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FNFT: A Software Library for Computing Nonlinear Fourier Transforms

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Summary

The conventional Fourier transform was originally developed in order to solve the heat equation, which is a standard example for a linear evolution equation. Nonlinear Fourier $transforms (NFTs)^1$ are generalizations of the conventional Fourier transform that can be used to solve certain nonlinear evolution equations in a similar way (Ablowitz et al. 1974). An important difference to the conventional Fourier transform is that NFTs are equationspecific. The Korteweg-de Vries (KdV) equation (Gardner et al. 1967) and the nonlinear Schroedinger equation (NSE) (Shabat and Zakharov 1972) are two popular examples for nonlinear evolution equations that can be solved using appropriate NFTs.

NFTs are well-established theoretical tools in physics and mathematics, but in several areas of engineering they have only recently begun to draw significant attention. An idealized fiber-optic communication channel can be described by the NSE, which is solvable with a NFT. In the last few years, there has been much interest in using NFTs for data transmission in optical fibers. We refer to Turitsyn et al. (2017) for a recent review. Several invited papers and tutorials on the topic have been presented at major conferences such as the Optical Fiber Communication Conference and Exhibition (OFC) and the European Conference and Exhibition on Optical Communication (ECOC) in the last few years. Several new research projects, such as the MSCA-ITN COIN or the ERC Starting Grant from which this project is funded (see below), have been initiated. Another area in which NFTs have found practical application is the analysis of waves in shallow water (Osborne 2010; Brühl and Oumeraci 2016). Here, the KdV-NFT is typically used.

The implementation of a numerical algorithm for computing a NFT is however not as simple as for the conventional Fourier transform. While quite a few algorithms have been presented in the literature, there is not a single publically available software library that implements numerical NFTs. We believe that the lack of a reliable and efficient software library for computing NFTs is currently hindering progress in the field. For this reason, we have published FNFT on GitHub. FNFT, which is short for "Fast Nonlinear Fourier Transforms", is a software library that provides implementations of the fast NFT algorithms that were developed by some of the authors (Wahls and Poor 2013, 2015; Prins and Wahls 2018). Our goal was to develop an efficient, easy to use and reliable library. Therefore, FNFT was written in C and ships with a MATLAB interface as well as currently more than 60 unit and integration tests. To simplify the build process as much as possible, FNFT uses CMake. FNFT has no external dependencies, but ships with some 3rd party code from the open source projects EISCOR (also see (J. L. Aurentz and Watkins 2017)) and KissFFT.

¹NFTs are also known as *direct scattering transforms* in the literature.



Features

FNFT currently provides algorithms for the numerical computation of the following NFTs:

- NSE with vanishing boundary conditions,
- NSE with periodic conditions (main and auxiliary spectrum),
- KdV with vanishing boundary conditions (continuous spectrum only).

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References

Ablowitz, M. J., D. J. Kaup, A. C. Newell, and H. Segur. 1974. "The Inverse Scattering Transform-Fourier Analysis for Nonlinear Problems." *Studies in Applied Mathematics* 53 (4):249–315. https://doi.org/10.1002/sapm1974534249.

Brühl, M., and H. Oumeraci. 2016. "Analysis of Long-Period Cosine-Wave Dispersion in Very Shallow Water Using Nonlinear Fourier Transform Based on KdV Equation." *Applied Ocean Research* 61 (December):81–91. https://doi.org/10.1016/j.apor.2016.09.009.

Gardner, C. S., J. M. Greene, M. D. Kruskal, and R. M. Miura. 1967. "Method for Solving the Korteweg-deVries Equation." *Physical Review Letters* 19 (19):1095–7. https://doi.org/10.1103/PhysRevLett.19.1095.

J. L. Aurentz, L. Robol, T. Mach, and D. S. Watkins. 2017. "Fast and Backward Stable Computation of Roots of Polynomials, Part Iia: General Backward Error Analysis." Technical report TW 683. KU Leuven. http://www.cs.kuleuven.be/publicaties/rapporten/tw/TW683.abs.html.

Osborne, A. R. 2010. Nonlinear Ocean Waves and the Inverse Scattering Transform, Volume 97 (International Geophysics). Academic Press. https://www.sciencedirect.com/science/journal/00746142/97/.

Prins, P. J., and S. Wahls. 2018. "Higher Order Exponential Splittings for the Fast Non-Linear Fourier Transform of the Korteweg-de Vries Equation." In *Proc. 2018 IEEE International Conference on Acoustics, Speech and Signal Processing, to appear.*

Shabat, A., and V. Zakharov. 1972. "Exact Theory of Two-Dimensional Self-Focusing and One-Dimensional Self-Modulation of Waves in Nonlinear Media." *Soviet Physics JETP* 34 (1):62. http://jetp.ac.ru/cgi-bin/e/index/e/34/1/p62?a=list.

Turitsyn, S. K., J. E. Prilepsky, S. T. Le, S. Wahls, L. L. Frumin, M. Kamalian, and S. A. Derevyanko. 2017. "Nonlinear Fourier Transform for Optical Data Processing and Transmission: Advances and Perspectives." *Optica* 4 (3):307. https://doi.org/10.1364/OPTICA.4.000307.

Wahls, S., and H. V. Poor. 2013. "Introducing the Fast Nonlinear Fourier Transform." In 2013 IEEE International Conference on Acoustics, Speech and Signal Processing. IEEE. https://doi.org/10.1109/ICASSP.2013.6638772.

——. 2015. "Fast Numerical Nonlinear Fourier Transforms." *IEEE Transactions on Information Theory* 61 (12):6957–74. https://doi.org/10.1109/TIT.2015.2485944.