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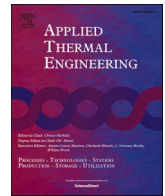
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# Modeling of a continuous physical vapor deposition process: Mass transfer limitations by evaporation rate and sonic choking

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## ABSTRACT

In recent years, Physical Vapor Deposition has been advanced to a continuous process which makes it amenable for in-line, high-quality and energy-efficient galvanization. To achieve the high and uniform mass flow required for in-line production, a Vapor Distribution Box is used, in which the zinc is evaporated. The zinc fills the Vapor Distribution Box at a relatively high pressure and leaves into the coating chamber via nozzles. A reliable modeling approach that can be used in the design and optimization of Vapor Distribution Boxes is as yet not available in the literature. The present paper analyses which phenomena play a major role and therefore have to be included in a simulation model of continuous Physical Vapor Deposition processes, and identifies process parameters which have a significant impact on deposition rate and uniformity.

To this end, a model for the flow and heat transfer is developed based on the numerical solution of the compressible Navier–Stokes–Fourier equations in combination with the Launder and Sharma low-Reynolds  $k-\epsilon$  turbulence model, using the open-source CFD-library OpenFOAM. To account for the vapor mass flow to be limited by both evaporation and sonic choking, a novel inlet boundary condition is proposed based on the Hertz-Knudsen condition. Results from the CFD model are compared to those of analytical models based on isentropic flow, the influence of various modeling parameters is evaluated against experiments, and sensitivity of the process to various process parameters studied.

The proposed numerical model predicts mass flow rates with a much better accuracy than analytical models previously proposed in the literature. The latter overpredict the mass flow rate by a factor of 2.1–2.5, whereas the proposed numerical model overpredicts only by a factor of 1.3. Next to the novel Hertz-Knudsen boundary condition, the inclusion of viscous effects is found to be crucial to achieve this improvement, since viscous effects – especially in the boundary layer inside the nozzles – severely reduce the mass flow. The numerical model is shown to be only weakly sensitive to uncertainties in the evaporation coefficients and metal vapor viscosity. For the device studied, the mass flow discharge efficiency was found to be relatively low ( $\approx 40\%$ ). To increase this efficiency, viscous losses in the nozzle boundary layers have to be reduced, for instance by employing shorter or a bigger radius nozzles (possibly impairing nozzle-to-nozzle uniformity) or by employing a higher melt temperature and vapor pressure.

## 1. Introduction

Physical Vapor Deposition (PVD) is a coating technique commonly used in the automotive [1–3], turbomachinery [4,5], textile [6], electronic [7] and solar energy industries [8,9]. The manufactured coatings may improve structural and optical properties [10], act as thermal

barriers [11] or protect steel from corrosion [12,13]. In the last two decades, PVD was adapted to coat steel in a continuous process [14–16]. Its advantage over commonly used hot-dip galvanization [17,18] and electro-galvanization processes [19] is that the heat impact which can change the steels structure is much lower [20]. In continuous PVD units, not only traditional zinc coatings can be applied, but also alloys such as zinc-magnesium-based coatings which provide a better protection

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**Nomenclature****Greek Symbols**

|            |                                |                                 |
|------------|--------------------------------|---------------------------------|
| $\alpha$   | Thermal conductivity           | $\text{kg m}^{-1}\text{s}^{-1}$ |
| $\alpha_t$ | Turbulent thermal conductivity | $\text{kg m}^{-1}\text{s}^{-1}$ |
| $\gamma$   | Specific heat ratio            | –                               |
| $\mu$      | Dynamic viscosity              | $\text{kg m}^{-1}\text{s}^{-1}$ |
| $\nu$      | Kinematic viscosity            | $\text{m}^2\text{s}^{-1}$       |
| $\nu_t$    | Turbulent viscosity            | $\text{m}^2\text{s}^{-1}$       |
| $\psi_T$   | Isothermal compressibility     | $\text{J kg}^{-1}\text{K}^{-1}$ |
| $\rho$     | Density                        | $\text{kg m}^{-3}$              |

**Roman Symbols**

|              |                                    |                                 |
|--------------|------------------------------------|---------------------------------|
| $\dot{m}$    | mass flow rate                     | $\text{kg s}^{-1}$              |
| $\mathbf{u}$ | Velocity                           | $\text{m s}^{-1}$               |
| $A$          | Surface area                       | $\text{m}^2$                    |
| $a$          | Speed of sound                     | $\text{m s}^{-1}$               |
| $c_p$        | Specific heat at constant pressure | $\text{J kg}^{-1}\text{K}^{-1}$ |
| $c_v$        | Specific heat at constant volume   | $\text{J kg}^{-1}\text{K}^{-1}$ |
| $C_{dis}$    | Discharge coefficient              | –                               |
| $e$          | Internal energy                    | $\text{J kg}^{-1}$              |
| $f$          | Evaporation coefficient            | –                               |
| $k$          | Kinetic turbulent energy           | $\text{J kg}^{-1}$              |
| $k_e$        | Kinetic energy                     | $\text{J kg}^{-1}$              |
| $M$          | Molar mass                         | $\text{kg mol}^{-1}$            |
| $p$          | Pressure                           | Pa                              |

|     |                        |                                      |
|-----|------------------------|--------------------------------------|
| $R$ | Universal gas constant | $8.314 \text{ J K}^{-1} \text{ mol}$ |
| $t$ | Time                   | s                                    |

**Superscripts**

|   |                              |
|---|------------------------------|
| * | Quantity in critical section |
|---|------------------------------|

**Subscripts**

|      |                                   |
|------|-----------------------------------|
| 0    | Quantity at stagnation conditions |
| $g$  | Gas                               |
| $HK$ | Hertz-Knudsen relation            |
| $in$ | Inlet                             |
| $is$ | isentropic relation               |
| $m$  | Melt                              |
| $n$  | Nozzles                           |
| $S$  | Sutherland law                    |
| $s$  | Static quantity                   |
| $t$  | Total quantity                    |
| $v$  | Vapor                             |
| VDB  | Vapor Distribution Box            |

**Dimensionless Numbers**

|                                 |                          |   |
|---------------------------------|--------------------------|---|
| $Br$                            | Brinkmann number         | – |
| $Ma = \frac{u}{a}$              | Mach number              | – |
| $Pr = \frac{\nu}{\alpha}$       | Prandtl number           | – |
| $Pr_t = \frac{\nu_t}{\alpha_t}$ | Turbulent Prandtl number | – |

against corrosion [21–25]. However, a reliable modeling approach that can be used in the design and optimization of continuous PVD units is as yet not available in the literature.

Traditional PVD processes are operated in batch mode and use physical means such as electro-beams or sputtering to evaporate coating material in a vacuum. The spreading atoms (or molecules) deposit on any object placed inside the chamber – including the chamber walls which consequently require regular cleaning. As a result, this diffuse distribution involves regular shut-downs of the PVD station, which is not feasible for a continuous production line. Furthermore, the evaporation rates reached by electro-beams and sputtering are quite low. A high mass flow directed towards the coating surface is necessary to integrate PVD in a strip production line. To achieve this, a continuous process was proposed in recent years [26]: The coating material, here zinc, is heated in a crucible and evaporates. The zinc vapor fills a Vapor Distribution Box (VDB), which is connected to the coating chamber via several small nozzles. Due to the high pressure ratio between the VDB and the coating chamber, which is under moderate vacuum, the vapor is drawn through the nozzles into the coating chamber. The zinc spreads into the vacuum at supersonic speed and eventually deposits onto the steel strip.

To the authors' knowledge, companies in South Korea, Belgium and the Netherlands are working on continuous PVD devices, but details are mostly not disclosed yet. A modification to the described setup was proposed by Banaszak et al. [27] who designed a VDB equipment with a longitudinal slot instead of nozzles and with a filter in front of the slot, which homogenizes flow speed and temperature before the vapor enters into the vacuum chamber. They also suggested using an induction heated filter consisting of a conductive material to avoid condensation. Zoestbergen et al. [15] heated the VDB wall to avoid condensation. While these measures are reasonable, the filter may hinder the flow and any heating inside the VDB decreases the metal vapor density which both lead to a decreased discharge.

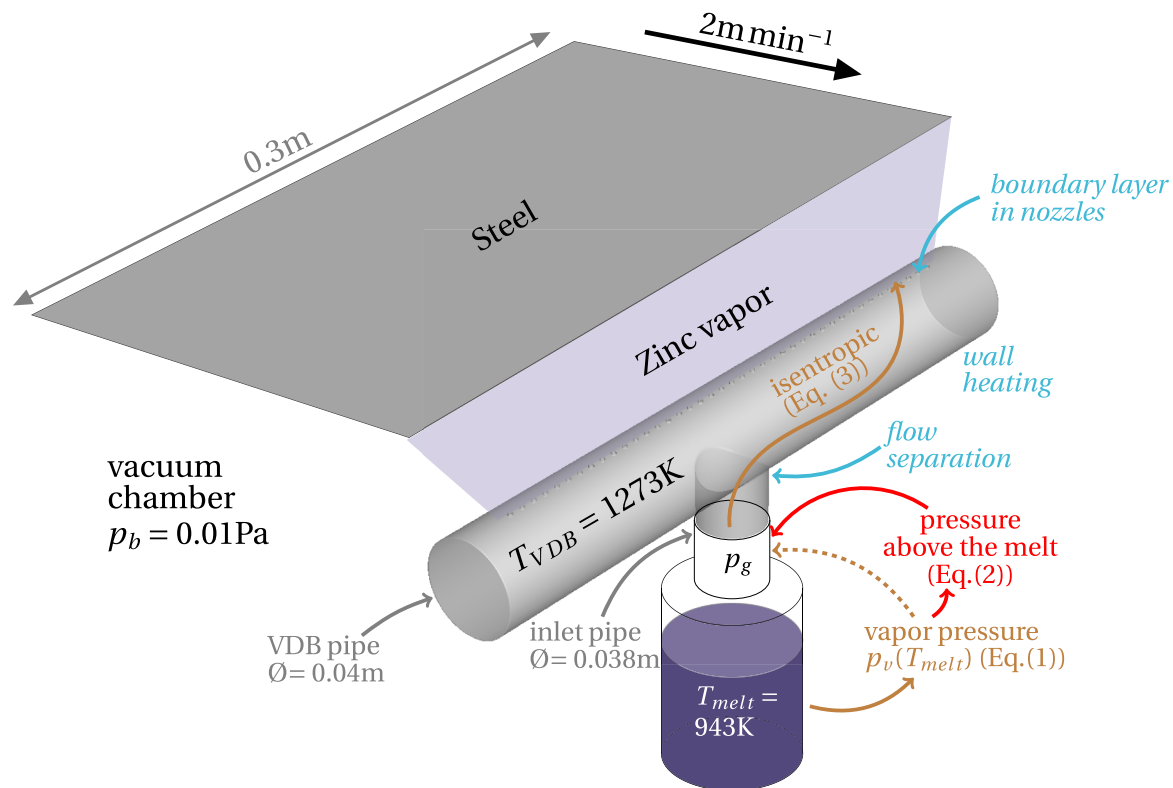
While multiple shortcomings (e.g., stray deposition of coating material in the coating chamber and condensation at high mass flow rates) are yet to be remedied, this paper focuses on optimizing the process conditions to meet the most crucial requirement for continuous

production: to obtain the required coating thickness within given tolerances at the typical speed of production lines, the mass flow has to be both high and uniform.

It is a major challenge to assess the effects of changes in design and process conditions. Measurements in high-temperature vacuum systems are difficult to perform and even simple geometry changes are costly. Theoretical predictions are complicated because the thermodynamic processes involved are highly non-linear and interwoven. Numerical simulation methods, e.g., continuum Computational Fluid Dynamics (CFD) or rarefied gas simulation techniques such as Direct Simulation Monte Carlo (DSMC), enable us to shed some light on the processes involved, as it allows to account for and distinguish between the influence of non-ideal and non-linear phenomena.

The deposition rate and uniformity of batch PVD processes have been studied by using continuum CFD [28–31] or DSMC [32–37]. Some studies also compared both methods [38–40]. Schmitz [14] developed a theoretical model for a continuous PVD process, in which he estimated the mass transfer from the VDB to the coated surface on the basis of isentropic and empirical relations. He approximated the jet vapor deposition process through a slot opening by splitting the flow into two parts: first, a continuum flow inside the VDB; second, a collisionless expansion outside the vacuum chamber. In the first part, he assumed a perfect, adiabatic gas flow with friction losses at the slot entrance and exit. Numerical simulation of a continuous PVD setup has so far been reported only as a subsidiary support of experiments [26,27] to show the uniform velocity profile in a choking nozzle, but studies did not address the discharge efficiency or consider the limitation to the evaporation rate at the melt surface. The mass flow rate can be estimated by coupling the Hertz-Knudsen relation for evaporation with the isentropic relations for compressible flow, assuming choking in the nozzles. This estimate does not account for viscous effects. A reliable mass flow prediction to assess process modifications and optimize the process is missing.

A comprehensive numerical model of a continuous PVD process has to deal with various phenomena that complicate numerical simulations, such as evaporation at the melt surface, the rapid increase in the Mach number of the vapor flow ranging from incompressible to compressible



**Fig. 1.** Sketch of Physical Vapor Deposition process. The simulated part of the Vapor Distribution Box is in gray. Brown denotes the modeling based on the Antoine vapor-pressure-equation and the isentropic relation, red the limitation of inlet pressure by the Hertz-Knudsen-equation, *italic cyan* the non-isentropic effects which require numerical modeling. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

supersonic flow, the high pressure ratio between the VDB and the vacuum chamber (up to  $\mathcal{O}(10^6)$ ) and the unknown thermodynamic, evaporation and transport properties of metal vapors. Furthermore, such a model has to account for multiple viscous phenomena, i.e., (i) viscous dissipation including heat generation [41], (ii) Fanno [42] and (iii) Rayleigh flow [43]. All of these phenomena may affect the discharge: (i) The dramatic velocity changes from zero-slip at the wall to supersonic velocity in the core result in high viscous dissipation, decreasing the pressure and possibly generating heat; (ii) in compressible subsonic flow, the pressure drop lowers the density and subsequently increases the velocity, whereas in supersonic flow, the pressure drop increases the density and decreases the velocity. The stagnation pressure and hence the mass flow decrease; (iii) The heating of the nozzles itself may give rise to a Rayleigh effect in the boundary layer which decreases the stagnation pressure and thus also the mass flow. It is unknown in the literature, and difficult to estimate a priori which of these phenomena significantly affect the flow and which can be neglected.

The present paper proposes important steps towards the development of such a model. To the authors' knowledge, it represents the first report on the development and assessment of a physically comprehensive numerical simulation model for continuous PVD coating processes that is validated against experimental data in an industrial setting. Various aspects of the numerical model discussed in this paper may not only benefit the emerging continuous Physical Vapor Deposition, but also other vacuum and turbomachinery technologies.

The present paper has two objectives: First, to evaluate which phenomena play a major role in the continuous PVD deposition process and have to be included in a numerical PVD model in order to capture all relevant physics. Second, to identify process modifications which have a significant impact on deposition rate and uniformity.

Gas flow and heat transfer in a pilot continuous PVD unit are modeled using the open-source CFD-library OpenFOAM [44]. To couple the limitation by the evaporation rate at the melt and the limitation the

choking inside the nozzles, a novel boundary condition is implemented based on the Hertz-Knudsen equation and the isentropic relation. The numerical simulation results are validated with experimental results. First, the experimental pilot case setup is described, the thermodynamics involved is summarized and the isentropic expressions are listed which are required to estimate the mass flow rate. Then, the numerical methods are presented with a focus on the boundary condition that we implemented to capture the evaporation process correctly. Subsequently, the numerical method is verified and validated. In the results section, we present the flow field, mass flow rate and viscous losses. Finally, the results section discusses the applicability of isentropic equations to estimate the mass flow rate, the significance of the above-mentioned viscous phenomena and parameter uncertainties for numerical mass flow rate modeling and possible design improvements for a higher discharge efficiency.

## 2. Experiment

The studied equipment, its dimensions and the known process conditions are summarized in Fig. 1. Zinc is heated up in a crucible enclosed by induction coils to melt temperatures between 903K – 943K. The zinc vapor flows from the melt surface via an inlet pipe into the VDB, where a relatively high pressure builds up. The vapor leaves the VDB via 41 nozzles with a diameter of 2mm and a length of 9.5mm (nozzle-axis-to-nozzle-axis distance 6mm). In the nozzles, the vapor is rapidly accelerated due to the large pressure difference between the VDB and the vacuum chamber (which is held at a background pressure  $p_b = 0.01\text{Pa}$ ). Subsequently, the flow chokes (i.e., it is limited to Mach numbers around one) at the nozzle outlet. Rarefied metal vapor jets emerge from the nozzles directed towards the moving steel strip, where the vapor solidifies upon impingement. The steel strip has a width  $l = 0.3\text{m}$  and moves at a speed of  $2\text{ m min}^{-1}$  (the speed of real line production is about 50 times higher). To avoid recondensation in the process, the wall of the

**Table 1**  
Specifications and sensitivities of used devices.

| Device                             | Specification                                 | Sensitivity |
|------------------------------------|-----------------------------------------------|-------------|
| Thermocouple                       | Mantel Thermocouple type K                    | 5K          |
| Vacuum pump                        | Pfeiffer Duo 125, oil diffusion, WKP<br>500 A | -           |
| Eddy current thickness measurement | Fischer Phascope PMP10                        | 0.5μm       |

**Table 2**  
Antoine equation coefficients for Zinc [45].

| A [K] | B     | C       | D [K <sup>-1</sup> ] | Temperature range in K |
|-------|-------|---------|----------------------|------------------------|
| 6883  | 9.418 | -0.0503 | -0.33                | 473–692.5              |
| 6670  | 12.00 | -1.126  | -                    | 692.5–1000             |

VDB is kept at a temperature of about 1273K by multiple resistance heating wires. Three thermocouples are placed to monitor the process: at the bottom of the crucible, in its center, and above the melt in the vapor. The coating thickness was measured using an eddy current device. The specifications and sensitivities of the devices are listed in Table 1. For each melt temperature  $T = 903\text{K}, 923\text{K}, 943\text{K}$ , two separate runs were conducted. The mass flow was determined by weighing the crucible before and after the run. A stray deposition rate between 8% and 11% was derived from mass flow rate and deposited film thickness.

### 3. Model

#### 3.1. Isentropic Approximation

Fig. 1 describes the thermodynamic relations and phenomena determining the flow. Neglecting all non-isentropic effects — such as flow separation, wall heating, viscous boundary layers — the mass flow rate can be estimated depending only on the melt temperature which is one of the few process conditions known from the experiment. Such an estimate is reasonable, (i) if the flow stays attached to the walls, which depends on geometry and Reynolds number, (ii) if the wall heat flux is not big enough to considerably heat the flow, and (iii) if the boundary layers are small compared with the bulk flow region. But even if this is not the case, an isentropic estimate is the best prediction available without a numerical simulation. In this section, we develop an ideal theoretical model assuming isentropic conditions. In addition, we assume that the pressure in the VDB is uniform, the gas inside the VDB is at stagnation conditions (i.e., the velocity is negligible) and the flow at the nozzle outlet is choked (i.e.,  $Ma = 1$ ) across the entire outlet cross section. All pressures used in this section are total pressures (i.e., static and dynamic pressure) and thus account for the flow dynamics. Fig. 1 shows the steps required for such a modeling. First, the saturation vapor pressure  $p_v$  has to be determined using the empirical Antoine equation which describes the pressure–temperature relation along the vapor-pressure curve as

$$\log_{10} \left( \frac{p_v(T_m)}{133.32} \right) = -\frac{A}{T_m} + B + C \log_{10} T_m + 10^{-3} D T_m, \quad (1)$$

where  $T_m$  is the melt temperature in K; the coefficients for zinc are listed in Table 2.

In a first estimate it is assumed that the gas pressure  $p_g$  inside the VDB is the same as the saturated vapor pressure  $p_v$ . Isentropic relations can then be used to determine the mass flow rate as [43]

$$\dot{m}_{is}^* = p_g \sqrt{\frac{\gamma M}{RT_g}} A_n^* \left( \frac{\gamma+1}{2} \right)^{-\frac{1}{2\gamma-1}}, \quad (2)$$

where  $A_n^*$  is the critical or sonic cross section of the nozzles (i.e., the

outlet area where  $Ma = 1$ ). As we neglect the subsonic viscous boundary layer, the sonic section corresponds to the total cross section  $A_n^* = A_n$ .

However, as the evaporation does not occur in a closed system, the actual gas pressure in the VDB adapts to a lower value than the vapor pressure used in Eq. (2). The actual vapor pressure  $p_g$  in the VDB determines both the mass flux evaporated from the melt and the outflow mass flux at the nozzles. The actual evaporation rate is proportional to the difference between the vapor pressure and the gas pressure  $p_g$  above the melt and is given by the Hertz-Knudsen equation [46,47]

$$\dot{m}_{HK} = f A_m (p_v(T_m) - p_g) \sqrt{\frac{M}{2\pi RT}}, \quad (3)$$

where  $A_m$  denotes the melt surface area and the evaporation coefficient is often assumed to be  $f = 1$ . However, multiple studies report values around  $f = 0.82$  for metal melts [48–50] and the mean value derived from zinc evaporation experiments conducted by Clair and Spendlove [51] was  $f = 0.75$  when neglecting negative value outliers, or  $f = 0.58$  when neglecting both negative values and values above unity.

By balancing the two mass flow rates from Eqs. (3) and (2), we obtain the actual value for  $p_g$  and from this the mass flow rate limited by the Hertz-Knudsen condition

$$\dot{m} = \frac{f A_m \sqrt{\frac{M}{2\pi RT}} p_v(T_m)}{1 + \frac{f A_m}{A_n} \sqrt{\frac{1}{2\pi \gamma}} \left( \frac{\gamma+1}{2} \right)^{\frac{1}{2\gamma-1}}}. \quad (4)$$

For numerical modeling (as described in the next section) it is useful to rewrite this equation in a form which has the mass flow rate on both sides of the equation

$$\dot{m} = \left[ p_v(T_m) - \underbrace{\frac{\dot{m}}{f A_m} \sqrt{\frac{2\pi RT}{M}}}_{\text{limitation by HK}} \right] \cdot \sqrt{\frac{\gamma M}{RT_g}} A_n \left( \frac{\gamma+1}{2} \right)^{-\frac{1}{2\gamma-1}}. \quad (5)$$

While the mass flow rate can be calculated explicitly from Eq. (4), Eq. (5) clearly illustrates the limitation of the mass flow rate due to the Hertz-Knudsen equation which shows that the gas pressure in the VDB is not equal to the vapor pressure, but rather reduced by the mass flow leaving the VDB, which in a steady system is the same as the evaporated mass flow. The higher the mass flux (e.g., due to a high outlet area  $A_n$ ), the higher the limitation. High availability of the evaporated metal (e.g., due to a high melt area  $A_m$  or a high evaporation coefficient  $f$ ) reduces the limitation.

In compressible flows through heated ducts, such as in the VDB nozzles, Rayleigh flow may occur which means that adding heat to the flow lowers the stagnation pressure [43]. Wall heating increases the thickness of the subsonic boundary layer and thus reduces the performance and mass flow rate of the nozzle. For a perfect one-dimensional flow this would reduce the stagnation pressure in the critical section, which would further decrease the mass flow rate to

$$\dot{m}_{\text{Rayleigh, HK}} = \frac{1}{\gamma+1} \left( \frac{\gamma+1}{2} \right)^{\frac{\gamma}{\gamma-1}} \dot{m} \quad (6)$$

and produce a discharge of  $\dot{m}_{\text{Rayleigh, HK}} = 0.77 \dot{m}$  for monatomic gases (for which  $\gamma = 5/3$ ). In the process under consideration, the Rayleigh effect is expected to be considerably lower, as the heating only occurs at the nozzle walls and the nozzles are not long enough to allow heat conduction to the core.

### 3.2. Numerical Modeling

#### 3.2.1. Governing Equations

The compressible Navier–Stokes–Fourier equations describe the flow by the conservation of mass, momentum and energy

$$\frac{\partial \rho}{\partial t} + \frac{\partial(\rho u_i)}{\partial x_i} = 0, \quad (7)$$

$$\frac{\partial(\rho u_i)}{\partial t} + \frac{\partial(\rho u_i u_j)}{\partial x_j} = -\frac{\partial p}{\partial x_i} + \frac{\partial}{\partial x_j} \left[ \underbrace{\left( \mu + \mu_t \right) \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} - \frac{2}{3} \frac{\partial u_k}{\partial x_k} \delta_{ij} \right)}_{=\tau_{ij}} \right],$$

$$\frac{\partial(\rho e)}{\partial t} + \frac{\partial(\rho u_j e)}{\partial x_j} + \frac{\partial(\rho k_e)}{\partial t} + \frac{\partial(\rho u_j k_e)}{\partial x_j} = -\frac{\partial(\rho u_i)}{\partial x_j} + \frac{\partial}{\partial x_j} \left[ \left( \alpha + \frac{\mu_t}{Pr_t} \right) \frac{\partial e}{\partial x_j} \right] + \frac{\partial(\tau_{ij} u_i)}{\partial x_j}, \quad (8)$$

where  $e$  is the internal energy and  $k_e = \frac{1}{2} u_i u_i$  is the kinetic energy. Viscous effects dissipate momentum and generate heat. As the Brinkman number (i.e., the dimensionless ratio between heat generated by viscous dissipation and heat conducted away by thermal diffusion) was  $Br = \mathcal{O}(1)$  in the nozzles, one simulation was run including heat generation due to viscous dissipation, which is the last term in the energy equation (Eq. (8)). However, the effect on temperature and the mass flow was negligible as the affected region was rather small. The difference in total mass flow rate was 0.3%. Therefore, heat generation by viscous dissipation was neglected in the simulations presented here. Modeling of compressible flows in similar geometries revealed that it may be important to consider turbulent losses as well [52]. After initial laminar simulations, Reynolds number calculations indicated that turbulence may have an effect on the flow field. The Reynolds number based on local velocity, local viscosity and VDB pipe diameter was  $Re = 2000\text{--}4000$  in wide regions of the inlet pipe and in the VDB pipe. Consequently, an eddy viscosity model was added. For further simulations, the turbulent viscosity  $\mu_t$  was modeled by the Launder and Sharma low-Reynolds  $k\text{--}\epsilon$  model [53] with a compression term based on rapid distortion theory (RDT) [54] (for brevity the turbulence model and corresponding boundary conditions are summarized in Appendix A.1). The turbulent Prandtl number was chosen as  $Pr_t = 1$ . Spontaneous nucleation and condensation may occur in the nozzle due to swift thermodynamic changes [55,56] and was reported for continuous PVD processes especially for high pressures inside the VDB [27,15]. Inspection of the regions of saturation (i.e., where  $p > p_v(T)$ ) revealed, that supersaturation is reached inside the nozzles only and not to an extent which makes spontaneous nucleation probable [57]. Nor was condensation observed in the experiments which were run at moderate vapor pressures.

#### 3.2.2. Numerical Solver

A pressure-based compressible solver in the open-source library OpenFOAM ®-v1806 (i.e., *sonicFoam*) is used to solve the governing equations [58]. For a description of a similar solver, the reader is referred to [59]. Our verification and validation of the solver can be found in Appendices B.1 and B.2. This solver is suitable in the transonic regime which is central to the flow we studied. Its limitations in supersonic flows, e.g., regarding exact shock location prediction and adiabatic expansion treatment, are not relevant for the flow region under consideration (i.e., inside the VDB). As the flow at the nozzle outlet is supersonic (except for a small subsonic region in the boundary layer), the flow inside the VDB is not affected by the flow in the vacuum chamber. The Navier–Stokes–Fourier and  $k\text{--}\epsilon$ -equations were discretized on a hexagonal mesh of 2.3 million cells in total and with 27 cells across the diameter of each nozzle. For a grid independence study we refer to Appendix B.3. The time integration was conducted using an implicit Euler scheme. The gradients were discretized by central differencing,

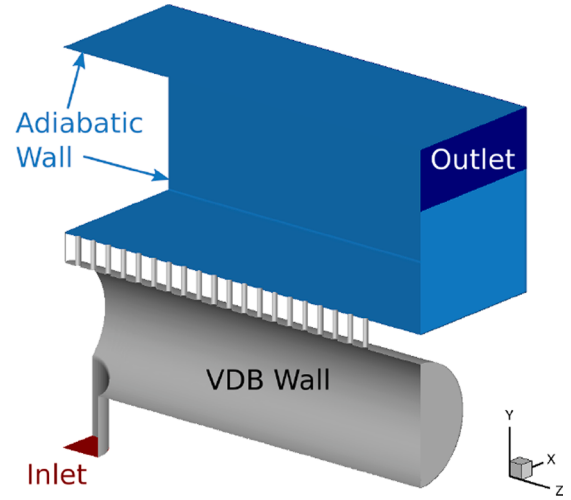


Fig. 2. Boundaries of computational domain. The outlet boundary extends around the entire domain.

Table 3

Boundary conditions.

| Boundary    | Pressure BC                                                       | Velocity BC                                                  | Temperature BC                                 |
|-------------|-------------------------------------------------------------------|--------------------------------------------------------------|------------------------------------------------|
| Inlet       | Total pressure or Hertz-Knudsen condition based on $p = p_v(T_m)$ | Zero normal gradient                                         | Total temperature based on $T_m = 943\text{K}$ |
| Outlet      | Wave transmissive $p_b = 0.01\text{Pa}$ at a distance of 0.01m    | Outlet: zero normal gradient inlet: zero velocity convective | Constant temperature $T_m$                     |
| Wall        | Zero normal gradient                                              | No slip                                                      | Wall temperature $T_w = 1273\text{K}$          |
| Outlet Wall | Zero normal gradient                                              | No slip                                                      | Zero normal gradient                           |

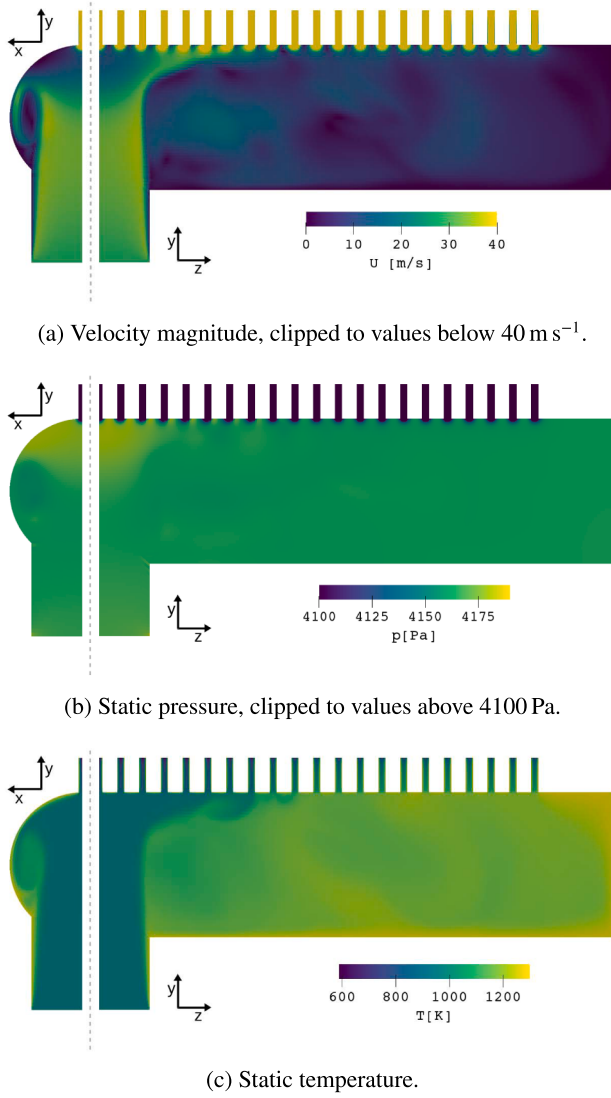
the fluxes were discretized by a second-order Total Variation Diminishing scheme (Sweby limiter [60]), only the  $k$  and  $\epsilon$  fluxes in the turbulence model were discretized by a first-order upwind scheme to stabilize the simulation (a second-order scheme would be preferable, but turbulence did not affect the flow significantly anyhow). The allowable maximum final residuals for the linear algebra solvers were set to  $10^{-10}$  for pressure, turbulent kinetic energy and turbulent dissipation and  $10^{-8}$  for velocity and energy. The mass flow rates at inlet and outlet were monitored; a solution was considered converged when the relative deviation of the two mass flow rates was below 0.5% (and no oscillations over time were observed).

#### 3.2.3. Closure of Thermophysical Properties

Since only the viscosity for alkali metal vapors has been reported in the literature, other metal vapor viscosities have to be approximated. We used the inverse-power-law-based method described by Fan et al. [37] first to estimate the collisional variable-hard-sphere diameter to be  $\sigma_{VHS} = 5.684 \cdot 10^{-10}\text{m}$  at a reference temperature of  $T_{ref,VHS} = 2000\text{K}$ , and then we applied the inverse power law to derive the temperature-dependent viscosity which we fitted with the Sutherland equation

$$\mu(T) = \frac{A_S \sqrt{T}}{1 + T_S/T}, \quad (9)$$

which gives  $A_S = 1.008 \cdot 10^{-6}\text{Pas}/\sqrt{\text{K}}$  at a reference temperature  $T_S = 400.9\text{K}$ . As temperature and pressure are far below the critical point, the ideal gas equation of state can be considered. The molecular weight of zinc is  $M = 65.38\text{g mol}^{-1}$ , the specific heat at constant pressure  $C_p = 317.901\text{JK}^{-1}\text{kg}^{-1}$  and the Prandtl number  $Pr = 0.7$ .



**Fig. 3.** Contours of the instantaneous velocity magnitude, pressure and temperature in the short and long cross section. Both the velocity magnitude and pressure are clipped to better visualize changes within the VDB.

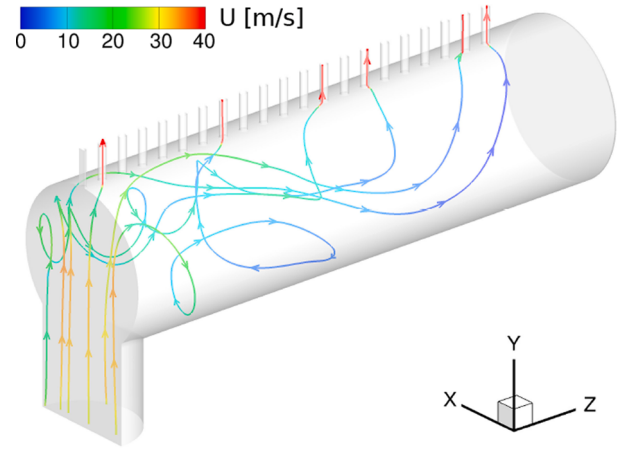
### 3.2.4. Boundary Conditions

The simulated domain and its boundaries are depicted in Fig. 2, the boundary conditions applied are listed in Table 3. Based on the existing total pressure boundary condition in OpenFOAM [44], we implemented a Hertz-Knudsen pressure inlet boundary condition to obtain the correct mass flow. The total pressure  $p_t$  above the melt is limited by the maximum evaporation rate described by the Hertz-Knudsen equation (see Eq. (3)), where we set  $\frac{\dot{m}}{fA_m} = \rho|U|$  and  $p_t = p_g$  to obtain

$$p_t = p_v \left( T_m \right) - \frac{\rho|U|}{f} \sqrt{\frac{2\pi RT}{M}}, \quad (10)$$

where the temperature in the second term is the static gas temperature at the inlet, which for the sake of simplicity was equated with the melt temperature (as in our simulations the gas temperature deviated less than 2 K from the melt temperature).

Furthermore, the computational domain does not start directly at the melt surface, but further downstream to reduce computational cost. The gap is bridged by assuming an isentropic acceleration of flow. Since it is in the incompressible flow regime (i.e.,  $Ma < 0.3$ ), the local static pressure  $p_{s,in}$  evaluates depending on the calculated local inlet velocity  $U$



**Fig. 4.** Streamlines colored by velocity magnitude, where values above 40  $\text{ms}^{-1}$  are clipped. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

as

$$p_{s,in} = p_t - \frac{1}{2} \rho |U|^2. \quad (11)$$

The isentropic total temperature inlet condition is given by

$$T_{s,in} = \frac{T_t}{1 + \frac{\gamma-1}{2} \psi_T |U|^2}, \quad (12)$$

where  $\psi_T = \left( \frac{\partial \rho}{\partial p} \right)_T$  is the isothermal compressibility. The pressure boundary condition which is limited by both the Hertz-Knudsen relation and the isentropic relation was implemented in OpenFOAM.<sup>1</sup> At the outlet, a wave-transmissive pressure boundary condition was used to avoid numerically reflected shocks in front of the boundary [61].

## 4. Results and Discussion

### 4.1. Flow Field Inside the VDB

Fig. 3 shows the contours of the simulated velocity, pressure and temperature fields in the short and long cross-sections of the VDB. The values are clipped to best visualize the VDB part so that the drastic changes inside the nozzles are not captured (which will be discussed in Section 4.3.4). The case shown applies to a melt temperature of 943K and a wall temperature of 1273K. In the simulation, a total pressure inlet boundary condition was used and the turbulence was modeled by means of the Launder and Sharma RDT-low-Reynolds  $k-\epsilon$  model (if not mentioned otherwise, the Results section refers to this case). The velocity at the inlet adjusts to approximately  $28 \text{ms}^{-1}$  (Fig. 3a). At the wall of the inlet pipe, a boundary layer develops, while the core flow accelerates. After the flow has entered the main part of the VDB, a shear layer forms between the jet and the surrounding vapor. On impinging onto the VDB wall, the flow stagnates, thus causing a local pressure rise. A wall jet emerges from the stagnation zone which is visible above the 4th to 6th nozzles from the left. The average static pressure at the inlet patch rises to 4171 Pa (Fig. 3b). This value remains similar in the entire VDB except for the stagnation region, where it is slightly higher, and the nozzle inlets where it drops dramatically (the pressure contours are clipped to values above 4100 Pa). The vapor temperature in the inlet

<sup>1</sup> The implemented inlet pressure boundary condition is available at <https://gitlab.tudelft.nl/vesper/HKLbc>.

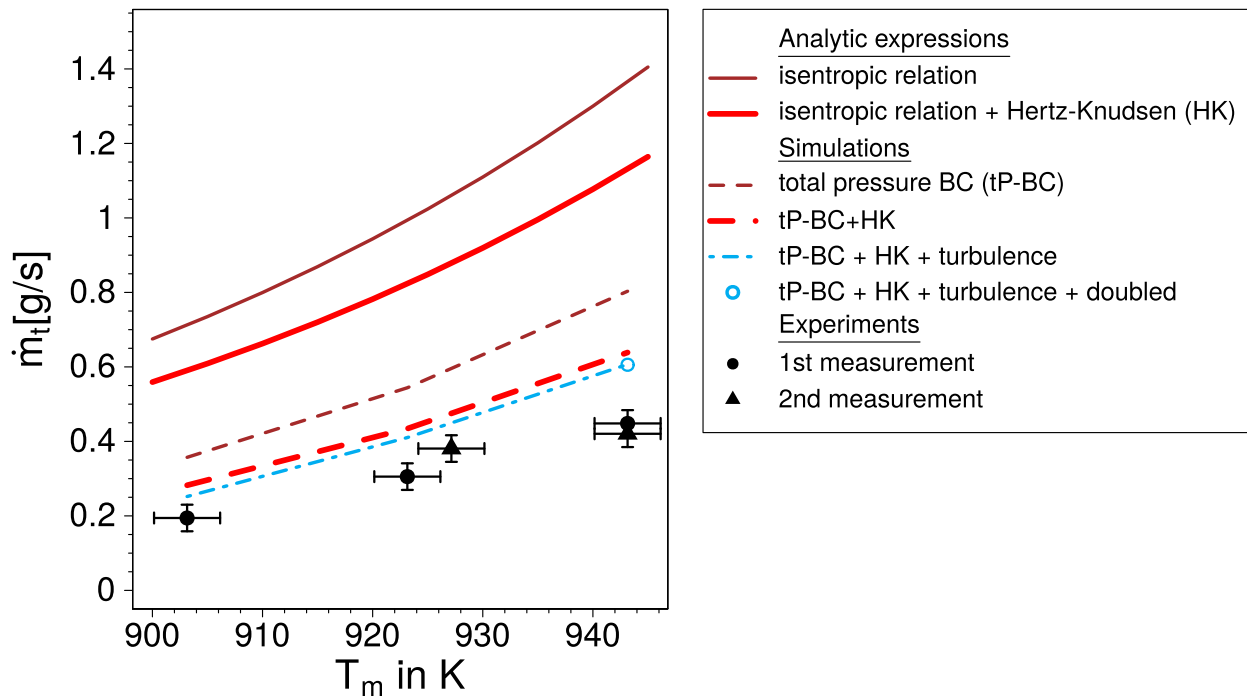


Fig. 5. Mass flow rate over melt temperature: solid lines analytic expression, dashed lines simulations, black points measurements.

pipe and the emerging jet is close to the melt temperature of 943K (Fig. 3c). A thin thermal boundary layer forms at the pipe walls. In the rest of the VDB pipe, wall heating and the slow swirling motion result in a uniform temperature rise to approximately 1100K. An additional insight in the flow dynamics can be gained from the streamlines shown in Fig. 4. While the streamlines are aligned with the wall in the inlet pipe, most of them swirl inside the VDB pipe at a lower speed, before accelerating rapidly when leaving via the nozzles (up to supersonic velocities).

## 4.2. Validation and Modeling

### 4.2.1. Total Mass Flow Rate

The total mass flow rate and the coating thickness over the strip width are known from the experiments and used for validating the model. Fig. 5 shows the mass flow rate as a function of the melt temperature. Both experimental runs are in good agreement with each other

and show an increase in mass flow rate at higher melt temperatures. The analytic isentropic relation (Eq. (2)) overpredicts the mass flow by a factor of 2.5–3, the relation limited by the Hertz-Knudsen equation (Eq. (3)) by a factor of 2.1–2.5. The simulation with the total pressure boundary condition overpredicts the mass flow by a factor of 1.8, while that limited by the Hertz-Knudsen equation overestimates by a factor of 1.4 and after adding a turbulence model by a factor of 1.3. It should be noted that simulating half the domain instead of one quarter does not affect the mass flow rate. We also checked for the influence of applying a real gas model which, however, had no effect as most of the gas is not near the vapor pressure curve. To check the sensitivity to a wrongly predicted metal vapor viscosity, we ran one simulation with a viscosity increased by 50% which reduced the mass flow by only 8%.

### 4.2.2. Influence of Evaporation Coefficient

As discussed above, considering the evaporation-limitation is crucial for modeling the discharge. Limiting the possible mass flow from the

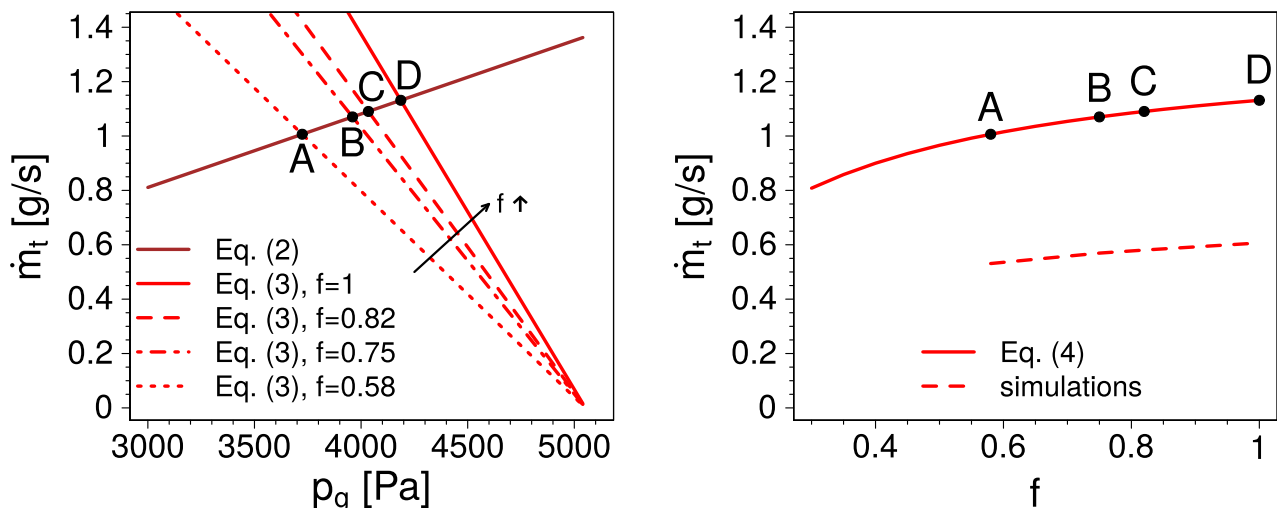
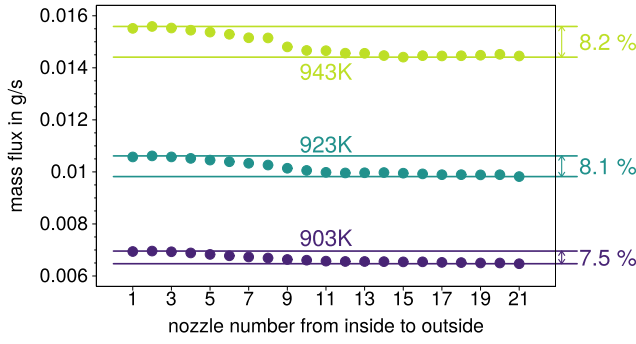


Fig. 6. Influence of the evaporation coefficient on the mass flow rate modeling.



**Fig. 7.** Mass flow rate per nozzle from simulations for different melt temperatures. The rate is given for the entire nozzle. The percentage on the right shows how much the maximum flow rate exceeds the minimum mass flow rate.

melt surface by the Hertz-Knudsen Equation (Eq. (3)), even when assuming an evaporation coefficient at the theoretical upper limit  $f = 1$ , results in a considerable ( $\approx 25\%$ ) drop in predicted mass flow rates. However, predicted mass flow rates are still 30–35% larger than experimental results. Assuming an evaporation coefficient  $f$  lower than 1 would further reduce the mass flow rate and could possibly explain the difference between experiments and simulations. In the literature, only few measurements of the evaporation coefficient were conducted for zinc [51] as well as for other metals [49,50,48]. The reported evaporation coefficients were in the range  $f \in [0.58 - 0.82]$ . We now discuss how the discharge depends on the evaporation coefficient. Before looking at the numerical results, we visualize in Fig. 6a, how the evaporation coefficient affects the slope of the Hertz-Knudsen equation (Eq. (3)) and its intersection with the isentropic relation (Eq. (2)). The intersection point is given by Eq. (4). For the range of reported values of  $f$ , a small change of the mass flow rate at the intersection point was found. Reducing the value of the evaporation coefficient from  $f = 1$  to the smallest reported experimental value  $f = 0.58$  reduces the mass flow rate by 12% only, thus still not explaining the 30–35% difference to our experimental data.

In Fig. 6b, the simulated mass flow rates are compared with those predicted by the theoretical relation (Eq. (4)). While the simulations produce a lower total mass flow rate, the relative dependence of the mass flow rate as a function of  $f$  is very similar in the simulations and in the theory. We may therefore use the theoretical curve to estimate the required reduction in  $f$  to reach a 35% reduction in the mass flow rate. suggests that the evaporation coefficient  $f$  would have to be as low as  $f = 0.33$  in order for the numerical simulations to predict mass flow rates in agreement with the experimental data. Such an  $f = 0.33$  value is much lower than reported experimental values. However, the experimental measurements of  $f$  were performed under process conditions ( $T_m = 730 - 810$  K and  $p_g = 6 - 266$  Pa) that strongly deviate from those in the current PVD experiments. Moreover, the reported experimental values are for pure uncontaminated zinc. In the current experiments, dross was found to accumulate at the melt surface during the heat-up of the equipment and the run of the experiments. To further clarify this issue, an experimental evaluation under actual PVD process conditions may be required for a better estimate of  $f$ .

#### 4.2.3. Uniformity of Mass Flow

Fig. 7 shows the mass flow per nozzle. When connecting this to the pressure contour (Fig. 3), it is apparent that the mass flow rate is higher for the stagnation zone with a high pressure and low temperature compared to the sides of the VDB, where the pressure is lower and the temperature is higher (thus decreasing the density). The deviation in mass flux for different nozzles is approximately 8% for all cases, which is roughly the coating thickness variation in the experiments of 8–10%. However, the latter is in the same range as the inaccuracy of the measurement device.

**Table 4**

Discharge coefficient  $C_{dis} = \frac{\dot{m}_{actual}}{\dot{m}_{theoretical}}$ , where the theoretical mass flow rate  $\dot{m}_{theoretical}$  is from Eq. (4).

| $T_m$         | 903K | 923K | 943K |
|---------------|------|------|------|
| $C_{dis,sim}$ | 0.43 | 0.50 | 0.54 |
| $C_{dis,exp}$ | 0.33 | 0.37 | 0.40 |

#### 4.3. Optimization of Process Conditions

##### 4.3.1. Isentropic Optimization

For weak evaporation (i.e., small mass fluxes from the melt surface), the second term of Eq. (5) is negligible and the mass flow rate is expected to vary proportionally to

$$\dot{m} \propto A_n \frac{p_t}{\sqrt{T_t}}, \quad (13)$$

where the total pressure  $p_t$  is approximately an exponential function of the melt temperature  $T_m$ , which is almost equal to the total temperature  $T_t$  at the VDB inlet. (It should be noted that while we used  $p_g$  and  $p_v$  to denote the total pressure at certain locations in Section 3.1, here, we use the total pressure  $p_t$  to distinguish from the static pressure  $p$  which is required for the discussion of the flow dynamics as the dynamic pressure has to be taken into account.) Consequently, a higher melt temperature increases the term  $\frac{p_t}{\sqrt{T_t}}$ . Considering only this isentropic approximation, this leaves two options to increase the mass flow rate, a bigger critical nozzle outlet area  $A_n$  or a higher melt temperature  $T_m$ . However, both experiments and simulations show a much lower mass flow rate than the isentropic prediction. In the following subsection, we quantify the discharge efficiency and determine where the non-isentropic losses occur; we then describe the influence of the wall temperature and finally, explain why the discharge coefficient increases with the melt temperature.

##### 4.3.2. Non-Isentropic Losses

The discharge coefficient of the VDB, i.e. the ratio of the actual (experimental or simulated) discharge  $\dot{m}_{actual}$  to the theoretical discharge  $\dot{m}_{theoretical}$  (calculated by Eq. (5))

$$C_{dis} = \frac{\dot{m}_{actual}}{\dot{m}_{theoretical}},$$

is listed in Table 4. For higher melt temperatures, the discharge coefficients increase for both the simulations and the experiments indicating a decline of non-isentropic effects. The total isentropic pressure  $p_t$ , which is the driving force, drops in the real process due to viscous and non-adiabatic losses, such as flow separation, turbulence or heating. This directly reduces the mass flow rate as can be seen in Eq. (13). The local total pressure (i.e., the pressure obtained by isentropically decelerating the flow to zero velocity) is calculated from the flow field as

$$p_t = p \left( 1 + \frac{\gamma - 1}{2} Ma^2 \right)^{\frac{\gamma}{\gamma - 1}}. \quad (14)$$

In addition, increases in total temperature reduce efficiency, though the total temperature has much less influence than the total pressure (refer to Eq. (13)). The total temperature is calculated from the flow field as

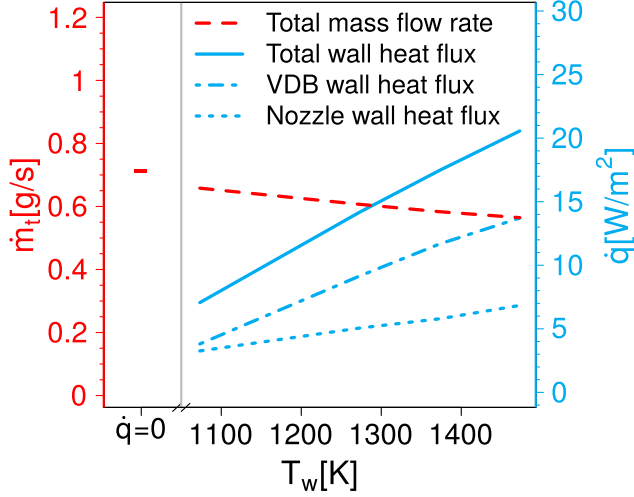
$$T_t = T \left( 1 + \frac{\gamma - 1}{2} Ma^2 \right). \quad (15)$$

Table 5 shows total pressure and total temperature averaged across certain z-planes to permit an estimation of the impact by different regions. Total pressure decreases by 4% between the VDB inlet and the nozzle inlet plane, but drops dramatically inside the nozzles by 30%. Total temperature rises by approximately 200K between the VDB inlet

**Table 5**

Total pressure and total temperature averaged across some z-planes.

|                     | Total pressure $p_t$ in Pa | Total temperature $T_t$ in K |
|---------------------|----------------------------|------------------------------|
| VDB inlet plane     | 4184                       | 948                          |
| Nozzle inlet plane  | 4011                       | 1144                         |
| Nozzle outlet plane | 2796                       | 1251                         |

**Fig. 8.** Mass flow rate and wall heat flux over wall temperature.

and the inlet of the nozzles, inside the nozzles it only increases by approximately 100K. If we use the values to compare the ratio  $\frac{p_t}{\sqrt{T_t}}$  from the approximation in Eq. (13) at the nozzle outlet plane with the one at the VDB inlet plane, the estimated efficiency is 0.58, which is close to the actual simulated discharge coefficient of 0.54 (Table 5).

The losses — either due to a reduction in total pressure or an increase in total temperature — can be broken down into different contributions: (1) flow separation or turbulence in the VDB, (2) the viscous boundary layer in the nozzles and (3) the wall heating. The first two impact on the total pressure; the wall heating impacts both the total temperature and the total pressure. Since the pressure drop between the VDB inlet and nozzle inlet is small, we will not discuss (1) any further, but rather focus first on wall heating and then on the boundary layer.

#### 4.3.3. Wall Heating

Wall heating is applied to prevent the metal vapor from condensing at the VDB walls. At the same time wall heating in compressible flow causes Rayleigh flow. This increases total temperature and reduces total pressure, both of which in turn lower the discharge coefficient.

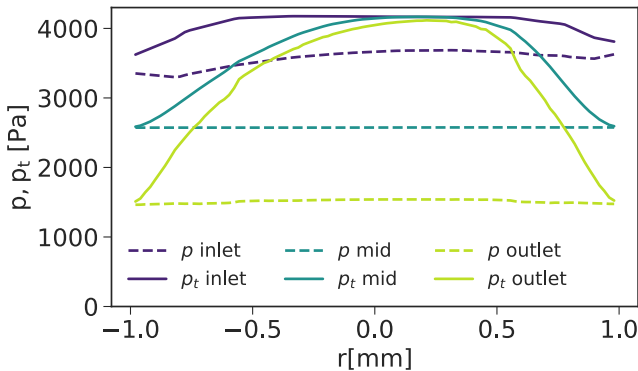
**(a)** Static pressure  $p$  and total pressure  $p_t$ .

Fig. 8 shows the total mass flow rate and the heat fluxes emerging from the VDB wall and the nozzle walls for different wall temperatures as well as for adiabatic walls. The introduced heat flux increases almost linearly with the wall temperature. The heat flux introduced by the VDB wall is approximately twice as high as that introduced inside the nozzles, in line with the 200K temperature increase in the VDB versus 100K in the nozzle, as listed in Table 5.

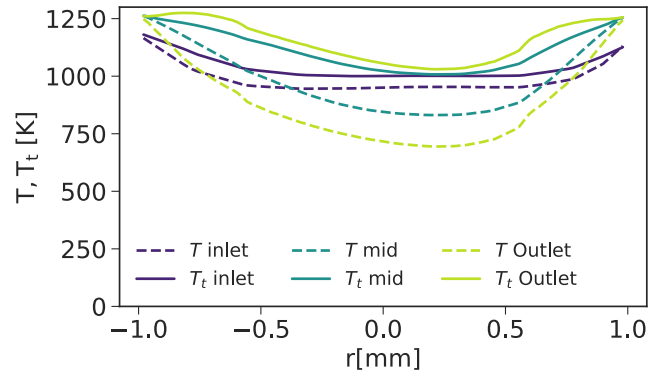
An increase in wall temperature by 100K lowers the mass flow rate by approximately 4%. For the range under consideration, the relation is linear. Even adiabatic walls produce only a moderately higher mass flow. This indicates that other non-ideal effects, such as the viscous boundary layer in the nozzles, are responsible for the low discharge coefficient.

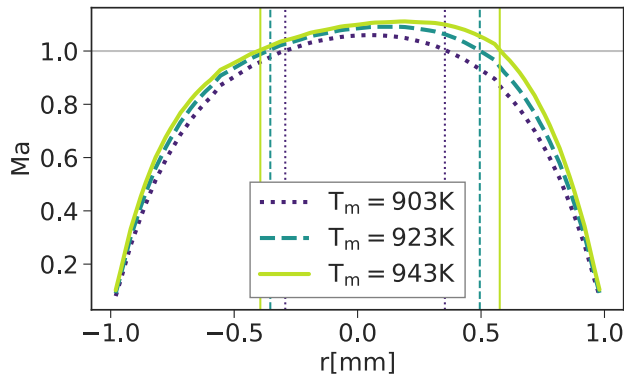
#### 4.3.4. Non-Isentropic Losses in the Nozzle Boundary Layer

To determine the nozzle regions, where the drastic pressure drop occurs, Fig. 9 plots static pressure, total pressure, static temperature and total temperature across the nozzle diameter at the inlet, in the middle and at the outlet of the seventh nozzle. The (static) pressure is constant across and decreasing downwards of the nozzle, whereas the total pressure is at a constant high level in the inner core of the nozzle, but drops significantly next to the walls, which denotes losses due to both viscous effects and wall heating. The temperature drops in the core along the nozzle due to the transfer of heat to kinetic energy, while it tends towards the wall temperature directly next to the wall. The total temperature increases in the same near-wall region where the total pressure drops, while it stays nearly constant in the core. The increase in total temperature is caused by the Rayleigh flow only, whereas the observed pressure drop in the boundary layer can be accounted for by multiple phenomena: increased viscosity due to the high wall temperature, viscous dissipation, Rayleigh and Fanno effects. In the core of the nozzle flow these effects are negligible. It should be noted that due to the radial geometry the total impact is weighted by the radius, so that the pressure drop in the boundary layer has a large effect. This indicates that the easiest way to improve the mass flow discharge are bigger nozzle radii as the nozzle outlet area increases quadratically with nozzle radius, while the wall boundary increases only linearly. Another possibility would be shorter nozzles to reduce the boundary layer length and thickness. Design optimization of the nozzle shape (e.g., converging-diverging nozzles) may be another option, but the efficiency increase strongly depends on process conditions [62].

#### 4.3.5. Melt Temperature

Earlier, we showed that the discharge coefficient increases with melt temperature. To analyze the influence of the melt temperature on non-isentropic losses in greater detail, Fig. 10 plots the Mach number for different melt temperatures as a function of the radius at the outlet of the seventh nozzle. As the nozzle inflow is not aligned with its axis, the

**(b)** Static temperature  $T$  and total temperature  $T_t$ .**Fig. 9.** Pressure and temperature profiles across the nozzle diameter at the inlet, half way downstream (mid) and outlet of the seventh nozzle.



**Fig. 10.** Mach number across the outlet of the seventh nozzle for different melt temperatures. The thin vertical lines mark the transition from sub- to super-sonic flow.

profiles are asymmetric. The Mach number shows a plug profile with values above the speed of sound in the core region. However, the critical area (i.e., the area where  $Ma > 1$ ) is significantly decreased by a substantial boundary layer (which we defined as the region where  $Ma < 1$ ). The boundary layer for  $T_m = 943K$  matches the region of pressure loss in Fig. 9. Considering the radial geometry of the nozzle, the critical area is reduced by approximately a factor of four for a melt temperature of  $T_m = 943K$ . For lower melt temperatures, the critical area is even smaller. A higher melt temperature produces a higher pressure in the VDB, which reduces the boundary layer thickness (in which the highest pressure drop appears) and expands the critical section, thus resulting in a higher discharge efficiency.

Hence it can be concluded, that a higher melt temperature improves the mass flow rate in two ways: The ideal isentropic mass flow rate increases and the non-isentropic losses become smaller.

## 5. Conclusions

A simulation model was developed to predict the total mass flux and mass flux uniformity in a continuous Physical Vapor Deposition apparatus. A crucial factor was the implementation of a new boundary condition, which considers the evaporation rate limitation by the Hertz-Knudsen relation. The simulations were validated by comparing the results with experiments and analytical approximations. The following conclusions can be drawn

1. For accurate modeling of continuous VDB processes:

- The mass flow limitation by the Hertz-Knudsen boundary condition is crucial for predicting evaporating flows. However, the exact evaporation coefficient (within the range reported in the literature) is less decisive.
  - The mass flow rate is not very sensitive to changes in viscosity.
  - Despite the clear improvement in prediction quality, the computational results still overpredict the mass flow rate by approximately 30%. We suppose that either dross at the melt surface, which was detected subsequent to running the experiments, hampers the evaporation, or the evaporation coefficient considerably differs under the process conditions studied from that in the literature (due to different process conditions or melt contamination). To minimize these uncertainties, more measurements of the metal properties would be required.
2. For optimizing the continuous VDB processes:
    - The total mass flow rate depends mainly on melt temperature and nozzle geometry.
    - Since the flow is fast, the mass flow decrease due to wall heating is marginal.
    - For the device studied, the discharge efficiency (i.e., the ratio of actual to ideal mass flow rate) was low (0.33–0.4 in experiments and 0.43–0.54 in simulations). This is mainly due to the boundary layer within the nozzles. To increase the discharge efficiency the influence of the boundary layer has to be reduced (e.g., through shorter nozzles or a bigger nozzle radius). This, however, might impair nozzle-to-nozzle uniformity.
    - Higher melt temperatures and thus higher VDB pressures reduce the boundary layer thickness in the nozzles and result in a higher discharge coefficient.

## Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

## Acknowledgments

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## Appendix A

### A.1. Turbulence Model

The turbulent viscosity  $\mu_t$  is modeled by the Launder and Sharma low-Reynolds  $k-\epsilon$  model [53] with a compression term based on rapid distortion theory (RDT) [54], which is available in OpenFOAM ®-v1806, as  $\mu_t = \rho C_\mu \frac{k^2}{\epsilon}$  where the turbulent kinetic energy  $k$  and the dissipation rate  $\epsilon$  are described by the following transport equations:

$$\begin{aligned} \frac{\partial(\rho k)}{\partial t} + \frac{\partial(\rho k u_j)}{\partial x_j} - \frac{\partial}{\partial x_j} \left[ \rho \left( \nu + \frac{\nu_t}{\sigma_k} \right) \frac{\partial k}{\partial x_j} \right] = \\ \rho G - \rho \epsilon - \rho D - \frac{2}{3} \rho \frac{\partial u_i}{\partial x_i}, \end{aligned} \quad (16)$$

$$\begin{aligned} \frac{\partial(\rho \epsilon)}{\partial t} + \frac{\partial(\rho \epsilon u_j)}{\partial x_j} - \frac{\partial}{\partial x_j} \left[ \rho \left( \nu + \frac{\nu_t}{\sigma_\epsilon} \right) \frac{\partial \epsilon}{\partial x_j} \right] = \\ (C_{\epsilon,1} P - C_{\epsilon,2} f_2 \rho \epsilon) \frac{\epsilon}{k} + \rho E - \frac{2}{3} C_{\epsilon,1} \rho \frac{\partial u_i}{\partial x_i} \epsilon, \end{aligned} \quad (17)$$

where the turbulence generation term is

$$G = \nu_t \frac{\partial u_k}{\partial x_k} \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} - \frac{2}{3} \frac{\partial u_l}{\partial x_l} \delta_{ij} \right)$$

the near-wall source terms and the near-wall damping functions are

$$D = 2\nu \frac{\partial \sqrt{k}}{\partial x_i} \frac{\partial \sqrt{k}}{\partial x_i} \text{ and } E = 2\nu \nu_t \frac{\partial^2 u_i}{\partial x_j \partial x_k} \frac{\partial^2 u_i}{\partial x_j \partial x_k}$$

$$f_2 = 1 - 0.3 \exp(-R_t^2) \text{ and } f_\mu = \exp\left(-\frac{3.4}{1 + \frac{1}{50} R_t}\right)$$

$$\text{where } R_t = \frac{k^2}{\nu \epsilon}.$$

The coefficients are  $C_\mu = 0.09$ ,  $C_{\epsilon,1} = 1.44$ ,  $C_{\epsilon,2} = 1.92$ ,  $C_3 = 0$ ,  $\sigma_k = 1$  and  $\sigma_\epsilon = 1.3$ . Based on the Reynolds number of a laminar test simulation  $Re = 2000$ , the inlet turbulent intensity was estimated to be  $I = 0.085$  [63], which corresponds to an inlet turbulent kinetic energy  $k \approx 9.75 \text{ m}^2 \text{ s}^{-2}$  and an inlet turbulent dissipation rate of  $\epsilon \approx 1880 \text{ m}^2 \text{ s}^{-3}$  [64].

## Appendix B. Verification, Validation and Mesh Independence

### B.1. Shock Tube Verification

The used solver, i.e., *sonicFoam*, is verified with a shock tube, which is a one-dimensional pipe that is initially split into a driver section at a high uniform pressure and a driven section at a low uniform pressure. When starting the simulation (or in an experiment when destroying the separating membrane), a shock is induced and travels into the driven section. Shock tubes are meaningful verification cases for compressible flow solvers, since on one hand, important compressible flow phenomena occur, such as shock, contact discontinuity and expansion. On the other hand, the simplicity allows for an analytic solution [43]. To stay close to the nozzle flow inside the VDB, the thermodynamic properties of zinc were used. No initial velocity or inlet velocity was applied. To verify the solver for the immense pressure drop across the domain, the pressure ratio was set to  $r_p = 1000$ . The initial conditions at  $t = 0$  are:

- driver section:  $p = 5000 \text{ Pa}$ ,  $T = 1000 \text{ K}$  for  $x < 0$
- driven section:  $p = 5 \text{ Pa}$ ,  $T = 500 \text{ K}$  for  $x > 0$

The grid has 20000 equidistant cells. Fig. 11 compares analytic and flow solver solutions at  $t = 5 \cdot 10^{-4} \text{ s}$ . The vertical gray lines mark from left to right the start and end of the expansion region, the contact discontinuity, across which temperature and density are discontinuous, but velocity and pressure are constant, and the shock. The shock speed is marginally overpredicted by *sonicFoam*, which results in a very small shift of the discontinuity in the profiles to the right. The numerical solver is in good agreement with the analytical solution.

### B.2. Sajben transonic diffuser validation

The solver *sonicFoam* and the turbulence model were validated with a transonic converging–diverging diffuser flow, which was experimentally studied by the group around Sajben [66] for multiple pressure ratios. The steady-state cases have been widely used for validation of compressible CFD codes [65,67–69] and are part of the NASA verification and validation archive [70]. Since we apply the solver later to flows without shocks, we chose the ‘no-shock’ case with a pressure ratio of  $r_p = 0.862$  for the validation. The two-dimensional diffuser geometry is visible in Fig. 12a; its throat height is  $h_{th} = 44 \text{ mm}$  and other details were described by Bogar et al. [66]. We used a grid of 94 cells in wall-normal direction with a strong vertical refinement towards both walls and 380 cells in streamwise direction with a progressive horizontal refinement towards the throat region with a grid-expansion ratio of 1.002–1.003. The cell centers in direct neighborhood to the wall had a distance less than  $y_1^+ = 0.9$  to the wall. A total pressure of  $p_s = 135000 \text{ Pa}$  and total temperature of  $285 \text{ K}$  is assumed. For the simulations, the isentropic relations were applied to obtain pressure, temperature and velocity for  $Ma = 0.46$ . The inlet turbulence intensity was set to  $I = 0.04$ . At the outlet, the pressure was set to  $p_o = 116770 \text{ Pa}$ . The boundary conditions are listed in Table 6. The fluid was air with a specific heat ratio  $\gamma = 1.4$ , a molecular mass of  $M = 28.9 \text{ g mol}^{-1}$ , specific heat at constant pressure  $c_p = 1005 \text{ J kg}^{-1} \text{ K}^{-1}$  and Prandtl number  $Pr = 0.72$ . The Sutherland law was applied in the form of Eq. 9 with a coefficient  $A_s = 1.7219 \cdot 10^{-6}$  at a reference temperature of  $T_0 = 288.167 \text{ K}$ . The solver, discretization schemes and turbulence model were the same as described in Section 3.2. The previously described Launder and Sharma low-Reynolds  $k-\epsilon$  model with RDT term was applied.

The Mach number contours are shown in Fig. 12a. The subsonic, turbulent inflow accelerates in the nozzle and reaches a maximum Mach number of  $Ma = 0.85$  close to the throat and afterwards decelerates. Figs. 12b and c compare pressure normalized by the inlet stagnation pressure along the bottom and top wall from the experiments, the simulations by Georgiades [65] using the Speziale  $k-\epsilon$  and Chien  $k-\epsilon$  turbulence models and the solver used in the present study, called *sonicFoam*. At the top wall (Fig. 12b), the pressure normalized by the inlet stagnation pressure drops to  $p/p_0 = 0.85$  at the inlet, reaches its maximum where the converging section starts, drops in the throat to its minimum and rises afterwards to the outlet pressure. The simulation by Georgiades using the Chien  $k-\epsilon$  turbulence model matches the experimental data well, the one using the Speziale  $k-\epsilon$  turbulence model reports a higher pressure in the trough, *sonicFoam* predicts here a marginally lower pressure. The profile at the bottom wall is similar to the one at the top wall except for the first small rise in pressure and the fact that the pressure drop is smaller. These differences occur, since the geometry changes only at the top wall and thus affects the pressure at the bottom wall less. *sonicFoam* again matches the experimental data well except for a small

underprediction in the throat. Overall, a reasonable agreement is reached between experiment and *sonicFoam*.

### B.3. Grid Independence Study

In compressible flows, adequate meshing is important for both the numerical stability and the accuracy of the result. The grid dependence of the solution was studied (for the standard case at a melt temperature of 943K) on three meshes listed in Table 7. As the gradients are expected to be highest within the nozzles, the resolution inside the nozzles is crucial. Fig. 13 shows the Mach number and temperature profile at the outlet of the second nozzle. While for the coarse mesh both Mach number and temperature deviate from the results of the finer meshes, the medium and fine mesh results are in good agreement. This is why we chose the medium mesh for further calculations.

To speed up the simulations, two symmetry planes were used and only a quarter of the VDB was simulated. This particularly constrains the swirling motion along the long extension of the VDB. To study the influence on the viscous losses, half of the VDB was also simulated for the standard case. Neither the total nor the local mass flow rate changed notably, which justifies the use of the quarter geometry.

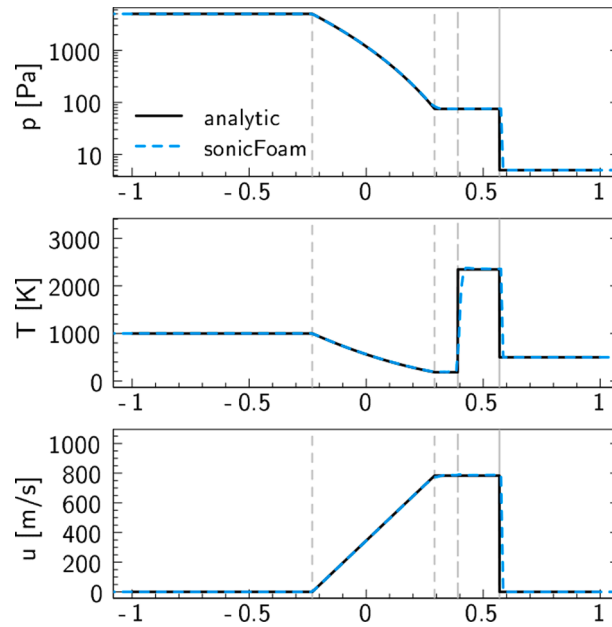


Fig. 11. Pressure, temperature and velocity in the shock tube at  $t = 0.0005s$ . Comparison of analytic and *sonicFoam* solutions. The thin vertical gray lines mark from left to right: the expansion head, the expansion tail, the slip surface and the shock.

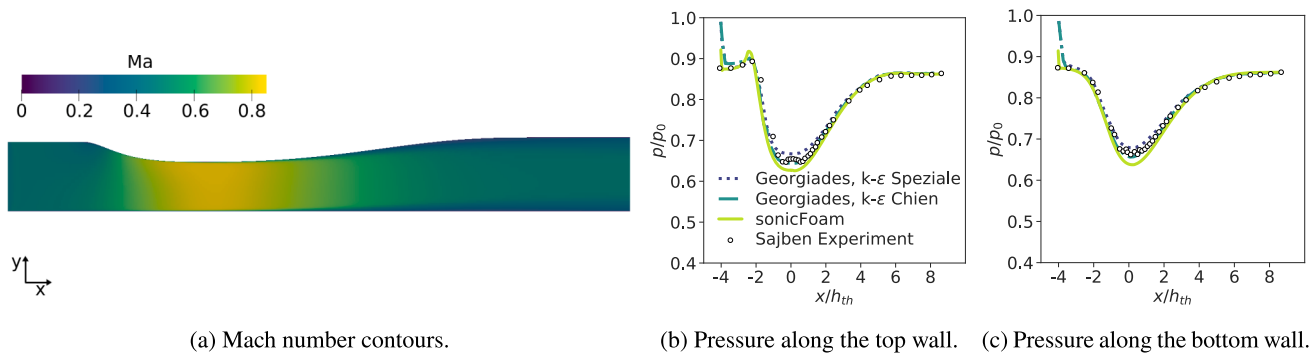


Fig. 12. Sajben transonic diffuser validation case. Contours and pressure profiles along the walls from *sonicFoam* compared to experimental results (data from [65]) and simulations by Georgiades et al. [65].

Table 6

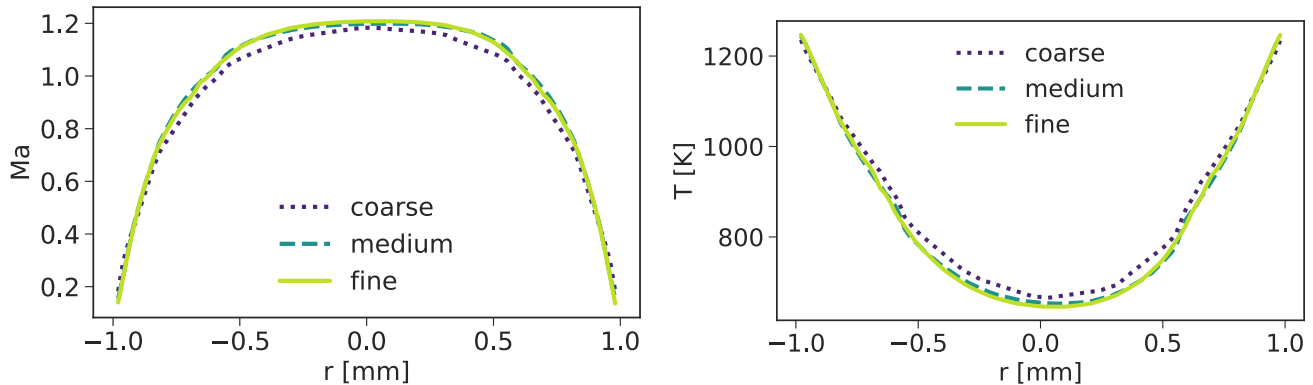
Boundary conditions for the Sajben transonic diffuser.

|        | pressure                          | velocity                        | temperature               | kinetic energy  | turbulent dissipation |
|--------|-----------------------------------|---------------------------------|---------------------------|-----------------|-----------------------|
| inlet  | static pressure $p_m = 116.77kPa$ | $152.45ms^{-1}$ ( $Ma = 0.46$ ) | static temperature 273.3K | $54.4m^2s^{-2}$ | $21966m^2s^{-3}$      |
| outlet | static pressure 110.66kPa         | zero gradient                   | zero gradient             | zero gradient   | zero gradient         |
| walls  | zero gradient                     | no slip                         | adiabatic                 | wall function   | wall function         |

**Table 7**

Grids, number of cells and mesh quality criteria.

|        | total No. of cells in Mio | No. of cells along one nozzle diameter | maximum non-orthogonality | mean non-orthogonality | maximum aspect ratio | maximum skewness |
|--------|---------------------------|----------------------------------------|---------------------------|------------------------|----------------------|------------------|
| coarse | 0.75                      | 13                                     | 62.01                     | 12.90                  | 12.06                | 2.03             |
| medium | 2.32                      | 27                                     | 67.10                     | 12.50                  | 13.02                | 2.26             |
| fine   | 4.47                      | 36                                     | 70.5921                   | 14.69                  | 52.64                | 2.52             |

**Fig. 13.** Mach number and temperature profile at the outlet of the second nozzle for different grids (see Table 7).

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