulations, of spontaneous formation of quasi-one-dimensional (Q1D) $H_2$ gas hydrates within single-walled carbon nanotubes (SW-CNTs) of nanometer-sized diameter (1−1.3 nm) occurring at near ambient temperature. It was observed that the guest $H_2$ molecules in the Q1D hydrates are contained within a 1D nanochannel in which the $H_2$ molecules form a molecule wire, while in conventional $H_2$ hydrates the guest $H_2$ molecules are contained in individual 3D cages.

**4.8.4. Hydrate Storage Capacities from Molecular Dynamics Simulations.** The pioneering work of Alavi et al.[336] was the first one to report anisotropic *NPT* MD simulations of pure sII $H_2$ hydrates with flexible cages and periodic boundary conditions. $H_2$ molecules were modeled using the potential developed within this study (see details in Section 3.1.1), while SPC/E force field was used for water. Water molecules of the hydrate lattice were allowed to move about their equilibrium positions. Simulations were performed at 1.013 and 2.5 kbar, temperatures in the range of 100−250 K, and for various $H_2$ occupancies in each cage type, ranging from (1L + 0S) to (4L + 2S). Alavi et al. showed that the energy per unit cell for each $H_2$ occupancy makes a large "jump" when going from the single to the double occupancy of the S cage. This was interpreted as a strong indication that the double occupancy in the S cages would not be stable. A subsequent study[343] using MD (*NPT*) simulations of pure sII $H_2$ hydrates with the SPC/E water model, and a $H_2/D_2$ potential parameterised to account for QM effects of $H_2$ motion at low temperatures, resulted in similar conclusions regarding the $H_2$ occupancies in the L and S cages.

Alavi et al.[948] extended their previous study of pure $H_2$ hydrates[336] to binary, THF + $H_2$ sII hydrates to study the energetics of the occupancy of the $H_2$ guests in the S and L cages, and again reached to similar conclusions regarding the cage occupancies. Furthermore, the simulations revealed that replacing a THF molecule in the L cages of the unit cell by a cluster of four $H_2$ molecules is accompanied by an increase in unit cell total potential energy and volume. The authors examined the possibility of observing the tuning effect, discussed earlier,[247] and concluded, based on MD data, that the formation of binary THF + $H_2$ sII hydrates with large fractions of the L cages occupied by the $H_2$ molecules is not likely to occur if large concentrations of THF are present in the initial hydrate-forming aqueous solution. Such an observation is consistent with MC simulations and experimental studies (e.g., see the detailed discussion in refs 177 and 248). Alavi et al.[949] also performed classical MD simulations for the case of the binary sH methyl-tert-butylether + $H_2$ clathrate hydrate, and similarly to prior literature,[336,343,948] it was observed that the double $H_2$ occupancy of the small (S) and medium (M) cages of the sH hydrate leads to a large increase in energy of the unit cell compared to the single $H_2$ occupancies of these cages.

Daschbach et al.[950] performed MD simulations in order to investigate $H_2$ storage in β-hydroquinone clathrate and showed that higher storage capacities are obtained at lower temperatures. Zhang et al.[594] studied the mixed sII $H_2$ + CH$_4$ hydrate with MD simulations, and reported cage occupancies at (i) 50 MPa and temperatures in the range 230−270 K, and (ii) at 250

K and pressures in the range 20−110 MPa. The findings were single $H_2$ cage occupancies for the case of $5^{12}$ cages, while up to triple $H_2$ occupancies for the case of $5^{12}6^4$ cages. In particular, the simulations indicated that the $5^{12}$ cages are occupied by either single $H_2$ or single CH$_4$ molecules, while the $5^{12}6^4$ cages are occupied by either single CH$_4$ or single or double or triple $H_2$ molecules. Note, however that the authors also mentioned the existence of $5^{12}6^4$ cages with simultaneous occupancy of $H_2$ and CH$_4$, encountered especially at high temperatures and pressures. The importance of this issue will be further discussed in Section 4.8.8. In similar studies, Tian and Zhang[595] and Kang et al.[938] studied the mixed sII $H_2$ + THF hydrate with MD simulations, focusing on occupancies at similar temperature and pressure ranges as in ref 594. The observations regarding the cages $H_2$ occupancy were consistent with the prior studies. Wang et al.[951] performed MD simulations to explore the $H_2$ storage capacity of the mixed sH $H_2$ + methylcyclohexane (MCH) hydrate at 240−260 K and 70−110 MPa. A $H_2$ storage capacity in the range 0.5 to 1.0 wt.% at pressures between 70−110 MPa and temperatures 250 or 260 K was reported, while the storage capacity increased to 1.6−2.0 wt.% at 240 K at the same pressure range. The authors also indicated that the $5^{12}$ cages at the hydrate crystal boundary can prevent the diffusion of $H_2$ inside the hydrate crystal phase.

The collective behavior of storage capacities of the three mixed hydrates (i.e., $H_2$ + CH$_4$; $H_2$ + THF; and $H_2$ + MCH) predicted from MD simulations as a function of pressure/temperature is shown in Fig. 57 and Fig. 58, respectively. As
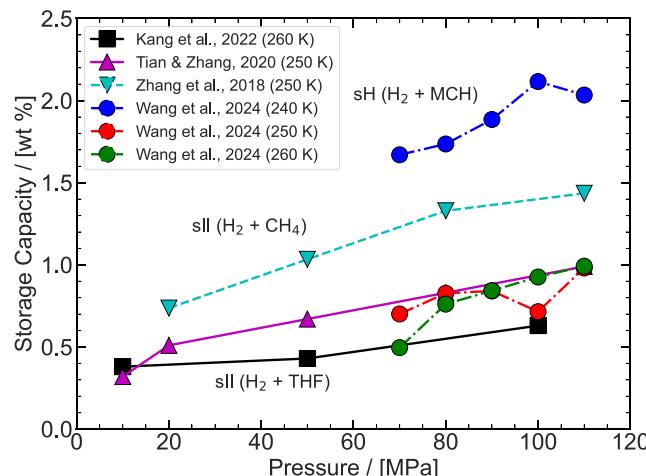
**Figure 57.** Hydrogen content (storage capacity in wt%) as a function of pressure for various temperatures and mixed hydrate systems (at stoichiometric promoter composition): (i) sII $H_2$ + CH$_4$ (Zhang et al.[594] − green triangles), (ii) sII $H_2$ + THF (Kang et al.[938] − red circles; Tian and Zhang[595] − red triangles), and (iii) sH $H_2$ + MCH (Wang et al.[951] − blue symbols). Lines connecting the symbols are to guide the eye.

can be observed from Fig. 57, at a fixed temperature, the storage capacity increases with pressure. In contrast, at a fixed pressure, higher storage capacities occur for the lower temperatures. Among the mixed hydrates considered, the hydrate with the highest storage capacity is the mixed sH $H_2$ + MCH, resulting from the increased amount of $H_2$ diffusing into the $5^{12}$ and $4^35^66^3$. Such behavior for the storage capacity will be further discussed in Section 4.8.5, where storage capacities computed via MC simulations are considered. Similar
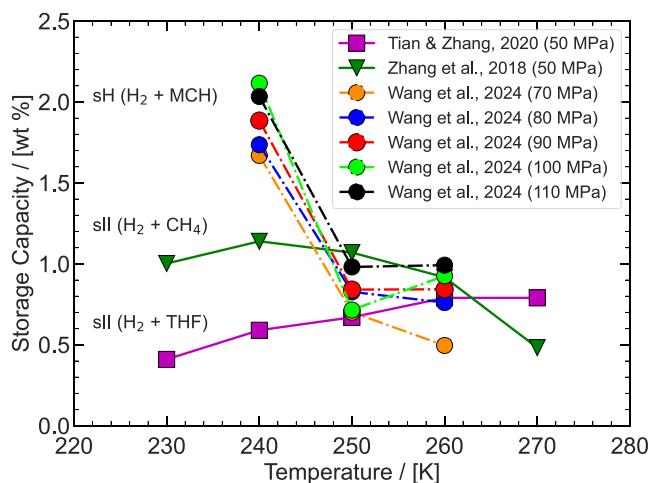
**Figure 58.** $H_2$ content (storage capacity) as a function of temperature for various pressures and mixed hydrate systems (at stoichiometric promoter composition): (i) sII $H_2$ + $CH_4$ (Zhang et al.[594] − green triangles), (ii) sII $H_2$ + THF (Tian and Zhang[595] − red circles), and (iii) sH $H_2$ + MCH (Wang et al.[951] − blue symbols). Lines connecting the symbols are to guide the eye.



**Figure 59.** $H_2$ content (storage capacity) as a function of promoter concentration: (i) sII $H_2$ + $CH_4$ (Hu et al.[940] − green squares), (ii) sII $H_2$ + THF (Kang et al.[938] − red symbols). Lines connecting the symbols are to guide the eye.

conclusions can be drawn from Fig. 58. A notable exception, however, is the study of Tian and Zhang[595] for the mixed hydrate $H_2$ + THF, where it shown that at 50 MPa, the storage capacity increases as the temperature increases as a result of the tuning effect (i.e., the THF concentration is lower than the stoichiometric one (5.56 THF mol%)). The hydrate tuning effect has been a controversial issue, extensively discussed in the literature (see the reviews by Tsimpanogiannis and Economou[240] and Alavi and Ripmeester[177] for more details on experimental and MC studies). Only limited work has been reported using MD simulations.

Hu et al.[940] studied the mixed $H_2$ + $CH_4$ hydrate with MD simulations, and reported the effect of the promoter (i.e., $CH_4$) concentration on the $H_2$ cage occupancies. Five types of cage occupancies for $H_2$ molecules were observed in the MD simulations, namely: (i) single $H_2$, (ii) single $H_2$ − single $CH_4$, (iii) double $H_2$, (iv) double $H_2$ − single $CH_4$, and (v) triple $H_2$. The $5^{12}$ cage can only be occupied by a single $H_2$, while for the $5^{12}6^4$ cage all five of the the above situations can occur. There was no strong tuning effect observed in their study. Kang et al.[938] performed MD simulations for the mixed $H_2$ + THF hydrate, and explored the effect of the promoter (i.e., THF) concentration on the $H_2$ cage occupancies. In this study, tuning effect was clearly identified. Fig. 59 shows the $H_2$ storage capacity of two sII mixed hydrates as a function of the promoter concentration for the two aforementioned studies. Notably, Wang et al.[951] could not identify any tuning behavior for the mixed sH $H_2$ + MCH hydrate.

As pointed out in the review article by Alavi and Ripmeester[177], a consensus is developing based on experimental, classical MD, and MC studies, indicating that in either pure or mixed $H_2$ hydrates (sI, sII, sH) the stable hydrate occupancy configuration is the one with a single $H_2$ molecule in the S cages (or M cage of sH hydrates), while multiple occupancies are possible for the L cages. It should be mentioned that DFT studies (e.g., see discussion in[177]) have reported occupancies higher than classical MD or MC simulations, however, a thorough discussion on this discrepancy is beyond the scope of our review.
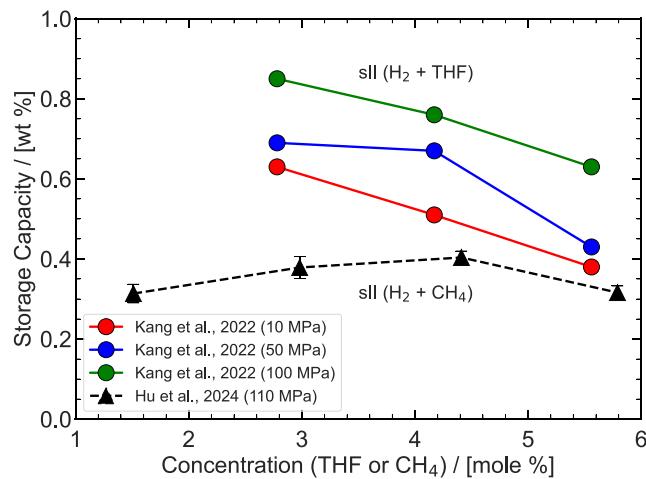
### 4.8.5. Hydrate Storage Capacities from Monte Carlo Simulations.
For a clathrate hydrate structure to be used as a gas-storage material, the number of guest gas molecules enclathrated inside each cavity becomes a critical factor that determines the total storage capacity of the specific hydrate structure. If quadruple occupancy of the L ($5^{12}6^4$) cavities and double occupancy of the S ($5^{12}$) cavities[171] is assmumed, the storage capacity of sII $H_2$ hydrate is 5.0 wt.%. Contrary, the storage capacity drops to 3.8 wt.% $H_2$ if single occupancy of the S cavities is assumed while retaining the quadruple occupancy of the L cavities.[952] The multiple occupancy of a single cavity can significantly increase the storage capacity of the particular hydrate structure. Therefore, it is essential to know how the cavity occupancies evolve as a function of temperature, pressure and the possible presence of other co-guests (promoters or inhibitors) to accurately calculate the storage capacity of different clathrate hydrate structures. To this purpose, GCMC simulations have been proven to be a valuable tool.

The first study to report GCMC simulations of the pure sII $H_2$ hydrate was by Katsumasa et al.[953] Subsequently, Papadimitriou et al.[634] examined the cases of (i) pure sII $H_2$ hydrate, and (ii) the binary sII $H_2$ + THF hydrate, Chun and Lee[954] considered the binary sII $H_2$ + THF hydrate, and Nakayama et al.[955,956] (using the TIP5P water model) studied binary sII $H_2$ + acetone hydrate. These MC studies computationally proved the single occupancy of the $5^{12}$ cages of structure sII, which is in good agreement with subsequent experimental measurements. For a detailed discussion on this subject, the reader is referred to ref 248. It should be noted though, that the GCMC simulations by Koh et al.[957] showed the opposite, i.e., double occupancy in the small cages.

Tanaka and co-workers, extended their previous work on $H_2$ storage in hydrates to various ices ($I_c$, II), as well.[958,959] After establishing the possibility of forming sII $H_2$ hydrates, other hydrate structures were examined as well. Duarte et al.[960] reported experiments of sH $H_2$ hydrate formation in the presence of methylcyclohexane (MCH), 1,1-dimethylcyclohexane (DMCH) and methyl tert-butyl ether (MTBE), followed by GCMC simulations of sH $H_2$ hydrate with MCH as promoter.[635] Subsequently, sI $H_2$ hydrates with promoter

(ethylene oxide) were studied via means of GCMC simulations in ref 636. Both these GCMC studies, also considered the hypothetical pure sH and sI $H_2$ hydrates, since they constitute the upper limiting case for the storage capacities of the two particular hydrate structures. Pure sI $H_2$ hydrate was subsequently experimentally synthesized,[961] thus, confirming the hypothesis of Papadimitriou et al.[636] regarding the existence of the pure sI $H_2$ hydrate.

Papadimitriou et al.[962] presented an overview and a detailed discussion of the three common $H_2$ hydrate structures considered in the earlier studies. The case of pure $H_2$ hydrates was later revisited in a series of GCMC studies.[248,341,640] In these studies, an elaborate and self-consistent MC-based approach was used to relate the chemical potential of the guest with the pressure of the system (see more details about this method in Section 3.3.3). This is important, since earlier studies had used a much simpler approach for the calculation of the chemical potential, based on the use of general-purpose[634−636] or component-specific[638] EoS.

A systematic study and quantification of the effect of the lattice constant of sII $H_2$ hydrate on the storage capacity of the particular hydrate structure was reported in ref 341 while preliminary results following a simpler approach were presented in ref 634. Both studies were motivated by experimental observations[957] indicating that the presence of different promoters in the binary "$H_2$ + Promoter" results in sII hydrates with differences in the lattice constant in the range $0.60 − 3.24\%$ comparing to the value (1.7047 nm)[171] of the sII pure $H_2$ hydrate. The increase in the lattice constant can result in an increase in the $H_2$ storage capacity by up to 3% when compared to the base case.

The effect of three water force fields (i.e., SPC/E, TIP4P/Ice, and TIP5P) on the computed storage capacities of the three most common pure $H_2$ hydrates (i.e., sI, sII, and sH) was reported in ref 248. It should be noted that this study did not reveal a significant effect of the different force fields on the cage occupancies and the corresponding storage capacities (i.e., less than 5% differences were reported). In this context, the use of SPC/E for water and the single-site FH effective potential (see Eq. (7) in Section 3.1.1) for $H_2$ was recommended for the use in GCMC simulations in order to calculate storage capacities. This conclusion is in contrast to the findings of MD simulations studies,[369,578] where it was shown that to accurately calculate the three-phase equilibria conditions, using a water model that can accurately predict the melting point of hexagonal ice, $I_h$, is essential. Therefore, the use of TIP4P/Ice was proposed in these studies. In a related context, Brumby et al.[633] performed MC simulations in the GE that are in good agreement with the results reported in ref 248.

Currently, there seems to be consensus between the various MC simulation studies regarding the occupancy of the small cavities of the three most common hydrates structures. These cavities are singly occupied and cannot accommodate more than one $H_2$ molecules even at the highest pressures examined (e.g., 500 MPa). Contrary, the large cavities of the sI, sII, and sH hydrates, may contain up to 2.3, 3.8, and 6.7 $H_2$ molecules, respectively. The deviation between the water models regarding these occupancy values is less than 4%.

A detailed comparison of the experimental[939,963−965] $H_2$ storage capacities in binary $H_2$+THF hydrates with earlier MC simulations[634,954] is shown in Fig. 60, along with a special modification[966] of the classical van der Waals−Platteeuw theory. Using the latter, one is capable of performing
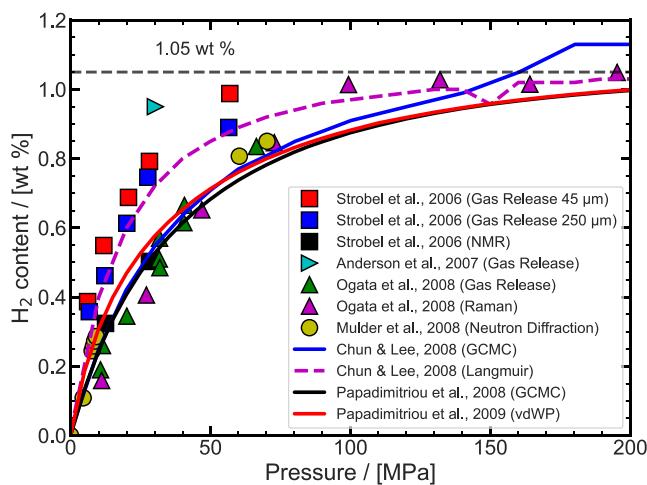


**Figure 60.** Hydrogen content as a function of pressure for the sII binary $H_2$ + THF hydrate. Comparison between: (i) experimental measurements (Strobel et al.;[963] Anderson et al.;[939] Ogata et al.;[964] Mulder et al.[965]), (ii) GCMC simulations (Chun and Lee[954], Papadimitriou et al.[634]), and (iii) the modified van der Waals−Platteeuw (vdWP) theory, proposed by Papadimitriou et al.[966] The horizontal black dashed line (at 1.05 wt.%) denotes the case where all small cavities (i.e., 100% occupancy) are occupied by a single $H_2$ molecule.

calculations at the limit of the 100% occupancy of cages for water-soluble promoters (such as THF). At this limit thermodynamic models based on the classical van der Waals−Platteeuw theory fail to provide any results.

An extensive comparison with results from updated MC simulation studies[248] and additional experimental measurement[967−971] was presented by Papadimitriou et al.[248] for the case of binary $H_2$ sII hydrates. This study presented comparisons under isothermal (i.e., 268, 274, and 278 K) conditions. Fig. 61 shows the data reported in ref 248 along with the corresponding comparison for the 255 K isotherm, using experimental data from Sugahara et al.[972,973] and Kawamura et al.[974] The GCMC results of Papadimitriou et al.[248] were later used by Tsimpanogiannis et al.[975] to develop engineering−type correlations for the $H_2$ storage capacity of the three most common hydrate structures. In principle, the considered methodology could be used to examine storage in hydrates with various promoters, using the assumption that there is no change in the lattice constant resulting from the use of different promoters. This is a reasonable assumption based on the conclusions of Papadimitriou et al.,[341] discussed earlier. This assumption could be relaxed in future studies, nevertheless, it would require a significant number of additional MC simulations to be performed to account for the change in the lattice constant of the hydrate crystals resulting from the use of different promoters.

A general observation we can make from all the GCMC simulation studies reviewed here is that the US DOE specifications regarding the $H_2$ storage capacity of pure $H_2$ hydrates are not met when considering mobility/vehicular applications.[192,197] Namely, the storage capacity is expected to be lower than 4 wt.%. Even lower storage capacities (i.e., less than 2 wt.%) are expected for the cases of mixed $H_2$ + promoter hydrates. However, there is still significant scientific interest on $H_2$ storage in clathrate hydrates for stationary applications.
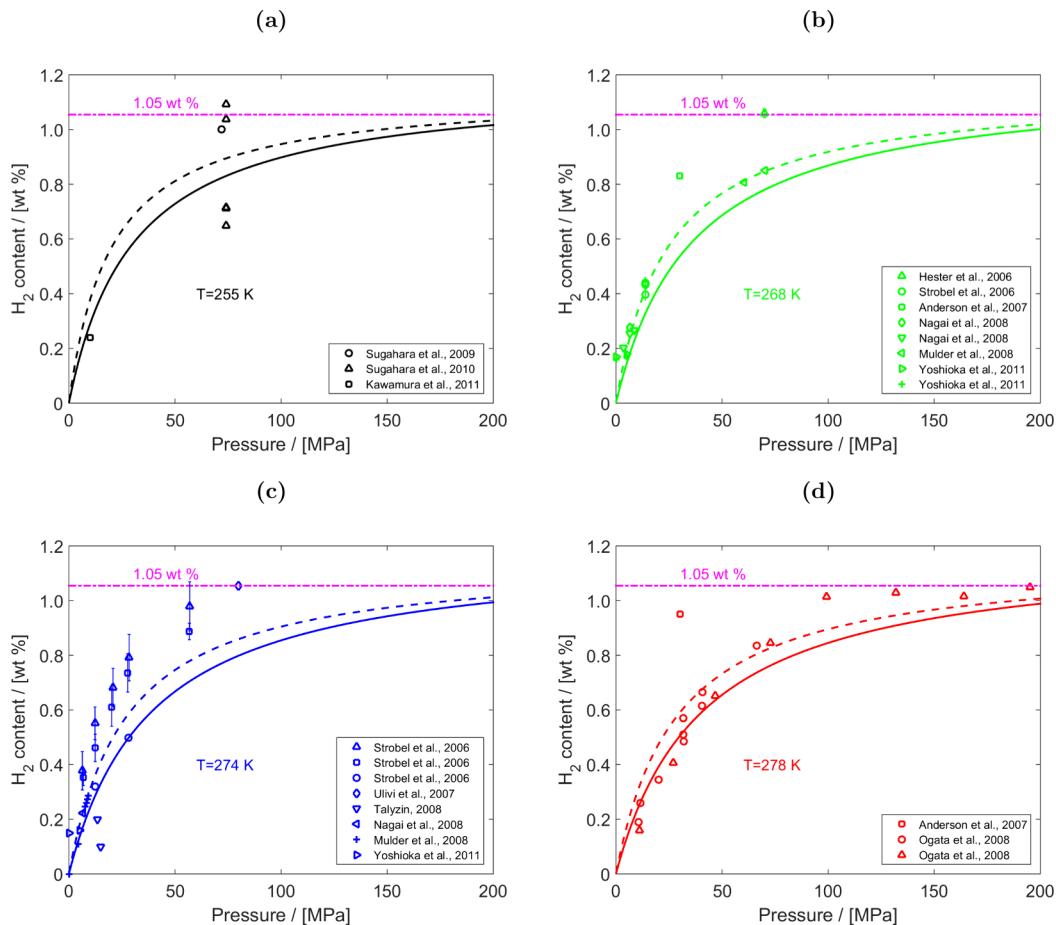
**Figure 61.** Hydrogen content (wt.%) as a function of pressure for the sII binary hydrate $H_2$ + THF using the Silvera−Goldman $H_2$ force field. Comparison between experimental measurements, denoted with symbols (Strobel et al.;[963] Anderson et al.;[939] Ogata et al.;[964] Mulder et al.;[965] Hester et al.;[967] Nagai et al.;[968] Yoshioka et al.;[969] Ulivi et al.;[970] Talyzin[971]), and the MC simulations by Papadimitriou et al.[248] (denoted with lines; solid lines correspond to SPC/E and dashed lines to TIP4P/Ice). The comparison is for four different temperatures: (a) 255 K, (b) 268 K, (c) 274 K, and (d) 278 K. The magenta dashed-dotted line corresponds to the limiting case of 100% of small and large cages occupied with a single $H_2$ and THF molecule respectively. The figure is reconstructed based on the data of ref 248. Error bars are shown only for cases that were reported in the original studies.

**4.8.6. Hydrate-Based Gas Mixture Separation Efficiencies.** While a considerable number of studies have focused on the experimental aspects of hydrate-based separation of $H_2$ − containing mixtures,[976−979] to the best of our knowledge, no relevant MC simulation study has been performed. MC studies for other hydrate mixtures, however, are available in literature: Glavatskiy et al.[980] performed GCMC simulations of mixed $CH_4$ + $CO_2$ hydrates, motivated by the possibility of $CO_2$ replacing $CH_4$ within hydrate deposits. Such a process has gained significant attention lately due to the fact that it can simultaneously take care of two important issues. Namely, the energy production (i.e., $CH_4$) and the sequestration of a "green-house" gas (i.e., $CO_2$) within a single process. In contrast, the study by Papadimitriou et al.,[981] which focused on computing the efficiencies of a hydrate-based gas-mixture separation process (the latter being the motivation), examined the same mixed $CH_4$ + $CO_2$ hydrate system, and reported good agreement between the experimental and GCMC simulations.

**4.8.7. Hydrate-Promoter Selection.** Atamas et al.[982] used the self-referential technique to compute the Gibbs free energy of molecular crystals. The self-referential technique utilizes the principle that the free energy is an extensive

quantity. Therefore, it follows that by constructing a reversible path between two systems that contain $N$ and $2N$ particles, respectively, the free energy difference between the two systems can be calculated as well as the free energy of the system itself. Subsequently, the authors examined the storage of $H_2$ in sII[983] and sH[984] hydrates. The binary $H_2$ + promoter hydrate with lower Gibbs free energy is more stable. The main purpose of both studies was to identify appropriate promoter molecules. An important conclusion of these studies is the identification of THF as one of the most promising promoters for $H_2$ hydrates. Hydrate promoters are molecules that shift the hydrate equilibrium curve to more moderate conditions (i.e., lower pressures or higher temperatures). Hydrate promotion acts in the opposite direction to hydrate inhibition (i.e., a hydrate inhibitor results in shifting the hydrate equilibrium curve to higher pressures or lower temperatures).

Motivated by the need to identify promoters for storing $H_2$ in clathrate hydrates, Frankcombe and Kroes[985] introduced a new predictive computational method for classifying clathrate hydrate promoter molecules, based on the interaction energies between potential promoters and the water networks of sII and sH clathrates. To this purpose, water was modelled using the TIP5P force field. On the other hand, the promoter molecules

were frozen at the geometries minimising the MP2/cc-pVTZ energy, either at the global minimum or at a metastable conformer. Ab initio calculations of the electronic structure of the promoter molecules, with the charges constrained to reproduce the calculated dipole moment of the guest molecule were performed using Gaussian 03. Atamas et al.[986] introduced a generalization of the method by Frankcombe and Kroes,[985] extending it to finite temperatures and pressures. The method is based on Gibbs free energy calculations of sI, sII, and sH $H_2$ clathrates. Atamas et al. reported that the van der Waals volume of a potential promoter is an important parameter which can determine the type (either sII or sH) of clathrate to be formed.

Iwai and Aokawa[987] performed MD simulations for the sII mixed $H_2$ + promoter hydrates to search for potential promoters to stabilise the $H_2$ hydrates. Simulations were performed at 10.1 MPa and an initial temperature 260 K (increased at a rate 0.1 K/s). A slow increase of the hydrate cell volume was initially observed, followed by a rapid increase. The temperature at which the cell volumes rapidly increased was identified as the simulated collapse temperature. The promoter (cyclobutane) which gave the highest simulated collapse temperature was identified as the one to best stabilise the hydrates.

Mi et al.[246] performed an extensive series of equilibrium MD simulation to study the effect of various promoters (i.e., $CH_4$, $CO_2$, $C_2H_6$, $C_3H_8$, $C_5H_{10}$, and THF) on the nucleation of mixed $H_2$ + promoter hydrates. Computations, up to 3 $\mu$s, were performed at a pressure of 110 MPa and a temperature of 240 K to compute free energies, diffusivities, residence time correlation functions, order parameters, and $H_2$ uptake. Mi et al. recommended that instead of using individual properties for identifying the suitability of a tentative promoter for enhancing the behavior of $H_2$-containing hydrates, it is essential to examine the collective control of the aforementioned thermodynamic factors. The authors identified four criteria that an ideal hydrate promoter should possess: (i) High solubility in water for maximizing the guest molecule availability close to the hydrate formation front; (ii) Optimized residence time to enhance nucleation without the need for excessive mobility; (iii) Strong hydrogen bonding interactions to facilitate stable cage formation; (iv) Environmental sustainability to minimize ecological impact.

**4.8.8. Self-Diffusivity of Hydrogen in Hydrates.** Here, we briefly review the most important experimental work in the area of diffusivity of $H_2$, to lay the ground for the review of molecular simulation studies. Earlier studies[988] considered that single $H_2$ molecules were too small to be confined within the hydrate cages, and thus, were unable to provide the required stability to any of the hydrate structures. It was assumed that eventually the $H_2$ molecules would be able to diffuse through the pentagonal or hexagonal faces of the cages and escape out of the hydrate crystal, ultimately leading to the complete dissociation of the hydrate. However, following the initial experimental synthesis of the $H_2$ hydrate,[241,244,245] experimental and computational evidence began to accumulate that under reduced pressure conditions, the $H_2$ content of the hydrate crystal can decrease with time, as a result of $H_2$ migration, however, without the complete breakdown of the hydrate crystal. The research in this direction was initially driven by the important experimental observation of Okuchi et al.[989] The authors used a pulsed-field gradient NMR method (at high $H_2$ pressures), and reported that if the pressure on the

binary THF + $H_2$ hydrate phase is relieved for temperatures 250 K or higher, the $H_2$ guest molecules can diffuse out of the hydrate crystal while the hydrate can still remain stable. On the other hand, upon reversal of the process (i.e., re-pressurisation), $H_2$ can reversibly fill some of the empty S cages of the THF hydrate by diffusing through the cage faces of the intact hydrate crystal. Okuchi et al.[989] reported experiments for $H_2$ diffusivity in hydrates for four different temperatures (250, 255, 260, and 265 K) and $H_2$ pressures in the range 1−20 MPa. The experiments (see Fig. 62) show that the diffusivity
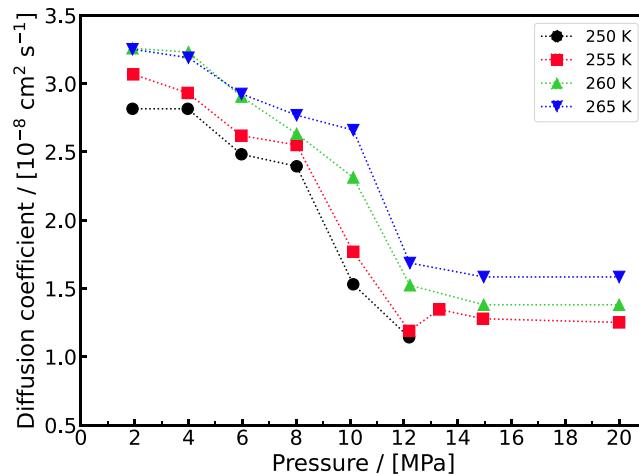


**Figure 62.** Diffusion coefficient of stored hydrogen in the hydrate as a function of pressure for different temperatures. The data are taken from Okuchi et al.[989] The dotted lines are drawn to guide the eye.

decreases as pressure increases. The decrease is attributed to the hypothesis that $H_2$ transport occurs only when there is a vacant guest site in the neighboring cage. Recall that at high pressures the cage occupancies increase (see Section 4.8.5), therefore the number of empty cages is reduced. The authors further suggested that the translation of the $H_2$ through pentagonal $H_2O$ rings between the $5^{12}$ cages is the most likely path for the activation barrier since all $5^{12}6^4$ cages are occupied by THF. Note, however, that the NMR experiments reported by Senadhere and Conradi[990,991] failed to confirm the previous observations of Okuchi et al.[989] for the $H_2$ diffusivity via the S cages.

The high mobility of $H_2$ molecules within the sII S cages has been demonstrated by the inelastic neutron scattering (INS) experiments of the $H_2$ + THF mixed hydrate reported by Choi et al.[992] The authors argued that the $5^{12}$ cages alone, form a network of corner−sharing tetrahedral. The channels connecting the S cages are shown in Fig. 63. It is evident that the neighboring S cages line up in a [101] and symmetrical directions to form linear tunnels via which $H_2$ diffuses, provided unoccupied neighboring cages are present. Information of such diffusion jumps are contained in quasi-elastic neutron scatter (QENS) signals. At low temperatures (i.e., $T <$ 60 K), $H_2$ molecules have not enough energy to overcome the potential barrier between the S cages. However, a sudden signal jump is observed between 60 and 65 K, persistent also at higher temperatures. This is a clear indication for the beginning of $H_2$ diffusion via the [101] direction, where the S cages are aligned (i.e., $H_2$ molecules have gained enough thermal energy to overcome the barrier and cross the pentagonal face connecting the neighboring S cages).
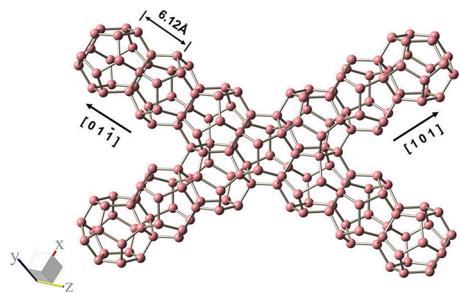
**Figure 63.** Channels formed by $5^{12}$ cages. Each S cage is connected to six other S cages through pentagonal faces.[992] [The figure is reprinted from International Journal of Hydrogen Energy, Vol 35, Yong Nam Choi et al., Dynamics of hydrogen molecules in the channels of binary THF-H$_2$ clathrate hydrate and its physicochemical significance on hydrogen storage, 13068−13072, Copyright (2022), with permission from Elsevier].

In a subsequent experimental study using Raman, Strobel et al.[993] proposed an alternative scheme: Only the $5^{12}6^4$ cages participate in the H$_2$ diffusion via the hexagonal faces. Fig. 64 is
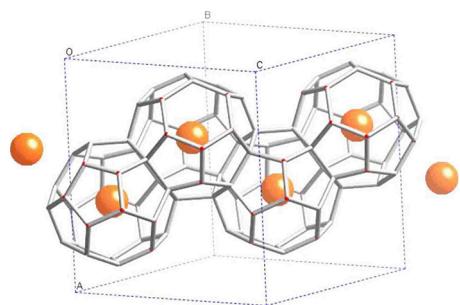


**Figure 64.** Portion of sII unit cell showing hexagonal face-sharing large cavities.[993] [The figure is reprinted from Journal of Chemical Physics, Vol 130, Strobel and Dendy, Raman spectroscopic studies of hydrogen clathrate hydrates, 014506, Copyright (2009), with permission from AIP Publishing].

a schematic of a portion of the sII hydrate unit cell that shows the hexagonal face-sharing L cages. The proposed scheme takes into account the DFT calculations of Alavi et al., which are discussed further, later in this Section (i.e., barriers for H$_2$ diffusion equal to 25−29 kcal/mol and 5−6 kcal/mol for the S and L cages respectively).

Russina et al.[994] performed neutron scattering experiments of mixed H$_2$ + THF. The authors reported significant H$_2$ diffusive mobility in the L cages even at 10−50 K. Contrary, H$_2$ confined in S cages were shown to be trapped at the center of the cages and, thus, were available for long range diffusion, independent of the activation barriers for the inter-cage jumps. Pefoute et al.,[995] based on an INS study, reported that under equilibrium conditions, a single H$_2$ molecule occupying the S cages of the binary THF + H$_2$ sII clathrate hydrate does not diffuse outside of its cage on pico-second time-scales (i.e., an observation opposite to Choi et al.[992]). Conversely, Mulder et al.[965] using neutron diffraction experiments, reported a value of H$_2$ diffusion in the S cages of the binary THF + H$_2$ hydrate equal to " . . .at least $10^{-11}$ cm$^2$/s at 264 K", inferred from the time required to enter and leave hydrate crystallites with size equal to 0.4 $\mu$m.

Parallel to the experimental work in this field, molecular simulation has played a pivotal role. Frankcombe and Kroes,[934]

performed equilibrium MD simulations, and showed that H$_2$ molecules in the L cages can readily diffuse through the hexagonal faces, and ultimately, reach the bulk gas phase in contact with the hydrate structure. Nevertheless, H$_2$ guests in the S cages have high energy barriers to migration, and thus, do not diffuse outside their cages. In a similar MD study, Cao et al.[996] performed MD simulations to study the mixed H$_2$ + THF system. The findings showed that H$_2$ intercage migration from S cages occurs only during double occupancy of the S cages, while no H$_2$ migration occurs during single H$_2$ occupations of the S cages.

Gorman et al.[997] reported MD simulations of the pure H$_2$ and binary THF + H$_2$ sII clathrate hydrates at 50 bar and temperatures up to 250 K. The authors detected diffusion of H$_2$ molecules only when configurations with 2 H$_2$ in the S cages were used. The S cages were observed to temporarily expand through a "breathing motion" (i.e., one of its pentagonal faces opened temporary) as one H$_2$ guest migrated to a neighboring cage. The cage structure remained intact during the migration process. Gorman et al. claimed that this migration exhibits an approximate Arrhenius temperature dependence in the range 200−250 K.

Iwai and Hirata[998] performed MD simulations of THF + H$_2$ clathrates with different H$_2$ occupancies in the S and L cages, at 300 and 310 K, and 10.1 MPa. The simulations revealed migration of H$_2$ molecules between S cages and L cages. However, it should be noted that the observed diffusion between cages may be related to the high temperature at which the simulations were performed, which is likely outside the stability range of the binary hydrate (i.e., possible occurrence of hydrate dissociation). Geng et al.[999] also observed the migration of H$_2$ in the pure H$_2$ and binary THF + H$_2$ hydrates using equilibrium MD simulations. The authors concluded that these migration phenomena lead to the hydrate decomposition process. The MD data also showed that the diffusion of H$_2$ is always larger than that of H$_2$O molecules. Contrary, THF molecules encaged in the $5^{12}6^4$ cavities perform as stabilisers because of the high interaction energy barrier restricting the motion of THF molecules.

Luis et al.[936] investigated the effects of externally−applied static electric fields on the H$_2$ diffusion in sII hydrates. The authors reported that the diffusion of H$_2$ molecules occurs only through the L cages, while the H$_2$ molecules diffuse, with a slight preference, in the same direction of the applied electric field.

Hasegawa et al.[1000] performed equilibrium MD simulations of sII mixed H$_2$ + SF$_6$ hydrates, and reported that the diffusion of H$_2$ molecules between L cages was found to occur more frequently. However, the presence of SF$_6$ molecules in the L cages was proved to inhibit H$_2$ diffusion. Therefore, the authors recommended that an optimal number of L cages should be occupied by SF$_6$ molecules as a means to increase the H$_2$ storage capacity of the mixed hydrate. Furthermore, Hasegawa et al. reported that a partial breaking of the hydrate structure was required to make room for the H$_2$ to diffuse through the open pentagonal ring in the case that a H$_2$ molecule diffused to/from an S cage. By contrast, no cage distortion was observed in H$_2$ diffusion via a hexagonal ring from an L cage. Hasegawa et al.[1000] also performed MD simulations of sII mixed H$_2$ + tert−butylamine hydrate, where the tert−butylamine molecules occupied the L cages. The authors reported that more H$_2$ molecules diffused into the hydrate as a result of a less stable, and partially distorted,

hydrate structure, which created enough space for $H_2$ molecules to move between adjacent cages.

Zhang et al.[594] studied the growth of mixed $H_2$ + $CH_4$ hydrate with MD simulations, and observed that $H_2$ can hop between the $5^{12}6^4$ cages through the six-membered rings connecting the cages without any distortion of the cages, even for cases that the L cages are occupied by $CH_4$. The observation of the simultaneous presence of two different guests (i.e., $H_2$ and $CH_4$) within the same L cage is of utmost importance since it can have a significant effect on the storage capacity of the hydrate. The possibility of the simultaneous occupancy of the L cages by two different guests was originally reported by Papadimitriou et al.[1001,1002] for the case of the mixed sII He + THF, based on observations from GCMC simulations. Subsequently,[1003] reported similar observations, based on experiments using *in situ* Raman spectroscopy for the mixed sII $H_2$ + Ar hydrates. Waage et al.[1004] performed MC simulations, which showed that $H_2$ molecules are capable of coexisting, even in S cages, with any of the other molecules (i.e., $CH_4$, $CO_2$, $N_2$) examined in their study.

In a similar context, Harada et al.[1005] reported MD simulations for the case of $H_2$ hydrate with crystal structure $C_1$, namely ice II filled with $H_2$ molecules. The authors observed fast diffusion of the $H_2$ molecules in the $C_1$ crystal. The $H_2$ molecules were observed to migrate (via a highly anisotropic in space diffusion process) only inside the tube−like voids of the $C_1$ hydrate. Harada et al. also pointed out the importance of the existence of defects or vacancies in the tube−like voids for $H_2$ diffusion to occur. In the absence of vacancies no diffusion was observed. In a related study, Arman and Nugroho[1006] reported MD simulations for the case of $H_2$ hydrate with structure $C_2$, namely ice $I_c$ filled with $H_2$ molecules. Additional MD simulations of anomalous $H_2$ diffusion in various ices have been performed by Smirnov and Stegailov.[1007]

Except from classical MD, other atomistic-scale simulations have been conducted to study the diffusion of $H_2$ in hydrate systems including, but not limited to the following: Alavi and Ripmeester[1008] performed DFT calculations at the B3LYP and MP2 levels of theory to compute the energy required for the $H_2$ molecules to migrate through a hexagonal face of the L-type cage or a pentagonal face of the S-type cage, considering both parallel and perpendicular configurations of the $H_2$ molecules with respect to the examined face. They reported energy barriers to diffusion equal to 5−6 kcal/mol and 25−29 kcal/mol for the L and S cages, respectively.

The calculation of the free−energy barrier for $H_2$ diffusion between cages has been been achieved using methods such as PIMD[1009] and ab initio simulations. Typical examples can be found in the works of Trinh et al.,[182] Cendagorta et al.,[366] and Burnham et al.[1010−1012] These alternative approaches are especially important at low temperatures, where $H_2$ molecules are affected by quantum effects.

The molecular simulations by Trinh et al.[182] demonstrated the importance of cage flexibility and cage occupancy on the diffusion of $H_2$ between cages. Furthermore, they showed that the multiple occupancy of cages helps reduce the free energy barrier for $H_2$ hopping between cages. Cendagorta et al.[366] used the Ring Polymer Molecular Dynamics (RPMD) rate theory. This work was motivated by the fact that the energy barrier to hopping is significant compared to the thermal energy. Therefore, $H_2$ diffusion is a rare event process, and thus, amenable to computation using rate theory. The PIMD

simulations by Burnham and English[1010] for the case of $H_2$ diffusion between two L hydrate cages at 200 K also yielded the quantum free−energy barrier higher than the classical one, by about 2 kJ/mol.

Waage et al.[1004] performed MC simulations to calculate the free energy barriers associated with $CH_4$, $CO_2$, $N_2$, and $H_2$ hopping through rings of water between the cages of the sI hydrate structure. The authors considered intact cages, as well as cages with $H_2$ vacancies. $H_2$ was shown to be capable of diffusing out from both the S or L cages.

Ghaani et al.[942] used non-equilibrium MD simulations to examine $H_2$ diffusion during release/uptake from/into propane planar clathrate surfaces in the temperature range 180−273 K. The simulations revealed that $H_2$ molecules exhibited higher movement during release studies (with hydrate being in contact with a vacuum) when compared with the uptake studies (with gas $H_2$ molecules located on top of the hydrate structure).

English and Burnham[1013] considered classical MD and PIMD simulation to study the intra-cage behavior of $H_2$ and $D_2$ molecules in doubly occupied L cages of sII hydrates at 100 K. Krishnan et al.[1014] examined transient, non-equilibrium inter-cage hopping, and presented a diffusional activation energy for the four nominal L cage occupancies (1 up to 4) using leakage−rate fits. Markov-chain models were utilized to study the inter-cage hopping of $H_2$ and $D_2$, and expressed at different temperatures and large-cage occupancies. Furthermore, the authors computed the free energy of guest "binding" in the L and S cages for all of the occupancies. Krishnan et al.[1015] conducted micro-second-long, non-equilibrium MD simulations, in the temperature range 140−180 K, to elucidate mechanistic effects of electric−field on guest diffusivity control in hydrates. It was found that a judicious selection of the electromagnetic fields (i.e., in the microwave frequency range), could act towards the dramatic enhancement of the $H_2$ release rate, without any breakup of the hydrate lattice itself. This is an important aspect for the kinetic control of large-scale $H_2$ storage systems. Krishnan et al.[1016] reported MD calculations exploring both $H_2$ and $D_2$ hydrates for cage occupancies and their self-diffusivity via inter−cage hopping. The authors studied these hopping phenomena as a function of temperature using a Markov chain model.

## 4.9. Interfacial Tensions of Aqueous Hydrogen Systems

Computing and analyzing the interfacial tension (IFT) between $H_2$ and brine systems is crucial for the effective and safe implementation of UHS in geological formations, such as saline aquifers. IFT directly influences the capillary forces at the interface between $H_2$ and reservoir fluids, governing $H_2$ migration, trapping efficiency, and retention capacity within subsurface reservoirs. Accurate knowledge of IFT allows precise prediction and optimization of storage capacities and operational efficiencies, ensuring efficient $H_2$ injection and withdrawal. IFT values, in addition, depend on thermodynamic and chemical conditions, including temperature, pressure, salinity, ionic composition, and the presence of cushion gases like $CO_2$ and $CH_4$, making its study essential for realistic reservoir modeling and design of storage strategies. Accurate IFT data support safety and risk mitigation by evaluating the sealing capability of caprocks, critical for preventing $H_2$ leakage. Given the challenges associated with experimental IFT measurements under reservoir conditions, MD simulations offer valuable atomic-level insights and extensive predictive

ability. Furthermore, understanding IFT helps optimize cushion gas composition and injection strategies, enhancing overall storage performance. The interplay between IFT and rock wettability significantly impacts capillary pressures, determining $H_2$ stability and displacement behavior in porous formations. Therefore, a comprehensive examination of IFT is fundamental to ensuring secure, efficient and large-scale storage $H_2$ in geological reservoirs. For a thorough introduction on the role of molecular simulation for designing and optimizing UHS the reader is referred to Section 2.3.4. Details on the computation of IFT via MD are provided in Section 3.2.16. A review of relevant studies is provided below.

van Rooijen et al.[630] computed IFTs of $H_2$ gas in contact with aqueous NaCl solutions, self-diffusivities and solubilities of $H_2$ in aqueous NaCl solutions using MD simulations at conditions relevant to UHS and $H_2O$ electrolysis. The IFTs were computed for temperatures of 298 to 523 K, pressures of 1 to 600 bar, and molalities of 0 to 6 mol NaCl/kg $H_2O$ using the TIP4P/2005 water model, Madrid-2019 force field for NaCl, and Vrabec force field for $H_2$ (for details on these force fields see Section 3.1). The results showed that IFTs do not exhibit significant pressure dependence, increase linearly with salt molality (by ca. 1.44 mN/m per mol NaCl/kg $H_2O$), and decrease non-linearly with temperature. This behavior is explained by the fact that IFT is related to the density difference between the two phases, with the low density of $H_2$ relative to water resulting in minimal pressure effects, while the increased density of saline water and the arrangement of ions at the interface (with anions being depleted from the bulk phase and cations being absorbed into it) strengthen the $H_2$ bond network of $H_2O$, leading to increased IFT. Temperature has the strongest influence on the IFT, causing a non-linear decrease due to its effect on the density difference between $H_2$ and aqueous solutions. The computed IFTs were compared with available experimental data from Hosseini et al.,[1017] showing excellent agreement with average deviations lower than 6.4% across the range of conditions studied. The authors proposed an engineering equation for IFT as a function of temperature and molality: $\gamma = c_1 + c_2 m + c_3 T^{c_4}$, valid for temperatures of $[298, 523]$ K, pressures of $[1, 600]$ bar, and molalities of $[0, 6]$ mol NaCl/kg $H_2O$. The IFT data generated in this work is particularly valuable because experimental measurements for the $H_2/H_2O/NaCl$ system are scarce, especially at high pressures and temperatures, which are highly relevant to $H_2$ technologies.

Omrani et al.[1018] investigated the IFT, density, and molecular distribution properties of the $H_2 -$ brine systems with various salts including $Na^+$, $K^+$, $Ca^{2+}$, and $Mg^{2+}$, under reservoir conditions. IFT was computed as a function of pressure (1−30 MPa), temperature (298−373 K), and salt molality/composition (up to 5.02 mol/kg for NaCl and up to 1.91 mol/kg for other salts). The results show that IFT decreases with increasing temperature, slightly decreases with increasing pressure, and increases with higher salinity, with values ranging roughly from 55.85 to 77.54 mN/m, depending on the conditions. Physically, these trends are explained by the interfacial molecular structure where higher temperature broadens the interfacial width and enhances $H_2 - H_2O$ mixing, reducing IFT, while increased salinity enriches $H_2$ accumulation at the interface, thinning the interface and increasing IFT. Temperature is identified as the strongest factor influencing IFT, followed by salinity, with pressure having a comparatively minor effect. The MD simulation

results for IFT showed excellent agreement with available experimental data, with deviations less than 3% when using the combined Marx force field for $H_2$, TIP4P/2005 model for $H_2O$, and Smith-Dang parameters for $Na^+$ and $Cl^-$. A general correlation for IFT as a function of reduced temperature, density difference between $H_2$ and brine phases, and NaCl mole fraction was developed using genetic programming, achieving high accuracy with $R^2 = 0.9783$ and absolute average relative deviation below 1%. The effect of cation type was also shown to be significant, with $CaCl_2$ yielding the highest IFT values and $K^+$ the lowest at comparable concentrations, attributed to differences in ion hydration enthalpy and interfacial distribution.

Xie et al.[1019] focused on accurately predicting the IFT of $H_2$ + $CO_2$ gas mixtures in contact with $H_2O$ and brines containing $Na^+$ and $Cl^-$ ions over a wide range of temperatures, pressures, gas compositions, and salinities. Molecular interactions were analyzed to elucidate the underlying mechanisms affecting IFT, while and ML approach was used to develop a general predictive equation. The parameters used to compute IFT included temperatures from 298 to 373 K, pressures in the range of 50 to 400 bar, gas compositions expressed as $H_2$ mole fraction, and brine salinities up to 3.15 mol/kg. The IFT was shown to decrease with increasing pressure and $CO_2$ content, while increasing salinity raised the IFT, with values ranging approximately between 20 and 60 mN/m depending on conditions. These trends arise from the interplay between molecular mobility of gas and water molecules (entropy) and intermolecular interactions primarily between gas molecules and water/brine ions (enthalpy). The higher pressure enhances gas solubility in the aqueous phase, which reduces the IFT, whereas the presence of salt ions ($Na^+$ and $Cl^-$) increases electrostatic and van der Waals interactions at the interface, thereby strengthening intermolecular forces and increasing IFT. Among the factors studied, pressure and gas composition exhibit the strongest influence on IFT behavior under the chosen conditions (relevant to UHS), with temperature showing a less dominant but still significant effect. MD simulations of IFT were validated against extensive experimental data, showing good agreement with average relative errors around 4.4%. A ML-based polynomial equation was developed to predict IFT as a function of temperature, pressure, $H_2$ mole fraction, and salinity, achieving high accuracy with $R^2 = 0.972$ on testing data. This equation outperforms previous empirical models, especially for ternary ($H_2$ + $CO_2$)-water/brine systems, and is suitable for reservoir simulation applications.

Yang et al.[602] computed IFT, contact angles, adhesion tension, density distributions, and relative adsorption in multiphase systems of $H_2$ + $H_2O$ with silica or kerogen under various conditions. IFTs, computed via MD simulations (INTERFACE force field for $H_2$ and TIP4P/2005 for $H_2O$) and density gradient theory (with PC-SAFT EoS), range from approximately 25 to 72 mN/m as functions of pressure (1 to 160 MPa) and temperature (298 to 523 K). A general outcome, IFT was shown to decrease with increasing pressure and temperature, but above about 448 K and 60 MPa, IFT increased with pressure due to an inversion of $H_2$ relative adsorption: at low $T$ and $P$, adsorption is positive (enrichment at the interface), decreases past a pressure threshold, and becomes negative at high $T$ (depletion at the interface). Temperature most strongly influences IFT by altering molecular distributions and thermal fluctuations. The INTER-

FACE + TIP4P/2005 combination of force fields accurately reproduces the surface tension of water, and matches experimental IFTs within 1.7 - 7.4 mN/m, while density gradient theory with PC–SAFT reproduces the same trends seen in both simulations and experiments. The authors note that the value of IFT in $H_2+H_2O$ is close to the surface tensions of pure water, and higher than in $CO_2+H_2O$, $CH_4+H_2O$, or $N_2+H_2O$ computed in other studies not reviewed here.

Doan et al.[1020] studied IFT and adsorption in water–$H_2$, $CH_4$, and $CO_2$ mixtures. IFT was computed at 1 to 70 MPa and at 300 and 323 K for pure water and binary gas mixtures. IFT was generally shown to decrease with pressure and temperature; for instance, $\gamma(CO_2 - H_2O)$ value fell from ca. 62 to ca. 34 mN/m, $\gamma(CH_4 - H_2O)$ from ca. 64 to ca. 53 mN/m, while $\gamma(H_2 - H_2O)$ remained equal to 62-63 mN/m, showing greater temperature sensitivity. Thus, $H_2$ yielded the highest IFT and $CO_2$ the lowest. This decrease was attributed to enhanced gas adsorption at the water interface, especially stronger $CO_2$ - water interactions compared to $CH_4$ or $H_2$, though detailed molecular mechanisms remain unexplored. The authors reported that pressure dominates IFT behavior, decreasing sharply up to 50 MPa and plateauing above, while temperature has a lesser effect, becoming negligible at high pressure. The computed IFTs agree well with experiments for $CO_2$-$H_2O$ and $CH_4$-$H_2O$, though underestimating low-pressure values by up to 10%, and underestimating $H_2$-$H_2O$ by 10 to 14%, likely due to the choice of force fields, inaccurate mixing rules for the intermolecular interactions, or system-size limitations. MD simulations show $H_2$ in ternary $H_2$ - $CH_4$ - $H_2O$ mixtures increases IFT relative to $CH_4$ - $H_2O$ and $CO_2$ - $CH_4$ - $H_2O$, owing to weaker $H_2$ intermolecular forces and lower interfacial adsorption.

Doan et al.[1021] computed IFT and flow properties of water–$H_2$ mixtures with cushion gases $CO_2$, $N_2$, and $CH_4$ under geological storage conditions. IFT was computed as a function of pressure [1, 70] MPa, temperature [300, 343] K, and cushion-gas mole fractions [10 to 90]%. For $H_2/CO_2/H_2O$, $H_2/N_2/H_2O$, and $H_2/CH_4/H_2O$ systems, IFT decreased from ca. 64 mN/m at low pressure to ca. 42 mN/m at 70 MPa at higher pressures and temperatures. Higher $H_2$ content raised IFT: $N_2$-containing mixtures yield the highest IFT, while $CO_2$-containing mixtures yield the lowest IFT at fixed conditions. These trends arise from gas adsorption at the $H_2O$ interface i.e., heavier $CO_2$ reduces IFT due to stronger inter-molecular interactions and higher adsorption, $CH_4$ moderately lowers IFT, and the light, inert $N_2$, yields higher IFT. Pressure was shown to most strongly affect IFT, which dropped sharply up to ca. 30 MPa, and then reached a plateau for all $CO_2$, $N_2$, and $CH_4$ mixtures across the 300 - 343 K temperature range. Temperature caused a gradual decrease in IFT (at fixed pressure), but had a weaker effect. The computed IFTs for $H_2/CO_2/H_2O$ agree with experiments within 12% at low pressures. For $H_2/N_2/H_2O$ and $H_2/CH_4/H_2O$ systems, the available experimental data are limited, making the molecular simulation predictions valuable.

Chen et al.[604] performed molecular simulations to study the IFT, surface excess, bubble evolution, and contact angle of $CO_2$, $H_2$, and their mixtures with $H_2O$ or brine ($Na^+$, $Cl^-$) at 10 MPa and temperatures ranging form 300 to 400 K. $CO_2/H_2$ mixtures included $H_2/CO_2$ ratios of 1:10, 2:10, 3:10 ($CO_2 - $ rich) and their inverses ($H_2 - $ rich). IFT was computed isobarically (10 MPa) over 300 to 400 K with 4% NaCl brine.

In $H_2 - $ rich mixtures, IFT decreased roughly linearly from ca. 65 mN/m at 300 K to ca. 50 mN/m at 400 K in both pure $H_2O$ and brines. $CO_2 - $ rich systems showed non-monotonic temperature dependence: IFT rose to ca. 20 mN/m at the range 320 - 360 K, and at higher temperatures decreased. The authors qualitatively attributed this peak to phase transitions and temperature-dependent surface adsorption, without though providing a detailed mechanistic explanation. Brine was shown to increase IFT by a few mN/m relative to pure $H_2O$. $CO_2$ significantly reduced IFT compared to $H_2$, which has minimal impact. This is due to the stronger electrostatic and quadrupolar interactions of $CO_2$ with $H_2O$, influencing the anisotropy of the tensor of the virial pressure, a concept noted but not elaborated further by Chen et al.[604] The weak van der Waals interactions of $H_2$ cause smaller IFT changes. The temperature change from 300 to 400 K, yielded a 10 mN/m IFT decrease in $H_2$-rich systems and non-monotonic variation of 5 mN / m in $CO_2 - $ rich systems, signifying temperature as the prime IFT variable. MD results agreed with experimental $CO_2 - H_2O$ and $H_2 - H_2O$ data (298 - 448 K, $\leq$ 45 MPa). The experimental data cover pure gas-water, but the trends of the mixture were shown to be consistent with the behavior of the extrapolated pure components. The simulations indicated linear temperature dependence in systems rich in $H_2$, and non-monotonic in systems rich in $CO_2$, with a consistently increasing IFT of brine.

Chen and Xia[605] computed transport properties, wettability, IFT, and surface adsorption of $H_2$, $CO_2$, and $CH_4$ interacting with $H_2O$ and silica under reservoir conditions. The IFT calculations were carried out at a fixed temperature of 320 K and pressures up to 60 MPa, considering pure water and silica substrates. Across all conditions, the IFT follows the order $\gamma_{CO_2-H_2O} < \gamma_{CH_4-H_2O} < \gamma_{H_2-H_2O}$. In particular, the $CO_2$-water IFT dramatically decreased by ca. 42% at 10 MPa before plateauing, the $CH_4 - $ water IFT decreased more gradually with pressure, and the $H_2 - $ water IFT remained nearly constant. These trends arise from differences in density and molecular interactions i.e., the higher density and quadrupole moment of $CO_2$ enhance its surface activity, while the low density of $H_2$ and weaker van der Waals forces lead to minimal variation in IFT. The primary factor influencing IFT is the density difference between the gas and water phases, which governs interfacial molecular interactions. MD-computed IFTs agree well with experimental data for $CO_2$ and $CH_4$ systems. For $H_2$, the simulations were shown to slightly underestimate the experimentally measured IFTs, but correctly capture the qualitative behavior. No significant pressure dependence of IFT for $H_2$ is observed in simulations, consistent with experimental observations of only slight decreases.

The study by Adam et al.[1022] reported data on IFT, structure, and solubility for UHS-relevant brine (NaCl) and gas mixtures of $H_2$, $CO_2$, and $CH_4$. IFTs were computed for pressures of 10−60 MPa, temperatures from 323.15 to 388.15 K, and salt concentrations 10-25 wt%, covering both pure gas-brine and mixed gas-brine systems. Pure gases included brine/$H_2$, brine/$CO_2$, and brine/$CH_4$, while mixtures considered were ternary brine/$H_2$/$CO_2$ and quaternary brine/40% mol $H_2$/60% mol cushion gases ($CO_2$ or $CH_4$). Pure brine/$H_2$ IFT remained nearly constant (around 59 mN/m) across pressures, whereas brine/$CO_2$ IFT decreased markedly from 44.4 to 30.6 mN/m, and brine/$CH_4$ showed a minor drop (53.6 to 51.8 mN/m). Mixed gas systems with $CO_2$ exhibited stronger

pressure dependence; brine/40% mol $H_2$/60% mol $CO_2$ IFT decreased about 14.6%, compared to a smaller 7.4% decrease with $CH_4$. Temperature significantly reduced IFT across all systems: brine/$H_2$ decreased roughly 20% (67.4 to 54.3 mN/m), brine/$CO_2$ from 37.1 to 31.6 mN/m, and brine/$CH_4$ from 57.5 to 50.2 mN/m. Similar trends occurred in mixed systems; brine/40% mol $H_2$/60% mol $CO_2$ IFT dropped by 8 mN/m, and brine/40% mol $H_2$/60% mol $CH_4$ by 12 mN/m. Higher $CO_2$ content lowered temperature sensitivity due to stronger molecular interactions requiring higher thermal energy to disrupt these intermolecular bonds. Radial distribution function analysis revealed weak hydrogen-bonding between $CO_2$ oxygen and $H_2O$ hydrogen atoms at the interface, leading to $CO_2$ clustering and reduced IFT as its mole fraction increased. Increasing salt concentration raised IFT in all systems via the salting-out effect, as ions attracted water molecules, reducing water-gas interactions. For example, increasing NaCl from 10 to 25 wt% raised IFT by approximately 3 mN/m for brine/$H_2$, 4 mN/m for brine/$CO_2$, and 7 mN/m for brine/$CH_4$. Pressure had a moderate impact on IFT, notably in systems with higher $CO_2$, whereas temperature and salinity exerted stronger effects. The computed IFT values closely agree with experimental data, validating the methodology and force fields used by Adam et al.[1022]. Engineering correlations using polynomial functions were developed to predict IFT based on pressure, temperature, $CO_2$ concentration, and salinity. It is important to note that the functional form (i.e., actual cubic polynomial) of the devised equations and the coefficients were not provided by the authors, hindering the wide, practical use of the presented model.

### 4.9.1. Handling Long-Range Dispersion Interactions.
Transitioning now from the specific findings presented by the studies reviewed earlier, we collectively address the approaches followed for calculating IFTs. A primary challenge associated with the slab method of determining IFTs in MD simulations is accurately handling long-range dispersion (LJ) interactions. Two principal strategies commonly applied are semi-analytic tail corrections and explicit mesh-based methods. Tail corrections adjust IFT values post-simulation, following the approach developed by Blokhuis et al.[1023] and elaborated by Allen and Tildesley,[52] and can significantly impact computed IFT values, sometimes by up to ca. 35% for LJ fluids. Alternatively, explicit mesh-based methods, such as smooth Particle Mesh Ewald (sPME)[1024] and Particle-Particle Particle-Mesh (PPPM),[1025,1026] directly compute long-range dispersion analogously to electrostatic Ewald summation, as comprehensively reviewed by Goujon et al.[1027] Sega and Dellago[1028] compared these approaches across seven water models, demonstrating that explicit mesh-based methods yield more accurate IFT predictions and correctly reproduce liquid and vapor densities. Furthermore, including the full dispersion interactions explicitly shifted the critical temperature of water upwards, a crucial thermodynamic effect not captured by semi-analytic tail corrections, highlighting the importance of explicitly incorporating long-range dispersion interactions.

Several studies have applied these methodologies specifically to $H_2$-water and $H_2$-brine systems, adopting various approaches to computing the long-range dispersion. For instance, van Rooijen et al.[630], Xie et al.,[1019] and Yang et al.[602] used explicit mesh-based methods (PPPM[1025] or PME[1029]), with Yang et al.[602] also validating the improved accuracy against NIST data when using PPPM. Omrani et

al.[1018] truncated dispersion interactions without applying tail corrections but mitigated potential underestimations in IFT by using an unusually large LJ cutoff (2.9 nm), requiring larger simulation cells and greater computational effort. Adam et al.[1022] also truncated dispersion interactions at 1.28 nm without long-range dispersion interactions. Doan et al.[1020,1021] used semi-analytic tail corrections proposed by Blokhuis et al.,[1023] Chen et al.[604] and Chen and Xia[605] use truncated LJ interactions without explicit tail corrections, potentially underestimating IFT values due to the omission of long-range dispersion effects. Consequently, differences in IFT predictions among these studies can often be attributed to varying treatments of long-range dispersion interactions. Although semi-analytic tail corrections provide computational efficiency, they may overlook important thermodynamic effects, whereas explicit mesh-based methods ensure higher accuracy at the expense of greater computational resources. Thus, consistently addressing long-range dispersion interactions is vital for obtaining reliable IFT predictions in $H_2$-water and $H_2$-brine systems.

Although here we focus on long-range dispersion in simulations of interfacial tension for $H_2$-water, the same considerations arise in nanoporous frameworks (e.g., MOFs, zeolites, COFs). Whether to apply homogeneous long–range (tail) corrections in crystalline hosts remains debated in the literature. One view argues against the use of these corrections because the standard assumption that the radial distribution function approaches unity beyond the interaction cutoff radius often fails in ordered solids (the radial distribution function can remain oscillatory and even peak near the cutoff). Thus, applying a homogeneous correction may introduce spurious energetic contributions.[1030] Moreover, in crystalline materials, the radial distribution function is inherently direction dependent. The opposing view recommends applying tail corrections to solid–fluid and fluid–fluid terms to reduce sensitivity to truncation, and to enable more consistent cross–study comparisons; substantial effects on Henry coefficients and loadings have been reported by Siperstein et al.[1031] and Jablonka et al.[1032]

Tail corrections are, ultimately, a modeling choice. In practice, we suggest: (i) following the force field as originally parametrized (its interaction cutoff radius and any prescribed tail correction), (ii) reporting these choices explicitly in the methodology section of the study, and (iii) where feasible, demonstrating robustness with brief sensitivity tests (for example, one can vary the interaction cutoff radius and toggle the correction on or off). As a way to sidestep the truncation/tail-correction decision entirely, one can use smooth finite–range pair potentials that vanish continuously, for example, the Wang-Ramírez-Dobnikar-Frenkel ("WF") LJ-like potential[1033] keeping in mind that using such potentials generally requires re–fitting parameters to reproduce the target adsorbate-framework interactions.

### 4.9.2. Importance of Force Field Selection on Interfacial Tension Computations.
As extensively discussed thusfar in this review, in MD simulations aimed at accurate predictions, selecting appropriate force fields to describe molecular interactions is essential. Omrani et al.[1018] extensively explored various force fields for $H_2$ including Vrabec,[48] Hirschfelder,[321] modified Silvera-Goldman,[335] 3-site Alavi,[336] Cracknell,[311] and Marx,[310] and for water TIP4P/2005,[305] TIP4P-$\mu$,[47] TIP4P OPLS/AA,[360] SPC/E,[346] TIP3P,[300] and TIP5P[359] (see Sections 3.1.1 and 3.1.2).

Omrani et al.[1018] computed IFTs under pressures of 5 and 20 MPa and temperatures of 323 and 373 K, alongside multiple NaCl models including the ones by Smith and Dang,[374] Joung and Cheatham,[371] the Madrid-2019,[1034] and from Loche et al.[1035] The combination of Marx[310] with TIP4P/2005[305] and Smith and Dang[374] provided the best agreement with the experimental IFT data of Hosseini et al.,[1017] with deviations being consistently lower than 5%. Notably, Omrani et al.[1018] did not include the widely-used IFF[313] force field for $H_2$, yet emphasized the superior performance of TIP4P/2005, aligning with earlier conclusions by Vega and Miguel.[1036]

Subsequent work by Yang et al.[602] evaluated the performance of the Hirschfelder,[321] IFF,[313] and Alavi[336] $H_2$ models combined with the TIP4P/2005[305] water model, showing that the IFF model is the most precise in reproducing experimental IFT values. Meanwhile, Xie et al.[1019] tested various force field combinations, observing a consistent underestimation (18%) of IFT when using the SPC/E water model. Adam et al.[1022] also indicated that SPC/E significantly deviated from experimental IFT data when compared to TIP4P/2005. For example, in the $H_2O/H_2$ system at 323 K and 5-20 MPa, SPC/E showed discrepancies of up to 15 mN/m, whereas TIP4P/2005 remained within ±0.15 mN/m. Similar trends were observed across brine/$CO_2$, brine/$CH_4$, and ternary brine/$H_2$/$CO_2$ systems, where TIP4P/2005 consistently reproduced experimental IFT values and pressure trends, while SPC/E underestimated IFT and failed to capture its pressure dependence. The results of Xie et al.[1019] and Adam et al.[1022] further highlight the critical role of the water force field, noting that variations between the IFF[313] and Alavi[336] $H_2$ force fields were less significant compared to those arising from the choice of the water model. Although Yang et al.[602] concluded that the Alavi force field failed to capture the pressure-dependent IFT trend, their conclusion was based on limited data, raising caution. In contrast, the more comprehensive study by Xie et al.[1019] demonstrated that while the 3-site Alavi model slightly underestimates absolute IFT values at 323 K, it does correctly reflect the pressure dependence. Collectively, these studies emphasize that selecting an accurate water force field has a greater impact on IFT predictions than the specific choice of the $H_2$ force field.

Another important detail to consider when performing MD simulations of non-homogeneous systems (e.g., gas/liquid systems used for the computation of the interfacial tension of $H_2$/water) is the use (or not) of analytic tail corrections.[51,52] Such corrections are only valid for systems that the radial distribution function converges to 1 at long distances (homogeneous gas and liquid phases).[51,52] Therefore, tail corrections are usually not used in systems containing interfaces, since this choice will produce simulation artifacts.[1037,1038] To minimize the error introduced from not considering the long-tail of the interactions potentials, cutoff radii larger than what the chosen force fields dictate can be used. However, such a choice will increase the computational requirements (since more interaction pairs will be considered in each timestep of the simulation), while it should be explicitly mentioned in the methodology section of the study to enable the reproducibility of the results. MD simulation software packages, such as LAMMPS[762] and GROMACS,[476,477] allow for the computation of the long-range LJ and electrostatic interactions with the PPPM[51] method. For more details on this approach, the reader is referred to the studies by Isele-Holder and co-workers.[1039,1040]

## 4.9.3. Comparison between Molecular Simulations and Experiments of Hydrogen−Water Interfacial Tensions. Fig. 65(a) shows a comparison between exper-
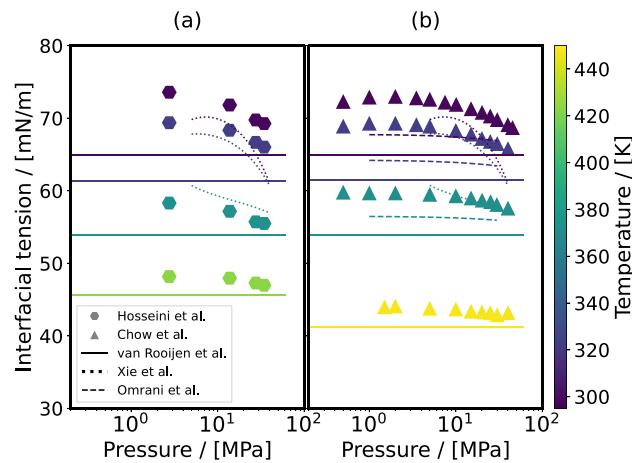


**Figure 65.** Interfacial tension of $H_2$-$H_2O$ as a function of pressure. Comparison between experiments (from: (a) Hosseini et al.[1017] and (b) Chow et al.[1041] shown as markers) and engineering equations fitted with data from three different MD simulations(from van Rooijen et al.[630]: solid line, Omrani et al.[1018]: dashed line, and Xie et al.[1019]: dashed dotted line). The colors of the markers represent the temperature at which the interfacial tension is reported. The MD simulation predictions are plotted within the range where the equation remains valid.

imental $H_2 − H_2O$ IFT data from Hosseini et al.[1017] with fitted MD data using the engineering correlations proposed by van Rooijen et al.,[630] Omrani et al.,[1018] and Xie et al.[1019] Notable deviations occur primarily below 325 K. Specifically, Xie et al.[1019] calibrated their model over a temperature range of 298−373 K and pressures of 5−40 MPa, whereas van Rooijen et al.[630] used a broader range of 298−523 K and 0.1−60 MPa. The weak pressure dependence of IFT observed experimentally by Hosseini et al.[1017] is qualitatively captured by Xie et al.,[1019] although their model exhibits roughly a 5% deviation and an overestimation of the pressure sensitivity, evidenced by a steeper slope. Conversely, the model by van Rooijen et al.,[630] assuming pressure independence, exhibits a deviation of ca. 10% from experimental data below 325 K, but aligns well (within 5%) at higher temperatures. Omrani et al.[1018] could not be directly compared due to their fit requiring gas-liquid density differences that were not provided. Fig. 65(b) shows a comparison of the experimental IFTs reported by Chow et al.[1041] with predictions from van Rooijen et al.[630] and Hosseini et al.,[1017] both achieving better than 5% agreement at temperatures above 370 K. Since Chow et al.[1041] also provided gas and liquid densities, Omrani et al.[1018] could be evaluated, revealing the near pressure independence of IFT, consistently with experiments, except for pressures above about 40 MPa, for which a notable decrease is observed. Overall, within their respective calibration ranges, the fit functions from Omrani et al.[1018] and Xie et al.[1019] achieve agreement within 1−10% of experimental values, while van Rooijen et al.[630] cover a broader range but remain within roughly 15%. Despite variability among MD-based predictions, the computed IFT values for $H_2 − H_2O$ systems consistently fall within approximately 10−15% of experimental measurements from Hosseini et al.[1017] and Chow et al.[1041]

**4.9.4. Interfacial Tensions of Hydrogen−Brine Systems.** Fig. 66 illustrates the IFTs of $H_2$ − NaCl brine systems
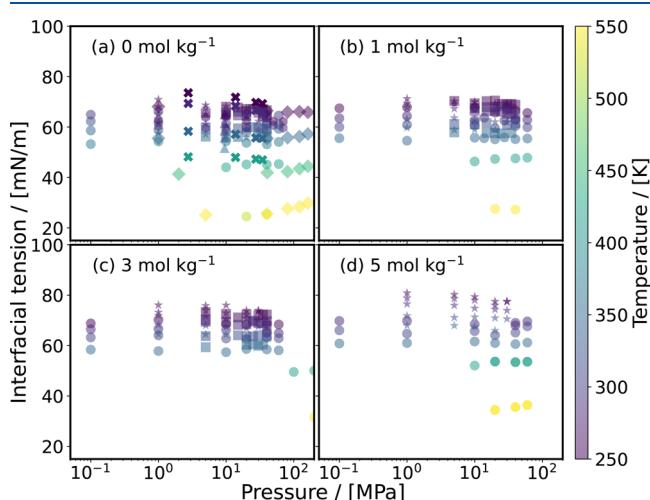


**Figure 66.** Interfacial tension of aqueous $H_2$-NaCl mixtures as a function of pressure computed from MD simulations for salt concentrations of (a) 0 mol of NaCl/kg of $H_2O$, (b) 1 mol of NaCl/kg of $H_2O$, (c) 3 mol of NaCl/kg of $H_2O$, and (d) 5 mol of NaCl/kg of $H_2O$. The colors of the markers represent the temperature at which the interfacial tension is reported. The data are taken from van Rooijen et al.[630] (circle), Omrani et al.[1018] (star), Xie et al.[1019] (square), Yang et al.[602] (diamond), Doan et al.[1021] (hexagon), and Chen et al.[604] (triangle). To facilitate comparison between simulations and experiments for pure water-$H_2$ system, the experimental data of Hosseini et al.[1017] (shown with marker x) is added in subfigure (a).

compiled from various studies (summarized in Table 19), collectively capturing key experimental observations such as the minimal sensitivity of IFT to pressure, the decreasing IFT with rising temperature, and increasing IFT with salt concentration. Fig. 66(a)-(d) predominantly show data points within pressure ranges of 1−50 MPa and temperatures of 300−400 K, relevant to UHS. For aqueous $H_2$ − systems, there is notable consistency across multiple studies, largely attributable to the widespread adoption of the TIP4P/2005 water model. Although various $H_2$ force fields (single-site versus multi-site) were used, the resulting discrepancies among the different studies[602,630,1018,1019] remain modest. However, the presence of salt significantly increases variability among predictions. Notably, at 298 K and 10 MPa, reported IFT values for aqueous $H_2$ systems without salt range from 64.9 to 68.2 mN/m across studies, whereas at a salt concentration of 3 mol NaCl/kg water yields IFTs in the range of 68.6 and 76.1 mN/m. While Omrani et al.[1018] and Xie et al.[1019] remain closely aligned, van Rooijen et al.[630] deviate by ca. 5%, potentially due to their use of a single-site $H_2$ model. Additionally, even studies using identical force fields for NaCl differ by around 5%, a discrepancy possibly intensified by the different choices for modeling long-range dispersion interactions relevant for correcting the IFTs (e.g., omitted in ref 1018). Overall, while TIP4P/2005[305] seems to ensure consistent and reliable IFT predictions for aqueous $H_2$, discrepancies emerge in $H_2$ − NaCl brine simulations due to variations in $H_2$ and salt force fields and methodological choices, such as neglecting long-range corrections. Despite these variations, most simulation predictions remain within a 5−10% margin, providing a reliable source of data for further

experimentation, modeling, and industrial practice. Future refinements in force field development and selection, and accurate treatment of ionic interactions may further reduce these discrepancies and enhance predictive accuracy.

**4.9.5. Interfacial Tensions of Gas Mixture−Hydrogen−Water Systems.** Fig. 67 highlights the distinct differences in IFT behavior for gas mixtures involving $H_2$/$CO_2$ compared to those containing $N_2$ or $CH_4$. Specifically, the $H_2$/$CO_2$ mixture displays a notably steeper slope, indicating a more pronounced decrease in IFT with increasing pressure. This behavior primarily arises due to $CO_2$ being near or above its critical point (7.3773 MPa and 304.15 K), where its density can fluctuate significantly, often changing by an order of magnitude within a narrow pressure interval. For instance, at 323.15 K, the density of $CO_2$ can increase dramatically from around 100 kg/m$^3$ at 5 MPa to roughly 1000 kg/m$^3$ at 20 MPa. Such significant density changes drastically reduce the liquid-vapor density contrast, causing a marked reduction in IFT. In contrast, mixtures involving $N_2$ or $NH_4$ remain well within supercritical conditions over comparable pressure ranges, resulting in more moderate density variations and correspondingly flatter IFT profiles. Additionally, the presence of $H_2$ does not significantly alter these general trends; the substantial decrease in IFT is predominantly driven by the supercritical transition of $CO_2$. From a practical standpoint, e.g., for subsurface storage and enhanced oil recovery applications, these observations highlight the acute sensitivity of interfacial properties to pressure variations near the critical region of $CO_2$.

## 4.10. Contact Angles of Hydrogen−Brine−Solid Systems

Contact angle (CA) is a key metric of wettability, which governs how $H_2$ gas, brine, and rock interact at nanoscale interfaces in UHS. Wettability controls capillary trapping, migration, and flow efficiency, yet experimental CA measurements under reservoir conditions are often hindered by surface roughness, contamination, and the challenges posed by extreme pressures and temperatures. MD simulations help overcome these limitations by resolving atomistic-scale interfacial structures, capturing gas adsorption, water layering, and ion-specific effects, while systematically varying pressure, temperature, salinity, gas composition, and mineral surface chemistry. When validated with experimental data, accurate force fields enable MD-derived CAs to inform larger-scale reservoir models, bridging molecular-level insights with field-scale performance. In what follows, we review studies that use MD simulations to investigate the CAs of water/brine droplets on different mineral substrates. Among these substrates, quartz surfaces are particularly important due to their prevalence in sandstone formations and their highly variable surface chemistry. To interpret the wettability trends observed in MD studies, it is useful to first outline the different types of quartz surfaces based on their degree of hydroxylation, as defined by Zhuravlev:[1047]

- Q4 Quartz Surface: Dehydroxylated (0 nm$^{-2}$ OH), weakly hydrophobic.

- Q3 Quartz Surface: Partially hydroxylated ($\approx$ 4.7 nm$^{-2}$ OH), strongly hydrophilic.

- Q2 Quartz Surface: Fully hydroxylated ($\approx$ 9.4 nm$^{-2}$ OH), hydrophilic but with some OH-OH hydrogen bonding that slightly reduces water affinity.

Understanding these surface chemistries provides essential context for interpreting how CA, and, by extension, wettability,

**Table 19. Summary of the MD Simulation Studies Investigating the IFTs of Hydrogen−Gas Mixtures in Contact with Water or Brine**[a]

| Study | System details | | Thermodynamic conditions | | |
|---|---|---|---|---|---|
| | Phases | Force fields | $p$ / [MPa] | $T$ / [K] | $c_{salt}$ / [molal] |
| van Rooijen et al.[630] | $H_2(g)$ | Vrabec[48] | 0.1 to 60 | 298 to 523 | |
| | $H_2O(l)$ | TIP4P/2005[1042] | (Logarithmic) | | |
| | Brine(l): $Na^+$ and $Cl^-$ | Madrid-2019[1034] | | | 0 to 5 |
| Omrani et al.[1018] | $H_2(g)$ | Marx and Nielaba[310] | 1 to 30 | 298 to 373 | |
| | $H_2O(l)$ | TIP4P/2005[1042] | (Logarithmic) | | |
| | Brine(l): $K^+$, $Na^+$ and $Cl^-$ | Smith and Dang[374,1043] | | | 0 to 5 |
| | Brine(l): $Ca^{2+}$, $Mg^{2+}$ | Aqvist[1044] | | | 0 to 5 |
| Xie et al.[1019] | $H_2(g)$ | IFF[313] | 5 to 40 | 298 to 373 | |
| | $CO_2(g)$ | Zhu[926] | | | |
| | $H_2O(l)$ | TIP4P/2005[1042] | (steps of 5) | | |
| | Brine(l): $Na^+$ and $Cl^-$ | Smith and Dang[374,1043] | | | 0 to 3 |
| Yang et al.[602] | $H_2(g)$ | IFF[336] | 1 to 160 MPa | 298 to 523 K | 0 |
| | $H_2O(l)$ | TIP4P/2005[1042] | | | |
| Doan et al.[1021] | $H_2(g)$ | IFF[313] | 1 to 70 | 300 to 343 | |
| | $CO_2(g)$ | EPM2[419] | | | |
| | $N_2(g)$ | OPLS[360] | | | |
| | $H_2O(l)$ | TIP4P/2005[1042] | | | |
| Doan et al.[1020] | $H_2(g)$ | IFF[313] | 1 to 70 | 300 and 323 | 0 |
| | $H_2O(l)$ | TIP4P/2005[1042] | | | |
| Chen and Xia[605] | $H_2(g)$ | IFF[313] | 1 to 60 | 320 | 0 |
| | $H_2O(l)$ | TIP4P/2005[1042] | | | |
| Chen et al.[604] | $H_2(g)$ | IFF[313] | 9.5 | 300, 400 | 2.22 (in unitls of molarity) |
| | $CO_2(g)$ | TraPPE[1045] | | | |
| | $H_2O(l)$ | TIP4P/2005[1042] | | | |
| | Brine(l): $Na^+$ and $Cl^-$ | Madrid-2019[1034] | | | |
| Adam et al.[1022] | $H_2(g)$ | Yang[325] | 10-60 | 323-388 | 1.9-4.75 |
| | $CO_2(g)$ | TraPPE[1045] | | | |
| | $CH_4(g)$ | TraPPE[301] | | | |
| | $H_2O(l)$ | TIP4P/2005[1042] | | | |
| | $Na^+$ | Chen et al.[1046] | | | |
| | $Cl^-$ | Chen et al.[1046] | | | |

[a]The salt concentrations in brine are reported in units of molality (mol salt / kg of $H_2O$). g and l in the parentheses indicate gas and liquid phases, respectively.

responds to changes in thermodynamic conditions and compositions relevant to UHS. The classification also helps prevent confusion when these surface types appear throughout the following sections.

Abdel-Azeim et al.[603] investigated the CA of water droplets in a $H_2$ gas atmosphere on caprock minerals mica, anhydrite, gypsum, and halite, examining the effects of pressure (5 to 20 MPa), temperature (298 to 323 K), and salinity (deionized water, seawater with 60000 ppm total dissolved solids, and formation water with 213000 ppm TDS). The system focuses on pure $H_2$ gas without mixtures such as $CH_4$ or $CO_2$, and brines containing ions like $Na^+$, $Ca^{2+}$, $Mg^{2+}$, $Cl^-$, and $SO_4^{2-}$ are used to represent different salinities. The CAs obtained for the water droplet on these mineral surfaces in a $H_2$ gas environment remain at or near zero degrees across all tested conditions, indicating strongly water-wet surfaces regardless of changes in pressure, temperature, or salinity. For example, in both MD simulations and sessile-drop experiments, the CA for water droplets on mica under $H_2$ pressure up to 20 MPa at 300 K was consistently zero, and similar behavior was observed on anhydrite, gypsum, and halite surfaces. The physical mechanism underlying these CA trends is attributed to the significantly stronger interactions between water molecules and the mineral surfaces compared to the interactions between

$H_2$ molecules and the mineral surfaces. Water forms strong adsorption and hydrogen bonds especially on calcium sulfate minerals (gypsum and anhydrite) due to divalent cations like $Ca^{2+}$. In contrast, $H_2$ is nonpolar and exhibits weak hydrophobic interactions with the mineral surfaces, making it unable to displace water or alter wettability even at elevated pressures. Temperature and salinity influence water diffusion and spreading kinetics but do not affect the ultimate water-wet state. Among the studied factors, the intrinsic molecular interactions between water and mineral surfaces most strongly influence the CA, overriding effects from pressure, temperature, or salinity variations. CAs computed with MD simulations were validated by sessile-drop experiments on plasma-cleaned mineral surfaces, showing excellent agreement with near-zero CAs, whereas higher CAs reported in the literature were attributed to organic surface contamination on uncleaned samples. No general empirical fit function for CA as a function of pressure, temperature, and salt composition was proposed in this study.

Al-Yaseri et al.[607] studied the CAs of water droplets on quartz and calcite mineral surfaces in a pure $H_2$ gas environment over a pressure range of 3.44 to 206.8 MPa, temperatures from 298 K to 323 K, and brine salinities from deionized water up to 213000 ppm total dissolved solids, with
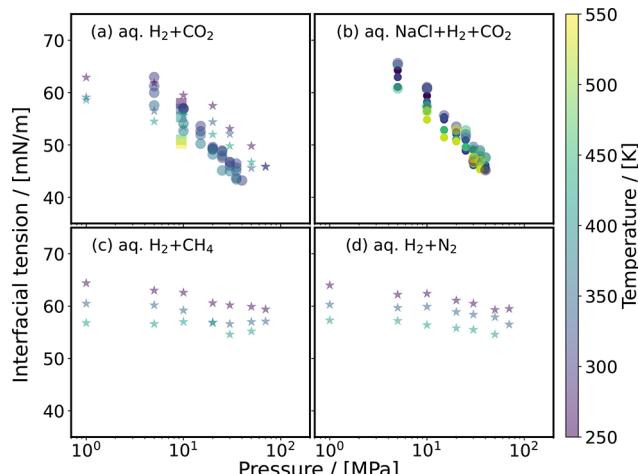
**Figure 67.** Interfacial tension of aqueous $H_2$-gas and $H_2$-gas-NaCl brine systems as a function of pressure computed with MD simulations. Gases considered in the $H_2$-gas-$H_2O$ system are (a) $CO_2$, (c) $CH_4$, and (d) $N_2$. (b) For the $H_2$-gas-NaCl brine (3 mol $kg^{-1}$), we consider only $CO_2$ for comparison. The colors of the markers represent the temperature at which the interfacial tension is reported. The data are taken from Xie et al.[1019] (circle), Doan et al.[1021] (star), and Chen et al.[604] (square). For comparison, a hydrogen mole fraction of 0.7 is chosen from the three different studies.

no additional gas mixtures such as $CH_4$ or $CO_2$ considered. The CAs measured for the water droplet on these mineral surfaces in a $H_2$ gas environment remain at or near zero degrees across all tested pressures, temperatures, and salinities, indicating a completely water-wet system; for example, CAs on quartz and calcite were zero even at the highest pressure of 206.8 MPa and formation water salinity. The MD simulations reveal that the dominant physical mechanism behind the zero CA is the significantly stronger molecular interactions between water and the mineral surfaces compared to the weaker $H_2$-water and $H_2$-mineral interactions, with water diffusion coefficients on quartz and calcite surfaces decreasing with increased salinity and stronger water-calcite interactions resulting in slower spreading times. Surface cleanliness was found to be the most critical factor influencing the CA measurements, as contamination can lead to artificially higher CAs, particularly on calcite surfaces. The CAs obtained experimentally using a carefully controlled cleaning protocol with air plasma treatment were in excellent agreement with MD simulations, both confirming the zero CA findings, resolving discrepancies in the literature reporting higher and variable CAs. No general empirical fit function for CA dependency on pressure, temperature, or salinity was proposed in the study.

Al-Yaseri et al.[606] studied the wettability properties as quantified by CAs of $H_2$ gas bubbles on quartz surfaces in the presence of brine containing 0.5M $Na^+$ ions at room temperature and ambient pressure. The study focused on the quartz-brine-$H_2$ interface, including the effect of organic acids such as Humic acid on wettability alteration. MD simulations were performed to measure the CAs of pure $H_2$ bubbles on silica surfaces in deionized water and in 0.5M NaCl brine, yielding CAs of approximately 120° and 122°, respectively. These values indicate poor $H_2$ wettability, consistent with a strongly water-wet quartz surface. In the simulations, the quartz surface was "aged" by introducing a model hydrophobic layer representing Humic acid decomposition products, such

as naphthenic acids and hexane, adsorbed onto the silica surface. This "aging" in MD refers to the surface modification step within the simulation framework rather than a physical experimental aging process. After this surface functionalization in the simulations, the CA of the $H_2$ bubble on the hydrophobized silica surface decreased significantly to about 44°, indicating a shift toward intermediate or $H_2$-wet conditions. This change is attributed to the hydrophobization of the silica surface by Humic acid, which enhances van der Waals interactions between $H_2$ molecules and the modified mineral surface, thereby promoting $H_2$ spreading. Experimentally, natural sandstone cores from the Lesueur Sandstone formation were aged by exposure to an aqueous Humic acid solution ($10^{-2}$M) for 42 days at 5°C and room pressure. This laboratory aging caused a wettability shift consistent with the MD results: the CA transitioned from strongly water-wet toward an intermediate wetting state. Although exact experimental CAs were not directly measured, the wettability alteration was inferred from changes in $H_2$ saturation and residual trapping, which are consistent with a CA reduction similar in magnitude to the 44° obtained in simulations. This study shows that the MD simulations capture the essential physics of wettability alteration by Humic acid.

MD simulations were conducted by Ali et al.[1048] to investigate the effects of varying gas compositions, including $H_2$, $CO_2$, and $CH_4$, on the wettability of kaolinite clay surfaces by brine droplets containing 10 wt% NaCl at 323 K and pressures between 5 and 40 MPa. The study focused on two distinct basal planes of kaolinite: the hydrophobic siloxane surface and the hydrophilic gibbsite surface, examining how CAs and IFTs respond to changes in pressure, temperature, and $H_2$ content. On the hydrophobic siloxane surface, CAs of brine droplets in pure $H_2$ environments ranged from approximately 91° to 106° over the pressure range studied, indicating an 'intermediate wet' behavior with relatively minor pressure dependence. When $CO_2$ was introduced as a cushion gas, the CAs increased significantly, ranging from about 118° at 5 MPa to nearly 160° at 40 MPa, corresponding to a transition from weakly gas-wet to strongly gas-wet surfaces. Mixtures of $H_2$ and $CO_2$ showed a marked reduction in the wettability of brine compared to pure $H_2$; for example, at 20 MPa, a system with 90 wt% $CO_2$ exhibited a CA of approximately 106°, lower than pure $CO_2$ but substantially higher than pure $H_2$. The effect of $CH_4$ as a cushion gas followed similar trends but was less pronounced than $CO_2$, with CAs increasing by up to 15° relative to pure $H_2$. Increasing pressure consistently increased CAs across all gas compositions, attributed to enhanced intermolecular interactions between the denser gas phases and the siloxane surface. Atomic density profiles revealed that $CO_2$ molecules adsorb closer to the siloxane surface (at approximately 2.7 Å) compared to $CH_4$ (ca. 3.1 Å) or $H_2$, effectively displacing some water molecules from the surface and reducing brine wettability. Water molecules form two distinct hydration layers near the surface, with gas molecules preferentially located within the first hydration layer; higher gas densities at elevated pressures amplify gas-surface affinity, further increasing CAs. On the hydrophilic gibbsite surface, $H_2$ formed cylindrical bubbles detached from the surface, indicative of strong water wettability and complete spreading of water. Increasing pressure from 20 to 80 MPa resulted in denser $H_2$ bubbles with reduced radius (from approximately 50.5 Å to 33.0 Å), reflecting increased water CAs and decreased $H_2$ affinity with the surface. Temperature increases from 303 K to

343 K led to reduced affinity between $H_2$ and the gibbsite surface, suggesting an increase in wettability at higher temperatures due to a decrease in $H_2$ density. The presence of $CO_2$ in $H_2$ bubbles on the gibbsite surface reduced $H_2$ density near the surface, further influencing wettability trends. Regarding temperature effects on the gibbsite surface, the study indicated a less pronounced influence compared to pressure. However, higher temperatures tend to reduce gas density, and thus, gas affinity, which would increase wettability, although these effects were secondary to pressure-driven trends. These observations indicate that pressure and temperature influence wettability on the hydrophilic surface in manners similar to those on the hydrophobic siloxane surface but with overall stronger water affinity leading to complete wetting. Overall, the simulations demonstrate that the wettability of kaolinite surfaces by brine is significantly modulated by gas composition and thermodynamic conditions, with $CO_2$ causing the most substantial increase in gas-wetting behavior on the hydrophobic siloxane surface, followed by $CH_4$, while pure $H_2$ maintains intermediate wettability. Pressure predominantly governs these effects by altering gas density and gas-surface interactions, whereas temperature has a subtler role, particularly on the hydrophilic gibbsite surface. The simulated CA trends align well with experimental observations reporting increased CAs with pressure and stronger gas wetting for $CO_2$ compared to $H_2$, although some discrepancies exist due to differences in surface basal planes studied.

The study by Alshammari et al.[1049] focused on IFT and wettability of water−$H_2$ systems-pure and with cushion gases ($CH_4$, $CO_2$)-in brines containing $Na^+$, $Mg^{2+}$, $Ca^{2+}$, and $Cl^-$. Simulations were performed at 298-323 K, 5−20 MPa, and salinities from deionized to formation water. CAs of water on calcite and silica were evaluated up to 20 MPa at $\approx$ 300 K. pH was represented by tuning the ionization of surface silanol groups on silica slabs: 0% ionization (all silanols protonated) reproduce acidic conditions (pH $\approx$ 3), whereas 10% ionization (partial deprotonation) correspond to near-neutral pH $\approx$ 6. This shift from a neutral to a negatively charged surface alters rock-fluid interactions, moving the quartz CA from an intermediate value toward a strongly water-wet state as water molecules increasingly displaced adsorbed $CO_2$. In $H_2$ gas, calcite stayed strongly water-wet (CA $\approx$ 0°); quartz showed CA $\approx$ 56 - 75°, shifting toward intermediate wetting with changing gas mixtures and surface charge. The highest CA was in $H_2$/$CO_2$ at low pH, as $CO_2$ strongly adsorbs on protonated silica, thickening the interfacial gas layer and slowing water spread. In contrast, $CH_4$ and pure $H_2$ interact weakly, keeping CA lower. Barbosa et al.[1050] reported wettability, specifically CAs, of water and brine droplets containing NaCl (up to 20 wt %) on siloxane, gibbsite, and defective siloxane surfaces of kaolinite in the presence of gases including $H_2$, $CH_4$, and $CO_2$ across conditions relevant to underground $H_2$ storage, with pressure at 10 MPa, temperature at 323 K, and varying defect densities on the substrate. The CAs of brine droplets on the siloxane surface without gas are approximately 93°, indicating hydrophobic behavior, whereas on gibbsite surfaces CAs are about 13°, showing hydrophilicity; the presence of $CO_2$ significantly increases CAs (e.g., up to 131° on siloxane), while $H_2$ (95°) and $CH_4$ (100°) cause smaller increases. Increasing defect density on siloxane surfaces by removing up to 30% of silicon sites reduces CAs for brine droplets, e.g., from 84° to 68° in $H_2$ environments and from 111° to 83° in

$CO_2$ environments, indicating enhanced wettability with more defects; CAs for pure water are generally lower than for brine and show greater variability. The physical mechanism behind these trends is attributed to stronger adsorption of $CO_2$ on heterogeneous surfaces displacing water and altering surface hydrophilicity, the formation of silanol nests at defect sites may alter hydrophilicity, and salt ions ($Na^+$, $Cl^-$) interacting with the surface to reduce CAs by modifying water-surface interactions. Surface defects, particularly their density and spatial coordination, most strongly influence CAs, with machine learning models showing improved prediction when defect arrangement is considered. The simulation data of CAs for brine on siloxane and gibbsite surfaces agree well with available experimental data, supporting the validity of the MD approach.

Fatah et al.[1051] performed MD simulations to compute the wettability and flow of $H_2$, $CH_4$, $CO_2$, and $N_2$ against 57-670 ppm brine ($Na^+$, $Mg^{2+}$, $Ca^{2+}$, $Cl^-$, $SO_4^{2-}$) on calcite at 25 °C and 1000 psi. In all cases the water droplet spread completely (CA $\approx$ 0°), confirming calcite is strongly water-wet; seawater-calcite interaction energies dwarfed gas-rock and water-gas terms. Although $CO_2$ adsorbed most strongly and its brine IFT was far lower than for $H_2$, $CH_4$, or $N_2$, these differences did not alter the CA. Hence gas type and brine composition exert negligible influence on calcite wettability, which is governed by the mineral's hydrophilicity, an insight vital for underground $H_2$-storage design.

Ghafari et al.[1052] used MD simulations to examine water CAs on silica surfaces in brine/gas environments under subsurface conditions (10 - 30 MPa, 333 - 413 K), with $H_2$ mole fractions varying from 0 to 1 and silica surface charges from 0 to -0.12 C m$^{-2}$. Binary gas mixtures of $H_2$ with $CO_2$, $CH_4$, or $N_2$ were considered at $x_{H_2}$=[0.0, 0.3, 0.7, 1.0], showing that increasing the mole fraction of cushion gases, especially $CO_2$, raises the CA, an effect amplified at higher pressures and lower temperatures. Five distinct silica surface models (Q2, Q3, and Q3/Q4 types) with silanol densities between 2.35 and 9.58 nm$^{-2}$ were tested, with $\alpha$-quartz (101) at 5.9 nm$^{-2}$ serving as the reference substrate. Surface charges were introduced by deprotonating a fraction of surface silanol (Si-OH) groups: 0% ionization (all silanols protonated) represents acidic conditions, whereas 10% ionization (partial deprotonation) mimics near-neutral pH. On neutral silica in pure $H_2$, the CA remains low and nearly independent of pressure and temperature. For neutral surfaces, the four cushion gases increase the contact angle in the following order: $CO_2$ > $CH_4$ > $N_2$ > $H_2$. This trend arises from competitive gas adsorption, $CO_2$ has the strongest affinity for silica—forming a thicker adsorbed layer that impedes water spreading under high—pressure, low-temperature conditions while $CH_4$ and $N_2$ exhibit weaker adsorption, and $H_2$ the weakest. The surface charge exerts the most pronounced influence: As ionization increases to -0.12 C m$^{-2}$, the silica becomes strongly water-wet (CA $\rightarrow$ 0°) regardless of the composition, pressure, or temperature of the gas, because deprotonation enhances the electrostatic interactions between rocks and water that displace the adsorbed gas. Simulations of $\alpha$-quartz (101) based on the INTERFACE force field closely reproduce experimental CA data, correcting the overestimation of hydrophilicity reported when using CLAYFF or DDEC force fields. These results emphasize that accurate force field selection and realistic

surface characterization are essential for predicting wettability in brine−gas−rock systems relevant to UHS.

Atomistic MD simulations were conducted by Phan et al.[1053] to investigate the wetting properties of brine droplets containing 20 wt% $Na^+$ and 1 wt% $K^+$ on talc and the hydroxylated basal face of kaolinite (kaoOH) substrates in gas mixtures comprising $H_2$ and cushion gases ($CH_4$ or $CO_2$) at geological conditions of 15 MPa and 333 K, with varying gas compositions including pure $H_2$, 75 mol% $H_2$ - 25 mol% cushion gas, 60 mol% $H_2$ - 40 mol% cushion gas, and pure cushion gas. The CAs of brine droplets on talc surfaces were found to be strongly hydrophobic with values greater than 90°, increasing from approximately 102.6° in pure $H_2$ to about 143.4° with pure $CO_2$, and to ca. 112.4° with pure $CH_4$, whereas on the kaoOH surface the CAs remained consistently low, between 11.4° and 15.8°, regardless of gas composition. The authors attribute these trends to the differences in clay-brine interactions and surface chemistry, where talc's hydrophobic siloxane basal face leads to more favorable cavity formation near the surface (lower free energy) and thus higher CAs, while kaoOH's hydrophilic hydroxylated surface exhibits stronger water adsorption and higher free energy of cavity formation, resulting in lower CAs. Among the factors studied, the nature of the clay surface chemistry most strongly influences the CA. The simulation results for CAs on kaoOH closely agree with experimental data reporting values near 15° to 20°, while differences with some experiments on kaolinite siloxane faces are noted, likely due to variation in the specific basal planes studied.

Yang et al.[602] studied interfacial properties of the $H_2$ + $H_2O$ and $H_2$ + $H_2O$ + solid systems with silica and kerogen substrates over a broad range of temperatures (298 to 523K) and pressures (1 to 160 MPa). The study focused on pure $H_2$ gas mixtures without additional gases such as $CH_4$ or $CO_2$ and did not address salt concentration effects in brine; CAs of $H_2O$ droplets on silica and kerogen surfaces in a $H_2$ gas environment were analyzed. The CAs of the $H_2O$ droplet on silica surfaces ranged from approximately 21.8° to 49.0° and generally increased with pressure while decreasing with temperature, with less pronounced temperature and pressure effects at low temperatures (298 and 373 K). For kerogen surfaces, the CAs ranged from 0° (fully water-wet) to about 61.9°, showing a decrease with increasing temperature and an increase with pressure, with CAs increasing from 0° to 31.4° as pressure rose from 5 to 160 MPa at 523 K. These CA trends were explained through variations in the IFT between $H_2O$-rich and $H_2$-rich phases and adhesion tensions representing fluid-solid interactions; the adhesion tension is defined as the difference between the IFT of the solid with the $H_2$-rich phase and that with the water-rich phase, reflecting the fluid-solid interaction contribution to wettability. Adhesion tensions decreased significantly with temperature and showed moderate pressure dependence on silica but decreased with pressure on kerogen, especially at lower temperatures. The strongest influence on CAs was identified as the balance between fluid-fluid IFT and fluid-solid adhesion tension, which both vary with temperature and pressure. CAs obtained from MD simulations were consistent with previous simulation studies and showed qualitative agreement with experimental trends, although absolute values for silica were somewhat higher likely due to differences in surface silanol group density; no explicit quantitative fit to experimental CAs was reported.

The MD study by Yao et al.[1054] examined bulk and interfacial properties (IFT and water−silica CAs) in $H_2$/brine systems, i.e., NaCl, KCl, $CaCl_2$, over 323 - 423 K, 14 - 150 MPa, and up to 5.4 mol/kg salt, and provided comparisons with $CO_2$/brine/silica systems. CAs on silica in $H_2$/brine span roughly 42.5° to 72.2°, as salt increases from 0 to 5.4 mol/kg in the order KCl < NaCl ≈ $CaCl_2$. Pressure and temperature effects on the angle are otherwise minor. By measuring $\cos\theta$ (CA) and $\gamma_{WG}$(brine-gas surface tension), the authors use Neumann's equation,[1055] with an empirical constant $\beta$, to evaluate $\gamma_{SG}$ (solid-gas surface tension) and $\gamma_{SW}$ (solid-brine surface tension), though $\gamma_{SG}$ and $\gamma_{SW}$ are challenging to directly obtain. They report $\gamma_{SG}$ remains effectively constant with salinity (whether imposed or derived is unclear from their article), and as a result $\gamma_{SW}$ decreases as salt concentration rises. Consequently, the adhesion tension ($\gamma_{SG} - \gamma_{SW}$) falls with salinity, explaining the larger CAs. Beyond noting these interdependencies, the study does not draw further conclusions from the trend in $\gamma_{SW}$ alone. It seems that ion exclusion (negative surface excess) raises $\gamma_{WG}$ and shifts the force balance at the contact line and drives the wettability behavior. Salt concentration thus most strongly controls the CA by altering adhesion tension. The computed angles and IFTs compared reasonably well with experimental data for $H_2$/NaCl brine on silica, though some discrepancies remain, likely due to force−field limitations.

Yu et al.[1056] performed MD simulations to compute the CAs of water droplets on organic-rich shale surfaces, represented by graphene, in pure $H_2$ environments and $H_2$-$CH_4$ and $H_2$-$CO_2$ gas mixtures, over pressure ranges from 5 to 40 MPa and temperature ranges from 292 to 343 K, with gas mole fractions varying from 25% to 100% $H_2$; salt concentration and specific brine ion effects are not explicitly modeled but are noted as future considerations. The CA of water on these substrates generally decreases with increasing temperature by up to about 5.8° at an intermediate pressure of 5 MPa and increases with increasing $H_2$ pressure by roughly 20° from 5 to 40 MPa, indicating a shift toward less water-wet conditions; in $CO_2$-$H_2$ mixtures, CAs remain high at 180° (fully gas-wet) when the $H_2$ fraction is below 25% and sharply decrease to strongly water-wet values around 22° as $H_2$ fraction approaches 100%, while in $CH_4$-$H_2$ mixtures, the system transitions from moderately gas-wet to strongly water-wet as $H_2$ fraction increases, with a neutrally wet state defined by CAs near 90° at about 75% $CH_4$. These trends are explained by molecular interactions where increased temperature (292−343 K) reduces $H_2$ density and adsorption due to higher kinetic energy, weakening $H_2$-surface interactions and lowering CAs, whereas increased pressure (5−40 MPa) enhances $H_2$ density and adsorption, increasing CA; competitive adsorption in gas mixtures causes preferential adsorption of $CO_2$ and $CH_4$ over $H_2$, influencing wettability and CA behavior. CA results from molecular simulations agree qualitatively with experimental data on $H_2$-organic shale systems but show variations attributed to differences in rock composition, surface roughness, and experimental uncertainties.

The study by Zhang et al.[1057] focused on CAs of $H_2$ with brines of varying salinity (up to about 1 mol/L NaCl) on mineral substrates quartz, calcite, halite, and montmorillonite, across pressure ranges of 5 to 25 MPa and temperatures from 300 to 400 K. The CAs of water on these mineral surfaces in a $H_2$ gas environment were examined using MD simulations under these reservoir-like conditions. CAs generally increase

with pressure; for example, CAs for quartz increased from approximately 25° at 5 MPa to about 40° at 25 MPa. Temperature effects on CAs are less pronounced. For all substrates, CA slightly decreases (by ca. 5°) when temperature increases from 300 to 400 K. Salinity increases tend to raise CAs by ca. 5°, except for calcite where the effect is negligible, less than 1° change up to 1 mol/L NaCl. The authors observe that the variation in the bulk density of $H_2$ with pressure correlates with the cosine of the contact angle: as the bulk density of $H_2$ increases with pressure (from ca. 5 kg/m$^3$ to 20 kg/m$^3$ between 5 and 25 MPa), the cosine of the contact angle decreases. Electrostatic interactions and the electrical double layer on charged minerals like montmorillonite enhance water wettability strongly, contributing up to 50% of the total interaction energy. Among the investigated factors, pressure, via its effect on $H_2$ density, exerts the strongest influence on CA. The simulated CAs were compared to various experimental measurements, showing reasonable agreement especially for clean mineral surfaces, with discrepancies attributed to organic surface contamination and surface heterogeneity in experiments. The authors propose a theoretical model based on a sharp-kink approximation that relates CA to $H_2$ density, IFT, and water-mineral interaction energy, which can predict trends of CA as functions of pressure, temperature, and salinity.

Using MD simulations Zheng et al.[609] studied the wettability of pure water droplets on quartz substrates in the presence of $H_2$ gas under various geo-storage conditions, covering pressures from 1 to 30 MPa and temperature fixed at 338 K. The study focuses on pure $H_2$ environments and considers hydroxylation states of quartz surfaces (Q2, Q3, and Q4 quartz). The CA of water on fully hydroxylated quartz surfaces in a $H_2$ environment fluctuates between approximately 30.7° and 37.1° across the pressure range studied, with CAs increasing from 4.5° on partially hydroxylated quartz (Q3) to 34° on fully hydroxylated quartz (Q2), and reaching 94.7° on dehydroxylated quartz (Q4), indicating a transition from hydrophilic to weakly hydrophobic behavior depending on surface chemistry. The authors attribute these CA trends primarily to the flexibility of the quartz substrate and the arrangement and area density of surface hydroxyl groups, where hydrogen bonding probability between water and hydroxyl groups strongly dictates hydrophilicity; the CA increase with hydroxyl density is nonmonotonic due to intramolecular hydrogen bonding among surface hydroxyls reducing available bonding sites for water. The simulated CAs fall within the range of experimental measurements reported in the literature, confirming the validity of the MD models, although discrepancies in pressure dependence of CA observed experimentally are suggested to arise from surface roughness and experimental conditions. No general empirical fit function for CA as a function of pressure, temperature, or salt composition is proposed in this work.

The study by Zheng et al.[608] focused on the wettability of quartz surfaces with varying surface chemistries and morphologies under subsurface $H_2$ geo-storage conditions, examining the effects of pressure up to 1000 MPa, temperature at 338 K, NaCl concentrations from 0 to 1.0 mol%, and gas mixtures including pure $H_2$ and $H_2$-$CH_4$ mixtures with $CH_4$ mole fractions up to 50 mol%. CAs of water droplets on fully hydroxylated, half-methylated, fully methylated, pristine, and rough quartz surfaces in $H_2$ and $H_2$-$CH_4$ environments are quantified to understand wetting behavior. For fully hydroxy-

lated (non-methylated) quartz surfaces, the water CA remains consistently near 34° across NaCl concentrations, showing negligible influence from salinity. Similarly, the addition of $CH_4$ as cushion gas only slightly increases the CA to about 36.1°, indicating minimal wettability change. With pressure variation up to 30 MPa, the CA on fully hydroxylated quartz fluctuates modestly between approximately 30.7° and 37.1°, driven primarily by the pinning effect due to surface heterogeneity at low pressures, and transitions to $H_2$-quartz interaction dominance at higher pressures. The fully hydroxylated rough quartz surfaces also exhibit a distinct jump in CA between 38 and 70 MPa, corresponding to a transition in the water film state on the rough surface. Moving to half-methylated quartz surfaces, CAs decrease from about 45.9° to 31.2° as NaCl concentration rises to 0.5 mol%. In $H_2$-$CH_4$ mixtures, the half-methylated quartz surfaces show a notable CA decrease from 45.9° to 32° with $CH_4$ mole fraction increasing to 20 mol%, followed by a slight increase at higher $CH_4$ content. The variation of CA with pressure on half-methylated quartz is non-monotonic, increasing from 41.2° to 49.3° between 1 and 20 MPa, then slightly decreasing at 30 MPa; this behavior is attributed to a competition between the pinning effect caused by surface heterogeneity (including organic ligand distribution) at low pressures and $H_2$-quartz interactions at higher pressures. Finally, for fully methylated quartz surfaces, the CA of water increases significantly with methylation degree, rising from about 32° at 12.5% methylation to 96.4° at 87.5% methylation. Interestingly, a slight decrease in CA from 34° to about 32° is observed when methylation increases from 0 to 12.5%, explained by the dual role of methyl groups: while their hydrophobic nature reduces surface hydrophilicity at high methylation, at low methylation they suppress hydrogen bonding among surface hydroxyl groups, thereby enhancing hydrophilicity. The study highlights that methylation degree is the strongest factor influencing the CA, whereas pressure and salinity effects are strongly dependent on the quartz surface chemistry and morphology. Simulated CAs for water on fully hydroxylated quartz in $H_2$ at 10 MPa and 338 K are ca. 34°, aligning well with experimental values ranging from 30° to 40°. This research reconciles prior experimental discrepancies by considering detailed variations in surface morphology and chemistry.

Chen et al.[604] computed interfacial properties including CA, IFT, surface excess, and bubble morphology of $CO_2$/$H_2$ mixtures in contact with brine containing $Na^+$ and $Cl^-$ ions and hydrophilic silica surfaces, over pressure of 10 MPa and temperature range 300-400 K, with gas mixtures varying in $H_2$ mole fraction from pure $H_2$ to $CO_2$-rich systems and brine salt concentration of ca. 2.22 molal. The CAs of $CO_2$ and $H_2$ bubbles on hydrophilic silica in $H_2O$ and brine environments are greater than 100°, with $CO_2$ showing smaller CAs (e.g., 109.8° to 134.3° for $CO_2$ and up to 156.8° for $H_2$) indicating stronger wetting affinity to silica compared to $H_2$; salts reduce CA, particularly at low temperatures, and CA for $CO_2$ increases with temperature while that of $H_2$ is less sensitive. The authors attribute CA trends to molecular interactions where $CO_2$ has stronger electrostatic and hydrogen bonding interactions with $H_2O$ and silica surfaces due to its quadrupole moment, while $H_2$ interacts weakly via van der Waals forces; NaCl ions modify surface polarity by forming an electrical double layer reducing CA, and temperature affects dissolution and diffusivity impacting wetting behavior. CAs predicted by MD simulations are consistent with available experimental

(a)



(b)
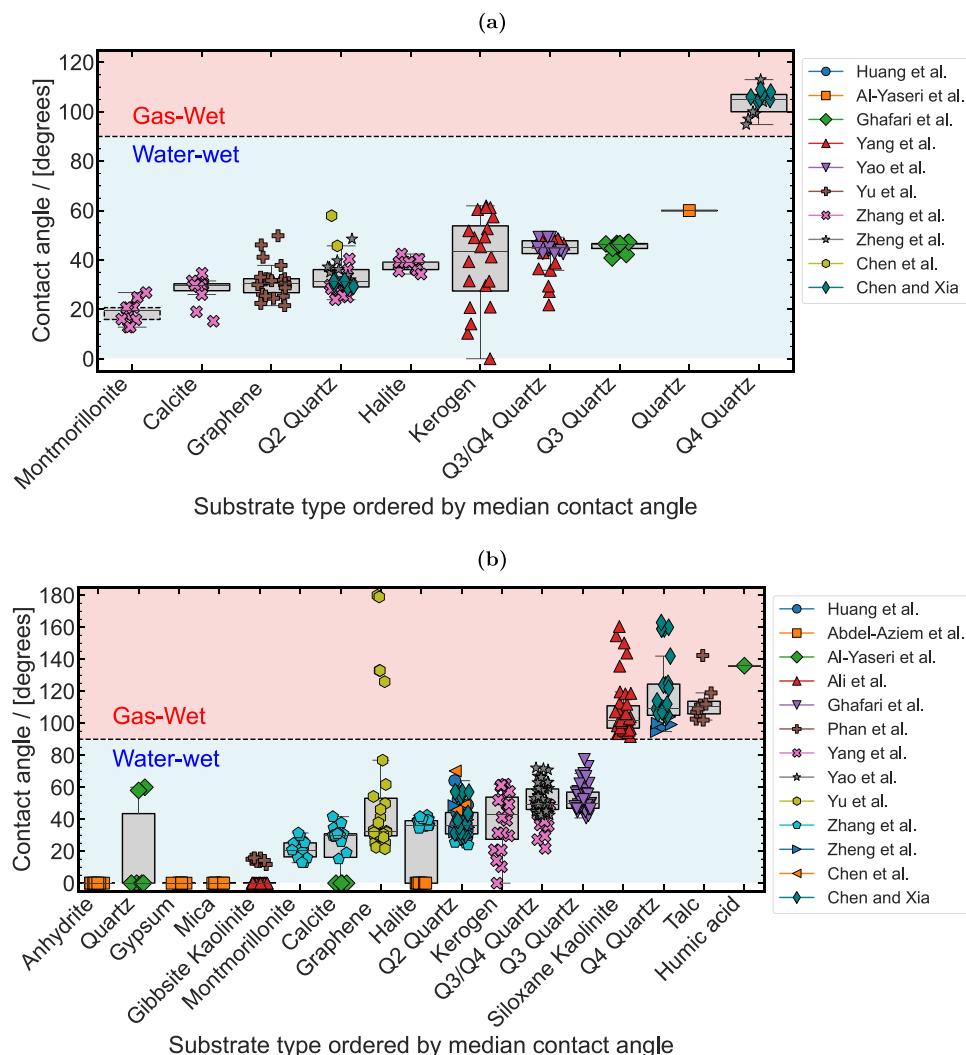


**Figure 68.** (a) Data for contact angles of pure water droplets immersed in pure $H_2$ for different substrates collected from multiple studies. Angles below 90° indicate water-wet surfaces, while those above 90° indicate gas-wet surfaces. All reported contact angles are shown regardless of temperature and pressure. (b) Data for contact angles of water/brine droplets immersed in a gas environment (pure $H_2$, $H_2$-$CO_2$, $H_2$-$CH_4$) collected from different sources. The complete list of studies and their temperature ranges are listed in Table 20.

data, showing similar trends in temperature and pressure dependence, although direct quantitative comparison is limited by experimental uncertainties and system complexities.

MD simulations were performed by Chen and Xia[605] to investigate the transport and interfacial properties including density, viscosity, diffusion coefficient, wettability, IFT, and surface adsorption of $H_2$, $CO_2$, and $CH_4$ gases interacting with $H_2O$ and silica substrates under typical subsurface reservoir conditions at a temperature of 320 K and pressures up to 60 MPa. The study focused on CAs of water droplets on two types of silica substrates, hydrophilic Q2 and hydrophobic Q4, in environments containing pure $H_2$, $CO_2$, or $CH_4$ gases. The CA of water on both Q2 and Q4 silica substrates generally increased with gas pressure for $CO_2$ and $CH_4$, reaching plateaus between 10 and 30 MPa, with $CO_2$ showing the highest CAs, followed by $CH_4$, and then $H_2$, which had minimal effect even up to 60 MPa. For example, the CA on hydrophobic Q4 silica was about 106° without gas and increased to approximately 142° in a $CO_2$ environment at 10 MPa, whereas $H_2$ caused negligible changes in CA under all pressures. The physical mechanism explaining these trends arises from the differences in intermolecular interactions: $CO_2$

exhibits strong electrostatic interactions with silica due to its quadrupole moment, leading to higher wettability and increased CAs, while $H_2$ interacts weakly via van der Waals forces and has low adsorption capability on silica surfaces, resulting in little alteration of the water CA. The CA correlates inversely with the gas–water IFT, which remains nearly constant for $H_2$ but decreases significantly with pressure for $CO_2$. Gas pressure, particularly of $CO_2$, is the most influential factor affecting CA, while substrate hydrophilicity or hydrophobicity also plays a significant role in baseline CA values. MD results for CAs show good qualitative agreement with available experimental data for $CO_2$ and $CH_4$ systems, although some discrepancies exist regarding the pressure dependence of CAs in $H_2$ environments.

Huang et al.[1058] performed MD simulations to study CAs of deionized water and brine droplets containing $Na^+$ and $Cl^-$ ions on fully hydroxylated $\alpha$-quartz (Q2 surface) substrates under varying gas environments including pure $H_2$, $CH_4$, and $CO_2$ gases. The simulations are conducted at a temperature of 333 K and a pressure of 20 MPa, with brine salinities of ca. 1.5 M and 3.5 M, mimicking typical geological conditions relevant for underground gas storage and recovery. The CA of water
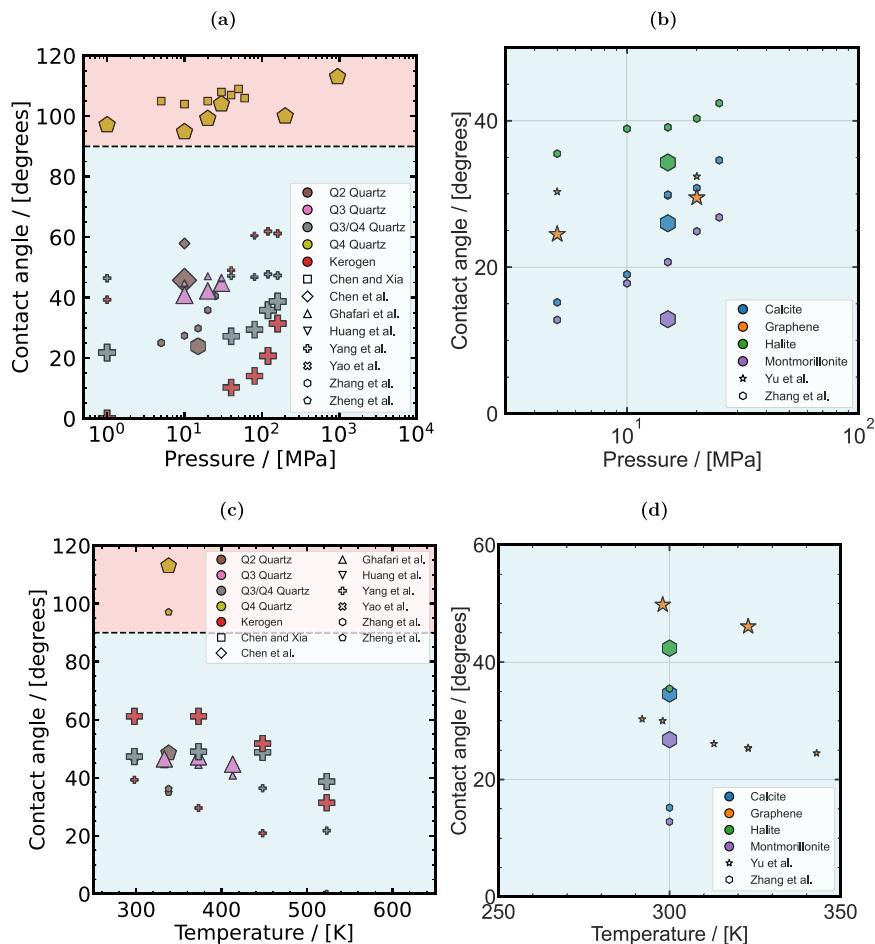
**Figure 69.** Computed contact angles of pure water droplets immersed in $H_2$ as a funtion of pressure (a: low pressure data and b: high-pressures data) and temperature (c and d: all pressures reported) compiled from multiple studies. Angles below 90° denote water-wet surfaces, while those above 90° denote gas-wet surfaces. From each study, only the data with the lowest and highest pressures/temperatures are shown. The marker size represents the magnitude of pressure/temperature: In (a) and (b) large and small symbols represent high and low temperatures, respectively, and in (c) and (d) large and small symbols represent high and low pressures, respectively. A complete list of the studies and the respective temperature ranges are provided in Table 20.

droplets on quartz in the presence of different gases follows the order $\theta_{H_2} < \theta_{CH_4} < \theta_{CO_2}$, with all values below 50°, indicating a strongly hydrophilic surface; the presence of salt ions generally increases the CA regardless of the gas type, thus reducing wettability. This trend is explained by the authors through interaction energy analyses showing that gas-quartz interactions decay faster than gas - water interactions, with the gas-quartz interaction energies ordered as $CO_2 > CH_4 > H_2$, while water-quartz interactions remain relatively constant and dominated by electrostatic forces ($\approx 95\%$), minimally affected by salt ions; the increased CA with salinity is attributed primarily to the augmented gas–water IFT caused by salt addition. The gas species type most strongly influences the CA, with $CO_2$ producing the largest values due to its stronger van der Waals and electrostatic interactions with quartz, and salt concentration also plays a significant role by increasing IFT and thus CA. The computed CAs are consistent with experimental observations showing quartz surfaces are more hydrophilic in $H_2$ environments and become less hydrophilic with increasing salinity.

### 4.10.1. Effect of Substrate Material, Pressure, Temperature, and Salinity on the Computation of Contact Angles. Based on the studies reviewed above, it is clear that

the CA of a water droplet varies with substrate, salt concentration, pressure, temperature, and surrounding gas composition. In Fig. 68(a), CAs collected from multiple studies[602,604,605,607,609,1052,1054,1056−1058] are shown. These data are shown irrespective of the pressure and temperature conditions to isolate substrate effects. A clear trend emerges where all substrates except Q4 Quartz are hydrophilic (water-wet in UHS terminology), with CAs below 60 degrees. In contrast, Q4 Quartz shows CA values of ca. 100 degrees, indicating weak hydrophobic (gas-wet) behavior. This aligns with its dehydroxylated surface having negligible hydroxyl group density (0 nm$^{-2}$),[1047] which limits hydrogen bonding. Also evident in Fig. 68(a) is the consistency across studies, i.e., CAs for Q2 Quartz, Q3/Q4 Quartz, and Q4 Quartz agree within 20 degrees. The key message is that CAs can range from 0 to 120 degrees depending on the substrate, with substrate effects outweighing those of pressure and temperature. To further emphasize this, Fig. 68(b) compiles CA data for water or brine droplets, regardless of pressure, temperature, salt concentration, or surrounding gas. Here, CAs span 0 to 180 degrees. Non-wetting substrates such as the siloxane surface of Kaolinite, Q4 Quartz, Talc, and Humic acid stand out clearly. Graphene also shows a non-wetting trend in the study by Yu et al.,[1056] with CAs above 90 degrees due to exposure to $CO_2$,
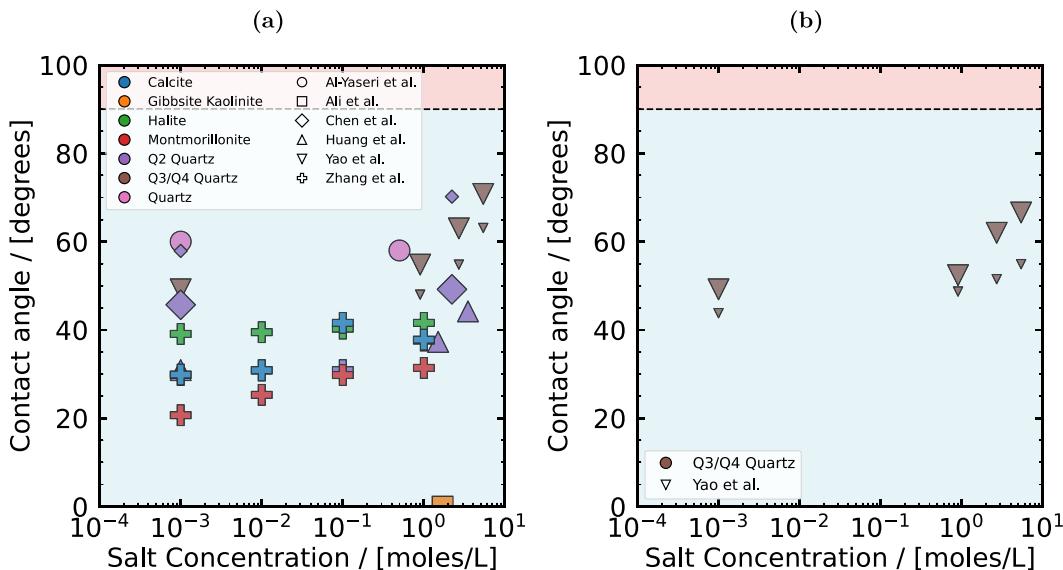
**Figure 70.** Data for contact angles of pure water droplets immersed in pure H$_2$ as a function of salt concentration of (a) NaCl and (b) KCl, compiled from multiple studies. Angles below 90° indicate water - wet surfaces (blue shade), while those above 90° indicate gas - wet surfaces (red shade). All reported pure-water CAs from each study are included, regardless of pressure and temperature. The CA data for the largest pressure and largest temperature is represented by larger - sized symbol and the smaller symbol represents the CA at the lowest pressure and lowest temperature by the same study. All CA data at intermediate pressures and temperatures are omitted for visual clarity. The complete list of studies and their pressure ranges are listed in Table 20.

which reduces water adsorption. Similarly, Ali et al.[1048] report brine droplets on Q4 Quartz with CAs ranging from 100 to 180 degrees depending on the CO$_2$ content in the environment surrounding the bubble. Chen and Xia[605] further show that water on Q4 Quartz in CO$_2$ exhibits a CA increase of nearly 60 degrees with pressure. In summary, surface chemistry has the strongest influence on CA, followed by the effect of CO$_2$ composition on substrates like Graphene[1056] and Q4 Quartz.[1048]

In Fig. 69(a) and Fig. 69(b), the effect of pressure across different substrates is shown. Clearly, CA increases with pressure. Data from Yang et al.[602] in Fig. 69(a) (small and large plus symbols) show CA rising from 0 to 30 degrees on Kerogen and from 20 to 40 degrees on Q3/Q4 Quartz as pressure increases from 1 to 160 MPa. A similar trend is reported by Zhang et al.,[1057] where CA increases from 25° to 40° at $T = 300$ K. Notably, Zheng et al.[608] computed CAs over a wide pressure range (1 - 1000 MPa) on Q4 Quartz and observed a maximum variation of only about 20 degrees. In contrast, Ghafari et al.[1052] have shown that CAs are weakly dependent on pressure shown specifically for water droplets on Q3 Quartz (pink triangles in Fig. 69(a)). In Fig. 69(b), contact angles on Calcite, Montmorillonite, and Halite from Zhang et al.[1057] show a modest increase with pressure. By contrast, Yu et al.[1056] in Fig. 69(b), and Chen et al.[604] in Fig. 69(a), report no clear pressure dependence. Overall, pressure tends to increase CA, although the effect is relatively weak. The underlying mechanism, as suggested by several authors, involves gas adsorption density increasing more strongly near the substrate than that of the liquid, due to gas compressibility. This enhances gas—substrate interactions, shifting the interfacial balance and increasing CA.

The effect of temperature on the CAs of water droplets is shown in Fig. 69(c) and Fig. 69(d). One can observe that increasing temperature reduces CA, enhancing water-wetness. In the study by Yang et al.,[602] water droplets on Kerogen show

a clear decrease in CA with temperature: at 160 MPa (large plus symbols), CA drops from 60° to 30°, and at 1 MPa (small plus symbols), from 40° to 0°. On Q3/Q4 Quartz, however, the reduction is less pronounced. At 1 MPa, CA decreases from approximately 45° to 20°, and at 160 MPa, from 45° to 40°, indicating substrate-dependent variation with temperature. Yang et al.[602] attribute this trend to weakened H$_2$ adsorption at higher temperatures, where entropic contributions dominate, allowing water to spread more readily by displacing gas molecules—a mechanism likely applicable to other gases as well. Similarly, CA variation on Q3 Quartz (pink triangles) in Ghafari et al.[1052] is minimal. As shown in Fig. 69(d), Yu et al.[1056] also reported a decrease of about 10° in CA for water on graphene as temperature increases from 260 to 340 K. As a concluding remark we can say that rising temperature weakens gas adsorption, facilitating water spreading and reducing contact angles.

The effect of salt concentration on the CAs of water droplets is shown in Fig. 70. It can be observed that increasing salt concentration raises CA by reducing water-wetness. In Fig. 70(a), the CAs of NaCl brine droplets from Yao et al.[1054] (Q3/Q4 Quartz) and Zhang et al.[1057] (Montmorillonite, Calcite, Halite, and Quartz, overlapping markers) show a clear increasing trend with salt concentration. Huang et al.[1058] reported a similar rise on Q2 Quartz. Thus, despite variations in substrate type, CAs consistently increase with salt concentration. Notable exceptions include Al-Yaseri et al.[607] and Chen et al.,[1046] where CA remains largely unchanged with increasing salt. In Fig. 70(b), Yao et al.[1054] show that KCl exhibits a similar trend on Q3/Q4 Quartz. Therefore, increasing the concentration of either NaCl or KCl appears to similarly increase CA. This rise is attributed to ion accumulation in the water bulk, which lowers the water-H$_2$ IFT.[1054] At the same time, the adhesion tension (difference between solid-brine and solid-gas interfacial energies) adjusts

**Table 20. Summary of the MD Simulation Studies Investigating the CAs in aqueous brine-$H_2$ Gas Mixture-Solid Systems.**[a]

| | System details | | Thermodynamic conditions | | |
|---|---|---|---|---|---|
| Study | Species | Force field | $p$ [MPa] | $T$ [K] | $c_{salt}$ [mol / L of solvent] |
| Abdel-Azeim et al.[603] | Flexible $H_2$ | IFF[313] | 5 and 20 | 300 and 323 | 0 |
| | $H_2O$ | SPC/E[346] | | | |
| | $KAl_2(Si_3Al)O_{10}(OH)_2$ (Mica) | ClayFF[422] | | | |
| | $CaSO_4.2H_2O$ (Gypsum) | ClayFF[422] | | | |
| | $CaSO_4$ (Anhydrite) | ClayFF[422] | | | |
| | NaCl (Halite) | ClayFF[422] | | | |
| | Brine : $Na^+$, $Ca^{2+}$, $Mg^{2+}$ | Aqvist[1044] | | | 0.001, 0.007 |
| | Brine : $SO_4^{2-}$, $Cl^-$, $HCO_3^-$ | Chandrashekhar[1059] | | | 0.001, 0.007 |
| Huang et al.[1058] | $H_2$ | Alavi[1060] | 20 | 333 | 1.5 and 3.5 |
| | $CO_2$ | Aimei et al.[926] | | | |
| | $CH_4$ | TraPPE[301] | | | |
| | $H_2O$ | OPC4[1061] | | | |
| | $Na^+Cl^-$ and | Yagasaki et al.[1062] | | | |
| | Quartz (Q2) | INTERFACE[1063] | | | |
| Ali et al.[1048] | $H_2$ | Buch[312] | 5−80 | 303−343 | 1.7 |
| | | Marx[310] | | | |
| | $CO_2$ | Cygan et al.[927] | | | |
| | $CH_4$ | [301] | | | |
| | $H_2O$ | SPCE[346] | | | |
| | $Na^+Cl^-$ and | Joung and Cheatham [371] | | | |
| | Kaolinite | [422] | | | |
| Chen and Xia[605] | $H_2$ | IFF[313] | 5 to 60 | 320 | 0 |
| | $H_2O$ | TIP4P/2005[1042] | (steps of 5) | | |
| | $SiO_4$ ($Q^2$ Silica) | INTERFACE[425] | | | |
| | $SiO_4$ ($Q^4$ Silica) | INTERFACE[425] | | | |
| Chen et al.[604] | $H_2$ | IFF[313] | 10 | 300, 400 | 0 and 2.22 |
| | $H_2O$ | TIP4P/2005[1042] | | | |
| | $SiO_4$ ($Q^2$ Silica) | INTERFACE[425] | | | |
| | Brine : $Na^+$ and $Cl^-$ | Madrid-2019[1034] | 10 | 300, 400 | NA |
| Al-Yaseri et al.[606] | $H_2$ (G) | IFF[313] | | 300 | |
| | $H_2O$ | SPC/E[346] | | | |
| | $Na^+$ | Aqvist[1044] | | | 0.5 |
| | $Cl^-$ | Chandrashekhar[1059] | | | 0.5 |
| | Humic Acid | OPLS-AA[360] | | | |
| | $SiO_4$ | CLAYFF[422] | | | |
| Al-Yaseri et al.[607] | $H_2$ | IFF[313] | 5, 20 | 300, 323 | |
| | $H_2O$ | SPC/E[346] | | | |
| | $Na^+$, $Ca^{2+}$, $Mg^{2+}$, | Aqvist[1044] | | | 0.001, 0.007 |
| | $Cl^-$ | Chandrashekhar[1059] | | | |
| | $SiO_4$ (S, Silica) | CLAYFF[422] | | | |
| | $CaCO_3$ (S, Calcite) | Xiao[1064] | | | |
| Yang et al.[602] | $H_2$ | IFF[1060] | 1 to 160 MPa | 298 to 523 K | 0 |
| | $H_2O$ | TIP4P/2005[1042] | | | |
| | $SiO_4$ ($Q^3/Q^4$ Silica) | INTERFACE[422] | | | |
| | $C_{175}H_{102}O_9N_4S_2$ (II-D, Kerogen) | CVFF[427] | | | |
| Zheng et al.[608] | $H_2$ | Three-site model[1060] | 1 to 30 MPa | 338 K | 0, 0.5, 1 |
| | $CH_4$ | OPLS-AA[360,1065] | | | |
| | $H_2O$ | SPC/E[346] | | | |
| | $Na^+$, $Cl^-$ | Joung and Cheatham[371] | | | |
| | $SiO_4$ (Quartz) ($Q^3/Q^4$ Silica) | CLAYFF[422] | | | |
| Zheng et al.[609] | $H_2$ | Three-site model[1060] | 1, 10, 20, and 30 | 338 | 0 |
| | $H_2O$ | SPC/E[346] | | | |
| | $SiO_4$ (S, $Q^3/Q^4$ Silica) | CLAYFF[422] | | | |
| Alshammari et al.[1049] | $H_2$ | IFF[313] | 0.1−70 | 293−373 | NA |
| | $CH_4$ | OPLS-AA[360,1059] | | | |
| | $CO_2$ | Cygan et al.[927] | | | |
| | $H_2O$ | SPCE[346] | | | |
| | $Na^+Cl^-$ | OPLS-AA[360] | | | |
| | $Mg^{2+}$ | Aqvist [1044] | | | |

**Table 20. continued**

| Study | System details | | Thermodynamic conditions | | |
|---|---|---|---|---|---|
| | Species | Force field | $p$ [MPa] | $T$ [K] | $c_{salt}$ [mol / L of solvent] |
| Barbosa et al.[1050] | Calcite | Xiao et al.[1064] | 10 | 323 | 20 wt% |
| | Silica | INTERFACE[1063] | | | |
| | $H_2$ | Buch[312] | | | |
| | $CO_2$ | Cygan et al.[927] | | | |
| | $CH_4$ | TraPPE[301] | | | |
| | $H_2O$ | SPCE[346] | | | |
| | $Na^+Cl^-$ | Joung and Cheatham[371] | | | |
| | Kaolinite (siloxane, gibbsite) | CLAYFF[422] | | | |
| Fatah et al.[1051] | $H_2$ | IFF[313] | 6.9 | 298.15 | NA |
| | $N_2$ | IFF[313] | | | |
| | $CO_2$ | Cygan et al.[927] | | | |
| | $CH_4$ | OPLS-AA[360] | | | |
| | $Na^+$, $Mg^{2+}$, $Ca^{2+}$ | Aqvist[1044] | | | |
| | $Cl^-$ | OPLS-AA[360] | | | |
| | $SO_4^{2-}$ | Cannon et al.[1066] | | | |
| Ghafari et al.[1052] | $H_2$ | IFF[313] | 10−30 | 333−413 | 0 |
| | $CO_2$ | Cygan et al.[927] | | | |
| | $CH_4$ | TraPPE[301] | | | |
| | $N_2$ | IFF[313] | | | |
| | $H_2O$ | SPC/E[346] | | | |
| | $Na^+Cl^-$ | Smith and Dang[374] | | | |
| | Silica | INTERFACE[1063] | | | |
| | | CLAYFF[422] | | | |
| | | DDEC[1067] | | | |
| | | BKS[1068] | | | |
| Phan et al.[1053] | $H_2$ | Lopez-Lazaro et al.[675] | 15 | 333 | 3.4 NaCl and 0.13 KCl |
| | $CO_2$ | EPM2[419] | | | |
| | $CH_4$ | TraPPE[301] | | | |
| | $H_2O$ | SPC/E[346] | | | |
| | $Na^+$, $K^+$, $Cl^-$ | Dang[1043] | | | |
| | Talc | CLAYFF[422] | | | |
| | Kaolinite | CLAYFF[422] | | | |
| Yao et al.[1054] | $H_2$ | IFF[313] | 14−150 | 323−423 | 0−5.4 |
| | $H_2O$ | TIP4P/2005[305] | | | |
| | $Na^+$, $K^+$, $Cl^-$ | CLAYFF,[422] Madrid-2019[1034] | | | |
| | Silica | INTERFACE[1063] | | | |
| Yu et al.[1056] | $H_2$ | Hirschfelder et al.[321] | 5−40 | 292−343 | |
| | $CO_2$ | CVFF[1069] | | | |
| | $CH_4$ | CVFF[1069] | | | |
| | $H_2O$ | SPC/E[346] | | | |
| | Graphene | Not mentioned | | | |
| Zhang et al.[1057] | $H_2$ | IFF[313] | 5−25 | 300-400 | 0−1 mol/L |
| | $H_2O$ | SPC/E[346] | | | |
| | Halite NaCl | Joung and Cheatham[371] | | | |
| | Quartz | CLAYFF[422] | | | |
| | Calcite | Xiao et al.[1064] | | | |
| | Montmorillonite | CLAYFF[422] | | | |
| | $Na^+Cl^-$ | Smith and Dang[374] | | | |

[a]The salt concentrations in brine are reported in units of molality, or kgs of salt per kg of solvent ($H_2O$). The gaseous (G), liquid (L) and the solid (S) phases and the respective force fields used to model the interactions between the like molecules are provided. The final column lists the thermodynamic conditions at which CAs were computed. Note that the salt concentrations reported by Barbosa et al.[1050] and Zhang et al.[1057] are in weight percentage and mol/L, respectively

such that its ratio with the water-$H_2$ IFT decreases, leading to a higher CA, consistent with Young's equation.

## 4.11. Atomistic Modeling of Hydrogen Embrittlement

HE poses a critical threat to structural integrity by severely degrading the ductility and toughness of metallic materials, leading to premature brittle fracture even under low external stresses. At the atomistic scale, HE involves several distinct, yet interconnected mechanisms, as shown in Fig. 71, all of which have been intensively studied using MD simulations.

H-enhanced decohesion (HEDE)[1070] occurs when H atoms segregate and accumulate at interfaces, GBs, and atomic-scale defects, significantly lowering the cohesive strength between
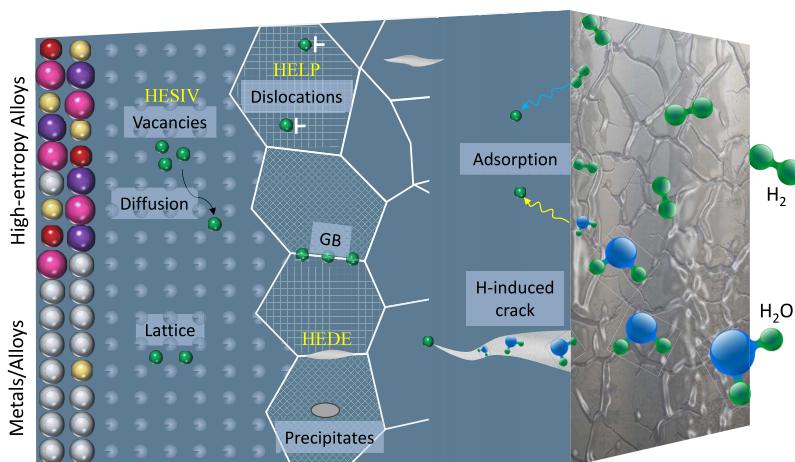
**Figure 71.** Illustration of hydrogen embrittlement mechanisms in high-performance materials (metals, alloys, and high-entropy alloys) with microstructural defects. Key processes include: (1) hydrogen adsorption, trapping, and diffusion; (2) hydrogen-defect interactions; and (3) the progression of hydrogen-induced damage. The figure emphasizes the interplay of these factors and their role in activating HE mechanisms, HEDE,[1070] HELP,[1071] HESIV.[1072]

atomic planes, and thus, promoting brittle intergranular or cleavage fracture. On the other hand, H-enhanced localized plasticity (HELP)[1071] describes the H-driven reduction of barriers for dislocation motion, leading to increased dislocation activity. While HELP initially facilitates plastic deformation, it ultimately results in severe strain localization and accelerated crack initiation due to locally intense deformation. Additionally, H-enhanced strain-induced vacancy formation (HESIV)[1072] emerges when H atoms stabilize vacancies, effectively lowering vacancy formation energies, which generates a higher density of defects and provides further preferential sites for crack initiation and growth. H also affects crack propagation dynamics directly by promoting dislocation emission or, conversely, inhibiting dislocation nucleation near crack tips, depending on the H concentration and the local stress state. Furthermore, H-dislocation interactions modify dislocation core structures and mobility, affecting overall material plasticity, fracture toughness, and resistance to fatigue crack growth. MD simulations uniquely enable direct visualization and quantification of these atomistic phenomena, providing detailed insights into the role of H at different length scales, defect configurations, and loading conditions. The complexity of H-induced effects is further magnified by the random and complex chemical environments, characteristic of high-entropy alloys (HEAs). For this reason, ML approaches have emerged as critical tools for navigating these complexities. In the following sections, we explore these mechanisms in detail and review the relevant literature.

**4.11.1. Atomic Hydrogen Diffusion in Metallic Materials.** H diffusion is critical for understanding and mitigating the detrimental effects of HE, as the migration of H atoms within the material microstructure precedes the degradation of mechanical properties. MD and KMC are commonly used to study H diffusion, with the simplest case being diffusion in a perfect lattice. For example, Zhou et al.[545] conducted a parametric study using MD simulations to investigate H diffusion in fcc Al (diffusion barriers and coefficients). This work provides a foundational reference for MD studies of H diffusion. However, MD simulations depend on empirical force fields, such as the EAM potential, which often lack sufficient accuracy as thoroughly discussed in Section 3.1. An alternative approach is KMC simulations with

predefined energy barriers obtained from DFT-based NEB calculations. A key advantage of KMC is the ability to incorporate ZPE corrections into the energy barriers, accounting for harmonic quantum effects. Yang and Oyeniyi[1073] performed KMC simualtions with ZPE−corrected barriers to study H diffusion in bcc W, achieving excellent agreement with experimental results. To fully capture quantum effects, e.g., proton tunneling, more advanced techniques such as PIMD and higher-accuracy force fields are required. Kimizuka et al.[546] demonstrated that in bcc Fe, quantum effects not only substantially reduce the H diffusion barrier but also alter the preferred diffusion pathway, even at room temperature.

Defects, such as vacancies, impurities, dislocations, GBs, and other interfaces play a critical role in H diffusion, as they significantly alter the energy landscape of diffusion pathways. MD simulations using EAM potentials have revealed key insights into these effects. The study by Zhu and Oda[1074] revealed that in bcc Fe, vacancies act as strong trapping sites, substantially reducing the effective H diffusivity. The authors showed that while bulk-dissolved H atoms dominate diffusion, trapped H at vacancies contributes negligibly to long−range diffusion of H. Similar suppression of H diffusion due to vacancies and dislocations has been observed in bcc W through MD simulations.[1075] The influence of GBs has also been extensively studied, particularly in nano-grained materials, where a large fraction of atoms resides near interfaces. Zhou et al.[1076] systematically investigated H diffusion in nanograined Fe by means of MD simualtions, and showed that decreasing grain size restricts H diffusion due to the increased density of triple junctions.

Beyond the inherent inaccuracies of empirical force fields, such as EAM, another critical limitation in modeling H diffusion near defects is the constrains of accessible time-scales by MD simulations. Given the femtosecond−scale time steps required to resolve H diffusion, an impractically large number of MD steps would be needed to capture diffusion near defects, particularly at room and low temperatures. To overcome these challenges, KMC simulations incorporating DFT-derived diffusion barriers have emerged as a powerful alternative for studying H-defect interactions. Implementing this approach requires either precomputing all possible H diffusion pathways
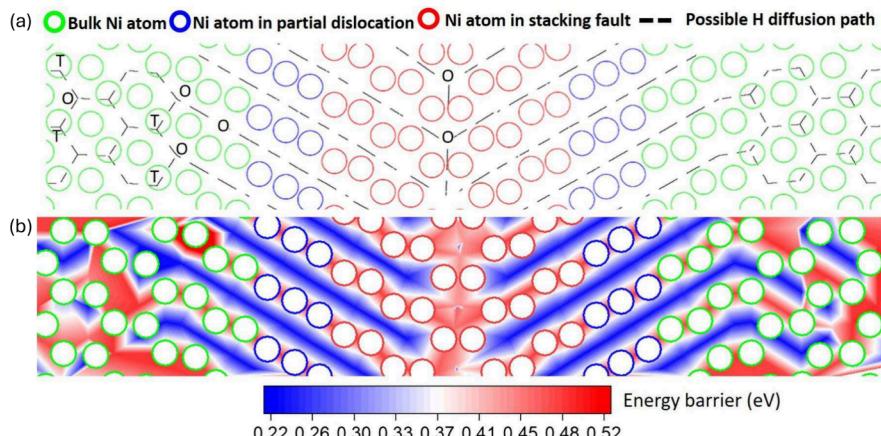
**Figure 72.** (a) Possible atomic hydrogen diffusion pathways on the glide plane and (b) the corresponding diffusion barrier contour map for an edge dislocation in fcc Ni. Octahedral (O) and tetrahedral (T) sites are indicated, with tetrahedral sites overlapping the host Ni atoms. Diffusion hops between adjacent sites are connected by dashed lines. [Reprinted from Acta Materialia, Vol 268, Xiao Zhou et al., Critical assessment of hydrogen pipe diffusion at dislocations in metals, 119758, Copyright (2024), with permission from Elsevier].

around defects to construct an event table for KMC or using advanced on-the-fly methods like the kinetic Activation-Relaxation Technique (k-ART) to dynamically identify diffusion paths during simulations. Zhou et al.[541] performed classical KMC simulations with DFT-derived barriers to investigate H diffusion across various GBs in fcc Ni. The authors demonstrated that high−angle GBs enhance H diffusion, whereas low-angle GBs hinder it. In a separate study, Zhou et al.[653] combined k-ART with KMC to examine H pipe diffusion along both edge and screw dislocations in fcc Ni (Fig. 72) and bcc Fe. This advanced computational framework enabled simulations spanning micro-second to second time-scales, revealing an unexpected suppression of H diffusion along dislocation cores, a phenomenon inaccessible to conventional MD simulations due to time-scale limitations.

From a methodological standpoint, both MD and KMC present distinct advantages and limitations for studying H diffusion in metals. MD captures the true dynamic evolution of the system, but its accuracy is inherently constrained by the quality of the force field. Moreover, MD becomes computationally prohibitive at low temperatures when high diffusion barriers necessitate excessively long simulation times. In contrast, KMC readily incorporates DFT−derived energy barriers with ZPE corrections, offering improved accuracy for H diffusion processes. Nevertheless, conventional KMC implementations neglect the temperature dependence of diffusion barriers and face two significant challenges: (1) the need to explicitly define all possible H diffusion pathways and the associated barriers within defective regions, and (2) the low−barrier problem where simulations may become trapped in local energy basins as discussed by Andersen et al.[650] These limitations underscore the urgency for advanced MD and KMC approaches capable of addressing such complexities in H diffusion studies. MLIPs (introduced in Section 3.1.5) show promise for addressing these challenges, combining accuracy and efficiency. A detailed discussion of these advanced methods will be presented in Section 4.11.7.

**4.11.2. Atomic Hydrogen Trapping and Hydrogen-Mediated Vacancy Behaviors.** H diffusion in metals and alloys is strongly governed by trapping phenomena, whereby H atoms become confined in sites with high escape barriers that retard their migration. These traps include interstitial impurities, such as carbon and nitrogen, substitutional solutes (e.g., Nb, Ti, Mg, Sc, and Y), intrinsic crystal defects including vacancies, nanovoids, dislocations, and GBs, and secondary-phase interfaces formed by carbides (TiC, $V_4C_3$, NbC, $Mo_2C$) or dispersed oxides, as reveled by Sagar et al.,[1077] Zhang et al.,[1078] Liu et al.[1079] and Wang et al.[1080] H trapping at GBs or precipitate−matrix interfaces can lead to HEDE, in which H reduces the cohesive strength of the GBs and the interfaces. DFT calculations and experimental measurements indicate that lattice defects (dislocations and GBs) and precipitates with coherent interfaces, typically exhibit trapping energies below 50 kJ/mol (often regarded as the reversibility limit), while semi- or incoherent precipitates can trap H much more strongly, with energies reaching up to 129 kJ/mol. For a thorough review of the available DFT and experimental studies the reader is referred elswhere.[1081]

H profoundly alters vacancy behavior in metals. The associated HE mechanism is known as HESIV, which hypothesizes that the density and clustering of vacancies is enhanced in the presence of H. Consequently, the vacancies can coalesce to form micro-voids, which in turn may combine to form larger voids leading to a decrease in ductile crack growth resistance. Hayward and Fu[544] combined MD and DFT to show that in bcc Fe, vacancy formation energies drop sharply as local H concentration increases, becoming negative at high coverage, and thus, provide an atomistic explanation for HESIV. Echeverri Restrepo et al.[1082] used parallel-replica dynamics alongside NEB calculations to quantify mono-vacancy diffusivity in bcc Fe with 0−3 H atoms. This study revealed that a single H raises the activation energy, slowing diffusion, whereas two to three H atoms lower the barrier, restoring or even enhancing vacancy mobility. Du et al.[1083] used a potential-of-mean-force method to investigate vacancies in Cu and Pd, and demonstrated that H enrichment at the saddle point (positive H Gibbs excess energy) lubricates vacancy migration, and significantly boosts diffusivity. These studies demonstrate that H creates superabundant vacancies by lowering formation energies, traps them at low coverage but enhances their diffusion at high coverage via saddle-point enrichment, and therefore, accelerates void nucleation and growth, leading to HE.

### 4.11.3. Dislocation Nucleation and Mobility.

H exerts a dual, system−dependent influence on incipient plasticity. In many fcc metals it facilitates dislocation nucleation by lowering the shear modulus, the line energy, and—when it enters the lattice—the intrinsic and extrinsic stacking-fault energies. These trends underlie the HELP signature reported by Barnoush and Vehoff[1084] during nano-indentation, where the first "pop-in" event is a direct measure of the nucleation of dislocation half-loops beneath the indenter. The MD study by Zhou et al.[547] refined this picture: in fcc Ni and Pd the pop-in load drops, primarily because interstitial H produces an isotropic lattice swelling that acts as a pre-strain, while little direct H−dislocation interaction is required. The GCMC simulations of Yu et al.[552] revealed that the H-induced increase in the core radius and decrease in the core energy of dislocations are the key factors affecting dislocation activities including dislocation nucleation, emission, mobility, and reaction that leads to HE. Equally well documented are cases where H suppresses dislocation nucleation. Early NEB calculations for fcc Ni crack tips performed by Wen et al.[1085] showed that adsorbed H raises the activation energy, and therefore, the stress-intensity factor for loop emission, an effect traced to a marked reduction in the activation volume when H decorates the embryo (i.e., the initial, critical-sized nucleus of a dislocation loop). Yin et al.[548] studied Ag−H nanowires both experimentally and by means of MD/NEB. The authors showed that surface−adsorbed H at ledges and steps increases the critical stress for loop formation, with the computed activation barrier rising accordingly. Here, H lowers the local surface energy, and relaxes the tensile stress concentration, effectively "locking" the most efficient surface sources. Using MD simulations coupled with NEB calculations, Li et al.[549] systematically elucidated the dual effect of H on dislocation nucleation: surface-segregated H raises the activation barrier, thus, inhibiting dislocation emission, while bulk-dissolved H lowers the barrier, thereby, promoting nucleation.

H can also profoundly alter the mobility of preexisting dislocations in metals, a topic that has been extensively explored using MD and other atomistic simulation approaches. Early DFT calculations combined with a line tension model by Itakura et al.[1086] showed that the effect of H on screw dislocation glide in bcc Fe depends sensitively on temperature, H concentration and applied stress. In that study, H both promoted kink nucleation, thereby softening the lattice, and trapped kinks behind the dislocation core, thereby producing a hardening effect. For a bulk H concentration of 0.1 parts per million (ppm), the softening window extended from ca. 200 to 300 K; at ten ppm it shifted to a range of 300 to 400 K. The subsequent NEB calculations and room temperature MD simulations of Yin et al.[548] confirmed these predictions. At a H line density of 0.4 per nanometer, the kink nucleation barrier decreased from 0.47 to 0.42 eV, and the critical shear stress for glide decreased from 32 to 22 MPa, consistent with experimental observations of H enhanced screw dislocation mobility. MD simulations by Song and Curtin[1087] revealed that H slows edge dislocation motion in bcc Fe by rapidly forming Cottrell atmospheres, which exert a strong solute drag effect over a wide concentration range. Kapci et al.[550] conducted GCMC simulations coupled with MD to further show that increasing the H concentration raises the critical stress required for edge dislocation depinning, underscoring the pervasive influence of H on dislocation based plasticity in Fe.

### 4.11.4. Crack Propagation and Grain Boundary Decohesion.

Song and Curtin[276] used atomistic MD and GCMC to show that, under stress, H concentrates at crack tips in single- and bi-crystal Ni to form nano-scale hydrides that suppress dislocation emission and inhibit crack-tip blunting. Song and Curtin[1088] then integrated H diffusion kinetics with criteria for dislocation emission and cleavage into a single nondimensional parameter that, without any fitting constants, predicts the ductile-to-brittle transition across different Fe-based alloys based on H concentration, temperature and loading rate. For fcc Ni, Tehranchi and Curtin[442] showed that H segregation reduces both the critical stress for dislocation emission and the cleavage fracture stress intensity at a range of GBs, yet under conditions of only initial equilibrium segregation, and no active diffusion, a ductile-to-brittle transition was not observed, and the Σ3(111) twin boundary remained essentially immune to HE. In a follow-up study, Tehranchi et al.[1089] explicitly coupled H nano-diffusion onto freshly-created crack surfaces with mechanical, thermodynamic and kinetic modelling to derive a quantitative, parameter-free criterion that predicts the onset of HE for both crack propagation and GB cleavage. The mechanistic and predictive frameworks developed in these studies are essential for guiding the design of HE−resistant materials. Jung et al.[553] conducted systematic MD simulations of crack propagation along GBs in bcc Fe, with and without H. The findings showed that the effects of H on crack growth vary significantly with GB character. Specifically, the Σ3 coherent twin boundary (CTB) markedly retards crack propagation, owing to its capacity to accommodate plastic deformation, indicating that CTBs can substantially enhance resistance to HE. These results under-score the promise of GB engineering as a strategy for improving materials resistance to HE.

Several atomistic MD studies have quantitatively assessed H−induced decohesion in Ni GBs. Tehranchi and Curtin[1090] systematically investigated 110 symmetric−tilt boundaries in fcc Ni, computing both the theoretical strength (rigid separation) and the yield strength (onset of dislocation emission), and showed that equilibrium H segregation has negligible impact on either metric. Li et al.[1091] extended this analysis to a broader spectrum of GB characters, reporting that, under equilibrium H coverage, the maximum tensile strength and fracture energy of the Σ5(210)100 and Σ17(530)100 boundaries decrease by only 6.6% and 15.8%, respectively. Crucially, by incorporating plastic deformation into the simulations, Li et al.[1091] demonstrated that the synergy between H−facilitated decohesion and dislocation activity can notably amplify embrittlement. Huang et al.[1092] further combined a polyhedral packing−unit identification of all interstitial trap sites with atomistic segregation energies and Rice−Wang thermodynamics to predict work−of−separation reductions under different fracture rates: in the fast−fracture (constant concentration) limit H lowers the work of separation by 10%, whereas the reduction approaches 50% in the slow-fracture (constant chemical potential) limit. Collectively, these works show that equilibrium H segregation alone weakens Ni GBs only modestly, while H diffusion kinetics and plasticity critically govern the full extent of HE.

### 4.11.5. Hydrogen Effects on Complex Deformations

MD simulations have become indispensable for clarifying how H modulates nanoscale plasticity and fracture. Focusing on dislocation-GB interactions, Adlakha and Solanki[1093] showed
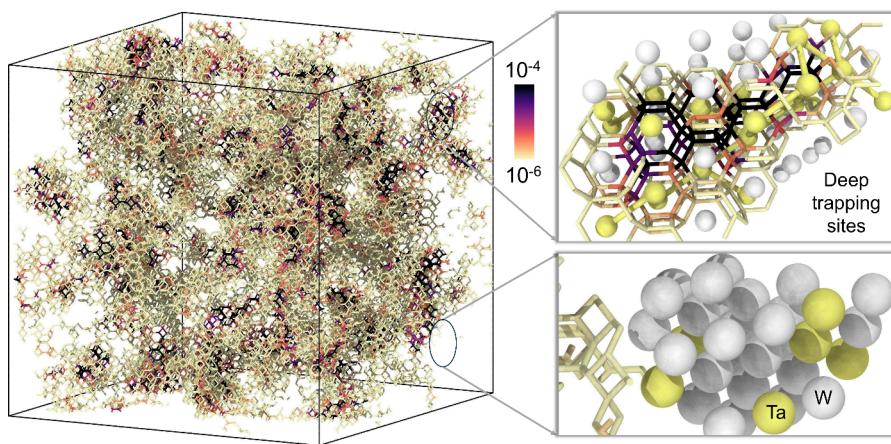
**Figure 73.** Visualization of H visitation frequencies at accessible tetrahedral (T) interstitial sites in $Ta_{20}W_{80}$ at 500 K. Frequencies are calculated by normalizing the visitation count of each T site by the total number of jumps in KMC simulations. The top-right and bottom-right panels highlight the metallic environments near trapping sites and inaccessible sites, respectively. H diffusion pathways between adjacent T sites are represented as atomic bonds. [Reprinted from Acta Materialia, Vol 289, Shuang et al.,[468] Decoding the hidden dynamics of super-Arrhenius hydrogen diffusion in multi-principal element alloys via machine learning, 120924, Copyright Elsevier (2025) (open access article distributed under the terms of the Creative Commons license - CC BY 4.0)].

that interstitial H raises the activation barrier for screw-dislocation transmission across 111 tilt GBs in bcc Fe. Using [110] symmetric tilt GBs, Li et al.[1094] showed that H shifts the reaction pathway from dislocation transmission to dislocation absorption, concomitantly increasing the initiation barrier. Tensile loading of H-segregated bicrystals conducted by Wan et al.[1095] further reveals complex coupled deformation mechanisms, providing an atomistic basis for embrittlement scenarios governed by dislocation-GB interactions. In polycrystalline models, the H effects on the mechanical properties become even richer. Zhou et al.[1096] demonstrated that decreasing the grain size in bcc Fe enhances resistance to HE, both by diluting H concentration at GBs and by activating a broader spectrum of GB-mediated deformation modes. For fcc Ni, Kuhr et al.[1097] observed an H-induced increase in yield strength at small strains, followed by accelerated dislocation emission from GB sources at larger strains. MD simulations of penta-twinned Ag nanowires by Yin et al.[548] revealed that surface-adsorbed H not only elevates the yield strength but also shifts the failure mode from distributed plasticity to localized necking. Surprisingly, MD simulations of HCP Mg polycrystals by Ji et al.[1098] revealed that H can enhance ductility without sacrificing strength.

From the perspective of multiscale modeling, Peng et al.[292] employed a concurrent atomistic−continuum (CAC) framework to simulate crack initiation at H-charged GBs in bicrystalline bcc Fe, bridging atomistic H diffusion, nanoscale GB cavitation/cracking, and mesoscale dislocation activity in a single model. The authors showed that tensile loading drives H toward the GB, where plasticity-induced clustering of H (PICH) acts as a mechanistic link between HELP and HEDE, greatly increasing local stress concentrations and weakening GB cohesion. Distinct failure modes emerge depending on GB character: Σ3 boundaries undergo micro-twinning−assisted void nucleation and coalescence, while Σ9 boundaries fail via crack initiation and growth concurrent with dislocation emission. By capturing long-range stress fields at sub-micron scales, their CAC simulations predict significantly lower GB cohesive strengths than conventional MD, and provides parameters for cohesive zone models, underscoring the necessity of multiscale simulation to reliably describe HE.

### 4.11.6. HE in High-Entropy Alloys

High-entropy alloys (HEAs), also known as multi-principal element alloys (MPEAs), have garnered significant research attention across various hydrogen-related fields, spanning H production, storage, and HE prevention. Recent experimental studies demonstrate exceptional HE resistance in HEAs, where H-charged specimens maintain higher strength while retaining comparable plasticity to their H-free counterparts (Luo et al.[1099,1100] and Li et al.[1101]). Two primary mechanisms have been proposed to explain this behavior: (1) significantly reduced H diffusion due to the complex chemical environment in HEAs, and (2) H-induced reduction in stacking fault energy, promoting stacking fault formation during deformation. These findings have spurred extensive investigations into H solubility, diffusion behavior, and deformation mechanisms in HEAs with H.

Unlike conventional metals and simple alloys, HEAs exhibit a non-uniform distribution of H solution energies even within an otherwise pristine lattice. The random spatial arrangement of multiple metallic elements produces a correspondingly random potential-energy landscape for interstitial H. DFT has therefore become the method of choice for quantifying site-to-site variations in solution energies and migration barriers. For equiatomic FeCuCrMnMo, Ren et al.[1102] demonstrated that the pronounced lattice distortion intrinsic to HEAs leads to large fluctuations in H migration barriers. In fcc FeMnCrCoNi, Xie et al.[1103] likewise reported a broad distribution of local solution energies; trapping in low-energy sites raises the effective diffusion barrier and thus slows long-range diffusion. Extending these insights, Yin et al.[1104] showed that chemical short-range order (CSRO) in fcc CrCoNi provides particularly deep traps, making CSRO an additional and tunable determinant of H diffusivity.

H diffusion in HEAs is inherently more intricate than in elemental metals. Because the governing timescales far exceed those accessible to direct AIMD, a variety of ML approaches have been developed to retain DFT-level fidelity at tractable cost. A comprehensive survey of ML techniques is given in Section 4.11.7. In fcc FeMnCrCoNi, Zhou et al.[654] trained ML models on DFT data to predict H solution energies and
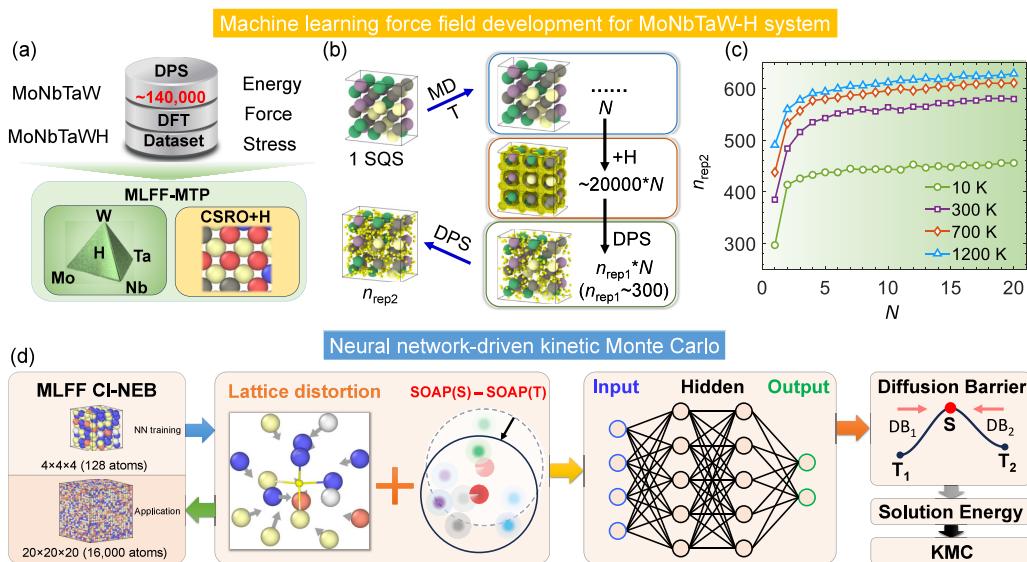
**Figure 74.** Machine learning-driven exploration of H diffusion with DFT-level accuracy. (a) Workflow for MLIP development. (b) Schematic of the distorted pathway sampling (DPS) method at various temperatures, where $n_{rep1}$ and $n_{rep2}$ denote selected configurations after initial and secondary DPS operations, respectively, and $N$ represents the number of distorted high-entropy alloy (HEA) configurations at temperature $T$. Large colored spheres indicate metallic atoms, while small yellow spheres represent H atoms. (c) Evolution of representative configurations ($n_{rep2}$) through a two-stage DPS process, showing the count of distorted HEA configurations ($N$) at different temperatures. (d) Neural network-driven KMC (NN-KMC) methodology flowchart. [Reprinted from Acta Materialia, Vol 289, Shuang et al.[468] Decoding the hidden dynamics of super-Arrhenius hydrogen diffusion in multi-principal element alloys via machine learning, 120924, Copyright Elsevier (2025) (open access article distributed under the terms of the Creative Commons license - CC BY 4.0)].

migration barriers within the random chemical environment; these energetics subsequently informed KMC simulations of long-range diffusion. Their analysis shows that H most stably occupies the octahedral site, while larger Co, Cr, and Mn fractions reduce the diffusion coefficient, whereas additional Fe or Ni has the opposite effect. In bcc MoNbTaW, Shuang et al.[468] integrated an MLIP, neural-network KMC, and symbolic regression into a unified framework capable of accessing experimental timescales for H diffusion. The study reveals a previously unreported super-Arrhenius temperature dependence, traced to the spontaneous emergence of nanoscale clusters enriched in H-favourable elements (Nb, Ta), as shown in Fig. 73. Disruption of these clusters by CSRO accelerates H diffusivity, thereby underscoring the critical interplay between local chemical order and diffusion kinetics.

H profoundly alters the deformation mechanisms and mechanical properties of HEAs. Using an EAM potential parameterized for FeNiCr-H, Zhou et al.[444] showed through extensive MD simulations that H statistically widens stacking faults by lowering both intrinsic and extrinsic stacking-fault energies. Building on the same potential, Guo et al.[1105] uncovered a dual influence of H on twinning: it facilitates homogeneous twin nucleation yet suppresses surface-initiated twinning. To provide higher-fidelity benchmarks beyond classical potentials, DFT calculations have long been employed. Xie et al.[1103] demonstrated that electron transfer from H to the lattice reduces both unstable and stable stacking-fault energies, thereby favoring deformation twinning. Systematic DFT calculations by Zhou and Curtin[1106] for 304/316 stainless steels and FeMnCrCoNi HEAs quantified H adsorption, surface energies, and GB fracture energies, illuminating the atomistic origins of HE resistance. The same DFT-guided strategy, coupled with mechanistic modelling, subsequently identified CoNiV as an exceptionally HE

resistant alloy.[1107] In a related study, Tan et al.[1108] showed that CTBs in fcc HEAs retard crack propagation and thus enhance HE resistance. To combine MD length- and time-scales with DFT accuracy, Zhou et al.[469] recently developed a MLIP for FeCoNiCrMn-H. Their simulations revealed that H lowers stacking-fault energy and promotes twinning, while dynamically formed local chemical ordering (LCO) traps H to create LCO−H complexes that pin dislocations more effectively than LCO alone. Moreover, segregation-induced Cr enrichment and Fe depletion at GBs raise the GB fracture energy, further improving HE resistance.

### 4.11.7. Machine Learning in Hydrogen Embrittlement Studies

The emergence of AI has revolutionized materials research (see also Section 4.6.2), with ML becoming a major tool for advancing our understanding of HE in metallic systems. ML techniques are transforming all aspects of HE research, spanning all scales from atomistic simulations of H diffusion to macroscopic predictions of mechanical properties in H-charged materials. Among various ML applications, the development of MLIP represents one of the most significant advances, enabling accurate large-scale simulations while maintaining near-DFT level accuracy. MLIPs typically require sophisticated ML architectures containing approximately $10^3$ trainable parameters that are optimized against extensive DFT datasets. Widely used MLIPs are the neural network potential (NNP),[460] Gaussian approximation potential (GAP),[461] spectral neighbor analysis potential (SNAP),[1109] moment tensor potential (MTP),[462] and atomic cluster expansion (ACE).[1110]

Kwon et al.[465] developed MTPs to investigate H diffusion in pristine bcc metals (Nb, Fe, W), using PIMD to demonstrate the significant influence of nuclear quantum effects below 500 K across a 100−1000 K temperature range. Similar progress in

fcc systems includes NNPs coupled with PIMD, which captured the quantum mechanical aspects of nonlinear H isotope diffusion in Pd.[464] The Bravais-Inspired Gradient-Domain Machine Learning (BIGDML) approach[1111] achieved comparable accuracy for H diffusion in Pd, while utilizing compact DFT datasets (10–200 structures). Other applications include H diffusion in hcp Mg and Ti hydrides using MTP, MACE, and CHGNet potentials.[466] Complementing these diffusion studies, Meng et al.[467] created a general-purpose MLIP for Fe-H systems capable of modeling diverse phenomena including surface processes, defect-mediated diffusion, and H-influenced plasticity.

Additionally, MLIPs have emerged as particularly powerful tools for investigating HE in HEAs, where they successfully capture the complex chemical interactions between H and multiple elements. The field advanced significantly through the work of Shuang et al.[468] who used D-optimality-based dataset construction to develop a high-accuracy MTP that comprehensively describes H-MoNbTaW interactions across the whole compositional space, including chemical short-range ordering effects (Fig. 74a-c). This MTP enabled the discovery of super-Arrhenius H diffusion behavior in bcc HEAs. Subsequent developments include a Deep Potential model capable of simulating coupled H diffusion and H-influenced plastic deformation in fcc FeMnCrCoNi HEAs, demonstrating the expanding capabilities of ML approaches for these challenging multicomponent systems.[469]

The significance of ML in HE studies extends beyond MLIP applications. Leveraging large-scale DFT datasets and the Sure Independence Screening and Sparsifying Operator (SISSO) algorithm, Korostelev et al.[1112] developed robust analytical models for accurate prediction of H absorption and migration energetics in metal alloys. For H diffusion specifically, Shuang et al.[468] implemented a neural-network KMC framework capable of computing hundreds of millions of DFT-accurate diffusion barriers (Fig. 74d), enabling unprecedented long-timescale simulations. The same work further applied SISSO to derive analytical models for H diffusivity in bcc HEAs, providing fundamental insights into diffusion mechanisms within complex chemical environments. Another work by Zhou et al.[654] established an ML−KMC framework to investigate H diffusion in fcc FeMnCrCoNi HEAs, employing whale optimization algorithms to identify atomic configurations with minimized H diffusivity. Tang et al.[1113] developed a reinforcement learning−guided transition kinetics simulator and a low-energy state sampler that leverage neural networks to predict transition rates, automatically uncovering the most probable diffusion pathways without explicit barrier calculations and enabling efficient long-timescale atomistic simulations.

# 5. CHALLENGES AND FUTURE OUTLOOK

## 5.1. Future Considerations on Molecular Simulation of Hydrogen in Geological Formations: From Molecules to Reservoir-Scale

Accurate prediction of $H_2$-brine IFTs, adsorption energies, and transport properties requires high-quality experimental data, mainly for training force fields and validating MD simulations. Based on, but not only limited to, our analysis of the available molecular simulation literature reviewed in Sections 4.7.1, 4.9, and 4.10, significant discrepancies in MD results can be seen. These often stem from the varying treatment of electrostatic interactions, cut-off distances, choice of force fields, surface model, all of which must be carefully validated against experiments. These discrepancies become more pronounced when modeling multicomponent systems (e.g., $H_2$ mixed with $H_2O$, $CO_2$, $CH_4$, and $N_2$) across an extended range of pressures, temperatures, and salinities. Therefore, a key research direction that we are confident should be explored in the future is the systematic investigation of IFTs, contact angles, and other interfacial properties under varying conditions, using both MD simulations and experimental measurements to refine interaction parameters. In parallel, ML methods, such as the approach demonstrated by Omrani et al.[1114], show great potential for developing predictive models that capture the dependencies of e.g., IFT on gas composition, thermodynamic conditions, and salinity. Nevertheless, robust experimental datasets for a wide range of $H_2$ properties (both for the pure component and mixtures) remain essential to validate these computational frameworks, ensuring accuracy and applicability for real−world processes such as UHS and $CO_2$ sequestration.

A thorough understanding of $H_2$ wettability in subsurface environments requires accurate experimental measurements, molecular modeling, and reservoir-scale simulations. Although significant progress has been made in molecular modeling, particularly in the parameterization of force fields and the characterization of mineral surface functionalities, important challenges remain. Addressing these is crucial for advancing $H_2$ storage technologies and improving our predictive capability of $H_2$ behavior at reservoir-scales. Some existing studies have already highlighted discrepancies in pressure-dependent behavior (e.g., Alavi[336] vs. IFF Wang et al.[313] models). Thus, future work should focus on systematically validating and refining force fields, especially for high-pressure regimes, against comprehensive experimental datasets. Efforts could include re-parameterizing $H_2$ models to better capture the pressure sensitivity observed in $H_2−H_2O$ interfacial systems. Also, many simulations assume uniform silanol distributions (e.g., $Q^2$, $Q^3$, $Q^4$). This approach, although providing a simple foundation, it does not reflect the actual rock surfaces (i.e., natural formations exhibit heterogeneous surfaces and multi-mineral interfaces). Extending MD simulations to capture such compositional complexities spanning organic matter, multivalent ions, and varying functional-group densities, will yield more accurate predictions of in-situ wettability. Discrepancies between simulation papers in contact-angle computations (e.g., $Q^2$ silica) emphasize the importance of robust sampling and sufficient equilibration. Although some experimental data exist for $H_2−H_2O$−solid contact angles, coordinated efforts where experiments and simulations target identical minerals, surface treatments, and thermodynamic conditions are urgently needed. Such collaborative studies would reduce uncertainties in force-field validation and identify key parameters controlling $H_2$ wettability under realistic subsurface conditions.

While molecular simulations have greatly helped the community in understanding the intrinsic $H_2 − H_2O −$ solid interactions, they are still almost exclusively performed in ideal, nm-scale slit pores or on perfectly flat crystal faces. Since molecular simulation cannot reach the cm-scale representative elementary volumes (REVs), multiphase transport modelling cannot be accurately performed. Natural reservoir rocks exhibit tortuous pore networks, angular throats, surface roughness, and mosaics of mineral and organic coatings. Together these features generate broad, hysteretic distributions of apparent

contact angles that may depart markedly from the single, intrinsic value obtained on a smooth, chemically uniform surface.

Lastly, it is important to point out is the scarcity of atomistic work on dynamic phenomena directly relevant to $H_2$ storage, e.g., advancing/receding contact angles, meniscus motion, and capillary trapping. In classical MD, Newton's equations of motion are integrated and momentum is conserved, thereby, recovering Navier−Stokes hydrodynamics at the nm−scale. Thus, MD could in principle capture such processes without added constitutive assumptions. However, in practice, the required length− and time−scales are prohibitive since even a simple cylindrical pore with a length of a few mm would contain on the order of billions of atoms. Moreover, the reliability of existing force fields for transient, far-from-equilibrium configurations, such as rapidly moving three-phase contact lines, has not been evaluated. Systematic benchmarks that compare dynamic contact angles and capillary entry pressures predicted from MD with well-controlled microfluidic experiments, are therefore, urgently needed (even before tackling complex rock geometries). In practice, this means using MD to supply key inputs such as the variation of interfacial tension and contact angle with pressure, temperature, and fluid composition to larger-scale solvers (e.g., pore network, lattice Boltzmann, or volume-of-fluid models) that run on cm−scale digital rock geometries. Reliable predictions of $H_2$ migration, trapping efficiency, and long−term storage security in geological formations are only possible if the atomistic inputs are carefully validated and combined with simulations at the pore scale and continuum, while guided by experiments.

## 5.2. Machine Learning Perspective on Atomistic Modeling of Hydrogen Embrittlement

ML has significantly advanced our ability to study H diffusion and HE in metals and alloys by providing interatomic potentials that approach first-principles accuracy. As discussed in Section 4.11.7, traditional studies have largely relied on empirical force fields, most commonly variants of EAM or modified EAM potentials, to describe H-metal interactions. While these potentials can capture qualitative trends, they often fail to reproduce quantitatively accurate H binding energies and diffusion barriers, particularly in the presence of crystalline defects such as vacancies, dislocations, and GBs. The emergence of MLIPs, such as NNP,[460] GAP,[461] SNAP,[1109] MTP,[462] and ACE,[1110] has begun to address these shortcomings. By training on diverse data sets of H-metal atomic configurations (drawn from DFT), MLIPs can reliably predict H interactions with pristine lattices and with a variety of defects. In practice, this means that vacancy formation energies, dislocation core structures, and GB binding sites can be characterized with near-DFT accuracy, enabling more predictive modeling of H diffusion coefficients and embrittlement mechanisms.

One major challenge in developing MLIPs for H-metal systems is adequately sampling the vast configurational space that arises from complex H-metal environments—particularly around defects and during dynamic processes. Domain expertise alone cannot exhaustively enumerate all relevant local environments. Active learning techniques, which iteratively identify and add the most informative new configurations during MD, have proven useful in accelerating potential development.[1115] More advanced strategies, such as

uncertainty−driven active learning, further enhance efficiency by focusing the sampling on rare events and underrepresented local environments,[1116] thus, reducing the total number of required DFT calculations. An alternative sampling strategy is to generate a broad, pre-computed pool of H-metal configurations before any DFT calculations are performed.[466] Universal MLIPs (uMLIPs) can serve as "sampling engines", driving MD simulations at scale to explore configurational space. Table 21 provides a list with the most important

**Table 21. State-of-the-Art uMLIP Architectures and DFT Datasets**

| Architecture | Organization | Dataset | # of structures |
|---|---|---|---|
| M3GNet[1117] | UC San Diego | MPtri | 1.58M |
| CHGNet[1118] | UC Berkeley | | |
| MACE[1119] | University of Cambridge | Alex(sAlex) | 30.50M |
| Orb[1120,1121] | Orbital Materials | | (10.45M) |
| MatterSim[1122] | Microsoft Research AI for Science | OMat24 | 100.82M |
| GRACE[1123] | ICAMS, RUB | | |
| SevenNet[1124] | Seoul National University | MatPES-PBE | 40M |
| DPA3[1125] | AI for Science Institute, Beijing | | |
| eqV2[1126] | FairChem at Meta | MatPES-r2SCAN | 40M |
| eSEN[1127] | FairChem at Meta | | |

uMLIPs to date, along with information of the associated datasets and archtectures. Although these uMLIPs do not match the accuracy of DFT, they excel at rapidly producing physically relevant atomic structures. Once a diverse pool of configurations is generated, single-point DFT calculations on these snapshots suffice to train a specialized H-metal MLIP, streamlining the workflow.

uMLIPs are MLIPs trained on extensive datasets spanning diverse elements, chemical environments, and material classes. Unlike specialized MLIPs (e.g., ACE or MTP) tailored to specific systems, uMLIPs prioritize broad transferability, achieved through training on hundreds of millions of DFT-labeled structures and architectures with hundreds of millions of parameters. Despite their general-purpose nature, modern uMLIPs can approach the accuracy of specialized MLIPs,[1128] enabling applications ranging from high-throughput materials screening to defect dynamics simulations. Prominent uMLIPs include M3GNet,[1117] CHGNet,[1118] Orb,[1120,1121] eqV2,[1126] MACE,[1119] DPA3,[1125] SevenNet,[1124] MatterSim[1122] and eSEN,[1127] all built on comprehensive DFT collections exceeding one hundred million structures. These collections include the Materials Project trajectory (MPtrj) dataset with 1.58 million structures,[1118] the Alexandria (Alex) dataset with 30.5 million structures or its subsampled version sAlex with 10.45 million structures,[1129] as well as the Open Materials 2024 (OMat24) dataset with 100.82 million structures.[1126] Whereas MPtrj and Alex (sAlex) focus primarily on near equilibrium configurations, OMat24 emphasizes far from equilibrium structures, making it the most extensive inorganic materials dataset to date. More recently two new datasets computed with the Perdew Burke Ernzerhof (PBE) functional (MatPES-PBE) and the revised regularized strongly constrained and appropriately normed (r2SCAN) functional (MatPES-r2SCAN) have become available to further improve consistency and accuracy of next generation uMLIPs.[1130] Among current models, the eqV2 and eSEN variants trained

on OMat24 by the FairChem group at Meta rank among the best for modeling general defects and hydrogen–metal interactions.[1128] These developments underscore the transformative potential of uMLIP-driven computational modeling in the materials science community by delivering accuracy comparable to DFT and enabling high fidelity predictions of H related trapping, embrittlement, storage and production processes at unprecedented scales.

The main limitation in developing specialized MLIPs is the vast amount of DFT data required, while uMLIPs face inference-speed constraints that typically limit them to systems of tens of thousands of atoms.[1131] A promising avenue to overcome both challenges is model distillation—deriving a smaller, task specific MLIP from a pretrained uMLIP can bypass much of the DFT sampling effort.[1132] The critical challenge which lies here is quantifying the uncertainty of uMLIP predictions in order to ensure that the distilled model inherits accurate energy and force predictions without introducing significant errors. Developing robust uncertainty metrics for uMLIPs will therefore be essential. Furthermore, ML techniques extend beyond interatomic potentials to higher-level property predictions. For example, supervised learning models can predict H-trapping energies and migration barriers directly from local structural and chemical descriptors. This capability is especially valuable for studying H diffusion and trapping in complex alloys—such as random solid solutions and HEAs, where enumerating every local environment and associated DFT calculation becomes impractical.[468] By combining ML-based property estimators with MLIPs, the community can build multiscale frameworks that predict H diffusion, trapping, and HE susceptibility in real-world engineering alloys with unprecedented accuracy.

## 5.3. Challenges in Force Field and Method Development for Predicting Properties of Liquid Hydrogen and Hydrogen Bubbles

This review highlighted many studies investigating the bulk fluid behavior of $H_2$. Based on our survey and analysis, clear knowledge gaps can be identified. Some of these gaps are especially relevant for technological applications and, thus, of interest to the chemical industry. Such a case is molecular modeling $H_2$ liquefaction. This requires force fields that can accurately capture phase transitions and the ortho-to-para conversion of $H_2$. To achieve this accuracy, a force field should automatically adjust the interaction parameters, for example as a function of the temperature. Classical models with such features could be inspired by the approach of Buch,[312] which uses a quadrupole interaction term to model $H_2$ at very low temperatures (1 to 3 K) (see Section 3.1.1). MLIPs can also provide approaches to simulate this behavior. Recent advances in MLIPs for magnetic materials resulted to inter-atomic potentials that are spin-state aware.[1133] A similar approach could provide accurate predictions of the ortho-to-para conversion as this would directly address the physical change within the $H_2$ molecule. Such an advanced model can then be combined with PIMD techniques to predict $H_2$ properties relevant to $H_2$ liquifaction and transport (i.e. heat capacity, thermal conductivity, viscosity, self-diffusion).

While the main focus of this review is on classical simulation methods of $H_2$, we are convinced that MLIPs will blur the barrier between classical and quantum simulations. MLIPs allow for large scale simulations of reactive systems, the modeling of which was limited to AIMD simulations. Recent

studies into Grotthuss transfer in water[105,1134−1137] have shown that MLIPs show a great potential in studying reactive systems. These studies revealed that both the details of the Grotthuss transfer events (i.e., energy barriers, local environment required for Grotthuss transfer), as well as the effects of these reactions on transport properties (i.e., self-diffusion coefficients and electrical conductivities) can be predicted. As discussed in Section 4.1.6, the electro-osmotic drag of $H_2$ in nafion membranes also requires accurate modeling of Grotthuss transfer. Only the study by Choe et al.[129] showed success in computing the EOD, as it combined AIMD and classical MD methods. Reactive MLIPs could provide a more efficient way to compute the EOD for larger system sizes. This will accelerate the simulations by orders of magnitude, and could lead to optimized membrane designs where the structure of the membrane promotes Grotthuss transfer, while minimizing the drag the $H_2$ experiences from the membrane.

$H_2$ dissolution in aqueous solutions is another area of great interest for advancing $H_2$ economy (e.g., for water electrolysis, subsurface storage, fuel cells). The development of fast polarizable force fields for $H_2$, $H_2O$, and ions (such as the water force field) can lead to accurate descriptions of $H_2$ bubble formation in aqueous electrolyte solutions. Capturing bubble formation provides valuable insight into the amount of water that can be dissolved in $H_2$ gas. The pressure inside $H_2$ bubbles is the highest at the moment of formation, as it inversely scales with bubble radius. Rahbari et al.[110] demonstrated that water solubility in $H_2$ decreases with increasing pressure, making the initial stages of bubble formation critical for predicting water impurities in the $H_2$ gas produced by the electrolyzer. Accurate molecular simulations if bubble formation under varying electrolyte compositions can lead to better informed design decisions for electrolysis setups. While MLIPs have shown great promise, we believe that there are still fundamental challenges that need to be addressed before MLIPs can be used in such simulations. Simulating bubble formation requires large systems, and while MLIPs provide significant speed-up compared to AIMD, they still require significant computational resources compared to classical force fields. Additionally, the long-ranged interactions in such systems pose challenges for MLIPs, since many of them implement a (smoothened) cut-off distance for all inter-atomic interactions. This leads to inaccuracies in systems where electrostatic interactions are dominant.[1138] Some support for long-ranged interactions has been implemented into several MLIPs.[1138−1140] Further development into MLIPs with less computational requirements, while maintaining the accuracy of the long-ranged interactions, is needed to make MLIPs suitable for simulating bubble formation in aqueous solutions. Lastly, MLIPs require accurate DFT data to train the model. While modern ab initio exchange correlation functionals (i.e. metaGGA and hybrid density functionals) have shown great improvement, they still have significant limitations. Recent studies showed that MLIPs trained on metaGGA functionals yield accurate trends in the computed properties. However, a relatively constant shift in temperature is observed with computations using MLIPs, for example in viscosity[1141] or melting temperature.[1142] While theses MLIPs are useful for predicting trends or providing insight into the underlying physics, they might not yet be suitable for predicting properties for industrial applications. Therefore, for MLIPs to become more broadly applicable, a key breakthrough will be the development of training frameworks that incorporate both

DFT data and experimental measurements instead of relying on more and more accurate and expensive DFT methods.

## 5.4. Pathways to Advance Research on Hydrogen Hydrates through Molecular Simulation

As thoroughly discussed in Section 4.8, molecular simulation is an indispensable tool for studying $H_2$ hydrates. As such, advancing $H_2$ technologies utilizing hydrate systems can be aided by exploring novel simulation routes. For example, investigating hydrate structural effects as a result of using different promoters could lead to increased $H_2$ storage capacities. Such studies can be coupled with conventional/ novel crystal engineering approaches and techniques. The partial replacement of $H_2O$ molecules by another species could result in modifying the lattice in way that larger cages could provide increased storage capacity. Other routes towards increasing $H_2$ storage capacity in hydrates are the screening of hypothetical structures (following the example of nanoporous materials such as MOFs and zeolites) and developing techniques which can reduce $H_2$ "leakage" rate out of the hydrate structure. Reducing the number of faces in a given hydrate crystal would function towards the reduction of "leakage". Alternatively, the use of certain ice structures could provide a solution, since channels can be more efficient storage structures than cages with faces. Studying the effect of flexible cages on $H_2$ storage capacity and leakage with molecular simulations, is another promising route.

To reliably predict thermophysical properties of hydrate systems requires a multi-scale approach, i.e., from the atomistic up to the continuum-level. To this end, developing hybrid computational tools, which couple multi-scale modeling methods is essential. Such tools can incorporate information obtained from ab-initio calculations, classical molecular and coarse-grained simulations, and ML predictive methods (e.g., using MLIPs (see also Sections 3.1.5 and 5.2) and/or physics-informed ML approaches).

Other promising future directions for molecular simulation research on $H_2$ hydrates are the investigation of confinement effects on the kinetics and thermodynamics of pure and mixed $H_2$ hydrate in solid materials, systematic exploration of semiclathrates and hydrate-based $H_2$ + $CO_2$ gas mixture separations, and coupling hydrate formation/dissociation with industrial processes such as LNG gasification and desalination.

## 5.5. Importance of Open-Source Software for Studying Properties of $H_2$ in Polymeric and Composite Materials

Evidently, the vast majority of the studies reviewed in Section 4.4 were conducted using commercial software (mainly Materials Studio[1143]). The use of commercial software instead of open-source comes with advantages and disadvantages. Major advantages are the ease of setting systems up (which is especially useful in the study of polymers and other highly viscous systems), the available pre- and post-processing options, access to a user interface (which may be particularly important in a corporate setting), professional support, and the overall less steep learning curve compared to an open-source code. Additionally, commercial software, such as Materials Studio[1143] and MAPS,[1144] provides access to proprietary force fields (e.g., COMPASS[316]). However, the relatively high price and the inaccessibility to the source code, and therefore, the inherent limitation in expanding, debugging, or modifying the scientific software, are the major drawbacks of commercial molecular simulation codes.

Another important point to consider is that since the early days of molecular simulation, algorithms and methods have been developed with an open-knowledge/source mentality, and mainly financed via national funds in United States and EU. Later on, when molecular simulations became more popular and commercial software arose, these algorithms and methods were incorporated in proprietary software. A characteristic example is the pioneering work by Theodorou and Suter,[1145−1148] who developed efficient methods for modeling polymeric systems, essentially allowing for the creation of initial configurations and relaxation of long hydrocarbons. Another, broader, example showcasing how open-source can aid the progress in the simulation community is LAMMPS,[473,475] one of the most widely used MD simulators, which is maintained by Sandia National Laboratories. As a final remark, codes such as LAMMPS and GROMACS,[476,477] being open to modification and enrichment by the simulation community worldwide, usually offer high performance, a plethora of features, access to new methods sooner, and easier implementation of new force fields compared to commercial software. Therefore, open-source software is considered one of the cornerstones of the molecular simulation field. The expansion and maintenance of open-source software should continue to be a priority of both research universities and governmental education bodies.

## 5.6. Transparency and Reproducibility in Molecular Simulation Workflows

In our review, we encountered several challenges related to the clarity and consistency of force field parametrizations in the literature of $H_2$ molecular simulation. In some studies, the rationale behind the choice of molecular models or interaction parameters was insufficiently explained. While such choices may be driven by computational efficiency, availability in simulation packages, or alignment with specific properties (e.g., density, viscosity, or interfacial tension), a clear and explicit justification is essential for scientific transparency. Ideally, this should include reference to the properties against which the force field was tuned, as well as known limitations in transferability or range of validity. Moreover, we observed that some studies do not cite the original source of the force field, but instead reference secondary literature that cited the original work. A notable example is the widely used force field from Hirschfelder,[321] which in its original formulation includes four different parameter variants (see relevant discussion in Section 3.1.1). In cases where studies cite a derivative reference rather than the primary source, it remains unclear whether the authors are fully aware of the specific force field variant used or its original context. We strongly recommend that future studies consult and cite the original work when reporting force field parameters and their origin, to ensure both scientific accuracy and reproducibility.

Another critical issue we observed is the limited availability of raw simulation data. While some studies commendably include detailed results (in tabulated or other form) along with uncertainty estimates, others provide only plots with densely populated data points and no accessible underlying values. This practice significantly hampers reproducibility, introduces uncertainty in data extraction, and complicates efforts to benchmark or validate results across independent studies. We therefore advocate for rigorous data reporting standards, wherein all key outputs (e.g., pressure, energy, interfacial tension, contact angle, diffusion coefficients) are made

available in machine—readable formats, along with metadata describing simulation settings. Such transparency not only enhances the credibility of the published work but also prevents unnecessary duplication of computational efforts in future studies. Promoting reproducibility and interpretability through open, well—documented datasets is essential if molecular simulation is to serve as a reliable and cumulative tool for advancing H$_2$ technologies.

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