

Beam Experiments on Acceptance Criteria for Bridge Load Tests

Lantsoght, Eva; Yang, Yuguang; van der Veen, Cor; de Boer, A.; Hordijk, Dick

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1 Environment, Utrecht, The Netherlands. He received his MSc and PhD from Delft University of
2 Technology. He is a member of some National Committees, *fib* Special Activity Group 5 and
3 member of an IABSE Working Committee. His research interests are remaining lifetime, existing
4 structures, computational mechanics, traffic loads and composites.

5 **Dick A. Hordijk** is a full professor at Delft University of Technology, Delft, the Netherlands. He
6 received his MS and PhD in civil engineering from Delft University of Technology, Delft, the
7 Netherlands, in 1985 and 1990, respectively. His research interests include concrete fracture
8 mechanics, assessment of existing structures, structural application of new concrete types and
9 forensic engineering.

11 ABSTRACT

12 Loading protocols and acceptance criteria are available in the literature for load tests on buildings.
13 For bridges, proof load tests are interesting when crucial information about the structure is missing,
14 or when the uncertainties about the structural response are large. The acceptance criteria can then be
15 applied to evaluate if further loading is acceptable, or could lead to permanent damage to the
16 structure. To develop loading protocols and acceptance criteria for proof loading of reinforced
17 concrete bridges, beam experiments were analysed. In these experiments, different loading speeds,
18 constant load level times, numbers of loading cycles, and required number of load levels were
19 evaluated. The result of these experiments is the development of a standard loading protocol for the
20 proof loading of reinforced concrete bridges. Based on these limited test results, recommendations
21 for acceptance criteria are also proposed.

22 **Keywords:** acceptance criteria; beam test; bending; load test; loading protocol; proof loading;
23 reinforced concrete slab; shear; slab bridge.

24

INTRODUCTION

1
2 In the Netherlands, a large number of reinforced concrete bridges that were built in the decades
3 following the second World War are reaching the end of their originally devised service life
4 (Lantsoght et al., 2013). These bridges were designed for lower live loads than the currently
5 governing live loads (CEN, 2003) and were designed according to codes that allowed higher shear
6 capacities than according to the current provisions from Eurocode 2 (CEN, 2005). The result is that
7 the shear capacity of 600 reinforced concrete slab bridges is subject to discussion in the Netherlands.
8 To systematically rate these bridges, an assessment procedure following different Levels of
9 Approximation is developed (Lantsoght et al., (in press)), called Levels of Assessment (LoA), based
10 on slab shear experiments . Lower Levels of Assessment are less time-consuming, but give a more
11 conservative assessment. If a bridge rates too low at LoA I, the calculation can be refined with the
12 next LoA. Proof loading is used as the last resource, LoA IV. In a proof load test, a load is applied
13 that results in the same sectional shear as the live load model. If the bridge can carry the applied
14 proof load without showing signs of irreversible damage, it is experimentally demonstrated that the
15 bridge is suitable for carrying the loads prescribed in the code. This paper deals with the
16 development of a loading protocol and acceptance criteria for reinforced concrete bridges that need
17 to be verified in shear and in bending moment. The acceptance criteria are used during the test to
18 evaluate if further loading is allowed. This approach deviates from load testing of buildings, where
19 the measurement results are evaluated after the test to see if the structural behavior is acceptable. If
20 the acceptance criteria are exceeded, there is a chance that further increasing of the load will result
21 in irreversible damage in the bridge.

RESEARCH SIGNIFICANCE

22
23 The novelty of the presented work is that acceptance criteria and a loading protocol are developed
24 that are suitable for reinforced concrete bridges subjected to a proof load test. The development of
25 the acceptance criteria is based on carefully executed experiments on reinforced concrete beams

1 without shear reinforcement. For the first time, a distinction between acceptance criteria for bending
2 moment and shear is made.

3 **LOAD TESTING AND ACCEPTANCE CRITERIA**

4 **Load testing**

5 Two types of load tests can be distinguished: diagnostic load tests and proof load tests. The goal of
6 diagnostic load tests (Fu et al., 1997; Olaszek et al., 2014; Russo et al., 2000; Sanayei et al., 2016)
7 is to improve analytical models of a structure based on measurements taken during a load test. A
8 diagnostic load test is carried out at relatively low load levels. A proof load test (Aguilar et al.,
9 2015; Casas and Gómez, 2013; Faber et al., 2000; Saraf et al., 1996) uses load levels that
10 correspond to the factored live loads, and is used to directly evaluate a structure.

11 A number of codes and guidelines exist for load testing of structures. ACI 437.2M-13 (ACI
12 Committee 437, 2013) and the German guidelines (Deutscher Ausschuss für Stahlbeton, 2000) deal
13 with load testing of existing buildings. The Irish (NRA, 2014), British (The Institution of Civil
14 Engineers - National Steering Committee for the Load Testing of Bridges, 1998) and French
15 (Cochet et al., 2004) guidelines describe diagnostic load tests on bridges. An NCHRP (NCHRP,
16 1998) report describes both diagnostic and proof load tests on bridges, but does not determine a
17 loading protocol, required load, and acceptance criteria for proof load tests.

18 In the Netherlands, a number of proof load tests have been carried out over the last decade in
19 order to establish guidelines for the proof load testing of reinforced concrete bridges. In particular,
20 bridges with ASR-damage were studied, such as the viaduct Heidijk (Dieteren and den Uijl, 2009),
21 the viaduct Vlijmen-Oost (Koekkoek et al., 2015b) and the viaduct Zijlweg (Koekkoek et al.,
22 2015a). Additionally, a posted bridge, the viaduct De Beek (Koekkoek et al., 2016), a bridge that
23 rated insufficiently for bending moment, the Halvemaans Bridge (Fennis and Hordijk, 2014), and a
24 bridge with corrosion damage the viaduct Medemblik (Kapphahn, 2009), were proof load tested.
25 The Ruytenschildt Bridge (Lantsoght et al., 2016a) was tested to failure.

1 **Acceptance criteria from ACI 437.2M-13**

2 ACI 437.2M-13 (ACI Committee 437, 2013) prescribes procedures and acceptance criteria for load
3 testing of concrete structures (prestressed and reinforced concrete, with a maximum concrete
4 compressive strength of 55 MPa = 8000 psi). The code describes a monotonic (Fig. 1a) and cyclic
5 loading protocol (Fig. 1b). In the monotonic loading protocol, each load step should be held for at
6 least 2 minutes, and the full test load should be applied for 24 hours. At least 24 hours after
7 removing the load, a final set of response measurements should be taken. For the cyclic loading
8 protocol, three load levels should be studied, with two cycles per load level (Casadei et al., 2005;
9 De Luca et al., 2014; Galati et al., 2008; Ziehl et al., 2008). The first two cycles study the
10 serviceability conditions, and the last two cycles study the full test load.

11 The first acceptance criterion is that the structure should show no evidence of failure. When
12 deflections exceed precalculated deflections, when cracking is observed, or when cracks indicating
13 anchorage problems appear, the licensed design professional should decide if the test can be
14 continued. At signs indicating that shear failure is imminent, the structure is considered as having
15 failed the load test. For monotonic loading, the measured deflection after the test (i.e. the residual
16 deflection) is limited to:

$$17 \quad \Delta_r \leq \frac{\Delta_l}{4} \quad (1)$$

$$18 \quad \Delta_l \leq \frac{l_t}{180} \quad (2)$$

19 For a cyclic loading protocol, the first acceptance criterion is the deviation from linearity index, I_{DL} ,
20 with the angles as shown in Fig. 2a:

$$21 \quad I_{DL} = 1 - \frac{\tan(\alpha_i)}{\tan(\alpha_{ref})} \leq 0.25 \quad (3)$$

22 The second acceptance criterion, see Fig. 2b, the permanency ratio I_{pr} , is defined as:

$$I_{pr} = \frac{I_{p(i+1)}}{I_{pi}} \leq 0.5 \quad (4)$$

where I_{pi} and $I_{p(i+1)}$ are the permanency indexes calculated for the i -th and $(i+1)$ -th load cycles:

$$I_{pi} = \frac{\Delta_r^i}{\Delta_{\max}^i} \quad (5)$$

$$I_{p(i+1)} = \frac{\Delta_r^{(i+1)}}{\Delta_{\max}^{(i+1)}} \quad (6)$$

The third acceptance criterion requires that the residual deflection, Δ_r , measured at least 24 hours after removal of the load, fulfils Eq. (1).

Acceptance criteria from the German guidelines

The German guideline for load testing (Deutscher Ausschuss für Stahlbeton, 2000), originally developed for concrete buildings, is suitable for plain and reinforced concrete. Testing of shear-critical structures or structures that could exhibit a brittle failure mode is not allowed. A cyclic loading protocol of three load levels with at least one cycle per level is prescribed. Five acceptance criteria are defined in the German guideline. The first criterion is a limiting concrete strain:

$$\varepsilon_c < \varepsilon_{c,lim} - \varepsilon_{c0} \quad (7)$$

The measured strain ε_c should be smaller than the limiting strain $\varepsilon_{c,lim}$ (0.6 ‰, or 0.8 ‰ if the compressive strength is larger than 25 MPa = 3626 psi) minus the strain ε_{c0} due to the permanent loads. In practice, ε_{c0} is taken from the linear finite element model that is used to prepare for a proof load test, and thus uses the assumption of linear elastic material behavior. The second criterion is a limiting strain in the steel:

$$\varepsilon_{s2} < 0.7 \frac{f_{ym}}{E_s} - \varepsilon_{s02} \quad (8)$$

This criterion becomes the following when the stress-strain relation of the steel is fully known:

$$\varepsilon_{s2} < 0.9 \frac{f_{0.01m}}{E_s} - \varepsilon_{s02} \quad (9)$$

1 The third criterion is based on the crack width w and the increase in crack width, Δw , as given in
2 Table 1. The fourth acceptance criterion is that no non-linear behavior can occur, typically
3 evaluated on the load-deflection graph, or if more than 10% permanent deformation is found after
4 removing the load. The fifth criterion limits the strains in the shear span of beams without shear
5 reinforcement to 60% of the strains from Eq. (7) for the strain in the concrete compressive strut and
6 to 50% of the strains from Eqs. (8) or (9) for the strain in the shear reinforcement. A test also needs
7 to be stopped when the measurements indicate critical changes in the structure, when the stability of
8 the structure is endangered, and when critical displacements occur at the supports.

9 **EXPERIMENTS**

10 **Test setup and instrumentation**

11 Two beams are tested specifically to study the acceptance criteria, and two additional experiments
12 from earlier testing at Delft University of Technology (Yang et al., 2016) were added to complete
13 the analysis. The beams are simply supported and subjected to a single concentrated load at a
14 distance a from the support. A sketch of the test setup is shown in Fig. 3a for beam P804 and in Fig.
15 3b for beam P502. The width of the support and loading plates was 100 mm (4 in.).

16 The instrumentation on the beam consists of LVDTs, laser distance finders and acoustic
17 emission sensors, see Fig. 3c. An overview of the functions of all applied sensors is given in Table
18 2.

19 **Specimens and materials**

20 The cross section of beam P804 is 800 mm \times 300 mm (31.5 in \times 11.8 in) and of beam P502 the
21 cross section is 500 mm \times 300 mm (19.7 in \times 11.8 in). Glacial river aggregates with a maximum
22 diameter of 16 mm (0.63 in) are used. The density of the concrete is 2429.6 kg/m³ (152 lb/ft³),
23 which gives a load of 23.8 kN/m³ (0.152 kip/ft³). The measured values of the concrete compressive
24 strength at 28 days is given in Table 3.

25 In P804, 6 plain reinforcement bars of soft steel with $\phi = 20$ mm (0.78 in) are used. In P502,

1 3 plain reinforcement bars with $\phi = 20$ mm (0.78 in) are used. This reinforcement is similar to the
2 reinforcement (plain bars, relatively low yield strength) that can be found in existing reinforced
3 concrete bridges. The measured yield strength of the steel is $f_{ym} = 296.8$ MPa (43047 psi) and the
4 measured tensile strength of the steel is $f_{um} = 425.9$ MPa (61771 psi).

5 In Table 3, the predicted maximum load to cause a bending moment failure is given as
6 P_{moment} and the predicted maximum load to cause a shear failure is given as P_{shear} . The
7 determination of the maximum loads takes the selfweight of the beam into account, and uses the full
8 static scheme of the test setup. For P_{shear} , the expression from NEN-EN 1992-1-1:2005 was used
9 (CEN, 2005), with $C_{Rd,c}/\gamma_c = 0.15$ for average values (König and Fischer, 1995). The expected
10 maximum load (the minimum of P_{moment} and P_{shear}) is then highlighted in grey in Table 3.

11 **Loading procedure**

12 The loading protocol for experiments P804A1 and P804A2 was determined to study acceptance
13 criteria and come up with recommendations for bridges. P804B and P502A2 are analyzed for
14 acceptance criteria, but were testing using a faster loading protocol.

15 First, the typical ratio of the applied proof load to the maximum load to cause failure has to
16 be estimated, to know which load levels in the beam tests will correspond to the loads in the field.
17 The results of viaduct Zijlweg are analyzed for this purpose (Koekkoek et al., 2015a). The failure
18 load is estimated with the Extended Strip Model, which leads to good predictions for the capacity of
19 reinforced concrete slab bridges (Lantsoght et al., 2016c). This analysis showed that the load level
20 that corresponds to the proof load is 46% of the estimated failure load (Lantsoght et al., 2016b). As
21 the depth of the field tests and the beams tested in the laboratory is similar, no influence of the size
22 effect is expected.

23 According to ACI 437.2M-13 (ACI Committee 437, 2013), at least 3 load levels should be
24 used. Instead of using two load cycles per load step, as shown in Fig. 1, 1 + 3 cycles are carried
25 out: in the first cycle, small steps are used to go to the load level, and then three cycles are carried

1 out without intermediate steps. In the first cycle, steps of 2 kN (0.45 kip) are used, and then the
2 measurements are checked to verify if no indication of nonlinearity or onset of damage can be
3 observed. After every cycle of the three regular cycles, the measurements are also checked for
4 nonlinearity or indications of the onset of damage. A baseline load level higher than 0 kN is used, to
5 make sure all measurements remain activated.

6 In P804A1, the influence of the loading speed is studied. At a low load level, four different
7 loading speeds were used. The standard loading speed was determined based on the loading speed
8 used for viaduct De Beek (Koekkoek et al., 2016). In the test, the loading speed was constant at 5.4
9 kN/s (1.21 kip/s) for the first test location and 7.3 kN/s (1.64 kip/s) for the second test location. A
10 loading speed of 5 kN/s (1.12 kip/s) is taken as a reference speed for the laboratory tests. Since the
11 loading is displacement-controlled, the applied loading speed used in the laboratory is 0.2 mm/s
12 (0.008 in/s). Additionally, the loading speeds 0.004 mm/s (0.00016 in/s), 0.04 mm/s (0.0016 in/s)
13 and 0.4 mm/s (0.016 in/s) are tested. The full loading protocol, as executed during the test, is shown
14 in Fig. 4a and contains 42 load cycles and 8 load levels.

15 In P804A2, the influence of keeping the load constant was studied. The 1 + 3 cycles loading
16 protocol was used starting at the second load level, but in the first cycle, the maximum load was
17 kept constant for 15 minutes, see Fig. 4b. In total, 17 load cycles and 5 load levels are tested. In
18 P804B (Fig. 4c), no cyclic loading was used; and in P502A2 (Fig. 4d), a cyclic loading protocol
19 with less cycles was used. In P804B, 11 load levels were used; and in P502A2, 8 load steps at 5
20 load levels were used.

21 RESULTS AND DISCUSSION

22 Test results

23 In P804A1, the first cracks developed prior to the first load level of 75 kN (17 kip). At higher load
24 levels, more flexural cracks developed until yielding of the reinforcement caused a flexural failure
25 at 207 kN (47 kip), see Fig. 5a. In P804A2, lengthening of the existing cracks from P804A1

1 occurred. A brittle shear failure occurred at 232 kN (52 kip), see Fig. 5b. P804B was tested on the
2 side of beam P804 that had no existing flexural cracks. A shear failure occurred at 196 kN (44 kip),
3 see Fig. 5c. P502A2 had existing flexural cracks, and failed in flexure at 150 kN (34 kip), see Fig.
4 5d. The load-displacement diagram of all tests is given in Fig. 6. The values of the failure loads P_u
5 and observed failure modes (flexure “F” or shear “S”) are given in Table 3. It can be seen that the
6 failure modes were generally predicted correctly. The four experiments are used to analyze four
7 cases: shear and flexural failures, both for previously cracked and uncracked beams.

8 **Loading speed**

9 In P804A1, the loading speed is varied: loading speeds of 0.004 mm/s (0.00016 in/s), 0.04 mm/s
10 (0.0016 in/s), 0.02 mm/s (0.008 in/s) and 0.4 mm/s (0.016 in/s) are used. First, the effect of the
11 loading speed on the increase in residual deformation is studied. If the time-dependent behavior of
12 concrete plays an important role, it is expected that for slow loading speeds, the increase in residual
13 deformation will be relatively larger. The increase in residual deformations is calculated as:

$$14 \quad res_i = \Delta_{r,0,i} - \Delta_{r,0,(i-1)} \quad (10)$$

15 No relation between res_i and the loading speed could be found. Additionally, the relation between
16 Δ_r and the loading speed is shown in Fig. 7a. The first point in this figure has a higher value,
17 because in the first load cycle, the cracking moment was exceeded in the beam, which influenced
18 the stiffness. The results shown no statistically relevant relation between Δ_r and the loading speed.

19 Next, the relation between the reduction in stiffness (comparing cycles i and $i-1$) and the
20 loading speed is studied. For slower loading speeds, a larger reduction in the stiffness is expected.
21 The stiffness of the unloading branch is analyzed, as it is less influenced by crack formation. It can
22 be concluded, see Fig. 7b, that the effect of the loading speed on the stiffness reduction is irrelevant
23 for the speeds used in field testing. Additionally, the influence of the loading speed on the strain
24 rate and the energy in the cycle was found to be insignificant (Lantsoght et al., 2016b).

1 **Number of loading cycles**

2 The influence of the number of loading cycles in P804A1 was studied at the 75 kN load level (16.9
3 kip) by using 8 loading at a speed of 0.2 mm/s (0.008 in/s) and 3 cycles at the other tested speeds.
4 The results are studied as a function of the energy in the cycle and in the loading branch of the
5 cycle, see Fig. 7c. It can be seen that the results stabilize in the 4th cycle, which supports the
6 proposal for a loading protocol of 1 + 3 cycles for higher load levels, and three cycles for lower
7 load levels.

8 **Constant load**

9 In P804A1 and P804A2, the period of time used for constant loading and between load cycles was
10 evaluated. In P804A1, cycles 30 (30 minutes constant load and rest), 34 and 38 (15 minutes load
11 and rest) have longer constant loading and rest periods. In P804A2, during the first load cycle of
12 each load level the load was applied for 15 minutes, followed by a rest period of 15 minutes, see Fig.
13 4. From the test results of P804A1, it seems that after a longer loading period, the stiffness is larger.
14 In other words, a longer loading period seems to create some recuperation in the beam. In P804A2,
15 the reduction of the stiffness during the experiment was very small, because the beam was fully
16 cracked by P804A1. No effect of the constant loading periods is observed on the energy in the
17 cycles, nor on the residual deformations. When looking at the results of the measured strains, a
18 decrease in strain between the beginning and end of a loading cycle can be observed. However,
19 because the experiment is executed in a displacement-controlled way, this observation is related to
20 the effect that the applied load is reduced when the applied deformation is kept constant.

21 **Analysis of acceptance criteria from the German guidelines**

22 First, the criteria from the German guidelines (Deutscher Ausschuss für Stahlbeton, 2000) are
23 evaluated. The acceptance criterion related to the steel strain, Eqs. (8) and (9), is not evaluated
24 because this criterion requires the removal of the concrete cover, which is not always allowed by
25 the bridge owner. The first evaluated acceptance criterion is related to the concrete strain, Eq. (7),

1 and the results of this analysis are given in Table 4, indicating the load at which the criterion is
2 exceeded, P_{emax} . The loads range from 44% to 62% of the failure load. This acceptance criterion can
3 thus be used in practice.

4 The second evaluated acceptance criterion is related to the crack width, see Table 1, and the
5 results of this analysis are given in Table 4. P804B was not tested in a cyclic way, and in P502A2
6 crack widths were not measured, so that only the results of P804A1 and P804A2 are analyzed.
7 P804A1 is a test on a beam with no existing cracks, so the requirements for new cracks from Table
8 1 can be evaluated. P804A2 has existing cracks, so the requirements for existing cracks from Table
9 1 are governing. During P804A1, the criterion is exceeded at LVDT12 in the second load cycle – a
10 result that would be too conservative for practice: further loading did not yet lead to irreversible
11 damage or failure. However, it must be noted that the absolute values of the measured crack widths
12 are extremely small. Therefore, it is proposed to omit all crack widths smaller than 0.05 mm (0.002
13 in) for the analysis – these results are reported in Table 4. In P804A2, the criterion for the maximum
14 increase in crack width is exceeded at LVDT15 in load step 9. It can thus be concluded that this
15 acceptance criterion can be applied, provided that crack widths smaller than 0.05 mm (0.002 in) are
16 neglected.

17 A last criterion that is evaluated is the residual deflection. The requirement that the residual
18 deflection Δ_r should not be more than 10% of the maximum deflection in a load cycle Δ_{max} is
19 evaluated. Since a baseline load level is used in the experiments, the residual deflection does not
20 correspond to a case with a load of 0 kN (0 kip). Therefore, the stiffness of the unloading branch is
21 used to find the residual deflection that would correspond to a load of 0 kN (0 kip), Δ_r^* , as sketched
22 in Fig. 2b. The results are given in Table 4. In P804A1, the requirement is exceeded in the first load
23 cycle. In P804A2, the requirement is exceeded in the first load cycle if Δ_r is used, and after failure if
24 Δ_r^* is used. In P502A2, unloading to 0 kN (0 kip) was used, so that $\Delta_r = \Delta_r^*$. The results in Table 4
25 indicate that the acceptance criterion based on the residual deflection is not generally applicable.

1 **Analysis of acceptance criteria from ACI 437.2M-13**

2 The deviation from linearity index I_{DL} , see Fig. 2a, is a function of the loading scheme. In P804A1,
3 the deviation from linearity index I_{DL} is exceeded in the 10th load cycle, one of the cycles to 75 kN
4 (16.9 kip). In P804A2, I_{DL} was not exceeded in any load cycle. The deviation from linearity index
5 I_{DL} can only be used with the cyclic loading protocol described in ACI 437.2M-13 (ACI Committee
6 437, 2013), see Fig. 1b, which cannot directly be used for bridges.

7 Similarly, it is found that the permanency ratio I_{PR} as an acceptance criterion can only be
8 used together with the cyclic loading protocol from Fig. 1b, in which fixed values for the minimum
9 and maximum loads need to be used (for example, by applying the loads in a load-controlled
10 manner). If a manually operated system with hydraulic jacks is used in the field, reaching the exact
11 same load over several load cycles becomes difficult. If the value of the residual deformation in the
12 $i+1$ -th cycle is smaller than in the i -th cycle, or if the maximum deformation in the $i+1$ -th cycle is
13 smaller than in the i -th cycle, I_{PR} becomes negative, which disturbs the results.

14 Finally, the criterion for the residual deflections can be evaluated. In ACI 437.2M-13 (ACI
15 Committee 437, 2013), the limit to the residual deflection is 25% of the maximum deflection. These
16 limiting values are given in Table 4 as $\Delta_{lim,ACI}$. In P804A1, this criterion was exceeded in every step,
17 and in P804A2 only in the loading cycle to failure. In P502A2, the criterion is never exceeded.
18 Again, it is concluded that a criterion based on residual deflections is not recommended.

19 **RECOMMENDATIONS FOR BRIDGE APPLICATIONS**

20 **Proposed loading procedure**

21 A cyclic loading protocol is recommended for load testing of bridges. Contrarily to ACI 437.2M-13
22 (ACI Committee 437, 2013), four load levels, and four cycles per load level are recommended. Of
23 these four load cycles, the first cycle will be used to gradually go to the maximum load in the cycle,
24 then keep the load constant until stabilization of the measurements, and then unload to the baseline
25 load level. The baseline load level is necessary to keep all instrumentation activated. Then, three

1 cycles without intermediate steps to the maximum load of that load level are carried out. The four
2 recommended load levels are:

- 3 1. A low load level, to check proper functioning of all sensors;
- 4 2. The serviceability limit state load level;
- 5 3. An intermediate load level;
- 6 4. The maximum load level for which the bridge should be rated through the proof load test.

7 For the low load levels (up to the serviceability limit state level), three load cycles are sufficient,
8 and the first slow load cycle can be omitted. An example of a loading procedure is shown in Fig. 8.

9 Even though the number of tested beams is limited, the number of cycles studied in these
10 experiments is sufficient to support the presented recommendations. As such, further research to
11 define the loading protocol is not urgently needed.

12 **Proposed acceptance criteria**

13 When analyzing the experimental results, the difference between acceptance criteria for shear and
14 flexure, and between previously cracked in bending and uncracked conditions becomes clear. An
15 overview of the recommended acceptance criteria for these resulting four cases is given in Table 5.
16 The concrete strain criterion, Eq. (7) from the German guideline (Deutscher Ausschuss für
17 Stahlbeton, 2000) is recommended. The requirements for w_{max} and w_{res} from Table 1 are simplified
18 and crack widths of smaller than 0.05 mm (0.002 in) are neglected.

19 The deviation from linearity index I_{DL} depends on the loading protocol, see Fig. 2a. A
20 simplification of this acceptance criterion uses the stiffness reduction, based on the stiffness as the
21 tangent in the load-displacement graph. An overview of these results is given in Table 4. For
22 P804A1, the first loading step had a low stiffness as the result of the occurrence of the first crack, so
23 that the second loading cycle is used instead. In P804B, small steps were used to increase the load,
24 which makes it difficult to find the stiffness from the load-displacement diagram. For the case of a
25 test for flexure, with no previous bending cracks, a stiffness reduction of $\leq 25\%$ can be used as an

1 recommended loading protocol for bridge proof load tests was developed. For the acceptance
2 criteria, all load cycles of each test need to be evaluated. Therefore, the proposed acceptance criteria
3 can be considered as a preliminary result, based on exploratory testing, which needs further
4 experimental verification in the future. The proposed acceptance criteria are based on the existing
5 acceptance criteria, but have been adjusted for practical considerations related to bridge proof load
6 testing.

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13 **NOTATION**

14 a = distance between the center of the load and the center of the support
15 a_v = distance between the face of the load and the face of the support
16 d = effective depth
17 $f_{0.01m}$ = average yield strength based on a strain of 0.01% (elastic zone)
18 $f_{c,cyl,m}$ = average cylinder concrete compressive strength
19 f_{ym} = measured yield strength of steel
20 f_{um} = measured tensile strength of steel
21 lim = criterion that is limiting
22 l_t = span length
23 res_i = the increase in the residual deformation between loading cycles $(i-1)$ and i
24 s_{laser} = deflection as measured by the laser distance finders at the position of the load
25 $\tan(\alpha_i)$ = the secant stiffness at any point i on the increasing loading portion of the load-deflection

- 1 envelope
- 2 $\tan(\alpha_{ref})$ = the slope of the reference secant line for the load-deflection envelope
- 3 w = crack width for a new crack
- 4 w_{lim} = limiting crack width, calculated based on w_{max}
- 5 w_{max} = crack width at maximum load of a given load cycle for a new crack, or increase in crack
- 6 width at the maximum load for an existing crack
- 7 w_{res} = residual crack width at unloading of a given load cycle
- 8 $C_{Rd,c}$ = calibration factor from Eurocode shear expression, = 0.18
- 9 E_s = modulus of elasticity of reinforcement steel
- 10 F = flexural failure
- 11 F = measured load
- 12 FM = failure mode
- 13 I_{DL} = deviation from linearity index
- 14 I_{Pi} = permanency index at the i -th load cycle
- 15 $I_{P(i+1)}$ = permanency index at the $(i+1)$ -th load cycle
- 16 I_{PR} = permanency ratio
- 17 Level = percentage of maximum load at which an acceptance criterion is exceeded
- 18 LS = load step
- 19 P = load
- 20 P_{def} = load in experiment at which the deformation profiles change
- 21 P_{EI} = load in experiment at which stiffness criterion is exceeded
- 22 P_{min} = baseline load level
- 23 P_{max} = maximum load in a given load cycle
- 24 P_{moment} = calculated load at which a bending moment failure takes place
- 25 P_{shear} = calculated load at which a shear failure takes place

- 1 P_u = load at failure of the specimen
- 2 P_w = load in experiment at which crack width criterion is exceeded
- 3 P_{emax} = load in experiment at which strain criterion is exceeded
- 4 P_{Δ} = load in experiment at which residual deflection criterion is exceeded
- 5 Red_{EI} = reduction in the stiffness with regard to the first load cycle
- 6 S = shear failure
- 7 γ_c = material factor for concrete, = 1.5
- 8 ε_c = strain measured during proof loading
- 9 $\varepsilon_{c,lim}$ = limit value of the concrete strain : 0.6 ‰, and for \geq B25 this can be increased up to
10 maximum 0.8 ‰
- 11 ε_{c0} = analytically determined short-term strain in the concrete caused by the permanent loads
12 that are acting on the structure before the application of the proof load
- 13 ε_{s2} = steel strain during experiment: directly measured or derived from other measurements
- 14 ε_{s02} = analytically determined strain (assuming cracked conditions) in the reinforcement steel
15 caused by the permanent loads that are acting on the structure before the application of the
16 proof load
- 17 ρ_l = ratio of longitudinal reinforcement
- 18 Δ = deflection
- 19 Δ_t = maximum deflection
- 20 $\Delta_{lim,DAfStB}$ = limit to residual deflection given in the German guideline
- 21 $\Delta_{lim,ACI}$ = limit to residual deflection given in ACI 437.2M-13 (ACI Committee 437, 2013)
- 22 Δ_{max} = maximum deflection of a load cycle
- 23 Δ^1_{max} = maximum deflection during load cycle 1
- 24 Δ^2_{max} = maximum deflection during load cycle 2
- 25 Δ^i_{max} = maximum deflection during load cycle i

- 1 Δ^{i+1}_{max} = maximum deflection during load cycle $i+1$
- 2 Δ_r = residual deflection
- 3 Δ_r^* = residual deflection recalculated at a load of 0 kN (0 kip)
- 4 $\Delta_{r,i}^*$ = residual deflection recalculated at a load of 0 kN (0 kip) in the i th loading cycle
- 5 Δ^1_r = residual deflection after load cycle 1
- 6 Δ^2_r = residual deflection after load cycle 2
- 7 Δ^i_r = residual deflection after load cycle i
- 8 Δ^{i+1}_r = residual deflection after load cycle $i+1$
- 9 Δw = increase in crack width for an existing crack

10 REFERENCES

- 11 ACI Committee 437, 2013, "Code Requirements for Load Testing of Existing Concrete Structures
12 (ACI 437.2M-13) and Commentary ", Farmington Hills, MA, 24 pp.
- 13 Aguilar, C. V., Jáuregui, D. V., Newton, C. M., Weldon, B. D. and Cortez, T. M., 2015, "Load
14 Rating a Prestressed Concrete Double-Tee Beam Bridge without Plans by Proof Testing,"
15 *Transportation Research Board Annual Compendium of Papers*, Washington DC, pp. 19.
- 16 Casadei, P., Parretti, R., Nanni, A. and Heinze, T., 2005, "In Situ Load Testing of Parking Garage
17 Reinforced Concrete Slabs: Comparison between 24 h and Cyclic Load Testing," *Practice*
18 *Periodical on Structural Design and Construction*, V. 10, No. 1, pp. 40-48.
- 19 Casas, J. R. and Gómez, J. D., 2013, "Load Rating of Highway Bridges by Proof-loading," *KSCE*
20 *Journal of Civil Engineering*, V. 17, No. 3, pp. 556-567.
- 21 CEN, 2003, "Eurocode 1: Actions on structures - Part 2: Traffic loads on bridges, NEN-EN 1991-
22 2:2003," Comité Européen de Normalisation, Brussels, Belgium, 168 pp.
- 23 CEN, 2005, "Eurocode 2: Design of Concrete Structures - Part 1-1 General Rules and Rules for
24 Buildings. NEN-EN 1992-1-1:2005," Comité Européen de Normalisation, Brussels, Belgium, 229
25 pp.

1 Cochet, D., Corfdir, P., Delfosse, G., Jaffre, Y., Kretz, T., Lacoste, G., Lefaucheur, D., Khac, V. L.
2 and Prat, M., 2004, "Load tests on highway bridges and pedestrian bridges," Sétra - Service
3 d'Etudes techniques des routes et autoroutes, Bagneux-Cedex, France, 60 pp. (in French)

4 De Luca, A., Zadeh, H. J. and Nanni, A., 2014, "In Situ Load Testing of a One-Way Reinforced
5 Concrete Slab per the ACI 437 Standard," *Journal of Performance of Constructed Facilities*, pp. 1-
6 10.

7 Deutscher Ausschuss für Stahlbeton, 2000, "DAfStb-Guideline: Load tests on concrete structures,"
8 Deutscher Ausschuss für Stahlbeton, 7 pp. (in German)

9 Dieteren, G. G. A. and den Uijl, J. A., 2009, "Evaluation Proof Loading Heidijk," V. 2008-
10 DWARS-MOIO, TNO Bouw en Ondergrond / TU Delft, 70 pp. (in Dutch)

11 Faber, M. H., Val, D. V. and Stewart, M. G., 2000, "Proof load testing for bridge assessment and
12 upgrading," *Engineering Structures*, V. 22, pp. 1677-1689.

13 Fennis, S. A. A. M. and Hordijk, D. A., 2014, "Proof loading Halvemaans Bridge Alkmaar," Stevin
14 Report 25.5-14-05, Delft University of Technology, Delft, The Netherlands, 72 pp. (in Dutch)

15 Fu, G., Pezze III, F. P. and Alampalli, S., 1997, "Diagnostic Load Testing for Bridge Load Rating,"
16 *Transportation Research Record*, V. 1594, pp. 125-133.

17 Galati, N., Nanni, A., Tumialan, J. G. and Ziehl, P. H., 2008, "In-situ evaluation of two concrete
18 slab systems. I: Load determination and loading procedure," *Journal of Performance of Constructed*
19 *Facilities*, V. 22, No. 4, Jul-Aug, pp. 207-216.

20 Kappahn, G., 2009, "Experimental Safety Analysis of Superstructure of Bridge Nr. 12 (14H04) in
21 street N240 in Medemblik," ifem, Markkleeberg, Germany, 70 pp. (in German)

22 Koekkoek, R. T., Lantsoght, E. O. L. and Hordijk, D. A., 2015a, "Proof loading of the ASR-
23 affected viaduct Zijlweg over highway A59," Stevin Report nr. 25.5-15-08, Delft University of
24 Technology, Delft, The Netherlands, 180 pp.

25 Koekkoek, R. T., Yang, Y., Fennis, S. A. A. M. and Hordijk, D. A., 2015b, "Assessment of Viaduct

1 Vlijmen Oost by Proof Loading," Stevin Report 25.5-15-10, 126 pp.

2 Koekkoek, R. T., Lantsoght, E. O. L., Yang, Y. and Hordijk, D. A., 2016, "Analysis report for the
3 assessment of Viaduct De Beek by Proof Loading," Stevin Report 25.5-16-01, Delft University of
4 Technology, Delft, The Netherlands, 125 pp.

5 König, G. and Fischer, J., 1995, "Model Uncertainties concerning Design Equations for the Shear
6 Capacity of Concrete Members without Shear Reinforcement," *CEB Bulletin 224, Model
7 Uncertainties and Concrete Barrier for Environmental Protection*, July, pp. 49-100.

8 Lantsoght, E.O.L, van der Veen, C. and de Boer, A., 2016a, "Shear and moment capacity of the
9 Ruytenschildt bridge," *IABMAS 2016*, pp. 8.

10 Lantsoght, E.O.L., Yang, Y., van der Veen, C. and Bosman, A., 2016b, "Analysis of beam
11 experiments for stop criteria," Stevin Report 25.5-16-06, 135 pp.

12 Lantsoght, E. O. L., van der Veen, C., de Boer, A. and Walraven, J. C., 2013, "Recommendations
13 for the Shear Assessment of Reinforced Concrete Slab Bridges from Experiments " *Structural
14 Engineering International*, V. 23, No. 4, pp. 418-426.

15 Lantsoght, E. O. L., van der Veen, C., de Boer, A. and Alexander, S., 2016c, "Bridging the gap
16 between one-way and two-way shear in slabs," *ACI SP International Punching Symposium*, pp. 20.

17 Lantsoght, E. O. L., De Boer, A. and Van der Veen , C., (in press), "Levels of Approximation for
18 the shear assessment of reinforced concrete slab bridges," *Structural Concrete*, pp. 53.

19 NCHRP, 1998, "Manual for Bridge Rating through Load Testing," V. NCHRP Project 12-28(13)A,
20 Washington, DC, 152 pp.

21 NRA, 2014, "Load Testing for Bridge Assessment," National Roads Authority, Dublin, Ireland, 11
22 pp.

23 Olaszek, P., Lagoda, M. and Ramon Casas, J., 2014, "Diagnostic load testing and assessment of
24 existing bridges: examples of application," *Structure and Infrastructure Engineering*, V. 10, No. 6,
25 Jun 3, pp. 834-842.

1 Russo, F. M., Wipf, T. J. and Klaiber, F. W., 2000, "Diagnostic Load Tests of a Prestressed
2 Concrete Bridge Damaged by Overheight Vehicle Impact," *Transportation Research Record*, V.
3 1696, pp. 103-110.

4 Sanayei, M., Reiff, A. J., Brenner, B. R. and Imbaro, G. R., 2016, "Load Rating of a Fully
5 Instrumented Bridge: Comparison of LRFR Approaches," *Journal of Performance of Constructed
6 Facilities*, V. 2016, No. 30, pp. 2.

7 Saraf, V. K., Nowak, A. S. and Till, R., 1996, "Proof load testing of bridges," *Probabilistic
8 Mechanics*, 526-529 pp.

9 The Institution of Civil Engineers - National Steering Committee for the Load Testing of Bridges,
10 1998, "Guidelines for the Supplementary Load Testing of Bridges," London, UK, 44 pp.

11 Yang, Y., van der Veen, C., Hordijk, D. and De Boer, A., 2016, "The shear capacity of reinforced
12 concrete members with plain bars," *Structural Faults and Repair 2016*, Forde, M., ed. Edinburgh,
13 2016, pp. 9.

14 Ziehl, P. H., Galati, N., Nanni, A. and Tumialan, J. G., 2008, "In-situ evaluation of two concrete
15 slab systems. II: Evaluation criteria and outcomes," *Journal of Performance of Constructed
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11 **Table 1 - Requirements for crack width for newly developing cracks w and increase in crack
12 width Δw for existing cracks.**

	During proof loading	After proof loading
Existing cracks	$\Delta w \leq 0.3 \text{ mm} = 0.01 \text{ in}$	$\leq 0.2 \Delta w$
New cracks	$w \leq 0.5 \text{ mm} = 0.02 \text{ in}$	$\leq 0.3 w$

13

Table 2 – Overview of applied sensors

nr	purpose
LVDT1	horizontal deformation
LVDT2	horizontal deformation
LVDT3	horizontal deformation
LVDT4	horizontal deformation
LVDT5	horizontal deformation
LVDT6	horizontal deformation
LVDT7	horizontal deformation
LVDT8	horizontal deformation
LVDT9	vertical deformation
LVDT10	vertical deformation
LVDT11	vertical deformation
LVDT12	crack width
LVDT13	crack width
LVDT14	strain over 1 m
LVDT15	crack width
LVDT16	crack width

Laser01	deflection at support
Laser02	deflection under load
Laser03	deflection at support
Laser04	deflection under load

1 **Table 3 – Properties of specimens. Conversion: 1 MPa = 0.145 ksi; 1 kN = 0.22 kip; 1 mm =**
2 **0.04 in.**

Test	a (mm)	d (mm)	a/d	a_v/d	ρ_l	$f_{c,cyl,m}$ (MPa)	P_{shear} (kN)	P_{moment} (kN)	P_u (kN)	FM
P804A1	3000	755	3.97	3.84	0.83	63.51	273	199	207	F
P804A2	2500	755	3.31	3.18	0.83	63.51	219	248	232	S
P804B	2500	755	3.31	3.18	0.83	63.51	219	248	196	S
P502A2	1000	465	2.15	1.94	0.68	71.47	150	154	150	F

3 **Table 4 – Evaluation of existing and proposed acceptance criteria. Conversion: 1 kN = 0.22**
4 **kip, 1 mm = 0.04 in.**

Strain criterion from German guideline								
Test	ε_{c0} ($\mu\varepsilon$)	$\varepsilon_{c,lim} - \varepsilon_{c0}$ ($\mu\varepsilon$)	P_{emax} (kN)	Level (%)				
P804A1	36	764	91	44				
P804A2	33	767	120	52				
P804B	33	767	111	57				
P502A2	22	778	93	62				
Crack width criterion from German guideline								
Test	LS	w_{max} (mm)	w_{res} (mm)	w_{lim} (mm)	lim	LVDT	P_w (kN)	Level (%)
P804A1	30	0.2441	0.0760	0.0732	w_{lim}	LVDT15	140	68
		0.0021	0.0640	0.0006		LVDT16		
P804A1	38	0.5569	0.2156	0.1671	w_{max}	LVDT15	180	87
P804A1	2	0.0024	0.0284	0.0007	w_{lim}	LVDT12	75	36
P804A2	9	0.3141	0.0144	0.0628	w_{max}	LVDT15	160	69
Residual deformation criterion from German guideline and ACI 437.2M-13								
Test	LS	Δ_{max} (mm)	Δ_r (mm)	Δ_r^* (mm)	$\Delta_{lim,DAfStB}$ (mm)	$\Delta_{lim,ACI}$ (mm)	P_Δ (kN)	Level (%)
P804A1	1	2.509	1.001	0.727	0.251	0.627	75	36
P804A2	1	3.172	0.416	-0.082	0.317	0.793	75	32
P804A2	17	12.973	11.348	11.239	1.297	3.243	230	100
P502A2	7	5.262	0.311	0.311	0.526	1.315	150	100
Proposed stiffness criterion								
Test	LS	Red_{EI} (%)	P_{EI} (kN)	Level (%)				

P804A1	25	24.67	95	46
P804A1	26	51.79	120	58
P804A2	5	6.37	115	50
P804A2	17	15.14	230	100
P804B	4	25.77	110	56
P502A2	2	21.72	75	50
Proposed criterion from deformation profiles				
	Horizontal deformations		Vertical deformations	
Test	P_{def} (kN)	Level (%)	P_{def} (kN)	Level (%)
P804A1	120	58	160	77
P804A2	200	87	-	-
P804B	110	56	110	56
P502A2	125	83	125	83

Table 5 – Overview of proposed acceptance criteria for reinforced concrete bridges.

Conversion: 1 mm = 0.04 in.

Failure mechanism	Previously cracked in bending moment or not?	
	<i>Uncracked</i>	<i>Cracked</i>
<i>Flexural failure</i>	Concrete strains (Eq. (7)) $w_{max} \leq 0.5$ mm $w_{res} \leq 0.1$ mm Stiffness reduction ≤ 25 % Deformation profiles Load-displacement graph	Concrete strains (Eq. (7)) $w_{max} \leq 0.5$ mm $w_{res} \leq 0.1$ mm Stiffness reduction ≤ 5 % Deformation profiles Load-displacement graph
<i>Shear failure</i>	Concrete strains (Eq. (7)) $w_{max} \leq 0.3$ mm Stiffness reduction ≤ 5 % Deformation profiles Load-displacement graph	Concrete strains (Eq. (7)) Stiffness reduction ≤ 5 % Deformation profiles Load-displacement graph

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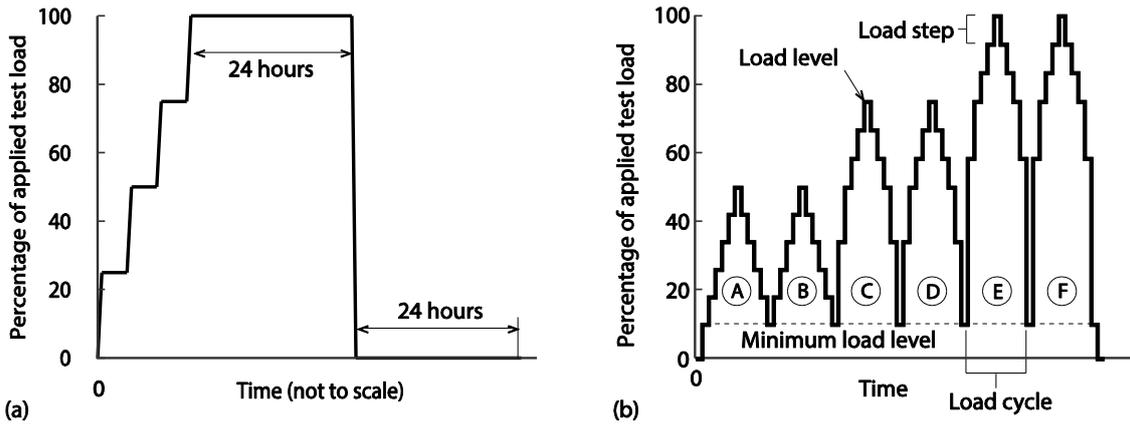
10 Fig. 6 – Measured load-displacement diagrams: (a) P804A1; (b) P804A2; (c) P804B; (d) P502A2.
11 Conversion: 1 mm = 0.04 in.

12 Fig. 7 – Evaluation of P804A1 for loading protocol: (a) Relation between residual deflection Δ_r and
13 the loading speed; (b) Relation between stiffness reduction and loading speed; (c) Influence of
14 number of cycles on energy in cycle or energy in loading branch of cycle. Conversion: 1 mm = 0.04
15 in, 1 kNm = 0.7 kip-ft.

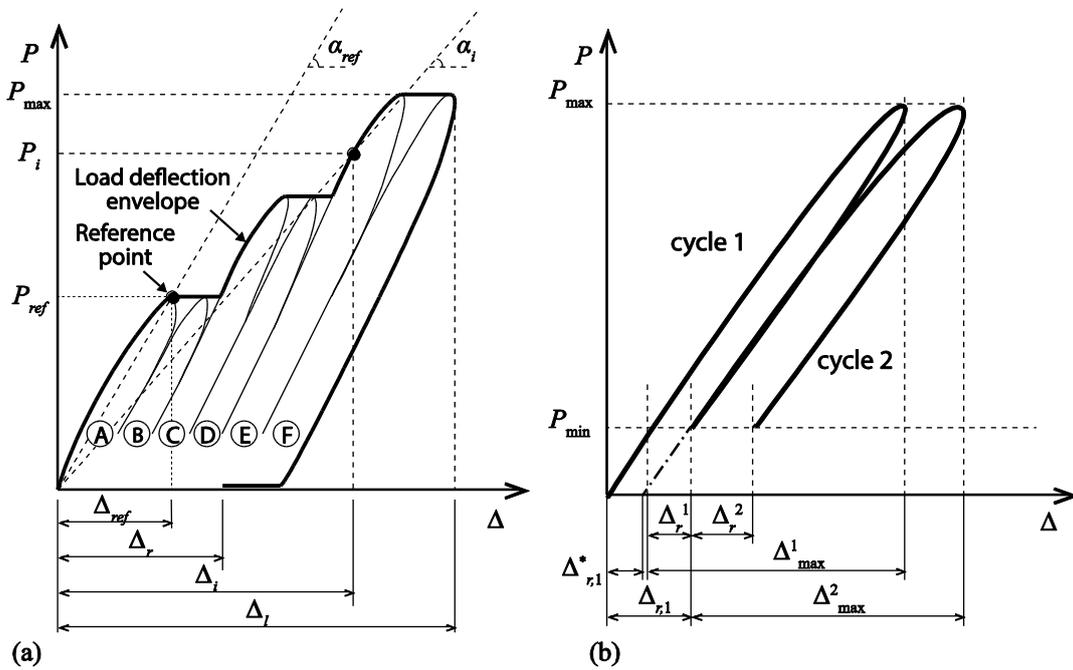
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18 deformations; (c) vertical deformations. Conversion: 1 mm = 0.04 in.

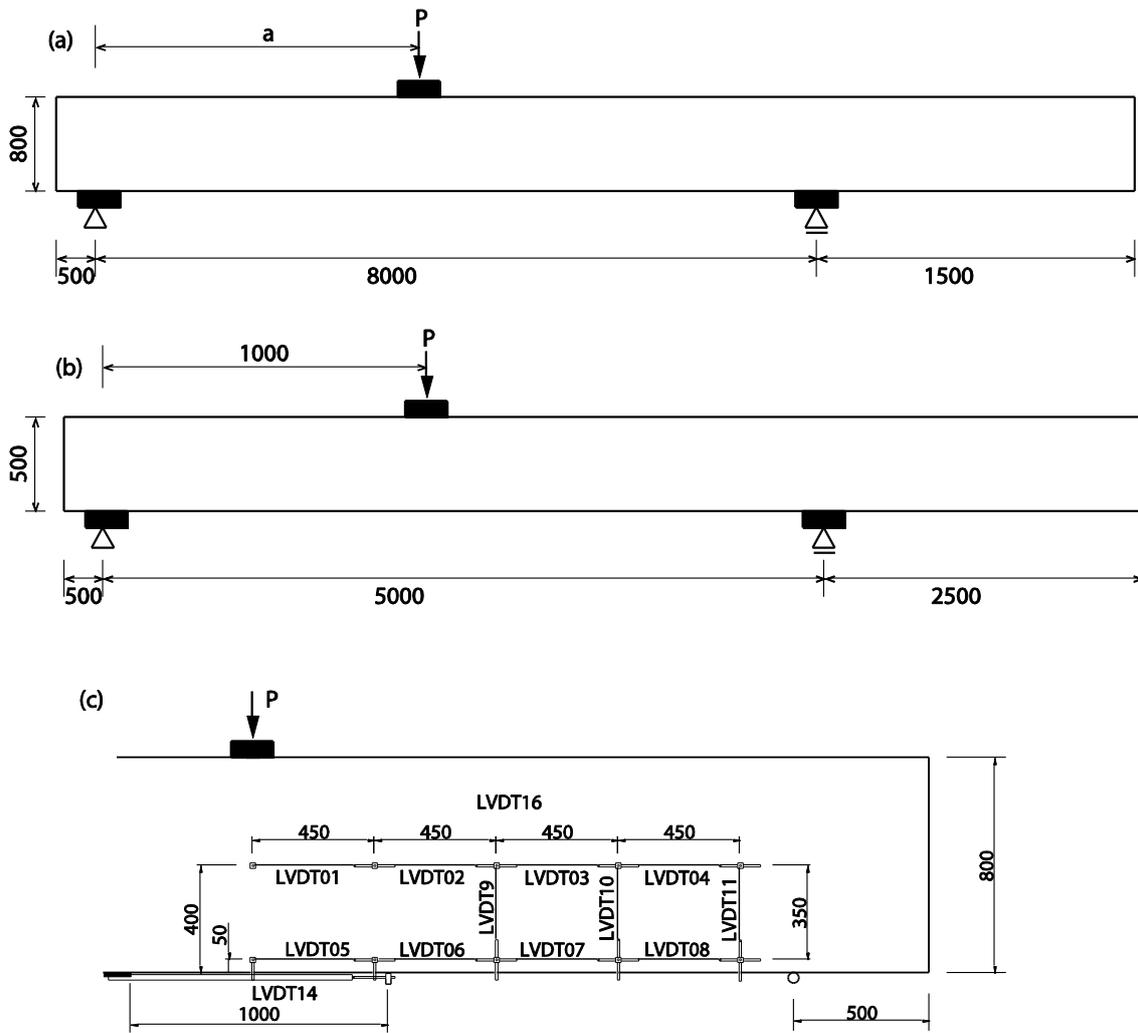
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3 **loading protocol; (b) cyclic loading protocol**

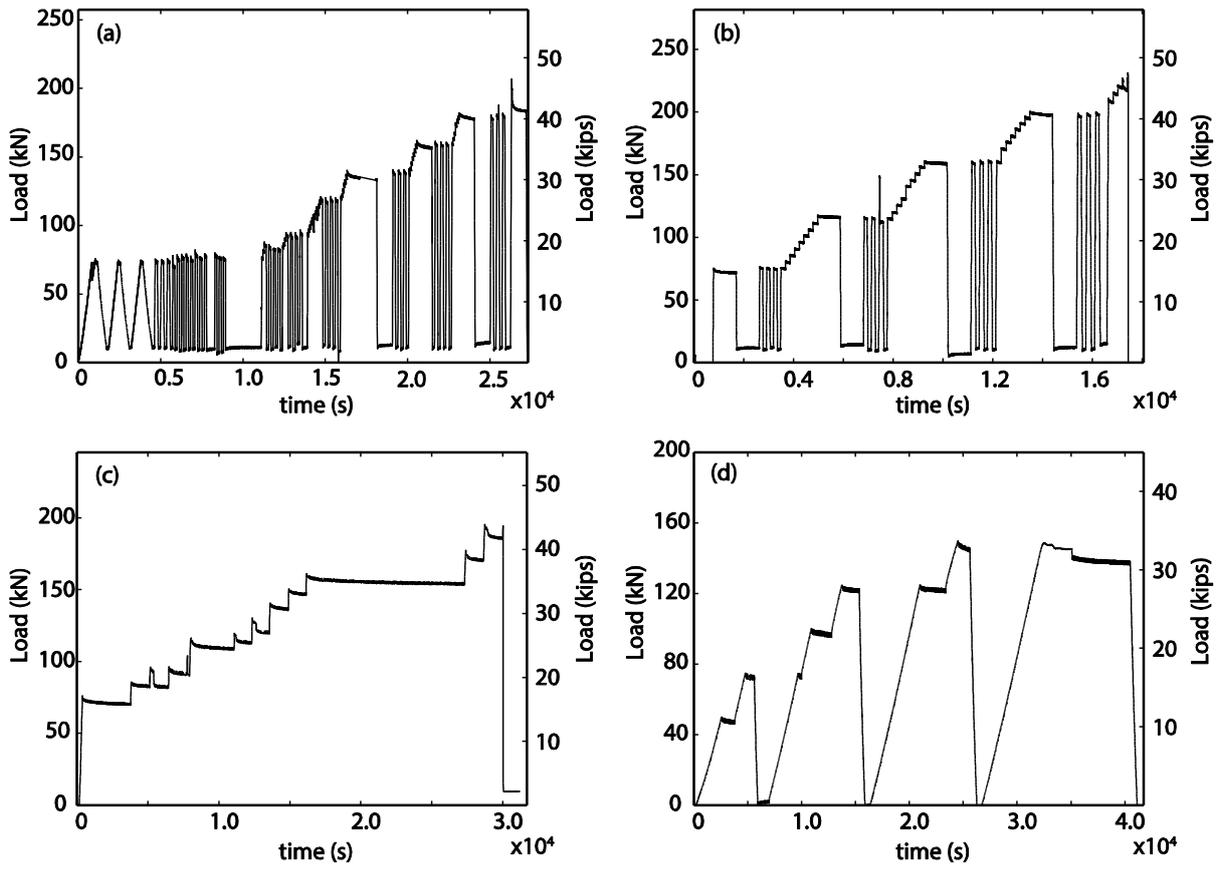


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5 **Fig. 2— Definitions used for the acceptance criteria from ACI 437.2M-13 (ACI Committee**
6 **437, 2013): (a) Deviation from Linearity, I_{DL} ; (b) Permanency Ratio, I_{PR} , also showing residual**
7 **deflection after a cycle $\Delta_{r,I}$ and the calculated value using the stiffness of the unloading branch**
8 **to zero load, $\Delta_{r,I}^*$.**



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Fig. 3– (a) Test setup and geometry of P804A1, P804A2 and P804B; (b) Test setup and geometry for P502A2; (c) instrumentation on P804A1. Conversion: 1 mm = 0.04 in.



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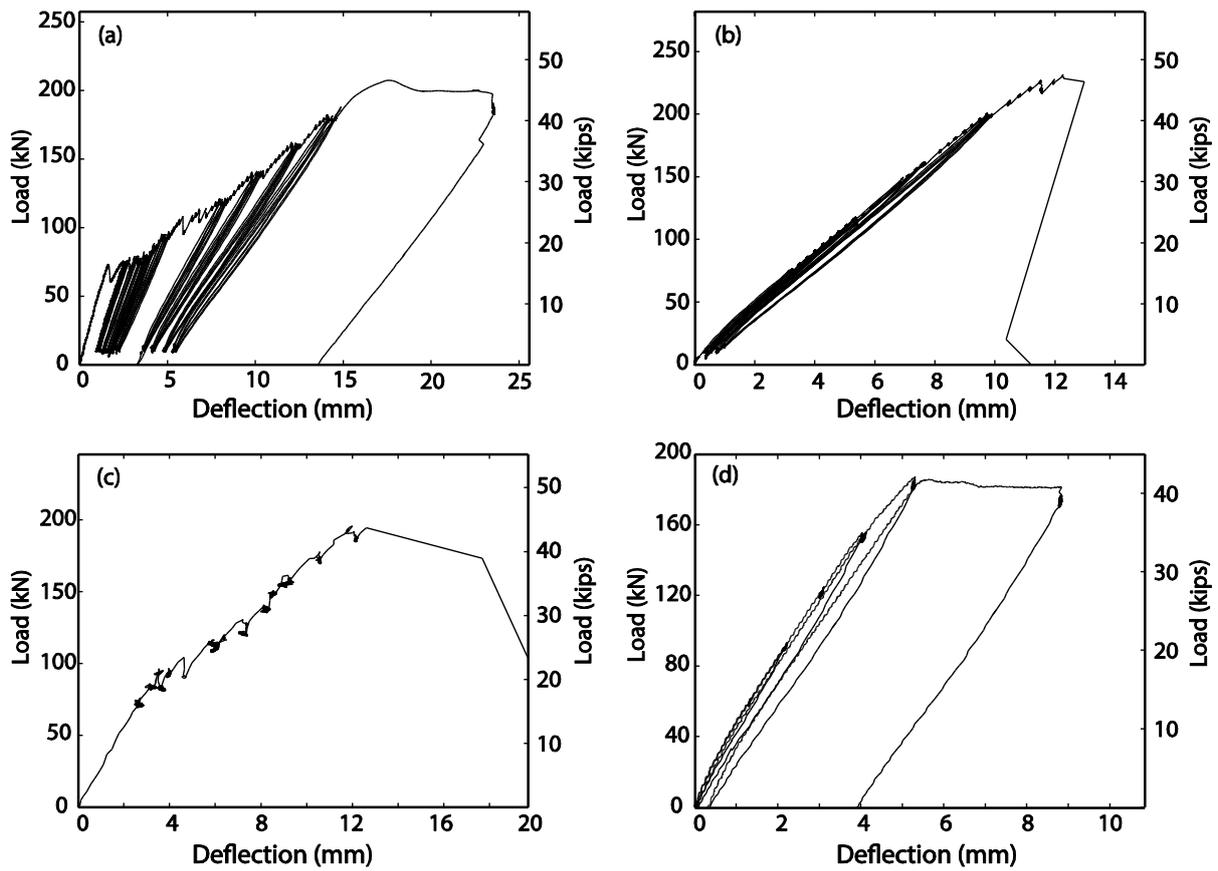
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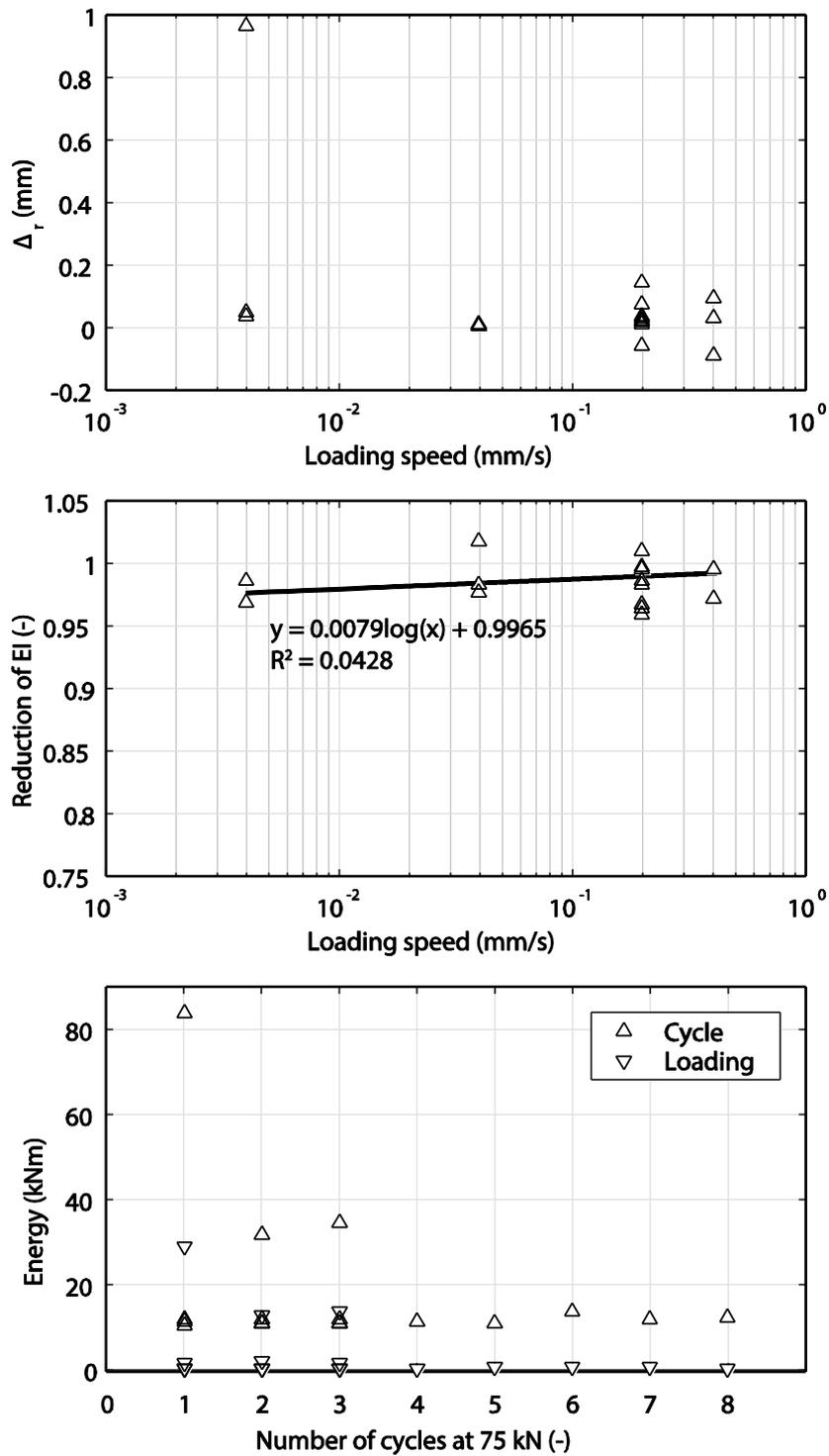


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2 **Fig. 6 – Measured load-displacement diagrams: (a) P804A1; (b) P804A2; (c) P804B; (d)**

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P502A2. Conversion: 1 mm = 0.04 in.



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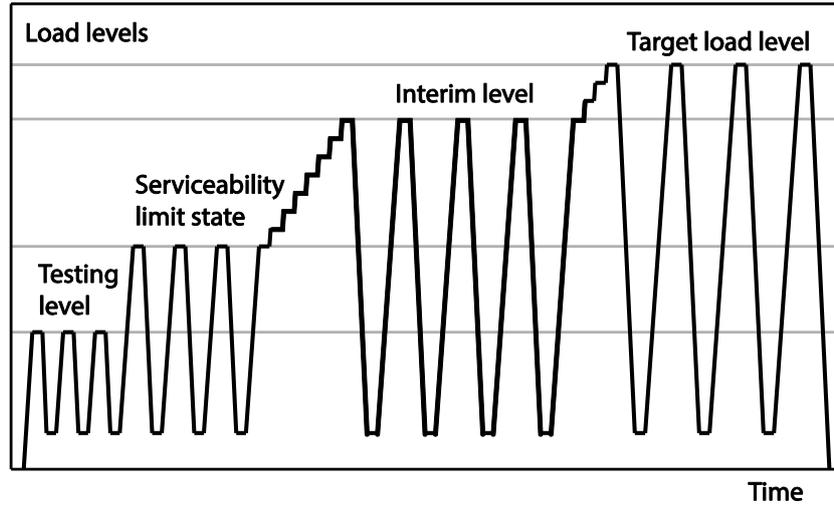
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Fig. 7 – Evaluation of P804A1 for loading protocol: (a) Relation between residual deflection Δ_r and the loading speed; (b) Relation between stiffness reduction and loading speed; (c) Influence of number of cycles on energy in cycle or energy in loading branch of cycle.

Conversion: 1 mm = 0.04 in, 1 kNm = 0.7 kip-ft.

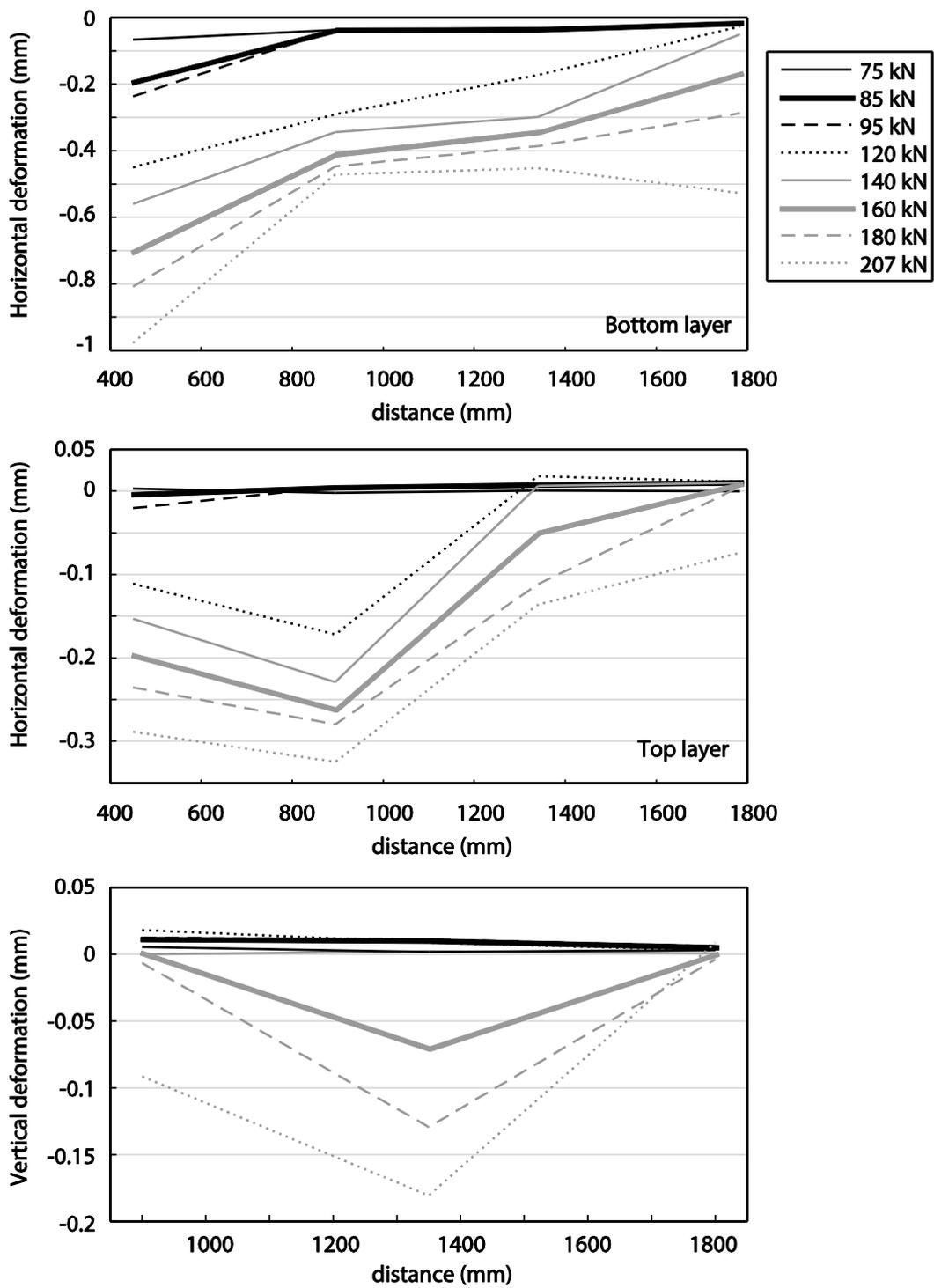
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Fig. 9 – Deformation plots: (a) upper layer of horizontal deformations; (b) lower layer of horizontal deformations; (c) vertical deformations. Conversion: 1 mm = 0.04 in.