



Delft University of Technology

## Preliminary analysis of ionosphere-corrected PPP-RTK user performance

Psychas, Dimitrios; Verhagen, S.; Liu, Xianglin

### Publication date

2019

### Document Version

Final published version

### Citation (APA)

Psychas, D., Verhagen, S., & Liu, X. (2019). *Preliminary analysis of ionosphere-corrected PPP-RTK user performance*. Poster session presented at EGU General Assembly 2019 , Vienna, Austria.

### Important note

To cite this publication, please use the final published version (if applicable).  
Please check the document version above.

### Copyright

Other than for strictly personal use, it is not permitted to download, forward or distribute the text or part of it, without the consent of the author(s) and/or copyright holder(s), unless the work is under an open content license such as Creative Commons.

### Takedown policy

Please contact us and provide details if you believe this document breaches copyrights.  
We will remove access to the work immediately and investigate your claim.



## 1. Introduction

The realization of the integer ambiguity resolution (IAR) enabled precise point positioning (PPP) method, the so-called **PPP-RTK**, is enabled by providing single-receiver PPP users with **satellite phase biases to recover the integerness of the user ambiguities**. Successful IAR can greatly reduce the solution convergence time. However, the unknown ionospheric delay parameters that are estimated by the PPP-RTK user (ionosphere-float model) do not allow for fast (or instantaneous) convergence to the centimeter level.

In this poster, we present a preliminary analysis on the improvement of PPP-RTK GPS dual-frequency user positioning performance **using precise ionospheric corrections**, which are expected to **greatly reduce the convergence time**. The ionospheric corrections used at the user level are determined by modeling PPP-RTK ionospheric slant delays computed from receivers of a regional network. The improvement of the PPP-IAR user performance is analyzed in terms of the required time to fix the integer ambiguities (TTFA) and the achieved convergence time to the 10 cm level.

## 2. PPP-RTK network system

The basis of the PPP-RTK network system is the **uncombined** GNSS code and carrier-phase observation equations:

$$E(p_{r,j}^s) = \rho_r^s + (dt_r - dt^s) + m_r^s \tau_r + \mu_j l_r^s + (d_{r,j} - d_{r,j}^s)$$

$$E(\phi_{r,j}^s) = \rho_r^s + (dt_r - dt^s) + m_r^s \tau_r - \mu_j l_r^s + \lambda_j (\delta_{r,j} - \delta_{r,j}^s + a_{r,j}^s)$$

Since not all the unknown parameters are unbiasedly estimable, we apply the S-system theory to eliminate the rank-deficiencies [1]. Assuming that precise orbits and clocks are used, the estimable parameters are:

$$\tilde{dt}_r = (dt_r + d_{r,IF}) - (dt_p + d_{p,IF}), \quad \forall r \neq p \quad (p: \text{pivot rec./sat.})$$

$$\tilde{l}_r^s = l_r^s + d_{r,GF} - d_{GF}^s, \quad \forall r, s \quad (\text{IF: ionosphere-free})$$

$$\tilde{\delta}_{r,j} = \left( \delta_{r,j} - \frac{1}{\lambda_j} [d_{r,IF} - \mu_j d_{r,GF}] + a_{r,j}^p \right) \quad (\text{GF: geometry-free})$$

$$- \left( \delta_{p,j} - \frac{1}{\lambda_j} [d_{p,IF} - \mu_j d_{p,GF}] + a_{p,j}^p \right), \quad \forall j, r \neq p$$

$$\tilde{\delta}_{r,j}^s = \left( \delta_{r,j}^s - \frac{1}{\lambda_j} [d_{r,IF}^s - \mu_j d_{r,GF}^s] \right)$$

$$- \left( \delta_{p,j} - \frac{1}{\lambda_j} [d_{p,IF} - \mu_j d_{p,GF}] + a_{p,j}^s \right), \quad \forall j, s$$

$$\tilde{a}_{r,j}^s = (a_{r,j}^s - a_{r,j}^p) - (a_{p,j}^s - a_{p,j}^p), \quad \forall j, r \neq p, s \neq p$$

## 3. PPP-RTK user system

The definition and estimability of the ionosphere-float PPP-RTK user parameters are the same as in the network component:

$$E(p_{u,j}^s + \tilde{dt}^s) = \rho_u^s + \tilde{dt}_u + m_u^s \tau_u + \mu_j \tilde{l}_u^s$$

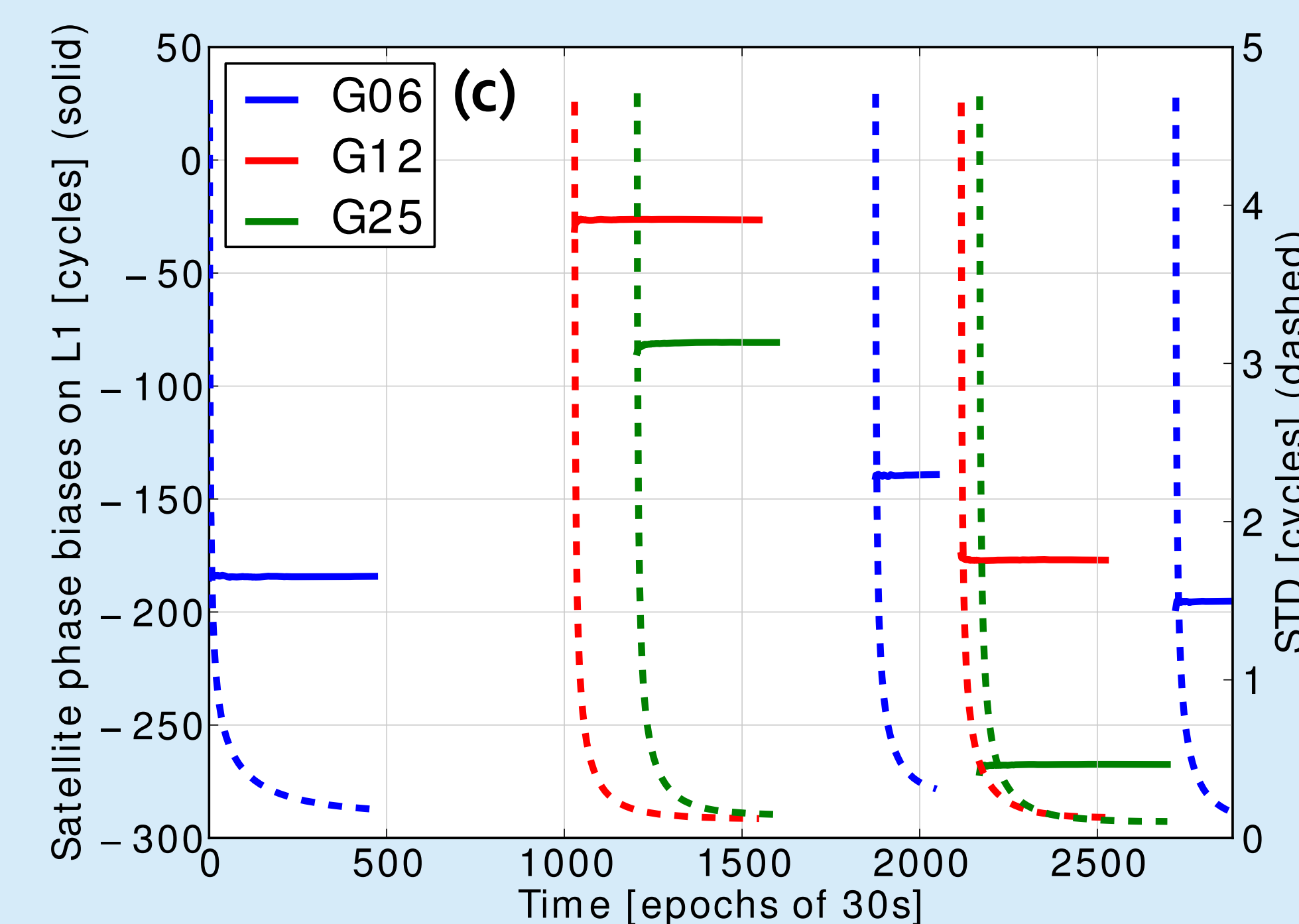
$$E(\phi_{u,j}^s + \tilde{dt}^s + \lambda_j \tilde{\delta}_{j,j}^s) = \rho_u^s + \tilde{dt}_u + m_u^s \tau_u - \mu_j \tilde{l}_u^s + \lambda_j (\tilde{\delta}_{u,j} + \tilde{a}_{u,j}^s)$$

The user phase ambiguities are now double-differenced and therefore **integer**.

If ionospheric corrections are provided to the user, the **receiver code bias parameter** of the user becomes estimable.

## 5. Results

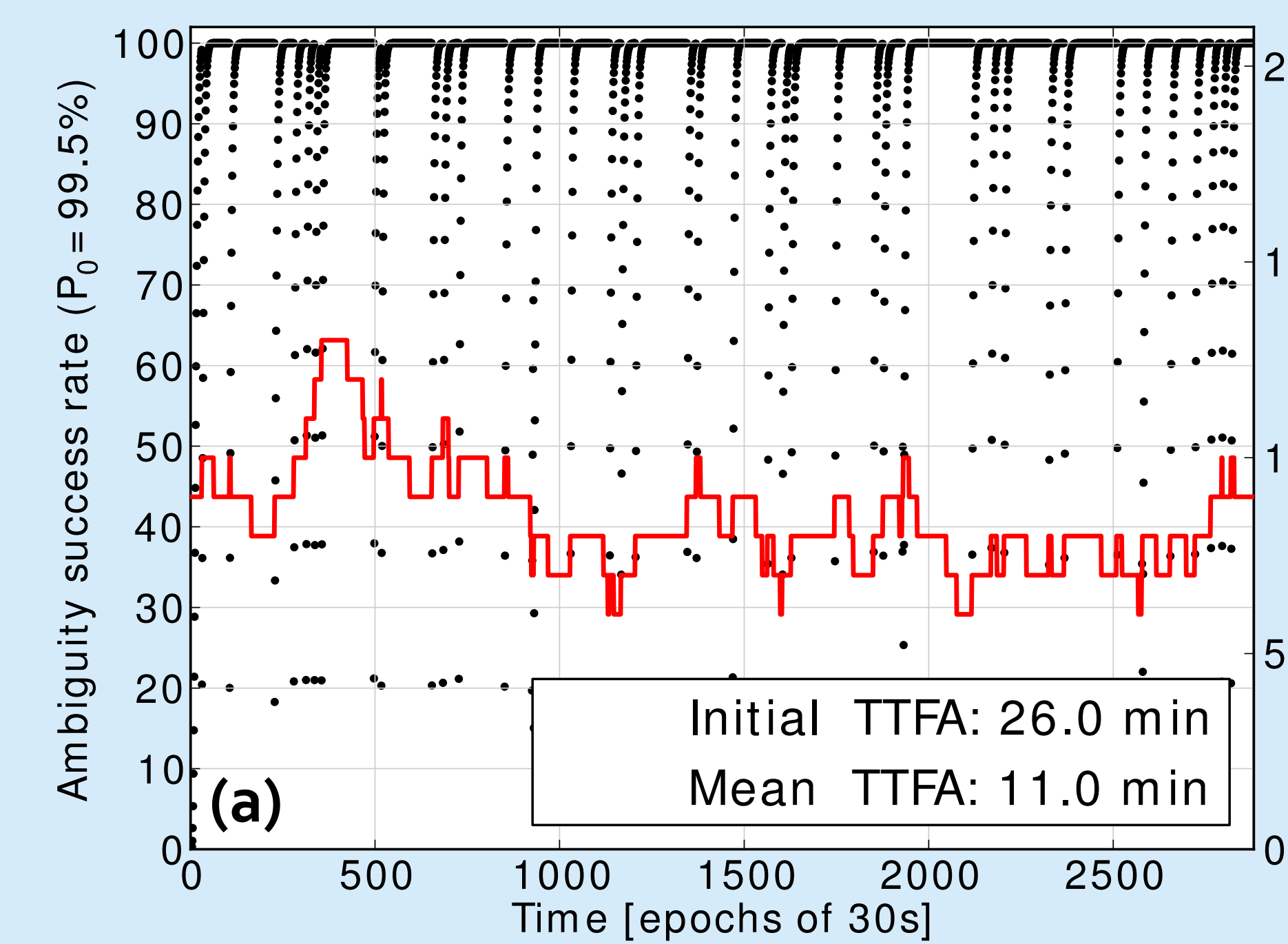
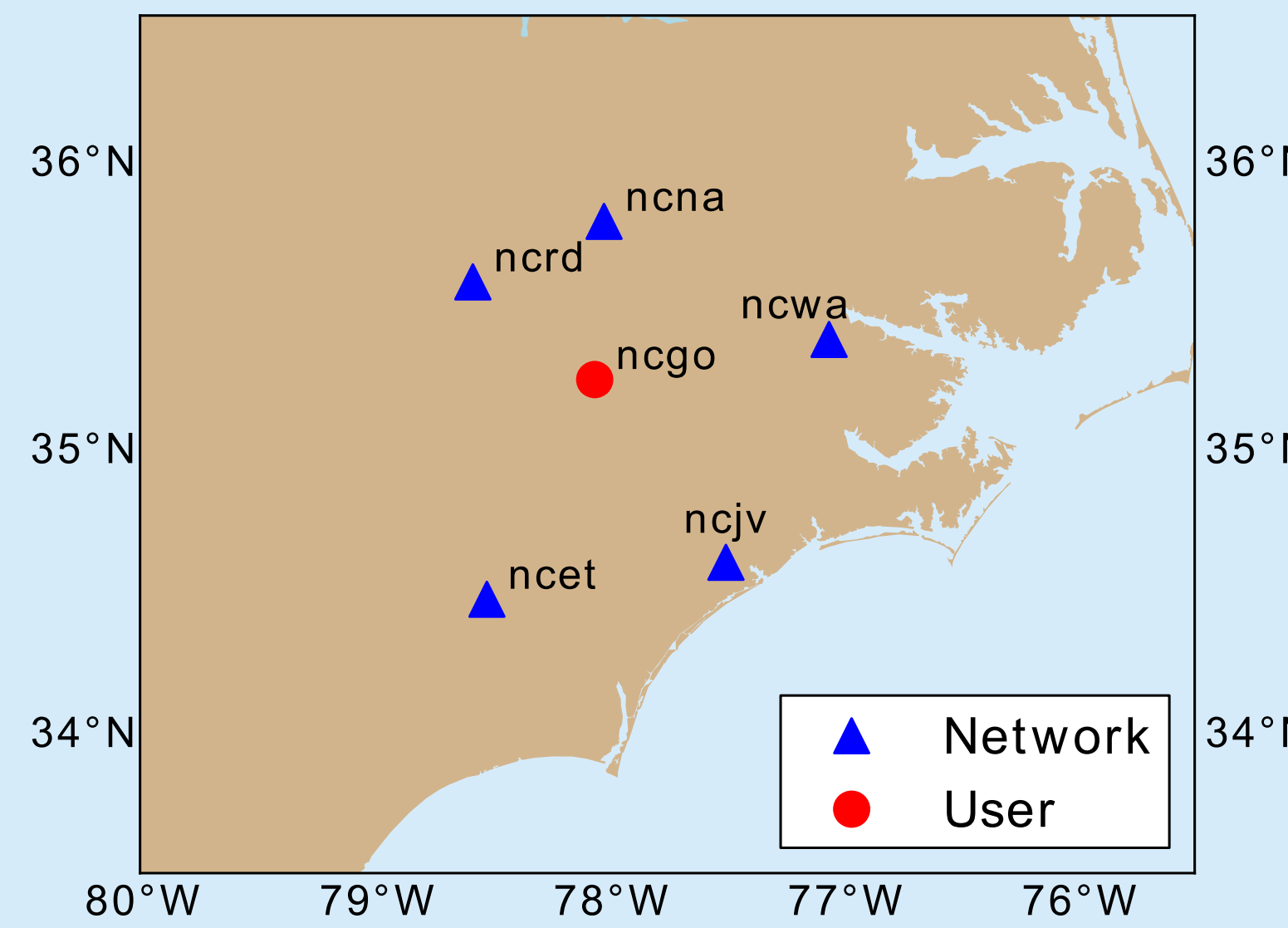
- When precise ionospheric corrections are provided to the user, **the model becomes stronger** than before leading to **more precise phase ambiguities** and, therefore, to higher ambiguity success rates and **shorter TTFA's**, see (a) and (b).
- The quite stable satellite phase biases, see (c), allow for realizing PPP-RTK. When **ionospheric corrections** are further used, the **convergence time** drops to **only 9 minutes**, see (d).
- The estimable **receiver code bias** shows a **stability over time**, with its daily variation not exceeding 20 cm, see (e).



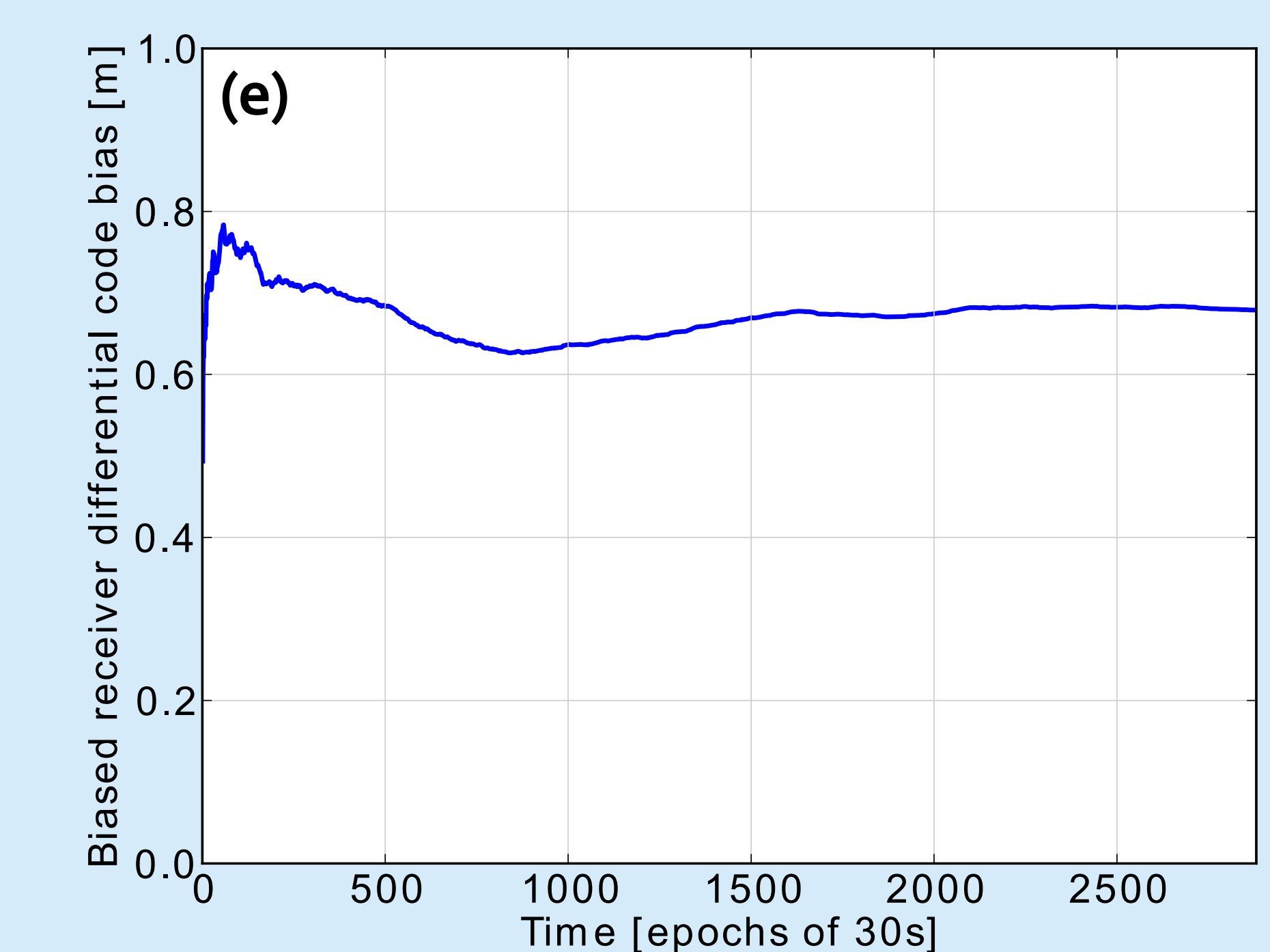
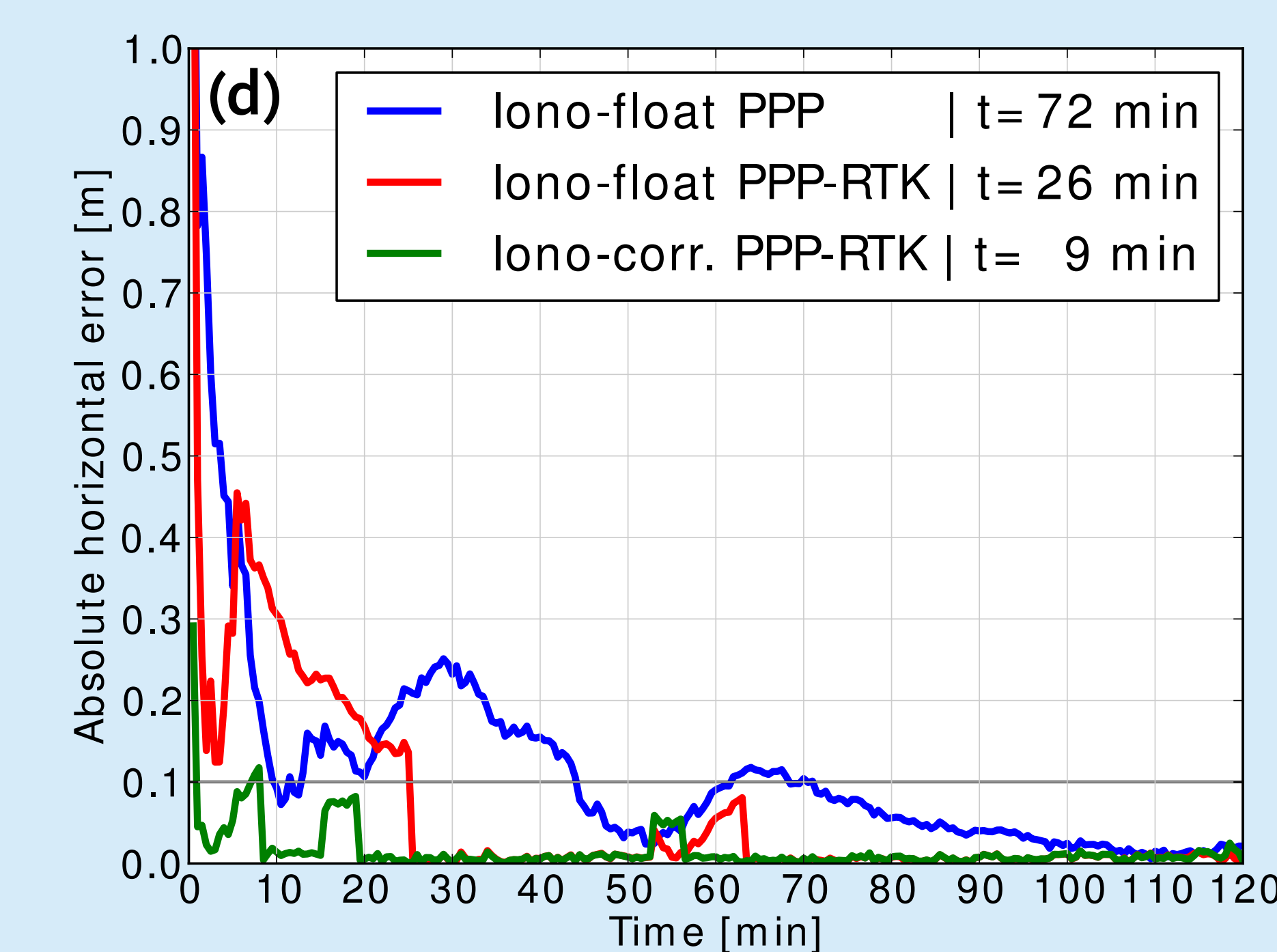
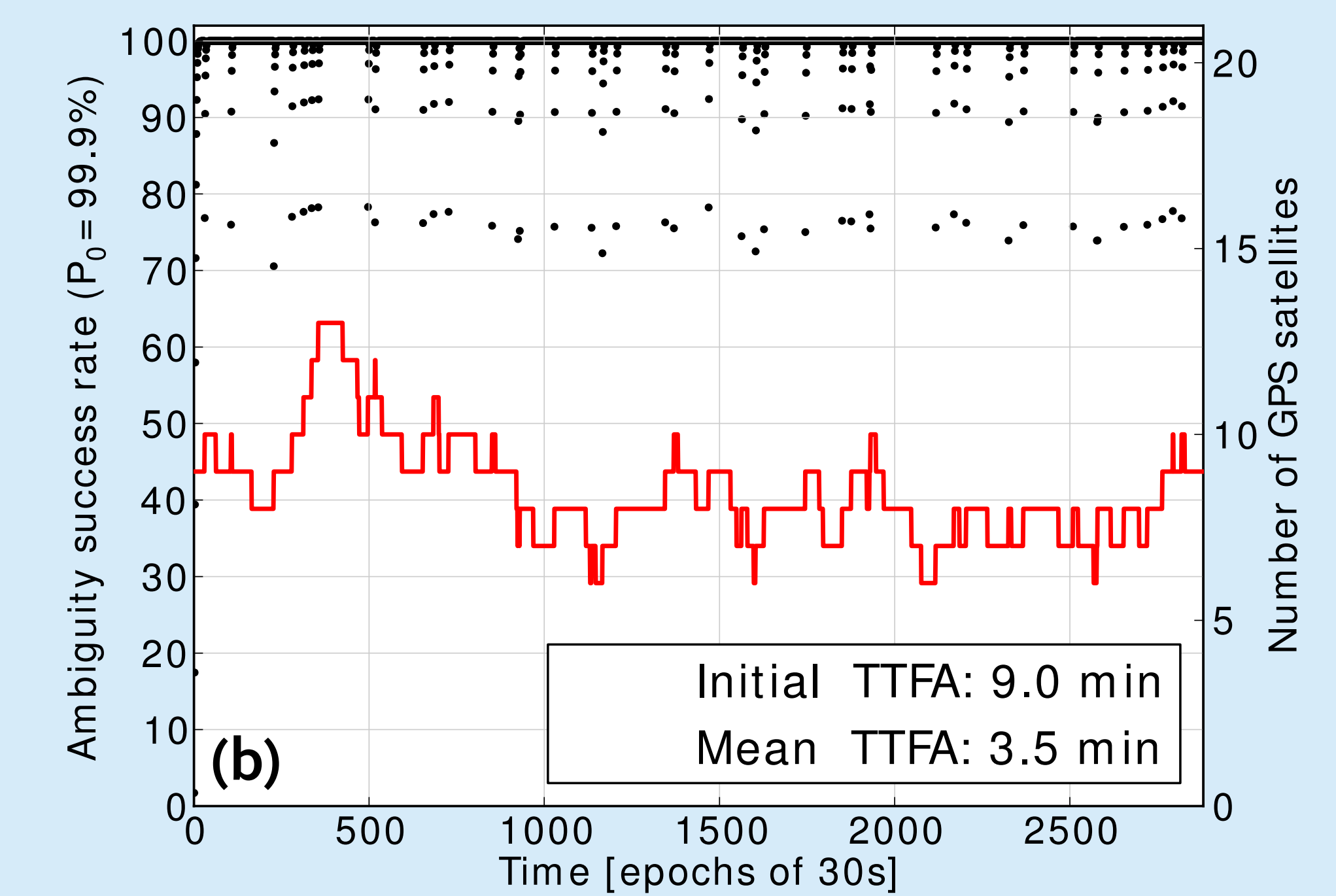
## 4. Data – Processing strategy

For the network and user processing, a network in US with the **largest inter-station distance being ~170 km** was processed for 24 hours on February 15, 2014. **Dual-frequency GPS-only** 30 s data are used for the processing with an elevation mask of 10 degrees.

- Meas. noise at zenith: 30cm / 3mm for code / phase
- Parameter estimation using **Kalman filter**
- Full integer ambiguity resolution using **LAMBDA** [2]
- **User-specific ionospheric slant delays are determined** using the least-squares collocation [3] and the best linear unbiased prediction model [4].



## Ionosphere-corrected PPP-RTK user



- ## 6. Conclusions
- The **ionosphere-float model is weak in terms of IAR** due to the increased number of unknown parameters.
  - Precise ionospheric corrections** can significantly reduce the convergence time.

**Outlook:** A large number of sample data will be processed to infer the **distribution of the achieved convergence times**, due to the **random nature of the GNSS data**.



## References:

- [1] Odijk, D., Zhang, B., Khodabandeh, A., et al., 2016. On the estimability of parameters in undifferenced, uncombined GNSS network and PPP-RTK user models by means of S-system theory. J. Geod. 90 (1), 15-44.
- [2] Teunissen, P.J.G., 1995. The least-squares ambiguity decorrelation adjustment: a method for fast GPS integer ambiguity estimation. J. Geod. 70 (1-2), 65-82.
- [3] Moritz, H., 1978. Least-squares collocation. Rev. Geophys. 16 (3), 421-430.
- [4] Teunissen, P.J.G., Khodabandeh, A., 2013. BLUE, BLUP and the Kalman filter: some new results. J. Geod. 87 (5), 461-473.

## Acknowledgements:

This project has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie Grant Agreement No 722023.

The authors would like to acknowledge the National Geodetic Survey of the United States for making its CORS GNSS data publicly available.

