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# Characterization and Analysis of On-Chip Microwave Passive Components at Cryogenic Temperatures

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**ABSTRACT** This paper presents the characterization and modeling of microwave passive components in TSMC 40-nm bulk CMOS, including metal-oxide-metal (MoM) capacitors, transformers, and resonators, at deep cryogenic temperatures (4.2 K). To extract the parameters of the passive components, the pad parasitics were de-embedded from the test structures using an open fixture. The variations in capacitance, inductance and quality factor are explained in relation to the temperature dependence of the physical parameters, and the resulting insights on the modeling of passives at cryogenic temperatures are provided. Modeling the characteristics of on-chip passive components, presented for the first time down to 4.2 K, is essential in designing cryogenic CMOS radio-frequency integrated circuits, a promising candidate to build the electronic interface for scalable quantum computers.

**INDEX TERMS** Cryo-CMOS, quantum computing, cryogenic, capacitor, inductor, transformer, resonator, quality factor.

## I. INTRODUCTION

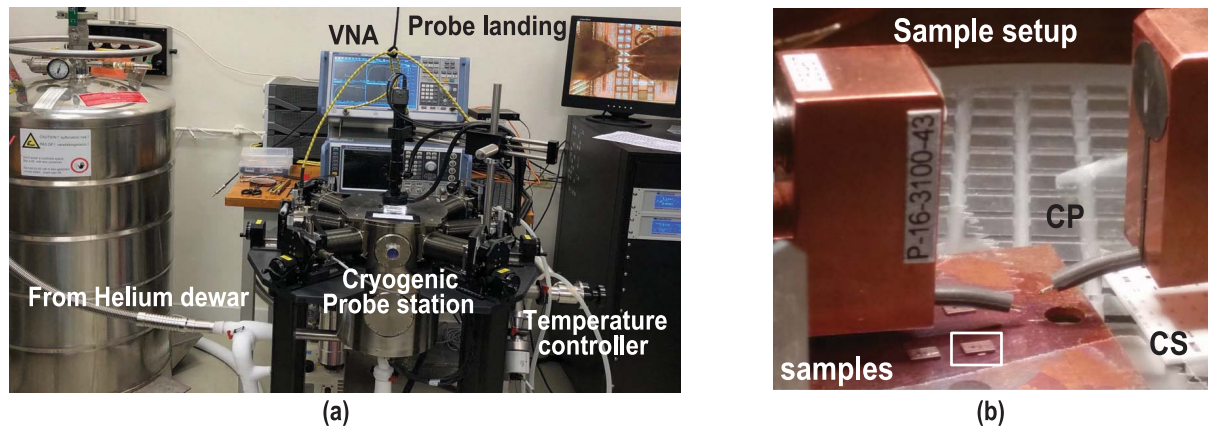
Solid-state circuits operating at cryogenic temperatures have been used for several applications. In quantum computing applications, as the number of qubits starts growing [1], it becomes infeasible to fit the cables between cryogenic quantum bits (qubits) and room-temperature control electronics into a standard cryogenic refrigerator. Thus, we advocate the integration of qubits and control electronics inside the refrigerator [2]. Complementary Metal Oxide Semiconductor (CMOS) circuits operating at cryogenic temperatures (Cryo-CMOS) have been proposed for the implementation of a scalable control and readout interface of cryogenic quantum processors [3], [4].

In deep-space applications, the telemetry link capacity is limited by the signal-to-noise ratio (SNR, i.e.,  $\sim -30$  dB) of the current radio-frequency downlink circuits. To obtain higher SNR, an optical link can be implemented as large

arrays of superconducting nanowire single-photon detectors (SNSPDs) at 1 K, all operating in parallel. The interface and readout of such arrays using room temperature electronics are impractical due to heat load and SNR degradation caused by attenuation of the cables. Moreover, the stringent low noise temperature requirements for the readout could only be achieved by operating at cryogenic temperatures [5].

In space applications, since the circuits have to operate at temperatures far beyond the military range, circuit designs also have to be optimized for cryogenic operation [6]. Besides that, cryo-CMOS technology has also been used in the past to fabricate cryogenic low noise amplifiers (LNAs) for high sensitivity receivers [3], [7] and cryogenic LC oscillators for electron spin resonance detectors [8].

The design of solid-state electronics at cryogenic temperatures has triggered the need for characterization of active



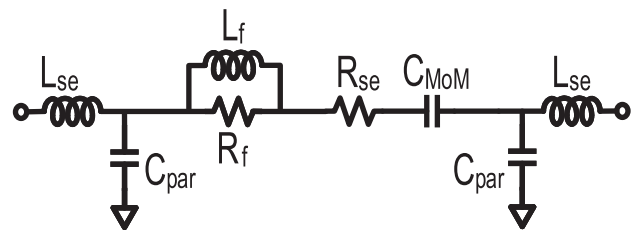
**FIGURE 1.** (a) Cryogenic probe station measurement setup. (b) Sample setup inside the 4 K chamber.

and passive components as required to reliably predict the performance of cryogenic radio-frequency integrated circuits (RFIC) [9]. To some extent, this has been pursued by the scientific community in the case of active devices, which is evident from papers that show DC characterization [10], [11], RF and noise characterization [12], device mismatch [13], [14] of bulk CMOS, as well as DC characterization [15], [16], small-signal and noise characterization [17] of SOI CMOS devices in different technology nodes. In the case of passive devices, cryogenic characterization of off-chip discrete commercial *off-the-shelf* capacitors and resistors [18], [19] proved that the capacitance/resistance can change drastically at those temperatures depending on the material, thus affecting circuit performance. In the case of on-chip passive devices, prior work is limited to the measurement of capacitor and resistor values [20], [21]. Consequently, there is a lack of cryogenic models for on-chip inductive/capacitive components predicting their behavior, variation and quality factor. In this paper, for the first time, we have modeled the characteristics of *on-chip* passive components in bulk CMOS at cryogenic temperatures, which would complement active device models for accurate prediction of the behavior of RFICs at cryogenic temperatures.

Section II presents the test structures and measurement setup. Section III elaborates on the measurement and modeling of metal-oxide-metal (MoM) capacitors. The characterization, lumped-component based modeling and electromagnetic (EM) simulation of a transformer are presented in Section IV. Section V emphasizes the impact of the developed cryogenic models on RFICs, followed by a conclusion in Section VI.

## II. TEST STRUCTURES AND MEASUREMENT SETUP

Several test structures were fabricated in the 1P7M-4X1Z1U TSMC 40-nm bulk CMOS with an ultra-thick metal layer to characterize passive components both at 300 K, and 4 K, comprehensively. A high-density rotative MoM capacitor with a poly shield was chosen from the library provided by the foundry. For the inductance and metal resistance characterization, a transformer with high-inductance *multi-turn*



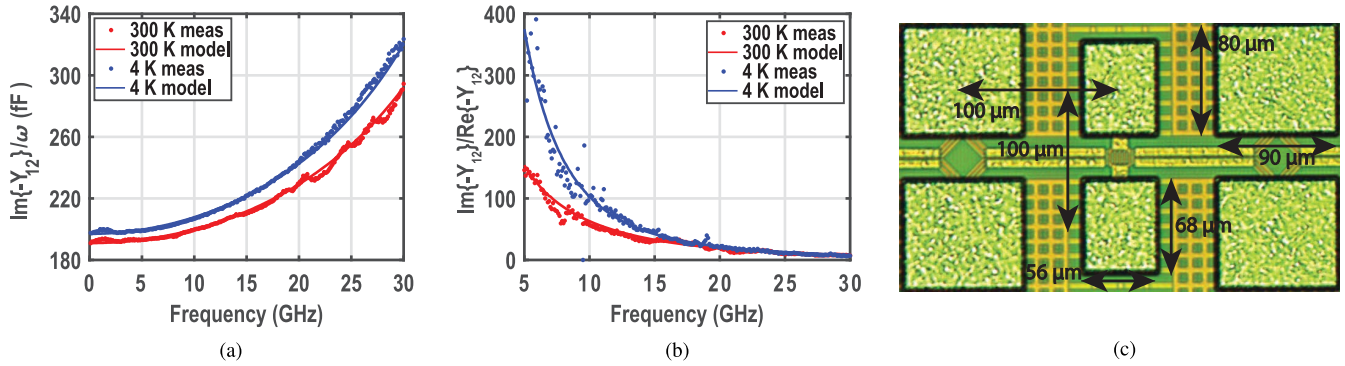
**FIGURE 2.** Lumped-element model of MoM capacitor.

windings was designed to be less sensitive towards calibration errors. Finally, a resonator was also fabricated to validate the cryogenic model of the transformer and capacitor. The substrate was left floating for all the test structures.

The measurements were done using ground-signal-ground (GSG) probes in a 40 GHz Lakeshore CPX cryogenic probe station with R&S ZNB40 vector network analyzer (VNA) (see Fig. 1(a)). To ensure proper thermalization, the dies were mounted with conductive glue on a copper plate (CP), which was securely taped to the sample holder (see Fig. 1(b)).

The thermal conductivity of the chip substrate<sup>1</sup> at temperatures below 20 K is comparable to that at 300 K [22], while thermal conductivity of copper remains the same or improves depending on its purity at 4 K [23], suggesting a good thermal link between the sample holder and device under test (DUT). Since all the measured test structures were passive components and the measurements were done by applying small AC signals, the self-heating should be negligible. During the measurement, it was ensured that the temperature sensor mounted on the sample holder was at 4.2 K. Consequently, although the die temperature was not measured directly, considering the large area under the DUT, no static power dissipation and large copper mass below the dies, it can be concluded that the DUT was at 4.2 K. Moreover, the probes were thermally anchored with thick copper wires to the 4 K stage of the probe station.

1. Boron-doped silicon layers.



**FIGURE 3.** Extraction of MoM (a) capacitance and (b) quality factor. (c) MoM micrograph.

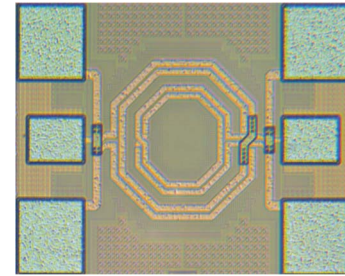
Due to the variation in the GSG probe electrical characteristics over temperature, short-open-load-through (SOLT) calibrations were done right before the measurement using a Picoprobe calibration substrate (CS-5) at the measurement temperature. Although the load standards in the CS-5 are accurately trimmed to their 50  $\Omega$  stated value at room temperature, their absolute value at cryogenic temperature is not specified, and therefore, it was measured by injecting a DC signal. The resistance of the short fixture was measured and it was subtracted from the measurement of the load, so as to remove the effect of cable and GSG probe and to yield the absolute resistance of the load fixture. At 300 K, the measured load was 50.55  $\Omega$ , while at 4.2 K, its value was 49.91  $\Omega$ , showing a negligible ( $\sim 1\%$ ) change. The measured value of the load was then used as part of the cal kit file for VNA calibration.

For probing, all the components were connected to a 100  $\mu\text{m}$  GSG pad without electrostatic discharge (ESD) protection diodes to minimize parasitic capacitance (see chip micrographs in Fig. 3 (c), 4, and 8 (b)). The two ground pads in the GSG structure are shorted to each other at metal-1 (M1) level after using vias from AlCu pad (AP) layer to M1 layer, thus creating the signal-to-ground parasitic capacitance of 60 fF. Finally, the pad parasitics were de-embedded from the measurement results of the test structures by using the open standard [24].

### III. MOM CAPACITOR

A high-density rotative MoM capacitor with a poly shield was taped-out using stacked inter-digitated metal fingers in layers 1 to 5 with a finger width of 100 nm and a spacing of 90 nm. To increase the capacitance to a measurable value and in order not to be dominated by the parasitics of pads, 10 such capacitors were connected in parallel, with 6 horizontal and 38 vertical fingers. This provides a capacitance of 202 fF for an area of 150  $\mu\text{m}^2$  (7.97  $\mu\text{m} \times 1.89 \mu\text{m} \times 10$ ). The pitch for landing the probes is 100  $\mu\text{m}$  and the estimated capacitive coupling between the probe tips based on 3D EM simulation is  $\sim 0.2$  fF.

The MoM capacitor can be modeled by a frequency-independent  $\pi$ -network [25], as shown in Fig. 2, where

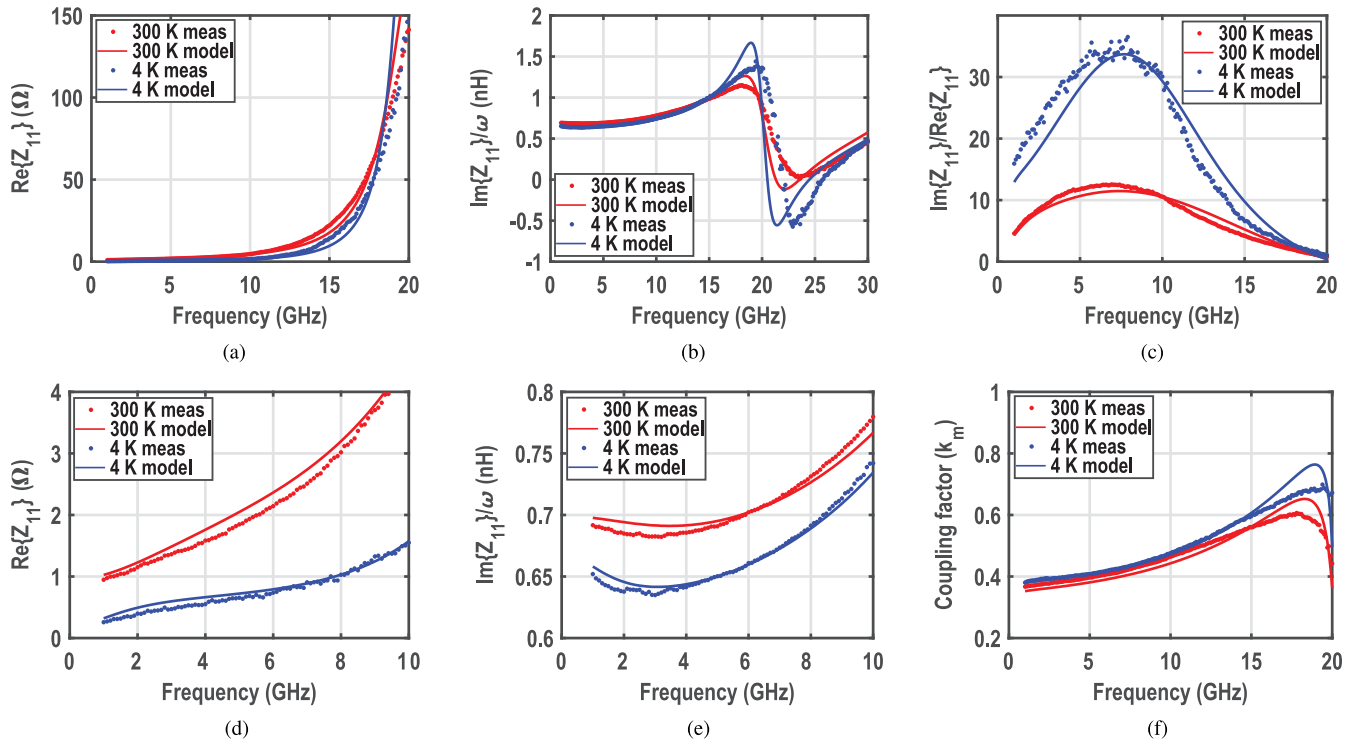


**FIGURE 4.** Transformer micrograph.

$C_{\text{MoM}}$  is the actual capacitance due to the interdigitated metal fingers across an extra low-k inter-metal dielectric [26], and  $C_{\text{par}}$  represents the parasitic capacitance between terminals and ground plane (poly shield).  $R_{\text{se}}$  and  $L_{\text{se}}$  represent the equivalent series resistance and inductance, respectively, of the traces and vias from the pad to the device terminals. Since, an open test fixture was used for de-embedding,  $R_{\text{se}}$  and  $L_{\text{se}}$  must be included in the model. The effect of  $R_{\text{se}}$  is negligible, since the top metal layer was used for interconnection to the pad. However,  $L_{\text{se}}$  affects the self-resonance frequency (SRF) of the structure. The frequency-dependent losses are modeled using  $R_f$  and  $L_f$ , which constitute both metal (skin effect) and dielectric loss.  $L_f$  is not a physical parameter, but a fitting parameter, used to model the frequency-dependent loss. The quality factor of the capacitor above 10 MHz is limited by the series resistance [27], and hence, the leakage resistance (modeled as a very high resistance across the capacitor terminals at DC) due to the interface traps [28] is ignored in the model. The parameters in the model can be extracted using Y-parameters.

Figure 3 (a) shows the measured  $\text{Im}\{-Y_{12}\}/\omega$  ( $\omega$  is the angular frequency), from which the  $C_{\text{MoM}}$  can be extracted at the lowest measured frequency (i.e., 100 MHz), where the effect of parasitic inductance is negligible [29]. The capacitance incurs a slight change at 4 K compared to room temperature (RT) due to variation in the dielectric constant, as the thermal contraction of metals is negligible [23]. Based on several measurements, the precision error in  $C_{\text{MoM}}$  value was obtained to be less than 1% (i.e.,  $\sim 0.5$  fF variation in 200 fF).



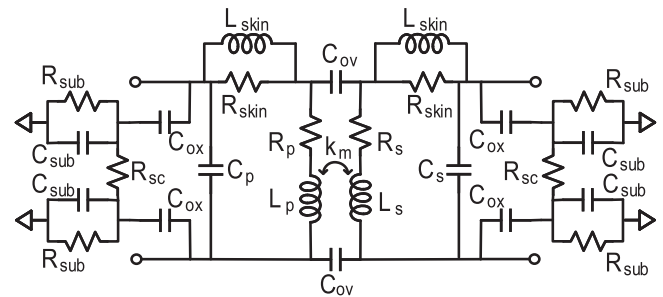


**FIGURE 5.** Extraction of (a) series resistance, (b) inductance, (c) quality factor, (d) series resistance (zoomed in), (e) inductance (zoomed in), (f) coupling factor, from measurement and lumped-element model of transformer.<sup>2</sup>

**TABLE 1.** Model parameters of MoM capacitor at RT and 4 K.

Parameter	Units	RT	4 K
$C_{\text{MoM}}$	fF	191	197
$R_{\text{se}}$	$\Omega$	0.5	0.1
$C_{\text{par}}$	fF	28	26.5
$L_{\text{se}}$	pH	20	20
$R_{\text{f}}$	$\Omega$	3	3
$L_{\text{f}}$	pH	17	24

For the quality factor measurement, the uncertainty increases when the desired real impedance is negligible compared to the VNA reference impedance of  $50 \Omega$  [30]. Hence, at frequencies below 5 GHz (where the quality factor tends towards infinity), the error in the determination of the equivalent series resistance and capacitor's quality factor ( $\text{Im}\{-Y_{12}\}/\text{Re}\{-Y_{12}\}$ ) would be significant and is excluded from Fig. 3 (b). Due to the reduction of dielectric and metal loss at lower temperatures, there is a boost in the quality factor at frequencies below 10 GHz. However, the dielectric loss does not improve over temperature above a certain frequency. This is also in line with the measurement results of capacitors in the military temperature range in a similar technology, as presented in [27]. Consequently, a negligible

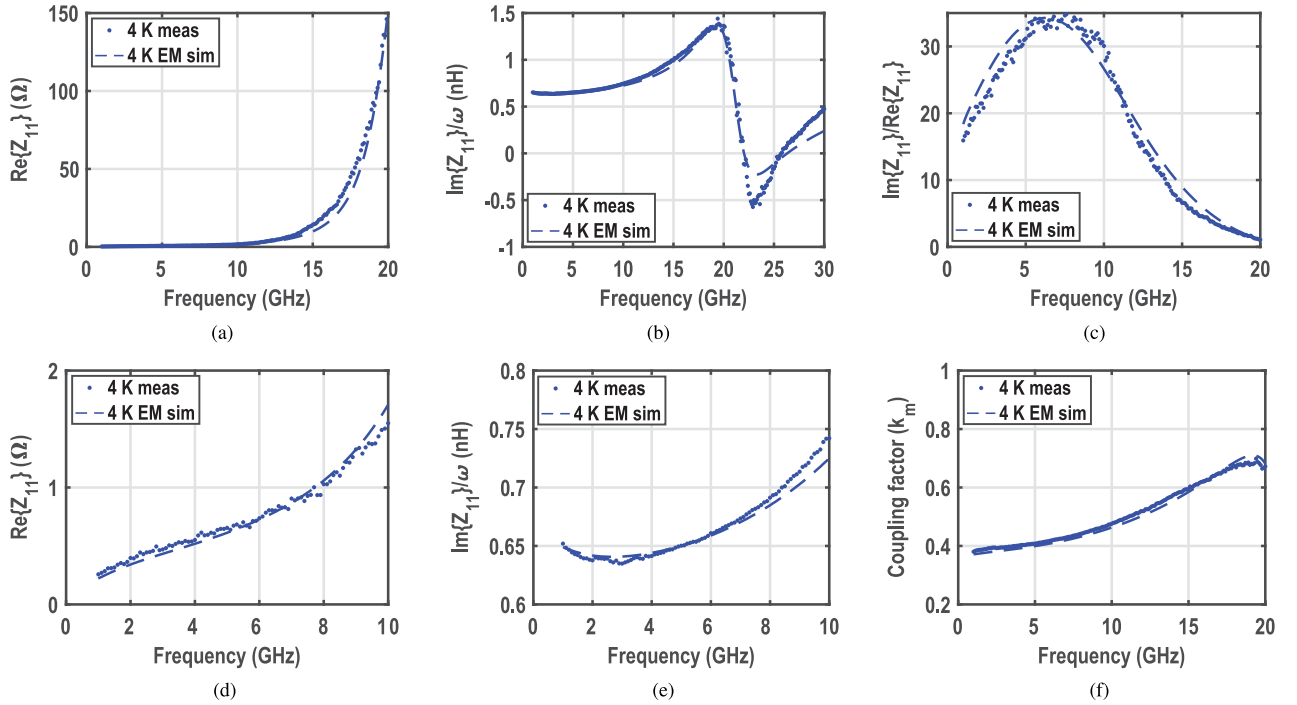


**FIGURE 6.** Transformer model.

quality factor improvement is observed above 15 GHz, as can be gathered from Fig. 3 (b). Table 1 concludes the discussion on MoM capacitors and summarizes the change of the model parameters over temperature.

#### IV. TRANSFORMER

A multi-turn transformer featuring a two-turn primary winding with  $190 \mu\text{m}$  diameter and  $8 \mu\text{m}$  trace width and a two-turn secondary coil with  $130 \mu\text{m}$  diameter and  $7 \mu\text{m}$  trace width, as illustrated in Fig. 4, was designed using the ultra-thick metal layer. Shielding of the transformer was prevented due to a highly resistive substrate at 4 K, thereby not having the need to reduce the tangential electric field losses in low-resistive substrates [31]. An open test fixture was used to de-embed the pad parasitics, which is sufficient for a transformer since the DUT plane is at the GSG pads.



**FIGURE 7.** Extraction of (a) series resistance, (b) inductance, (c) quality factor, (d) series resistance (zoomed in), (e) inductance (zoomed in), (f) coupling factor, from measurement and EM simulation of the transformer.<sup>2</sup>

The dotted lines in Fig. 5 show the extracted parameters of the transformer versus frequency based on the S-parameter measurement at both RT and 4 K. At first glance, it can be observed that there is a slight reduction in transformer inductance, an increase in coupling factor and a substantial improvement in the quality factor of the transformer windings at 4 K compared to RT. To gain more insight and to track the changes in various parameters over temperature, a lumped-element model is presented in Section IV-A. Based on the developed model, some modifications in the physical parameters of the metal stack provided by the foundry are suggested in Section IV-B. The measurement results are also replicated by using EM simulation.

#### A. LUMPED ELEMENT MODEL

The transformer can be modeled using the well-known frequency-independent lumped model for on-chip spiral inductors [32], as depicted in Fig. 6, where  $L_p$  and  $L_s$  represent the inductance,  $R_p$  and  $R_s$  describe the DC ohmic loss, of the primary and secondary windings, respectively.  $k_m$  represents the coupling factor of the transformer.  $C_{ov}$  models the interwinding capacitance,  $C_{ox}$  denotes the oxide capacitance, while  $C_p$  represents the capacitance due to metal lines running in parallel in the multi-turn primary winding.  $C_{sub}$  and  $R_{sub}$  model the substrate capacitance and resistance, respectively.  $R_{skin}$  and  $L_{skin}$  model the frequency-dependent losses (skin effect) in the transformer windings.

$R_p$  (extracted from  $Re\{Z_{11}\}$  shown in Fig. 5(a), (d) at 1 GHz where the skin effect is negligible) is  $\sim 5\times$  lower at

4 K compared to RT, due to the increase in copper conductivity [23]. Note that the resistivity of copper does not reduce proportionally with temperature until 4 K but it saturates at certain temperatures, due to impurities and crystallographic defects in the metal layers [9]. At higher frequencies, the skin effect dominates and the loss becomes proportional to  $1/\sigma_{cu}\delta$ , in which the skin depth  $\delta = \sqrt{2/\omega\mu\sigma_{cu}}$ , where  $\mu$  and  $\sigma_{cu}$  represent the magnetic permeability and conductivity of copper respectively. Since the conductivity increases by  $5\times$ , skin depth and thus the inductor loss at higher frequencies decreases by  $\sim \sqrt{5}$  [33], as confirmed by Fig. 5(a) for frequencies above 10 GHz.

The inductance associated with a loop has two components; internal ( $L_{int}$ ) and external ( $L_{ext}$ ) inductance [34].  $L_{ext}$  dominates the total inductance and is dictated by the currents flowing on the surface of the conductor. Its value is determined by the phase velocity and characteristic impedance of the inductor trace and hence, is a strong function of the coil dimension.  $L_{int}$ , the non-dominant component, is associated with the internal current of the inductor and can be calculated by

$$L_{int} = \frac{R_{ac}}{\omega} = \frac{l}{2W} \sqrt{\frac{\mu}{\sigma_{cu}\pi f}} \quad (1)$$

where  $R_{ac}$  is the ac resistance,  $f$  is frequency,  $l$  and  $W$  are the length and width of the trace, respectively [34]. Intuitively, an increase in conductivity would reduce the skin depth and force the current to flow in the boundary of the conductor. Consequently, the current flowing in the conductor interior reduces, decreasing  $L_{int}$ , and thus, the total inductance. This

**TABLE 2.** Lumped-element model parameters of transformer at RT and 4 K.

Parameter	Units	RT	4 K
$L_p$	pH	691	650
$R_p$	$\Omega$	0.95	0.22
$R_{skin}$	$\Omega$	1.2	0.53
$L_{skin}$	pH	48	48
$C_p$	fF	18	19
$C_{ox}$	fF	50	52
$C_{sub}$	fF	19	22
$R_{sub}$	k $\Omega$	1.24	1000
$R_{sc}$	k $\Omega$	2	2000
$C_{ov}$	fF	4.5	4
$k_m$	-	0.367	0.39

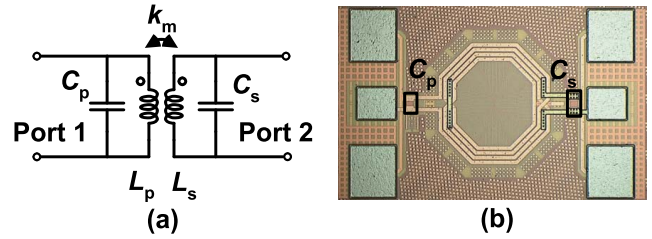
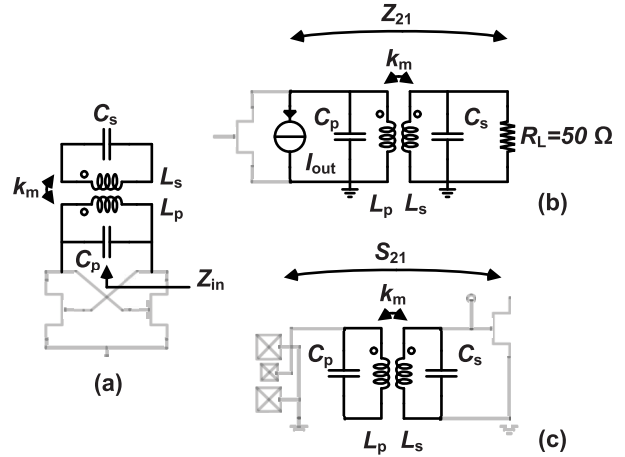
phenomenon is also observed in our measurement results; the  $5\times$  increase in conductivity led to a  $\sim 5\%$  reduction in inductance (extracted from  $Im\{Z_{11}\}$  at the lowest measured frequency), as shown in Fig. 5 (b), and (e).

Figure 5(c) reveals that the peak quality factor of the primary winding of the transformer (extracted from  $Im\{Z_{11}\}/Re\{Z_{11}\}$ ) increases by  $2.7\times$  from RT to 4 K. The improvement is partially contributed ( $1.6\times$  as verified from EM simulation in Section IV-B) by the increase in conductivity and partly due to the reduction of tangential electric field losses in the silicon substrate, as it becomes highly resistive due to dopant freeze-out.

Figure 5(f) shows the measured  $k_m$ , calculated as  $k_m = Im\{Z_{21}\}/\sqrt{Im\{Z_{11}\} \cdot Im\{Z_{22}\}}$ , at both RT and 4 K. The coupling factor is mainly set by the physical dimensions of the transformer, which barely change over temperature (i.e.,  $<1\%$  as shown in [23]). Since the magnetic coupling is not temperature dependent, the slight increase in the coupling factor at 4 K is due to the change in capacitive coupling.

Table 2 summarizes the values of model parameters at RT and 4 K.  $R_{sub}$  and substrate coupling resistance ( $R_{sc}$ ) increases by 3 orders of magnitude at 4 K mainly due to substrate freeze out [35]. For low resistive substrates, the capacitance from the windings to the ground plane is dominated by  $C_{ox}$  [36], [37], while for highly resistive substrates, the effective capacitance is lowered by  $C_{sub}$  in series with  $C_{ox}$ , resulting in a slight increase in the frequency where peak quality factor occurs. The self-resonance frequency of the transformer increases by 5 %, due to the decrease

2. As can be gathered from Fig. 5 (b), the transformer SRF is at 21 GHz. Hence, Fig. 5 (a), Fig. 5 (c), Fig. 5 (f) have been plotted up to 21 GHz. To keep the visibility, the zoomed in version of  $Im\{Z_{11}\}/\omega$  and  $Re\{Z_{11}\}$  are shown up to 10 GHz.

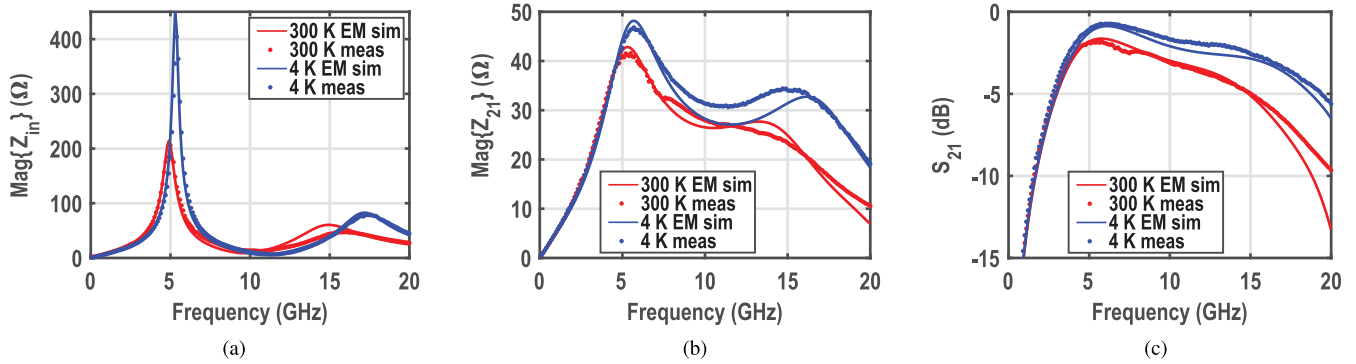
**FIGURE 8.** Tank (a) schematic and (b) micrograph.**FIGURE 9.** Schematic of transformer-based resonator used in (a) oscillator, (b) power amplifier, and (c) low-noise amplifier.

in both inductance and effective parasitic capacitance to ground.

## B. EM MODEL

Besides using lumped-element models of integrated passives, it is convenient for circuit designers to perform EM simulations to generate S-parameters of inductors/transformers and use them for circuit design. For this reason, and to extend the scope of this work towards the design of cryogenic custom integrated passive networks (e.g., hybrid coupler, power splitter, etc.), the metal stack provided by the foundry was modified to enable EM simulations, predicting cryogenic operation.

Based on the performed measurements, the following material properties have been modified in the foundry metal stack: the conductivity of metal-7 (M7) layer was incremented  $5\times$ , to reproduce the copper conductivity increase, while the substrate resistivity was increased  $1000\times$ , to reproduce the effect of carrier freeze-out. The obtained modified metal stack was used to perform EM simulations in Keysight ADS®Momentum®, with an infinite conductive plane beneath the substrate as the current return path, while the simulator temperature was kept at 300 K. The obtained results could accurately predict the performance of the transformer at 4 K, as can be gathered from Fig. 7 (a)-7 (f). The measured quality factor of the windings was slightly different from the simulation results at 4 K. This is attributed to the exclusion of metal fill in EM simulations, which is required to satisfy the density rules [38].



**FIGURE 10.** Tank (a) input impedance ( $Z_{in}$ ), (b) trans-impedance ( $Z_{21}$ ) and (c) insertion loss ( $S_{21}$ ).

## V. IMPACT ON RFICS

To validate the developed models and combine the use of modified EM simulation for inductors/transformers, with the cryogenic lumped-element model of capacitors, a custom transformer-based resonator (matching network), shown in Fig. 8, was designed. The tank is also used to analyze the impact of the cryogenic operation of passive components on the performance of RFIC blocks like oscillators [39], power amplifiers (PAs) [40], and wideband LNAs [41]. The application of the transformer-based resonator in such circuits is shown in Fig. 9.

The custom transformer was realized by an interwinding multitrans spiral inductor in the ultra-thick metal-7 layer with metal-6 underpass and AlCu pad (AP) overpass, while capacitors were implemented as design kit rotative MoM capacitors. The resonator parameters are  $L_p = 1.25$  nH,  $L_s = 1.07$  nH,  $k_m = 0.72$ ,  $C_p = 340$  fF, and  $C_s = 385$  fF. Its performance at 4 K was estimated by combining EM simulation of the developed cryogenic metal stack for the spiral transformer and the modified cryogenic model for the capacitors, through layout abutment. The simulation results are compared with the measurement results in Fig. 10.

Figure 10(a) shows the input impedance of the resonator with Port-2 open ( $|Z_{in}|$ ), which is inversely proportional to the power consumption of a transformer-based oscillator [39]. There is an increase in the impedance peak of the resonator, from RT to 4 K, due to the overall increase in quality factor, which is well predicted by the cryogenic models. Thanks to this improvement, one can obtain the same output voltage swing for smaller current consumption, thus improving the oscillator's power efficiency. The reduction in inductance and the effective parasitic capacitance causes the first resonance to shift towards higher frequencies by 8%. The ratio of the resonant frequencies (i.e., the frequency separation between the impedance peaks in  $\text{Re}\{Z_{in}\}$ ) merely depends on the coupling factor ( $k_m$ ), which increases by 8% as predicted by the model.

Figure 10(b) shows the trans-impedance  $Z_{21}$  of a matching network, where the tank in Fig. 9 (b) is terminated with a  $50 \Omega$  load resistance. This parameter is widely used in calculating the output transfer function when designing wideband

PAs [40]. It can be observed that there is a substantial increase in the  $Z_{21}$  at 4 K compared to RT, especially at higher frequencies. Moreover, there is a slight increase in bandwidth due to the increase in  $k_m$  and an overall shift of the poles of the transfer function towards higher frequencies, due to the decrease in inductance of the windings. Such improvements can be exploited to deliver larger output power for the same current, and over a larger bandwidth at 4 K with respect to RT. So, this is a considerable advantage for PA design at cryogenic temperatures.

Figure 10(c) shows the measured  $S_{21}$  of the tank, which is required to predict the insertion loss (IL) of input/output or inter-stage matching networks in LNAs/PAs. At cryogenic temperatures, the  $S_{21}$  improves, consequently reducing the insertion loss. Note that, for an LNA, the insertion loss of the input matching network directly adds to the overall noise figure. Therefore, such an improvement represents a clear advantage in designing multi-stage LNAs with large bandwidth operating at cryogenic temperatures. As can be gathered from Fig. 10, the developed models can fairly predict the cryogenic performance of the passive network in such circuits.

Such models have also been employed to design more complex circuits, such as a cryogenic CMOS circulator [42], based on LC first- and second-order all-pass filters, and a parametric CMOS LNA [43], with transformer-based passive amplification. The developed models were used to predict the performance of such circuits at 4 K, leading to more optimized designs and gaining more insights about the cryogenic operation of the circuits.

## VI. CONCLUSION

Passive components at cryogenic temperatures show in general higher quality factor ( $\sim 2\times$ ) due to higher metal conductivity and lower loss in the substrate. However, the value of inductive and capacitive on-chip components slightly changes ( $\sim 5\%$ ) from RT to 4 K. These variations can be replicated in an EM simulation by manipulating the resistivity of metals and substrate. As a result, RFIC designers can predict the performance of cryogenic passive devices both by using EM simulation and/or by scaling the presented



lumped model parameters. This enables, in combination with active device models, the reliable design of cryogenic RFICs needed for future large-scale quantum computers.

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