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# Multi-decadal stability of water ages and tracer transport in a temperate-humid river basin

#### Siyuan Wang<sup>1,2,\*</sup>, Markus Hrachowitz<sup>1</sup>, Gerrit Schoups<sup>1</sup> and Anna Störiko<sup>1</sup>

<sup>1</sup> Department of Water Management, Faculty of Civil Engineering and Geosciences, Delft University of Technology, Stevinweg 1, 2628CN Delft, The Netherlands

<sup>2</sup> Faculty of Technology Water, Energy and Environmental Engineering, University of Oulu, Pentti Kaiteran katu 1, 8000 Oulu, Finland
\* Author to whom any correspondence should be addressed.

E-mail: Siyuan.Wang@oulu.fi and S.Wang-9@tudelft.nl

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#### Abstract

The temporal dynamics of water ages provide crucial insights into hydrological processes and transport mechanisms, yet there remains a significant gap in quantifying water age variability across different temporal scales. This study utilizes a comprehensive dataset spanning 70 years of hydrological observations and tritium records (1953–2022) with a semi-distributed hydrological model with integrated tracer routing routine based on StorageAge Selection functions SAS, to explore the temporal evolution of water ages in the 4000 km<sup>2</sup> Upper Neckar River basin, Germany. Our findings indicate a systematic convergence of the variability of young water fractions and other metrics of water age in riverflow and evaporation towards stable values when averaging over increasing time scales. While at daily scales exhibiting considerable variability with young water fractions in riverflow  $F_{wy,Q} \sim 0.01$ –0.91 and in evaporation  $F_{wy,E} \sim 0.02$ –0.75, the variability of  $F_{\rm wy,Q}$  and  $F_{\rm wy,E}$  gradually reduces with increasing averaging time scales and converge to 0.45–0.47 and 0.96–0.97, respectively, between individual decades. Liquid water input  $(P_L)$ , comprising rainfall and snow melt, emerges as the dominant driver of  $F_{wy,Q}$  across all time scales. In contrast,  $F_{wy,E}$  shows varying controls with time scale: soil moisture content governs daily fluctuations, whereas P<sub>L</sub> dominates at the decadal scale. Overall, water ages demonstrate remarkable stability with only minor deviations in response to climatic variability: a 20% fluctuation in average decadal  $P_{\rm L}$  results in only ~4% variation in  $F_{\rm wy,Q}$  and ~1% in  $F_{\rm wy,E}$  over the study period. These findings suggest a lack of major long-term dynamics in water ages. Consequently, the results suggest that the physical transport dynamics in the Upper Neckar River basin, and potentially in comparable river basins with similar water age characteristics, can be considered near-stationary over multiple decades.

#### 1. Introduction

As the crucial link between hydrology and water quality at the catchment scale, water ages and distributions thereof (i.e. transit time distributions; TTDs) are a metric of physical transport through a hydrological system (Hrachowitz *et al* 2016). As such they are a descriptor of how water and, as a consequence, nutrients and pollutants are stored in and released from catchments via different flow paths (Rinaldo *et al* 2015, Sprenger *et al* 2018, Benettin *et al* 2022). The celerity-driven hydrological response, including riverflow and evaporation, acts at different time scales than the velocity-driven TTDs that underlie the water quality response in catchments (Weiler *et al* 2003, McDonnell and Beven 2014, Hrachowitz *et al* 2016). Temporal variability of the hydrological response over a spectrum of time-scales from minutes to multiple decades has been extensively described in literature (Thompson and Katul 2012, Berghuijs *et al* 2014, Sivapalan and Blöschl 2015, McMillan 2020, Berghuijs and Slater 2023). In contrast, the majority of studies that seek to analyse temporal variability of water ages and the underlying drivers have so far focused on daily time scales. These studies demonstrate that water ages in fluxes such as riverflow or evaporation, can fluctuate considerably at this time scale and that the main driver behind this variability is the available water supply and the associated magnitude of precipitation input at that time scale (Benettin et al 2015, 2017, Harman 2015, Hrachowitz et al 2015, Soulsby et al 2016, Rodriguez et al 2018, Kuppel et al 2020, Wilusz et al 2020). Beyond that, several studies have reported significant, albeit attenuated variability at time scales from monthly (Kaandorp et al 2018, Knapp et al 2019, Stockinger et al 2019) over seasonal (Birkel et al 2016, Remondi et al 2018) to yearly (Heidbüchel et al 2013, Birkel et al 2015, Wilusz et al 2017, von Freyberg et al 2018, Stockinger and Stumpp 2024). At these scales, switches between distinct storage compartments, such as the unsaturated root-zone or the groundwater, as dominant source of water can become an additional factor regulating variability of water ages (Hrachowitz et al 2013).

However, as a result of insufficiently long tracer records in many catchments, there is only a handful of studies that have analysed water ages over time periods longer than 10-20 years (Hrachowitz et al 2010, Wang et al 2023). Thus, little is known about the variability over such longer time scales and the resulting long-term dynamics of water ages, including potentially systematic trends over time arising therefrom. This is in particular concerning as there is evidence that changes in land management and the associated changes to (sub-)surface flow paths and water storage volumes do affect water ages at such time scales (Danesh-Yazdi et al 2016, Hrachowitz et al 2021). Similarly, altered precipitation and atmospheric water demand due to climate change can, as 'external transport variability' (Kim et al 2016), directly impact water ages. As a consequence, catchment properties such as vegetation cover may adjust to a changing climate, potentially leading to additional changes in subsurface flow paths and/or water storage volumes (Wang et al 2024), as 'internal transport variability' (Kim et al 2016).

This knowledge gap increases uncertainties in our ability to predict removal of legacy solutes such as nitrate (Basu *et al* 2010, Howden *et al* 2011) or chloride (Hrachowitz *et al* 2015) over time-scales of several decades but also the mobilization of solutes at shorter time-scales, such as phosphorus (e.g. Dupas *et al* 2018) under changing environmental conditions. The problem would be further exacerbated if water ages are non-self-averaging. Such a non-selfaveraging behaviour has been widely observed for tracer and solute concentrations in stream water and is related to the fractal scaling of these variables (Kirchner *et al* 2000, Hrachowitz *et al* 2009, Godsey *et al* 2010, Kirchner and Neal 2013, Aubert *et al* 2014). In non-self-averaging time series, the variability of their daily, monthly, yearly or decadal means remains constant or converges towards stable averages at rates lower than predicted by the central limit theorem. Such non-self-averaging time series can give rise to trends that can be robust but nevertheless artefacts and thus unreliable predictors of future solute dynamics, as demonstrated by Kirchner and Neal (2013).

The objective of this study is to quantify the temporal variability in water ages as well as to identify their dominant controls across time-scales from daily to multi-decadal and to analyse the associated temporal evolution of water ages for riverflow and evaporation in the Neckar River basin, Germany. The analysis is based on hydrological data and tritium records over a 70 year period (1953-2022) that we use together with a hydrological model with integrated tracer-routine to estimate water age distributions in riverflow and evaporation. More specifically, we test the hypotheses that (1) water ages of riverflow and evaporation are non-self-averaging and thus unpredictable over decadal time-scales, that (2) different drivers control variability of water ages at different time scales and that (3) water ages are subject to significant long-term dynamics on decadal time scales, reflecting hydro-climatic variability and associated changes in catchment (sub-)surface structure.

#### 2. Study area and data

The study area is the 4000 km<sup>2</sup> Upper Neckar River basin in South-West Germany (figure 1 and supplementary material table S1). Briefly, the basin is characterized by a temperate-humid climate with longterm mean precipitation  $P \sim 880$  mm yr<sup>-1</sup> and temperature  $T \sim 8.2$  °C. Summer precipitation of ~500 mm yr<sup>-1</sup> (May–October) is balanced by winter precipitation of ~380 mm yr<sup>-1</sup> (November–April), respectively (figure S1). The landscape is characterized by terrace-like elements, undulating hills and steep and narrow forested valleys in the uplands (figure 1(c)).

For the analysis we used daily hydrometeorological data for the time period 01/01/1953– 31/12/2022 from the German Weather Service (DWD) and the German Federal Institute of Hydrology (BfG) (figure S1). Daily potential evaporation  $E_P$  (mm d<sup>-1</sup>) was estimated using the Hargreaves equation. Daily riverflow records were available for the same time period at the basin outlet at Plochingen and for three additional nested sub-catchments (figure 1(a)) from the BfG. Tritium (<sup>3</sup>H) data in precipitation and riverflow were available from the stations Stuttgart and Obertürkheim close to the



**Figure 1.** (a) Elevation of the Neckar catchment with discharge and hydro-meteorological stations as well as the water sampling locations in this study, three distinct precipitation zones P1—P3 (black outline), and three sub-catchments (red outlines; C1:Rottweil, C2:Plochingen at Fils, C3:Horb) within the upper Neckar basin, (b) selected part of the time series of observed (blue line) and modelled daily riverflow (Q) from 01/01/2001 to 01/01/2006, where the red dashed line indicates modelled Q for the best solution, and the red shaded area the 5th/95th inter-quantile range obtained from all pareto optimal solutions, (c) selected time series of observed (pink dots) river <sup>3</sup>H signals with the error bars and modelled river <sup>3</sup>H signals from 01/01/2001 to 01/01/2006, where purple dots indicate the modelled river <sup>3</sup>H signal for the best solution and the light purple shaded area indicates the 5th/95th inter-quantile range optimal solutions.

basin outlet for the period 1978–2018 (figure S1) from the Global Network of Isotopes in Precipitation and the BfG (Schmidt *et al* 2020). For the preceding 1953–1977 period the precipitation record was reconstructed by bias- correcting data from stations Vienna and Ottawa. A more detailed description of the study region and the data used can be found in the supplementary material and in Wang *et al* (2023), (2024)).

#### 3. Methods

We used a semi-distributed process-based hydrological model, which has previously been implemented and tested for the study basin (Wang *et al* 2023, 2024) and other environments world-wide (e.g. Prenner *et al* 2018, Hulsman *et al* 2021a, 2021b, Hanus *et al* 2021), based on the DYNAMIT modular modelling scheme (Hrachowitz *et al* 2014). Briefly, this model features three parallel hydrological response units, i.e. forest, grass/cropland and wetland, which are linked through a common storage component representing the groundwater system (figure S2). Overall, the model consists of an elevation-stratified snow storage  $(S_{snow})$  as well as individual interception  $(S_i)$ , unsaturated root zone  $(S_u)$ , fast responding  $(S_f)$  and slow responding groundwater storage  $(S_s)$  components for each hydrological response unit.

The storage-age selection function (SAS) approach (e.g. Rinaldo *et al* 2015) was integrated with the hydrological model to route <sup>3</sup>H fluxes through the model. Briefly, each storage component used a uniform distribution as SAS function. Although this entails that each storage is fully mixed, the different time-scales of the individual storage components, lead to a 'combined' SAS functions that does not result in an overall fully mixed system response. The passive water storage  $S_{s,p}$  (mm), characterized by  $dS_{s,p}/dt = 0$ , that physically represents groundwater volumes below the level of the river bed (Zuber 1986), was added as parameter to the active groundwater storage  $S_s$  for a sufficiently large mixing volume (Birkel *et al* 2011, figure S2).

Note that while the outflow  $Q_s$  from the groundwater storage is exclusively regulated by the active storage volume in  $S_s$  (equation (S6)), the <sup>3</sup>H of that outflow is sampled from the total groundwater storage volume  $S_{s,tot} = S_s + S_{s,p}$ .

Following a multi-objective strategy to ensure a plausible representation of model internal processes, the model was calibrated to simultaneously reproduce seven river flow signatures and river water <sup>3</sup>H dynamics. To reflect the vegetation adapting its active root system to changing climatic conditions during the 70 year study period, we independently estimated the model root-zone storage capacity parameter S<sub>umax</sub> for each decade, as described by Wang et al (2024) and accordingly hardcoded the different values of Sumax in the model, varying between 95 and 115 mm throughout the study period. Tracking the <sup>3</sup>H signals, through the model allowed us to estimate the distributions of water ages in riverflow (Q) and actual evaporation, which here is the sum of interception evaporation and transpiration ( $E = E_i + E_t$ ).

We used young water fractions ( $F_{wy}$ ), i.e. water younger than 3 months (Kirchner 2016), as robust descriptor to describe water ages in the main text. The results of other age metrics, such as  $F_{w10}$ , i.e. fraction of water younger than 10 years, is provided in the supplementary material.

Detailed descriptions of the model implementation and calibration in the study region are provided by Wang *et al* (2023), (2024)) and in the supplementary material together with the model equations (table S2).

#### 4. Results and discussion

The model reproduces the main features of the hydrological response over the entire study period, both at the basin outlet (figure 1(b), supplementary figure S3; table S5) and, as model test without further recalibration, in three nested sub-catchments (figure S4). It does not only capture the timing of flows (figure S3(a)), but also simultaneously reproduces well other observed riverflow signatures including the flow-duration curves (figure S3(d)), seasonal runoff coefficients (figure S3(c)) and autocorrelation functions (figure S3(e)). Similar to a previous implementation in the greater study region by Wang et al (2023), the model also catures the overall decline of river water 3H levels with NSE3H >0.93. In spite of somewhat underestimating peaks, the magnitude of seasonal 3H amplitudes and intra-annual fluctuations are represented well (figures 1(c), S5).

## 4.1. How do water ages vary over different time scales?

Tracking water fluxes through the model, a median non flow-weighted fraction of young water  $F_{wy,Q} \sim 0.34$  emerged for riverflow on a daily time

scale. At the same time, a pronounced variability with daily  $F_{wy,Q}$  fluctuating between 0.01 and 0.91 (5th/95th percentile) was observed, reflecting differences in daily preciptiation and evaporation (figures 2(a) and (b)). Describing older river water, daily  $F_{w10,O}$  varied between 0.41 and 0.95 and thus to a lesser degree in response to changing daily hydroclimatic conditions (figures 2(a) and (b)). To analyse the variability of water ages at different time scales, we computed block averages of  $F_{wy}$ , aggregating to weekly, monthly, seasonal, yearly and decadal values. With increasing averaging time scales, a reduction of variability was found. While average monthly  $F_{wy,O}$ oscillates between 0.02 and 0.75, this is eventually reduced to 0.44-0.47 for decadal averages with similarly reduced variability for  $F_{w10,Q}$  (figure 2(a),b) and other age fractions (table S6). The observed convergence towards increasingly stable water ages is an indicator for a self-averaging process. As robust quantity to further test for self-averaging behaviour in the time series of water ages we plotted the root mean square differences (RMSD) of pairs of adjacent averages against the time interval n over which the averages were computed (figure 2(c)) as suggested by Kirchner and Neal (2013). It was found that at averaging time scales of >1 month, the rates of convergence of both  $F_{wy,Q}$  and  $F_{w10,Q}$  come close to  $n^{-0.5}$ , which describes a self-averaging and thus stationary process (e.g. white noise) as dictated by the central limit theorem. Such a process is characterized by weak persistence and thus little long-term fluctuations in water ages at low frequencies over time that here applies to time scales of at least multiple decades.

Evaporation is characterized by a markedly different age structure that is dominated by much younger water as illustrated by median  $F_{\rm wy,E} \sim 0.96$  and  $F_{\rm w10,E}$  > 0.99, respectively. The daily  $F_{\rm wy,E}$  ranges from 0.56 to 1, while fractions of older water do not decrease below  $F_{w10,E} \sim 0.75$  and thus exhibit less variability (figures 2(d) and (e)). Similar to riverflow, the variability in evaporation ages decreases with increasing averaging time scales (table S7), as illustrated by average monthly  $F_{wy,E}$  that ranges from  $\sim$ 0.81–1 which further decreases to a range of 0.96– 0.97 for decadal averages (figures 2(d) and (e)). Correspondingly, the traces of RMSD of adjacent means as function of the averaging time scale n for both  $F_{wv,E}$  and  $F_{w10,E}$  show convergence rates close to  $n^{-0.5}$  at averaging time scales larger than 6 months (figure 2(f)). This suggests that the age structure of evaporation is not subject to major long-term fluctuations and can thus also be assumed stationary at multi-decadal time scales.

## 4.2. What are the hydro-climatic drivers of water age variability at different time scales?

To explore which factor can best explain variability in  $F_{wy}$  regression analysis was used. For the



**Figure 2.** The variability of river flow TTDs (eCDF<sub>Q</sub>) and evaporation TTDs (eCDF<sub>E</sub>) from the most balanced model solution over various time scales. (a) The blue shades from lighter to darker indicate the 5th/95th intervals of the eCDF<sub>Q</sub> of the river water age distributions from daily to decadal averaging time-scales, (b) the blue and navy blue box plots (whiskers indicate 5th/95th percentiles) from lighter to darker indicates  $F_{wy,Q}$  and  $F_{w10,Q}$  from daily to decadal, respectively, (c) Root mean squared differences (RMSD) between pairs of successive average values in  $F_{wy,Q}$  (the gradient blue line) and  $F_{w10,Q}$  (the gradient navy blue line) plotted against corresponding averaging intervals, (d) the orange shades from lighter to darker indicate the eCDF<sub>E</sub> of the evaporation water age distributions from daily to decadal, (e) the yellow and brown boxes from lighter to darker indicates  $F_{wy,E}$  and  $F_{w10,E}$  from daily to decadal, respectively, (f) RMSD in  $F_{wy,E}$  (the gradient yellow line) and  $F_{w10,E}$  (the gradient brown line). Note that the dashed grey line is the slope of -0.5 predicted by the central limit theorem for self-averaging time series and *n* is the number of averaging time steps (here: years).

entire 70 year study period 1953–2022, the pronounced variability of young water fractions in riverflow  $F_{wy,Q}$  at a daily time-scale is to first order controlled by daily liquid water input  $P_L = P_{rain} + M_{snow}$ (figure 3(a)). This is illustrated by the sensitivity ( $\psi$ ) of  $F_{wy,Q}$  to  $P_L$ , approximated by a linear relationship  $\psi = \Delta F_{wy,Q}/\Delta P_L \sim 0.03$  ( $R^2 = 0.34$ ). Other potential hydro-climatic drivers, including Q as aggregate metric of catchment wetness ( $R^2 = 0.22$ ), evaporation E ( $R^2 = 0.22$ ) or root-zone moisture content  $S_u$  ( $R^2 = 0.20$ ) exert weaker controls on  $F_{wy,Q}$ . Across all tested averaging time-scales,  $P_{\rm L}$  remains the strongest driver, reaching  $R^2 = 0.89$  with a sensitivity  $\psi \sim 0.07$  at the decadal time-scale.  $P_{\rm L}$  also becomes relatively more important compared to the other hydro-climatic variables ( $R^2 = 0.25$ –0.82; figure 3). At the seasonal time-scale it is notable that  $F_{\rm wy,Q}$  is somewhat more sensitive to  $P_{\rm L}$  in winter ( $\psi \sim 0.10$ ) than in summer ( $\psi \sim 0.07$ ). Further analysis revealed that this effect can be attributed to the influence of winter snow melt. Periods of snow cover preceding snow melt, are characterized by low  $F_{\rm wy,Q} \sim 0.2$ , on



**Figure 3.** Relationship between the young water fraction in river flow ( $F_{wy,Q}$ ) and hydro-climatic variables over different time scales from daily to decadal including (a) liquid precipitation  $P_L$  (rainfall +snowmelt), (b) liquid precipitation intensity  $P_{L,intensity}$ , (c) river flow  $Q_0$ , (d) evaporation E (e) soil moisture  $S_u$ . The dashed lines indicate the linear relationships between the  $F_{wy,Q}$  and the various hydro-climatic variables x, used to approximate the sensitivity  $\psi = \Delta F_{wy,Q}/\Delta x$ .



**Figure 4.** Sensitivity analysis of variability of the young water fractions (<3 months) in river flow ( $F_{wy,Q}$ ) and evaporation ( $F_{wy,E}$ ) as well as soil moisture  $S_u$  in response to the selected snowmelt events in winter in (a)–(d) and rainfall events in summer in (e)-(h).

average (figure 4(b)). Snow melt water is rather young as the presence of snow over periods longer than a few weeks is rare in the study region. As a consequence, snow melt inputs (figure 4(a)) increase  $F_{wy,Q}$  to ~0.7. In contrast,  $F_{wy,Q}$  preceding summer rainfall events (figure 4(e)) is, on average, with  $F_{wy,Q} \sim 0.4$  considerably higher (figure 4(f)), due to frequent summer rain events. Although summer  $F_{wy,Q}$  also reaches ~0.7, the



Figure 5. Relationship between the young water fraction in evaporation ( $F_{wy,E}$ ) and hydro-climatic variables over different time scales from daily to decadal including (a) liquid precipitation  $P_L$  (rainfall+snowmelt), (b) liquid precipitation intensity  $P_{L,intensity}$ , (c) river flow  $Q_0$ , (d) evaporation E and (e) soil moisture  $S_u$ . The dashed lines indicate the linear relationships between the  $F_{wy,E}$ and the various hydro-climatic variables x, used to approximate the sensitivity  $\psi = \Delta F_{wy,E}/\Delta x$ .

rate of increase from 0.4 to 0.7, and thus its sensitivity, is lower. Overall, controls on fractions of older water  $F_{w10,Q}$  correspond to those above with  $P_{L}$  being the strongest control on  $F_{w10,Q}$  (figure S6).

The variability in daily young water fraction in evaporation  $F_{wy,E}$  is driven to a lesser degree by liquid water input  $P_{\rm L}$  ( $R^2 = 0.07$ ;  $\psi \sim 3 \cdot 10^{-3}$ ), but is more dependent on soil moisture  $S_u$  ( $R^2 = 0.21$ ,  $\psi \sim 10^{-3}$ ; figure 5). Aggregating the history of water input and release over the past weeks, Su captures the interaction between water supply and atmospheric water demand. However, with increasing averaging timescale the strength of  $S_u$  as driver gradually reduces to  $R^2 < 0.01 ~(\psi \sim 10^{-5})$ . Instead, E exhibits the strongest relation with  $F_{wy,E}$  at seasonal scale, with  $P_L$ emerging as dominant control on  $F_{wy,E}$  at the decadal time-scale ( $R^2 = 0.60$ ;  $\psi \sim 0.01$ ). This switch from  $S_{\rm u}$  over E to  $P_{\rm L}$  as dominant control illustrates that the history of water supply and release interactions in S<sub>u</sub> preserves merely the system's memory of the past few weeks. At time-scales longer than that, the water fluxes released from the system become better predictors, while over decadal time-scales variations in water supply, expressed as  $P_{\rm L}$ , control fluctuations in  $F_{wy,E}$ . It can also be observed that at seasonal time-scale,  $F_{wy,E}$  is more sensitive to  $P_L$  and E in winter than in summer (figure 5). For  $P_L$ , this difference is explained by the higher sensitivity of  $F_{wy,E}$ to winter snow melt (figure 4(c)) than to summer rainfall (figure 4(g)), similar to  $F_{wy,Q}$ . Low evaporation due to low temperatures together with little input of new liquid water during periods with snow cover cause water to remain in S<sub>u</sub> longer, resulting in older ages during such periods (and thus lower  $F_{wy,E}$ ). With higher temperatures, snow melt and thus input of young water increases, accompanied by higher evaporation rates, that lead to quicker removal of water from  $S_{\rm u}$ . This younger water that is evaporated at higher rates then leads to a faster turnover of water in  $S_{\rm u}$  and thus to a distinct switch ( $\psi \sim 0.11$ ) towards a younger water pool from which evaporation is sourced and the markedly higher  $F_{wy,E}$  (figure 5). Due



**Figure 6.** The differences of variability of the young water fractions in river flow ( $F_{wy,Q}$ , (a)–(f)) and evaporation ( $F_{wy,E}$ , (g)–(l)) over multi-decades for each time scale (from lighter to darker for daily to decadal). Note that the relatively darker and lighter colour shades in (d) and (j) indicate the  $F_{wy}$  in summer (May–October) and winter months (November–April), respectively.



 $\epsilon = 0.32$  in the estimated water ages at decadal time-scale. Briefly, an elasticity of  $\epsilon = 1$  implies that a 1% increase in  $F_{yw,Q}$  (i.e.  $\Delta F_{wy,Q}/F_{wy,Q} = 0.01$ ) follows from a 1% increase in  $P_L$  (i.e.  $\Delta P_L/P_L = 0.01$ ). In contrast, for example  $\epsilon = 0.32$  implies a 0.32% increase in  $F_{yw,Q}$  (i.e.  $\Delta F_{wy,Q}/F_{wy,Q} = 0.0032$ ) in response to a 1% increase in  $P_L$ . At daily ( $\epsilon \leq \sim 1.5$ ) to seasonal ( $\epsilon \leq \sim 0.5$ ) time-scales, a considerable proportion of liquid water inputs resulted in higher elasticities  $\epsilon$  than at decadal time scales ( $\epsilon \leq 0.32$ ), i.e. the grey dots that plot on the right side of the dashed grey line in (a)–(e).

to the absence of snow, the fluctuation in summer  $F_{\rm wy,E}$  is more gradual, as evident by its lower sensitivity to E ( $\psi \sim 0.03$ ). The controls on  $F_{\rm w10,E}$  are comparable to those of  $F_{\rm wy,E}$  (figure S7).

## 4.3. Temporal evolution and long-term dynamics of water ages

Over the seven study decades, remarkably stable water ages can be observed (figure 6). As a consequence of the above, the fluctuations of average riverflow water ages between the individual decades are very minor. The same is true for the inter-decadal variabilities around these average water ages, for which merely some limited changes in the extremes can be observed (e.g. figure 6(c)). In spite of higher absolute sensitivities to hydro-climatic variability at decadal  $(\psi \sim 0.07)$  than at daily time-scales  $(\psi \sim 0.03)$ , the relative sensitivities or elasticities of  $F_{wy,Q}$  to  $P_L$ , expressed by  $\epsilon = \psi \cdot (P_{\rm L}/F_{\rm wy,Q})$ , were for wide parts of the  $P_{\rm L}$ - $F_{\rm wy,Q}$  space much lower at the decadal time-scale ( $\epsilon \leq \sim 0.32$ ) than at the daily time-scale ( $\epsilon \leq \sim 1.5$ ; figure 7). This implies that while average inter-decadal  $P_{\rm L}$  varied by ~650–803 mm yr<sup>-1</sup> and

thus by ~20%,  $F_{\rm wy,Q}$  varied between 0.45–0.47 and thus by only ~4%. For evaporation  $F_{\rm wy,E}$  it was found that  $\epsilon \sim 0.11$ , which entails that the 20% fluctuation in  $P_{\rm L}$  as dominant control led to a  $F_{\rm wy,E}$  fluctuation of merely ~2%, making average  $F_{\rm wy,E}$  similarly stable throughout the study period, (figures 6(g)–(i)).

#### 4.4. Implications

The general magnitudes of  $F_{wy,Q}$  and  $F_{wy,E}$  from this study are broadly consistent with previous studies (von Freyberg *et al* 2018, Asenjan and Danesh-Yazdi 2020, Ceperley *et al* 2020). Our results also qualitatively correspond with previous studies that report reductions in water age variability for timescales from daily to yearly (Wilusz *et al* 2017) and up to 8 years (Stockinger and Stumpp 2024).

As first study to analyse water ages over multiple decades we have found no evidence for pronounced non-self-averaging behaviour. The limited fluctuation of decadal  $F_{wy,Q}$  and  $F_{wy,E}$  in response to the  $\sim$ 20% variation in  $P_L$  and significant 10% increase in  $E_P$  over the 70 year study period suggests that the study basin buffers water ages against long-term

hydro-climatic variability so that water ages and the associated conservative physical transport processes do not exhibit major long-term dynamics and can thus be assumed near-stationary at decadal timescales with limited 'external transport variability' (Kim et al 2016). Wang et al (2024) have shown that vegetation adaptation to inter-decadal hydroclimatic variability in the study basin led to fluctuations in root-zone storage capacities, represented by parameter S<sub>u,max</sub> in our model. In spite of accounting for the fluctuations of this catchment subsurface property in our analysis  $F_{wy,Q}$  and  $F_{wy,E}$  remained remarkably insensitive to these changes. This therefore also indicates limited 'internal transport variability', which is consistent with the very minor changes to  $F_{\rm wy,Q}$  from 0.12 to 0.13 as a result of deforestation that led to a >50% reduction in  $S_{u,max}$  in a nearby catchment (Hrachowitz et al 2021).

The self-averaging and temporally stable water ages contrast with the fractal scaling and non-selfaveraging behaviour that is frequently observed in dynamics of river water tracer and solute concentrations and that indicates the potential presence of long-term fluctuations or trends in solute circulation dynamics. In spite of several sources of uncertainty in the modelling process (Beven 2016), our findings that water ages are near-stationary suggest that long-term solute dynamics as manifest by their fractal scaling in many river basins are unlikely to arise from changes in conservative transport processes. Instead, longterm solute dynamics may emerge as an inherent consequence of anomalous transport and the associated heavy-tails of TTDs (Dentz et al 2023) in combination with other potential factors such as long-term changes in solute supply and/or mobilization. The latter may include variations in solute input (e.g. fertilizer application, solute concentration in precipitation) but also alterations of (bio-) geochemical transformation processes due to changing ambient conditions, such as temperature or soil water content that regulate for example mineral dissolution kinetics in the subsurface (e.g. Maher 2011, Li et al 2017) but also plant nutrient uptake (e.g. Marschner and Rengel 2023).

It can be expected that water ages may be more sensitive to hydro-climatic variability in catchments which are characterized by younger water, i.e. higher  $F_{yw,Q}$ , and thus faster physical transport processes. However, it is plausible to assume that physical transport processes in river basins with similar water age structure (Koeniger *et al* 2005, Stewart *et al* 2010, Visser *et al* 2019, Birkel *et al* 2020) may exhibit similarly low elasticity to hydro-climatic variability and thus only limited long-term dynamics.

Overall, there are two wider implications following from the results of this study. Firstly, predictions of future solute dynamics in riverflow over longtime scales may be more robust than the frequently observed fractal scaling in river solute concentrations may suggest if estimated based on water ages instead of on the solute time series themselves. Secondly, the low elasticity of water ages to variability in water supply and the resulting long-term stability of physical transport processes poses practical limits for mitigation and remediation measures of legacy contamination such as nitrate (Basu *et al* 2022) that may aim to alter not only reactive processes but also physical transport characteristics by interventions such as wetland restoration or land management.

To further improve accuracy of estimated water ages and their long-term dynamics, additional tracers that allow age tracing of older water, such as CFCs and SF6 (Stewart *et al* 2007, Molénat *et al* 2013, Solomon *et al* 2015), may prove valuable for future studies.

#### **5.** Conclusions

Based on hydro-climatic records and <sup>3</sup>H data we have analysed the variability of water ages, described by the fraction of young water in riverflow ( $F_{yw,Q}$ ) and evaporation ( $F_{yw,E}$ ), at daily to decadal time-scales in the Upper Neckar Basin, Germany over the 70 year period 1953–2022. The main findings of our study are the following:

- (1) Riverflow is, on average, with  $F_{wy,Q} \sim 0.4$  characterized by considerably older water than evaporation with  $F_{wy,E} > 0.95$  across all time-scales.
- (2) The variabilities of both,  $F_{wy,Q}$  and  $F_{wy,E}$  systematically decreases with increasing averaging timescale: decadal average  $F_{yw,Q}$  fluctuates merely between 0.45–0.47 and  $F_{wy,E}$  between 0.96–0.97 between individual decades. This indicates that  $F_{wy,Q}$  and  $F_{wy,E}$  can be considered near-stationary across several decades. These results therefore provide no evidence to support the hypothesis that  $F_{wy,Q}$  and  $F_{wy,E}$  are non-self-averaging and unpredictable.
- (3) Liquid water input  $P_L$  is the dominant driver of  $F_{wy,Q}$  across all time-scales. In contrast,  $F_{wy,E}$ is characterized by varying drivers: while soil moisture is the dominant control at daily timescale, this switches to liquid water input  $P_L$  at the decadal time-scale. Thus the hypothesis that the dominant controls on  $F_{yw}$  vary across different time-scales can only be rejected for  $F_{wy,Q}$ .
- (4) Average water ages were rather stable and subject to minor fluctuations over time. In response to a 20% fluctuation in decadal  $P_{\rm L}$ ,  $F_{\rm wy,Q}$  varied only by ~4% and  $F_{\rm wy,E}$  by ~1% over the study period. The hypothesis that water ages are subject to major long-term dynamics on decadal time scales in the study basin was therefore rejected.
- (5) Overall, as first study to systematically analyse water ages over multiple decades, it demonstrates that there is no evidence for non-selfaveraging and unpredictable behaviour in water

ages. Instead long-term average water ages were rather stable and subject to merely minor fluctuations in the Upper Neckar basin. Consequently, and in spite of hydro-climatic variablity, the associated physical transport processes can be assumed to be near-stationary across multiple decades.

#### Data availability statement

All data that support the findings of this study are included within the article (and any supplementary files).

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#### ORCID iDs

Siyuan Wang <sup>®</sup> https://orcid.org/0000-0002-9639-9241

Markus Hrachowitz () https://orcid.org/0000-0003-0508-1017

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