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STABILITY OF HIGH DENSITY CUBE ARMoured BREAKWATERS

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ABSTRACT

The performance of high-density cubes in the armor layer of a breakwater was investigated through an experimental study. For this purpose, two different cross-sections, one with a conventional cross-section and one with a berm, were modelled in a wave flume. A total of ten tests were performed for both cross-sections. Different concrete densities of cubes and different placement methods were applied. The dimensions of the cubes with two different densities were the same for all tests to avoid potential scale effects caused by the dimensions of HD cubes. The experimental study showed that HD cubes were more stable than ND cubes; the characteristic wave height for HD cubes was 1.5 times higher than that of the ND cubes. The use of HD cubes may provide economic efficiency and enables a significant reduction of the concrete volume, transportation of material, and reduction of required construction area for manufacturing, etc. HD cubes in a single layer turned out to be very stable. However, only using HD cubes in a part of the armor layer or only used on the second (upper) layer caused a decrease in the stability of the armor layer, especially in comparison to the armor layers that fully consist of HD cubes. The performance of HD cubes was also evaluated by comparing the experimental results with the Van der Meer (1988) formula and the suitability of the stability number for HD cubes was discussed.

Key Words: Breakwaters, Cube Blocks, High Density Concrete Armor Units, Single layer, Berm type breakwaters

1. INTRODUCTION

There might be some reasons and concerns leading the armor layer design to be constructed by high density concrete units. These might be drawn with the followings: 1- the difficulty of finding large rock materials; 2- Economical effects due to the increased concrete units' volume when normal density is considered; 3- Increasing waves caused by climate change requiring larger armor units; 4- Minimizing the manufacturing and construction site costs.

High density concrete armor units have been considered for variety type of armor units and one of them is cube armor unit which is the oldest and has a wide range of application on shore protection structures as being a conventional or a berm type breakwater depending on the design requirement and the conditions of the project area.

Many researchers demonstrated that concrete cubes can be used as armor unit (e.g., Van der Meer (1988), Van Gent et al. (1999), Triemstra (2000), Van Gent et al. (2001), Van Gent et al. (2003), Bueno Esposito et al. (2015), Van Gent and Van der Werf (2017), Sarfaraz and Pak, (2017), Howe and Cox (2018), Vieira et al. (2020,) Yuksel et al. (2020), Vieira et al. (2021)). However, few of these researchers have studied the importance and influence of density.

The main stability formula for concrete armor units was presented by Hudson (1953). Additionally, Van der Meer (1988) produced an empirical stability formula for cube units as follows,

$$N_s = \frac{H_s}{\Delta D_n} = \left[6.7 \frac{N_0^{0.4}}{N^{0.3}} + 1.0 \right] s_{0m}^{-0.1} \quad (1)$$

where H_s is the significant wave height, Δ is the relative density, D_n is the nominal diameter (which is the side length of the cube), N_0 is the relative damage number, N is the number of waves, s_{0m} is the wave steepness based on the mean wave period. The formula defines the stability number (N_s) in terms of the ratio of $H_s/\Delta D_n$ and the ratio contains the influence of the density of the concrete unit. Therefore, considering high density (HD) concrete unit rather than normal density (which is about 24 kN/m^3) would result in reduction on the required size of the armor unit.

The effect of changing the density of the armor units has been investigated by only few studies in the past (such as Hudson, 1959, Ito et al., 1994, Triemstra, 2000, Van Gent et al., 2001, Van Gent, 2003), although the densities of the materials in Hudson's tests were between 2146 kg/m^3 and 3076 kg/m^3 .

1 Concrete cubes can be placed single or double layer with different placement methods
2 of regular or irregular. According to Van Gent et al. (1999), Van Gent et al. (2001), Van
3 Gent et al. (2003), and Vieira et al. (2020 and 2021), the use of concrete armor cubes in
4 a single layer is a feasible and cost-effective solution specifically when it is compared to
5 the other concrete units constructed with one-layer like xblocs, core-loc and accropode.
6 In a similar way, the use of high-density cube as a single or double layer is also applicable
7 and effective in decreasing the costs (Triemstra, 2000; Van Gent et al., 2001; and Van
8 Gent, 2003). Obviously, single layer cubes are also economically competitive with two-
9 layer armor units such as Tetrapod and Antifer.

10 By implementing today's technological improvements, it is possible to produce concrete
11 cube armor units with 40 kN/m^3 density using magnetite or other high-density materials
12 (Triemstra (2000) and Van Gent et al. (2001)). However, in accordance with the literature,
13 in order to test the validity of the linear relationship between H_s/D_n and Δ in cubes with
14 40 kN/m^3 density, flume tests are required. Triemstra (2000) also studied other variables
15 such as packing density, influence of filter layer and wave steepness.

16 Ito et al. (1994) conducted some experiments with high density Tetrapodes varying
17 between 17.8 and 42.8 kN/m^3 . The authors suggested a relationship between K_D and the
18 specific gravity, where K_D decreases with increasing specific gravity. As it is known that
19 K_D was proposed by Hudson (1959) to characterize the hydraulic performance of
20 different armor units placed on conventional double-layer armors (Medina and Gomez-
21 Martin, 2012). On the other hand, they concluded that the stability of high-density armor
22 blocks was found to be significantly affected by scale effects due to the very small
23 dimensions of the units. Because concrete armor unit sizes are usually limited in the
24 model by the available sizes (often $>3.0\text{cm}$). A practical limitation can be that the
25 detection of rocking becomes increasingly difficult for small concrete unit size. However,
26 Ito et al. (1994) used very small concrete units in their experiments (Hydralab III, 2007).

27 Van Gent et al. (2001) conducted some tests with high density cubes (almost 40 kN/m^3)
28 in a traditional double top layer and single top layer over a strait slope. They revealed
29 that high density cubes were as stable as normal density cubes. They also noticed that
30 an increase of the density by a factor of 1.5 would lead to a reduction in the weight by a
31 factor of 5, a reduction in volume per unit by a factor of 8, would lead to a reduction in
32 the volume of concrete in the top layer by a factor of 2.

33 Cube stability as an armor layer is a complex problem and still needs to be investigated
34 in detail. The stability number is an empirical formula that is to be used for the conceptual
35 design of rubble mound breakwaters and in fact it is a function of several parameters

1 and depends on unit shape, placing method, slope angle, relative density, etc., and these
2 parameters are not taken into account by the formula itself. Therefore, a design formula
3 is needed in order to obtain more reliable results such as for high density cube blocks
4 with different placement methods. This study therefore aims not only investigating the
5 performance of HD cube units, but also the convenience of using the existing formula for
6 high density cube units with different placements.

7 In this study, the impact of the using high-density cubes as armor units was investigated
8 for conventional and berm type breakwaters. A 1/1.5 straight slope was used for
9 conventional breakwater, and 1/1.5 lower and 1/2 upper slopes were used for berm type
10 breakwaters. Both regular and irregular placement methods of units were used, and
11 moreover high density (HD) cubes in a single layer were tested. These different
12 placement techniques using HD cubes were discussed based on their stability. So, the
13 idea about designing relatively more economical, environmental-friendly, and stable
14 breakwaters with the use of HD concrete blocks would be revealed.

15 The remainder of the present paper is organized as follow: A description of the
16 methodology for investigation of the stability of conventional and berm type breakwaters
17 in terms of placement techniques and the density of the cubes used in the armor layer is
18 provided in Section 2, with the test conditions detailed in Section 3. Results and
19 discussions from the stability experiments are, provided in Sections 4 and 5 respectively.
20 Conclusions are presented in Section 6.

21 **2. METHODOLOGY**

22 Two different conventional cross-sections were considered: (1) with a single layer using
23 regular placement, (2) with a double layer using irregular placement. The second model
24 was a berm type breakwater consisting of an irregularly placed double layer on the lower
25 slope. For these model tests, normal-density (ND) and high-density (HD) cubes were
26 utilized. For the berm type breakwater models, the water depth was varied between 0.45
27 m and 0.65 m, where the berm level was kept constant at 0.55 m similar to the study of
28 Yuksel et al. (2020). Consequently, with the combination of these various circumstances,
29 10 different breakwater models were tested. Table 1 shows all tested breakwater models
30 where ND and HD mean that the density of cubes are 24 kN/m^3 and 31.5 kN/m^3 ,
31 respectively where d_{toe} is the depth of breakwater toe and packing density (ψ_S) is ratio
32 between the real and the maximum number of blocks per unit area.

33 The tested conventional cross-sections are elaborated below. Placement styles for these
34 models can also be seen from Figures 1a, b.

1 Case 1-(CID) First (lower) layer ND cube – Second (upper) layer HD cube using
 2 irregular placement: In this experiment, ND cubes were placed in the first (lower)
 3 layer and HD cubes were placed in the second (top; upper) layer.

4 Table 1 Experimental conditions

Test Case	Breakwater type	Placement type	Layer	d_{toe} (m)	Used cubes	Packing density (ψ_s)
1-CID	Conventional	Irregular	Double	0.55	First Layer ND	0.59
					Second Layer HD	
2-CID*	Conventional	Irregular	Double	0.55	First and Second Layer ND	0.59
					Second Layer HD in the reference area	
3-CID	Conventional	Irregular	Double	0.55	First Layer HD	0.59
					Second Layer HD	
4-CRS	Conventional	Regular	Single	0.55	ND	0.59
5-CRS	Conventional	Regular	Single	0.55	HD	0.59
6-BID	Berm	Irregular	Double	0.45	First Layer ND	0.59
					Second Layer HD	
7-BID	Berm	Irregular	Double	0.55	First Layer ND	0.59
					Second Layer HD	
8-BID	Berm	Irregular	Double	0.65	First Layer ND	0.59
					Second Layer HD	
9-BID**	Berm	Irregular	Double	0.45	First and Second Layer ND	0.59
					Second Layer HD in the reference area	
10-CID	Conventional	Irregular	Double	0.55	First Layer ND	0.59
					Second Layer ND	

5 *2-CID; HD cubes was placed only over the reference area in the second (upper) layer including
 6 first row at the top layer of crest. Rest of the armor layers have ND cubes.

7 ** 9-BID; HD cubes were placed only over the reference area both in the first (lower) and second (upper)
 8 layers including two rows in berm close the water side. Rest of the armor layers have ND cubes.

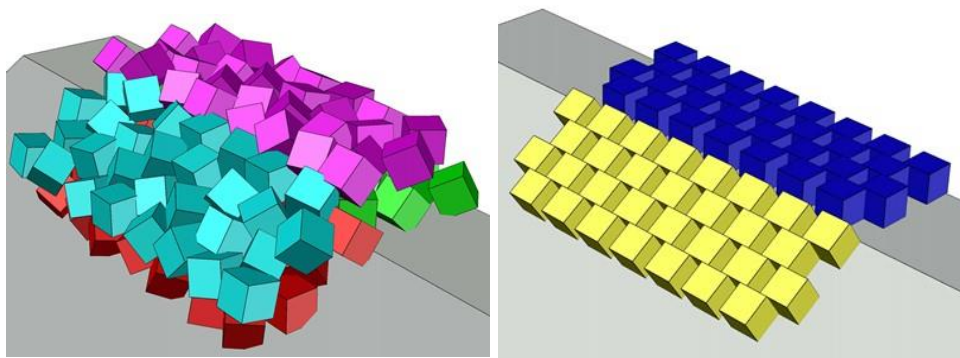
9 Case 2-(CID) Reference Area HD with irregular placement: HD cubes on the second
 10 (upper) layer considered only in the reference area and in the area from the upper
 11 boundary of the reference area to the top of the crest. The rest consisted of ND
 12 cubes. The placement method was irregular for both layers.

13 Case 3-(CID) Double Layer HD cubes using irregular placement: In this model, both
 14 first (lower) and second (upper) layers consisted of HD cubes only.

1 Case 4-(CRS) Single layer ND cubes with regular placement: ND cubes were placed
2 regularly in a single layer over the slope.

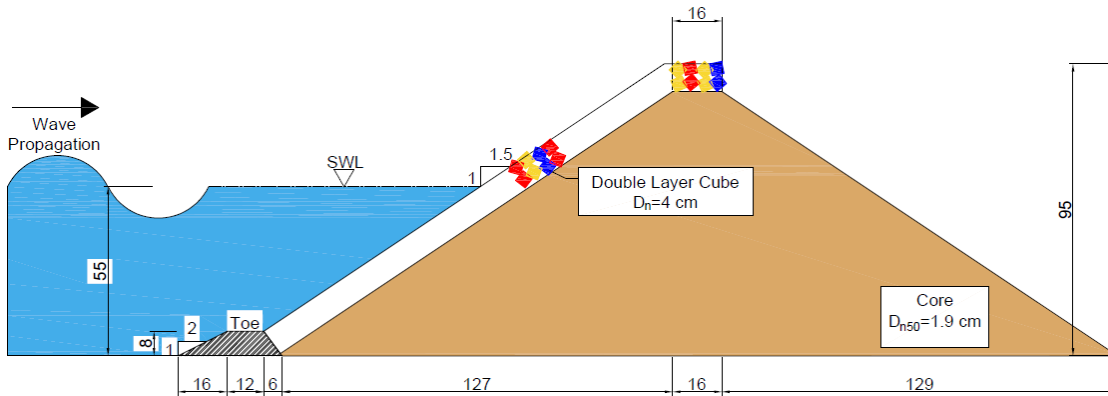
3 Case 5-(CRS) Single layer HD cubes with regular placement: HD cubes were placed
4 regularly in a single layer over the slope.

5 Tested conventional breakwater cross-sections for double layer and single layer can be
6 seen in Figure 2 and 3, respectively. An additional test was conducted for a conventional
7 breakwater with double layer ND cube over the slope as Case 10 to verify the test with
8 Van der Meer (1988) formula and to discuss the results with the results obtained from
9 HD tests.



10
11 (a) (b)

12 Figure 1 Irregular (a) and regular (b) placement styles.



13
14 Figure 2 Cross-section for double layer models (units are in cm).

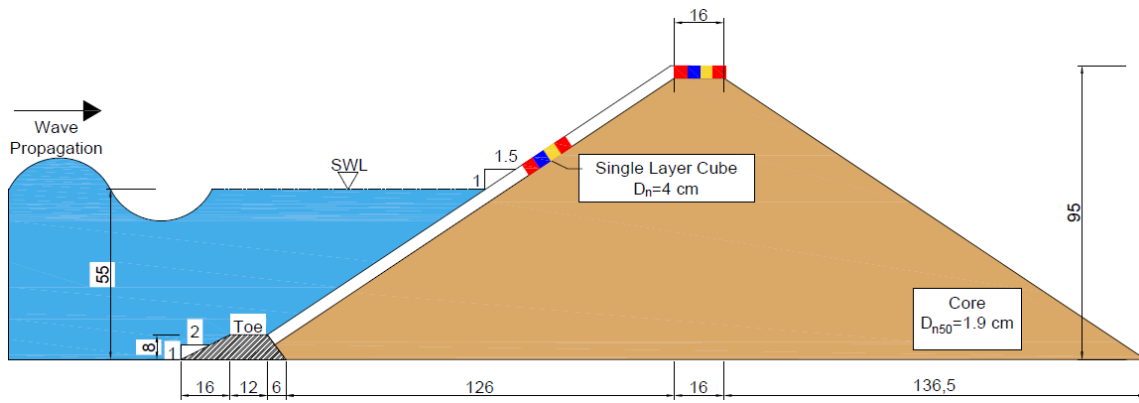


Figure 3 Cross-section for single layer models (units are in cm).

Tested cross-sections with berm, are given below in details. Placement styles and cross-sections with different water levels are depicted in Figure 4. Figure 5 shows the transition from the lower slope to the berm according to Yuksel et al. (2018).

Case 6-(BID) Emerged berm (Irregular): ND cubes were placed in the first (lower) layer and HD cubes were placed in the second (upper) layer. The berm was 10 cm above the SWL. The placement method was irregular for both layers.

Case 7-(BID) Berm at SWL (Irregular): ND cubes were placed in the first (lower) layer and HD cubes were placed in the second (upper) layer. The berm was at the still water level.

Case 8-(BID) Submerged berm (Irregular): ND cubes were placed in the first (lower) layer and HD cubes were placed in the second (upper) layer. The berm was 10 cm below the SWL. The placement method was irregular for both layers.

Case 9-(BID) Emerged berm with HD cubes over reference area (Irregular): HD cubes were placed over the reference area both in the first (lower) and second (upper) layers including first two rows of the berm. The rest was filled with ND cubes. The placement method was irregular for both layers.

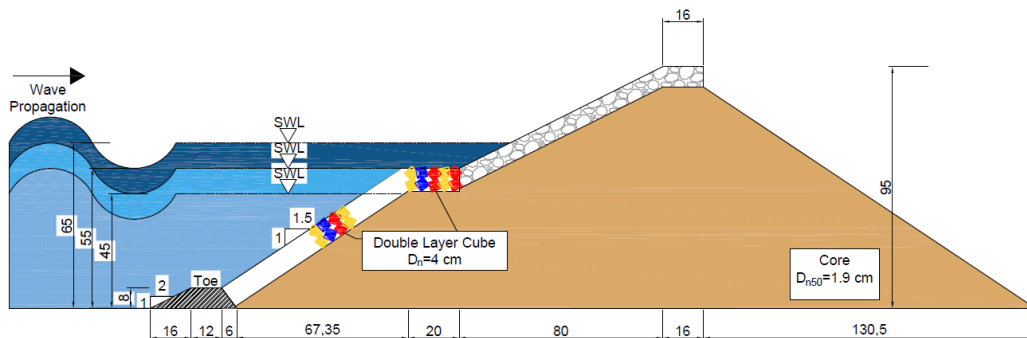
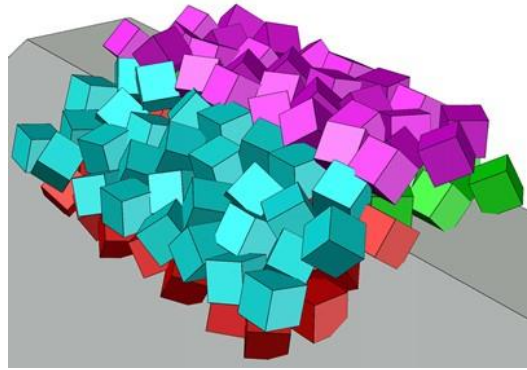


Figure 4 Cross-section for models with berm (units are in cm).



1

2 Figure 5 Irregular placement style for the transition section of the breakwaters with
3 berm (Yuksel et al., 2018).

4 To determine the damage accurately, it is important to define the reference area because
5 the displaced and moved units are not uniformly distributed over the slope due to wave
6 action. The reference area was defined as the area between two levels of $SWL \pm H_s$,
7 which corresponds to $SWL \pm 5D_n$ for the selected design wave height of $H_s=0.20$ m and
8 nominal cube diameter of 4 cm. By considering these issues, the reference area was
9 kept constant as $10D_n$ below the crest for the conventional breakwater model and the
10 area below the berm for berm type breakwater (Yuksel et al., 2020).

11 Unit displacement or movement is termed as damage; however their definitions are
12 different. In this study damage is defined by displaced units in the following way (Frens,
13 2007 and Yuksel et al., 2020):

- 14 • No damage: No units are displaced.
- 15 • Initial damage: A few units are displaced.
- 16 • Failure: The under layer is exposed to direct wave attack.

17 According to above definitions, damage was calculated and evaluated as follow:

18 1-Displacement ratio was calculated with the equation given below:

$$19 \text{ Displacement Ratio } (D_i) = \frac{\text{Number of displaced units}}{\text{Total number of units within reference area}} (\%) \quad (2)$$

20 The displacement of units is defined as the movement of a block more than distance of
21 D_n (Van der Meer, 1988) from their original position. The displacement ratio was
22 classified as D_1 , D_2 , and D_T which represent the displacements between $1D_n$ and $2D_n$,
23 above $2D_n$, and above $1D_n$, respectively. Hence, D_T indicates all (total) displaced cubes
24 in the reference area (Frens, 2007).

1 On the other hand, movement can be considered as an action of mobility which can be
 2 defined as an amount of displacement less than D_n .
 3 Movement may be occurred before displacement and the units may lose support from
 4 their adjacent units. In a similar way using Equation (2), three different categories of
 5 movement are expressed in relation to the nominal diameter: $<0.5D_n$, $0.5-1.0D_n$, and $0.0-$
 6 $1.0D_n$ which are indicated with M_1 , M_2 , and M_T (total movement), respectively (Frens,
 7 2007).

8 Between each sea state, the damage was not repaired, so the displacement and
 9 movement ratio after each sea state is the cumulative damage.

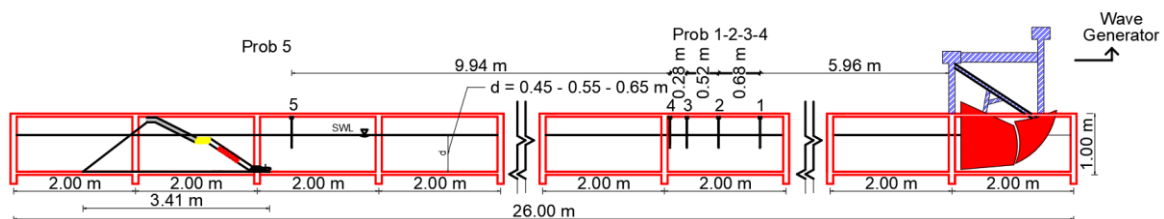
10 2- Relative damage number: Damage to concrete units can be described by the relative
 11 damage number N_0 which is defined by the actual number of displaced units related to a
 12 width (along the longitudinal axis of the breakwater) of one nominal diameter, D_n . In this
 13 study, the damage number was found by counting the displaced units of one nominal
 14 diameter width in the reference area from the camera records.

$$15 \quad N_0 = \frac{\text{Number of displaced units of one nominal diameter } D_n \text{ in reference area}}{L/D_n} \quad (3)$$

16 where L is the width of the model structure excluded one nominal diameter from each
 17 side wall and D_n is the nominal diameter of the cube.

18 3. EXPERIMENTAL SETUP AND PROCEDURES

19 Experimental research was carried out in the wave flume of the Coastal and Harbor
 20 Engineering laboratory at Yildiz Technical University. The flume has a length of 26 m, a
 21 width of 1 m and a height of 1 m. The channel is equipped with a piston-type wave
 22 generator that has an active reflection system (Figure 6).



23

24

Figure 6 Longitudinal cross-sections of the wave channel

25 The nominal diameters for both normal and high-density cube models were 40 mm to
 26 avoid the scale effects as indicated by Ito et al. (1994). Densities were 24.0 kN/m^3 and
 27 31.5 kN/m^3 for ND and HD cubes, respectively. The breakwater models were placed on

1 a horizontal foreshore. All models have 1 m width and 0.95 m height consisting of a
2 permeable core layer with quartz stone, a toe and the armor layer. The under layer
3 consisted of stones with a nominal diameter of 19 mm for all cases. The packing density
4 per layer of the blocks was kept 59% for both ND and HD cubes for all tests. The slope
5 of the conventional breakwater was 1:1.5. For berm type breakwater, the lower slope
6 was 1:1.5 with cube armor layer while the upper slope was 1:2 with rock armor layer with
7 a nominal diameter of 32.5 mm and it was fixed with a wire mesh in order to focus on the
8 investigation of the performance of the lower slope which this method is similar to the
9 study of Yuksel et al. (2020).

10 The water level was varied with respect to the berm level. Three different water depths
11 (d) of 0.45, 0.55 and 0.65 m were selected to investigate the effect of the berm position
12 relative to the still water level. In other words, the still water levels (SWL) were 0.1 m
13 below, at, and 0.1 m above the berm level ($d_b/d = -0.222, 0$ and 0.154 where d_b is the
14 vertical distance between berm and SWL; $d_b/D_n = -2.5, 0$ and 2.5). The berm width on the
15 other hand was kept constant as $5D_n$ according to the definition given by Yuksel et al.
16 (2020).

17 Figure 7a, b and c show different breakwater models in the experimental study for double
18 layer irregular placement, single layer regular placement for conventional breakwater
19 and double layer irregular placement for berm type breakwater, respectively.

20 For the irregular placement, the blocks were placed by letting them fall free from a height
21 of half a nominal diameter above and to increase the irregularity of the placement. In
22 these experiments for irregular placements of the armor layers, special attention was
23 given to reproduce a similar irregularity for both normal and high-density cubes, which
24 was indicated by Van Gent et al. (2001). For regular single layer placement, blocks were
25 placed one by one for each calculated location on the slope, and they were placed
26 staggered over the slope (Figure 1b). For both placement methods, the units were
27 placed in colored bands to improve the visualization of the displacement and so to
28 measure the damage.



(a) (b) (c)

Figure 7 Tested breakwater models in the experimental study

The standard Froude scaling method for the under layer, which is the core material, is based on a relation between the armor block weight and the under-layer material weight, $M_{\text{armour}} / M_{50, \text{underlayer}}$. A relation based on the nominal diameter of the armor and under layers $D_{n, \text{armour}} / D_{n50, \text{underlayer}}$ is also commonly used. Van Gent (2003) recommended a ratio between 2 and 2.5. The ratio was considered as $D_{n, \text{armour}} / D_{n50, \text{underlayer}} = 40 / 19 = 2.1$ for both conventional and lower slope and berm, and $D_{n50, \text{armour}} / D_{n50, \text{underlayer}} = 34 / 19 = 1.8$ for upper slope of the berm type breakwater.

The viscous scale effects are negligible when the Reynolds number is larger than 2×10^3 (Hughes, 1993; Lykke Andersen, and Burcharth, 2010; Wolters et al., 2010). The Reynolds number is calculated by $Re = U \cdot D / \nu$ where D is the characteristic dimension of the armor material and ν is the kinematic viscosity, which for the water at 10°C is $1.33 \times 10^{-6} \text{ m}^2/\text{s}$, U is the seepage velocity $U = (P \cdot H_i \cdot L_m) / (2 \cdot d \cdot T_m)$, P is the volumetric porosity of the core material, H_i is the significant wave height at the toe, L_m is the mean wave length of the waves, and T_m is the mean wave period at the toe. The resulting Reynolds number is 5×10^3 for the typical values used in this study, i.e., $P=0.49$, $H_i=0.14 \text{ m}$, $T_m=1.16 \text{ s}$, $d=0.45 \text{ m}$, $D_{n50}=0.019 \text{ m}$, which indicates that the experiments are not influenced by the scale effects. However, in a small-scale physical model, the friction forces between units may not be equal to those in the prototype because the armor unit surface can be relatively rougher in the model than for the large-scale units. Painting the unit provides somewhat a smoother surface, hence all units were painted (with different colors).

1 Toe stability of the structure was out of the scope of this research. The toe stability was
2 ensured by fixed with steel frame for all cases not to affect the stability performance of
3 the armor. The width and the thickness of the toe were $4D_n$ and $2D_n=8$ cm, respectively.
4 The crest width of the structure was $G_c=4D_n$.

5 A total of 13 irregular wave conditions with a JONSWAP spectrum ($\gamma = 3.3$) in deep water
6 were selected for all tests. Wave conditions were measured by wave probes at five
7 different locations. One of them was located in front of the structure toe. The other four
8 probes were in constant water depth with known spacing to separate incident and
9 reflected waves from the measured surface elevations (Figure 6). The applied method
10 for separating the incident and reflected waves was employed by using the Mansard and
11 Funke (1980) method. The spectral significant wave height H_s (in this paper:
12 $H_s=H_{m0}=4(m_0)^{0.5}$) and wave period $T_{m-1,0}$ ($T_{m-1,0}=m_{-1}/m_0$) were obtained from the measured
13 wave energy spectrum. A number of additional experiments were performed to check
14 the repeatability of the tests. The analysis was based on the time series of the incident
15 waves at the toe. In addition, waves were also calibrated at the toe of the structure by
16 comparing the incident waves for the experiments without structure (using a gravel beach
17 instead of structure).

18 For each test, the incoming significant wave height in front of the toe was gradually
19 increased to define the wave height leading to failure. The characteristic wave height
20 was determined as $H_s=0.20$ m based on ND cubes. Moreover, beyond characteristic
21 wave height was considered when the related model did not reach to failure. The
22 characteristic wave was only increased by around 10% due to limitations of larger waves
23 associated with the model dimensions chosen, the wave generator capacity and water
24 depth at the structure toe.

25 The damage was repaired after each series of test run, but not after each individual test
26 run. Each placement method was tested for the wave steepness of around
27 $s_p = 2\pi H_s / g T_p^2 = 0.033$.

28 Each test run consisted of about 1000 waves. The damage was cumulative for each test
29 series and detected using a visualization technique by taking digital photos before and
30 after each run from a fixed location perpendicular to the slope. The damage was
31 determined by counting the moved armor units and measuring the movement distance
32 in terms of displaced units related to a width (along the longitudinal axis of the
33 breakwater) of nominal diameter (D_n). To avoid potential side wall effects that could affect

1 the results, $1D_n$ widths from both sides of the wall were not considered for the calculation
 2 of the damage (Frens (2007), Van Gent, (2013), Yuksel et al. (2020)).

3 In this study, heavy concrete production with a targeted density of 31.5 kN/m^3 was
 4 obtained by using barite aggregate. Castings in different mixing ratios designed to
 5 achieve the desired density were realized and the density criterion, which is the main
 6 target, was achieved. The optimum mixing ratio was chosen in this way and in heavy
 7 concrete production a barite aggregate with 0-5 mm of grain size, CEM II 42.5 R type
 8 cement and the super plasticizer were used. In the mixture design, the water/cement
 9 ratio was determined as 0.55, and the super plasticizer ratio was determined as 0.44%.

10 Table 2 provides an overview of the applied values of the most important parameters for
 11 both type of breakwaters (conventional and berm type). Wave series with wave heights
 12 and corresponding N_s values for ND and HD cubes in the experiments were given in the
 13 appendix.

14 Table 2 Ranges of the parameters for the experimental data set

Parameter	Symbol	Value
Slope angle for conventional type	$\cot \alpha$	1.5
Upper and lower slope angle for berm type	$\cot \alpha$	2 and 1.5 respectively
Relative density for ND cubes, HD cubes and rocks	Δ	1.4 and 2.15 respectively
Rock size upper slope for berm type (m)	$D_{n50\text{-upper}}$	0.034
Cube size for both of ND and HD cubes (m)	D_n	0.040
Grading armor material	D_{n85}/D_{n15}	1.4
Grading underlayer material (core)	D_{n85}/D_{n15}	1.38
Berm width (m)	B	0.20
Berm level w.r.t. SWL (m)	d_b	-0.1 - 0.1
Berm level ratio (positive: submerged; note $H_s=H_{m0}$)	d_b/H_s	0.5 - 2.0
Berm level ratio for submerged, at SWL and emerged	d_b/d_{toe}	0.22-0.0(-0.15) respectively
Wave steepness ($s_{m-1,0} = 2\pi H_s / gT_{m-1,0}^2$ note $H_s=H_{m0}$)	$s_{m-1,0}$	0.026 - 0.050
Wave steepness ($s_p = 2\pi H_s / gT_p^2$ note $H_s=H_{m0}$)	s_p	0.021 - 0.045
Deep water wave height over depth (note $H_s=H_{m0}$)	H_s/d_{toe}	≤ 0.4
Wave height ratio (note $H_s=H_{m0}$)	$H_{2\%}/H_s$	1.4
Number of waves	N	1000
Stability number (note $H_s=H_{m0}$)	$N_s = H_s / \Delta D_n$	0.58 - 3.93

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1 **4. Results and Discussion**

2 **4.1 Conventional Cube Armored Breakwaters**

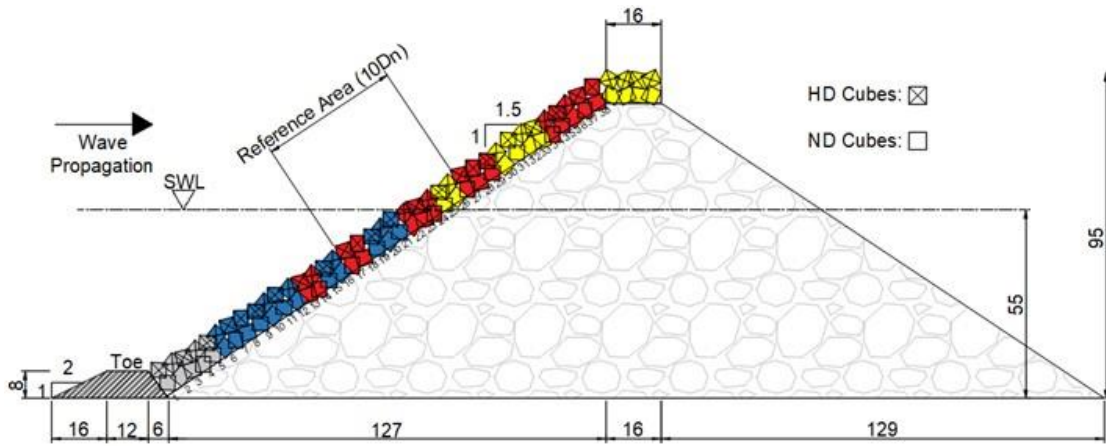
3 The tests were conducted only for 55 cm water depth. Double layer irregular placement
4 and single layer regular placement techniques were used.

5 **(i) Case 1: (CID) First (Lower) layer ND – Second (Upper) layer HD with irregular** 6 **placement**

7 Positions of both high density and normal density cubes and considered reference area
8 can be observed in Figure 8.

9 The wave heights were low at the start of the experiment, such as $H_{m0}=0.05$ m (at wave
10 series 1; W1) and $H_{m0}=0.08$ m (at wave series 2; W2). Thus, armor layer was stable, yet
11 movements were observed (10%). For wave series 3 (W3) and 4 (W4), significant wave
12 heights were relatively higher than the previous waves, $H_{m0}=0.10$ and 0.11 m, total
13 movement ratios increased and reached to 14% and 23%, respectively under these wave
14 conditions (Figure 9). The wave series 4 (W4) was the last series without displacements
15 and, the stability number (N_s) was 1.28.

16 The first displacement was observed at W5 ($H_{m0}=0.14$ m and $N_s=1.63$) and total
17 displacement ratio was 2% (Figure 9). From W5 ($H_{m0}=0.14$ m) to W7 ($H_{m0}=0.16$ m),
18 movements reached their maximum ratio of 37%. At W7, total displacement ratio
19 reached to 6%. W8 ($H_{m0}=0.17$ m and $N_s=1.98$) possessed notable wave conditions due
20 to wave-structure interaction under highly energetic waves when compared to the
21 previous wave series. Total displacement ratio became 20%, while total movement ratio
22 decreased to 29%. Beyond this condition, the variations of movement and displacement
23 ratios were quite low regarding to clamping strength between adjacent cubes. From W9
24 ($H_{m0}=0.18$ m) to W13 ($H_{m0}=0.21$ m), displacement ratio increased slightly. At W13, the
25 stability number was $N_s=2.44$. Total movement and total displacement ratios were found
26 to be 26% and 24%, respectively. At W13, wave height was considerably energetic
27 ($H_{m0}=0.21$ m; which is bigger than the characteristic wave height of 0.20 m), and wave
28 forces were quite strong on the armor units. Filter layer of the model breakwater was
29 never visible, and there was no displacement, yet movements were observed at the first
30 layer of ND (lower layer).

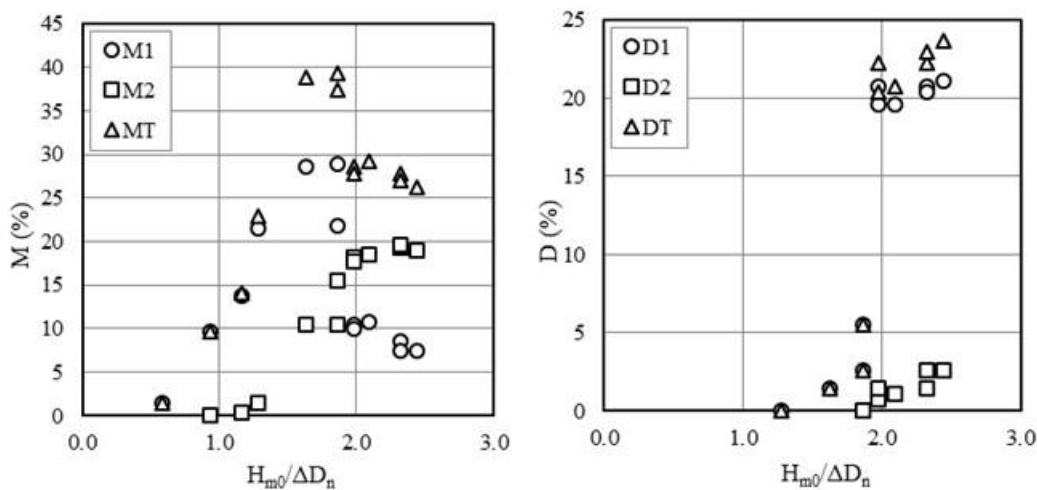


1
 2 Figure 8 Positions of the HD and ND cubes for the case1 (CID); First Layer (lower
 3 layer) ND and Second Layer (upper layer) HD (units are in cm).

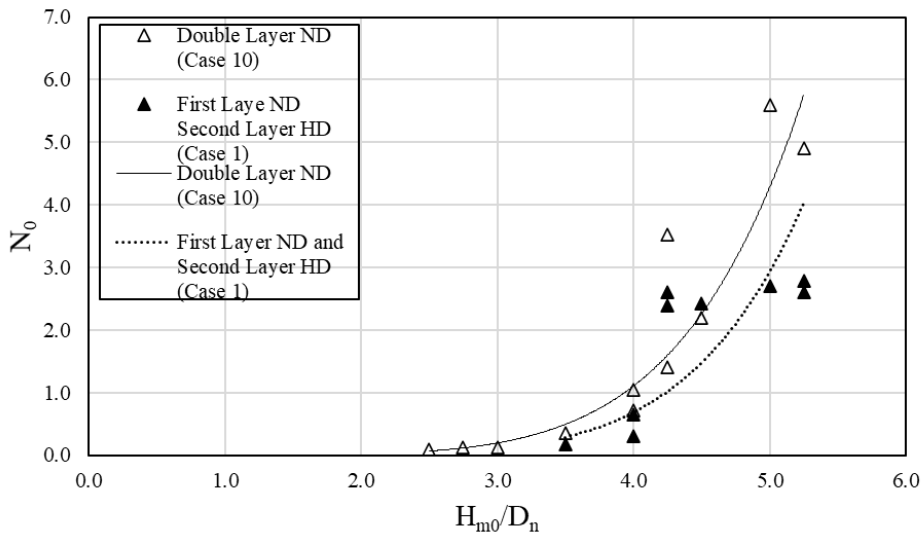
4 The movement of cubes in the first layer (lower layer) directly affected the stability of the
 5 second layer (upper layer) for this case. Visual observations showed that the first (lower)
 6 armor layer (ND) behaved quite different when compared to the second (upper) armor
 7 layer (HD). W8 was defined as a critical test series in relation to wave-structure
 8 interaction, this claim can be justified with the movement of ND cubes at the first (lower)
 9 layer triggered the HD cubes at the second (upper) layer and then caused to increase
 10 the displacement capability of the HD blocks. This resulted that the HD cubes at the
 11 reference area lost their connection with the ND cubes, and movements at the first layer
 12 considerably increased the instability of the HD cubes (Figure 9). However, after
 13 clamping adjacent armor units, the stability of the HD cubes increased again.
 14 Consequently, the HD cubes at the second (upper) layer did not show more
 15 displacements and the filter layer never became visible, even for beyond the
 16 characteristic wave condition (W13, $H_{m0}=0.21$ m). These HD cubes contributed to the
 17 stability of the ND cubes, even for significant wave loading.

18 In order to reveal the advantage of using HD cubes (Case 1) on the second layer, the
 19 results were compared with the results of two-layer ND cubes (Case 10) by considering
 20 the measured relative damage (N_0) versus the ratio of H_{m0}/D (Figure 10a). The relative
 21 damage (N_0) increases gradually for both cases, except for Case 1 where a sudden
 22 increment occurs due to the movement of ND units on the first layer triggered the HD
 23 units on the second layer at W8 and then continued slightly. On the other hand, at the
 24 end of the wave series, the relative damage is smaller for Case1 where N_0 corresponding
 25 to the ratio of H_{m0}/D of 5.0 is 2.7 and 5.6 for Case1 and Case10, respectively. Therefore,
 26 this outcome supports the idea that using HD cubes on the second layer provides more
 27 stability than that of the case using ND cubes, as it can be expected. On the other hand,

1 when the stability number (N_s) versus the relative damage (N_0) is drawn in Figure 10b
 2 including the measurement results obtained from Case 1 (filled triangles), Case 2
 3 (crosses), and Case 10 (open triangles) together with the calculation result of Van der
 4 Meer (1988) formula for normal density units (ND), the calculated stability numbers
 5 obtained for HD cube cases (Case 1 and 2) are found to be lower than that of ND cube
 6 case (Case 10). Figure 10b suggests that if only the upper layer consists of HD units
 7 (Case 1, filled triangles) or if only in the reference area HD units are used in the upper
 8 layer (Case 2, crosses), the stability is less than for a double layer of normal density units
 9 (Case 10, open triangles). However, this is partly because in Figure 10b the relative
 10 density Δ on the horizontal axis for Case 1 and Case 2 is the relative density of the high-
 11 density units while for Case 10 the relative density is for normal-density units.
 12 Nevertheless, the stability of the armor layers where a part of the armor layer consists of
 13 HD units, is less than the stability parameter would suggest. Figure 10 clearly shows that
 14 if HD units are used only in the upper layer of a reference area (Case 2: crosses) leads
 15 to more damage than if the entire upper layer consists of HD units (Case 1: filled
 16 triangles). Comparison between the Van der Meer (1988) formula and measurement
 17 results of two-layer ND units (Case 10) gave good agreement. If the stability parameter
 18 on the horizontal axis correctly accounts for the effects of high-density, the curve would
 19 be valid also for an armor layer of which both layers consist of HD units. Figure 10
 20 indicates that applying only HD in the upper layer (Case 1) or a part of the upper layer
 21 (Case 2) leads to more damage than if HD units are placed over the entire armor layer
 22 (curve).



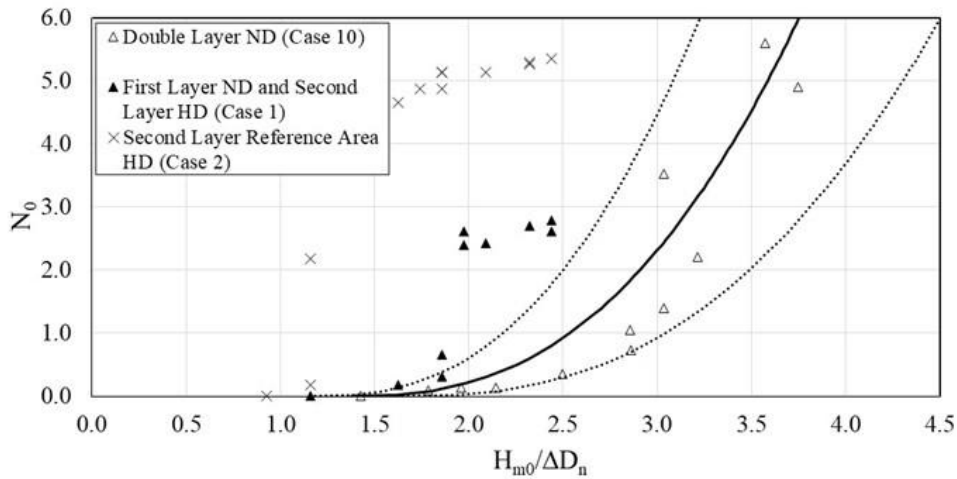
23
 24 Figure 9 Movement (left: M) and displacement (right: D) in the reference area for the
 25 (CID) First Layer ND Cubes and the Second (upper) Layer HD Cubes (the stability
 26 number based on HD).



1

2

(a)



3

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(b)

5 Figure 10 (a) Relative damage for Case 1 and Case 10 versus the ratio of H_{m0}/D_n (b)
 6 Relative damage for case 1 based on HD (filled triangles), case 2 based on HD
 7 (crosses) and case 10 based on ND (open triangles) together with the formula of Van
 8 der Meer (1988) for conventional cube armored breakwaters, where the solid line
 9 represents the result of formula itself and dashed lines show the confidence bands.

10 **(ii) Case 2: (CID) Reference area HD with irregular placement**

11 The cube arrangement together with the reference area is shown in Figure 11. The HD
 12 cubes were placed over the first (lower) layer of the ND cubes only from the 17th row
 13 which corresponds to “SWL- H_s equals to $5D_n$ ” to the second-row crest (i.e., only including
 14 first row). The ND cubes constituted the first (lower) layer and the second layer as they
 15 were from the 16th row (below SWL- $5D_n$) to the toe.

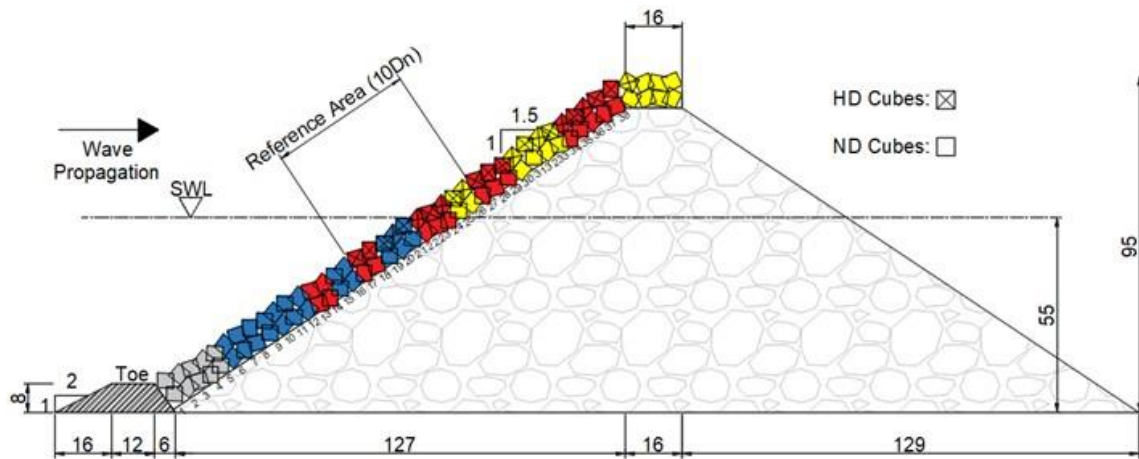


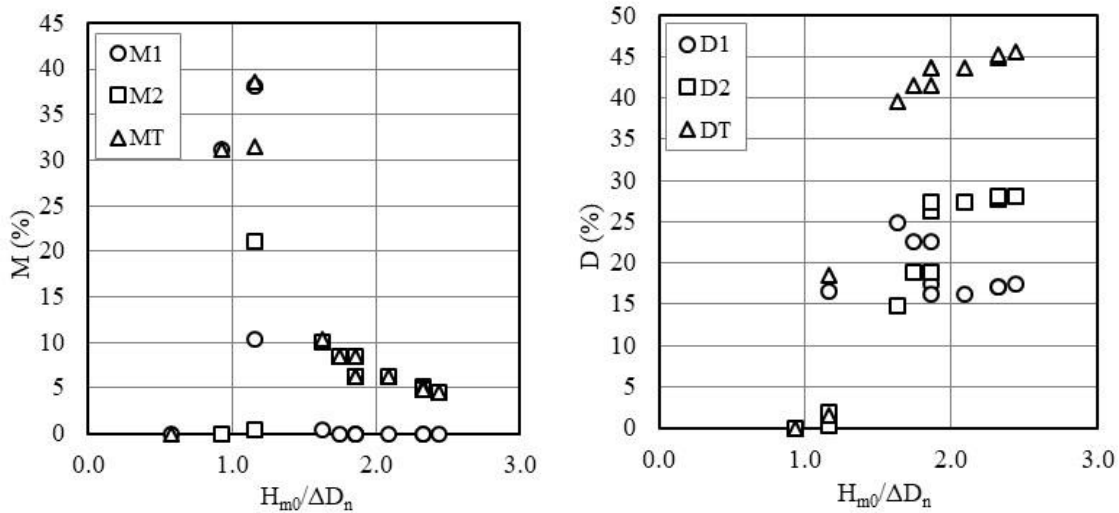
Figure 11 Positions of HD and ND cubes for the case; Reference Area HD Cubes (units are in cm).

In this experiment, although wave heights were low at W1 ($H_{m0}=0.05$ m and $N_s=0.58$) and at W2 ($H_{m0}=0.08$ m and $N_s=0.93$), movement ratio M_1 ($D_n < 0.5$) reached to 31% due to the rocking behavior of HD cubes. The number of the rocking cubes increased and reached to their maximum ratio of 38% ($H_{m0}=0.10$ m and $N_s=1.16$) and the first displacement was also observed at W3 (Figure 12). Total movement ratio and displacement ratio reached to 31%, and 18%, respectively with a sudden increase of W4 ($H_{m0}=0.10$ m and $N_s=1.16$). On the other hand, total movement ratio suddenly decreased to 10% at W5 ($H_{m0}=0.14$ m and $N_s=1.63$) and total displacement almost doubled and reached to 40%. Displacement ratio increased in a small amount from W6 ($H_{m0}=0.15$ m) to W13 ($H_{m0}=0.21$ m) because sliding occurred, and clamping strength increased over the lower slope. Filter layer became visible (close to the crest) through the armor layer at W13 ($H_{m0}=0.21$ m and $N_s=2.44$) because segregation occurred in the armor layer above the reference area due to sliding damage. Maximum displacement ratio was reached to 46% at W13. In this case, very large amount of movements occurred even for the lower stability numbers ($M < 30\%$) which was unacceptable.

It is necessary to elaborate the behavior of the model at W4 ($H_{m0}=0.10$ m) and at W5 ($H_{m0}=0.14$ m). Starting from W4 to the end of W5, "Sliding" behavior was observed. This behavior was also referred in CEM (2003). The high-density cubes in the second layer pushed the normal density cubes downwards due to their movements. Mostly normal density cubes lost their positions and dislocated to the toe of the structure.

26 (4 HD and 22 ND) dislocated cubes were observed at the toe of the structure after W13. Sliding damage also caused the packing density to increase below the reference area while the packing density above the lower limit of the reference area decreased.

1 As indicated before, Figure 10 shows the relative damage (N_0) obtained from the tests
 2 against the results calculated by the Van der Meer (1988) formula. The stability number
 3 (N_s) was calculated using the relative density of the HD cubes for Case 2. The stability
 4 number predicted by Van der Meer (1988) formula was much higher than that of Case 2
 5 because it does not consider the damage due to sliding.



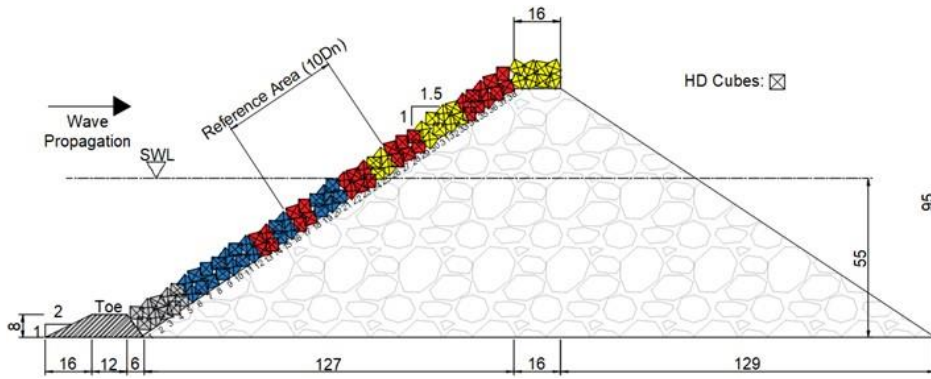
6
 7 Figure 12 Movement (left: M) and displacement (right; D) in the reference area for the
 8 Reference Area HD Cubes (the stability number based on HD).

9 **(iii) Case 3: (CRS) Double layer HD with irregular placement**

10 HD cubes were used in both of the first and second armor layers. Positioning of the HD
 11 cubes can be seen in Figure 13.

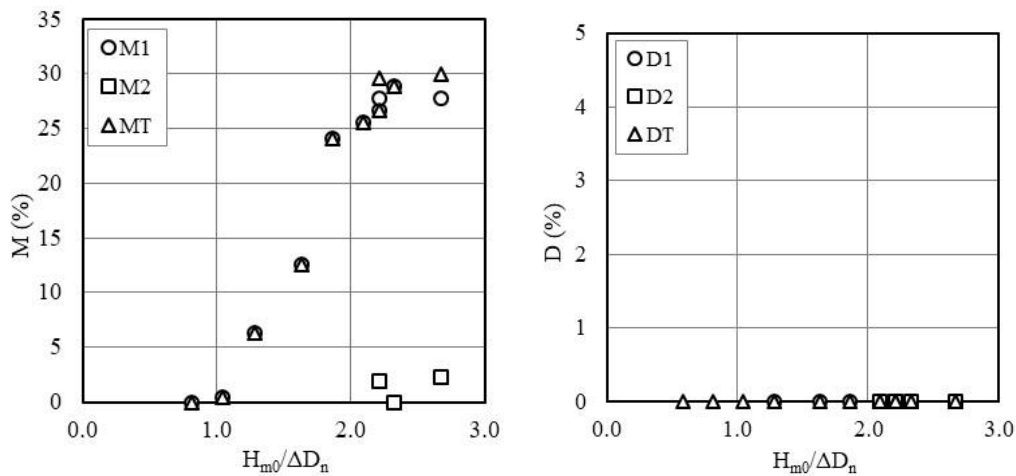
12 HD cubes were found to be stable, and displacement did not occur. However, the first
 13 movement started at W3 ($H_{m0}=0.09$ m) with the movement ratio of 0.4% and became 6%
 14 at W4 ($H_{m0}=0.11$ m). For W5 ($H_{m0}=0.14$ m) and W6 ($H_{m0}=0.16$ m), the movement ratios
 15 almost doubled and reached to 13% and 24%, respectively. From W7 ($H_{m0}=0.18$ m) to
 16 W11 ($H_{m0}=0.23$ m, which is beyond the characteristic wave height), movement ratio
 17 increased slightly and reached to 30% at W11. Only movement was observed under this
 18 test condition and there were no displacements (Figure 14). Using the applied high
 19 density in the stability number, the results indicate that the stability of the HD armor layer
 20 is more stable than the stability formula by Van der Meer (1988) suggests.

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Figure 13 Positions of the HD cubes for the case of Double Layer HD Cubes



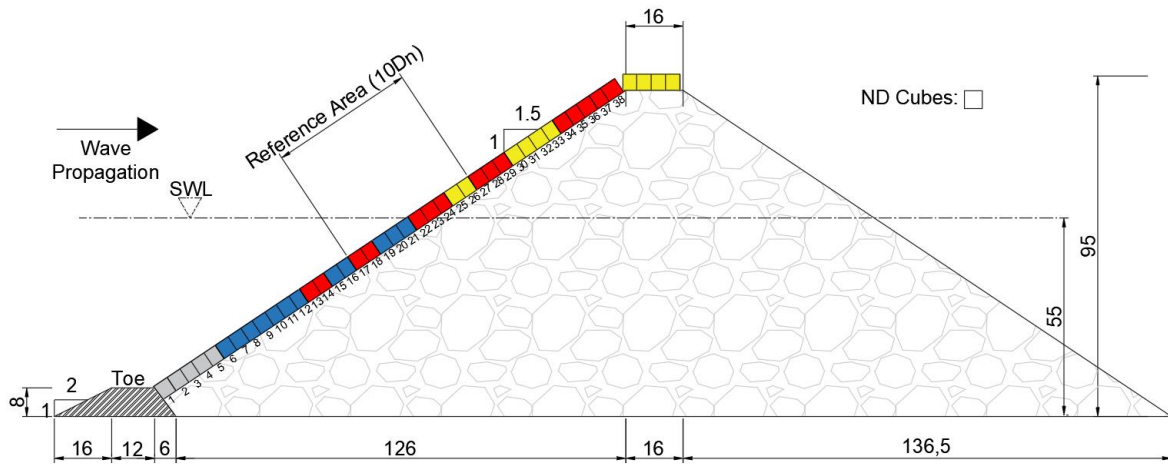
3

4 Figure 14 Movement (left: M) and displacement (right: D) in the reference area for the
5 case of Double Layer HD Cubes (the stability number based on HD).

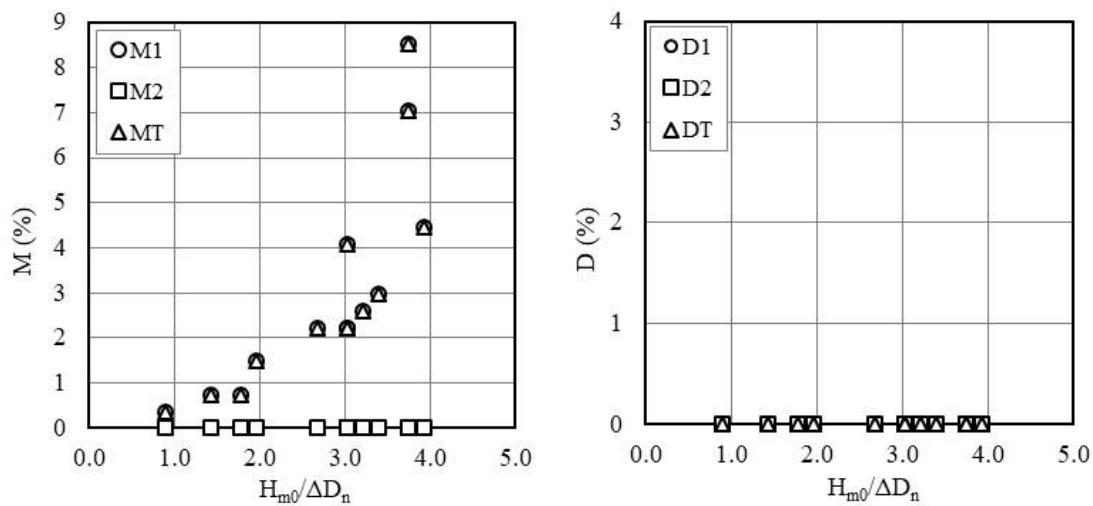
6 **(iv) Case 4: (CRS) Single layer ND cubes with regular placement**

7 Figure 15 shows the reference area and cube arrangement of the ND cubes over the
8 slope.

9 Displacement was not observed in the armor layer for this case (Figure 16). Only
10 movements occurred due to friction between adjacent armor units. Movement started at
11 W1 ($H_{m0}=0.05$ m) and the movement ratio was 3% at W8 ($H_{m0}=0.18$ m). Then, movement
12 gradually increased, and the ratio reached to 9% at W13 ($H_{m0}=0.21$ m and $N_s=3.75$)
13 which was the last wave. Only 23 cubes (9%) performed movement behavior (Figure
14 16). These cubes moved lower than $0.5D_n$ which means that “ $0.5D_n-1.0D_n$ ” movement
15 (M_2) was not observed.



1
2 Figure 15 Positions of the ND cubes for the experiment Single Layer ND Cubes with
3 Regular Placement



4
5 Figure 16 Movement (left: M) and displacement (right: D) in the Single Layer ND Cubes
6 with Regular Placement (the stability number based on ND).

7 **(v) Case 5: (CRS) Single layer HD cubes with regular placement**

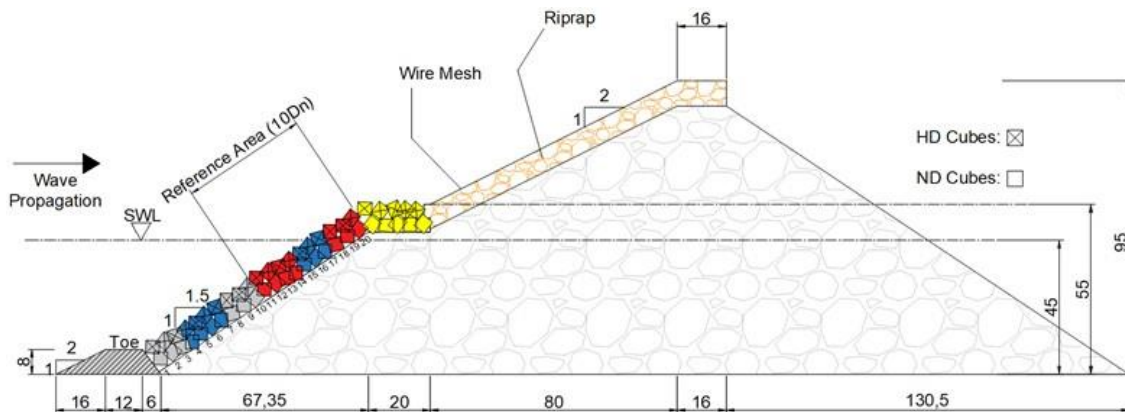
8 Figure 17 shows the reference area and cube arrangement of the HD cubes over the
9 slope.

10 Displacement was not observed in this experiment. Only movements occurred due to
11 friction between adjacent armor units (Figure 18). The movement started at W1
12 ($H_{m0}=0.05$ m), and the ratio became 2% at W5 ($H_{m0}=0.14$ m). Then, movement reached
13 its maximum ratio of 4% at W9 ($H_{m0}=0.19$ m). From W9 ($H_{m0}=0.19$ m) to W13 ($H_{m0}=0.21$
14 m), neither movement nor displacement occurred. At the end, only 10 cubes (4%)
15 performed movement behavior and these cubes moved lower than $0.5D_n$. Therefore, M_2
16 was not observed throughout the experiment.

1 emerged berm where HD cube units in this case did not cover entire second layer but
 2 used only on the first and second layer of the reference area and on the first two rows of
 3 the berm. For all experiments, the upper slope was fixed as mentioned in Section 2.
 4 Arrangements of both ND and HD cubes are given in Figure 7 for the berm type
 5 breakwater.

6 **(i) Case 6: (BID) Emerged berm with irregular placement**

7 The reference area and cube arrangements can be seen in Figure 19 for this case. For
 8 low wave height at W1 ($H_{m0}=0.05$ m), only M_1 ($<0.5D_n$) movement was observed. At W2
 9 ($H_{m0}=0.08$ m), rocking movements were dominant, and the movement ratio was 16%.
 10 From $H_{m0}=0.11$ (W3) m to $H_{m0}=0.12$ m (W4), M_2 type movements started, and M_T
 11 reached to 42%. This wave was the last wave condition without displacement (Figure
 12 20). At W5 ($H_{m0}=0.14$ m and $N_s=1.63$) the first displacements occurred (Figure 20). The
 13 displacement ratio was 1% for this wave condition. Until the end of the wave series of
 14 W6 ($H_{m0}=0.15$ m), the displacement ratio was constant, but total movement ratio
 15 changed and reached to its maximum value of 49%. At W7 ($H_{m0}=0.15$ m) displacements
 16 started again and the ratio reached to 2%. At W9 ($H_{m0}=0.16$ m) displacements kept
 17 increased to the end of the series and the displacement ratio became 3% and reached
 18 to 6% at W11 ($H_{m0}=0.18$ m).

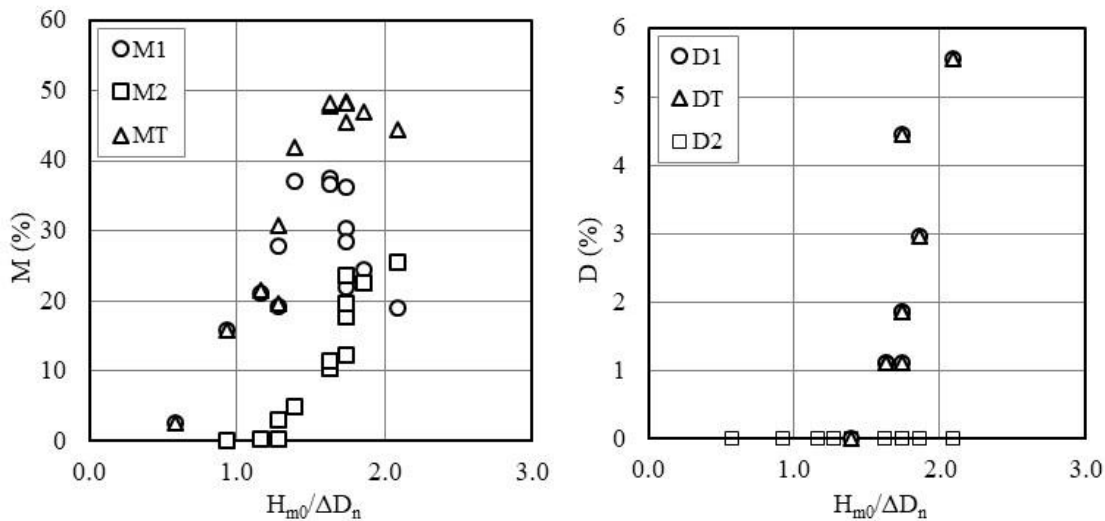


19
 20 Figure 19 Positions of the HD and ND cubes for the experiment Emerged Berm

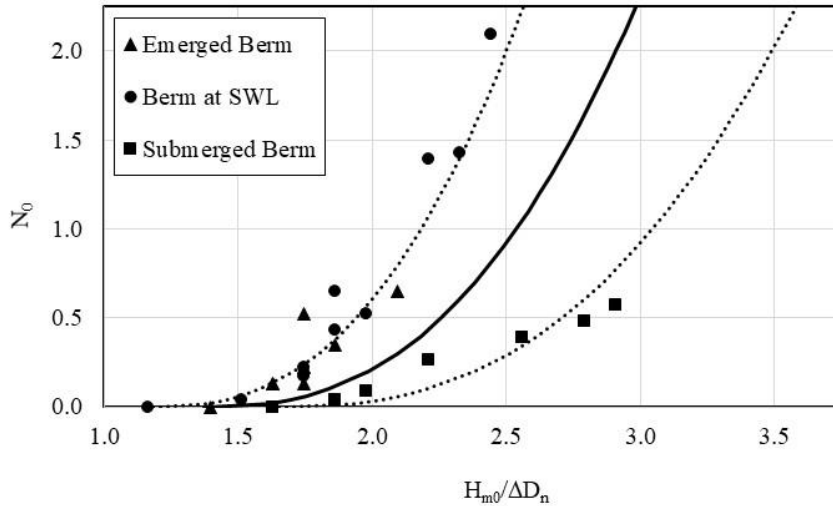
21 One of the most important observations in this experiment was that no sudden damage
 22 was declared. Most of the damage was observed in the upper rows of the reference area.
 23 Lower rows behaved more stable when compared to upper rows in the reference area.
 24 At the end of the experiment, the lower slope preserved its stability and core layer never
 25 became visible through the armor layer, and no cubes dislocated to the toe of the
 26 structure.

1 Stability number (N_s) versus relative damage (N_0) values were drawn and they are
 2 presented in Figure 21 including the results of the first three cases (emerged, at SWL,
 3 and submerged berm) with the Van der Meer (1988) formula for conventional breakwater
 4 cross-section consisted of ND cube units. The results for this case where the berm was
 5 emerged seemed to be compatible with the lower confidence band of the Van der Meer
 6 (1988) formula.

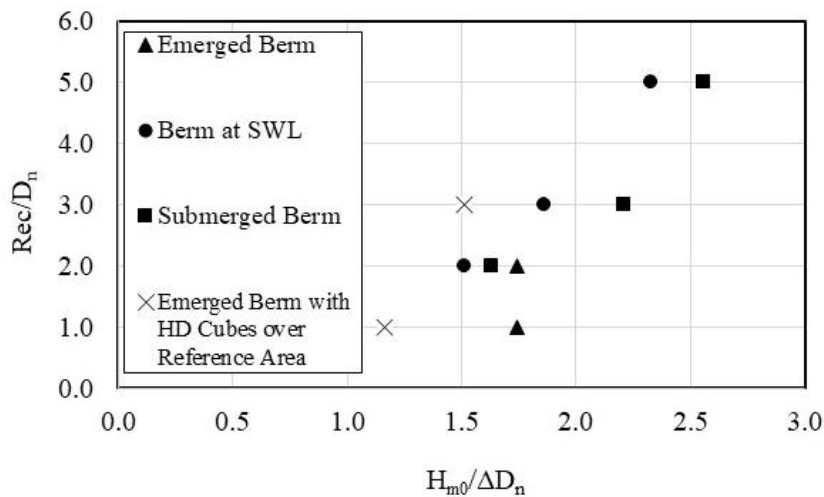
7 Figure 22 represents the results of dimensionless recession including the first three
 8 cases. For this case, from W1 ($H_{m0}=0.05$ m) to W7 ($H_{m0}=0.15$ m), there were no
 9 displacements in the berm. At W7 ($H_{m0}=0.15$ and $N_s=1.74$), the first displacement was
 10 observed in the 1st row of the berm, close to water side. In other words, recession started
 11 at the 1st row of the berm. At W9 ($H_{m0}=0.16$ m), there was no additional displaced cube
 12 observed. Only, 5 cubes dislocated from berm to lower slope.



13
 14 Figure 20 Movement (left: M) and displacement (right: D) in the lower layer HD Cubes
 15 with irregular placement for emerged berm case (the stability number based on HD).



1
 2 Figure 21 Relative damage for the emerged berm (Case 6), berm at SWL (Case 7) and
 3 submerged berm (Case 8) with the formula by the Van der Meer (1988) for
 4 conventional cube armored breakwaters using ND cubes where solid line indicates the
 5 Van der Meer (1988) formula and dashed lines show the confidence bands.



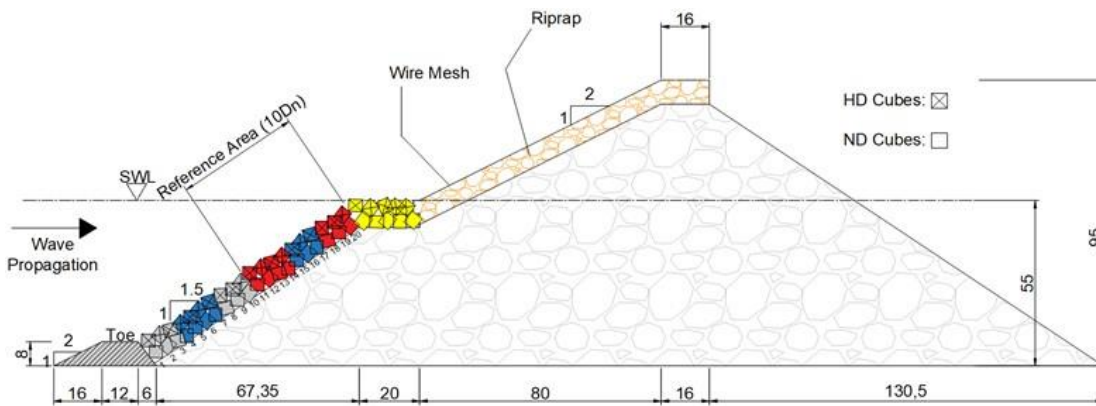
6
 7 Figure 22 Stability number (N_s) and dimensionless recession (Rec) for berm (case 6-7-
 8 8) with the HD cubes (the stability number based on HD).

9 **(ii) Case 7: (BID) Berm at SWL with irregular placement**

10 The reference area and cube arrangements can be seen in Figure 23 for this case. There
 11 was no movement at W1 ($H_{m0}=0.05$ m) in the lower slope. The first movements were
 12 observed at W2 ($H_{m0}=0.08$ m). After that, no additional movements occurred at W3
 13 ($H_{m0}=0.09$ m). At W4 ($H_{m0}=0.10$ m and $N_s=1.16$), the total movement ratio became 8%,
 14 and both M_1 and M_2 type movements were observed (Figure 24). W5 ($H_{m0}=0.13$ m and
 15 $N_s=1.51$) was one of the most important wave series because the first displacement
 16 occurred in this wave condition (Figure 24). From W6 ($H_{m0}=0.15$ m) to W10 ($H_{m0}=0.16$

1 m), total movement and displacement ratios increased gradually. At W10 ($H_{m0}=0.17$ m
 2 and $N_s=1.98$) total movement and displacement ratios became 42% and 5%,
 3 respectively. In addition, 42% was the highest total movement ratio for this experiment.
 4 After this wave, the movement ratio decreased gradually. At W11 ($H_{m0}=0.19$ m and
 5 $N_s=2.21$) the displacement ratio almost doubled and reached to 12%. After W11, total
 6 displacement ratio increased and reached to its maximum ratio of 18%, at W13
 7 ($H_{m0}=0.21$ m and $N_s=2.44$ which is beyond the characteristic wave).

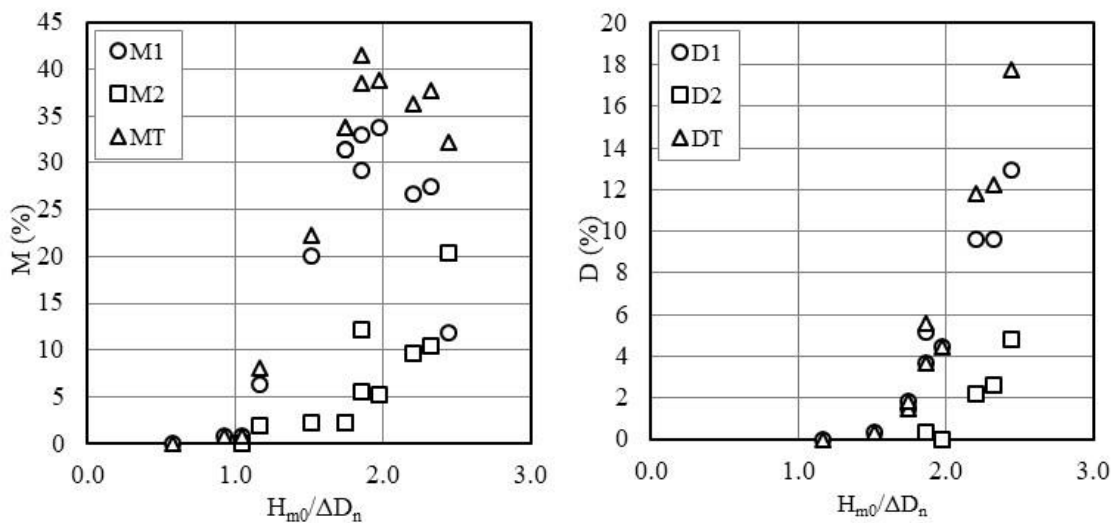
8 Flume observations showed that lower slope stability was affected by the berm
 9 recession. Wave run-down forces were substantially influential on some displaced cubes
 10 in the first row of the berm. Thereby, some cubes in the lower slope lost their stability
 11 due to these displaced cubes at the berm, while HD cubes kept ND cubes as stable as
 12 possible and only one dislocated HD cube was observed at the toe of the structure.



13

14

Figure 23 Positions of the HD and ND cubes for the experiment Berm at SWL



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Figure 24 Movement (left: M) and displacement (right: D) in the lower layer HD Cubes with irregular placement for berm at SWL (the stability number based on HD).

1 The results of the dimensionless recession number for this case were given in Figure 22.
2 From W1 ($H_{m0}=0.05$ m) to W4 ($H_{m0}=0.10$ m), there was no displacement at the berm. At
3 W5 ($H_{m0}=0.13$ m and $N_s=1.51$), first displacement occurred at the 2nd row and
4 movements were observed for other cubes close to the water side. From W6 ($H_{m0}=0.15$
5 m) to W10 ($H_{m0}=0.16$ m), displacements occurred at both 1st row and 2nd row of the berm,
6 but recession was still at the 2nd row. At W10 ($H_{m0}=0.17$ m and $N_s=1.98$), recession
7 started at 3rd row of the second layer of berm. At W11 ($H_{m0}=0.19$ m and $N_s=2.21$), new
8 displacements were observed but these displaced cubes were at the first three rows.
9 Thus, recession was still in the 3rd row. W12 ($H_{m0}=0.20$ m and $N_s=2.33$) was the first
10 wave series that recession reached to the 5th row at the second layer, total number of
11 displaced cubes reached to 18. At the last wave series of this case, W13 ($H_{m0}=0.21$ m
12 and $N_s=2.44$, beyond characteristic wave), 12 more cubes displaced, and the total
13 displacements reached to 30. Since the berm level was at SWL, it was strongly affected
14 by the wave forces.

15 **(iii) Case 8: (BID) Submerged berm with irregular placement**

16 The reference area and cube arrangements can be seen in Figure 25 for this case. Water
17 depth was 65 cm. The stability number versus the movement and displacement ratios
18 are given in Figure 26. There was no movement for the first two wave series, at W1
19 ($H_{m0}=0.05$ m) and at W2 ($H_{m0}=0.07$ m). Movements started at W3 ($H_{m0}=0.09$ m) with the
20 ratio of 3%. From W4 ($H_{m0}=0.08$ m) to W7 ($H_{m0}=0.14$ m), displacement was not observed,
21 but total movement ratio reached to 37%. Visual observations showed that wave forces
22 acting on lower slope was relatively low at waves from W1 ($H_{m0}=0.05$ m) to W7 ($H_{m0}=0.14$
23 m). However, at W8 ($H_{m0}=0.16$ m and $N_s=1.86$), wave forces were slightly greater than
24 the previous wave. The first displacement occurred in this wave series (Figure 26).
25 Displacement ratio increased to 0.7% at W9 ($H_{m0}=0.17$ m).

26 Starting from W3 ($H_{m0}=0.09$ m), rocking (M_1) was observed significantly in the lower
27 slope. It reached to its maximum ratio at W11 ($H_{m0}=0.22$ m which is beyond the
28 characteristic wave) with 39%. Also, total movement M_T reached to its maximum ratio at
29 W12 ($H_{m0}=0.24$ m) with 46%. From W10 ($H_{m0}=0.19$ m and $N_s=2.21$) to W13 ($H_{m0}=0.25$
30 m and $N_s=2.91$), the displacement ratio increased as well, but this increment was
31 gradual. At W13 ($H_{m0}=0.25$ m), total displacement at lower slope was 5%. Therefore,
32 movements were dominant in the lower slope. Most of the wave forces were found to be
33 more effective on the upper slope of the breakwater. However, run-down forces were
34 effective in the lower slope significantly for the high energetic waves.

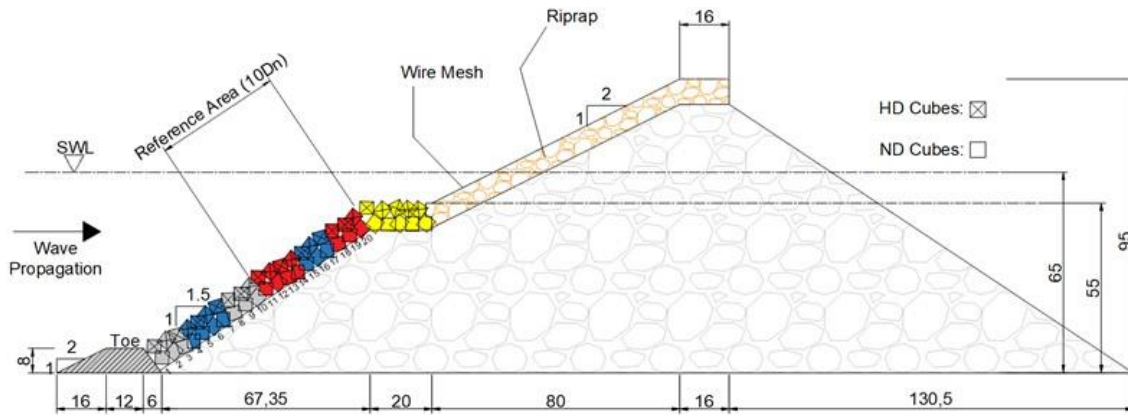


Figure 25 Positions of the HD and ND cubes for the Submerged Berm case

The relative damage (N_0) results against to the stability number (N_s) values obtained for this case can be seen in Figure 21. The comparison between the case results and the Van der Meer (1988) formula showed that the experimental results were mostly consistent with the upper confidence band of the formula. This indicates that applying the formula for the tested case with the berm at the still water level provides an underestimate of the actual damage.

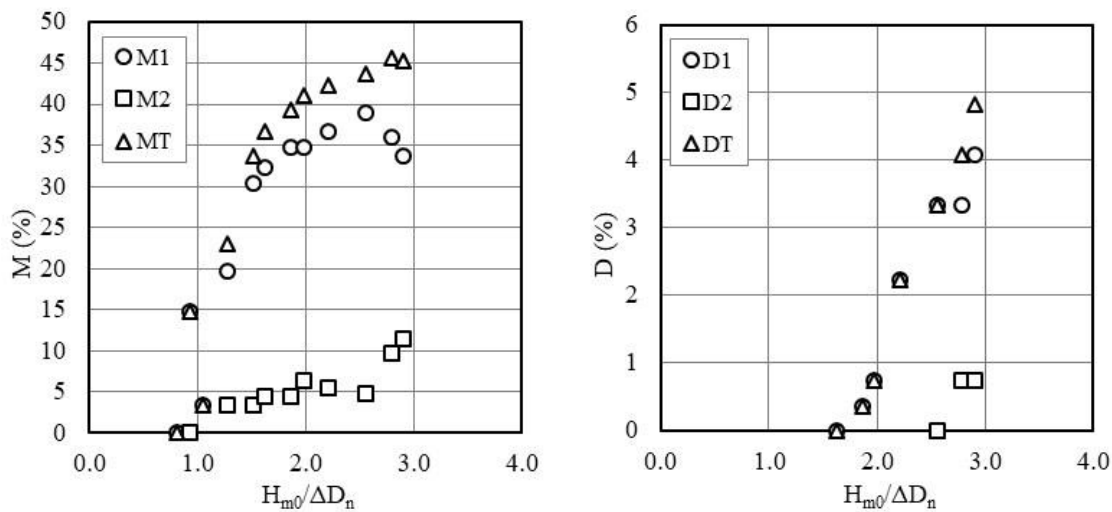


Figure 26 Movement (left: M) and displacement (right: D) in the lower layer HD Cubes with irregular placement for submerged berm (the stability number based on HD).

The dimensionless recession number results for this case are given in Figure 22. From W1 ($H_{m0}=0.05$ m) to W6 ($H_{m0}=0.13$ m), there was no displacement in the berm, but movements were detected at the berm as M_1 and M_2 . At W7 ($H_{m0}=0.14$ m and $N_s=1.63$) recession started at the 2nd row of the berm with one cube. At W8 ($H_{m0}=0.16$ m) and W9 ($H_{m0}=0.17$ m) additional displacements were observed but these displaced cubes were at the 1st and 2nd row of the berm. Thus, recession was still at the 2nd row. Also, at W8 ($H_{m0}=0.16$ m) and W9 ($H_{m0}=0.17$ m), wave interaction between the berm and the lower

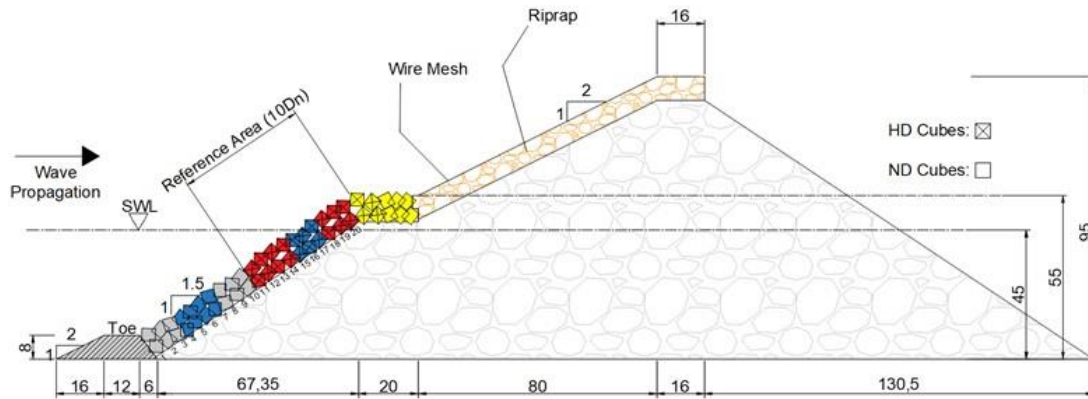
1 slope increased because run-down wave forces started to be influential on the berm. At
2 W10 ($H_{m0}=0.19$ m and $N_s=2.21$), additional displacements occurred at the berm, and
3 recession reached to the 3rd row. W11 ($H_{m0}=0.22$ m and $N_s=2.56$) was the first wave
4 series that recession reached to the 5th row of the berm. Additional displacements
5 occurred at the 4th row as well. Run-down forces were effective on the berm. For W12
6 ($H_{m0}=0.24$ m) and W13 ($H_{m0}=0.25$ m), additional displacements were detected at the
7 berm. At W13 ($H_{m0}=0.25$ m and $N_s=2.91$), total number of displaced cubes in the berm
8 were 30 which corresponds to the ratio of 22%. All displaced cubes were from the second
9 (upper) layer of the berm, yet the berm shape was not deformed throughout the
10 experiment. Eight of those total displaced cubes dislocated from the berm to the lower
11 slope.

12 **(iv) Case 9: (BID) Emerged berm with HD cubes over reference area with irregular** 13 **placement**

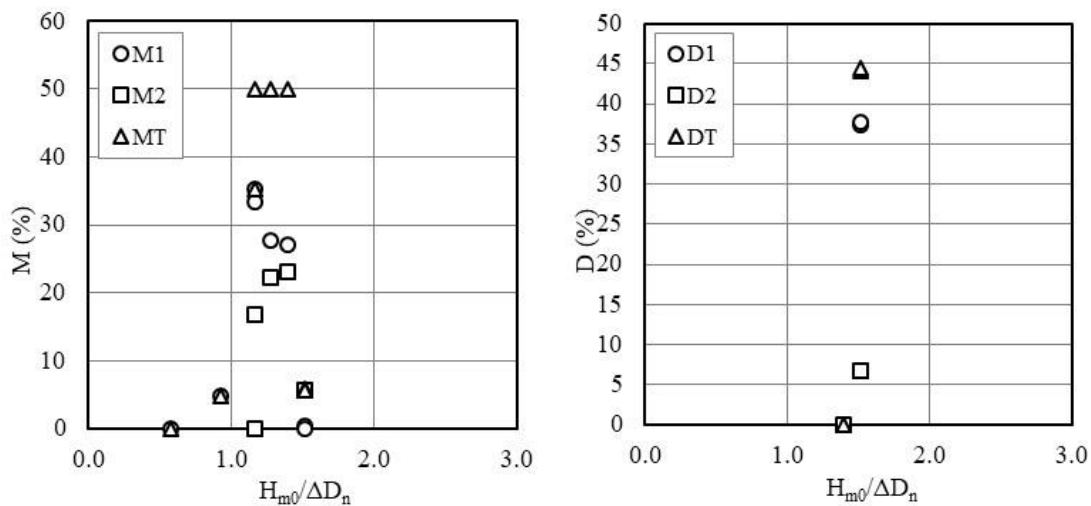
14 Arrangements of the HD and ND cubes are shown in Figure 27. Figure 28 depicts that
15 there were no movements against the first wave, W1 ($H_{m0}=0.05$ m). Rocking started at
16 W2 ($H_{m0}=0.08$ m), and the movement ratio was 5%, and then increased to its maximum
17 value of 35% at W3 ($H_{m0}=0.10$ m). It should be noted that, only rocking (M_1) occurred in
18 these wave series. After W3 ($H_{m0}=0.10$ m and $N_s=1.16$), rocking ratio decreased, but M_2
19 movement started to initiate, and the ratio reached to 17%. After W4 ($H_{m0}=0.11$ m), total
20 movement ratio was 50%, which was half of the considered cubes in the reference area.
21 After W4 ($H_{m0}=0.11$ m) M_1 ratio (rocking ratio) decreased and M_2 ratio increased, but
22 total movement ratio M_T was constant at 50% (maximum M_T). At W5 ($H_{m0}=0.13$ m and
23 $N_s=1.51$), M_T suddenly decreased to 6% and first displacement occurred in this wave
24 condition with the ratio of 37% (Figure 28), because “Sliding” behavior was detected in
25 the lower slope of the model breakwater. This behavior changed the packing density of
26 the breakwater. Packing density decreased at the top of the reference area, while it
27 increased significantly at the lower part of the reference area. Hence, neither
28 displacement nor movement was observed remarkably on underside of the lower slope
29 after the W5 wave series ($H_{m0}=0.13$ m).

30 In this case, a very large amount of movement occurred even for the lower stability
31 numbers ($M>30\%$), which was unacceptable. The amount of displacements was also
32 very large for $N_s>1.5$. The behavior of the HD cubes in the reference area is very similar
33 to Case 2 for the conventional breakwater.

1 Remarkable movements and then sliding behavior in the lower slope were observed, that
 2 were affected by the recession on the berm. The lower slope armor layer showed
 3 significant damage, but the core layer was never visible.



4
 5 Figure 27 Positions of the HD and ND cubes for the case of Emerged Berm with HD
 6 Cubes over Reference Area



7
 8 Figure 28 Movement (left: M) and displacement (right: D) in the lower layer HD Cubes
 9 over the reference area with irregular placement for emerged berm (the stability
 10 number based on HD).

11 The dimensionless recession number results of this case are presented in Figure 22.
 12 Recession was not observed for waves W1 ($H_{m0}=0.05$ m), W2 ($H_{m0}=0.08$ m) and W3
 13 ($H_{m0}=0.10$ m). Only M_1 (rocking) movements were observed at W3. Displacements at
 14 berm started at W4 ($H_{m0}=0.11$ m and $N_s=1.28$) at the 1st row and then remained constant
 15 until the end of W5 ($H_{m0}=0.13$ m). At W5 ($H_{m0}=0.13$ m and $N_s=1.51$), another 10
 16 displacements occurred on the berm ("Sliding" behavior occurred in the lower slope at
 17 this wave) and recession began at the 3rd row. Fourteen cubes were displaced from the
 18 berm to the lower slope.

1 **5. DISCUSSION**

2 The detailed discussion was made separately for conventional and berm type
3 breakwaters given in the followings.

4 **(i) Conventional Breakwaters**

5 The damage initiation parameters are presented in Table 3 for all cases conducted for
6 conventional breakwaters. To reveal the advantage of using HD units can be made by a
7 comparison between Case 3 (double layer HD) and Case 10 (double layer (ND)). Double
8 layer HD cubes of Case 3 has a stability number larger than 2.67 obtained at W11 with
9 $H_s=0.23\text{m}$, while it was 1.79 at W3 with $H_s=0.10\text{m}$ for Case 10.

10 As for single layer cases of HD (Case 5) and ND cubes (Case 4), the stability number of
11 ND cubes were larger than for HD cubes at the same wave condition of W3. However,
12 when the amount of the movement ratios was checked for each case, they were 4% and
13 9% for HD and ND cubes, respectively. It should be noted that there was no displacement
14 observed for the Case 3, 4 and 5.

15 Similarly, the comparison between “Case 1 and Case 10” and “Case 2 and Case 10” can
16 be made through the results presented in Table 3 and Figure 10. The damage initiation
17 was started at W5 for Case 1, while it was at W3 for Case 10, although the stability
18 number N_s was 9% lower for HD cubes than for the ND cubes. On the other hand, the
19 observations showed that the first (lower) layer of ND cubes triggered the second armor
20 layer (HD) and increased the displacement capability of the HD units. This is also why
21 the damage was larger for the Case 1 than for the Case 3 where the armor layers entirely
22 consisted of HD cubes. Besides, the stability number N_s corresponding to the damage
23 initiation in the Case 3 was more than 1.5 times of the Case 1.

24 When the Case 2 and Case 10 are compared, both has the damage initiation at the same
25 wave condition of W3 with $H_s=0.10\text{m}$ and the stability number of HD cubes is lower than
26 that of ND cubes. Case 2 found to be less stable can be observed in Figure 10 that the
27 results shifted more to the left comparing to the Case 1 due to the involvement of sliding
28 behavior and so the relative damage of the Case 2 was about twice as much of the Case
29 1.

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1 Table 3 Properties of the damage initiation of cube armored conventional breakwaters

Experiment	Case	Wave series	H_{m0} (m)	N_s
First Layer ND Cubes and Second Layer HD Cubes	1	W5	0.14	1.63
Reference Area Double Layer HD Cubes	2	W3	0.10	1.16
Double Layer HD Cubes	3	W11	0.23	>2.67
Single Layer ND Cubes	4	W13	0.21	>3.75
Single Layer HD Cubes	5	W13	0.21	>2.44
Double Layer ND Cubes	10	W3	0.10	1.79

2

3 When all the results were evaluated through observations, HD cubes in general showed
 4 more stable behavior than ND cubes except for the Case 2 due to the sliding event.
 5 Comparing Case 3 (HD) with Case 10 (ND) showed that the HD cubes are clearly more
 6 stable than the ND cubes (damage starts at $N_s > 2.67$ versus 1.79). If the stability number
 7 N_s would account for the effects of the relative density, these values should have been
 8 similar. Since they are not the same, the stability number N_s does not seem to account
 9 for all effects of the density. That is also why the experimental results of HD cubes did
 10 not match with the Van der Meer (1988) formula which gave good agreement with the
 11 ND cubes results.

12 Van Gent et al. (2001) indicated that criteria for “failure of the top layer” cannot be taken
 13 equal for single and double top layers since for double top layers reserve much more
 14 stability. They suggested that $N_0 = 2.0$ was used to indicate the failure of double top layers,
 15 while it was 0.2 for single top layers. Moreover, Vieira et al. (2021) on the other hand
 16 proposed a threshold relative damage of $N_0 = 0.1$ for single top layers due to taking the
 17 direct wave attack on the filter through the leaving gap into consideration. For this study
 18 there were no displacements occurred for both single layer of HD and ND cubes and for
 19 double layer of HD cubes and it was not possible to reach to the threshold stability that
 20 corresponds to the displaced units of one diameter width owing to the limitations of the
 21 model dimensions, wave generation capacity and water depth at the toe of the structure
 22 preventing of larger waves. However, the obtained results showed that single layers
 23 (case 4 and 5) were more stable than that of double layers when HD (single/double layer)
 24 and ND (single/double layer) cube cases were compared to each other. As it can be seen
 25 from Table 3, the damage initiation started at an earlier wave series for double layer
 26 cases (Case 3 and 10). This can be explained by the strength of single layers that is a
 27 combination of the strength due to weight (also valid for double layers), the strength due
 28 to contact forces between the adjacent blocks (as for placed block revetments) and less
 29 wave attack on single units due to smoother surface of the entire slope. Triemstra (2000)

1 also indicated that the stability of elements on the slope was largely influenced by the
2 “laying roughness” of the elements and the “laying roughness” of the elements was
3 affected by placing method as well as density. This statement also supports the reason
4 why the single layer as being more stable than that of double layer.

5 **(ii) Berm type breakwaters**

6 Table 4 reveals the damage initiation parameters at the lower slope. The current
7 experiments were tested at 0.45 m (emerged berm), 0.55 m (at SWL), and 0.65 m
8 (submerged berm) water depths using irregular placement method for the berm width of
9 $5D_n$. Results of the HD cubes experiments were also compared with results of berm type
10 breakwaters consisted of ND cubes only conducted by Yuksel et al. (2020).

11 Figure 29 shows comparison of the HD between ND cubes for berm type breakwaters.
12 It can be seen that displacements started early for berm at SWL similar to ND, but
13 displacements started at higher stability numbers for the submerged berm. More
14 displacements were observed in berms at SWL, and less displacements occurred for
15 submerged berms. The initiation of the displacement found at the higher wave condition
16 for all berm levels with HD cubes than the ND cubes.

17 Although the HD cubes were used at the second (upper) layer of the armor layer, the
18 results of presented experiments for berm type breakwaters were found to be compatible
19 with the Van der Meer formula (Figure 29). Figure 30 represents measured stability
20 number versus predicted stability number for berm type breakwaters. The predicted
21 stability number was calculated based on Yuksel et al. (2020). Based on the physical
22 model tests in Yuksel et al. (2020), prediction method was derived for the stability of the
23 lower slope for ND cubes and their prediction method offered a reduction in cube size.
24 An empirical formula was described to determine the required cube size for each berm
25 level where the berm emerged, at SWL and submerged in their study. In order to account
26 for the influence of the berm on the lower slope with cubes, the reduction factors related
27 to the width of the berm, the position of the berm and the wave steepness were
28 considered. Good agreement between the measured and predicted stability parameters
29 using Yuksel et al. (2020) formula was obtained for all berm levels in Figure 30.

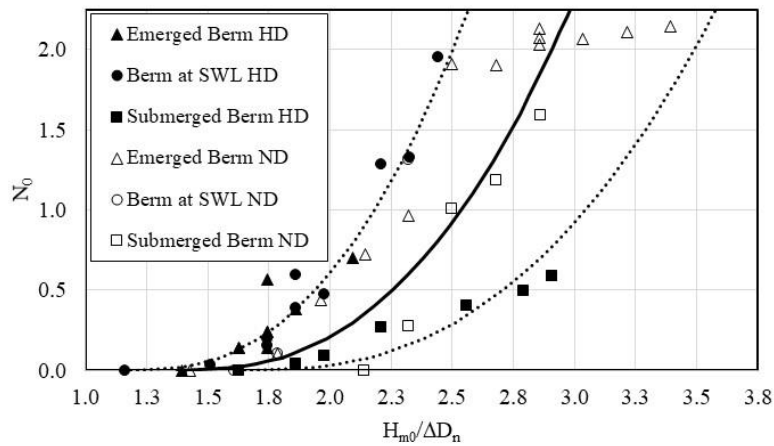
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Table 4 Properties of damage initiation parameters of the lower slope

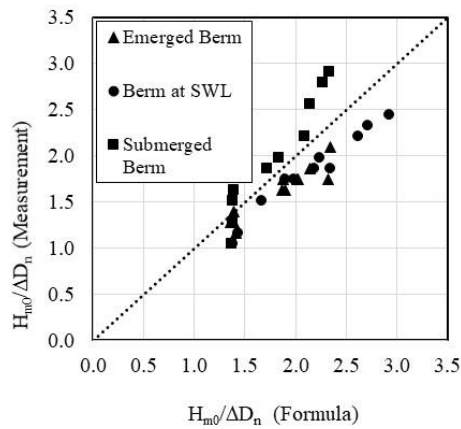
Experiment	Wave	H_{m0} (m)	N_s	N_s
			(Measurement)	(Yuksel et al., 2020)
Emerged Berm (▲)	W5	0.14	1.63	1.87
Berm at SWL (●)	W5	0.13	1.51	1.66
Submerged Berm (■)	W8	0.16	1.86	1.71
Emerged Berm with HD Cubes over Reference Area (x)	W5	0.13	1.51	N.A.
Emerged Berm* (△)	W3	0.10	1.79	1.82
Berm at SWL* (○)	W4	0.10	1.79	1.91
Submerged Berm* (□)	W6	0.13	2.32	2.03

2



3

4 Figure 29 Comparison for experimental results of berm type breakwaters for HD and
 5 ND cubes with the Van der Meer (1988) formula for conventional cube armored
 6 breakwaters



7

8 Figure 30 Measured stability number against predicted stability number using Yuksel et
 9 al., (2020) formula

1 7. CONCLUSIONS

2 The main purpose of this study was to provide insight into the performance of armor
3 layers that consist of high-density cubes by analyzing effects of using different concrete
4 densities of cubes and different placement methods. To determine the influence of
5 different densities and different placement methods, conventional and berm type
6 breakwater sections were modelled in a wave flume. Different configurations were
7 considered for each type of breakwater cross-section by using normal (ND) and high-
8 density cubes (HD) in single or double layers with regular or irregular placements.

9 The tests conducted for conventional breakwater cross-sections show that the armor
10 layers with a first (lower) layer of ND cubes and a second (upper) layer of HD cubes
11 (Case 1) are more stable than that of a traditional double layer of ND cubes (Case 10).
12 On the other hand, the observations showed that the first (lower) layer of ND cubes
13 triggered the second armor layer (HD) and increased the displacement capability of the
14 HD units. This is also caused by the damage being larger for the case 1 than for the case
15 3 where the armor layers entirely consisted of HD cubes. Moreover, the stability number
16 N_s corresponding to the relative damage initiation was more than 1.5 times higher for
17 case 3 than for Case 1. This result meets the expectations that the stability of two layers
18 of HD cubes is better than if HD cubes are only used in the upper layer.

19 The stability number for structures with only HD cubes in a reference area around the
20 still water level were found to be lower compared to the other cases with HD cubes due
21 to the sliding of HD cubes.

22 Only movement behavior was observed for the cases of the single layer with regularly
23 placement of HD and ND cubes and there were no displacements or extractions
24 occurred. Both breakwater models maintained their stability throughout the experiments.
25 The amount of movements during the experiments with single layer of ND cubes (Case
26 4) was higher than that of the single layer of HD cubes (Case 5). The HD cubes in a
27 single layer having relatively better performance and allowing for higher characteristic
28 wave conditions might make it preferable due to the consideration of a potential
29 increment of wave conditions in the future caused by the climate change.

30 All in all, HD cubes in general showed more stable behavior than ND cubes except for
31 the case 2 due to the sliding. However, the stability numbers evaluated by the equation
32 that is derived for ND cubes seemed not to represent the observed performance of HD
33 cubes, not if HD cubes are only used in a part of the armour layer but also not if HD
34 cubes are placed in the entire armour layer. The results show that using the current

1 stability number N_s in a stability formula that has been derived for ND cubes, is not
2 necessarily convenient for HD cubes.

3 The berm type breakwater cases were investigated for different berm levels and the
4 cross-sections were created by ND cubes on the first layer and HD cubes on the second
5 layer. These cases were compared with the previous study of Yuksel et al. (2020) where
6 the same configurations were studied, but only with ND cubes. For all berm types it was
7 found that the HD cubes used on the second layer of the lower slope and berm were
8 more stable than that of the berm type breakwaters with the ND cubes.

9 In conclusion, HD concrete cubes were found to be more stable than ND cubes. HD
10 cubes in a design would provide economic efficiency with a significant decrease of
11 concrete volume compared to ND cubes. In the present test program, the characteristic
12 wave height for the HD cubes was approximately a factor 1.5 higher than for normal
13 density cubes.

14 *Recommendations*

15 The analysis was limited to the data obtained in the experiments carried out in this study.
16 It is recommended to carry out additional testing for different densities and concrete block
17 geometries.

18

19 **Acknowledgement**

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1 **Appendix-** Wave series with wave heights and corresponding N_s values for ND and HD cubes in the experiments.

Case 1: First Layer ND - Second Layer HD (Conventional Type)			Case 2: Reference Area HD with Irregular Placement (Conventional Type)			Case 3: Double Layer HD with Irregular Placement (Conventional Type)			Case 4: Single Layer ND with Regular Placement (Conventional Type)			Case 5: Single Layer HD with Regular Placement (Conventional Type)		
Wave	H_{m0} (m)	N_s	Wave	H_{m0} (m)	N_s	Wave	H_{m0} (m)	N_s	Wave	H_{m0} (m)	N_s	Wave	H_{m0} (m)	N_s
W1	0.05	0.58	W1	0.05	0.58	W1	0.05	0.58	W1	0.05	0.89	W1	0.05	0.58
W2	0.08	0.93	W2	0.08	0.93	W2	0.07	0.81	W2	0.08	1.43	W2	0.08	0.93
W3	0.10	1.16	W3	0.10	1.16	W3	0.09	1.05	W3	0.10	1.79	W3	0.10	1.16
W4	0.11	1.28	W4	0.10	1.16	W4	0.11	1.28	W4	0.11	1.96	W4	0.11	1.28
W5	0.14	1.63	W5	0.14	1.63	W5	0.14	1.63	W5	0.15	2.68	W5	0.14	1.63
W6	0.16	1.86	W6	0.15	1.74	W6	0.16	1.86	W6	0.17	3.04	W6	0.17	1.98
W7	0.16	1.86	W7	0.16	1.86	W7	0.18	2.09	W7	0.17	3.04	W7	0.17	1.98
W8	0.17	1.98	W8	0.16	1.86	W8	0.19	2.21	W8	0.18	3.21	W8	0.18	2.09
W9	0.18	2.09	W9	0.18	2.09	W9	0.20	2.33	W9	0.19	3.39	W9	0.19	2.21
W10	0.17	1.98	W10	0.16	1.86	W10	0.20	2.33	W10	0.17	3.04	W10	0.17	1.98
W11	0.20	2.33	W11	0.20	2.33	W11	0.23	2.67	W11	0.22	3.93	W11	0.22	2.56
W12	0.20	2.33	W12	0.20	2.33				W12	0.21	3.75	W12	0.21	2.44
W13	0.21	2.44	W13	0.21	2.44				W13	0.21	3.75	W13	0.21	2.44

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Case 6: Emerged Berm with Irregular Placement (Berm Type)			Case 7: Berm at SWL with Irregular Placement (Berm Type)			Case 8: Submerged Berm with Irregular Placement (Berm Type)			Case 9: Emerged Berm with HD Cubes over Reference Area with Irregular Placement (Berm Type)			Case 10: Double Layer ND with Irregular Placement (Conventional Type)		
Wave	H _{m0} (m)	N _s	Wave	H _{m0} (m)	N _s	Wave	H _{m0} (m)	N _s	Wave	H _{m0} (m)	N _s	Wave	H _{m0} (m)	N _s
W1	0.05	0.58	W1	0.05	0.58	W1	0.05	0.58	W1	0.05	0.58	W1	0.05	0.89
W2	0.08	0.93	W2	0.08	0.93	W2	0.07	0.81	W2	0.08	0.93	W2	0.08	1.43
W3	0.11	1.28	W3	0.09	1.05	W3	0.09	1.05	W3	0.10	1.16	W3	0.10	1.79
W4	0.10	1.16	W4	0.10	1.16	W4	0.08	0.93	W4	0.10	1.16	W4	0.11	1.96
W4.1	0.11	1.28	W5	0.13	1.51	W5	0.11	1.28	W4.1	0.11	1.28	W4.1	0.12	2.14
W4.2	0.12	1.40	W6	0.15	1.74	W6	0.13	1.51	W4.2	0.12	1.40	W5	0.14	2.50
W5	0.14	1.63	W7	0.15	1.74	W7	0.14	1.63	W5	0.13	1.51	W6	0.16	2.86
W5.1	0.14	1.63	W8	0.16	1.86	W8	0.16	1.86	W5.1	0.13	1.51	W7	0.16	2.86
W6	0.15	1.74	W9	0.16	1.86	W9	0.17	1.98				W8	0.17	3.04
W7	0.15	1.74	W10	0.17	1.98	W10	0.19	2.21				W9	0.18	3.21
W8	0.15	1.74	W11	0.19	2.21	W11	0.22	2.56				W10	0.17	3.04
W9	0.16	1.86	W12	0.20	2.33	W12	0.24	2.79				W11	0.20	3.57
W10	0.15	1.74	W13	0.21	2.44	W13	0.25	2.91				W12	0.21	3.75
W11	0.18	2.09												

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