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An adaptive robust optimization scheme for water-flooding optimization in oil reservoirs using residual analysis^{*}

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Abstract: Model-based dynamic optimization of the water-flooding process in oil reservoirs is a computationally complex problem and suffers from high levels of uncertainty. A traditional way of quantifying uncertainty in robust water-flooding optimization is by considering an ensemble of uncertain model realizations. These models are generally not validated with data and the resulting robust optimization strategies are mostly offline or open-loop. The main focus of this work is to develop an adaptive or online robust optimization scheme using residual analysis as a major ingredient. The models in an ensemble are confronted with data and an adapted ensemble is formed with only those models that are not invalidated. As a next step, the robust optimization is again performed (i.e., updated/adjusted) with this adapted ensemble. The adapted ensemble gives a less conservative description of uncertainty and also reduces the high computational cost involved in robust optimization. Simulation example shows that an increase in the objective function value with a reduction of uncertainty on these values is obtained with the developed adaptive robust scheme compared to an open-loop offline robust strategy with the full ensemble and an adaptive scheme using Ensemble Kalman Filter (EnKF), which is one of the most common parameter estimation methods in reservoir simulations.

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Keywords: Uncertainty handling, water-flooding optimization, residual analysis, online robust optimization

1. INTRODUCTION

Dynamic optimization of the water-flooding process has shown significant scope for improvement of the economic life-cycle performance of oil fields compared to a more conventional reactive strategy, see e.g., Brouwer and Jansen (2004); Jansen et al. (2008); Foss (2012); Van den Hof et al. (2012). Besides computational complexity, induced due to complex non-linear dynamics and hence non-convexity, one of the key challenges in this model-based dynamic optimization is the high levels of uncertainty arising from the modeling process of water flooding and from strongly varying economic conditions.

Various approaches to decision making under uncertainty can be implemented in two different ways, see e.g., Bertsimas and Thiele (2006). In open-loop or offline schemes, robust optimization is performed only once under a given description of uncertainty. Robust optimization can also be used in an adaptive or online fashion where the uncertainty is reduced with the information that is revealed over time. A general practice of quantifying uncertainty in water-flooding optimization is a scenario-based approach where an ensemble of uncertain parameters (e.g., reser-

voir models), see e.g., Van Essen et al. (2009); Capolei et al. (2013) is considered. These models are mostly either generated by using geostatistical tools, see e.g., Mariethoz and Caers (2014) or hand drawn, and are typically not (in)validated by the production data. Hence they may provide a (very) conservative description of uncertainty. An adaptive scheme, i.e., Closed-Loop Reservoir Management (CLRM) has been introduced in Jansen et al. (2005), where the reservoir model variables (states and/or parameters) are updated using data assimilation or Computer Assisted History Matching (CAHM) techniques, such as Ensemble Kalman Filter (EnKF), variational approaches, etc., see e.g., Evensen (2009); Aanonsen et al. (2009); Oliver and Chen (2011) and the optimization is adapted with updated model(s). In the robust settings, as robust optimization uses an ensemble of model realizations, posterior ensemble, e.g., estimated by EnKF, can be directly used in an adaptive fashion resulting in a robust CLRM, see e.g., Chen et al. (2009), Chen et al. (2010), Capolei et al. (2013).

The purpose of this work is to devise an adaptive robust scheme that can be updated with the given production data. The main focus is to address the question: how the available information (data) with time can be used to shrink the uncertainty space by selecting fewer number of

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representative models in an ensemble (reduce the ensemble size) or in other words how uncertainty is propagated and can be reduced in an adaptive online setting? The concept of residual analysis is used, where the models in an ensemble are confronted with data and are invalidated if they do not sufficiently agree with the observed data. An adapted ensemble is formed with only those models that are not invalidated thus providing a less conservative description of uncertainty with a reduced number of models in an ensemble. The adapted ensemble is used in a robust optimization in an online fashion. Residual analysis follows an 'exclusion approach' to uncertainty modeling, see e.g., Tarantola (2006); Caers (2011), which focuses on starting from all possibilities (models) and then excluding those possibilities (models) that can be 'rejected' by any information available to us, e.g., with rejection sampling which is a probabilistic approach of rejecting models. EnKF is also implemented and the posterior ensemble is used in robust optimization. The results of the EnKF in terms of uncertainty reduction and performance improvement are compared with the developed approach.

The paper is organized as follows: in the next section, model-based water-flooding optimization and uncertainty quantification are discussed. The concept of residual analysis is presented in section 3. In section 4, the adaptive robust scheme is introduced. Simulation example with the introduced scheme is given in section 5 followed by the conclusions in section 6.

2. UNCERTAINTY IN WATER-FLOODING OPTIMIZATION

Water-flooding involves the injection of water in an oil reservoir to increase oil production. Net Present Value (NPV), as an objective for the dynamic optimization of the water-flooding process, can be mathematically represented in the usual fashion as:

$$J = \sum_{k=1}^K \left[\frac{r_o \cdot q_{o,k} - r_w \cdot q_{w,k} - r_{inj} \cdot q_{inj,k}}{(1+b)^{\frac{k}{\tau_t}}} \cdot \Delta t_k \right] \quad (1)$$

where r_o , r_w and r_{inj} are the oil price, the water production cost and the water injection cost in $\frac{\$}{m^3}$ respectively. K represents the production life-cycle i.e., the total number of time steps k and Δt_k the time interval of time step k in days. The term b is the discount rate for a certain reference time τ_t . The terms $q_{o,k}$, $q_{w,k}$ and $q_{inj,k}$ represent the total flow rate of produced oil, produced water and injected water at time step k in $\frac{m^3}{day}$.

Model uncertainty is the prime source of uncertainty in model-based optimization of the water-flooding process. Traditionally an ensemble of uncertain dynamic model realizations is considered to quantify the uncertainty space Θ , i.e., $\{\mathcal{M}(\theta_1), \mathcal{M}(\theta_2), \dots, \mathcal{M}(\theta_{N_{geo}})\}$, where \mathcal{M} is a dynamic model with $\theta_i \in \Theta$, $i = 1, 2, \dots, N_{geo}$ a realization of a vector of uncertain parameters. This ensemble-based uncertainty set can be used with various robust schemes. One of the simplest offline or open-loop scenario-based robust approaches is to maximize the average of NPV over the model uncertainty ensemble, as introduced in Van Essen et al. (2009). Robust optimization (or Mean Optimization (MO)) can be formulated as:

$$J_{MO} = \frac{1}{N_{geo}} \sum_{i=1}^{N_{geo}} J(\mathbf{u}, \theta_i) \quad (2)$$

where J is NPV and \mathbf{u} is the input decision variable. Other offline (open-loop) robust approaches in water-flooding optimization, e.g., mean-variance and mean-CVaR have been introduced in e.g., Capolei et al. (2015); Siraj et al. (2015). In these offline strategies, the optimal solution is devised for the complete production life of the reservoir under a given uncertainty set and the optimization is not updated/adapted to the available information with time. These offline (open-loop) approaches mainly aim only at minimizing the negative effect of uncertainty on the achieved NPV and do not deal with shrinking the uncertainty space Θ .

The uncertainty reduction can be achieved with the help of available information. The estimation of physical parameters with the available production data is one of the ways to reduce uncertainty. Data assimilation or CAHM algorithms such as the Ensemble Kalman Filter (EnKF), variational methods are typically used in reservoir simulation offering a joint state and parameter estimation. This parameter estimation problem, due to a large number of to-be-estimated parameters, is ill-posed, i.e., many combination of parameter values will result in the same minimum value of the cost function. Therefore, CAHM typically uses a Bayesian framework with a prior distribution of the parameters reflected by a prior ensemble. Hence the estimation of physical parameters is highly influenced by the selection of this prior ensemble of parameter. These estimated parameters and the resulting posterior (adapted) ensemble with CAHM can be used in an adaptive fashion to update the robust strategies as presented, e.g., in Chen et al. (2009); Capolei et al. (2013), which is also referred to as closed-loop approaches in the petroleum engineering literature. The application of CAHM with nominal optimization has been presented, e.g., in Jansen et al. (2005); Sarma et al. (2005); Jansen et al. (2009). As the number of realizations in the adapted ensemble with CAHM are not reduced, the computational complexity of these adaptive robust optimization is not decreased. Another way to adapt the ensemble is by using clustering techniques. The number of realizations in an ensemble is reduced by clustering the models with the similar (static or dynamic) behavior, see e.g., Sarma et al. (2013). The clustering techniques are not data driven and the ensemble size reduction may not correspond to uncertainty reduction, hence it will only reduce the complexity of the robust optimization problems.

In the next sections, residual analysis is introduced which offers minimization of uncertainty space and a reduction of computational complexity of robust optimization.

3. RESIDUAL ANALYSIS

Model validation is usually performed by confronting the model with available information, e.g., production data, a priori knowledge. For a given ensemble of models, residual analysis follows an 'exclusion approach' to uncertainty, which focuses on rejecting models by available production data. Therefore, it does not only aim at minimizing the uncertainty space Θ but it also reduces the size of the ensemble, leading to complexity reduction of subsequent

robust optimization. A principle difference between residual analysis and other data assimilation techniques is that residual analysis is performed on the model space which is smaller in size compared to the assimilation methods which focus on the large parameter space. Hence residual analysis does not suffer from the problem of ill-posedness and the effect of the selection of a poor prior ensemble.

Fig. 1 illustrates a detailed overview of techniques which can be used to update the ensemble of realizations. CAHM techniques, such as variational methods follow a gradient-based approach while EnKF uses ensemble-based approach for joint state and parameter estimation. Rejection sampling is a probabilistic technique to reject models in an ensemble and requires knowledge of data likelihood probability. These techniques can be used in a adaptive robust optimization settings where the robust optimization is defined over the posterior (adapted) ensemble. For a linear

Data-driven methods to adapt model/ensemble				Without data
Variational methods	EnKF	Rejection Sampling	Residual analysis	Clustering techniques
<ul style="list-style-type: none"> Prior model/ensemble Objective = data mismatch + regularization 	<ul style="list-style-type: none"> Prior ensemble $\theta_1, \theta_2, \dots, \theta_N$ Forward simulations $\hat{y}_1 = g(\theta_i)$ 	<ul style="list-style-type: none"> Prior ensemble $\theta_1, \theta_2, \dots, \theta_N$ Forward simulations $\hat{y}_1 = g(\theta_i)$ 	<ul style="list-style-type: none"> Prior ensemble $\theta_1, \theta_2, \dots, \theta_N$ Forward simulations $\hat{y}_1 = g(\theta_i)$ 	<ul style="list-style-type: none"> Prior ensemble $\theta_1, \theta_2, \dots, \theta_N$ Forward simulations $\hat{y}_1 = g(\theta_i)$
↓ Data = y	↓ Data = y	↓ Data = y	↓ Data = y	↓ No data
<ul style="list-style-type: none"> Minimize objective using gradient based methods with adjoint + typically Bayesian regularization 	<ul style="list-style-type: none"> Update ensemble with the linear estimator conditioned on innovation e_i 	<ul style="list-style-type: none"> If $\hat{y} = y$, accept the model else reject it. Or accept the model if data likelihood $p = P(Y = y \theta = \theta_i)/P^{max} > p^*$, where p^{max} is the max p and p^* is threshold. 	<ul style="list-style-type: none"> Define residual: $e_i = \hat{y}_i - y$ If $E[BFR(\theta_i)] \geq$ threshold in %, accept the model else reject it. 	<ul style="list-style-type: none"> clustering the models with the similar (static or dynamic) behavior
<ul style="list-style-type: none"> Posterior model 	<ul style="list-style-type: none"> Posterior ensemble $\hat{\theta}_1, \hat{\theta}_2, \dots, \hat{\theta}_N$ with sample mean and covariance 	<ul style="list-style-type: none"> Posterior ensemble $\theta_1, \theta_2, \dots, \theta_r$ with $r \leq N$ 	<ul style="list-style-type: none"> Posterior ensemble $\theta_1, \theta_2, \dots, \theta_r$ with $r \leq N$ 	<ul style="list-style-type: none"> Adapted ensemble $\theta_1, \theta_2, \dots, \theta_r$ with $r \leq N$

Fig. 1. A comparison of methods for updating an ensemble of models to be used with robust optimization.

regression problem, first order statistics provide a complete characterization of the validation problem, e.g., in the correlation analysis, the residual should be asymptotically uncorrelated with past input samples. For a nonlinear regression problem, the first order moments are not sufficient to draw any conclusions about the validity of the models. As the reservoir models are strongly nonlinear in nature, we use a deterministic metric, i.e., Best-fit-ratio (BFR) to define an invalidation test. The available production data is used for invalidation.

The residual ϵ is defined as the difference between the observed (measured) output \mathbf{y} and the simulation output $\hat{\mathbf{y}}$.

$$\text{Residual} = \text{measured output} - \text{simulation output},$$

$$\epsilon = \mathbf{y} - \hat{\mathbf{y}}.$$

The Best-Fit Ratio (BFR) or the fit ratio is defined as:

$$\text{BFR} = 100\% \times \max \left(1 - \frac{\|\epsilon\|_2}{\|\mathbf{y} - \bar{\mathbf{y}}\|_2}, 0 \right)$$

where $\bar{\mathbf{y}}$ is the average of the measured output \mathbf{y} . The BFR percentage is a relative measure often used in system identification, and a low value of BFR indicates a poor fit to data, see Ljung (1999). BFR is a unit-less quantity and gives an indication of fit in a percentage. Generally, as

the reservoir models contain multiple outputs, an average BFR over each individual output channel is considered. The selection of BFR is not unique and other metrics, e.g., Mean Squared Error (MSE) or Variance Accounted For (VAF), see Ljung (1999) can also be used for defining the invalidation test. VAF measures how much variation in data (variance) is captured by the model output and disregards the mismatch (bias) of data with model output while the MSE measure is dependent on the unit of physical quantity being measured, therefore BFR is used for residual analysis.

The test for invalidating models is chosen as:

$$\mathcal{M}(\theta_i, \mathbf{u}) \text{ is not invalidated if } \mathbb{E}[BFR(\mathcal{M}(\theta_i, \mathbf{u}))] > 30\%,$$

for a given \mathbf{u}

where $\mathbb{E}[\cdot]$ is the expected value and calculated as the average over all outputs. It implies that all those models with an average BFR of above 30% are retained in the adapted ensemble. The selection of 30% is chosen in an ad-hoc way. One of the risks with this selection criterion is that all the models in an ensemble can be rejected. An alternative choice for the invalidation test is by considering e.g., 10% models who score the highest average BFR within the ensemble. This criterion is not used in this work.

A flow chart as shown in Fig. 2 explains residual analysis. At a given time step, the concept of residual analysis from generating prior models to forming an adaptive ensemble is performed and later, as a final step of the developed adaptive strategy as discussed in the next section, the robust optimization is conducted with the adaptive ensemble. At the next time step, the adaptive ensemble in the previous step is considered as a prior and the procedure is repeated as shown in Fig. 2.

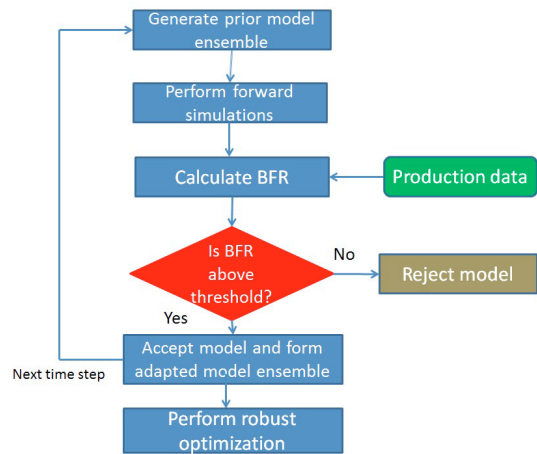


Fig. 2. Adapting a model ensemble using residual analysis

4. AN ADAPTIVE ROBUST OPTIMIZATION

The key elements of the introduced adaptive robust strategy using residual analysis are displayed in Fig. 3. The top of the figure represents the physical system consisting of reservoirs, wells and facilities with inputs and outputs. The center of the figure displays the residual analysis step, which starts from considering a prior ensemble. The sensors on the right side of the figure are used for measurements which are used to invalidate models with residual analysis. A robust optimization is defined using the

adapted ensemble as shown at the left side of the figure. Throughout this work, the MO approach of Van Essen et al. (2009) is used for robust optimization. Other robust measures such as mean-variance, mean-CVaR can also be used. An implementation of the adaptive robust strategy is

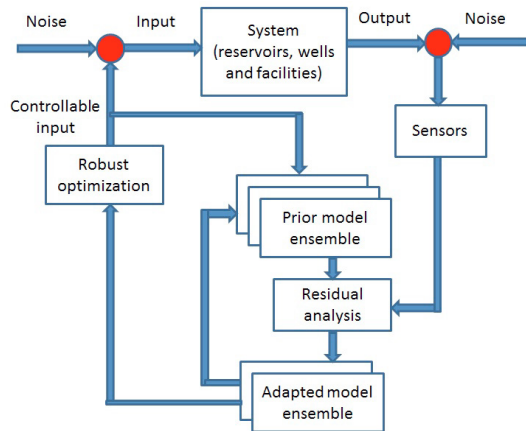


Fig. 3. An adaptive robust approach by updating the ensemble with residual analysis at each time step.

presented in the next section to investigate if model invalidation by residual analysis can be an appropriate tool for reducing uncertainty and improving robust optimization of economic performance of oil reservoir in an online setting.

5. SIMULATION EXAMPLE

5.1 Ensemble of reservoir models

An ensemble of 100 geological realizations of the standard egg model is considered. Each model in the ensemble is a three-dimensional realization of a channelized reservoir produced under water flooding conditions with eight water injectors and four producers based on the original Egg model proposed in Van Essen et al. (2009). The life-cycle of each reservoir model is 3600 days. The complete list of parameters and the details about the model set are presented in Jansen et al. (2014). The true permeability field is considered to be the unknown parameter. The number of 100 realizations is assumed to be large enough to be a good representative of this parametric uncertainty space. The absolute-permeability field of the first realization in the set is shown in Fig. 4. Fig. 5 shows the permeability fields of six randomly chosen realizations of the standard egg model in an ensemble of 100 realizations. Each realization in the set is considered equiprobable.

5.2 An offline (open-loop) MO approach with complete ensemble

All the simulation experiments in this work are performed using MATLAB Reservoir Simulation Toolbox (MRST), see Lie et al. (2012).

Economic data for NPV An un-discounted NPV is used. Other economic parameters, i.e., oil price r_o , water injection r_{inj} and production cost r_w are chosen as $126 \frac{\$}{m^3}$, $6 \frac{\$}{m^3}$ and $19 \frac{\$}{m^3}$ respectively.

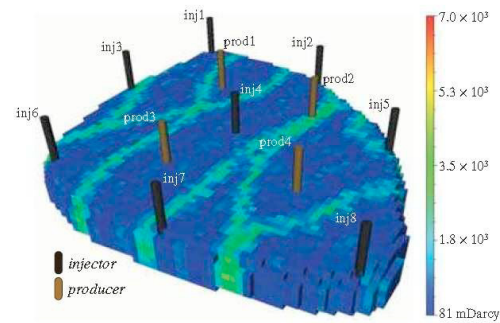


Fig. 4. Permeability field of realization 1 of a set of 100 realizations

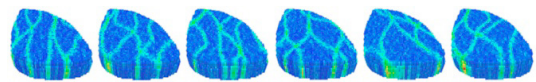


Fig. 5. Permeability fields of 6 randomly chosen realizations. (Van Essen et al. (2009))

Control input The control input \mathbf{u} involves injection flow rate trajectories for each of the eight injection wells. The minimum and the maximum rate for each injection well are set as $0.2 \frac{m^3}{day}$ and $79.5 \frac{m^3}{day}$ respectively. The production wells operate at a constant bottom-hole pressure of 395bar. The control input \mathbf{u} is reparameterized in control time intervals with input parameter vector φ . For each of the eight injection wells, the control input \mathbf{u} is reparameterized into twenty time periods of t_φ of 180 days during which the injection rate is held constant at value φ_i . Thus the input parameter vector φ consists of $N_u = 8 \times 20 = 160$ elements. The initial input value for the optimization is the maximum possible injection rate, i.e., $79.5 \frac{m^3}{day}$ for each injection well. The optimal input, \mathbf{u}_{off} is obtained by using MO as in eq. (2) with the complete ensemble.

5.3 The adaptive robust approach for a synthetic truth

Residual analysis with synthetic truth One of the models in the ensemble, i.e., model 10, is considered as the synthetic truth to generate data \mathbf{y} . The optimal solution from the offline (open-loop) approach, i.e., \mathbf{u}_{off} is applied to the truth to collect data \mathbf{y} . The output \mathbf{y} is defined as the total production rate from each production well, i.e., $\mathbf{y} = \{\mathbf{y}_1, \mathbf{y}_2, \mathbf{y}_3, \mathbf{y}_4\}$. The data is collected at time $t = 360$ days. The input \mathbf{u}_{off} is also applied to each member of the ensemble to collect simulation data $\hat{\mathbf{y}}$. An average BFR is calculated for each model simulation output $\hat{\mathbf{y}}$ and subsequently the invalidation test is performed. The average BFR values for each model in the ensemble and the model retained in adapted ensembles are shown in Fig. 6. The adapted ensemble contains 22 models and provides a less conservative description of uncertainty.

Data assimilation with EnKF EnKF is also implemented with the standard egg model ensemble to estimate only the permeability field based on production data measurement. The production data is generated by the synthetic truth. We used a straightforward implementation using the EnKF module of MRST without localization or inflation. The output \mathbf{y} is defined as the total production rate from

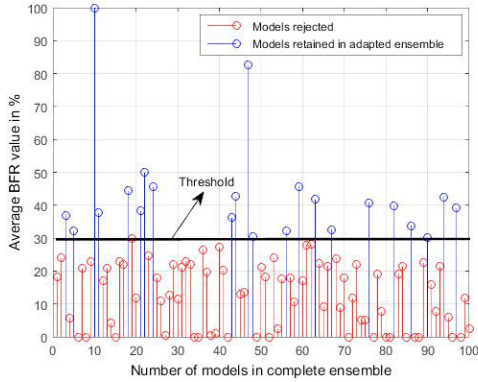


Fig. 6. Average BFR values for each model in the ensemble and the models retained in adapted ensemble

each production well and the data is collected at time $t = 360$ days. In EnKF, all ensemble members are updated, and so this also leads to an updated ensemble which can be directly used in robust optimization. However, unlike residual analysis, it has the same number of elements as the original ensemble.

MO with the adapted ensemble Robust optimization is updated/adjusted with information revealed, i.e., MO is again performed with the adapted ensembles generated by residual analysis and EnKF. The economic parameters are kept the same. The initial input value for the optimization is \mathbf{u}_{off} . As the first sample of \mathbf{u}_{off} , i.e., from the time 0 day to 360 days is already applied to the system, the remaining part of the input from time 360 days to 3600 days (end of simulation time) is used. The time horizon for MO is reduced to $3600 - 360 = 3240$ days. Optimal inputs are obtained as a result of robust optimization over the different ensembles for both residual analysis $\mathbf{u}_{\text{on,RA}}$ and EnKF $\mathbf{u}_{\text{on,EnKF}}$ and they are applied to the synthetic truth. Fig. 8 shows the comparison of time evolutions of NPV with the offline approach (open-loop with complete ensemble) and the adaptive approaches (online with adapted ensembles). We note that NPV is often defined as the cumulative discounted cash flow (CDCF) over the entire project life. Here we have chosen to use the term NPV (specifically NPV time-evolution) also for intermediate values of the CDCF. The introduced adaptive approach using residual analysis gives an increase of 0.62% in the NPV value compared to the offline (open-loop) approach and hence provides better optimization results. MO with the posterior ensemble with EnKF gives poor results and a decrease of 1.2% in NPV value compared to offline (open-loop) approach is observed. From the computational complexity viewpoint, as the number of model realizations in posterior ensemble by EnKF are not reduced compared to the adapted ensemble by residual analysis with only 22 members, the computational complexity of robust optimization using residual analysis is drastically reduced.

To analyze uncertainty reduction, the optimal solutions, i.e., \mathbf{u}_{off} , $\mathbf{u}_{\text{on,RA}}$ and $\mathbf{u}_{\text{on,EnKF}}$ are applied to the complete and the adapted/posterior ensembles respectively. NPV points are collected and the corresponding PDFs are obtained by approximating a non-parametric KDE with MATLAB routine 'ksdensity' on these NPV data values

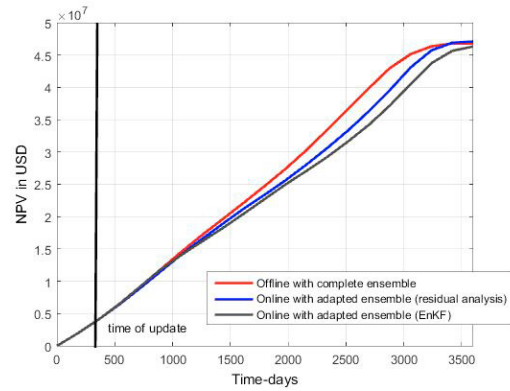


Fig. 7. NPV comparison of adaptive online (adapted ensembles by residual analysis and EnKF) and offline (complete ensemble) strategies for the synthetic truth. At $t = 360$ days a new optimization has started in the online cases.

as shown in Fig. 8. It can be observed that the standard deviation of NPV points with the adapted ensemble by residual analysis is reduced compared to the one resulted on the complete ensemble. A drastic reduction in standard deviation of 27.62% is observed. Another indicator for the effect of uncertainty is the worst-case value. As the adapted ensemble by residual analysis provides a less conservative description of uncertainty, the worst-case value has also improved. An increase of 7.91% in the worst-case NPV value is obtained. MO with EnKF ensemble results in the lowest worst-case NPV value with the lowest mean value while it results in the highest value for the best-case NPV, which shows poor uncertainty reduction of EnKF.

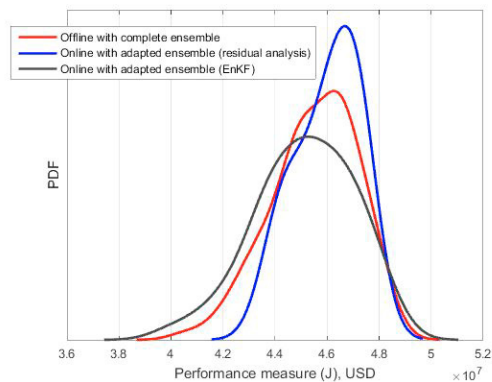


Fig. 8. PDF (long-term NPV) by applying optimal inputs from adaptive online (adapted ensembles by residual analysis and EnKF) and offline (complete ensemble) strategies to the respective ensembles

The effect of uncertainty on the time evolutions of NPV is shown in Fig. 9. The maximum and the minimum values of the time evolutions of NPV from both ensembles will form a band. The width of the band shows the variability of the strategy over the ensemble of the model realizations. The smaller width of resulting from the adaptive strategy with residual analysis ensemble shows the effect of uncertainty reduction compared to adaptive strategy with EnKF and offline approach.

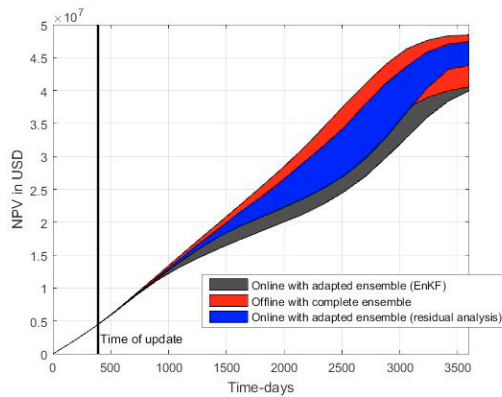


Fig. 9. Max and min (band) for time evolutions of NPV by applying optimal inputs from adaptive online (adapted ensembles by residual analysis and EnKF) and offline (complete ensemble) strategies to the respective ensembles. At $t = 360$ days a new optimization has started in the online cases.

6. CONCLUSIONS

The question of reducing uncertainty in an adaptive setting is addressed by residual analysis. The adapted ensemble with residual analysis corresponds to propagation of uncertainty and it consists of fewer number of representative model realizations which provide a less conservative description of uncertainty and also substantially reduce the computational complexity of robust optimization. Reduction of uncertainty is evident by a reduction in variance of NPV distribution and an improvement in the worst-case performance compared to EnKF and the offline open-loop approach with complete ensemble.

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