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DOI 10.1016/j.watres.2015.10.021

Publication date 2016 **Document Version** Accepted author manuscript

Published in Water Research

Citation (APA) Post, J. A. B., Pothof, I. W. M., Dirksen, J., Baars, E. J., Langeveld, J. G., & Clemens, F. H. L. R. (2016). Monitoring and statistical modelling of sedimentation in gully pots. Water Research, 88, 245-256. https://doi.org/10.1016/j.watres.2015.10.021

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# Monitoring and statistical modelling of sedimentation in gully pots

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- 9 Abstract

10 Gully pots are essential assets designed to relief the downstream system by trapping solids and 11 attached pollutants suspended in runoff. This study applied a methodology to develop a quantitative gully pot sedimentation and blockage model. To this end, sediment bed level time series from 300 12 gully pots, spanning 15 months, were collected. A generalised linear mixed modelling (GLMM) 13 14 approach was applied to model and quantify the accumulation of solids in gully pots and to identify 15 relevant physical and catchment properties that influence the complex trapping processes. Results 16 show that the retaining efficiency decreases as sediment bed levels increase. Two typical silting 17 evolutions were identified. Approximately 5% of all gully pots experienced progressive silting, 18 eventually resulting in a blockage. The other gully pots show stabilising sediment bed levels. The depth of the sand trap, elapsed time since cleaning and the road type were identified to be the main 19 properties discriminating progressive accumulation from stabilising sediment bed levels. 20 21 Furthermore, sediment bed levels exhibit no residual spatial correlation, indicating that the 22 vulnerability to a blockage is reduced as adjacent gully pots provide a form of redundancy. The

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- 23 findings may aid to improve maintenance strategies in order to safeguard the performance of gully
- 24 pots.
- 25 Keywords: sediment accumulation; gully pot blockage; Bayesian inference; generalised linear mixed
- 26 modelling

# 27 Nomenclature

- 28 t observation number
- 29 *i* gully pot identity
- 30 *p* the probability of 'success'
- 31  $\varepsilon$  random part of the generalised linear model
- 32  $\eta$  Linear predictor containing the deterministic part of the generalised linear model
- 33 *d* available sump depth
- 34 *y* measured sediment bed level
- 35 v normalised sediment bed level with respect to the sump depth
- 36 *x* quantitative explanatory variable
- 37  $\beta$  model weight assigned to explanatory variable x
- 38  $\phi$  autocorrelation strength
- 39  $\omega$  noise term
- 40 *a* shape parameter for the beta distribution
- 41 *b* shape parameter for the beta distribution
- 42  $\theta$  over-dispersion parameter
- 43 z row incidence vector for the random effects

# 44 **1** Introduction

45 Street inlets are essential sewer assets responsible for collecting and conveying excess water from

the urban surface. These structures are commonly designed as gully pots, referring to the presence

47 of a sand trap. By capturing suspended particles in runoff, silting and wear of downstream sewer 48 components are reduced. In addition, the impact on the pollutant wash-off to the sewer system is 49 considerable (Ashley et al. 2004, Butler et al. 1995). Therefore, gully pots decrease the pollution load 50 to receiving water bodies, especially for storm sewers. Depending on the retaining efficiency of the 51 sand trap, the supply of solids induces progressive silting over time. When the trap capacity of is 52 exceeded, the hydraulic performance of the gully pot is impaired. In the absence of alternative flow 53 routes, water will pond and spread over adjacent areas causing potential health risks (De Man et al. 54 2014, Ten Veldhuis et al. 2010) and tangible damage (Arthur et al. 2009). The role of gully pot blockages as main contributor to sewer flooding events has been recognised by several studies (e.g. 55 56 Ten Veldhuis et al. (2011) and Caradot et al. (2011)).

57 Unlike most sewer system components, gully pots are generally maintained with a proactive preventive approach (Butler and Davies 2004, Karlsson and Viklander 2008). It comprises of cleaning 58 59 activities that are undertaken after a fixed period of time. Currently, the cleaning frequency is based 60 on either the available budget (Fenner 2000), expert judgment, or vulnerability of the urban environment. The effectiveness of this type of management depends on the number of a blockages 61 62 in a system within the specified interval (Swanson 2001). Yet, authorities lack quantitative data to 63 support observed blockages. If data on the operational condition of gully pots are utilised to 64 determine the maintenance interval, it is possible to balance the effectiveness of strategies and the 65 associated resources to provide cost-effective service provision.

Adopting a condition-based approach for maintenance requires prediction tools and field data (Van Riel et al. 2014). Prediction models for solids transport in gully pots are described by e.g. Fulcher (1994) Butler and Karunaratne (1995) and Deletic et al. (2000). These models are based on dense time series with a duration varying from one to several storm events or artificial events for a limited (1 - 60) number of gully pots. Although this duration is adequate to simulate transport processes during individual events, the characteristic time scale of the solids induced blockage process in gully

3

72 pots calls for time series covering a period of at least one year. Considering the complex transport processes and the corresponding parameter uncertainty, Rodríguez et al. (2012) and Pratt et al. 73 (1987) opted for a probabilistic approach. This study modelled the long term accumulation of solids 74 75 that leads to blockages by applying a generalised linear mixed modelling (GLMM) approach to time 76 series of multiple gully pots. This approach allows for the identification of catchment and physical 77 properties of gully pots that affect the accumulation of solids. Sufficient monitoring locations are 78 essential for probabilistic modelling, as the potential correlation between successive measurements 79 over time results in less unique information. To this end, sediment bed levels of 300 gully pots were 80 measured monthly for over a year. Findings from this study may support overall maintenance 81 strategies on a system scale and improve gully pot design. Furthermore, this work complements 82 previous research on sediment accumulation and water quality aspects (e.g. Ellis and Harrop (1984), 83 Memon and Butler (2002) and Butler and Karunaratne (1995)). This paper first presents an overview 84 of literature on the relevant processes to identify the main explanatory variables that influence the 85 occurrence of gully pot blockages. Second, the collection of sediment bed level data is discussed. 86 Subsequently, a procedure for modelling is introduced and applied to these data.

# 87 2 Relevant transport processes and parameters

Various processes govern sediment accumulation. The following review identifies properties that arerelevant for modelling sedimentation in gully pots.

#### 90 2.1 Supply to gully pots

Particles present in the urban environment are predominately inorganic, comparable to sand and silt (Lager 1977, Sartor and Boyd 1972). These particles originate from different sources, such as local traffic (Deletic et al. 2000), construction activities (Ashley and Crabtree 1992), weathering of buildings (Jartun et al. 2008), animal wastes, litter, and de-icing materials (Brinkmann 1985). Particles that are transported to gully pots during storm events are generally not well removed by street

96 sweeping (Brinkmann 1985, Sartor and Boyd 1972). Material available for wash-off to gully pots may vary spatially, as the presence of potential sources is subject to local circumstances. Pratt and Adams 97 (1984) reported a relation between characteristics of the contributing area (e.g. size, drainage path 98 length) and the mean mass of the measured sediment wash-off in the field. These data did, however, 99 100 originate from the same gully pots, indicating a potential dependence between successive 101 measurements over time. In addition to spatial variation, the supply to gully pots may also vary 102 temporally. Grottker (1990b) analysed the organic content of sediment samples and found a higher 103 organic loading (5 – 10%) in autumn. Peaks in the material supply in June, autumn and after 104 snowmelt were mentioned by Pratt et al. (1987), indicating seasonal variation. On a shorter 105 timescale, flow characteristics dominate the temporal variation. Ellis and Harrop (1984) found that 106 the antecedent dry period was only weakly correlated with the sediment loading to gully pots. 107 Rainfall intensity was, however, strongly correlated. Similar results lead Pratt and Adams (1984) to 108 the conclusion that the shear force required to suspend material is limiting, rather than the 109 availability of material. The overall variation in particle loading results in models that typically calls 110 for several site specific calibration parameters (Memon and Butler 2002).

# 111 2.2 Retaining efficiency

112 The fraction of solids captured by gully pots has been studied extensively. Field studies reported retaining efficiencies ranging from 20 – 50% (Deletic et al. 2000, Pitt and Field 2004). Both Butler and 113 114 Karunaratne (1995) and Grottker (1990a) conducted lab experiments where the solids supply to gully 115 pots was varied. They found that the retaining efficiency was independent from the solids 116 concentration, which support model results from Butler and Memon (1999). Butler and Clark (1995) 117 found the build-up rate to vary between 14 – 24 mm / month for urban areas. This variation may well 118 be related to the substantial variation in grain size distributions of samples from different gully pots 119 (Jartun et al. 2008), as solids with a smaller diameter are captured less efficiently (Butler and 120 Karunaratne 1995, Lager 1977).

121 Laboratory tests by Butler and Karunaratne (1995) with varying sediment bed levels up to the level of 122 the outlet pipe of a gully pot show a marginal increase in the retaining efficiency with increasing 123 sediment depths. This is contradictory with experimental results reported by Lager (1977), who 124 found that solids removal efficiencies decreased when a threshold of 40% of the gully pot storage 125 was exceeded. The latter is supported by the increase in the retaining efficiency with an increasing cleaning frequency (Memon and Butler 2002, Mineart and Singh 2000). Field measurements from 126 127 Butler and Clark (1995) indicate that equilibrium sediment bed levels were reached at the level of the 128 outlet pipe. Conradin (1990) reported similar results for 63 gully pots monitored for 16 months; 129 sediment bed levels did not exceed the level of the outlet pipes and equilibrium depths were 130 generally reached in 6 months.

# 131 2.3 Re-suspension of sediments

132 There is a general consensus that the sedimentation rate is inversely proportional to the rainfall 133 intensity (e.g. Morrison et al. (1988), Deletic et al. (2000) and Ciccarello et al. (2012)). Depending on 134 the particle size, the jetting effect induces erosion of the gully pot sediment bed (Butler and Memon 135 1999). Sartor and Boyd (1972) applied flushing tests equivalent to heavy storms and found only 1% of 136 the sediment bed to be re-suspended. This confirms earlier results reported by Fletcher and Pratt 137 (1981), who mentioned that the majority of solids discharged from gully pots are due to a lack of 138 sedimentation rather than re-suspension. As the top layer of the sediment bed is more unstable, 139 these solids may be eroded (Pitt and Field 2004). However, bed erosion decreases substantially as 140 these particles are depleted and the bed becomes graded (Butler and Karunaratne 1995).

# 141 2.4 Summary of relevant transport parameters

A statistical approach calls for data on gully pots properties that may influence solids accumulation in a sand trap. Gully pots are subject to successive storm events over time, where sediment bed levels increase or decrease depending on the rainfall regime. As the height of the bed increases over time the trapping efficiency reduces, indicating the relevance of the gully pot sump depth as an explanatory variable. In addition, the transient trapping efficiency implies interaction terms between
the physical properties and the elapsed time since last maintenance. Catchment properties govern
both the flow rate and the supply of solids. As such, these properties are potential explanatory
variables. An overview of the explanatory variables included in the model is presented in Table 4-1.
Model residuals are potentially correlated, as the availability of particles from the urban surface
varies both spatially and temporally.

# 152 **3 Materials**

Sediment bed levels of gully pots in a residential urban area in Amsterdam, the Netherlands were been monitored. The catchment area has 10.5 ha of surfaces that contribute to the runoff into the separate sewer system.

156 Figure 3.1: Schematisation of a roadside gully pot, with the outlet pipe positioned at the back

157 A sample size of 300 gully pots was selected from the catchment with 801 gully pots to allow for valid 158 inferences given the spatial variation of the process measured. Data on the properties of gully pots in 159 the study area was inventoried prior to the measurements. This includes geometrical data describing 160 the physical properties of each gully pot (depth of the sand trap, surface area, manufacturer, 161 presence of a water seal, position of the outlet pipe with respect to the grating) and catchment 162 properties (contributing area, slope, road type). Based on the spatial distribution of the physical 163 properties of the gully pots (see Figure 3.1), a stratified sampling design was applied. This sampling 164 technique improves estimates of both the population and the sub-groups by taking a proportional 165 sample from each sub-group. Stratification distinguished between the presence of a water seal, the 166 position of the outlet pipe and the depth of the sand trap. Table 3-1 shows the frequency distribution over the different strata. 167

168 Table 3-1: Frequency distribution of the different strata

Water	Depth	sand	Posit	ion out	let pipe
seal	trap (cm	)	Back	Front	Side
No	[0 - 20]		11	23	14

	(20 - 40]	5	9	12
Yes	[0 - 20]	13	37	75
	(20 - 40]	11	21	79

169

170 The associated costs and spatial spread render continuous monitoring for this sample size impractical. Instead, an apparatus able to rapidly measure the height of the bed has been 171 172 constructed. The principle is illustrated in Figure 3.2. It consists of a punctured disk attached to a 173 shaft, with a retractable rod in the middle. The disk rests on the sediment bed, while the rod is driven 174 through until the bottom of the gully pot is reached. The rod is equipped with a sequence of marks at  $5 \cdot 10^{-3}$  m intervals enabling the operator to determine the height of the bed. Tests with repeated 175 176 measurements from the same gully pot indicate the error to be smaller than the increment of the 177 instrument scale.

178 Figure 3.2: Schematisation of the device used to measure sediment bed levels in gully pots.

179 Three weeks prior to the first measurement, all gully pots were emptied and lateral connections 180 cleaned. In addition, the hydraulic capacity of the lateral connections was tested by means of a 181 vehicle mounted sewer jetting installation capable of providing a flow of 100 l/min, equivalent to 60 mm/hr on 100 m<sup>2</sup>, assuming the design standard applied in the Netherlands (Ganzevles and Oomens 182 2008). In case of a defect, the gully pot was removed from the dataset. This excluded the influence of 183 184 external failure mechanisms not related to the sedimentation mechanism, such as collapse or 185 deformation of the geometry. Gully pots were removed from the monitoring set when more than 186 one measurement was missing, e.g. due to accessibility, or in case of signs of tampering. In addition, gully pots presumed blocked due to the accumulation of sediment during the monitoring period 187 188 were tested by means of a vehicle mounted sewer jetting installation to validate this observation. 189 The duration of the campaign was chosen to be longer than the standard preventive cleaning interval 190 of once or twice per year and to include all four seasons.

#### 191 3.1 Catchment properties

192 The contributing area and average slope for each gully pot was determined by means of the eight-193 direction flow approach described in Jenson and Domingue (1988). The digital elevation model (DEM) 194 used to deduct these flow patterns is based on high-resolution altimetry data obtained by airborne 195 laser scanning (Van der Zon 2011) and has a spatial resolution of 0.5 · 0.5 m. The vertical stochastic error for the grid is 2.5 · 10<sup>-3</sup> m. Confounding objects (e.g. cars and trees) were filtered from the DEM 196 197 and were interpolated from the surrounding data. Both Kriging with an external drift (KED) based on 198 land use and Ordinary Kriging (OK) were considered as interpolation methods. However, analysis of 199 the variogram of the regression residuals showed no substantial improvement (1.5%) of the 200 semivariance. Hence, Ordinary Kriging was applied to interpolate the DEM.

The area has two road types, being main roads and local roads (see preview photos in Figure 3.3). The former has a continuous traffic flow (2000 – 6000 vehicles/day) and a road surface consisting of asphalt pavement. The latter is characterized by brick paving (< 2000 vehicles/day) and parking lots. The area is considered to be a dense urban environment, developed as a residential area with some commercial properties concentrated around the main roads. An overview of the monitoring area is given in Figure 3.3.

207 Figure 3.3: Measurement area in Amsterdam, the Netherlands. Gully pots are marked by circles.

#### 208 4 Methods for data analysis

As the processes associated with the transport and subsequent sedimentation of solids are complex and not fully understood, deterministic storm water quality modelling is associated with various difficulties (Deletic et al. 2000, Freni et al. 2009). Moreover, a deterministic approach requires the estimation of various site specific parameters, which are subject to uncertainty (David and Matos 2002). Based on these considerations, this study applies a probabilistic approach. Sediment bed level data were analysed by applying a Generalised Linear Mixed Model (GLMM) from a Bayesian perspective. The four components that compose this model are discussed in chapter's 4.1 - 4.4. Selection of the structure of these components follows the protocol suggested by (Zuur et al. 2009), which is summarised in Figure 4.1. First, the data exploration procedure outlined in chapter 4.5 was applied. Subsequently, the random part and the distribution of the response variable were determined with the complete deterministic part including interactions between the physical properties and the elapsed time since cleaning. After validation, model selection was applied to identify relevant explanatory variables in the deterministic part.

Figure 4.1: procedure for the selection of the components of a GLMM. References to the corresponding paragraphs where the results are presented have been added.

- 224 4.1 Structure of the deterministic part
- 225 The linear predictor  $\eta$  contains the deterministic part of the model, which is a linear function of k
- 226 explanatory variables and is given by

227 
$$\eta_{t,i} = \beta_0 + \beta_1 x_{t,i,1} + \dots + \beta_k x_{t,i,k}$$
 (4.1)

- 228 where *t* represents the observation number and *i* the gully pot.  $\beta$  refers to the weights assigned to
- the respective explanatory variables *x*, summarised in Table 4-1.  $\beta_0$  is the intercept.

#### 230 Table 4-1: Explanatory variables and their characteristics

Variable	Index	Туре	Unit	Range
Depth sand trap	X1	continuous	(cm)	[9 - 44]
Catchment slope	X2	continuous	(%)	[1.3 - 4.3]
Time since cleaning	X <sub>3</sub>	continuous	(days)	[21 - 420]
Contributing area	X4	continuous	(m²)	[5 - 1380]
Cum. Rainfall depth	X5	continuous	(mm)	[115 - 1160]
Water seal	X <sub>6</sub>	categorical	-	yes / no
Position outlet pipe	X7	categorical	-	front / back
Position outlet pipe	X <sub>8</sub>	categorical	-	side / back
Road type	X <sub>9</sub>	categorical	-	main / local

232 4.2 Structure of the random part

231

The model assumption of independence is not guaranteed, as successive observations from the same gully pot can be expected to be more similar compared to observations from other gully pots. This violation of independence was resolved by extending the deterministic part  $\eta$  with a correlation structure to model inter-gully pot variation and the correlation caused by this variation. Two extensions were considered. The first candidate was a random intercept, which implies that all pairs of observations from the same subject gully pot are equally correlated (i.e. compound symmetry correlation) and defines the random part as

240 
$$\varepsilon_{t,i} = N(0,\sigma_i^2)$$
 (4.2)

Alternatively, an auto-regressive process of order 1 (AR-1) model was considered. It is a special case of the autoregressive–moving-average model family. This structure has correlations, between observations from the same gully pot, that decline exponentially with time and is given by

244 
$$\varepsilon_{t,i} = \phi \varepsilon_{t-1,i} + \omega_{t,i}$$
$$\omega_{t,i} = N(0, \sigma^2)$$
(4.3)

245 where the estimated parameter  $\phi$  is the strength of the autocorrelation and  $\omega$  the noise term.

#### 246 4.3 Distribution of the response variable

Each outcome of the response variable is assumed to be generated from a particular distribution. This study analyses the normalised sediment bed level *v*, which is defined as the sediment bed level *y* normalised with respect to the available sump depth *d*. Two distributions were considered, the first being the binomial distribution, with probability *p*, specified by

251 
$$\frac{y_{t,i} \square Binomial(p_{t,i}, d_{t,i})}{E(y_{t,i}) = p_{t,i} \cdot d_{t,i}} \operatorname{and} \operatorname{var}(y_{t,i}) = p_{t,i} \cdot d_{t,i} \cdot (1 - p_{t,i})$$
(4.4)

However, when the variation of the data is inflated compared to the theoretical expected variance according to the binomial model (i.e. over-dispersion), a more general model is required. Alternatively the response variable can be described by a beta-binomial distribution. This mixed distribution permits heterogeneity by modelling the probability of success as a beta distribution. Parameters *a* and *b* describe the beta distribution. The expected value of the beta-binomial is similar to the expected value of the binomial distribution in eq. 4.4. Yet, the variance is given by

258 
$$\operatorname{var}(y_{t,i}) = p_{t,i} \cdot d_{t,i} \cdot \left(1 - p_{t,i}\right) \cdot \left(1 + \frac{d_{t,i}}{\theta + 1}\right)$$
(4.5)

11

259 Where the parameter  $\theta = a + b$  accounts for over-dispersion. For large values of theta, the variance 260 converges to that of the binomial distribution.

#### 261 4.4 Link function

Subsequently, the link function describes the relationship between the expectation of the responsevariable and the extended deterministic part. The logistic link is such a function and is given by

264 
$$p_{t,i} = \frac{e^{\eta_{t,i} + \varepsilon_{t,i}}}{1 + e^{\eta_{t,i} + \varepsilon_{t,i}}}$$
 (4.6)

Introduced by (Berkson 1944), it approximates the inverse cumulative distribution function of the
Gaussian distribution and is able to model binomial data effectively (Hardin and Hilbe 2007).

#### 267 4.5 Data exploration and model validation

The process of exploration and validation provides information about eligible model structures and explanatory variables. Outliers may influence the statistical analysis and cause over-dispersion (Hilbe 2007). In addition, an abundance of zero measurements may result in biased parameter estimates and incorrect standard errors (Zuur et al. 2010). Graphical exploration of the explanatory variables and the response variable allowed for the identification of both zero abundances and outliers.

273 Strong collinearity between explanatory variables may result in unreliable parameter estimates, as 274 the estimates may respond erratically to small changes in the data (Zuur et al. 2013). Collinearity was 275 assessed by inspecting pair-plots and computing Variance Inflation Factors (VIF) for high-dimension 276 relations.

Following the model specification, the influence of individual observations was analysed by computing Cook's distance (Cook 1977). This statistic represents the normalised change in fitted values when one observation is removed. Pearson residuals were extracted from the model to verify the assumptions inherent to GLMM's. Homogeneity of variance was verified by graphical techniques, as statistical tests are sensitive to non-normality (Sokal and Rohlf 1995). Non-linear patterns in the

12

residuals may indicate that the model needs to be extended with quadratic terms (Zuur et al. 2013).
Mantel correlograms of the residuals were analysed to determine whether there is any inherent
spatial or temporal dependency.

## 285 4.6 Bayesian Inference

In recent years, Bayesian inference has gained an increasing amount of attention in the field of environmental engineering (e.g. Kanso et al. (2006), Liu et al. (2008), Korving et al. (2006) and Egger et al. (2013)). The Bayesian framework considers unknown parameters as random variables. The uncertainty about these parameters is expressed by the posterior density function. This approach is not hindered by the potential inaccurate penalized quasi-likelihood generally applied to GLMM's in a frequentist framework (Zhao et al. 2006). Bayes' theorem evaluates the posterior density by updating prior information when new observations are available and is given by,

293 
$$P(\boldsymbol{\beta} | \mathbf{y}) = \frac{P(\mathbf{y} | \boldsymbol{\beta}) P(\boldsymbol{\beta})}{P(\mathbf{y})} = \frac{P(\mathbf{y} | \boldsymbol{\beta}) P(\boldsymbol{\beta})}{\int P(\mathbf{y} | \boldsymbol{\beta}) P(\boldsymbol{\beta}) d\boldsymbol{\beta}}$$
(4.7)

where  $P(\beta \mid \mathbf{y})$  is the joint posterior density of parameter vector  $\boldsymbol{\beta}$  based on prior information and observations  $\mathbf{y}$  ( $y_{1,1}$ ,  $y_{1,2,...}$ ,  $y_{n,t}$ ) from *n* different gully pots on *t* occasions. The prior probability density  $P(\boldsymbol{\beta})$  represents expert information or historical observations before new data are involved. The marginal likelihood is denoted by  $P(\mathbf{y})$  and is a fixed normalising factor, scaling the sum of the posterior likelihood to one.  $P(\mathbf{y}|\boldsymbol{\beta})$  is referred to as the likelihood function, which for a binomial generalised linear mixed model can be expressed as,

300 
$$P(\mathbf{y} | \boldsymbol{\beta}, \varepsilon) = \prod_{n=1}^{N} \prod_{t=1}^{T} \begin{pmatrix} d_{n,t} \\ y_{n,t} \end{pmatrix} \left[ p_{n,t} \left( \boldsymbol{\beta}_{n,t}, \varepsilon_{n} \right) \right]^{y_{n,t}} \left[ 1 - p_{n,t} \left( \boldsymbol{\beta}_{n,t}, \varepsilon_{n} \right) \right]^{d_{n,t} - y_{n,t}}$$
(4.8)

301 where,

302 
$$p_{n,t}(\boldsymbol{\beta}_{n,t},\varepsilon) = \left[1 + e^{\mathbf{x}_{n,t}^{\mathrm{T}}\boldsymbol{\beta}_{n,t} + \mathbf{z}_{n}^{\mathrm{T}}\varepsilon}\right]^{-1}$$
 (4.9)

includes both the deterministic and random part. z is a row incidence vector for the random part.
 Non-informative priors were used for the regression parameters, representing the lack of knowledge

about the parameters. These distributions have a negligible influence on the posterior distribution. A
half-Cauchy(25) prior was used for the standard deviation parameter, as recommended by Gelman
(2006) and Marley and Wand (2010). This prior expresses the belief that the random intercepts are
concentrated close to the common intercept.

309 Integration over the denominator of eq. 4.7 is considered to be infeasible for most practical 310 applications due to high-dimensionality of  $\beta$  (Qian et al. 2003). Markov Chain Monte Carlo (MCMC) 311 algorithms do not require evaluation of the marginal likelihood, since the posterior distribution is 312 sampled directly. This study applied the Gibbs sampler (Geman and Geman 1984) as MCMC 313 algorithm. It is referred to as an alternating conditional sampler, as it samples from the conditional 314 distribution of each parameter with respect to the remaining parameters. The Gibbs sampler has 315 been found to be particular suited for multidimensional problems (Gelman et al. 2003) and is 316 implemented in the open source software JAGS (Plummer 2003), which was called from the R 317 software environment (R Core Team 2014).

Convergence of the MCMC algorithm is essential for a correct estimation of the posterior distribution for the parameters of interest. To this end, the Gelman-Rubin diagnostic (Gelman and Rubin 1992) was used. This diagnostic compares the variance of the independent Markov chains to the variance between the chains.

# 322 5 Results and discussion

4500 sediment bed level measurements spanning 15 months (Sept. 2013 – Nov. 2014) were available at the end of the monitoring campaign introduced in chapter 3. 2% of the locations were removed from the set due to missing measurements or suspected tampering. A total rainfall depth of 1160 mm was recorded. Section 5.1 presents the results of this campaign. The remainder of this chapter is dedicated to applying the procedures introduced in chapter 4. This involves applying a generalised 328 linear mixed modelling (GLMM) approach to the field data in order determine how the properties of329 gully pots affect their operational condition over time.

#### 330 5.1 Field measurements

The distribution of measured sediment bed levels for each measurement day are presented in the respective violin plots in Figure 5.1. This figure shows a main cluster, consisting of a majority of the gully pots, which experienced stable bed levels several months after cleaning. In contrast, a fraction of all measured gully pots experienced progressive accumulation, eventually resulting in a blockage. The latter group covers approximately 5% of all gully pots at the end of the campaign. Based on the measured sediment levels, gully pots in this group were distinctly separated from the main cluster.

Analysis of the median sediment bed levels over time indicates that more sediment was retained in the first weeks after cleaning, compared to subsequent measurements. Since the measurement campaign lasted more than one year the increased retention of sediments cannot be attributed to seasonal variation, as later measurements in the same season do not display similar patterns. This implies a reduction in the retaining efficiency over time, under the assumption of a stationary solids load from the urban surface. Increased skewness of the distribution over time indicates dispersion of the main cluster, characterising the long term accumulation of solids.

Figure 5.1: Box-violin plot of the measured sediment bed levels over time. The symmetrical density plot shows the distribution of sediment bed levels for each day of measurement. The box plot presents quartiles and individual points representing outliers. Vertical jitter was added to the outliers to aid visual interpretation.

#### 347 **5.2** Data exploration

Graphical exploration of the data revealed no clear signs of outliers or zero-inflation. Analysis of the Cook's distance statistic discussed in section 4.5 showed no particular influential observation. A pairplot of the normalised sediment bed levels v, and all explanatory variables is depicted in Figure 5.2. All explanatory variables were standardised to improving mixing of the MCMC chains. This pair-plot shows that the elapsed time since cleaning  $x_3$  and the cumulative rainfall depth  $x_5$  are strongly correlated, demonstrating that these variables cannot be identified separately. This is confirmed by the corresponding variance inflation factor of 64.16, which is larger than the cut-off range of 5 - 10 suggested by Montgomery and Peck (1992). Therefore it was decided to exclude the cumulative rainfall  $x_5$  as explanatory variable.

Figure 5.2: Pair-plot of the response variable and all continuous standardised (dimensionless) explanatory variables *x*. The lower left part contains pair-wise correlations, whereas the upper right part contains scatterplots with a locally weighted polynomial (LOESS) added to reveal patterns in the scatter.

360 Subsequently, the Bayesian approach presented in section 4.6 was applied to the collected sediment

361 bed data in order to determine which physical and catchment properties distinguish progressive

362 accumulation from stabilizing sediment bed levels.

#### 363 5.3 Random part and probability distribution of the response variable

364 Estimations of the relative quality of the proposed probability distributions and random parts in 365 section 4.2 - 4.3 was obtained by means of the Akaike information criterion (AIC) (Akaike 1973), which is a penalized likelihood method. Each model included the complete set of explanatory 366 367 variables and interactions for the physical properties. The AIC values given in Table 5-1 reveal that 368 the models with an autoregressive component outperform their counterparts. The binomial GLMM 369 with AR-1 correlation structure has the best relative performance. The Akaike weights (wi) in this 370 table represents the probability that this model has the best performance, given the data and the 371 other proposed models.

#### 372 Table 5-1: AIC analysis for four competing model structures

Model		AIC	<i>wi</i> AIC
Binomial with AR-1	GLMM	19416.24	1.00E+00
Binomial GL	MM	30597.16	0.00E+00
Beta-binomial GLMM with AR-1		19474.30	2.47E-13
Beta-binom GLMM	ial	20566.96	1.33E-250

<sup>373</sup> 

374 Analysis of the Pearson residuals revealed that the binomial GLMM is subject to an over-dispersion of

375 2.92. The beta-binomial GLMM allows for this extra dispersion through  $\theta$  in eq. 4.5. A comparison of

- the mean values for  $\theta$  derived from the beta-binomial GLMM with and without an AR-1 correlation
- structure,  $4.32 \cdot 10^4$  versus 20.03 respectively, demonstrates the effectiveness of this component to
- 378 capture the over-dispersion. Since  $4.32 \cdot 10^4 \square d_{r_i}$  (available sump depth), the variance of the beta-
- binomial distribution in eq. 4.5 converges to the variance of the binomial distribution.

#### 380 5.4 Deterministic structure

The optimal deterministic structure was obtained by applying backwards selection based on the 95% highest probability density interval (HPDI). None of the interaction terms for the physical properties were significant. In addition, the explanatory variables:  $x_6$  "presence of a water seal" and  $x_2$  "catchment slope" are not significant from 0 at a 5% level and were excluded from the model. Exclusion of the interaction terms implies that the effect of the physical properties on the retaining efficiency does not change as the sand trap progressively silts. Figure 5.3 presents the marginal posterior distributions of the weights  $\beta_k$  for each explanatory variable  $x_k$  of the optimal model.

Figure 5.3: Marginal posterior distributions of the weights  $\beta_k$  for each explanatory variable  $x_k$ . The horizontal line shows the 95% credible interval for 800 MCMC samples. The vertical line depicts the intersection with the y-axis, indicating whether the credible interval contains zero.

The variables  $x_8$  "position of the outflow pipe (side)" and  $x_4$  "contributing area" have the largest pvalues, 0.001 and 0.005 respectively. The deterministic component of the estimated GLMM with standardised (dimensionless) covariates and mean weight values from Figure 5.3 can be written as:

394  $\eta_{t,i} = -2.490 - 0.415 \cdot Depth_{t,i} + 0.261 \cdot Time_{t,i} + 0.084 \cdot Area_{t,i} + 0.710 \cdot PipeOut_{t,i}$  (front) + 0.503 · PipeOut\_{t,i}

395 (side) + 
$$0.481 \cdot Road_{t,i}$$
 (main)

The predicted mean values for the normalised sediment bed level *v*, without the random component, for the different levels of the categorical explanatory variables are visualised in Figure 5.4. Credible intervals provide a region that contains the mean fitted values with a 95% probability, based on the marginal posterior distribution of the explanatory variables. The positive weight for  $\beta_9$  "road type (*Main Road*)" compared to the baseline, corresponds to a higher sediment bed level for the gully pots located in main roads. Similar inferences hold for the weights  $\beta_7$  and  $\beta_8$  corresponding to the

(5.1)

side of the outlet pipe. The higher sediment bed levels for main roads are in accordance with the statements in chapter 2, which ascribe the difference to the increased solids supply associated with the traffic intensity. It is possible that the position of the outlet pipe influences the rolling motion of flows in the sump reported by Faram and Harwood (2003), which results in high velocities near the sediment–water interface.

Figure 5.4: Fitted normalised sediment bed levels v for the entire population (without the random component) based on the marginal posterior distribution of categorical explanatory variables  $x_9$  "road type" and  $x_7 - x_8$  "position of the outlet pipe", with 95% credible intervals

Memon and Butler (2002) found that the depth of the sand trap is an important parameter, having a considerable impact on the reduction of the suspended solids load to downstream sewer components. The negative weight  $\beta_9$  in eq. (5.1) corresponding to the depth of the sand trap demonstrates that in addition to improving the water quality, increasing the depth of the sand trap also reduces the probability of a blockage. Evidently, a reduction in the ability to retain sediment does not compensate for the smaller volume of the sand trap under similar solids loading conditions.

The contributing area to each gully pot  $x_4$  is positively correlated with the normalised sediment bed

417 level. Therefore it seems that, for the range of values for the contributing area in this study (5 – 1380

418 m<sup>2</sup>), the impact of a higher solids supply associated with a larger contributing area predominates the

419 scouring effect of an increased flow rate.

Figure 5.5: Model results of the Binomial GLMM with AR-1 correlation for the normalised sediment bed level *v* over time, including a prediction interval containing 95% of the observed data. Horizontal jitter was added to visualise overlaying points.

Estimated normalised sediment bed levels including the random part are presented in Figure 5.5. This figure illustrates that the proposed modelling approach is able to reproduce the dense cluster of gully pots in a near equilibrium state perceived in Figure 5.1, as well as the blocked gully pots. Figure 5.6 shows the propagation of the estimated blockage rate for the area, given the parameter uncertainty. The threshold where the monitored gully pots become susceptible to blockages was found to be 100 days.

429 Figure 5.6: The mean estimated cumulative blockage probability over time, including 95% credible intervals.

Further analysis of the model estimates for the last day of measurement is presented in Figure 5.7. The measured normalised sediment bed levels are within the 95% credible intervals for each bin, suggesting agreement between model estimates and field observations over the entire range. This confirms that the model is able to discriminate progressive accumulation from stabilizing sediment bed levels, given the estimated model parameters.

Figure 5.7: Kernel density plot of the distribution of the measured sediment bed levels for the final day of measurement, expressing the variability of the sediment bed levels over a gully pot population of 298 individuals. In addition, a histogram of the corresponding model estimate including 95% credible intervals is added.

#### 438 5.5 Model validation

439 Analysis of the model residuals is provided in Appendix B. The Mantel correlogram in Figure 5.8 440 shows that there is no significant spatial correlation present in the model residuals at distances of 441 more than 5 meters. The corresponding density graph presents the distribution of the Euclidean distances between each gully pot. This graph reveals that although there was some spatial 442 443 dependence present at small distances, this concerns only a small fraction  $(2 \cdot 10^{-4})$  of the total sample 444 of gully pots. As such, this figure demonstrates that there are no spatially correlated variables (e.g. 445 trees, local construction activities) missing in the model. The absence of a residual spatial dependence demonstrates that there are no clusters of gully pots with higher normalised sediment 446 447 bed levels. This implies that maintenance strategies can be optimised when taking into account the 448 explanatory variables  $x_k$  of the deterministic structure. Moreover, in the presence of a gully pot blockage there is no evidence of an increased blockage probability for adjacent gully pots. Therefore, 449 the vulnerability to an event is reduced, as alternative flow routes may compensate for the 450 451 occurrence of a blockage. With respect to the design of the public space, this entails that increasing 452 the gully pot density directly adds to redundancy.

457 The effectiveness of the AR-1 model to catch the temporal dependence in the residuals was 458 illustrated in Figure 5.9. This figure shows the difference between the rejected binomial GLMM with

Figure 5.8: Spatial correlation of the model residuals, including 95% confidence bounds, plotted together with the empirical density function of gully pots interdistances.

 <sup>455</sup> Figure 5.9: Autocorrelation of the rejected binomial GLMM with compound correlation and the chosen binomial GLMM
 456 with AR-1 correlation structure. 95% confidence bounds were added.

a compound correlation structure and the selected binomial GLMM with AR-1 correlation structure. The former model structure was positively autocorrelated for several orders, as successive residual values tend to persist on one side of the mean. It exhibits a slow meandering pattern, in which residuals were consistently overestimated at the start of the time series and underestimated at the end. A clear seasonal pattern was, however, not present. Furthermore, the low-lag positive autocorrelation confirms that the sampling density of the monitoring campaign was sufficient to reconstruct the long term sedimentation process in gully pots.

#### 466 **5.6 Generalisation**

The results presented in Figure 5.5 - Figure 5.7 are case specific due to the set of properties for gully pots in the study area. Under the assumption of sample representativeness, the marginal posterior distributions of the model parameters in Figure 5.3 can be generalised and applied to similar designed gully pots beyond the frame of the study area, e.g. to improve gully pot design. Results found in this study are generally consistent with the literature in Chapter 2. In addition, the proposed method for modelling sedimentation in gully pots can be applied to measurements from other study areas.

# 474 6 Conclusions

This study provides a procedure to model the long term accumulation of solids that leads to blockages. To this end, field measurements from 300 gully pots were analysed by means of a generalised linear mixed model (GLMM). Analysis of the measurements revealed a majority of the gully pots to have stable sediment bed levels after several months. However, a fraction (5%) experienced a blockage due to the progressive accumulation of sediment.

From the model results it can be concluded that the depth of the sand trap and the position of the outlet pipe are physical properties that distinguish progressive accumulation from stabilising sediment levels. The latter was believed to influence the velocity profile at the sediment-water

20

interface. The former demonstrates that requirements concerning hydraulic efficiency and pollutant retention for water quality purposes are not necessarily conflicting; both benefit from deeper sand traps. No interaction between the physical properties and the elapsed time since cleaning was found to be significant. This entails that the effect of these physical properties do not change as the sediment bed level increases. The road type and the area contributing to runoff were found to be relevant catchment properties. As the parameter estimate for the latter is positive, this indicates that the higher solids supply predominates the scouring effect associated with an increased flowrate.

The absence of residual spatial correlation indicates that there are no clusters of gully pots with higher normalised sediment bed levels. Since the blockage probability is spatially independent, alternative drainage paths through adjacent gully pots may be available. As this limits the exposure to flood events, the vulnerability of the public space to blockages reduces.

Findings from this study may aid to support maintenance strategies on a system scale and to improve gully pot design. Knowledge of properties that contribute to progressive accumulation and eventually blockages, may justify investments during the design phase in order to minimise future maintenance and blockages. That is, decision makers should consider the physical and catchment properties that prevent progressive accumulation of solids, when aiming to prevent gully pot blockages. In addition, the absence of a residual spatial dependence allows for directing preventive maintenance, taking these properties into account.

# 501 7 Acknowledgements

502 The authors would like to thank Wietse Dijkstra for his effort during the monitoring campaign. The 503 research is performed within the Dutch 'Kennisprogramma Urban Drainage' (Knowledge Programme 504 Urban Drainage). The involved parties are: ARCADIS, Deltares, Gemeente Almere, Gemeente Breda, 505 Gemeente 's-Gravenhage, Gemeentewerken Rotterdam, Gemeente Utrecht, GMB 506 Rioleringstechniek, Grontmij, KWR Watercycle Research Institute, Royal HaskoningDHV, Stichting 507 RIONED, STOWA, Tauw, vandervalk+degroot, Waterboard De Dommel, Waternet and
508 Witteveen+Bos.

# 509 Appendix A. Supplementary data

# 510 Appendix B

511 Fitted values from the Binomial GLMM model with AR-1 correlation structure versus the Pearson

residuals are depicted in Figure B.1. Values on the right side of this graph represent gully pots which

513 are blocked according to the model. The change in variation for larger fitted values is not substantial,

taking into consideration the increase in point density for lower fitted values. The model does,

515 however, seem to underestimate values for nearly blocked gully pots to some extent. This is

attributed to the delineation of the upper asymptote of the applied link function, which cannot

return a probability of 1. Therefore, model estimations can only approximate the top full sand traps

- 518 associated with perceived blockages.
- 519 Figure B.1: Fitted values from the model versus the Pearson residuals

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Posterior marginal distribution of weights  $\beta_k$ 





#### Model estimate

- median
- predictions
- 95% prediction interval









