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Persistent atomic frequency comb based on Zeeman sub-levels of an erbium-doped crystal waveguide

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Long-lived sub-levels of the electronic ground-state manifold of rare-earth ions in crystals can be used as atomic population reservoirs for photon echo-based quantum memories. We measure the dynamics of the Zeeman sub-levels of erbium ions that are doped into a lithium niobate waveguide, finding population lifetimes at cryogenic temperatures down to 0.7 K as long as seconds. Then, using these levels, we prepare and characterize atomic frequency combs (AFCs), which can serve as a memory for quantum light at 1532 nm wavelength. The results allow predicting a 0.1% memory efficiency, limited mainly by unwanted background absorption that we believe to be caused by excitation-induced erbium spin flips and frequency shifting due to two-level systems or non-equilibrium phonons. Hence, while it should be possible to create an AFC-based quantum memory in $\text{Er}^{3+}:\text{Ti}^{4+}:\text{LiNbO}_3$, improved crystal growth together with optimized AFC preparation will be required to make it suitable for applications in quantum communication. © 2020 Optical Society of America

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1. INTRODUCTION

Cryogenically cooled rare-earth-ion-doped (REI-doped) crystals have been extensively studied for their use in classical optical signal processing applications for several decades [1]. This is partially due to their convenient optical and spin-level structure, long population and coherence lifetimes, large inhomogeneous broadening, and their tunability with externally applied fields [2]. More recently, this work has spawned applications in quantum signal processing, including photon echo-based quantum memories for light [3–9].

Several such protocols, including the widely employed atomic frequency comb (AFC) protocol [10], require frequency-selective optical pumping (or persistent spectral hole burning) of REIs into a long-lived energy level, referred to as a shelving level [see Fig. 1(a)]. Typically, this level is a spin (hyperfine) level within the electronic ground-state manifold that features a much longer population lifetime than that of the optically excited level. This allows waiting for excited atoms to decay at

the end of the optical pumping sequence without losing the spectral population grating in the ground state, which is key to quantum-state storage with high fidelity and efficiency [11].

Among the REIs, Er^{3+} is the only one that features a transition from the ground level to an excited level at a telecommunication wavelength of around 1.5 μm . Since Er^{3+} is a Kramer's ion, the ground level (more precisely, its lowest-lying crystal field level) is split into two electronic Zeeman sub-levels under the application of a magnetic field. If a host crystal contains nuclear spins, these may couple to the Zeeman sub-levels of Er^{3+} , resulting in further splitting into superhyperfine levels [2]. Both Zeeman and superhyperfine levels are potentially useful as shelving levels for the AFC memory preparation, with the key requirement that they must feature a long population lifetime. But since the memory bandwidth assuming high-efficiency storage is limited by ground-state splitting, optical pumping into electronic Zeeman levels is preferred due to their larger splitting in a magnetic field.

Partially motivated by its remarkably long optical coherence lifetime of 4.4 ms [12], initial studies towards a telecommunication-wavelength quantum memory have focused on $\text{Er}^{3+}:\text{Y}_2\text{SiO}_3$ [13] and electronic Zeeman levels for spectral hole burning. However, their 130-ms population lifetime [14] (limited by Er^{3+} spin flip-flops [15]) in conjunction with 11-ms optical population lifetime has so far prevented reaching efficiencies in excess of 0.25%. Later, AFC-based storage of entangled photons in an Er-doped SiO_2 fiber [16] was achieved by exploiting spin disorder, which reduces spin flip-flops between Zeeman levels compared to those in crystals. On the other hand, the amorphous nature of SiO_2 also leads to small optical coherence lifetimes, thereby restricting storage times to less than 100 ns. Furthermore, the disorder-induced inhomogeneous broadening of the spin-transition has limited storage efficiencies similar to values as in $\text{Er}^{3+}:\text{Y}_2\text{SiO}_3$ [17,18]. More recently, storage of heralded single photons using AFCs in an Er- and Ti-doped LiNbO_3 ($\text{Er}^{3+}:\text{Ti}^{4+}:\text{LiNbO}_3$) waveguide was achieved by taking advantage of population shelving in superhyperfine levels [19]. However, as before, the efficiency did not exceed the percent level, this time due to remaining absorption in the AFC troughs caused by the complexity of the superhyperfine structure and excitation-induced spin relaxation [19]. In addition, the superhyperfine splitting limits the bandwidth for high-efficiency AFCs to around 100 MHz, even assuming magnetic fields of several Tesla. Finally, AFC-based storage of qubits encoded into attenuated laser pulses has been demonstrated using $^{167}\text{Er}^{3+}:\text{Y}_2\text{SiO}_3$. This work relied on spectral hole burning into nuclear spin levels of the ^{167}Er isotope [20], and the use of a nanocavity to reduce the lifetime of the excited level by means of the Purcell effect. However, the small storage bandwidth of 150 MHz, determined by the inhomogeneous linewidth of $^{167}\text{Er}^{3+}:\text{Y}_2\text{SiO}_3$, and the small efficiency of less than 1% support the general conclusion that the creation of a workable quantum memory for telecommunication-wavelength photons remains an open challenge. An interesting possibility is the use of the same crystal in a magnetic field of

several Tesla [21], but, so far, no storage experiment has been reported.

Here, we explore the generation of AFCs in $\text{Er}^{3+}:\text{Ti}^{4+}:\text{LiNbO}_3$ using Zeeman sub-levels for population shelving. First, we quantify the population lifetime of these levels using time-resolved spectral hole burning at a temperature of around 0.7 K and at magnetic fields of up to 1 kG. Next, we create AFCs that persist for up to a few seconds. However, the AFC structures are consistently marred by a significant absorption background, which restricts potential storage efficiencies. Probing the origin of this background, we believe, after exclusion of other causes, that it is due to (1) coupling between laser-induced excitations of two-level systems (TLSs) and spins of erbium ions (leading to spin flips), (2) coupling between laser-induced excitations of TLSs and electronic levels of erbium ions (leading to spectral diffusion of optical transitions) [22–25], or (3) laser-induced excitations of non-equilibrium phonons, which may also cause spectral diffusion of optical transitions [26]. We conclude that improved crystal growth together with optimized AFC preparation will be required to create an efficient and high-bandwidth quantum memory.

2. EXPERIMENTAL DETAILS

Our experiments are performed using the $^4\text{I}_{15/2} \leftrightarrow ^4\text{I}_{13/2}$ transition of $\text{Er}^{3+}:\text{Ti}^{4+}:\text{LiNbO}_3$, which is cooled to a temperature of around 0.7 K using an adiabatic demagnetization refrigerator. Details of the waveguide fabrication can be found in Ref. [19]. The waveguide is exposed to magnetic fields up to 5 kG oriented parallel to the c axis of the crystal. The field lifts the Kramer's degeneracy of the ground and excited electronic levels of erbium, giving rise to Zeeman levels [see Fig. 1(a) for a simplified energy level scheme of Er^{3+}]. To interact with the erbium ions, we use light from a continuous-wave laser at around 1532 nm wavelength. As shown in Fig. 1(c), it is frequency and intensity modulated, and then fiber butt-coupled into and out of the waveguide.

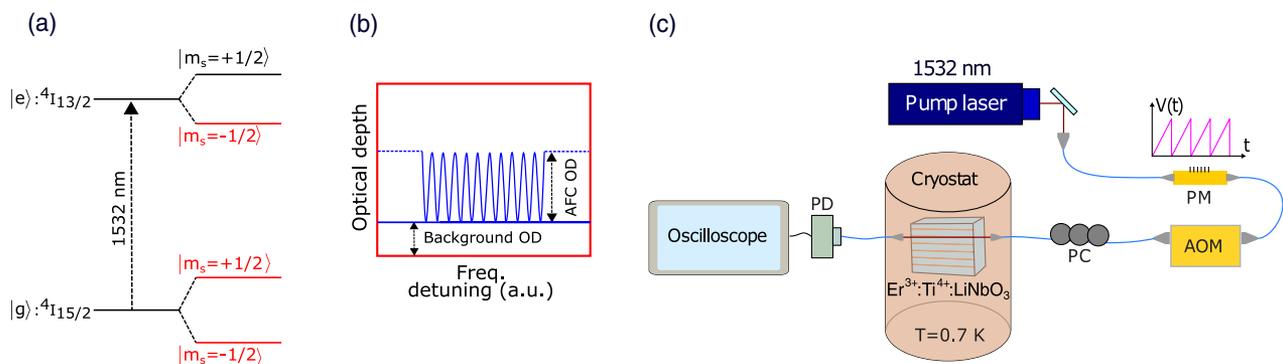


Fig. 1. (a) Simplified energy level structure of the $^4\text{I}_{15/2} \leftrightarrow ^4\text{I}_{13/2}$ transition of Er^{3+} . Excited and ground levels are indicated with $|e\rangle$ and $|g\rangle$, respectively, and electronic Zeeman sub-levels with $|m_s = \pm 1/2\rangle$. To create an atomic frequency comb (a periodic modulation of the frequency-dependent optical depth into equally spaced narrow peaks), persistent spectral holes are created (burned) by pumping all undesired population into shelving levels, e.g. $|g, m_s = +1/2\rangle$. (b) Example of an AFC, showing the resulting spectral population grating. (c) Experimental setup. Continuous-wave light at 1532 nm wavelength is directed through a phase modulator (PM) and an acousto-optic modulator (AOM), which allow frequency and intensity modulation. After passing a polarization controller (PC), the light creates spectral holes and AFC structures in the erbium-doped lithium niobate waveguide, and furthermore allows probing previously created structures with the help of a photo-detector (PD) and an oscilloscope. The PM is driven by a serrodyne voltage $V(t)$ modulation similar to that depicted in the plot.

For time-resolved spectral hole burning measurements, we first optically excite erbium ions within a narrow spectral bandwidth, detuned by 250 MHz w.r.t the unmodulated laser light, using pulses of around 300 ms duration. The resulting decay redistributes the ions among the Zeeman sub-levels of the ground state, resulting in a spectral hole. After a varying time delay that exceeds the 2.1 ms population lifetime of the $^4I_{13/2}$ excited level, we measure the decay of the area of the spectral hole (which is proportional to the number of shelved atoms) by linearly varying the frequency of the laser light during 1 ms over a 100 MHz wide frequency window surrounding the hole. Frequency sweeps are achieved by using a phase modulator and serrodyning, resulting in a modulation efficiency at 1 GHz detuning of approximately 50%.

For AFC generation, we frequency and intensity modulate the excitation light to burn up to 130 spectral pits over a bandwidth of up to 6.4 GHz during 300 ms. Each spectral pit is detuned by 50 MHz from its nearest neighbor to create a periodic modulation in the inhomogeneously broadened atomic absorption spectrum. This frequency spacing of the spectral pits corresponds to an AFC storage time of 20 ns [10]. The absorption profile of the comb is read after a time delay of 30 ms by performing a frequency sweep over bandwidths of up to 6.4 GHz in 1 ms. All measurements are repeated 20 times, and hole and AFC absorption profiles are determined by averaging.

3. RESULTS AND DISCUSSION

A. Population Dynamics of Ground-State Sub-Levels

Time-resolved spectral hole burning is performed at fields of 350, 600, and 800 G. The time-dependent decay of the hole area is plotted in Fig. 2, indicating the occupation and the population lifetime of the ground-state Zeeman sub-levels along with those of any other shelving level [17]. We find that the best fit corresponds to a double exponential decay in which the shortest decay exhibits an e^{-1} population lifetime of $t_{\text{short}} \approx 0.06$ s that is independent of the magnetic field, whereas the e^{-1} population lifetimes of the long decays are $t_{\text{long}} = 1.00, 1.36,$ and 2.44 s for magnetic fields of 350, 600, and 800 G, respectively. The relative weights of the exponentials do not change with field. Note that we are unable to burn the hole to transparency, and we also do not resolve any side-holes or anti-holes, which arise from pumping of atomic population between different, well-defined, atomic levels [27].

The short, field-independent decay is caused by population trapping in ground levels that couple only weakly to magnetic

fields. Previous hole burning measurements [19], in conjunction with the temperatures and fields used here, suggest that these levels are likely superhyperfine levels arising from the coupling of Nb and Li spins of LiNbO_3 .

The approximately linear field dependence of the population lifetimes of the long decays (t_{long}) suggests that it is governed by spin flips [17]. An increasing magnetic field causes more ions to become spin polarized at low temperatures, which leads to a reduced spin flip-flop probability. Furthermore, the spin inhomogeneous broadening increases with field and reduces the flip-flop rate, since it is less likely for two neighboring spins to be resonant [17]. We fit the relaxation rate of the long decays $1/t_{\text{long}}$ using a model that describes the temperature (T) and field (B) dependence of spin flip-flops and inhomogeneous broadening [17]:

$$\frac{1}{t_{\text{long}}} = \frac{\alpha}{\Gamma_s + \gamma_s B} \text{sech}^2\left(\frac{g\mu_B B}{2kT}\right). \quad (1)$$

The magnitude of the spin inhomogeneous broadening is described by a static term Γ_s and a field-dependent term $\gamma_s B$, g is the g -factor, μ_B the Bohr magneton, and α a scaling coefficient.

For a reliable fit of the limited experimental data shown in Fig. 2(d), we assume $g = 15.13$, which was inferred from measurements of an $\text{Er}^{3+}:\text{LiNbO}_3$ bulk crystal [28,29]. Furthermore, fixing the scaling factor of α at 10^9 s^{-2} , as in [17], we find static and field-dependent spin inhomogeneous broadenings of $\Gamma_s = 0.4 \pm 0.1$ GHz and $\gamma_s = 14.5 \pm 3.0$ GHz/T, respectively. The relatively large values are not surprising given the significant spin inhomogeneous broadening of nuclear Zeeman levels of Tm^{3+} in a $\text{Ti}^{4+}:\text{LiNbO}_3$ waveguide (0.7 GHz/T) [30,31]. This broadening has been attributed to the congruent growth of LiNbO_3 , a material property that also affects the results of the current study [32].

B. Creation of AFCs Using Zeeman Sub-Levels

In order to assess the possibility for broadband quantum memory using Zeeman sub-levels as a population reservoir, we generate AFCs with bandwidths between 0.2 and 6.4 GHz symmetrically around zero detuning. All AFCs are centered at 1532.05 nm (corresponding to a spectral region with an optical depth of two for light propagating perpendicular to the crystal c axis), created under the application of a 3 kG magnetic field (oriented along the crystal c axis), and feature peak spacings of 50 MHz. Furthermore, the overall duration of the optical pumping cycle is kept constant. Figure 3 shows a 200 MHz

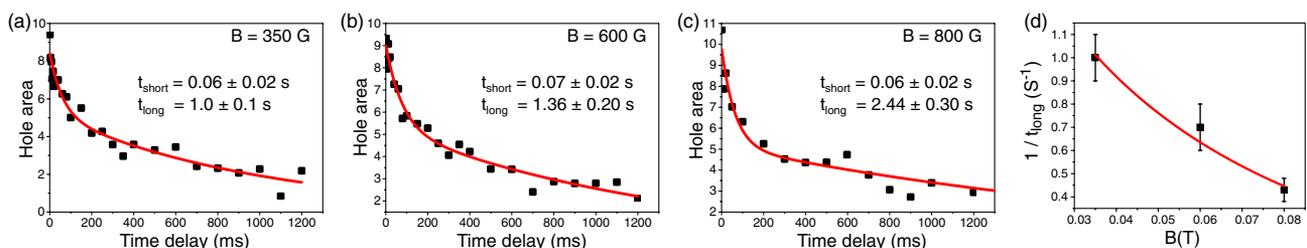


Fig. 2. Time-resolved spectral hole decays at magnetic fields of (a) 350 G, (b) 600 G, and (c) 800 G. (d) Long-decay relaxation rate versus magnetic field.

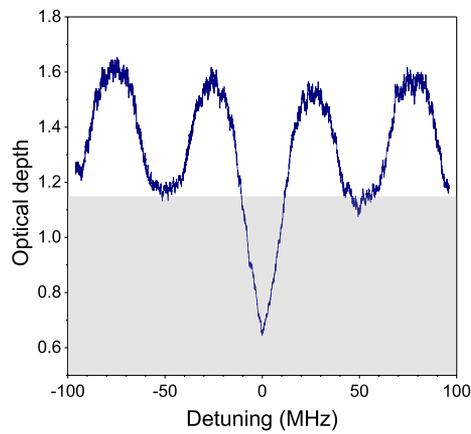


Fig. 3. Absorption profile of 200 MHz section of a 6.4 GHz wide AFC at $\lambda = 1532.05$ nm and $B = 3$ kG. The gray shaded area indicates remaining background absorption. The central dip is caused by unmodulated pump laser light.

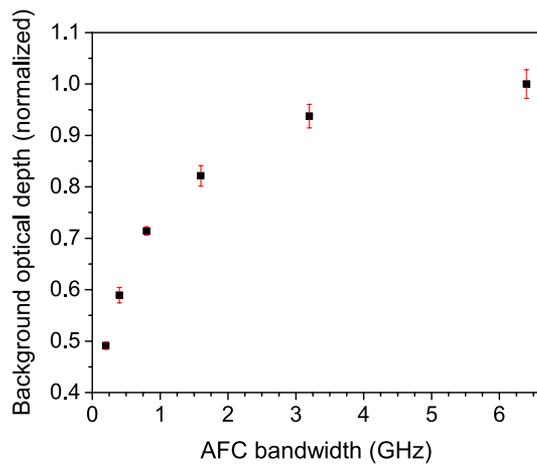


Fig. 4. Average background absorption as a function of AFC bandwidth.

section of a 6.4 GHz wide AFC. Note the significant absorption background, which exponentially reduces the storage efficiency of our AFCs compared to the case of no background [10]. The deep hole at zero detuning is due to optical pumping by unmodulated light leaking through the phase modulator. As shown in Fig. 4, we find that the background absorption, which is assessed at detunings between -100 and $+100$ MHz, increases when the bandwidth of the AFC increases.

C. Determining the Origin of the Background Absorption

1. Anti-Hole Broadening

One possible explanation for the bandwidth-dependent background absorption is that there is spectral overlap between broad anti-holes (caused by optical pumping) and the AFC. Provided the frequency difference between holes and anti-holes is larger than the anti-hole broadening, the spectral overlap—and hence the background absorption—increases as the AFC bandwidth

Table 1. Background Absorption for 200 MHz Wide AFCs and Varying Frequency Differences^a

AFC Detuning (GHz)	Background Absorption
0	0.66 ± 0.01
0.6	0.60 ± 0.01
1.0	0.73 ± 0.03
1.4	0.66 ± 0.02

^aThe case of a single AFC (zero detuning) is included for reference.

approaches the hole-to-anti-hole splitting. This is the case in $Er:LiNbO_3$, for which the Zeeman level splitting at 3 kG exceeds 50 GHz, and the anti-hole broadening at the same field is expected to be only around 5 GHz. However, the small AFC widths compared with the Zeeman splitting makes spectral overlap between AFCs and anti-holes unlikely.

To fully rule out AFC background absorption due to inhomogeneous broadening of ground-state levels (whether arising from Zeeman splitting or not), we generate, at an optical depth of 0.8 (with light propagating parallel to the c axis of the crystal), pairs of 200 MHz bandwidth AFCs with varying detunings between their center frequencies, up to 1.4 GHz. If the broadened anti-holes, created by the second AFC, indeed overlap with the first AFC, we expect to see an increase in background optical depth of the first AFC. This back-filling method is similar to the one used for characterization of the inhomogeneous broadening of Zeeman sub-levels in an Er-doped fiber [17]. In this case, two individual spectral holes (or trenches) with variable detunings were burnt, and filling of one trench by the inhomogeneously broadened anti-hole created by the second trench was assessed by measuring the optical depth of the first trench. Table 1 quantifies the background absorption of the first AFC at different detunings between the two AFCs. We find that measured values do not increase but rather scatter around a mean of around 0.66. This confirms that the anti-hole broadening indeed does not explain the observed increase in background shown in Fig. 4—at least not for AFC bandwidths up to around 1 GHz. Hence, another mechanism must be responsible, and we conjecture that it will also explain the background for large-bandwidth AFCs.

We note that the inhomogeneous broadening of the superhyperfine levels is too small at the applied magnetic fields to cause a constant absorption background [19], and their contribution to the observation in Fig. 4 can thus be ignored.

2. Instantaneous Spectral Diffusion

An alternative reason for the increase in background absorption with AFC bandwidth stems from the related increase in excited atoms during AFC preparation. (Even though the average laser power and pump-cycle duration, i.e., the total energy of the pumping light, remain constant, the number of excited atoms grows due to the nonlinear dependence of the absorption rate with the light power spectral density, which decreases with AFC bandwidth.) This may result in two undesired processes: instantaneous spectral diffusion (ISD) [33] (discussed below) and erbium spin flips [15] (discussed in the following sections).

ISD can be introduced by optical pumping, during which Er^{3+} ions are promoted to the excited state, leading to an uncontrollable shift in the transition energies of nearby Er^{3+} ions

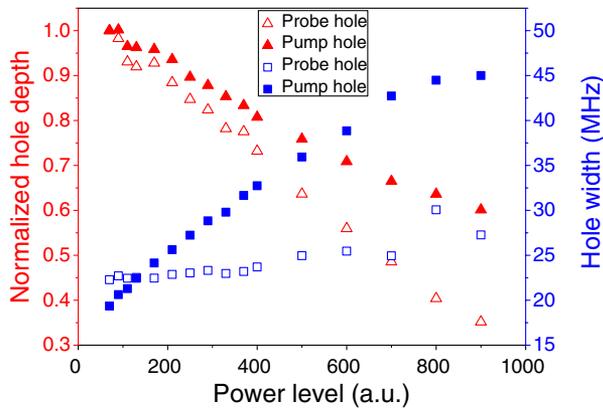


Fig. 5. Laser-excitation-induced change of a spectral hole. Widths and depths of the pump and probe holes are plotted as a function of excitation power (see text for details).

compared to their unperturbed values. The consequence of addressing the latter ions during subsequent hole burning is a smeared-out AFC with increased background. Indeed, as the cause for ISD—the presence of excited ions—will disappear at the end of the pumping sequence, transition frequencies will shift back to their unperturbed values, leading to a modification of the previously created absorption profile. ISD increases with the number of excited ions [33], which is consistent with the observed increase in the background absorption with bandwidth.

To characterize broadening and AFC background, which could potentially be due to ISD, we burn two 25 MHz wide spectral holes with 200 MHz central frequency difference. We vary the laser excitation power used to create one of the holes, which we refer to as the pump hole, while constant power is used to burn the other, which we refer to as the probe hole. The width of the pump hole is expected to increase due to power broadening [2], and ISD would manifest itself by simultaneous broadening and shallowing of the probe hole. We plot the widths and depths of the two holes as a function of optical excitation power used for the pump hole in Figs. 5(a) and 5(b), and find that the width of the probe hole increases by around 5 MHz. Additionally, we observe decrease in the depths of the pump and probe holes with increasing pump power [Fig. 5(b)]. Note that due to optical pumping, the reduction in the pump hole depth with increasing pump power is less than that of the probe hole, which decreases by a factor of three. The shallowing of the probe and pump holes is consistent with the increase in the background absorption of the AFCs with their bandwidths, as shown in Fig. 4. However, the level of probe hole broadening of only 5 MHz explains neither the large shallowing of the probe hole nor the increased background optical depth observed in AFCs with 50 MHz tooth spacing (although it will impact the quality of AFCs with small peak spacing, i.e., AFCs that allow for longer storage times).

We also estimate the effect of ISD from measurements of a 0.1% $\text{Er}^{3+}:\text{LiNbO}_3$ bulk crystal [28]. Assuming a maximum laser excitation power of ~ 0.5 mW, 0.2% Er^{3+} concentration, and an ISD coefficient of $\sim 2 \times 10^{-13}$ Hz \cdot cm³/excited ion, we predict the maximum spectral broadening to be on the order of kHz. This value is three orders of magnitude smaller than

the observed increase in the width of the probe hole in Fig. 5(a). Hence, our experimental results and our estimate suggest that ISD is the cause neither for the observed spectral broadening of the probe hole, nor for the remaining background absorption of the probe hole and the AFCs. In the next sections, we elaborate on two other power-dependent mechanisms that may cause these observations.

3. Spin Flip-Flops

Another process that could be affected by the increase in Er^{3+} excitation when creating AFCs of larger bandwidths is the number of spin flip-flops. In this case, spins in one ground-state sub-level (Zeeman shelving level) that are within the AFC bandwidth resonantly exchange state with other spins that are in the other ground-state sub-level and outside of the AFC bandwidth: one spin will be flipped up, the other flopped down. This leads to redistribution of the population within the AFC, and hence to background. However, as the spin flip-flop rate decreases with the sixth power of the distance between Er ions, we estimate its contribution to be small. Indeed, using Eq. 8 of [34], an approximate Er-doping concentration of 3.6×10^{19} cm⁻³ (or 0.2%), which corresponds to an average distance of 7.11 nm between erbium ions, and a spin inhomogeneous broadening of 5 GHz for an applied magnetic field of 3 kG, we find a flip-flop rate of 100 Hz—by far too little to explain the AFC background. We also estimated a frequency shift of around 1 MHz due to spin–spin interactions [35]. While significant, this value is not sufficient to explain the observed background absorption, since the width of the troughs in the AFCs is around 20 MHz.

4. TLSs and Non-Equilibrium Phonons

Another power-dependent mechanism that may be responsible for the increase in the width of the probe hole and the AFC background is that of light-induced TLS excitation, which can cause spin flips of erbium ions through TLS–spin coupling, and can induce optical linewidth broadening (frequency shifting), known as spectral diffusion. The former occurs when a TLS is resonant with the electronic spin transition of an erbium ion, and the latter happens when the electronic transition frequency of a nearby ion shifts through modification of the electric strain coupling between the TLS and the ion [22–25].

In support of this hypothesis, we note that congruent LiNbO_3 is known to contain various impurities and imperfections, and previous measurements of REI-doped LiNbO_3 suggest significant lattice disorder. Such disorder could be the origin of the above-described TLSs [29–32,36,37]. We also point out that laser-induced excitation and decay of TLS impurities determines photo-refraction in LiNbO_3 . It is well known that this effect is enhanced in waveguides compared to bulk crystals due to high confinement of the laser field and, consequently, greater light intensities. This is consistent with the fact that the emergence of an absorption background in AFCs due to spectral hole filling is not observed in bulk LiNbO_3 .

Another excitation-induced phenomenon is that of non-equilibrium phonons. As described in Ref. [26], “non-equilibrium phonons are generated directly by spontaneous decays from the pumped electronic state to ground-state

phonon modes by electron-phonon coupling.” Thus, depending on the Stark level structure and their splitting, non-equilibrium phonons can be generated through optical excitation. This can cause line shifting and thereby the hole filling (increasing background absorption) observed in Fig. 4.

D. Discussion and Conclusion

We experimentally study ground-state Zeeman sub-levels of Er^{3+} ions doped into a $\text{Ti}^{4+}:\text{LiNbO}_3$ crystalline waveguide as shelving levels for AFC-type quantum memory for light. Despite promising lifetimes in excess of a second, several changes are required to increase the storage efficiency for telecommunication-wavelength photons beyond the current state of the art of around 1%. Most importantly, the memory efficiency, which is limited by the available optical depth (at most two in our waveguide) and the absorption background need to be improved. The former can be addressed using an impedance-matched cavity [38], and the absorption background may be reduced through optimization of the optical pumping procedure. This includes the use of optimized optical excitation power, laser scan rate, and magnetic field strength and direction, which may result in longer-lived Zeeman levels and a favorable branching ratio into the shelving level. But ultimately, it seems necessary to improve the LiNbO_3 crystal itself, e.g., by varying growth conditions, to reduce the number of TLSs.

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