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## SHEAR TESTS ON LARGE PRESTRESSED CONCRETE T-BEAMS

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### ABSTRACT

The experimental results of shear tests on two prefabricated large prestressed concrete T-beams are presented and discussed. The beams were used in previous experiments after which they remained undamaged. The beams are a 1:2 scale model of the approach bridge of the Van Brienenoord bridge in Rotterdam (the Netherlands). However, the reinforcement and prestressing is not an exact scale of the real bridge beams and was designed with requirements of the previous experiments and can be considered as over dimensioned.

The beams have a length of 12 m and a depth of 1.3 m. The depth can be considered quite high for laboratory tests especially in terms of the equipment needed to load the beam until failure. Also, when considering a 1:1 scale structure, a beam with this depth could easily have a span of 30 m. Empty ducts in the top flange, used in the previous experiments for transverse prestressing, are filled with high strength cement mortar to prevent a premature flexural failure of the compression zone (crushing).

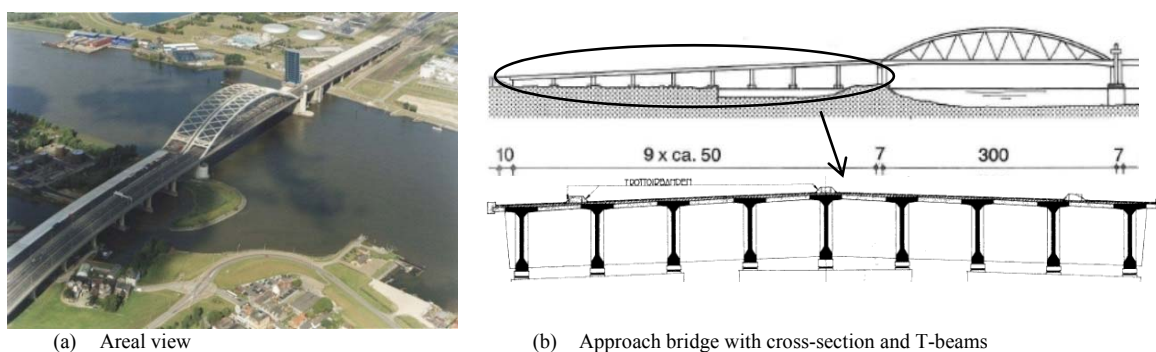
The four shear tests consist of a single point load at a distance of  $2.1d$  from the support. In previous tests a distance of  $2.7d$  was used resulting in a close to shear but ultimately flexural type of failure (Ensink 2015). However, in the previous tests the flexural type of failure was also triggered by the empty ducts.

Finally, the results of the shear tests are compared to non-linear 3D finite element analysis and Eurocode design formula using real material properties.

**Keywords:** prestressed concrete, T-beam, bridge girder, shear, non-linear analysis, Eurocode.

### 1. Introduction

The cross-section of the T-beams are a 1:2 scale model of the approach bridge of the Van Brienenoord bridge in Rotterdam (the Netherlands), see Fig. 1. The reinforcement and prestressing was designed with requirements of a previous experiment. This previous experiment consisted of four T-beams with cast in between slabs, transverse end beams and transverse prestressing (Amir 2014). The ultimate limit state behaviour of the slabs in between the beams was the aim of this previous experiment so the beams were over dimensioned. After these experiments, it was decided to carry out shear tests on the beams themselves as part of the ongoing research in the field of existing structures at the concrete structures section at TU Delft.

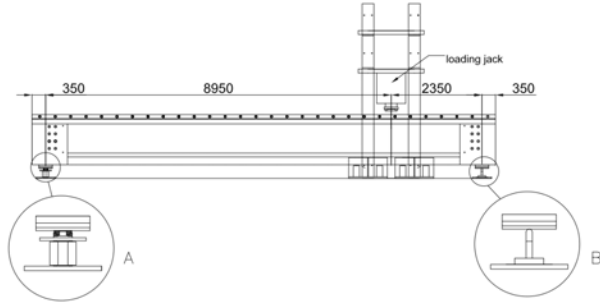


**Fig. 1.** Van Brienenoord bridge Rotterdam

The self-compacting concrete type is C53/65. However, at the time of the shear tests the actual mean cube compressive strength was  $f_{cm,cube} = 89.8 \text{ N/mm}^2$  ( $f_{cm} = 0.85 \cdot f_{cm,cube} \approx 77 \text{ N/mm}^2$ ) and the mean tensile strength, taken from splitting tests, was  $f_{ctm} = 0.9 \cdot f_{ctm,sp} = 0.9 \cdot 6.30 = 5.7 \text{ N/mm}^2$ . Steel reinforcement (stirrups  $\phi 10$ ) was removed and tested after the experiments resulting in a mean yielding strength of  $f_{yk} = 547 \text{ N/mm}^2$  and an ultimate strength of  $f_{tk} = 635 \text{ N/mm}^2$ . The total prestressing force is  $F_p = 4096 \text{ kN}$  resulting in an average compressive concrete stress of  $\sigma_c = 12.0 \text{ N/mm}^2$  (beam 301) and  $\sigma_c = 11.5 \text{ N/mm}^2$  (beam 401). Additional data regarding material properties is presented in Ensink, van der Veen & de Boer 2015.

### 3. Experimental setup

In the shear tests the center of the loading jack is positioned at a distance of 2350 mm from the center of the support (2.1d) see Fig. 4 and 5. The dimensions of the loading plate are 250·250 mm whereas the dimensions of the support plates are 350·280 mm (support type A/B). Therefore the width of the support plate is equal to the thickness of the beam at the end block. In order to prevent excessive rotation or horizontal movement during testing a support frame is positioned at the supports with rollers close to the top flange, see Fig. 7.



**Fig. 4.** Position of the load and supports



**Fig. 5.** Overview of test setup (first test beam 301)

Each beam is tested at both ends. After the first test of a beam, although now heavily damaged, the prestressing still prevents a complete fracture of the beam. To resist the forces of the second test the damaged area is outfitted with a support frame consisting of steel beams and vertical prestressing, see Fig. 6.



**Fig. 6.** Support frame with vertical prestressing



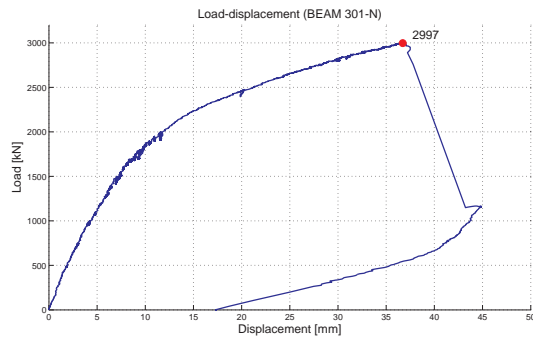
**Fig. 7.** Horizontal support at end of beam

During testing the measurements include displacements at the position of the load and at the supports on both sides of the beam using laser sensors, the reaction forces at the supports using load cells and the force and displacement of the loading jack. The loading jack is displacement controlled and paused during the experiment at fixed load levels to record the crack development, take photographs and measure the crack width. In addition the fracture is filmed by cameras.

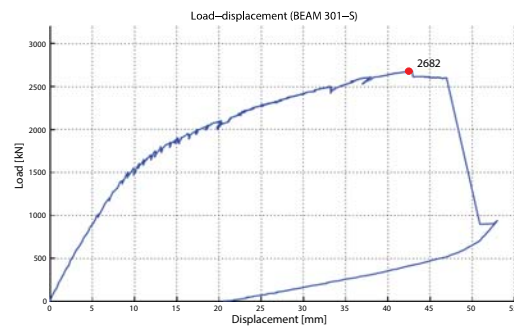
### 4. Test results

#### 4.1 Beam 301

Fig. 8 shows the load versus displacement of the tests on beam 301. The failure load is 2997 kN in the first test and 2682 kN in the second test (average of 2840 kN). The difference is therefore 12%.



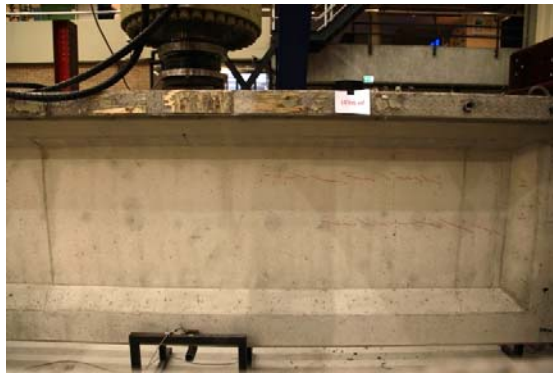
(a) North side (first test)



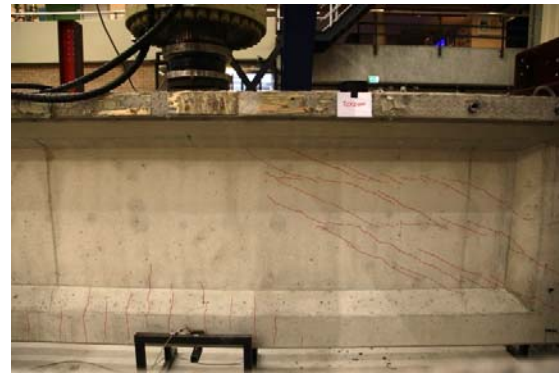
(b) South side (second test)

**Fig. 8.** Load-displacement beam 301

The crack development of the first test is shown in Fig. 9. The cracking starts with horizontal cracks in the web at a load of 1500 kN. Next inclined shear cracks occur at a load of 1700 kN followed shortly by bending cracks at a load of 1750 kN. Both shear and bending cracks continue to expand and grow until failure. The crack development of the second test is consistent with the first test and shows a similar crack pattern. However, in the second test inclined shear cracks occur at a load of 1550 kN.



(a) 1500 kN



(b) 2000 kN

**Fig. 9.** Crack development beam 301 (first test)

The fracture of the beam is shown in Fig. 10. During failure several transverse cracks occurred in the top flange near the end block, see Fig. 10b. Because of the filling of the empty ducts almost no crushing of the top flange underneath the loading jack is observed. The fracture of the second test is consistent with the first test. The minimal shear crack angle in both tests is about  $25^\circ$ .



(a) side view



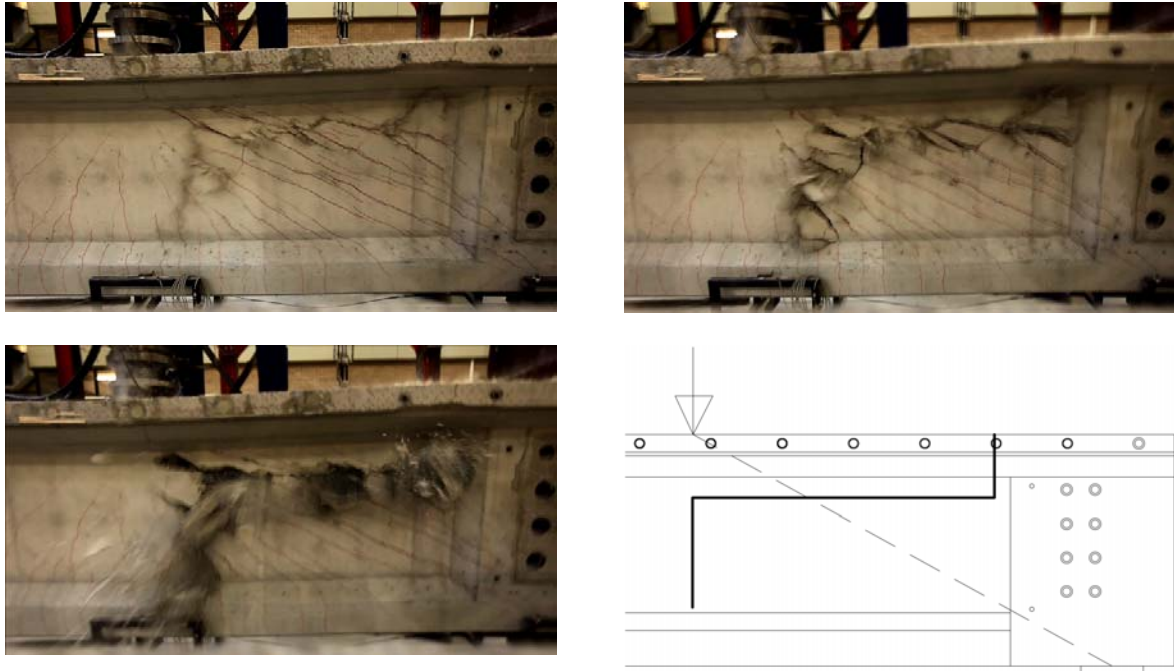
(b) top view

**Fig. 10.** Failure of beam 301 (first test)

On the slow-motion video at failure, both tests show a large horizontal crack in the web between the load and the end block near the top flange with explosive spalling of the concrete cover, see Fig. 11 which also



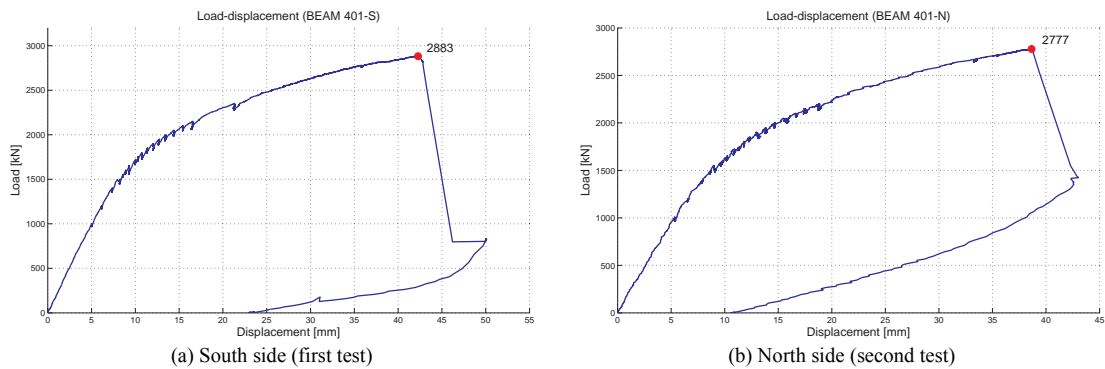
shows the schematized fracture line. At failure the beam basically splits into two parts with only the bottom flange, containing much of the prestressing, still intact. The failure is initiated by the horizontal shear crack between the top flange and the web.



**Fig. 11.** Fracture from slow-motion video and fracture line at failure (bottom right)

#### 4.2 Beam 401

Fig. 12 shows the load versus displacement of the tests on beam 401. The failure load is 2883 kN in the first test and 2777 kN in the second test (average of 2830 kN). The difference is therefore 4%.



**Fig. 12.** Load-displacement beam 401

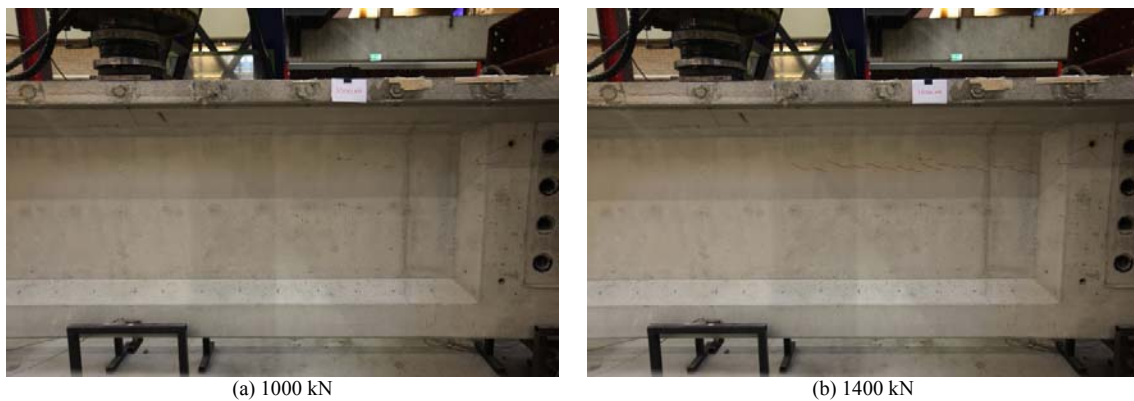
The crack development of the first test is shown in Fig. 13 showing the narrow flange side of the beam. Contrary to beam type 301 tests no horizontal cracks are observed. The cracking starts at a load of 1500 kN with a single inclined shear crack. Shear cracking continues until a load of 1850 kN when the first bending crack is visible. Both shear and bending cracks continue to expand and grow until failure.

The second test starts with a horizontal crack at an unusual low load of 1400 kN. Also, already at a load of 1000 kN small horizontal cracks are observed, see Fig. 14 left. After this initial cracking stage the shear and bending cracks start at similar load levels compared to the first test until failure.

In both tests on the non-symmetric beam type 401, contrary to previous tests at 2.7d, no rotation of the cross-section or horizontal deflection was observed during testing. Also, both sides of the beam show similar cracking. In the previous tests at 2.7d the rotation was caused by the non-symmetric cross-section.



**Fig. 13.** Crack development beam 401 (first test) narrow flange side



**Fig. 14.** Crack initiation beam 401 (second test) narrow flange side

The fracture of the beam is shown in Fig. 15. Similar to the beam type 301 during failure several transverse cracks occurred in the top flange near the end block, see Fig. 15b. Because of the filling of the empty ducts almost no crushing of the top flange underneath the loading jack is observed. The fracture of the second test is consistent with the first test. On the slow-motion video at failure, both tests again show a large horizontal crack in the web between the load and the end block near the top flange with explosive spalling of the concrete cover (see also Fig. 11). The minimal shear crack angle in both tests is about  $26^\circ$ .

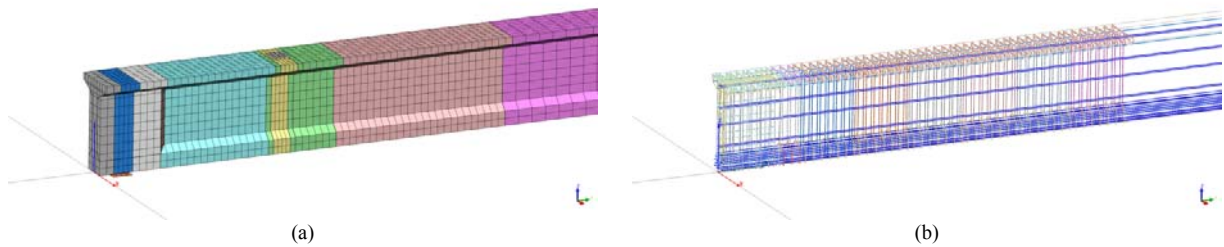


**Fig. 15.** Failure of beam 401 (first test)

## 5. Finite element analysis

The previous four shear tests, at  $2.7d$ , were part of an international shear contest held at the university of Parma in 2014 (Ensink, van der Veen & de Boer 2015). In this contest predictions were made using finite element analysis with different software packages and the participants were asked to make use of the “Guidelines for Nonlinear Finite Element Analysis of Concrete Girders” (Rijkswaterstaat 2012).

This section describes a refined non-linear analysis of beam 301, now at  $2.1d$ , using DIANA (DIANA 2014) and following the same ‘best practices’ from this guideline. Fig. 16a shows part of the 3D FEM model including the load and support plates. The stirrups, splitting reinforcement, longitudinal reinforcement and prestressing tendons are all modelled using embedded reinforcement with full bond, see Fig. 16b. Since the empty ducts close to the load were filled with cement mortar and the remaining empty ducts are of less importance they are not included in the model. In all cases linear elements are used.



**Fig. 16.** FEM model beam 301 mesh (a) embedded reinforcement (b)

For the concrete a total strain rotating crack model and non-linear Hordijk tension softening is used. Furthermore, the material model uses a parabolic compression diagram and the influence of lateral cracking (tension-compression) is taken into account. Also a constant Poisson’s ratio, i.e. no decrease with cracking, is used. The steel reinforcement and the tendons both use an elasto-plastic stress-strain diagram with strain hardening. The main physical properties used in the FEM calculation are given in Table 1.

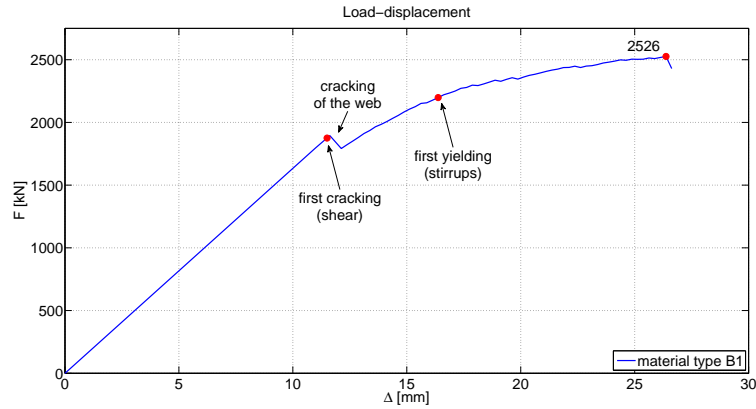
**Table 1.** FEM material properties

<b>Concrete</b>			
mean compressive strength	$f_{cm}$	77	N/mm <sup>2</sup>
mean tensile strength <sup>1)</sup>	$f_{ctm}$	5.67	N/mm <sup>2</sup>
fracture energy	$G_f$	0.1565	Nmm/mm <sup>2</sup>
compressive fracture energy	$G_c$	38.55	Nmm/mm <sup>2</sup>
Poisson’s ratio	$\nu$	0.15	-
Young’s modulus <sup>2)</sup>	$E_c$	34475	N/mm <sup>2</sup>
<b>Steel reinforcement</b>			
assumed mean yielding strength <sup>3)</sup>	$f_{ym}$	540	N/mm <sup>2</sup>
assumed ultimate tensile strength <sup>3)</sup>	$f_{tk}$	620	N/mm <sup>2</sup>
Poisson’s ratio	$\nu$	0.3	-
Young’s modulus	$E_s$	200000	N/mm <sup>2</sup>
ultimate strain	$\epsilon_{uk}$	5.0	%
<b>Prestressing steel</b>			
assumed 0.1% proof stress <sup>3)</sup>	$f_{p0.1k}$	1655	N/mm <sup>2</sup>
assumed ultimate tensile strength <sup>3)</sup>	$f_{pk}$	1953	N/mm <sup>2</sup>
Poisson’s ratio	$\nu$	0.3	-
Young’s modulus	$E_p$	195000	N/mm <sup>2</sup>
ultimate strain	$\epsilon_{uk}$	3.5	%
<sup>1)</sup> $f_{ctm} = 0.9 \times 6.30 = 5.67$ N/mm <sup>2</sup> (average from splitting tests at age of 273 days)			
<sup>2)</sup> reduced with a reduction factor equal to 0.85 to account for initial cracking due to creep, shrinkage etc. according to guideline (Rijkswaterstaat 2012)			
<sup>3)</sup> based on past experimental results			

The load-displacement curve is given in Fig. 17. The calculated failure load is 2526 kN which is 84-94% of the experimental failure loads. In general using a rotating crack model results in a lower limit failure

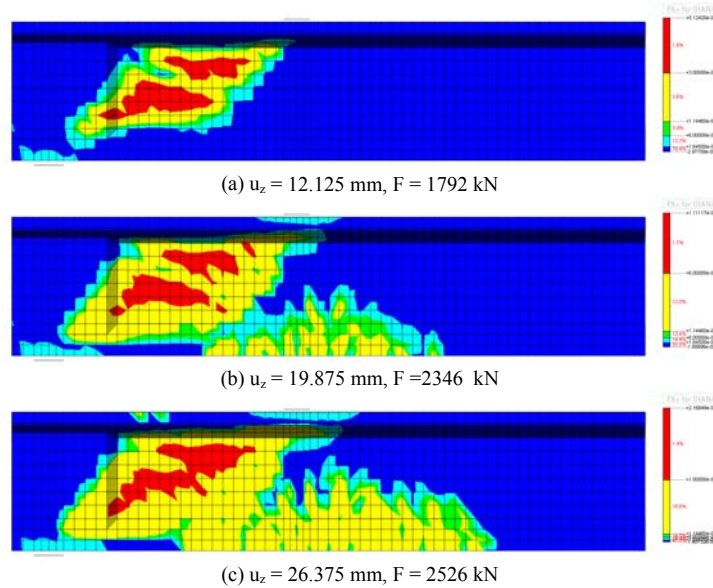


load as compared to a fixed crack model (Rots 1988). Also, it is important that predictions using finite element analysis are on the ‘safe side’.



**Fig. 17.** Load-displacement non-linear analysis (beam 301)

In the analysis yielding of the prestress tendons or longitudinal reinforcement does not occur, the beam fails in shear with yielding of the stirrups. The principal total strain at three load levels is plotted in Fig. 18. The yellow/red parts indicate fully open cracks, the cyan/green parts indicate partially open cracks and the dark blue indicate the uncracked parts.



**Fig. 18.** Principal total strain (beam 301)

The crack pattern from the non-linear analysis is in good agreement with the experiments, showing large shear and bending cracks as well as horizontal transverse cracks in the top flange near the end block (see Fig. 18c top left).

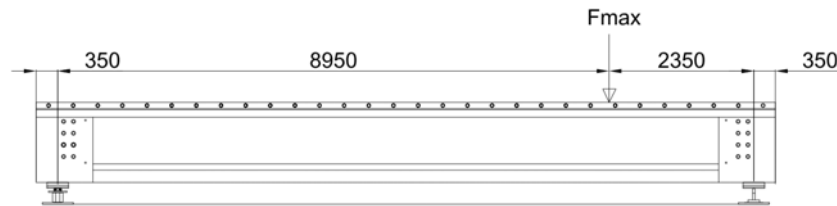
## 6. Eurocode design formula

The shear strength of beam 301 is calculated according to NEN-EN 1992-1-1 using the mean value for the concrete compressive strength ( $f_{cd} = f_{cm} = 77 \text{ N/mm}^2$ ) and the mean ultimate tensile strength of the shear reinforcement ( $f_{ywd} = f_{tk} = 635 \text{ N/mm}^2$ ). The average compressive stress is:  $\sigma_{cp} (t = 640 \text{ days}) = 11.95 \text{ N/mm}^2$  therefore  $\alpha_{cw} = 1 + 11.95/77 = 1.16$ . The effective depth of the cross-section is taken as  $d = 1095 \text{ mm}$ . For the angle of the compression strut, the most favourable value is taken for which the resistance of the stirrups equals the resistance of the compression strut, i.e.  $\theta = 23.39^\circ$ .

Resistance of the shear reinforcement (formula (6.8)):

$$V_{Rd,s} = \frac{A_{sw}}{s} z f_{ywd} \cot \theta = \frac{157}{114.3} \cdot 0.9 \cdot 1095 \cdot 635 \cdot \cot 23.39 \cdot 10^{-3} = 1989 \text{ kN} \quad (1)$$

Although the load is relatively close to the support, reducing the shear force with  $\beta$  is not allowed since condition (6.19) of NEN-EN 1992-1-1 is not met (insufficient shear reinforcement). The shear resistance of 1989 kN, reduced with the shear force of the dead weight (51 kN), translates into an applied maximum load at 2.35 m from the support of approximately (see also Fig. 19):  $F_{max} = (1989 - 51) \cdot 11.3 / 8.95 = 2447$  kN. This is approximately 82-91% of the failure load.



**Fig. 19.** Load at position 2.1d (2350 mm)

## 7. Conclusions

1. All four test showed a clear shear type of failure with a large horizontal crack in the web near the top flange indicating that the stirrups have failed.
2. Behaviour beam 301 versus 401 (symmetric versus non-symmetric)  
Comparing the results of beam 301 with 401 does not reveal any significant difference in behaviour or ultimate failure load. Contrary to previous tests at 2.7d no rotation of the cross-section was observed.
3. Behaviour experiment versus NLFEA  
The overall load-deflection curve, the failure mode as well as the crack pattern from the experiments is in good agreement with the refined 3D non-linear analysis. Also, the local transverse cracks in the top flange near the end block are correctly captured. The failure load itself is somewhat underestimated (84-94%) possibly as a result of a rotating crack model. However, using the guideline for non-linear analysis the failure load is on the 'safe side'.
4. Behaviour experiment versus Eurocode 2  
When using an optimal angle for the compression strut and the actual material properties, the shear resistance calculated with Eurocode 2 translates into a maximum load of approximately 82-91% compared to the experiments.

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