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# Transported PDF modeling of jet-in-hot co-flow flames

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## Abstract

A probability density function (PDF) based combustion modeling approach for RANS simulation of a jet issuing into a hot and diluted coflow is performed. A tabulated chemistry-based model, i.e. Flamelet Generated Manifold (FGM), is adopted in the PDF method. The manifolds are constructed using igniting counter-flow diffusion flamelets with different coflow composition. To handle the inhomogeneity of the coflow and the entrainment of the ambient air, a second mixture fraction is defined to quantify the mixing of a representative coflow composition with the ambient air. The chemistry is then parameterized as a function of two mixture fractions and a reaction progress variable. To assess the modeling approach, Adelaide JHC flames, namely HM1, HM2, and HM3, having different oxygen concentrations in the hot coflow, 3%, 6%, and 9% O<sub>2</sub> respectively, have been simulated for Reynolds number (Re) = 10,000. Profiles of mean mixture fraction and major species are accurately captured by the model along with the mean temperature. The mean temperature profiles are also captured nicely while the sensitivity of Progress Variable (PV) on the predictions is highlighted.

**Keywords:** Hybrid RANS/PDF, FGM, Jet-in-Hot-Coflow

## 1. BACKGROUND

The need to avoid pollutant emissions has resulted in the development of new combustion techniques. These techniques include High-Temperature Air Combustion (HiTAC), Flameless Oxidation combustion (FLOX), and Moderate and Intense Low oxygen Dilution (MILD) combustion which falls under the category of 'clean combustion techniques.' One of the features of MILD combustion is the high re-circulation ratio. The hot gas re-circulation serves the combustion process in two ways; first, it raises the reactant temperature, providing the heat needed for stable ignition. Secondly, it reduces the oxygen concentration of the mixture which reduces the flame temperature and the thermal NO<sub>x</sub> emissions. Other features of the MILD combustion include flat temperature field, low turbulence fluctuations, smooth radiation flux, barely visible, and audible flame [1-8].

Dally et al. [9] of the Adelaide University designed a jet-in-hot-coflow burner and carried out experiments producing detailed profiles of major as well as minor species. The experiments performed on this burner provided a comprehensive database that has been used in the present study. Various numerical studies [10-18] have also been carried out using these databases to evaluate the performance of different turbulence and combustion models.

There have been various RANS based modeling studies carried out in the context of the Adelaide burner, most notable among them being the ones carried out by Christo et al. [10-11]. The major finding was the fact that the SKE turbulence model with a modified dissipation constant ( $C_{\epsilon 1}=1.6$ ) produces the best agreement with the experimental results. Other notable RANS based modeling studies include the ones carried out by Frassoldati et al. [12], Mardani et al. [13-14], and Aminian et al. [15]. All of these studies made use of the EDC combustion model in combination with DRM 22 [18], GRI 2.11 [20], and KEE-58 [21] chemical mechanisms to study the flame structure and the effects of molecular diffusion on flame characteristics in the MILD regime. Kim et al. [16] simulated the JHC flames using the Conditional Moment Closure (CMC) with the primary goal of understanding the flame structure and NO formation in the MILD regime. Ihme et al. [17-18] studied the JHC flames using LES with the Flamelet/Progress Variable (FPV) approach. They considered the burner as a three-stream mixing problem by introducing an additional conserved scalar to identify flamelets of different mixture composition and showed that the coflow mixture composition could only inadequately be represented by one mixture fraction.

From the above review, it is evident that a major problem while modeling these flames is the non-linear interaction between fluid mixing and finite rate chemistry in the MILD regime. The transported probability density function (PDF) method is suited to handle this problem. It allows us to include the effects of turbulence-chemistry interaction in the Reynolds Averaged Navier Stokes (RANS) framework [22].

The objective of this work is to explore the predictive capability of Flamelet Generated Manifold (FGM) chemistry [23] in a RANS/PDF framework. The FGM has been successfully applied to simulations of various combustion

systems [24-26]. In all these cases, a mixture fraction and a progress variable were adequate to create the table. This study is the first attempt to extend the FGM with a second mixture fraction to account for coflow in-homogeneity and air entrainment in predicting JHC flames in the MILD combustion regime. The numerical predictions obtained using this model are compared with experimental databases.

## 2. TABULATED CHEMISTRY CONSTRUCTION\*

### 2.1 Coflow representation

In the following, the tabulated chemistry model is presented for describing a three mixing problem. The chemistry data have been tabulated using the FGM approach. The FGM is based on laminar diffusion flamelets between the fuel ( $\text{CH}_4+\text{H}_2$ ) and the coflow (a mixture of combustion products and air). Since the coflow composition and temperature vary in space (Fig. 1), flamelets with different coflow compositions and temperatures are required. The mean temperature and mass fractions have been measured along the radial direction of the coflow at  $x=4$  mm above the jet nozzle as shown in Fig. 1. Following the approach of Ihme and See [17], a second mixture fraction  $Z_2$  is introduced, which will quantify the mixing between a coflow representative and the surrounding air and at the same time, can be used to describe the variation in the coflow composition based on oxygen concentration. The coflow representative is defined at the radial position  $r = r_{rep}$  such that:

$Y_{O_2}(r_{rep}) = \min(Y_{O_2}(r))$ . For every point in the radial direction, we define:

$$Z_2(r) = \frac{Y_{O_2}(r) - Y_{O_2}(r_{rep})}{Y_{O_2}(r_{air}) - Y_{O_2}(r_{rep})} \quad (1)$$

The coflow representative is given by  $Z_2 = 0$ , and the cold ambient air is provided by  $Z_2 = 1$ . In this approach, the enthalpy deficit ( $\Delta h$ ) relative to the adiabatic mixing is assumed strictly correlated with  $Z_2$ . To take into account that the enthalpy deficit is not a unique function of  $Z_2$  and to allow independent fluctuations of  $Z_2$  and  $\Delta h$ , it would be necessary to consider  $\Delta h$  as an extra independent variable. Assuming chemical equilibrium at the coflow inlet, the full composition is entirely determined from  $Z_2$ . With this definition, the composition and temperature at the coflow inlet are functions of  $Z_2$

$$\begin{aligned} Y_i(r) &= Y_i(Z_2(r)), \\ T(r) &= T(Z_2(r)). \end{aligned} \quad (2)$$

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\*This section is reproduced from Sarras et al. [27]

## 2.2 3D manifold construction

The FGM method is based on laminar flamelets. A flamelet is the solution of a low Mach number formulation of the one-dimensional Navier-Stokes equations supplemented with species and enthalpy equations, including detailed chemistry. The detailed chemistry model presently employed is the GRI 3.0 [20] reaction mechanism. Since the auto-ignition is the primary stabilization mechanism for the JHC [10] flames, unsteady effects should be included. Non-premixed unsteady laminar flamelets are formulated and solved in physical space and time with the CHEM1D code [28, 29]. Preferential diffusion effects are included using the mixture average approach. The initial condition for the unsteady flamelet solution is given by a pure mixing solution of the above boundary value problem. The oxidizer composition is a function of the second mixture fraction

$$Y_i^{ox} = (1 - Z_2) Y_i^{rep} + Z_2 Y_i^{air}.$$

FGM tables have been constructed for a set of values of the second mixture fraction with corresponding enthalpy deficit levels. First, the values for the second mixture fraction have been chosen which correspond to a particular radial location, and these values are needed to represent accurately the enthalpy deficit range of the coflow. For each  $Z_2$  value, a FGM table is constructed from a non-premixed igniting flamelet between fuel and the coflow composition at  $Z_2$  with the corresponding enthalpy deficit, according to Fig. 1. A moderate strain rate  $a = 100s^{-1}$  is used in all the flamelet calculations. For each of the coflow compositions, the solution is stored at successive time instances. These solution files form the base of the 2D-FGM construction. A total of ten 2D-FGMs are obtained.

The first step in the 2D-FGM construction consists of defining a suitable progress variable  $Y$ . In any given flamelet (i.e. fixed  $Z_2$  value), the progress variable must be a monotonic function of time at each physical position. Since the first mixture fraction is a monotonically increasing function of the spatial coordinate [25], this requirement can also be stated in terms of the first mixture fraction instead of the spatial position. The reaction progress variable in this work is defined by

$$Y = \sum_i \frac{Y_i}{M_i}, \quad (3)$$

Where  $Y_i$  is the mass fraction of  $CO_2$ ,  $CO$ ,  $H_2$ ,  $H_2O$ , or  $CH_4$  and  $M_i$  denotes the molar mass of the considered species. Then, the 2D-FGM is simply obtained by transforming the dependence on the spatial coordinate into a dependence on the first mixture fraction and time into dependence on the reaction progress variable

$$\phi(x, t; Z_2) \rightarrow \phi_{FGM}(Z_1, Y; Z_2) \quad (4)$$

where  $\phi$  stands for any thermo-chemical variable. In practice, this transformation is obtained by sorting and relabeling the data in each flamelet such that all dependent variables are stored as a function of the mixture fraction  $Z_1$  and the scaled progress variable  $c$ . The scaled progress variable is defined by

$$c = \frac{Y - Y_{\min}(Z_1)}{Y_{\max}(Z_1) - Y_{\min}(Z_1)}, c \in [0, 1] \quad (5)$$

The minimum  $Y_{\min}$  and maximum  $Y_{\max}$  values of the unscaled progress variable are also stored.

The 3D-FGM is obtained by combining the 10 different 2D-FGMs. Then, every local thermochemical state can be described by using the three independent variables  $Z_1, Z_2, Y$ ,

$$\phi = \phi(Z_1, Y; Z_2). \quad (6)$$

The computer program FLAME [30] developed at the TU-Delft has been used to optimize the tabulation of the 3D-FGM. In the FLAME code, the physical range of the four independent variables is mapped onto a cube  $[0, 1]^3$  to facilitate adaptive grid refinement. The grid refinement automatically detects regions in composition space  $(Z_1, Z_2, Y)$  with large gradients of the dependent variables and inserts grid points as necessary to resolve the gradients. The adaptive tabulation uses linear interpolation between any two 2D-FGMs ( $Z_2$  direction) and within each 2D-FGM ( $Z_1 - Y$  plane). For consistency, the density is not interpolated but is recalculated based on the interpolated temperature and composition. In addition to the relevant thermo-chemical variables, the source term of the progress variable is stored in the table,

$$S_Y(Z_1, Z_2, Y) = \frac{\dot{\omega}_Y}{\rho}. \quad (7)$$

However, special care has to be taken for the source term at the boundary  $Y = Y_{\max}(Z_1, Z_2)$  which corresponds to the steady-state flamelet solution. In the steady state we have

$$\frac{\partial \rho u Y_{\max}}{\partial t} - \frac{\partial}{\partial x} \left( \frac{\lambda}{c_p} \frac{\partial \rho Y_{\max}}{\partial x} \right) + \rho G Y_{\max} - \rho S_{Y_{\max}} = 0 \quad (8)$$

and hence, in general  $S_{Y_{\max}} \neq 0$ . Without any further measures, this leads to the occurrence of  $Y > Y_{\max}(Z_1, Z_2)$ . To avoid this problem, we set  $S_{Y_{\max}} = 0$  which holds in chemical equilibrium as obtained in a steady flamelet with a strain rate  $a \rightarrow 0$ .

### 3. PDF FORMULATION WITH 3D FGM TABLE

The details of the in-house PDFD code and the PDF method can be found in references [31-33]. Here we only describe the modifications that have been made to use the 3D-FGM in the PDFD simulations. Every Monte-Carlo particle carries two mixture fractions  $Z_1, Z_2$  and a reaction progress variable  $Y$ . This means that every particle now evolves in composition space according to the general equation:

$$d\phi_\alpha^* = \theta_{\alpha, mix}^* dt + S_\alpha(\vec{\phi}) dt \quad (9)$$

where  $\vec{\phi} \equiv (Z_1, Z_2, Y)$  and  $\alpha = 1, 2, 3$ . Also,  $\theta_{\alpha, mix}$  represents the chosen micro-mixing model and  $S_\alpha(\vec{\phi})$  the chemical source term of the progress variable. The mixture fractions are not affected by chemical reactions, and their values only change according to the chosen micro-mixing model. Radiative heat losses are not included here. The evolution of the reaction progress variable is split into a micro-mixing step and a reaction step. Micro-mixing is performed first, and then the reaction step is mainly based on an explicit Euler scheme:

$$dY = S_Y(\vec{\phi}) \cdot dt \quad (10)$$

where  $S_Y$  is the source term and  $t$  is the time step. A Runge-Kutta method [33] is implemented to accurately advance the progress variable changes due to the highly nonlinear source terms. In all the igniting flamelets, the source term is a very smooth function of the progress variable, and hence the gradients are small. The boundary conditions for the reaction progress variable at any radial position at the inlet is given by

$$Y = Y_{\min}(0, Z_2(r) = const) \quad (11)$$

The local composition is given by the two mixture fractions and the reaction progress variable. All other scalar variables (temperature, species mass fractions, density, etc.) are retrieved from the look-up table.

### 4. SIMULATION DETAILS

A detailed description of the burner geometry can be referred from Dally et al. [20-21]. In the context of the numerical setup, a very similar numerical setup, explained above, with a few changes has been used to model the methane-hydrogen JHC flames in the Adelaide burner. Two different flames with different oxygen content in the hot coflow have been simulated, namely, HM1 (3% O<sub>2</sub>), HM2 (6% O<sub>2</sub>), and HM3 (9% O<sub>2</sub>). The Reynolds number has been kept constant at Re=10000 for all three flames.

A 2D axisymmetric grid has been used in the simulations. As the central fuel jet protrudes 4 mm at the jet exit, the computational domain starts 4 mm downstream of the jet exit and extends for 300 mm in the axial direction and 80 mm

in the radial direction. The grid consists of 200x120 cells in the axial and radial direction, respectively (stretched in both directions). At the end of the computational domain, in the axial direction, the boundary condition is set to outflow. For the fuel jet inlet, the velocity profiles are used from a detailed separate simulation, whereas at the hot and cold coflow inlets, the velocity boundary conditions are set to 3.2 m/s and 3.3 m/s, respectively. As per the studies carried out by Frassoldati et al. [22], the solution is very sensitive to the turbulent quantities at the inlet, therefore, the turbulent intensities at the hot and cold coflow have been set to 5% while it is set to 7% at the fuel jet inlet as per the published results [22].

The flamelet generated manifold for the methane-hydrogen combustion is based on the GRI 3.0 [23] chemical mechanism with 53 species and 325 chemical reactions. The radial profiles of the temperature and species mass fraction with experimental values at  $x=4$  mm have been used to create the FGM tables. The FGM table resolution is set to  $ZxY=201x201$  points with equidistant spacing.

The PDF transport equation was solved using the Lagrangian Monte Carlo approach initialized with approximately 20 particles per cell. The effect of micro-mixing models is also studied with a mixing constant  $C_\phi = 2$ . The Reynolds number has been kept constant at  $Re=10000$ . The results obtained are compared with the respective experimental database, and the profiles of mean temperature, mean mixture fraction and major species are reported.

## 5. RESULTS AND ASSESSMENT\*\*

In this section, the simulation results are presented for three flames, i.e. HM1, HM2, & HM3. The profiles of mean temperature, mean mixture fraction and major species are reported and are compared with the respective experimental database.

### 3.1 Effect of Progress Variable

Initially, we have considered a different linear combination of PV to test the sensitivity of the PV in predictions. The mixing model is kept constant for all the simulation, and that is IEM. The considered combination is defined as:

$$\begin{aligned} PV1 &= CO_2 + H_2O + H_2 \\ PV2 &= CO + CO_2 + H_2O \\ PV3 &= CO + CO_2 + H_2O + H_2 \\ PV4 &= CO + CO_2 + H_2O + H_2 + CH_4 \end{aligned}$$

Figures 1-3 depict the radial profiles of mean Mixture fraction, temperature and one major species ( $O_2$ ) using different PV. As observed from the figures that the predictions are not sensitive to the different combinations of PV, thereby not showing any significant differences in results.

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\*\*Some portion of this section is reproduced from De et al. [8]

This means the linear combination of major species is good enough for the predictions of these flames. Hence, the rest of the results are reported with PV3 only, which is precisely the same as reported in the published work by Ihme et al. [24] to make an assessment of our predictions.

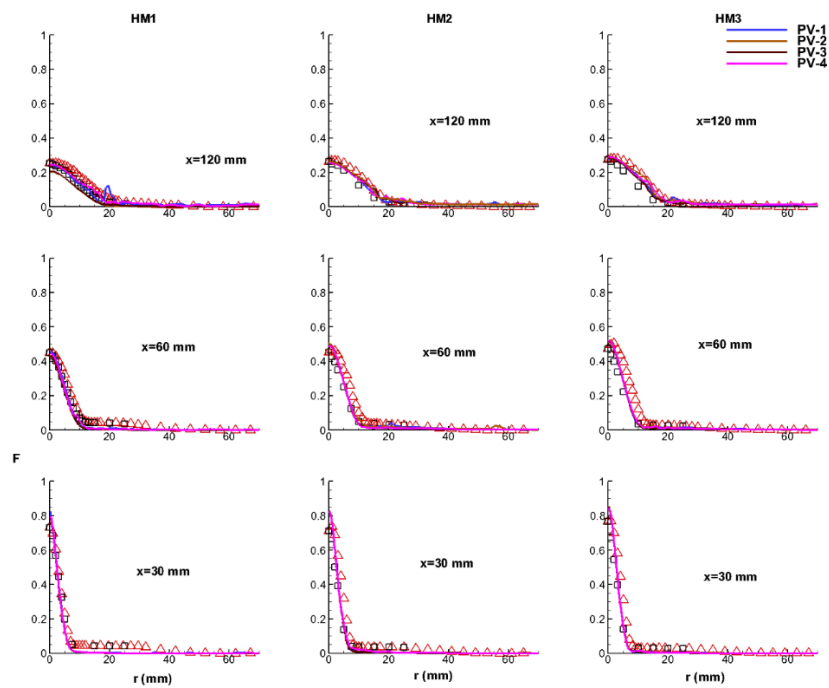


Figure 1: Radial profiles of mean Mixture fraction ( $F$ ) using different PV: (*triangle*  $0 \leq r \leq 70$ , *squares*  $-25 \leq r \leq 0$ ) symbols are measurements and lines are predictions

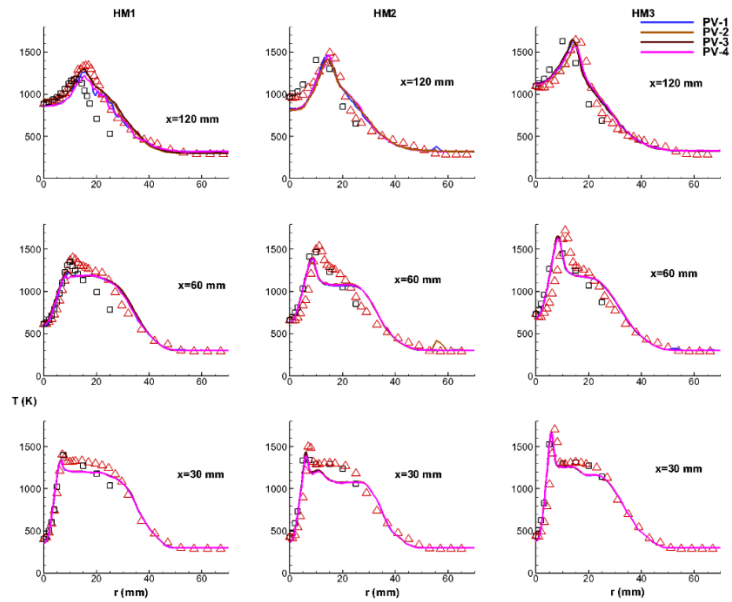


Figure 2: Radial profiles of mean temperature using different PV: symbols are measurements and lines are predictions (Legends are the same as Fig.1)

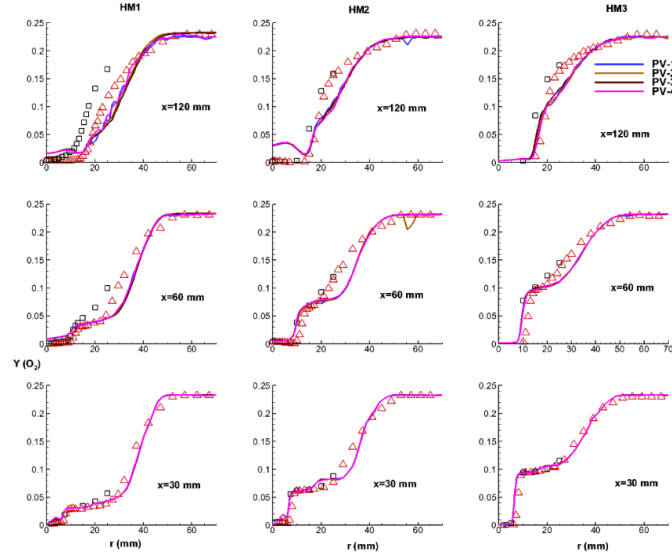


Figure 3: Radial profiles of mean  $O_2$  using different PV: symbols are measurements and lines are predictions (Legends are the same as Fig.1)

### 3.2 Effect of mixing models and PDF models

In this section, using the PV3 definition, a detailed analysis is carried out. Two critical parameters are varied here are: (a) Mixing models: IEM, CD, EMST, (b) PDF models: Scalar-composition PDF, Joint Velocity-Scalar Composition PDF.

Figure 4 shows the profiles of the mean mixture fraction obtained for HM1 flame. As observed, all the models capture the profiles accurately, and no significant differences are observed amongst these predictions except the CD model. Some discrepancies can be observed in the mean temperature profiles as depicted in Figure 4. The predictions are similar for HM2 & HM3 flames. For HM1 flame, the center-line temperature profiles are overpredicted; however, the predictions are improved along with the shear layer. Among the transported PDF models, the LPDF-EMST predictions are better compared to the LPDF-IEM and LPDF-CD predictions, especially for HM1 flame. No significant differences are observed using only the Scalar Composition PDF method, as represented using “Sc” in all the plots. The peak temperature predictions are reasonably well, while some discrepancies are observed at the outer shear layer, especially the case with lower  $O_2$  concentration, i.e. HM1 flame. Even though the LPDF-CD predictions are consistently poor in all three flames, we can observe an improvement in the predictions as the oxygen content in the coflow increases. As the oxygen content in the hot coflow increases from 3% (by mass) in HM1 to 6% in HM2 and to 9% in HM3 flames, the reaction rate improves due to which the models are able to predict the flames with better accuracy and a clear improvement in the temperature predictions, obtained using all the models.

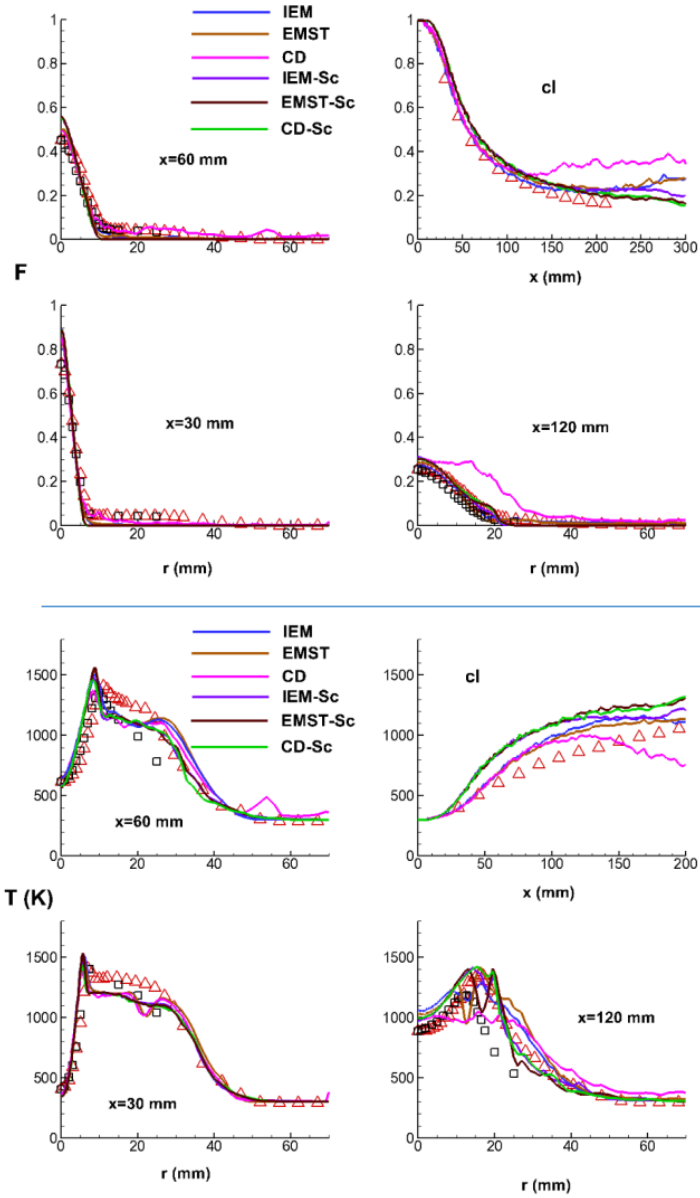


Figure 4: Profiles of mean mixture fraction and Temperature for HM1 flame (Legends are the same as Fig.1). “Sc” stands for Scalar Composition PDF

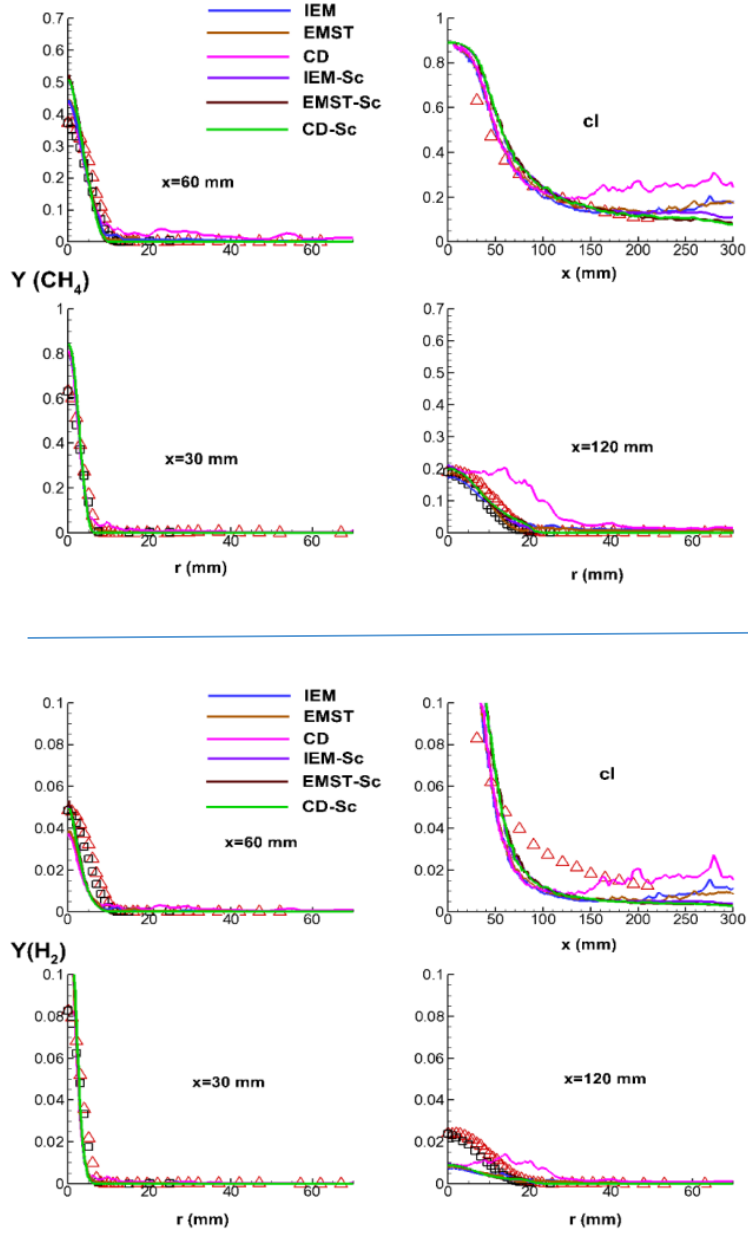


Figure 5: Profiles of mean  $\text{CH}_4$  and  $\text{H}_2$  for HM1 flame (Legends are the same as Fig. 1)

Figure 5 depicts the profiles of mean  $\text{CH}_4$  and  $\text{H}_2$  mass fraction obtained for HM1 flame. Near the jet exit, the peak of  $\text{CH}_4$  is over-predicted by all the models, but the mean  $\text{H}_2$  profiles are found to be good. Major discrepancies can be observed in  $\text{O}_2$  predictions for all three flames, as shown in Figures 6-8. In this case, the dominance of Scalar composition PDF is observed at the downstream locations. Even after providing better boundary conditions for oxygen (obtained from  $x=4$  mm measurements) for all three flames, the evolution of  $\text{O}_2$  could not be captured accurately. This discrepancy is primarily due to the handling of reaction rate in modeling (turbulence-chemistry interaction) and cannot be quantified unless we look at the velocity statistics in the domain, and this remains another drawback of this burner as it does not provide any velocity data. Among the LPDF models, there are no substantial differences observed between IEM and EMST predictions for all three flames, but as we move to HM2 and HM3, we observe the predictions appear to be in better shape, especially, for HM3 flame. For all three flames, LPDF-CD predictions show substantial differences from the other two models [8].

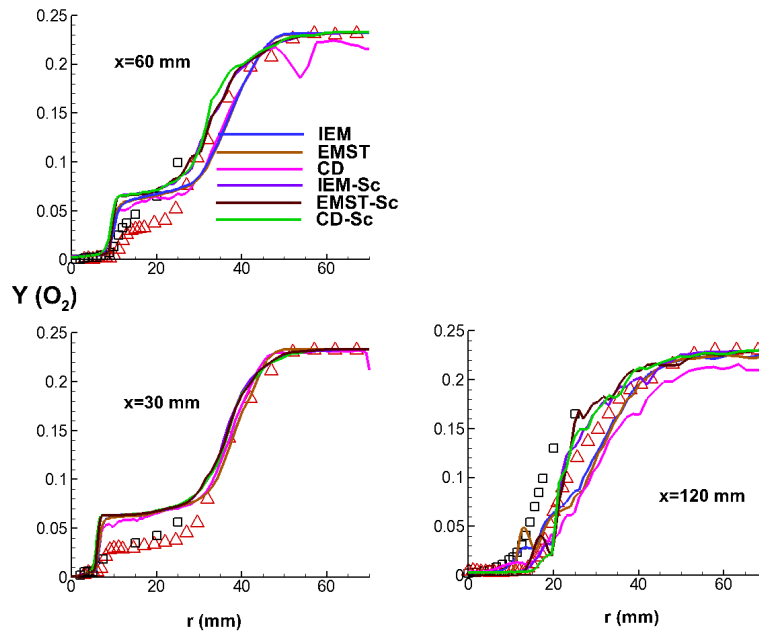


Figure 6: Profiles of mean  $\text{O}_2$  for HM1 flame (Legends are the same as Fig.1)

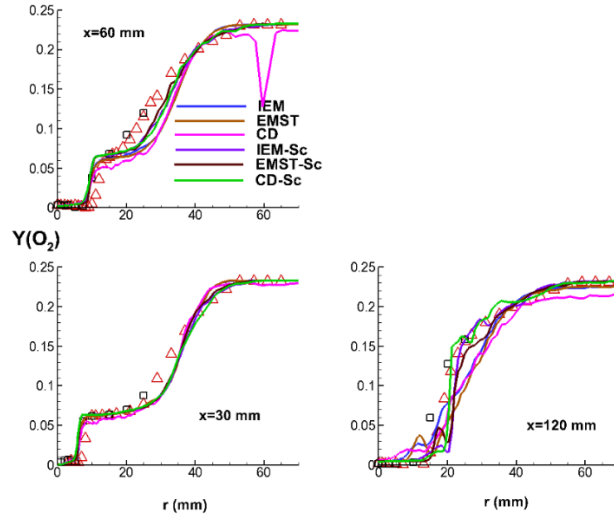


Figure 7: Profiles of mean  $O_2$  for HM2 flame (Legends are the same as Fig.1)

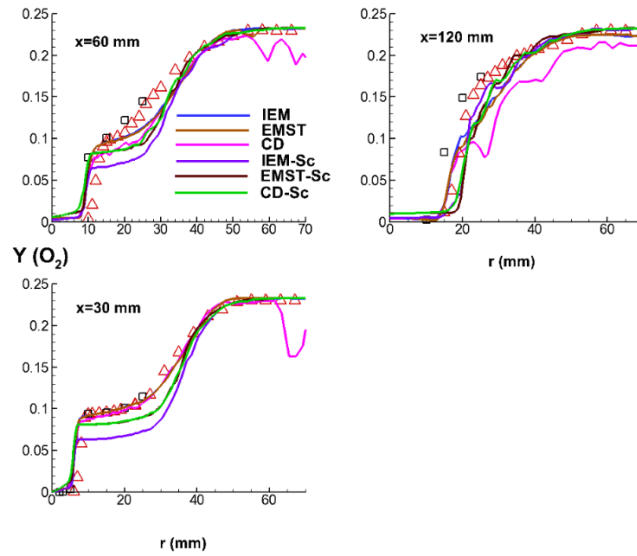


Figure 8: Profiles of mean  $O_2$  for HM3 flame (Legends are the same as Fig.1)

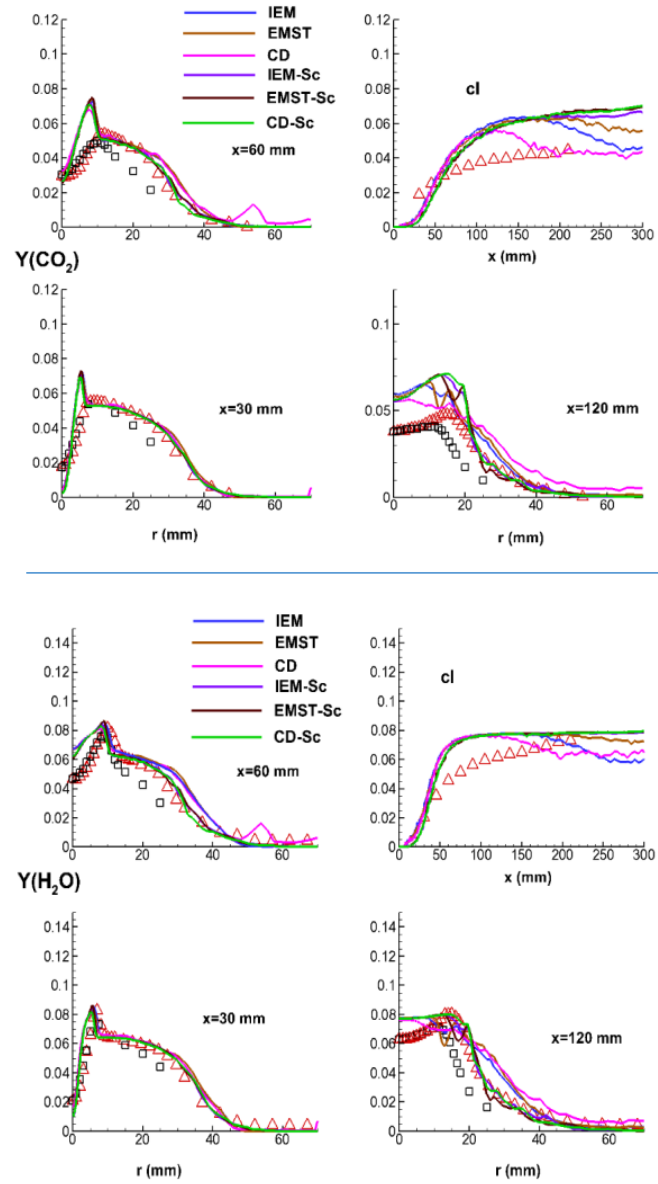


Figure 9: Profiles of mean  $\text{CO}_2$  and  $\text{H}_2\text{O}$  for HM1 flame (Legends are the same as Fig. 1)

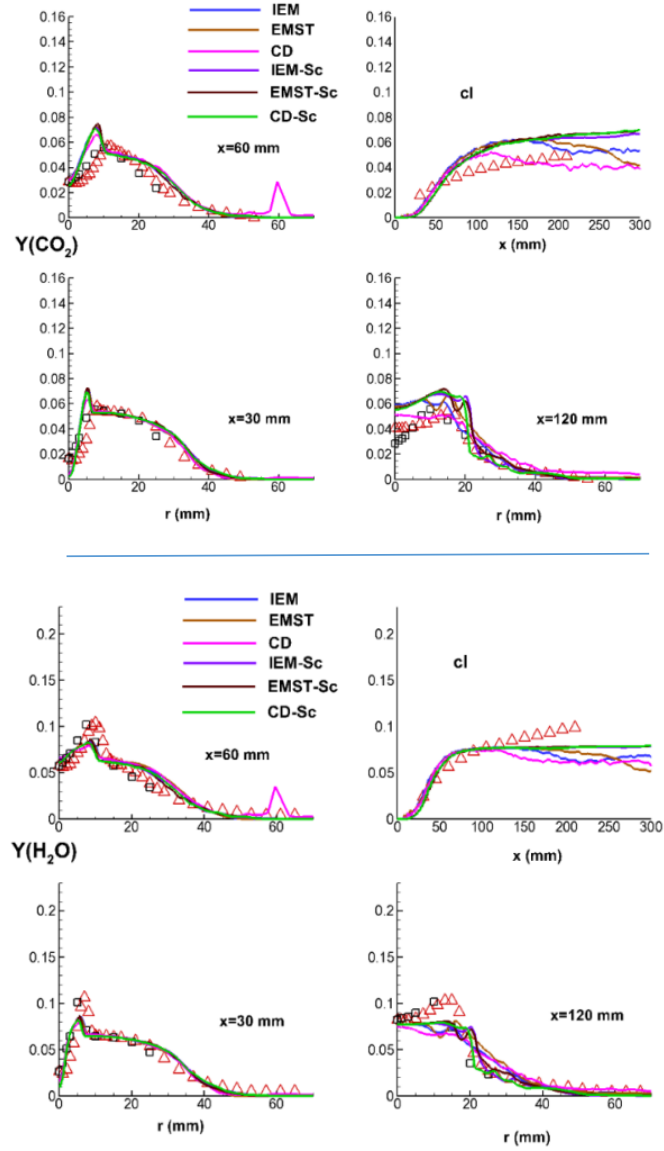


Figure 10: Profiles of mean  $\text{CO}_2$  and  $\text{H}_2\text{O}$  for HM2 flame (Legends are the same as Fig.1)

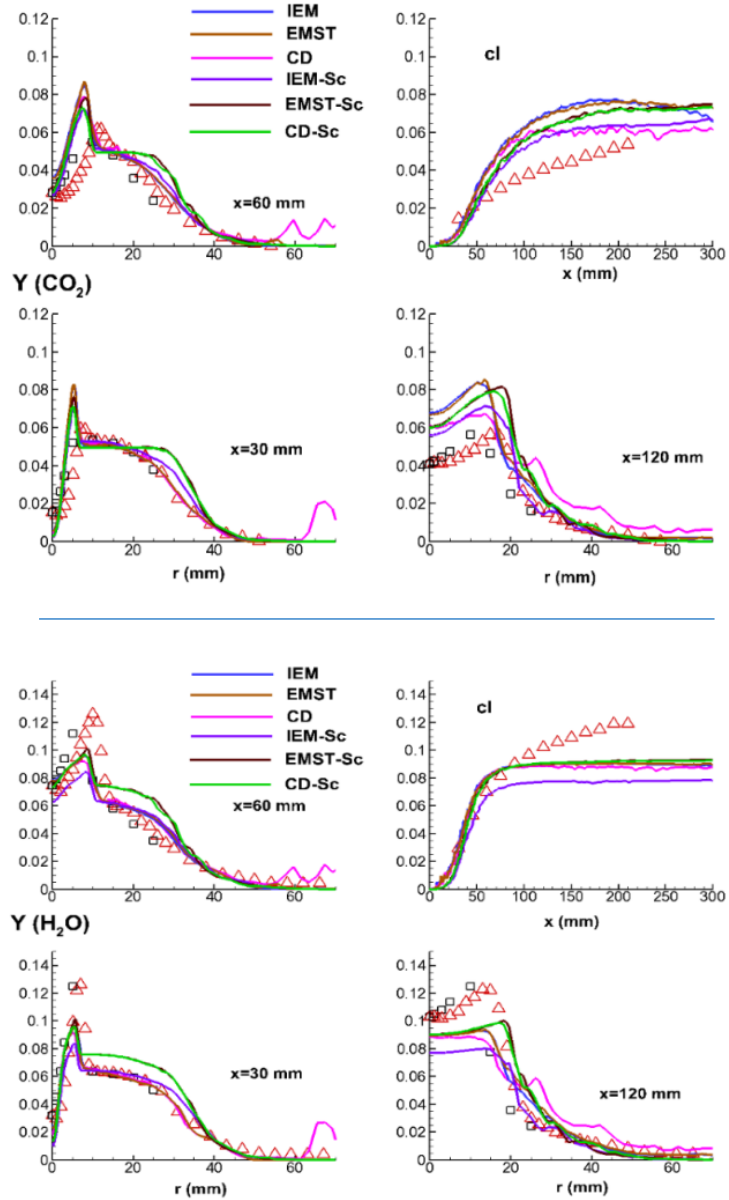


Figure 11: Profiles of mean  $\text{CO}_2$  and  $\text{H}_2\text{O}$  for HM3 flame (Legends are the same as Fig. 1)

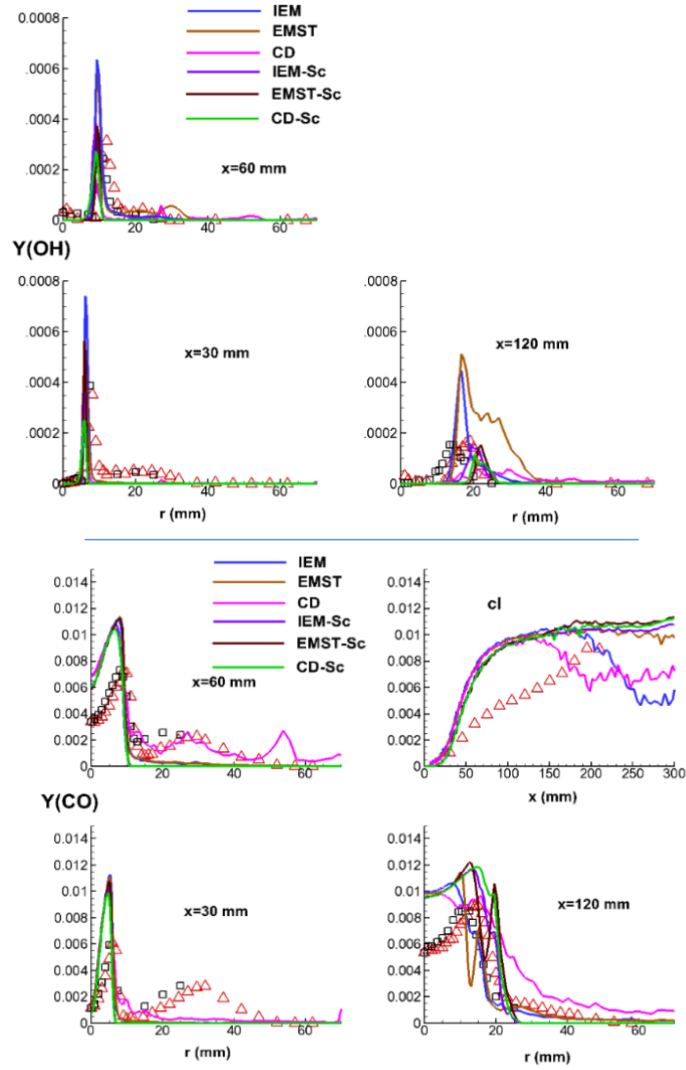


Figure 12: Profiles of mean OH and CO for HM1 flame (Legends are the same as Fig. 1)

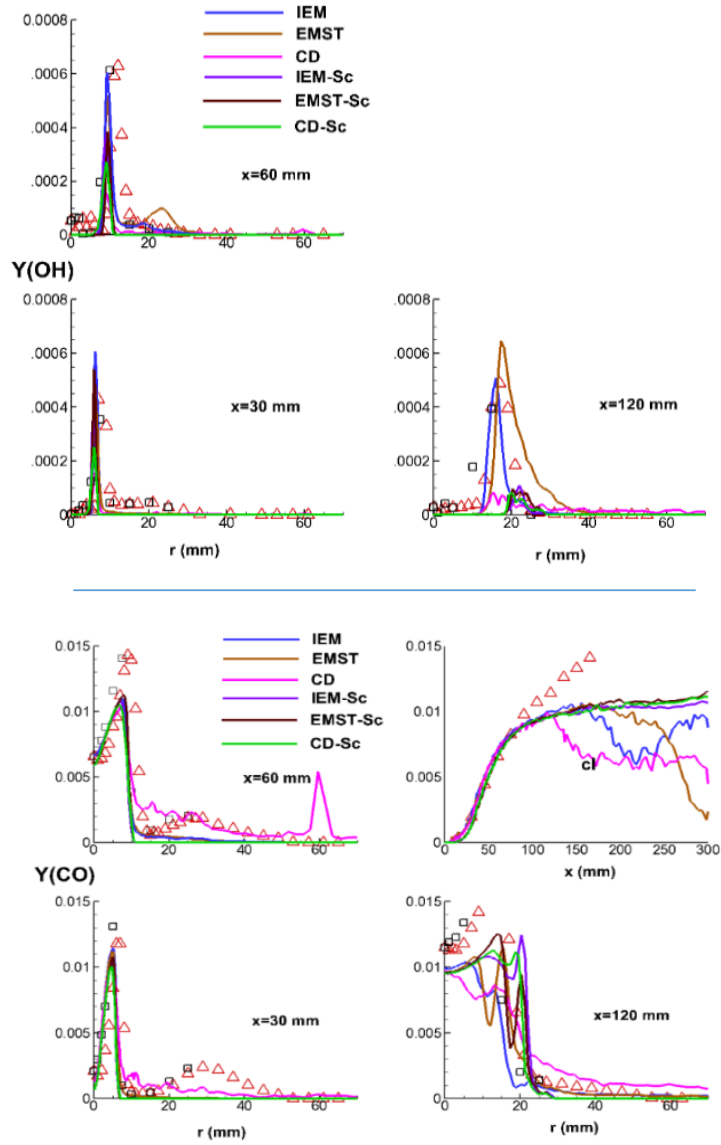


Figure 13: Profiles of mean OH and CO for HM2 flame (Legends are the same as Fig. 1)

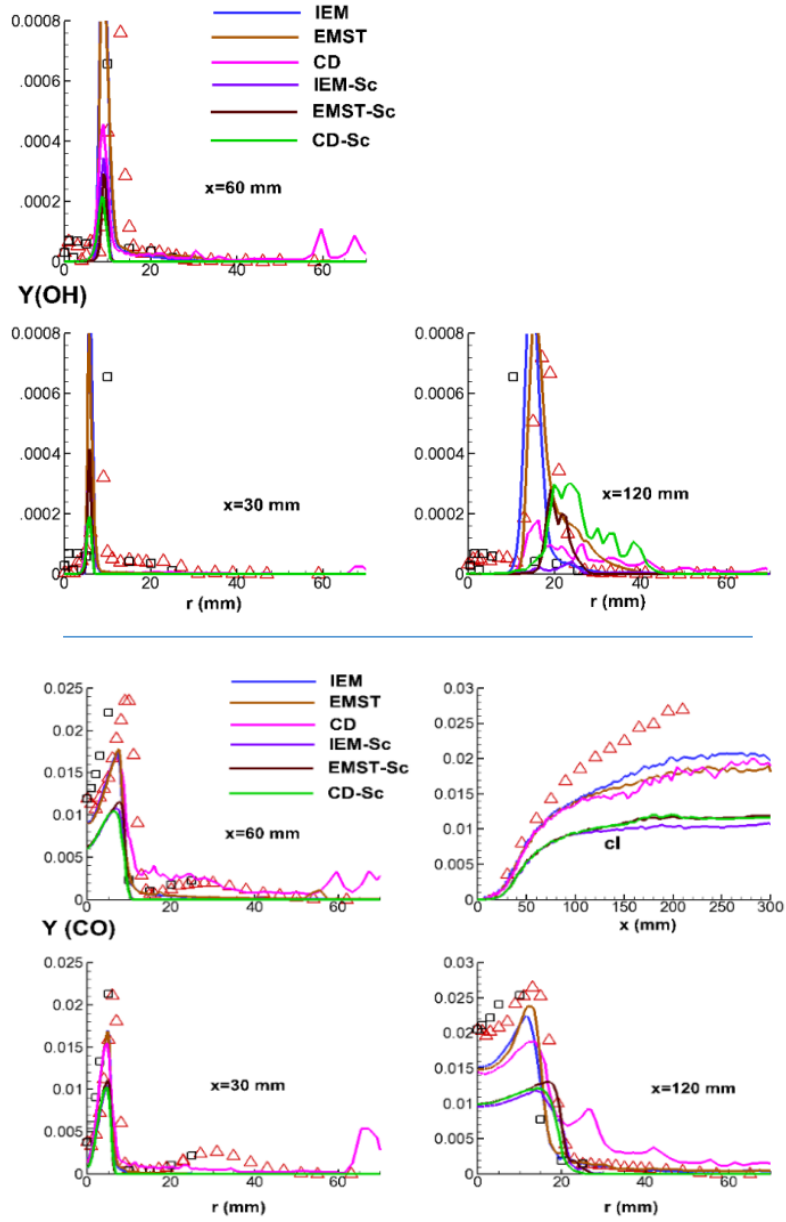


Figure 14: Profiles of mean OH and CO for HM3 flame (Legends are the same as Fig.1)

The profiles of mean  $\text{CO}_2$  and  $\text{H}_2\text{O}$  mass fraction obtained for HM1, HM2, and HM3 flames are shown in Figures 9-11. All the models adequately capture the profiles near the jet exit area, but the centerline profiles are consistently over-predicted. Discrepancies can be observed for the predictions away from the jet exit at  $x=120$  mm location. The profiles of mean  $\text{H}_2\text{O}$  mass fraction exhibit a completely different picture from that of  $\text{CO}_2$  profiles. As the oxygen content increases in the coflow from HM1 to HM3 flames, the extent of under-prediction at the centerline also increases. Previous studies all reported similar behavior where they have looked at the impact of chemical kinetics; however, the present study includes fairly detailed chemistry. Thus, we can assert that the chemical mechanism is not primarily responsible for the predictions obtained herein. However, it should be noted that the turbulent time scale is the dominant factor along the centerline, which supersedes the scalar dissipation time scale, and hence the combustible mixture dissipates quickly as the species are not allowed to stay for a longer duration in this region to complete reaction. This is one of the major reasons behind the discrepancies observed in species profiles along the centerline, especially the  $\text{O}_2$  profiles and temperature, in-turn, affecting the  $\text{CO}$  and  $\text{H}_2\text{O}$  profiles. This slow chemistry increases the chemical time scales, in turn, reduces the Damkohler number, and all the combustion models are unable to capture the flame characteristics in this low Damkohler number range, which has significantly affected the species predictions.

To better understand the model behavior, it is worthwhile to look at the predictions of minor species like  $\text{OH}$  and  $\text{CO}$ . Major discrepancies can be observed in Figures 12-14 depicting  $\text{OH}$  and  $\text{CO}$  profiles, respectively. Looking at the radial profiles of  $\text{OH}$  obtained for HM2 and HM3 flames, it can be seen here that the predictions are in better shape compared to those obtained for HM1 flame as the oxidation of  $\text{O}_2$  into  $\text{OH}$  is sufficiently captured. The  $\text{CO}$  profiles are significantly under-predicted in the shear layer between fuel jet and hot coflow for HM2 and HM3 flames. The  $\text{CO}$  profiles are better in HM3 compared to those obtained in the HM2 flame owing to the better performance of combustion models due to improved reaction rates and oxygen contents in the coflow. While comparing all the models, it has been observed that the differences between EMST and IEM predictions are small and better compared to the CD predictions, which show considerable deviation from the two. It can be noted that the  $\text{CO} \rightarrow \text{CO}_2$  conversion is significantly affecting the proper predictions of  $\text{CO}_2$ , whereas  $\text{OH} \rightarrow \text{H}_2\text{O}$  conversion is not significantly affecting the  $\text{H}_2\text{O}$  predictions. These phenomena are strongly coupled between turbulence-chemistry interaction models and chemical mechanism which needs further investigation [8].

The discrepancies observed, so far, with the finite rate chemistry-based models arise due to multiple reasons. Slower reaction rates in JHC flames, compared to standard combustion processes, make it more challenging for modeling. Despite having the chemical source terms in closed form, the transported PDF models cannot also be precisely accurate as the major source of errors in these models comes from the inaccuracies of the micro-mixing closures. The predictions in the shear layer are primarily affected due to mixing between the hot coflow and the fuel jet. This mixing between the streams, due to turbulence and species gradients, emphasizes the role of micro-mixing here. In case of IEM model [34], the

composition of all the scalars relaxes towards the mean composition at the same rate whereas in case of CD mixing model, a number of particles in a cell are randomly selected and their individual compositions are moved towards the mean composition [35]. Therefore, both of these mixing models are missing the effect of localness in the flow field which is a potential source of errors for the discrepancies observed in the predictions obtained through these models. However, on the contrary, the EMST model [36] takes into account the effects of local mixing among the particles in the composition space and thereby making it more accurate compared to the CD and the IEM models. Since, in the case of the CD mixing model, the particles, in a cell, are selected randomly, CD formulation is missing the effects of localness in the composition space, which is the main reason behind the differences observed between EMST and CD predictions. Another potential source of errors may arise from the 'notional particles' used in Lagrangian PDF approach: one due to particle tracking scheme, and another one due to Monte-Carlo methods. The mean density of particles in physical space should remain proportional to the local mean fluid density all the times, and this can be satisfied as long as the particle systems evolve consistently with the Eulerian equation systems. Therefore, the accuracy of the particle tracking scheme may induce some errors. The second source of discrepancies in the LPDF predictions is the numerical errors associated with the Monte-Carlo methods, e.g. statistical errors, bias errors. Statistical errors are the random errors whereas bias errors are deterministic errors and both of them are strongly dependent on the number of particles used per cell. Statistical errors are not present in the present simulations; however, the bias errors, which arise from the mean quantities, are not completely reduced by averaging [8, 22].

In the JHC flames, the initiation of reaction is delayed, and overall reaction rates are lower than the conventional flames with lower temperatures and  $\text{NO}_x$  emissions. For the HM1 flame, there's 3% oxygen in the coflow, which is too much dilution for a JHC flame, and hence the HM1 flame forms a very crude case for studying the combustion models. Thus, comparing all the flames spread over a wide range of  $\text{O}_2\%$  (3-9) at the end, it is evident that predictions improve as the oxygen content of the coflow increases, the reaction rate also increases, which, in turn, increases the Damkohler number. Therefore, we can say that we obtain better results at high Damkohler numbers irrespective of the chosen turbulence-chemistry interaction models. Overall, the mean predictions obtained through transported PDF-based models are in good agreement with some discrepancies observed mostly in the shear layer between the fuel jet and the hot coflow.

## 6. CONCLUSION

The performance of hybrid RANS/PDF method including tabulated chemical kinetics to predict the JHC flames, is reported. A 3D FGM table based on two mixture fractions and a reaction progress variable has been constructed to account for the inhomogeneity of the coflow and the entrainment of the ambient air. Igniting counterflow diffusion flamelets are created for different coflow compositions quantified

by the second mixture fraction. To assess the predictive capability of the 3D tabulated chemistry manifold, Adelaide JHC flames have been considered for varying degrees of parameters. Comparison between predicted and measurements are found to be in good agreement. It can be inferred from the present simulations that the 3D FGM based tabulated chemistry has the potential to predict JHC flames combustion with greater accuracy, and the sensitivity of current methodology needs further investigation for betterment.

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