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Robust and Predictive Fuzzy Key Performance Indicators for Condition-Based Treatment of Squats in Railway Infrastructures

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ABSTRACT

This paper presents a condition-based treatment methodology for a type of rail surface defect called "squat". The proposed methodology is based on a set of robust and predictive fuzzy key performance indicators. A fuzzy Takagi Sugeno interval model is used to predict squat evolution for different scenarios over a time horizon. Models including the effects of maintenance to treat squats, via either grinding or replacement of the rail, are also described. A railway track may contain a huge number of squats distributed in the rail surface with different levels of severity. We propose to aggregate the local squat interval models into track-level performance indicators including the number and density of squats per track partition. To facilitate the analysis of the overall condition, we propose a single fuzzy global performance indicator per track partition based on a fuzzy expert system that combines all the scenarios and predictions over time. The proposed methodology relies on the early detection of squats using Axle Box Acceleration measurements. We use real-life measurements from the track Meppel-Leeuwarden in the Dutch railway network to show the benefits of the proposed methodology. The use of robust and predictive fuzzy performance indicators facilitates the visualization of the track health condition and eases the maintenance decision process.

Keywords: Design of key performance indicators, railway track condition monitoring and maintenance, interval fuzzy models.

INTRODUCTION

During the recent years, a modal shift from road to rail has been promoted in Europe. The idea is to increase the share of transport demand for mobility of people and freight. Reduce road traffic congestion, make efficient use of the energy resources and tackle the major challenges of climate change. Major contributions are needed in the optimal management of railway assets, evolving towards a more automated predictive operation where functional assets are monitored. This includes all the important indicators such as economical, safety and societal impacts, considering the perspective of both railway infrastructure manager and users (Zoeteman 2001).

A typical set of railway assets is shown in Figure 1, and it includes the track, station, superstructure, substructure, communication, catenary, control room, signalling system, rolling stock, barrier, security and surrounding. In order to monitor and properly maintain the railway assets, it is necessary to measure the evolution of important health condition indicators over time, also called key performance indicators (KPIs), for each of the critical assets. For example, in the Figure 1, $J_{label}^{Asset}(t)$ relates to the KPI for the health condition of an asset called "Asset", uniquely labelled as "label" at time t . In The Netherlands, the assets in the railway network includes more than 3,000 km of track, 388 stations, being one of the densest networks in Europe. In this network, the design of an optimal maintenance plan for all its assets is a challenging problem. To optimally design the maintenance plans, infrastructure manager requires to provide crucial information of each asset (Stenström et al. 2015), and maintenance decision making considering risk averse situations (Rockafellar and Royset 2015). Thus, the optimal maintenance plan is a necessity because of the high demand from users and government for a better quality of service, and the need of keeping costs as low as possible.

Maintenance Performance Indicators evaluate the system performance and can be used to guarantee that these assets operate at an acceptable level of functionality and safety. In Parida and Chattopadhyay (2007), a

general systems framework is proposed using a hierarchical structure of multicriteria maintenance performance measurements. In Ahren and Parida (2009), the same framework is applied to the case of benchmarking railway infrastructures maintenance operations. Three different hierarchical levels are proposed: strategic level for top management decisions, tactical level for middle management and functional level for supervisors/operators. The general framework requires effective measurements of the health condition of the assets considering that the different assets degrade with different rates due to the effect of different exogenous sources. Particularly, the focus of this paper is to design robust and predictive fuzzy performance indicators for health condition monitoring of railway tracks, considering a particular major type of Rolling Contact Fatigue (RCF) called squat (see Li et al. 2015).

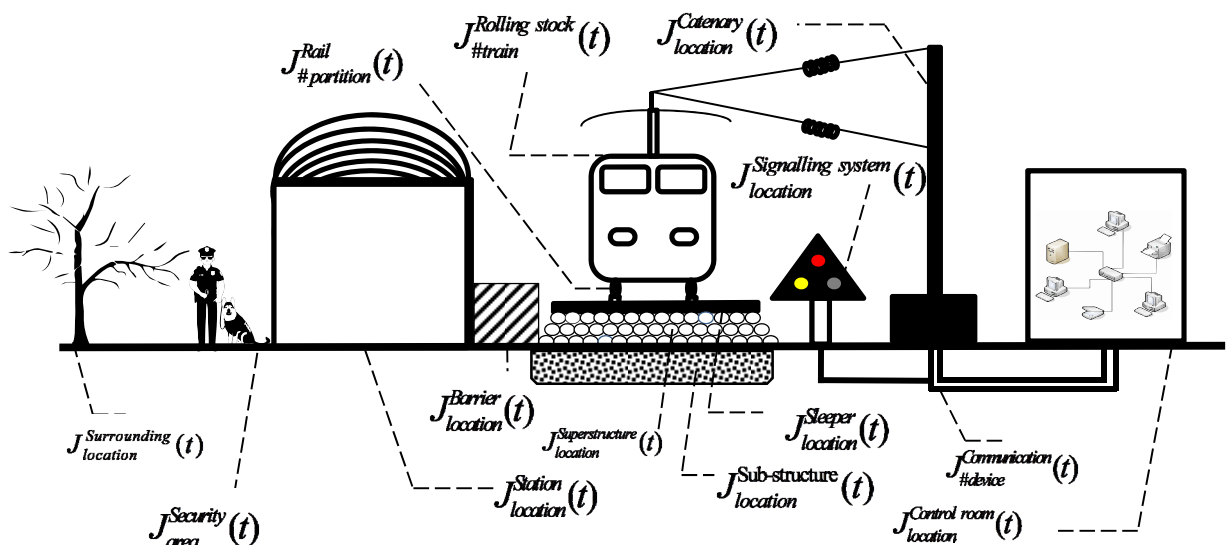


Figure 1: Main components of railway infrastructures.

In The Netherlands over forty percent of the railway maintenance budget is allocated yearly to track maintenance (Zoeteman and van Meer 2006; Zoeteman et al. 2014). The presence of RCFs accelerates track degradation which negatively influences its health condition. It also increases the noise level that affects

75 people living in the surroundings and in a worst case making a huge impact on safety as severe RCF's can
76 result in derailment. For track maintenance to be effective, the planning should consider not only costs but
77 also the dynamics of RCFs. Complex interactions between environment, vehicles, wheels and track interface,
78 structure and also different behaviours under maintenance operation such as grinding and rail replacement
79 can be considered. In Patra et al. (2009) rail degradation is modelled by a time to failure function using MGT
80 (million gross tons) measurements and around 12 failure events, decision making is proposed in a Monte
81 Carlo simulation setting. The maintenance operations are modelled as different cost functions, including rail
82 grinding costs, track tamping costs, rail lubrication costs, among other maintenance operations. Stenstrom et
83 al., (2015) assess the value of preventive maintenance in comparison with corrective maintenance. The idea
84 is to analyse cost-benefit of using preventive maintenance including four different maintenance costs:
85 maintenance inspections, repair of potential failures, repair of functional failures and service/production loss.
86 In the case study for a Swedish railway line, the ten costliest railway sections are found to have three times
87 the tonnage compared to the sections with the lowest costs, and also the costliest sections experience 4.5
88 times more track failures. The conclusion is that the railway sections with the lowest total maintenance cost
89 have implemented more preventive maintenance actions.

91 In the literature, different studies have been carried out to present how a degradation model for tracks can
92 be embedded on asset management to facilitate maintenance plans. Track geometry measurements relying
93 on statistical analysis are used to capture the track degradation effect (Sadeghi and Askarinejad 2010;
94 Andrade and Teixeira 2011; Andrews 2012; Andrade and Teixeira 2012; Vale and Lurdes 2013; Nathanail
95 2014; Guler 2014; Weston et al., 2015). In those papers, different time-dependent degradation models are
96 proposed, they can all be used to improve maintenance interventions. Estimation of the track safety and
97 considering the probability of rail break has also been investigated (Schafer and Barkan 2008; Burstow et al.
98 2002; Sandstrom and Ekberg 2009). Detailed mechanical models can give many insights about the evolution

of rail defects; however, the use of those models for maintenance planning operations require sophisticated knowledge about the track and its operational conditions that are not always available or easy to obtain in practice. Fuzzy logic has increasingly been used in different fields; in particular, in the ones where uncertainties can influence the decision process. It is used to measure performance in different infrastructures by predicting failure of components (Senouci et.al 2014; Sadiq et al. 2004), optimizing asset condition (Xu et al. 2014; Wang and Liu 1997) and decision making (Khatri et al. 2011). In this paper, we propose the use of interval fuzzy model to capture the most important dynamics of squats in railway infrastructure, from the maintenance operation point of view. We aim to keep the prediction as simple as possible, but suitable enough to ease decision making in practice. The use of key performance indicators (KPIs) that are able to explicitly include the dynamics of the deterioration of the assets, together with an appropriate set of scenarios for the principal sources of stochasticities that might affect their performance are recommended. A fuzzy Takagi Sugeno (TS) interval model (Škrjanc, 2011; Núñez and De Schutter, 2012; Sáez et al., 2015) is calibrated using real-life data collected over years of field test and measurements. That helps obtaining numerical models capable to predict squat growth over a time horizon under different possible scenarios and under different maintenance decisions.

Based on the interval fuzzy models for squats, a condition-based methodology for rails is proposed using different KPIs that are defined in a track-partition level which allows the grouping of defects located in a given track partition. In this methodology, number and density of squats are considered over a prediction horizon under three different scenarios, vis. slow, average and fast growth. Then, to facilitate visualization of the track health condition and to ease the maintenance decision process, we propose a fuzzy global KPI based on fuzzy rules for each partition that merges the different KPIs over prediction horizon and scenarios. The methodology is evaluated with data from a Dutch railway track, relying on the use of technology based Axle Box Acceleration (ABA) measurements, capable to detect the early stage squats on the rail (Molodova et

al. 2014, Li et al. 2015). An introduction of the ABA measuring system is described in ABA based health condition monitoring in railways, including background of the ABA measurement system and its application in rail condition monitoring based on ABA.

Figure 2 shows the flowchart of the proposed methodology divided in three steps. In Step 1, relying on ABA measurements, the health condition of the track and severity are estimated. A list of defects is assumed to be provided by the detection algorithm. In Step 2, using interval fuzzy TS model, the growth of each detected defect i is evaluated over time and different possible evolution scenarios are considered. Three models are evaluated, with grinding, replacement and without maintenance. The idea is to see the consequences of the maintenance operations on the detected squats for different scenarios over a prediction horizon. At the end, in Step 3, a global fuzzy KPI is used to describe the condition at a track partition level, for a given travel direction, left and right rails. The global fuzzy KPI at a partition, combines the effects of a vector of KPIs over a prediction horizon, considering three most representative defect evolution scenarios.

The paper is divided as follows. In next section, the main elements of the ABA based detection methods are presented. Next, fuzzy interval models for squats are presented for three cases: without maintenance, after grinding and after replacement. After, different KPIs are defined at a track partition level in order to aggregate the local dynamic behaviour of squats. Because of the number of scenarios and prediction horizon, the fuzzy global KPI is proposed to facilitate decision making. Later, the numerical results and discussion are presented. Finally conclusions and further research are discussed.

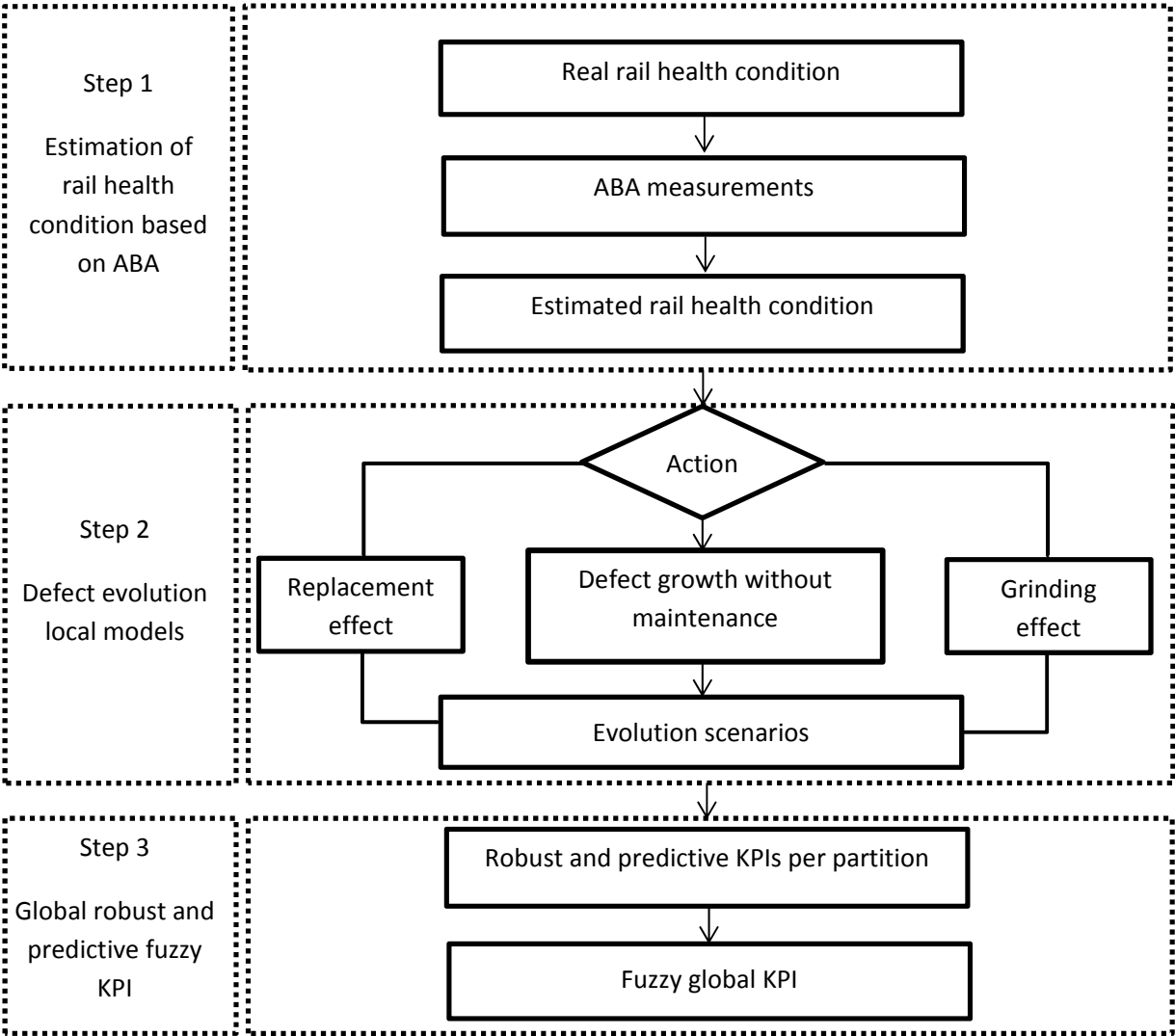


Figure 2: flowchart of the proposed methodology

ABA BASED HEALTH CONDITION MONITORING IN RAILWAYS

a. BACKGROUND OF THE ABA MEASUREMENT SYSTEM

There are different methods to diagnose the condition of rail defects, including ultrasonic measurements, eddy current testing, image recognition and guided-wave based monitoring among other technologies. Each of them has different advantages and disadvantages. In this paper, we need a technology capable to detect defects in an early stage, thus we consider the use of ABA measurements (Li et al. 2008; Molodova et al.

2014). Li et al. (2015) investigated the feasibility of detecting early-stage squats using an ABA prototype. It is reported that squats could be detected by analysing the frequency content of the ABA signals in the wavelet power spectrum. In practice, the useful frequency band for early detection of squats ranges from 1000-2000 Hz and 200-400 Hz (Molodova et al. 2014). In the literature, it has been reported that ABA systems can be employed to detect surface rail defects like corrugation, squats and welds in poor condition. The ABA system offers the advantages of (1) having a lower cost than other types of detection methods, (2) it is easy to maintain and (3) can be implemented in-service operational trains. Other significant advantages that ABA offers over similar measurement systems are (4) the ability to detect small defects with the absence of complicated instrumentation and (5) the ability to indicate the level of the dynamic contact force (Molodova et al. 2015).

b. RAIL CONDITION MONITORING BASED ON ABA

In this study, we are users of the ABA detection methodology presented in Li et al. (2015) and Molodova et al. (2014); thus, we assumed that a list of squats and their location are available. Let's define the counter of squat defects as $i=1,2,\dots,N_{defects}$, where x_i represents the position of the squat i . We define $H(x,k)$ and $L(x,k)$ as the real rail condition and real squat length respectively, defined at position x and time step k . We only focus on positions x_i where squats are detected. To simplify the notation, we assume $H_i(k)=H(x_i,k)$ and $L_i(k)=L(x_i,k)$ represent the severity and the length of squat i at time step k .

To systematically classify squats in terms of severity, we follow the terminology used in Smulders (2003), UIC Code (2002) and Rail Damages (2001). The definitions of these three references are compatible to one another. Although the transition between one class to the other is not always abrupt, we have defined fixed values for those transitions according to our experience. Depending on the squat length $L_i(k)$, measured in mm, the severity of the squat can be used to represent the health condition of the rail at location x_i as follows:

$$H_i(k) = \begin{cases} S & \text{if } 0 \leq L_i(k) < 8 \\ A & \text{if } 8 \leq L_i(k) < 30 \\ B & \text{if } 30 \leq L_i(k) < 50 \\ C & \text{if } 50 \leq L_i(k) < 60 \\ RC & \text{if } L_i(k) \geq 60 \end{cases} \quad (1)$$

where S refers to a seed squat, A is a light squat (A squat), B is a moderate squat (B squat), C is a severe squat (C squat) and RC is a squat with risk of derailment. The boundaries were defined based on general guidelines to classify squats. Figure 3 depicts an example of defects growths collected from field measurements in the track Meppel-Leeuwarden. In the figure, x-axis represents kilometre position of the track where the squats are located and y-axis indicates time in three different months, month 0 (moment of the measurement), month 6 and month 12. In the diagram, A squats are drawn as circles and B squats are squares. Different squats grow with different rates. In the average case, the track measurements show that it takes approximately 9 months for a A squat of 20 mm to evolve into a B squat of 30 mm.

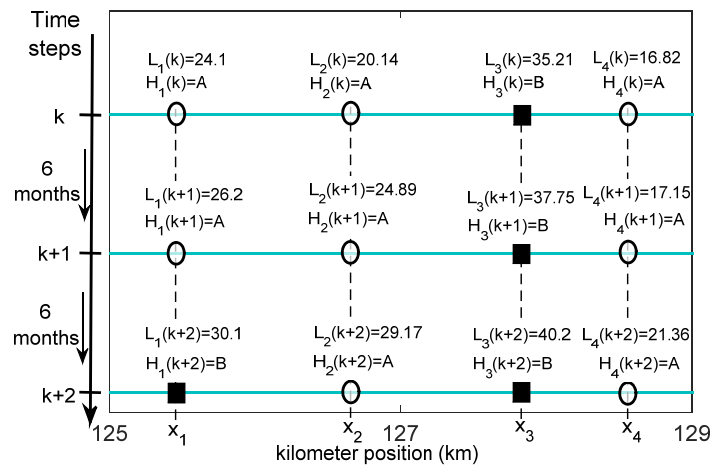


Figure 3: An example of defects evolution over time. The x axis is the kilometre position in the track, x_i the position of squat i , y axis is time every six months. In circles are A squats, squares are B squats.

In this study, the ABA measurements are used to develop a model for defect evolution. For each squat, the related energy of the ABA is available using wavelet spectrum analysis and advanced signal processing

methods (Molodova et al. 2014). Relying on the ABA measurement, the energy values of the ABA signals can be calculated at every position x at time step k as $E(x, k)$. From the energy signal, we are interested only in those locations with squats, namely $E_i(k) = E(x_i, k)$. For using the energy of the ABA signal to predict the squat length evolution, a correlation between the squat length and energy of the ABA signal was performed. Photographs from track visits of several years are used to measure the lengths of the squats and to fit the piecewise linear correlation model. The estimated length $\hat{L}_i(k)$ of squat i at time step k as function of the energy value $E_i(k)$ is given by:

$$\hat{L}_i(k) = \begin{cases} g_1 E_i(k) + q_1 & \text{if } E_i(k) < 80 \\ g_2 E_i(k) + q_2 & \text{if } 80 \leq E_i(k) < 170 \\ g_3 E_i(k) + q_3 & \text{if } 170 \leq E_i(k) < 300 \\ g_4 E_i(k) + q_4 & \text{if } E_i(k) \geq 300 \end{cases} \quad (2)$$

where the slope of local linear functions is g_m , $m=1, \dots, 4$, and the bias q_m , $m=1, \dots, 4$, are adjusted to the specific track. For relation (2), we have been users of previous work of our group, Li et al. 2011, Li et al. 2015, Molodova et al. 2015. In general, we can say that the correlation coefficient and residual standard get affected by the speed of the measurement train. In this paper, we assumed that the measurement is done at commercial speed as was done for the test measurement so far, and we have disregard segments that were measured out of a reasonable range of speed.

A global view of the Step 1 of the methodology, estimation of track health condition based on ABA, is presented in Figure 4. As shown in the figure, in order to estimate length $L_i(k)$, the energy value $E_i(k)$ is calculated using the ABA measurement. Hence, relying on the estimated squat lengths, the rail health condition $H_i(k)$ can be approximated. In the figure, a squat is detected with an energy value $E_i(k) = 145 \text{ m}^2/\text{s}^4$, the estimated squat length $\hat{L}_i(k) = 43 \text{ mm}$ and the estimated health condition $\hat{H}_i(k) = B$.

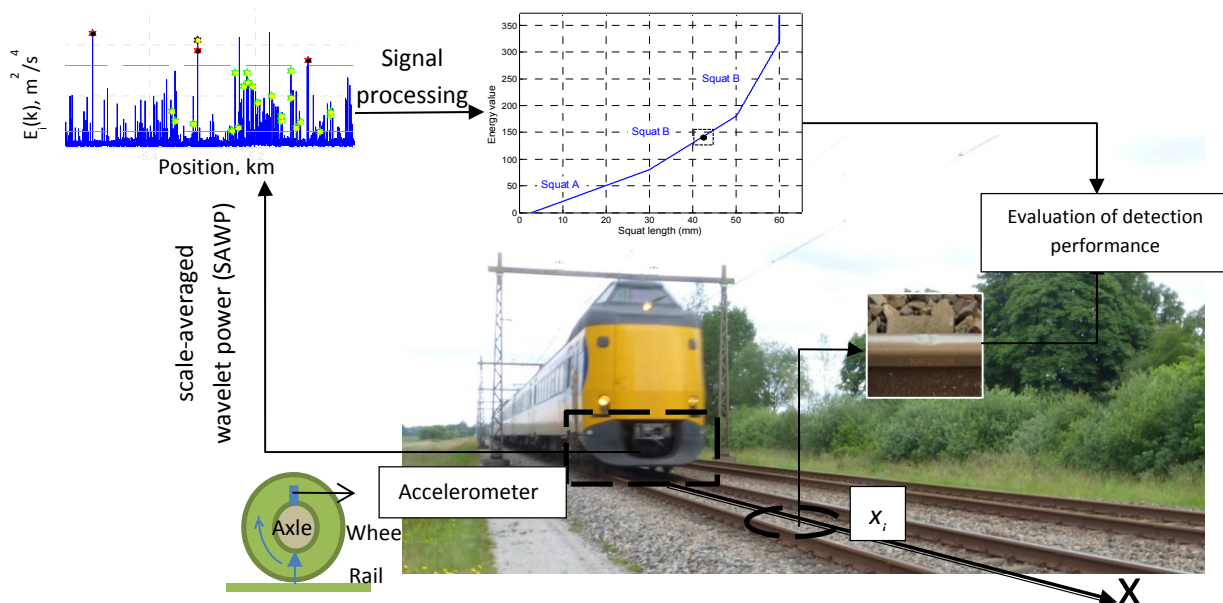


Figure 4: Global scheme of the main components of the Step 1: Estimation of track health condition based on ABA

FUZZY INTERVAL MODELS FOR SQUATS

a. MAINTENANCE ORIENTED MODELS FOR SQUATS

Typically, maintenance slots in the Dutch railway network are decided based on long and short term planning for preventive and corrective maintenance respectively. In the long term, the contractor should inform asset manager at least one year before cyclic grinding for using the equipment needed. In the short term, normally, the maintenance is performed when the squats are in the last stage of growth (C squat). Thus, a predictive approach by employing well designed KPIs should aim to improve both short and long term planning, (1) keeping a good balance between costs and health condition of the track, (2) simplify the design of maintenance plan over the whole time horizon and (3) increase indirectly the track safety.

The experimental results show that each squat can grow with different rates. The estimation of squat lengths can be affected by the subjectivity of the human error. For instance, one source of uncertainty comes from the fact that visually only the rusty area of the defects is used to measure length, while the defect might be longer. Fuzzy systems can work under subjective environments. In the proposed methodology, the design of the global fuzzy KPI deals with the subjectivity. The definition of a low or a big number of defects will depend on the subjectivity of the inframanager, and on how this information is incorporated for maintenance decision making. In order to generalize this characteristic, fuzzy confidence intervals can be used to capture the stochasticities of different scenarios for the squat growth. The upper bound of the interval represents a worst case scenario, while the lower bound represents a slow rate grow scenario. In the fuzzy interval approach, the average behaviour is given by a Takagi-Sugeno (TS) fuzzy model. This is used to approximate nonlinearities by smoothly interpolating affine local models. Each local model is involved in the global model based on the activation of a membership function. According to literature, the identification of fuzzy interval models is divided on three steps: clustering method to generate fuzzy rules, identification of the TS local linear parameters (average model), and identification of the fuzzy variance for each rule (Škrjanc et al. 2004; Škrjanc 2011). In this paper, we use the fuzzy interval approach proposed in Nunez and De Schutter (2012) and Sáez et al. (2015), which includes Gustafson Kessel clustering, local identification of the linear parameters and optimization of a parameter α to adjust the width of the interval, minimizing both area of the band and number of data points outside the band.

The general problem of interval defect evolution is as follows. Let's consider different defect growth scenarios $h = h_1, h_2, \dots, h_H$, time steps $t = k, k+1, k+2, \dots, k+N_p$, and $u(k)$ the maintenance action at time step k . The prediction model for the growth of a squat can be written as:

$$\hat{L}_i^h(k+1) = f_j^h(L_i(k), u(k)), \quad x_i \in [x_j, x_{j+1}] \quad (3)$$

where $\hat{L}_i^h(k+1)$ is an estimation of length of the squat i located in the track partition j at the time step $k+1$ considering the scenario h . The model considers the effect of maintenance $u(k)$ and the initial condition of the squat $L_i(k)$. Depending on the location of the squat i , x_i , we use a local model corresponding to the track partition j where the squat is located, $x_i \in [x_j, x_{j+1})$. We assume the dynamics for different squats are similar if they are in the same track partition under the same scenario.

In this paper, three maintenance actions are considered, $u(k) = \{u_1, u_2, u_3\}$, where u_1 is without maintenance, u_2 is grinding and u_3 is replacement. Also three scenarios are evaluated, $h = h_1, h_2, h_3$, where h_1 represents slow growth, h_2 average growth and h_3 is fast growth scenarios.

b. DYNAMICS OF SQUATS WITHOUT MAINTENANCE

In the absence of maintenance, $u(k) = u_1$, the prediction model for the average growth scenario, h_2 , is formulated based on TS fuzzy model:

$$\hat{L}_i^{h_2}(k+1) = f_j^{h_2}(L_i(k), u_1) = f_j^{\text{TS}}(L_i(k)) = \sum_{r=1}^{N_R} \beta_{jr}(L_i(k)) L_{jr}(k), \quad (4)$$

$$L_{jr}(k) = a_{jr} L_i(k) + b_{jr}, \quad (5)$$

$$\beta_{jr}(L_i(k)) = \frac{A_{jr}(L_i(k))}{\sum_{r=1}^{N_R} A_{jr}(L_i(k))}, \quad (6)$$

where a_{jr}, b_{jr} are the parameters of the fuzzy local model on rule r , $r=1, 2, \dots, N_R$ and $\beta_{jr}(L_i(k))$ is the normalized activation degree of the rule r . In this paper we will use Gaussians to model the membership

degrees, $A_{jr}(L_i(k)) = \exp\left(-0.5c_{jr,1}\left(L_i(k) - c_{jr,2}\right)^2\right)$, defined by parameters $c_{jr,1}$ and $c_{jr,2}$ given by the Gustafson Kessel clustering algorithm.

Once the TS model is obtained, slow growth scenario and fast growth scenario are used as lower and upper bound of the average growth scenario, $\hat{L}_i^{h_2}(k+1)$, respectively. The equations can be defined as:

$$\hat{L}_i^{h_3}(k+1) = \overline{f_j}^{\text{TS}}(L_i(k)) = \sum_{r=1}^{N_R} \beta_{jr}(L_i(k)) \left(L_{jr}(k) + \alpha^{h_3} \Delta_{jr}(L_i(k)) \right) \quad (7)$$

$$\hat{L}_i^{h_1}(k+1) = \underline{f_j}^{\text{TS}}(L_i(k)) = \sum_{r=1}^{N_R} \beta_{jr}(L_i(k)) \left(L_{jr}(k) - \alpha^{h_1} \Delta_{jr}(L_i(k)) \right) \quad (8)$$

$$\Delta_{jr}(L_i(k)) = \sigma_{jr} (1 + \psi_{jr}^T (\phi_{jr} \phi_{jr}^T)^{-1} \psi_{jr})^{0.5} \quad (9)$$

where $\hat{L}_i^{h_3}(k+1)$ is the estimated growth length of squat i in time step $k+1$ in fast scenario, and $\hat{L}_i^{h_1}(k+1)$ is estimated growth length in slow scenario, α^{h_3} and α^{h_1} are tuning parameters in the fast growth scenario and the slow growth scenario respectively. Moreover, $\phi_{jr} \phi_{jr}^T$, $\psi_{jr} = [L_i(k), 1]^T$ and σ_{jr} are covariance matrix, regression matrix and variance of the local model.

Figure 5 depicts the proposed fuzzy confidence interval model including 177 data points used to capture the squat evolution in different stage of growth. A subset of the data used for analysis is included in Table 1. A squats from 8 to 30 mm in length have no or shallow cracks. The B squats ranging from 30 to 50 mm grow quickly. The B squats evolve to C squats when the network of cracks beneath the squat gets further spread. All three stages are shown by reference photos of A squat, B squat and C squat in Figure 5.

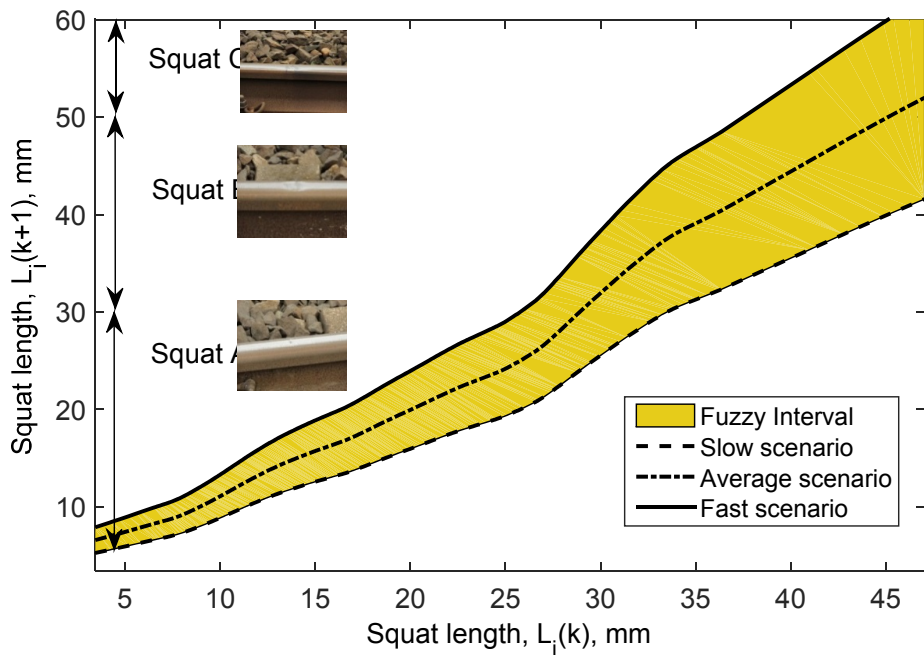


Figure 5: Interval fuzzy model for squat growth in the case study track.

Table 1: a subset of data used for squat analysis including defect position, km, and visual length, mm, at time k and k+1

Squat	Position, km	$L_i(k)$, mm	$L_i(k+1)$, mm	Squat	Position, km	$L_i(k)$, mm	$L_i(k+1)$, mm
1	104.8438	30.7260	34.7465	11	105.4613	22.8311	24.6695
2	105.1051	37.7420	40.5086	12	105.4953	19.5933	22.0216
3	105.1404	33.2264	37.0496	13	105.5827	14.5360	16.7962
4	105.2116	34.2207	37.7779	14	105.5852	19.5432	21.9787
5	105.3215	46.7870	49.1017	15	105.6353	11.0032	13.9019
6	105.3901	33.0151	36.8862	16	105.6591	25.1642	27.1955
7	105.4195	19.1797	21.6607	17	105.7462	15.4564	17.7552
8	105.4269	20.2236	22.5435	18	106.3105	28.7262	32.2116
9	105.4344	9.4918	12.4747	19	106.8735	55.1141	57.1707
10	105.4561	33.2798	37.0903	20	107.2845	17.8761	20.4044

c. RAIL GRINDING EFFECT

Squats can be effectively treated by grinding when they are in early stage of growth. Cyclic rail grinding keeps control of not only maintaining the rail profiles but to plan track maintenance efficiently (Magel and Kalousek 2002). Figure 6 depicts squat growth before and after grinding where black points show those squats that did

not disappear after grinding. As seen in the figure, some A squats are located in the effective zone of grinding such that these squats have a zero length after grinding. Those A squats that are imminent to become B squats are located in the ineffective zone for grinding as well as B squats and C squats. Moreover, three growth scenarios in the effective zone are specified to capture the squat evolution rate. Even though grinding severe squats postpones rail replacement, it could accelerate squat evolution as the cracks are not totally disappeared.

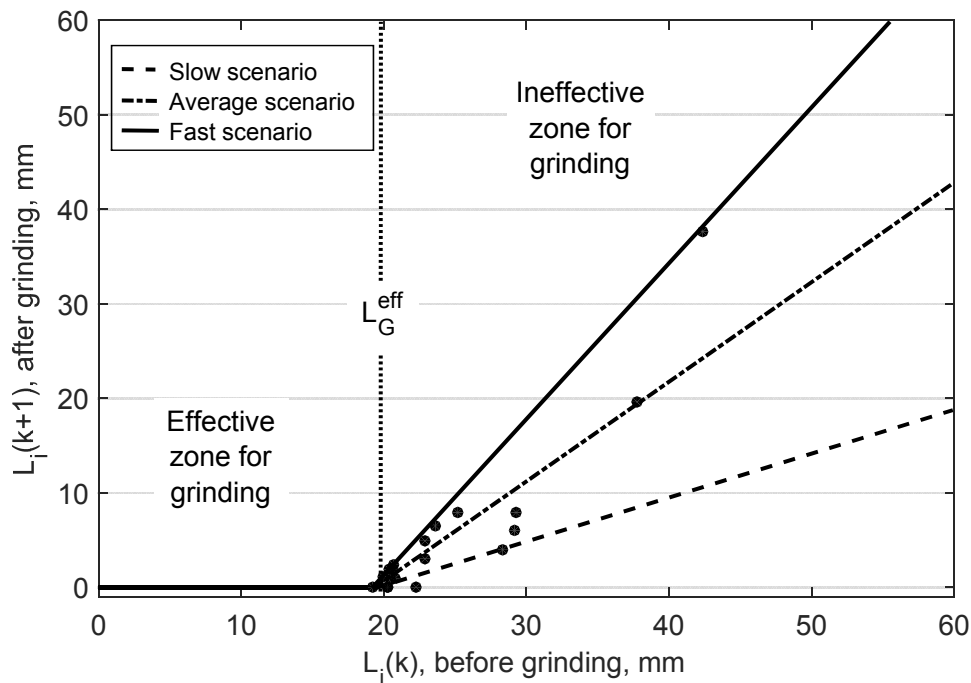


Figure 6: Squat growth before grinding and after grinding classified in two effective and ineffective zones for grinding operations. In this case, the depth of the grinding was around 1.0 mm.

The growth model for squat i by considering grinding effect can be expressed as:

$$\hat{L}_i^h(k+1) = \begin{cases} 0 & L_i(k) \leq L_G^{eff} & \text{Effective zone for grinding} \\ z_G^h(L_i(k) - L_G^{eff}) & L_i(k) > L_G^{eff} & \text{Ineffective zone for grinding} \end{cases} \quad (10)$$

where L_G^{eff} is the critical squat length that estimate effectivity of grinding, L_G^{eff} is around 20mm in Figure 6 for a grinding depth of 1.0 mm, z_G^h is the slope of the linear model in the ineffective zone for grinding for different scenarios h , slow, average and fast growth scenarios.

d. RAIL REPLACEMENT EFFECT

When the squat severity becomes worse and cracks are grown considerably, grinding is not efficient anymore. Therefore, replacement is the only solution. As replacing a piece of rail takes time and it is costly, an optimal decision making for when and where the rail should be replaced is important. Higher rail (larger radius) and low rail (smaller radius) have different degradation behaviours (Patra et al. 2009), thus usually only the most needed rail is replaced. Rail replacement is performed using welds to connect the new rail with the old one. After replacement, the rail surface defects will totally disappear by the installation of new rail whereas development of new squats will depend on various factors, like track conditions, MGT, and other different factors. In the case of the welds, because they are composed by materials with different properties than the rails, they are prone to squat defect appearance (Lewis and Olofsson 2009).

Figure 7.a and 7.b show squat growth before and after rail replacement. Figure 7.a shows the squat growth between welds where all the squats will disappear after replacement. The model assumes that no squats will appear during a long horizon by considering that new developed squats can be detected in the next measurement campaign. Figure 7.b shows squat growth on the welds a period after replacement. The exact time instant when the growth starts is related to quality of the weld. This means that for those welds that have good quality, the starting point would be much later.

In the case of between welds, the squat length after replacement is equivalent to zero during a time horizon N_1 . The growth model on the weld can be expressed according to the time N_2 , when squat can appear. Before time $k + N_2$ no squat is present in the weld, while at $k + N_2 + 1$ the squat will start to appear and evolved based on the proposed growth scenarios.

$$\hat{L}_i^h(x_{w_1}, k+t) = 0 \quad t = 1, 2, \dots, N_1, h = h_1, h_2, h_3 \quad (11)$$

$$\hat{L}_i^h(x_{w_2}, k+t) = 0 \quad t = 1, 2, \dots, N_2, h = h_1, h_2, h_3$$

$$\hat{L}_i^h(x_{w_2}, k+N_2+1) = \begin{cases} f_i^{TS}(\Delta L_i) & \text{if } h = h_1 \\ f_i^{TS}(\Delta L_i) & \text{if } h = h_2 \\ \bar{f}_i^{TS}(\Delta L_i) & \text{if } h = h_3 \end{cases} \quad (12)$$

where x_{w_1} is some position between the welds, x_{w_2} is the location of the weld, and ΔL_i is small value that triggers the growth when the squat i starts evolving at the thermite weld at time instant $k + N_2 + 1$. After the squat appears, the interval fuzzy model will capture its evolution over time.

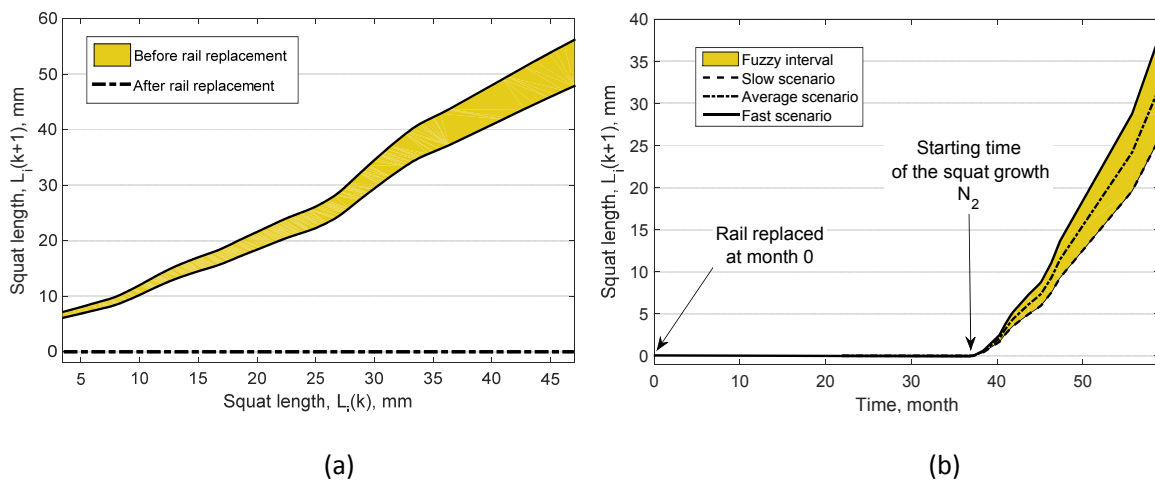


Figure 7: (a) After rail replacement with a piece of new rail free of damage, the length of squats $L_i(k+1)$ will become zero no matter their initial length $L_i(k)$; (b) on welds after rail replacement a squat is prone to appear.

KPIs FOR RAIL HEALTH CONDITION

KPI DESCRIPTION

The monitoring of the evolution of a single squat might not be practical from the maintenance perspective. Aggregated information over bigger track partitions can facilitate infrastructure manager decision over the maintenance plans. In the case of squats, we propose key performance indicators (KPI's) considering the number of A , B and C squats and the number of squats with potential risk of rail break called RC squats, at different time t and different growth scenario h . Moreover, as significant number of B and C squats near to each other indicate a high potential risk to track safety, a KPI is proposed relying on a measure of density of squats B and C . Let's assume the function $\delta_{h,j}^d(x,k)$ is provided by the ABA detection algorithm, for the current instant of measurement k . The function equals to 1 if a squat type $d \in \{A, B, C, RC\}$ is located at position x , instant k , partition j and growth scenario h and equals to zero otherwise. Used as initial condition, and relying on the interval fuzzy model, it is possible to predict $\delta_{h,j}^d(x,t)$ for any time horizon, $t=1, \dots, N_p$. The growth of new squats during the prediction horizon is not considered in this work, because we assume that new squats will be detected in the next measurement campaign at instant $k+1$, where the models can be updated according to the new conditions. The KPIs of squat numbers at partition j , instant t , scenario h , can be expressed as:

$$\begin{aligned} y_{h,j}^A(t) &= \sum_{x \in [x_j, x_{j+1})} \delta_{h,j}^A(x,t) \\ y_{h,j}^B(t) &= \sum_{x \in [x_j, x_{j+1})} \delta_{h,j}^B(x,t) \\ y_{h,j}^C(t) &= \sum_{x \in [x_j, x_{j+1})} \delta_{h,j}^C(x,t) \\ y_{h,j}^{RC}(t) &= \sum_{x \in [x_j, x_{j+1})} \delta_{h,j}^{RC}(x,t) \end{aligned} \tag{13}$$

Also, to estimate density of B and C squats $d_{h,j}^{BC}(x,t)$, a window is defined around the coordinate x (in this paper, the window is 50 m in track length). The function $d_h^{BC}(x,t)$ equals the number of squats B or C in the moving window $[x - 0.025, x + 0.025]$. The KPI density for partition j , instant t , and scenario h can be defined as the area of the density function as follows:

$$y_{h,j}^{dBC}(t) = \frac{\sum_{x \in [x_j, x_{j+1}]} d_h^{BC}(x,t)}{x_{j+1} - x_j} \quad (14)$$

Let's define a vector containing all the KPIs called $y_{h,j}(t)$ for partition j , instant t , and scenario h :

$$y_{h,j}(t) = [y_{h,j}^A(t), y_{h,j}^B(t), y_{h,j}^C(t), y_{h,j}^{RC}(t), y_{h,j}^{dBC}(t)]^T \quad (15)$$

where $y_{h,j}^A(t)$, $y_{h,j}^B(t)$, $y_{h,j}^C(t)$, $y_{h,j}^{RC}(t)$ and $y_{h,j}^{dBC}(t)$ are the number of A squats, B squats, C squats, RC squat and the density of B squats C squats, respectively. Due to the large number of KPI's obtained in terms of all the growth scenarios and predictions over time, we propose two simple steps to include the effect of the trajectories of the KPIs into one global KPI:

Step 1: First, transform the vector $y_{h,j}(t)$ for each partition j , scenario h and instant t , into a single

KPI using a fuzzy expert system $y_{h,j}^M(t) = f_{\text{Mamdani}}(y_{h,j}^A(t), y_{h,j}^B(t), y_{h,j}^C(t), y_{h,j}^{RC}(t), y_{h,j}^{dBC}(t))$.

Step 2: Then, aggregate the single KPI over the set of scenarios and over the prediction horizon, for each partition j . This results into a single global KPI for the current instant k , $J_j^{\text{Rail}}(k)$:

$$J_j^{\text{Rail}}(k) = f_{\text{aggregate}}(y_{h_1,j}^M(k), \dots, y_{h_1,j}^M(k + N_P), \dots, y_{h_H,j}^M(k), \dots, y_{h_H,j}^M(k + N_P)) \quad (16)$$

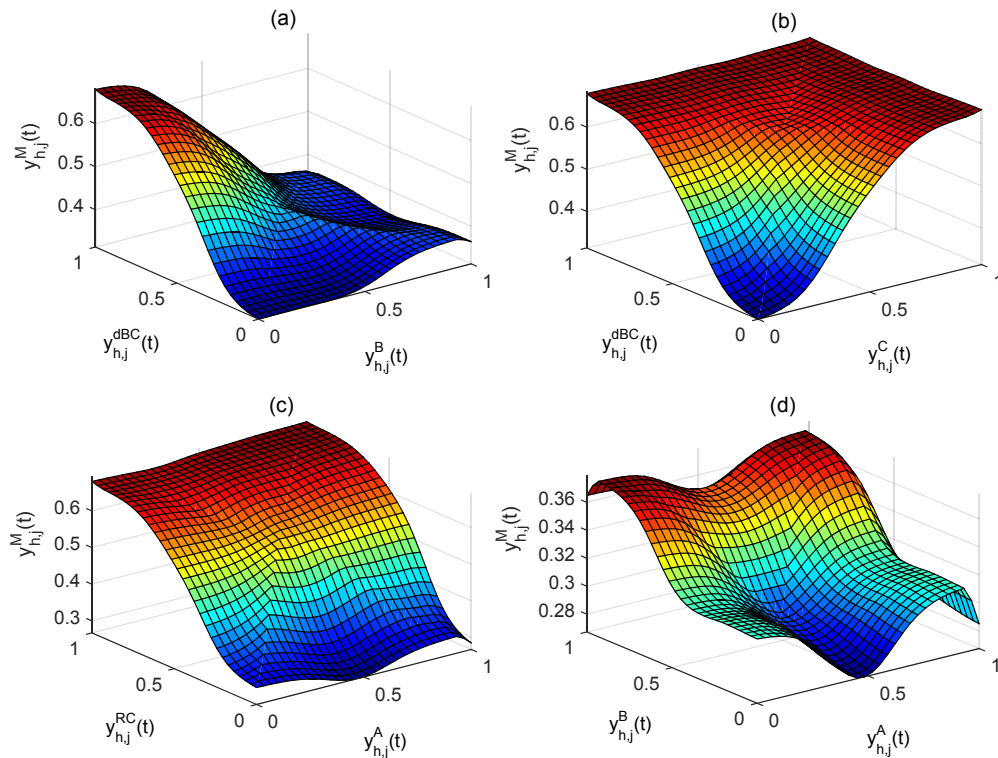
Mamdani fuzzy KPI

For Step 1, a Mamdani fuzzy expert system is used to calculate a single KPI (Mamdani and Assilian 1975). Even though the Mamdani fuzzy system approach was proposed more than 40 years ago, it is still popular because of its simplicity and interpretability (Camastra et al. 2015; Rezaei et al. 2015; Ozgur 2013). In this case, 32 fuzzy if-then rules are generated. The aim is to assign membership degree to each KPI to represent the contribution of each KPI in the rail health condition:

$$\text{If } y_{h,j}^A(t) \text{ is } A_1^r \text{ and } y_{h,j}^B(t) \text{ is } A_2^r \text{ and } y_{h,j}^C(t) \text{ is } A_3^r \text{ and } y_{h,j}^{RC}(t) \text{ is } A_4^r \text{ and } y_{h,j}^{dBC}(t) \text{ is } A_5^r \\ \text{then } y_{h,j}^M(t) \text{ is } G^r$$

where A_1^r , A_2^r , A_3^r , A_4^r , A_5^r and G^r are the membership functions for rule r and $y_{h,j}^M(t)$ is the output Mamdani KPI. The KPIs are first normalized, then Gaussian membership functions are used to fuzzify the KPIs. Also, to defuzzify, centre of gravity method is applied in order to obtain crisp value at the end. Furthermore, relying on the fuzzy rules, interdependency of KPIs and Mamdani KPI are captured as shown in Figure 8. In this figure, it is presented how Mamdani KPI models the influence in the health of the track of two KPIs, varying from fully healthy (equals to zero) to completely unhealthy (equals to one), while all the other KPIs are assumed to be fully healthy (equals to zero). Four plots are presented. In Figure 8(a), a higher value for the BC density is much relevant than the contribution of the number of B squat. In Figure 8(b), a high number of C squats makes the most significant impact on the rail health condition. The rail condition will get highly unhealthy with high values of either density of the BC squats or number of C squat. In Figure 8(c), a high number of RC squats will influence much strongly on the health condition than the number of A squats. In the last plot, Figure 8(d), a high number of A squats or B squats will not have strong influence in the short term (the condition moves between the values 0.28 to 0.37). However, the number of B squats effects more negatively the rail health condition than the number of A squats. In Figure 8, appears the intuitive fact that rail condition gets worse with the increasing number of squat from A , B , C to RC .

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Figure 8: Interdependency of KPIs over Mamdani KPI, $y_{h,j}^M(t)$.

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In general, number of A squats will not have significant impact on the current rail health condition. However in the long term, if not ground, A squats will evolve into severe defects. In order to capture this and other dynamic effects, the prediction model is used, and the global KPI is calculated over time and under different scenarios.

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c. FUZZY GLOBAL KPI

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Relying on defined Mandani KPIs $y_{h,j}^M(t)$, a fuzzy global indicator is calculated to give a KPI over growth

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scenarios in partition j :

$$J_j^{Rail}(k) = \frac{\sum_{h \in \{h_1, h_2, h_3\}} \sum_{t=k}^{k+N_p} w_h \cdot w_t \cdot y_{h,j}^M(t)}{\sum_{h \in \{h_1, h_2, h_3\}} \sum_{t=k}^{k+N_p} w_h \cdot w_t} \quad (17)$$

where $J_j^{Rail}(k)$ is fuzzy global indicator, w_h is growth weight per scenario and w_t is a weight exponentially showing time effect on the KPIs. In this way, we aggregate different KPIs into a single one, that captures together stochasticities and evolution over time.

NUMERICAL RESULTS

a. FUZZY CONFIDENCE INTERVAL

This section summarizes the simulation results to predict the squats length. A data set of squat lengths collected from different track visits are used to evaluate performance of squat growth model. Identification data and validation data for the interval fuzzy TS model are selected randomly, using 60% of the data for identification and 40% for validation (see Figure 9).

To optimize number of clusters, models from two to ten clusters are tested. For each number of cluster, the root mean square (RMS) of the prediction error is used to determine the best model. During the training, tuning parameters of the confidence interval fuzzy model are considered the same for the lower and upper fuzzy bounds. The idea is to obtain optimum parameter α , that results into a minimum number of data points outside the band whereas the band is as narrow as possible. Figure 10(a) depicts the Pareto front of the normalized area of the band versus the normalized number of data points outside the band ranging α from 0 to 40. Figure 10(b) shows how α behaves in terms of area of the band. As shown in the Figure 10(b), the area will reach maximum value if α equals to 32.

In reality, the variance of the worst case scenario is much larger than the best case scenario; thus the assumption of a fixed α must be relaxed. Using full trajectories of different squats, ad-hoc α^{h_1} and α^{h_3}

were obtained to better fit the dynamics. The use of interval fuzzy model for prediction is presented in Figure 12, with a selected $\alpha=1.5$ from the Pareto front, and modified parameters $\alpha^{h_1} = 0.32 \cdot \alpha$, and $\alpha^{h_3} = 1.7 \cdot \alpha$. The squat length starts from a small defect in 8 mm to a severe squat in 60 mm. An important characteristic is when the predictive model reaches the highest bound 60 mm. This happens for squats of 48 mm for the one-step ahead prediction (within 6 months), and it will happen for squats of 18 mm in the case of four-step ahead prediction (within 24 months). For testing purposes, we have evaluated this model with another data set of the trajectories presented in Li et al. (2010). All of them are contained within the interval model.

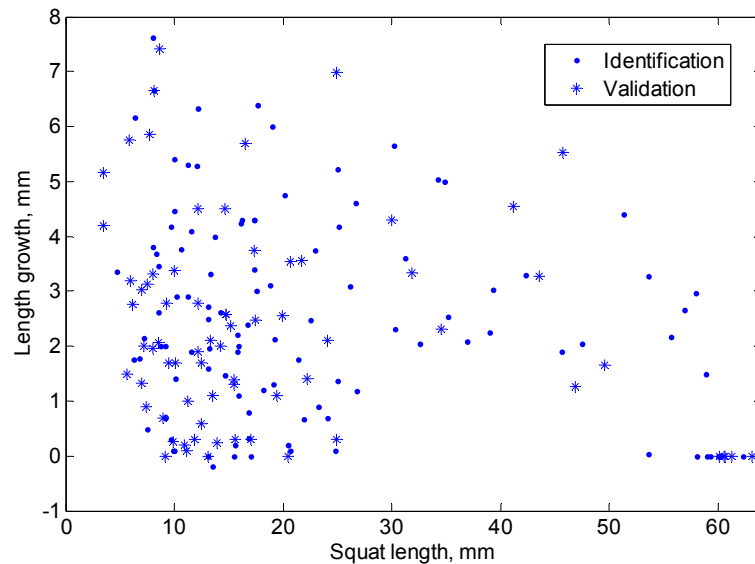


Figure 9: Validation and identification data for the squats length.

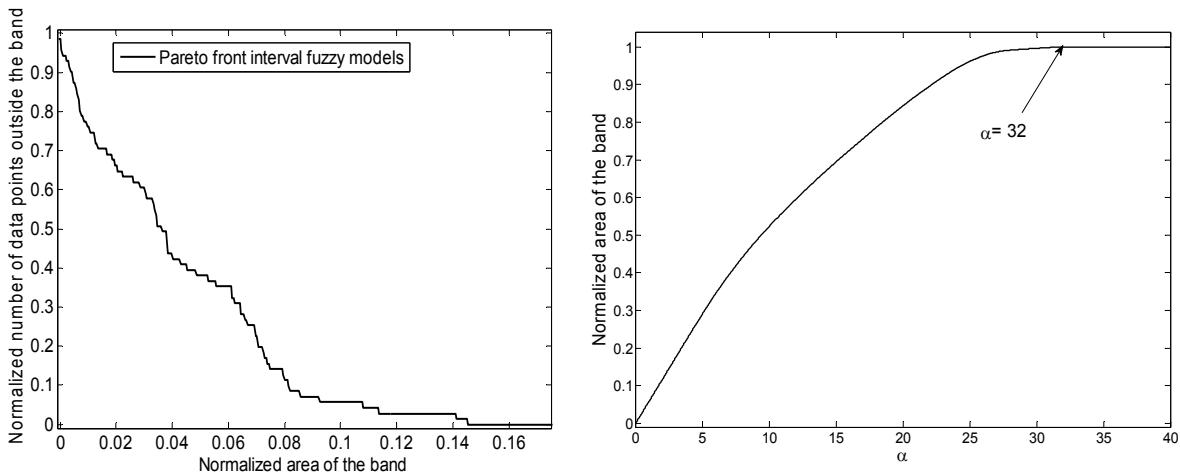


Figure 10: (a) pareto front of number of data point outside v.s area of the band. (b) area of the band over α .

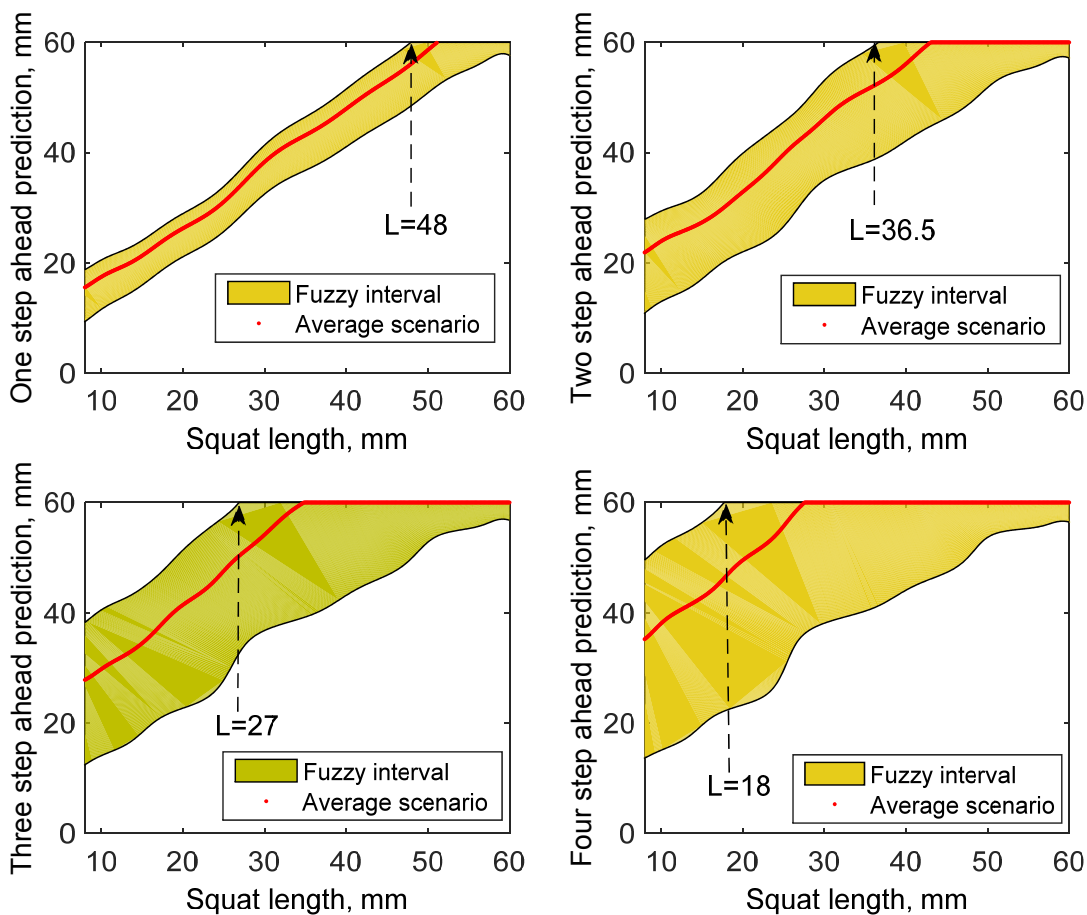


Figure 11: Interval fuzzy model predictions, one, two, three and four steps-ahead.

b. FUZZY GLOBAL KPI FOR TRACK HEALTH CONDITION

The full track of the Meppel-Leeuwarden is used to show the proposed methodology. The Figure 12 shows a simple map of the track and the four partitions j_1, j_2, j_3 and j_4 . The partitions can be adapted according to the maintenance plans or other design considerations. The partitions in this paper, are all around 10 kilometres long, except the last one which is 15 kilometres long. Meppel is in kilometre at 105, Leeuwarden is at 150, the partitions are defined between the kilometres: $x_{j_1} = 105$, $x_{j_2} = 115$, $x_{j_3} = 125$, $x_{j_4} = 135$ and $x_{j_5} = 150$.

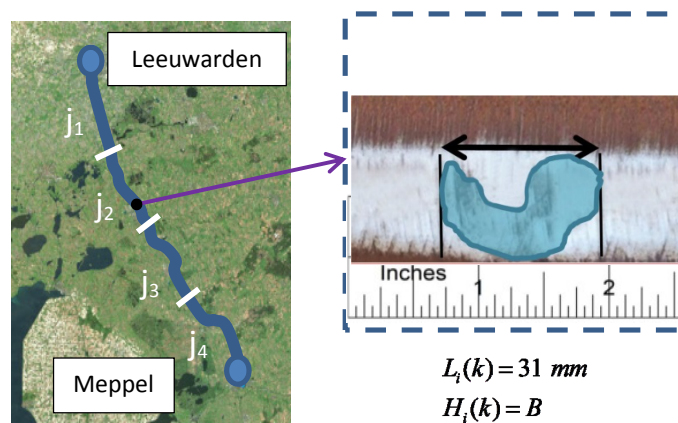


Figure 12: Schematic track map between two stations, Meppel and Groningen, divided into four partitions, j_1, j_2, j_3 , and j_4

Figure 13 shows the different KPIs squats number over four step-ahead prediction when no maintenance is performed. All the cases are calculated for the scenarios slow (in blue), average (in yellow) and fast (in red). In Figure 13(a), the number of A squat tends to get reduced over time, as they are becoming B squats. In Figure 13(b), the number of B squat increases because of the A squats becoming B squats, but after $t=12$, the number of B squat decreases as most of them are becoming C squat. When no corrective maintenance is

performed, it can be seen from Figure 13(c) that after $t=12$, huge number of C squats are in the track (worst case scenario), which is a very expensive situation as the only solution will be to replace the rails. In Figure 13(d), it is possible to see the moment when operational risk locations start to appear, indicating that maintenance should be done before the worst case scenario indicates their appearance.

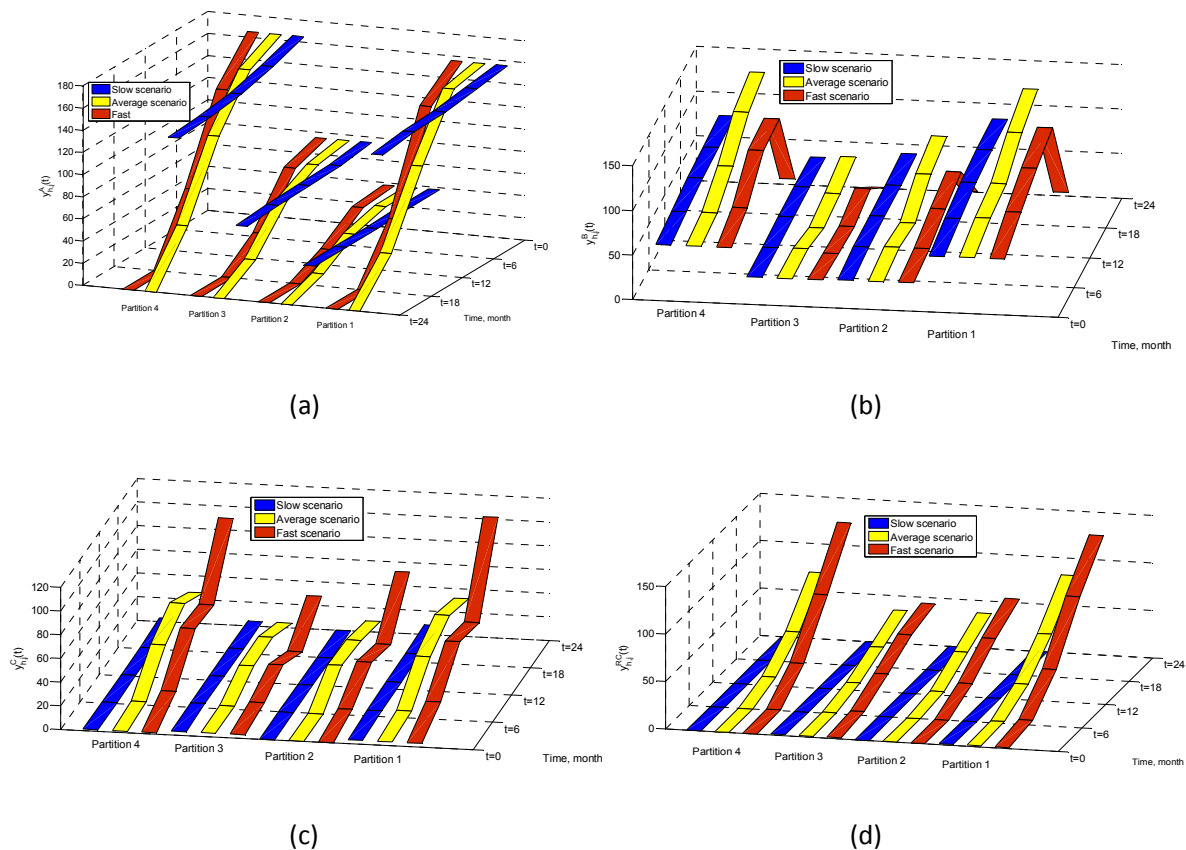


Figure 13: Squat number KPIs for the slow, average and fast growth scenarios in the absence of maintenance operation, (a) number of A squat, (b) number of B squat, (c) number of C squat and (d) number of RC squats.

Figure 14a shows how potential risk squats will start to appear over time. Figure 14b shows the KPI related to density of B and C squats. As seen in Figure 14a, the first squats with high potential risk of derailment, RC squats, appear for the worst case scenario at $t=12$, in four kilometre positions $\{130.9, 132.0, 132.5, 133.0\}$.

Three of those four locations were already detected at $t=0$ in Figure 14b, while all of them are already present in the B-C squat density signal at $t=6$ for all the scenarios. It means that within the first 12 month, the infrastructure manager is expected to take actions, to prevent risk of derailment.

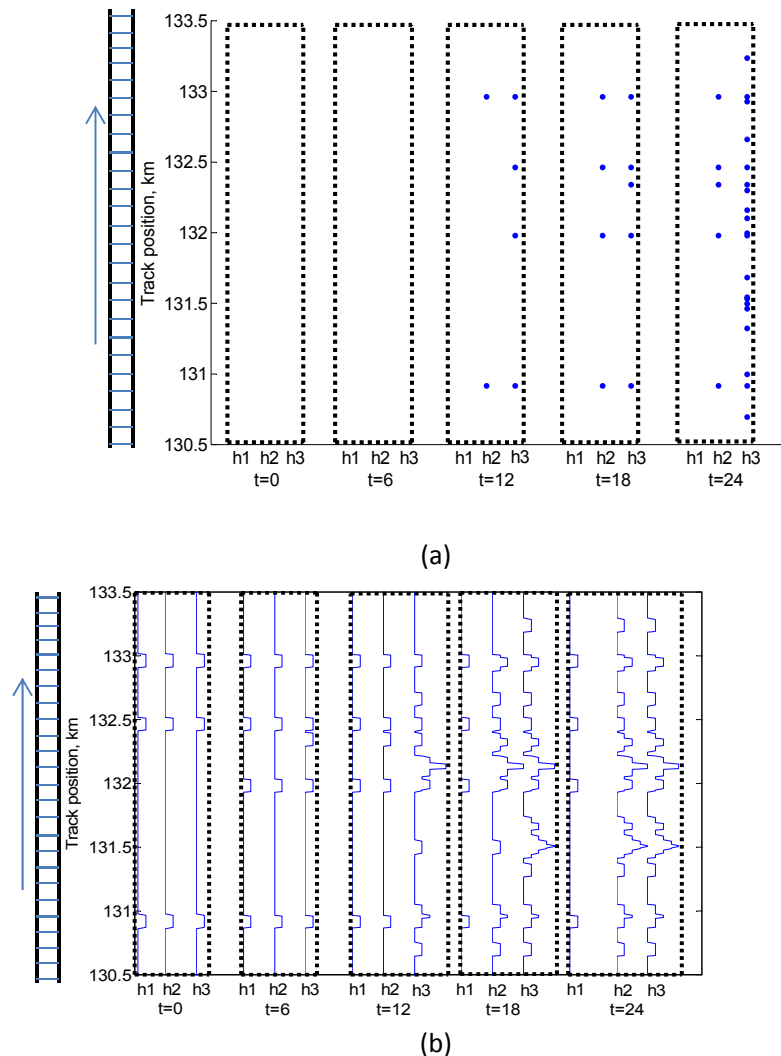


Figure 14: For track position between 130.5 and 133.5km, predictions over 24 months and three scenarios for: (a) Potential risk locations, (b) B-C squats density.

The Figure 15 collects all the scenarios and the signals over the whole prediction horizon, to indicate a single global fuzzy KPI for each track partition. Three cases are considered, no maintenance, grinding at $t=0$, and local rail replacement at $t=0$ for each severe squat. Maintenance considerably can improve the rail health

condition, but to be fully efficient a combination of both grinding and replacement is necessary. After the maintenance operations, the condition is in the average condition range, where the potential risk of derailment is considerably lower during the prediction horizon. The following result allows the infrastructure manager to decide how to manage the rail in the future at each track partition. As in the case of the absence of maintenance operation, a cost of zero Euro with the clear consequence of the bad rail health condition. In the case of the grinding effect and the replacement effect, the results can be applied as an effective factor for cost analysis of the track maintenance plan.

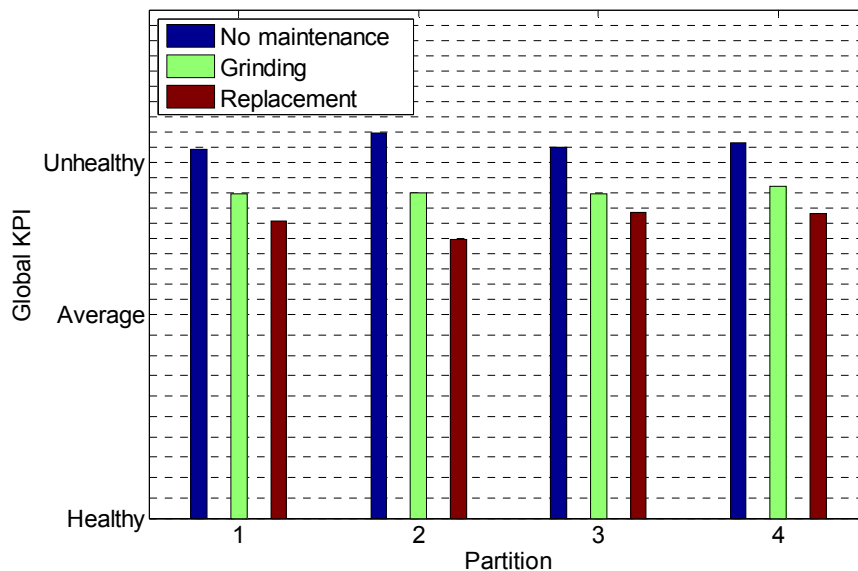


Figure 15: Fuzzy global KPIs

CONCLUSION AND FUTURE RESEARCH

In this paper a condition-based monitoring methodology is developed for a type of surface defect in the rail called "squats". This methodology is employed to construct an interval-based TS fuzzy prediction modelling in order to monitor the track condition over maintenance time horizon per track partition.

The idea of using fuzzy interval is to capture all the possible growth scenarios. Based on the interval fuzzy models for squats, a condition-based methodology for railway tracks is proposed using different KPIs defined

in a track-partition level, allowing the grouping of defects located in a given track partition. In the methodology, number and density of squats are considered over a prediction horizon under three different scenarios, slow, average and fast growth. Then, to facilitate visualization of the rail health condition and to ease the maintenance decision process, we propose a fuzzy global KPI based on fuzzy rules for each partition, that combine the different KPIs over prediction horizon and scenarios. Hence, the proposed methodology adds value by defining fuzzy global KPIs which are predictable over time to facilitate maintenance decision making of the rail. As an example, the KPIs obtained are presented for the track Meppel-Leeuwarden. As a further research, the study will be oriented into an optimization-based methodology to reduce life cycle costs effectively and to fit the methodology much closely to the real-life maintenance operations. The use of new predictive and robust KPIs defined for different parties will be considered, including infrastructure manager, rolling stock manager, contractors and users.

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