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Image analysis for morphology, rheology and degradation study of railway ballast: A review

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Abstract: The performance and deformation of ballast bed are significantly influenced by the particle morphology (size and shape), the rheology (translation and rotation), and the degradation (breakage and abrasion). Regarding the ballast particle morphology, the ballast particle size is generally measured by sieving and described with the Particle Size Distribution (PSD), while the particle shape is normally classified as three characteristics, the form, angularity, and surface texture. Quantifying particle morphology with current manual methods is difficult to obtain accurate results (often subjective).

Concerning the ballast particle rheology, almost all the related studies are based on numerical simulations, e.g. the Discrete Element Method (DEM). A limited number of studies were performed to record the translation and rotation with the electronic devices embedded in ballast layer. However, the numerical simulations can only precisely reflect the ballast particle rheology in quasi-static tests (e.g. direct shear test), and the electronic devices can only record the ballast particle rheology in the limited areas, where they were placed.

The ballast breakage could be evaluated by the change of the PSD, but the determination of PSD involves significant errors. Additionally, the manual methods could not fully quantify the ballast abrasion. As a result, more accurate evaluation methods need to be developed and utilised for the validation and confirmation of the degradation-related studies.

22 Towards these limitations, the studies on two-dimensional (2D) and three-dimensional (3D) image analysis methods for
23 granular materials are reviewed, discussing their existing and potential utilisation in railway ballast applications. This paper
24 can be of interest to the researchers, who are dealing with the performance and deformation of ballast bed. Additionally, a
25 special attention can be paid to utilising the image analysis for accurate particle morphology quantification, particle rheology
26 investigation and ballast degradation evaluation.

27 **Keywords:** Ballast; Image analysis; Morphology; Rheology; Degradation; X-ray; PIV

28 **1 Introduction**

29 Ballast particles, uniformly graded crushed rocks, are one of the most fundamental components in railway tracks.
30 They are placed between and under the sleepers to form the ballast track. Furthermore, the presence of ballast
31 particles in railway tracks help keep the track in the required position, transfer the loads to the subgrade, as well
32 as provide sufficient drainage. To guarantee the critical performance of ballast bed, the ballast particle properties,
33 such as the parent rock type, particle size and shape, etc. should be well assessed. Usually, the material of the
34 parent rock is analysed using the petrographic methods, and other important properties, such as, the particle size
35 distribution (PSD) and the percentage of the flaky or elongated particles are tested as well. Although the ballast
36 particles are carefully tested, they still need more comprehensive and reliable tests, which is necessary for the
37 increasing demand of the higher train speed, the heavier axle load and the larger operation intensity. Most
38 importantly, the increasing usage of ballast tracks leads to unacceptable deformation and poor (fast degraded)
39 performance of the ballast bed, which directly affect the maintenance frequency and the lifespan of ballast track
40 [1].

41 To solve these issues, more emphasis should be put on studying the effect factors affecting the performance and
42 deformation of ballast bed. The performance and deformation of ballast bed are significantly influenced by the
43 ballast particle morphology (size and shape), the rheology (translation and rotation), and the degradation (breakage
44 and abrasion). Besides, the ballast deformation is mostly affected by three primary mechanisms: densification,
45 distortion, and degradation [2]. The densification can be described as the change of shape and compressibility of
46 the ballast particles; the distortion is defined by the rheology (translation and rotation) of individual ballast particles;
47 and the degradation is controlled by the two main processes, namely, breakage and abrasion. Generally, the

48 performance includes durability, shear strength, stiffness and resilience. In a number of studies, it was shown that
49 the high performance of ballast particles mainly consists of the following factors [3]:

- 50 • hardness and durability of the particles,
- 51 • high density and low water absorption of the particle material,
- 52 • reasonable PSD of the ballast particles,
- 53 • presence of angular particles,
- 54 • limited percentage of flaky or elongated particles,
- 55 • presence of the rough particles with fresh fracture surface.

56 Obviously, most of the listed characteristics are related to the ballast particle morphology. Similar conclusions can
57 be found in the studies on other granular materials, such as, sands, asphalt mixtures, rock-fill and concrete [4-6].
58 Therefore, the ballast particle morphology, rheology, and degradation are the three key factors determining the
59 performance and deformation of ballast bed.

60 However, most of the studies on these three factors have some limitations and drawbacks, such as the rough indices
61 for particle morphology evaluation, the types of ballast degradation etc. The image analysis is the more cutting-
62 edge and rapidly developing one. The image analysis is used to analyse the 2D images (photography, particle
63 projection) or recorded videos of the particles. Alternatively, it can also be used to analyse the 3D images obtained
64 through laser scanning, recombination of pictures from different viewpoints, or cone beam X-ray tomography.

65 The limitations and drawbacks of the traditional methods for these three factors are introduced in the following
66 three sub-sections, the 1.1, 1.2, and 1.3 respectively. Afterwards, the image analysis methods for these three factors
67 are presented in the three sections, the Section 2 (Morphology) and Section 3 (Rheology).

68 **1.1 Morphology**

69 Evaluating the particle morphology more accurately and efficiently is necessary for studying its correlation with
70 the performance and deformation of ballast bed [2, 7]. The particle morphology includes the particle size and the
71 particle shape. The size of ballast particles is usually determined using the sieving and expressed in the PSD, while
72 the shape is normally evaluated roughly with the aspect ratio of the particles [8]. More importantly, because of the
73 rough particle morphology evaluation, the evidence of its effects on the performance and deformation of ballast
74 particles is inconclusive.

75 For instance, the size is traditionally based upon the sieve analysis, and presented as the PSD curve, however, that
76 is a rough evaluation. Because the ballast particles are irregular compared to simple spheres, specifically, one
77 ballast particle can have plenty of different dimensions. Even though the particles pass through the sieve that
78 cannot accurately measure the size of the particles and only presents the smallest particle projection can go through
79 the sieve mesh. Furthermore, the final separation results of the particles mainly rely on the sieving duration, which
80 means longer time sieving can increase the passing possibility by making the particles rotate more to fit the sieve
81 mesh [9]. Even though measuring the particle size one by one is more precise, it is time-consuming and with large
82 personal errors. For example, to obtain the three main dimensions of the individual ballast particles, the
83 proportional calliper is often used. The length and the height are easy to measure with this device, but measuring
84 the width is complicated and its result depends on the experience of the measuring person in most cases.

85 Because of the rough particle size evaluation, the evidence of particle size or the PSD effects on ballast
86 performance is still inconclusive. Such as in [10], it is reported that particle size has little influence on shear
87 strength, however, in other studies [11, 12] it is shown that the shear strength can increase or decrease as the
88 particle size increases. Regarding the PSD effect, most researchers believe that a narrower PSD can provide better
89 ballast performance, while some researchers argue that ballast assemblies with the mixture of large and small
90 particles that results in wider PSD, can perform better [13].

91 Currently, in the case of ballast particle shape, the clear standards are still not available, and normally it is evaluated
92 by manual means (often subjective). For instance, the general method for particle shape evaluation [14] is to
93 manually measure the three main dimensions of the particle (length, width, and height), producing the two rough
94 indices, the Flat or Elongated ratio (*FR* or *ER*). They are respectively expressed as the equations in Table 8, at [Flat](#)
95 [or Elongated ratio](#) (marked with the reference, Fernlund, 2005, 2007). Recently, several morphological indices are
96 proposed, including the Sphericity [15], the Angularity index [16] and the Surface texture index [17], consisting
97 of numerous manual procedures. Therefore, the current particle morphology evaluation methods cause of low
98 efficiency and accuracy, thus in most cases they only produce very rough indices [13].

99 Because of the rough indices, the earlier studies on the particle shape effects on the performance of ballast layers
100 did not always reach a consensus. For example, it is found that ballast specimens with flaky or elongated particles
101 can cause lower resilience [13]. However, a limited percentage of flaky or elongated particles leads to higher shear
102 strength and thus a lower rate of settlement accumulation [12]. Nevertheless, it is reported that adding flaky or
103 elongated particles results in more severe degradation and higher deformation [18]. That is due to different particle
104 morphology will further differ the compaction of ballast layer, the contact number between ballast particles and

105 the ballast particle degradation etc., which will finally lead to different performance [19, 20].

106 Accordingly, the accurate and efficient methods for ballast particle morphology evaluation are significant for the
107 further studies (i.e. performance and deformation of ballast bed). The techniques of image analysis have been
108 developed for evaluating the morphology of particles in pavement layer, concrete, and railway ballast bed. As an
109 efficient, accurate and viable solution, it should have further been studied.

110 **1.2 Rheology**

111 Ballast particle rheology is defined as the movement of individual particles, and further the flow of the whole
112 ballast layer, which has the similar definition as the particle rheology in concretes [21]. For the granular level, it
113 has two properties, the particle translation and the particle rotation, while for the entirety level, it can be
114 characterised by the irrecoverable distortion.

115 Studies on ballast particle rheology should be performed deeper, because according to the studies so far, the
116 performance and deformation of ballast bed are mainly dependent on the ballast particle rheology [22, 23]. For
117 example, track irregular geometry (e.g. hanging sleeper) that is caused by the differential settlement, which results
118 from the different ballast particle rheology at different parts, as well as the corresponding ballast rearrangement
119 and compaction diversity under adjacent sleepers [24]. This can be also proved by using the geosynthetics to
120 restrict the ballast particle rheology for providing better performance and less deformation of ballast layer [1].

121 For the importance of ballast particle rheology, plenty of studies were performed including numerical simulations
122 (using the DEM), laboratory tests and in-site tests. However, there exist some limitations and drawbacks of these
123 research methods.

124 Concerning the numerical simulation studies, the DEM is the most widely utilised due to its ability of obtaining
125 the complete particle information (acceleration, velocity, displacement, contact force). Additionally, it can simulate
126 the characteristics of granular materials (density, morphology), and more importantly study the effects of particle
127 breakage and abrasion on the performance (shear strength, resilience) [1]. However, using the DEM has two main
128 limitations, computing time and energy dissipation.

129 Regarding the computing time, it is not sufficient to study the ballast particle rheology with only a few cyclic
130 loadings, however, more cycles cost more computing time. For instance, in the simulation of cyclic triaxial tests,
131 thousands of particles may be involved in one 3D DEM model, to analyse that costs large amounts of time. This
132 problem becomes more serious when non-spherical particles are modelled for more realistic particle shape [25,

133 26], e.g. when clumps or clusters are used in the software, Particle Flow Code (PFC) [27-29]. They are generated
134 by adding two or more spheres together to form one particle. There is a difference between the clump (a rigid
135 particle) that cannot break up regardless of the forces loading on it, and the cluster that is crushable due to the
136 component spheres are bonded together by the parallel bonds. The clusters will crush when the force acting on
137 them is over the prescribed value [30]. Although in some other software, the polyhedral particles are utilised with
138 better shapes than spheres, the main possible imperfection is that the applied particles are uncrushable [24]. For
139 instance, in [31], a novel statistical method was proposed to generate virtual 3D particles with realistically complex
140 yet controllable shapes.

141 When the kinetic energy is not properly dissipated in DEM simulations, the particle movements are larger than
142 real, making the particle rheology unrealistic. The energy dissipation is related to model calibration, which means
143 the energy supplied to the ballast layer is dissipated through the ballast sliding, rolling, breaking and wearing,
144 practically. However, in the DEM models, that is extremely difficult to adjust. For example, in most PFC models
145 of railway ballast, the kinetic energy is dissipated through frictional sliding and local damping [28, 29]. The local
146 damping applies a damping force (magnitude proportional to unbalanced force) to each ball. Mostly, the value of
147 the local damping is taken as 0.7, which means that 70% of the unbalance force between particles is lost after each
148 time interval. Using the local damping is the most appropriate for quasi-static deformation simulations (e.g. direct
149 shear test model [32]). However, when it comes to the dynamic simulation of compact particles (e.g. cyclic triaxial
150 test [33]), only local damping is not sufficient to dissipate the energy. This becomes intensified when the simulation
151 is dominated by rapid impacts (e.g. tamping tine inserting). More explanations about how damping works are
152 shown in [34].

153 Regarding the laboratory tests for the study on ballast particle rheology, the SmartRock [24] and Sensing stones
154 [35] are the latest technological devices. The SmartRock is a 3D printed particle with an electronic unit embedded
155 inside. The electronic unit is a 9-degree-of-freedom motion/vibration sensor consisting of a triaxial gyroscope, a
156 triaxial accelerometer, and a triaxial magnetometer, which records rotation, translation, and orientation,
157 respectively. The Sensing stones are piezoelectric-type triaxial acceleration sensors, simultaneously measuring the
158 acceleration in three directions. Therefore, the SmartRock can record real-time ballast particle rheology, including
159 translation and rotation, but it can only record the rheology of the positions, where the SmartRock was placed.
160 Moreover, when the particle rheology of every individual particles needs to be studied, this technological device
161 seems insufficient. The other technological device, the Sensing stones can measure all the vibrations actuating in
162 the ballast layer, however, it has the same limitation as the SmartRock.

163 The above discussions demonstrate that cutting-edge methods are needed for the study on ballast particle rheology.
164 The image analysis methods can be an effective solution for that, because they can accurately record the initial and
165 final information (e.g. position) of every individual particle. Moreover, among the image analysis methods, the
166 Particle Image Velocimetry (PIV) is already performed in the particle rheology studies of sands and soil. Most
167 importantly, the results of particle rheology can be utilised to calibrate the particle movement in numerical
168 simulations (DEM models). The PIV will be introduced in details in Section 3.

169 **1.3 Degradation**

170 Ballast degradation is another important factor influencing the ballast performance and deformation, including two
171 main types, breakage and abrasion [1]. However, the current evaluation methods for the breakage and abrasion are
172 still insufficient and need improvement. That will affect the test results when ballast degradation frequently occurs
173 and has great influences, such as the shear strength measurement in triaxial tests and the degradation quantification
174 in laboratory tests (e.g. the micro-Deval test). They are discussed in the following paragraphs, furthermore, the
175 limitations and insufficiency of the widely-used degradation evaluation methods are discussed.

176 Particle breakage significantly influences the performance (e.g. shear strength) and the deformation of any kinds
177 of ballast material [1]. On one hand, particle size would be changed after crushing and generally cause the
178 densification and the contaminations clogging the voids, which may further increase the shear strength [13]. On
179 the other hand, the drainage failure would also induce dramatic ballast settlement. As reported in [36], saturation
180 increased settlement by about 40% of that of dry ballast. Accordingly, the effects of particle breakage on the
181 performance and deformation of ballast bed are complicated, which results from the insufficient breakage
182 evaluation.

183 For instance, all the breakage evaluation methods are based on sieving, analysing the change of the PSD or the
184 percentage of particles passing some certain sieve size, when performing laboratory tests, e.g., the Los Angeles
185 Abrasion test, the triaxial test, and the prismoidal triaxial test [1, 37]. The breakage index B_g (proposed in [38])
186 calculates particle sizes between the initial and final particle size distributions. To be more specific, it is the sum
187 of the difference in percentage retained on sieves, having the same sign. However, it may not be sufficient to
188 evaluate ballast breakage only by calculating the PSD, since the final PSD results are obtained based on various
189 types of ballast breakage, including corner breakage, splitting in the middle, and breaking into several parts.

190 Most of the current methods that can evaluate ballast abrasion are related to the image analysis. For example, in
191 [39], the abrasion is evaluated by the changes of ballast particle morphology. The University of Illinois aggregate

192 image analyser (UIAIA) and a second-generation aggregate imaging system (AIMS) are utilised to capture changes
193 of individual particles before and after the micro-Deval test [39].

194 Consequently, among the previous methods, image analysis is the most potential and effective one, which can be
195 a significant method to evaluate the ballast degradation. More studies based on that should be performed for better
196 understanding of the ballast degradation mechanism and further its effects on the performance and deformation of
197 ballast bed [1, 40].

198 This paper reviews the studies on the 2D and 3D image analysis for the morphology, rheology and degradation of
199 granular materials. An overview of image analysis methods is presented, afterwards, their existing and potential
200 utilisations in railway ballast studies are discussed. The images are obtained from various technological means,
201 such as, the laser scanning and the X-ray. In this paper, the various methods are summarised, which will assist
202 future researchers to develop new methods until a more accurate and efficient method is achieved. Moreover, the
203 research gaps and promising research directions of the image analysis for railway ballast are discussed. Gathering
204 all the information into a paper can also offer researchers with a beneficial reference for future work.

205 The paper is structured as follows. The image analysis methods for the particle morphology are introduced in
206 Section 2. A detailed and critical review of particle degradation studies are highlighted in this section as well, due
207 to the better morphology evaluation leads to a better ballast degradation evaluation. Additionally, this can help
208 analysing the possibility of the morphology evaluation methods to quantify ballast particle degradation. The
209 particle rheology studies (Section 3) are introduced with the PIV emphatically discussed. Finally, the discussions
210 and perspectives of the image analysis for railway ballast studies are given in the last section.

211 **2 Morphology and degradation evaluation**

212 Particle morphology (size and shape) has direct effects on the performance and deformation of the granular
213 material layer, such as, the sands, rock-fills, and asphalt or concrete layers [4-6]. The particle morphology is
214 significant for railway ballast as well [41]. However, the traditional methods are somewhat insufficient for the
215 particle morphology evaluation [9]. For instance, the PSD (for size) and the Flat or Elongated ratio (for shape) are
216 the two main indicators analysed before laboratory tests or railway line construction. The rough quantification of
217 ballast particle morphology normally leads to inconclusive test results and controversial conclusions [13].

218 Consequently, image analysis methods with advanced technical means have been developed [42, 43]. These

219 methods are more efficient and can provide more accurate particle morphology evaluation and corresponding
220 morphological indices, including:

221 Size: 1. the Particle size distribution,

222 2. the Volume & Surface area;

223 Shape: 3. the form (Flat or Elongated ratio, Sphericity etc.),

224 4. the angularity (Roundness, Angularity index),

225 5. the surface texture (Roughness, Surface texture index).

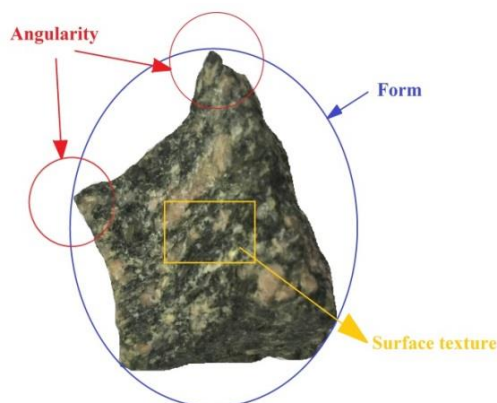
226 Ballast degradation is another crucial factor that influences the ballast performance and deformation, due to the
227 morphology change during degradation. It generally classified as two main types: breakage and abrasion. Ballast
228 particle breakage has significant influences on the shear strength and the deformation of any kinds of ballast
229 material, which consequently affects the track stability [13]. The ballast particle abrasion is another important type
230 of ballast degradation, and it is demonstrated in [44] that permanent settlement is related to the ballast abrasion.
231 However, few studies concern the degradation evaluation methods, and most studies utilised only rough evaluation
232 indices, e.g. indices from the PSD comparison, causing inaccurate results. Therefore, it is vital to develop an
233 evaluation method before studying the relationship between ballast degradation and the degradation-related
234 performance or deformation.

235 In this section, the image analysis methods for particle morphology evaluation are introduced in details. It should
236 be noted that these methods for granular materials are already or potentially used for the railway ballast application.
237 This will help analysts and engineers select an appropriate image analysis method and a suitable technical mean,
238 when performing laboratory/in-site ballast tests or building a railway line. Moreover, all the technical means have
239 the advantages and disadvantages, therefore, analysing and comparing them is helpful to know where to improve
240 the technical means. Most importantly, introducing the image analysis methods will assist future researchers to
241 improve existing morphology evaluation methods. Moreover, using the image analysis, the degradation evaluation
242 methods for granular materials are introduced as well. Most of them rely on the morphological indices from the
243 morphology evaluation. In other words, they mostly measure the 2D particle morphology change (size, form,
244 angularity, surface texture) of the whole testing sample. Particularly, cutting-edge 3D degradation evaluation
245 methods for individual particles are introduced, providing promising image analysis methods for ballast
246 degradation evaluation.

247 2.1 Particle morphology evaluation with image analysis

248 2.1.1 Shape and size evaluation

249 The particle shape can be described with various kinds of characteristics. Among them, the most widely-accepted
250 one includes the form, the angularity, and the surface texture, as shown in Figure 1. The three shape characteristics
251 are defined based on the different scales. According to [45], they are utilised to characterise particle shape, because
252 each of shape characteristics is independent and can be different without influencing the other two characteristics.



253

254 *Figure 1 Shape characteristics of ballast particle (reproduced from [20])*

255 Therefore, the particle shape is mostly evaluated by quantifying the three shape characteristics. The form, as the
256 large scale, is mainly quantified with the morphological indices, e.g. the Flat or Elongated ratio [20, 46] and the
257 Sphericity [15, 47-49]. Some other morphological indices are also proposed in some studies, e.g. the Ellipsoidness
258 [50] and the Form index [43, 51-53]. The angularity is quantified with the morphological indices, e.g. the
259 Angularity index and Roundness [42, 43, 53-55], and the Roughness (Surface texture index) is used for the surface
260 texture evaluation [42, 43, 51, 56].

261 In the reviewed references, the applied apparatuses, image acquisition methods (raw data), the study highlights
262 and the output (morphology indices) are given in Table 3, Table 4, Table 5, Table 6 and Table 7, and the
263 corresponding calculation methods of the morphological indices for the shape quantification are summarised in
264 Table 8, Table 9 and Table 10.

265 The particle size is traditionally evaluated by the Particle Size Distribution (PSD), which is the curve presenting
266 the mass percentage that can pass some certain sieve sizes. More accurately, the PSD can be obtained by measuring
267 all the particle sizes of one sample with image analysis methods. The three axes of a particle can be measured and
268 one of them can be used as the particle size. Moreover, the particle volume or surface area can also reflect the

269 particle size. The image analysis methods for size evaluation are combined with the shape evaluation, given in the
270 Table 3, Table 4, Table 5 and Table 7, and the corresponding calculation methods are given in Table 11.

271 It should be noted that the morphological indices almost cover all the popular indices utilized for particle
272 morphology evaluation. By doing this can help researchers compare the calculation methods and find the
273 morphological indices that are suitable for their research. Moreover, analysing the development tendency of these
274 indices will also assist to find insufficient points that need improvement. These morphological indices are
275 categorized based on the techniques that are utilised for particle shape acquisition, i.e. manual measurement and
276 image analysis.

277 The techniques for the manual measurement use some less accuracy devices (e.g. convexity gage and sliding rod
278 caliper). Based on the measured values (e.g. perimeter and area of particle projection), many morphological indices
279 for particle shape evaluation are proposed, as shown in Table 8, Table 9, and Table 10 (marked with “Manual
280 measurement”). It should be noted that some calculation methods of these morphological indices are also used for
281 image analysis in some studies, because they can be accurate when the needed parameters (e.g. particle volume
282 and surface area) are precisely measured with image analysis methods. Examples can be found in the Table 8-12,
283 such as the [Circularity](#) and the [Sphericity](#) (Hyperlink), whose reference, description and the utilised equations are
284 given in Table 8, marked with the “Riley, 1941”.

285 In recent decades, the techniques for particle image acquisition and analysis are rapidly developing. Compared
286 with the traditional means, the particle morphology evaluation with image analysis methods is more accurate and
287 objective. Image analysis methods analyse 2D or 3D images that are acquired with various technical means
288 (apparatus), such as, photography (camera), X-ray (computed tomography scanner), 3D imaging (3D scanner) and
289 laser scanning (laser scanner), etc. Various technical means with different apparatus significantly influence the
290 precision of the images, thus the results of particle morphology evaluation. Photography utilises cameras to take
291 particle photos, and in most cases the photos are converted into binary images. X-ray can take photos at different
292 cross sections of particles, and the cross sections of which can be used to form the 3D image for the same particle.
293 3D imaging utilises the particle pictures from different views to form the 3D image. Laser scanners collect the
294 relative positions (coordinates) of the surface points and subsequently the 3D image is formed by the triangle
295 meshes (by connecting every three adjoint points).

296 The image analysis methods are categorized as the Static Image Analysis (SIA) and the Dynamic Image Analysis
297 (DIA). This categorisation is according to whether particles are moving during the image capture. The SIA utilises

298 cameras to capture images of particles lying down on a flat plate/belt, while the DIA captures images of particles
299 falling from a conveyer belt. The image analysis methods and the corresponding morphological indices (SIA, DIA)
300 will be introduced in the two following sub-sections.

301 *2.1.1.1 Static Image Analysis*

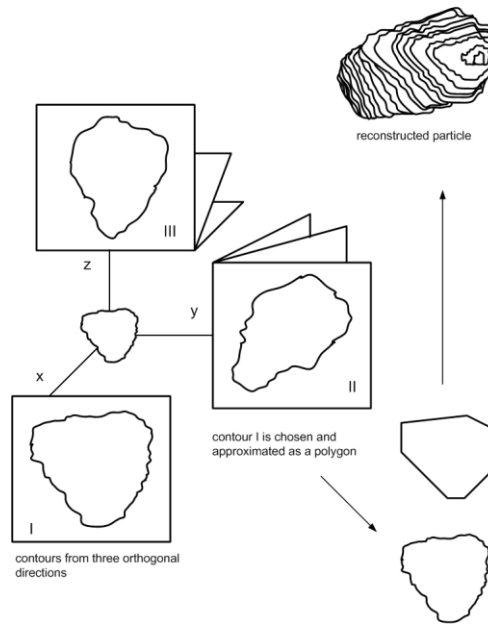
302 In this sub-section, the SIA methods are introduced, and they are classified in the following aspects. The
303 classification is according to the image acquisition methods.

- 304 • the Photography analysis with 2D output (Table 3),
- 305 • the Photography analysis with 3D output (Table 4),
- 306 • the image analysis systems (Table 5)
- 307 • and others (Table 6).

308 The Photography analysis utilises 2D digital images or projections of particles (i.e. particle outline), which are
309 obtained with cameras or projectors, respectively. The Photograph analysis outputs have two types, the 2D and the
310 3D, which are given in the Table 3 and Table 4, respectively. The image analysis systems for particle morphology
311 evaluation (introduced in Table 5) include the Aggregate Image Measurement System (AIMS), University of
312 Illinois Aggregate Image Analyzer (UIAIA), Laser-Based Aggregate Scanning System (LASS), Quantimet Q570
313 Image Analysis System, Quantimet Q600 image analyser, 3D laser-digitising system and Council for Scientific
314 and Industrial Research (CSIR). The image analysis methods that do not belong to the Photograph analysis or the
315 image analysis systems are classified as “others” in Table 6. In the Table 3-7, the applied apparatuses, image
316 acquisition (raw data), the study highlights and the output (morphology indices) are introduced.

317 *2.1.1.1.1 Apparatus and raw data*

318 The applied apparatuses in SIA methods include the camera, X-ray CT scanner, laser scanner and 3D scanner. The
319 camera takes the digital 2D particle image and is mainly utilised in the Photography analysis (PA) methods. The
320 X-ray CT scanner obtains the cross section image of the particle, and the cross sections of one particle can be
321 reconstructed to make one 3D particle image. The laser scanner sheds the laser beams onto the particle surfaces,
322 after using the black and white camera for photographing the image of the scene, the uneven surface is indicated
323 by appearing the reflected laser beams as a dashed line. The 3D scanner takes the particle images from various
324 viewpoints and recombine the images to form the 3D particle image, as shown in Figure 2 (described in detail in
325 [57]).



326
327 *Figure 2 Principle of imaging from multiple views (reproduced from [58])*

328 In the various SIA methods, the above four kinds of apparatuses are utilised dissimilarly for better image
329 acquisition. For example, in [59], with the laser scanner the whole particle is scanned, whereas the LASS system
330 only scans the upper sides of particles [60]. Another example of prominent difference is taking the particle images
331 from various view sides, comparing with some methods that only take one particle image, as shown in the Table
332 3-7. Also for better image acquisition, in the image analysis systems, the apparatuses are combined with some
333 other facilities (e.g. transparent trays [60], green backlight [61]). each apparatus has the advantages and the
334 disadvantages, as shown in Table 1.

335 *Table 1 Advantages and disadvantages of the apparatuses*

Analysis method	Advantage	Disadvantage
Photograph analysis	Cheap; easy to access	Human intervention to appropriately arrange the particles
AIMS; AIMS2	Measure three particle axes; capture particle images at different resolutions based on particle size; measure particle surface texture.	Good contrast requirement between particles and background; expensive
UIAIA; E-UIAIA	Use three cameras to capture three images of one particle moving on a conveyor belt; measure particle surface texture	Uses same camera magnification to take images of all particle sizes
LASS	Measures the three dimensions of aggregates; half 3D particle image; scan several particles each time	Use the same scan to analyse different size particles; considerable manual work
3D laser-digitising system	Complete particle information	Low efficiency; considerable manual work
X-ray CT scanner	Complete particle information	Low efficiency; time-consuming reconstruction for 3D image;

336

337 By different apparatus utilisation way, the obtained raw data types are different. In the PA methods, they include
338 unique image of particle, unique image of particles, two/three images of particle and two images of particles. In
339 the analysis systems (Table 5) and other methods (Table 6), the raw data have more types, i.e. One grey image and
340 one black and white image, three orthogonal images of particle, upper side of particle and 3D image.

341 The unique image of particle is taking only one image for one particle, and the unique image of particles means to
342 take one image for several particles, which is for saving time but requiring more complex algorithm (image
343 segmentation). For higher accuracy of image analysis results, two or three images of one particle from different
344 view sides are applied, resulting to the raw data types of two/three images of particle. For the other types, in the
345 AIMS, different shape scales are analysed with different images, specifically, the one grey image is for surface
346 texture and one black and white image is for form and angularity. Three orthogonal images of particle are taking
347 the images of one particle from three orthogonal directions (UIAIA). The LASS utilises the upper side of particle
348 as raw data type, which is the half of one particle, whereas some types utilise the complete 3D image for one
349 particle.

350 The analysis result accuracy is significantly influenced by the raw data types. Initially, unique image for one
351 particle is utilised for image analysis, and improving the image resolution is the only means for higher accuracy
352 analysis (e.g. [62, 63]). The resolution of the digital images has effects on the image analysis results, because
353 higher resolution can present clearer particle outline with more pixels, which can reduce the calculation error of
354 the perimeter and area of the particle, especially for the surface texture evaluation. However, two limitations need
355 improvements. One is the low efficiency of photographing particle one by one in a sample. The other is that a
356 single 2D image for each particle causes the inaccuracy of measuring the particle information (e.g. volume and
357 thickness), which are mostly inferred from a 2D particle projection.

358 To overcome the low efficiency limitation, the whole sample is placed in a proper position and photographed [61,
359 64-68], and many particle image segmentation algorithms are proposed for precise and automatic extraction,
360 especially with the cutting-edge computer technology. For example, based on the convolutional neural networks
361 (CNN), Tong presents an efficient and automatic PA method to evaluate particle angularity through digital images
362 [69]. It is proved that the CNN can locate and abstract each particle from a digital image of particle assemblies by
363 dividing it into several overlapping sub-windows for extracting image features.

364 Towards the second limitation, many solutions are proposed using more advanced apparatuses or other aided

365 facilities. For example, the transparent plastic trays are used with two perpendicular faces for attaching the particles
366 and then photographing other particle sides automatically [70]. This can be more efficient than the earlier methods,
367 i.e. the human intervention for proper particle arrangement (e.g. [71, 72]). In [73], with a special cylindrical carrier,
368 the image of particle shadows can be utilised for the measurement of three axes. A camera and two lighting sources
369 are utilised for obtaining the image of the perpendicular particle shadows, which are processed to measure the
370 three principal particle axes. Even though the two methods can measure three particle axes, there still exists plenty
371 of inevitable manual work. The work is replacing the particles on the plexiglass holders or the cylindrical carrier
372 with new particles.

373 In addition, in the image analysis systems, the aided facilities can help to obtain more particle information, leading
374 to more efficient and accurate morphology evaluation. For instance, the UIAIA/E-UIAIA places particles on a
375 conveyor belt and employs three cameras for three orthogonal particle images, as they consider that two images
376 lost vital particle information, causing imprecise morphology evaluation. The AIMS/AIMS2 utilises two cameras
377 to take one black and white image and one grey image for particle outline and surface texture respectively, and the
378 particle thickness can also be estimated when taking the particle outline. Although both systems successfully obtain
379 the 3D particle information, it still needs to arrange the particles in proper positions, so that two or three images
380 of one particle can be captured simultaneously. More importantly, in all the above-mentioned methods, despite
381 using three camera views, inferences must be performed based on 2D projections for particle 3D characteristic
382 evaluation.

383 More advanced apparatuses include the 3D scanner, laser scanner and X-ray CT scanner, and can help to obtain
384 complete particle information (e.g. volume, surface area) through 3D image or half 3D image. In the LASS, the
385 half 3D image is utilised for shortening the scanning time, however, the three axes cannot be precisely computed.
386 Complete 3D image can provide the complete particle information, however, performing all the above-mentioned
387 apparatuses and processing the image are time-consuming (e.g. merging two half 3D images [59]). For example,
388 as reported in [59], X-ray CT scanning takes about 20 min to complete one particle scanning operation, and the
389 post-processing of the scanned data costs even more time. That is due to the scanning equipment efficiency and
390 the post-processing software. The scanned data should be processed and analysed with external software. This is
391 also commonly found when utilising the other advanced apparatuses, i.e. the 3D scanner and the laser scanner.

392 From the discussion of the apparatuses and raw data types, the advantages and disadvantages can be seen,
393 furthermore, the development trend can be observed as well. Specifically, the raw data types are the only one 2D
394 image for one particle, afterwards, two/three 2D images for one particle or particles emerge. Finally, the complete

395 3D image is utilised for particle morphology evaluation. Moreover, more and more advanced apparatuses are
396 utilised for image acquisition with higher and higher resolution. However, the main problem is the efficiency when
397 not only applying the advanced apparatus but also using the cameras with aided facilities.

398 2.1.1.1.2 Study highlights

399 In the Table 3-7, the study highlights describe the main results or progress that are achieved in the literature,
400 including raw data process and morphology-related performance.

401 **Raw data process**

402 The raw data process is the means to process the image for conveniently obtaining the particle information. For
403 example, the binary images are obtained after a kind of 2D digital image process for better performing other image
404 process procedures (e.g. Dilate, Open, Close-, Fill Holes, Watershed, etc. [74]). Another example is the 3D image
405 process in [20, 46, 59, 75], which is combining the two half 3D images of one particle into the complete 3D image.
406 Likewise, the 2D radiographies of one particle (from X-ray CT scanning) can be reconstructed into the complete
407 3D particle image [45, 76]. The raw data process is mainly performed with some commercial software or
408 programming codes. More information can be found in the Table 3-7. It needs to note that the Fourier series utilised
409 for morphology evaluation is emphasized in the study highlights as an important raw data process means and
410 discussed particularly in this sub-section.

411 **Morphology-related performance**

412 The morphology-related performance is also described at the study highlights in the Table 3-7. Currently, limited
413 studies were performed on the particle morphology on the ballast performance, for this, they are emphasized as a
414 promising research prospective. For example, in [54], the base course performance is related with the particle
415 morphology (form, angularity and surface texture). Another example in [77] proves the strong correlation between
416 particle morphology with the drained friction angle and void ratio. The effects of particle morphology on ballast
417 shear strength is studied in [78], demonstrating the correlation also exists in the ballast particles. Even though
418 some related studies have performed, it is still not sufficient to draw a recognized conclusion. This is due to limited
419 studies were performed, and more importantly in the studies only 2D image/images for one particle were utilised
420 other than 3D images. Additionally, the ballast degradation was not considered during the studies.

421 The Fourier series is the definition of an image process means for image analysis using the Fourier transform. It
422 can be used for image analysis to quantify the form, angularity, and surface texture of the particle. This method

423 has been developing from analysing 2D images to 3D ones over years. Subsequently, the calculation methods for
424 image process have been advancing as well.

425 **Fourier series**

426 In the Table 3-7, how the Fourier series is utilised is described in details. Specifically, unrolling the particle outline
427 into polar coordinates or rectangular coordinates is the first step [63, 65]. Afterwards, comparing the shape
428 descriptor values of regular shapes (e.g. triangle, rectangle) with those of particles can quantify the particle shape
429 [65, 79]. Using the cumulative error (amplitude of the radial vector) or area ratio between the reconstructed particle
430 profile and the original one, the particle shape can be quantified as well [80, 81]. All the above-described Fourier
431 series means are based on the 2D image. In [82], the 3D image is processed with the Fourier series, however, only
432 the particle reconstruction is achieved with this. It needs to note that in the LASS, the [Wavelet transform](#) is a
433 Fourier series means for 3D image. It is decomposing a signal (polar coordinates of particle upper surface) into a
434 group of linear combinations. Afterwards the mother wavelet is dilated and translated. The morphological indices
435 are calculated by determining how well the dilated and translated versions of the mother wavelet coincides with
436 the signal [51]. The fine scale wavelets represent surface texture (also used by AIMS), while the larger scale
437 wavelets characterise the form or angularity. That depends on the enlargement degree of the mother wavelet.

438 The advantages of the Fourier series methods can be summarised. On one hand, some of the Fourier series methods
439 are utilised to analyse 3D particle images for more accurate particle shape evaluation. The methods started from
440 analysing 2D images, afterwards the 3D images can be analysed with the [Spherical harmonics series](#) or [Wavelet
441 transform](#). According to the authors' knowledge, to date only using the Fourier series methods can calculate
442 morphological indices for the angularity of 3D particle images. On the other hand, the Fourier series provides
443 different shape quantification methods from the methods used in earlier studies. To be more specific, the three
444 particle shape characteristics (form, angularity, and surface texture) can all be quantified by the same function (e.g.
445 [Wavelet transform](#)), while most of the other methods quantify the particle shape with particle geometrical
446 properties (e.g. area, perimeter, volume and three particle dimensions).

447 2.1.1.1.3 Outputs

448 In the Table 3-7, the output contains the form, angularity, surface texture, size and degradation. The definitions of
449 form, angularity, surface texture and size have been introduced at the beginning of Section 2.1.1 (Shape and size
450 evaluation). The degradation evaluation is also introduced as a kind of output based on the image analysis results.
451 Specifically, the degradation is mostly quantified by comparing the morphological indices change before and after

452 tests or the in-site tests/operations.

453 **Form**

454 Using the geometrical characteristics (obtained with image analysis), the morphological indices for particle form
455 can be calculated. For the 2D images, the geometrical characteristics include perimeter, area, Feret diameter, three
456 particle axes, inscribed circle, circumscribed circle and equivalent ellipse. For the 3D images, the geometrical
457 characteristics include volume, surface area, three particle axes, equivalent ellipsoid, equivalent sphere,
458 circumscribed sphere. The morphological indices calculated with the characteristics are given in the Table 3-7, and
459 the calculation methods are described in the Table 8-12 (with hyperlinks).

460 The Sphericity (Circularity for 2D analysis) or Flat or elongated ratio are the most widely-used indices, and various
461 calculation methods for this index can be found in the literatures. For example, one kind of calculation methods
462 utilises the ratio of particle volume to circumscribed sphere volume or the ratio of particle surface to that of
463 equivalent sphere. Other calculation methods are mostly based on the three particle axes. However, the [Sphericity](#)
464 [15] illustrates a surprisingly high association with Krumbein's [Roundness](#) [48], notwithstanding Sphericity and
465 Roundness are regarded as the morphological indices for form and angularity, respectively.

466 Therefore, some morphological indices are proposed to present the particle form differently, e.g., the modified true
467 sphericity [59] and Ellipsoidness [50] (Ellipseness for 2D [83]). They are expressed by combining the equivalent
468 ellipsoid (equivalent ellipse for 2D) and three particle axes. These morphological indices show little correlation
469 with Roundness or particle size. Other than modifying the Sphericity, the Form index is proposed using different
470 calculation methods. To be more specific, one calculation method utilises the deviation of the global particle outline
471 from a circle [77]. The other one is in the AIMS/AIMS2, which calculates the incremental changes in the particle
472 radius in all directions [84]. However, whether the indices present the form precisely is not clear and no studies
473 have been found to compare these indices to check the feasibility and differences. The same question can be found
474 in the angularity or surface texture evaluation.

475 **Angularity**

476 The morphological indices for particle angularity contain the Roundness and Angularity index. The Roundness
477 (common in earlier studies) is computed with the geometrical characteristics, i.e., three particle axes,
478 perimeters/radii of corners (or convex parts), particle outline area and particle outline perimeter. For instance, in
479 [15], the Roundness is expressed as the ratio of the radius summation of corners to the inscribed circle. Afterwards,
480 in the later studies, the Angularity index is proposed and computed by measuring the corners' angles instead of

481 their perimeters/radii. An example can be found in [85], which utilises the corner angles, the distance of the corner
482 tip to the centre and the inscribed circle radius. The latest Angularity index calculation method is proposed in the
483 AIMS/AIMS2, which is applying the Erosion-Dilation technique. It calculates the area change ratio after the
484 Erosion-Dilation operations. Another cutting-edge calculation method is based on the probability of the adjacent
485 subtended angle change (UIAIA/E-UIAIA).

486 However, these calculation methods are based on the 2D images, which is not accurate especially applied for
487 railway ballast. Because ballast particle size is larger, compared with the sands or soils. The different view of the
488 particle will provide the different results. This problem is more severe when calculating morphological indices for
489 particle surface texture.

490 ***Surface texture***

491 Specifically, most of the calculation methods are based on the 2D particle outline (examples in [54, 56, 66]). In
492 [54], the method computes the ratio of the particle outline perimeter to the convex perimeter for evaluating surface
493 texture as the Roughness (morphological index). This is not accurate, because the particle can be considered as the
494 combination of large amounts of the particle outlines. Towards this issue, the [Wavelet transform](#) is proposed to
495 analyse the surface texture from the grey particle image (LASS/AIMS/AIMS2), which is more accurately than
496 only analysing one particle outline. The Wavelet transform is an image process means using the Fourier series.
497 Based on that, the Surface texture index is proposed in the later studies [51, 86]. It needs to note that most of the
498 morphological indices for particle surface texture apply the Fourier series, e.g. [65, 79-81].

499 ***Size***

500 Particle size is based on one of the three particle axes, volume or area. For instance, the AIMS or AIMS2 evaluates
501 the form with the [Flat or Elongated ratio](#). During this evaluation, the three dimensions of a particle are measured
502 and one of them can be used as the particle size. Another example to measure the particle size utilises the equivalent
503 diameter (based on the particle surface area) [87]. Instead of measuring the sizes of particles one by one, more
504 efficient methods for measuring the particle sizes are proposed. The method is taking a photo of the entire particle
505 sample, and then drawing the particle size distribution of the sample [61].

506 Volume is evaluated with the images from the three orthogonal views, as proposed in the UIAIA/E-UIAIA with
507 the average absolute error is at 11.5% [42]. The LASS utilises the upside 3D image for volume calculation, but it
508 needs modification [88]. With higher accuracy, another two methods are proposed, utilising the 3D X-ray images
509 to calculate the particle volume and surface area. Higher accuracy measurement of the volume and surface area of

510 particles can contribute to better size measurement and shape evaluation. To measure them more precisely, the
511 cutting-edge technical devices are used for more high-resolution images. Also, the images are developing from 2D
512 to 3D until the error of the volume measurement is less than 0.1% [20]. However, obtaining the 3D particle image
513 costs large amounts of time. From the discussion, it can be seen that the image analysis methods can be utilised to
514 obtain particle size distribution. They are more accurate than traditional sieving.

515 Almost all the methods with 2D images are still analysing the binary image or projection of particles. That means
516 the geometrical properties (for morphological index calculation) are still measured using the particle outline. This
517 will significantly influence the accuracy of the particle shape evaluation because of two aspects. On one hand, the
518 particle outline can only provide two dimensions (i.e. the longest and shortest axe). When the particle image is
519 taken at another side, the results of the dimensions will be quite different. On the other hand, the surface texture
520 cannot be fully quantified. The roughness of the particle outline was utilised for the particle surface texture in [54,
521 66, 89], their details are given in Table 10 (Hyslip & Vallejo, 1997; Janoo, 1998; Kuo et. al., 1998). However, one
522 particle outline roughness cannot reflect the surface texture of the whole particle, unless using more outlines of
523 the particle. As reported in [81], when the number of the particle outlines are more than 30, the average
524 quantification value of the surface texture becomes stable.

525 ***Degradation***

526 Most particle degradation evaluation methods using image analysis are based on the particle morphology change.
527 They compare the differences of morphological indices after laboratory tests. For generating deteriorated particles
528 rapidly, the laboratory tests are performed, i.e. Los Angeles Abrasion (LAA) test or the micro-Deval test. The
529 description of the two tests can be found in [37]. The laboratory tests are utilised for deteriorating ballast particles,
530 because that has the advantage of controlling the degradation stages (or degree) by setting the testing duration.
531 Two types of testing duration can be set. One is by setting the revolution number of the LAA tests (or micro-Deval
532 tests), e.g. [45, 61, 90, 91]. the other is by setting various testing time, e.g. [92, 93].

533 Besides the laboratory tests, the image analysis is also utilised for the ballast degradation study in the field [94].
534 The image analysis method is an automated alternative, machine-vision-based inspection system. It has the
535 potential to directly and objectively evaluate the condition of ballast layer and degradation levels with ballast layer
536 image, which are captured in the field. More importantly, the imaging-based index, average Percent Degraded
537 Segments (PDS) was proposed and successfully implemented for evaluating different levels of ballast degradation
538 with the images of ballast layers.

539 In most studies, the degradation is evaluated by the particle size change, presented by the shift of the PSD, e.g.
540 [61, 91, 95]. However, during the degradation, the particle abrasion/breakage cannot be precisely evaluated or
541 reflected only with the PSD change. Therefore, the shape change is presented by the distribution shift of the Flat
542 or elongated ratio (for form) in [61, 95]. After development, more specific morphological indices (for form,
543 angularity) applied in degradation study can be found in [92]. In this study, the distribution of the two
544 morphological indices are presented, i.e. [Aspect ratio](#) and [Angularity index](#). However, this study did not evaluate
545 the surface texture reduction. In the studies [91, 93], the surface texture reduction is presented by the distribution
546 change of morphological index for surface texture ([Surface texture index](#)).

547 However, the methods for degradation evaluation are generally performed on a 2D basis. This means the
548 measurement of the particle morphology, especially the angularity, are mainly dependent on the orientation and
549 posture of the particles. Consequently, it is necessary to perform the degradation analysis and develop degradation
550 evaluation methods based on 3D images. For example, in [20], the two 3D images of one particle are compared
551 (before and after LAA test), and the results show that the main degradation mechanism is the sharp corner loss
552 (angularity reduction). In this study, the single particle degradation is presented instead of the earlier studies that
553 evaluate the morphological indices' change of a whole sample. In addition, the results of degradation evaluation
554 are visible and reliable, demonstrating the feasibility of developing 3D degradation evaluation. However, this
555 method still needs further modification, such as, to shorten the scanning duration time.

556 Among the earlier studies, 3D image analysis is the most potential and effective for degradation evaluation,
557 nevertheless, it still needs more development and further studies. Because most of the methods (2D or 3D) were
558 estimating the abrasion degree, and few evaluation methods were established for the other degradation type, e.g.
559 particle breakage. Furthermore, the only study, proposing image-based particle breakage evaluation method uses
560 the 2D image to obtain the change of the PSD [96], and accurate particle breakage evaluation is difficult to be
561 performed. Consequently, more studies on 3D image analysis should be performed for a deeper understanding of
562 the ballast degradation mechanism and its effect factors. More importantly, understanding those also help further
563 studies on ballast performance and deformation considering the ballast degradation.

564 *2.1.1.2 Dynamic Image Analysis*

565 In this sub-section, the DIA methods are introduced, and they are classified in the following aspects. The
566 classification is according to the apparatus. The specific of these methods are given in the Table 7, including, the
567 apparatus, raw data type, study highlights and output.

- 568 • the Micrometrics OptiSizer System,
- 569 • the Video Imaging System,
- 570 • the Buffalo Wire Works System,
- 571 • the VDG-40 Videograder,
- 572 • the Computer Particle Analyser,
- 573 • and the Camsizer.

574 **2.1.1.2.1 Apparatus and raw data**

575 The above-mentioned DIA methods rapidly obtain the particle images, avoiding a lot of manual work. The methods
 576 provide a rapid alternative means for capturing and processing 2D digital images to present the PSD. Mostly, the
 577 CCD camera (i.e. line-scan or matrix) is utilised for rapid image acquisition. The matrix CCD camera captures 2D
 578 image in each photographing, whereas the line scan camera captures narrow stripes of particle that are subsequently
 579 reconstructed into a 2D image. The line-scan CCD camera captures a more accurate falling particle image, due to
 580 it scans every strip sequentially. However, with the matrix CCD camera, the odd lines (or every other line) are
 581 scanned in the first pass and the even lines are scanned during the second pass. Therefore, the matrix CD camera
 582 method is adequate for SIA methods, but it will produce error when photographing falling particles.

583 The raw data types were introduced in the Sub-section 2.1.1.1.1, and they are also applicable for the DIA methods.
 584 the raw data types of the DIA methods are given in Table 7. Whereas, the advantages, disadvantages and some
 585 other information of these methods are given in Table 2.

586 *Table 2 Comparison of the DIA methods [97, 98]*

Name	Camera	Scanned sample type	Advantage	Disadvantage
Micrometrics OptiSizer System	Matrix CCD camera	Portion of particles	Measure large particle form	Cannot measure angularity or surface texture; assume particle as idealized ellipsoid; use one camera magnification to capture different sizes' particle images; Separate vibratory feed systems; backlights required for both fine or coarse particles
Video Imaging System	Matrix CCD camera	Portion of particles	Measure large particle form	Cannot measure angularity or surface texture; assume particle as idealized ellipsoid; use one camera magnification to capture different sizes' particle images; Separate vibratory feed systems; backlights required for both fine or coarse particles

Buffalo Wire Works System	Matrix CCD camera	Portion of particles	Measure particle form	Cannot measure angularity or surface texture; 2D form index
VDG40 Videograder	Line-scan CCD camera	All particles	Measure large particle form, especially, the Flat or elongated ratio	Cannot measure angularity or surface texture; assume particle as idealized ellipsoid; use one camera magnification to capture different sizes' particle images
Computer Particle Analyser	Line-scan CCD camera	All particles	Measure large particle form	Cannot measure angularity or surface texture; assume particle as idealized ellipsoid; use one camera magnification to capture different sizes' particle images
Camsizer	Two matrix CCD cameras	All particles	Measure particle form and angularity; two cameras to capture particle images at various magnifications based on particle sizes	Cannot measure surface texture; assume particle as idealized ellipsoid

587

588 **2.1.1.2.2 Study highlights**

589 **Raw data process**

590 The 2D images of falling particles are processed with various kinds of image transformation algorithms
591 respectively. Raw data process of these DIA methods is performed by various kind of proprietary software, which
592 are developed by the device developers or companies. In these kinds of software, the process involves various
593 assumptions to provide a 3D particle form evaluation. For example, in the Micrometrics OptiSizer System, the
594 spherical type analysis converts each imaged particle profile area into a circle with equal area. The volumetric
595 information is calculated with the radius of the circle as a sphere volume.

596 The DIA methods can accurately and rapidly measure the size and the two dimensions of particles. However, their
597 limitation is that they cannot sufficiently evaluate the particle angularity or surface texture [99]. That is due to the
598 lack of enough development in the image processing methods and the morphological indices have not been utilised
599 in these methods. Moreover, the CCD camera might not be fast enough to photograph the falling particles.
600 Additionally, when particles are falling, they might change orientation or rotate, which could cause inaccuracies.
601 Most importantly, there are the potential that particles are overlapped during falling.

602 **2.2 Discussion**

603 In this section, the image analysis methods for particle morphology evaluation are summarised. They include the
604 manual methods and methods using image analysis. The image analysis methods are categorized as the Static
605 Image Analysis (SIA) and the Dynamic Image Analysis (DIA), and the apparatus raw data type, study highlight

606 and the output were introduced. Giving the pros and cons of the image analysis methods can help researchers easily
607 compare calculation methods and find the proper method that is suitable for their research. More importantly,
608 analysing the limitations will assist to find insufficient points that can be improved. After introducing the image
609 analysis methods, the areas for improvement can be observed for better morphology evaluation, such as, from 2D
610 image analysis to 3D image analysis, a comprehensive morphological index, and a both efficient and accurate
611 image analysis method, etc. They are discussed later in the Sub-section 4.1.

612 Better morphology evaluation can assist to study the effects of the ballast particle morphology on the performance
613 and deformation more accurately and convincible, as discussed in the Sub-section 1.1. However, until now,
614 according to the authors' knowledge, only one study has been reported with image analysis methods to study the
615 effects of ballast particle morphology on the performance and deformation [78].

616 Using the 3D image and corresponding image analysis methods, the geometrical properties can be measured with
617 high precision, e.g. the volume, surface area and three dimensions of the particle. Almost all the corresponding
618 morphological indices utilise these geometrical properties to quantify the form and the angularity of the particle.
619 It is undeniable that precisely measuring the geometrical properties can help improve the accuracy of the particle
620 shape quantification. Moreover, the precision can still improve with the development of the image acquisition and
621 processing means.

622 However, most of the morphological indices are still calculated based on the volume, surface area and three
623 dimensions of the particle. More advanced calculation methods should be developed based on the precise data of
624 3D particle image. For example, the three dimensions of the particle are still utilised for the form quantification
625 [46], even though the distance between any two points on the particle surface can be measured with the 3D particle
626 image. This is not utilised in any reported studies. More importantly, few studies are devoting to the angularity and
627 surface texture quantification with 3D images. It should be noted that the Fourier series is the only method that the
628 authors can find until now to analyse the 3D angularity.

629 **3 Rheology**

630 The particle rheology mechanism is characterised by translation and rotation of individual particles. According to
631 the studies so far, it has been demonstrated that ballast performance and deformation of ballast bed are mostly
632 dependent on the ballast particle rheology. The irregular geometry of ballast track, such as the hanging sleeper due

633 to the differential settlement, is usually caused by large ballast particle rheology. Consequently, the potential
634 damages to the sleepers, fastening system and rails would emerge, hence, it is significant to study the ballast
635 particle rheology.

636 However, the research on ballast particle rheology are mostly performed with numerical simulations, and a limited
637 number of studies were by tests with sensors or transducers. Numerical simulations could only reflect the quasi-
638 static ballast particle rheology, while the tests can only present the particle rheology of some limited positions,
639 where the sensors or transducers are placed.

640 Therefore, the image analysis methods for the rheology study on granular materials will be reviewed and discussed
641 in this section, providing a deep exploration of utilising the image analysis for ballast particle rheology study.
642 Particularly, the Particle Image Velocimetry (PIV), as a technique for analysing digital images, can measure the
643 particle displacement and velocity etc., and its application for granular materials (sands and soil) will be introduced
644 in this section. Finally, some image analysis methods for ballast particle rheology study are presented in the last
645 sub-section.

646 **3.1 Particle Image Velocimetry**

647 With the rapid development in digital imaging acquisition and processing technology, image analysis is feasible to
648 measure the displacement/strain of the granular materials. As a member of image analysis techniques, the PIV was
649 first proposed to measure the velocity of the gas or fluid. It measures the motion of the target markers in a fluid,
650 and observes the locations of the target markers at two or more time points [100]. Its fundamental principle for the
651 velocity measurement is the evaluation of the local velocity \mathbf{u} from

652 *Equation 1*
$$\mathbf{u}(x,t) \doteq \frac{\Delta \mathbf{x}(x,t)}{\Delta t}$$

653 where, $\Delta \mathbf{x}$ is the displacement of a target marker, located at the position \mathbf{x} at the time t , while Δt is the short time
654 interval between two observations.

655 The rheology of soil particles could be treated as a low-velocity flow process, and hence the PIV (after improved)
656 was firstly applied for the non-contact measurement of soil deformation in geotechnical tests [101]. Its main
657 improvement is the detection of the soil displacements without installing target markers. Because when using target
658 markers, the number of measured targets is limited, which could not reflect the rheology of the whole sample.

659 However, there still exist some difficulties when applying the PIV in geotechnical tests. For example, the success
660 of the test depends on the variation of intensity or texture in the images, however, it was found necessary to enhance
661 the texture by adding reflective particles. Despite this difficulty, it is convinced that the PIV would ultimately be
662 applied to similar geotechnical studies, owing to the fast development of image processing technology, as well as
663 better image texture with higher-resolution cameras [102]. Another difficulty in PIV is the determination of the
664 correlation between the image and object coordinates. To solve that, more complex procedures for camera
665 calibration using the three-layer back-propagation neural networks algorithm, was proposed. The algorithm helps
666 to provide more accurate results, which are independent of the angle between the image plane and the object plane,
667 and its rapid and accurate calibration will extremely facilitate the PIV application into geotechnical tests [103].

668 The rheology of sand particles can also be treated as a low-velocity flow process, and therefore, it can be also
669 studied with the PIV. For instance, the rheology of sand particles around the rigid ribbed plate was studied with a
670 direct shear box plus image analysis. The direct shear box is built with plexiglas walls in order that the CCD camera
671 can observe and measure sand particle displacements. Using the devices, the main work includes monitoring the
672 individual sand particle movements, mapping the dilation and contraction zones, as well as showing the shear
673 strain [104].

674 Another example is that series of biaxial tests on sands are performed with a CCD camera recording the specimen
675 deformation during compression. A square grid pattern is printed on the latex membrane surface, and the
676 deformation is detected by noting the grid displacement. Based on the comparison of selected images (captured
677 from the video), the shear band formation analyses are performed to characterise the specimen failure and to
678 compare with two other classical methods [105].

679 Without printed grid pattern on the latex membrane surface, the biaxial tests are performed on dense sands. The
680 image analysis was used to show localized displacements, to quantify the shear band volumetric strains, and to
681 measure the shear band inclination and thickness. The displacements are measured with higher accuracy by
682 matching pixels between the digital images, and can be further used for the volume strain calculation. The shear
683 band inclination and thickness can be computed because the shear band boundary can be clearly defined from the
684 images [106].

685 Boldyrev demonstrated that the PIV can be used to study not only the sand rheology, but also the rheology-related
686 performance or deformation [107]. The PIV can obtain the following parameters: particle displacement vectors,
687 particle vertical and lateral displacements, shear and volume strain. It was applied for the two following tests. One

688 is load tests in a chamber with one plexiglas wall, specifically, two sand specimens (with or without geogrid) are
689 loaded respectively with a test plate in plain strain [107]. The other test on sands is performed in the same chamber
690 but with the specimens penetrated by a pile. It examines the sand deformation pattern during the continuous
691 penetration with the PIV to measure the strains, including the shear strain, dilatational strain and the depth and
692 width strain development [108]. It is concluded that the PIV can evaluate sand rheology and the rheology-related
693 performance or deformation both quantitatively and qualitatively.

694 Besides the measurement of the particle displacement or velocity, the PIV can also quantify the particle rotation
695 when applying 2D assembly of disks as ideal particles [109]. Therefore, for achieving that, two or more identifiable
696 points need to be followed for each disk. Specifically, the orientation θ of each disk can be defined based on the
697 centroids of the two identifiable points, (x_c, y_c) and (x_s, y_s) :

698 *Equation 2* $\theta = \arctan\left(\frac{y_s - y_c}{x_s - x_c}\right) \quad (0 \leq \theta < 2\pi)$

699 *Equation 3* $\Delta\theta = \theta_j - \theta_i$ (counterclockwise positive)

700 It needs to be noted that the two identifiable points are the centroids of the central and side markers on one disk
701 respectively.

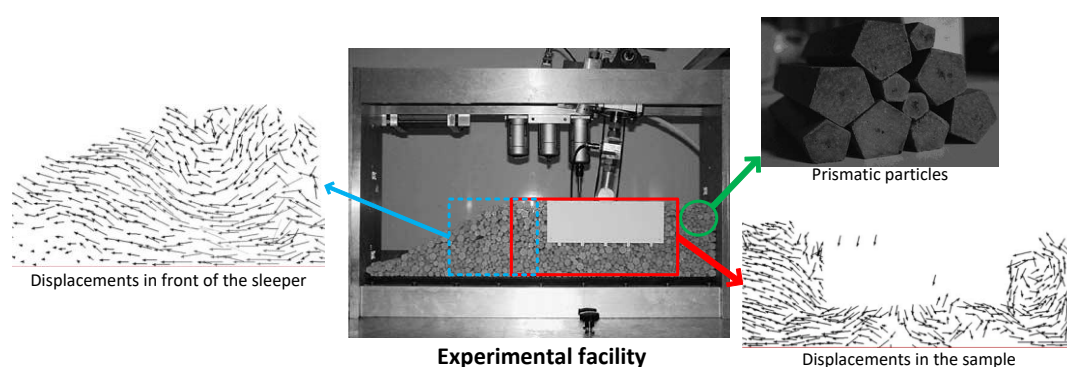
702 From the introduced studies, it can be concluded that the image analysis can be utilised for the rheology study on
703 granular materials, such as soil and sands. Particularly, the PIV (image analysis method) is efficient and accurate
704 for the rheology and rheology-related study for the performance or deformation. Accordingly, it can provide a
705 potential utilisation for railway ballast rheology study, which is relatively unexplored until now. Therefore, the
706 existing applications of image analysis for ballast rheology study are introduced and discussed in the following
707 sub-section. Whilst, some PIV applications for ballast rheology study are also introduced for its future promising
708 utilisation in ballast particle rheology study.

709 **3.2 PIV for railway ballast**

710 Until now, the study on railway ballast rheology is at the initial stage, and it should be focused because the ballast
711 performance and deformation are mainly dependent on its rheology. Some studies have been performed on ballast
712 rheology, however, they could reflect the rheology only at a limited degree. Using the image analysis can efficiently
713 and accurately track all the particles' trajectory during motion, thus it can deepen the understanding of the effect

714 of particle rheology on the performance and deformation.

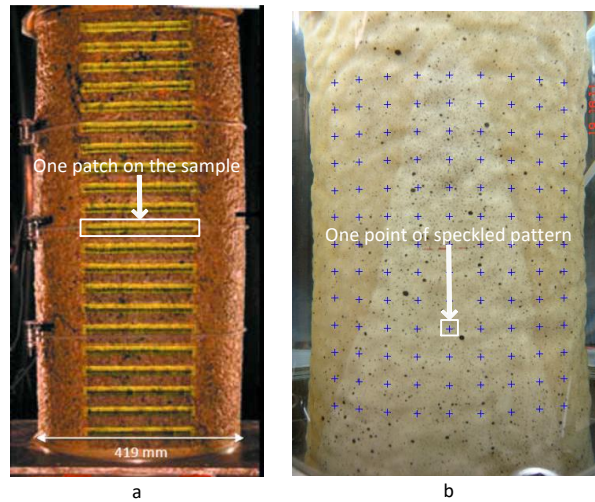
715 For instance, with the lateral view of the whole sample captured periodically by a digital camera, a sinusoidal
716 loading is performed on assemblies of prismatic mineral particles, as shown in Figure 3 (an early-stage PIV
717 example). This article mainly uses the results for the validation of the discrete element simulation in the LMGC90
718 platform, including the settlement and the displacements [23]. The displacement and settlement results demonstrate
719 that the photogrammetry technique can become a tool for ballast rheology study and can be developed further,
720 even though the ballast particles in this test are simplified and scaled down as prismatic particles. The
721 simplification is performed only for matching the element shape in the LMGC90 program.



722

723 *Figure 3 Experimental facility and the displacement results (Modified after [23])*

724 With the development of digital image processing and analysis, the PIV becomes more powerful with more
725 applications in the ballast rheology study (or rheology-related study). For example, the volumetric strain during
726 the triaxial tests can be computed with the PIV by tracking and measuring the movement of the patches painted on
727 the triaxial specimen (Figure 4a). The obtained radial volumetric strain results (different elevations on the sample)
728 is compared with the results (measured by wire extensionometers), demonstrating the possibility and efficiency of
729 the PIV for volumetric strain measurement [110]. However, strain measurement with the PIV is still not sufficient
730 for the ballast rheology study (or rheology-related study), because the translation and rotation of ballast particles
731 cannot be reflected directly from the radial volumetric strain change.



732

733

Figure 4 Markers on triaxial specimen (modified after [110] and [111])

734

Towards these issues, a modified PIV method (proposed in [112]) is utilised for the deformation measurement

735

(principal and maximum shear strains) in the triaxial tests of 1/3rd and 1/5th scaled railway ballast (Figure 4b).

736

From the figure, the markers for tracking have been improved into a speckled pattern, and it can measure the

737

displacements in both the x (circumferential) and y (vertical) directions [111]. The improved PIV method could

738

partly solve the issues by tracking more monitoring points, which can reflect the deformation more accurately and

739

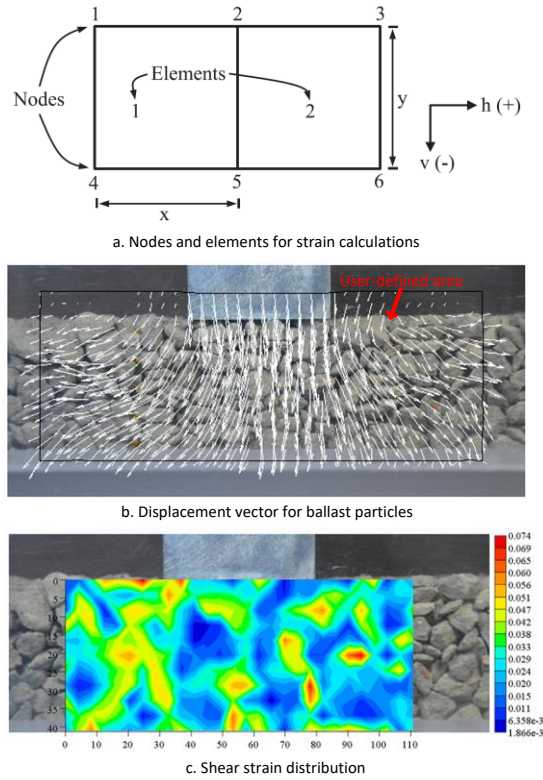
efficiently. However, it still needs improvement when applied for the ballast rheology study (or rheology-related

740

study), because the deformation is measured based on the displacements of the monitoring points rather than the

741

particles.



742

743

Figure 5 Strain calculation method and distribution (modified after [74])

744 Without markers, the deformation and the strains for elements/meshes (Figure 5) could be calculated according to
 745 the displacements of node points (like the markers). The calculation method for strains is shown below. For
 746 example, the vertical strain at element 1 (Figure 5a) could be obtained with the strains between nodes 1 and 4 ($\epsilon_{v,1-4}$)
 747 and between nodes 2 and 5 ($\epsilon_{v,2-5}$), as given in Equation 4.

748 *Equation 4*
$$\epsilon_{v,1} = \frac{\epsilon_{v,1-4} + \epsilon_{v,2-5}}{2}$$

749 Using the strains of all the elements, the strain distribution could be obtained, as shown in Figure 5c. The
 750 improvement is that the number of node points can be determined automatically by users instead of manually-
 751 painting markers, which is achieved by tracking the motions of the same or similar pixels on a user-defined area
 752 in an image (Figure 5b). However, the displacements obtained by tracking the node points are still not the particle
 753 displacements, although the point number can be large enough in high-resolution images [74, 113]. The introduced
 754 examples demonstrate that using the PIV for rheology study of every ballast particles has not been studied so far.
 755 Nevertheless, the PIV is developing step by step, and it is used in more tests, providing more reliable results. For
 756 example, in the rheology study of ballast bed under cyclic longitudinal loadings [114], the PIV is used for tracking

757 the motion of ballast particles, as well as revealing the ballast deformation mechanism and the longitudinal
758 resistance performance. Additionally, this method is worth modification and can provide a potential solution to the
759 difficulty of displacement and velocity tracking of every particles. For instance, tracking the rotation of the ballast
760 particles has not been explored, while in the introduced study [109], this has been successfully applied.

761 **4 Discussion and perspective**

762 This paper reviews the studies on using image analysis to study the morphology, rheology and degradation of
763 granular materials (soil, sands and ballast etc.), due to their significant effects on the ballast performance and
764 deformation. The main aim of this review is to gain insights into the application of image analysis for ballast
765 studies, including the morphology, rheology and degradation.

766 Regarding the morphology, the image analysis methods are introduced, as well as their utilised morphological
767 indices. Moreover, the correlations between the morphological indices and performance or deformation are also
768 presented. Concerning the rheology, the PIV is introduced as a promising image analysis method, for analysing
769 the rheology and rheology-related performance or deformation of granular material layer. Finally, the image
770 analysis methods for particle degradation evaluation are introduced.

771 From the presented image analysis methods, it can be concluded that there still exists some research gaps and
772 aspects for improvement. They are proposed and discussed in the following three sub-sections.

773 **4.1 Morphology**

774 Concerning the morphology, most of the studies focused on using image analysis to replace the traditional
775 measurement methods for accurate particle morphology quantification. In most cases, the shape is categorised into
776 three aspects, the form, angularity and surface texture. Moreover, the size could be evaluated using the
777 morphological indices for the form. The reviewed studies demonstrate the feasibility of image analysis for particle
778 morphology quantification with higher accuracy. However, the image analysis methods may still need
779 improvement at the following aspects.

780 ***From 2D to 3D***

781 The development tendency of image analysis is from 2D to 3D. The image analysis started from the 2D projection

782 or binary image analysis, afterwards, images were taken at two orthogonal directions for higher accuracy. It should
783 be noted that the binary image is similar with the projection. To meet the requirement of higher accuracy, two
784 solutions were proposed. One was utilising the laser scanning to obtain one side image of the particle. The other
785 one was to acquire images at three orthogonal directions. However, they are still not sufficient to present the real
786 particle morphology, because the projections or binary images could not provide the accurate morphological
787 indices until the number of binary images or projections is large enough.

788 After the emergence of 3D image acquisition technology, such as the 3D X-ray, laser scanning etc., several studies
789 were performed with them. From the studies, it was demonstrated that the 3D image analysis methods can present
790 the real particle morphology. More importantly, 3D image analysis is more promising at high accuracy and
791 resolution for even tiny surface details, and it does not enlarge the particle morphology. Furthermore, 3D image
792 analysis enables the quantification of the particle edge, 3D angularity and 3D surface texture, which are still
793 relatively unexplored.

794 ***Comprehensive morphological index***

795 It is more convenient and efficient to combine the three shape characteristics (form, angularity and surface texture)
796 and develop one comprehensive morphological index. Most of the studies estimated the shape characteristics, the
797 form, the angularity and the surface texture respectively, and correlated them respectively with the performance or
798 deformation. However, all of them contribute to the performance and deformation, in other words, it is not accurate
799 to correlate one shape characteristic with the performance or deformation when ignoring the other two.
800 Consequently, it is necessary to create a comprehensive morphological index using the combination of the three
801 or more characteristics e.g. the particle edge.

802 ***Efficient and accurate analysis***

803 It is necessary to improve the image processing and analysis efficiency. Current measurement methods based on
804 image analysis are either accurate but not efficient or fast but not accurate. For example, the Dynamic Image
805 Analysis method, the VDG-40 Videograder (introduced in Sub-section 2.1.1.2) is fast to obtain the particle
806 morphology, however, the obtained form or angularity are not as accurate as the results from 3D image analysis.
807 Whereas, the 3D image acquisition and analysis cost more time and manual work. Therefore, a fast, accurate and
808 automatic method should be developed for acquiring and analysing 3D particle images efficiently.

809 ***Effects of ballast particle morphology on performance and deformation***

810 To date, no studies have been reported on the effects of the ballast particle morphology on performance and
811 deformation using the image analysis methods. However, plenty of studies have proved that particle morphology
812 has significant influence on performance and deformation of granular materials (e.g. sands, soils). The early studies
813 on ballast were only using rough indices to evaluate ballast particle morphology, such as the PSD and the Flat or
814 elongated ratio. That is not sufficient to correlate the ballast particle morphology with the performance and
815 deformation. More importantly, rough indices lead to inconclusive test results and controversial conclusions, as
816 discussed in the Sub-section 1.1. Therefore, it is critical to deepen the understanding of the quantitative relation
817 between ballast particle morphology and the performance and deformation. Moreover, according to the accurate
818 and reliable results, it is easier to reveal the mechanism of ballast mechanics.

819 **4.2 Rheology**

820 According to the reviewed studies, the PIV development history can be observed. It started with the displacement
821 measurement, and then was used to measure the velocity and strain. Moreover, it started with recording the
822 displacement/velocity/strain of the target markers, afterwards, it can measure those of the whole sample without
823 target markers. Based on its development history, it shows the feasibility of image analysis for rheology study.
824 More importantly, the PIV developing trend could provide the suggestions and directions for improvement, which
825 are given as follow.

826 ***Rotation measurement***

827 It is important to develop the particle rotation measurement with the PIV, because the rotation is a significant
828 aspect of particle rheology study. Whereas almost all studies were focusing on the particle translation, measuring
829 the displacement/velocity/strain. Only one author proposed to utilise the PIV for particle rotation measurement,
830 but the particles were idealized as simple discs. Therefore, further developing the PIV for the rotation measurement
831 of normal particles is promising for particle rheology and rheology-related studies.

832 ***Particle morphology***

833 From the reviewed studies on the PIV for railway ballast, the ballast particles were either simplified as prismatic
834 mineral particles or substituted by the 1/3 or 1/5 scaled stones. That is not enough for the ballast rheology study,

835 because the particle shape influences the performance and deformation. Moreover, the rheology is influenced by
836 the gravity and the bulk density, and small particles would usually reach higher compaction.

837 ***Track every individual particle***

838 It is more accurate and convictive to study the particle rheology by tracking every individual particle with the PIV,
839 because archiving this could correlate the performance and deformation with the particle rheology at mesoscopic
840 level. The PIV started by tracking the target markers, obviously, the number of tracked particles is not large enough
841 to reflect the ballast particle rheology. Afterwards, the target markers were replaced by tracking the motions of the
842 same or similar pixels on a user-defined area in an image. However, that is still not tracking the
843 displacement/velocity of every individual particles. Therefore, improvements should be made at this aspect for
844 accurate ballast rheology and rheology-related studies.

845 ***3D PIV***

846 It is necessary to perform the particle rheology study in 3D, because the particle translation and rotation could be
847 presented veritably by 3D. Currently, the PIV was performed on the 2D basis, in other words, it compares the two
848 or more 2D pictures to measure the displacement/velocity. However, the translation could be at any directions
849 rather than only two certain directions, more inaccurately, when it comes to describing the particle rotation in 2D.
850 Consequently, the PIV could be more beneficial if it could measure the particle displacement/velocity in 3D.

851 **4.3 Degradation**

852 It can be concluded that image analysis can be utilised for particle degradation evaluation from the reviewed studies.
853 More importantly, the developing trend is from 2D to 3D, and from the particle morphology change of whole
854 sample to that of every individual particle. However, the current methods are still not enough to evaluate the
855 particle degradation, and it is not sufficient to correlate that with the performance and deformation. Therefore, the
856 improvement aspects are proposed as below.

857 ***From 2D to 3D***

858 One aspect is the estimation of the particle degradation in 3D. Because the particle morphology evaluation in 3D
859 is more promising at high accuracy and resolution and can have more morphological indices e.g. the particle edge
860 (discussed in the sub-section 4.1), while the particle morphology change was utilised in all the introduced

861 degradation evaluation methods.

862 ***Particle breakage evaluation***

863 Another aspect is to propose breakage evaluation methods in 3D. Because the fracture surface of a crushed particle
864 is rough, and that could not be estimated clearly based on 2D images. Moreover, the breakage has many types, e.g.
865 breakage at the sharp corner, in the middle or into pieces, which could also not be estimated in 2D. Nevertheless,
866 limited methods for particle breakage evaluation were found, and no methods were reported for the particle
867 breakage evaluation in 3D. Consequently, it is significant to propose a method for particle breakage evaluation in
868 3D.

869 ***Particle degradation mechanism characterisation***

870 It is not sufficient to evaluate ballast degradation only by characterising it as the breakage and abrasion. In [115],
871 degradation is characterised as the wear (surface polishing), fracture (internal breakage), attrition (removal of sharp
872 edges), abrasion (spherical mother particle left), fragmentation (into different fragments) and chipping (removal
873 of chips). However, according to the introductions, most of the image analysis methods evaluate the ballast
874 degradation by quantifying the morphology change from three aspects, the form, angularity and surface texture.
875 Therefore, more studies could be performed on the possibility of image methods to reveal ballast degradation
876 mechanism from more detailed scales.

877 ***Particle degradation at experimental tests or in the field***

878 The last aspect is a discussion about the difference of particle degradation between experimental tests and field
879 operation. The reviewed studies mostly utilised the experimental tests (the LAA test or the micro-Deval test) for
880 generating the deteriorated particles, although it was demonstrated in [116] that the degradation trend from the
881 LAA tests could not correlate well with the field. Because the deteriorated ballast particles can be generated by the
882 two tests rapidly, and the different degradation stages are easily controlled by setting different revolution numbers.
883 Whereas, the two tests were mostly used to validate the image analysis methods, and hence using them are
884 sufficient for these purposes.

885 However, that is not accurate or sufficient to reflect the real particle degradation form. Moreover, using this kind
886 of deteriorated particles to study their performance or deformation is also far from the reality. Most importantly,
887 ballast particle degradation in the field normally costs years. To solve this problem, it is advised to use the cyclic

888 triaxial test or the similar tests, because they are more realistic than the LAA tests or micro-Deval test, easy to
889 control the degradation stages and faster than in the field tests. Therefore, it is more promising and convictive to
890 combine the cyclic triaxial tests (or similar tests) with the image analysis methods for degradation evaluation and
891 degradation-related studies.

892 **4.4 Perspective**

893 After critically reviewing the research and finding the gap, the authors believe that the image analysis has great
894 potential for railway ballast studies, therefore, some possible research directions are proposed as follows:

- 895 • Image analysis methods for the whole ballast layer should be considered. The image analysis methods
896 should be used to solve the problems as a final goal, (e.g. ballast degradation mitigation and performance
897 improvement). As a first step, the image-based studies for individual ballast particles have been performed
898 in depth. Afterwards, based on that, the image analysis methods for the performance and deformation of
899 the whole ballast layer should be developed, considering the morphology, rheology and degradation. For
900 instance, the images of Ground Penetration Radar (GPR) may be analysed for detecting the ballast
901 rheology when the train is passing.
- 902 • The image analysis could be utilised for exploring the mechanisms of the ballast particle rheology or
903 degradation, and then using the results in the numerical simulations. For more accurate particle
904 morphology presentation in the numerical simulations, the particle images were used to create a shape
905 library in the numerical simulations. However, using the image analysis results of the rheology and
906 degradation in the numerical simulations is relatively unexplored. It is especially interesting to use the
907 mechanisms of the ballast particle rheology or degradation to validate the numerical simulations.
- 908 • The image analysis, including for the particle morphology, rheology and degradation, could be combined
909 for systematic railway ballast studies. Image analysis can be applied for studies from the mesoscopic level
910 (surface texture) to the macroscopic scale (deformation). More interestingly, using the images from the
911 satellite can monitor and predict the railway settlement, as proposed in [117]. The combination of these
912 image analysis methods could provide a deeper understanding of some railway ballast problems,
913 differential settlement et. al, and make the progress for solving these kinds of problems.

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1149

1150 Table 3 Photography analysis (SIA) with 2D output

Reference	Apparatus	Raw data	Study highlights	Output				
				Form	Angularity	Surface texture	Size	Degradation
Clark, 1981	Camera	Unique image of particle	1. Reviewed and summarised three methods for unrolling the particle outline, as explained at the Fourier series .	-	-	-	-	-
Janoo, 1998	Camera	Unique image of particles	1. Summarised the direct methods (image analysis) of form, angularity and surface texture evaluation, and the index tests (indirect methods, e.g. pouring test) for the combination of the three shape characteristics evaluation. 2. Reviewed studies of effects of the three characteristics on the base course performance. 3. Given the prospective of the combined effects of particle shape, fines content and moisture on base course performance.	Circularity	Angularity index or Roundness	Roughness	-	-
Palasamudram & Bahadur, 1997	-	Unique image of particle	The proposed angularity evaluation method considers the sharpness of particle corners and the probability of these corners contacting the target surface.	-	Angularity index	-	-	-
Hyslip & Vallejo, 1997	Camera	Unique image of particles	Fractal dimensioning technique (parallel-line method) is proposed to evaluate the particle surface texture and size (further particle size distribution, PSD). The PSD of well-graded granular soils can be quantified accurately.	-	-	Fractal dimension	Fragmentation fractal dimensioning	-
Brzezicki et al., 1999	Camera; Particles placed on perpendicular walls	Unique image of particles	Single particle projection and two shadows of the particle (in one image) are used to evaluate three dimensions of the particle.	Flat or Elongated ratio	-	-	-	-
Bowman et al., 2000	Scanning electron microscope	Unique image of particles	The Fourier descriptor method is used to solve the problem when the particle outline has a concave shape and has two possible $r(\theta)$ value. Moreover, the Fourier descriptor is utilised to describe the particle shape, and the surface texture.	Fourier descriptor method	Fourier descriptor method	Fourier descriptor method for surface texture	-	-
Kuo & Freeman, 2000	Camera; Particles placed on adhesive transparent	Two perpendicular projections of particles	1. The adhesive Plexiglas tray with two perpendicular walls are used for capturing two perpendicular projections of one particle. 2. The image-based morphological indices of particles correlates well to the effects of particle shape characteristics on hot-mix asphalt concrete mixtures. 3. The particle intermediate axe is utilised as the particle size instead of	Form index and Aspect ratio	Angularity index or Roundness	Roughness	Particle intermediate axe as particle size	-

	plastic trays with two perpendicular faces		the sieve size.					
Mora et al., 2000	Quantimet Q600 image analyser, with 3-chip CCD video camera and a frame grabber with three A/D converters	Unique image of particles	The analyser can measure image characteristics such as area, perimeter and size distribution. The proposed image analysis method can estimate the thickness and volume of the particles. After comparing the earlier angularity evaluation methods with the proposed convexity ratio and fullness ratio, it is found the convexity ratio and fullness ratio can be used for angularity evaluation. 2. The particle size distribution is presented with the percentages by particle area on a stable horizontal surface (area gradation).	Sphericity ; Flaky or elongated ratio ; Shape factor	Convexity ratio and Fullness ratio	-	Volume ; Area gradation	-
Sukumaran & Ashmawy, 2001, 2003	Quantimet 570 image analyser;	Unique image of particles	The analyser can measure image characteristics such as area, perimeter and size distribution. It is demonstrated that the shape characteristics has strong correlation with the drained friction angle and void ratio and the measured maximum or minimum void ratio, further, the flow rate through a flow cone (hopper).	Form index	Angularity index	-	-	-
Wettimuny et al., 2004	Camera; Laser scanning confocal microscope	Two perpendicular projections of particle; 2D contours	The Summation of the square of residual (TSSR; see Table 8), another Fourier series method analysing 2D particle images, is calculated based on the cumulative error (amplitude of the radial vector) between the reconstructed particle profile and the original one.	Form index	-	Roughness factor	-	-
Wang et al., 2005	Camera	Unique image of particle	By the ratio of the reconstructed and original profile areas, the Particle signature is determined. Particle signature at different ranges of frequency are used for the quantification of form, angularity and surface texture. It needs to be noted that this method allows more definitive physical interpretation of the particle's profile features, by using Particle signature at different ranges of frequency.	Form index	Angularity index	Surface texture index	-	-
Sekine et al., 2005	Camera	-	After the LAA tests generating deteriorated ballast particles, the triaxial test and the cyclic loading test (upon a large-scale track model) are performed to study the performance and deformation of ballast particles at different degradation stages. The degradation stages are quantified using the morphological indices from Fourier series. The results show a correlation between the degradation stages and the particle performance or deformation (stiffness, strength and settlement), and demonstrate that the Fourier series method is effective and objective.	Aspect ratio	Angularity index	-	-	Degradation quantification with Fourier series

Zhang et al., 2012	Camera	Two images of particles	The morphological index, Angularity and Surface texture (AT) index is proposed to characterise the combined effect of the particle angularity and surface texture.	-	Angularity index and the Surface texture index	Angularity index and the Surface texture index	-	-
Ozen & Guler, 2014	Desktop flatbed scanner	The scanned images were recorded in grey scale format	After comparing three methods (right side) for particle size distribution evaluation, the maximum ferret diameter is the most suitable size parameter to evaluate particle size distributions.	-	-	-	Equivalent ellipse major axis , particle area and Maximum ferret diameter for particle size distribution	-

1151 Note: the mark “-“ presents not mentioned or not studied in the reference article.

1152

1153 *Table 4 Photography analysis with 3D output*


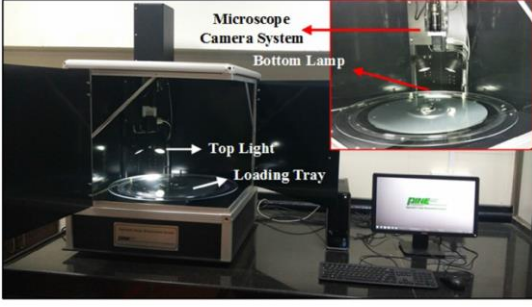
Reference	Apparatus	Raw data	Study highlights	Output				
				Form	Angularity	Surface texture	Size	Degradation
Barksdale et al., 1991	Penpad digitizer, scanning electron microscope	Unique image of particles	The particle shadow is utilised to calculate particles thickness (the shortest axe).	Form index ; Sphericity	-	Roughness	-	-
Kuo et al., 1996	Quantimet Q570 Image Analysis System; Particles placed on	Two perpendicular projections of particles	3D analysis for particles was performed by attaching particles in sample trays with two perpendicular walls for obtaining three axes of the particles.	Sphericity ; Flat or Elongated ratio	Roundness ; Fullness ratio	-	-	-

	adhesive transparent plastic trays with two perpendicular faces							
Fernlund, 2005, 2007	Camera	Two images of particles (maximum and minimum projected area of the particles)	1. With the image-based particle size and shape distribution, the ballast degradation is evaluated by comparing the distribution change.	Flat or Elongated ratio ; Zingg's classification	-	-	All three axes of all the particles	PSD change ; Flat or elongated ratio change
Clayton et al., 2009	Leica Z16APO monocular microscope fitted with a SIS/Olympus CC12 colour camera	Three projected images of particles in three-orthogonal directions	1. After reviewed earlier studies on form, it demonstrates that many proposed measures are 2D and therefore not well suited to the particle shape evaluation. 2. An image-based morphological index for form evaluation is proposed, which is according to the smallest dimension of a scalene ellipsoid with the same volume as the given particle, and the method of measuring it using static imaging is introduced.	Scalene Ellipsoid Equivalent Sphericity	-	-	-	-
Le Pen et al., 2013	Camera	Two different orthogonal projections of particle	1. Developed the Ellipseness, a morphological index, for evaluating and quantifying particle shape. 2. Presented that there are measurable and quantifiable differences (although small) in particle shape with size.	Scalene Ellipsoid Equivalent Sphericity , Zingg's classification	Ellipseness	-	-	-
Okonta et al., 2015 [61]	CCD video camera	Unique image of particles	Two different PSDs of ballast samples are performed LAA tests. Results show that the morphology affected the degradation degree differently, and with the LAA loss decreasing, mean roundness becomes increasingly dependent on both the effect of degradation and grading. This demonstrates the potentiality of using image analysis (digital images) for degradation evaluation and quantification.	-	Roundness	-	-	Mean Roundness change

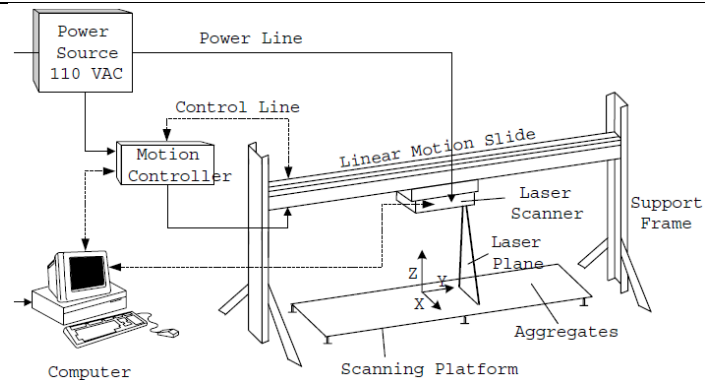
1154

1155 *Table 5 Image analysis systems*



Reference	Apparatus	Raw data	Study highlights	Output				
				Form	Angularity	Surface texture	Size	Degradation


Masad et al., 2011	Aggregate Image Measurement System (AIMS); second generation of Aggregate Image Measurement System (AIMS2)	One high-resolution grey image and one black and white image of particle projections	<p>Apparatuses: the AIMS consists of independent software for characterising particle shape and a computer-controlled system (particle image acquisition). It is equipped with a camera connected with a video microscope (for auto focus), three closed-loop DC servo motor linear actuators, a particle tray and a backlighting table, as shown in figure below. The three actuators are utilised for independent and simultaneous precision movement along three coordinate-axes. The second generation of Aggregate Image Measurement System (referred as AIMS2) is more advanced, which is equipped with two lighting configurations (back lighting and top lighting) and a microscope-camera system enclosed in a box, isolating particles from the outside light sources, as shown in figure below. Besides the lighting improvements, the rotating tray is used to align each particle directly under the camera to ensure that each particle is in full view for the better image acquisition. Both the AIMS and the AIMS2 rank the particle sources the same among every morphological indices and provide comparable results, as reported in [43].</p> <p>Raw data process: the developed user-friendly software is used to analyse the captured images and can evaluate form, angularity and surface texture for both fine and coarse aggregates.</p>	Circularity ; Form index ; Flat or Elongated ratio ; Aspect ratio ; Sphericity ; From index	Radius method ; Gradient method ; Surface Erosion-Dilation technique	Surface Erosion-Dilation technique ; Wavelet transform	-	Surface texture index change ; Angularity index change	
<div style="display: flex; justify-content: space-around; align-items: center;">   </div> <p style="text-align: center;"><i>AIMS (left; reproduced from [118]) and AIMS2 (right; reproduced from [119])</i></p>									
Tutumluer & Rao, 2000, 2009 [42]	University of Illinois Aggregate Image Analyzer (UIAIA); Enhanced-University of Illinois Aggregate Image Analyzer (E-UIAIA)	Three orthogonal images of particle	<p>The UIAIA uses 3 cameras from three orthogonal directions to obtain images. The E-UIAIA is later developed with high-resolution, progressive-scan digital colour cameras. The E-UIAIA is different from the first version (using black-and-white images). By enhancing this together with an advanced colour-thresholding scheme, the E-UIAIA can scan various type of mineral particles [120]. The UIAIA and E-UIAIA can provide more accurate evaluation of the particle shape by calculating the morphological indices with the weighted average of the indices at the three directions automatically. The morphological indices include the Flat and elongated ratio, Angularity index, Surface texture index, Surface area and Volume.</p> <p>Raw data process: The National Instruments LabVIEW™ software and the inserted image analysis package IMAQ Vision library is utilised for performing the necessary</p>	Flat & elongated ratio	Angularity index	Surface texture index	Volume ; Surface area	Morphological indices change	

			user-programmed functions to capture and analyse particle images. The UIAIA operating software includes the following functions: image acquisition, particle volume computation, particle size, particle angularity calculation, and surface texture evaluation.					
				<i>Components of the UIAIA system and details of aggregate detection system (left; reproduced from [121]); E-UIAIA system (right; reproduce from [120])</i>				
Kim et al., 2002	Laser-Based Aggregate Scanning System (LASS)	Upper side 3D image of particles	<p>The Laser-based Aggregate Scanning System (LASS) can solve the problem by obtaining and analysing the 3D particle images. A laser scanner (linear motion slide) passes over the particles with a beam of light spreading out on a platform, as shown in figure below. The scanner captures the coordinates of the points of the laser stripe on the surface. It has a 120 mm scanning width, which means that if the particles are spread within 120 mm, simultaneous scanning of multiple particles is possible. With the resolution at about 0.5 mm in three orthogonal directions, the LASS can scan 15 particles per second, if the particles are smaller than 10 mm (longest axis). The LASS analyses the 3D particle images with higher accuracy, however, it only scans the upper surfaces of the particles. Therefore, the LASS can be considered as the method between 2D and 3D image analysis.</p> <p>Raw data process: The software is written with the IMAQ Vision image processing tool, which is developed by National Instruments. It converts the obtained data into a 2D image and the processing algorithms are utilised to evaluate particle shape from the image, due to the computational efficiency. It also provides almost complete 3D information of every particles, by storing the height data of every particles separately, so that the full 3D data are saved while the 2D image processing techniques are applied to the obtained images. The half 3D images are transformed into grey-scale digital images. Grey-scale pixels determine the height of each datum point.</p>	Form index	Angularity index	Surface texture index	Volume	-



Laser-based aggregate scanning system (figure reproduced from [51])

	3D laser-digitising system	3D image of particle	<p>The 3D laser-digitising system evaluates the particle shape with the Fourier series or the geometrical methods (Cylindrical encompassing method and the Parallel-plane encompassing method). The laser scanner is used to measure the coordinates of the particles by moving along three orthogonal directions.</p> <p>Raw data process: After the particle is scanned, data of its upper and lower sides are saved as the point clouds. The images of the two sides are combined to form a complete 3D particle image. The Fast Fourier series are used for particle shape evaluation based on the rectangular coordinates, when combined with the power spectrum analysis. This method analyses the cross-sections of the 3D particle image, and it is explained at the Analytical Fourier analysis (Lanaro, 2001).</p>	Particle shape categories	-	Roughness	Volume	Degradation index
Lanaro, 2001								
Anochi e-	3D Laser scanning device at CSIR	3D image of particle	The device utilises the laser scanner to scan particles in three dimensions and its resolution can be up to a 0.1mm. A combination of precision optics and motion control	Sphericity; Flat	-	-	Volume	-

Boateng et al., 2012, 2013		<p>with a rigid cast aluminium frame produces high quality scanning of particles. It is able to scan with rotary or plane scanning modes, which is suitable for particles of various types and sizes.</p> <p>Raw data process: the inserted software can combine and merge the scanned surfaces to obtain the complete particle, and then directly obtaining the longest, intermediate and shortest axes of a particle. The surface area and the volume of the particle can be also computed with the inserted software. More importantly, it is proved in [46] that the results of the particle volume and surface area agree quite well with numerical computations. The particle volume can reach the excellent correlation ($R^2 = 0.9994$), while the particle surface area has the difference value within 10^{-5} mm².</p>	and elongate ratio ;			Surface area	
							

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1157 *Table 6 Other image analysis methods*

Reference	Apparatus	Raw data	Study highlights	Output				
				Form	Angularity	Surface texture	Size	Degradation
Hayakawa et al., 2005	3D Scanner	3D image of particle	The device is the same product as the 3D Laser scanning device at CSIR in Table 5. As shown in figure below, two images of the particle with diverse orientations are aligned and merged with the software, PixForm 1.0. With geometrical properties of the 3D image, two morphological indices, i.e. the Modified Wadell's Sphericity and Roundness are utilised for the quantification of the form and the angularity, respectively.	Modified Wadell's Sphericity	Roundness	-	Volume; Surface area	-

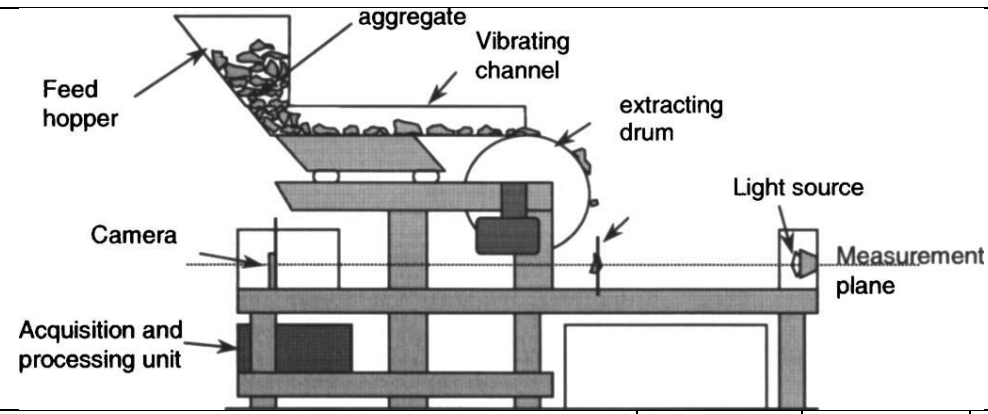
			<p>The Sphericity illustrates a surprisingly high association with Krumbin's Roundness, notwithstanding Sphericity and Roundness are regarded as the morphological indices for form and angularity, respectively. The new morphological index (modification of the true sphericity) is proposed to show the differences of particle shape from an ellipsoid that has given axe lengths. This morphological index shows little correlation with Roundness and particle size.</p>					
<p><i>3D particle image acquisition (reproduced from [59])</i></p>								
Ouhbi et al., 2017	3D scanner	3D Surface points of particle	<p>After the 3D scanning, around 300,000 surface points for one particle are obtained. The 3D scanner was not described in details in their research paper. Raw data process: normal aim of the proper orthogonal decomposition (POD) is extracting the dominant features from the total data, afterwards building a simplified model. Here, the method utilises the method for enabling shape description with a controlled accuracy.</p>	Form index	-	-	-	-
Sun et al., 2014	3D laser scanner (VIVID 910)	3D image of particle	<p>The specific description of the device is not mentioned in their paper. The study utilises the three dimensions and surface area of the particle to calculate the morphological index. A morphological index for form evaluation is proposed. Raw data process: the computer software Geomagic Qualify 12 (version 15.0) is utilised for the raw data process, including, forming the 3D triangulate model, restoring the small holes and eliminating the noises. The surface area of the particle is computed by summing up all the triangles' area, while the volume is calculated by summing up all the sub-volumes of the tetrahedral mesh, which are the same methods that are mentioned in the Anochie-Boateng's study.</p>	-	Ellipsoidness	-	Volume; surface area	-
Garboczi et al., 2002	X-ray CT scanner	3D image of particle	<p>For the 3D images, the Spherical harmonics series (Fourier series method) is utilised for reconstructing and quantifying the particle shape according to measurements performed on the 3D images [82].</p>	-	-	-	Volume; surface area	-
Erdoğan et al., 2006	X-ray CT scanner	Reconstructed 3D image of particle	<p>2D images from X-ray can be reconstructed to form the 3D image with appropriate algorithms, which is the spherical harmonic reconstruction.</p>	Flat or Elongated ratio	-	-	-	-

Tunkin & Denis, 2014	X-ray CT scanner; laser displacement sensor	Reconstructed 3D image of particle; a face of particle	<p>The main components of X-ray CT scanner include the X-ray generator, detector and rotation stage, which are put into a large box. The 2D images at different angular positions reconstruct the 3D image of the particle with appropriate algorithms. The abraded parts after tests can be seen after aligning and comparing the 2D images together with transforming the 2D images into 3D ones.</p> <p>The laser displacement sensor uses the direct reflected light of a red laser beam for obtaining the distance to the surface by measuring the light traveling time.</p> <p>Raw data process: the particle form and angularity are analysed with the Spherical harmonics series. The spherical harmonic coefficients utilised for the form and angularity are 5 and 25, respectively.</p>	Sphericity ; Flat or Elongated ratio ; Form index	Angularity index	Several indices are given in [45]	-	Abraded part of particle ; changes of morphological indices
Guo et al., 2018	3D scanner	3D image of particle	<p>A particle is placed on a black turntable, which can spin during scanning process to get images of every particle side. The blue light reflected from particle surface is captured by coupled device camera. About 500,000 vertices are transmitted to the computer, and three consequent images are used to form one triangular plane. Finally, all small triangular planes constitute the 3D ballast particle image.</p> <p>Raw data process: the two particle images before and after LAA test are aligned and compared for checking the differences. In addition, the volume change is also checked in this study.</p>	Sphericity	-	-	Volume ; surface area	Degradation evaluation by 3D image difference

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1159 *Table 7 Dynamic image analysis methods*

Reference	Apparatus	Raw data	Study highlights	Output				
				Form	Angularity	Surface texture	Size	Degradation
Descantes, et al., 2006 [122]	VDG40 Videograder	Unique projection of particle	<p>As shown in figure below (reproduced from [122]), the VDG40 is developed by the Laboratoire Central des Ponts et Chaussées (LCPC). It consists of an apparatus to feed the particles (passing the backlight), and a line-scan CCD camera to capture particle images. The CCD camera has a resolution of 1,024 dots and a 13 kHz scan frequency. The VDG-40 can be used for measuring granular materials, whose size ranges are from 1.18 mm to 38.1 mm.</p> <p>Raw data process: the algorithm (assuming particles are elliptical) is utilised to compute each particle's three axes with the 2D projection.</p>	Shape Class Average Ratio (SCAR)	Angularity index	Surface texture index	Particle size distribution; volume	Angularity index change



<p>Rauch et al., 2002 [123]</p>	<p>Micrometrics OptiSizer System</p>	<p>Unique image of particles</p>	<p>This apparatus was originally developed for online measurements. It utilises a matrix CCD camera to photograph and evaluate particles when falling in front of the backlight (about twice per second). The particle sizes that can be measured are from a No. 200 mesh sieve size (0.075 mm) up to at least 1.5 inch (38.1 mm). Like the above DIA system, an idealized shape of particles is used to provide information about particle size distribution and shape. Raw data process: The spherical type analysis converts each imaged particle profile area into a circle with equal area. The volumetric information is calculated with the radius of the circle as a sphere volume. The cubic analysis converts particle profile area into a square with equal area. The volume information is then calculated as a cube with the side dimension of the square.</p>	<p>Spherical analysis; cubic analysis</p>	<p>-</p>	<p>-</p>	<p>Volumetric information</p>	<p>-</p>
<p>Rauch et al., 2002 [123]</p>	<p>Video Imaging System</p>	<p>Unique image of particles</p>	<p>The Video Imaging System (VIS) is developed for on-line particle measurements. It is designed to combine the Micrometrics OptiSizer System with the developed conveyor belt sweep samplers. It can analyse particles from 1.18 mm sieve to 38.1 mm. Raw data process: it is not described in details in the literature.</p>	<p>Yes</p>	<p>-</p>	<p>-</p>	<p>Yes</p>	<p>-</p>
<p>Rauch et al., 2002 [123]</p>	<p>Buffalo Wire Works System Particle Size Distribution Analyzer (PSDA)</p>	<p>Unique image of particle</p>	<p>The PSDA utilises vibratory feeder to create a curtain of backlit and a progressive matrix CCD camera. It does not take all the particles' images in the sample. It can automatically adjust the camera focus and optimise the backlight according to the settings for various particle size ranges. It can measure particles ranging from 0.075 to 38 mm. After the samples are put into the vibratory</p>	<p>Form index</p>	<p></p>	<p></p>	<p>Yes</p>	<p>-</p>

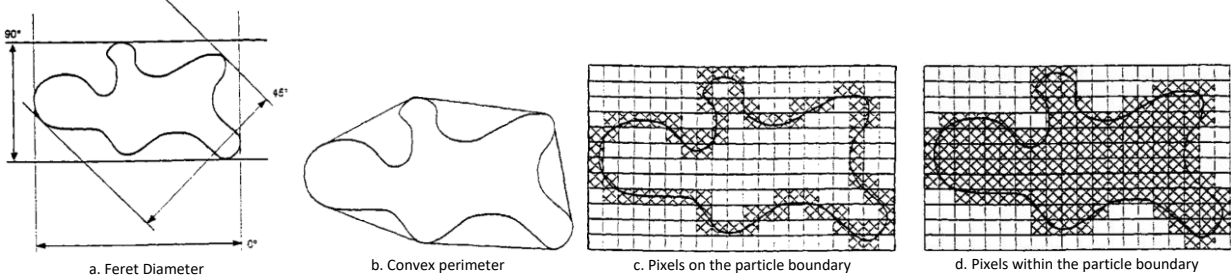
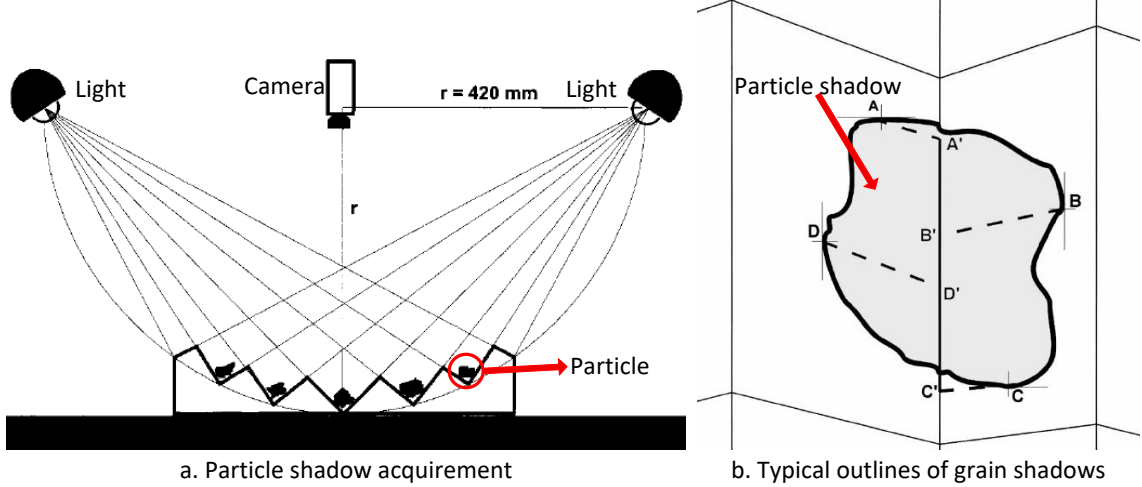
			feeder, the computer controls the measuring process. It has the unique feature that is the automatic measurement stops once enough data for the correct PSD have been obtained. Raw data process: the proprietary software is utilised to obtain the size and shape.					
Browne et al., 2002 [87]	Computer Particle Analyser (CPA)	Unique projection of particle	Like the VDG40, the CPA utilises a line-scan CCD camera to photograph each particle in the sample when they are falling in front of a backlight. Particle size is tabulated as a function of particle count, afterwards a simple correlation factor is utilised to transform the data into the volume gradation. Three different version of CPA can measure three different particle size ranges. The CPA-4 analyses particle size up to 600 μ m in size. Raw data process: the proprietary software is utilised to obtain the size and shape.	Flat or elongated ratio	-	-	Size method; shape method	-
Rauch et al., 2002 [123]	Camsizer	Two images of particle	The Camsizer system uses two cameras to photograph images at different resolutions. It measures the particles in the sample when they are falling in front of a backlight. Using two cameras improves the accuracy of measuring the morphology of both coarse and fine particles. It measures the particle size range from 20 μ m to 30 mm. Raw data process: the proprietary software is utilised to obtain the size and shape.	Sphericity; convexity	Roundness	-	Particle width	-

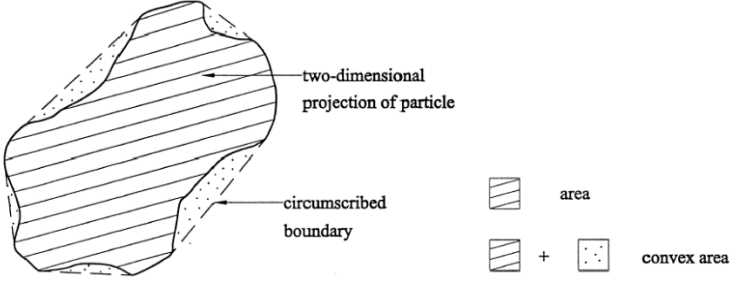
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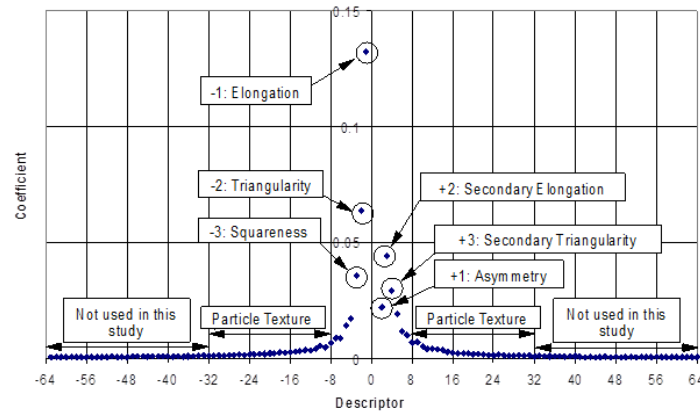
1161 *Table 8 Descriptions of the morphological indices for the form quantification (summarised from [8, 39, 42, 45, 50, 124-126])*

Reference	Description of the morphological indices	Calculation methods
Two-dimensional		
Manual measurement Pentland, 1927 [127]	The Circularity (C) is the ratio of the outline area to circle area. In the equation: A – the outline area; A_C – the longest length as diameter of outline area.	$C = \frac{A}{A_C}$
Manual measurement Tickell, 1931 [124]	The Circularity (C) is the ratio of the outline area to the circumscribed circle. In the equation: A – the outline area; A_C – the area of smallest circumscribed circle.	$C = \frac{A}{A_C}$
Manual measurement Wadell, 1935 [15]	The Sphericity (ψ) is computed based on the particle and sphere diameters. In the equation: D_A – the diameter of a circle with the same area; D_C – the diameter of the smallest circumscribed circle. The Circularity (C) is the ratio of the circle perimeter to outline perimeter. In the equation: P_C – the circle perimeter with the same area as the particle outline; P – the actual particle outline perimeter.	$\psi = \frac{D_A}{D_C}$

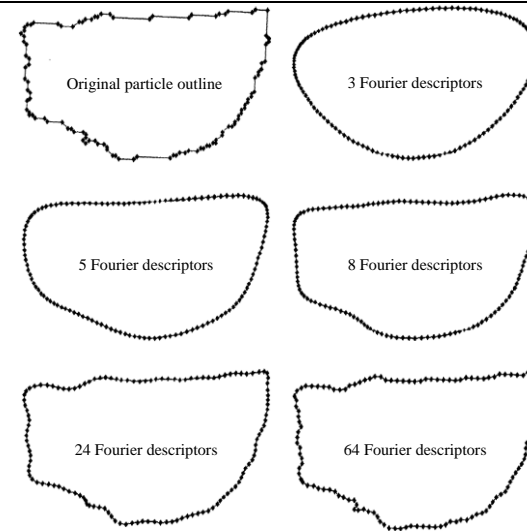
		$C = \frac{P_C}{P}$
Manual measurement Riley, 1941; AIMS Masad et al., 2000; Al-Rousan et al., 2007 [124]	The Circularity (C_1) is expressed as the ratio of the outline area to perimeter, shown in the Equation 1. In the equation: A – the outline area; P – the outline perimeter. The Sphericity (C_2) is expressed as the diameters of inscribed and circumscribed circles, shown in the Equation 2. In the equation: D_I – the diameter of inscribed circle; D_C – the diameter of circumscribed circle. Note: C_1 was reused in 2000 by Masad [8], and in 2007 by Al-Rousan with image analysis [53].	$C_1 = \frac{4\pi A}{P^2} \quad (1)$ $C_2 = \sqrt{\frac{D_I}{D_C}} \quad (2)$
Fourier series Clark, 1981 [63]	Radius Expansion method is expressed at the right side. In the equations: $r(\theta)$ – the radius length at angle θ ; A_n – the phase angles; c_n – the amplitudes. It needs to note that the Equation 1 depends on the point around the periphery from where the outline starts, for that the Equation 2 as the alternative representation is more convenient.	$r(\theta) = a_0 + \sum_{n=1}^{\infty} a_n \sin(n\theta) + \sum_{n=1}^{\infty} b_n \cos(n\theta) \quad (1)$ $r(\theta) = c_0 + \sum_{n=1}^{\infty} c_n \cos(n\theta - A_n) \quad (2)$ $c_n^2 = a_n^2 + b_n^2 \quad (3)$ $A_n = \tan^{-1}(b_n / a_n) \quad (4)$
	Angular bend function is presented at the right side. The outline is presented as chords that change their angular direction. The length and the angle are utilised for the Fourier series. In the equation, $\theta = 2\pi l/L$; L – the total perimeter length; α^* is the cumulative angular change from the origin.	$\alpha^*(l) = c_0 + \sum_{n=1}^{\infty} c_n \cos(n\theta - A_n)$
	In the Complex function, particle outline is treated as a complex function generated by a point moving around the boundary. In the equations, l – the arc length along the outline; $\theta = 2\pi l/L$; L – the total perimeter length;	$u(l) = x(l) + iy(l) \quad (1)$ $x(l) = \sum_{n=-\infty}^{\infty} c_n \cos(n\theta) \quad (2)$ $y(l) = i \sum_{n=-\infty}^{\infty} c_n \sin(n\theta) \quad (3)$
PA Janoo, 1998 [54]	The Circularity (C) is computed according to the outline perimeter and area, as shown in the equation. In the equation: P – the perimeter of the particle outline; A – the area of the particle outline. The Feret Diameter was also introduced in [54], which is described as the longitude between two parallel tangents, as shown in Figure a. Based on the Feret Diameter at eight different degrees (0, 22.5, 45, 67.5, 90, 112.5, 135, and 157.5), the convex perimeter is measured as the string around the tips of the eight Ferets (Figure b). Note: as shown in the Figure c & d, the particle area is computed by the sum of pixels within the particle boundary, while the particle perimeter is by the sum of pixels on the particle boundary (figures modified after [54]).	$C = \frac{P^2}{A}$

	 <p>a. Feret Diameter b. Convex perimeter c. Pixels on the particle boundary d. Pixels within the particle boundary</p>	
<p>PA</p> <p>Brzezicki et al., 1999 [73]</p>	<p>Three dimensions of a particle (L, W, H) are obtained from its shadow, as shown in Figure a & b (figure modified after [73] with permission from ASCE). In the equations: width (W) – BB' (Figure b); height (H) – DD'; length (L) – $A'C'$. Elongated ratio (ER) – the ratio of the length to the width; Flat ratio (FR) – the ratio of the width to the height.</p>	$ER = L/W \quad (1)$ $FR = W/H \quad (2)$
<p>PA</p> <p>Brzezicki et al., 1999 [73]</p>	 <p>a. Particle shadow acquisition b. Typical outlines of grain shadows</p>	
<p>PA</p> <p>Mora et al., 2000 [67]</p>	<p>The Convexity ratio (R_C) and the Fullness ratio (R_F) are expressed based on the outline area and the convex area, as shown in figure below and the equations at right side (figure modified after [67]). In the equations: Convex area (A_{CON}) – the area of the minimum convex boundaries circumscribing the particle; A – the outline area.</p>	$R_C = \frac{A}{A_{CON}} \quad (1)$ $R_F = \sqrt{\frac{A}{A_{CON}}} \quad (2)$

	 <p style="text-align: center;">Evaluation of area and convex area</p>	
<p>PA Kuo & Freeman, 2000 [89]</p>	<p>The Form index (FI) is the square of the ratio of the perimeter (P_C) of an equivalent circle to the perimeter (P) of the particle.</p> <p>The Aspect ratio is presented by the ratio of the length to the width. In the equation: Length – the maximum Feret diameter; Width – the minimum Feret diameter. The Feret diameter was introduced at Janoo, 1998 in Table 8.</p>	$FI = \left(\frac{P_C}{P} \right)^2 \quad (1)$ $Aspect\ ratio = \frac{Length}{Width} \quad (2)$
<p>Fourier series Bowman et al., 2000 [65]</p>	<p>The Fourier descriptor method is to use general shapes to determine the coefficient values of the Fourier shape descriptors. Afterwards the descriptor coefficients of the particle are compared with the descriptor coefficients of the general shapes to decide the particle morphology, as shown in Figure a & b and the equations at right side (figure modified after [65]).</p> <p>In the Equation 1: x, y – coordinates describing the particle outline; N – the total number of descriptors; n – the descriptor number; M – the total number of points describing the particle; m – the index number of a point on the particle; a, b – coefficients for each descriptor; i – an imaginary number.</p> <p>The descriptor coefficient (c_n) is computed by the coefficients for each descriptor (a_n, b_n), as shown in the Equation 2.</p> <p>Note: Fourier shape descriptors (for morphological description): the elongation, trigularity, squareness, irregularity; 0 – Radius, -1 – elongation, -2 – triangularity, -3 – squareness, +1 – irregularity, +2 – second order Elongation, +3 – second order triangularity.</p>	$x_m + iy_m = \sum_{n=-N/2+1}^{N/2} (a_n + ib_n) \left[\cos\left(\frac{2\pi nm}{M}\right) + i \sin\left(\frac{2\pi nm}{M}\right) \right] \quad (1)$ $c_n = \sqrt{a_n^2 + b_n^2} \quad (2)$



a. Descriptor magnitudes for a typical particle



b. The effect of reconstruction of a particle from complex Fourier descriptors using successively fewer descriptors

The Form index (FI) is defined as the deviation of the global particle outline from a circle, as shown in the figure below and the equation at right side (figure modified after [77]). In the equation: N – the number of sampling intervals; α_i – shown in the figure.

$$FI = \frac{\sum_{i=1}^N |\alpha_i|}{N \times 45^\circ}$$

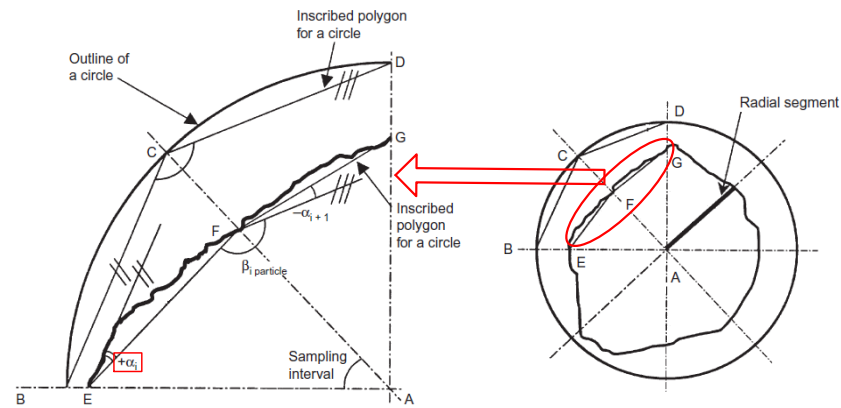


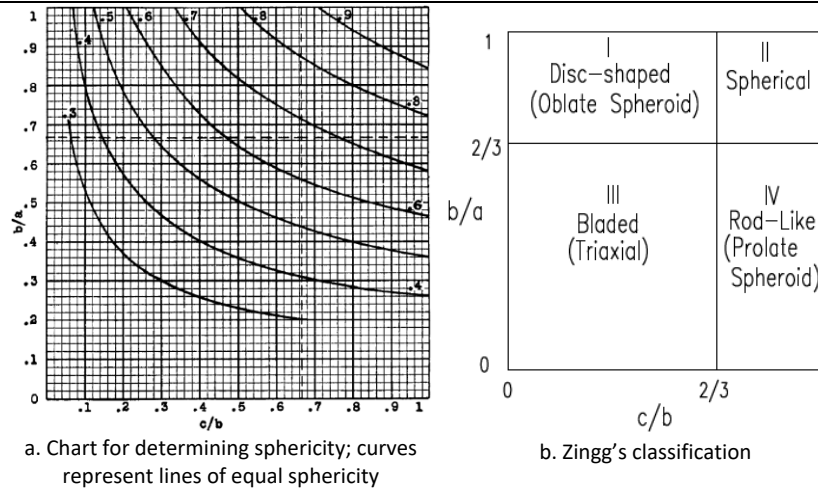
Illustration of the geometric quantities used to determine Slope and Angularity Factors

PA

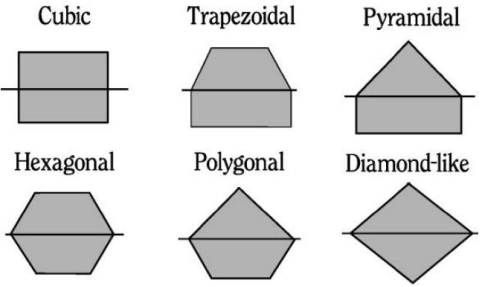
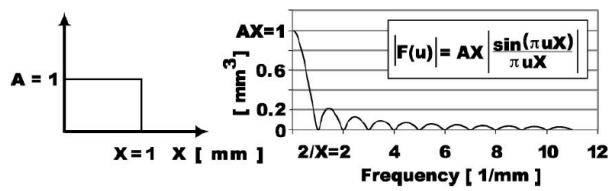
Sukumaran & Ashmawy, 2003 [77]

<p>Fourier series Wettimuny et al., 2004 [80]</p>	<p>The Form index (<i>FI</i>) is defined as the average of the $TSSR_n$ ($n = 2,3,4,5,6$), as shown in the Equation 2. The $TSSR_n$ (total summation of the square of residual) is defined as the Equation 1. In the equation: i – the ith sampling angle for the radial measurement; d – the total number of the radial measurements; $r_{o,i}$ – the amplitude of the original radial vector; $r_{o,i/n}$ – the amplitude of radial vector of the reconstructed shape profile using n largest harmonics.</p>	$TSSR_n = \sqrt{\sum_{i=0}^{d-1} \left(\frac{r_{o,i} - r_{o,i/n}}{r_{o,i}} \right)^2} \quad (1)$ $FI = \text{average}(TSSR_2, TSSR_3, TSSR_4, TSSR_5, TSSR_6) \quad (2)$
<p>Fourier series Wang et al., 2005 [81]</p>	<p>The Particle signature parameter α is defined according to the equivalent radius of a circle (R_0) and the average radius (a_0) of the profile outline. In the equation: α_s – the form; α_r – the angularity; α_t – the surface texture; R_0 – obtained with the Equation 2 & 3. In the equation 2 & 3: A – the area of the particle outline. Note: the particle size in this study is around 25 mm in diameter. The following ranges of frequency are used to define the form, angularity, and surface texture should be used, form terms ($m \leq 4$); angularity terms ($5 \leq m \leq 25$); and surface texture terms ($26 \leq m \leq 180$).</p>	$\alpha = \left(\frac{R_0}{a_0}\right)^2 = 1 + \frac{1}{2} \sum_{m=1}^{m=n1} \left[\left(\frac{a_m}{a_0}\right)^2 + \left(\frac{b_m}{a_0}\right)^2 \right] + \frac{1}{2} \sum_{m=n1+1}^{m=n2} \left[\left(\frac{a_m}{a_0}\right)^2 + \left(\frac{b_m}{a_0}\right)^2 \right] + \frac{1}{2} \sum_{m=n2+1}^{m=\infty} \left[\left(\frac{a_m}{a_0}\right)^2 + \left(\frac{b_m}{a_0}\right)^2 \right] = 1 + (\alpha_s + \alpha_r + \alpha_t) \quad (1)$ <p>where $\alpha_s = \frac{1}{2} \sum_{m=1}^{m=n1} \left[\left(\frac{a_m}{a_0}\right)^2 + \left(\frac{b_m}{a_0}\right)^2 \right]$ $\alpha_r = \frac{1}{2} \sum_{m=n1+1}^{m=n2} \left[\left(\frac{a_m}{a_0}\right)^2 + \left(\frac{b_m}{a_0}\right)^2 \right]$ $\alpha_t = \frac{1}{2} \sum_{m=n2+1}^{m=\infty} \left[\left(\frac{a_m}{a_0}\right)^2 + \left(\frac{b_m}{a_0}\right)^2 \right]$</p> $R_0^2 = A/\pi \quad (2)$ $A = \int_0^{2\pi} \frac{1}{2} R_2(\theta) d\theta = \pi \left[a_0^2 + \frac{1}{2} \sum_{m=1}^{\infty} (a_m^2 + b_m^2) \right] \quad (3)$
<p>AIMS Masad et al., 2001; Al-Rousan et al., 2005, 2007 [53]</p>	<p>The Form index (<i>FI</i>) is computed by the sum of the incremental changes in the particle radius in all directions. In the equation: R – the radius of the particle in different directions; θ – the directional angle. Note: this morphological index could analyse the 3D images and was utilised by Rousan in 2007.</p>	$FI = \sum_{\theta=0}^{355} \frac{ R_{\theta+5} - R_{\theta} }{R_{\theta}}$
<p>Fourier series Sekine et al., 2005 [92]</p>	<p>Aspect ratio with Fourier series (Radius Expansion): $r(\alpha)$ – the distance from the point on the outline to the centre; the nth amplitude spectrum is expressed by the Equation 2; a_n and b_n are expressed by the Equation 3 and 4, respectively; the Aspect ratio is calculated by the ratio of the second and zero order amplitude spectrums, as shown in the Equation 5.</p>	$r(\alpha) = b_0/2 + \sum_{n=1}^{\infty} \{ a_n \sin(n\alpha) + b_n \cos(n\alpha) \} \quad (1)$ $c_n = \sqrt{a_n^2 + b_n^2} \quad (2)$ $a_n = \frac{1}{\pi} \int_{\alpha_0}^{\alpha_0+2\pi} r(\alpha) \sin(n\alpha) d\alpha \quad n=1,2, \quad (3)$ $b_n = \frac{1}{\pi} \int_{\alpha_0}^{\alpha_0+2\pi} r(\alpha) \cos(n\alpha) d\alpha, \quad n=0,1,2 \quad (4)$

		$R_{fv} = c_2/c_0$ (5)
Descantes, et al., 2006	The Shape Class Average Ratio (SCAR) is computed by the product of the slenderness ratio and flattening factor. Slenderness ratio (SR) is the ratio of the particle length (a) to width (b), as shown in the equation. The flattening factor is calculated by the ratio of the particle width to an estimate of the average particle thickness	$SR = a/b$
AIMS Al-Rousan et al., 2007 [53]	The Aspect ratio (A_r) is the ratio of the major axe (L) to the minor axe (W) of the ellipse equivalent to the particle outline. The equivalent ellipse has the same area, first degree moment, and second-degree moment as the particle outline.	$A_r = \frac{L}{W}$
PA Clayton et al., 2009 [128]	The scalene ellipsoid equivalent sphericity ($SEES$) is expressed as the equation at the right side. In the equation: W – the mass of the specimen; n – the number of particles; G_s – the density; L – the average major particle dimension; I – the average intermediate particle dimension.	$SEES = \frac{S}{L} = \frac{(W / nG_s)(6 / \pi IL)}{L}$
Three-dimensional		
Manual measurement Wentworth, 1922 [49]	The Sphericity (Ψ) is expressed based on the three orthogonal dimensions, as shown in the equation at right side. In the equation: a – the longest axe; b – the medium axe; c – the shortest axe.	$\psi = \frac{a+b}{2c}$
Manual measurement Wadell, 1932, 1934 [15]	The Sphericity (Ψ_1) is expressed as the Equation 1. In the equation: S_n – the surface area of a sphere having the same volume as the particle; S_o – the actual surface area. The Sphericity (Ψ_2) is expressed using the particle and sphere volumes, as shown in the Equation 2. In the equation: V_P – the volume of the particle; V_{CIR} – the volume of the circumscribed sphere. The Sphericity (Ψ_3) is expressed using the diameters of the particle and its equivalent sphere, as shown in Equation 3. In the equation: D_{SV} – the sphere diameter with the same volume value as the particle; D_{CIR} – the diameter of a circumscribed sphere.	$\psi_1 = \frac{S_n}{S_o}$ (1) $\psi_2 = \sqrt[3]{\frac{V_P}{V_{CIR}}}$ (2) $\psi_3 = \frac{D_{SV}}{D_{CIR}}$ (3)
Manual measurement Krumbein, 1941 [48]	The Sphericity (Ψ) is expressed based on the three dimensions of the particle, as shown in the equation at right side. In the equation: a – the longest axe; b – the medium axe; c – the shortest axe. The chart for determining Sphericity and the Zingg’s classification are decided according to the described morphological index, as shown in Figure a & b (figure reproduced from [48]).	$\left(\frac{b}{a}\right)^2 = \frac{\psi^3}{(c/b)}$



Manual measurement Pye & Pye, 1943; Kuo et al., 1996 [89]	The Sphericity (Ψ) is expressed based on the three dimensions of the particle, as shown in the equation at right side. In the equation: a – the longest axis; b – the medium axis; c – the shortest axis. Note: this morphological index was also used by Kuo in 1996 with image analysis.	$\Psi = \sqrt[3]{\frac{b \cdot c}{a^2}}$
Manual measurement Corey, 1949; PA Barksdale et al., 1991; Kuo et al., 1996 [64]	The Form index (FI) is expressed based on the three dimensions of the particle, as shown in the equation at right side. In the equation: a – the longest axis; b – the medium axis; c – the shortest axis. Note: this parameter was used by Barksdale in 1991, and also by Kuo in 1996.	$FI = \frac{c}{\sqrt{a \cdot b}}$
Manual measurement Aschenbrenner, 1956 [129]	The Form index (FI) is expressed based on the three dimensions of the particle, as shown in the equation at right side. In the equation: a – the longest axis; b – the medium axis; c – the shortest axis.	$FI = \frac{a \cdot c}{b^2}$
Manual measurement Williams, 1965 [130]	The Form index (FI) is expressed based on the three dimensions of the particle, as shown in the equations at right side. In the equation: a – the longest axis; b – the medium axis; c – the shortest axis.	$FI = 1 - \frac{a \cdot c}{b^2} \quad \text{when } b^2 > ac ;$ $FI = \frac{a \cdot c}{b^2} - 1 \quad \text{when } b^2 \leq ac$
Manual measurement Janke, 1966 [124]	The Form index (FI) is expressed based on the three dimensions of the particle, as shown in the equation at right side. In the equation: a – the longest axis; b – the medium axis; c – the shortest axis.	$FI = \frac{c}{\sqrt{\frac{a^2 + b^2 + c^2}{3}}}$

<p>Manual measurement Dobkins & Folk, 1970 [131]</p>	<p>The Oblate-prolate index (<i>OPI</i>) is expressed based on the three dimensions of the particle, as shown in the equation at right side. In the equation: <i>a</i> – the longest axis; <i>b</i> – the medium axis; <i>c</i> – the shortest axis.</p>	$OPI = \frac{10 \left(\frac{a-b}{a-c} - 0.5 \right)}{\frac{c}{a}}$
<p>Manual measurement Sneed & Folk, 1985 [47]</p>	<p>The Sphericity (Ψ) is expressed based on the three dimensions of the particle, as shown in the equation at right side. In the equation: <i>a</i> – the longest axis; <i>b</i> – the medium axis; <i>c</i> – the shortest axis.</p>	$\Psi = \sqrt[3]{\frac{c^2}{a \cdot b}}$
<p>PA Kuo et al., 1996 [89]</p>	<p>The Sphericity (Ψ) is expressed based on the three dimensions of the particle, as shown in the Equation 1. In the equation: <i>a</i> – the longest axis; <i>b</i> – the medium axis; <i>c</i> – the shortest axis. The Form index (<i>FI</i>) is expressed based on the three dimensions of the particle, as shown in the Equation 2. In the equation: <i>a</i> – the longest axis; <i>b</i> – the medium axis; <i>c</i> – the shortest axis. Note: the above-mentioned two morphological indices were proposed by Krumbein in 1941 [48] and Corey in 1949 [124], respectively, with manual measurement. Afterwards, Kuo utilised them with image analysis method. The method acquires the two perpendicular projections of one particle for 3D analysis.</p>	$\Psi = \sqrt[3]{\frac{b \cdot c}{a^2}} \quad (1)$ $FI = \frac{c}{\sqrt{a \cdot b}} \quad (2)$
<p>Fourier series Lanaro, 2001 [75]</p>	<p>The Fourier series is utilised for the form estimation by comparing the power spectrum of particle image cross-section with that of the particle shape categories, shown in Figure a (modified after [75]). The power spectrum is expressed based on the equations at right side. Equation 1 is the Fourier transform. In the equation, the u/M and v/n are the frequency variables, and the sine and cosine curves explicitly appear when using Euler's formula for <i>i</i>. Equation 2 is the theoretical expression of the power spectrum (Figure b). In the equation: $1/X$ – the period of the frequency spectrum; AX – the maximum value of the spectrum.</p>	$F(u, v) = F \{ f(x, y) \}$ $= \sum_{u=0}^{M-1} \sum_{v=0}^{N-1} f(x, y) \cdot \exp \left[-2\pi i \left(\frac{xu}{M} + \frac{yv}{N} \right) \right] \quad (1)$ $ F(u) = AX \left \frac{\sin(\pi u X)}{\pi u X} \right \quad (2)$
<div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: center;"> <p>a. Particle shape categories</p>  </div> <div style="text-align: center;"> <p>b. Frequency spectrum for a rectangular</p>  </div> </div>		

<p>LASS Kim et al., 2002 [51]</p>	<p>The Form index (FI) is expressed as the Equation 1. In the equation: E – energy, summation of absolute values of all the elements; $d_{i,j,k,l}$ – wavelet coefficients at a decomposition level i. The wavelet coefficients ($d_{i,j,k,l}$) are obtained from two steps. Equation 2 is the first step, which is to transform Cartesian coordinates into the polar coordinates. In the equation: α – the horizontal angle; β – the vertical angle; i – the decomposition level; j – the scale coefficients; k – the translation coefficients; $f(\alpha, \beta)$ – the length of the radius vector at angle α and β; $W_{i,j,k,0} = \varphi(2^{-i} \alpha^j) \psi(2^{-i} \beta^k)$; $W_{i,j,k,l} = \psi(2^{-i} \alpha^j) \varphi(2^{-i} \beta^k)$; $W_{i,j,k,2} = \psi(2^{-i} \alpha^j) \psi(2^{-i} \beta^k)$. Equation 3 is the second step, which is to express the Wavelet coefficients. Note: the detailed procedures of wavelet transform decomposing for signals are introduced in [51].</p>	$FI = \frac{E(d_{0,j,k,l}) + E(d_{1,j,k,l})}{\text{average radius}} \quad (1)$ $d_{i,j,k,l} = \left[f(\alpha, \beta), W_{i,j,k,l}(\alpha, \beta) \right]$ $= \int_{-\infty}^{\infty} f(\alpha, \beta) W_{i,j,k,l}(\alpha, \beta) d\alpha d\beta \quad i, j, k \in Z, l \in [0, 2] \quad (2)$ $f(\alpha, \beta) = \sum_{i=-\infty}^{\infty} \sum_{j=-\infty}^{\infty} \sum_{k=-\infty}^{\infty} \sum_{l=0}^2 d_{i,j,k,l} W_{i,j,k,l}(\alpha, \beta) \quad i, j, k \in Z, l \in [0, 2] \quad (3)$
<p>Fourier series Garboczi et al., 2002 [82]</p>	<p>The first step is to measure the radius of the particle at 240 surface points, which are Gaussian quadratures. Afterwards, the Equation 1 is utilised to reconstruct the particle. In the Equation 1: $R(\theta, \phi)$ – the radius measured from the centroid to the surface; θ – the angle measured from positive z-axis ($0, \pi$); ϕ – angle measured from positive x-axis ($0, 2\pi$); n – degree; m – order; $Y_n^m(\theta, \phi)$ – the spherical harmonic function at degree n and order m (expressed in the Equation 2). The quantification of particle form, angularity and surface texture is according to solving the a_{nm} in the Equation 3. The asterisk denotes the complex conjugate in Equation 3. The functions $P_n^m(x)$ are the associated Legendre function and are a set of orthogonal polynomials found in quantum mechanics (more descriptions in [82]).</p>	$R(\theta, \phi) = \sum_{n=0}^{\infty} \sum_{m=-n}^n a_{nm} Y_n^m(\theta, \phi) \quad (1)$ $Y_n^m(\theta, \phi) = \sqrt{\left(\frac{(2n+1)(n-m)!}{4\pi(n+m)!} \right)} P_n^m(\cos(\theta)) e^{im\phi} \quad (2)$ $a_{nm} = \int_0^{2\pi} \int_0^{\pi} d\phi d\theta \sin(\theta) R(\theta, \phi) Y_n^{m*} \quad (3)$
<p>AIMS Fletcher et al., 2003; Chandan et al., 2004; Al-Rousan et al., 2007 [53]</p>	<p>The Sphericity (Ψ) is expressed with the ratios of the dimensions of the particle. In the equation: a – the longest axis; b – the medium axis; c – the shortest axis. The Form index (FI) is expressed by the ratios of the dimensions of the particle. Note: the methods for the dimension acquisition applied in AIMS are introduced briefly as follow. The three dimensions are measured using the autofocus microscope (for the shortest axis) and the grey images (for the longest and the medium axes). For the grey images, the eigenvector method is utilised for the longest and medium axes of a 2D particle outline. Each pixel in the particle outline is treated as a 2D vector. The vectors are utilised for the calculation of the mean vector and covariance matrix. Afterwards, the covariance matrix eigenvectors that are orthogonal to each other are analysed. The major and minor axes of the outline are aligned along the orthogonal eigenvectors. The length of the axes is the same as the distance from the particle centroid to the outline along the two orthogonal eigenvectors.</p>	$\Psi = \sqrt[3]{\frac{d_s \cdot d_l}{d_L^2}} \quad (1)$ $FI = \frac{d_s}{d_L \cdot d_l} \quad (2)$
<p>Fourier series Masad et al., 2005 [8]</p>	<p>Based on the theory of Spherical harmonic series, proposed by Garboczi et al. in 2002, the three descriptors are decided respectively for the form, angularity or surface texture. As shown in the equations at right side, the Form index (FI) was taken as the summation of indices with $1 < n < 4$; the Angularity</p>	$FI = \sum_{n=0}^5 \sum_{m=-1}^n a_{nm} \quad (1)$

	index (AI) is quantified with $5 < n < 25$; the Surface texture index (STI) is quantified with $n \leq 25$.	$AI = \sum_{n=6}^{25} \sum_{m=-1}^n a_{nm} \quad (2)$ $STI = \sum_{n=26}^{n_{\max}} \sum_{m=-1}^n a_{nm} \quad (3)$
3D image analysis Hayakawa et al., 2005 [59]	The Modified Wadell's Sphericity (E_s) is proposed to express the similarity of a particle to an ellipsoid with the same dimensions. In the equation: e_n – the surface area of an ellipsoid with the same dimensions, expressed as the Equation 2; S – the surface area of the particle.	$E_s = e_n / S \quad (1)$ $e_n = \frac{\pi}{2} \left(c^2 + b\sqrt{a^2 - c^2} \int_0^\alpha \sqrt{1 - k^2 \sin^2 \varphi} d\varphi + \frac{bc^2}{\sqrt{a^2 - c^2}} \int_0^\alpha \frac{d\varphi}{\sqrt{1 - k^2 \sin^2 \varphi}} \right) \quad (2)$
3D image analysis Fernlund, 2005, 2007 [9]	The Elongated or Flat ratio (ER or FR) are expressed as the equations at right side. In the equation: a – the longest axis; b – the medium axis; c – the shortest axis. In [9], the authors used two particle images (in lying and standing positions) for the three dimensions acquisition.	$ER = \frac{a}{b} \quad (1)$ $FR = \frac{b}{c} \quad (2)$
3D image analysis Erdoğan et al., 2006 [76]; Anochie-Boateng et al., 2012, 2013 [46]	Compared with the last method, the Elongated or Flat ratio (ER or FR) are expressed with the same equations, shown at right side. In the equation: a – the longest axis; b – the medium axis; c – the shortest axis. Additionally, the difference is the means of image acquisition. Specifically, Anochie-Boateng utilised 3D images from laser scanning for individual ballast particle analysis, while Erdoğan used those from the X-ray computed tomography.	$ER = \frac{a}{b} \quad (1)$ $FR = \frac{b}{c} \quad (2)$
UIAIA Tutumluer et al., 2005 [42]	The Flat & Elongated ratio (FE) is expressed with the longest dimension and the shortest perpendicular dimension, as shown in the equation at right side.	$FE = \frac{\text{Longest Dimension}}{\text{Shortest Perpendicular Dimension}}$
PA Le Pen et al., 2013 [83]	The Ellipseness (E) is expressed as the equation at right side. In the equation: P_e – the perimeter of an ellipse having the same area as the particle outline; P_o – the actual perimeter of the outline. The ellipse has the same major dimension and area as the particle outline.	$E = \frac{P_e}{P_o}$
3D image analysis Sun et al., 2014 [50]	The Ellipsoidness (E) is expressed as the ratio of the surface area (S_e) of the equivalent ellipsoid to the particle surface area (S_o), as shown in the Equation 3. In the equation: a – one half of the longest axis; b , c – the minor radius, obtained from Equation 1 ($b = c$); V – particle volume; S_e – obtained with the Equation 2.	$b = \left(\frac{3V}{2\pi L} \right)^{1/2} \quad (1)$ $S_e = 4\pi \left(b^2 + a^2 \frac{\cos^{-1}(b/a)}{\tan[\cos^{-1}(b/a)]} \right) \quad (2)$ $E = S_e / S_o \quad (3)$

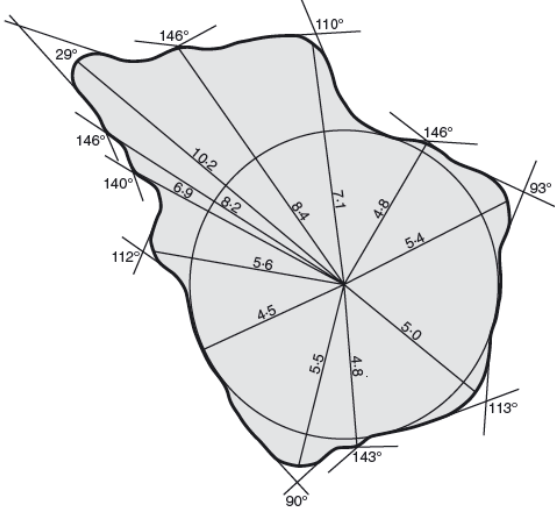
<p>3D image analysis</p> <p>Ouhbi et al., 2017 [132]</p>	<p>The Form index (FI) is expressed based on the difference between each grain and the average grain. The radius differences written in Equation 2 define matrix A, and its line vectors Δr_i for $1 \leq i \leq n$, by subtracting vector r from each line of A_j. For any matrix a denote its Frobenius norm as $\ a\$: $\ a\ ^2 = \sum_i \sum_j a_{ij}^2$. $\ \bar{r}\$ being the norm of d-dimensional vector \bar{r}, one has the definition as Equation 3. The importance of the variation from grain to grain, relatively to the average shape, is expressed as the Equation 4.</p>	$\bar{r}_j = \frac{1}{n} \sum_{k=1}^n r_{kj} \quad (1 \leq j \leq d) \quad (1)$ $\Delta r_{ij} = r_{ij} - \bar{r}_j \quad (2)$ $\ A_1\ ^2 = n \ \bar{r}\ ^2 + \ A\ ^2 \quad (3)$ $\delta_1 = \frac{\ A\ }{n^{1/2} \ \bar{r}\ } \quad (4)$
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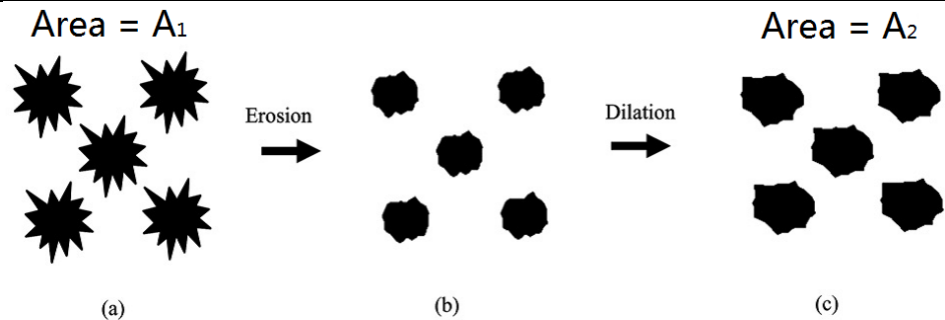
1162

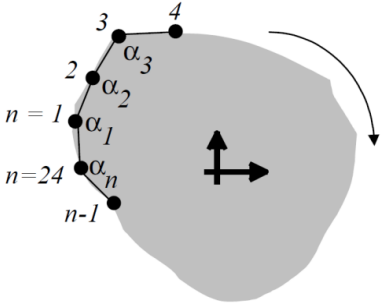
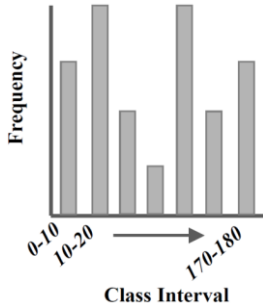
1163 *Table 9 Morphological indices for the angularity quantification (summarised from [8, 39, 42, 45, 50, 124-126])*

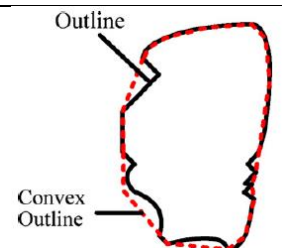
Reference	Description of the morphological indices	Calculation methods
<p>Manual measurement</p> <p>Wentworth, 1923 [49]</p>	<p>Wentworth proposed four methods for Roundness quantification (R_1, R_2, R_3, R_4):</p> <p>In the Equation 1: L – the longest axis of the maximum particle projection; S_M – the shortest axis of the minimum projection; D_s – the diameter of a circle fitting the sharpest corner.</p> <p>In the Equation 2: L – the longest axis; B – the intermediate axis, perpendicular to the longest axis; R_{CON} – the radius of the most convex part.</p> <p>In the Equation 3: D_s – the diameter of the sharpest corner; D_x – the diameter of a pebble through the sharpest corner.</p> <p>In the Equation 4: R_{CON} – the radius of the sharpest corner; R_{AVG} – the average radius of the pebble, calculated with the Equation 5.</p>	$R_1 = \frac{D_s}{(L + S_M)/2} \quad (1)$ $R_2 = \frac{R_{CON}}{(L + B)/4} \quad (2)$ $R_3 = \frac{D_s}{D_x} \quad (3)$ $R_4 = \frac{R_{CON}}{R_{AVG}} \quad (4)$ $R_{AVG} = \frac{1}{2} D_{AVG} = \frac{1}{2} \sqrt[3]{a * b * c} \quad (5)$
<p>Manual measurement</p> <p>Szadeczsky-Kardos, 1933 [124]</p>	<p>The Roundness (R) is expressed as the equation at right side. In the equation: P_{CON} – the perimeter of concave parts; P – the perimeter of the particle outline.</p>	$R = \frac{P_{CON}}{P} * 100$

Manual measurement Fischer, 1933 [124]	The particle central point joins the outline points to divide the outline into the non-curved parts and the convex parts. Based on that, two equations are used to express the Roundness (R_1 , R_2), as shown at right side. In the equations: ANG_{PLA} – the central angles of the non-curved parts; ANG_{CON} – the central angles of the convex parts.	$R_1 = \frac{\sum ANG_{PLA}}{360^\circ} \quad (1)$ $R_2 = \frac{\sum ANG_{CON}}{\sum ANG_{PLA}} \quad (2)$
Manual measurement Wadell, 1935	The Roundness (R) is expressed with the average radius of the corners and the inscribed circle diameter, as shown in the equation at right side. In the equation: R_{max-in} – the radius of the inscribed circle; r – the radius of the corners. Note: many studies made a chart (classification) based on this morphological index for comparison [16, 48, 133].	$R = \frac{\sum \left(\frac{r}{R_{max-in}} \right)}{N}$
Manual measurement Cailleux, 1947 [124]	The Roundness (R) is expressed with the radius of the most convex part and the longest axe, as shown at right side. In the equation: R_{CON} – the radius of the most convex part of the particle outline; L – the longest axe of the particle outline.	$R = \frac{R_{CON}}{L/2}$
Manual measurement Kuenen, 1956 [134]	The Roundness (R) is expressed as the equation. In the equation: D_S – the diameter of circle fitting sharpest corner; B – the intermediate axe of the particle outline.	$R = \frac{D_S}{B}$
Manual measurement Lees, 1964	The Roundness (R) is expressed by measuring the angularity instead of the roundness, as shown in figure below and the equation at right side (figure modified after [55]). In the equation: α – the angles; R_{max-in} – the radius of the largest inscribed circle of the particle outline; x – the distance of the tip of the corner from the centre of the largest inscribed circle.	$R = (180 - \alpha) \frac{x}{R_{max-in}}$

[55]	 <p>The diagram shows an irregular particle outline with an inscribed circle. Several diameters are drawn from the center of the circle to the particle's boundary, labeled with values: 10.2, 6.9, 8.2, 8.4, 7.1, 4.8, 5.4, 5.6, 4.5, 5.0, 5.5, 4.8, and 5.0. Angles are also labeled at the points where the diameters meet the boundary: 29°, 146°, 110°, 146°, 140°, 93°, 112°, 113°, 143°, and 90°.</p>	
Manual measurement Dobkins & Folk, 1970 [131]	The Roundness (R) is expressed with the sharpest corner and inscribed circle diameters, as shown in the equation at right side. In the equation: D_S – the diameter of circle fitting sharpest corner; D_i – the diameter of the largest inscribed circle of the particle outline.	$R = \frac{D_S}{D_i}$
Manual measurement Swan, 1974 [135],	The Roundness (R) is expressed with the sharpest corner and inscribed circle diameters, as shown in the equation at right side. In the equation: D_{S1} , D_{S2} – the diameter of circle fitting sharpest corner and the second sharpest corner, respectively; D_i – the diameter of the largest inscribed circle of the particle outline.	$R = \frac{(D_{S1} + D_{S2})/2}{D_i}$
PA Palasamudram & Bahadur, 1997 [62]	The Angularity index (A_n) is expressed as the Equation 1. In the equation: K – an arbitrary constant; i – the i th angle of the particle outline; a_i – expressed as the Equation 2; α_i – the i th angle degree; p_i – expressed as the Equation 3.	$A_n = K \sum_{i=1}^n a_i \cdot p_i \quad (1)$ $a_i = K/\alpha_i \quad (2)$ $p_i = \frac{\pi - \alpha_i}{2\pi} \quad (3)$
PA Janoo, 1998;	The Roundness (R) is expressed with the particle outline perimeter and the particle outline area, as shown in the equation at right side. In the equation: P – the particle outline perimeter; A – the particle outline area.	$R = \frac{4\pi A}{P^2}$

Kuo & Freeman, 1998, 2000 [54]		
PA Sukumaran & Ashmawy, 2001, 2003 [77]	The Angularity index (<i>AI</i>) is expressed as the equation. In the equation: <i>N</i> – the number of sampling intervals; $\beta_{particle}$ – angle <i>EFG</i> in the figure (Sukumaran & Ashmawy, 2001, 2003) in Table 8.	$AI = \frac{\sum_{i=1}^N (\beta_{i \text{ particle}} - 180)^2 - (360^2 / N)}{3 \times (180)^2 - (360^2 / N)} \times 100\%$
AIMS Masad et al., 2001 [8]	The Angularity index (<i>AI</i>) is expressed with the distance difference in a certain direction between the distance from the inscribed circle centre to the corner and the equivalent ellipse radius, as shown in the equation at right side. In the equation: R_θ – the distance from the inscribed circle centre to the corner at the directional angle θ ; $R_{EE\theta}$ – the radius of the equivalent ellipse at the same directional angle θ .	$AI = \sum_{\theta=0}^{\theta=360-\Delta\theta} \frac{ R_\theta - R_{EE\theta} }{R_{EE\theta}}$
AIMS Masad et al., 2000 [53]	The Angularity index (<i>SP</i>) is expressed as the equation at right side. It is obtained with the surface Erosion-Dilation technique as shown in the figure below (figure reproduced from [53]). In the equation, A_1 and A_2 are the areas of particle image before and after applying the Erosion-Dilation operations, respectively. Note: more angular particles lose more area when applying the Erosion-Dilation operations. Additionally, the <i>SP</i> could be used to analyse the angularity in low resolution images, while the higher resolution images can be utilised for surface texture analysis.	$SP = \frac{A_1 - A_2}{A_1} \times 100\%$
AIMS Masad et al., 2000 [53]	 <p style="text-align: center;">Erosion-Dilation Technique</p>	
LASS Kim et al., 2002 [51]	The Angularity index (<i>AI</i>) is expressed as the equation at right side. The explanations of the equation are at the part of Wavelet transform (LASS; Kim et al., 2002) in Table 8.	$AI = \frac{E(d_{2,j,k,l}) + E(d_{3,j,k,l})}{\text{average radius}}$

<p>Fourier series Wang et al., 2005 [81]</p>	<p>The Angularity index (α_r) is expressed as the equation at right side. The details of the equation were explained at the Fourier series (Wang et al., 2005) in Table 8.</p>	$\alpha_r = \sum_{j=5}^{25} \left[\left(\frac{a_n}{a_0} \right)^2 + \left(\frac{b_n}{a_0} \right)^2 \right]$
<p>3D image analysis Hayakawa et al., 2005 [59]</p>	<p>The Roundness (X_s) is expressed as the equation at right side. In the equation: a – the longest axe; b – the medium axe; c – the shortest axe; V – particle volume; S – particle surface area.</p>	$X_s = V/S(abc)^{1/3}$
<p>AIMS Chandan et al., 2004; Al-Rousan et al., 2005 [53]</p>	<p>The Angularity index (AI) is expressed based on the change in the gradient on a particle outline, named the gradient method. In the equation: i – the ith point on the particle outline; N – total number of points on the particle outline; θ_i – the angle of orientation values of the ith edge points.</p>	$AI = \frac{1}{N/3-1} \sum_{i=1}^{N-3} \theta_i - \theta_{i+3} $
<p>UIAIA Tutumluer et al., 2005 [42]</p>	<p>The Angularity index (AI) is computed by averaging the Angularity index values of three orthogonal views (weighted by their areas) as the Equation 1 & 2. In the equations: e – the starting angle value for each 10° class interval (0, 10, 20, 30, ..., 170), as shown in the Figure b, the horizontal axis; $P(e)$ – the probability that the angle change β in the range of e to $(e + 10)$. β is expressed as the Equation 3. In the equation: α_n – the subtended angle at the nth vertex, as shown in the Figure a. (figure reproduced from [53])</p>   <p>a. Illustration of An n-sided Polygon Approximating the Outline of a Particle</p> <p>b. Frequency distribution for the change in vertex angles</p>	$AI = \frac{A(\text{front}) \times \text{Area}(\text{front}) + A(\text{top}) \times \text{Area}(\text{top}) + A(\text{side}) \times \text{Area}(\text{side})}{\text{Area}(\text{front}) + \text{Area}(\text{top}) + \text{Area}(\text{side})} \quad (1)$ $A = \sum_{e=0}^{170} e \times P(e) \quad (2)$ $\beta_n = (\alpha_n - \alpha_{n-1}) \quad (3)$
<p>Fourier series Sekine et al., 2005 [92]</p>	<p>Angularity index is calculated with the Fourier series (Argument function). The Argument function applies the distance of the outline point and the reference point, as well as the angle between the tangential line (outline point) and the reference line (reference point). In the equations: L – the outline perimeter; $\theta_N(x)$ is a periodic function with the period L; the Angularity index (AI) is calculated by the sum of the third to</p>	$\theta(x+L) = \theta(x) + 2\pi \quad (1)$ $\theta_N(x) = \theta(x) - 2\pi(x/L) \quad (2)$

	twentieth amplitude spectra, as presented in the Equation 7.	$\theta_N(x) = b_0/2 + \sum_{n=1}^{\infty} \{a_n \sin(2\pi nx/L) + b_n \cos(2\pi nx/L)\} \quad (3)$ $c_n = \sqrt{a_n^2 + b_n^2} \quad (4)$ $a_n = \frac{2}{L} \int_{x_0}^{x_0+L} f(x) \sin(2\pi nx/L) dx, n=1,2,\dots \quad (5)$ $b_n = \frac{2}{L} \int_{x_0}^{x_0+L} f(x) \cos(2\pi nx/L) dx, n=0,1,2,\dots \quad (6)$ $AI = \sum_{k=3}^{20} c_k \quad (7)$
Descantes et al., 2006	The Angularity index (<i>AI</i>) is calculated by measuring the average value of the sharpest salient angles between two adjacent straight lines (Figure). In the equation: α_i – salient angle between two adjacent straight lines; n – number of angles that are taken into consideration ($n \leq 8$).	$AI = \frac{1}{n} \sum_{i=1}^n (1 - \frac{\alpha_i}{180}) \alpha_i \in [0, 180^\circ]$
PA Zhang et al., 2012 [71]	<p>The AT index (<i>AT</i>) is a morphological index to characterise the combination of the angularity and the surface texture. The AT index of an aggregate particle is computed by averaging the AT_i values of the particle's different cross sections, and they are weighted by their areas, as shown in equations at right side. In the Equation 2: P_O – the outline perimeter of the ith cross section; P_C – the perimeter of the convex outline of the ith cross section. In the equation 1: A_i – the area of the ith cross section.</p> 	$AT = \frac{\sum_1^n A_i \cdot AT_i}{\sum_1^n A_i} \quad (1)$ $AT_i = \frac{P_O - P_C}{P_C} \quad (2)$

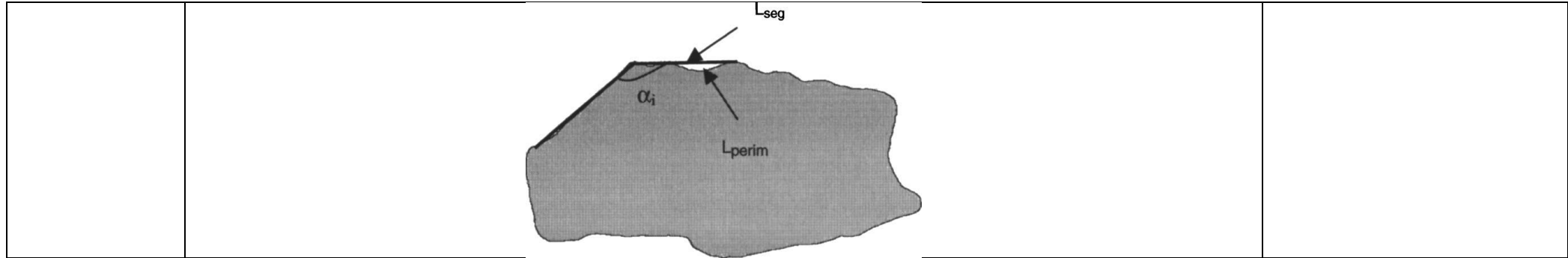
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1165 Table 10 Morphological indices for the surface texture quantification (summarised from [8, 39, 42, 45, 50, 124-126])

Reference	Description of the morphological indices	Calculation methods
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Manual measurement Wenzel, 1949 [56]	The Roughness factor (R) is expressed as the equation at right side. In the equation: A – the surface area of the particle; a – the surface area of the particle outline.	$R = \frac{A}{a}$
Barksdale et al., 1991 [64]	The Roughness factor (R) is expressed as the equation at right side. In the equation: L_T – true length of the surface segment being analysed; L_P – length of the line of best fit for the surface segment.	$R = L_T / L_P$
PA Hyslip et al., 1997 [66]	The quantitative descriptor of roughness (D_R) is computed by solving it from the Equation 1. As shown in the figure below, the particle outline is divided into segments for roughness quantification (figure modified after [66]). In the Equation 1: $P(\lambda)$ – the length of the line (curve) based on unit measurement length λ ; n – a proportionality constant (equal to the actual and indeterminate length of the line). By taking the logarithm of both sides of Equation 1, the roughness descriptor (D_R) is related to the linear slope coefficient, m , as shown in Equation 2. In the Equation 2: m – the linear slope coefficient.	$P(\lambda) = n\lambda^{1-D_R} \quad (1)$ $D_R = 1 - m \quad (2)$
PA Janoo, 1998[54]	The Roughness (R) is expressed as the equation at right side. In the equation: P – the perimeter of the particle outline; C_{PER} – the convex perimeter of the particle outline. Note: the convex is explained with the figure shown at Janoo, 1998 in Table 8.	$R = \frac{P}{C_{PER}}$
PA Kuo et al., 1998 [89]	The Roughness (R) is expressed as the equation at right side. In the equation: P – the perimeter of the particle outline; D_{AVG} – the average of the 12 Feret diameters (details explained at Janoo, 1998 in Table 8).	$R = \frac{P}{\pi * D_{AVG}}$
Fourier series Bowman et al., 2000 [65]	The Fourier shape descriptors (c_n) uses higher order descriptors to present the particle surface texture. The computation method was introduced at Bowman et al., 2000 , in Table 8. It is proposed that the descriptors from +/-8 to +/-32 can measure of the particle surface texture.	-
AIMS Masad et al., 2000 [53]	The Surface texture index (SP) is expressed as the equation at right side. In the equation: A_1 and A_2 are the areas of particle image before and after applying the Erosion-Dilation operations, respectively. The Erosion-Dilation technique was explained in the former part (angularity) at Masad, 2000 in Table 9. Note: the equation used for surface texture quantification is the same one used for the angularity quantification. Because the SP can quantify both surface texture and angularity after controlling the image resolution. The high-resolution image can cause the fine details (surface texture) disappear, and for that it can be used for the surface texture quantification.	$SP = \frac{A_1 - A_2}{A_1} \times 100\%$
Fourier series Lanaro et al., 2001	Fractal surfaces are dependent on the frequency ranges following a power law of the spatial frequency for an isotropic surface with fractal constant F_0 given by Equation 1. The Hurst exponent H correlates with the Fractal dimension (FR) as explained at Hyslip et al., 1997 (Equation 2). The roughness is characterised by the FR or H and the F_0 .	$ F(u, v) = F_0 (\sqrt{u^2 + v^2})^{-\alpha/2}$

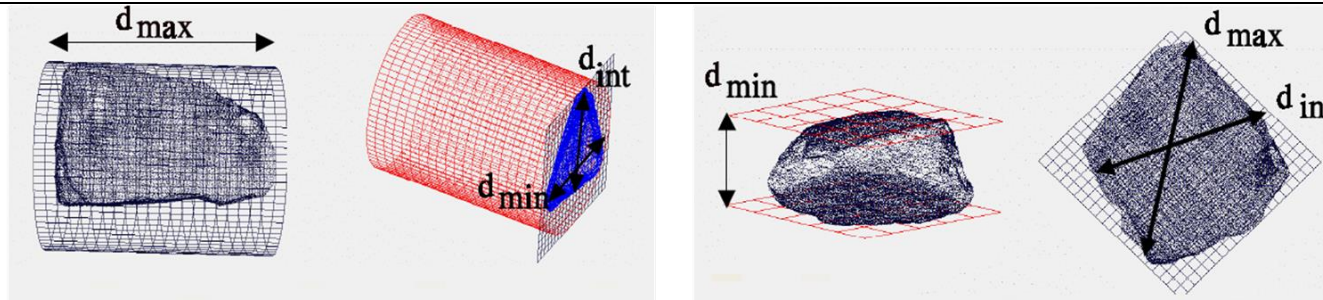
		$FR = 3 - H = (7 - \alpha)/2 \quad (2)$
LASS Kim et al., 2002 [51]	The Surface texture index (<i>STI</i>) is expressed as the equation at right side. The explanations of the variables in this equation are at the Wavelet transform in Table 8 (Kim et al., 2002).	$STI = \frac{E(d_{4,j,k,l}) + E(d_{5,j,k,l})}{\text{average radius}}$
AIMS Fletcher et al., 2002-2003; Chandan et al., 2004 [53]	The Surface texture index (<i>STI_n</i>) is expressed as the equation. In the equation: <i>n</i> – the decomposition level; <i>N</i> – the total number of coefficients in a detailed image of texture; <i>i</i> – taking the values 1, 2, or 3, for the three detailed images of texture; <i>j</i> – the wavelet coefficient index; (<i>x, y</i>) – the location of the coefficients in the transformed domain. Note: The Wavelet transform was briefly introduced at the LASS in Table 8 (Kim et al., 2002). The decomposition level, <i>n</i> = 6, are utilised, because level 6 is the least affected by colour discrepancies and the dust existence on the surface.	$STI_n = \frac{1}{3N} \sum_{i=1}^3 \sum_{j=1}^N [D_{ij}(x, y)]^2$
Fourier series Wettimuny et al., 2004 [80]	The Roughness factor (<i>RF</i>) is expressed as the equation at right side. In the equation: <i>TSSR_i</i> – defined by the equation of <i>TSSR_n</i> when the <i>i</i> = 1 (details explained at Wettimuny et al., 2004 in Table 8); <i>FI</i> – the average of the <i>TSSR_n</i> (<i>n</i> = 2,3,4,5,6).	$RF = TSSR_1 - FI$
Fourier series Wang et al., 2005 [81]	The Surface texture index (<i>α_i</i>) is expressed as the equation at right side. The details of the equation were explained at the Fourier series (Wang et al., 2005) in Table 8.	$\alpha_i = \sum_{j=26}^{180} \left[\left(\frac{a_n}{a_0} \right)^2 + \left(\frac{b_n}{b_0} \right)^2 \right]$
UIAIA Tutumluer et al., 2005	The Surface texture index (<i>ST</i>) is expressed as the Equation 1. In the equation: <i>A₁</i> – area of the particle outline before Erosion-Dilation operation; <i>A₂</i> – area of the particle outline after <i>n</i> cycles of Erosion-Dilation operation. The Erosion-Dilation cycles (<i>n</i>) is determined by the Equation 2. In the equation: <i>L</i> – longest intercept of a particle outline; <i>β</i> – scaling factor for erosion and dilation operations (constant value). The final particle surface texture (<i>ST_{particle}</i>) is computed as the weighted average of each <i>ST</i> value form three orthogonal views, shown in Equation 3. In the equation: <i>i</i> – from 1 to 3 for top, front, and side views.	$ST = \frac{A_1 - A_2}{A_1} \times 100 \quad (1)$ $n = \frac{L}{\beta} \quad (2)$ $ST_{particle} = \frac{\sum_{i=1}^3 ST(i) * Area(i)}{\sum_{i=1}^3 Area(i)} \quad (3)$
Descantes et al., 2006	The roughness (<i>STI</i>) is calculated with the length of a straight line segment (<i>L_{perm}</i>) and the corresponding outline length (<i>L_{seg}</i>), as shown in the figure below (reproduced from [122]).	$STI = mean\left(\frac{L_{perm} - L_{seg}}{L_{perm}}\right)$



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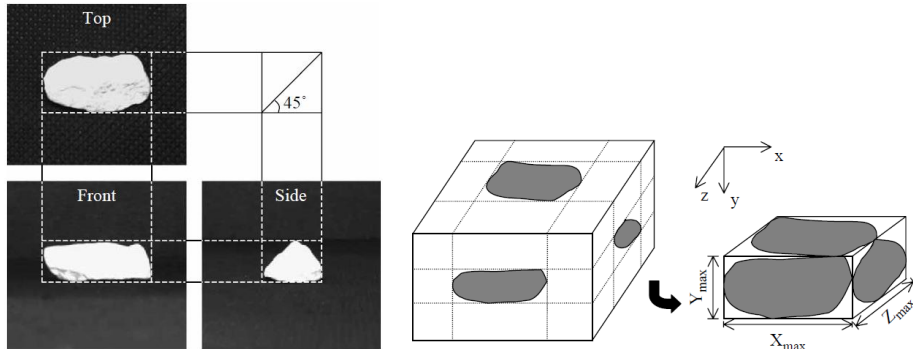
1167 *Table 11 Calculation methods with the Image analysis for particle size evaluation*

Reference	Description of the morphological indices	Calculation methods
Hyslip & Vallejo, 1997	Fragmentation fractal dimensioning (D_F) is proposed for particle size distribution. In the equations, $M(R < r)$ is the total mass of the particles with size R smaller than r , which is the sieve size opening; M_T is the total mass of particles; r_L is the maximum particle size as defined by the largest sieve size opening. Logarithmic transformation of Equation 1 results in a linear relationship of the $M(R < r)$ and r for D_F (Equation 2).	$\frac{M(R < r)}{M_T} = \left(\frac{r}{R_L}\right)^{3-D_F}$ $D_F = 3 - m$
Mora et al., 2000	The volume (V) is calculated with the particle intermediate axe (b), parameter λ and area (A). The parameter λ is calculated with the Equation 2. In the Equation 2, n is the total number of particles; ρ is the density; M is total mass of the particle sample.	$V = \lambda \times b \times A$ $\lambda = \frac{M}{\rho \times \sum_{i=1}^n (b \times A)}$
Lanaro, et al., 2001	The particle volume is calculated by the summation of the areas of the cross sections. The particle can be treated as parallel cross sections and the areas of every cross sections can be obtained. After defining the space between the cross sections, the particle volume is calculated by summation of the cross section area times the space. The particle axe can be measured by two geometrical methods as shown in the figure below.	-



Two geometrical methods for particle dimension measurement (reproduced from [75])

<p>Garboczi et al., 2002</p>	<p>In the Garboczi's method, the surface area is calculated by the derivatives of the spherical harmonic functions. Additionally, the particle volume is computed by the general integral using spherical polar coordinates, which are transformed with the Spherical harmonic.</p>	$V = \frac{1}{3} \int_0^{2\pi} \int_0^{\pi} r^3(\theta, \phi) \sin(\theta) d\theta d\phi$ $S_A = \int_0^{2\pi} \int_0^{\pi} r \left[r_{\phi}^2 + r_{\theta}^2 \sin^2(\theta) + r^2 \sin(\theta) \right]^{1/2} d\theta d\phi$
<p>LASS Kim et al., 2002</p>	<p>The volume is calculated by the equation at right side. A pixel corresponds to a volume element in a 3D image (called a voxel) which can be presented by $\Delta x \times \Delta y \times \Delta z$. H is the height that is the Z-coordinate of the surface point as described at the Table 5 Image analysis systems.</p>	$V = \sum H(\Delta x \times \Delta y \times \Delta z)$
<p>Browne et al., 2002</p>	<p>The size method takes the particle length as the particle size. The shape method takes the equivalent diameter as the particle size. The equivalent diameter is the diameter of the circle that has the same particle area.</p>	<p style="text-align: center;">-</p>
<p>UIAIA Tutumluer et al., 2005 [42]</p>	<p>The surface area is measured through the three orthogonal views of the particle. The 3D reconstruction of the particle is accomplished based on three orthogonal images, when all the voxels are in the 3D framework. Afterwards, the surface area of the particle is computed as the summation of the 2D area elements forming the surface voxels [136]. The volume of the rectangular box is considered as the particle volume, however, the average absolute error is at 11.5% as reported in [42].</p>	$V = abc$

	 <p>a. Three orthogonal views of a particle</p> <p>b. The smallest rectangular box</p> <p><i>Each view of the 3 cameras for one particle (front, top, and side) and the box (framework) for dimension determination (figure reproduced from [136])</i></p>	
Descantes, et al., 2006	The particle width is utilised for calculating the PSD curve. The particle volume is assumed as the ellipsoid that is created by revolving the ellipse around its major axis. The longest particle axe (length) is obtained and treated as the major axis of an equivalent ellipse.	-
Anochie-Boateng et al., 2012, 2013	The particle surface area (SA_T) is computed d by summing up all the poly-face surface areas that constitute the particle. The tetrahedrons that constitute the particle can be treated as four vertices $a = (a_1, a_2, a_3)$; $b = (b_1, b_2, b_3)$; $c = (c_1, c_2, c_3)$; $d = (d_1, d_2, d_3)$, and its volume (V) can be calculated with Equation 2. The particle volume is computed with the summation of all the tetrahedrons (Equation 3).	$SA_T = \sum_{i=1}^n A_i \quad (1)$ $V = (a-d) \cdot ((b-d) \times (c-d)) / 6 \quad (2)$ $V_T = \sum_{i=1}^n V_i \quad (3)$
PA Ozen & Guler, 2014 [137]	The Equivalent ellipse major axe (E) is expressed as the equation at right side. In the equation: P – the perimeter of particle outline; A – the area of particle outline.	$E = \sqrt{\frac{P^2}{2\pi^2} + \frac{2A}{\pi}} - \sqrt{\frac{P^2}{2\pi^2} - \frac{2A}{\pi}}$

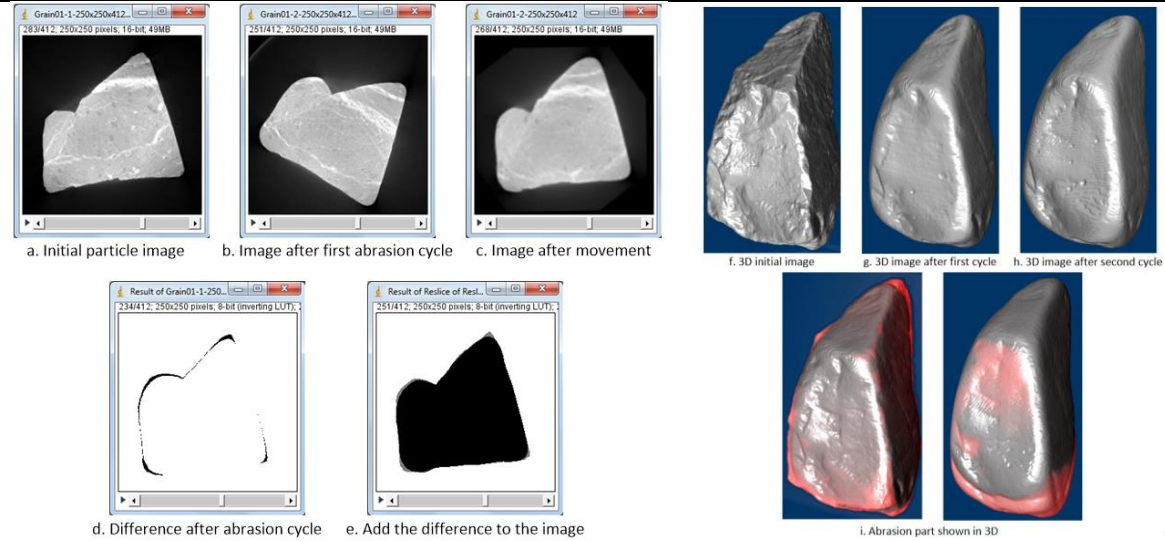
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1169 *Table 12 Description of degradation evaluation methods*

Reference	Description of the degradation procedure	Calculation methods
Tolppanen, 2001 [75]	The LAA test is utilised for deteriorating ballast particles. Four times of laser scanning are performed at the beginning, after 100, 400 and 500 revolutions, respectively. One particle from each sample (7 types in total) is analysed. The Degradation index (DI) is proposed as the average value of the	$DI = 0.5 \times (\Delta F_0 / F_0 + \Delta a / a)$

	roughness change (E_0) percentage and the longest axis (a) change percentage.	
Sekine et al., 2005 [92]	The degradation stages are classified into three levels according to the duration of the LAA tests, i.e. Level 0 (0 min), Level A (10 min) and Level B (35 min). Their morphological indices (i.e. the Angularity index and the Aspect ratio) are obtained using the Fourier series. For ballast particles at each level, 100 particles are photographed and analysed the Aspect ratio and the Angularity index . The distribution of the two morphological indices are compared.	The particle degradation is evaluated by comparing the morphological indices of ballast particles at different LAA test duration.
Fernlund, 2005, 2007	The LAA tests are utilised for obtaining deteriorated ballast particles. Before and after the LAA test, the sample particles are photographed and analysed the three axes of the particles. Afterwards, the PSD change and Flat or elongated ratio change are given for presenting the ballast degradation.	The particle degradation is evaluated by comparing the PSD and the Flat and elongated ratio before and after LAA tests.
Descantes et al., 2006 [122]	The degradation was generated with the micro-Deval milling test (24,000 cycles) until the 2% mass loss is represented. The average Angularity indices of the sample at different stages are presented. The morphological indices (in 2D) of the testing sample are acquired with the VDG40 videograder, including the Angularity index and the Roughness. The different degradation stages are defined based on the micro-Deval abrasion value (5%, 10%, 15%). The results show that the VDG40 videograder can obtain the particle angularity efficiently and accurately.	The results are repeatable with the variation less than 1.5% for Angularity index change.
AIMS Mahmoud et al., 2007	Six different kinds of materials are performed with the micro-Deval polishing for the duration at 15, 30, 45, 60, 75, 90, 105, and 180 mins. The Surface texture index and the Angularity index of particle samples is measured with the AIMS before and after the micro-Deval tests [93]. Another study focuses on the effectiveness of both E-UIAIA and AIM2 on capturing morphology change (form, angularity and surface texture) [39]. The micro-Deval tests are performed on the 11 particle materials with the duration at 15, 30, 45, 60, 75, 90, 105, 180, or 210 mins. The image analysis results are utilised for regression-based statistical model development to determine particle polishing and degradation trends with the consideration of both rate and magnitude of morphology changes.	Surface texture index change; Angularity index change and correlated it with the weight loss. The form change is presented by Flat or elongated ratio change or the Sphericity change.
Okonta et al., 2015 [61]	The LAA test is utilised to create deteriorated ballast at different stages, and the stages are defined based on the machine revolutions (500/1000/1500/2000). The values of the morphological indices at different degradation stages are compared with the initial values to quantify degradation. The abrasion degree decreased as the Roundness increases. The relative ballast fouling ratio can better predict the ballast fouling than the Fouling index, which is concluded by correlating them with the sample roundness changes.	Roundness change and correlated it with the ballast fouling.
UIAIA Qian et al., 2017	The different degradation stages are defined according to the different revolutions in LAA tests (250/500/750/1000/1250/1500/1750/2000). The morphological indices change (AI, F&E, STI and Vol) are used for the degradation evaluation, and the distribution of the ballast samples are given to show the change [91].	Morphological indices change, and correlated with the ballast fouling
Tunkin & Denis, 2014 [45]	The micro-Deval test is used to generate deteriorated particles rapidly. The samples (10 kg) are abraded twice with the same settings, including no steel balls and 100 rpm for three hours. 3D degradation evaluation method can be developed by reconstructing 2D images. For example, in, fifteen 2D images of one particle are reconstructed into one 3D image for degradation evaluation. Degradation is illustrated with the voxels lost, and evaluated by the change of the morphological	The morphological indices include several methods, especially for the surface texture change (details at Chapter 9).

indices of Form index and Angularity index, obtained with the [Spherical harmonics series](#). As shown in figures below, for comparing particles after each abrasion cycle, it is required to match the particle images in order that the orientation and their centres are the same. Comparing the images before and after abrasion respectively, the difference of the two images can be observed. Difference addition is adding the abraded part to the images after the first cycle of abrasion. The abraded parts are presented in 3D view.

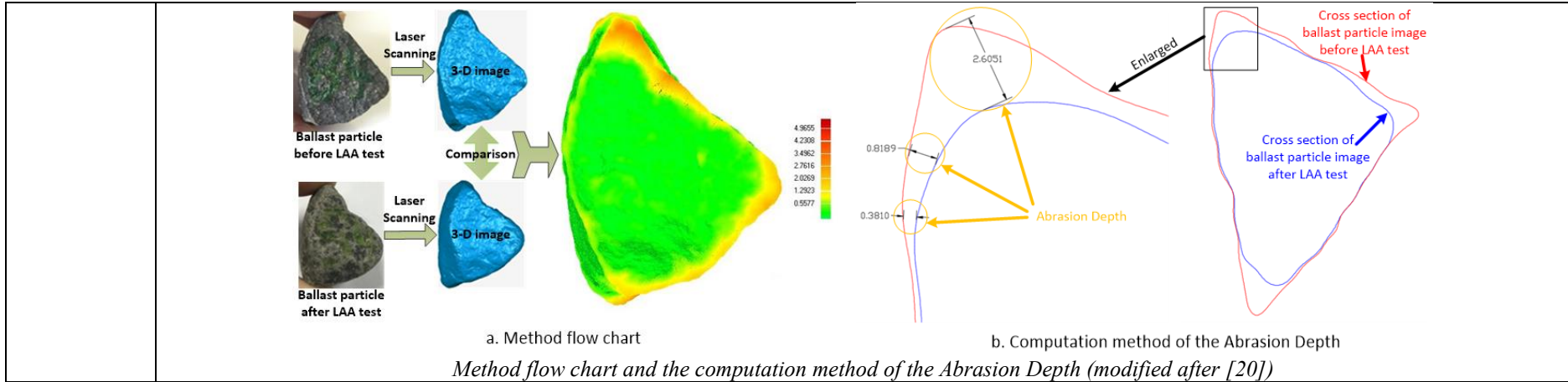


Example for the procedure explanation of degradation evaluation (modified after [45])

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The LAA tests are performed to generate deteriorated ballast particles. By comparing the 3D images before and after the LAA test, the results can be obtained, shown in the figure below. The Abrasion Depth is defined as the value difference of each point at the particle surface. Average Abrasion Depth (AAD) is calculated by averaging the summation of all the Abrasion Depth of one ballast particle. The Maximum Abrasion Depth (MAD) is the maximum value of the Abrasion Depth. More importantly, the breakage is evaluated by the broken number percentage.

Sphericity change, AAD, MAD for degradation evaluation; the AAD correlates well with the LAA loss value.



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