

Model Reduction & Interface Modeling in Dynamic Substructuring

Application to a Multi-Megawatt Wind Turbine



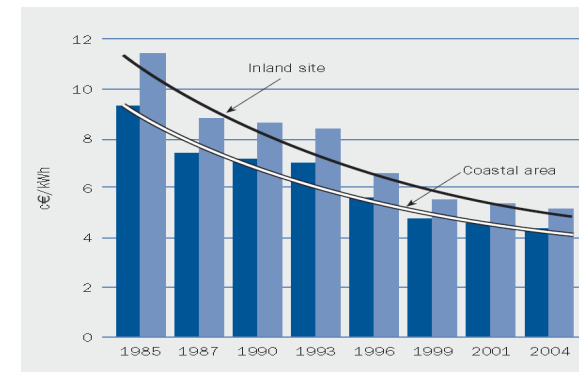
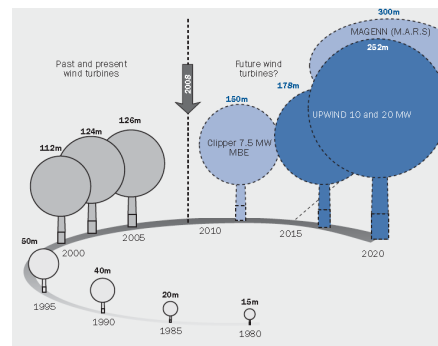
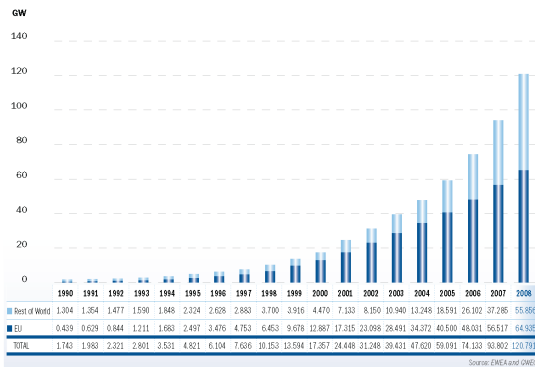
MSc. Presentation

Paul van der Valk

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Introduction

- Trends in wind power
 - Increase in installed GW
 - Larger turbines
 - Decrease of cost (€/kWh)
- Turbines become larger and more optimized



Introduction

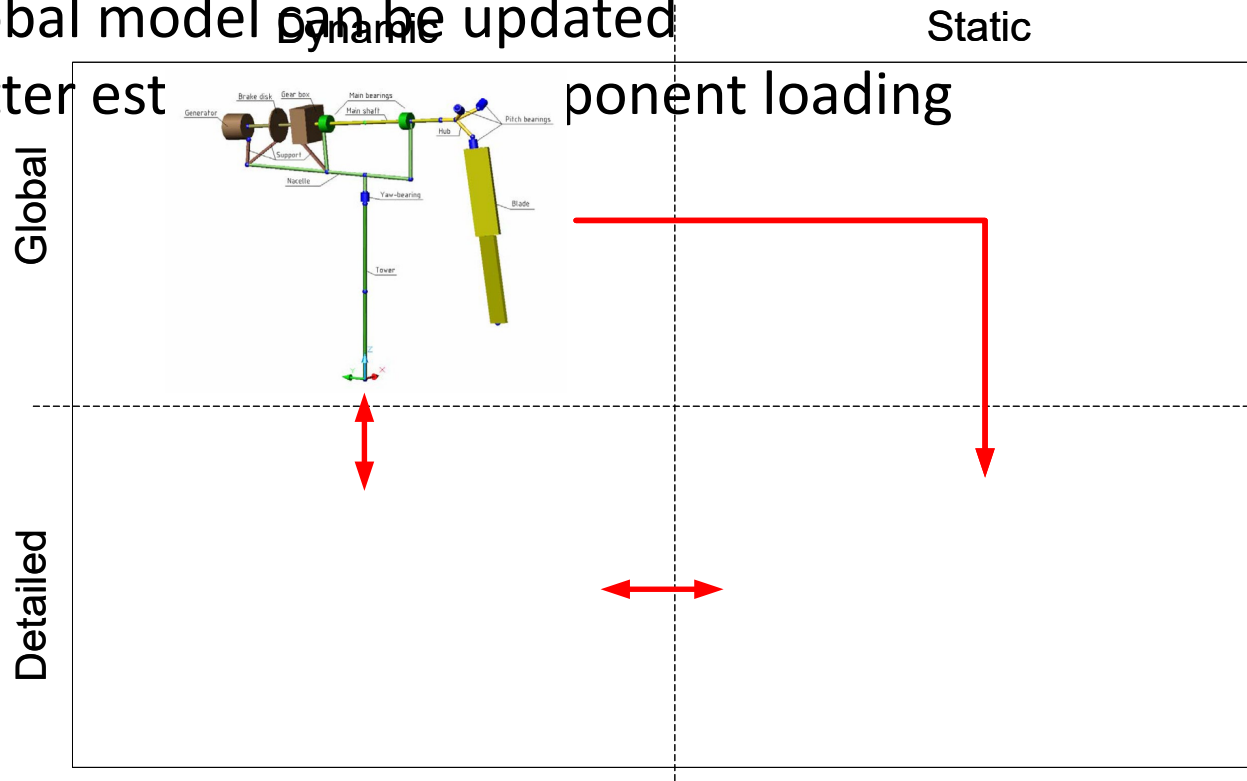
Optimization of components:

- Less material used
 - Decrease in turbine weight
 - Transport and installation is easier
 - Smaller foundations
- Increase in flexibility of component
- Local dynamic behavior
- Higher component loading

Introduction

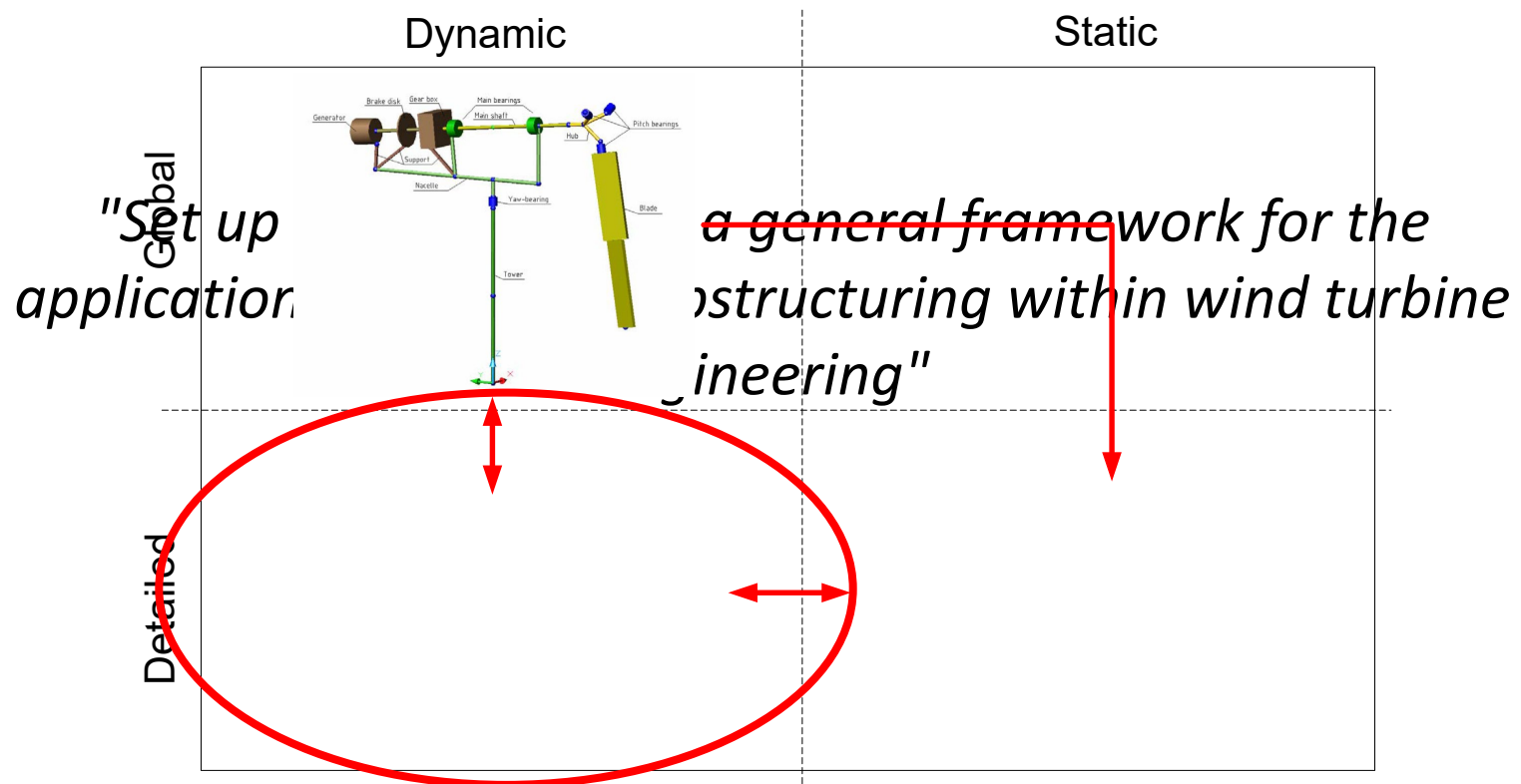
Desired workflow in WT engineering

- Crucial component dynamics can be identified
- Local dynamic behavior not taken into account
- Global model can be updated
- Better estimate of component loading



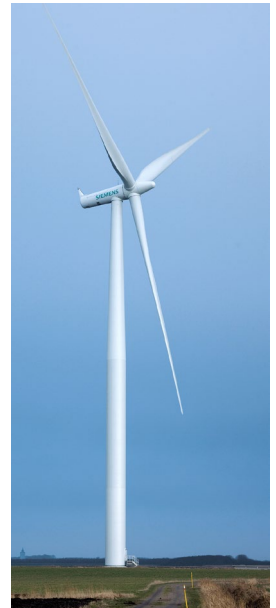
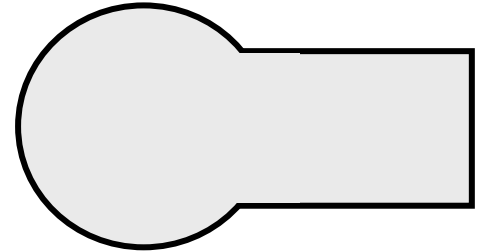
Introduction

Dynamic substructuring is proposed to fill this need for a more detailed dynamic analysis tool



Content

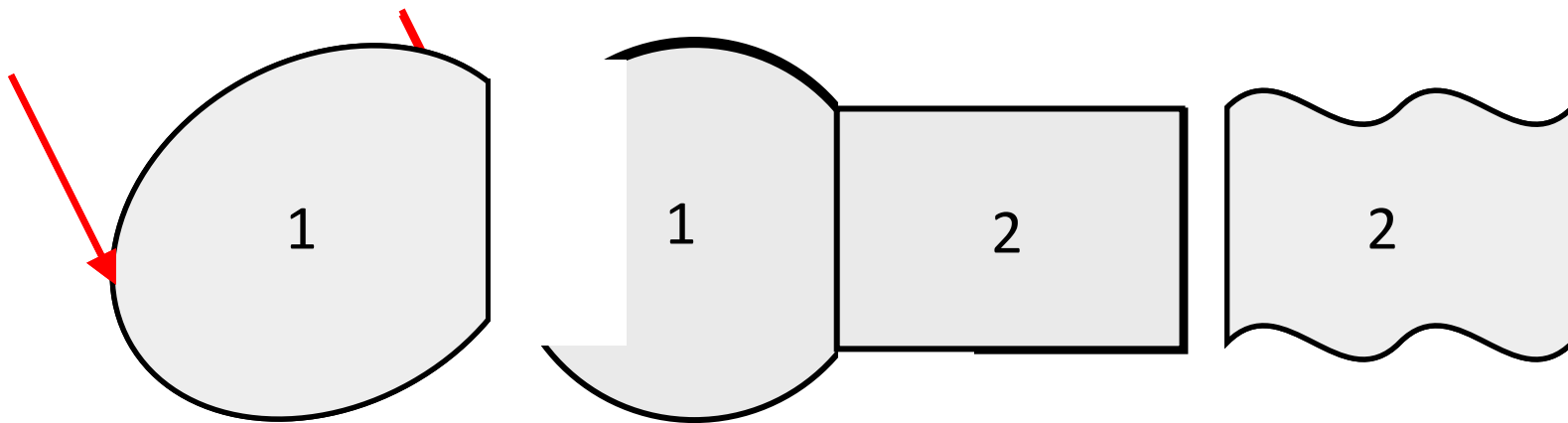
- Theory of dynamic substructuring
 - What is dynamic substructuring?
 - Techniques for dynamic substructuring
- Application to a multi-MW wind turbine
 - Yaw system
 - Component models
 - Validation measurements
 - Analysis results
- Conclusions and recommendations



Theory of dynamic substructuring

What is dynamic substructuring?

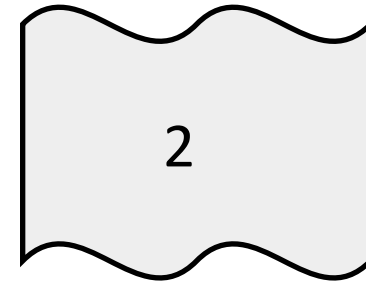
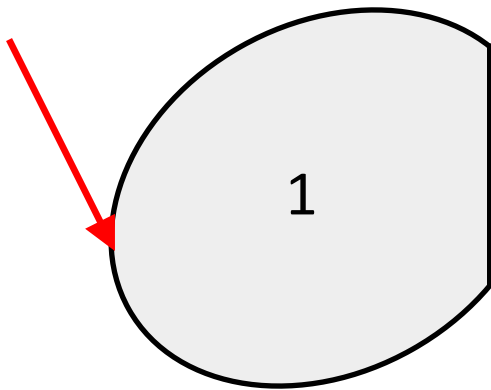
Split the structure in terms of most important dynamic behaviour



Theory of dynamic substructuring

What is dynamic substructuring?

~~Aspects the simplified problem in terms of~~
Aspects the simplified problem in terms of most important dynamic behaviour



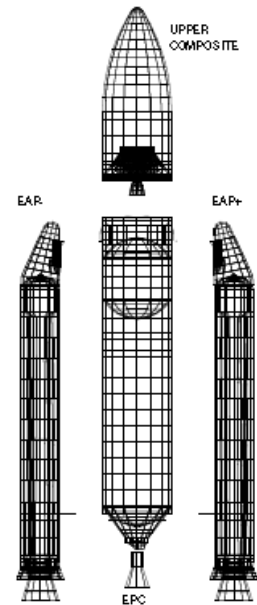
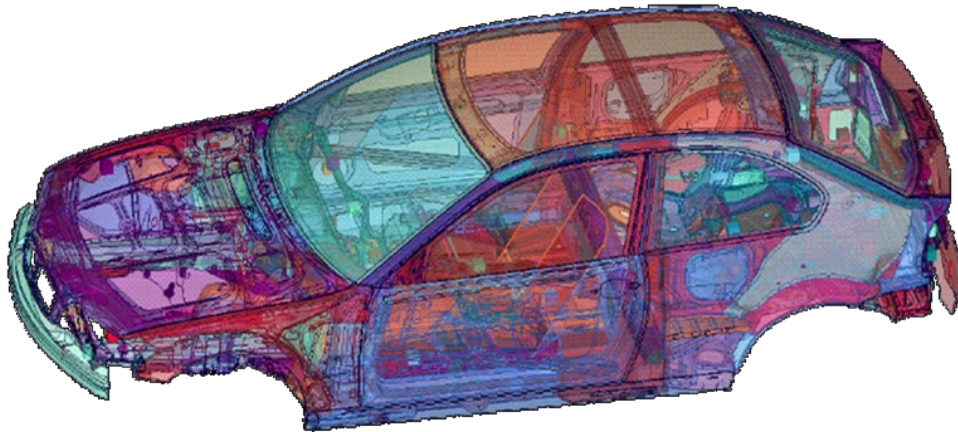
Results in a less complex and more compact set of equations, while accurately describing the assembled behavior

Theory of dynamic substructuring

What is dynamic substructuring?

Several advantages:

- Allows evaluation of large complex structures
- Experimental substructures combined with numerical (component) models
- Local dynamic behavior is easier to identify

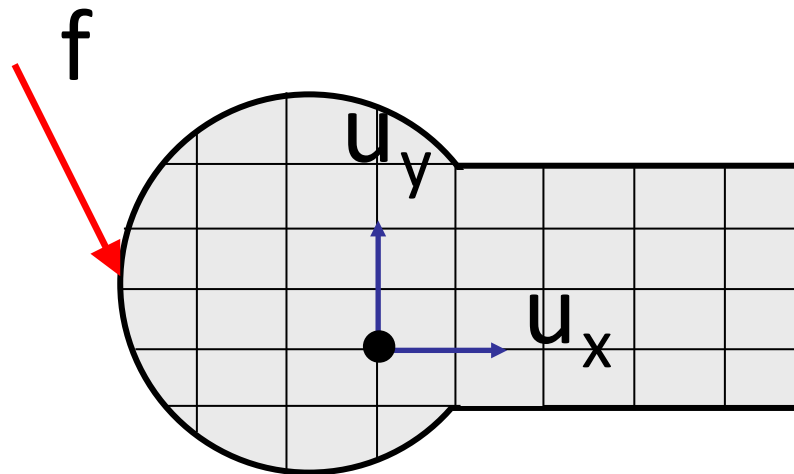


Theory of dynamic substructuring

What is dynamic substructuring?

Equations of motion of total structure:

$$M \ddot{u} + K u = f$$



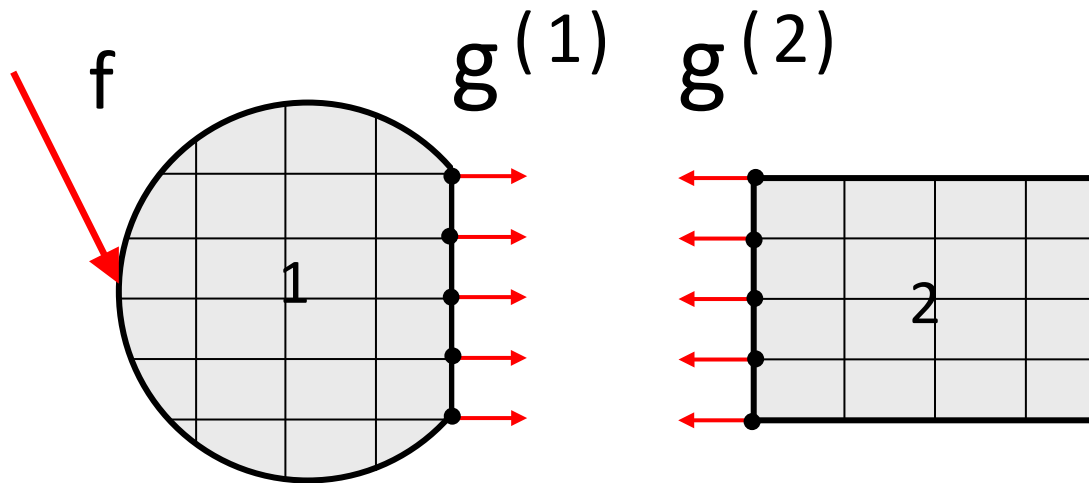
Theory of dynamic substructuring

What is dynamic substructuring?

Equations of motion of separate substructures:

$$M^{(1)} \ddot{u}^{(1)} + K^{(1)} u^{(1)} = f + g^{(1)}$$

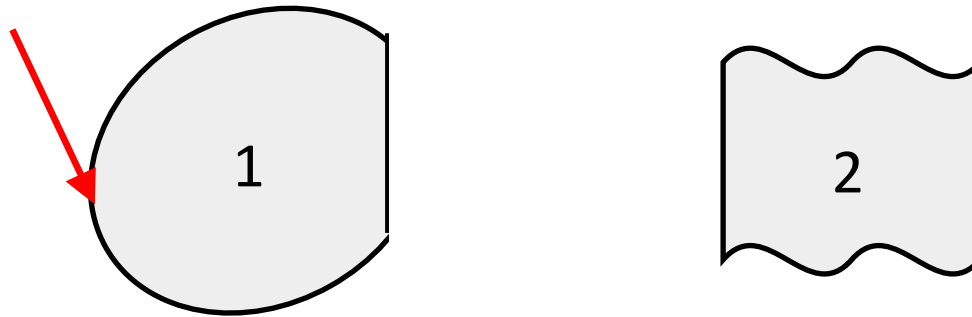
$$M^{(2)} \ddot{u}^{(2)} + K^{(2)} u^{(2)} = g^{(2)}$$



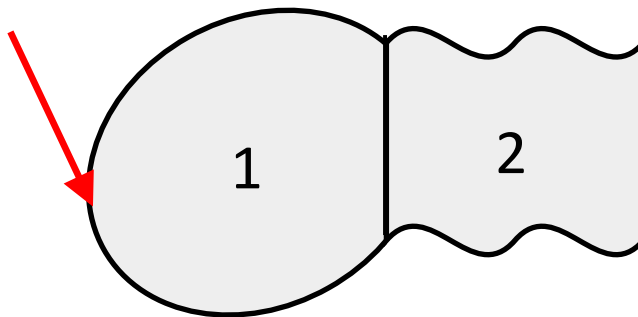
Theory of dynamic substructuring

Techniques for dynamic substructuring

- Reduction of components



- Assembly of components

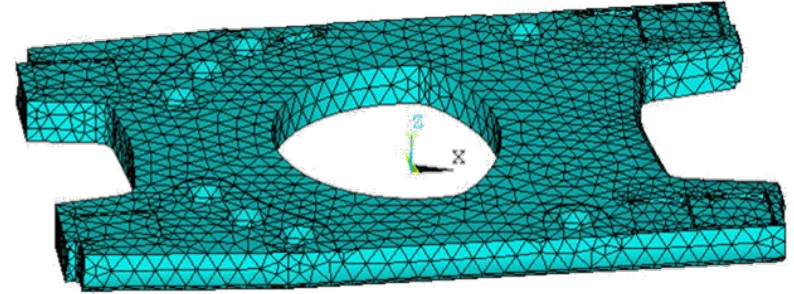


Theory of dynamic substructuring

Reduction of component models

Often FE models are very refined

- High accuracy
- Large number of DoF
 - Results in high computational effort for dynamic problems
- Re-meshing could be very expensive
 - *Component model reduction methods*

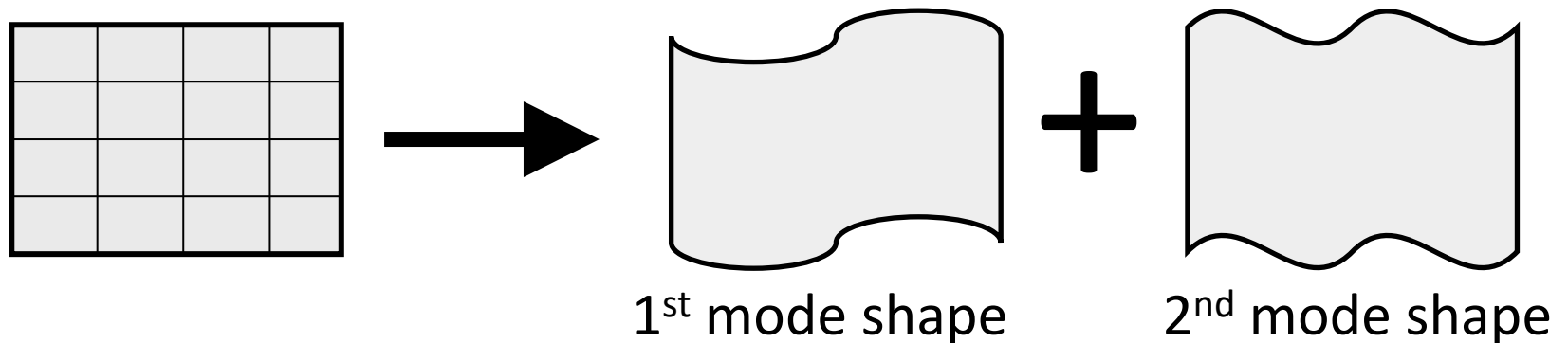


Theory of dynamic substructuring

Reduction of component models

Basic idea:

- Description in terms of vibration mode shapes instead of nodal displacements:

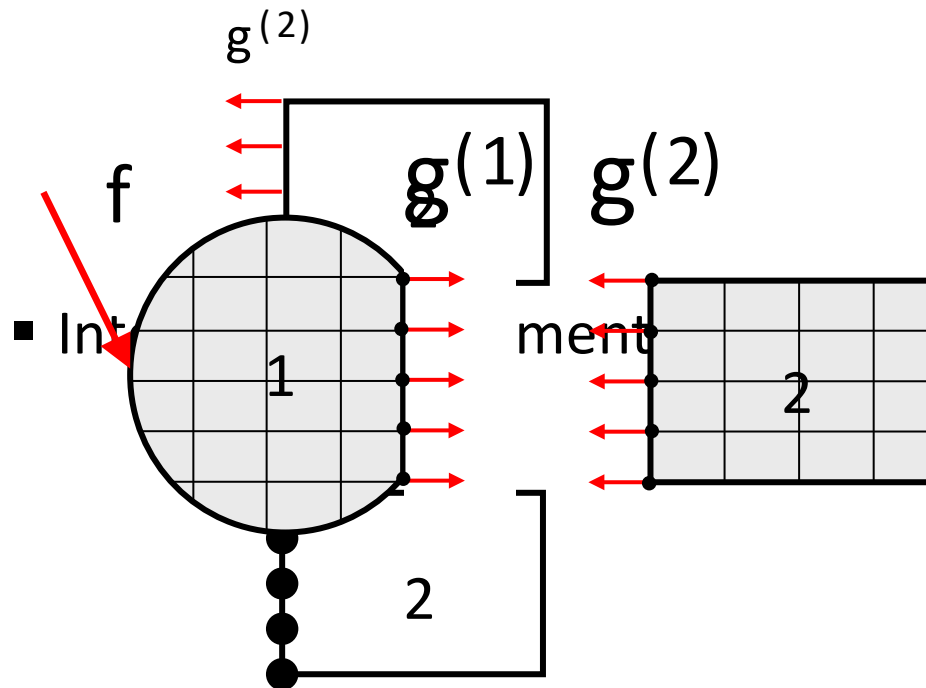


- Exact if all mode shapes are included
- Reduction is performed by only including a number of mode shapes

Theory of dynamic substructuring

Reduction of component models

- “Communication” between substructures needed
→ Add DoF on the interface
 - Interface forces (g_b)



Theory of dynamic substructuring

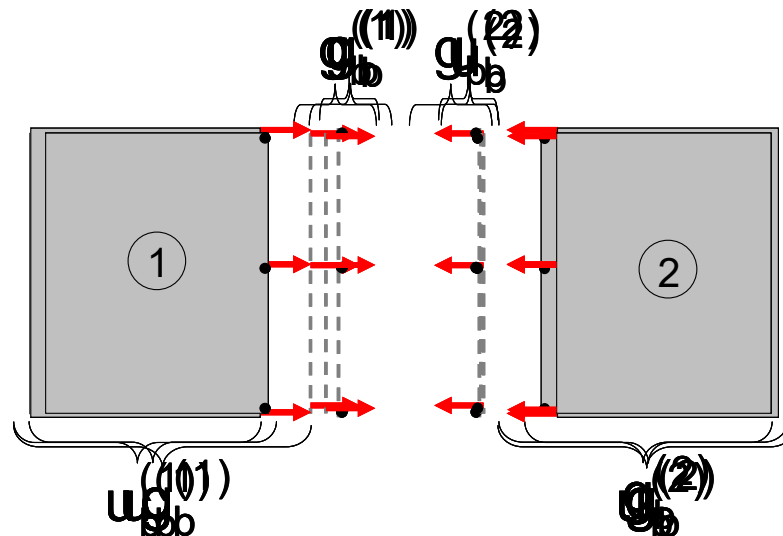
Assembly of component models

Three possible assembly cases:

- $u_b \nleftrightarrow u_b$

- $g_b \nleftrightarrow g_b$

- $u_b \nleftrightarrow g_b$



Theory of dynamic substructuring

Assembly of component models

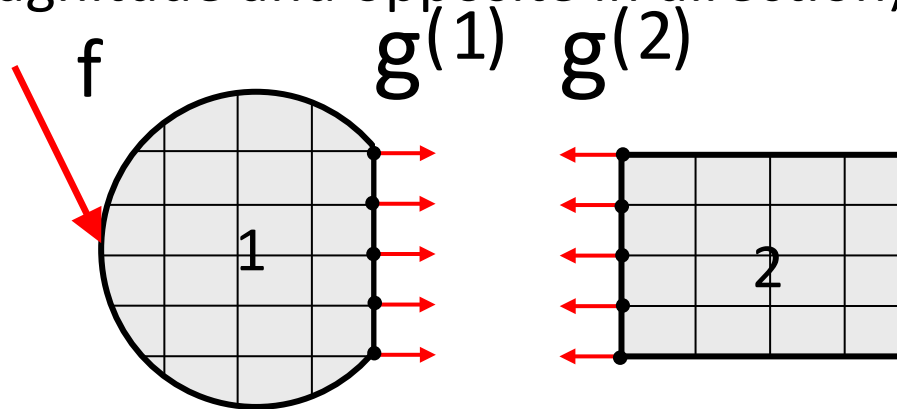
Two conditions:

- *Compatibility*

→ Displacements on both sides of the interface must be the same

- *Equilibrium*

→ Connecting forces must be in equilibrium (i.e. equal in magnitude and opposite in direction)



Theory of dynamic substructuring

Assembly of component models

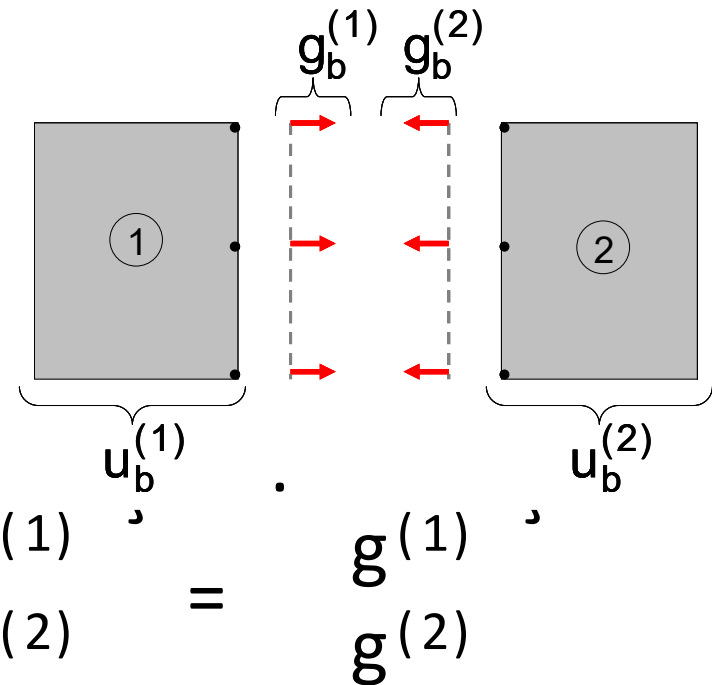
Interface displacements (u_b) to Interface displacements (u_b)

- Compatibility

$$u_b^{(1)} - u_b^{(2)} = 0$$

- Equilibrium

$$\begin{bmatrix} g_b^{(1)} & 0 \\ 0 & g_b^{(2)} \end{bmatrix} \begin{bmatrix} K^{(1)} & 0 \\ 0 & K^{(2)} \end{bmatrix} \begin{bmatrix} u_b^{(1)} \\ u_b^{(2)} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

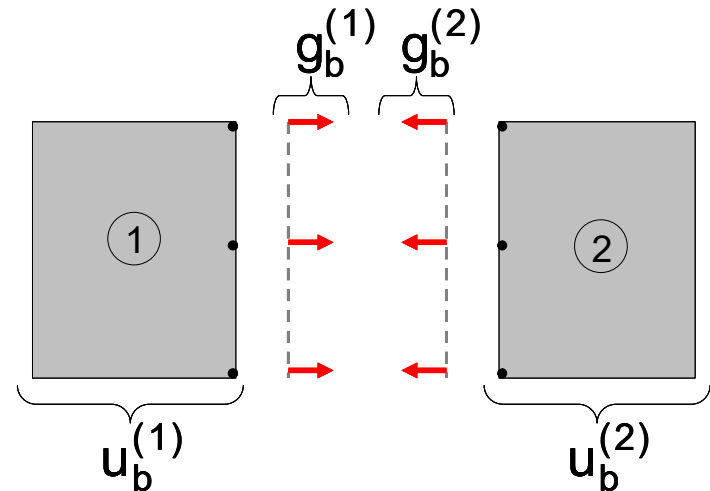


Theory of dynamic substructuring

Assembly of component models

Interface displacements (u_b) to Interface displacements (u_b)

$$\begin{bmatrix} u_b^{(1)} \\ u_b^{(2)} \end{bmatrix} = L u$$



$$g_b^{(1)} + g_b^{(2)} = 0$$

- Relation between Boolean matrices:

$$\begin{bmatrix} L & B \\ B^T & 0 \end{bmatrix} \begin{bmatrix} u \\ g_b \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \Rightarrow L u + B g_b = 0, B^T u = 0$$

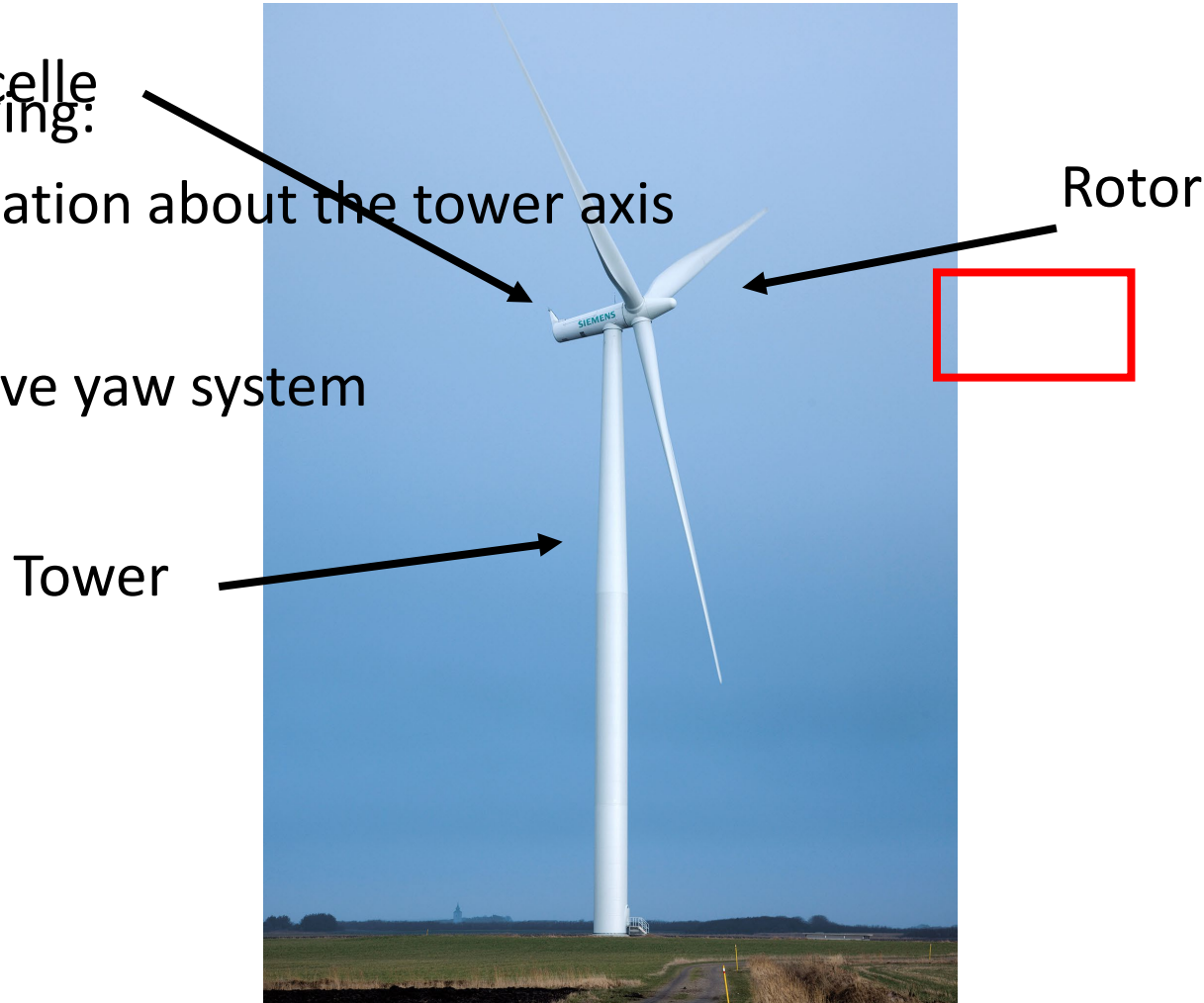
Application to a multi-MW wind turbine

- Yaw system
- Component models
- Measurements for component validation
- Analysis results

Application to a multi-MW wind turbine

Yaw system

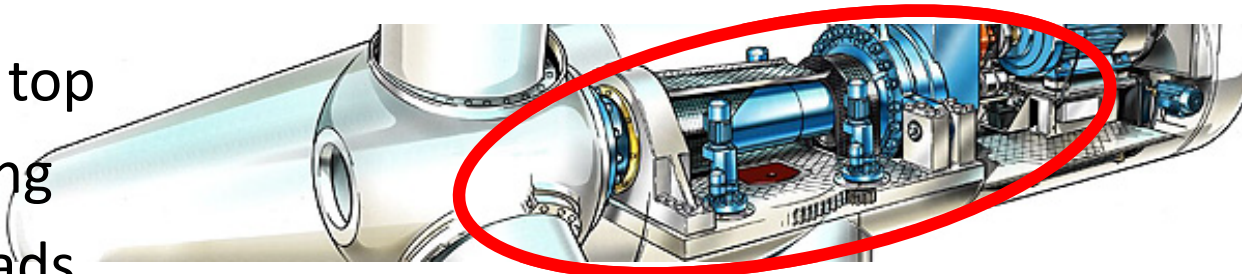
- Nacelle yawing:
Rotation about the tower axis
- Active yaw system



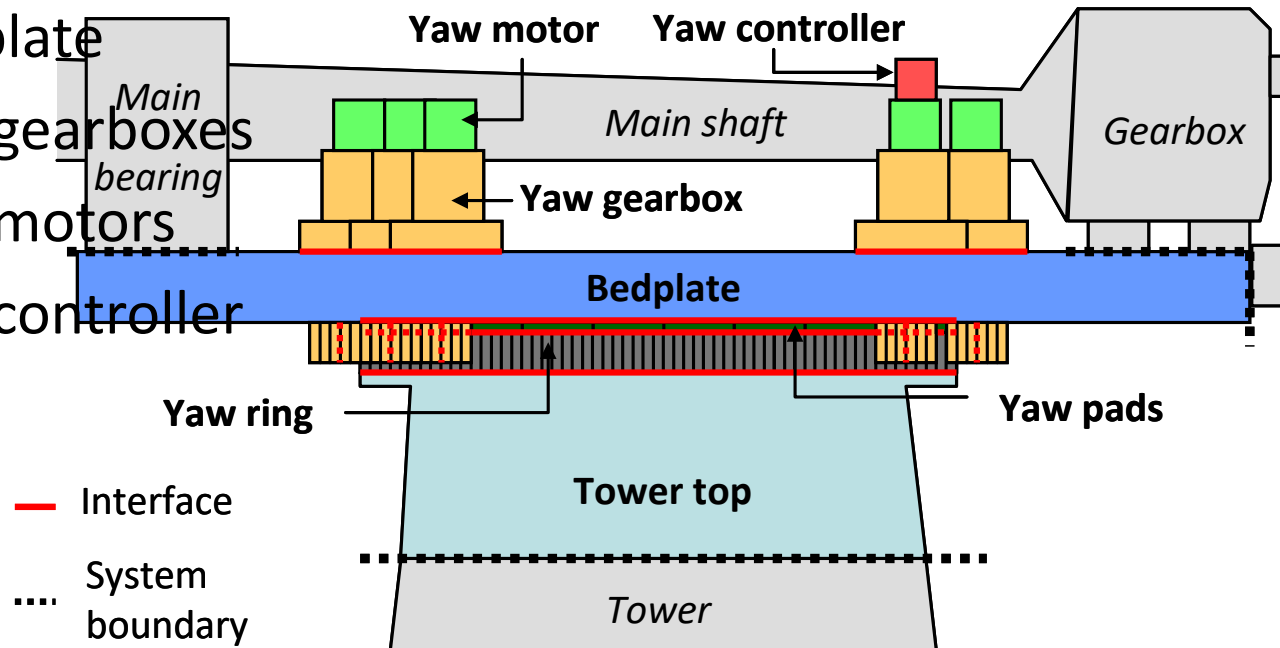
Application to a multi-MW wind turbine

Yaw system

- Tower top
- Yaw ring
- Yaw pads

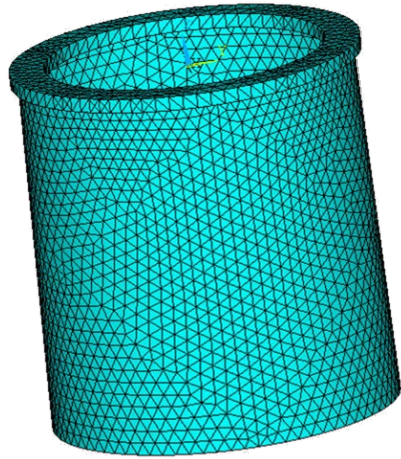


- Bedplate
- Yaw gearboxes
- Yaw motors
- Yaw controller

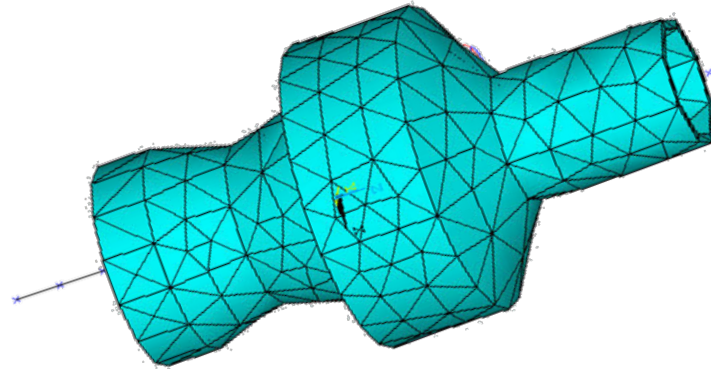


Application to a multi-MW wind turbine

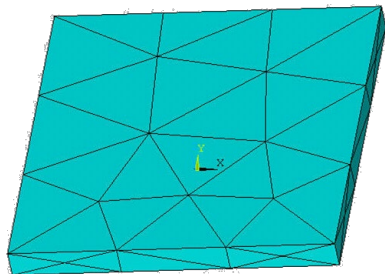
Component models



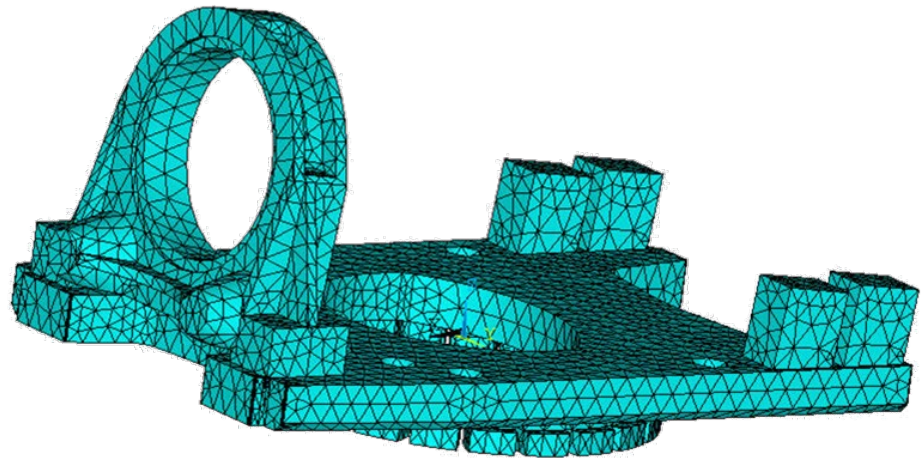
Tower top and yaw ring



Yaw gearbox



Yawpad

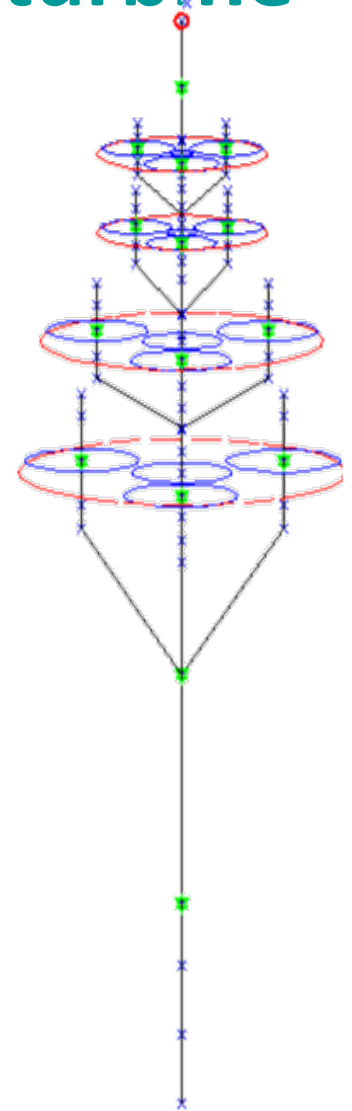
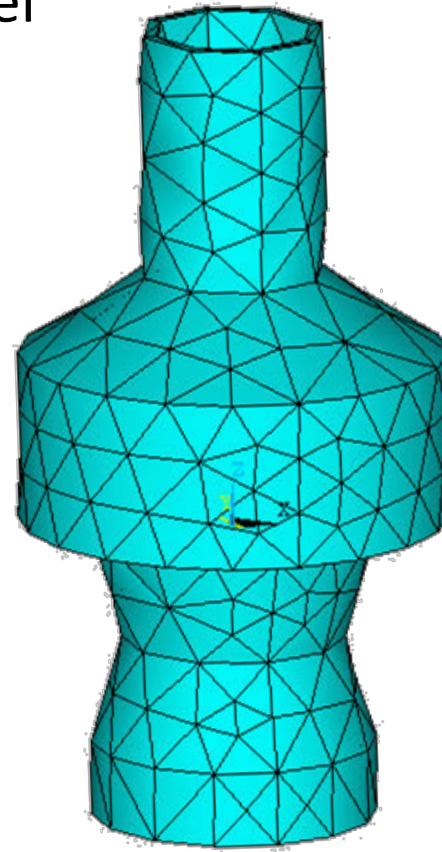


Bedplate

Application to a multi-MW wind turbine

Component models

- Yaw gearbox model is built from 2 submodels:
 - Yaw gearbox housing model
 - Yaw gearbox gear model

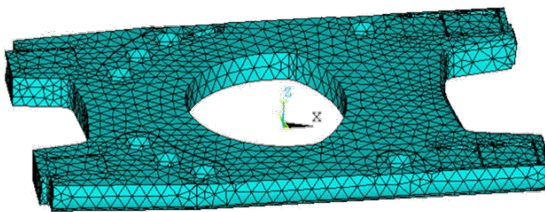
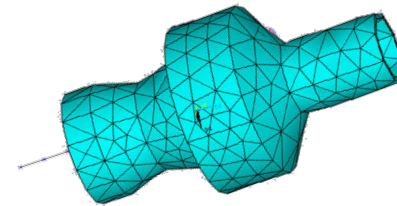
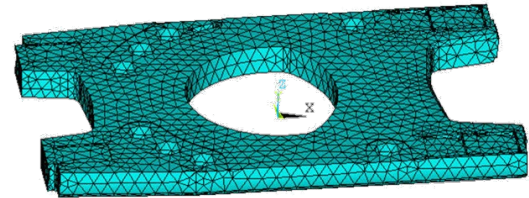


Application to a multi-MW wind turbine

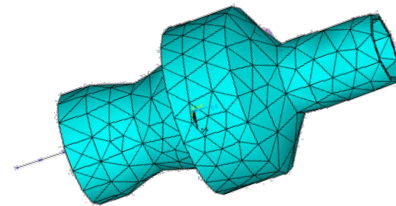
Measurements for component validation

Measurements performed to validate:

- Simple bedplate model:
- Yaw gearbox model:
- Assembly of bedplate and 4 yaw gearboxes:



+ 4 x



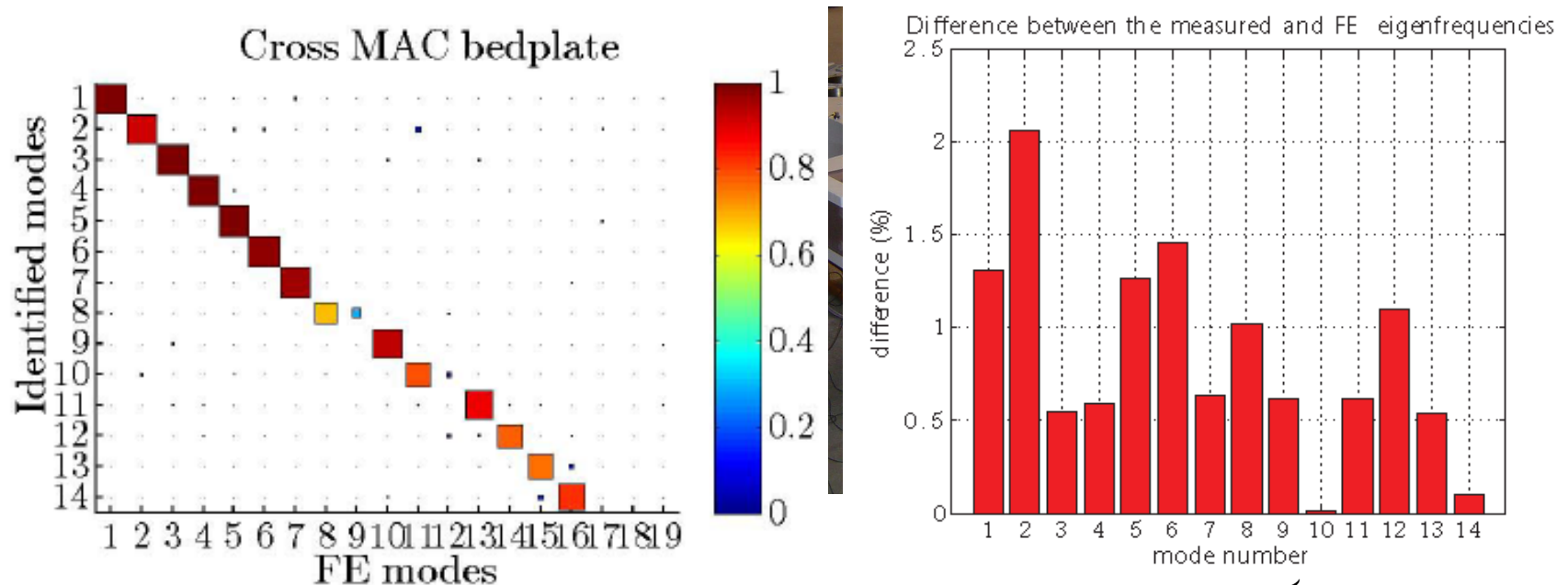
Application to a multi-MW wind turbine

Measurements for component validation

Bedplate

Measurement performed to validate the bedplate model

- 33 locations measured using 3D accelerometers
- Excitation in z-direction using random signal



Application to a multi-MW wind turbine

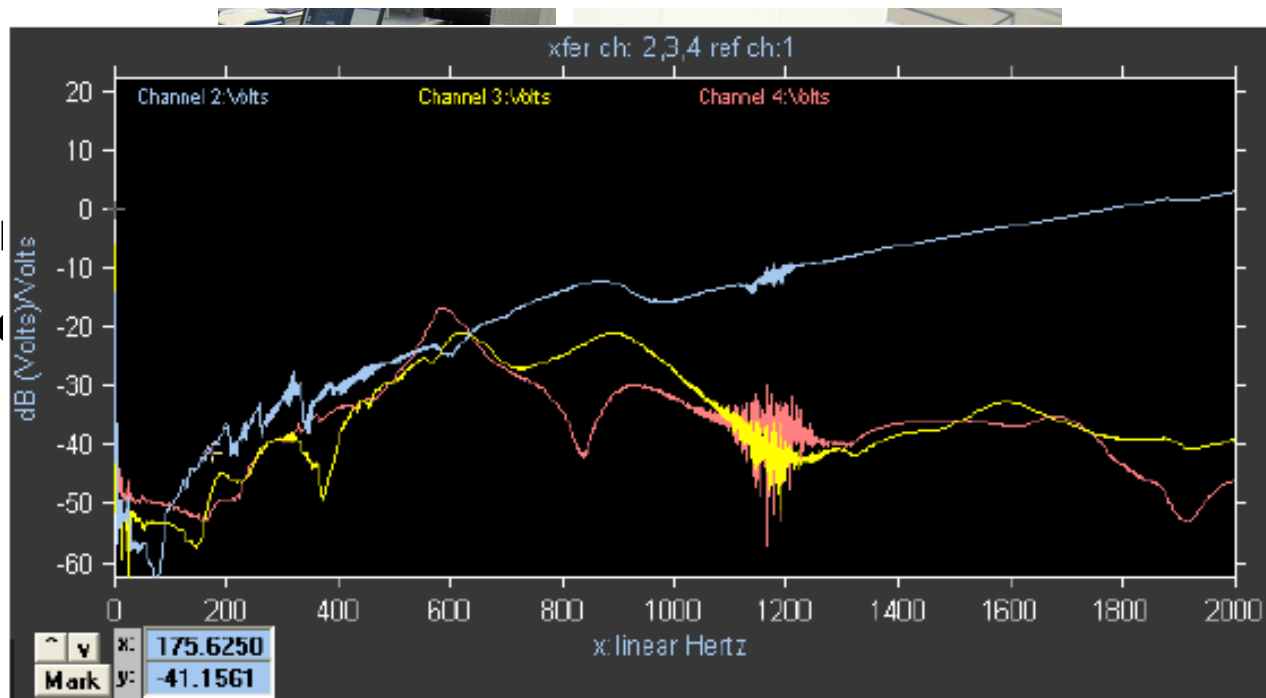
Measurements for component validation

Yaw gearbox

- Shaker attached to output pinion
- 3D accelerometer at input pinion

Crucial

- Gear
- Preload



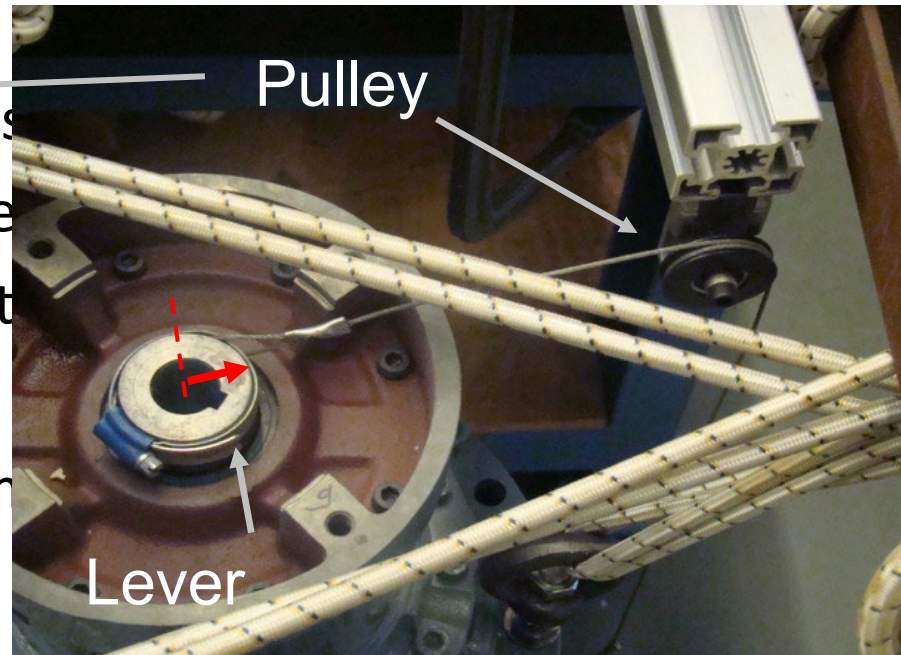
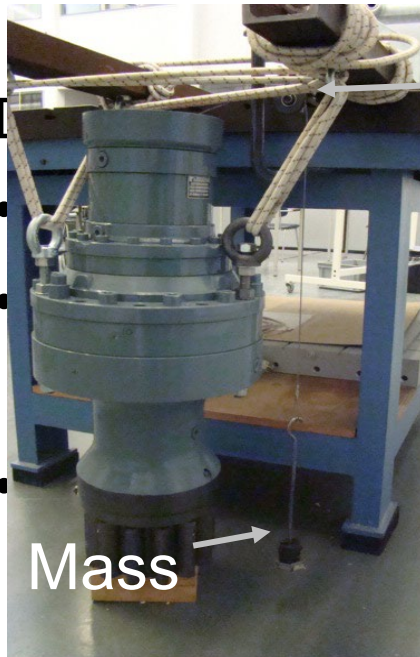
Application to a multi-MW wind turbine

Measurements for component validation

Yaw gearbox

Preload applied:

- Using a mass suspended on a cable



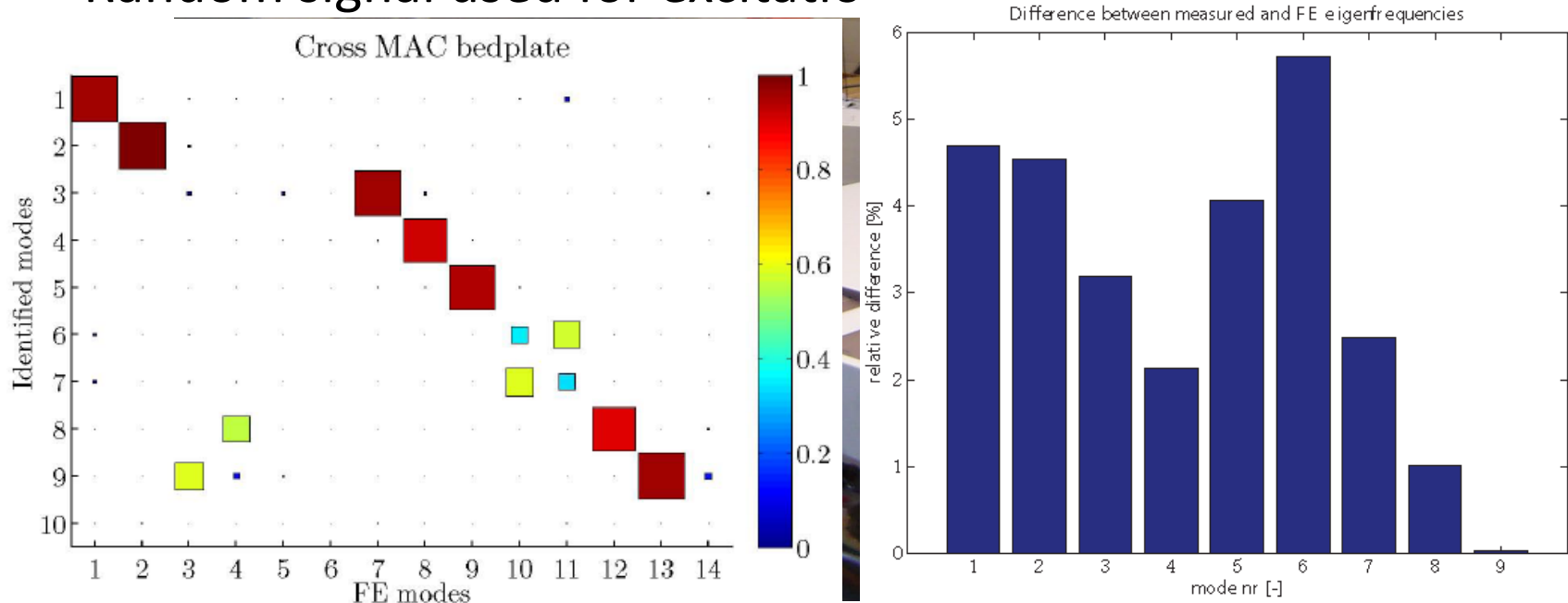
Application to a multi-MW wind turbine

Measurements for component validation

Bedplate – yaw gearboxes assembly

An Assembly was created from bedplate and 4 yaw gearboxes

- Eigenfrequencies measured using accelerometers
- Random signal used for excitation

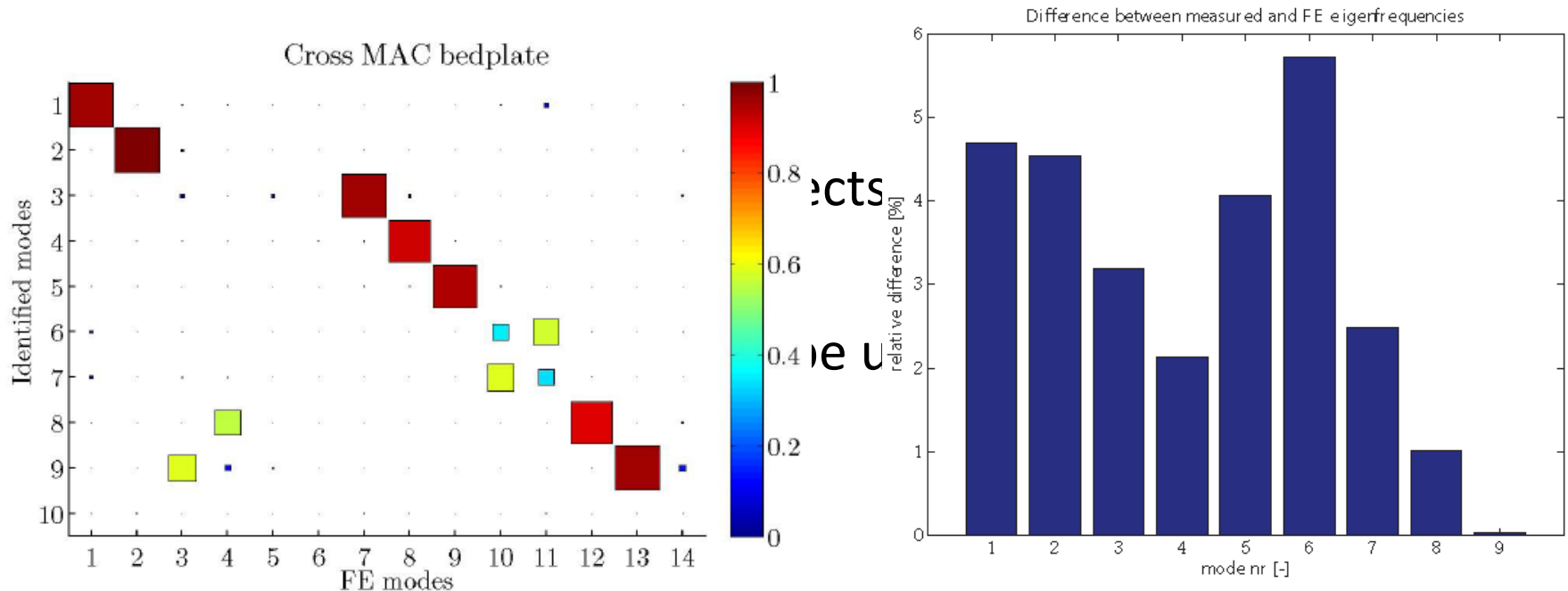


Application to a multi-MW wind turbine

Measurements for component validation

An assembly was created of a bedplate and 4 yaw gearboxes

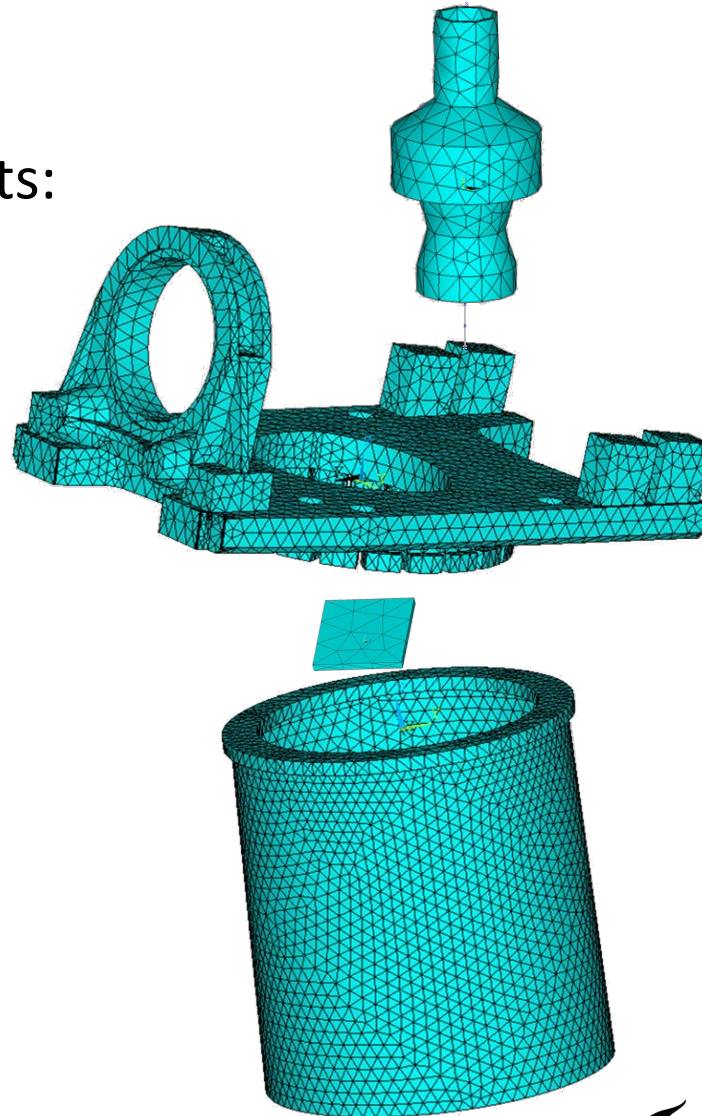
- First 5 eigenmodes and 8 and 9 show a high correlation
- Frequency difference $< 5\%$



Application to a multi-MW wind turbine

Analysis results

- Assembly of components:
- 1 Bedplate
- 22 Yaw pads
- 1 Tower top and yawring



Application to a multi-MW wind turbine

Analysis results

Full structure model as reference (293.000 DoF):

Frequency error [%]

- 1-MAC value [-]

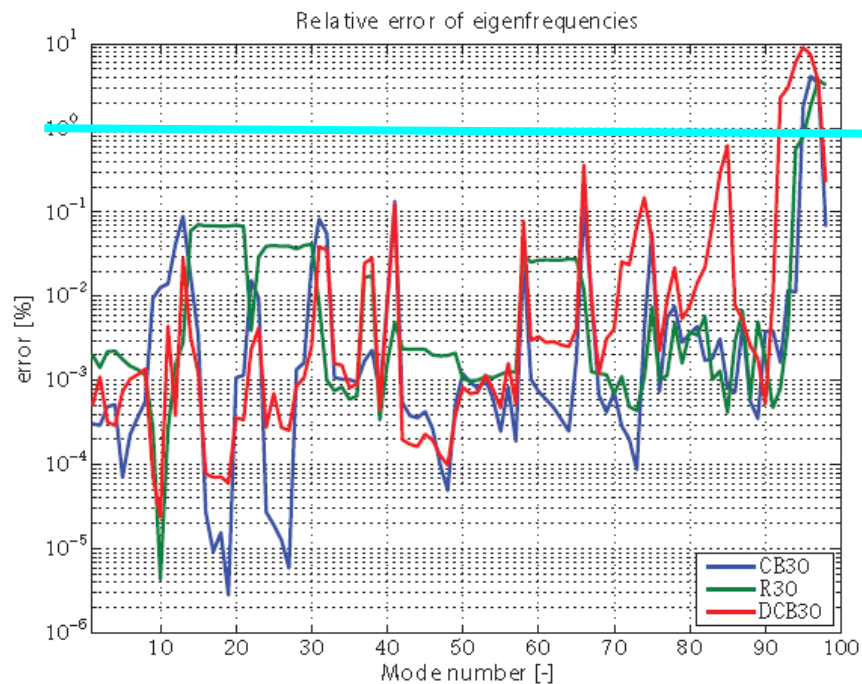
Reduced structure models

- Craig Bampton method (7929 DoF)
- Dual Craig Bampton method (8637 DoF)
- Rubin's method (7881 DoF)

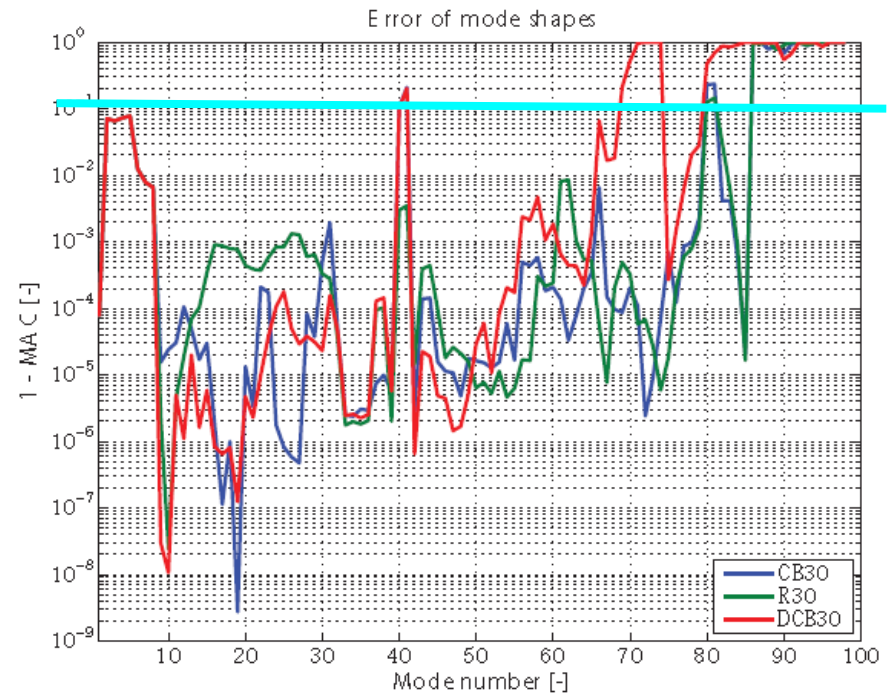
Comparison of results

Reduction methods

Error on frequencies [%]



1 - MAC [-]



Comparison of results

Reduction methods

- Reduced models accurate up to the 80th eigenmode
- Reduction of approximately a factor of 35!
- Large number of DoF are interface DoF (> 90%)
- Apply an extra reduction step to reduce the interface DoF

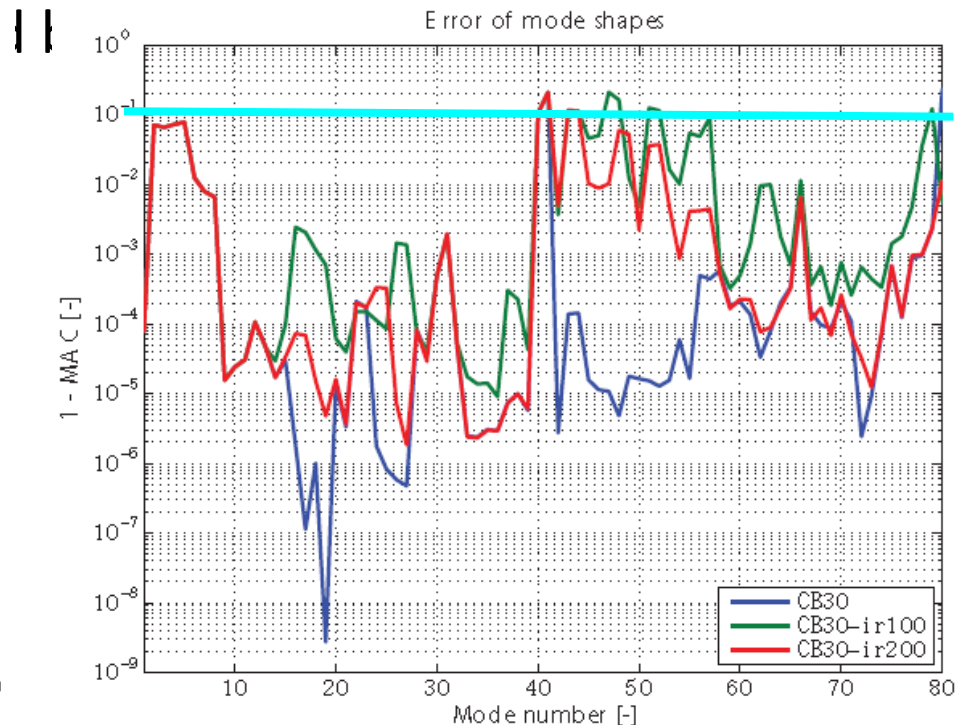
Reduced models

- Craig Bampton, 100 interface modes (730)
- Craig Bampton, 200 interface modes (830)

Comparison of results

Interface reduction methods

- Accurate up to the 80th eigenmode
- Small number of total DoF (730 vs. 293.000) - MAC [-]



Conclusions and recommendations

Conclusions

- The general framework was implemented
- Y system was accurately modeled using only 730 DoF
- Total reduction of a factor 400!
- The "goal of the MSc assignment was to develop a framework for the application of dynamic substructuring within wind turbine engineering"

Questions

