

## Patterned grid-shell

Designing a method to analyse and compare grid-shell influenced by traditional lattice patterns of north Asia.



*An attempt to embrace native design characteristics in contemporary architecture with the help of modern designing and simulation techniques*



*An attempt to embrace native "design characteristics" in contemporary architecture with the help of modern designing and simulation techniques*

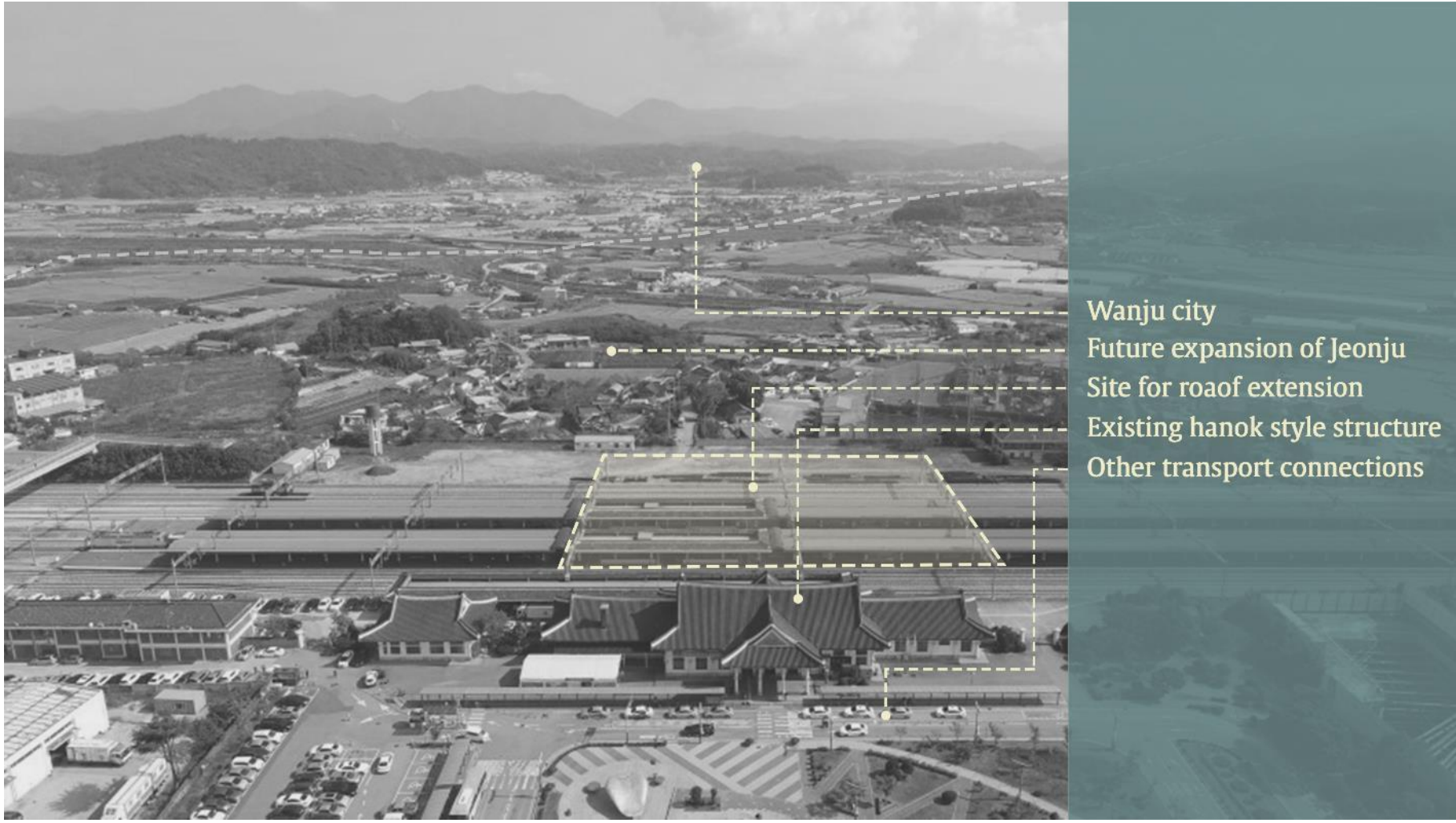


*An attempt to embrace native "traditional art" in contemporary architecture with the help of modern designing and simulation techniques*



[Project Scope, 2019]

Jeonju, train station, South Korea



Wanju city  
Future expansion of Jeonju  
Site for roof extension  
Existing hanok style structure  
Other transport connections

Jeonju, train station, South Korea



[Jeonju Hanok Village, 2019]



[Jeonju travel blog , 2018]



[Jeonju travel blog , 2018]



[Jeonju travel blog , 2018]

## Jeonju Hanok village

### Form



[Pxhere, n.d.]

Hanok style shelter drives human vision to sky

### Colours



[Pxhere, n.d.]

Colours highlights and distinguishes building elements

### Lattice



[Pxhere, n.d.]

Minimal space configuration dramatized with patterns of lattice frames of window

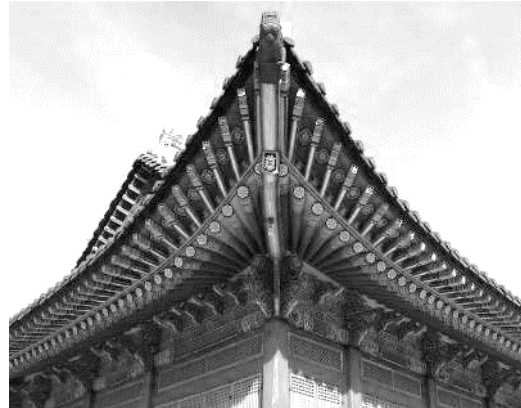
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Key design features





[Pxhere, n.d.]



[Pxhere, n.d.]



[Pxhere, n.d.]

## Lattice

Minimal space configuration dramatized  
with patterns of lattice frames of window

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Key design features



[CHANG, n.d.]



[Pxhere, n.d.]

## Lattice

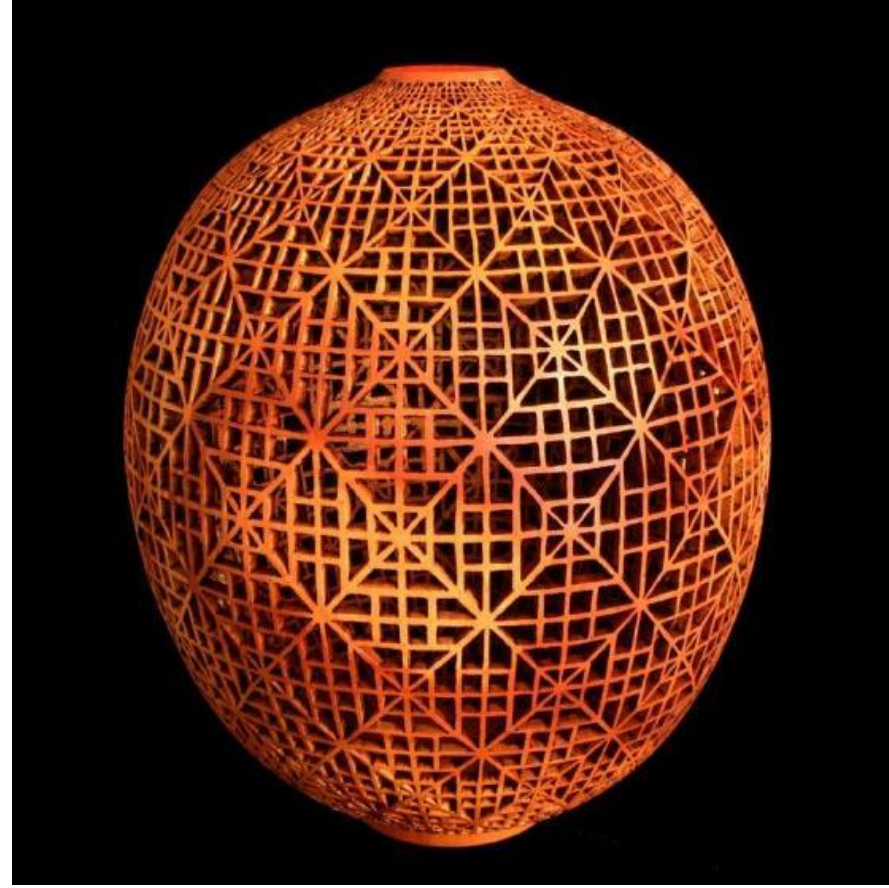
Minimal space configuration dramatized  
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Key design features



[Fennell, n.d.]

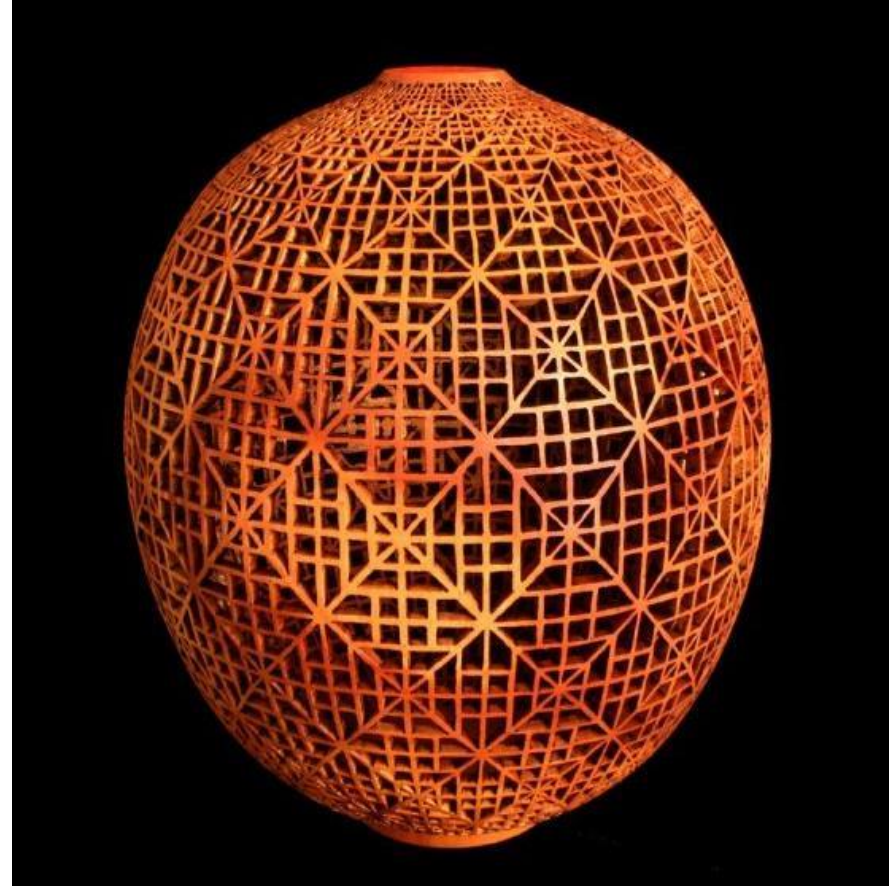


[Fennell, n.d.]

## Inspiration

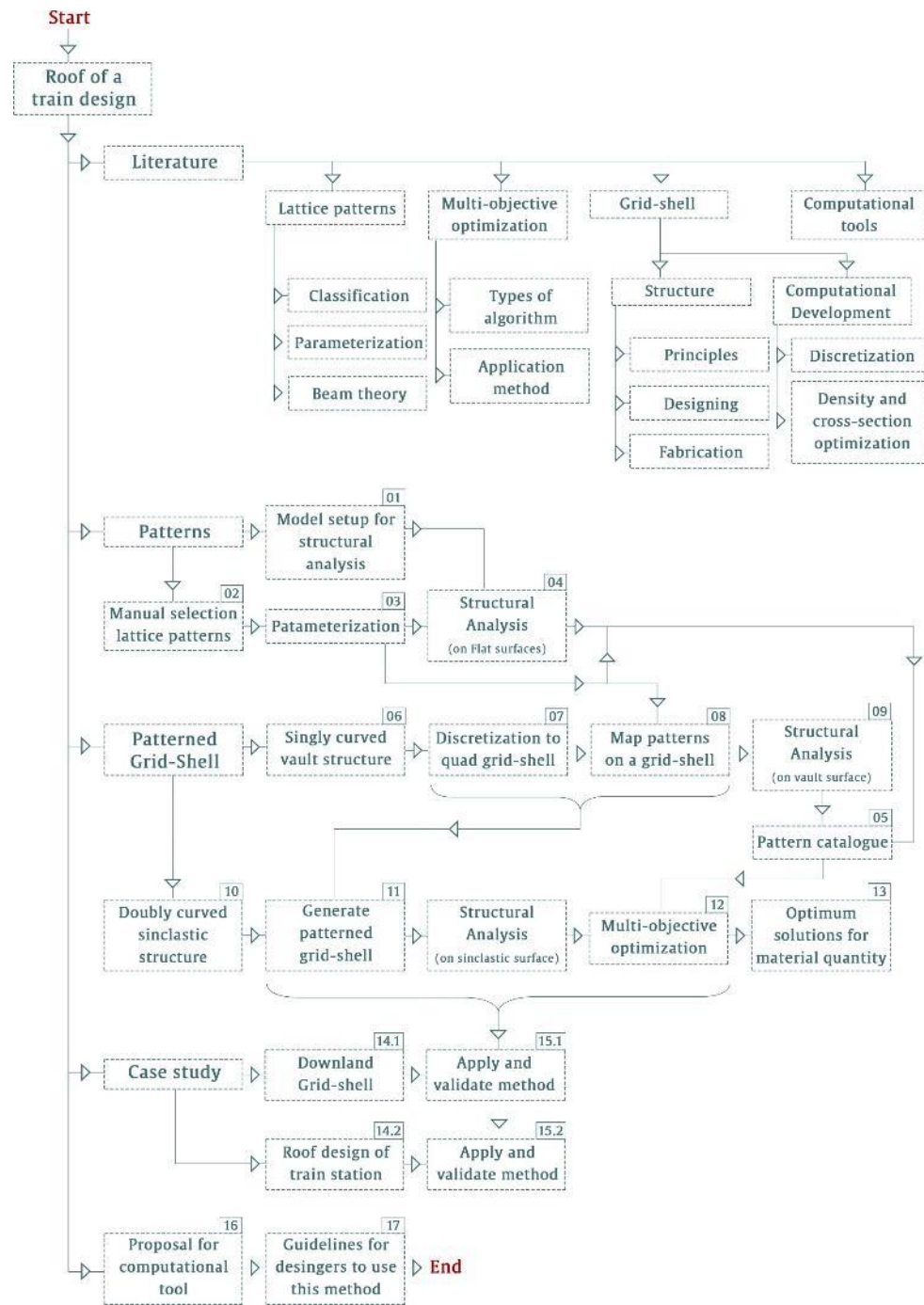


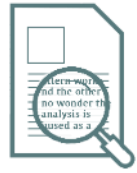
[Fennell, n.d.]



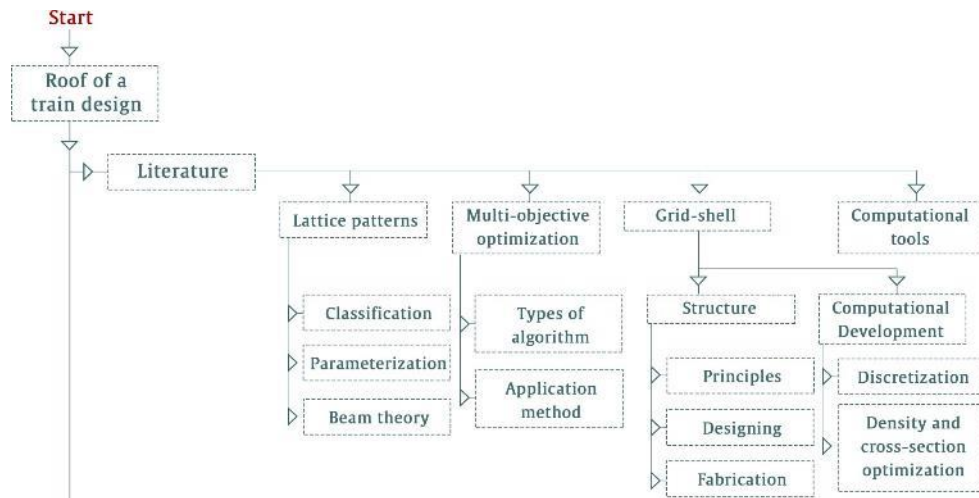
## Inspiration

## Graduation plan

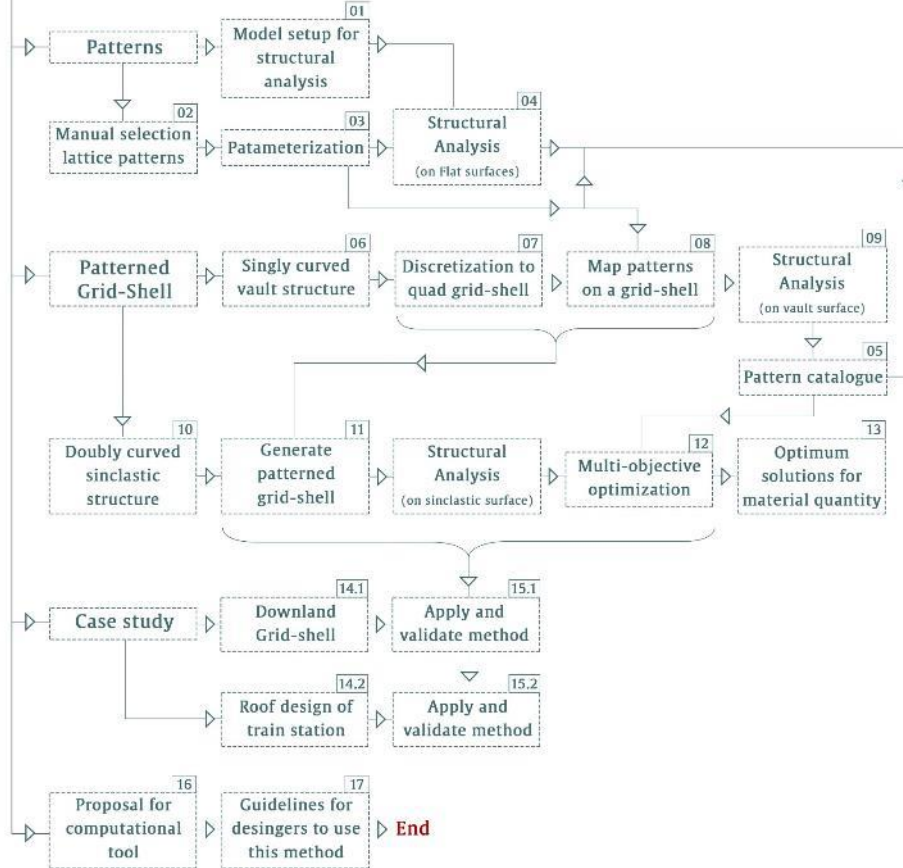




Literature research

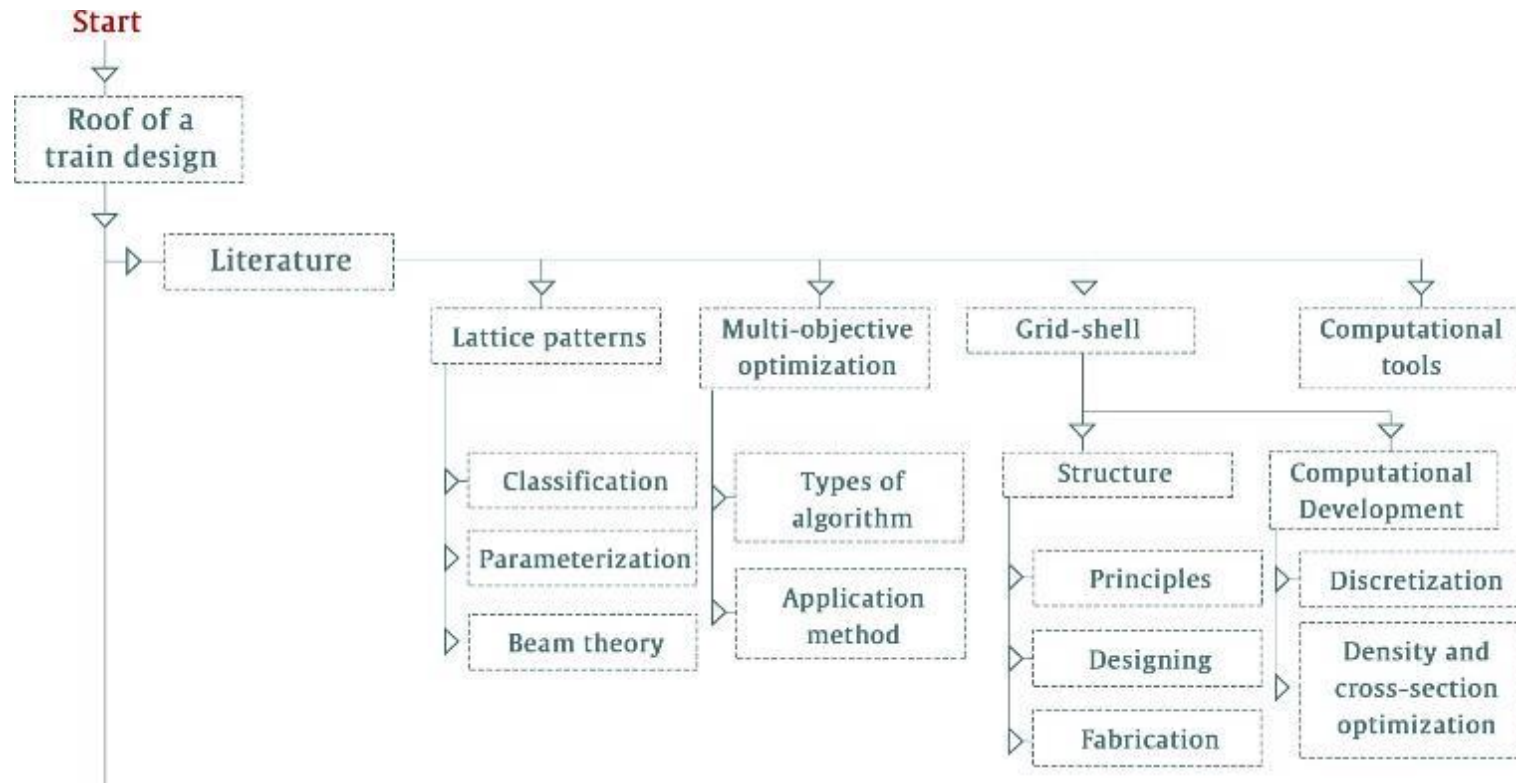


Project Development





## Literature research





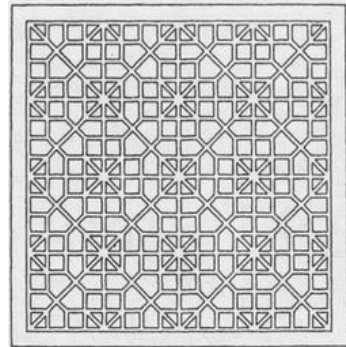


## Lattice designs

### Chinese lattice designs:

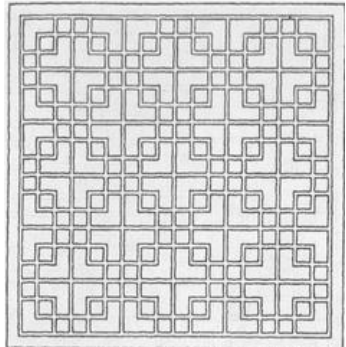
- 3000 years old art
- Evolved in China and North-East Asian plateau
- 300+ patterns collection
- Classified in 26 different types based on geometry and symbolic values.

B. Octagon (B10a)



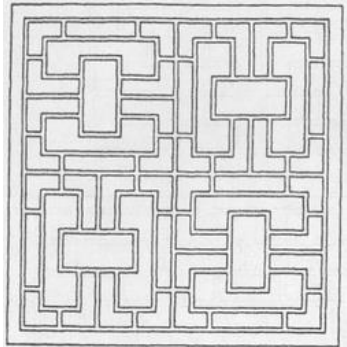
[Dye, 1974]

H. No Focus (H7a)



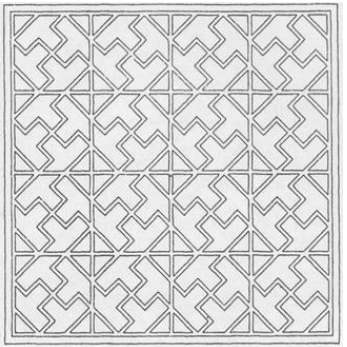
[Dye, 1974]

J. Presentation (J4a)



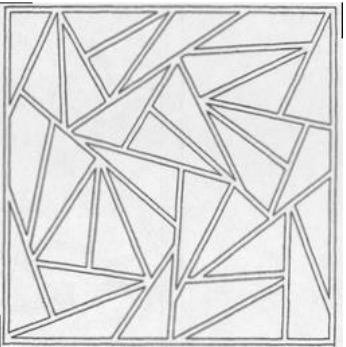
[Dye, 1974]

R. Like Swastika (R11a)



[Dye, 1974]

X. Rustic Ice-ray (X6b)



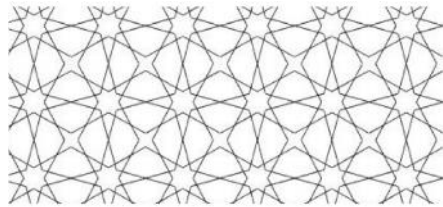
[Dye, 1974]



## Parameterization

### Methods of parameterization

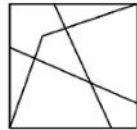
#### 1. Find the smallest motif



Group of pattern



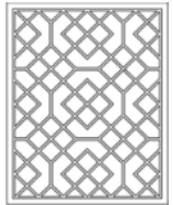
pattern



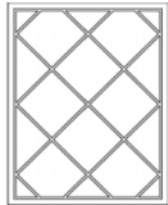
Base module

[Yaser Shahbazi, 2017]

#### 3. Find the hierarchy of geometry



Lattice frame

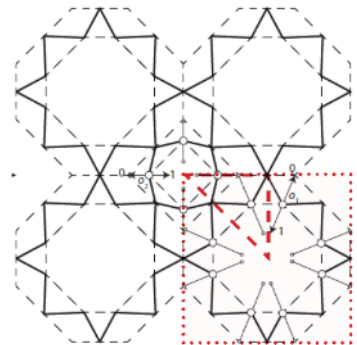


Global pattern



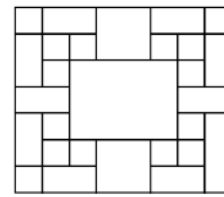
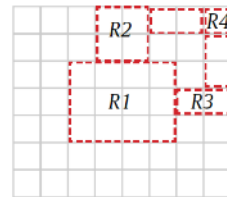
Local pattern  
[Wu, 2012]

#### 2. Find variable junctions



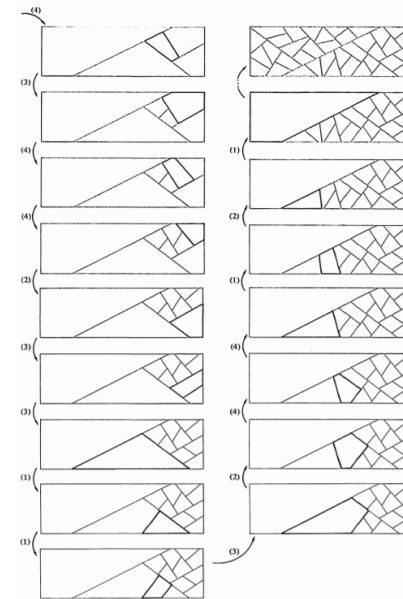
[Khouri, 2015]

#### 4. Find an equation for the proportional area



[Seungmook Kang, 2010]

#### 5. Find Shape Grammar



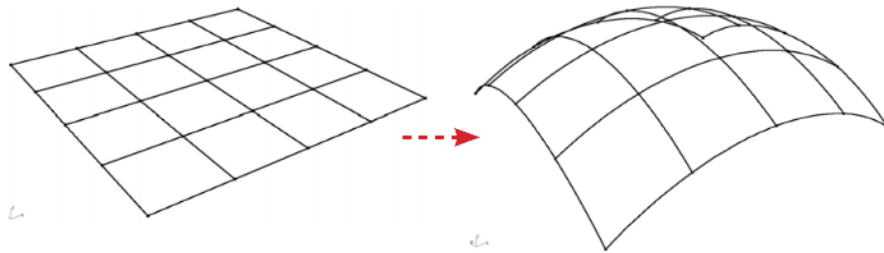
[Stiny, 1977]



## Grid-shell

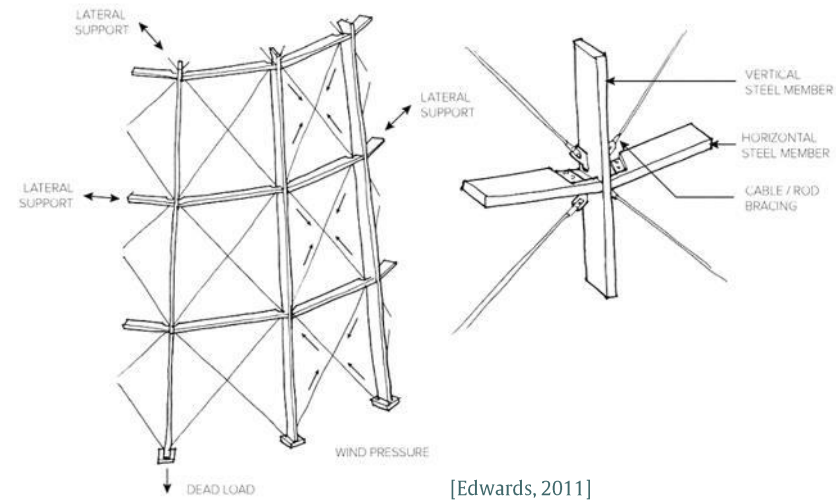
### Types of grid shell:

Strained grid-shell



- Bent after making a horizontal grid
- Buckling strength of material is important

Unstrained grid-shell



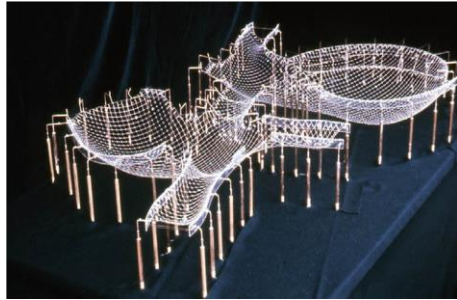
- Pre-bent members are connected at the required angle
- Moment resistant connection is important



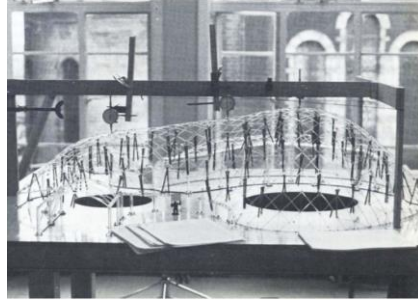
## Grid-shell

### Designing grid-shell:

#### Dynamic Relaxation



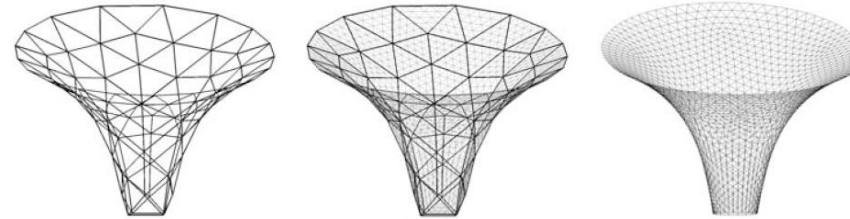
[Liddell, 2015]



[E. Happold, 1975]

- Gives compression only form
- Can be used for various tessellation
- Drawing the specific tessellation for desired shape is prolonged task

#### Geometric Approach



[Dimic, 2011]

- Used for pre-designed form
- Tessellation is drawn in steps as per the requirement of smoothness

## **Research questions**

## Research questions

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**Main Question:** *With the help of parametric workflow, how to design an urban grid shell structure, where the line patterns (in this case, north Asian lattice pattern) are selected based on the structural performance and used in load distribution as a grid geometry?*

## Research questions

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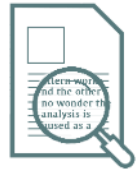
**Main Question:** *With the help of parametric workflow, how to design an urban grid shell structure, where the line patterns (in this case, north Asian lattice pattern) are selected based on the structural performance and used in load distribution as a grid geometry?*

**Sub-question 1:** *How to assess the **structural performance** of such line patterns?*

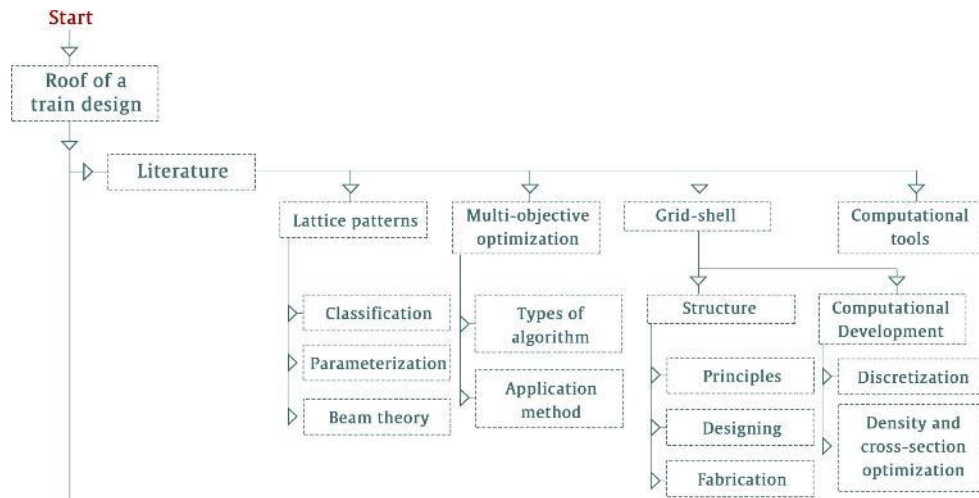
**Sub-question 2:** *How to **parameterize** such line patterns with static and variable junctions that can be used in a pattern grid for structural analysis?*

**Sub-question 3:** *In a parametric model, how to **apply the patterns on a quadrilateral grid-shell** and make a homogeneous grid-shell?*

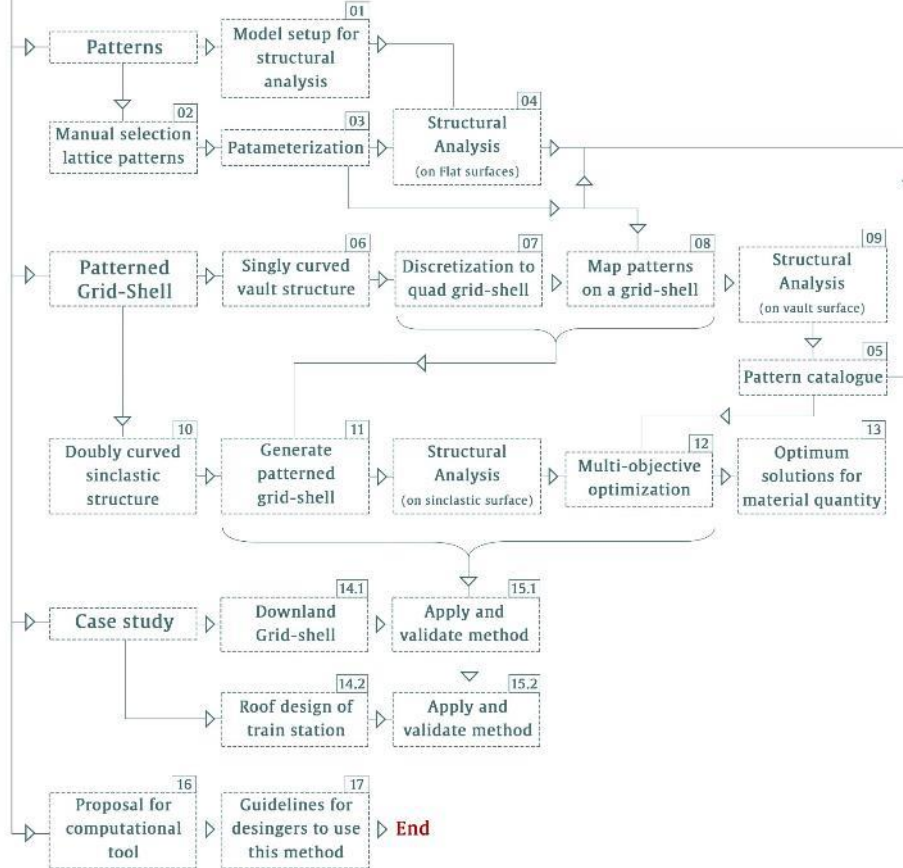
**Sub-question 4:** *Using **multi-objective optimization**, how to find the optimum set of cross-section of a member and density of the mapped pattern for which the grid shell performs similar regular quadrilateral grid shell?*



Literature research



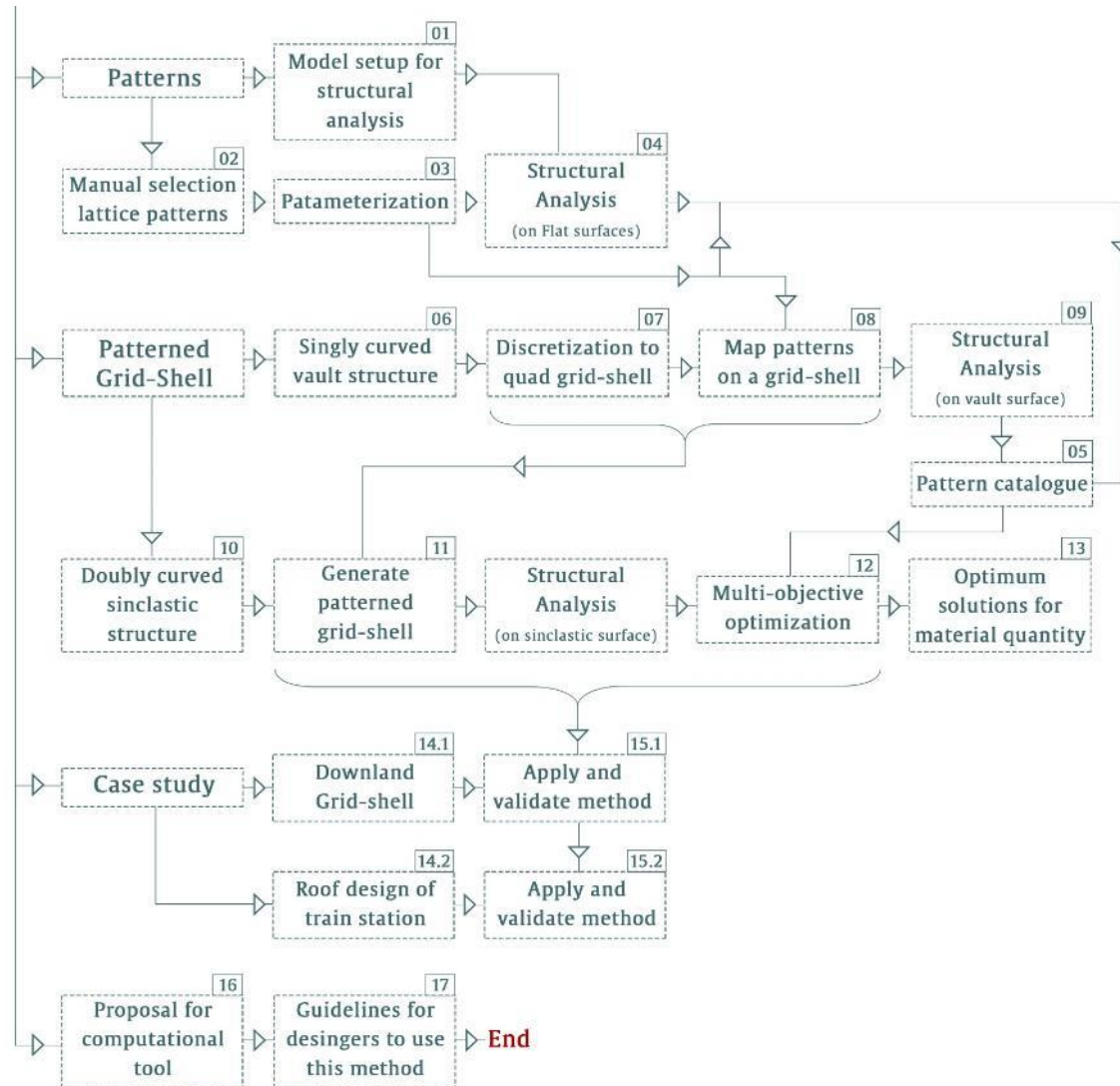
Project Development





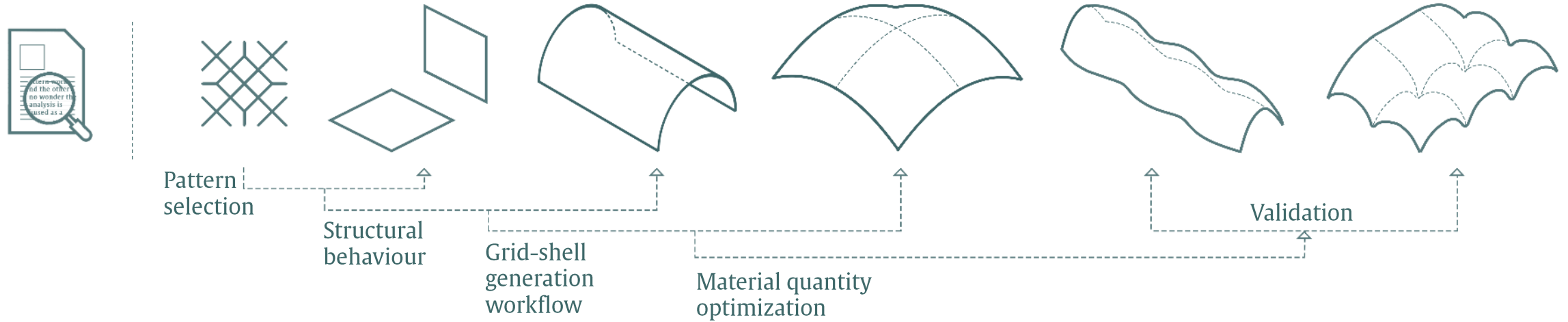


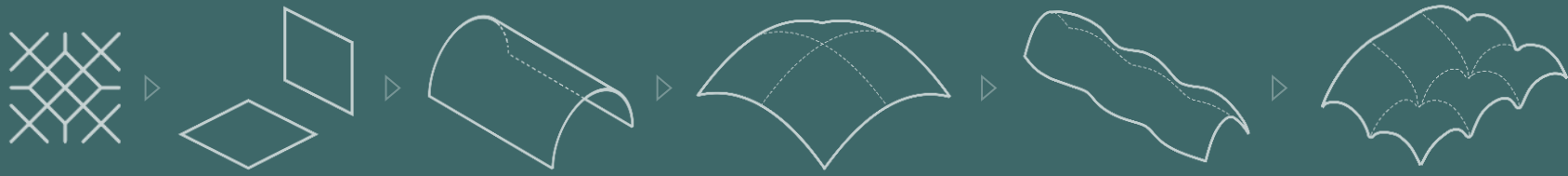
## Project Development





## Project Development



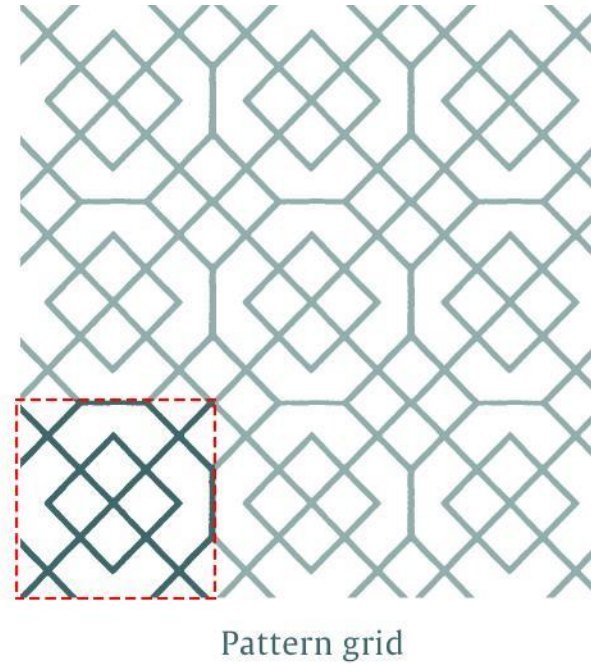
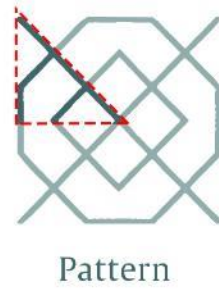


## Project Development

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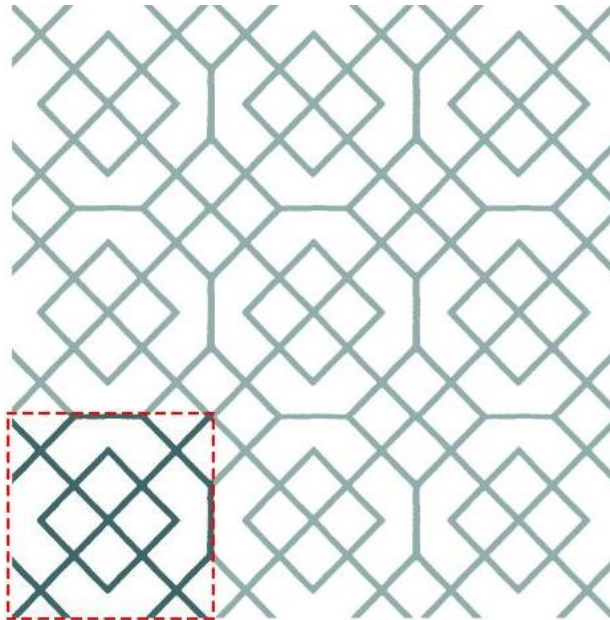


## Model setup





## Model setup



### Grid density:

The total length of all the elements in Pattern grid. Higher the grid density better the structural stiffness.

### Grid Factor:

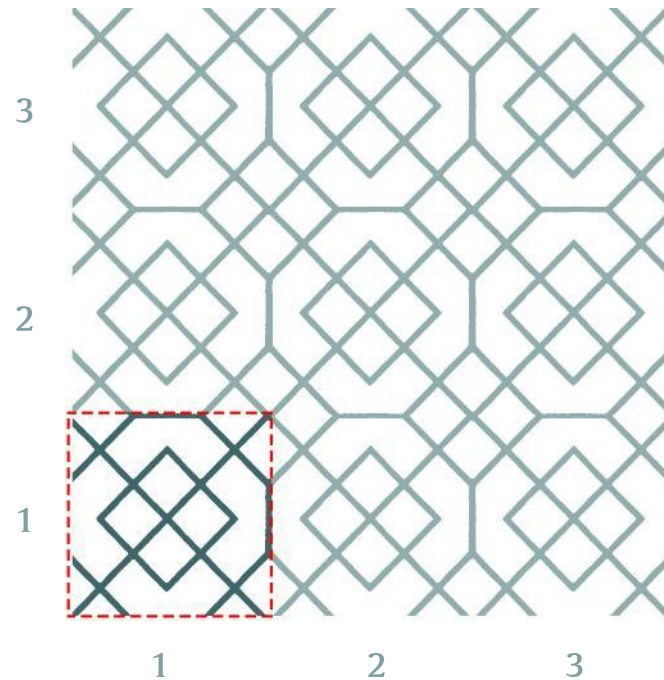
A number by which the pattern is repeated in X and Y direction. (As the test module is 1m x1m square, the Grid factor is same in both directions).

### Mean Grid Density:

A pre-decided number of grid density from which the closest possible grid density for each pattern is found.



## Model setup



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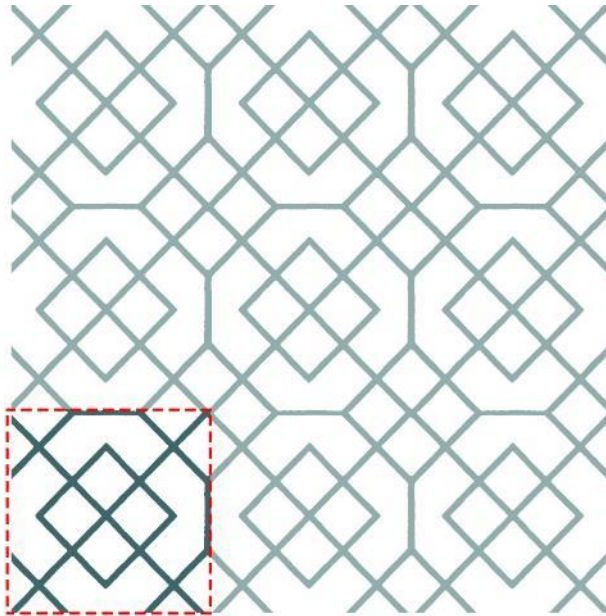
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## Model setup

Mean grid-density = 22m

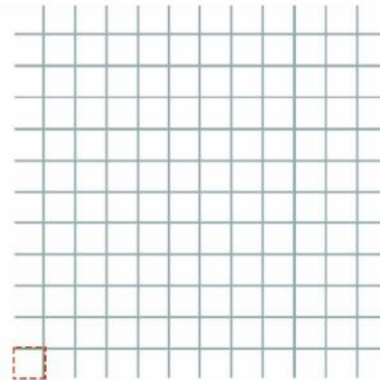


Motif



Pattern

Grid density = 22m  
Grid factor = 12



Pattern Grid

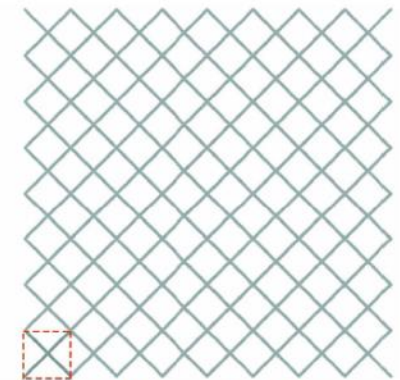


Motif



Pattern

Grid density = 22.62m  
Grid factor = 8



Pattern Grid

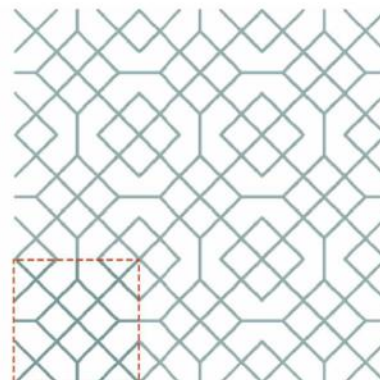


Motif



Pattern

Grid density = 21.11m  
Grid factor = 3



Pattern Grid

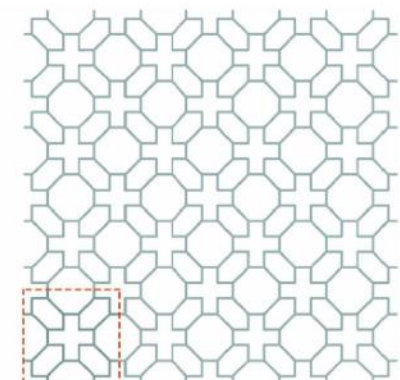


Motif



Pattern

Grid density = 22.36m  
Grid factor = 4

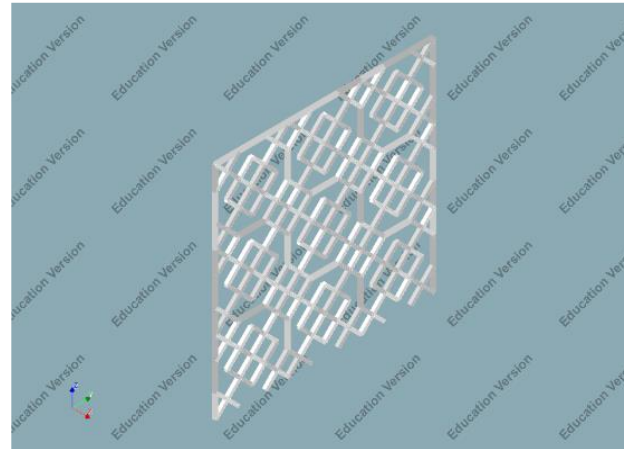
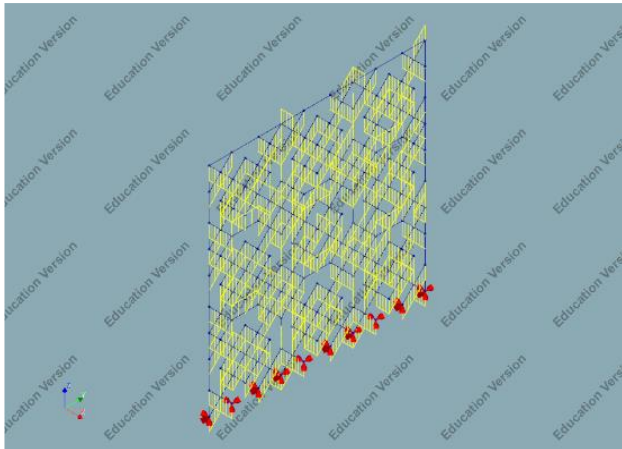
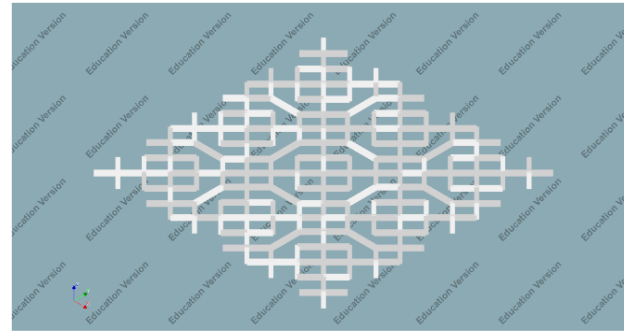
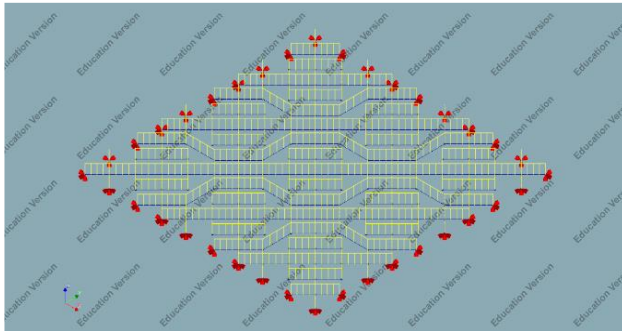


Pattern Grid



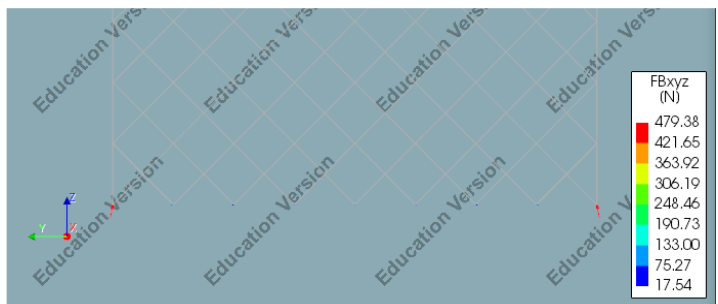
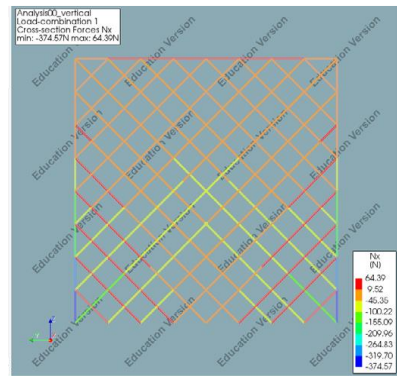
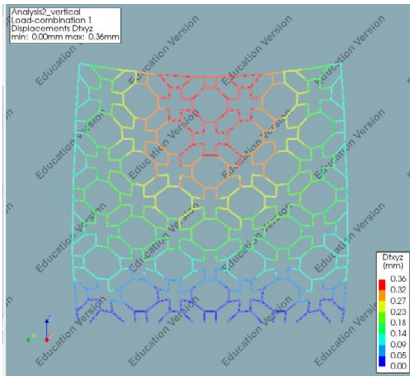
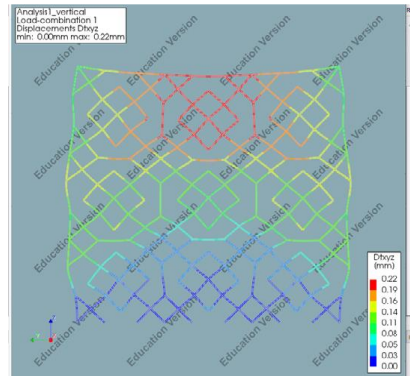
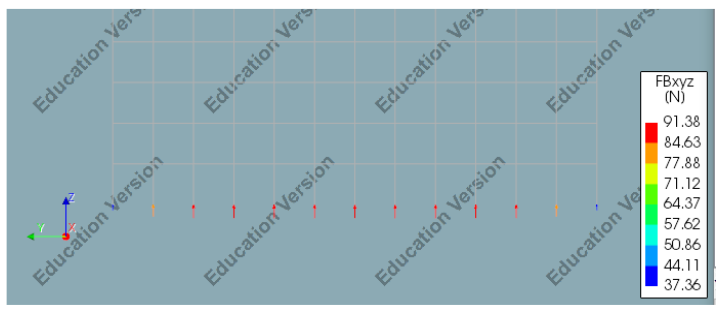
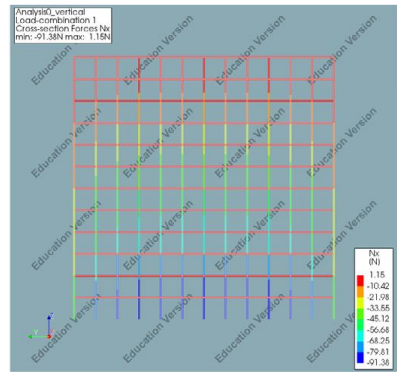
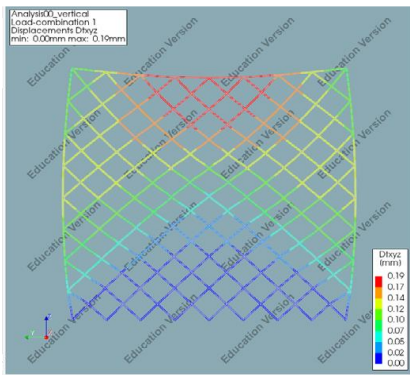
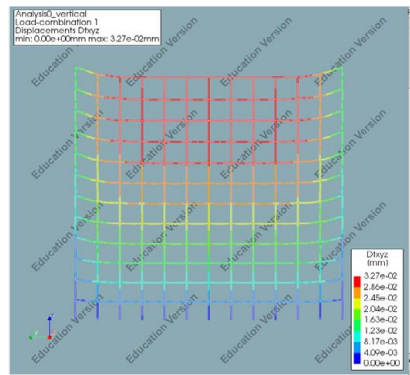


## Diana analysis





## Diana analysis

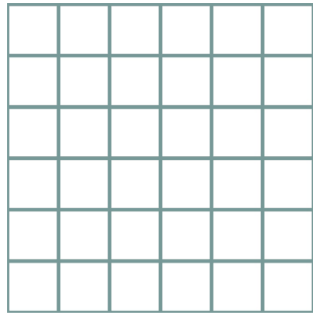


Deformation characteristics

Normal force and reaction force

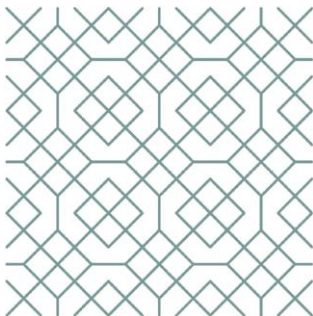
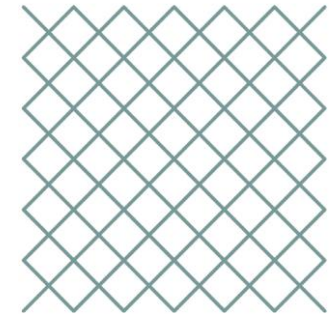


## Diana analysis



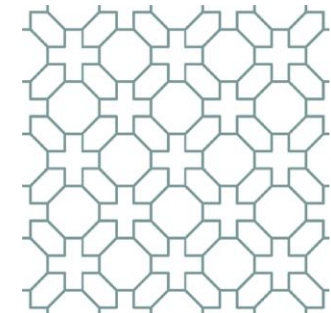
Parallel Grid	Horizontal	Vertical
Deflection (mm)	49.07	0.038
Max reaction force (N)	40.7	91.38
Max compressive stress (N/mm <sup>2</sup> )	31.13	0.59
Max tensile stress (N/mm <sup>2</sup> )	8.82	0.91
Max shear stress (N/mm <sup>2</sup> )	9.63	0.037
Max banding moment (Nmm)	5188.49	97.97
Max normal force (N)	40.7	91.38
Max shear force (N)	40.7	3.72

Diagonal Grid	Horizontal	Vertical
Deflection (mm)	34.46	0.19
Max reaction force (N)	74.63	479.38
Max compressive stress (N/mm <sup>2</sup> )	36.34	2.16
Max tensile stress (N/mm <sup>2</sup> )	40.49	4.32
Max shear stress (N/mm <sup>2</sup> )	2.85	0.0805
Max banding moment (Nmm)	6782.19	315.14
Max normal force (N)	78.84	374.57
Max shear force (N)	78.84	8.05



B6b	Horizontal	Vertical
Deflection (mm)	43.65	0.22
Max reaction force (N)	105.25	421.41
Max compressive stress (N/mm <sup>2</sup> )	50.1	3.96
Max tensile stress (N/mm <sup>2</sup> )	47.67	4.74
Max shear stress (N/mm <sup>2</sup> )	5.9	0.19
Max banding moment (Nmm)	8350.05	661.58
Max normal force (N)	108.79	275.57
Max shear force (N)	-108.79	18.66

B15a	Horizontal	Vertical
Deflection (mm)	57.9	0.36
Max reaction force (N)	72.79	287.64
Max compressive stress (N/mm <sup>2</sup> )	35.58	6.72
Max tensile stress (N/mm <sup>2</sup> )	16.12	7.03
Max shear stress (N/mm <sup>2</sup> )	-16.18	0.43
Max banding moment (Nmm)	5929.19	1146.04
Max normal force (N)	72.79	287.42
Max shear force (N)	72.79	43.5





## Manual selection of patterns

Out of more than 300 different options **25** patterns are manually selected based on the preliminary conclusions of structural analysis.



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Conclusions ▶ 12 characteristics

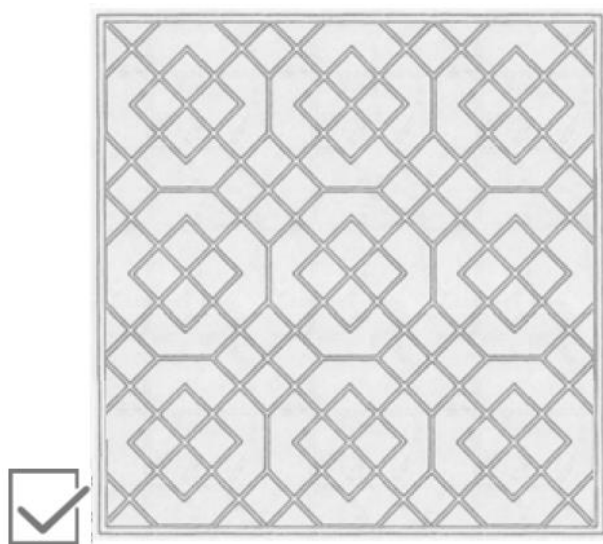


## Manual selection of patterns

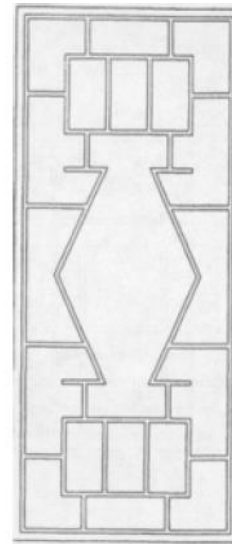
Out of more than 300 different options **25** patterns are manually selected based on the preliminary conclusions of structural analysis.

Conclusions ▶ 12 characteristics

- Continuity in lattice grid



[Dye, 1974]



[Dye, 1974]

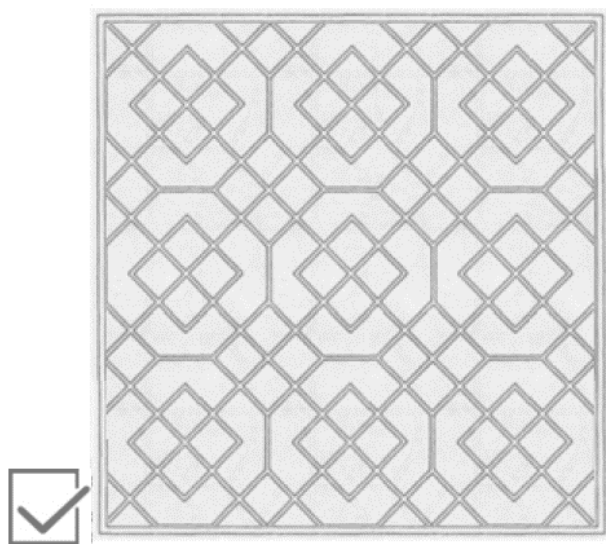


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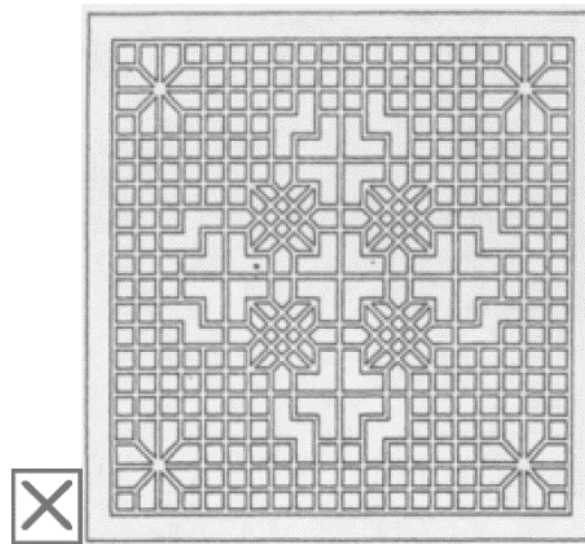
Out of more than 300 different options **25** patterns are manually selected based on the preliminary conclusions of structural analysis.

Conclusions ▶ 12 characteristics

- Similar grid densities



[Dye, 1974]



[Dye, 1974]

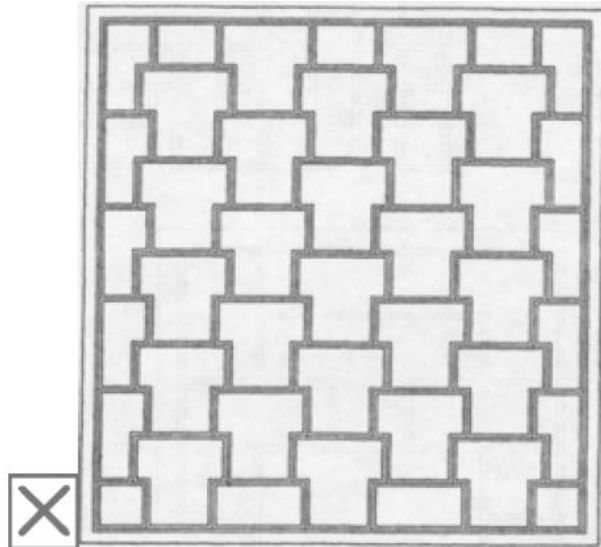


## Manual selection of patterns

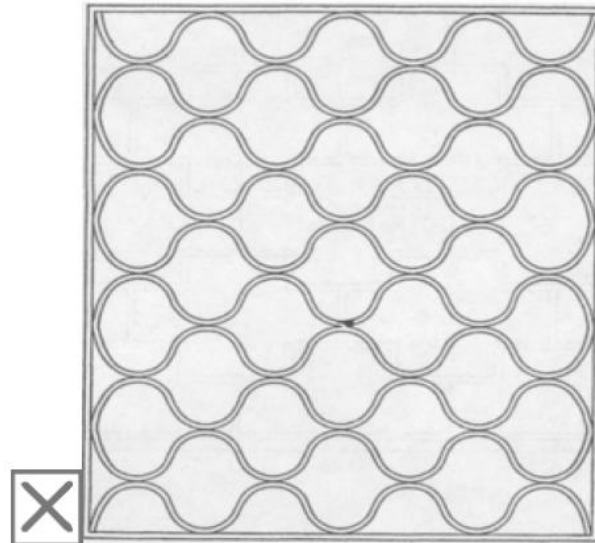
Out of more than 300 different options **25** patterns are manually selected based on the preliminary conclusions of structural analysis.

Conclusions ▶ 12 characteristics

- Select unique native design



[Dye, 1974]



[Dye, 1974]



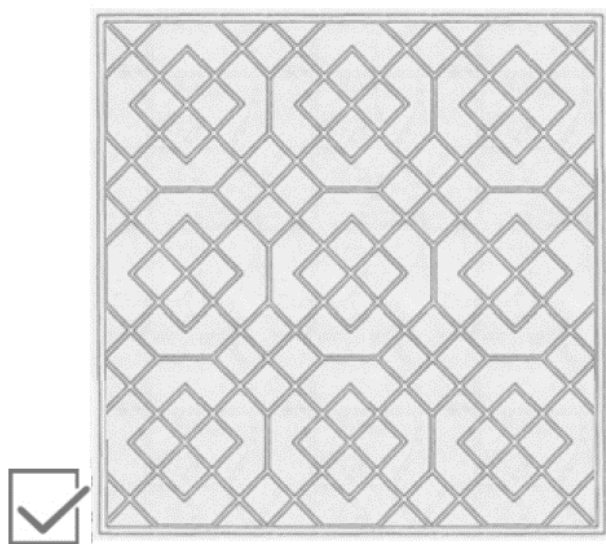


## Manual selection of patterns

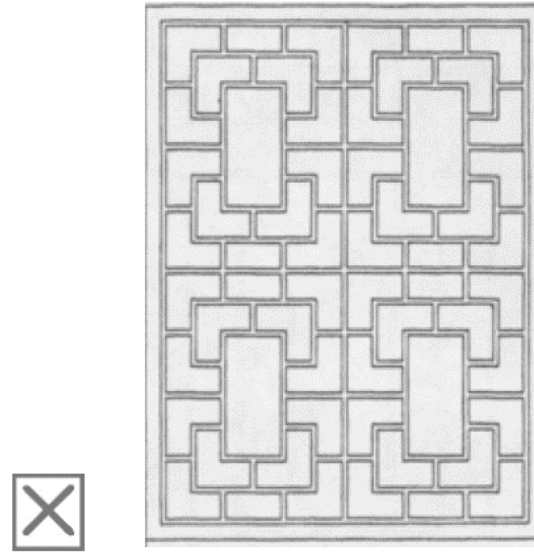
Out of more than 300 different options **25** patterns are manually selected based on the preliminary conclusions of structural analysis.

Conclusions ▶ 12 characteristics

- Pattern which has same geometric configuration from all four sides



[Dye, 1974]

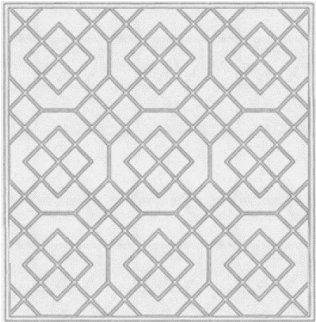


[Dye, 1974]



## Parametric workflow

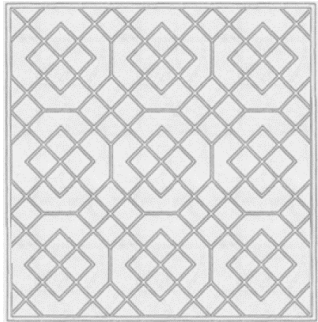
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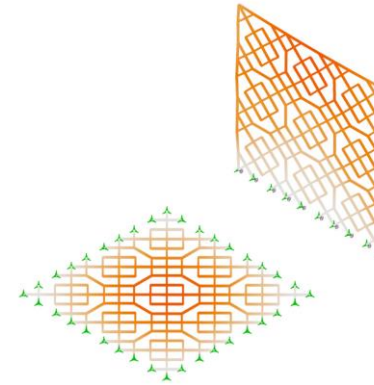
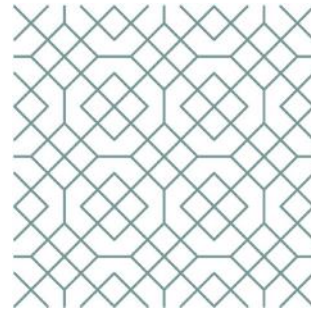
[Dye, 1974]



## Parametric workflow

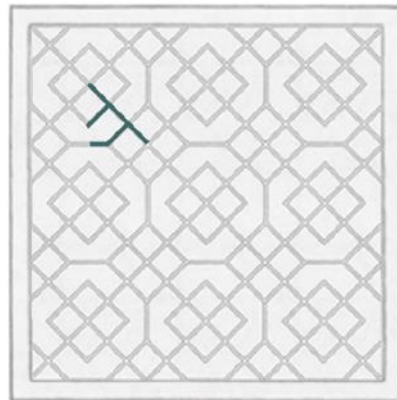


[Dye, 1974]

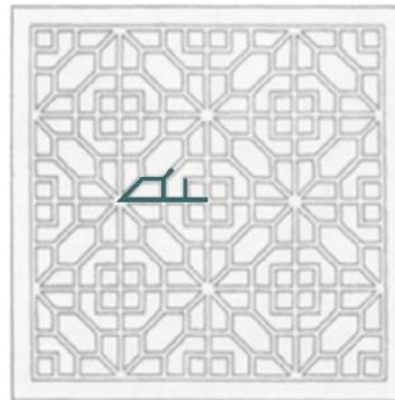




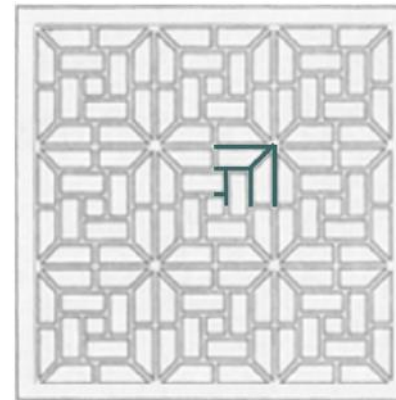
## Parameterization



(1)



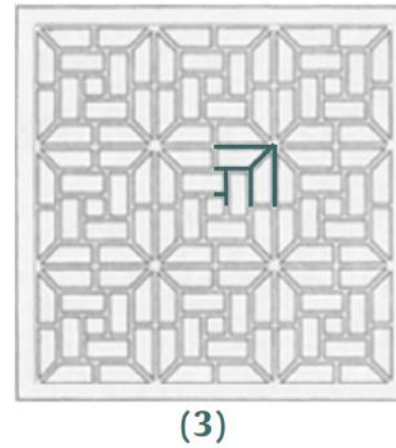
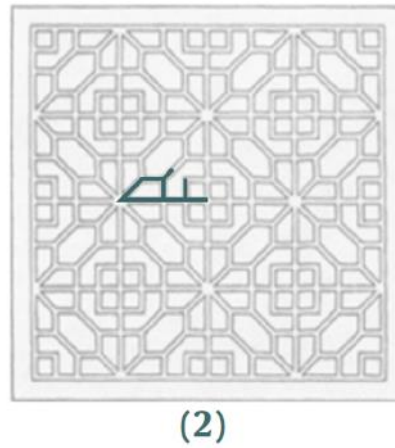
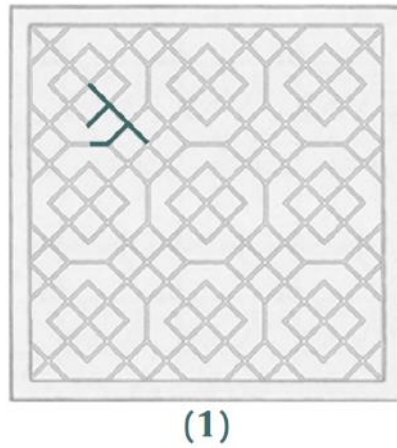
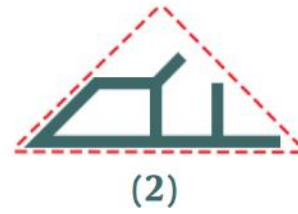
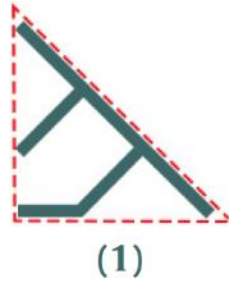
(2)



(3)

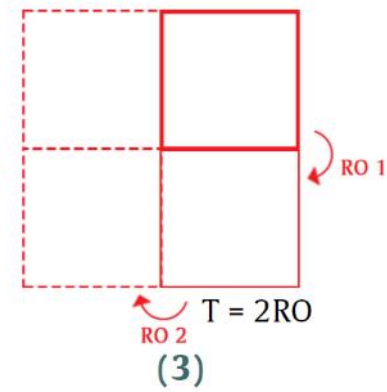
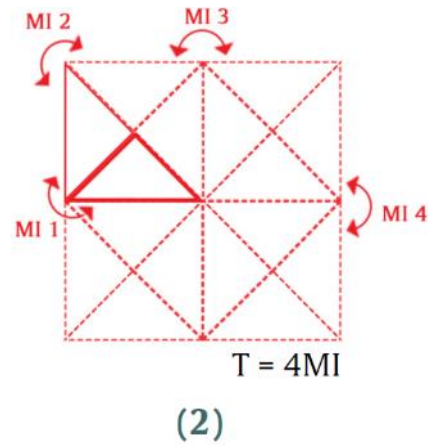
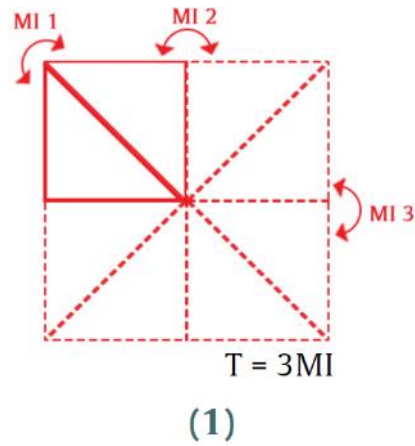
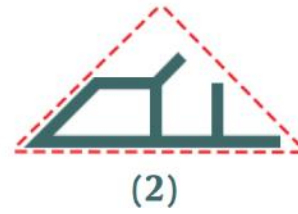
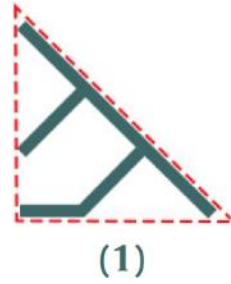


## Parameterization



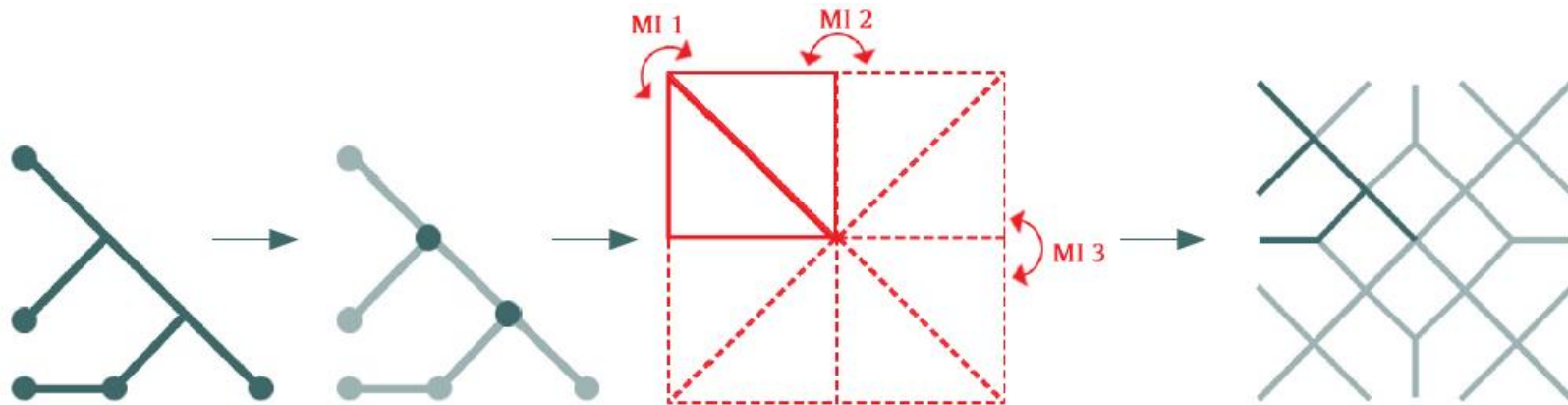


## Parameterization



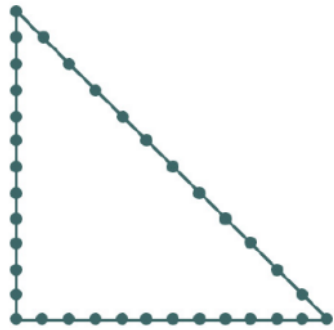


## Parameterization





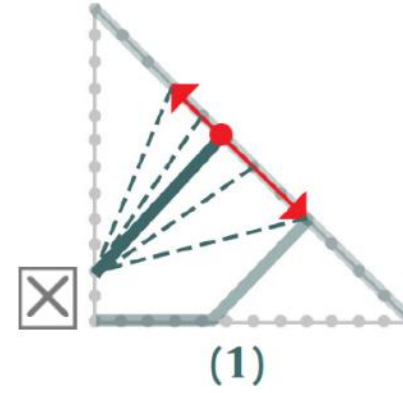
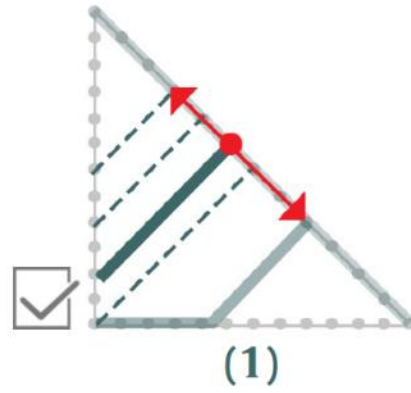
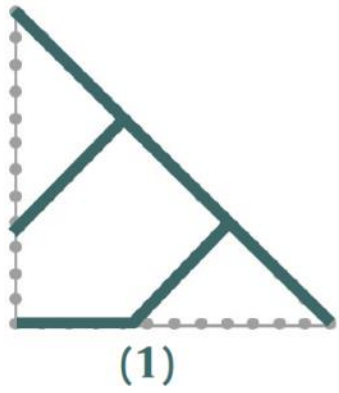
## Parameterization





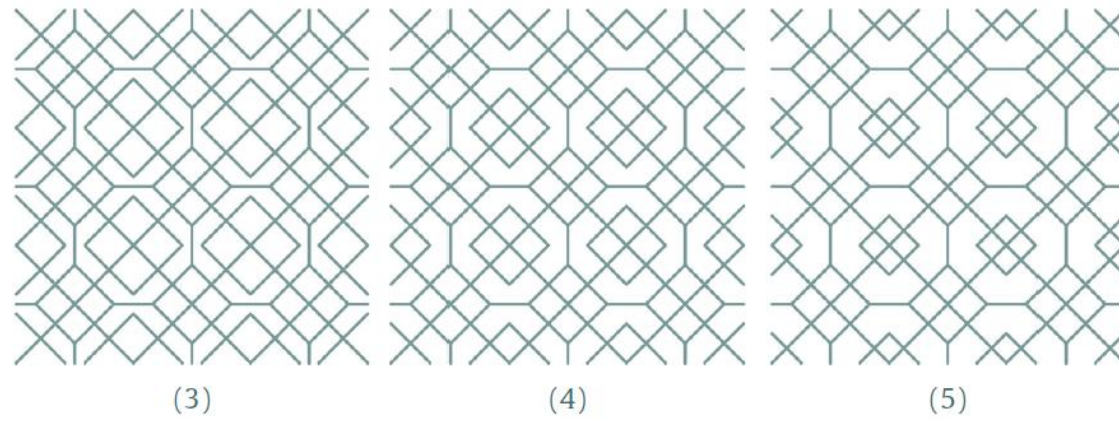
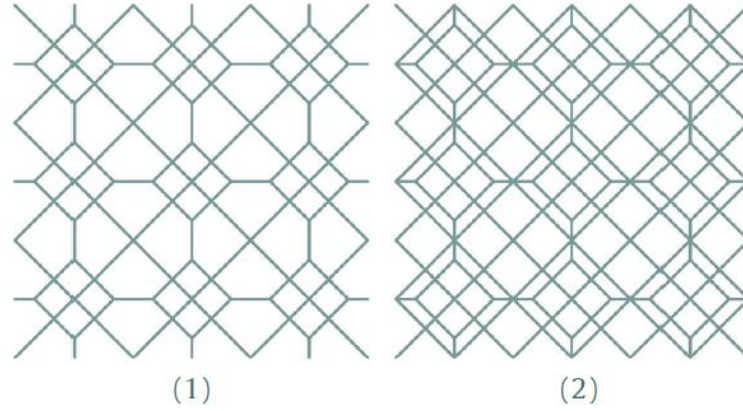
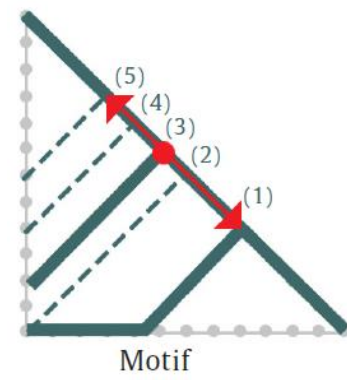


## Parameterization





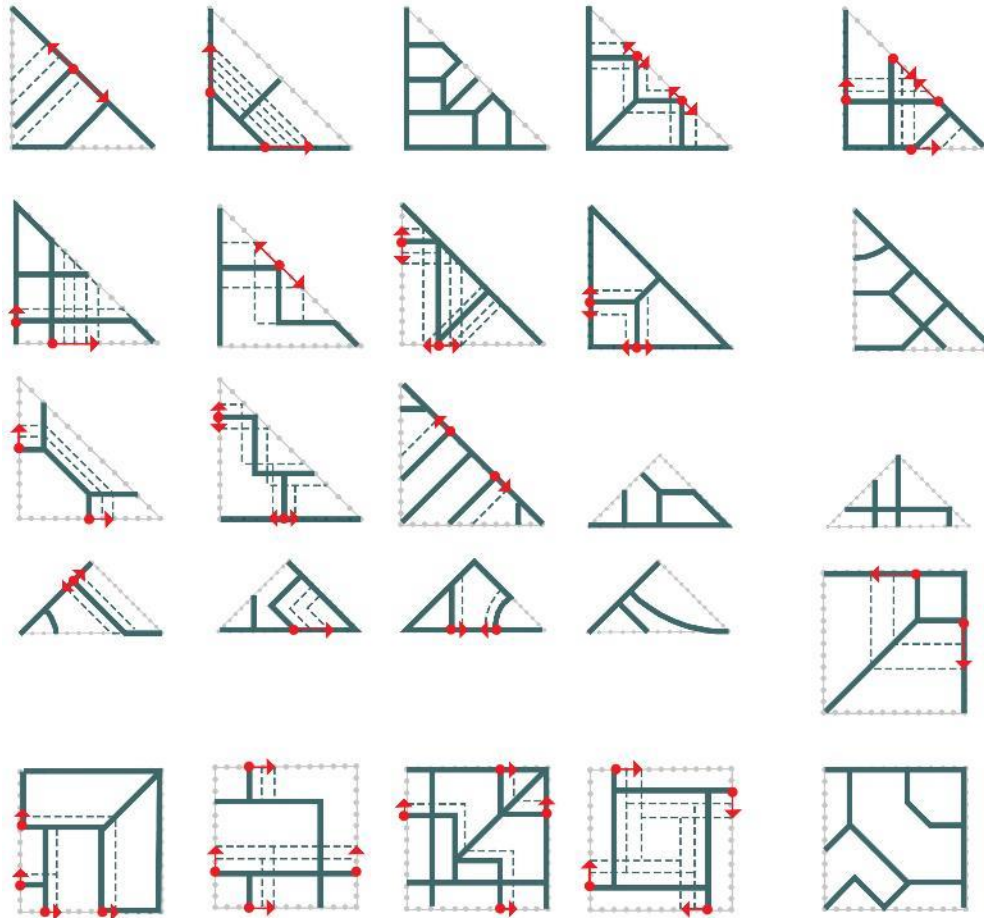
## Parameterization





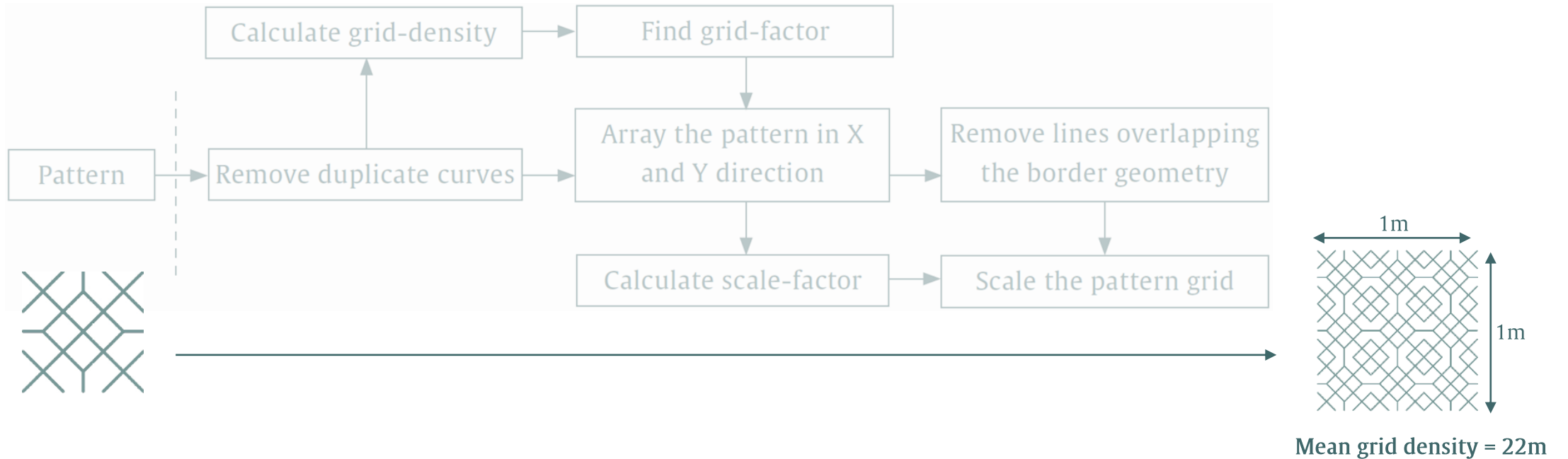
## Parameterization

Likewise out of **25** selected patterns, **81** options are generated



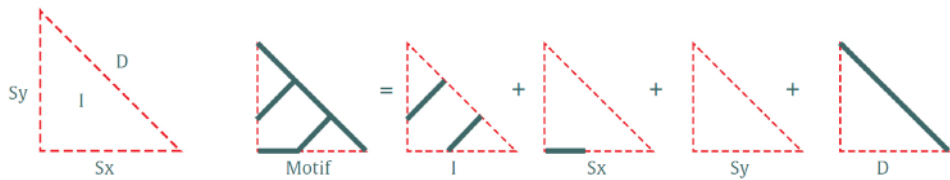


## Pattern grid-arrangement

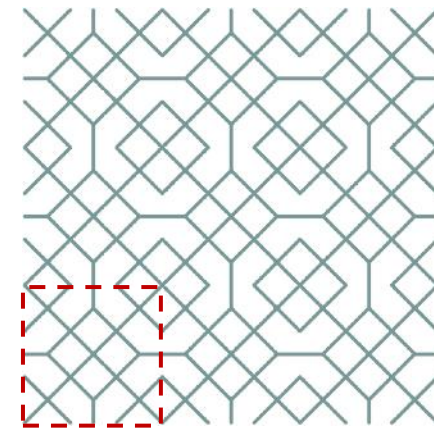




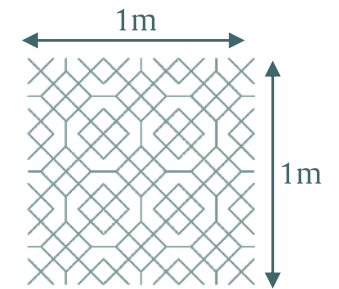
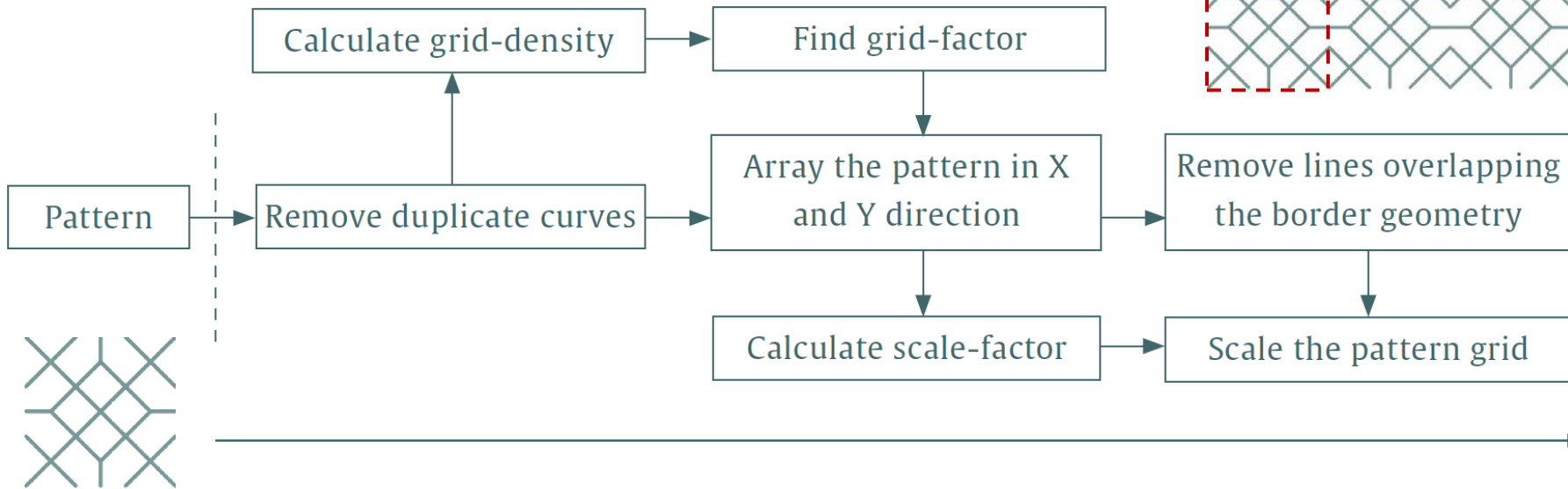
### Pattern grid-arrangement



$$\text{Grid density} = \frac{8n^2 I}{2} + \frac{8n^2(D + Sx)}{2} + \frac{8n^2 Sy - 4(2n)}{2}$$



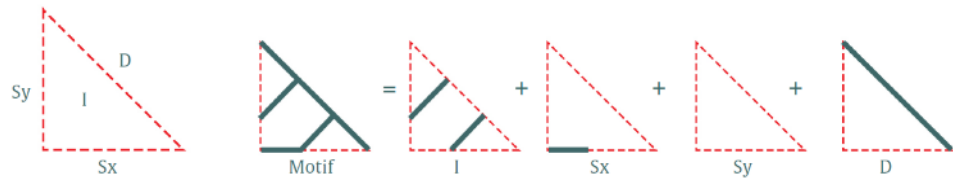
Grid-factor = 3



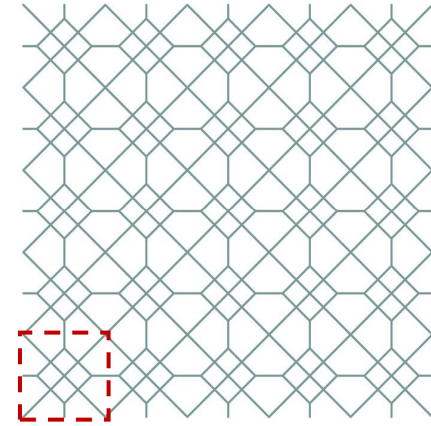
Mean grid density = 22m



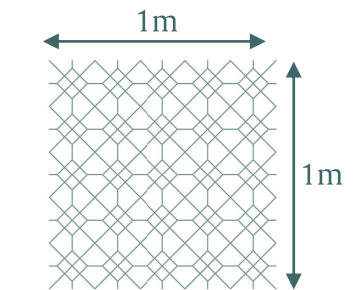
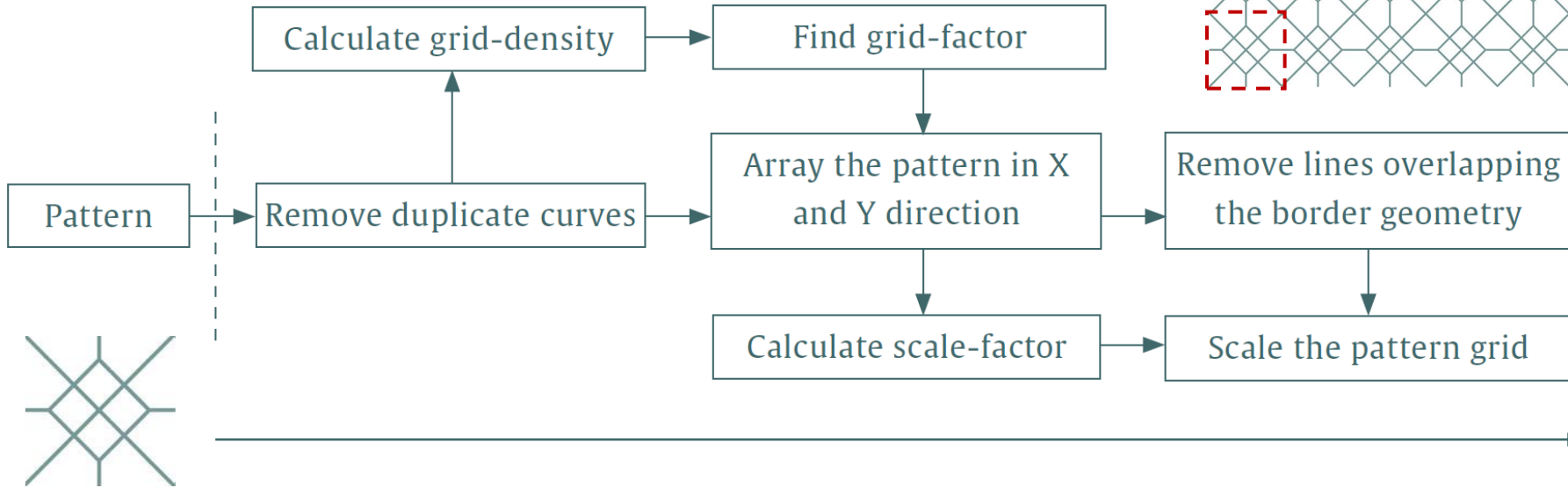
### Pattern grid-arrangement



$$\text{Grid density} = \frac{8n^2 I}{2} + \frac{8n^2(D + Sx)}{2} + \frac{8n^2 Sy - 4(2n)}{2}$$



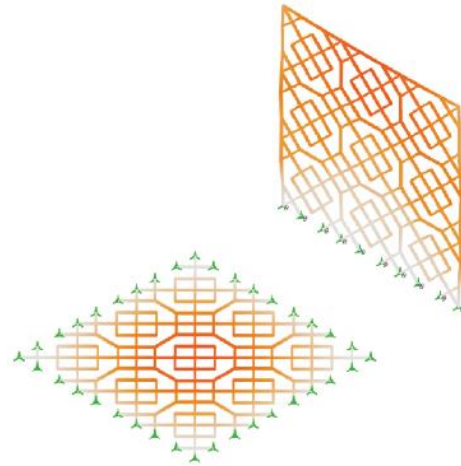
Grid- factor = 5



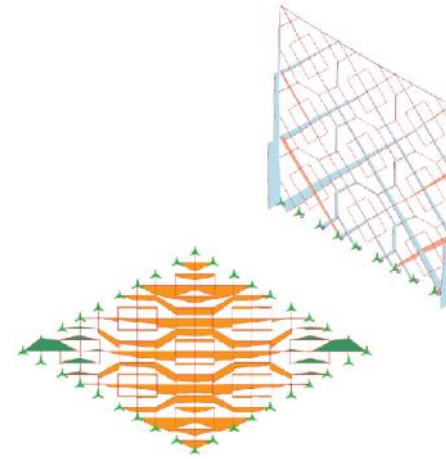
Mean grid density = 22m



## Structural analysis



Deformation



Bending moment  $M_y$  in horizontal orientation  
and normal force  $N_x$  in vertical orientation



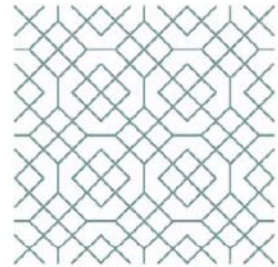
## Structural analysis

### Example 1 (B6b\_4)

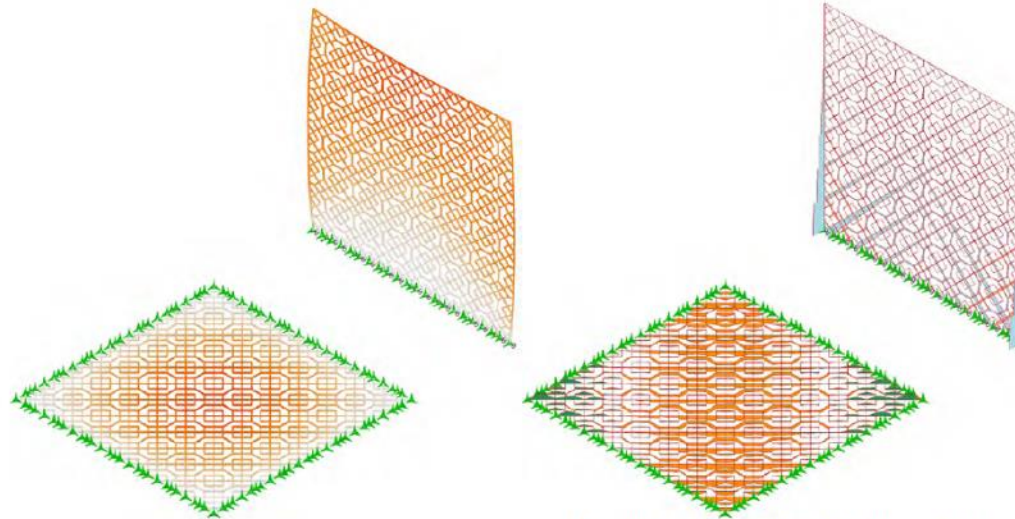


Motif

Pattern



Pattern Grid



Deformation in vertical and horizontal orientation

Normal force in vertical and bending moment in horizontal orientation

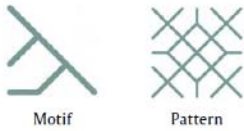
Transformation	3MI		Horizontal		Vertical	
	Grid Density	Grid Factor	Value	% Difference	Value	% Difference
Grid Density	50.8643	-2.0357	71.57	-11.04	0.18	80.01
Grid Factor	7					
Deflection (mm)			20.74	13.08	0.73	70.71
Avg Max Axial Stress (MPa)			-20.74	13.08	-1.14	48.28
Avg Min Axial Stress (MPa)			-	-	-10.36	19.79
Avg Normal Force (N)			1,221.10	7.32	54.50	56.31
Avg Bending Moment (Nmm)			13.62	21.60	3.22	42.06
Avg Shear Force (N)			0.35	13.08	0.02	48.28
Avg Utilizatio Ratio						



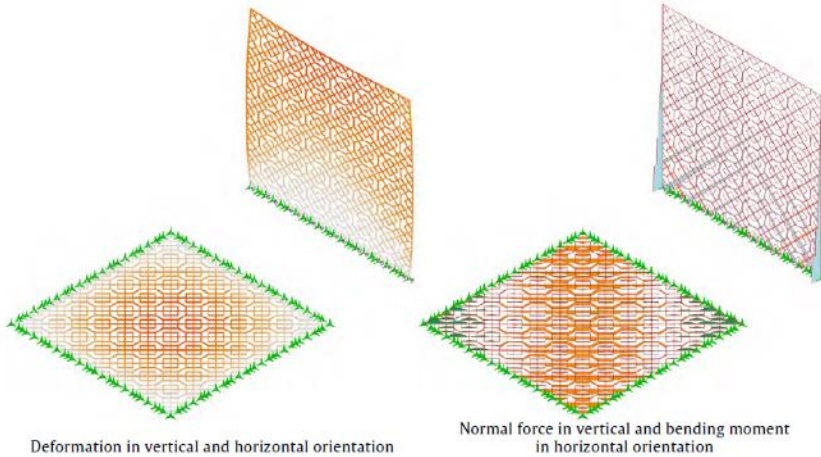


## Structural analysis

### Example 1 (B6b\_4)



Pattern Grid

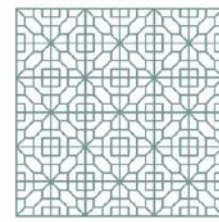


Deformation in vertical and horizontal orientation

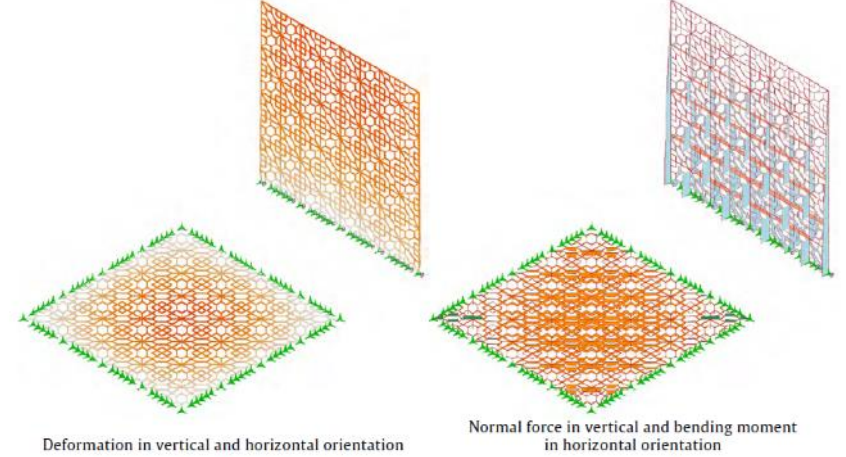
Normal force in vertical and bending moment in horizontal orientation

Transformation	3MI		Horizontal		Vertical	
	Value	% Difference	Value	% Difference	Value	% Difference
Grid Density	50.8643	-2.0357				
Grid Factor	7					
Deflection (mm)	71.57	-11.04	0.18	80.01		
Avg Max Axial Stress (MPa)	20.74	13.08	0.73	70.71		
Avg Min Axial Stress (MPa)	-20.74	13.08	-1.14	48.28		
Avg Normal Force (N)	-	-	-10.36	19.79		
Avg Bending Moment (Nmm)	1,221.10	7.32	54.50	56.31		
Avg Shear Force (N)	13.62	21.60	3.22	42.06		
Avg Utilizatio Ratio	0.35	13.08	0.02	48.28		

### Example 2 (B14a\_1)



Pattern Grid



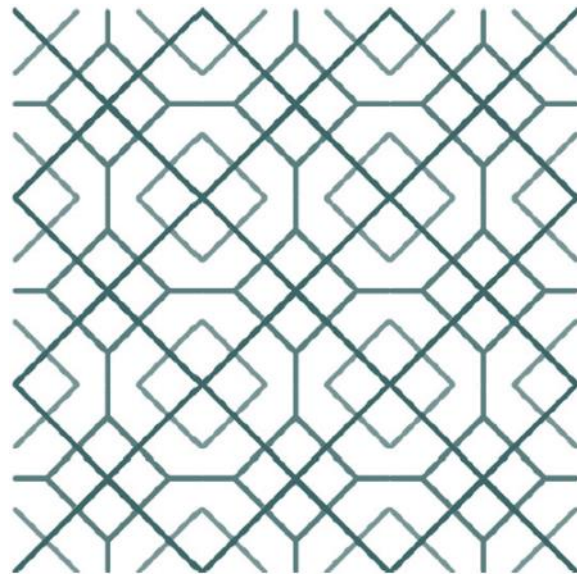
Deformation in vertical and horizontal orientation

Normal force in vertical and bending moment in horizontal orientation

Transformation	4MI		Horizontal		Vertical	
	Value	% Difference	Value	% Difference	Value	% Difference
Grid Density	49.3137	-3.5863				
Grid Factor	4					
Deflection (mm)	80.64	0.23	0.05	-44.85		
Avg Max Axial Stress (MPa)	17.93	-2.28	0.15	-65.91		
Avg Min Axial Stress (MPa)	-17.93	-2.28	-0.51	-34.18		
Avg Normal Force (N)	-	-	-9.11	5.32		
Avg Bending Moment (Nmm)	1,093.28	-3.92	19.00	-45.49		
Avg Shear Force (N)	6.88	-38.62	1.07	-52.80		
Avg Utilizatio Ratio	0.30	-2.28	0.01	-34.18		



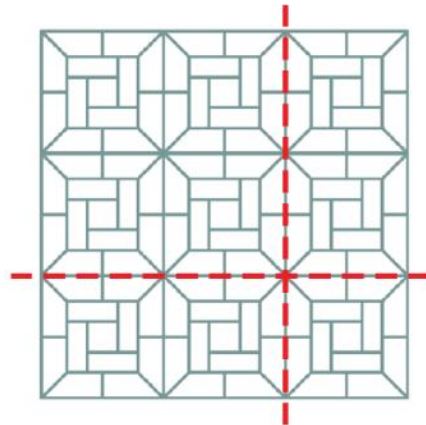
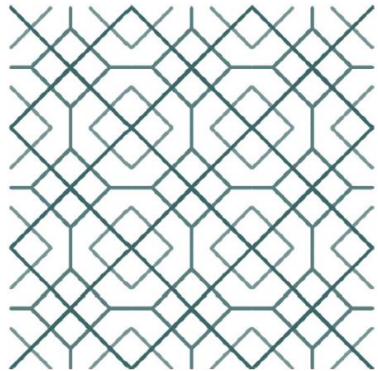
## Conclusion for patterns



- Primary elements
- Secondary elements
- Overhang elements

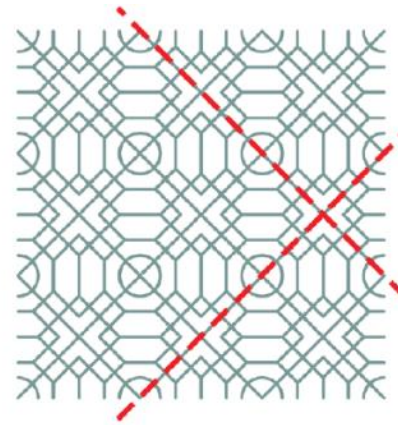


## Conclusion for patterns



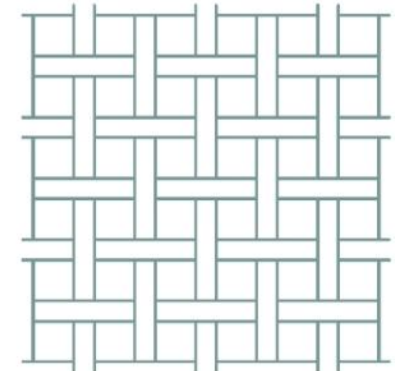
### Parallel direction

- Performs good in vertical orientation



### Diagonal direction

- Performs good in horizontal orientation



### No primary structure

- High performance values

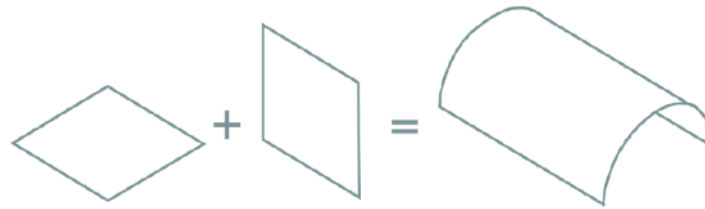


## Conclusion for patterns

						Horizontal orientation					
	Name	Grid Density	Grid Factor	Trasformation	Deflection (mm)	Avg Max Axial Stress (MPa)	Avg Min Axial Stress (MPa)	Avg Bending Moment (Nmm)	Avg Shear Force (N)	Utilizatio Ratio	
1	B6b_1	53.80712	10	3 MI	59.84705	19.192404	-19.192404	1122.018407	10.799397	0.319873	
2	B6b_2	49.25483	6	3 MI	59.56602	20.366885	-20.366885	1191.480643	8.902101	0.339448	
3	B6b_3	54.16414	7	3 MI	72.815057	22.090213	-22.090213	1301.320919	13.765882	0.36817	
4	B6b_4	50.86431	7	3 MI	71.568955	20.743591	-20.743591	1221.104882	13.623927	0.345727	
5	B6b_5	54.3594	8	3 MI	69.295571	19.076642	-19.076642	1118.668297	14.569109	0.317944	
6	B7b_1	54.04857	7	3 MI	79.518382	17.901062	-17.901062	1085.954282	7.099986	0.298351	
7	B7b_2	55.69849	7	3 MI	80.96364	18.262552	-18.262552	1110.290204	6.881624	0.304376	
8	B7b_3	48.87006	6	3 MI	82.773986	19.131983	-19.131983	1155.134684	6.788033	0.318866	
9	B7b_4	50.28427	6	3 MI	82.774417	19.525843	-19.525843	1175.687766	6.787438	0.325431	
10	B7b_5	51.69849	6	3 MI	81.666724	19.845463	-19.845463	1192.044803	6.793425	0.330758	
11	H11b_1	56.14214	4	3 MI	87.692073	19.595721	-19.595721	1240.576304	13.359395	0.326595	
12	H13a_1	53.11845	5	3 MI	72.484833	17.65324	-17.65324	1080.735711	6.858492	0.294221	
13	H13a_2	54.09476	5	3 MI	72.871137	17.593831	-17.593831	1083.827165	6.735434	0.293231	
14	H13a_3	55.07107	5	3 MI	73.172886	17.490619	-17.490619	1085.506328	6.737892	0.29151	
15	H14a_1	51.45178	5	3 MI	80.495957	19.269503	-19.269503	1213.446404	11.699645	0.321158	
16	H14a_2	49.43994	5	3 MI	80.314169	18.990281	-18.990281	1193.533058	11.499383	0.316505	
17	H14a_3	57.31371	6	3 MI	79.803952	17.926512	-17.926512	1112.169136	11.320923	0.298775	
18	H14a_4	50.96362	5	3 MI	77.582036	18.898502	-18.898502	1182.381831	10.771103	0.314975	
19	H14a_5	48.95178	5	3 MI	77.966052	18.508392	-18.508392	1153.597238	10.112517	0.308473	
20	H14a_6	56.72792	6	3 MI	76.941411	17.439111	-17.439111	1078.352352	10.642463	0.290652	
21	H14a_7	50.47547	5	3 MI	74.650104	18.425522	-18.425522	1146.822477	10.263399	0.307092	
22	L3a_1	55.55922	5	3 MI	78.980666	17.353059	-17.353059	1077.350223	8.105001	0.289218	
23	L3a_2	55.07107	5	3 MI	78.238295	17.606068	-17.606068	1087.541243	7.827201	0.293434	
24	L3a_3	54.58291	5	3 MI	77.386109	17.78055	-17.78055	1093.581856	7.974659	0.296342	
25	L3a_4	54.09476	5	3 MI	76.409584	19.722625	-19.722625	1209.009974	7.349358	0.32871	
26	L3a_5	53.6066	5	3 MI	76.835297	20.833583	-20.833583	1262.062496	7.963339	0.347226	
27	L3a_6	55.07107	5	3 MI	78.52902	17.193145	-17.193145	1068.17377	8.472605	0.286552	
28	L3a_7	54.58291	5	3 MI	77.800563	17.429401	-17.429401	1076.302583	8.035431	0.29049	
29	L3a_8	54.09476	5	3 MI	76.959991	17.571946	-17.571946	1080.577789	8.095061	0.292866	
30	L3a_9	53.6066	5	3 MI	75.987458	19.445294	-19.445294	1193.108539	7.383694	0.324088	
31	L3a_10	53.11845	5	3 MI	76.35164	20.636677	-20.636677	1248.792016	8.280867	0.343945	
32	Q5a_1	55.10457	8	3 MI	94.700598	17.722297	-17.722297	1107.459872	8.149014	0.295372	
33	Q5a_2	50.29983	7	3 MI	100.28436	18.602559	-18.602559	1171.553048	8.331365	0.310043	
34	Q5a_3	52.63317	7	3 MI	104.487353	19.106695	-19.106695	1206.253213	8.809917	0.318445	

						Vertical orientation					
	Name	Grid Density	Grid Factor	Deflection (mm)	Avg Max Axial Stress (MPa)	AvgMin Axial Stress (MPa)	Avg Normal Force (N)	Avg Bending Moment (Nmm)	Avg Shear Force (N)	Utilizatio Ratio	
1	B6b_1	53.80712	10	0.119507	0.646674	-1.084178	-10.997511	50.361426	3.896257	0.01807	
2	B6b_2	49.25483	6	0.194597	0.724157	-1.162824	-10.974681	54.91169	2.85573	0.01938	
3	B6b_3	54.16414	7	0.18533	0.806158	-1.247631	-11.054369	59.754702	3.535866	0.020794	
4	B6b_4	50.86431	7	0.178345	0.729878	-1.143098	-10.36313	54.496527	3.215579	0.019052	
5	B6b_5	54.3594	8	0.159593	0.643885	-1.042932	-10.023587	49.074951	3.283307	0.017382	
6	B7b_1	54.04857	7	0.044501	0.03641	-0.365624	-8.317073	11.699934	0.918942	0.006094	
7	B7b_2	55.69849	7	0.045378	0.016511	-0.354109	-8.517386	10.789159	0.773711	0.005902	
8	B7b_3	48.87006	6	0.046319	0.017266	-0.358627	-8.639429	10.946828	0.695278	0.005977	
9	B7b_4	50.28427	6	0.046399	0.019799	-0.372294	-8.923388	11.413783	0.725996	0.006205	
10	B7b_5	51.69849	6	0.046226	0.02602	-0.391641	-9.262569	12.168291	0.813179	0.006527	
11	H11b_1	56.14214	4	0.060816	0.258854	-0.607128	-8.778141	25.189863	1.711344	0.010119	
12	H13a_1	53.11845	5	0.040285	0.152485	-0.499276	-8.752348	18.978374	1.294714	0.008321	
13	H13a_2	54.09476	5	0.044562	0.138789	-0.49177	-8.894264	18.362856	1.079467	0.008196	
14	H13a_3	55.07107	5	0.046209	0.144098	-0.507182	-9.14923	18.96542	1.150414	0.008453	
15	H14a_1	51.45178	5	0.067428	0.424524	-0.763872	-8.607468	34.561748	2.437371	0.012731	
16	H14a_2	49.43994	5	0.063129	0.458915	-0.785868	-8.287613	36.205253	2.417668	0.013098	
17	H14a_3	57.31371	6	0.048291	0.333902	-0.660054	-8.232996	28.912641	2.547718	0.011001	
18	H14a_4	50.96362	5	0.067408	0.463717	-0.798243	-8.47943	36.707161	2.258415	0.013304	
19	H14a_5	48.95178	5	0.058762	0.447488	-0.772418	-8.210882	35.483686	2.366692	0.012874	
20	H14a_6	56.72792	6	0.041225	0.238126	-0.562731	-8.19097	23.297326	2.464623	0.009379	
21	H14a_7	50.47547	5	0.060949	0.441916	-0.776106	-8.45209	35.432528	2.275597	0.012935	
22	L3a_1	55.55922	5	0.056545	0.288321	-0.642617	-8.932763	27.082128	1.734243	0.01071	
23	L3a_2	55.07107	5	0.052929	0.284256	-0.639508	-8.970244	26.871893	1.758937	0.010658	
24	L3a_3	54.58291	5	0.044967	0.22253	-0.579592	-9.016377	23.341276	1.917389	0.00966	
25	L3a_4	54.09476	5	0.036361	0.028699	-0.414591	-9.726484	12.917086	0.820309	0.00691	
26	L3a_5	53.6066	5	0.041963	0.122884	-0.614182	-10.150877	24.075123	1.802434	0.010236	
27	L3a_6	55.07107	5	0.059824	0.289547	-0.640783	-8.854263	27.066173	1.735865	0.01068	
28	L3a_7	54.58291	5	0.055536	0.283223	-0.63595	-8.897114	26.74239	1.763104	0.010599	
29	L3a_8	54.09476	5	0.04655	0.212737	-0.571897	-8.9427	22.964429	1.928118	0.009532	
30	L3a_9	53.6066	5	0.036994	0.011801	-0.394378	-9.632958	11.838819	0.75802	0.006573	
31	L3a_10	53.11845	5	0.041044	0.190702	-0.588558	-10.068822	22.683464	1.836354	0.009809	
32	Q5a_1	55.10457	8	0.072032	0.359251	-0.663927	-7.69311	29.76016	2.20921	0.011065	
33	Q5a_2	50.29983	7	0.083844	0.382877	-0.677023	-7.443853	30.8367	1.912319	0.011284	
34	Q5a_3	52.63317	7	0.091665	0.363819	-0.661458	-7.504506	29.819956	1.844863	0.011024	



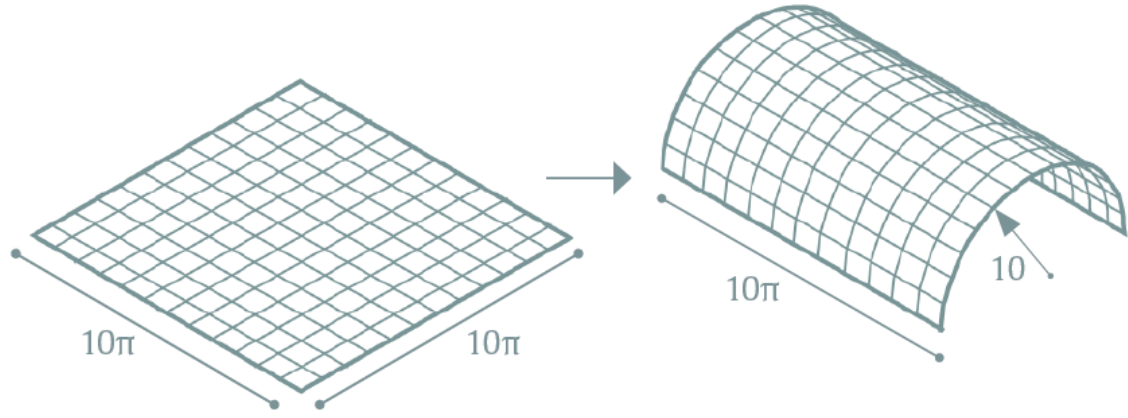


**Aim:**

- Design a parametric workflow to generate patterned grid-shell
- Compare the structural performance all the patterns with each other
- Compare the structural performance all the patterns with flat structure



## Model properties





## Model properties

### Material:

- Pine wood

### Cross-section :

- 15cm x 24.75cm (H/B ratio is 1.65)

### Joints:

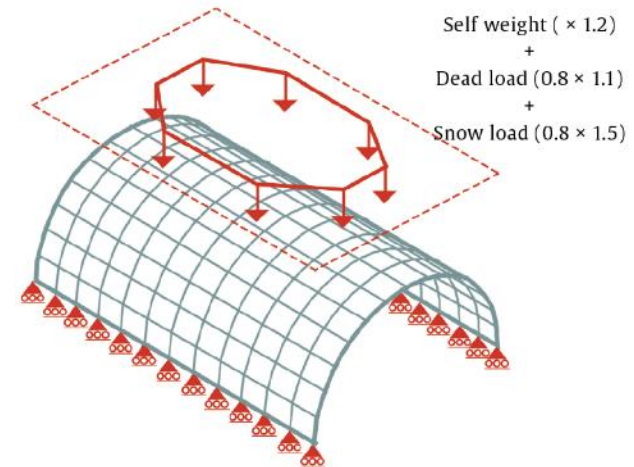
- Fixed joint (metal connection)

### Planarity:

- Linear elements without bend

### Grid Density :

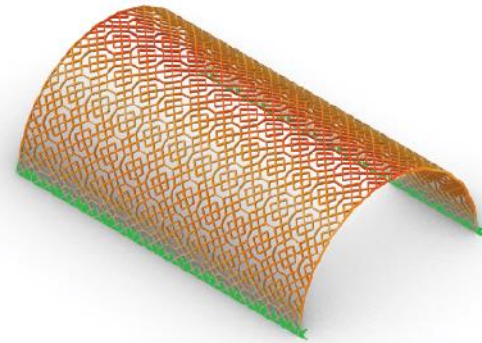
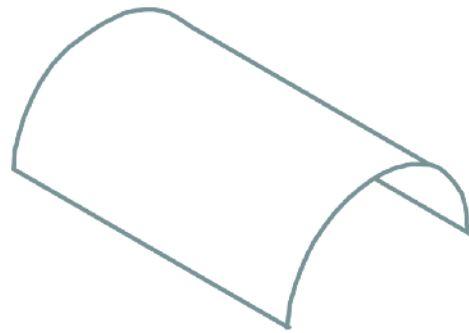
- Grid density is used which is closest to 3200m





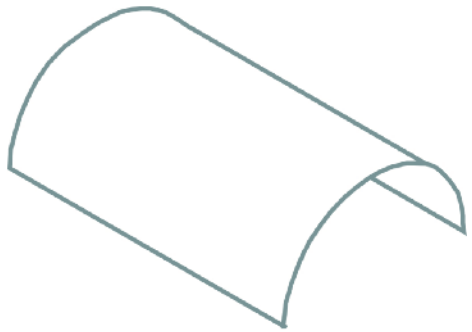


## Parametric workflow

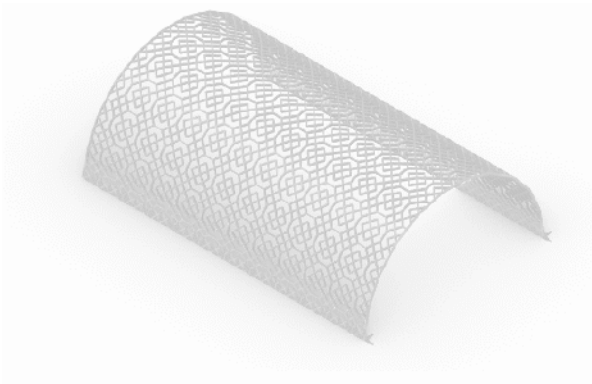




## Parametric workflow

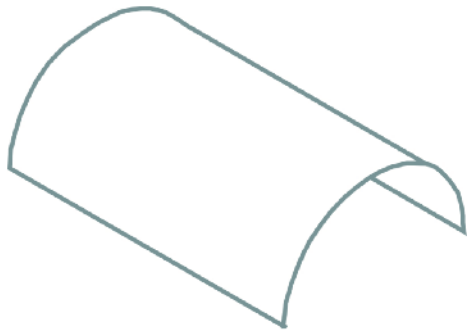


- Untrimmed surface of form

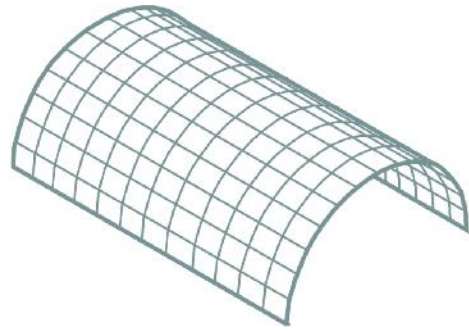




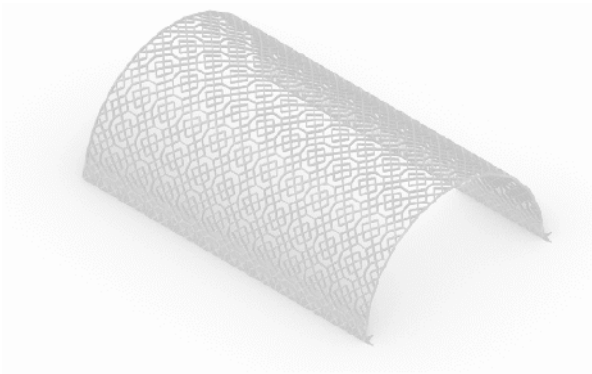
## Parametric workflow



- Untrimmed surface of form

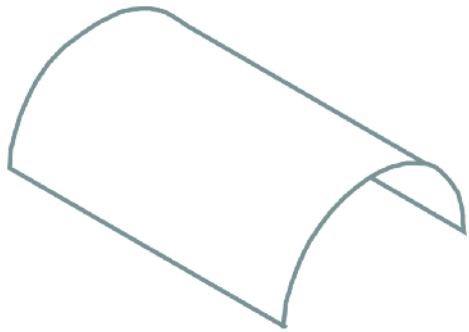


- Mesh division as per grid factor

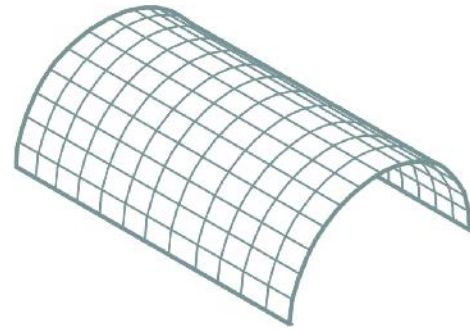




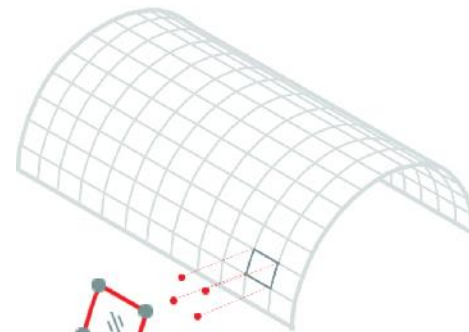
### Parametric workflow



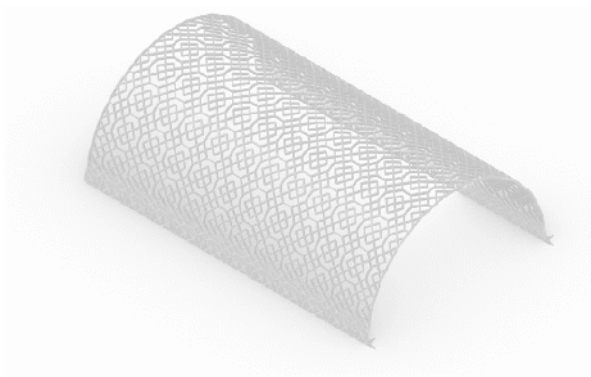
- Untrimmed surface of form



- Mesh division as per grid factor

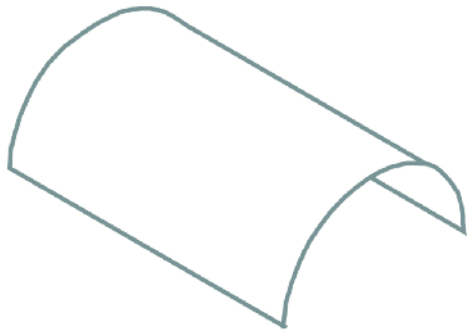


- Regenerate individual surfaces

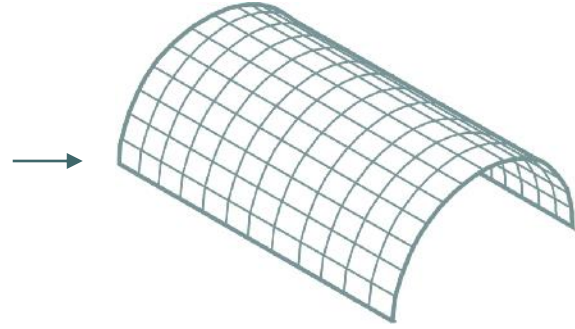




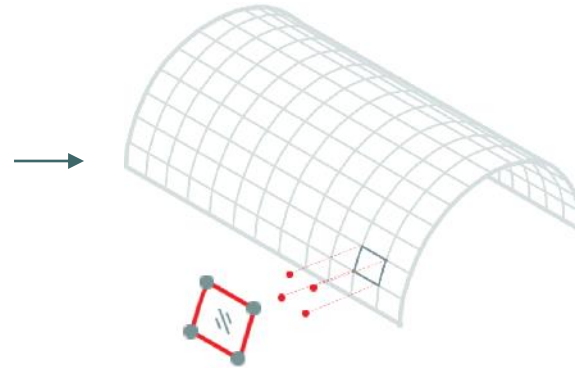
### Parametric workflow



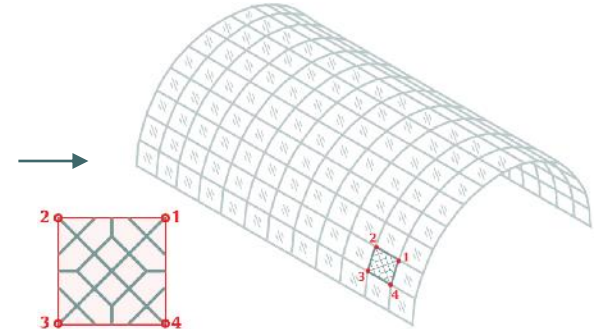
- Untrimmed surface of form



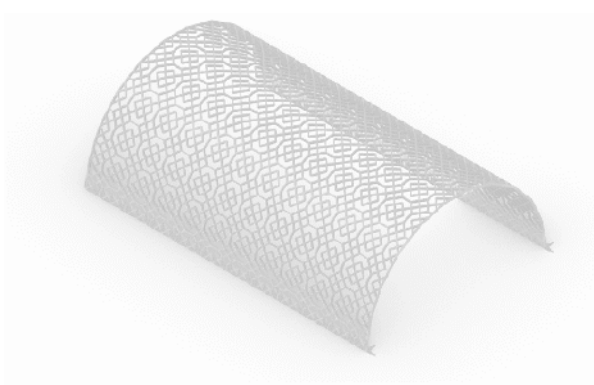
- Mesh division as per grid factor



- Regenerate individual surfaces

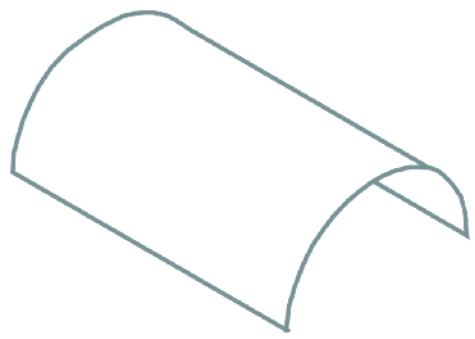


- Morph patterns with reference

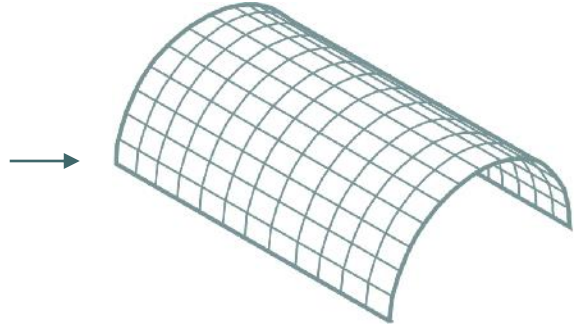




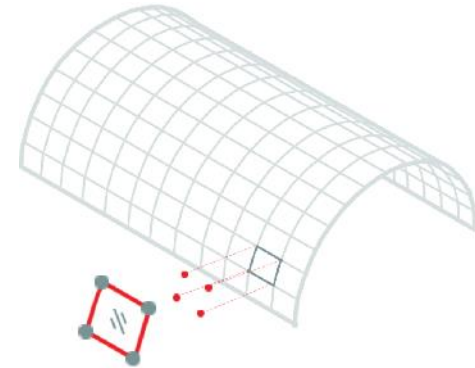
### Parametric workflow



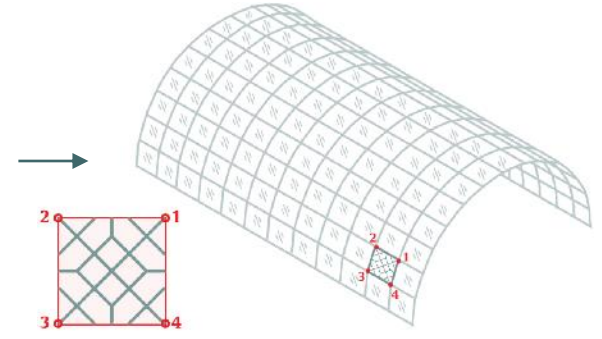
• Untrimmed surface of form



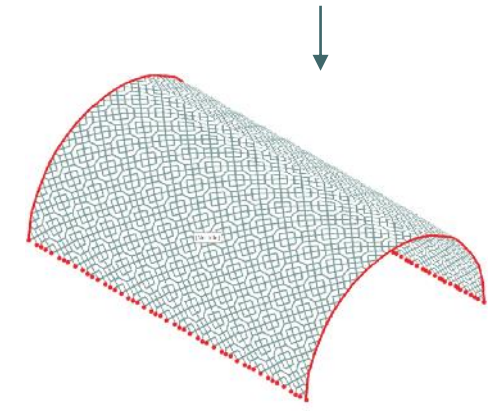
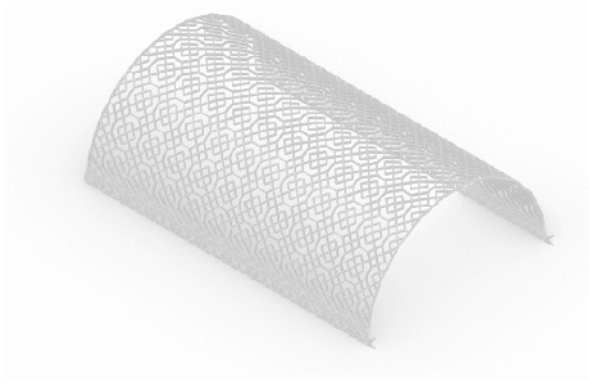
• Mesh division as per grid factor



• Regenerate individual surfaces



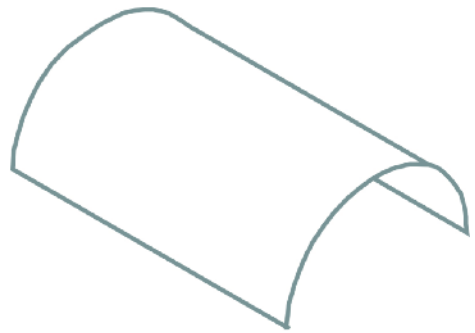
• Morph patterns with reference



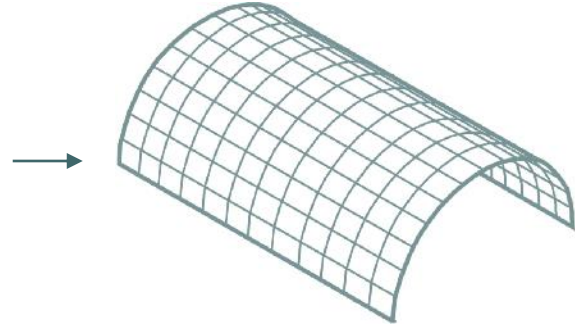
• Arrange ends and support points



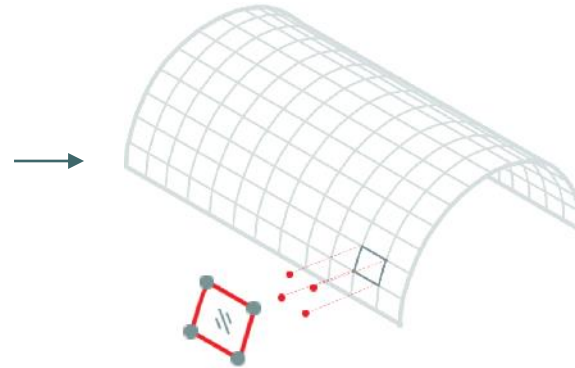
### Parametric workflow



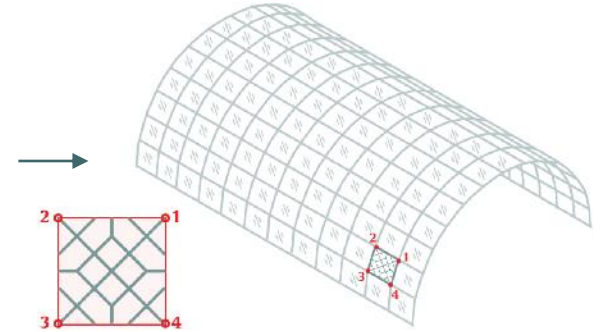
• Untrimmed surface of form



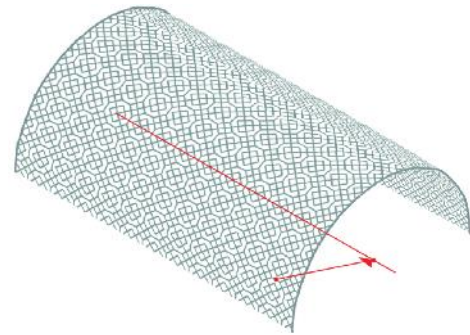
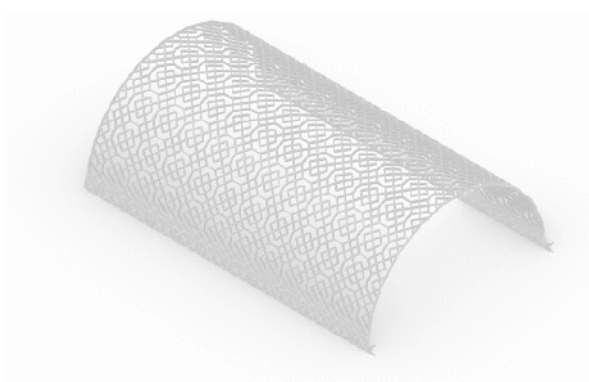
• Mesh division as per grid factor



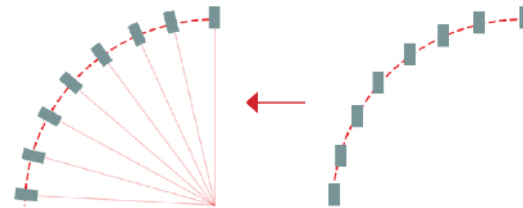
• Regenerate individual surfaces



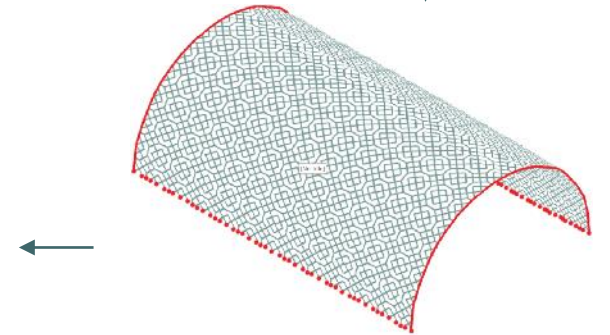
• Morph patterns with reference



• Direction vector for cross-section



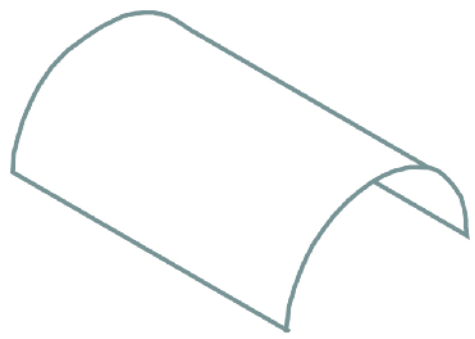
• Rotating local Z axis



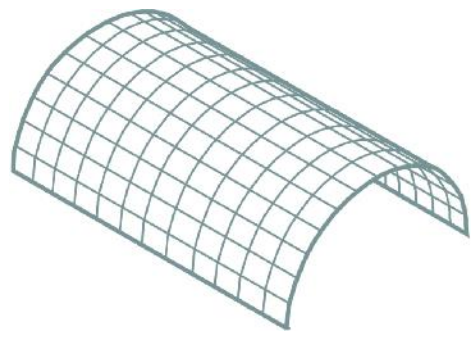
• Arrange ends and support points



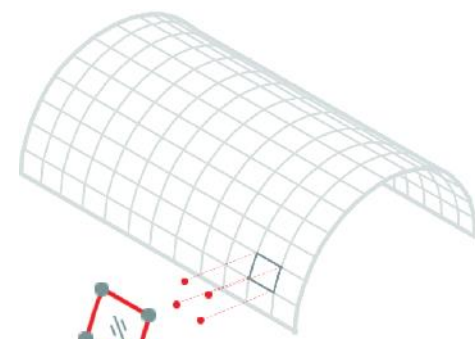
### Parametric workflow



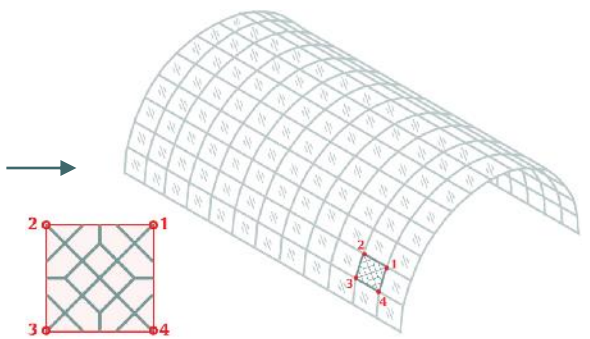
• Untrimmed surface of form



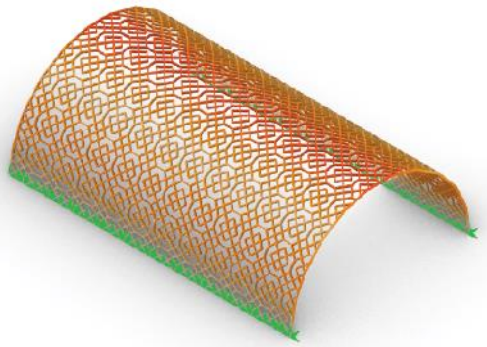
• Mesh division as per grid factor



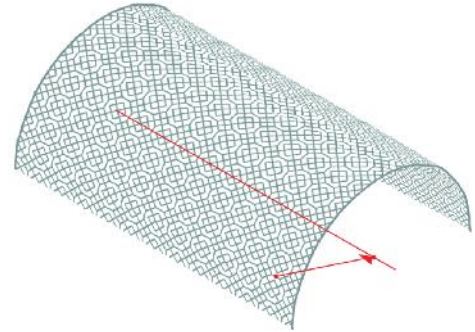
• Regenerate individual surfaces



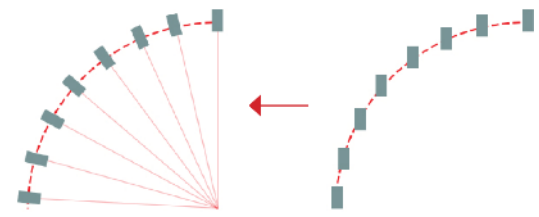
• Morph patterns with reference



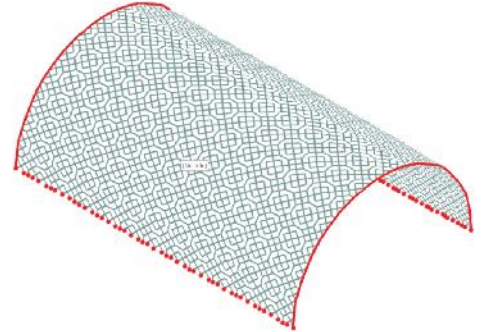
• Setup for structural analysis



• Direction vector for cross-section



• Rotating local Z axis

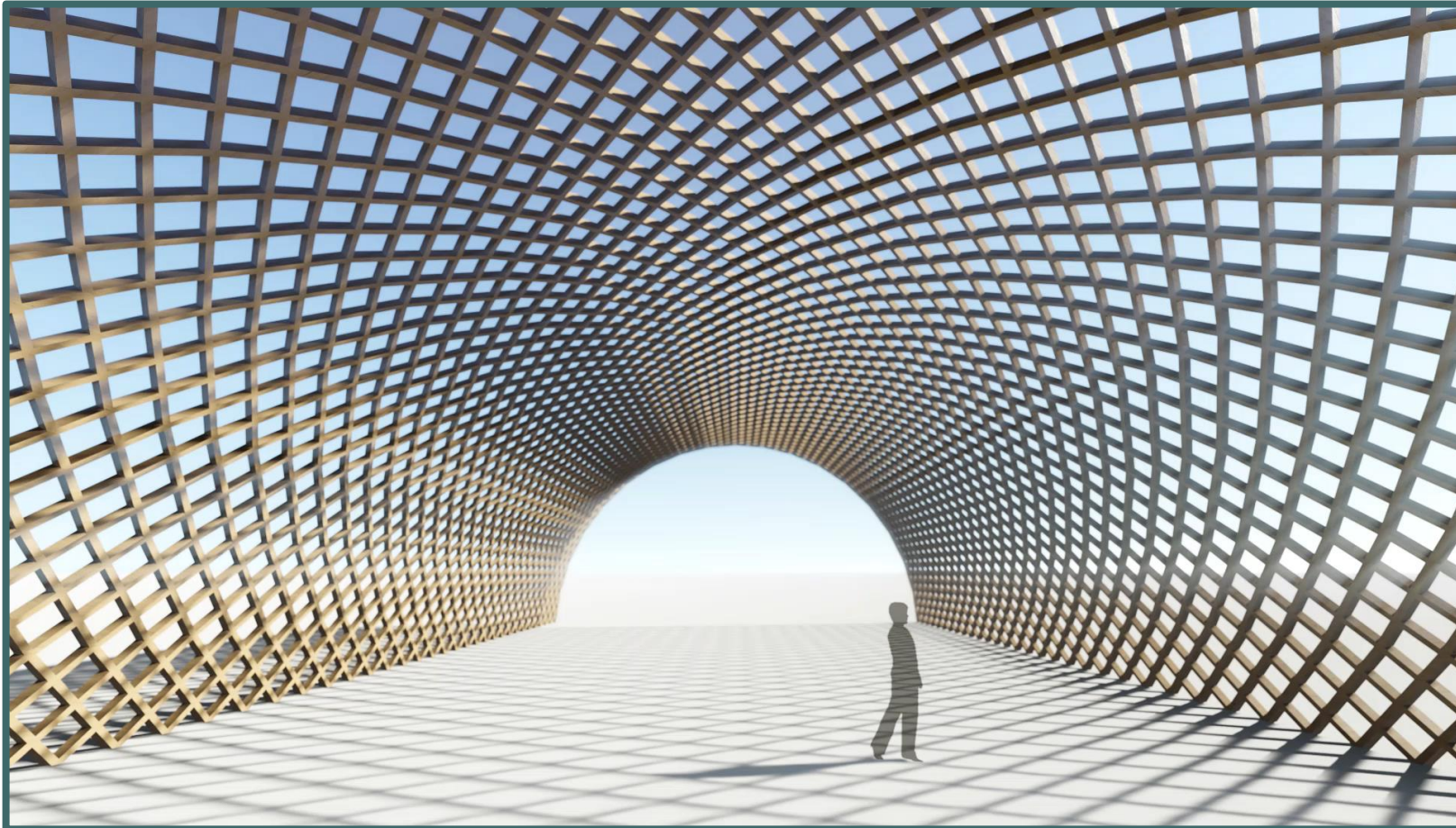


• Arrange ends and support points





## Parametric workflow





## Structural analysis

### Example 1 (B6b\_4)

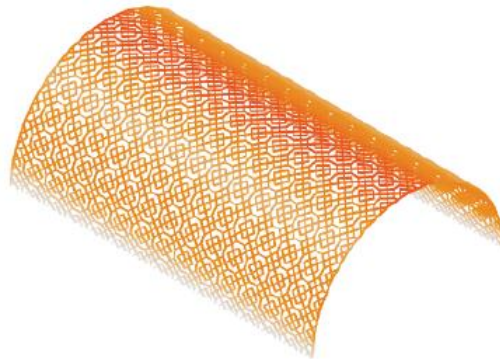


Experiential quality

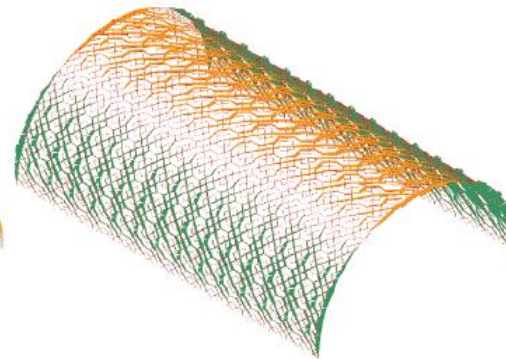
Grid density : 3255.96  
Grid Factor : 19

	Value	% Difference
Deflection (mm)	173.02	29.86
Avg Max Axial Stress (MPa)	4.70	22.50
Avg Min Axial Stress (MPa)	-4.70	22.50
Avg Normal Force (N)	-12,537.36	27.25
Avg Bending Moment (Nmm)	81,36,800.00	14.28
Avg Shear Force (N)	5,152.50	-11.25
Avg Utilization Ratio	0.08	22.50
Buckling Factor	3.56	-13.56

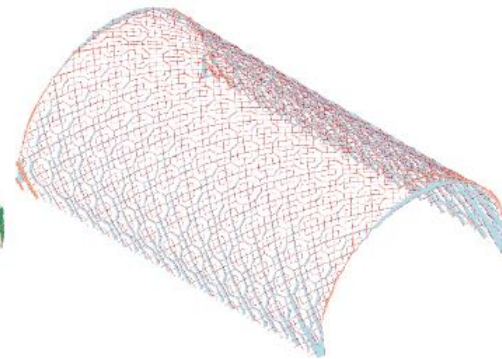
Structural performance



Deformation in Vault



Bending moment in Vault



Normal force in Vault



## Structural analysis

### Example 1 (B6b\_4)

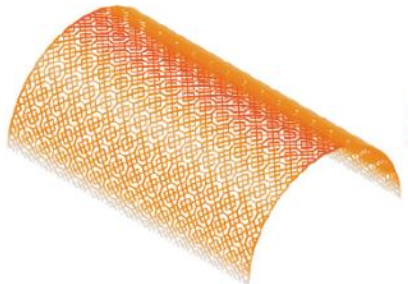


Experiential quality

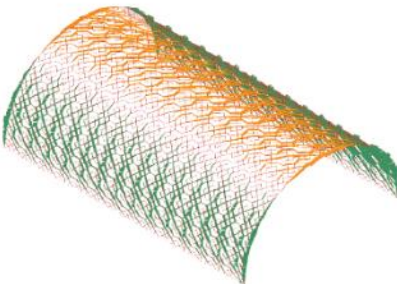
Grid density : 3255.96  
Grid Factor : 19

	Value	% Difference
Deflection (mm)	173.02	29.86
Avg Max Axial Stress (MPa)	4.70	22.50
Avg Min Axial Stress (MPa)	-4.70	22.50
Avg Normal Force (N)	-12,537.36	27.25
Avg Bending Moment (Nmm)	81,36,800.00	14.28
Avg Shear Force (N)	5,152.50	-11.25
Avg Utilizatio Ratio	0.08	22.50
Buckling Factor	3.56	-13.56

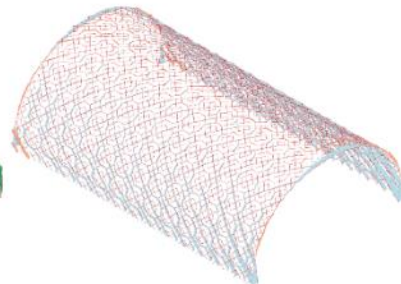
Structural performance



Deformation in Vault



Bending moment in Vault



Normal force in Vault

### Example 2 (B14a\_1)

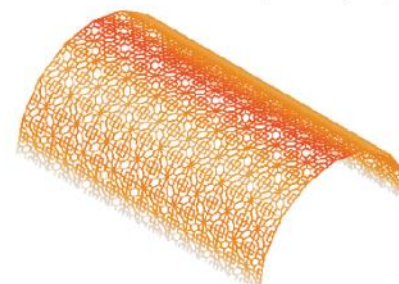


Experiential quality

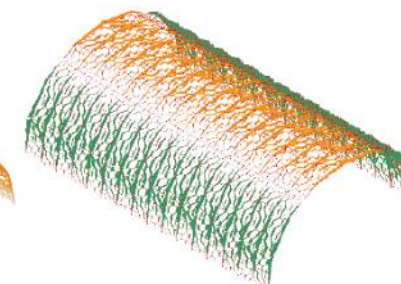
Grid density : 3213.69  
Grid Factor : 8

	Value	% Difference
Deflection (mm)	113.40	-14.88
Avg Max Axial Stress (MPa)	3.48	-9.38
Avg Min Axial Stress (MPa)	-3.48	-9.38
Avg Normal Force (N)	-9,882.90	0.31
Avg Bending Moment (Nmm)	66,60,200.00	-6.46
Avg Shear Force (N)	4,420.17	-23.87
Avg Utilizatio Ratio	0.06	-9.38
Buckling Factor	4.25	3.23

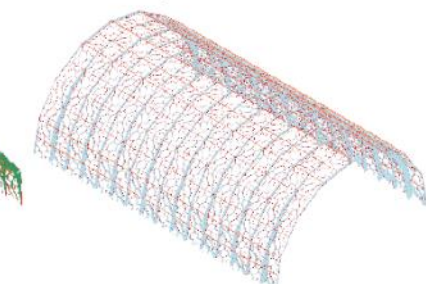
Structural performance



Deformation in Vault



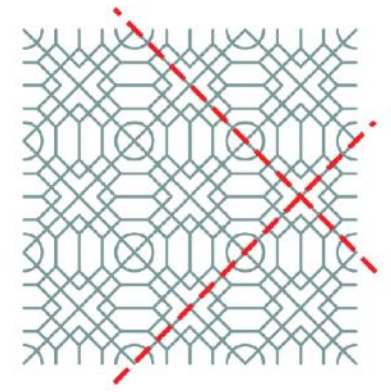
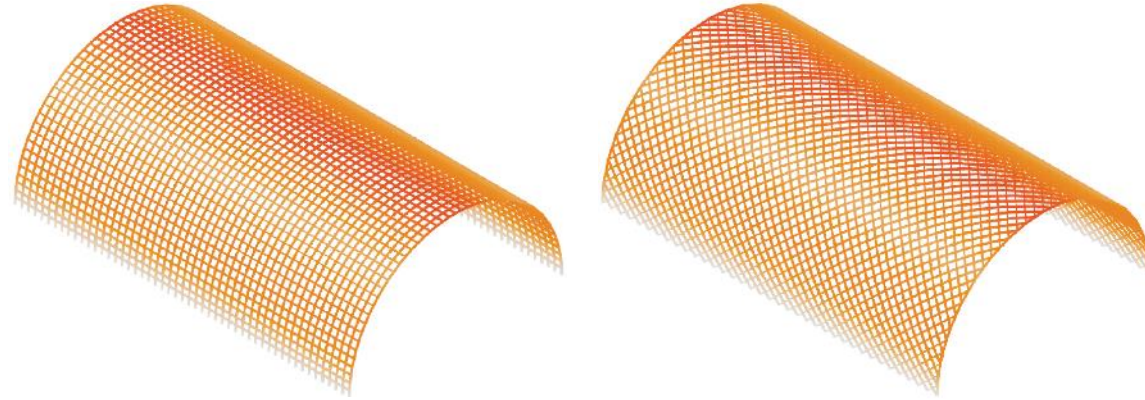
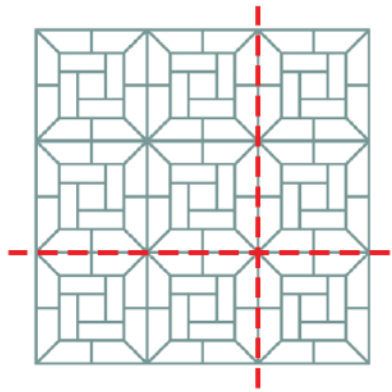
Bending moment in Vault



Normal force in Vault



## Conclusion



	Parallel grid		Diagonal grid	
	Value	% Difference	Value	% Difference
Deflection (mm)	99.11	<b>-25.61</b>	150.98	<b>13.32</b>
Avg Max Axial Stress (MPa)	2.94	<b>-23.31</b>	5.13	<b>33.66</b>
Avg Min Axial Stress (MPa)	-2.94	<b>-23.31</b>	-5.13	<b>33.66</b>
Avg Normal Force (N)	-9,120.55	<b>-7.43</b>	-12,566.06	<b>27.54</b>
Avg Bending Moment (Nmm)	59,63,500.00	<b>-16.24</b>	85,53,700.00	<b>20.14</b>
Avg Shear Force (N)	1,908.36	<b>-67.13</b>	5,434.90	<b>-6.39</b>
Avg Utilizatio Ratio	0.05	<b>-23.31</b>	0.09	<b>33.66</b>
Buckling Factor	5.29	<b>28.65</b>	4.15	<b>0.73</b>



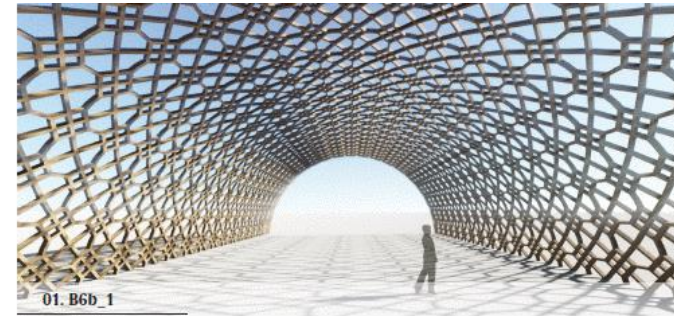
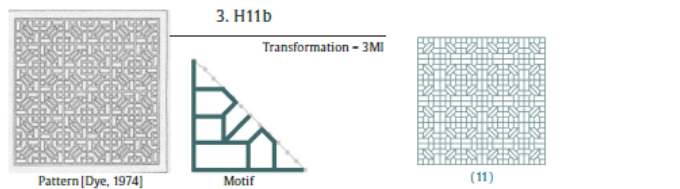
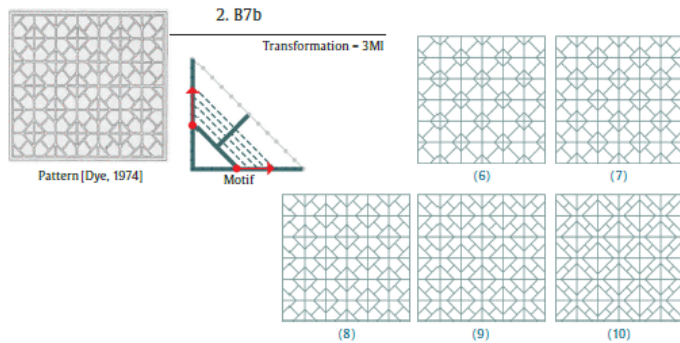
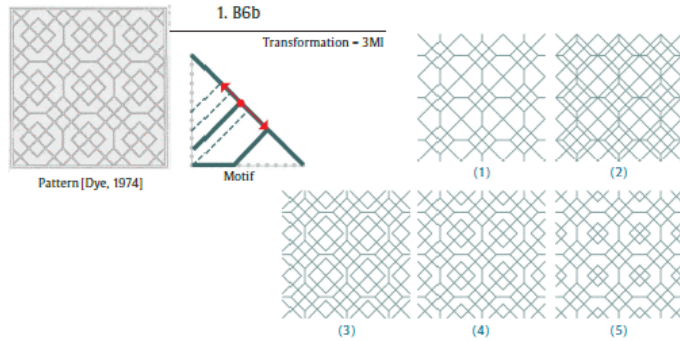
## Conclusion

Vault grid-shell										
	Name	Grid Density	Grid Factor	Deflection (mm)	Avg Max Axial Stress (MPa)	Avg Min Axial Stress (MPa)	Avg Normal Force (N)	Avg Bending Moment (Nmm)	Avg Shear Force (N)	Utilizatio Ratio
1	B6b_1	53.80712	10	142.674739	4.526132	-4.526132	-12003.35927	7.96E+06	5295.29218	0.075436
2	B6b_2	49.25483	6	143.818666	4.998356	-4.998356	-12936.70664	8.50E+06	5764.24522	0.083306
3	B6b_3	54.16414	7	181.170517	5.081687	-5.081687	-13521.19348	8.72E+06	5479.03834	0.084695
4	B6b_4	50.86431	7	173.019128	4.700963	-4.700963	-12537.36331	8.14E+06	5152.50442	0.078349
5	B6b_5	54.3594	8	167.197557	4.3592	-4.3592	-11675.58168	7.60E+06	4889.2192	0.072653
6	B7b_1	54.04857	7	127.747519	3.201299	-3.201299	-8541.624977	6.31E+06	2885.27058	0.053355
7	B7b_2	55.69849	7	132.819886	3.363313	-3.363313	-8983.894735	6.68E+06	2832.16039	0.056055
8	B7b_3	48.87006	6	131.205011	3.364779	-3.364779	-9011.632136	6.70E+06	2722.7343	0.05608
9	B7b_4	50.28427	6	128.8562	3.386394	-3.386394	-9099.710881	6.71E+06	2676.23182	0.05644
10	B7b_5	51.69849	6	131.56074	3.606567	-3.606567	-9824.516329	7.16E+06	2808.78534	0.060109
11	H11b_1	56.14214	4	110.828579	3.511762	-3.511762	-9758.138038	6.63E+06	5616.45503	0.058529
12	H13a_1	53.11845	5	98.575846	3.30986	-3.30986	-9677.236131	6.41E+06	5052.70742	0.055164
13	H13a_2	54.09476	5	96.499585	3.427171	-3.427171	-9648.531026	6.53E+06	4035.05818	0.05712
14	H13a_3	55.07107	5	94.465886	3.433348	-3.433348	-9536.164471	6.51E+06	3647.75506	0.057222
15	H14a_1	51.45178	5	107.228648	3.683131	-3.683131	-9364.753331	6.89E+06	6155.69451	0.061386
16	H14a_2	49.43994	5	107.450646	3.569813	-3.569813	-9034.457573	6.71E+06	6464.49082	0.059497
17	H14a_3	57.31371	6	107.499951	3.388919	-3.388919	-8715.588231	6.43E+06	6962.85358	0.056482
18	H14a_4	50.96362	5	107.083752	3.675677	-3.675677	-9337.30702	6.81E+06	6285.09028	0.061261
19	H14a_5	48.95178	5	107.136068	3.475002	-3.475002	-8956.70773	6.54E+06	6754.79941	0.057917
20	H14a_6	56.72792	6	106.773644	3.200233	-3.200233	-8617.106877	6.12E+06	6971.87067	0.053337
21	H14a_7	50.47547	5	106.665669	3.533503	-3.533503	-9246.603068	6.63E+06	6613.36324	0.058892
22	L3a_1	55.55922	5	100.983818	3.457286	-3.457286	-9391.946523	6.48E+06	4929.07514	0.057621
23	L3a_2	55.07107	5	100.262975	3.364561	-3.364561	-9515.340874	6.37E+06	5357.22647	0.056076
24	L3a_3	54.58291	5	99.181397	3.224124	-3.224124	-9489.845507	6.14E+06	5669.43182	0.053735
25	L3a_4	54.09476	5	96.958732	3.330966	-3.330966	-10178.32067	6.51E+06	3132.47606	0.055516
26	L3a_5	53.6066	5	101.030634	3.723025	-3.723025	-10917.47268	7.08E+06	4928.91213	0.06205
27	L3a_6	55.07107	5	103.000299	3.50522	-3.50522	-9593.164974	6.56E+06	5057.6157	0.05842
28	L3a_7	54.58291	5	102.25371	3.397674	-3.397674	-9716.045165	6.43E+06	5475.27063	0.056628
29	L3a_8	54.09476	5	101.119968	3.244212	-3.244212	-9653.615312	6.18E+06	5804.77914	0.05407
30	L3a_9	53.6066	5	98.790645	3.344235	-3.344235	-10290.24223	6.55E+06	3289.25887	0.055737
31	L3a_10	53.11845	5	102.792309	3.677666	-3.677666	-10962.75957	7.06E+06	5482.21989	0.061294
32	Q5a_1	55.10457	8	146.90749	3.505169	-3.505169	-8657.220986	6.70E+06	7445.40733	0.058419
33	Q5a_2	50.29983	7	151.583651	3.575811	-3.575811	-8502.324746	6.82E+06	6961.31077	0.059597
34	Q5a_3	52.63317	7	164.586507	3.813874	-3.813874	-8715.839244	7.37E+06	6673.98026	0.063565

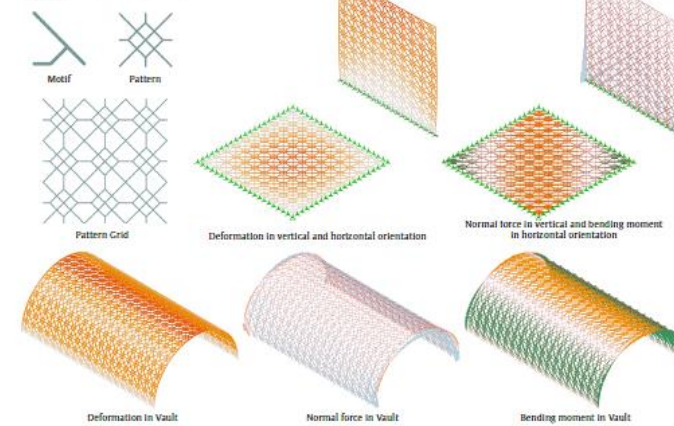
Vertical orientation										
	Name	Grid Density	Grid Factor	Deflection (mm)	Avg Max Axial Stress (MPa)	Avg Min Axial Stress (MPa)	Avg Normal Force (N)	Avg Bending Moment (Nmm)	Avg Shear Force (N)	Utilizatio Ratio
1	B6b_1	53.80712	10	0.119507	0.646674	-1.084178	-10.997511	50.361426	3.896257	0.01807
2	B6b_2	49.25483	6	0.194597	0.724157	-1.162824	-10.974681	54.91169	2.85573	0.01938
3	B6b_3	54.16414	7	0.18533	0.806158	-1.247631	-11.054369	59.754702	3.535866	0.020794
4	B6b_4	50.86431	7	0.178345	0.729878	-1.143098	-10.36313	54.496527	3.215579	0.019052
5	B6b_5	54.3594	8	0.159593	0.643885	-1.042932	-10.023587	49.074951	3.283307	0.017382
6	B7b_1	54.04857	7	0.044501	0.03641	-0.365624	-8.317073	11.699934	0.918942	0.006094
7	B7b_2	55.69849	7	0.045378	0.016511	-0.354109	-8.517386	10.789159	0.773711	0.005902
8	B7b_3	48.87006	6	0.046319	0.017266	-0.358627	-8.639429	10.946828	0.695278	0.005977
9	B7b_4	50.28427	6	0.046399	0.019799	-0.372294	-8.923388	11.413783	0.725996	0.006205
10	B7b_5	51.69849	6	0.046226	0.02602	-0.391641	-9.262569	12.168291	0.813179	0.006527
11	H11b_1	56.14214	4	0.060816	0.258854	-0.607128	-8.778141	25.189863	1.711344	0.010119
12	H13a_1	53.11845	5	0.040285	0.152485	-0.499276	-8.752348	18.978374	1.294714	0.008321
13	H13a_2	54.09476	5	0.044562	0.138789	-0.49177	-8.894264	18.362856	1.079467	0.008196
14	H13a_3	55.07107	5	0.046209	0.144098	-0.507182	-9.14923	18.96542	1.150414	0.008453
15	H14a_1	51.45178	5	0.067428	0.424524	-0.763872	-8.607468	34.561748	2.437371	0.012731
16	H14a_2	49.43994	5	0.063129	0.458915	-0.785868	-8.287613	36.205253	2.417668	0.013098
17	H14a_3	57.31371	6	0.048291	0.333902	-0.660054	-8.232996	28.912641	2.547718	0.011001
18	H14a_4	50.96362	5	0.067408	0.463717	-0.798243	-8.47943	36.707161	2.258415	0.013304
19	H14a_5	48.95178	5	0.058762	0.447488	-0.772418	-8.210882	35.483686	2.366692	0.012874
20	H14a_6	56.72792	6	0.041225	0.238126	-0.562731	-8.19097	23.297326	2.464623	0.009379
21	H14a_7	50.47547	5	0.060949	0.441916	-0.776106	-8.45209	35.432528	2.275597	0.012935
22	L3a_1	55.55922	5	0.056545	0.288321	-0.642617	-8.932763	27.082128	1.734243	0.01071
23	L3a_2	55.07107	5	0.052929	0.284256	-0.639508	-8.970244	26.871893	1.758937	0.010658
24	L3a_3	54.58291	5	0.044967	0.22253	-0.579592	-9.016377	23.341276	1.917389	0.00966
25	L3a_4	54.09476	5	0.036361	0.028699	-0.414591	-9.726484	12.917086	0.820309	0.00691
26	L3a_5	53.6066	5	0.041963	0.212884	-0.614182	-10.150877	24.075123	1.802434	0.010236
27	L3a_6	55.07107	5	0.059824	0.289547	-0.640783	-8.854263	27.066173	1.735865	0.01068
28	L3a_7	54.58291	5	0.055536	0.283223	-0.63595	-8.897114	26.74239	1.763104	0.010599
29	L3a_8	54.09476	5	0.04655	0.217237	-0.571897	-8.9427	22.964429	1.928118	0.009532
30	L3a_9	53.6066	5	0.036994	0.011801	-0.394378	-9.632958	11.838819	0.75802	0.006573
31	L3a_10	53.11845	5	0.041044	0.190702	-0.588558	-10.068822	22.683464	1.836354	0.009809
32	Q5a_1	55.10457	8	0.072032	0.359251	-0.663927	-7.69311	29.76016	2.20921	0.011065
33	Q5a_2	50.29983	7	0.083844	0.382877	-0.677023	-7.443853	30.8367	1.912319	0.011284
34	Q5a_3	52.63317	7	0.091665	0.363819	-0.661458	-7.504506	29.819956	1.844863	0.011024



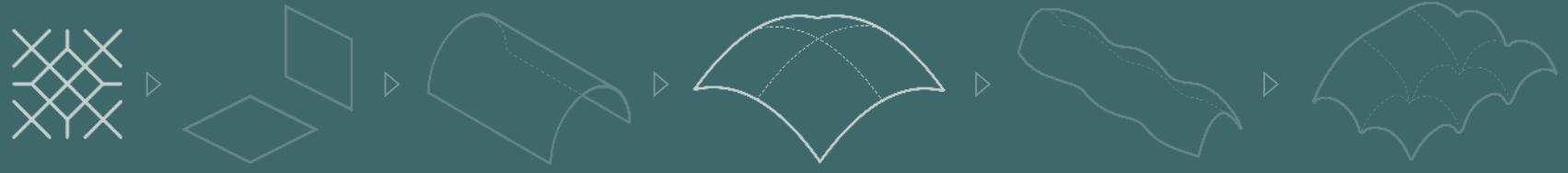
## Pattern Catalogue

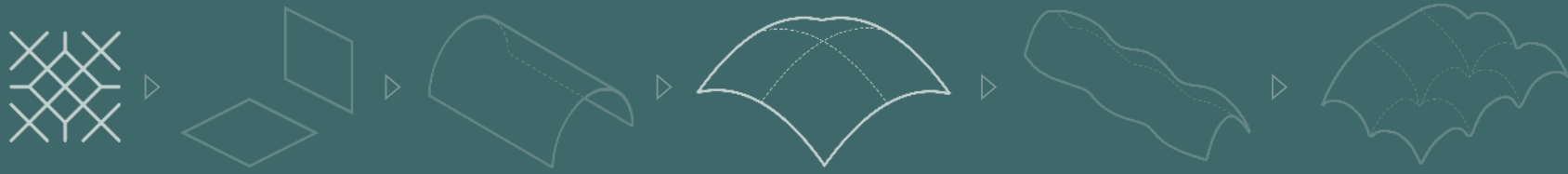


Transformation	3 MI
Grid Density	53.8071   0.90712
Grid Factor	10



	Horizontal		Vertical		Vault	
	Value	% Difference	Value	% Difference	Value	% Difference
Deflection (mm)	59.85	-25.61	0.12	20.62	142.67	7.09
Avg Max Axial Stress (MPa)	19.19	4.62	0.65	51.25	4.53	17.94
Avg Min Axial Stress (MPa)	-19.19	4.62	-1.08	40.64	-4.53	17.94
Avg Normal Force (N)	-	-	-11.00	27.12	-12,003.36	21.83
Avg Bending Moment (Nmm)	1,122.02	-1.39	50.36	44.45	79,64,600.00	11.86
Avg Shear Force (N)	10.80	-3.61	3.90	72.13	5,295.29	-8.79
Avg Utilization Ratio	0.32	4.62	0.02	40.64	0.08	17.94
Buckling Factor	-	-	-	-	4.39	6.70

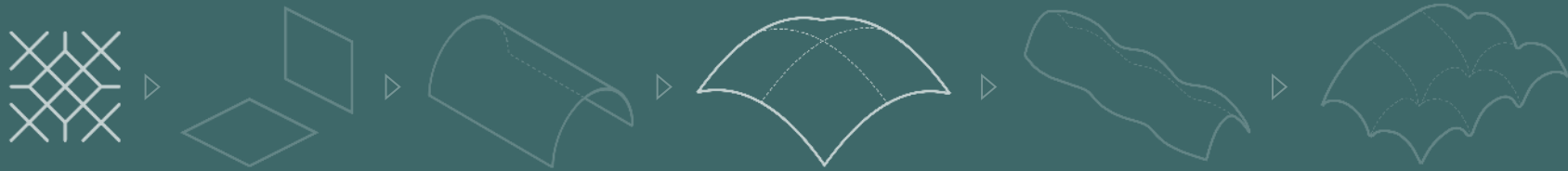




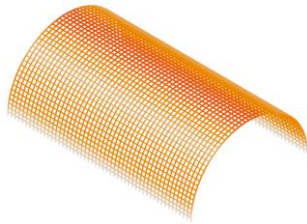
### Aim:

- Arrange multi-objective optimization setup to find optimum material quantity.
- Validate the usability of results in pattern catalogue.

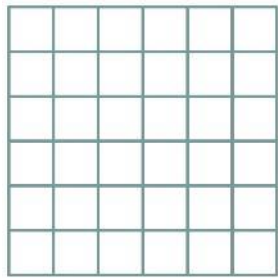




## Use of Pattern Catalogue

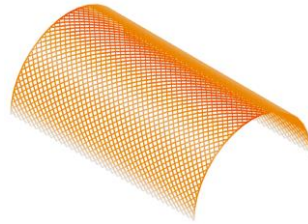


82

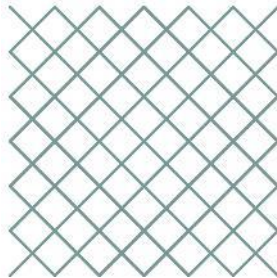


Value	% Difference
99.11	<b>-25.61</b>

1



83

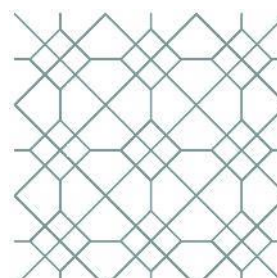


Value	% Difference
150.98	<b>13.32</b>

4

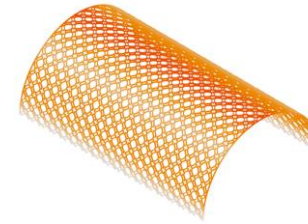


1

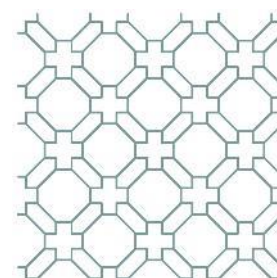


Value	% Difference
142.67	<b>7.09</b>

3

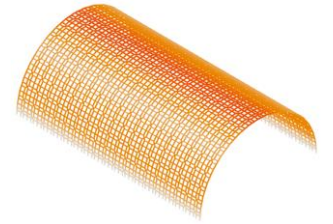


45

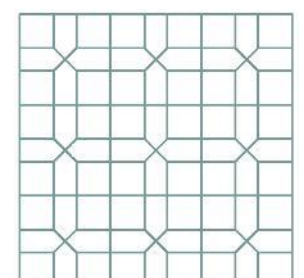


Value	% Difference
198.68	<b>49.12</b>

5



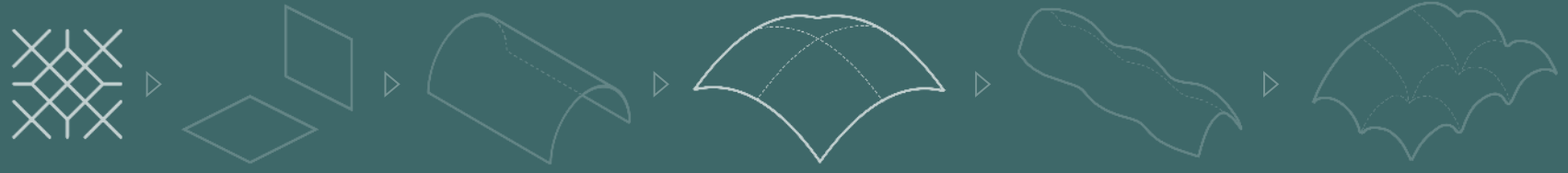
65



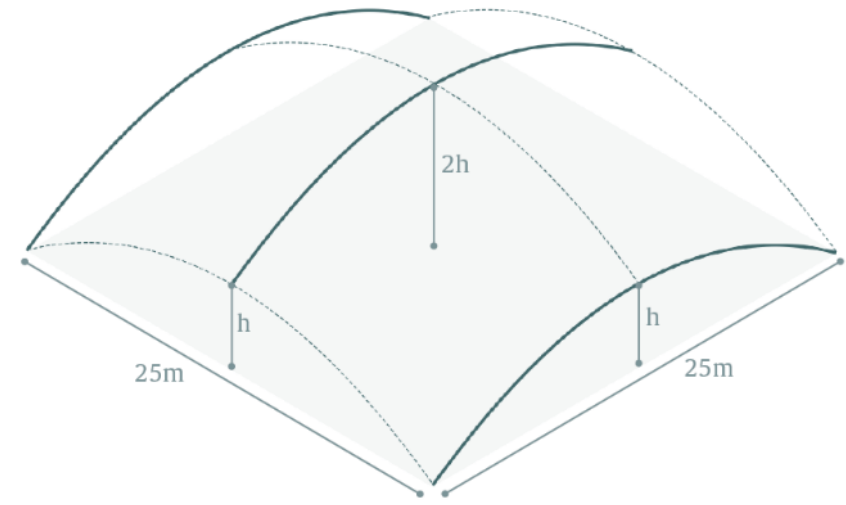
Value	% Difference
109.15	<b>-18.08</b>

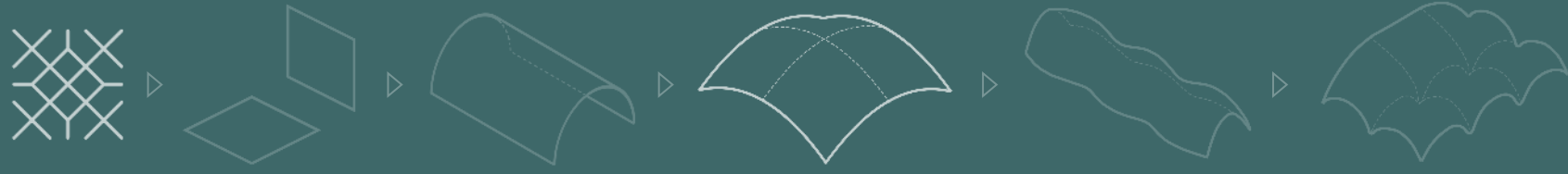
2

Deflection (mm)

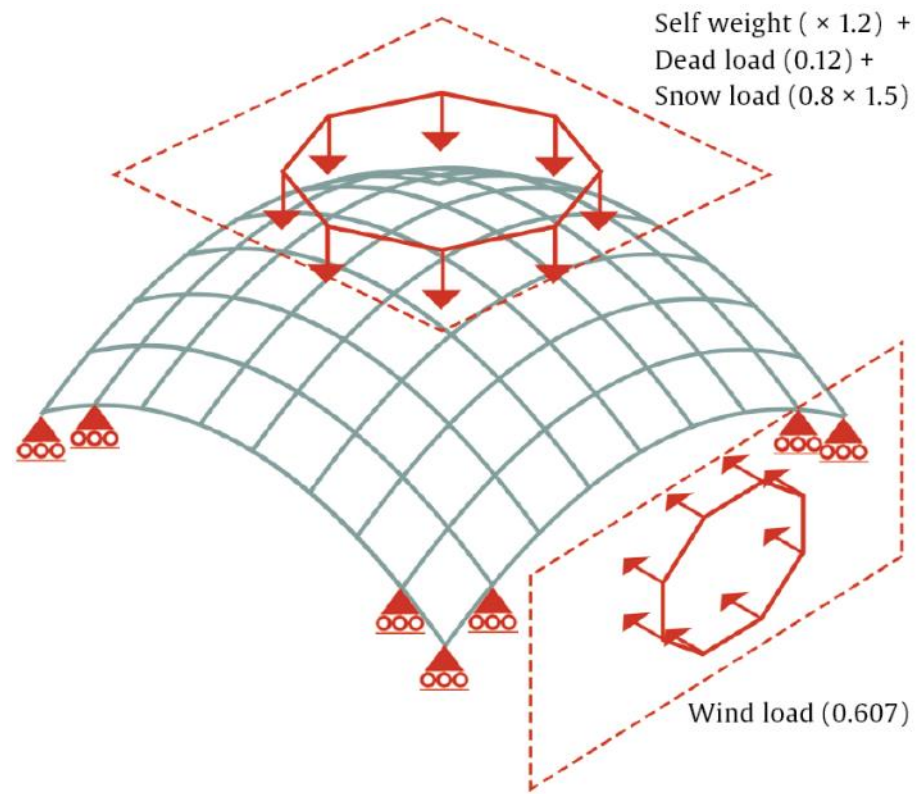


## Model properties



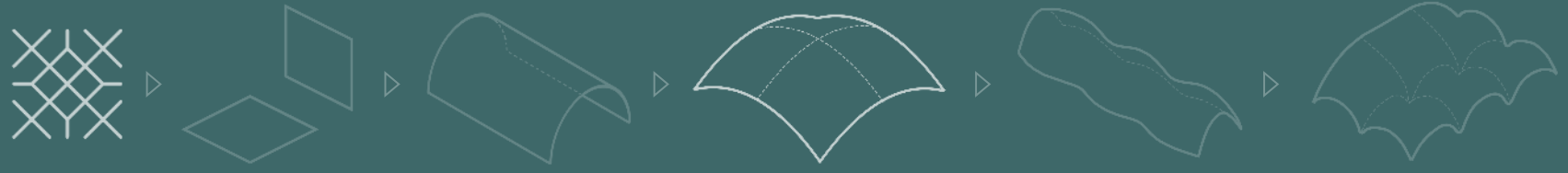


### Model properties

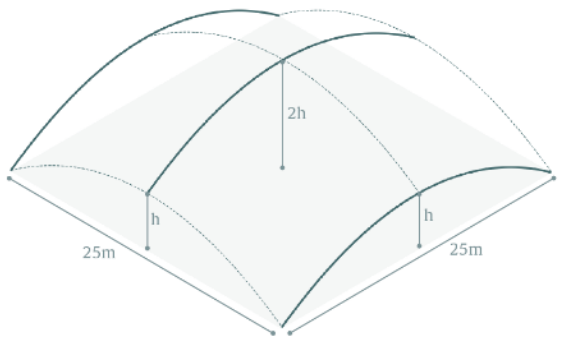


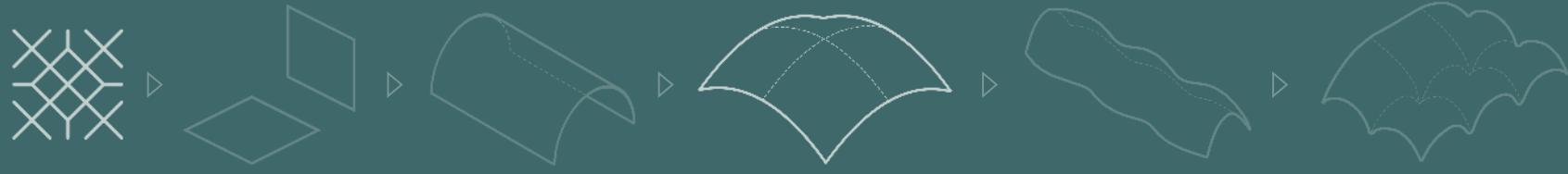
Self weight (  $\times 1.2$  ) +  
Dead load (0.12) +  
Snow load (  $0.8 \times 1.5$  )

Wind load (0.607)

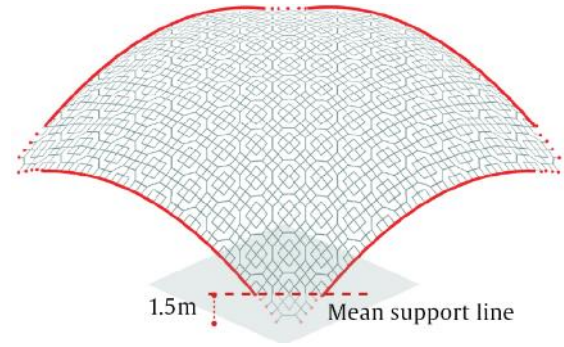
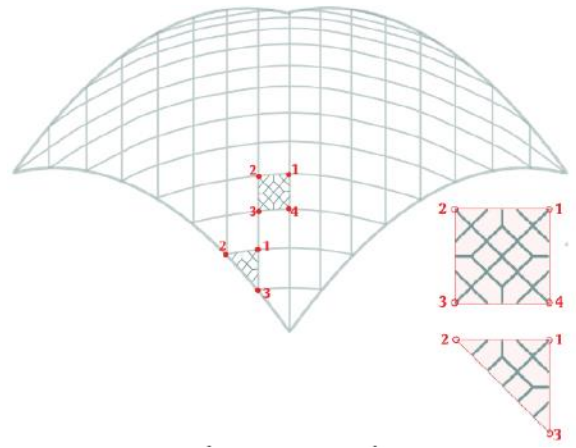
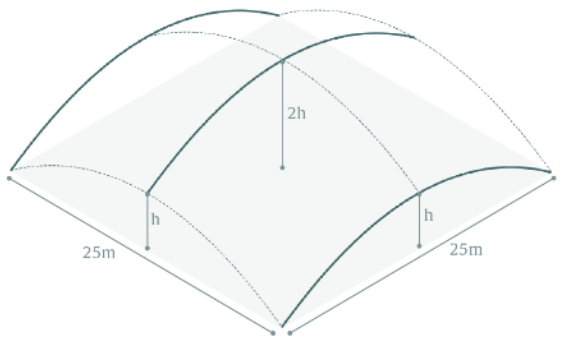


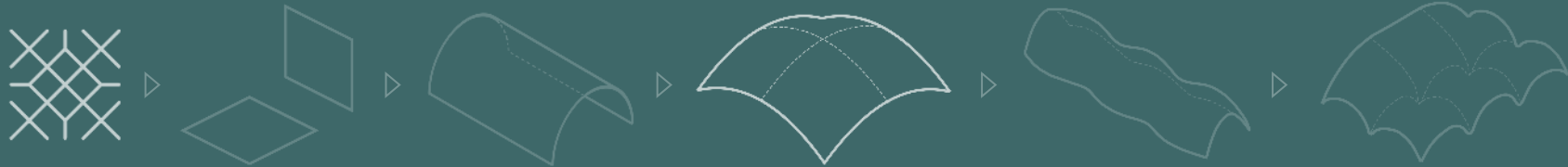
Parametric workflow



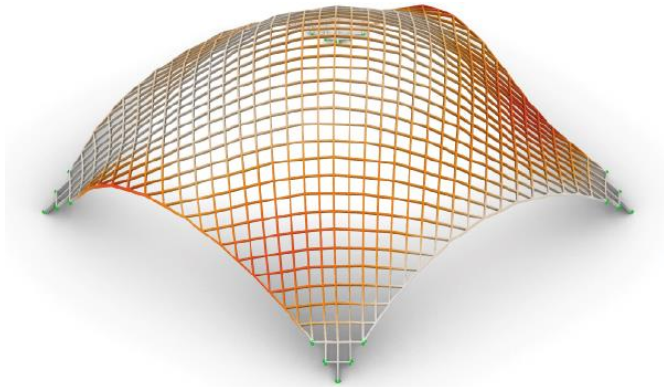


### Parametric workflow





## Material quantity optimization



Scaled visualization of deflection

Grid factor = 10  
 Cross-section width = 100.7mm  
 Height of opening = 6m

	Results	Allowable results
Deflection (mm)	141.3	Span/250 = 141.42 Height of C/S = 166.15
Max normal stress (MPa)	-30.36	60
Buckling factor	3.13	2
Max. utilization ratio	-0.506	1
Grid density (m)	1684.2	-
Volume (m3)	28.18	-

### Allowable limits

#### Allowable Deflection:

- Height of cross section
- or
- Shell span/250 (whichever is less)

#### Allowable maximum normal stress:

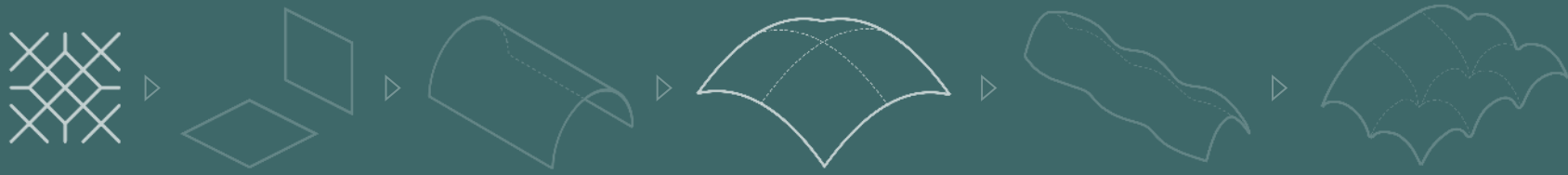
- Less than the yield strength of a material (<60 MPa)

#### Allowable buckling factor:

- >2

#### Minimum grid factor:

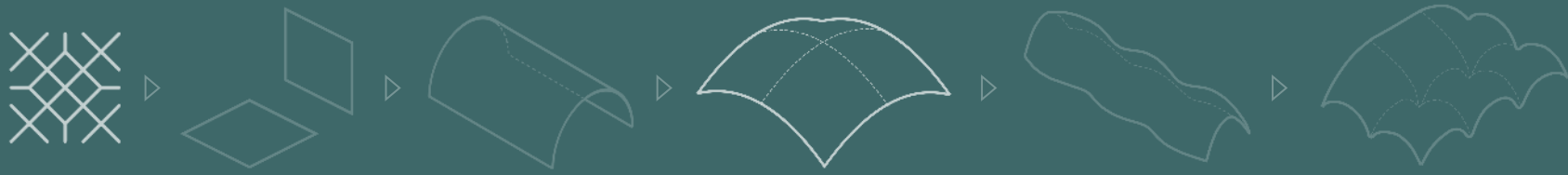
- 7 (to make it less course mesh)



## Material quantity optimization

### Multi objective optimization setup

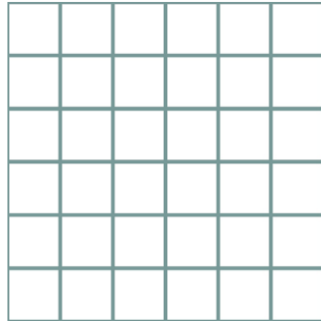
Objectives	Parameters
(V) Minimize Volume	(b) Cross-section width
( $\Delta$ ) Minimize Deflection (till the allowable limit)	(g) Grid factor (for grid-density)
(U) Maximize avg. Utilization ratio	(h) Height of opening



## Material quantity optimization

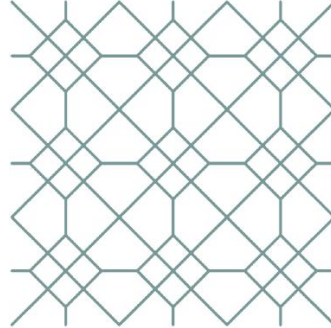
Rank as per the deflection  
of vault in catalogue

1



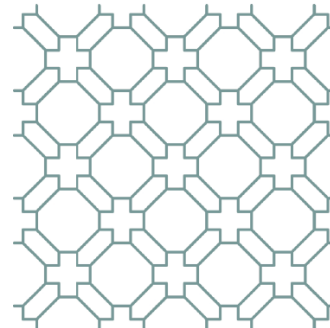
82

3



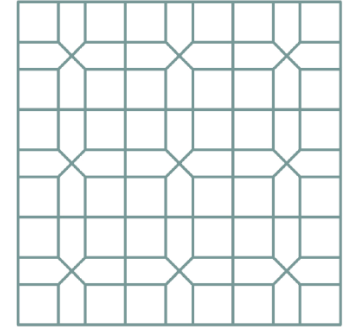
01

4



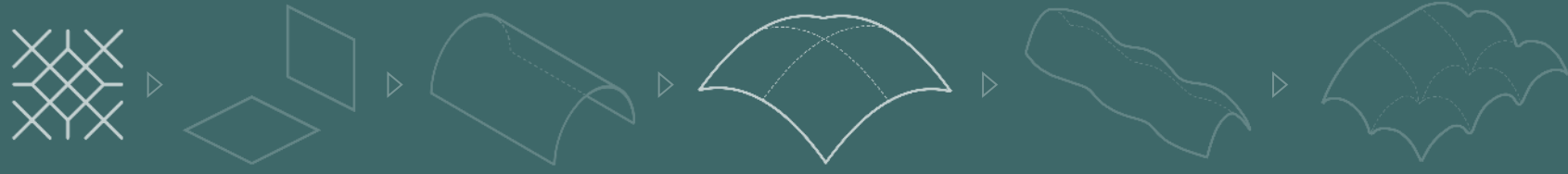
45

2

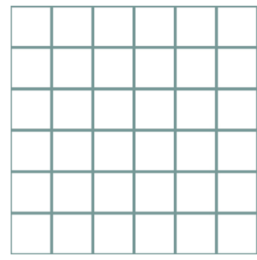


65



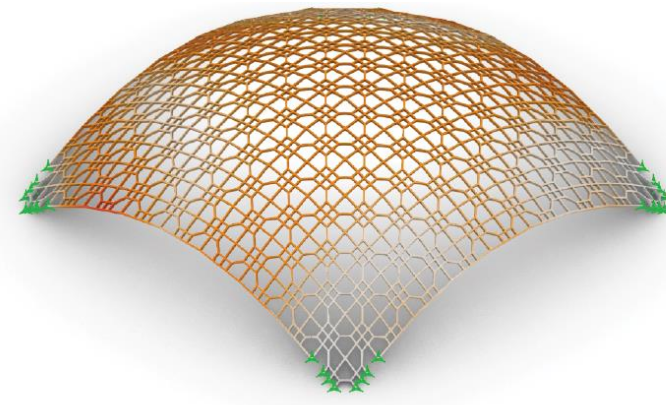
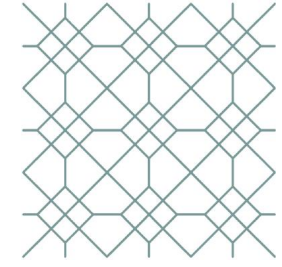


## Material quantity optimization



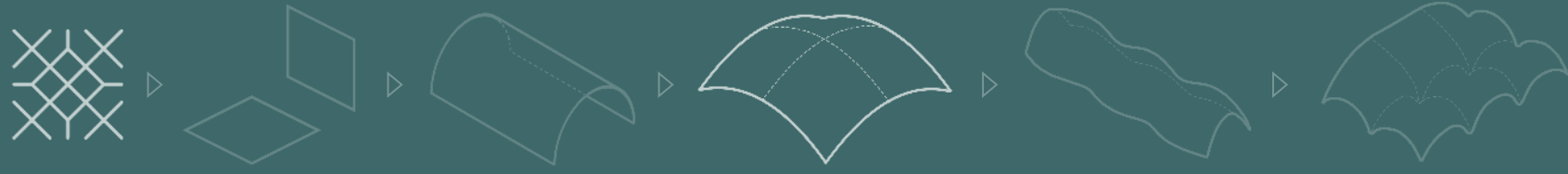
Pattern 82 (Parallel grid)		
Input	Fitness value	Performance value
	{48;19;0}	
8	813.88855	28.528732
11.36	2.690664	133.291409
5.25	6.253283	0.159916
	{48;40;0}	
8	501.030608	22.383713
10.2	0.522938	135.459135
4.66	4.943838	0.202272
	{48;41;0}	
8	477.184321	21.844549
10.1	5.607733	141.589806
4.51	4.806999	0.20803
	{49;11;0}	
8	479.076971	21.887827
10.11	4.947112	140.929185
4.51	4.822345	0.207368
	{49;22;0}	
8	479.076971	21.887827
10.11	4.947112	140.929185
4.51	4.822345	0.207368
	{49;28;0}	
8	479.076971	21.887827
10.11	4.947112	140.929185
4.51	4.822345	0.207368
	{49;47;0}	
8	511.424068	22.614687
10.28	5.15865	130.823423
4.5	5.106027	0.195847

Grid-factor	8	479.076971	21.887827	Volume
C/S width	10.11	4.947112	140.929185	Deflection
Height	4.51	4.822345	0.207368	Utilization ratio



Pattern 1 (B6b_1)		
Input	Fitness value	Performance value
	{48;36;0}	
7	648.753757	25.470645
10.25	3.269245	139.251318
4.55	6.322551	0.158164
	{49;5;0}	
7	657.683156	25.645334
10.27	4.437253	140.419326
4.64	6.368088	0.157033
	{49;12;0}	
7	669.632999	25.877268
10.33	0.797328	136.779401
4.56	6.401967	0.156202
	{49;35;0}	
7	648.753757	25.470645
10.25	3.269245	139.251318
4.55	6.322551	0.158164
	{49;38;0}	
7	648.753757	25.470645
10.25	3.269245	139.251318
4.55	6.322551	0.158164
	{49;39;0}	
9	573.218311	23.941978
8.79	5.639845	141.621918
4.55	6.811432	0.146812
	Modified	
9	23.996484	23.941978
8.8	-4.701645	140.683718
4.55	0.146292	0.146812

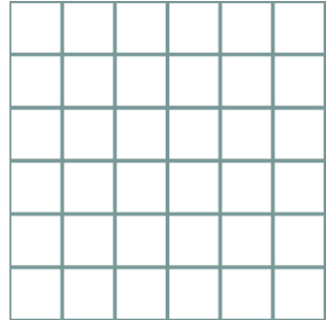
Grid-factor	9	573.218311	23.941978	Volume
C/S width	8.79	5.639845	141.621918	Deflection
Height	4.55	6.811432	0.146812	Utilization ratio
Grid-factor	9	23.996484	23.941978	Volume
C/S width	8.8	-4.701645	140.683718	Deflection
Height	4.55	0.146292	0.146812	Utilization ratio



Material quantity optimization

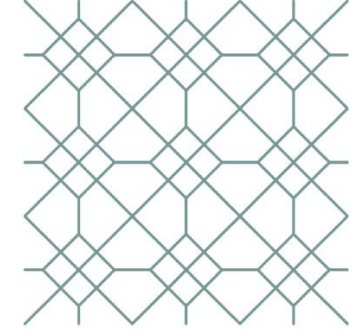
Rank as per the deflection of vault in catalogue

1



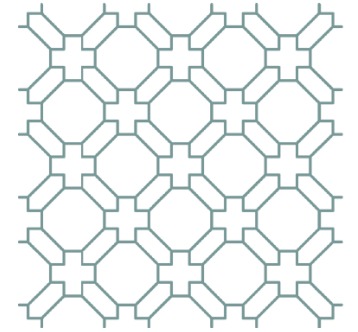
82

3



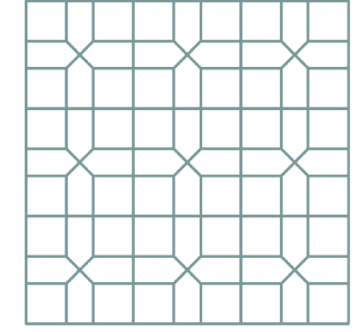
01

4

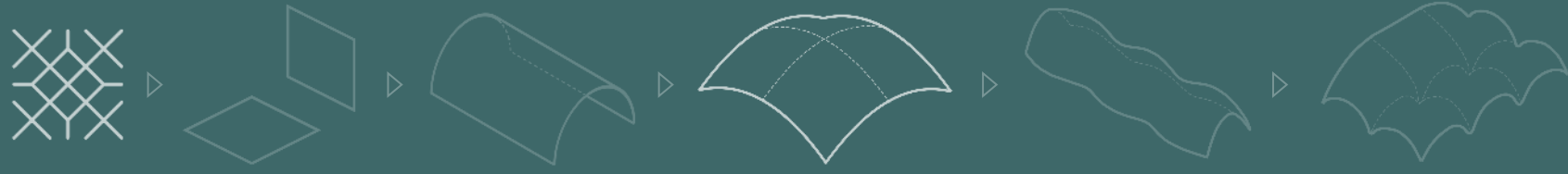


45

2



65



### Material quantity optimization

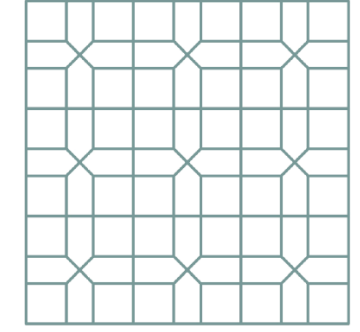
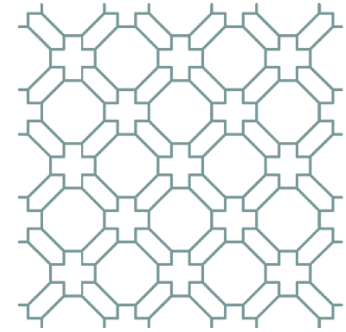
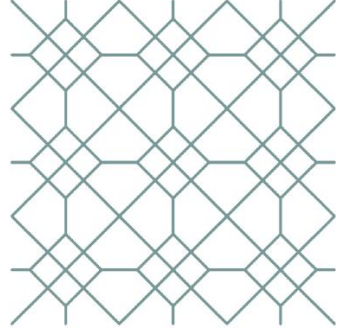
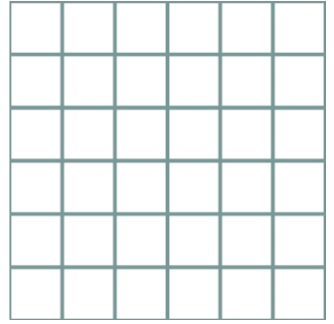
Rank as per the deflection of vault in catalogue

1

3

4

2



82

01

45

65

**Volume**

**Deflection**

**Utilization ratio**

21.88
140.92
0.20

23.94
140.68
0.14

26.79
139.95
0.18

23.36
139.52
0.17

Rank as per the volume

1

3

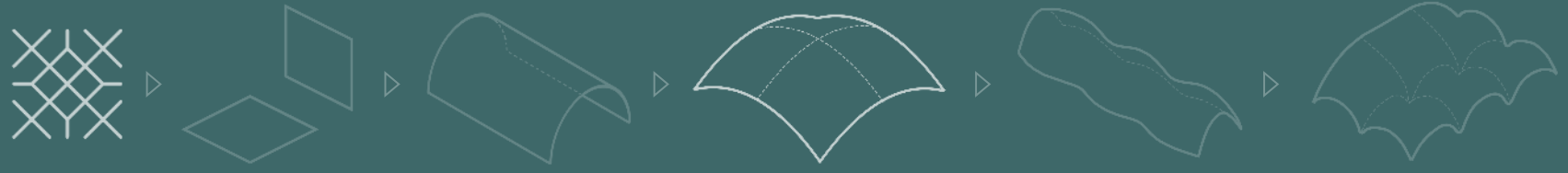
4

2

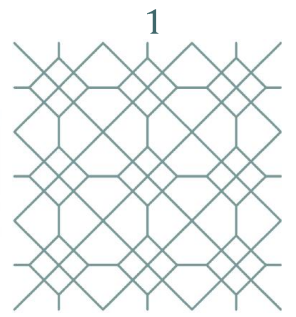
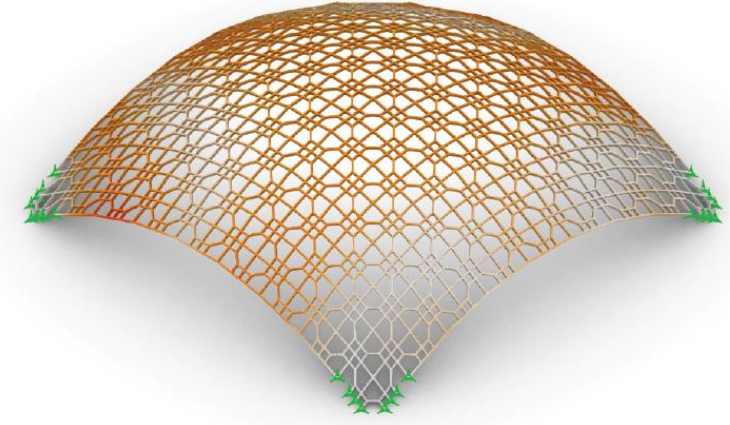
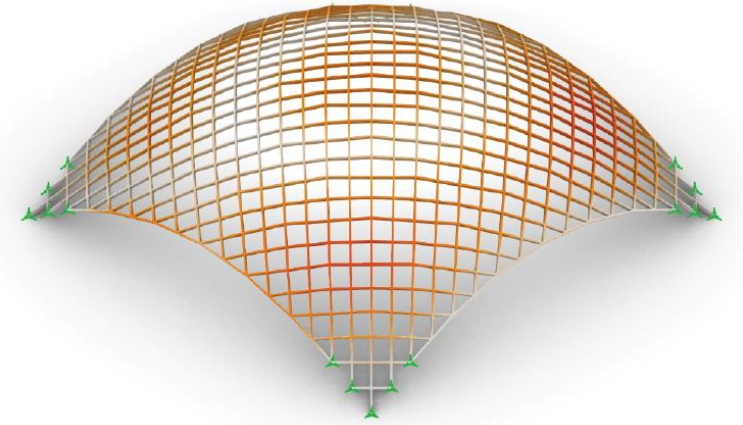
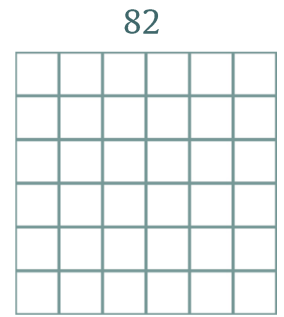
9.6% ^

22.66% ^

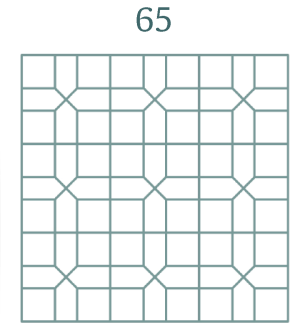
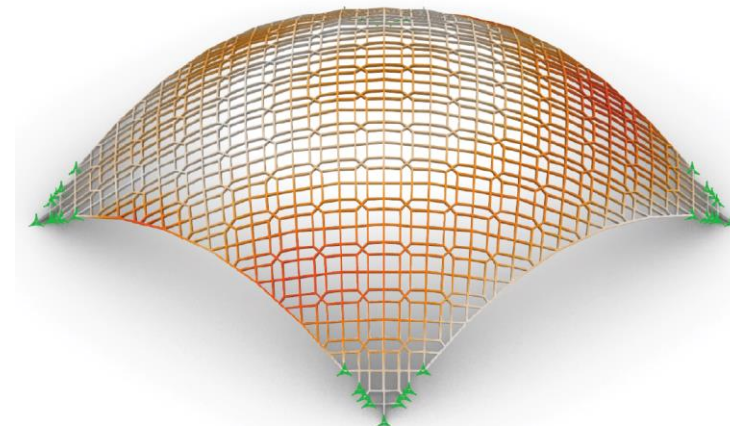
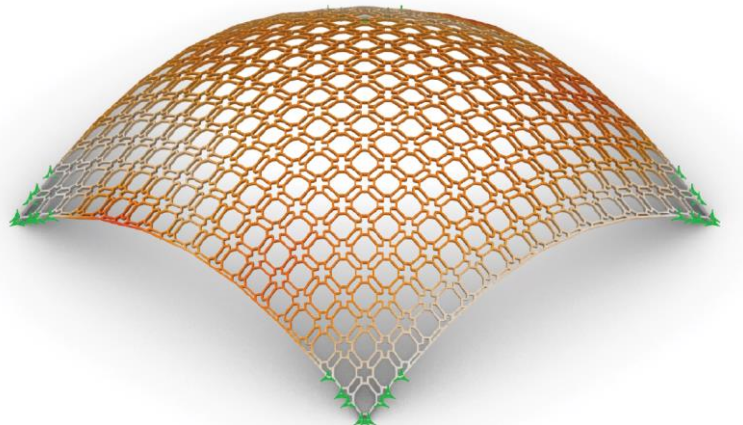
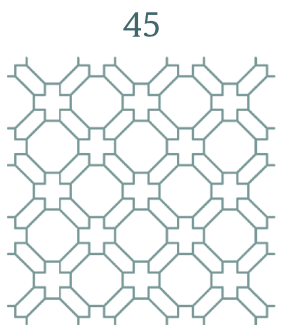
6.9% ^



### Material quantity optimization



9.6% ^



6.9% ^



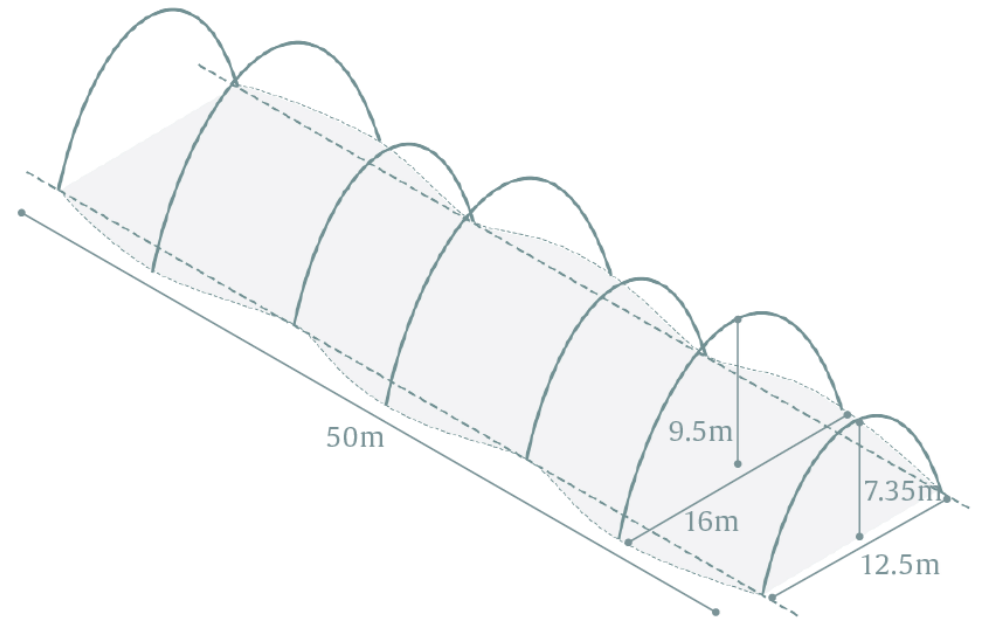


## Model properties

### Case study 1 (Existing building)



[Weald and Downland Gridshell, 2020]



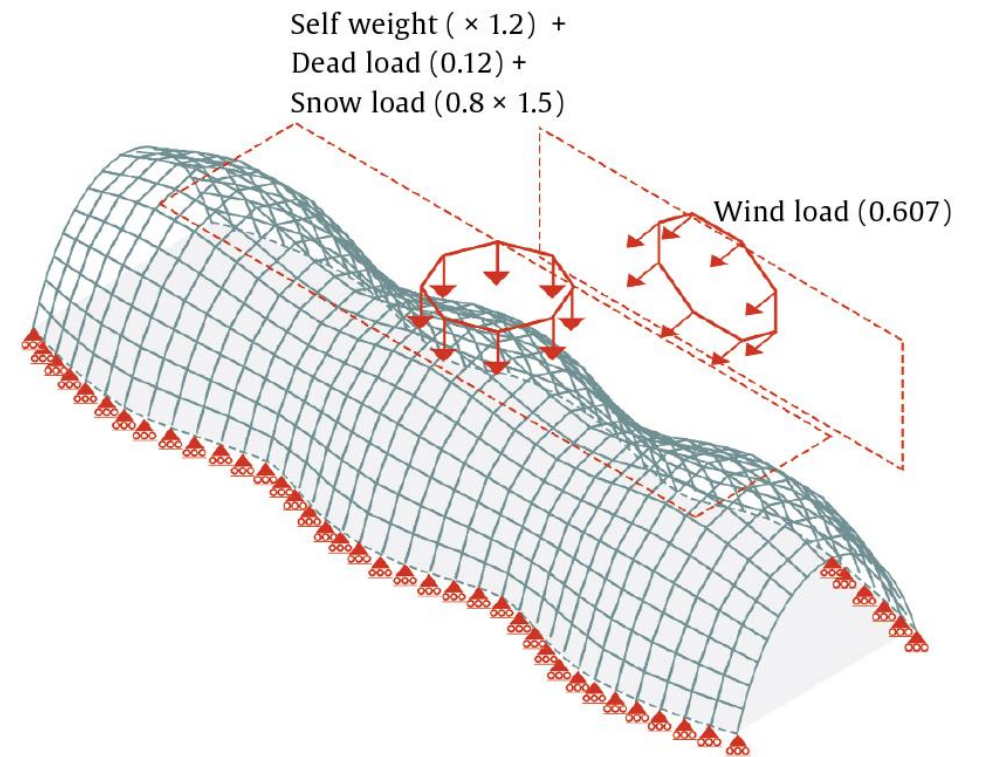


## Model properties

### Case study 1 (Existing building)

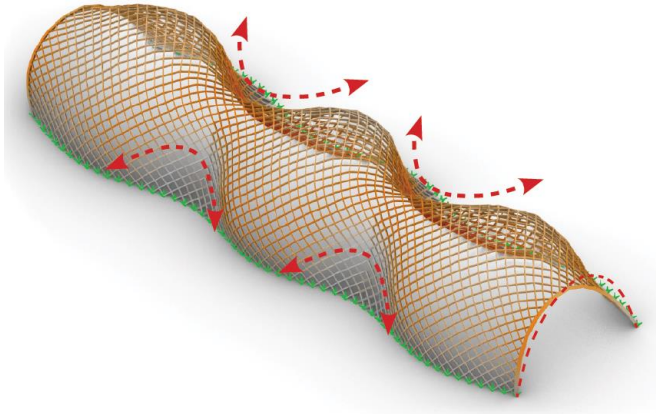


[Weald and Downland Gridshell, 2020]





## Material quantity optimization



Scaled visualization of deflection

Grid factor = 10  
Cross-section width = 90.6mm

Pattern 83	Results	Allowable results
Deflection (mm)	63.79	Span/250 = 64 Height of C/S = 148.66
Max normal stress (MPa)	-19.12	60
Buckling factor	13.19	2
Max. utilization ratio	-0.318	1
Grid density (m)	2925.13	-
Volume (m3)	41.14	-

### Allowable limits

#### Allowable Deflection:

- Height of cross section
- or
- Shell span/250 (whichever is less)

#### Allowable maximum normal stress:

- Less than the yield strength of a material (<60 MPa)

#### Allowable buckling factor:

- >2

#### Minimum grid factor:

- 7 (to make it less course mesh)





## Material quantity optimization

### Multi objective optimization setup

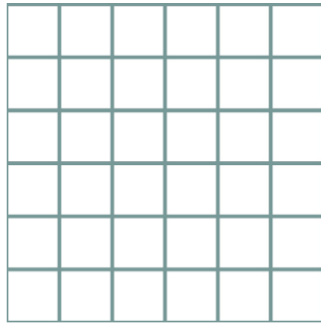
Objectives	Parameters
(V) Minimize Volume	(b) Cross-section width
( $\Delta$ ) Minimize Deflection (till the allowable limit)	(g) Grid factor (for grid-density)
(U) Maximize avg. Utilization ratio	



## Material quantity optimization

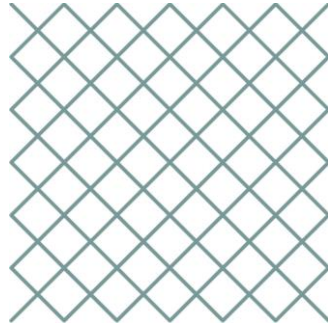
Rank as per the deflection  
of vault in catalogue

1



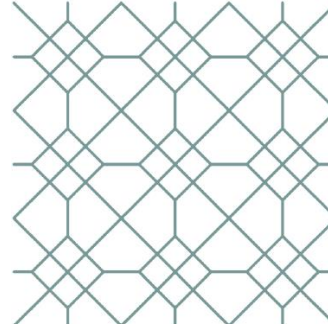
82

4



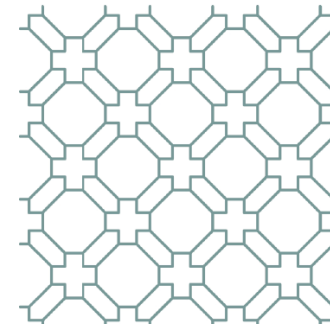
83

3



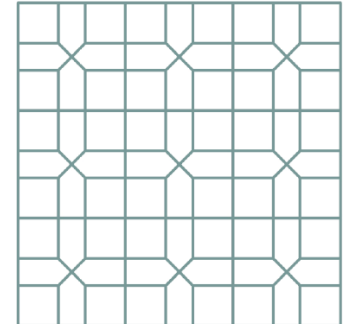
01

5



45

2



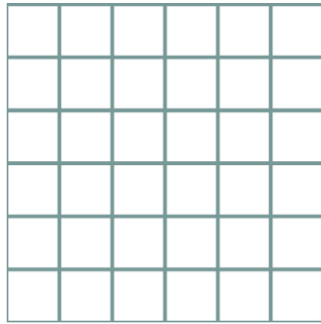
65



## Material quantity optimization

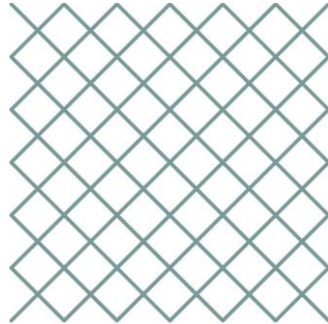
Rank as per the deflection of vault in catalogue

1



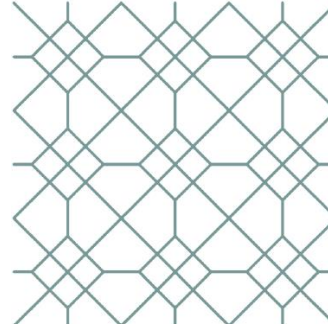
82

4



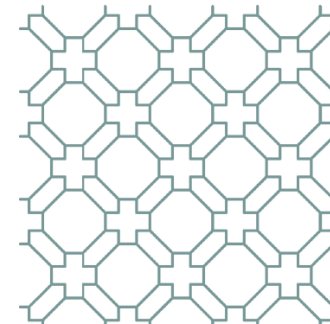
83

3



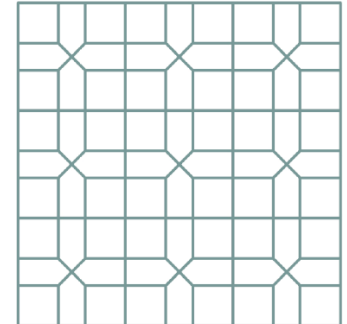
01

5



45

2



65

Volume
Deflection
Utilization ratio

67.15
63.80
0.08

38.94
63.90
0.09

30.03
63.72
0.10

45.37
63.10
0.09

61.37
63.95
0.08

Rank as per the volume

5

2

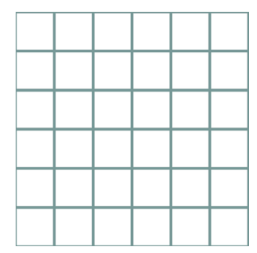
1

3

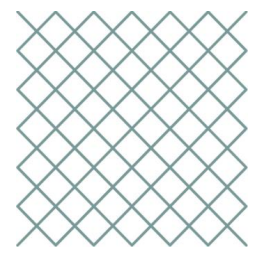
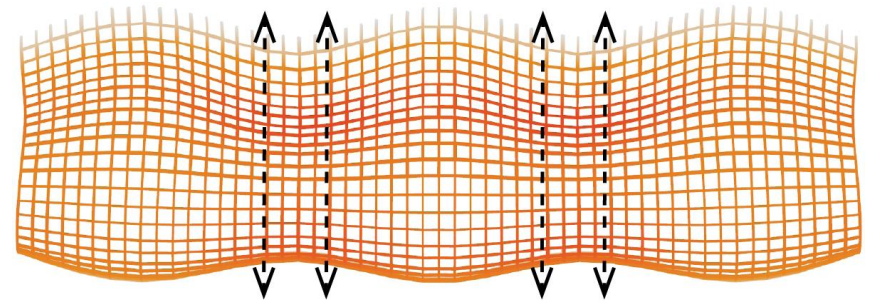
4



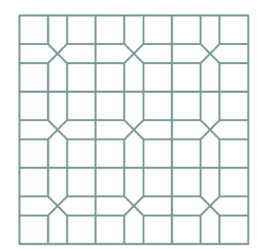
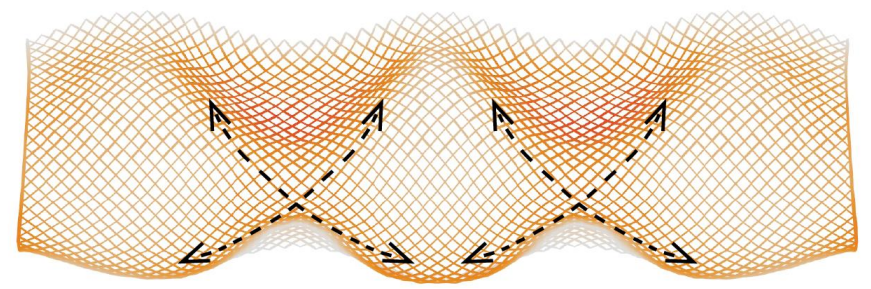
Material quantity optimization



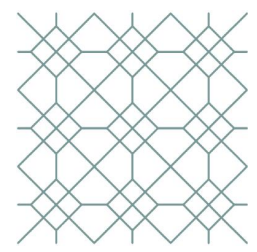
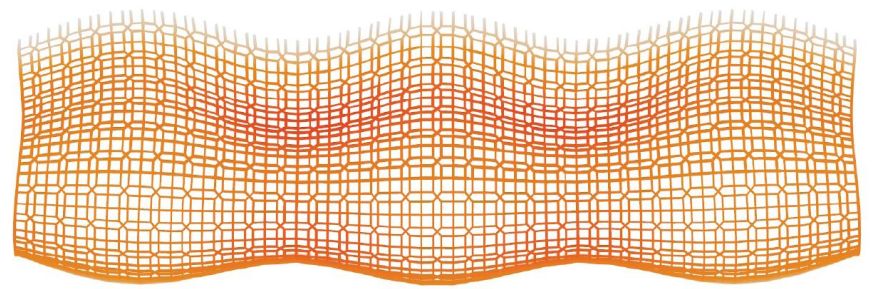
Parallel grid



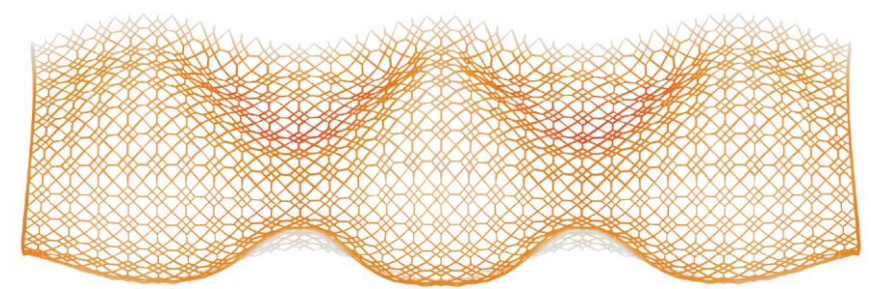
Diagonal grid



65



01

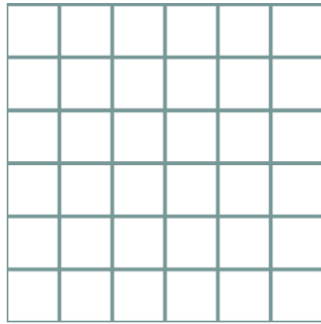




## Material quantity optimization

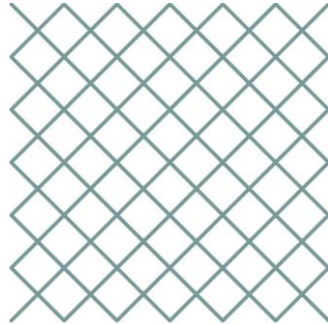
Rank as per the deflection of vault in catalogue

1



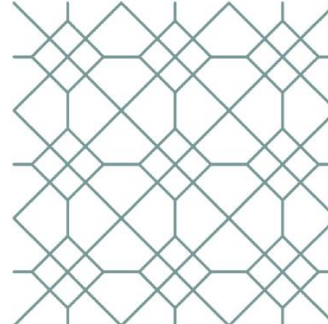
82

4



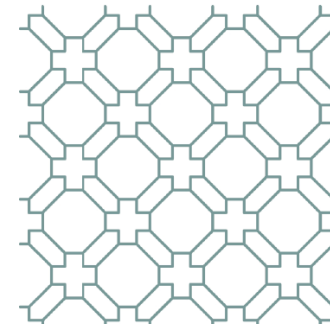
83

3



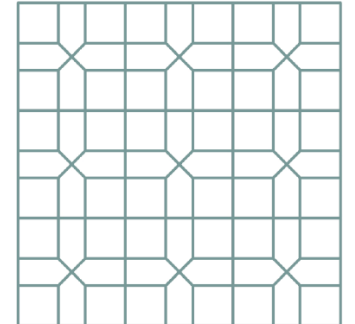
01

5



45

2



65

Volume

67.15

38.94

30.03

45.37

61.37

Deflection

63.80

63.90

63.72

63.10

63.95

Utilization ratio

0.08

0.09

0.10

0.09

0.08

Rank as per the volume

5

2

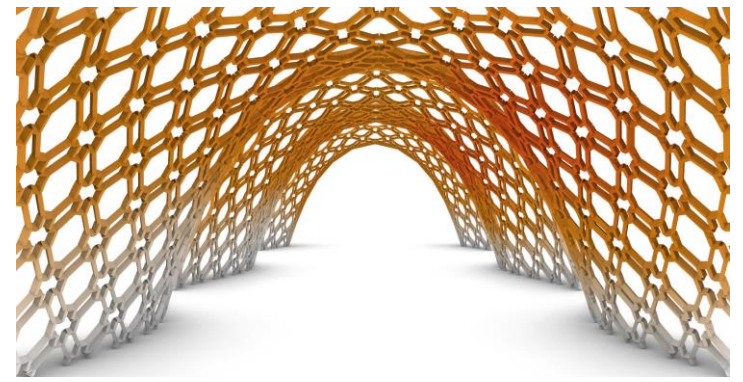
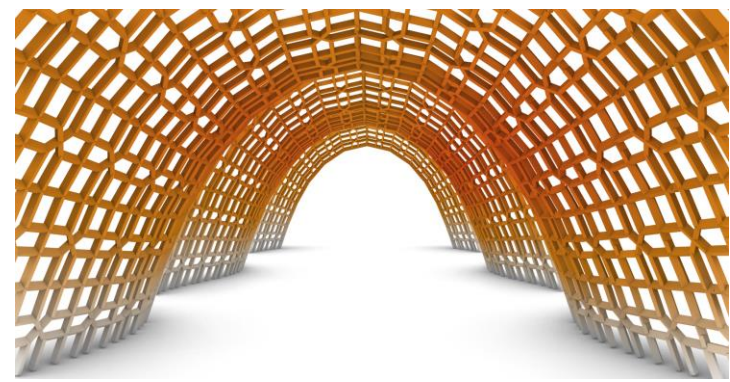
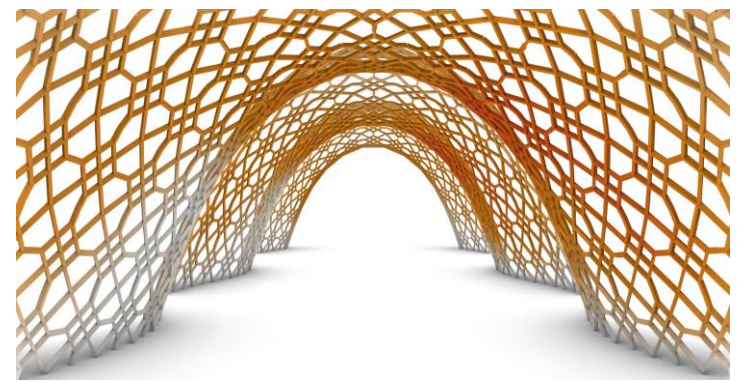
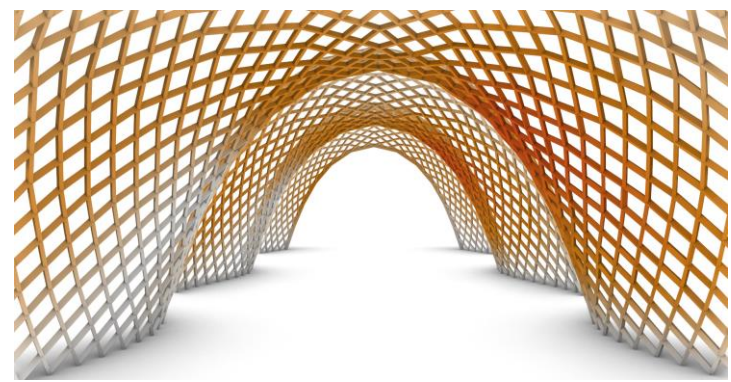
1

3

4



Material quantity optimization



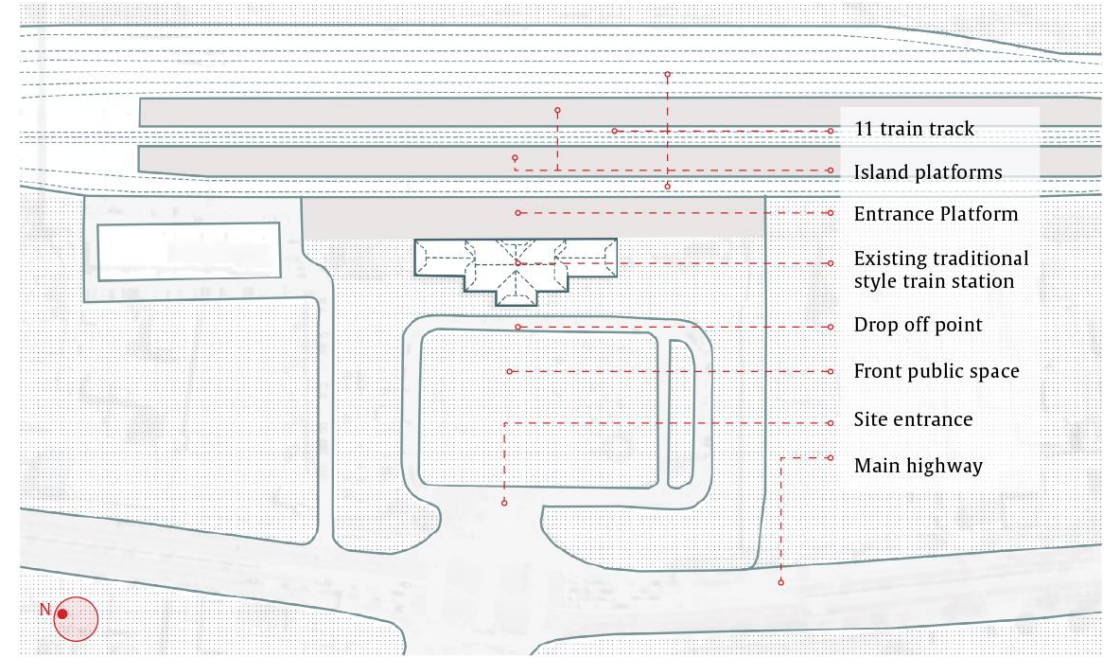




## Roof design



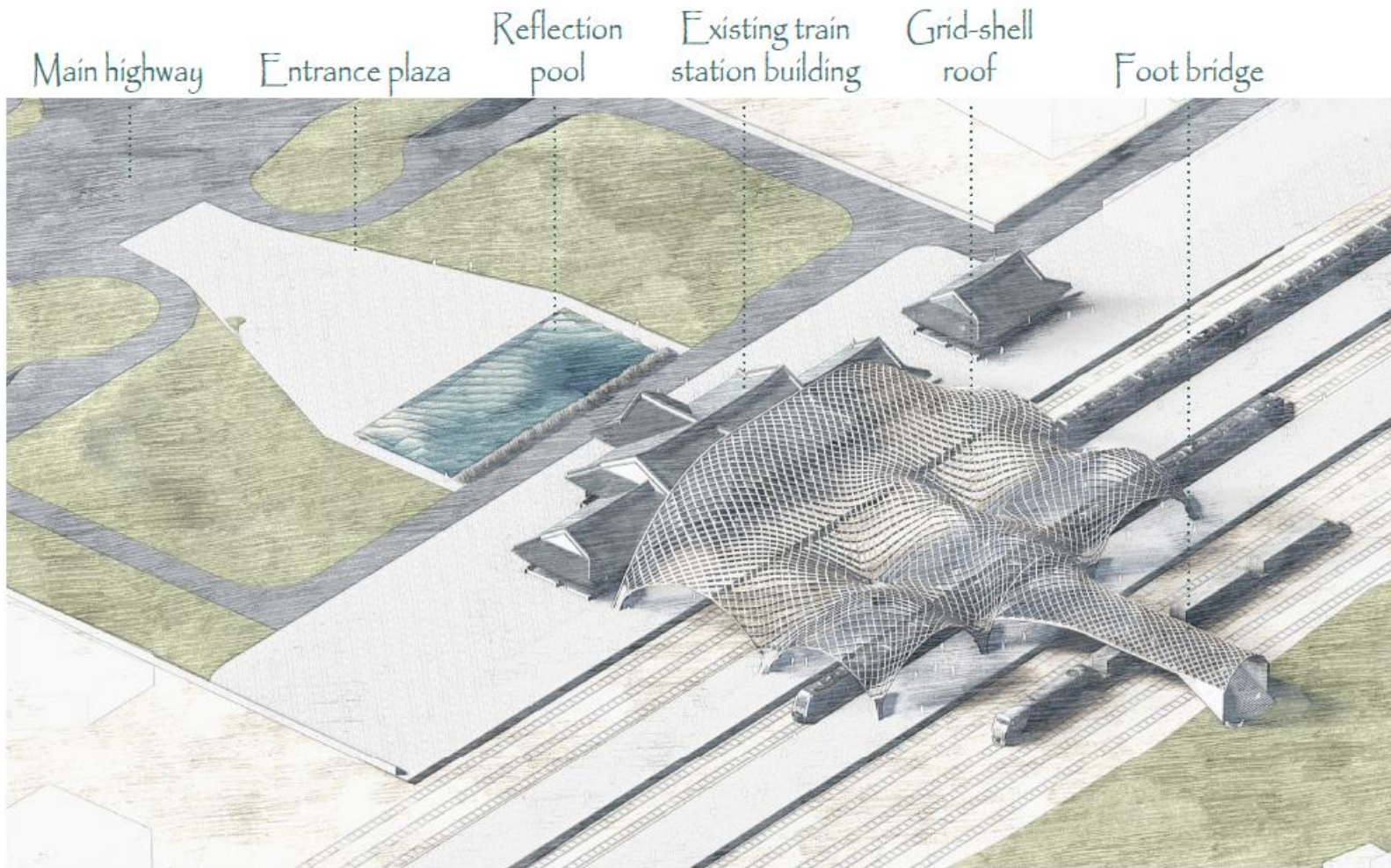
[Project Scope, 2019]







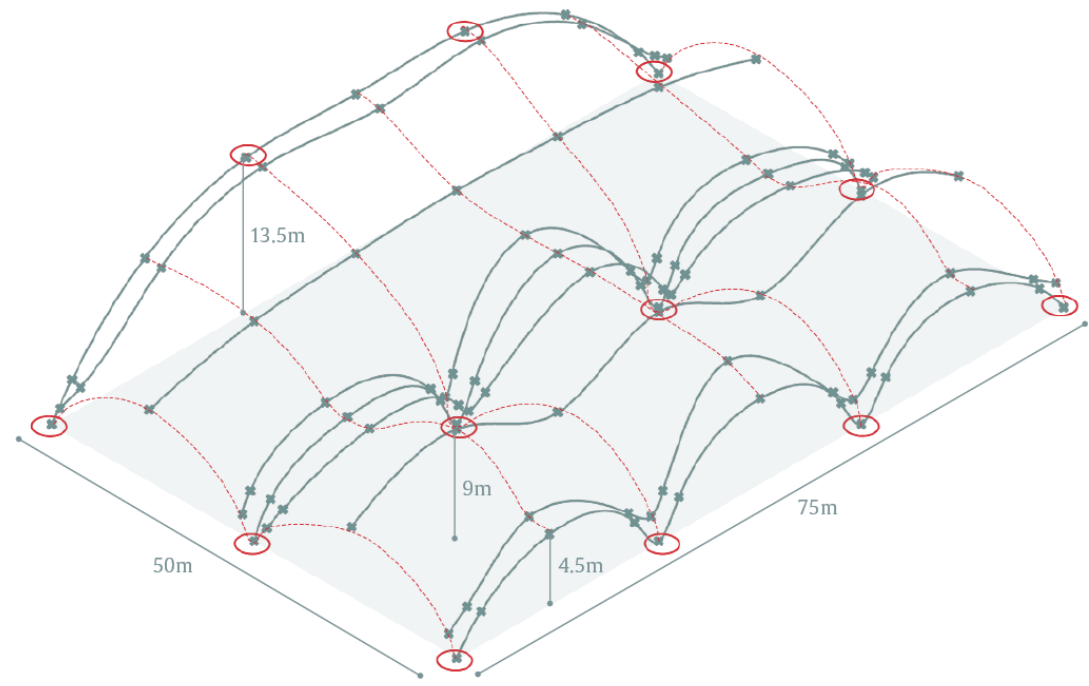
## Roof design





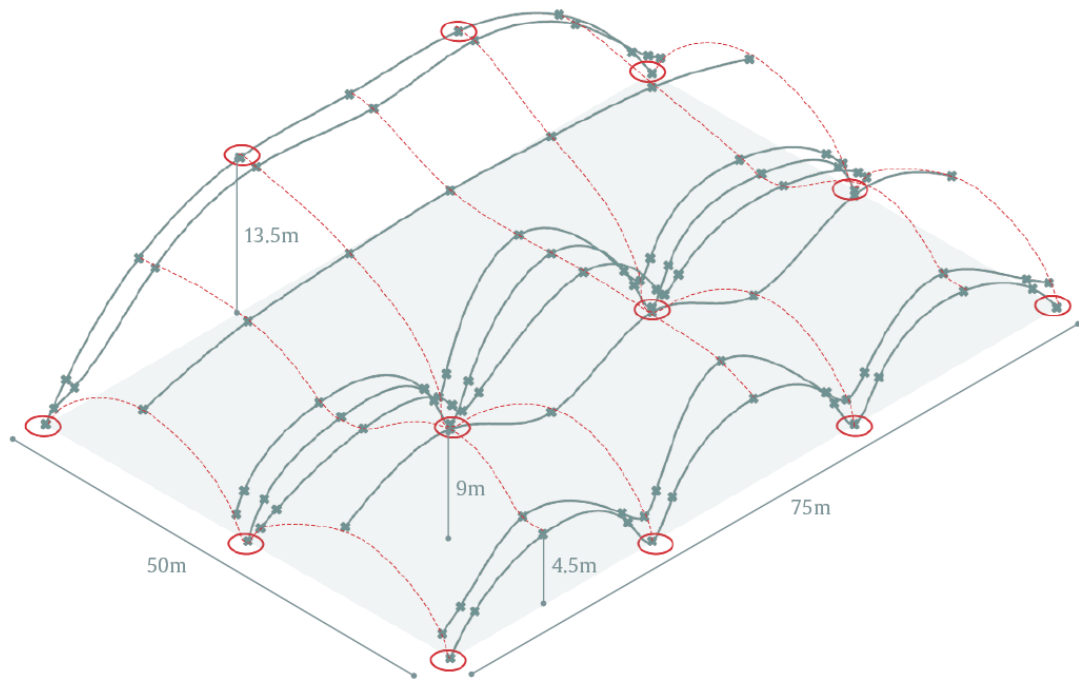


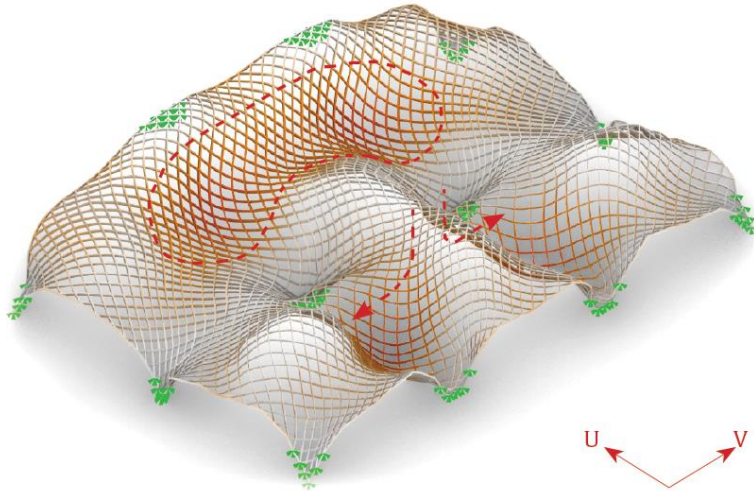
## Roof design





## Roof design





Scaled visualization of deflection

Grid density = 7796m  
 Cross-section width front = 16.84mm  
 Cross-section width rear = 13.15mm

Pattern 82	Results	Allowable results
Deflection (mm)	141.3087	Span/250 = 141.42
		Height of front C/S = 277.86
		Height of back C/S = 216.97
Max normal stress (MPa)	-59.94	60
Buckling factor	6.845276	2
Max. utilization ratio	-0.99	1
Grid density (m)	7796.548	-
Volume (m3)	291.573	-

### Allowable limits

#### Allowable Deflection:

- Height of cross section
- or
- Shell span/250 (whichever is less)

#### Allowable maximum normal stress:

- Less than the yield strength of a material (<60 MPa)

#### Allowable buckling factor:

- >2

#### Minimum grid factor:

- 7 (to make it less course mesh)



### Manual optimization plan

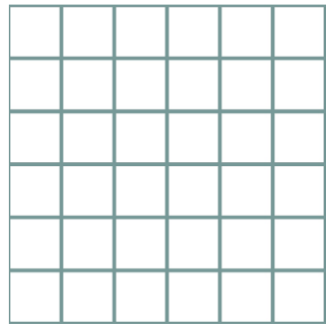
Target	Parameters
Minimize Volume	Cross-section width for front side
Minimize Deflection (till the allowable limit)	Cross-section width for rear side
Minimize Normal stress (till the allowable limit)	



Material quantity optimization

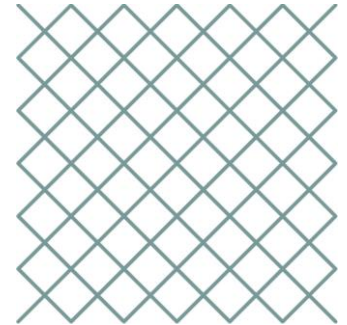
Rank as per the deflection of vault in catalogue

1



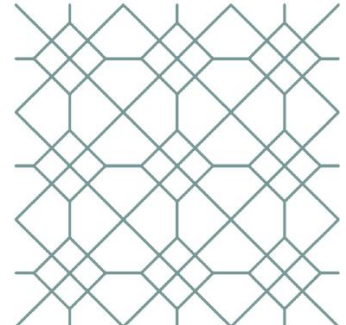
82

4



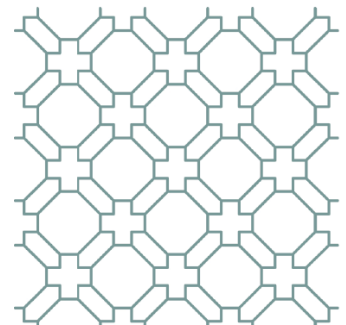
83

3



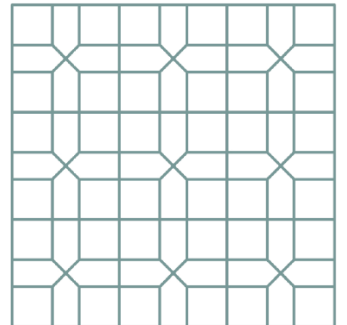
01

5



45

2



65



## Material quantity optimization

Rank as per the deflection of vault in catalogue

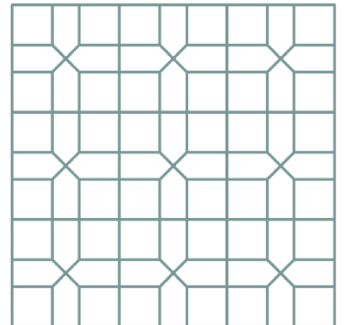
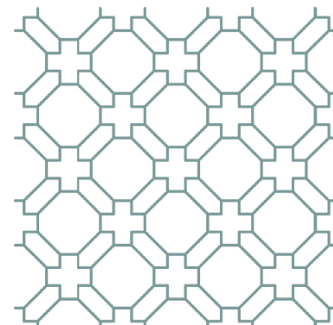
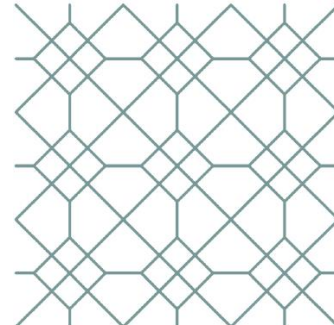
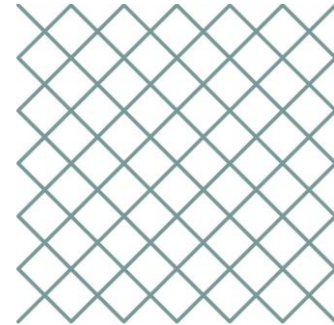
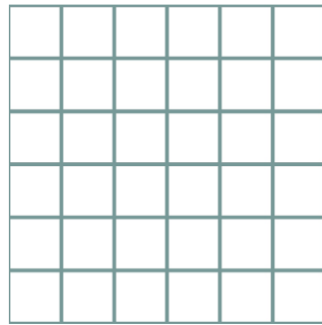
1

4

3

5

2



82

83

01

45

65

**Volume**  
**Deflection**  
**Max. Normal stress**

291.57
141.31
-59.94

509.19
141.30
-59.88

409.90
141.34
-59.97

528.30
141.29
-59.82

324.07
141.29
-59.90

Rank as per the volume

1

4

3

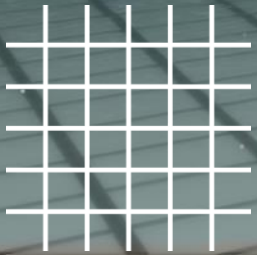
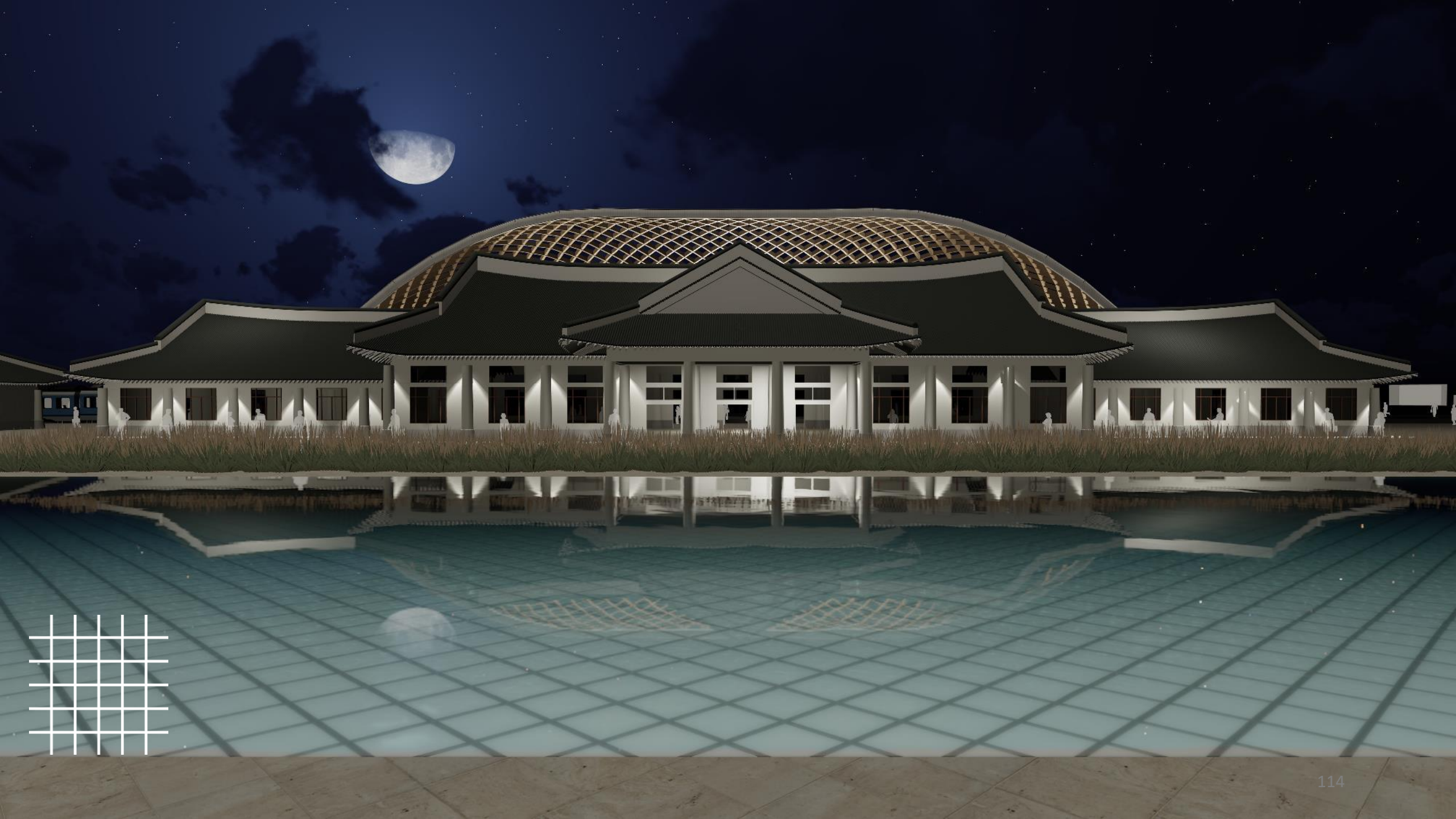
5

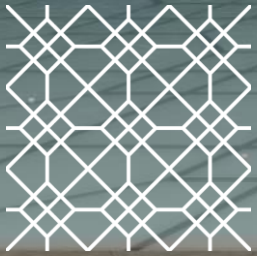
2

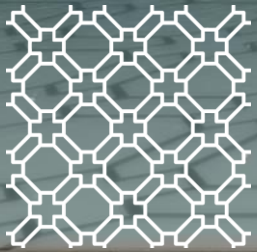


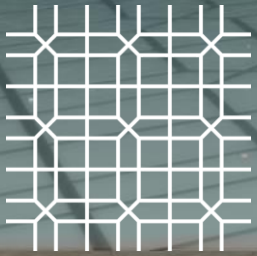


Visual experience



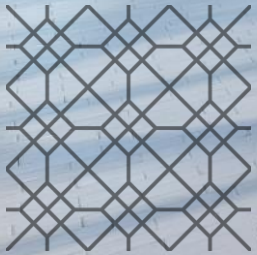




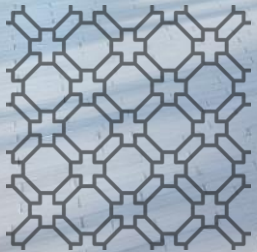


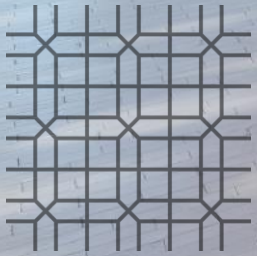














## Project development

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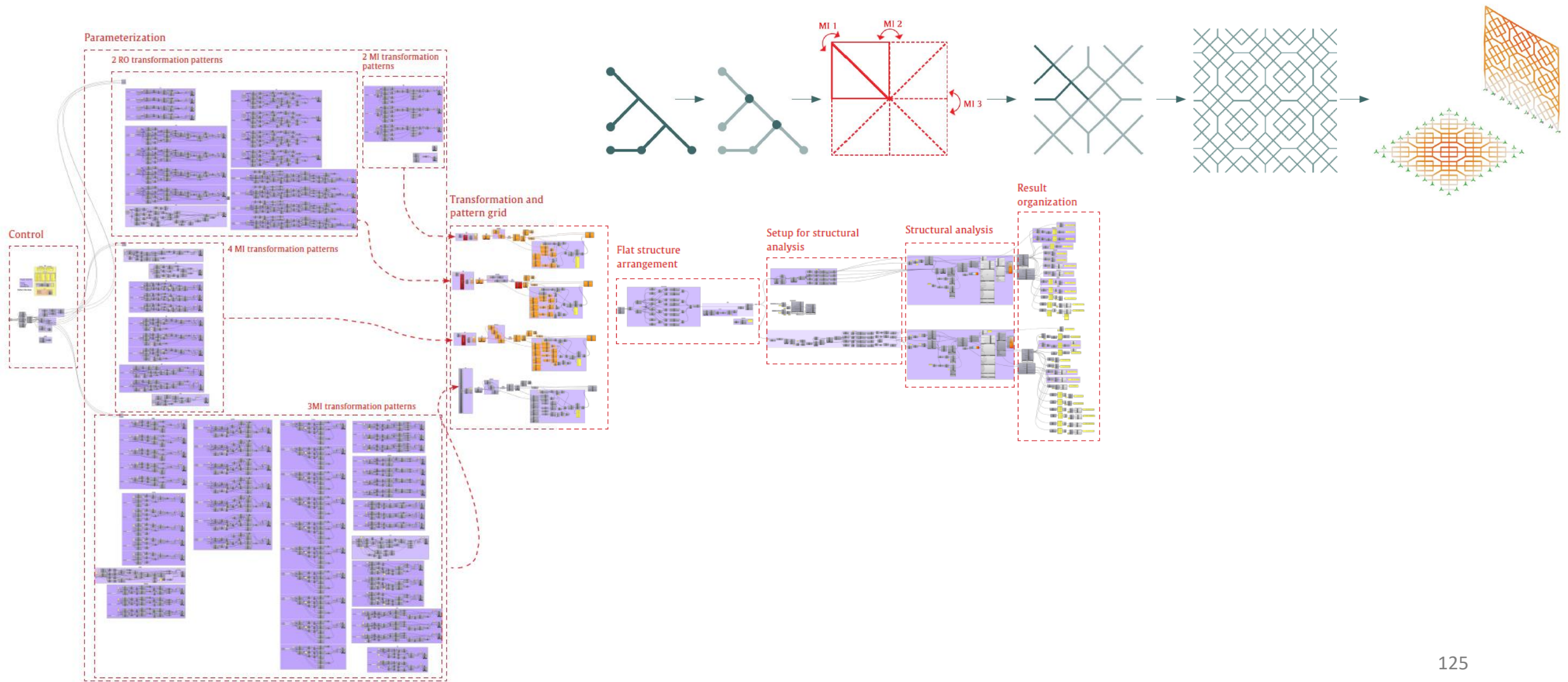


## Application in practice

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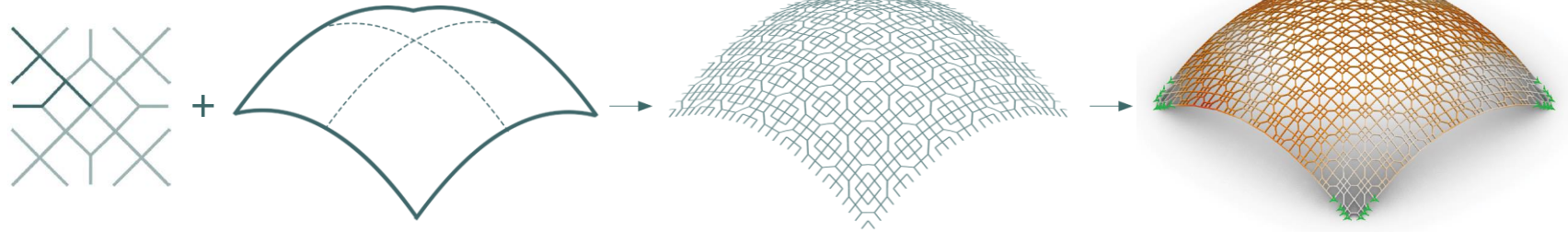
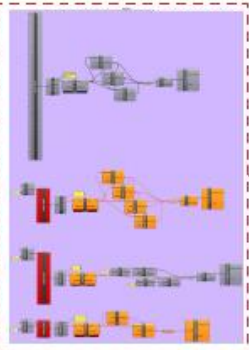
## Application in practice



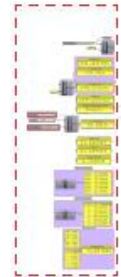


## Application in practice

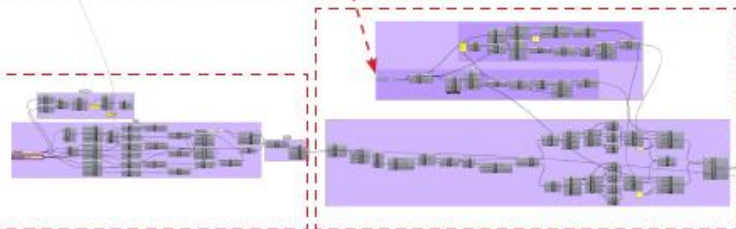
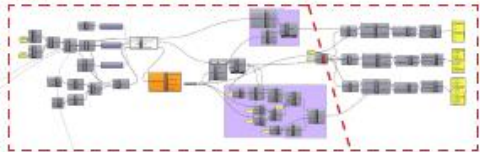
Parameterized patterns internalized



Multi-objective optimization

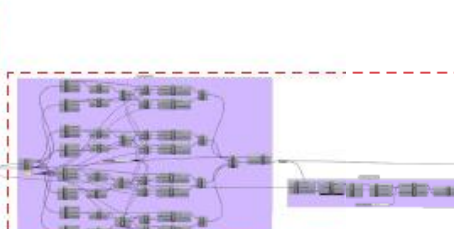


Control

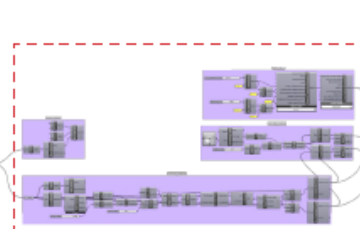


Surface to quad mesh

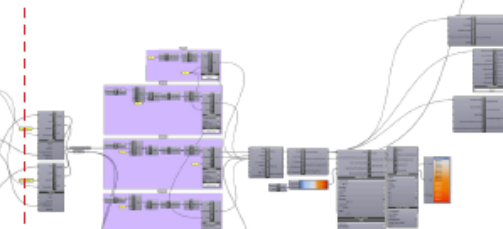
Quad mesh to individual surface and mapping of patterns



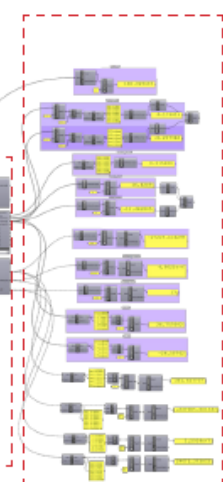
Patterned-grid arrangement



Wind load and cross-section arrangement



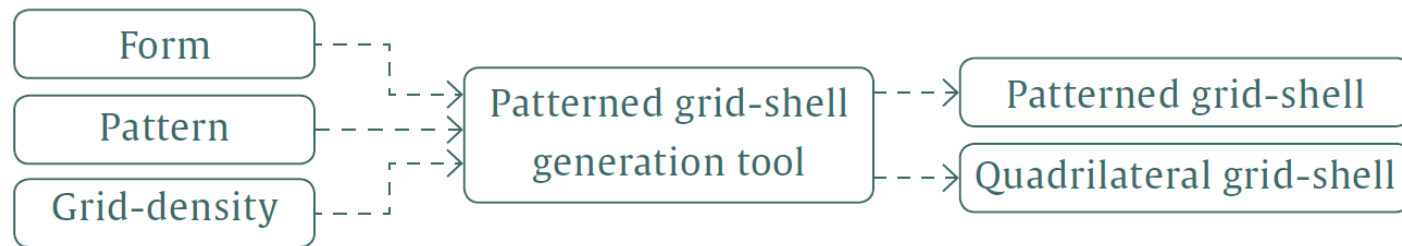
Structural analysis setup



Structural analysis results  
126

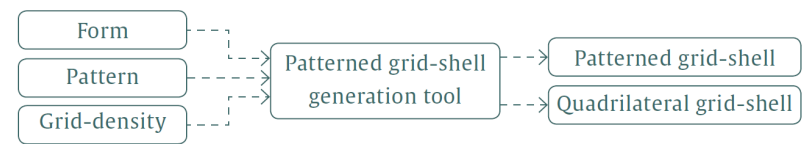


## Computational tool

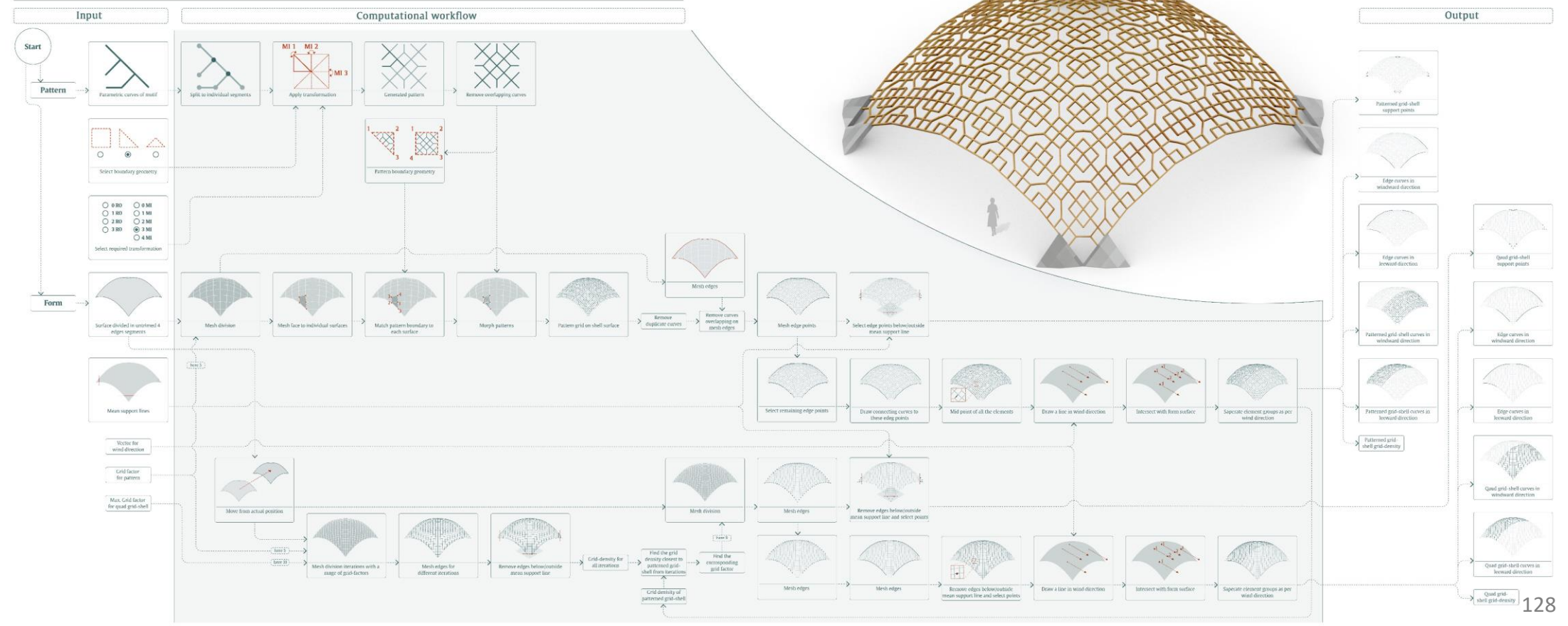




# Computational tool



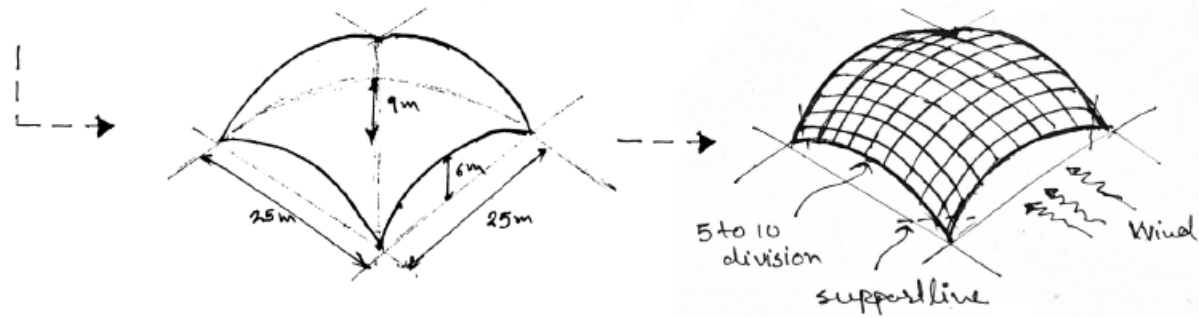
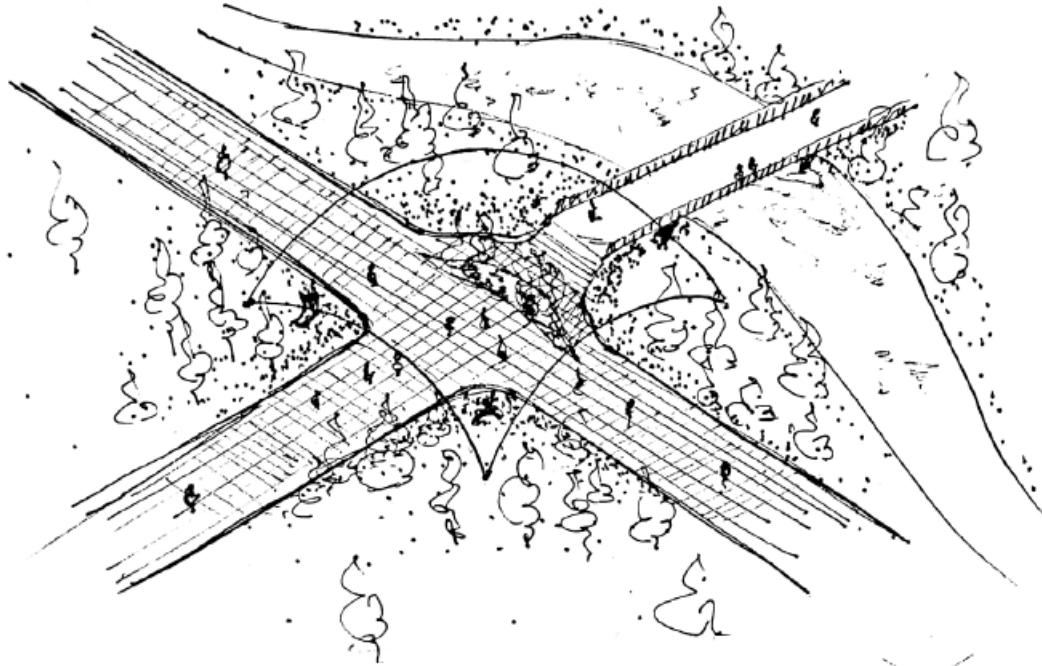
## Patterned grid-shell generation workflow





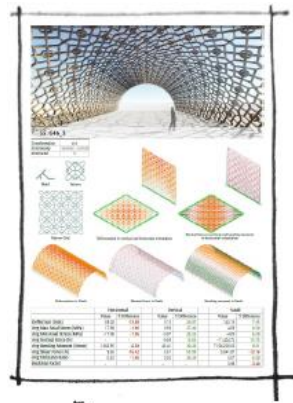


## Computational tool

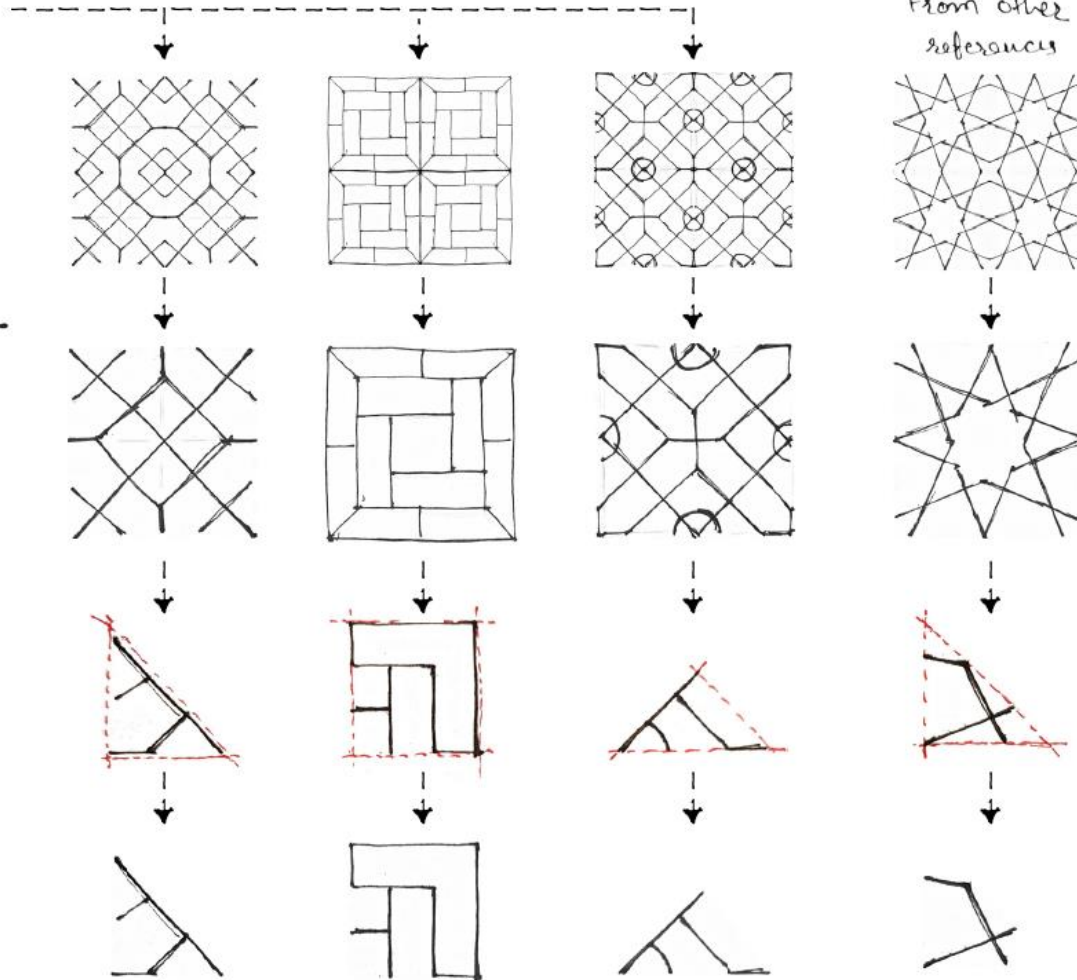




## Computational tool

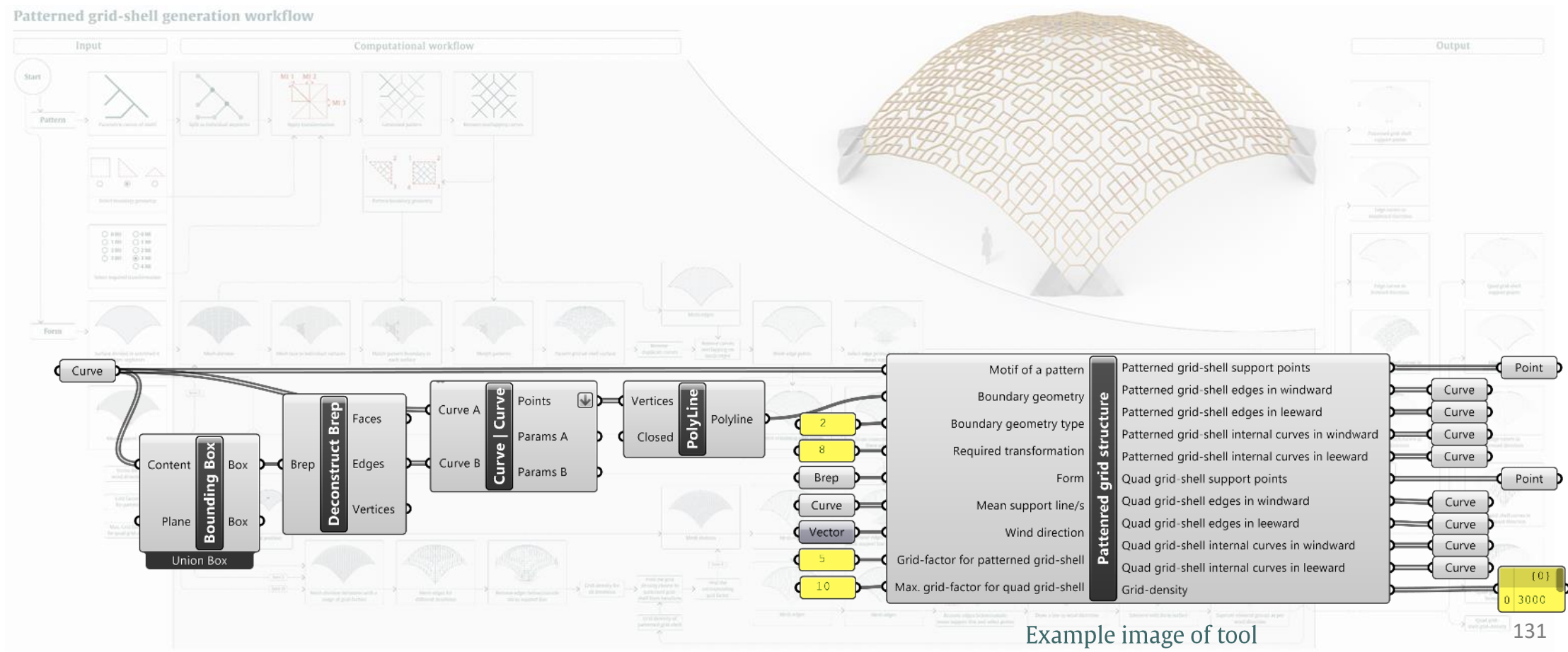
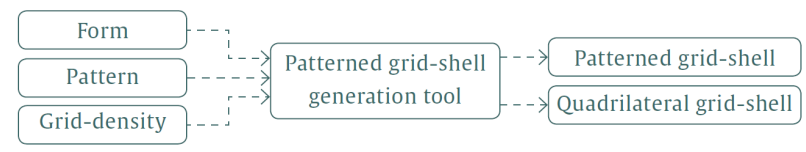


From Pattern catalogue





# Computational tool



Example image of tool



# Computational tool



### Patterned grid-shell generation workflow

**Input**

- Start
- Pattern
- Form

**Computational workflow**

Start -> Pattern -> Form -> [Grid Generation Steps] -> [Shell Construction Steps] -> [Final Output]

**Patterned grid structure**

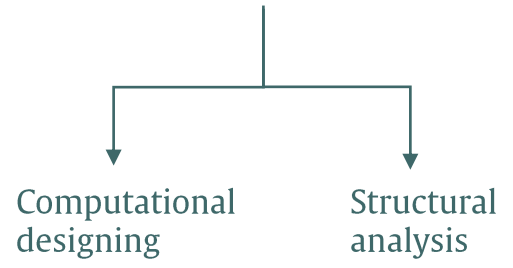
Motif of a pattern	Patterned grid-shell support points	Point
Boundary geometry	Patterned grid-shell edges in windward	Curve
Boundary geometry type	Patterned grid-shell edges in leeward	Curve
Required transformation	Patterned grid-shell internal curves in windward	Curve
Form	Patterned grid-shell internal curves in leeward	Curve
Mean support line/s	Quad grid-shell support points	Point
Wind direction	Quad grid-shell edges in windward	Curve
	Quad grid-shell edges in leeward	Curve
	Quad grid-shell internal curves in windward	Curve
	Quad grid-shell internal curves in leeward	Curve
Grid-factor for patterned grid-shell		
Max. grid-factor for quad grid-shell		
	Grid-density	{0} 0 3000

Example image of tool



## Utility

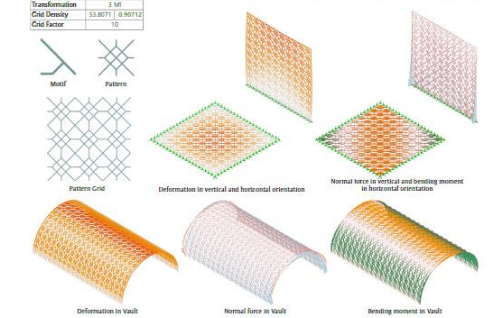
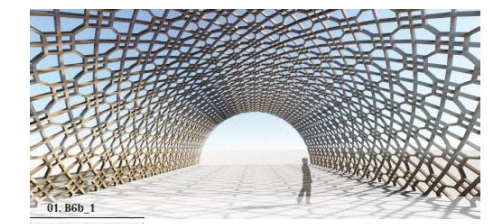
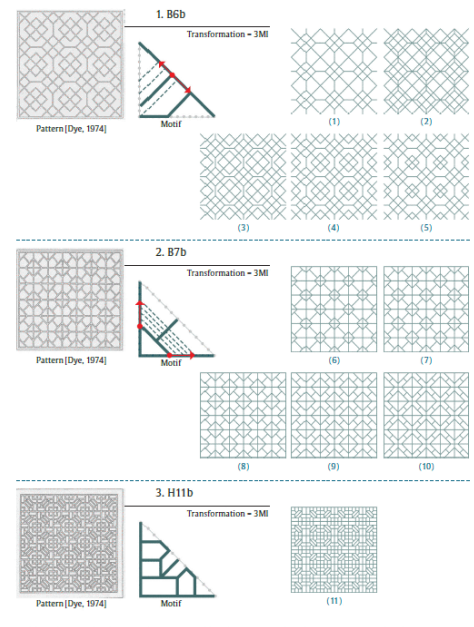
### Guidelines to make choices



### Pattern catalogue

#### Parameterization

#### Structural performance



	Horizontal		Vertical		Vault	
	Value	% Difference	Value	% Difference	Value	% Difference
Deflection (mm)	59.85	-25.61	0.12	20.62	142.67	-7.09
Avg Max Axial Stress (MPa)	19.19	4.62	0.85	51.25	4.51	17.94
Avg Min Axial Stress (MPa)	-19.19	4.62	-1.08	40.64	-4.51	17.94
Avg Normal Force (N)	-	-	-11.00	27.12	-12.001.36	21.83
Avg Bending Moment (Nmm)	1.122.02	-1.39	50.36	44.45	79.64.600.00	11.86
Avg Shear Force (N)	10.80	-3.61	3.90	72.13	5.295.29	-8.79
Avg Utilization Ratio	0.32	4.62	0.02	40.64	0.08	17.84
Buckling Factor	-	-	-	-	4.39	6.70



## Conclusion

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## Conclusion

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### Research question

---

**Main Question:** *With the help of parametric workflow, how to design an urban grid shell structure, where the line patterns (in this case, north Asian lattice pattern) are selected based on the structural performance and used in load distribution as a grid geometry?*



## Conclusion

---

### Research question

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**Main Question:** *With the help of parametric workflow, how to design an urban grid shell structure, where the line patterns (in this case, north Asian lattice pattern) are selected based on the structural performance and used in load distribution as a grid geometry?*

1

Structure of  
patterns

2

Parameterization  
of a patterns

3

Generating  
patterned grid-shell

4

Material quantity  
optimization



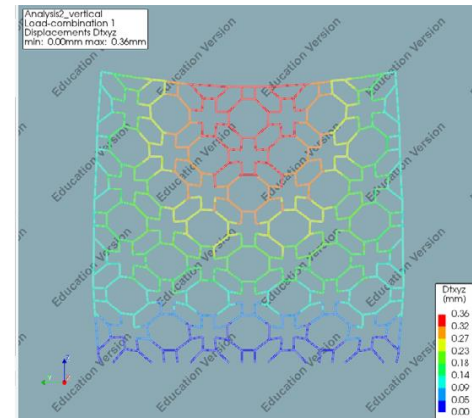
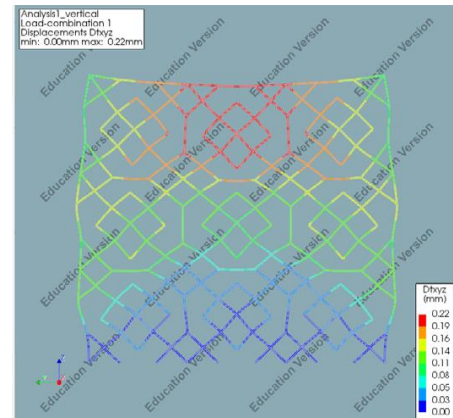
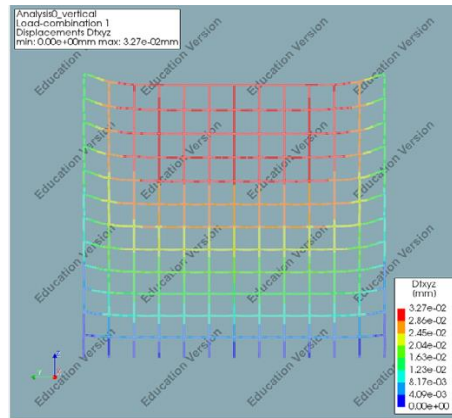


## Conclusion

### Research question

**Main Question:** *With the help of parametric workflow, how to design an urban grid shell structure, where the line patterns (in this case, north Asian lattice pattern) are selected based on the structural performance and used in load distribution as a grid geometry?*

1  
Structure of  
patterns



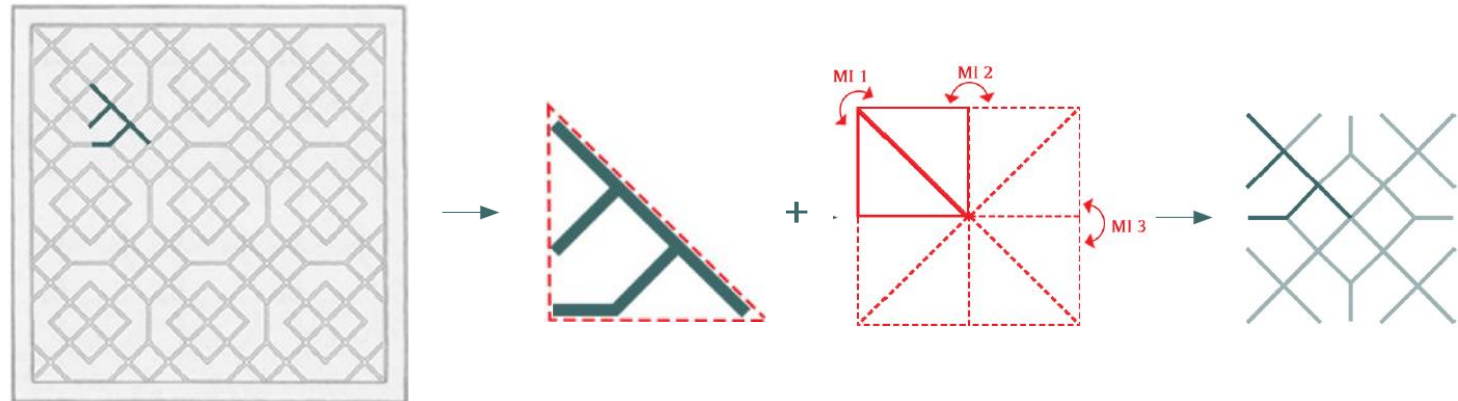


## Conclusion

### Research question

**Main Question:** *With the help of parametric workflow, how to design an urban grid shell structure, where the line patterns (in this case, north Asian lattice pattern) are selected based on the structural performance and used in load distribution as a grid geometry?*

2  
Parameterization  
of a patterns



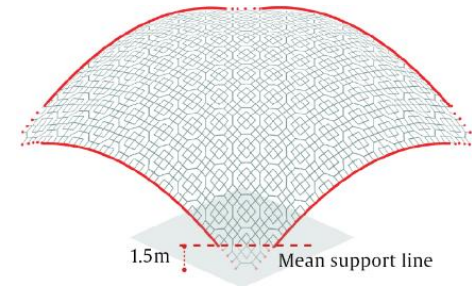
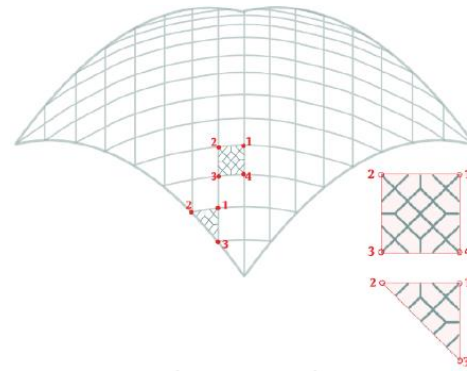
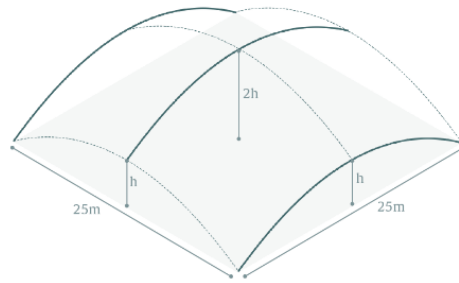


## Conclusion

### Research question

**Main Question:** *With the help of parametric workflow, how to design an urban grid shell structure, where the line patterns (in this case, north Asian lattice pattern) are selected based on the structural performance and used in load distribution as a grid geometry?*

3  
Generating  
patterned grid-shell





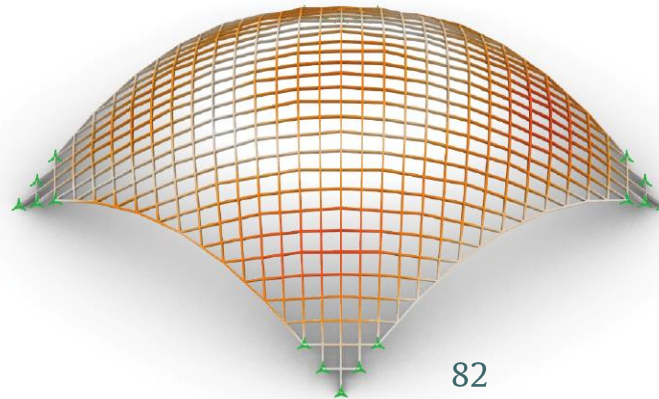
## Conclusion

### Research question

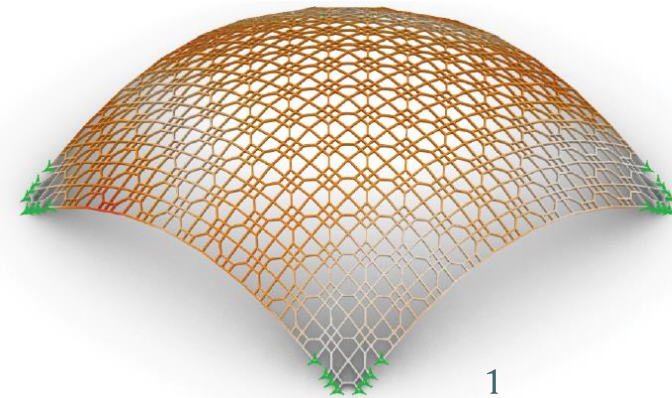
**Main Question:** *With the help of parametric workflow, how to design an urban grid shell structure, where the line patterns (in this case, north Asian lattice pattern) are selected based on the structural performance and used in load distribution as a grid geometry?*

4

Material quantity  
optimization



82



1

9.6% ^

### **End note**

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*This method is an attempt to utilize the ancient traditional art of lattice patterns in contemporary architectural style with the help of building technology. By which, it aim to establish socio-cultural sustainability in built environment. However, it certainly consumes comparative high amount of material than the conventional methods. Thus, it has a tread-off between material usage and socio-cultural sustainability, which a designer can balance.*

### **End note**

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*This thesis is dedicated to all the designers as an encouragement to adapt the ethos of a city/town from a different layer of urban settlements in their designs. It will create much more vibrant and unique cities and technology has an enormous potential to make it sustainable for us!*

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Thank you.

**AUTHOR:** Shasan Chokshi

**MAIN MENTOR:** Dr MSc Arch. Michela Turrin

**SECOND MENTOR:** Ir. Peter Eigenraam

**DELEGATE EXAMINERS:** Dr. H.T. Remoy

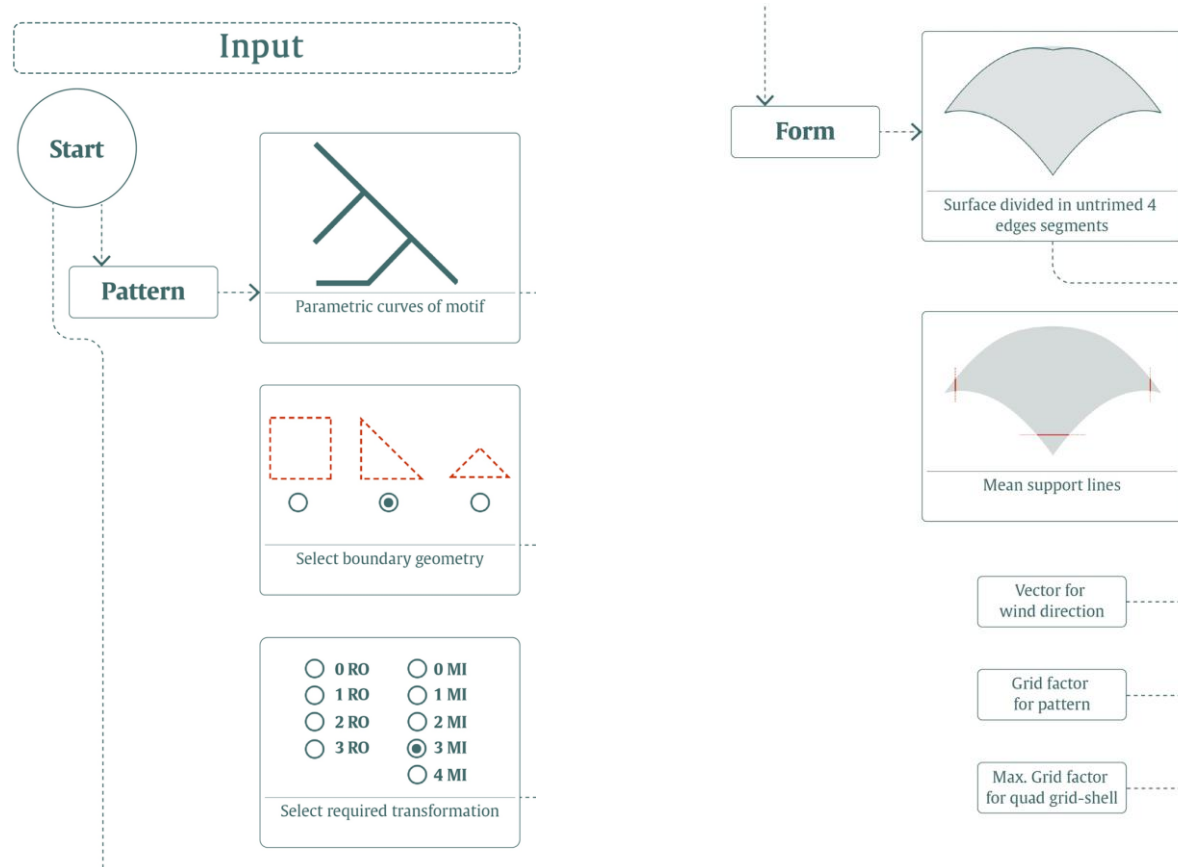
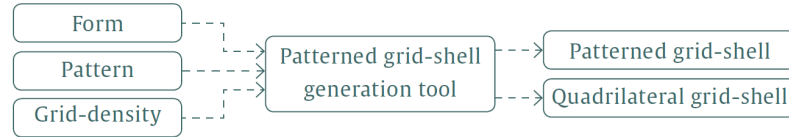


30/06/2020



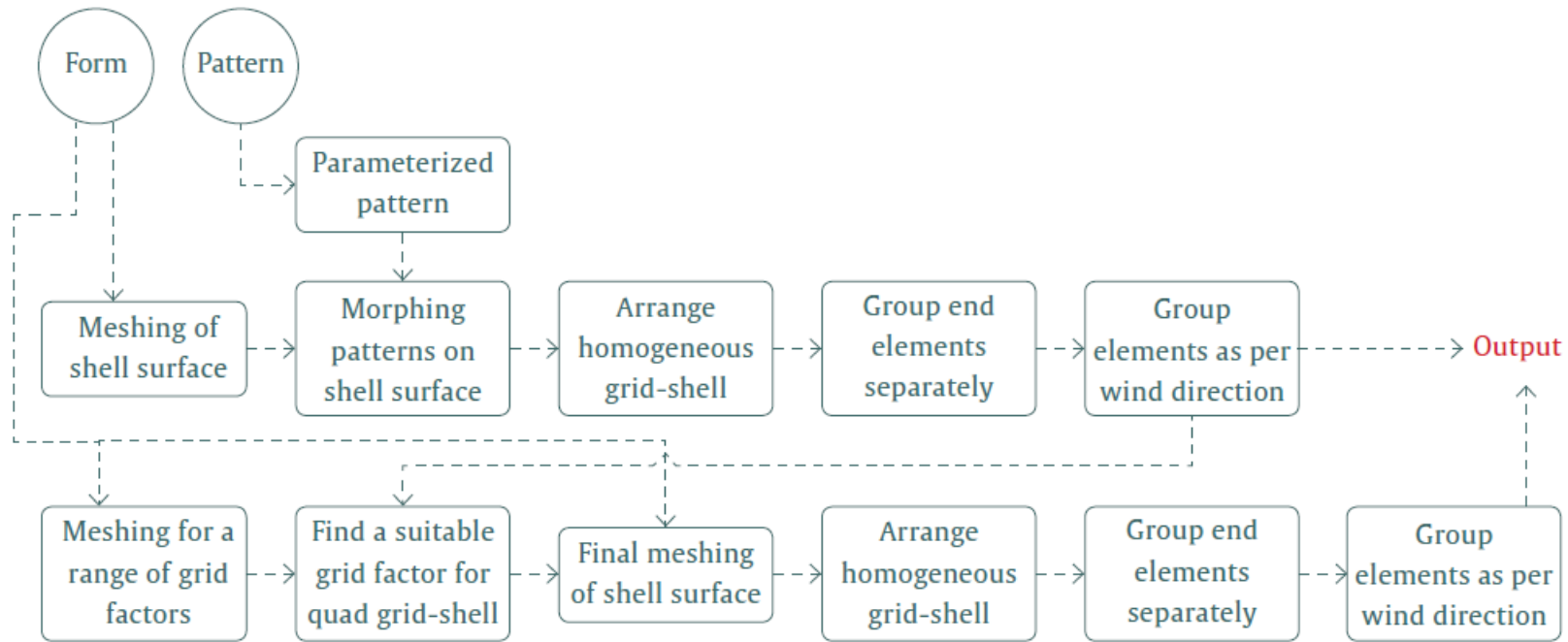
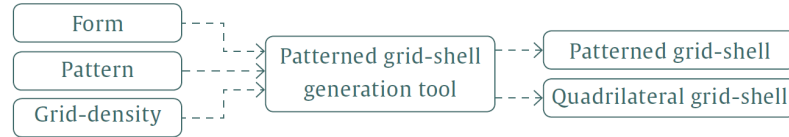


## Computational tool





## Computational tool





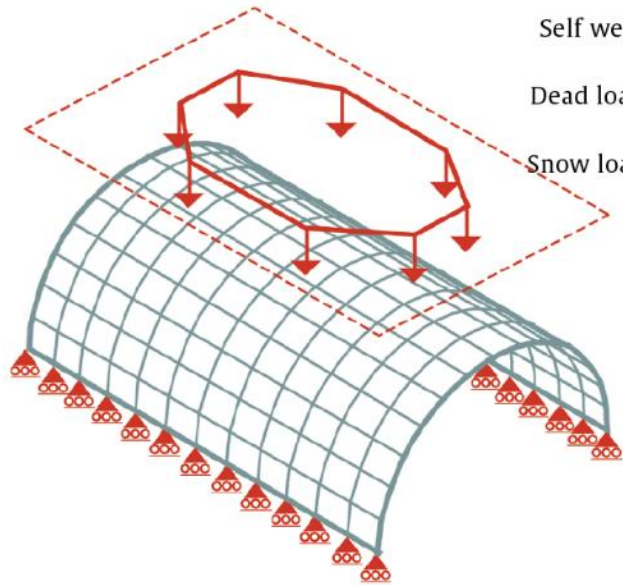
## Future development

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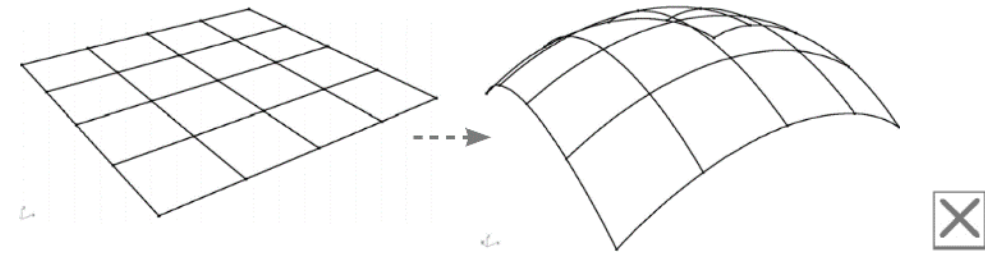
- The simultaneous exploration of patterns, materials, cross-sections and planarity of beam.
- Variation in grid-density and cross-section as per load distribution.
- Development of joints with topology optimization technique.
- More elaborate use of multi objective optimization by optimizing the overall moment of joints.
- The workflow can be coupled with dynamic relaxation methods in plug-ins like Kangaroo.
- The workflow can be further developed to generate patterned grid-shell with 3D patterns (different version of spaceframe)



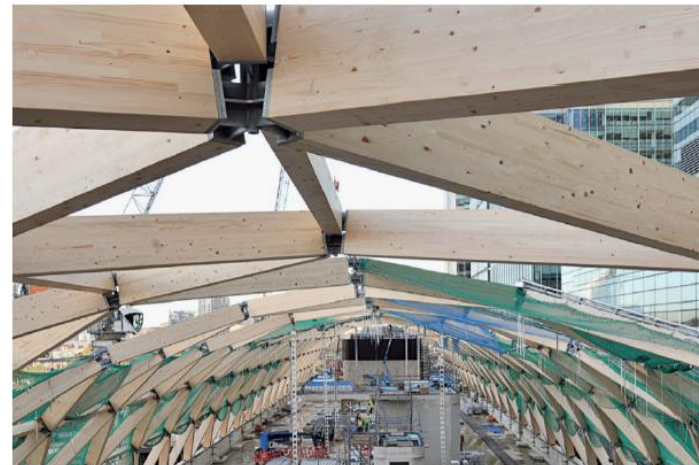
### Expected fabrication



Self weight (  $\times 1.2$  )  
+  
Dead load (  $0.8 \times 1.1$  )  
+  
Snow load (  $0.8 \times 1.5$  )



[Seele, 2014]



[Tim M. Worsfold, 2018]



[Seele, 2014]





[Seele, 2014]



[Tim M. Worsfold, 2018]



[Seele, 2014]



Roof of a Lobby [Rondina, 2014]



Bending of wooden elements (top left), Bent beams with grooves (top middle), Assembled roof (bottom left), Metal joint at supports (bottom middle), Assembly of a pre-fabricated roof segment (right) [Rondina, 2014]



## Limitations

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### Patterned grid-shell generation

---

- Only compatible for rectangular grid at the present and related pattern.
- Grid divisions is similar throughout the surface. Variations of grid-density is not possible.
- Need more elaborate logic to end different patterned grid-shells at the supports.
- Workflow is limited to linear elements. Curved elements are not generated.

### Structural performance results

---

- Comparison is derived only based on different geometries, different materials, cross-section shape and sizes are not explored.
- For joints, fixed configuration is used and possible stiffnesses are not considered.
- The reference results in pattern catalogue are validated to be useful with single curvature surface (like vault, sinclastic or anticlastic surfaces). For surfaces with more than one curvatures the results may differ from the expectations.



## What should have had done differently

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Should have given more time between flat structure and vault structures to study possible fabrication techniques

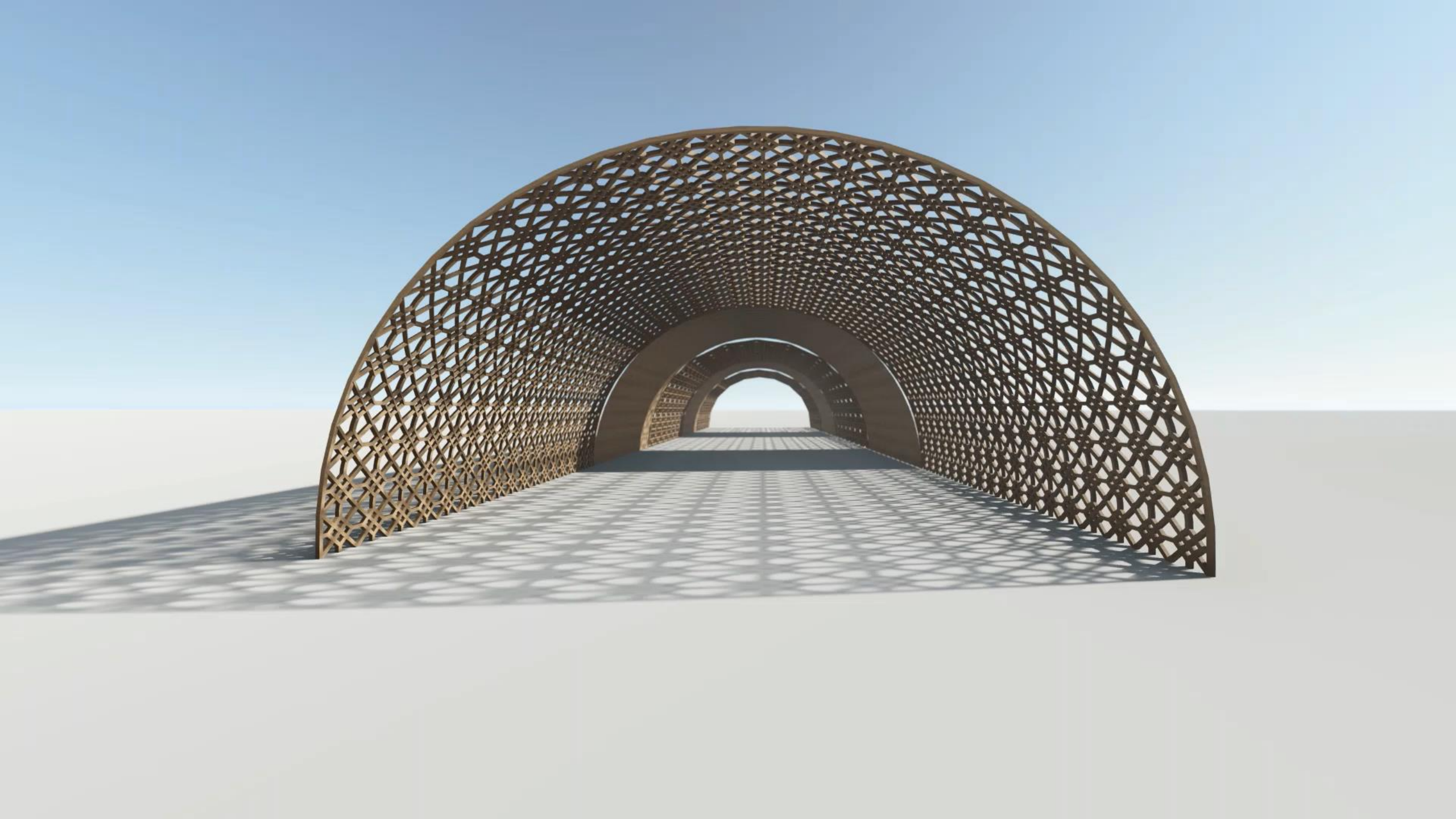
**For**

Different edge element cross-section

Preliminary idea of joints

Better smoothness of generated grid-shell







## Roof design

