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MINOR PROJECT

FLOW VELOCITY
AT
RUBBLE MOUND BREAKWATER TOES

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1. INTRODUCTION

1.1 BACKGROUND OF STUDY

This study is being undertaken as a minor research project at TU Delft as part of a Masters Programme in Hydraulic Engineering. A minor project has a typical duration of 8-12 weeks which is significantly shorter than a masters project which typically lasts 6-9 months. Minor research projects aim to assist and complement larger research projects or existing master thesis work and are more limited in scope due to the short time frame involved.

This study aims to complement work undertaken by Stephan Baart in 2008 where he investigated 'Toe structures for rubble mound breakwaters'.

1.2 BACKGROUND OF RESEARCH

Rubble mound breakwaters are frequently constructed in the maritime sector to protect infrastructure or land and to provide calmer waters. In the past research has been focused on armour layer stability as well as serviceability criteria. A result of the research into stability of armour has led to the frequently used Van der Meer and Hudson stability formulas for design. However, knowledge of stability criteria for the toe is still limited resulting in designers using past experience or rules of thumb based on practical knowledge.

Most outline breakwater designs are scale tested in a flume, which may result in design changes to improve stability. An improvement in knowledge and design guidance on toe stability would reduce the risk of major design changes being discovered at the scale testing phase and may reduce costs in design, testing and construction as overdesign would be reduced and an optimal design chosen early on.

Currently, toe stability is assessed by considering an acceptable damage level (NoD or %) which is linked to external loading parameters (wave height/ water level etc.) and resisting parameters (rock diameter / height of toe) typically via a stability number. This approach is mainly based on empirical experiments and fitted curves and has a limited relationship with the physical processes. A disadvantage of this approach is that the acceptable damage level as expressed does not take into account where the damage takes place or the structural impact of this damage. In addition, this approach is often limited in the application by the constraints and geometry of the experiments i.e. any significant deviations from the experimental set-up in the design conditions may result in large errors in the design.

Hence, a more process oriented approach with hopefully fewer drawbacks is desirable for design. A two step parameterisation model which focuses on physical processes has been proposed by Baart in his Master's Thesis in 2008 (Baart 2008). He proposes a two step model which seeks to correlate the load parameters and geometry to determine a local flow velocity in a first step. In a second step the model seeks to correlate the local velocity to a damage/ transport level. This short laboratory based research work intends to focus on the first step, the premise of correlating load parameters and geometry to determine a local flow velocity.

Laboratory tests have been carried out in the past concerning themselves with stability to breakwater toes establishing a direct link between load and a damage parameter (NoD) rather than a flow velocity. Notably, Gerding (Gerding 1993), Docters van Leeuwen (1996) and Van der Meer (1998) have carried out tests recently on breakwater toes. Most relevant to this research study is the laboratory work by Gerding which indicates the damage parameter for a given wave load and geometry.

Due to the short nature of the research duration and associated short report it is assumed that the reader is reasonably familiar with the subject matter discussed. Readers unfamiliar with the subject are encouraged to refer to 'Bed, Bank and Shore Protection' by Schiereck in the first instance and thereafter refer to the original thesis work undertaken by Baart and Gerding which elaborate the theory and relevant work in detail.

1.3 OBJECTIVE OF RESEARCH

This short research study aims to focus on the physical processes involved in the stability of breakwater toes and their parameterisation.

In particular, this research aims to further research linking load, geometry and a local velocity at the toe of a breakwater which would help lay the foundations for a possible two step parameterization model such as proposed by Baart.

The objective for this research is to focus solely on the velocity at the breakwater toe and its parameterisation or possible formulation as this is seen to be a first step towards a physical process model. It is expected that further research will be required to verify any initial results produced within the study as the number of experiments conducted will be very limited due to the time frame available. Further additional studies will also be required to consider the link between the damage level and any parameterized critical threshold velocity and a damage parameter which would enable design work.

2. OVERVIEW OF KEY PROCESSES & FORMULATIONS

A brief overview of the key forces, processes and formulations involved is given below.

2.1 OVERVIEW OF PROCESSES & FORCES

An overview schematic of a typical breakwater cross section is provided in Figure 1 below. Rocks in the toe structure are exposed to stabilising forces such as weight and friction/interlock and destabilising forces primarily due to wave action resulting in local flows through and above the toe. This includes forces due to porous flow through the structure and forces due to a flow over the toe bund refer to Figure 2.

Schematic of typical breakwater cross section

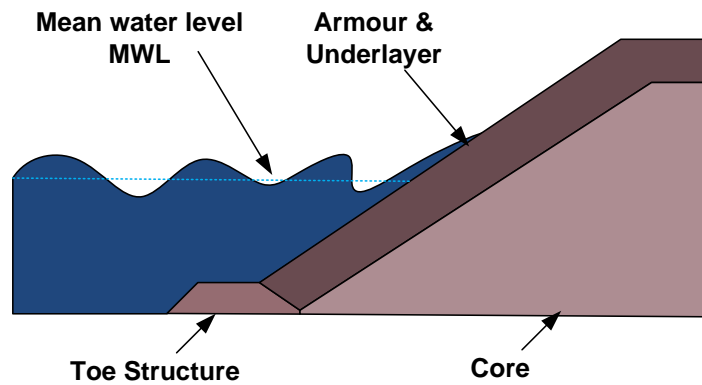


FIGURE 1 - SCHEMATIC OF BREAKWATER CROSS SECTION

Stylised cross-section of a Breakwater Toe

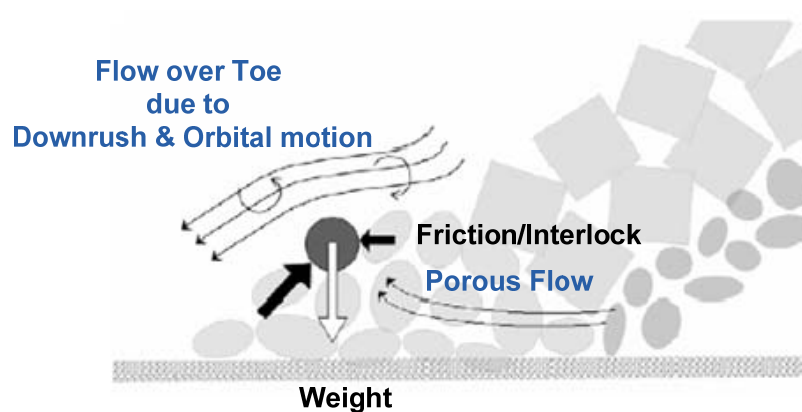


FIGURE 2-- FORCES ON TOE ROCKS, INITIAL FIGURE BY BAART 2008 WITH MINOR AMENDMENTS

2.2 OVERVIEW OF GOVERNING PARAMETERS

The porous flow velocity is likely to be dependent on the permeability of the structure, the head difference (Run-up, Run down, wave height, wave period) and the distance from slope.

The flow over the toe comprises of an element of wave down rush and wave orbital motion which are likely to depend on the wave height, period, run-up, rundown, slope of foreshore, slope of armour, permeability, roughness and the distance from slope.

Several of these parameters are dependent on each other and can be absorbed into key parameters and therefore do not require explicit inclusion in a model.

The perceived key governing parameters driving the local flow velocity u are

Loading based

- Wave height H expressed as either H_{m0} or H_s [m]
- Wave period, typically measured as peak, T_p [s]
- Water depth at the structure h_m [m]
- Kinematic Viscosity of fluid ν [$m^2 \cdot s^{-1}$]
- Gravity [ms^{-2}]

Toe Geometry Based

- Height of toe h_t [m]
- Width of toe structure b_t [m]
- Nominal stone diameter (roughness/voids) $Dn50$ [m]
- Slope of armour [-]
- Slope of foreshore [-]
- Distance from slope X [m]

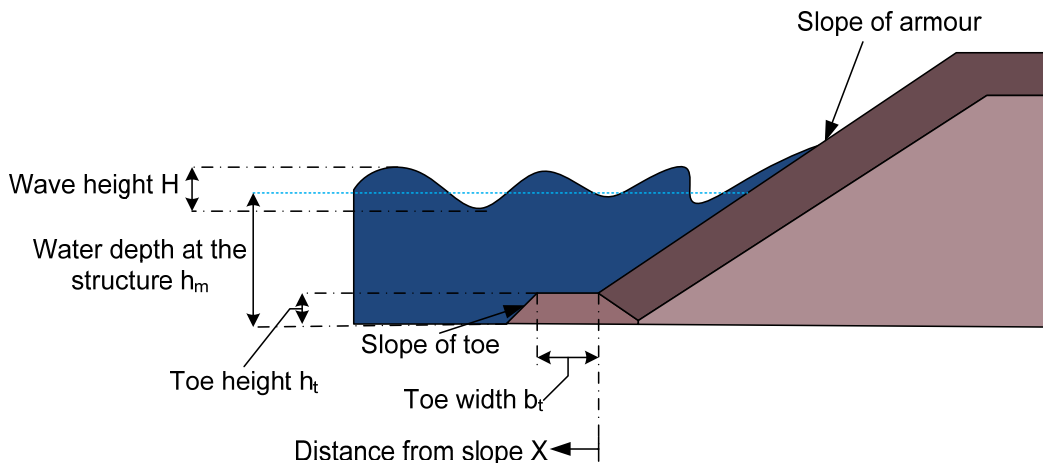


FIGURE 3- DEFINITION OF KEY PARAMETERS

2.3 POTENTIAL FORMULATION FOR LOCAL VELOCITY

There are existing formulations for local wave induced velocities in deep and shallow water without obstructions such as breakwaters. Observation shows that waves cause orbital or ellipsoidal motions which diminish in magnitude with increasing water depth. A common expression for a local wave induced velocity is provided by the linear wave theory which presents horizontal and vertical velocity for waves respectively as:

$$\text{EQUATION 1} \quad \mathbf{u} = \frac{\pi H \cosh [k(z+d)]}{T \sinh [kd]} \cos(\mathbf{kx} - \omega t)$$

$$\text{EQUATION 2} \quad \mathbf{w} = \frac{\pi H \sinh [k(z+d)]}{T \sinh [kd]} \sin(\mathbf{kx} - \omega t)$$

Where

- \mathbf{u} is the horizontal wave component of orbital velocity [m/s]
- \mathbf{w} is the vertical wave component of orbital velocity [m/s]
- H is the wave height
- T is the wave period
- k is the wave number ($2\pi/L$)
- ω is the wave angular frequency ($2\pi/T$)
- t is time and
- x is the horizontal direction

However, this expression is not valid in more complex cases when non-linear effects become significant.

Stephan Baart presented in his thesis the idea that the velocity at the toe of a breakwater may be presented by the two sinusoidal contributions one representing the orbital wave motion due to the incoming wave and a second sinusoidal type function due to the down rush component. He presents this as follows:

$$\text{EQUATION 3} \quad \mathbf{ub} = \hat{\mathbf{u}}_b \sin(\omega t + \varphi) = \hat{\mathbf{u}}_{bi} \sin(\omega t + \varphi_{TA}) + \hat{\mathbf{u}}_{bdr} \sin(\omega t)$$

Where

- $\hat{\mathbf{u}}_{bi}$ is the velocity of the incoming wave,
- $\hat{\mathbf{u}}_{bdr}$ is the velocity due to the downrush,
- φ_{TA} is the phase lag between the down rush and the incoming wave and
- φ is the phase lag between the run-up and the resulting velocity

3. APPROACH

3.1 OVERVIEW

The investigative approach chosen was to undertake physical model testing in a laboratory setting to determine whether typical velocity profiles exist at the toe and if they did, if they could be correlated to the geometry, loads and Baart's proposal.

This involved constructing a scale model of a breakwater toe inside a wave flume and generating specific wave fields (loads) with a wave generator whilst measuring velocities near the toe. The effect of the variation of key parameters on the local velocity is then reviewed.

3.2 LIMIT PARAMETERS & ENABLE COMPARISON

The study duration is relatively short; hence it has been decided to only investigate the effect of a few perceived key parameters. The remaining parameters are kept constant and may be investigated by later researchers.

Further, in order to enable a later comparison between velocity and damage, it has been decided to recreate Gerding's original experiments as far as possible whilst focusing on measuring local velocities. Hence, measured velocities in this study may later be correlated to levels of damage found by Gerding. The measured velocities are then analyzed to see whether there is a correlation between geometry and loads and whether the velocity potentially 'fits' Baart's proposed velocity equation. Dimensionless analysis and parametric curve fitting of data may also indicate potential formulations of velocity for a physical parameterization model.

4. LABORATORY TESTING

4.1 INTRODUCTION

All testing was undertaken at the TU Delft Hydraulics laboratory. The flume section available at the time was approximately 27m long, 0.8m wide and 0.9m high. This is smaller than the flume section available to Gerding who had a test flume of 50m length, 1m wide and 1.2m high. Hence, the experimental set-up by Gerding had to be marginally modified to fit within the available flume, a comparison between the model characteristics is provided in Table 1.

TABLE 1 - COMPARISON OF KEY PARAMETERS IN GERDING EXPERIMENT AND NEW EXPERIMENT

Description	Gerding Experiment	New Experiment
Flume Dimension	<ul style="list-style-type: none"> • 50m long • 1m wide • 1.2m high 	<ul style="list-style-type: none"> • 27m long • 0.8m wide • 0.9m high
Wave Characteristics	<ul style="list-style-type: none"> • Preset Jonswap spectrum 	<ul style="list-style-type: none"> • Regular waves • Pre-set Jonswap spectrum
Pre-set Significant Wave Height	<ul style="list-style-type: none"> • $H_s = 0.15\text{m}$, • $H_s = 0.2\text{m}$, • $H_s = 0.25\text{m}$ 	<ul style="list-style-type: none"> • $H_s = 0.1\text{m}$, • $H_s = 0.15\text{m}$, • $H_s = 0.2\text{m}$
Wave steepness $s = \frac{2\pi H_s}{gT^2}$	<ul style="list-style-type: none"> • $s = 0.02$ • $s = 0.04$ • $s = 0.03$ 	<ul style="list-style-type: none"> • $s = 0.02$ • $s = 0.04$
Toe stone diameter	Split flume into three sections <ul style="list-style-type: none"> • $D_{n50} = 0.017\text{m}$, • $D_{n50} = 0.025\text{m}$, • $D_{n50} = 0.035\text{m}$, • $D_{n50} = 0.04\text{m}$ with $D_{85}/D_{15} = 1.15 - 1.3$	Split flume into two sections: <ul style="list-style-type: none"> • Use $D_{n50} = 0.035\text{m}$ • Use $D_{n50} = 0.025\text{m}$ with $D_{85}/D_{15} = 1.15 - 1.3$
Water depths at structure	<ul style="list-style-type: none"> • $h_m = 0.5\text{m}$, • $h_m = 0.4\text{m}$, • $h_m = 0.3\text{m}$ 	<ul style="list-style-type: none"> • $h_m = 0.4\text{m}$, • $h_m = 0.3\text{m}$, • $h_m = 0.2\text{m}$
Duration	Each test 1000 waves	<ul style="list-style-type: none"> • Regular wave test approx. 50 waves • Jonswap wave field 1000 waves
Foreshore slope	<ul style="list-style-type: none"> • 1:20 	<ul style="list-style-type: none"> • 1:20
Armour slope	<ul style="list-style-type: none"> • 1:1.5 	<ul style="list-style-type: none"> • 1:1.5
Toe height variation	<ul style="list-style-type: none"> • $h_t = 0.08\text{m}$, • $h_t = 0.15\text{m}$, • $h_t = 0.22\text{m}$ 	<ul style="list-style-type: none"> • $h_t = 0.08\text{m}$, • $h_t = 0.15\text{m}$
Toe width variation	<ul style="list-style-type: none"> • $b_t = 0.12\text{m}$, • $b_t = 0.2\text{m}$, • $b_t = 0.3\text{m}$ 	<ul style="list-style-type: none"> • $b_t = 0.12\text{m}$
Measurements	Rock displacement Damage no	Measurements to be taken : <ul style="list-style-type: none"> ○ Flow Velocity along a constant horizontal line (ADV) ○ Run-up/ run-down (mesh-gird) ○ Use dye/reflective particles to visualise particle orbit/ path

4.2 EXPERIMENTAL SET-UP

4.2.1 OVERVIEW

The Figure 4, 5 and 6 below provide a cross sectional overview and detailed cross section of the experimental set-up and measuring points. The Figure 7 provides an overview of the instrument and measuring set-up.

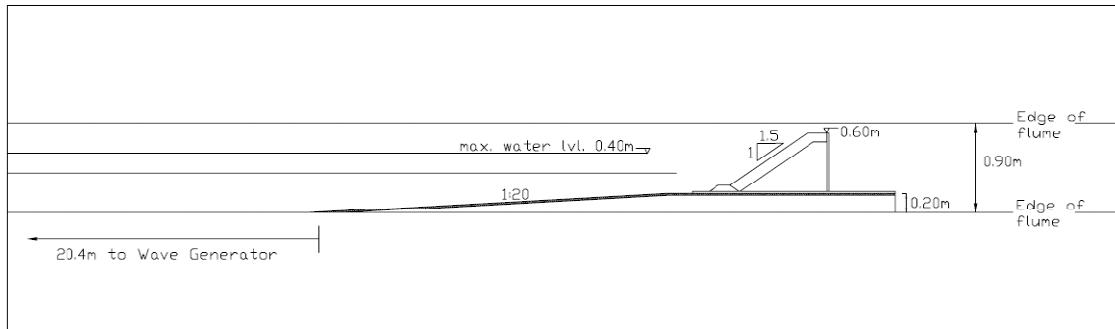


FIGURE 4- EXPERIMENTAL SET UP – CROSS SECTIONALOVERVIEW

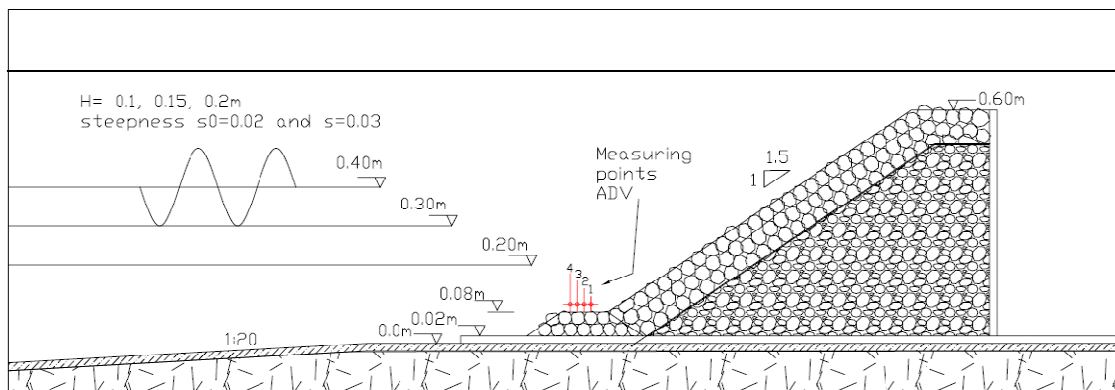


FIGURE 5- EXPERIMENTAL SET-UP – DETAILED CROSS SECTION

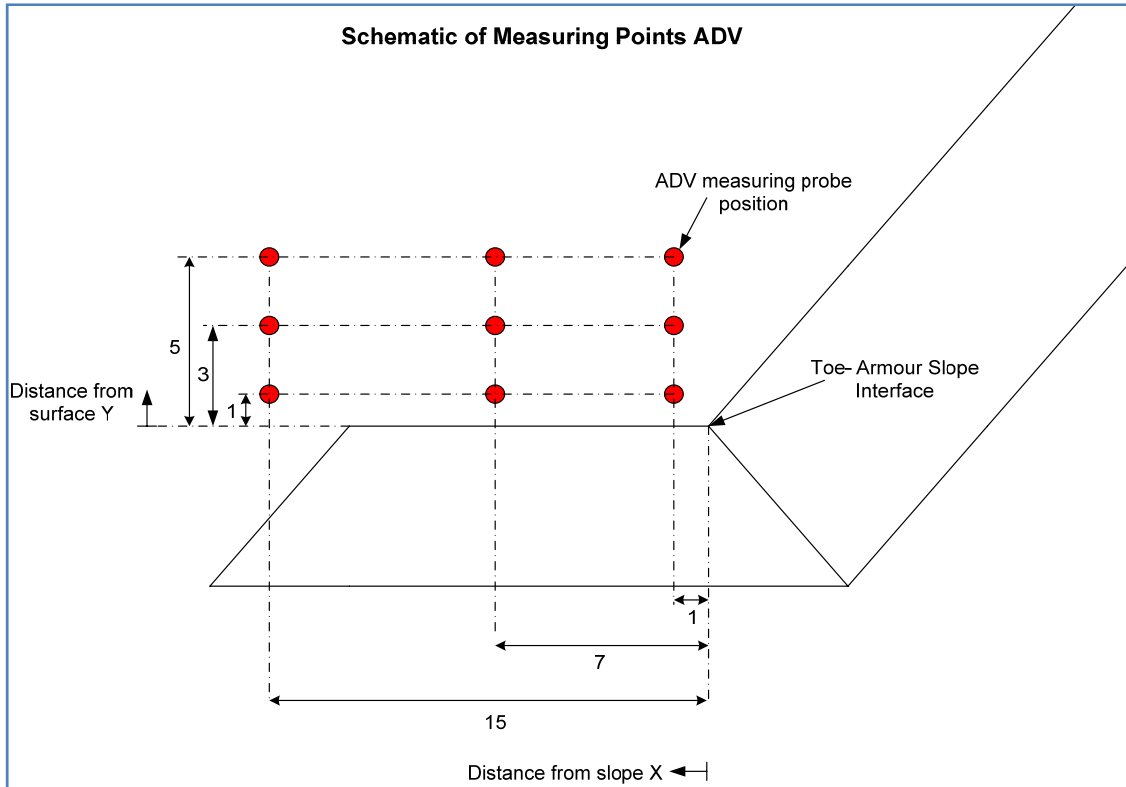


FIGURE 6- EXPERIMENTAL SET-UP – SCHEMATIC OF MEASURING POINTS (ALL MEASUREMENTS IN CM)

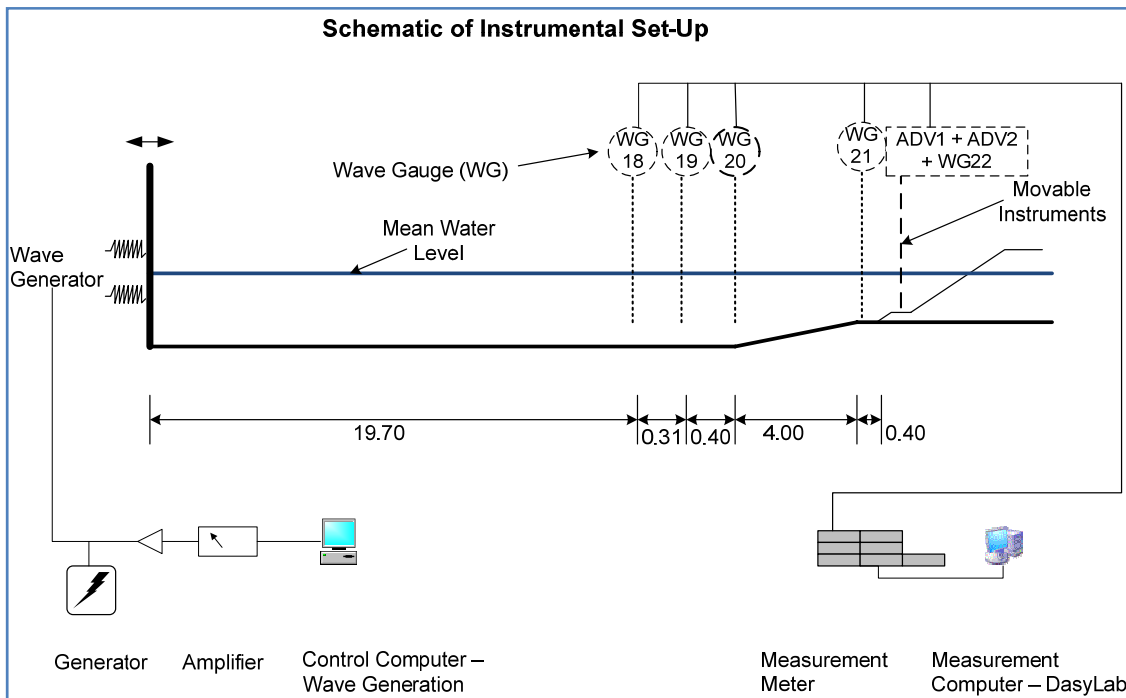


FIGURE 7- INSTRUMENTAL SET-UP (ALL MEASUREMENTS IN M)

4.2.2 DESCRIPTION

During the experiment waves were generated by a programme according to the testing schedule and then transferred to a 'control computer' which steered the wave generator. During the initial set-up and testing phase of the experiment numerous errors occurred with the 'wave compensator' due to the short length of flume and the large reflection caused by the presence of the breakwater. Systematic error checking was undertaken and the compensator repaired and the settings optimised by laboratory staff. However, even after repair the compensator remained vulnerable to high wave heights relative to low water levels. This meant that several scheduled tests could not be completed due to instrumental failure.

Wave gauges were placed before the slope to measure the actual wave height in the channel and to enable validation of the pre-set level. The wave gauge number shown in the figure above corresponds to the actual TU Delft water laboratory numbering system of wave gauges.

For the velocity measurement two Acoustic Doppler Velocimeters (ADV) have been utilized due to availability in the laboratory, ease of set-up and relatively high accuracy. The ADVs were placed on a moveable timber frame with a wave gauge (WG22) fixed on the centre line of the flume.

The ADV 1 has been fixed on the frame midway across the larger rock armour section ($D_{n50}=0.035\text{m}$). Similarly, the ADV2 instrument has been fixed in the centre of the smaller rock armour section ($D_{n50}=0.025\text{m}$). The timber frame allowed incremental horizontal movements and handles on the individual instruments with the measuring rod attached allowed for vertical movement. It was noted during prior experimentation with the ADVs that ADV1 has previously shown errors on one beam, the beam 3. Hence during testing the positive y-direction beam was placed in direction parallel to the incident waves to enable accurate measurements in this direction. For the ADV2, the standard setting of the x-direction parallel to the incident wave direction has been used. The Table 2 indicates the direction and output of velocity files.

It should be noted that an important limitation of any ADV is the requirement to be immersed in water to provide readings. Further, the instruments provides inaccurate readings in too clear or too 'dirty' water due to the need to have a reasonable number of particles in the water to reflect the acoustic signal. Therefore the ADV readings were monitored during the experiment and the measured particle count was adjusted throughout accordingly to provide reasonable accuracy.

All instrument measurements were recorded synchronously via the software 'DasyLab'. The key parameters and output format are presented in the table below. Calibration coefficients on the output files were used to translate the output into actual beam velocities, xyz velocities and water level elevations. The calibration coefficients are given in the Table 3. For reference, an extract of the laboratory lab book is provided in the Appendix A.

TABLE 2 - DASYLAB OUTPUT AND FILE CONVENTION

<i>Instrument Input Channel</i>	<i>Description of measured quantity</i>		<i>Description</i>	<i>Output Column</i>
0	Time		Time	1
1	G18		Water level at G18	2
2	G19		Water level at G19	3
3	G20		Water level at G20	4
4	G21		Water level at G21	5
5	G22		Water level at ADV	6
measuring point (G22)				
6	ADV1-x	Beam 1	Southern Beam*	7
7	ADV1-y	Beam 2	Western Beam*	8
8	ADV1-z1	Beam 3	Northern Beam*	9
9	ADV1-z2	Beam 4	Eastern Beam*	10
10	ADV2-x	Beam 1	Western Beam*	11
11	ADV2-y	Beam 2	Northern Beam*	12
12	ADV2-z1	Beam 3	Eastern Beam*	13
13	ADV2-z2	Beam 4	Southern Beam*	14

* The convention for direction assumes a plan view from above onto the ADV, where the western beam is pointing towards the wave generator and the eastern beam towards the breakwater

TABLE 3 - INSTRUMENTAL CALIBRATION COEFFICIENTS

Description		Coefficient	Description	Coefficient
Water level		0.025		
Beam velocity		0.12		
Beam Velocity (BV) to X,Y,Z velocity Transformation Matrix (TM) coefficients as per instrument output file	ADV1 – B1 cof 1	8318/4096	ADV2 - B1cof 1	8161/4096
	ADV1 – B1 cof 2	8329/4096	ADV2 - B1cof 2	8165/4096
	ADV1 - B2 cof 1	8458/4096	ADV2 - B2cof 1	8425/4096
	ADV1 - B2 cof 2	8494/4096	ADV2 - B2cof 2	8362/4096
	ADV1 - B3cof 1	2134/4096	ADV2 - B3cof 1	2122/4096
	ADV1 - B3cof 2	2091/4096	ADV2 - B3cof 2	2108/4096
	ADV1 - B4cof 1	2182/4096	ADV2 - B4cof 1	1986/4096
	ADV1 - B4cof 2	2038/4096	ADV2 - B4cof 2	2236/4096

4.3 SUMMARY OF TESTING SCHEDULE

A testing schedule has been devised to enable the analysis of the change one parameter on the velocity. A summary of the testing schedule is provided in the tables below.

The local velocity measurements were undertaken in regular intervals at the same or similar geometric position for all experiments for comparison purposes. The typical grid positions include:

- typically a distance to the measuring probe from the average horizontal toe surface level Y of
 - 1cm, 3cm, and 5cm
- Two detailed experiments with additional Y measurements at:
 - 7cm, 9cm, 11cm, 13cm, 15cm and 17cm
- typically a distance from the toe/slope interface to the measuring probe X of
 - 1cm, 7cm and 15cm
- In addition some further positions of X
 - 3cm , 5cm, 9cm, 11cm and 13cm
- Measurements with the increased toe height of $h_t=0.15\text{m}$ were offset in the x-direction by 0.5cm due to a measuring error during the experiments

In some instances it was not possible to take measurement at a standardized measuring point due to localized water drawdown and excessive air entrainment affecting the measuring probe. In such cases an adjacent measurement position was sought in the first instance and if this also failed to yield adequate results then the point was abandoned.

TABLE 4 - TESTING SCHEDULE FOR REGULAR WAVES WITH TOE HEIGHT OF 0.08M

Regular Waves Test Name	Height of toe h_t [m]	Height of water h_m [m]	Wave Height H_s [m]	Wave Period T [s]	Wave Steepness S	Tested
R001	0.08	0.4	0.10	1.790	0.02	✓
R002	0.08	0.4	0.10	1.265	0.04	✓
R003	0.08	0.4	0.15	2.197	0.02	✓
R004	0.08	0.4	0.15	1.898		✓
R005	0.08	0.4	0.15	1.550	0.04	✓
R006	0.08	0.4	0.20	2.531	0.02	✓
R007	0.08	0.4	0.20	1.789	0.04	✓
R008	0.08	0.3	0.10	1.790	0.02	✓
R009	0.08	0.3	0.10	1.265	0.04	✓
R010	0.08	0.3	0.15	2.197	0.02	✓
R011	0.08	0.3	0.15	1.898		✓
R012	0.08	0.3	0.15	1.550	0.04	✓
R013	0.08	0.3	0.20	2.531	0.02	✗ failure
R014	0.08	0.3	0.20	1.789	0.04	✗ failure
R015	0.08	0.2	0.10	1.789	0.02	✓
R016	0.08	0.2	0.10	1.265	0.04	✓
R017	0.08	0.2	0.15	2.197	0.02	✓
R018	0.08	0.2	0.15	1.898		✗ failure
R019	0.08	0.2	0.15	1.550	0.04	✗ failure

TABLE 5 - TESTING SCHEDULE FOR IRREGULAR WAVES WITH TOE HEIGHT OF 0.08M

Irregular Waves Test Name	Height of toe h_t [m]	Height of water h_m [m]	Wave Height H_s [m]	Wave Period T [s]	Wave Steepness S	Tested
I020	0.08	0.4	0.10	1.790	0.02	✓
I021	0.08	0.4	0.10	1.265	0.04	✓
I022	0.08	0.4	0.15	2.197	0.02	✓
I023	0.08	0.4	0.15	1.550	0.04	✓
I024	0.08	0.4	0.20	2.531	0.02	* failure
I025	0.08	0.4	0.20	1.789	0.04	* failure
I026	0.08	0.3	0.10	1.790	0.02	✓
I027	0.08	0.3	0.10	1.265	0.04	✓
I028	0.08	0.3	0.15	2.197	0.02	✓
I029	0.08	0.3	0.15	1.550	0.04	✓

TABLE 6 - TESTING SCHEDULE FOR REGULAR WAVES WITH TOE HEIGHT OF 0.15M

Regular Waves Test Name	Height of toe h_t [m]	Height of water h_m [m]	Wave Height H_s [m]	Wave Period T [s]	Wave Steepness S	Tested
R030	0.15	0.4	0.10	1.790	0.02	✓
R031	0.15	0.4	0.10	1.265	0.04	✓
R032	0.15	0.4	0.15	2.197	0.02	✓
R033	0.15	0.4	0.15	1.898		✓
R034	0.15	0.4	0.15	1.550	0.04	✓
R035	0.15	0.4	0.20	2.531	0.02	✓
R036	0.15	0.4	0.20	1.789	0.04	✓
R037	0.15	0.3	0.10	1.790	0.02	✓
R038	0.15	0.3	0.10	1.265	0.04	✓
R039	0.15	0.3	0.15	2.197	0.02	✓
R040	0.15	0.3	0.15	1.898		✓
R041	0.15	0.3	0.15	1.550	0.04	✓
R042-R048						* failure

TABLE 7 - TESTING SCHEDULE FOR REGULAR WAVES WITH TOE HEIGHT OF 0.15M

Irregular Waves Test Name	Height of toe h_t [m]	Height of water h_m [m]	Wave Height H_s [m]	Wave Period T [s]	Wave Steepness S	Tested
I049	0.15	0.4	0.10	1.790	0.02	✓
I050	0.15	0.4	0.10	1.265	0.04	✓
I051	0.15	0.4	0.15	2.197	0.02	✓
I052	0.15	0.4	0.15	1.550	0.04	✓
I053	0.15	0.4	0.20	2.531	0.02	* failure
I054	0.15	0.4	0.20	1.789	0.04	* failure
I055	0.15	0.3	0.10	1.790	0.02	✓

5. RESULTS AND ANALYSIS

5.1 REGULAR WAVES

5.1.1. VERIFICATION OF LOAD CHARACTERISTICS

The recorded water level measurements were reviewed prior to analysis of other data to determine that the specified input wave height and periods were achieved for each experiment. For the verification of the actual wave heights and periods achieved in the model the measurements were evaluated using a standard TU DELFT matlab routine 'decomp'.

For the regular wave tests the measured 'offshore' wave height deviated by approx. 3-7mm and the measured peak wave period deviated by typically by about 0.002 of a second from those specified in the testing schedule.

5.1.2. REVIEW OF HORIZONTAL VELOCITY OVERALL

For the regular wave test, the measured velocity displayed a regularly repeating pattern for all experiments and both rock sizes tested. An extract from a typical velocity measurement record is shown in Figure 8 below. The measured regular pattern was not always simply sinusoidal and there appear to be other contributions affecting the velocity. Further, there are fluctuations in the local measured velocity which appear to be partly due to turbulence and partly due to measuring inaccuracies.

Nevertheless, the period of the measured velocity determined by a power spectrum density (PSD) estimate of the velocity was the same as the wave period which is in line with expectations. A plot of a typical PSD estimate is shown in Figure 9.

The PSD plot also shows a number of smaller peaks which are typically at frequencies which are a multiple of (a natural number) the peak period. In addition to this, there appear to be in some tests some very small peaks at around 40 to 45Hz which may be due to instrument noise. Noise overall in the PSD is small which only seen when zooming in very close and no particular pattern has been identified in this.

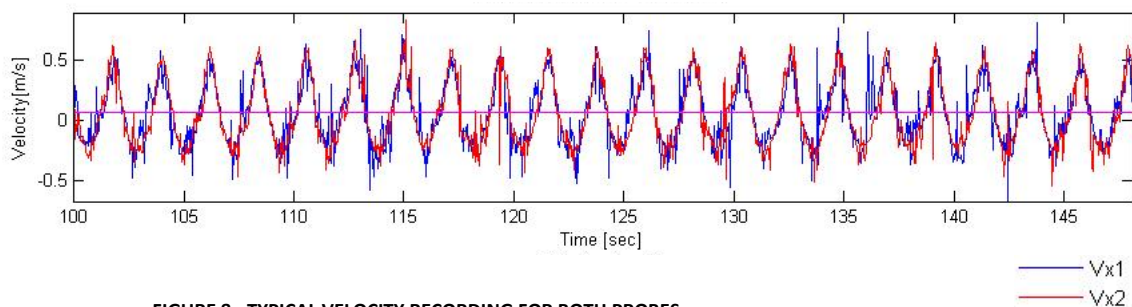


FIGURE 8 - TYPICAL VELOCITY RECORDING FOR BOTH PROBES

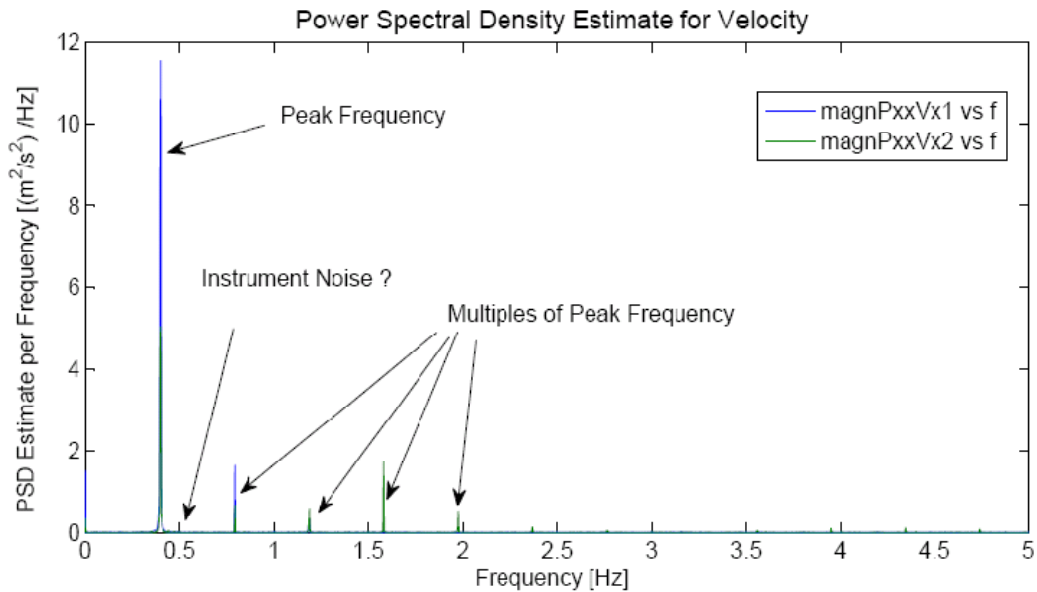


FIGURE 9 - TYPICAL PLOT OF PSD ESTIMATE FOR VELOCITY

5.1.3 REVIEW OF LOCAL WATER LEVEL AND HORIZONTAL VELOCITY

The PSD plot results have shown that the water level and velocity have the same period which indicates that the water level is the main driver of the velocity.

A Lissajous type plot correlating the local water level and velocity as measured at various locations along the toe has been undertaken for all experiments to develop an overall understanding regarding the relationship between the period of the water level and the period of the velocity and to establish whether these are in phase. In the plots the x and y axis have been fixed to the same scale for all experiments for comparison purposes.

Note

For readability of the report only a select few figures are included in the main body of the report, Lissajous type figures for all regular wave experiments are presented in the Appendix C. For the reader unfamiliar with Lissajous plots, the Figure 10 below has been included to show the most common shapes and their meaning in relation to phase and amplitude.

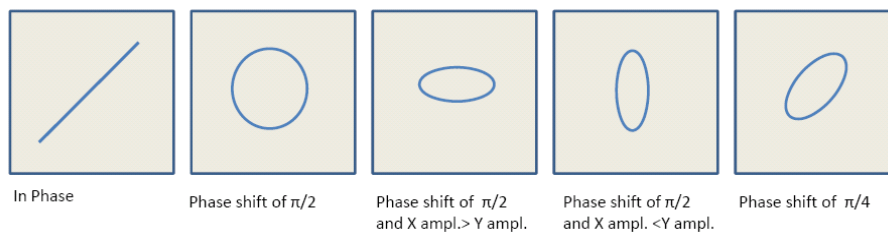


FIGURE 10 - TYPICAL SHAPES OF LISSAJOUS PLOTS

Influence of Toe Height

The figures indicate that the height of toe has little influence on the phase and only marginal differences are visible when comparing the R001 experiment series of plots with the R030 series of plots when all other parameters are kept the same. A representative example of the similarity is given in Figure 11 and Figure 12 which have identical wave loading parameters but different toe heights. Generally the shapes of the curves are very similar, but there appears to be a marginally larger phase shift for the higher toe level (the R030 series of experiments).

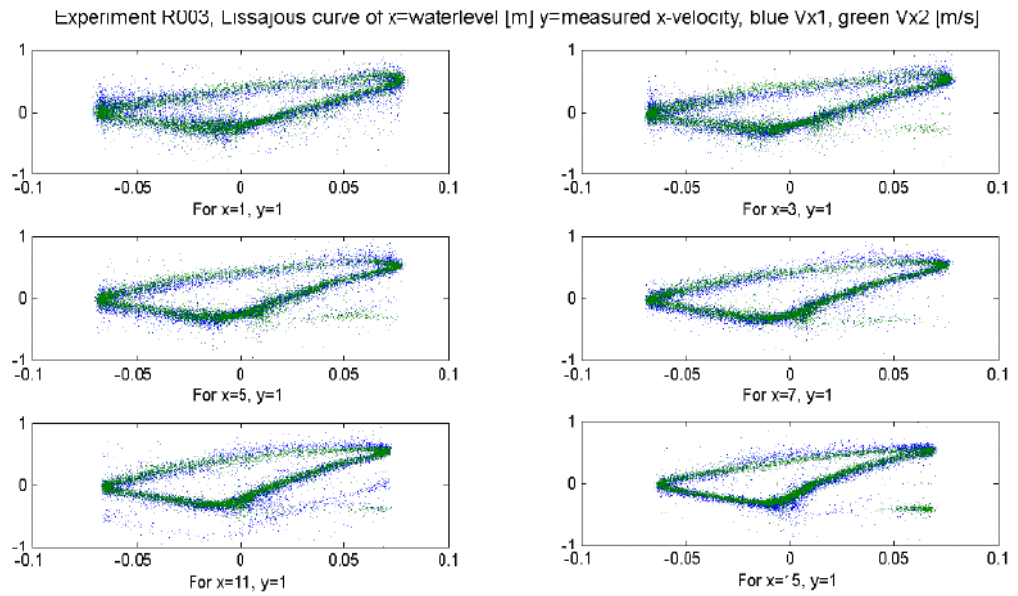


FIGURE 11 - LISSAJOUS PLOTS FOR R003 WITH HT=0.08M, HS=0.15M, HM=0.4M, TP=2.197

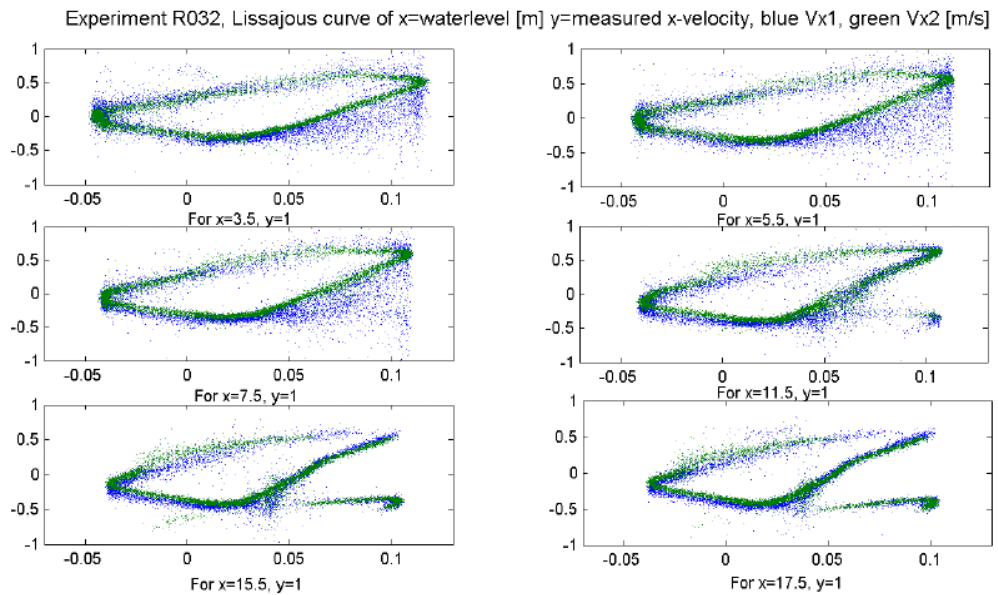


FIGURE 12 - LISSAJOUS PLOTS FOR R032 WITH HT=0.15M, HS=0.15M, HM=0.4M, TP=2.197

Influence of Wave Height to Water Level Ratio (Breaker Index)

The plots indicate that for low ratios of 'offshore' significant wave height to water level (typically $H_s/H_m < 0.3$) there is a small to no phase shift (approx. $0^\circ \leq \delta \leq 45^\circ$) dependent on the distance away from the toe (indicated by $x=$ below the plot). This ratio is also referred to in literature as the breaker index γ . An example of a Lissajous type plot with a low breaker index is given in Figure 13 below.

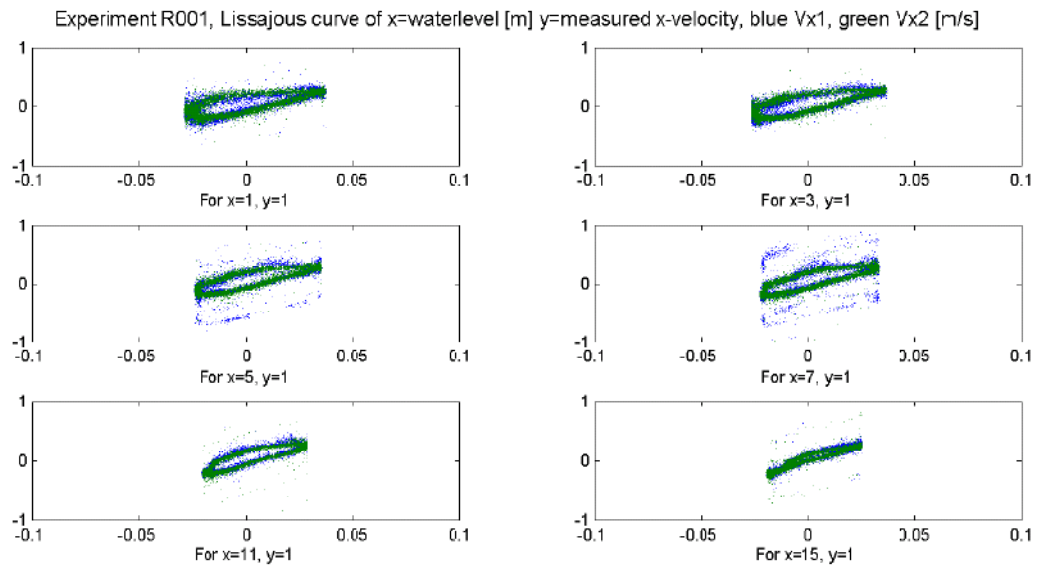


FIGURE 13 - EXAMPLE OF LOW BREAKER INDEX (WAVE HEIGHT TO WATER LEVEL RATIO < 0.3)

For larger breaker ratios (typically > 0.3) a significant phase shift is typically present. In addition the trough of the wave up to the mean still water level seems to display an inclined b-shape or wedge-shape in the Lissajous plot. An example of such a plot is shown in Figure 14.

Often, the crest of the wave appears in these plots in phase or only marginally out of phase. The bottom of the Lissajous shape indicates the presence of a sizeable additional velocity component which results in an increased amplitude and/or a phase difference at those location, particularly at the trough of a wave.

The additional velocity component could be viewed as the 'down rush' whereas the more regular oval shapes and lines could be seen as the regular wave orbital wave component. No attempt has been made to separate these contributions due to the variability in the data, the difficulty involved and the short time scale of the study. However, this may be an approach to quantify down rush in future and may validate the proposed velocity formulation by Baart (Equation 3).

Influence of Wave Period

The plots indicate that a higher wave period increases the phase shift.

Influence of Distance from Toe

The phase shift also appears to be dependent on the distance from the toe and varies. However, no particular pattern has been identified.

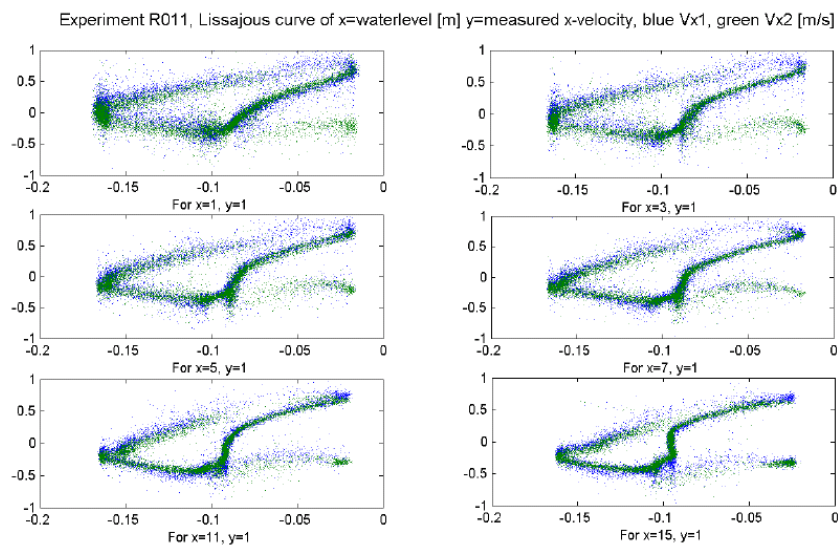


FIGURE 14 - EXAMPLE OF HIGH BREAKER INDEX (WAVE HEIGHT TO WATER LEVEL RATIO > 0.3)

5.1.4 CHARACTERISATION OF LOCAL HORIZONTAL VELOCITY

The measured results of the regular wave tests are numerous and large in size making analysis and characterization difficult. Curve fitting has been utilized to 'distil' the data to highlight potentially useful information from the remainder to enable the formation of any conclusions about the tests.

The velocity profile has been analyzed and fitted to a first order Fourier series (as shown in Equation 3) to determine a characteristic velocity and characteristic maximum velocity (as shown in Equation 4) that can be compared for a number of tests.

Further, Equation 3 is similar to Gerding's proposal for velocity (Equation) and can be easily transformed to fit Gerding's equation format. The residual, as shown in Equation 5, is considered the 'error' of the fit which includes random noise and turbulence. An example of measured versus Fourier fitted velocity curve and remaining residual is shown below in the Figure 15. A table which presents all Fourier coefficients for all regular tests is included in Appendix B.

EQUATION 3 $U_{fitted} = a_0 + a_1 \cos(\omega x) + b_1 \sin(\omega x)$

where $\omega = 2 * \pi / T$ and

T is the wave height period and

a_0 , a_1 and b_1 are constants of the fit

EQUATION 4 $U_{fitted\ max} = (a_1^2 + b_1^2)^{0.5} \pm a_0$

EQUATION 5 $Residual\ R = U_{measured} - U_{fitted}$

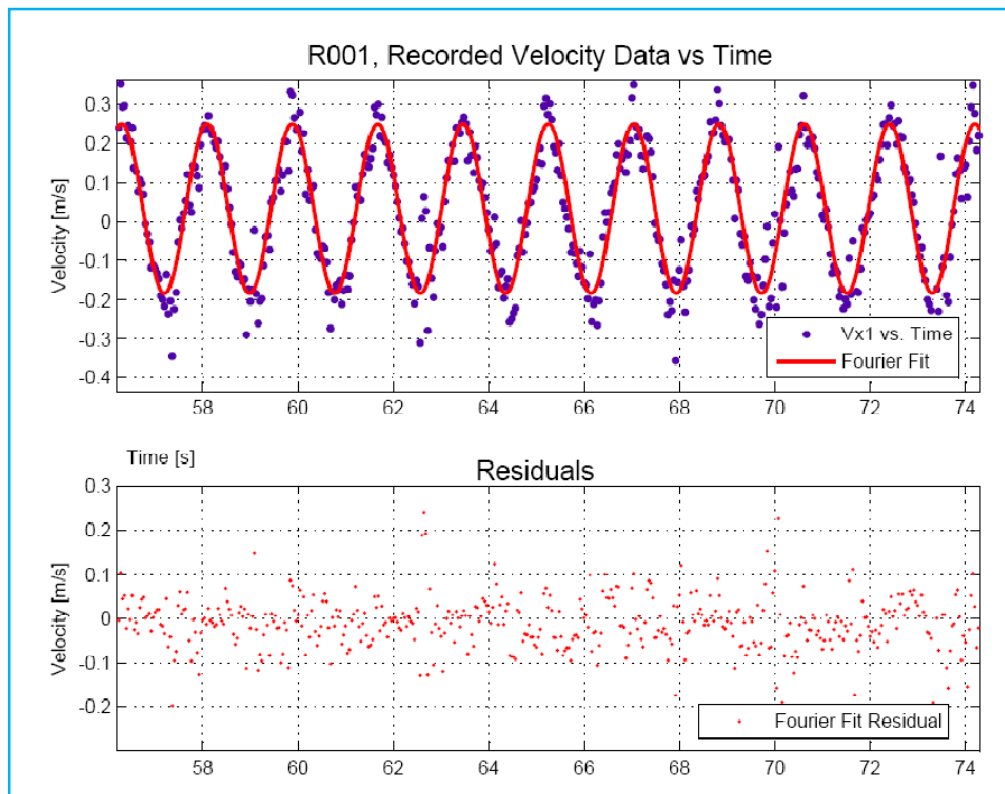


FIGURE 15 - FOURIER FITTED VELOCITY PROFILE FOR TEST R001

It should be noted that the first order Fourier fit utilized is less good for higher waves and for the rougher armour rock where turbulence is higher and higher order terms become more important. This means that the residual for those experiments is higher and the accuracy of the fit is lower and that curve fitted results of those experiments should be utilized with caution.

For each experiment a plot of the maximum characteristic velocity was undertaken to determine the maximum velocity distribution across the toe of the breakwater. For readability, only two representative plots one for the toe height of 0.08m (Figure 16) and one for the toe height of 0.15m (Figure 17) are included in the main body of the report, plots for all experiments are in the Appendix C.

The x-axis in the figures indicates the distance from the rock slope and toe interface positive in the direction away from the interface to the measuring point; the y-distance indicates the vertical distance from the average horizontal level surface of the rock toe to the measuring point. The dashed error bars indicate the averaged standard error of the first order Fourier fit for each ADV and measuring position.

Typically the figures show that the velocity measurements for the larger armour rocks (ADVx1 with rock armour $D_{n50}=0.035\text{m}$) are marginally higher than for the smaller rock armour (ADVx2 with $D_{n50}=0.025\text{m}$), and both are marginally higher than the theoretical results for velocity using linear wave theory in shallow water (U_0).

Further, on most plots a minor magnitude variation in maximum horizontal velocity is visible across the toe in a regular type distribution for both velocity probes (i.e. no major discontinuities present, not highly irregular across x direction).

It seems that for plots with a high water level to wave height ratio (H_s/H_m greater than 0.3) the velocity profile varies more and has a bigger difference between adjacent velocity positions than for low ratios. The plots with a low water to wave height ratio appear to have a 'flatter' velocity profile.

The location of the maximum velocity point in the distribution profile varied and no distinct pattern or trend has been identified in its location.

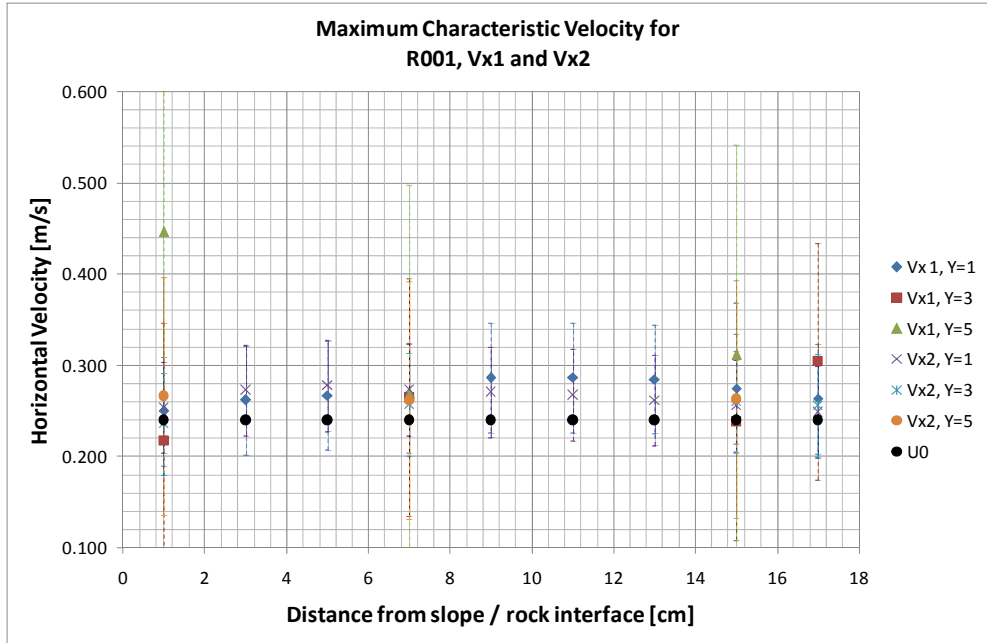


FIGURE 16 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R001

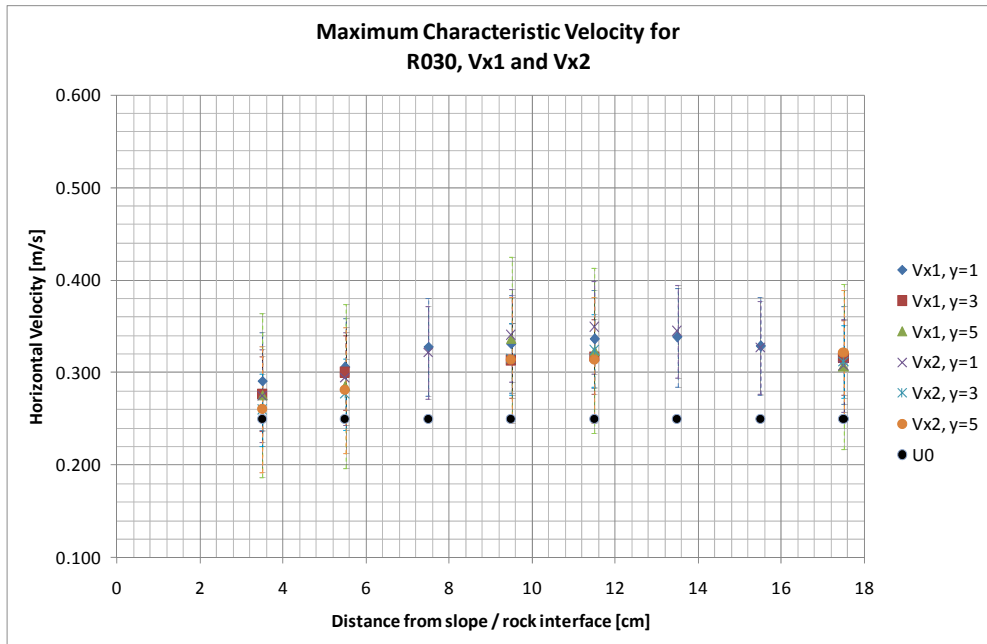


FIGURE 17 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R030

5.1.5 ANALYSIS OF CHARACTERISTIC LOCAL HORIZONTAL VELOCITY

The fitted measured maximum velocities derived in section 5.1.4. have been plotted against the theoretical linear shallow water maximum velocity at various locations along the breakwater toe to compare them. The figures are all formatted to the same linear scale and placed next to each other on the following three pages to facilitate comparison between them.

The plots shown in Figure 18 to Figure 23 indicate that for each water level and toe height a distinct pattern emerges which appears somewhat independent of the location from the toe along x and y.

The effect of the various positions of x and y appear result in a 'spread' of the graphs rather than changing the actual shape. The spread between the results for various locations x and y appears to be larger for the higher toe level than for the lower toe level which is shown in Figure 22 compared to Figure 18, however the number of tests is too small to come to a definitive conclusion on this.

Further, a similar shape pattern is achieved for both stone diameters i.e. ADVx1 and ADVx2, however the magnitude of the ADVx1 (the larger rock with $D_{n50}=0.035\text{m}$) pattern is generally higher. Refer to Figure 18 and Figure 19 which display similarity in shape, both figures show the characteristic maximum velocity versus the maximum linear velocity for the same geometric and loading conditions but different rock sizes.

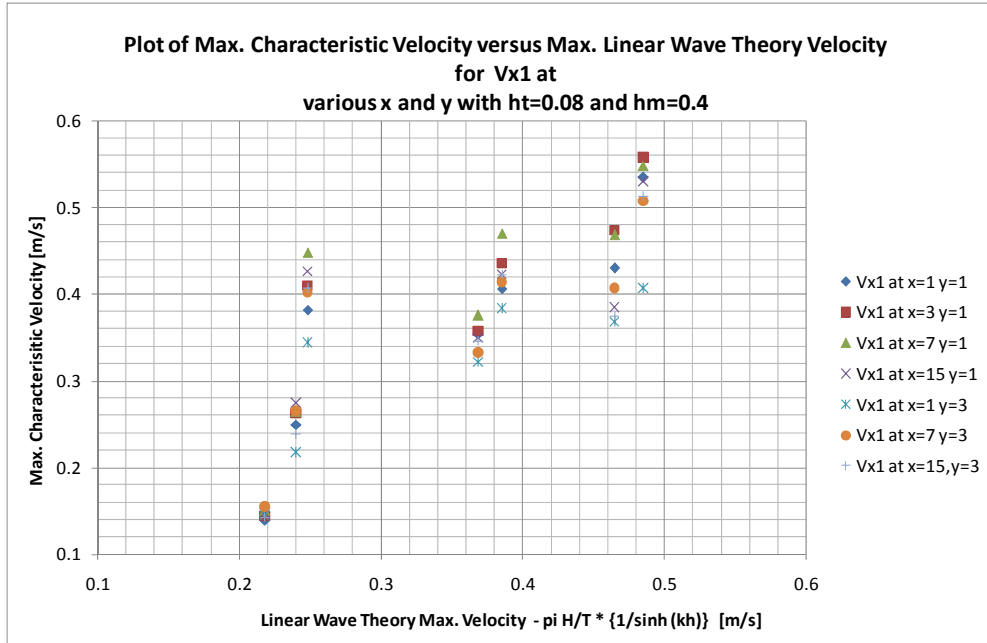


FIGURE 18 - MAX. MEASURED VELOCITY VERSUS LINEAR VELOCITY FOR HT=0.08M AND HM=0.4M FOR ADVX1

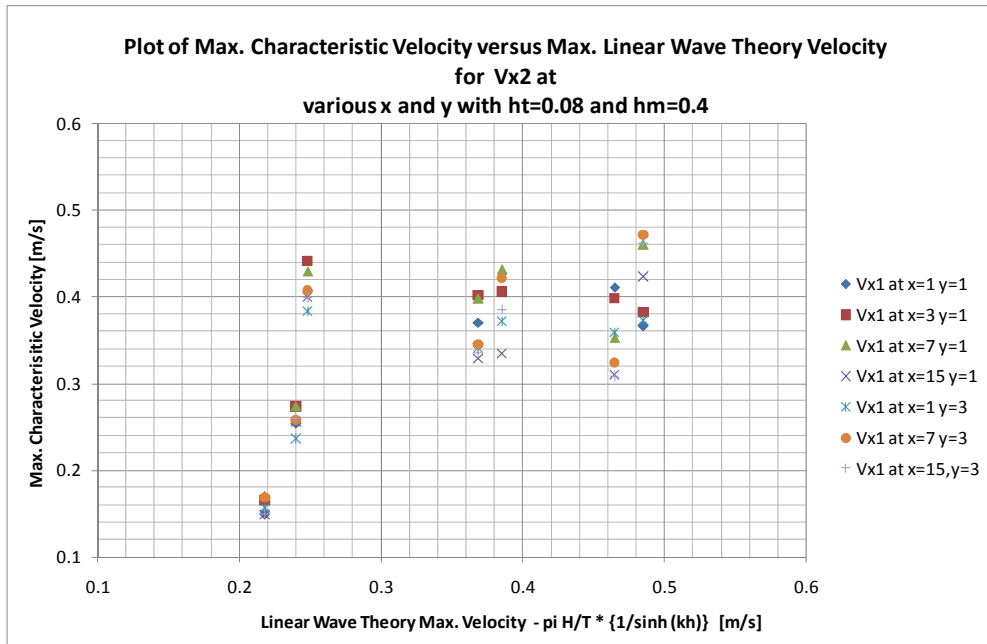


FIGURE 19 - MAX. MEASURED VELOCITY VERSUS LINEAR VELOCITY FOR HT=0.08M AND HM=0.4M FOR ADVX2

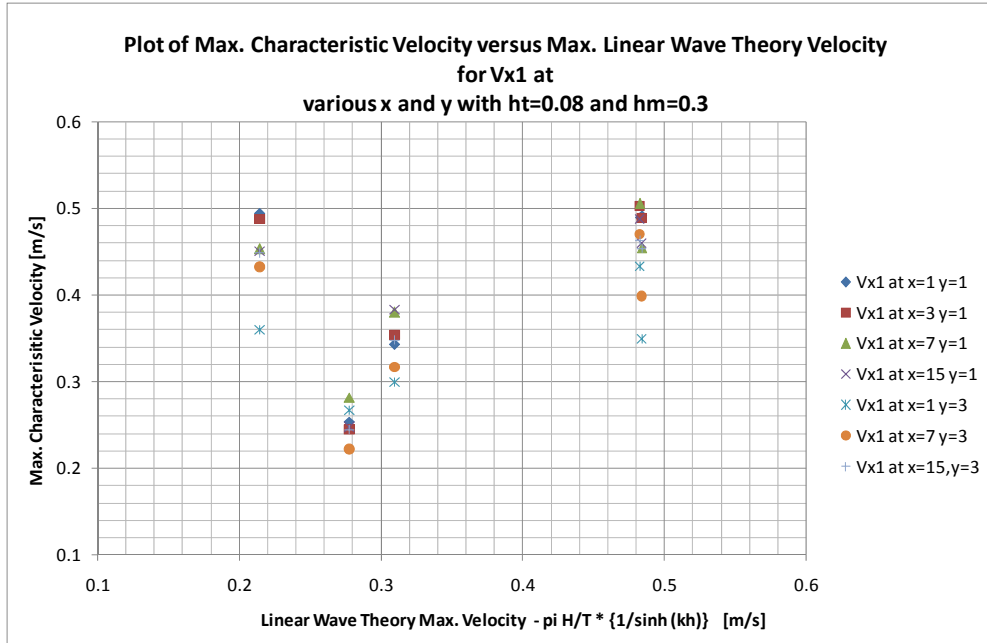


FIGURE 20- MAX. MEASURED VELOCITY VERSUS LINEAR VELOCITY FOR HT=0.08M AND HM=0.3M

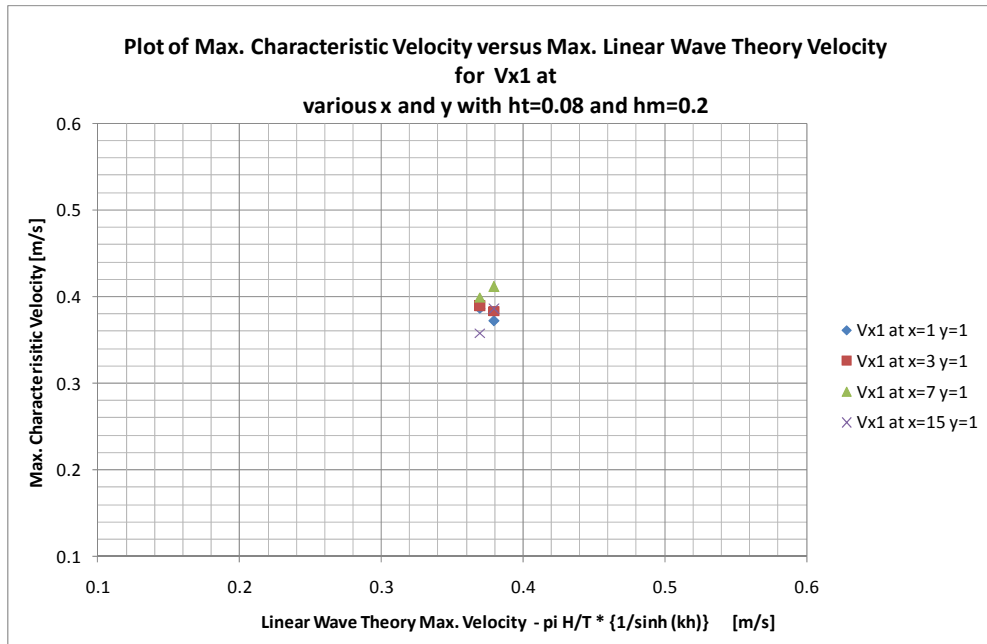


FIGURE 21 - MAX. MEASURED VELOCITY VERSUS LINEAR VELOCITY FOR HT=0.08M AND HM=0.2M

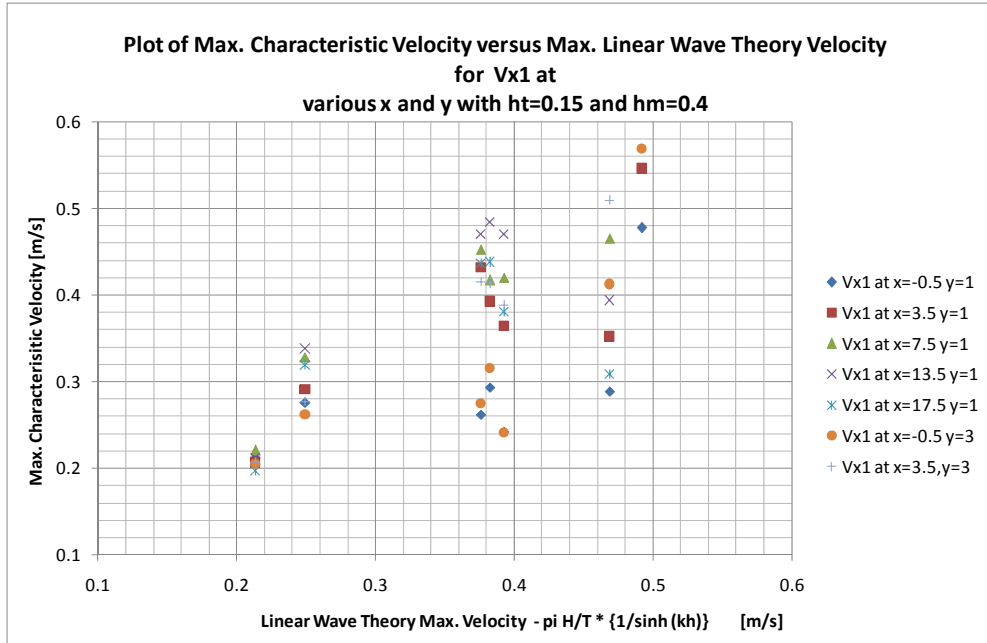


FIGURE 22 - MAX. MEASURED VELOCITY VERSUS LINEAR VELOCITY FOR HT=0.15M AND HM=0.4M

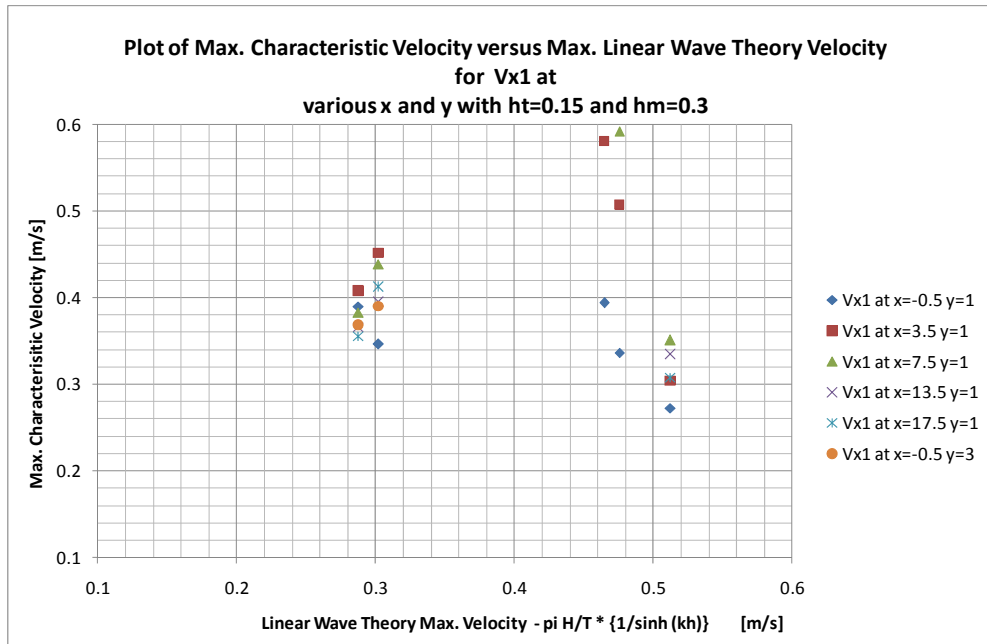


FIGURE 23 - MAX. MEASURED VELOCITY VERSUS LINEAR VELOCITY FOR HT=0.15M AND HM=0.3M

Development of adimensional empirical relationships

Plots of adimensionalised maximum velocity versus adimensionalised toe and water level (ht/ hm) have been undertaken for both rock sizes to determine if a 'generic' shape or relationship can be determined for any water level (hm). It was hoped that this would simplify the general shapes found in the previous plots.

The adimensionalised plots, refer to Figure 24 and Figure 25 appear to be showing a typical shape, a line with a step change or a straight line with scatter or two straight lines, for each wave height and wave period combination for both stone diameters (i.e. ADVx1 and ADVx2). The error bars show the standard error of the Fourier fit adimensionalised with respect to the linear wave theory shallow water velocity. The band width of the error and the spread between the individual sets of data points makes a determination of a simple linear formulation or description difficult.

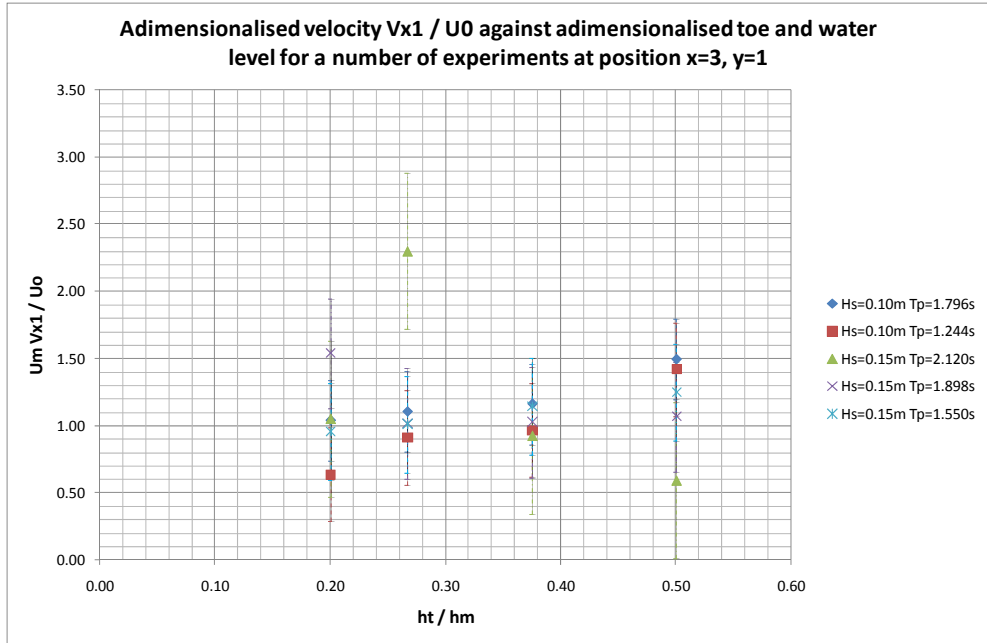


FIGURE 24 - ADIM. VELOCITY V_{X1} VERSUS TOE AND WATER LEVEL FOR VARIOUS WAVE HEIGHTS AND PERIODS

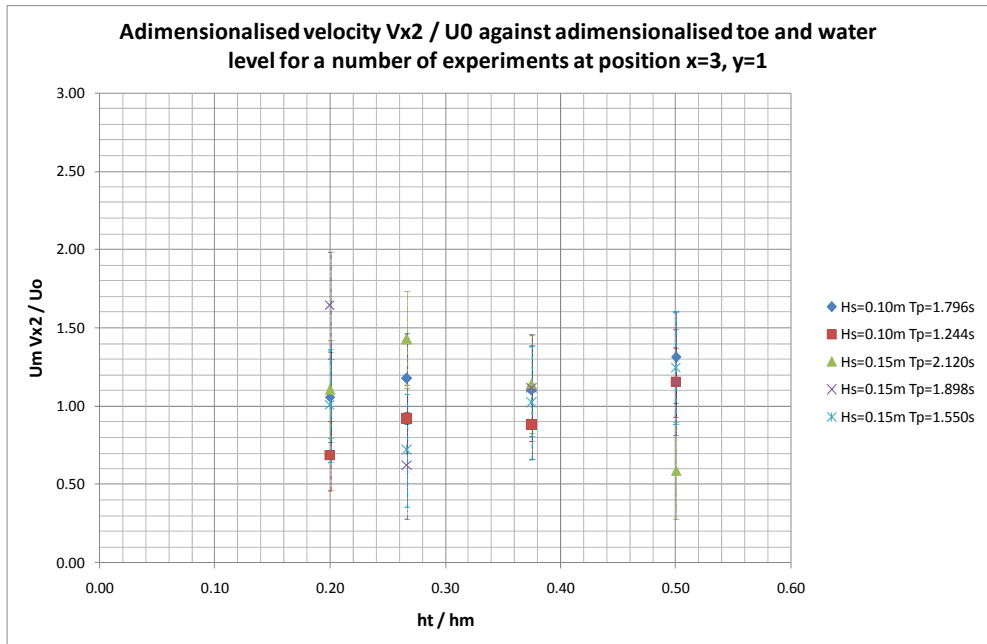


FIGURE 25 - ADIM. VELOCITY V_{X2} VERSUS TOE AND WATER LEVEL FOR VARIOUS WAVE HEIGHTS AND PERIODS

A further plot has been undertaken in order to reduce the spread between the sets of data points to enable a simple linear description of the data.

In this plot fictitious wave steepness has been included in the x-axis in order to be able to correlate to the Iribarren number. The Iribarren number represents the physical behavior of waves and would allow later researchers undertaking similar tests to include slope comparisons.

This new plot appears to be reducing the spread of the individual points, however significant scatter is still present. A linear trendline of the standard form shown in Equation 6 shows that the larger rock armour of Dn50=0.035m has a slope factor m of 0.017 and a coefficient of 1.105. For the smaller rock armour, Dn50=0.25, the results are similar with a slope factor of 0.015 and a coefficient of 1.034. However, the error bars are significant which raises the doubt on the reliability of these values. Please refer to Figure 26 and Figure 27 on the next page.

EQUATION 6 $y = mx + a$

EQUATION 7 $U_{max} = U_0 \left\{ m \frac{1}{\sqrt{s}} \left[\frac{h_t}{h_m} \right] + a \right\}$

EQUATION 8 $\xi = \frac{\tan(\alpha)}{\sqrt{s}}$

EQUATION 9 $U_{max} = U_0 \left\{ m\xi \left[\frac{h_t}{h_m} \right] + a \right\}$

Where α is the angle of the slope

s is the fictitious wave steepness $s = \frac{2\pi H}{gT^2}$

h_t is the toe height

h_m is the water level at the toe

ξ is the Iribarren number

U_0 is defined as $U_0 = \frac{\pi H_0}{T} \frac{1}{\sinh(k[h_m - h_t])}$

Final Comments

The results should be considered preliminary as the number of tests is insufficient to come to a definitive conclusion on empirical relationships and linear coefficient values. Significant more research is required to validate the above formulation. In further research the effect of the slope could be considered using the form of Equation 9.

Finally, it may be argued that in the Fourier curve fitting process, data was reduced and potentially some peaks may have been lost resulting in a reduced overall characteristic velocity. However, since the velocity is considered 'characteristic' and will be linked to actual armour movements in a two step model an absolute value is probably not necessary.

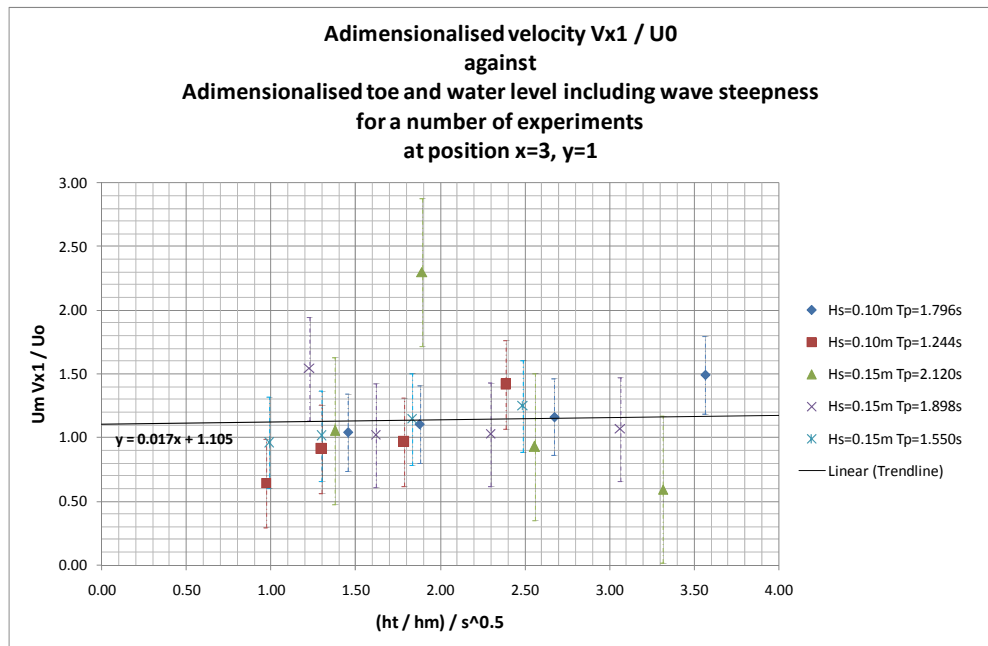


FIGURE 26 ADIMENSIONALISED VELOCITY PLOT FOR V_{X1}

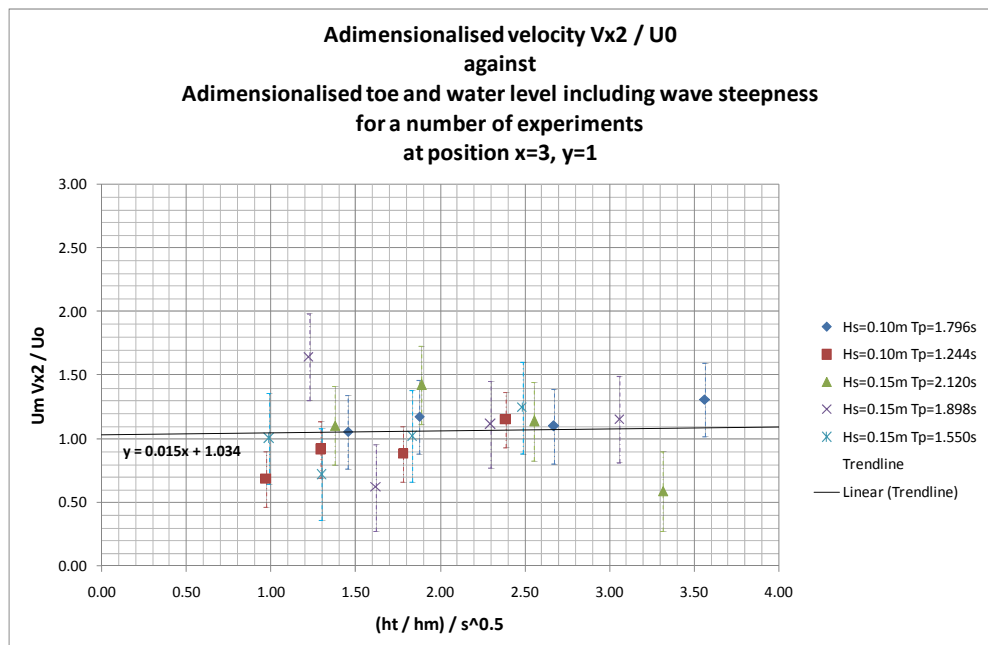


FIGURE 27 - ADIMENSIONALISED VELOCITY PLOT FOR V_{X2}

5.1.6 VERTICAL AND LATERAL VELOCITY COMPONENTS

No analysis of vertical and lateral velocity components has been undertaken due to time constraints. Recordings of those directions are available for analysis by others. However, caution should be exercised with these measurement results as the ADV1 has previously produced erroneous results for the beam 3. Further, a previous researcher using the ADV for velocity measurements has noted that the accuracy of the vertical velocity components is less and in some instances large errors are noted.

5.2 IRREGULAR WAVES

The irregular test data has not been reviewed or analysed due to time constraints and a number of associated difficulties inherent in the data collection and data analysis and hence these results are not presented in this report. The difficulties are briefly elaborated below.

5.2.1 IRREGULAR WAVES - DATA COLLECTION PROBLEMS

During and after recording the input significant wave height was verified against measured wave heights and generally large discrepancies were found, waves were typically significantly smaller than programmed/ scheduled.

It is believed that this is due to difficulties by the wave generator and compensator who were found to have a too short piston to cope with larger waves and large wave reflection. A couple of the tests were re-run again with higher wave settings than those in the testing schedule to compensate the overall lower output, but the generator tended to fail. Due to the problems with the generator in compensating reflecting waves no guarantee can be given that the input load characteristic are conform with a Jonswap spectrum at a given wave height and care needs to be taken when analyzing the data.

5.2.2 IRREGULAR WAVES - DATA ANALYSIS PROBLEMS

It is believed that the analysis method employed for the regular waves will not be applicable for the irregular wave tests due to their nonlinear nature. A spectral type approach or similar would be a possibility in analyzing the data and could lead to a characteristic maximum velocity.

Further, a decision will have to be made on the nature and definition of the characteristic velocity as there is no simple re-occurring maximum that can be statistically averaged. The wave loading characteristics change continuously for irregular waves and no repeat of the exact same conditions occurs. Therefore, should one use for example the mean of the 10% largest velocity contributions when ranked in order for each load and geometry combination as a characteristic velocity or any other reasonable value such a 5%, the mode rather than the mean etc? The choices in defining a characteristic velocity will invariably be somewhat arbitrary and open to discussion. A consequence of any arbitrary definition of characteristic velocity is that the results and formulations for the regular and irregular tests are not strictly comparable.

6.0 CONCLUSION

6.1 INTRODUCTION AND OBJECTIVE

This short research report presents data from a number of regular wave tests undertaken at the TU Delft to assist in the understanding of flow velocity at rubble mound breakwater toes. The particular objective of the study is to assist in the development of a physical parameterization model which links load, geometry and local velocity in a first step as part of a two step model approach to parameterize toe stability under wave action.

6.2 LABORATORY WORK AND EXPERIMENT

Laboratory testing in combination with empirical curve fitting has been chosen to develop a better understanding of the physical processes and the impact of parameters. An experiment has been set up as similar as possible to that of a previous researcher, Gerding, who has undertaken damage level tests at breakwater toes in 1993 to enable correlation of results at a later stage. Due to the short time period available for the testing only a limited number of load and geometry parameters were varied whilst the local velocity was measured by two Acoustic Doppler Velocimeters (ADV) at regularly geometric intervals. The most important key parameters of the experiment are listed in the Table 8 below.

TABLE 8 - KEY PARAMETERS

Water level	Wave Height	Steepness	Toe Height	Rock Size	Toe Width	Foreshore slope	Rock Slope
hm [m]	Hs [m]	s	ht [m]	Dn50 [m]	bt [m]		
• 0.4	• 0.1	• 0.02	• 0.08	• 0.035	0.12	1:20	1:1.5
• 0.3	• 0.15	• 0.04	• 0.15	• 0.025			
• 0.2	• 0.2						

6.3 RESULTS

An analysis of the measurements revealed that the horizontal wave velocity has the same period as the wave. However the local water level and velocity are not having a constant phase relationships in space (along the toe) and most likely not in time (crest versus trough).

For low breaker indices (water level to wave height ratios less than 0.3) the phase difference appears small, for large breaker indices (> 0.3) the phase difference typically increases. In addition, between the trough of the wave and the mean surface water level, a significant additional velocity component is visible on the Lissajous type plot. This additional velocity component is most likely down rush. It is difficult to determine whether a predominant phase shift and/ or an amplitude increase takes place at those instances. It may be a possibility to study this phenomenon further to validate Baart's proposed velocity formulation. However, it is expected that it will be difficult to separate the down rush component from wave orbital motion.

Increasing the wave period increases the phase difference between the local water level and velocity. Increasing the toe height has a marginal influence on the phase and the shape of Lissajous plots remains essentially the same. The rock size appears to have no to a negligible effect on the phase difference.

Curve fitting has been deployed to develop an empirical formulation linking the perceived key characteristics in a linear relationship which is presented in Equation 9 below. The data indicates that the linear slope coefficient is 0.017 and 0.015 and the linear y-intercept coefficient is 1.105 and 1.034 for a rock size D_{n50} of 0.035m and 0.025m respectively. Further studies are required to confirm the formulation as the data has a significant error bands and scatter. A notable advantage of the Equation 7 is that it can be adjusted to form Equation 9 to incorporate slopes should further research be carried out.

$$\text{EQUATION 7 } U_{max} = U_0 \left\{ m \frac{1}{\sqrt{s}} \left[\frac{h_t}{h_m} \right] + a \right\}$$

$$\text{EQUATION 9 } U_{max} = U_0 \left\{ m \xi \left[\frac{h_t}{h_m} \right] + a \right\}$$

Where a is a linear coefficient for the y-intercept

m is a linear slope coefficient

s is the wave steepness

h_t is the toe height

h_m is the water level at the toe

ξ is the Iribarren number

$$U_0 \text{ is defined as } U_0 = \frac{\pi H_0}{T} \frac{1}{\sinh(k[h_m - h_t])}$$

6.4 FURTHER WORK

Further studies are required to validate the results of the tests and the parameterization formulation chosen due to the limited number of tests in the study and the significant error bands.

In addition, the regular vertical velocity component as well as irregular wave induced characteristic velocities should be studied further to develop an effective understanding of toe velocities.

8.0 LIST OF SYMBOLS

Symbol	Definition	[units]
α	is the angle of the slope	[RAD]
a_0	is a Fourier fit coefficient (constant)	[-]
a_1	is a Fourier fit coefficient (cos)	[-]
a	is a linear constant for the y-intercept	[-]
b_1	is a Fourier fit coefficient (sin)	[-]
b_t	Width of breakwater toe structure	[m]
D_{n50}	Median Nominal stone diameter	[m]
g	is gravity ≈ 9.81	[ms ⁻²]
h_m	is the water level at the toe	[m]
h_t	is the toe height	[m]
H	is the wave height	[m]
H_{m01}	is the significant wave height based on spectral moments	[m]
H_s	is the significant wave height based on visual observations	[m]
k	is the wave number $k = \frac{2\pi}{L}$	[1/m]
m	is a linear slope coefficient	[-]
ω	is the wave angular frequency ($2\pi/T$)	[rad/s]
φ_{TA}	is is the phase lag between the down rush and incoming wave	[rad]
φ	is the phase lag between the run-up and resulting velocity	[rad]
ν	Kinematic Viscosity of fluid	[m ⁻² ·s ⁻¹]
s	is the fictitious wave steepness $s = \frac{2\pi H}{gT^2}$	[-]
T	is the wave period	[s]
t	is time	[s]
u	is the horizontal wave component of orbital velocity	[m/s]

Symbol	Definition	[units]
\hat{u}_{bi}	is the velocity of the incoming wave	[m/s]
\hat{u}_{bdr}	is the velocity due to the downrush	[m/s]
U_{fitted}	is the Fourier fitted velocity	[m/s]
$U_{fitted\ max}$	is the maximum amplitude of the Fourier fitted velocity	[m/s]
U_0	is defined as $U_0 = \frac{\pi H_0}{T} \frac{1}{\sinh(k[hm-h\ell])}$	[m/s]
x	is the horizontal distance in direction of the wave	[m]
X	is the horizontal distance from the toe rock/slope interface	[m]
Y	is the vertical distance from the toe surface	[m]
ξ	is the Iribarren number	[-]

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VAN DER MEER (1998) Geometrical design of coastal structures, Infram Publication no.2 (www.infram.nl)

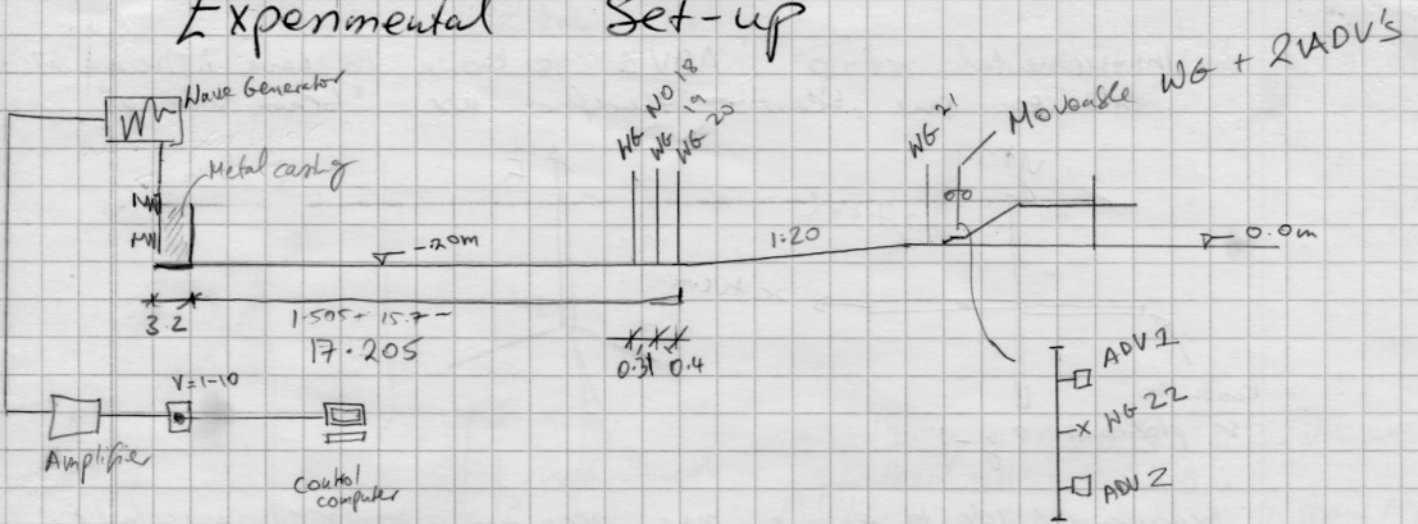
APPENDIX A – EXTRACTS FROM LAB LOG BOOK

APPENDIX B – TABLES OF RESULTS

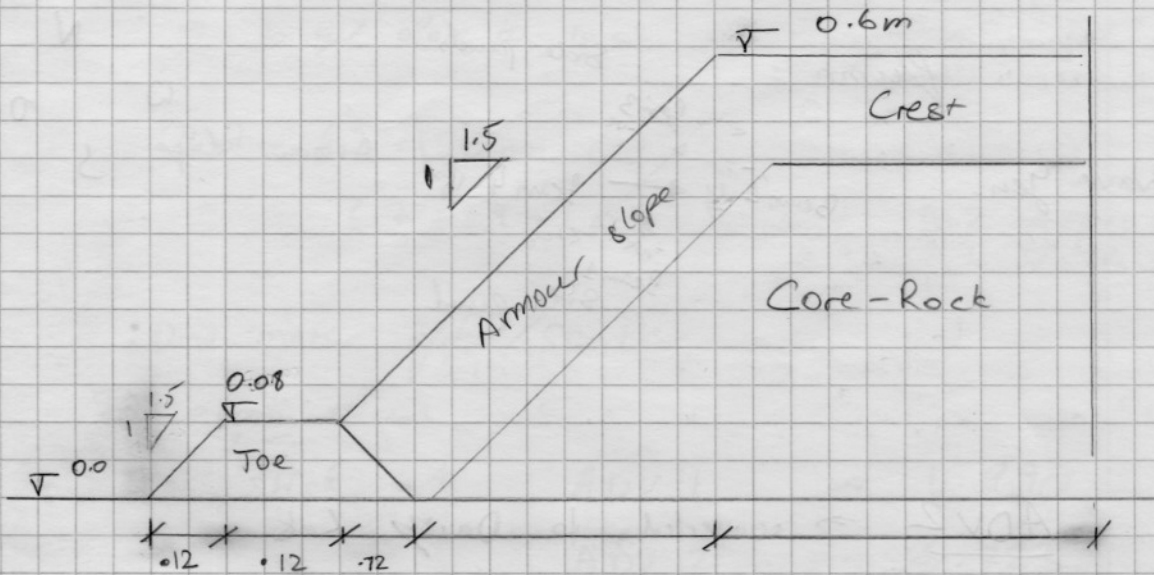
APPENDIX C – LISSAJOUS PLOTS

APPENDIX D— MAXIMUM VELOCITY DISTRIBUTION PLOTS

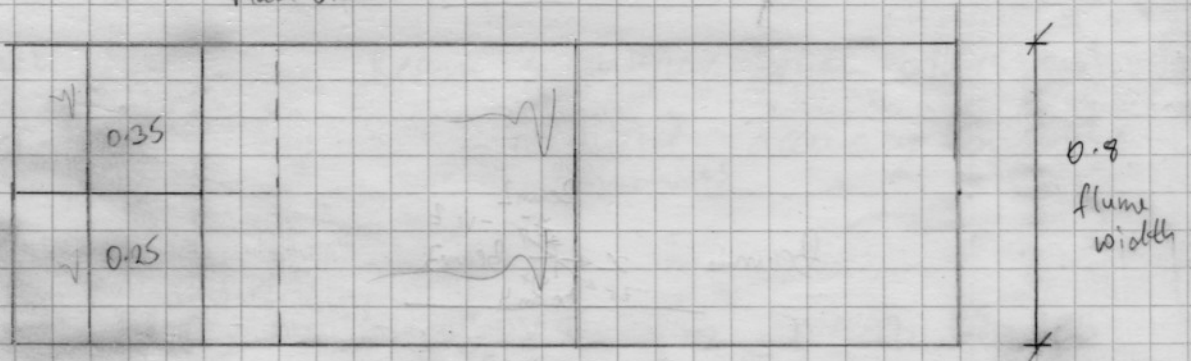
Experimental Set-up



Detail on Rock armour slope
X-Section



Plan view

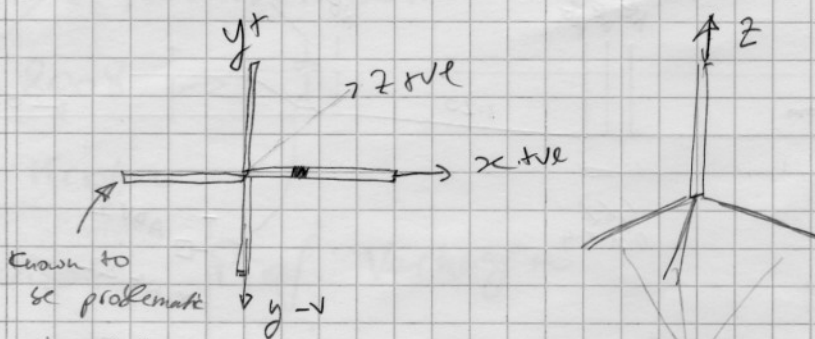


toe split into two halves 0.35 & 0.25

Rock armour 0.4m

→ see excel file for details

Instrumental set-up ADV1 is known to have instrumentation error on one beam \rightarrow therefore use "beam set-up"

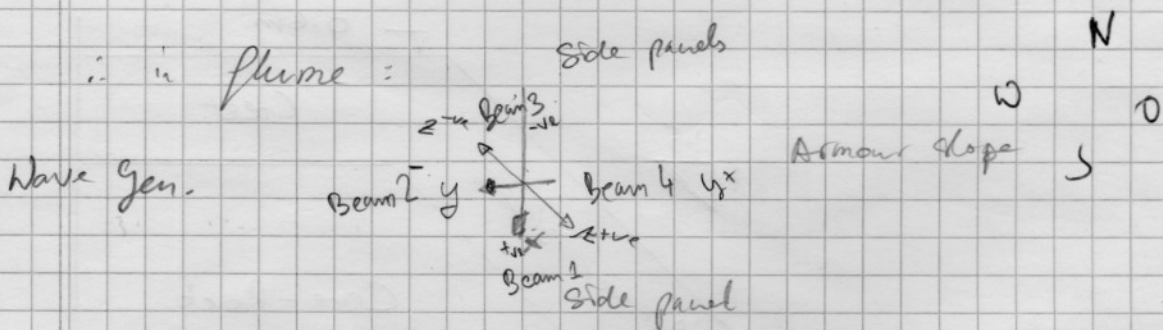


Known to be problematic

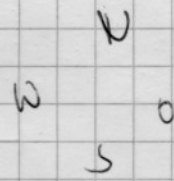
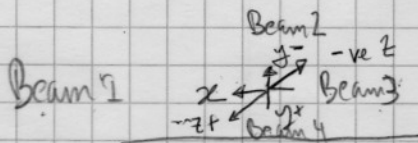
\therefore rotate

measurement probe to ensure max. accuracy in most important flow

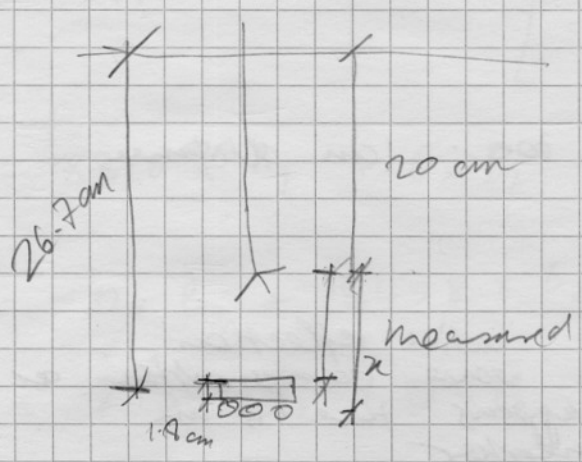
\therefore "flume"



ADV2 \rightarrow connected to Daisy Lab



Test Ventriho height



ADV1 → meas. 6.7 ; instrument 6.8
 level stick 1.957
 ADV2 → meas. 6.5 ; instrument 6.6
 level stick 4.690

→ to get dist to rock:

$$26.7 - 6.7 = 20 \text{ cm}$$

$$6.7 + 1.8 = 8.5$$

want 5.2 approx
3.3cm to & lowered

Dist. meter off / scatter

For experiment use

Dist. stick at ADV 1 → 1.990

ADV 2 → 4.723

check probe + beam 3 higher than others

→ limited accuracy on soft machines

final position

ADV 1 → 1.990 ~~1.993~~

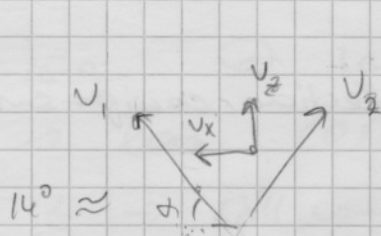
ADV 2 → 4.720

This means beam at 5.5cm height from sed

Check output in Dary

0-5V ; Analogue output $\pm 0.3ms^{-1}$

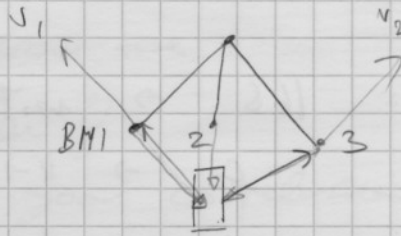
2.5V = 0



$$V_1 = V_x \sin(\alpha) + V_2 \cos \alpha$$

$$V_2 = \dots$$

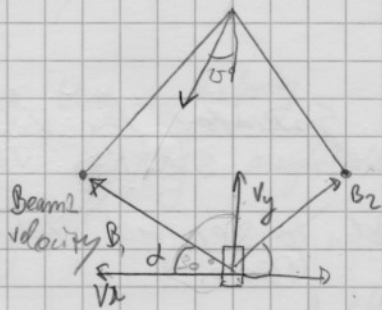
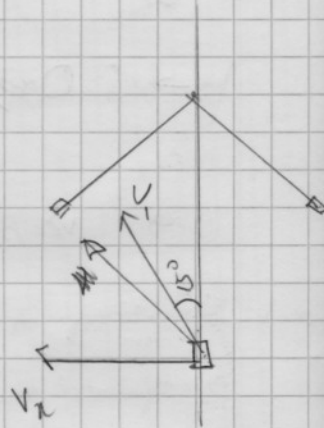
etc.



$$V_x = \frac{V_1 - V_2}{2 \sin \alpha}$$

$$V_z = \dots$$

$$\begin{bmatrix} V_x \\ V_y \\ V_z \\ V_{error} \end{bmatrix} = M \cdot \begin{bmatrix} V_1 \\ V_2 \\ V_3 \\ V_4 \end{bmatrix}$$



$\alpha = 15^\circ$

$$B_1 = V_x \sin \alpha + V_y \cos \alpha$$

$$B_3 = -V_x \sin \alpha + V_y \cos \alpha$$

$B_1 - B_3$

$$B_1: \begin{matrix} x: B_1 \cos \alpha \\ y: B_1 \sin \alpha \end{matrix}$$

$$B_2: \begin{matrix} x: B_2 \cos \alpha \\ y: -B_2 \sin \alpha \end{matrix}$$

$$B_2 = -V_x \cos \alpha + V_y \sin \alpha$$

$$V_1 = V_{x1} \cos \alpha + V_z \sin \alpha$$

$$V_2 = -V_{x2} \cos \alpha + V_z \sin \alpha$$

$$V_1 - V_2 = V_x \cos \alpha + \dots$$

$$V_x = \frac{V_1 - V_2}{2 \cos \alpha}$$

$$\Rightarrow V_x = \frac{B_1 \cos \alpha - B_2 \cos \alpha}{2 \cos \alpha}$$

$$V_z = (B_1 + B_2) \sin \alpha$$

col. 3 \rightarrow 4

$$ADN1 \begin{bmatrix} 8318 & 0 & -8329 & 0 \\ 0 & 8458 & 0 & -8494 \\ 2134 & 0 & 2091 & 0 \\ 0 & 2182 & 0 & 2038 \end{bmatrix} \begin{bmatrix} B_1 \\ B_2 \\ B_3 \\ B_4 \end{bmatrix} = \begin{bmatrix} V_1 \\ V_2 \\ V_3 \\ V_4 \end{bmatrix}$$

$$V_1 = 8318 \times B_1 + 0 \times B_2 + (-8329) \times B_3 + 0 \times B_4$$

$$V_2 = 0 \times B_1 + 8458 \times B_2 + 0 \times B_3 + -8494 \times B_4$$

$$V_3 = 2134 \times B_1 + 0 \times B_2 + 2091 \times B_3 + 0 \times B_4$$

$$V_4 = 0 \times B_1 + 2182 \times B_2 + 0 \times B_3 + 2038 \times B_4$$

$$\Rightarrow V_1 = \frac{8318}{4096} B_1 - \frac{8329}{4096} B_3$$

$$= 2.0307 B_1 - 2.03547 B_3$$

$$ADN2 = \begin{bmatrix} 8161 & 0 & -8165 & 0 \\ 0 & 8425 & 0 & -8362 \\ 2122 & 0 & 2108 & 0 \\ 0 & 1986 & 0 & 2236 \end{bmatrix}$$

$$\begin{bmatrix} \cdot & \cdot & \cdot & \cdot \\ 0 & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \\ 0 & \cdot & \cdot & \cdot \end{bmatrix}$$

$$V_1 = 8161 \times B_1 - 8165 \times B_3$$

$$V_2 = 8425 \times B_2 - 8362 \times B_4$$

$$V_3 = 2122 \times B_1 + 2108 \times B_3$$

$$V_4 = 1986 \times B_2 + 2236 \times B_4$$

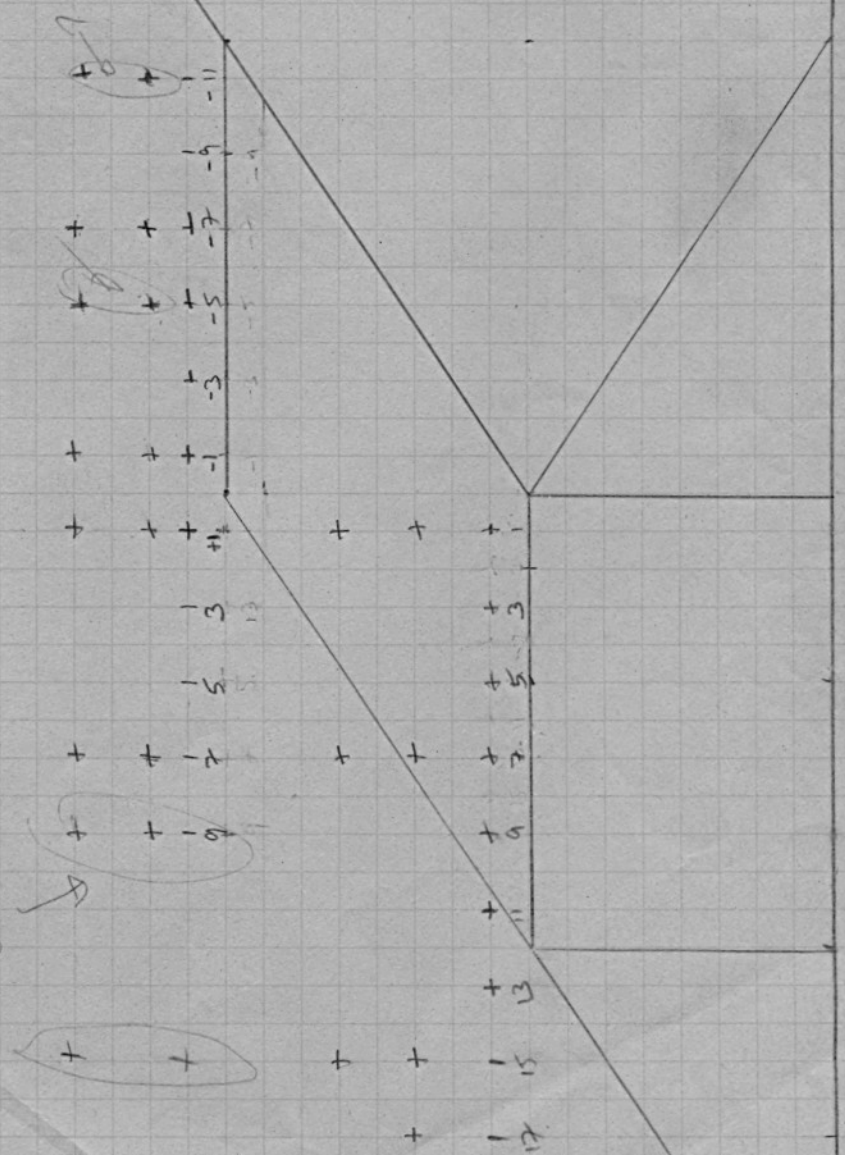
gmarcelawsky@yahoo.com

Singapore views 7

✓



could be good



J

Steering FilesR001. $\rightarrow h_m = 0.4$; $H = 0.1$; $T = 1.790s$ ($s = 0.02$)R002 $\rightarrow h_m = 0.4$; $H = 0.1$; $T = 1.265s$ ($s = 0.04$)R003 $\rightarrow h_m = 0.4$; $H = 0.15$; $T = 2.197$ ($s = 0.02$)R004 $\rightarrow h_m = 0.4$; $H = 0.15$; $T = 1.898$

Data trigger changes experimental time
 Re-do Experiments with wave comp repaired on
 Test 1 → $h_m = 0.4$; $H = 0.15$; $T = 2.197$; Duration = 300s
 Test 1a → 11-11 but duration 60s R003

all at 0 height
 1m from Rock

- b. → Same set-up check timer
- Test 2 → @ 7cm from toe
 - Test 3 → @ 5cm from toe
 - Test 4 → @ 3cm from toe
 - Test 5 → @ 9cm from toe
 - Test 6 → @ 11cm from toe
 - Test 7 → @ 13cm from toe
 - Test 8 → @ 15cm from toe = ~~15cm~~
 - Test 9 → @ 17cm from toe = ~~17cm~~

ADV 2 at level = 372.5

ADV 1 at level = 199.4

3cm from Rock

- move ADV'S by 2cm up to
- | | | |
|--|-------|-------|
| | ADV 2 | 370.5 |
| | ADV 1 | 197.4 |
- Test 10 → @ 17cm from toe
 - Test 11 → @ 15cm from toe
 - 12 → @ 13cm from toe
 - 13 → @ 11cm from toe
 - 14 → @ 9cm from toe
 - 15 → @ 7cm from toe
 - 16 → @ 5cm from toe
 - 17 → @ 3cm from toe
 - 18 → @ 1cm from toe

✓

Move ADV's up 2cm

R.E. EBBENS @ student. Techelt

to ADV2 at 468.5
ADV1 at 195.4

- Test 19 @ 1cm from toe
- Test 20 @ 3cm from toe
- Test 21 @ 5cm from toe
- Test 22 @ 7cm from toe
- Test 23 @ 9cm from toe
- Test 24 @ 11cm from toe
- Test 25 @ 13cm from toe
- Test 26 @ 15cm from toe
- Test 27 @ 17cm from toe

5cm from toe
rock

max ADV2 to 466.5
ADV1 to 193.4

Run-up: 13cm
Run-down: 7.5cm

- Test 28 @ 17cm from toe
- Test 29 @ 15cm from toe
- Test 30 @ 13cm from toe
- Test 31 @ 11cm from toe
- Test 32 @ 9cm from toe
- Test 33 @ 7cm from toe
- Test 34 @ 5cm from toe
- Test 35 @ 3cm from toe
- Test 36 @ 1cm from toe

→ Monday 9th Jun

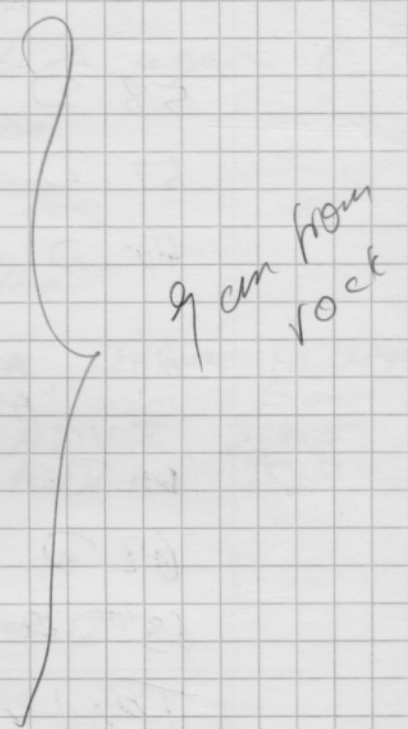
7cm from toe

mean vx1 ; location [x y]
mean vx2

✓

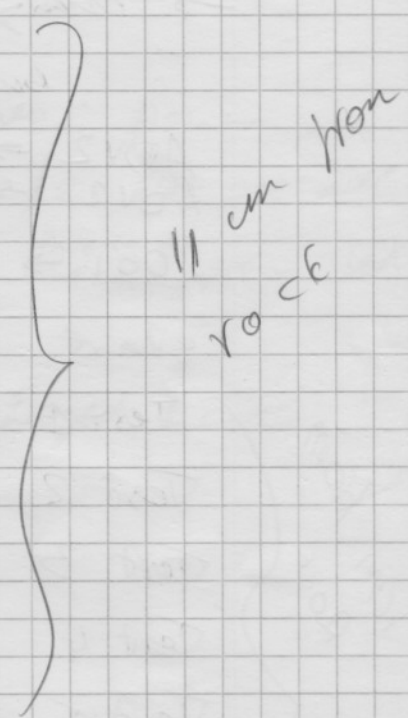
to ADV 2 @ 464.5
ADV 1 @ 197.4

- test 37 @ 1 cm from toe
- 38 @ 3 cm from toe
- 39 @ 5 cm from toe
- 40 @ 7 cm from toe
- 41 @ 9 cm from toe
- 42 @ 11 cm from toe
- 43 @ 13 cm from toe
- 44 @ 15 cm from toe
- 45 @ 17 cm from toe



to ADV 2 @ 462.5
1 @ 189.4

- 46 @ 17 cm from toe
- 47 @ 15 cm from toe
- 48 @ 13 cm from toe
- 49 @ 11 cm from toe
- 50 @ 9 cm from toe
- 51 @ 7 cm from toe
- 52 @ 5 cm from toe

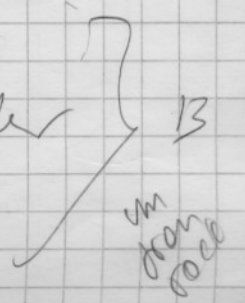


shut down & repair & have load
measurements v. DSG

- 53 @ 3 cm from toe
- 54 @ 1 cm from toe

move ADV 2 - 2 460.5
ADV 1 - 189.4

- 55 @ 1 cm from toe & removed header
- 56 @ 7 cm from toe
- 57 @ 15 cm from toe



✓

max ADV 1 185.4
ADV 2 458.5

58 @ 15 cm from toe }
59 @ 7 cm from toe } 15 cm from rock
60 @ 1 cm from toe }

move ADV 2 456.5
ADV 1 183.4

61 @ 1 cm from toe }
62 @ 7 cm from toe } 17 cm from rock
63 @ 15 cm from toe }

Test concluded! Done dye test!

→ Change wave height. Redo R001
but with wave comp?

ADV 2 → 472.5
ADV 2 → 199.4

R001 → H = 0.1; T = 1.79 s

start

1 cm from Rock {
Test 1 @ 1 cm from toe at 1 cm above
Test 2 @ 3 cm from toe
Test 3 @ 5 cm Done Dye Test
Test 4 @ 7 cm Run-up 6 cm
Test 5 @ 9 cm Run-down 6 cm
Test 6 @ 11 cm
Test 7 @ 13 cm
Test 8 @ 15 cm
Test 9 @ 17 cm

move ADV to 2 cm up to ADV 2 370.5
ADV 1 197.4

✓
 2 cm from rock
 Can handle leaders free for 2 days again!
 Test 10 = 20 17 cm from toe very B
 Test 11 20 15 cm from toe
 Test 12 20 7 cm from toe
 Test 13 20 1 cm from toe
 Test 14 20 1 cm from toe
 Test 15 20 1 cm from toe
 Test 16 20 15 cm from toe

ADV 2 368.5
 ADV 1 195.4
 MOVE HOUGHT
 5 cm

5 cm from rock
 smooth on downward moves
 Test 15 20 7 cm from toe
 Test 16 20 15 cm from toe

— Done for the day

Tuesday 10th June 08

Re-do calibrations to see if any changes! Done

Rep. Rock ROD2 ; Run prof check to see all
 ADV 2 372.5
 ADV 1 199.4
 OR mount run sed
 lots

1 cm from rock
 Test 1 20 1 cm from toe at least 1 cm
 Test 2 20 3 cm from toe
 Test 3 20 5 cm from toe
 Test 4 20 7 cm from toe
 Test 5 20 9 cm from toe
 Test 6 20 11 cm from toe
 Test 7 20 13 cm from toe

Run - up : 5 cm
 Run - down : 4.5 cm

Test 8 20 15 cm from toe
 Test 9 20 17 cm from toe

✓
 3 cm from toe
 Test 10 change ADV position to ADV2 370.5
 ADV1 197.4
 @ 17 cm from toe
 Test 11 @ 15 cm from toe
 Test 12 @ 17 cm from toe
 Test 13 @ 1 cm from toe
 5 cm from toe
 Test 14 @ 1 cm from toe ADV2 368.5
 ADV1 195.4
 Test 15 @ 7 cm from toe
 Test 16 @ 15 cm from toe
 Dye test Done

Start experiment 2004.
 ADV2 372.5
 ADV1 197.4

1 cm from toe
 Test 1 @ 1 cm from toe
 Test 2 @ 3 cm from toe
 Test 3 @ 5 cm from toe
 Test 4 @ 7 cm from toe
 Test 5 @ 9 cm from toe
 Test 6 @ 11 cm from toe
 Test 7 @ 13 cm from toe
 Test 8 @ 15 cm from toe
 Test 9 @ 17 cm from toe
 3 cm from toe
 Test 10 @ 17 cm from toe move ADV2 370.5
 ADV1 197.4
 Test 11 @ 15 cm from toe
 Test 12 @ 7 cm from toe
 Test 13 @ 1 cm from toe
 5 cm from toe
 Test 14 @ 1 cm from toe move ADV2 368.5
 ADV1 195.4
 Test 15 @ 7 cm from toe
 Test 16 @ 15 cm from toe
 Dye test
 Run up = 12 cm
 Run down = 8 cm

✓ Start experiment R005

ADV2 372.5
ADV1 199.4

1 cm from rock

- Test 1 @ 1 cm from toe
- Test 2 @ 3 cm from toe
- Test 3 @ 5 cm from toe
- Test 4 @ 7 cm from toe
- Test 5 @ 9 cm from toe
- Test 6 @ 11 cm from toe
- Test 7 @ 13 cm from toe
- Test 8 @ 15 cm from toe
- Test 9 @ 17 cm from toe

mean WL = -0.012

3 cm from toe

- Test 10 @ 17 cm from toe
- Test 11 @ 15 cm from toe
- Test 12 @ 7 cm from toe
- Test 13 @ 1 cm from toe

move ADV2 = 370.5
ADV1 = 197.4

5 cm from toe

- Test 14 @ 1 cm from toe
- Test 15 @ 7 cm from toe
- Test 16 @ 15 cm from toe

move ADV2 = 368.5
ADV1 = 195.4

eye test Done

Run-up 11 cm
Run-down 6.5 cm

Start experiment R006

ADV2 342.5
ADV1 199.4

1 cm from rock

- Test 1 @ 1 cm from toe
- Test 2 @ 3 cm from toe
- Test 3 @ 5 cm from toe
- Test 4 @ 7 cm from toe
- Test 5 @ 9 cm from toe
- Test 6 @ 11 cm from toe
- Test 7 @ 13 cm from toe
- Test 8 @ 15 cm from toe
- Test 9 @ 17 cm from toe

mean WL @ -0.0071

3cm from toe

- Test 10 @ 17cm
- Test 11 @ 15cm
- Test 12 @ 7cm from toe
- Test 13 @ 1cm from toe

ADV2 370.5
 ADV1 197.4
 Start on 11th June 08
Wednesday

5cm from toe

- Test 14 @ 1cm from toe
- Test 15 @ 7cm from toe
- Test 16 @ 15cm from toe

ADV2 368.5
 ADV1 195.4

Dye test

Run up 19.5
 Run down 8.5

Start Experiment Roof

1cm from rock

- Test 1 @ 1cm
- Test 2 @ 3cm
- Test 3 @ 5cm
- Test 4 @ 7cm
- Test 5 @ 9cm
- Test 6 @ 11cm
- Test 7 @ 13cm
- Test 8 @ 15cm
- Test 9 @ 17cm

ADV2 372.5
 ADV1 199.4

3cm from rock

- Test 10 @ 17cm
- Test 11 @ 15cm
- Test 12 @ 7cm
- Test 13 @ 1cm

move ADV2 370.5
 ADV1 197.4

5cm from rock

- Test 14 @ 1cm
- Test 15 @ 7cm
- Test 16 @ 15cm

move ADV2 368.5
 ADV1 195.4

Dye test

Run up 17.5 cm
 Run down 9.0 cm

Done

✓ Loess

~~Set~~ test out number of flume to 0.5

Roob = $h_m = 0.3$; $H = 0.1$; $T = 1.790s$

1 cm from toe	Test 1	∅	1 cm	from toe	ADV2	372.5
	Test 2	∅	3 cm	from toe	ADV1	199.4
	Test 3	∅	5 cm	from toe		
	Test 4	∅	7 cm	from toe		
	Test 5	∅	9 cm	from toe		
	Test 6	∅	11 cm	from toe		
	Test 7	∅	13 cm	from toe		
	Test 8	∅	15 cm	from toe		
	Test 9	∅	17 cm	from toe		
3 cm from toe	Test 10	∅	17 cm	from toe	more ADV2 to	370.5
	Test 11	∅	15 cm	from toe	ADV1 to	197.4
	Test 12	∅	7 cm	from toe		
	Test 13	∅	1 cm	from toe		
5 cm from toe	Test 14	∅	1 cm	from toe	more ADV2	369.5
	Test 15	∅	7 cm	from toe	ADV1	195.4
	Test 16	∅	15 cm	from toe		

Dye test

Run up = 10.5 cm
Run down = 5 cm

Roob = $h_m = 0.3$; $H = 0.1$; $T = 1.265s$

1 cm from toe	Test 1	∅	1 cm	from toe	ADV2	371.5
	Test 2	∅	3 cm	from toe	ADV1	199.4
	Test 3	∅	5 cm	from toe		
	Test 4	∅	7 cm	from toe		
	Test 5	∅	9 cm	from toe		
	Test 6	∅	11 cm	from toe		
	Test 7	∅	13 cm	from toe		

✓ 1 cm from rock { Test 8 @ 15 cm from toe Start Thursday 12/08
 Test 9 @ 17 cm from toe

3 cm from rock { Test 10 @ 17 cm from toe move ADV2 370.5
 ADV1 197.4
 Test 11 @ 15
 Test 12 @ 7
 Test 13 @ 1

5 cm from rock { Test 14 @ 1 cm from toe ADV2 368.5
 ADV1 195.4
 Test 15 @ 7 cm
 Test 16 @ 15 cm

Dye test Run up = 6.8 cm
 Run down = 4.0 cm

$R_{010} = H_m = 0.3 ; H = 0.15 ; T = 2.197$

1 cm from rock { Test 1 @ 1 cm ADV2 372.5
 ADV1 199.4
 Test 2 @ 3 cm
 Test 3 @ 5 cm
 Test 4 @ 7 cm

Run up = 14.3 cm
 Run down = 5.5 cm

3 cm from rock { Test 5 @ 9 cm
 Test 6 @ 11 cm
 Test 7 @ 13 cm
 Test 8 @ 15 cm
 Test 9 @ 17 cm

5 cm from rock { Test 10 @ 17 cm move ADV2 370.5
 ADV1 197.4
 Test 11 @ 15 cm
 Test 12 @ 7 cm
 Test 13 @ 1 cm

5 cm from rock { Test 14 @ 1 cm ADV2 368.5
 ADV1 195.4
 Test 15 @ 7 cm
 Test 16 @ 15 cm

Dye test ✓

Roll ; $H_m = 0.3$; $H = 0.15$; $T = 1.898$

1 cm from rock	Test 1	@ 1 cm	from toe		
	Test 2	@ 3 cm	from toe		
	Test 3	@ 5 cm	from toe		
	Test 4	@ 7 cm	from toe		
	Test 5	@ 9 cm	from toe		
	Test 6	@ 11 cm	from toe		
	Test 7	@ 13 cm	from toe		
	Test 8	@ 15 cm	from toe		
	Test 9	@ 17 cm	from toe		
3 cm from rock	Test 10	@ 17	from toe	ADV2	370.5
	Test 11	@ 15	from toe	ADV1	197.4
	Test 12	@ 7	from toe		
5 cm from rock	Test 13	@ 1	from toe		
	Test 14	@ 1	from toe	ADV2	368.5
	Test 15	@ 7		ADV1	195.4
	Test 16	@ 15			

Run up = 17.5 cm
Run down = 5.5 cm

Dye Test

Roll ; $H_m = 0.3$; $H = 0.15$; $T = 1.550$

1 cm from rock	Test 1	@ 1 cm	from toe	ADV2	372.5
	Test 2	@ 3 cm		ADV1	197.4
	Test 3	@ 5 cm			
	Test 4	@ 7 cm			
	Test 5	@ 9 cm			
	Test 6	@ 11 cm			
	Test 7	@ 13 cm			
	Test 8	@ 15 cm			
	Test 9	@ 17 cm			

✓

R012 continued

3 cm from rock

- Test 10 @ 17 cm
- Test 11 @ 15 cm
- Test 12 @ 7 cm
- Test 13 @ 1 cm

move ADV2 370.5
ADV1 197.4

5 cm from rock

- Test 14 @ 1 cm
- Test 15 @ 7 cm
- Test 16 @ 15 cm

ADV2 368.5
ADV1 195.4

eye test

run-up = 13.8
run-down = 6 cm

R013 $h_m = 0.3$ $H = 0.2$; $T = 2.531$

→ Not possible wave generator trips!

Try R014 ; $h_m = 0.3$; $H = 0.2$ $T = 1.789$ →

Test 1 @ 1 cm from toe → vector 1 doesn't read

Test 3 @ 5 cm from toe

→ Not possible wave gen. trips after short while let out water

R015 $h_m = 0.2$ $H = 0.1$ $T = 1.790$ Start Fr 137

1 cm from rock

- Test 1 @ 1 cm from toe
- Test 2 @ 3 cm from toe
- Test 3 @ 5 cm from toe
- Test 4 @ 7 cm from toe
- Test 5 @ 9 cm from toe
- Test 6 @ 11 cm from toe
- Test 7 @ 13 cm from toe
- Test 8 @ 15 cm
- Test 9 @ 17 cm

ADV2 372.5
ADV1 199.4

Test 10 @ 17 cm move ADV to 370.5
197.4

too high ; partially out of water

✓

2m from rock

use
 Test 11 @ 17cm
 Test 12 @ 15cm
 Test 13 @ 7cm
 Test 14 @ 1cm
 Test 15* @ 1cm
 dye test

* 0.5m from rock

371.5
198.4

→ partially out of water

move to 372.0
run up = 9cm
run down = 4cm

R016 $h_m = 0.2$ $H = 0.1$ $T = 1.2650$

Test 1 @ 1cm
 Test 2 @ 3cm
 Test 3 @ 5cm
 Test 4 @ 7cm
 Test 5 @ 9cm
 Test 6 @ 11cm
 Test 7 @ 13cm
 Test 8 @ 15cm
 Test 9 @ 17cm

ADV2 372.5
199.4

Run up = 4cm
Run down = 3.5cm

dye test

R017 $H_m = 0.2$ $H = 0.15$ $T = 2.197$

→ Test 1 → moved probe to face & lowered to ensure still within water.

At 17cm from toe ADV2 174.0
 ADV1 200.9 }
 Test 2 @ 15cm

↳ prox check ok & still water
restart machine

stopped test run after completion
damage near toe @ slip toe interface occurring repaired

probe check ok

no other test possible due to limited water depth

Cancel test 18 & 19 → wave generator cannot be moved wave gauges

✓
Recalibrate wave gauges
Run prox. deck at ADV 2 372.5
ADV 1 199.4

OK; mouse under carpet still present
affects V1 less than V2

Start Irregular wave series @ 3:40

Duration 1790s

Actual
in side of
dam

IO20 ; $h_m = 0.4m$; $H_s = 0.1m$; $T_p = 1.790s$

Test 2 @ 1cm from toe ADV 2 372
ADV 1 199.4

Test 2 @ 7cm from toe

Test 3 @ 15cm from toe

Test 4 @ 7cm at ADV 2 370.5
ADV 1 197.4

Test IO21 ; $h_m = 0.4$; $H_s = 0.1$ $T_p = 1.265s$

Test 1 @ 1cm from toe ADV 2 372
ADV 1 199.4

Duration 1300s

Test 2 @ 7cm from toe

Test 3 @ 15cm from toe

Test 4 @ 7cm from toe ADV 2
370
197.4

Finish

Tuesd.
17th June '09

Test IO22 ; $h_m = 0.4$; $H_s = 0.15$; $T = 2.197$

Test 1 @ 1cm from toe ADV 2 372.5
ADV 1 199.4

Stopped due to wave maker breaking down

restart as 1a

Stopped due to wave maker breaking down

change input file so that it repeats every
10min the wave climate

restart as 1b change to 10min duration to
steering file this reduces max. wave height

Test 2 @ 7cm from toe
 Test 3 @ 15cm from toe
 Test 4 @ 7cm from toe
 ADV2 370.5
 ADV1 197.4

Wednesday 18th June 08 → Sanders is measuring

IO23 ; $h_m = 0.4$; $H = 0.15$; $T = 1.550$

Test 1 @ 1cm from toe signal quality ↓
 Test 2 @ 7cm from toe signal qual. ↓ ; added powder in last m. signals improve
 Test 3 @ 15cm from toe
 Test 4 @ 7cm ; ADV2 370.5
 ADV1 197.4

after ≈ 1200s power failure

Test 4b signal not good → stopped
 Test 4c reset after adding powder

Thursday 19th June 08 → Sanders / JK

IO24 skriptes result is too high Voltage
 × cancelled ($H = 0.2$; $T = 2.531$)

IO25 generator stopped after 2min
 changed ref - file from $H = 0.2 \rightarrow H = 0.18$
 $T = 1.781s$
 lower Voltage of $\pm 6.3V$ as this should work if generator
 Normally covers higher if forward the put it height

Test 1 @ position 7cm ; ADV2 370.5
 Rename 4 ADV1 197.4

↳ Rename afterwards to Test 4

Test 1 @ position 1cm ; ADV2 372.5
 ADV1 199.4
 Test 2 ✓
 Test 3 ✓

✓ Test I 022 b

I 024 B → changed pct. file $H=0.2$

with no reflect. coup.

no second order

200 - 580 sec

I 025 → $h_m = 0.4$; $H = 0.2$; $T = 1.789s$ → not possible

I 026 $h_m = 0.3$; $H = 0.1$; $T = 1.790s$

pos 1 @ 1cm

pos 2 @ 7cm

pos 3 @ 15cm

pos 4 @ 7cm

ADV2 370.5
ADV1 397.4

Dye test done

I 027 $h_m = 0.3m$; $H = 0.1$; $T = 1.265s$

pos 1 @ 1cm done

JK left

Sandals clear tests

pos 2 @ 7cm

pos 3 @ 15cm

pos 4 a @ 1cm

pos 4 b @ 7cm

} 2cm higher
370.5
197.4

Dye test done

I 028 $h_m = 0.3$; $H = 0.15$; $T = 2.197s$

pos 1 @ 1cm

→ $h_{m0} = 0.108m$

pos 2 @ 7cm

pos 3 @ 15cm

$h_{m0} = 0.108m$

pos 4 @ 7cm ; 2cm higher

Dye test done but forget to check no of of ass and

Slope damaged ; Sandals required slope

I 029 $h_m = 0.3$; $h_t = 0.15$; $T = 1.550 s$

pos 1 @ 1cm done $\rightarrow h_{m0} = 0.104$

pos 2 @ 7cm done $h_{m0} = 0.105$

pos 3 @ 15cm

pos 4 @ 7cm but 2cm higher ADV2 3705 cm
197.4 cm

Dye test done

Let out water,

Tuesday \rightarrow JK: Rebuild slope with ROEE & increase for length

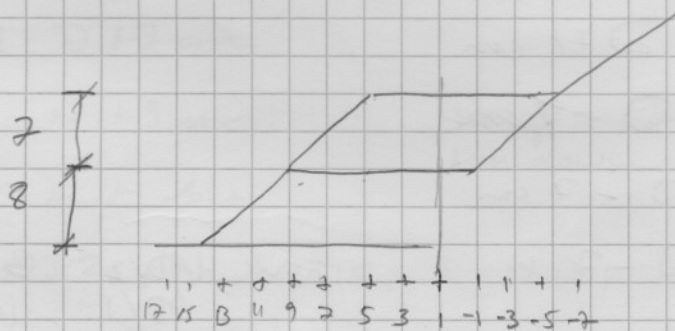
Wednesday

25th June '08

\rightarrow Let in water, JK restarts with measurements

RO30 ; $h_t = 0.15$; $h_m = 0.4$; $H = 0.1$; $T = 1.790$

positions



Start at

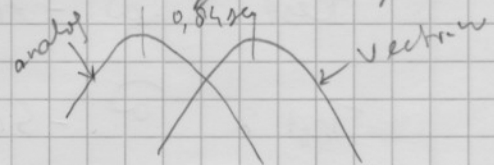
pos. 1 @ -7 cm, height at ADV2: 3655 ; ADV1: 192.4

check probe, OK ; approx. 1.5 cm from sed

check calibration

\rightarrow Sanders checked delay in analogue output

\rightarrow 0.84 s before
Vechirino



but between analog / analogue
no delay

$\Delta t = 0.06 \mu s$

✓

After level start tests

Test 1 @ -7cm

ADV2 365.5

ADV1 192.4

Test 2 @ -5cm

$H_{mo} = 0.099 m$

Test 3 @ -3cm

Test 4 @ -1cm

Test 5 @ +1cm

Test 6 @ +3cm

Test 7 @ +5cm

Test 8 @ +7cm

Test 9 @ +9cm

Test 10 @ +9cm

move ADV2 363.5

ADV1 190.4

Test 11 @ +7cm

Test 12 @ +1cm

Test 13 @ -7cm

Test 14 @ -7cm

Test 15 @ -7cm

max ADV2 361.5

ADV1 188.4

Test 16 @ -1cm

Test 17 @ +1cm

Test 18 @ +7cm

Test 19 @ +9cm

Run up - 6.5cm

Run down - 5.5cm

Eye test done ✓

R031 $H_t = 0.15$; $H_m = 0.4$; $H = 0.1$; $T = 1.26$

Test 1 @ -7cm

ADV2 365.5

ADV1 192.4

Test 2 @ -5cm

Test 3 @ -3cm

Test 4 @ -1cm

Test 5 @ +1cm

Test 6 @ +3cm

✓

- Test 7 @ +5cm
- Test 8 @ +7cm
- Test 9 @ +9cm
- Test 10 @ +9cm

move ADV 2 to 363.5
ADV 1 to 190.4

Stop at 6.15 pm

Test 11 @ +7cm

Restart Thursday 26th June '08

Test 12 @ +1cm

Test 13 @ -1cm

Test 14 @ -7cm

Test 15 @ -7cm

move ADV 2 361.5
ADV 1 188.4

Test 16 @ -1cm

Test 17 @ +1cm

Test 18 @ +7cm

Test 19 @ +9cm

Run up - 5.5cm
Run down - 4.5cm

Day - test done

Test R032 ; $h_f = 0.15$; $H = 0.15$; $T = 2.197_s$

Test 1 @ -7cm

ADV 2 365.5
ADV 1 192.4

Test 2 @ -5cm

Test 3 @ -3cm

Test 4 @ -1cm

Test 5 @ +1cm

Test 6 @ +3

Test 7 @ +5

Test 8 @ +7

Test 9 @ +9

Test 10 @ 15cm

Test 11 @ 15cm move ADV 2 363.5
ADV 1 190.4

✓

Test 12 a +9cm

Test 13 a +7cm

Test 14 a +1cm

Test 15 a -1cm

Test 16 a -3cm

Test 17 a -5cm

Test 18 a -7cm

Test 19 a -9cm

Test 20 a -11

Test 21 a -11

→ Test 22 a -11

Test 23 a -9

Test 24 a -7

Test 25 a -5

Test 26 a -3

Test 27 a -1

Test 28 a +1

Test 29 a +3

Test 30 a +5

Test 31 a +5

Test 32 a +5

Test 33 a +7

Test 34 a +1

Test 35 a -1

Test 36 a -5

ADV lowered again 365.5;

ADV raised to 361.5; 188.4

ADV raise to 359.5; 186.4

→ "dirty signal"

✓

Start Friday

Redo Test 36 as 36a @ -5

Test 37 @ -7

Test 38 @ -9

Test 39 @ -11

Test 40 @ -11 ADV2 357.5 ; ADV1 184.4

Test 41 @ -5

Test 42 @ -1

(Test 43 @ +1)

Test 43 @ +7

Run up 14.6 cm
Run down 8.0 cm

Test 45 @ +15

Done

Redo R031 for pos -11, -5

Test 20 @ -11 , ADV2 @ 365.5 , ADV1 192.4

Test 21 @ -11 ADV2 @ 363.5 , ADV1 190.4

Test 22 @ -5

Test 23 @ -5 ADV2 @ 361.5 ; ADV1 188.4

Test 24 @ -11

Redo R030 for pos -11, -5

Test 20 @ -11 ADV2 @ 365.5 ; ADV1 192.4

Test 21 @ -11 ADV2 @ 363.5 ; ADV1 190.4

Test 22 @ -5

Test 23 @ -5 ADV2 @ 361.5 ; ADV1 188.4

Test 24 @ -11

✓ Test R033 $h_c = 0.15$; $h_m = 0.4$; $H = 0.15$; $T = 1.898_s$

Test 1 $\omega = 11$; ADV2 365.5 ; ADV1 192.4

Test 2 $\omega = 9$

Test 3 $\omega = 7$

Run up = 11.8 cm
Run down = 8 cm

Test 4 $\omega = 5$

Test 5 $\omega = 3$

Test 6 $\omega = 1$

Test 7 $\omega = +1$

Test 8 $\omega = 3$

Test 9 $\omega = 7$

Test 10 $\omega = 15$

Test 11 $\omega = 15$; ADV2 363.5 ; ADV1 ; 190.4

Test 12 $\omega = 7$;

Test 13 $\omega = 3$

Test 14 $\omega = 1$

Test 15 $\omega = -1$

Test 16 $\omega = -5$

Test 17 $\omega = -7$

Test 18 $\omega = -11$

Test 19 $\omega = -11$ ADV2 361.5 ; 188.4

Test 20 $\omega = -5$

Test 21 $\omega = 4-1$

Test 22 $\omega = +1$

Run up ; Run down

Test R034 ; $h_c = 0.15$; $h_m = 0.4$; $H = 0.15$; $T = 1.550_s$

Test 1 $\omega = 11$; ADV2 365.5 ; ADV1 192.4

Test 2 $\omega = 9$

Run up 11.5 cm
Run down 7 cm

Test 3 $\omega = 7$

Test 4 $\omega = 5$

✓

Test 5 ω -3

Test 6 ω -1

Test 7 ω +1

Test 8 ω +3

Test 9 ω +7

Test 10 ω +15

Test 11 ω +15 ; ADV2 363.5 ; ADV1 190.4

Test 12 ω +7

Test 13 ω +3

Test 14 ω +1

Test 15 ω -1

Test 16 ω -5

Test 17 ω -7

Test 18 ω -11

Test 19 ω -11 ADV2 361.5 ; 188.4

Test 20 ω -5

Test 21 ω -1

Test 22 ω +1

Oye test done on Monday morning

Test R035 ; $h_t = 0.15$; $h_m = 0.4$; $H = 0.2$; $T = 2.531s$

Test 1 ω -11 ADV2 365.5 ADV1 192.4

Test 2^{1a} ω -7

Test 3 ω -7

Test 4^{3a} ω -5

test 4n ω -5 with different range $\pm 1ms^{-1}$

Test 5 ω -3 with range $\pm 1ms^{-1}$

Test 5n ω -3 with range $\pm 0.3ms^{-1}$

Test 6 ω -1

Test 7 ω +1

✓ Test 8 a +3

Test 9 a +5

Test 10 a +7

Test 11 a +15

Test 12 a +15

Test 12a a +15

Test 13a a +7

Test 13 a +7

Test 14 a +3

Test 14a a +3

Test 15 a a +1

Test 16 a a -1

Test 17a a -5

Test 18a a -7

Test 19a a -11

Test 20a a -11

Test 21 a a -5

Test 22a a -1

Test 23a a +1

Test Q036

Test 2 a -11

1a a -11

Test 2 a -9

Test 3 a -7

Test 4 a -5

Test 5 a -3

Test 6 a -1

Test 7 a +1

move ADV2 3635 ; 190.4

, change to $\pm 1m/s$

at $\pm 1m/s$

a $\pm 0.3cm$

$\pm 0.3cm$

at $\pm 1m/s$

at $\pm 1m/s$

} $\pm 1ms$

, move ADV2 361.5 ; 188.4

} $\pm 1ms$

Dye test Done

$h_s = 0.15 ; h_m = 0.4 ; H = 0.2 ; T = 1.78$

→ About stones moved i.e.

redo as
all outputs to
 $\pm 1ms$

- ✓ Test 8 @ +3
- Test 9 @ +5
- Test 10 @ +7
- Test 11 @ +15
- Test 12 @ +15
- Test 13 @ +7
- Test 14 @ +3
- Test 15 @ +1
- Test 16 @ -1
- Test 17 @ -5
- Test 18 @ -7
- Test 19 @ -11
- Test 20 @ -11
- Test 21 @ -5
- Test 22 @ -1
- Test 23 @ +1

ADV2 363.5 ; 190.4

Stores moved → placed back

move 361.5 ; 188.4

Run-up 16cm
Run-down 11.5cm

Dye test done

Do irregular tests at same water level

Flow; $h_f = 20.15$; $h_m = 0.4$; $h_s = 0.1$; $T_p = 1.790$

Test 1 @ -11 ; } ADV2 @ 365.5 ; ADV1 @ 192.4

Test 2 @ -5 ; } ± 0.3 output

Test 3 @ -1 ;

Test 4 @ +1 ;

Test 5 @ +1 move ADV2 @ 363.5 ; 190.4

Test 6 @ -1

Test 7 @ -5 Restart Wednesday

Dye test

✓

I 050 ; $h_t = 0.15$; $h_m = 0.4$; $h_s = 0.1$; $T_p = 1.265$

Test 1 @ -11 ; ADV2 365.5 ; ADV1 192.4

Test 2 @ -5

Test 3 @ -1

Test 4 @ +1

Test 5 @ +1 move ADV2 363.5 ; ADV1 190.4

Test 6 @ -1

Test 7 @ -5

Dye test ✓

F 051 ; $h_t = 0.15$; $h_m = 0.4$; $h_s = 0.15$; $T_p = 2.197$

Test 1 @ -11

Test 2 @ -5

Test 3 @ -1

Test 4 @ +1

Dye test done ✓

Test 5 @ +1 move ADV2 363.5 ; ADV1 190.4

Test 6 @ +1 Restart on Friday at 2:30 pm

Test 7 @ -1

Test 8 @ -5

Test I 052 ; $h_t = 0.15$; $h_m = 0.4$; $h_s = 0.15$; $T_p = 1.550s$

Test 1 @ -11

Test 2 @ -5

Test 3 @ -1

Test 4 @ +1

Dye test done

Test 5 @ +1 move ADV2 363.5 ADV1 190.4

Test 6 @ -1

Start Monday for

Test 7 @ -5

✓

TEST 1053

- Wavemaker not working
→ machine cannot operate!

1054 first; $h_c = 0.15$; $H = 0.2$; $T = 1.789$; $h_m = 0.4$

Test 1 @ -11 somewhat spicing gravel
rock moved under seat
redo experiment & change velocity output

Test 1a @ -11 ; output at $\pm 1 \text{ ms}^{-1}$

Test 2 @ -5

Test 3 @ -1

Test 4 @ +1

Test 5 @ +1 ADV2 363.5 ; ADV1 190.4

Test 6 @ -1

Test 7 @ -5

R 038 $h_m = 0.3$; $h_c = 0.15$; $H = 0.1$; $T = 1.790$

Test 1 @ -11 ; ADV2 365.5 ADV1 192.4
1a $u_x \pm 1 \text{ ms}^{-1}$

Test 2 @ -9

Test 3 @ -7

Test 4 @ -5

Test 5 @ -3 with more particles but 7mm, 46 more particle 2.5mm

Test 6 @ -1

Test 7 @ +1

Test 8 @ +3

Test 9 @ +5

Test 10 @ +7

Test 11 @ +9 change volume of seawater to 7mm from 25

Test 12 @ +15

Test 13 @ +1 move ADV2 to 363.5 ; 190.4

Test 14 @ +7

Test 15 @ +1

Test 15 @ -1

✓

Test 1 a -5

Test 2 a -11

Run up 7.8m
Run down 5.5m

Psych test

R038 $h_0=0.15$; $h_m=0.3$; $h=0.1$; $T=1.265$

Test 1 a -11

ADV2 365.5 ; ADV1 192.4

Test 2 a -9

Test 3 a -7

Test 4 a -5

Test 5 a -3

Test 6 a -1

Restart on Wed. 9th July

Test 7 a +1

Test 8 a +3

Test 9 a +5

Test 10 a +7

Test 11 a +15

Test 12 a +15

more ADV2 363.5 ADV1 190.4

Test 13 a +7

Test 14 a +1

Test 15 a -1

Test 16 a -5

Test 17 a -11

Run up : 7.3m
Run down : 4.5m

Psych test ✓

R039

Test 1 a -11

ADV2 365.5 ADV1 192.4
at limit → almost out of water at p

Test 2 a -9

Test 3 a -7

Test 4 a -5

- ✓ Test 5 @ -3
- Test 6 @ -1
- Test 7 @ +1
- Test 8 @ +3
- Test 9 @ +5
- Test 10 @ +7
- Test 11 @ +15

Run up 21 cm
Run down 7.2 cm

Cannot move wiper as at limit due to wave draw down

Dye test ✓

Row 0 ; $h_m = 0.3$; $h = 0.15$; $T = 1.898$; $h_e = 0.15$

- Test 1 @ -11
- Test 2 @ -9
- Test 3 @ -7
- Test 4 @ -5
- Test 5 @ -3
- Test 6 @ -1
- Test 7 @ +1
- Test 8 @ +3
- Test 9 @ +5
- Test 10 @ +7
- Test 11 @ +15

Run up 15 cm
Run down 7 cm

Dye test ✓

- Row 1 ;
- Test 1 @ -11
 - Test 2 @ -9
 - Test 3 @ -7
 - Test 4 @ -5
 - Test ⁵6 @ -3
 - Test ⁶7 @ -1
 - Test ⁷8 @ +1

✓ Test 8 ω +3

Test 9 ω +5

Test 10 ω +7

Test 11 ω +15

Run up 13.5 cm

Run down 7cm

Byc test done ✓

Extra test

IOSS ; $h_m = 0.3$; $l_t = 0.1$; $T_p = 1.790$ s

Test 2 ω -11

Test 2 ω -5

Measurement PC No : Meetpc 08

Analysis PC No : Meetpc 11

→ CD/DVD backup done

→ one copy with Sanders

photo's still camera } still to be backed
2 tapes for video } up

To:

(1)

Sanders,

I haven't done IO23 yet, run out of time

$$h_m = 0.4 \quad H = 0.15 \quad ; \quad T = 1.5505 \quad \begin{matrix} 28 \text{ MIN} \\ 4 \times 1700 \text{ sec} \end{matrix}$$

If you could run that one first that would be great.

Thank you for all your help,

Julian

P.S. Camera is in lockable cupboard with green key - I left it in the safer near loo

test 1 the signals from the ADV's are not nice.

test 2 last minute some curling of the water after curling, the signal is better.

test 3 (146 + 1700 = 1846) to stir something

test 4 (40 + 1700 = 1740) nice signal from the ADV
↳ after 1200 sec power fail

test 4b (73 + 1700 = 1773) signal is not nice stopped!

show ch's 4, 6, 11, 13

after curling it's better

test 4c (1750) P

I 024 not possible to make the steer file

I 025 the generator stopped after 2 minutes.

(± 6.3V) changed the .pcf file $H = 0.2 \rightarrow H = 0.18$

(1900 sec) \rightarrow pos. 4. done $\rightarrow H_r = 0.13 m$
 pos 1 done
 pos 2 done
 pos 3 done

I 024b changed the .pcf file $H = 0.2$
 200 - 500 sec no reflection compensation
 5000 - 14500 samples no second-order

I 026
 pos 1 ✓
 pos 2 ✓
 pos 3 ✓
 pos 4 ✓

Dye test done

I 027
 pos 1 Done \rightarrow Sanders / Wout
 pos 2 done $\rightarrow H_r = 0.07$ & in till Monday
 pos 3 done $\rightarrow H_m = 0.07$ eve about
 5-15 pm as
 my exam finishes
 5pm.

not on 7cm but on 1cm

Dye test \leftarrow pos 4 done
 redone on position 7cm as test dyb
 done \rightarrow signal not nice

if you have time then combine otherwise do not worry. Julia
 ☺

I 028
 pos 1 done $\rightarrow H_m = 0.108 m$
 pos 2 done
 pos 3 done $\rightarrow H_m = 0.108 m$
 pos 4 done

Dye test done (numbers not correct!)

Testing

Locations

Position ① is at 1cm from toe

ADV2 @ 372.5
ADV1 @ 199.4

Position ② is at 7cm from toe

ADV2 @ 372.5
ADV1 @ 199.4

Position ③ is at 15cm from toe

ADV2 @ 372.5
ADV1 @ 199.4

Position ④ is at 7cm from toe

move 2cm! * } → ADV2 @ 370.5
→ ADV1 @ 197.4

Always test for 1000 waves + allow some 100s slack ~~etc~~

∴ Test no

I024 is at $h_m = 0.4$ water level (ie. 0.6 near wave generator)

$H_s = 0.2m$; $T_p = 2.531s$

test 1 ⇒ Position 1

test 2 ⇒ Position 2

test 3 ⇒ Position 3

test 4 ⇒ Position 4

Do a quick short dye test with video cam to help visualise motion. say 3m long or so; label stake on glass panel accordingly to ensure later can be identified

✓ notation / folder org in computer

all data goes into

D:\Julia\Measurements\hm = 0.4 \ H = 0.152 \ Jawsnap

T = 2.197

Test 1
Test 2
Test 3
Test 4

Vect_1 - Test 1
Vect_2 - Test 1

Vect_1 - Test 2
Vect_2 - Test 2

⋮

Tests to be done:

- is possible? *
- ~~I024 → $h_m = 0.4$; $H = 0.2$; $T = \underline{2.531}$ s
Positions 1 → 4 + Dye test 45 min~~
 - ~~I025 → $h_m = 0.4$; $H = 0.2$; $T = \underline{1.789}$ s
Positions 1 → 4 + Dye test 31 min~~
 - I026 → $h_m = 0.3$; $H = 0.1$; $T = 1.790$ s
Positions 1 → 4 + Dye test 32 min
 - I027 → $h_m = 0.3$; $H = 0.1$; $T = 1.265$ s
Positions 4 → 4 + Dye test 23 min
 - I028 → $h_m = \underline{0.3}$; $H = \underline{0.15}$; $T = \underline{2.197}$ s
Positions 1 → 4 + Dye test 38 min
 - I029 → $h_m = 0.3$; $H = 0.15$; $T = 1.550$ s
Positions 1 → 4 + Dye test 29 min

Completed this series → thereafter

need to change toe structure!

Let water out?

Explanation of notation in tables

Location

X	Y
---	---

Refers to the X and Y location of the measurement probe

Loading Parameters

Hm0	Tp
-----	----

Refers to the generated offshore wave height and period, based on results from spectral analysis using Decomp or from expected result if Decomp did not work

U0

Expected theoretical shallow water wave velocity based on $U0 = \pi H/T * \{1/\sinh(kh)\}$, where $h = h_m - h_t$ and k is determined using Eckarts approximation formulation $k \sim \alpha(\tanh(\alpha)^{-0.5})/h$ and $\alpha = k_0 * d$

Resultant Max.

R - Vx1	R - Vx2	R - WL
---------	---------	--------

R-Vx1 is the resultant maximum value of the horizontal velocity vector of the ADV1

R-Vx2 is the resultant maximum value of the horizontal velocity vector of the ADV2

R-WL is the resultant maximum value of the waterlevel

Test

R001

R001 is the overall test series name i.e. R001 to R041 relating to the input parameters

Test1 is the sub test name i.e. relating to each position in X and Y

Coefficient for Vx1

a0	a1	b1	w
----	----	----	---

a0 refers to the a0 constant of the Fourier fit

a1 refers to the a1 coefficient of the Fourier fit (cos)

b1 refers to the b1 coefficient of the Fourier fit (sin)

w refers to the angular phase velocity of the Fourier fit

Goodness of fit parameters

sse	rsq	dfc	adj	rmse
-----	-----	-----	-----	------

For each Fourier fit, the goodness of fit parameters are provided,

sse is the sum of squares due to error

rsq is the Coefficient of determination

dfc is Degrees of freedom

adj Degree-of-freedom adjusted coefficient of determination

rmse Root mean squared error (standard error)

Appendix B - Tables of Results

Location		Loading Parameters			Resultant Max.			Test Coefficient for Vx1				Goodness of fit parameters					Coefficient for Vx2			Goodness of fit parameters					Coefficient for WL			Goodness of fit parameters					
X	Y	Hm0	Tp	U0	R - Vx1	R - Vx2	R - WL	R001	a0	a1	b1	w	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse
1	1	0.09533	1.796	0.2401	0.250	0.254	0.029	Test 1	0.0339	-0.2055	0.0665	3.51	36.1681	0.8287	7489	0.829	0.0695	0.0333	-0.2013	0.09044	21.442	0.895	7489	0.895	0.0535	5.30E-05	-0.028	0.009	0.18	0.9473	7489	0.947	0.0049
3	1	0.09533	1.796	0.2401	0.262	0.273	0.036	Test 2	0.0275	0.2279	0.0556	3.51	22.3385	0.9022	7489	0.902	0.0546	0.0376	0.2349	0.01851	16.799	0.925	7489	0.925	0.0474	7.94E-03	0.02054	0.019	0.173	0.9442	7489	0.944	0.0048
5	1	0.09533	1.796	0.2401	0.267	0.278	0.035	Test 3	0.0196	-0.0772	-0.2355	3.51	80.6156	0.7406	7489	0.741	0.1038	0.0301	-0.09198	-0.2301	15.37	0.937	7489	0.937	0.0453	8.77E-03	0.0056	-0.026	0.156	0.9439	7489	0.944	0.0046
7	1	0.09533	1.796	0.2401	0.265	0.274	0.025	Test 4	0.0292	-0.0847	0.2199	3.51	165.096	0.5575	7489	0.557	0.1485	0.0206	-0.1001	0.2324	23.76	0.91	7489	0.91	0.0563	5.00E-07	-0.0201	0.015	0.13	0.9472	7489	0.947	0.0042
9	1	0.09533	1.796	0.2401	0.287	0.271	0.024	Test 5	0.0291	-0.1439	0.2135	3.51	12.9472	0.9508	7537	0.951	0.0414	0.0171	-0.1413	0.2107	11.09	0.956	7537	0.956	0.0384	4.40E-04	-0.0212	0.011	0.113	0.9504	7537	0.95	0.0039
11	1	0.09533	1.796	0.2401	0.287	0.268	0.023	Test 6	0.0285	-0.2498	0.0664	3.51	11.5007	0.9561	7489	0.956	0.0392	0.0139	-0.2472	0.05766	17.797	0.931	7489	0.931	0.0487	7.66E-04	-0.0221	0.005	0.087	0.9565	7489	0.957	0.0034
13	1	0.09533	1.796	0.2401	0.285	0.262	0.031	Test 7	0.0271	0.0355	0.2555	3.51	9.8966	0.9618	7489	0.962	0.0364	0.0133	0.03235	0.2465	17.254	0.931	7489	0.931	0.048	9.42E-03	0.00334	0.021	0.071	0.9609	7489	0.961	0.0031
15	1	0.09533	1.796	0.2401	0.275	0.256	0.030	Test 8	0.0222	-0.1633	0.1925	3.51	12.1677	0.9515	7489	0.952	0.0403	0.0108	-0.1694	0.1769	18.28	0.925	7489	0.925	0.0494	9.16E-03	-0.0162	0.013	0.061	0.9634	7489	0.963	0.0029
17	1	0.09533	1.796	0.2401	0.264	0.249	0.020	Test 9	0.0172	0.2449	0.0286	3.51	15.8218	0.935	7489	0.935	0.046	0.0125	0.2325	0.04295	35.511	0.855	7489	0.855	0.0689	0.000121	0.0192	0.006	0.053	0.9664	7489	0.966	0.0027
17	3	0.09533	1.796	0.2401	0.304	0.256	0.020	Test 10	-0.0551	-0.0153	0.2488	3.51	434.351	0.349	7489	0.349	0.2408	0.0178	-0.02499	0.2373	33.099	0.866	7489	0.866	0.0665	0.000154	0.00425	0.02	0.054	0.9654	7489	0.965	0.0027
15	3	0.09533	1.796	0.2401	0.239	0.260	0.024	Test 11	0.0364	-0.1432	-0.1427	3.51	220.959	0.4095	7489	0.409	0.1718	0.0177	-0.1843	-0.1575	37.385	0.855	7489	0.855	0.0707	3.45E-03	-0.0128	-0.016	0.062	0.9628	7489	0.963	0.0029
7	3	0.09533	1.796	0.2401	0.265	0.257	0.035	Test 12	0.0177	0.2458	-0.0288	3.51	37.1135	0.8607	7489	0.861	0.0704	0.0142	0.2387	-0.0465	9.8521	0.957	7489	0.957	0.0363	9.97E-03	0.02301	0.01	0.13	0.9474	7489	0.947	0.0042
1	3	0.09533	1.796	0.2401	0.217	0.236	0.030	Test 13	0.0068	-0.1773	-0.1137	3.51	14.6983	0.9188	7489	0.919	0.0443	0.0148	-0.1933	-0.1076	13.098	0.933	7489	0.933	0.0418	0.000145	-0.0123	-0.027	0.176	0.9483	7489	0.948	0.0049
1	5	0.09533	1.796	0.2401	0.446	0.266	0.030	Test 14	0.3252	-0.1192	0.0223	3.51	662.861	0.0768	7496	0.077	0.2974	0.0485	-0.184	0.1169	599.73	0.229	7496	0.229	0.2829	0.000131	-0.029	0.005	0.18	0.9475	7496	0.948	0.0049
7	5	0.09533	1.796	0.2401	0.269	0.262	0.025	Test 15	0.0238	0.0783	-0.2319	3.51	178.548	0.5571	7496	0.557	0.1543	0.0197	0.08818	-0.2255	28.182	0.886	7496	0.886	0.0613	0.000119	0.01963	-0.015	0.13	0.9475	7496	0.948	0.0042
15	5	0.09533	1.796	0.2401	0.312	0.263	0.027	Test 16	0.0370	0.2724	0.0376	3.51	358.485	0.4415	7496	0.441	0.2187	0.021	0.2333	0.06582	31.338	0.876	7496	0.875	0.0647	6.31E-03	0.01842	0.009	0.063	0.9621	7496	0.962	0.0029

X	Y	Hm0	Tp	U0	R - Vx1	R - Vx2	R - WL	R002	a0	a1	b1	w	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse
1	1	0.10250	1.244	0.218	0.139	0.149	0.026	Test 1	-0.0060	0.1194	-0.0594	4.96	33.190	0.668	7496	0.668	0.067	0.0068	0.1377	-0.0359	19.435	0.796	7496	0.796	0.0509	0.000606	0.02091	-0.015	0.076	0.9702	7496	0.97	0.0032
3	1	0.10250	1.244	0.218	0.144	0.165	0.028	Test 2	0.0030	0.0283	0.1379	4.97	16.142	0.822	7496	0.821	0.046	0.0077	0.04814	0.1496	12.389	0.882	7496	0.882	0.0407	0.000254	0.01535	0.023	0.088	0.9701	7496	0.97	0.0034
5	1	0.10250	1.244	0.218	0.147	0.180	0.029	Test 3	0.0015	0.1330	-0.0590	4.97	9.061	0.898	7496	0.898	0.035	0.0098	0.1441	-0.0899	37.807	0.741	7496	0.741	0.071	5.11E-05	0.01796	-0.023	0.112	0.9662	7496	0.966	0.0039
7	1	0.10250	1.244	0.218	0.150	0.171	0.031	Test 4	0.0131	0.0635	0.1215	4.97	148.826	0.321	7496	0.321	0.141	-0.011	0.06605	0.1453	21.448	0.817	7496	0.817	0.0535	0.000315	0.0261	0.016	0.133	0.9637	7496	0.964	0.0042
9	1	0.10250	1.244	0.218	0.158	0.166	0.033	Test 5	0.0092	0.1179	0.0917	4.97	276.357	0.232	7496	0.232	0.192	0.0092	0.1294	0.08866	31.467	0.746	7496	0.746	0.0648	0.000529	0.03198	0.003	0.139	0.9651	7496	0.965	0.0043
11	1	0.10250	1.244	0.218	0.187	0.160	0.034	Test 6	0.0268	-0.0726	-0.1426	4.97	149.029	0.392	7496	0.392	0.141	0.0052	-0.07258	-0.1366	10.835	0.892	7496	0.892	0.038	0.000747	-0.0282	-0.018	0.146	0.9663	7496	0.966	0.0044
13	1	0.10250	1.244	0.218	0.151	0.150	0.036	Test 7	0.0032	0.0417	0.1413	4.97	4.796	0.944	7496	0.944	0.025	0.0016	0.03398	0.1447	18.546	0.817	7496	0.817	0.0497	0.000943	0.02438	0.025	0.144	0.9693	7496	0.969	0.0044
15	1	0.10250	1.244	0.218	0.148	0.148	0.037	Test 8	0.0047	0.1401	0.0288	4.97	6.341	0.924	7496	0.924	0.029	0.0052	0.1384	0.03653	16.519	0.823	7496	0.823	0.0469	0.001172	0.03267	-0.016	0.138	0.9727	7496	0.973	0.0043
17	1	0.10250	1.244	0.218	0.140	0.145	0.039	Test 9	0.0035	-0.0317	-0.1324	4.97	3.088	0.958	7496	0.957	0.020	0.0084	-0.02359	-0.1346	19.904	0.779	7496	0.779	0.0515	0.001352	-0.0291	-0.024	0.126	0.9766	7496	0.977	0.0041
17	3	0.10250	1.244	0.218	0.139	0.144	0.039	Test 10	0.0035	0.0428	-0.1291	4.97	3.720	0.949	7496	0.949	0.022	0.0072	0.04157	-0.1306	25.346	0.736	7496	0.736	0.0581	0.001379	0.00908	-0.036	0.126	0.9765	7496	0.977	0.0041
15	3	0.10250	1.244	0.218	0.143	0.150	0.037	Test 11	0.0014	-0.1365	0.0367	4.97	5.819	0.928	7496	0.928	0.028	0.0064	-0.1381	0.03919	26.989	0.741	7496	0.741	0.06	0.001166	-0.0246	0.027	0.139	0.9725	7496	0.973	0.0043
7	3	0.10250	1.244	0.218	0.155	0.168	0.031	Test 12	0.0002	0.1298	0.0842	4.97	46.390	0.659	7496	0.659	0.079	0.0079	0.1326	0.08983	30.23	0.761	7496	0.761	0.0635	0.00024	0.0306	0.003	0.139	0.9622	7496	0.962	0.0043
1	3	0.10250	1.244	0.218	0.144	0.157	0.027	Test 13	0.0046	0.1258	-0.0607	4.97	24.939	0.746	7496	0.746	0.058	0.0094	0.136	-0.0569	58.876	0.581	7496	0.58	0.0886	0.000605	0.02135	-0.016	0.076	0.972	7496	0.972	0.0032
1	5	0.10250	1.244	0.218	0.437	0.157	0.027	Test 14	0.3050	-0.1227	-0.0487	4.96	988.740	0.062	7496	0.062	0.363	-0.018	-0.1302	-0.0474	179.53	0.286	7496	0.286	0.1548	0.000585	-0.0261	0.005	0.077	0.9716	7496	0.972	0.0032
7	5	0.10250	1.244	0.218	0.168	0.164	0.031	Test 15	0.0051	-0.1043	0.1254	4.97	165.648	0.376	7496	0.376	0.149	0.002	-0.1048	0.1242	30.127	0.767	7496	0.767	0.0634	0.000209	0.00623	0.03	0.135	0.9632	7496	0.963	0.0042
15	5	0.10250	1.244	0.218	0.140	0.154	0.037	Test 16	0.0032	0.0059	-0.1369	4.97	42.008	0.626	7496	0.626	0.075	0.0069	0.00488	-0.1473	27.05	0.751	7496	0.751	0.0601	0.001094	-0.0206	-0.03	0.141	0.9718	7496	0.972	0.0043

X	Y	Hm0	Tp	U0	R - Vx1	R - Vx2	R - WL	R003	a0	a1	b1	w	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse
1	1	0.14815	2.120	0.3855	0.406	0.427	0.058	Test 1	0.06989	-0.0777	0.327																						

Appendix B - Tables of Results

Location	Loading Parameters			Resultant Max.			Test Coefficient for Vx1					Goodness of fit parameters					Coefficient for Vx2			Goodness of fit parameters					Coefficient for WL			Goodness of fit parameters					
17	5	0.14815	2.120	0.3855	0.437	0.393	0.042	Test 27	0.0327	0.0481	0.401	2.86	43.8687	0.9332	7496	0.933	0.0765	0.0259	0.034	0.366	107.58	0.826	7496	0.826	0.1198	0.000262	-0.0239	0.034	2.824	0.6959	7496	0.696	0.0194
17	7	0.14815	2.120	0.3855	0.432	0.312	0.042	Test 28	0.0318	0.328	0.23	2.86	42.3362	0.9346	7496	0.935	0.0752	-0.043	0.21	0.169	371.52	0.432	7496	0.432	0.2226	0.000283	0.00785	0.041	2.822	0.6957	7496	0.696	0.0194
15	7	0.14815	2.120	0.3855	0.420	0.406	0.044	Test 29	0.03	0.131	0.367	2.86	83.6186	0.8746	7656	0.875	0.1045	0.0259	0.129	0.358	88.759	0.863	7656	0.863	0.1077	0.00019	-0.0201	0.039	2.862	0.7179	7656	0.718	0.0193
13	7	0.14815	2.120	0.3855	0.413	0.410	0.047	Test 30	0.0328	-0.228	0.304	2.86	101.798	0.8425	7496	0.842	0.1165	0.0301	-0.231	0.302	94.687	0.852	7496	0.852	0.1124	-0.0014	-0.0446	0.008	2.861	0.7295	7496	0.729	0.0195
11	7	0.14815	2.120	0.3855	0.282	0.410	0.049	Test 31	0.025	-0.178	-0.186	2.86	557.072	0.31	7496	0.31	0.2726	0.0342	-0.271	-0.26	104.6	0.836	7496	0.836	0.1181	-0.00158	0.00082	-0.047	2.721	0.7529	7496	0.753	0.0191
9	7	0.14815	2.120	0.3855	0.428	0.367	0.050	Test 32	0.0478	-0.299	0.235	2.86	122.742	0.8162	7496	0.816	0.128	0.0435	-0.268	0.182	294.56	0.573	7496	0.573	0.1982	-0.0016	-0.0483	-0.007	2.639	0.7725	7496	0.772	0.0188
7	7	0.14815	2.120	0.3855	0.376	0.409	0.052	Test 33	0.0304	-0.327	-0.111	2.86	205.375	0.6867	7496	0.687	0.1655	-0.063	-0.337	-0.0798	537.33	0.457	7496	0.457	0.2677	-0.00144	-0.0221	-0.046	2.651	0.785	7496	0.785	0.0188
5	7	0.14815	2.120	0.3855	0.409	0.211	0.054	Test 34	0.0438	0.0852	0.355	2.86	66.7903	0.8823	7496	0.882	0.0944	-0.066	0.0453	0.138	739.47	0.097	7496	0.096	0.3141	-0.00142	-0.0287	0.044	2.604	0.7992	7496	0.799	0.0186
3	7	0.14815	2.120	0.3855	0.326	0.314	0.056	Test 35	0.016	-0.22	-0.218	2.86	354.847	0.5041	7496	0.504	0.2176	0.0172	-0.209	-0.211	409.17	0.449	7496	0.448	0.2336	-0.00153	0.0043	-0.054	2.539	0.8149	7496	0.815	0.0184
1	7	0.14815	2.120	0.3855	0.263	0.292	0.058	Test 36	-0.00431	-0.123	0.228	2.86	484.613	0.3433	7496	0.343	0.2543	-0.005	-0.12	0.26	510.01	0.377	7496	0.377	0.2608	-0.00166	-0.0548	0.014	2.451	0.8303	7496	0.83	0.0181
1	9	0.14815	2.120	0.3855	0.349	0.289	0.058	Test 37	0.0256	-0.1	-0.308	2.86	181.266	0.6876	7496	0.688	0.1555	-0.013	-0.0798	-0.264	335.17	0.46	7496	0.46	0.2115	-0.0017	0.0317	-0.047	2.431	0.8318	7496	0.832	0.018
3	9	0.14815	2.120	0.3855	0.318	0.359	0.056	Test 38	0.00412	-0.092	0.3	2.86	645.021	0.367	7496	0.367	0.2933	0.02	-0.111	0.32	157.71	0.732	7496	0.732	0.145	-0.0015	-0.0508	0.019	2.517	0.8161	7496	0.816	0.0183
5	9	0.14815	2.120	0.3855	0.391	0.240	0.054	Test 39	0.0374	-0.342	-0.09	2.86	107.297	0.8155	7496	0.816	0.1196	-0.032	-0.194	-0.0753	515.09	0.24	7496	0.24	0.2621	-0.00143	-0.0197	-0.049	2.629	0.7976	7496	0.798	0.0187
7	9	0.14815	2.120	0.3855	0.386	0.308	0.052	Test 40	0.0332	-0.222	0.274	2.86	199.404	0.7013	7496	0.701	0.1631	0.0366	-0.177	0.206	580.6	0.323	7496	0.323	0.2783	-0.00151	-0.0508	0.002	2.656	0.7856	7496	0.786	0.0188
9	9	0.14815	2.120	0.3855	0.401	0.361	0.050	Test 41	0.0351	-0.324	0.17	2.86	150.719	0.7695	7496	0.769	0.1418	0.0273	-0.294	0.157	302.11	0.581	7496	0.581	0.2008	-0.00162	-0.0451	-0.019	2.699	0.7684	7496	0.768	0.019
11	9	0.14815	2.120	0.3855	0.429	0.341	0.048	Test 42	0.0428	0.38	-0.0703	2.86	52.6423	0.9142	7496	0.914	0.0838	-0.003	0.334	-0.0505	206.78	0.675	7496	0.675	0.1661	-0.00165	0.0373	0.028	2.729	0.7516	7496	0.752	0.0191
13	9	0.14815	2.120	0.3855	0.429	0.354	0.046	Test 43	0.0406	0.0405	0.386	2.86	58.4191	0.9063	7496	0.906	0.0883	0.0006	0.0276	0.352	165.13	0.739	7496	0.739	0.1484	-0.00162	-0.029	0.034	2.762	0.7342	7496	0.734	0.0192
15	9	0.14815	2.120	0.3855	0.426	0.392	0.040	Test 44	0.0374	-0.0818	-0.38	2.86	63.2906	0.9	7496	0.9	0.0919	0.009	-0.0919	-0.372	65.274	0.894	7496	0.894	0.0933	-0.0015	0.0234	-0.03	2.767	0.7145	7496	0.714	0.0192
17	9	0.14815	2.120	0.3855	0.364	0.383	0.042	Test 45	0.0208	0.343	0.0199	2.86	433.037	0.506	7496	0.506	0.2404	0.006	0.377	0.0123	81.998	0.867	7496	0.867	0.1046	-0.00152	0.028	0.029	2.782	0.6936	7496	0.694	0.0193
17	11	0.14815	2.120	0.3855	0.422	0.397	0.042	Test 46	0.0311	0.378	-0.1	2.86	52.7386	0.9162	7496	0.916	0.0839	-0.009	0.373	-0.105	65.922	0.895	7496	0.895	0.0938	-0.00147	0.0371	0.017	2.815	0.6911	7496	0.691	0.0194
15	11	0.14815	2.120	0.3855	0.426	0.392	0.045	Test 47	0.0329	-0.0159	-0.393	2.86	52.3297	0.9176	7496	0.918	0.0836	-0.006	0.0464	-0.383	73.555	0.884	7496	0.884	0.0991	-0.00166	0.0272	-0.033	2.76	0.7161	7496	0.716	0.0192
13	11	0.14815	2.120	0.3855	0.425	0.375	0.047	Test 48	0.0323	0.366	0.142	2.86	51.5299	0.9183	7496	0.918	0.0829	-0.001	0.343	0.149	109.47	0.828	7496	0.828	0.1208	-0.00165	0.0201	0.04	2.764	0.7336	7496	0.734	0.0192
11	11	0.14815	2.120	0.3855	0.426	0.372	0.049	Test 49	0.0361	0.39	-0.00184	2.86	51.8412	0.917	7496	0.917	0.0832	0.0019	0.37	-0.0035	107.6	0.829	7496	0.829	0.1198	-0.00172	0.0322	0.034	2.733	0.7528	7496	0.753	0.0191
9	11	0.14815	2.120	0.3855	0.417	0.365	0.051	Test 50	0.0349	-0.0869	0.372	2.86	59.8085	0.9018	7496	0.902	0.0893	-0.006	-0.055	0.354	148.67	0.765	7496	0.764	0.1408	-0.00171	-0.0419	0.025	2.706	0.7687	7496	0.769	0.019
7	11	0.14815	2.120	0.3855	0.404	0.352	0.052	Test 51	0.0325	0.249	-0.276	2.86	78.84	0.8684	7496	0.868	0.1026	-0.005	0.227	-0.263	165.9	0.733	7496	0.733	0.1488	-0.00162	0.05	-0.002	2.704	0.7826	7496	0.783	0.019
5	11	0.14815	2.120	0.3855	0.395	0.338	0.054	Test 52	0.03	0.168	-0.324	2.86	91.8262	0.8451	7496	0.845	0.1107	-0.003	0.159	-0.294	202.99	0.675	7496	0.674	0.1646	-0.00169	0.0512	-0.011	2.632	0.7975	7496	0.797	0.0187
3	11	0.14815	2.120	0.3855	0.375	0.315	0.055	Test 53	0.0259	0.0253	-0.348	2.86	114.728	0.7995	7496	0.8	0.1237	-0.026	0.0209	-0.289	292.4	0.519	7496	0.519	0.1975	-0.00179	0.042	-0.033	2.543	0.8144	7496	0.814	0.0184
1	11	0.14815	2.120	0.3855	0.328	0.317	0.058	Test 54	0.0145	-0.102	-0.296	2.86	359.066	0.5066	7496	0.506	0.2189	0.0193	-0.0982	-0.281	689.45	0.326	7496	0.326	0.3033	-0.0019	0.0292	-0.048	2.444	0.8303	7496	0.83	0.0181
1	13	0.14815	2.120	0.3855	0.325	0.300	0.058	Test 55	-0.00845	0.206	-0.24	2.86	252.646	0.5988	7489	0.599	0.1837	-0.071	0.145	-0.177	424.07	0.318	7489	0.317	0.238	-0.00191	0.0555	-0.011	2.444	0.8308	7489	0.831	0.0181
7	13	0.14815	2.120	0.3855	0.383	0.366	0.053	Test 56	0.0139	-0.326	0.173	2.86	131.662	0.7955	7489	0.795	0.1326	-0.032	-0.29	0.166	241.37	0.636	7489	0.636	0.1795	-0.00168	-0.0495	-0.012	2.715	0.782	7489	0.782	0.019
15	13	0.14815	2.120	0.3855	0.409	0.400	0.045	Test 57	0.0235	-0.2	-0.33	2.86	96.7743	0.8562	7489	0.856	0.1137	-0.022	-0.2	-0.32	109.78	0.834	7489	0.834	0.1211	-0.00182	0.00984	-0.042	2.768	0.7168	7489	0.717	0.0192
15	15	0.14815	2.120	0.3855	0.395	0.410	0.045	Test 58	0.00977	-0.29	-0.254	2.86	129.773	0.8114	7489	0.811	0.1316	-0.046	-0.275	-0.239	196.98	0.717	7489	0.717	0.1622	-0.00179	-0.008	-0.043	2.776	0.7163	7489	0.716	0.0193
7	15	0.14815	2.120	0.3855	0.370	0.380	0.052	Test 59	-0.00624	-0.363	-0.0212	2.86	181.219	0.7328	7489	0.733	0.1556	-0.057	-0.322	-0.0253	311.21	0.557	7489	0.557	0.2039	-0.00174	-0.0358	-0.036	2.704	0.7805	7489	0.78	0.019
1	15	0.14815	2.120	0.3855	0.330	0.299	0.058	Test 60	-0.03	-0.3	-0.00545	2.86	320.713	0.5446	7489	0.544	0.2069	-0.089	-0.21	0.00443	493.14	0.264	7489	0.263	0.2566	-0.00204	-0.042	-0.037	2.401	0.8342	7489	0.834	0.0179
1	17	0.14815	2.120	0.3855	0.368	0.318	0.059	Test 61	-0.0487	0.144	-0.285	2.86	391.903	0.4953	7489	0.495	0.2288	-0.096	0.113	-0.191	549.27	0.252	7489	0.252	0.2708	-0.002	0.0499	-0.027	2.425	0.8326	7489	0.833	0.018
7	17	0.14815	2.120	0.3855																													

Appendix B - Tables of Results

Location	Loading Parameters				Resultant Max.			Test Coefficient for Vx1				Goodness of fit parameters					Coefficient for Vx2			Goodness of fit parameters					Coefficient for WL					Goodness of fit parameters				
15	1	0.15332	1.550	0.3687	0.349	0.329	0.039	Test 8	0.00592	0.3421	0.03017	4.05	25.8773	0.9447	7496	0.945	0.0588	0.002	0.3251	0.03418	15.905	0.962	7496	0.962	0.0461	0.002909	0.03495	0.009	0.482	0.9103	7496	0.91	0.008	
17	1	0.15332	1.550	0.3687	0.332	0.311	0.0401	Test 9	0.00337	-0.2893	0.1569	4.05	28.9798	0.9334	7496	0.933	0.0622	0.0012	-0.2757	0.1411	33.775	0.914	7496	0.914	0.0671	0.002605	-0.024	0.029	0.552	0.9053	7496	0.905	0.0086	
17	3	0.15332	1.550	0.3687	0.320	0.328	0.0401	Test 10	0.0006	-0.2106	-0.2402	4.05	88.2878	0.8126	7496	0.813	0.1085	0.011	-0.2011	-0.2445	35.261	0.914	7496	0.914	0.0686	0.002592	-0.0354	-0.012	0.547	0.9062	7496	0.906	0.0085	
15	3	0.15332	1.550	0.3687	0.346	0.335	0.0389	Test 11	0.0172	-0.1443	-0.2952	4.05	144.364	0.7372	7496	0.737	0.1388	0.0094	-0.131	-0.2984	28.732	0.933	7496	0.933	0.0619	0.002934	-0.0283	-0.022	0.469	0.912	7496	0.912	0.0079	
7	3	0.15332	1.550	0.3687	0.333	0.345	0.0373	Test 12	-0.01121	-0.3005	-0.1143	4.05	161.826	0.7054	7496	0.705	0.1469	0.0095	-0.3225	-0.0928	26.915	0.94	7496	0.94	0.0599	0.004091	-0.0315	-0.011	0.264	0.9398	7496	0.94	0.0059	
1	3	0.15332	1.550	0.3687	0.321	0.341	0.0405	Test 13	-0.02201	0.03239	-0.2977	4.05	86.7586	0.795	7496	0.795	0.1076	0.0147	0.03682	-0.3239	49.567	0.889	7496	0.889	0.0813	0.004352	0.00942	-0.035	0.359	0.9317	7496	0.932	0.0069	
1	5	0.15332	1.550	0.3687	0.376	0.271	0.0404	Test 14	-0.134	0.01168	-0.2413	4.05	630.405	0.2577	7496	0.257	0.29	0.0225	0.08777	-0.2324	472.68	0.329	7496	0.328	0.2511	0.004343	0.01647	-0.032	0.365	0.9304	7496	0.93	0.007	
7	5	0.15332	1.550	0.3687	0.290	0.339	0.0373	Test 15	0.00189	0.258	-0.1274	4.05	379.944	0.4497	7496	0.45	0.2251	0.0162	0.2762	-0.1669	162.4	0.706	7496	0.706	0.1472	0.004058	0.02808	-0.018	0.261	0.9406	7496	0.941	0.0059	
15	5	0.15332	1.550	0.3687	0.328	0.336	0.039	Test 16	0.03793	0.2106	-0.1991	4.05	282.168	0.5274	7496	0.527	0.194	0.0146	0.2322	-0.2225	145.1	0.728	7496	0.728	0.1391	0.002893	0.01548	-0.033	0.464	0.9133	7496	0.913	0.0079	

X	Y	Hm0	TP	U0	R - Vx1	R - Vx2	R - WL	R006	a0	a1	b1	w	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse
1	1	0.17552	2.439	0.4649	0.430	0.411	0.0759	Test 1	0.1024	-0.1092	-0.309	2.48	188.939	0.6807	7496	0.681	0.1588	0.0541	-0.09434	-0.3444	165.49	0.743	7496	0.743	0.1486	0.002648	0.06112	-0.04	3.625	0.8474	7496	0.847	0.022
3	1	0.17552	2.439	0.4649	0.474	0.398	0.0741	Test 2	0.08397	0.1109	0.3738	2.48	208.301	0.7324	7496	0.732	0.1667	0.0326	0.07602	0.3577	235.87	0.68	7496	0.68	0.1774	0.002519	-0.0624	0.035	3.661	0.8401	7496	0.84	0.0221
5	1	0.17552	2.439	0.4649	0.485	0.321	0.0719	Test 3	0.07024	-0.4093	0.06401	2.48	229.386	0.7373	7496	0.737	0.1749	-0.035	-0.2807	0.05495	347.09	0.469	7496	0.469	0.2152	0.002294	-0.0326	-0.062	3.779	0.8279	7496	0.828	0.0225
7	1	0.17552	2.439	0.4649	0.469	0.353	0.0701	Test 4	0.04824	0.07523	0.4135	2.48	290.993	0.6947	7496	0.695	0.197	-0.026	0.03673	0.325	378.71	0.514	7496	0.514	0.2248	0.002157	-0.058	0.035	3.899	0.8161	7496	0.816	0.0228
9	1	0.17552	2.439	0.4649	0.406	0.345	0.0681	Test 5	0.00803	0.3108	0.2484	2.48	403.568	0.5953	7496	0.595	0.232	-0.043	0.2193	0.2084	390.44	0.468	7496	0.468	0.2282	-0.00207	-0.0203	0.063	4.017	0.803	7496	0.803	0.0231
11	1	0.17552	2.439	0.4649	0.393	0.337	0.0663	Test 6	-0.02322	0.0319	-0.3687	2.48	601.416	0.5257	9736	0.526	0.2485	-0.061	0.02984	-0.2741	522.45	0.415	9736	0.415	0.2317	0.002031	0.06206	-0.017	5.331	0.7906	9736	0.791	0.0234
13	1	0.17552	2.439	0.4649	0.387	0.324	0.0643	Test 7	-0.05792	-0.2899	0.155	2.48	512.888	0.4413	7496	0.441	0.2616	-0.075	-0.2245	0.1099	412.2	0.362	7496	0.362	0.2345	0.002011	-0.0475	-0.04	4.084	0.7809	7496	0.781	0.0233
15	1	0.17552	2.439	0.4649	0.385	0.310	0.0623	Test 8	-0.09146	0.08779	0.2799	2.48	539.46	0.3744	7496	0.374	0.2683	-0.084	0.06505	0.2157	398.46	0.323	7496	0.323	0.2306	0.002244	-0.045	0.04	4.055	0.7692	7496	0.769	0.0233
17	1	0.17552	2.439	0.4649	0.373	0.275	0.0605	Test 9	-0.1198	-0.0644	-0.245	2.48	562.74	0.2996	7496	0.299	0.274	-0.099	-0.06374	-0.1647	377.48	0.237	7496	0.236	0.2244	-0.00232	0.04067	-0.042	4.031	0.7591	7496	0.759	0.0232
17	3	0.17552	2.439	0.4649	0.356	0.301	0.0603	Test 10	-0.05479	0.2842	-0.0984	2.48	392.243	0.4638	7496	0.464	0.2288	-0.073	0.2194	-0.0623	370.55	0.345	7496	0.345	0.2223	-0.00222	0.04411	0.038	4.079	0.7562	7496	0.756	0.0233
15	3	0.17552	2.439	0.4649	0.375	0.308	0.0619	Test 11	-0.02528	-0.3491	-0.02602	2.48	355.704	0.5637	7496	0.564	0.2178	-0.062	-0.245	-0.0234	353.58	0.391	7496	0.391	0.2172	0.002456	-0.0245	-0.054	4.457	0.7485	7496	0.748	0.0244
7	3	0.17552	2.439	0.4649	0.407	0.324	0.0702	Test 12	0.02857	-0.3783	-0.0119	2.48	324.629	0.6234	7496	0.623	0.2081	0.0017	-0.3214	-0.0228	303.25	0.562	7496	0.562	0.2011	0.002688	-0.0312	-0.06	4.064	0.808	7496	0.808	0.0233
1	3	0.17552	2.439	0.4649	0.368	0.359	0.0769	Test 13	0.0528	0.2098	0.235	2.48	308.902	0.5465	7496	0.546	0.203	0.0305	0.1749	0.2782	249.89	0.619	7496	0.618	0.1826	0.003494	-0.0299	0.067	3.605	0.8487	7496	0.849	0.0219
1	5	0.17552	2.439	0.4649	0.317	0.270	0.077	Test 14	0.00784	-0.2448	-0.1886	2.48	379.933	0.4852	7496	0.485	0.2251	-0.022	-0.1885	-0.1603	414.12	0.357	7496	0.356	0.235	0.003424	0.01794	-0.071	3.594	0.8495	7496	0.849	0.0219
7	5	0.17552	2.439	0.4649	0.405	0.327	0.0702	Test 15	0.02707	-0.3513	0.14	2.48	285.445	0.6527	7496	0.653	0.1951	0.0006	-0.3057	0.1154	281.65	0.587	7496	0.587	0.1938	0.002677	-0.0535	-0.041	4.064	0.8081	7496	0.808	0.0233
15	5	0.17552	2.439	0.4649	0.371	0.320	0.0626	Test 16	-0.01229	0.2247	0.279	2.48	360.796	0.5715	7496	0.571	0.2194	-0.055	0.1578	0.2129	347.04	0.432	7496	0.431	0.2152	0.002639	-0.0192	0.057	4.254	0.7601	7496	0.76	0.0238

X	Y	Hm0	TP	U0	R - Vx1	R - Vx2	R - WL	R007	a0	a1	b1	w	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse
1	1	0.19340	1.769	0.4852	0.535	0.366	0.0636	Test 1	0.1006	0.3601	-0.2427	3.51	164.721	0.811	7496	0.811	0.1482	0.0093	0.3185	-0.1612	370.5	0.563	7496	0.563	0.2223	0.005734	0.05378	0.021	2.188	0.8515	7496	0.851	0.0171
3	1	0.19340	1.769	0.4852	0.558	0.382	0.0614	Test 2	0.07822	0.357	-0.3209	3.51	144.827	0.8565	7496	0.856	0.139	-0.012	0.3061	-0.2072	386.82	0.57	7496	0.57	0.2272	0.005701	0.05525	0.007	2.325	0.8335	7496	0.833	0.0176
5	1	0.19340	1.769	0.4852	0.565	0.430	0.0586	Test 3	0.05693	-0.4303	-0.2699	3.51	158.346	0.8594	7496	0.859	0.1453	-0.034	-0.3027	-0.2558	380.85	0.607	7496	0.607	0.2254	-0.00597	-0.0153	-0.05	2.179	0.8269	7496	0.827	0.017
7	1	0.19340	1.769	0.4852	0.548	0.460	0.056	Test 4	0.0389	0.4231	0.2839	3.51	197.798	0.831	7496	0.831	0.1624	-0.039	0.3199	0.2747	347.33	0.657	7496	0.657	0.2153	-0.00657	0.0161	0.047	1.925	0.8262	7496	0.826	0.016
9	1	0.19340	1.769	0.4852	0.527	0.477	0.0533	Test 5	0.01467	-0.507	0.07515	3.51	234.763	0.8076	7496	0.808	0.177	-0.029	-0.4475	0.0177	303.18	0.713	7496	0.7									

Appendix B - Tables of Results

Location		Loading Parameters			Resultant Max.			Test Coefficient for Vx1				Goodness of fit parameters					Coefficient for Vx2			Goodness of fit parameters					Coefficient for WL			Goodness of fit parameters					
X	Y	Hm0	TP	U0	R - Vx1	R - Vx2	R - WL	R009	a0	a1	b1	w	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse
1	1	0.09799	1.217	0.2777	0.253	0.255	0.1223	Test 1	0.00467	0.2145	-0.1255	4.96	237.991	0.4932	7496	0.493	0.1782	0.0283	0.1805	-0.1379	44.793	0.812	7496	0.812	0.0773	-0.0994	0.02056	-0.01	0.149	0.9297	7496	0.93	0.0045
3	1	0.09799	1.217	0.2777	0.244	0.268	0.1212	Test 2	0.00496	-0.1339	-0.1985	4.97	157.054	0.5778	7496	0.578	0.1447	0.0227	-0.1519	-0.1926	38.384	0.855	7496	0.855	0.0716	-0.0995	-0.0109	-0.019	0.03	0.9835	7496	0.984	0.002
5	1	0.09799	1.217	0.2777	0.253	0.268	0.1204	Test 3	0.00441	-0.142	-0.2045	4.97	105.504	0.6878	7496	0.688	0.1186	0.0139	-0.1544	-0.2024	40.614	0.857	7496	0.857	0.0736	-0.09948	-0.0135	-0.016	0.009	0.9943	7496	0.994	0.0011
7	1	0.09799	1.217	0.2777	0.282	0.262	0.1204	Test 4	0.08923	-0.1228	0.1482	4.96	393.744	0.2608	7496	0.261	0.2292	0.0069	-0.1954	0.1647	40.277	0.859	7496	0.859	0.0733	-0.09929	-0.0137	0.016	0.022	0.9872	7496	0.987	0.0017
9	1	0.09799	1.217	0.2777	0.268	0.255	0.1209	Test 5	0.00716	-0.2612	-0.00626	4.97	32.2298	0.8881	7496	0.888	0.0656	0.0013	-0.2511	-0.0337	7.732	0.969	7496	0.969	0.0321	-0.09909	-0.0209	0.006	0.048	0.9739	7496	0.974	0.0025
11	1	0.09799	1.217	0.2777	0.260	0.250	0.1221	Test 6	0.00803	0.1152	0.2242	4.97	15.81	0.9378	7496	0.938	0.0459	0.002	0.08609	0.2321	6.0184	0.975	7496	0.975	0.0283	-0.09874	0.01787	0.015	0.095	0.9557	7496	0.956	0.0036
13	1	0.09799	1.217	0.2777	0.251	0.245	0.1235	Test 7	0.00941	0.2268	-0.08441	4.97	7.8696	0.9654	7496	0.965	0.0324	0.0059	0.2272	-0.0748	7.8451	0.965	7496	0.965	0.0324	-0.09834	0.0162	-0.019	0.143	0.9434	7496	0.943	0.0044
15	1	0.09799	1.217	0.2777	0.247	0.236	0.1251	Test 8	0.01094	-0.2241	0.0746	4.96	8.7412	0.9599	7496	0.96	0.0341	0.0045	-0.224	0.05817	4.8798	0.976	7496	0.976	0.0255	-0.09846	-0.0162	0.021	0.247	0.9149	7496	0.915	0.0057
17	1	0.09799	1.217	0.2777	0.234	0.227	0.1269	Test 9	0.0089	0.2246	0.00621	4.97	4.5543	0.9765	7496	0.977	0.0246	0.0025	0.2244	0.00325	5.0181	0.974	7496	0.974	0.0259	-0.09803	0.02189	-0.019	0.226	0.9329	7496	0.933	0.0055
17	3	0.09799	1.217	0.2777	0.246	0.232	0.1271	Test 10	0.01811	0.09556	-0.2065	4.97	6.004	0.97	7496	0.97	0.0283	0.0028	0.1019	-0.2048	5.6427	0.972	7496	0.972	0.0274	-0.09805	-0.0101	-0.027	0.204	0.9393	7496	0.939	0.0052
15	3	0.09799	1.217	0.2777	0.244	0.243	0.1257	Test 11	0.0068	0.00426	0.2373	4.97	84.8714	0.7134	7496	0.713	0.1064	0.0042	-0.01546	0.2382	8.6379	0.961	7496	0.961	0.0339	-0.09844	0.01434	0.023	0.169	0.9429	7496	0.943	0.0048
7	3	0.09799	1.217	0.2777	0.222	0.260	0.1208	Test 12	-0.1211	0.09984	0.01296	4.97	326.249	0.1043	7496	0.104	0.2086	0.0022	0.2418	-0.0892	11.653	0.955	7496	0.955	0.0394	-0.09977	0.01746	-0.012	0.018	0.9894	7496	0.989	0.0015
1	3	0.09799	1.217	0.2777	0.267	0.251	0.1231	Test 13	-0.02739	-0.0268	0.2378	4.97	19.4824	0.9168	7496	0.917	0.051	0.0062	-0.02918	0.2435	7.4787	0.968	7496	0.968	0.0316	-0.09992	0.00739	0.022	0.087	0.9585	7496	0.959	0.0034
1	5	0.09799	1.217	0.2777	0.265	0.264	0.123	Test 14	-0.01457	0.25	0.00161	4.97	10.2826	0.958	7496	0.958	0.037	0.0031	0.2607	0.01434	16.96	0.938	7496	0.938	0.0476	-0.09989	0.02255	0.005	0.087	0.9583	7496	0.958	0.0034
7	5	0.09799	1.217	0.2777	0.275	0.279	0.1208	Test 15	0.00213	-0.1575	-0.2226	4.97	95.1932	0.7454	7496	0.745	0.1127	-0.012	-0.157	-0.2155	9.4368	0.966	7496	0.966	0.0355	-0.09976	-0.016	-0.014	0.019	0.9885	7496	0.989	0.0016
15	5	0.09799	1.217	0.2777	0.262	0.257	0.1258	Test 16	0.02398	0.09121	0.2202	4.96	117.523	0.6444	7496	0.644	0.1252	-0.01	0.05654	0.2402	4.8784	0.979	7496	0.979	0.0255	-0.09843	0.02212	0.016	0.182	0.9388	7496	0.939	0.0049

X	Y	Hm0	TP	U0	R - Vx1	R - Vx2	R - WL	R0010	a0	a1	b1	w	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse
1	1	0.15	2.197	0.2145	0.494	0.306	0.1582	Test 1	0.102	0.3077	0.2423	3.31	237.94	0.7074	7496	0.707	0.1782	0.0045	0.208	0.2182	314.52	0.52	7496	0.52	0.2048	-0.1021	-0.0174	0.053	3.265	0.7833	7496	0.783	0.0209
3	1	0.15	2.197	0.2145	0.487	0.327	0.155	Test 2	0.0704	0.215	-0.3574	3.31	272.181	0.7056	7496	0.706	0.1906	-0.02	0.1866	-0.2436	323.25	0.522	7496	0.522	0.2077	-0.1017	0.05327	5E-04	3.209	0.7683	7496	0.768	0.0207
5	1	0.15	2.197	0.2145	0.472	0.370	0.1522	Test 3	0.04375	-0.4214	-0.07642	3.31	291.725	0.7021	7496	0.702	0.1973	-0.04	-0.3173	-0.0899	323.34	0.558	7496	0.558	0.2077	-0.1014	-0.0202	-0.047	3.275	0.747	7496	0.747	0.0209
7	1	0.15	2.197	0.2145	0.453	0.401	0.1497	Test 4	0.01678	0.2981	-0.3184	3.31	299.91	0.7041	7496	0.704	0.2	-0.05	0.2592	-0.2356	308.41	0.599	7496	0.599	0.2028	-0.1012	0.04798	0.007	3.375	0.7231	7496	0.723	0.0212
9	1	0.15	2.197	0.2145	0.436	0.425	0.1475	Test 5	-0.01041	0.05004	-0.4227	3.31	331.098	0.6724	7496	0.672	0.2102	-0.061	0.08993	-0.352	314.03	0.612	7496	0.612	0.2047	-0.1014	0.03881	-0.025	3.41	0.7003	7496	0.7	0.0213
11	1	0.15	2.197	0.2145	0.455	0.436	0.145	Test 6	-0.0354	-0.1169	0.4028	3.31	343.154	0.6578	7496	0.658	0.214	-0.073	-0.1338	0.3376	335.07	0.596	7496	0.596	0.2114	-0.1016	-0.0384	0.02	3.465	0.671	7496	0.671	0.0215
13	1	0.15	2.197	0.2145	0.461	0.429	0.1429	Test 7	-0.06723	0.3908	0.05027	3.31	373.495	0.6092	7496	0.609	0.2232	-0.087	0.3362	0.06328	358.23	0.551	7496	0.551	0.2186	-0.1017	0.03025	0.028	3.523	0.6443	7496	0.644	0.0217
15	1	0.15	2.197	0.2145	0.450	0.415	0.1406	Test 8	-0.09829	0.321	-0.1443	3.31	416.124	0.5274	7496	0.527	0.2356	-0.096	0.29	-0.1321	364.46	0.511	7496	0.511		-0.1016	0.03861	0.006	3.675	0.6087	7496	0.609	0.0221
17	1	0.15	2.197	0.2145	0.432	0.403	0.1389	Test 9	-0.1353	0.1267	-0.268	3.31	445.995	0.425	7496	0.425	0.2439	-0.099	0.09785	-0.2877	348.8	0.498	7496	0.498	0.2157	-0.1014	0.02729	-0.026	3.821	0.5797	7496	0.58	0.0226
17	3	0.15	2.197	0.2145	0.435	0.436	0.1388	Test 10	-0.05061	-0.3649	-0.1211	3.31	235.462	0.7019	7496	0.702	0.1772	-0.055	-0.3577	-0.1323	238.75	0.696	7496	0.696	0.1785	-0.1014	-0.0239	-0.029	3.815	0.5792	7496	0.579	0.0226
15	3	0.15	2.197	0.2145	0.448	0.457	0.1407	Test 11	-0.03101	-0.275	0.3139	3.31	213.768	0.7534	7496	0.753	0.1689	-0.047	-0.2773	0.3019	200.84	0.758	7496	0.758	0.1637	-0.1017	-0.0382	0.008	3.652	0.6095	7496	0.609	0.0221
7	3	0.15	2.197	0.2145	0.432	0.424	0.1496	Test 12	0.01478	0.2392	0.3415	3.31	269.508	0.7075	7496	0.707	0.1896	-0.026	0.2137	0.335	264.88	0.691	7496	0.691	0.188	-0.1013	0.00657	0.048	3.351	0.7228	7496	0.723	0.0211
1	3	0.15	2.197	0.2145	0.359	0.310	0.1581	Test 13	0.05425	-0.0322	0.312	3.31	443.682	0.454	7496	0.454	0.2433	-0.022	-0.06321	0.281	390.02	0.444	7496	0.444	0.2281	-0.1023	-0.0498	0.025	3.199	0.7849	7496	0.785	0.0207
1	5	0.15	2.197	0.2145	0.322	0.225	0.1586	Test 14	-0.01246	-0.2902	0.108	3.31	487.926	0.4242	7496	0.424	0.2551	0.0015	-0.2037	0.09226	737.58	0.203	7496	0.202	0.3137	-0.1024	-0.0467	-0.031	3.198	0.7873	7496	0.787	0.0207
7	5	0.15	2.197	0.2145	0.443	0.439	0.1499	Test 15	0.01601	0.3876	0.179	3.31	240.413	0.7398	7496	0.74	0.1791	-0.04	0.3616	0.1697	294.46	0.67	7496	0.67	0.1982	-0.1014	0.0212	0.044	3.339	0.7255	7496	0.725	0.0211
15	5	0.15	2.197	0.2145	0.439	0.456	0.1407	Test 16	-0.01841	-0.3847	-0.1699	3.31	249.67	0.7265	7496	0.726	0.1825	-0.036	-0.3868	-0.1647	207.93	0.761	7496	0.761	0.1665	-0.1017	-0.0203	-0.033	3.648	0.6098	7496	0.61	0.0221

X	Y	Hm0	TP	U0	R - Vx1	R - Vx2	R - WL	R0011	a0	a1	b1	w	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse
1	1	0.15261	1.898	0.484	0.492	0.300	0.1585	Test 1	0.1017	-0.2153	0.3257	3.31	322.96	0																			

Appendix B - Tables of Results

Location	Loading Parameters			Resultant Max.			Test Coefficient for Vx1				Goodness of fit parameters					Coefficient for Vx2			Goodness of fit parameters					Coefficient for WL			Goodness of fit parameters						
17	3	0.15752	1.548	0.4828	0.448	0.481	0.1331	Test 10	0.0004	0.4288	0.1289	4.05	121.499	0.8609	7496	0.861	0.1273	-0.043	0.4146	0.1428	86.358	0.893	7496	0.893	0.1073	-0.1037	0.02781	0.009	1.659	0.6609	7496	0.661	0.0149
15	3	0.15752	1.548	0.4828	0.462	0.500	0.1343	Test 11	0.00066	0.2352	-0.3973	4.05	124.134	0.8656	7496	0.866	0.1287	-0.037	0.2434	-0.3933	52.655	0.938	7496	0.938	0.0838	-0.1037	0.01552	-0.026	1.82	0.6588	7496	0.659	0.0156
7	3	0.15752	1.548	0.4828	0.470	0.476	0.142	Test 12	0.02281	0.2027	-0.3981	4.05	214.105	0.7775	7496	0.777	0.169	-0.035	0.2122	-0.3866	167.68	0.813	7496	0.813	0.1496	-0.1023	0.0319	-0.024	2.701	0.6865	7496	0.686	0.019
1	3	0.15752	1.548	0.4828	0.433	0.360	0.15	Test 13	0.0707	0.3424	-0.1177	4.05	311.275	0.6123	7496	0.612	0.2038	-0.054	0.3045	-0.0292	413.86	0.459	7496	0.459	0.235	-0.1028	0.04305	0.019	2.536	0.7672	7496	0.767	0.0184
1	5	0.15752	1.548	0.4828	0.400	0.372	0.1499	Test 14	-0.00397	0.366	-0.1503	4.05	311.243	0.6535	7496	0.653	0.2038	-0.035	0.3218	-0.0979	472.05	0.473	7496	0.473	0.2509	-0.1028	0.04529	0.013	2.541	0.7661	7496	0.766	0.0184
7	5	0.15752	1.548	0.4828	0.430	0.518	0.1421	Test 15	-0.01596	0.1373	0.3904	4.05	320.772	0.6669	7496	0.667	0.2069	-0.05	0.1266	0.451	77.143	0.914	7496	0.914	0.1014	-0.1024	-0.0054	0.039	2.691	0.687	7496	0.687	0.0189
15	5	0.15752	1.548	0.4828	0.459	0.528	0.1343	Test 16	0.00733	0.2347	-0.3857	4.05	237.503	0.7629	7496	0.763	0.178	-0.064	0.2697	-0.3773	52.801	0.939	7496	0.939	0.0839	-0.1037	0.01929	-0.024	1.839	0.657	7496	0.657	0.0157

X	Y	Hm0	TP	U0	R - Vx1	R - Vx2	R - WL	R0015	a0	a1	b1	w	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse
1	1	0.08653	1.769	0.3797	0.372	0.344	0.0364	Test 1	0.05655	0.07112	0.3074	3.51	181.168	0.6732	7496	0.673	0.1555	0.0526	0.08114	0.2799	184.83	0.633	7496	0.633	0.157	0.001542	-0.0183	0.03	0.778	0.8544	7496	0.854	0.0102
3	1	0.08653	1.769	0.3797	0.383	0.329	0.0345	Test 2	0.04899	0.1662	-0.2902	3.51	254.714	0.6222	7496	0.622	0.1843	0.0313	0.125	-0.2706	203.94	0.62	7496	0.62	0.1649	0.001312	0.03276	0.005	0.811	0.8362	7496	0.836	0.0104
5	1	0.08653	1.769	0.3797	0.403	0.298	0.0326	Test 3	0.04109	-0.3258	0.158	3.51	207.365	0.7032	7496	0.703	0.1663	0.0082	-0.2473	0.1507	230.3	0.577	7496	0.577	0.1753	0.001178	-0.0281	-0.014	0.882	0.8074	7496	0.807	0.0108
7	1	0.08653	1.769	0.3797	0.412	0.337	0.0309	Test 4	0.03443	-0.3745	0.04545	3.51	225.89	0.7025	7496	0.702	0.1736	-0.036	-0.2952	0.05859	227.62	0.599	7496	0.599	0.1743	0.001151	-0.0222	-0.02	0.961	0.7759	7496	0.776	0.0113
9	1	0.08653	1.769	0.3797	0.404	0.372	0.0294	Test 5	0.01843	-0.2373	-0.3042	3.51	165.875	0.771	7496	0.771	0.1488	-0.049	-0.2035	-0.2516	193.55	0.67	7496	0.67	0.1607	0.001264	0.00026	-0.028	1.081	0.7337	7496	0.734	0.012
11	1	0.08653	1.769	0.3797	0.403	0.389	0.0282	Test 6	0.01005	0.3785	-0.1047	3.51	157.154	0.7864	7496	0.786	0.1448	-0.06	0.3154	-0.0934	184.96	0.687	7496	0.687	0.1571	0.001418	0.02524	0.009	1.196	0.6927	7496	0.693	0.0126
13	1	0.08653	1.769	0.3797	0.388	0.401	0.0269	Test 7	0.00054	0.3706	0.1136	3.51	143.4	0.7971	7496	0.797	0.1383	-0.058	0.324	0.1127	146.33	0.751	7496	0.751	0.1397	0.001573	0.01551	0.02	1.314	0.6457	7496	0.646	0.0132
15	1	0.08653	1.769	0.3797	0.386	0.398	0.0255	Test 8	-0.00638	0.117	-0.3612	3.51	139.661	0.7947	7496	0.795	0.1365	-0.051	0.1184	-0.326	114.41	0.798	7496	0.798	0.1235	0.001795	0.01865	-0.015	1.431	0.596	7496	0.596	0.0138
17	1	0.08653	1.769	0.3797	0.377	0.381	0.0242	Test 9	-0.0162	0.3611	0.00596	3.51	124.369	0.7973	7496	0.797	0.1288	-0.045	0.3359	0.00859	77.106	0.846	7496	0.846	0.1014	0.002044	0.01992	0.01	1.562	0.5413	7496	0.541	0.0144
17	3	0.08653	1.769	0.3797	0.344	0.321	0.0243	Test 10	0.02051	0.2783	0.1642	3.51	570.91	0.4068	7496	0.407	0.276	-0.011	0.2805	0.1318	551.11	0.395	7496	0.395	0.2711	0.002097	0.00697	0.021	1.563	0.5414	7496	0.541	0.0144
17	2	0.08653	1.769	0.3797	0.372	0.393	0.0243	Test 11	-0.01865	0.3348	-0.1115	3.51	123.236	0.7912	7496	0.791	0.1282	-0.052	0.3264	-0.1005	59.873	0.88	7496	0.88	0.0894	0.002055	0.02192	0.003	1.551	0.5437	7496	0.544	0.0144
15	2	0.08653	1.769	0.3797	0.379	0.407	0.0254	Test 12	-0.01462	0.2718	0.242	3.51	144.85	0.7741	7496	0.774	0.139	-0.055	0.2552	0.2423	72.773	0.865	7496	0.864	0.0985	0.001738	0.00864	0.022	1.425	0.5959	7496	0.596	0.0138
7	2	0.08653	1.769	0.3797	0.391	0.340	0.031	Test 13	0.03413	-0.1668	-0.315	3.51	472.171	0.5022	7496	0.502	0.251	-0.032	-0.1501	-0.2689	404.2	0.468	7496	0.468	0.2322	0.001229	0.01262	-0.027	0.965	0.7753	7496	0.775	0.0113
1	2	0.08653	1.769	0.3797	0.351	0.292	0.0366	Test 14	0.04218	-0.0704	-0.3007	3.51	484.777	0.4245	7496	0.424	0.2543	0.0145	-0.05866	-0.2714	322.77	0.473	7496	0.472	0.2075	0.001557	0.0211	-0.028	0.773	0.8561	7496	0.856	0.0102
1	2	0.08653	1.769	0.3797	0.358	0.307	0.0366	Test 15	0.04672	0.06047	0.3058	3.51	267.266	0.5769	7496	0.577	0.1888	0.0282	0.06261	0.2715	217.16	0.573	7496	0.573	0.1702	0.001573	-0.0217	0.027	0.763	0.8577	7496	0.858	0.0101

X	Y	Hm0	TP	U0	R - Vx1	R - Vx2	R - WL	R0016	a0	a1	b1	w	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse
1	1	0.08796	1.217	0.3697	0.387	0.381	0.0287	Test 1	0.04965	-0.0563	0.3324	4.96	119.769	0.7806	7496	0.781	0.1264	0.0367	-0.02228	0.3431	69.53	0.864	7496	0.864	0.0963	0.001429	-0.0197	0.019	0.528	0.8409	7496	0.841	0.0084
3	1	0.08796	1.217	0.3697	0.389	0.370	0.0267	Test 2	0.04557	0.2235	-0.2614	4.97	183.702	0.7072	7496	0.707	0.1565	0.0033	0.2598	-0.2581	56.559	0.899	7496	0.899	0.0869	0.001435	0.02407	0.008	0.581	0.8046	7496	0.805	0.0088
5	1	0.08796	1.217	0.3697	0.387	0.410	0.0245	Test 3	0.02455	0.04746	-0.3595	4.97	92.3868	0.8422	7496	0.842	0.111	-0.033	0.06604	-0.3703	53.635	0.908	7496	0.908	0.0846	0.00128	0.01379	-0.019	0.636	0.7614	7496	0.761	0.0092
7	1	0.08796	1.217	0.3697	0.399	0.430	0.0227	Test 4	0.02621	-0.3058	0.2136	4.97	241.272	0.6838	7496	0.684	0.1794	-0.051	-0.3099	0.2171	55.552	0.906	7496	0.906	0.0861	0.001128	-0.0203	0.007	0.663	0.7255	7496	0.725	0.0094
9	1	0.08796	1.217	0.3697	0.409	0.430	0.022	Test 5	-0.01155	0.3098	0.249	4.97	203.487	0.7443	7496	0.744	0.1648	-0.053	0.2478	0.2846	46.669	0.92	7496	0.92	0.0789	0.001253	0.0108	0.018	0.697	0.6984	7496	0.698	0.0096
11	1	0.08796	1.217	0.3697	0.393	0.417	0.0221	Test 6	0.03045	0.3593	-0.0451	4.96	172.996	0.7397	7496	0.74	0.1519	-0.046	0.3715	0.00924	41.204	0.926	7496	0.926	0.0741	0.001224	0.02081	0.002	0.68	0.7067	7496	0.707	0.0095
13	1	0.08796	1.217	0.3697	0.369	0.400	0.0227	Test 7	0.0003	-0.3174	-0.1879	4.97	81.6362	0.862	7496	0.862	0.1044	-0.044	-0.283	-0.2164	28.919	0.943	7496	0.943	0.0621	0.001855	-0.0189	0.009	0.718	0.6945	7496	0.694	0.0098
15	1	0.08796	1.217	0.3697	0.358	0.378	0.0219	Test 8	0.00545	-0.3502	0.03805	4.97	65.7468	0.8762	7496	0.876	0.0937	-0.037	-0.341	0.01424	26.446	0.943	7496	0.943	0.0594	0.001801	-0.0193	0.006	0.561	0.7303	7496	0.73	0.0086
17	1	0.08796	1.217	0.3697	0.333	0.357	0.0216	Test 9	0.00565	0.3183	-0.07794	4.97	48.7542	0.892	7496	0.892	0.0806	-0.034	0.3173	-0.065	41.324	0.905	7496	0.905	0.0742	0.001859	0.01553	-0.012	0.407	0.7814	7496	0.781	0.0074

X	Y	Hm0	TP	U0	R - Vx1	R - Vx2	R - WL	R0017	a0	a1	b1	w	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse	a0	a1	b1	sse	rsq	dfe	adj	rmse
17	1	0.15303	2.120	0.6782	0.347	0.283	0.0199	Test 1	-0.1864	-0.0774	-0.1411	5.72	546.33	0.1509	7496	0.151	0.27	-0.169	-0.05649	-0.0993	562.76	0.08	7496	0.08	0.274	0.002848	-0.0169	0.002	7.511				

Geometric Re-Adjustment Factor for x to transpose
lab book result to distance from toe

Location		Loading Parameters			Resultant Max.			Test Coefficient for Vx1				Goodness of fit parameters					Coefficient for Vx2					Goodness of fit parameters					Coefficient for WL			Goodness of fit parameters							
X	Y	Hm0	TP	U0	R - Vx1	R - Vx2	R - WL	R030	a0	a1	b1	w	sse	rsq	dfe	adj	rms	a0	a1	b1	sse	rsq	dfe	adj	rms	a0	a1	b1	sse	rsq	dfe	adj	rms				
-0.5	1	0.09916	1.796	0.249711	0.275	0.238	0.071	Test 20	0.03775	-0.1496	0.1847	3.51	60.75	0.777	7496	0.7772	0.09	0.04542	-0.1247	0.1461	29.34	0.825	7496	0.825	0.0626	0.0311	-0.04	0.003	0.198	0.968	7496	0.968	0.005				
3.5	1	0.09916	1.796	0.249711	0.291	0.275	0.070	Test 1	0.02801	-0.0919	0.2459	3.51	25.82	0.909	7496	0.9091	0.0587	0.02984	-0.1056	0.2211	12.35	0.948	7496	0.948	0.0406	0.033	-0.034	0.0141	0.1913	0.964	7496	0.964	0.005				
5.5	1	0.09916	1.796	0.249711	0.305	0.294	0.069	Test 2	0.02466	0.2465	-0.1343	3.51	31.94	0.902	7496	0.9024	0.0653	0.03473	0.2337	-0.1118	13.09	0.951	7496	0.951	0.0418	0.034	0.0338	0.0104	0.1898	0.961	7496	0.961	0.005				
7.5	1	0.09916	1.796	0.249711	0.328	0.321	0.068	Test 3	0.02752	-0.2831	0.1004	3.51	29.3	0.92	7496	0.9202	0.0625	0.04082	-0.2612	0.102	10.47	0.966	7496	0.966	0.0374	0.0341	-0.032	-0.01	0.1858	0.958	7496	0.958	0.005				
9.5	1	0.09916	1.796	0.249711	0.331	0.340	0.066	Test 4	0.0219	0.3029	-0.0618	3.51	19.62	0.948	7496	0.9481	0.0512	0.04195	0.2871	-0.0811	9.319	0.973	7496	0.973	0.0353	0.0342	0.0293	0.0127	0.19	0.953	7496	0.953	0.005				
11.5	1	0.09916	1.796	0.249711	0.336	0.349	0.065	Test 5	0.01993	0.09909	-0.3002	3.51	16.57	0.958	7496	0.9576	0.047	0.03735	0.08407	-0.3002	10.61	0.972	7496	0.972	0.0376	0.0343	0.0239	-0.019	0.1869	0.949	7496	0.949	0.005				
13.5	1	0.09916	1.796	0.249711	0.338	0.345	0.063	Test 6	0.01764	0.1247	0.2952	3.51	13.22	0.967	7496	0.9668	0.042	0.02804	0.1436	0.2824	12.15	0.969	7496	0.969	0.0403	0.0343	0.0031	0.0288	0.1746	0.948	7496	0.948	0.00				
15.5	1	0.09916	1.796	0.249711	0.328	0.327	0.062	Test 7	0.0144	0.247	-0.194	3.51	11.99	0.969	7496	0.9686	0.04	0.0169	0.2389	-0.1978	13.21	0.965	7496	0.965	0.042	0.0344	0.0267	-0.007	0.1585	0.947	7496	0.947	0.00				
17.5	1	0.09916	1.796	0.249711	0.319	0.307	0.061	Test 8	0.00914	-0.0562	-0.3045	3.51	9.516	0.974	7496	0.9742	0.0356	0.008925	-0.05977	-0.2924	10.96	0.968	7496	0.968	0.0382	0.0345	0.0064	-0.025	0.1357	0.95	7496	0.949	0.00				
19.5	1	0.09916	1.796	0.249711	0.304	0.266	0.059	Test 9	0.00491	0.283	0.0965	3.51	10.88	0.969	7496	0.9686	0.0381	-0.01566	0.239	0.0732	119.8	0.662	7496	0.662	0.1264	0.0346	0.0204	0.0141	0.115	0.953	7496	0.953	0.00				
19.5	3	0.09916	1.796	0.249711	0.304	0.305	0.059	Test 10	0.00504	-0.2031	-0.2194	3.51	9.526	0.972	7496	0.9724	0.0356	0.01766	-0.1998	-0.2065	12.59	0.961	7496	0.961	0.041	0.0347	0.0088	-0.023	0.113	0.953	7496	0.953	0.00				
17.5	3	0.09916	1.796	0.249711	0.316	0.312	0.061	Test 11	0.00846	0.2956	0.08484	3.51	9.045	0.975	7496	0.9751	0.0347	0.01752	0.2849	0.0733	11.46	0.966	7496	0.966	0.0391	0.0347	0.0198	0.0171	0.1366	0.95	7496	0.95	0.00				
11.5	3	0.09916	1.796	0.249711	0.317	0.324	0.065	Test 12	0.01248	0.236	0.1924	3.51	8.757	0.975	7496	0.9754	0.0342	0.02929	0.2359	0.1764	6.8	0.98	7496	0.98	0.0301	0.0347	0.0082	0.0295	0.1887	0.949	7496	0.949	0.005				
9.5	3	0.09916	1.796	0.249711	0.313	0.315	0.067	Test 13	0.01625	0.0569	0.2912	3.51	10.15	0.97	7496	0.9702	0.0368	0.03126	0.06867	0.2749	11.53	0.963	7496	0.963	0.0392	0.0347	-0.014	0.029	0.1935	0.952	7496	0.952	0.005				
5.5	3	0.09916	1.796	0.249711	0.300	0.276	0.067	Test 22	0.01904	0.2525	0.1234	3.51	9.236	0.97	7496	0.9698	0.0351	0.02122	0.2285	0.1138	6.29	0.975	7496	0.975	0.029	0.0317	0.0132	0.0325	0.1915	0.96	7496	0.96	0.005				
3.5	3	0.09916	1.796	0.249711	0.277	0.260	0.072	Test 14	0.00864	-0.1941	0.1851	3.51	14.17	0.95	7496	0.95	0.0435	0.0153	-0.1812	0.164	18.08	0.925	7496	0.925	0.0491	0.0347	-0.037	0.0018	0.2217	0.959	7496	0.959	0.005				
-0.5	3	0.09916	1.796	0.249711	0.261	0.231	0.071	Test 21	0.02077	0.1574	0.1821	3.51	29.36	0.881	7496	0.881	0.0626	0.00666	0.1396	0.176	17.43	0.916	7496	0.916	0.0482	0.0311	0.0047	0.0396	0.2118	0.966	7496	0.966	0.005				
-0.5	5	0.09916	1.796	0.249711	0.249	0.210	0.071	Test 24	0.00089	0.00589	-0.2483	3.51	21.87	0.914	7496	0.9136	0.054	-0.04196	0.005225	-0.1677	192.6	0.354	7496	0.354	0.1603	0.0312	0.0274	-0.029	0.2106	0.966	7496	0.966	0.005				
3.5	5	0.09916	1.796	0.249711	0.276	0.261	0.072	Test 15	0.00738	0.08478	-0.2544	3.51	10.79	0.962	7496	0.9615	0.0379	0.01332	0.07176	-0.2367	34.01	0.871	7496	0.871	0.0674	0.0348	0.0332	-0.017	0.2225	0.959	7496	0.959	0.005				
5.5	5	0.09916	1.796	0.249711	0.285	0.281	0.067	Test 23	0.00526	0.00736	0.2797	3.51	6.658	0.978	7496	0.9778	0.0298	0.02163	0.01596	0.2589	4.643	0.982	7496	0.982	0.0249	0.0317	-0.023	0.0267	0.1905	0.96	7496	0.96	0.005				
9.5	5	0.09916	1.796	0.249711	0.337	0.314	0.067	Test 16	-0.08213	0.2538	0.0175	3.51	384.3	0.387	7496	0.3867	0.2264	0.02988	0.2771	0.0606	9.822	0.969	7496	0.969	0.0362	0.0349	0.0221	0.0234	0.1948	0.952	7496	0.952	0.005				
11.5	5	0.09916	1.796	0.249711	0.324	0.314	0.066	Test 17	0.02252	-0.0597	0.2952	3.51	220.2	0.607	7496	0.6068	0.1714	0.01026	-0.05586	0.2981	72.67	0.826	7496	0.826	0.0985	0.0351	-0.023	0.0208	0.1904	0.949	7496	0.949	0.005				
17.5	5	0.09916	1.796	0.249711	0.307	0.321	0.061	Test 18	0.00373	-0.2795	-0.1168	3.51	15.55	0.957	7496	0.9567	0.0455	0.02427	-0.278	-0.1044	12.37	0.964	7496	0.964	0.0406	0.0351	-0.02	-0.017	0.1355	0.95	7496	0.95	0.00				
19.5	5	0.09916	1.796	0.249711	0.300	0.315	0.060	Test 19	0.00174	-0.2754	0.1134	3.51	31.51	0.914	7496	0.9135	0.0648	0.02355	-0.2681	0.1144	17.66	0.948	7496	0.948	0.0485	0.0352	-0.025	0.0002	0.1143	0.953	7496	0.953	0.00				
																																			0.05022	0.0394	0.0681
X	Y	Hm0	TP	U0	R - Vx1	R - Vx2	R - WL	R031	a0	a1	b1	w	sse	rsq	dfe	adj	rms	a0	a1	b1	sse	rsq	dfe	adj	rms	a0	a1	b1	sse	rsq	dfe	adj	rms				
-0.5	1	0.10228	1.217	0.213728	0.211	0.182	0.057	Test 20	0.02733	-0.1602	0.09001	4.97	19.58	0.866	7496	0.866	0.0511	0.02592	-0.1215	0.0978	17.82	0.837	7496	0.836	0.0488	0.0306	-0.025	0.0067	0.0922	0.965	7496	0.965	0.00				
3.5	1	0.10228	1.217	0.213728	0.207	0.188	0.058	Test 1	0.02137	-0.1591	0.09506	4.96	14.24	0.9	7496	0.9004	0.0436	0.01478	-0.1395	0.1033	16.4	0.873	7496	0.873	0.0468	0.0304	-0.02	0.0122	0.0362	0.983	7496	0.983	0.00				
5.5	1	0.10228	1.217	0.213728	0.226	0.203	0.059	Test 2	0.02541	0.0855	-0.1815	4.96	6.037	0.962	7496	0.9615	0.0284	0.01646	0.06799	-0.1739	5.22	0.962	7496	0.962	0.0264	0.0353	0.0106	-0.021	0.0314	0.985	7496	0.985	0.00				
7.5	1	0.10228	1.217	0.213728	0.221	0.212	0.060	Test 3	0.01898	0.1819	-0.087	4.97	6.657	0.958	7496	0.9582	0.0298	0.01683	0.1645	-0.1041	5.726	0.961	7496	0.961	0.0276	0.0358	0.0183	-0.015	0.0451	0.979	7496	0.979	0.00				
9.5	1	0.10228	1.217	0.213728	0.218	0.219	0.061	Test 4	0.01686	-0.1414	0.1424	4.97	6.218	0.961	7496	0.9605	0.0288	0.01845	-0.137	0.1469	6.429	0.959	7496	0.959	0.0293	0.036	0.0084	0.0231	0.064	0.973	7496	0.973	0.00				
11.5	1	0.10228	1.217	0.213728	0.213	0.226	0.062	Test 5	0.01396	0.1987	0.00967	4.97	4.522	0.97	7496	0.9704	0.0246	0.01992	0.2054	-0.0175	9.989	0.941	7496	0.941	0.0365	0.0363	0.0224	-0.013	0.0864	0.966	7496	0.966	0.00				
13.5	1	0.10228	1.217	0.213728	0.212	0.226	0.064	Test 6	0.01303	0.04143	0.1943	4.97	3.144	0.979	7496	0.9792	0.0205	0.01769	0.04143	0.2042	3.028	0.982	7496	0.982	0.0201	0.0367	0.0192	0.0188	0.1128	0.96	7496	0.96	0.00				
15.5	1	0.10228	1.217	0.213728	0.203	0.218	0.065	Test 7	0.01294	0.1593	-0.1044	4.97	4.079	0.971	7496	0.9709	0.0233	0.01541	0.1646	-0.1179	5.858	0.963	7496	0.963	0.028	0.037	0.0117	-0.026	0.1304	0.958	7496	0.958	0.00				
17.5	1	0.10228	1.217	0.213728	0.197	0.206	0.067	Test 8	0.01287	0.1839																											

Appendix B - Tables of Results

Location	Loading Parameters			Resultant Max.			Test Coefficient for Vx1				Goodness of fit parameters					Coefficient for Vx2					Goodness of fit parameters					Coefficient for WL			Goodness of fit parameters				
25.5	1	0.15102	2.120	0.392947	0.291	0.307	0.075	Test 10	-0.053	-0.0828	-0.2232	2.86	556.1	0.277	7496	0.2763	0.2724	-0.03566	-0.1131	-0.2466	410.3	0.402	7496	0.402	0.2339	0.0304	0.013	-0.042	2.5838	0.74	7496	0.74	0.019
25.5	3	0.15102	2.120	0.392947	0.252	0.339	0.075	Test 11	-0.04735	-0.0232	0.2029	2.86	607.3	0.205	7496	0.2045	0.2846	-0.05328	-0.01951	0.2848	355.1	0.463	7496	0.462	0.2176	0.0304	-0.029	0.0333	2.5847	0.739	7496	0.739	0.019
19.5	3	0.15102	2.120	0.392947	0.398	0.323	0.081	Test 12	-0.07738	-0.3036	0.1025	2.86	398.7	0.491	7496	0.4911	0.2306	-0.1062	-0.2046	0.0706	414.5	0.298	7496	0.297	0.2352	0.0302	-0.047	-0.019	2.4964	0.795	7496	0.794	0.018
17.5	3	0.15102	2.120	0.392947	0.421	0.330	0.083	Test 13	-0.07935	0.1606	0.3014	2.86	342.6	0.561	7496	0.5605	0.2138	-0.101	0.1072	0.2019	399.8	0.329	7496	0.329	0.231	0.0303	-0.013	0.0509	2.4461	0.81	7496	0.809	0.018
11.5	3	0.15102	2.120	0.392947	0.481	0.396	0.089	Test 14	-0.00998	0.1308	0.452	2.86	101.3	0.891	7496	0.8912	0.1163	0.005402	0.1146	0.3733	239.2	0.705	7496	0.705	0.1786	0.03	-0.028	0.0515	2.2039	0.854	7496	0.854	0.017
9.5	3	0.15102	2.120	0.392947	0.460	0.446	0.091	Test 15	-0.00176	0.438	-0.1341	2.86	133.6	0.855	7496	0.8548	0.1335	0.02842	0.3913	-0.1448	175.3	0.788	7496	0.788	0.1529	0.0299	0.0533	0.03	2.1446	0.867	7496	0.867	0.017
7.5	3	0.15102	2.120	0.392947	0.452	0.430	0.093	Test 16	0.0078	0.4353	-0.0908	2.86	146.1	0.835	7496	0.8353	0.1396	0.03187	0.3853	-0.1005	187.6	0.76	7496	0.76	0.1582	0.0298	0.0526	0.036	2.1185	0.878	7496	0.878	0.017
5.5	3	0.15102	2.120	0.392947	0.419	0.395	0.096	Test 17	0.01644	-0.1652	0.3671	2.86	244.9	0.713	7496	0.7126	0.1808	0.02936	-0.1462	0.3354	231.7	0.684	7496	0.684	0.1758	0.0295	-0.064	0.0165	2.1149	0.886	7496	0.886	0.017
3.5	3	0.15102	2.120	0.392947	0.388	0.323	0.098	Test 18	0.04148	-0.1145	0.3269	2.86	370.6	0.548	7496	0.5481	0.2224	0.01577	-0.1304	0.2786	317.8	0.528	7496	0.527	0.2059	0.0292	-0.068	0.0138	2.0985	0.895	7496	0.895	0.017
1.5	3	0.15102	2.120	0.392947	0.348	0.231	0.100	Test 19	0.05183	0.2435	-0.1693	2.86	431.8	0.433	7496	0.4329	0.24	0.009317	0.197	-0.1018	454	0.289	7496	0.289	0.2461	0.0288	0.0613	0.0355	2.05	0.902	7496	0.902	0.017
-0.5	3	0.15102	2.120	0.392947	0.241	0.094	0.101	Test 20	0.03648	-0.1974	-0.0543	2.86	570.6	0.216	7496	0.2157	0.2759	-0.04275	-0.01359	-0.0497	772.8	0.013	7496	0.012	0.3211	0.0286	-0.012	-0.071	1.9304	0.911	7496	0.911	0.016
-0.5	5	0.15102	2.120	0.392947	0.172	0.230	0.101	Test 22	0.06125	0.1102	-0.0146	2.86	878.5	0.05	7496	0.0497	0.3423	-0.1361	-0.09221	0.0151	872.9	0.036	7496	0.036	0.3412	0.0285	0.042	0.0591	1.9134	0.912	7496	0.911	0.016
1.5	5	0.15102	2.120	0.392947	0.329	0.203	0.100	Test 23	0.08146	-0.1798	0.1703	2.86	682.5	0.252	7496	0.2517	0.3018	0.007903	-0.1729	0.0895	624.3	0.186	7496	0.185	0.2886	0.0287	-0.065	-0.028	2.0256	0.904	7496	0.904	0.016
3.5	5	0.15102	2.120	0.392947	0.378	0.297	0.098	Test 24	0.04779	0.05607	-0.3256	2.86	513.6	0.444	7496	0.4433	0.2617	0.000386	0.0913	-0.2822	427.2	0.436	7496	0.436	0.2387	0.029	0.0654	-0.022	2.0877	0.895	7496	0.895	0.017
5.5	5	0.15102	2.120	0.392947	0.387	0.359	0.095	Test 25	0.02088	0.03311	0.3649	2.86	419.2	0.546	7496	0.5455	0.2365	0.01893	0.005924	0.3403	362	0.545	7496	0.545	0.2197	0.029	-0.049	0.0449	2.0731	0.888	7496	0.888	0.017
7.5	5	0.15102	2.120	0.392947	0.434	0.337	0.093	Test 26	-0.01318	0.1504	0.3932	2.86	243.2	0.732	7496	0.732	0.1801	0.07347	0.09438	0.246	744.1	0.259	7496	0.259	0.3151	0.0297	-0.027	0.0577	2.0814	0.879	7496	0.879	0.017
9.5	5	0.15102	2.120	0.392947	0.460	0.404	0.091	Test 27	-0.02374	0.4055	-0.1616	2.86	234.8	0.753	7496	0.7526	0.177	0.006103	0.3698	-0.1477	204.2	0.744	7496	0.744	0.165	0.0298	0.0549	0.0274	2.1179	0.87	7496	0.87	0.017
11.5	5	0.15102	2.120	0.392947	0.483	0.357	0.089	Test 28	-0.02954	0.4011	-0.2124	2.86	179.9	0.811	7496	0.811	0.1549	-0.04785	0.2562	-0.1738	351.3	0.506	7496	0.506	0.2165	0.0299	0.0564	0.0175	2.1757	0.857	7496	0.857	0.017
17.5	5	0.15102	2.120	0.392947	0.442	0.347	0.083	Test 29	-0.03598	-0.4056	-0.0149	2.86	273	0.694	7496	0.6934	0.1908	-0.08059	-0.2654	-0.024	381.5	0.411	7496	0.411	0.2256	0.0302	-0.04	-0.035	2.3741	0.814	7496	0.814	0.018
19.5	5	0.15102	2.120	0.392947	0.424	0.358	0.081	Test 30	-0.04493	0.3711	-0.0789	2.86	336.8	0.616	7496	0.6155	0.212	-0.06993	0.2846	-0.0457	372	0.456	7496	0.456	0.2228	0.0302	0.0436	0.0259	2.4226	0.8	7496	0.799	0.018
25.5	5	0.15102	2.120	0.392947	0.425	0.355	0.074	Test 31	-0.0359	0.05097	0.3858	2.86	233.1	0.709	7496	0.7088	0.1763	-0.05777	0.01349	0.297	330	0.501	7496	0.501	0.2098	0.0303	-0.022	0.0382	2.5456	0.742	7496	0.742	0.018
25.5	7	0.15102	2.120	0.392947	0.433	0.373	0.074	Test 32	-0.02969	-0.3633	0.175	2.86	229.4	0.727	7496	0.7266	0.1749	-0.05375	-0.3015	0.1057	301.2	0.56	7496	0.56	0.2005	0.0303	-0.043	0.0086	2.5502	0.741	7496	0.741	0.018
17.5	7	0.15102	2.120	0.392947	0.443	0.352	0.083	Test 33	-0.0365	-0.1729	0.3674	2.86	319.9	0.659	7496	0.6589	0.2066	0.06904	-0.1313	0.2506	680.4	0.306	7496	0.306	0.3013	0.0302	-0.049	0.0192	2.3771	0.814	7496	0.814	0.018
11.5	7	0.15102	2.120	0.392947	0.452	0.408	0.089	Test 34	-0.03248	0.3508	0.2296	2.86	285.5	0.698	7496	0.6976	0.1952	-0.02962	0.3211	0.2	208.8	0.72	7496	0.72	0.1669	0.0299	0.0144	0.0573	2.152	0.859	7496	0.859	0.017
9.5	7	0.15102	2.120	0.392947	0.433	0.346	0.091	Test 35	-0.02956	0.00616	0.4037	2.86	351.8	0.635	7496	0.6346	0.2166	0.0222	0.009168	0.3241	453.3	0.465	7496	0.465	0.2459	0.0299	-0.044	0.0426	2.1151	0.868	7496	0.868	0.017
5.5	7	0.15102	2.120	0.392947	0.346	0.358	0.096	Test 36	0.01173	-0.2916	0.1632	2.86	592.2	0.414	7496	0.4139	0.2811	0.006338	-0.3127	0.1599	400	0.536	7496	0.536	0.231	0.0296	-0.059	-0.031	2.0522	0.89	7496	0.89	0.017
3.5	7	0.15102	2.120	0.392947	0.311	0.294	0.097	Test 37	0.0347	0.2187	0.1686	2.86	711.9	0.287	7496	0.2862	0.3082	-0.00575	0.2088	0.1983	530.2	0.37	7496	0.37	0.2659	0.0288	-0.012	0.0674	2.0604	0.895	7496	0.895	0.017
1.5	7	0.15102	2.120	0.392947	0.287	0.193	0.099	Test 38	0.06974	0.1812	-0.119	2.86	839.2	0.174	7496	0.1732	0.3346	-0.00867	0.1743	-0.0603	760.7	0.144	7496	0.143	0.3186	0.0284	0.0558	0.0435	1.9682	0.905	7496	0.905	0.016
-0.5	7	0.15102	2.120	0.392947	0.177	0.213	0.100	Test 39	0.07135	0.05059	-0.0932	2.86	1016	0.04	7496	0.0395	0.3681	-0.03637	-0.1427	0.1049	1201	0.089	7496	0.089	0.4003	0.0282	0.0682	0.0239	1.8649	0.913	7496	0.913	0.016
-0.5	9	0.15102	2.120	0.392947	0.109	0.065	0.101	Test 40	0.04503	-0.0427	0.04701	2.86	1133	0.013	7496	0.0128	0.3889	-0.03625	-0.00551	-0.0283	1173	0.003	7496	0.002	0.3956	0.0282	-0.072	0.0071	1.8967	0.912	7496	0.912	0.016
5.5	9	0.15102	2.120	0.392947	0.284	0.213	0.095	Test 41	0.0003	-0.1121	0.2603	2.86	685.6	0.305	7496	0.305	0.3024	0.08541	-0.04847	0.1182	939.2	0.061	7496	0.061	0.354	0.0293	-0.063	0.0205	2.0372	0.889	7496	0.889	0.017
9.5	9	0.15102	2.120	0.392947	0.349	0.412	0.090	Test 42	-0.0186	-0.2543	0.2107	2.86	571.5																				

Appendix B - Tables of Results

Location	Loading Parameters				Resultant Max.			Test Coefficient for Vx1				Goodness of fit parameters					Coefficient for Vx2					Goodness of fit parameters					Coefficient for WL			Goodness of fit parameters				
13.5	1	0.15645	1.549	0.376137	0.470	0.459	0.063	Test 8	0.0131	-0.2924	-0.3506	4.05	46.07	0.944	7496	0.9443	0.0784	0.0284	-0.2877	-0.3205	64.49	0.915	7496	0.915	0.0928	0.0281	-0.02	-0.029	0.4012	0.92	7496	0.92	0.007	
17.5	1	0.15645	1.549	0.376137	0.436	0.421	0.062	Test 9	0.00052	-0.1074	0.422	4.05	25.76	0.965	7496	0.965	0.0586	0.006762	-0.09457	0.4035	26.74	0.96	7496	0.96	0.0597	0.0284	0.0066	0.0327	0.3433	0.924	7496	0.924	0.007	
25.5	1	0.15645	1.549	0.376137	0.369	0.357	0.065	Test 10	0.00337	0.0182	0.365	4.05	21.52	0.959	7496	0.9588	0.0536	0.0127	0.04419	0.3417	13.18	0.971	7496	0.971	0.0419	0.0298	0.0179	0.0309	0.4816	0.908	7496	0.908	0.008	
25.5	3	0.15645	1.549	0.376137	0.382	0.384	0.066	Test 11	0.00266	-0.365	-0.1016	4.05	20.56	0.963	7496	0.9632	0.0524	0.02058	-0.3535	-0.0835	45.19	0.916	7496	0.916	0.0776	0.0297	-0.036	0.0032	0.4572	0.914	7496	0.914	0.008	
17.5	3	0.15645	1.549	0.376137	0.441	0.423	0.062	Test 12	0.00548	0.4097	-0.1479	4.05	22.08	0.97	7496	0.9699	0.0543	0.01234	0.3786	-0.1593	15.63	0.976	7496	0.976	0.0457	0.0283	0.0301	-0.015	0.3232	0.928	7496	0.928	0.007	
13.5	3	0.15645	1.549	0.376137	0.462	0.445	0.063	Test 13	0.0149	-0.054	0.4434	4.05	23.52	0.97	7496	0.9695	0.056	0.02425	-0.02908	0.4199	14.8	0.978	7496	0.978	0.0444	0.028	-0.011	0.0335	0.3714	0.926	7496	0.926	0.007	
11.5	3	0.15645	1.549	0.376137	0.458	0.446	0.065	Test 14	0.01768	-0.4403	0.01501	4.05	24.34	0.968	7496	0.9676	0.057	0.02992	-0.4126	0.0543	17.39	0.974	7496	0.974	0.0482	0.0281	-0.036	0.0075	0.4401	0.921	7496	0.921	0.008	
9.5	3	0.15645	1.549	0.376137	0.454	0.437	0.067	Test 15	0.01753	0.4359	0.01722	4.05	23.93	0.968	7496	0.9676	0.0565	0.03165	0.4046	-0.0143	22.01	0.965	7496	0.965	0.0542	0.0283	0.0366	0.0139	0.537	0.915	7496	0.915	0.009	
5.5	3	0.15645	1.549	0.376137	0.433	0.390	0.073	Test 16	0.01853	-0.3262	0.2553	4.05	42.39	0.938	7496	0.9382	0.0752	0.02064	-0.2831	0.2377	32.61	0.94	7496	0.94	0.066	0.0288	-0.042	0.0118	0.7908	0.901	7496	0.901	0.01	
3.5	3	0.15645	1.549	0.376137	0.415	0.359	0.075	Test 17	0.01653	-0.395	-0.054	4.05	67.97	0.898	7496	0.8976	0.0952	0.01078	-0.345	-0.0482	49.32	0.902	7496	0.902	0.0811	0.0288	-0.039	-0.025	0.8667	0.903	7496	0.903	0.011	
-0.5	3	0.15645	1.549	0.376137	0.275	0.151	0.079	Test 18	0.02354	-0.1437	-0.2063	4.05	467.9	0.336	7496	0.3359	0.2498	-0.03477	-0.0537	-0.1032	603.7	0.078	7496	0.077	0.2838	0.0281	0.0096	-0.05	0.9323	0.912	7496	0.912	0.011	
-0.5	5	0.15645	1.549	0.376137	0.275	0.132	0.079	Test 19	0.00226	0.426	-0.1069	4.05	545.6	0.305	7496	0.3048	0.2698	0.003291	0.09101	-0.0917	698	0.082	7496	0.082	0.3052	0.0282	0.0495	0.0112	0.9292	0.912	7496	0.912	0.011	
5.5	5	0.15645	1.549	0.376137	0.428	0.353	0.073	Test 20	0.00105	0.426	-0.0202	4.05	36.16	0.95	7496	0.9496	0.0695	-0.00476	0.3459	-0.0358	146.9	0.755	7496	0.755	0.14	0.0287	0.0405	0.0168	0.78	0.902	7496	0.902	0.01	
9.5	5	0.15645	1.549	0.376137	0.448	0.421	0.067	Test 21	-0.02061	-0.0339	0.4263	4.05	203	0.772	7496	0.7715	0.1645	0.02007	-0.02754	0.3998	52.63	0.92	7496	0.92	0.0838	0.0282	-0.018	0.0345	0.5259	0.915	7496	0.915	0.008	
11.5	5	0.15645	1.549	0.376137	0.441	0.411	0.065	Test 22	0.00083	0.4392	0.03097	4.05	166.4	0.814	7496	0.8136	0.149	0.004341	0.4066	0.0074	201.6	0.755	7496	0.755	0.164	0.0279	0.0351	0.0108	0.4181	0.924	7496	0.924	0.008	

X	Y	Hm0	TP	U0	R - Vx1	R - Vx2	R - WL	R035	a0	a1	b1	w	sse	rsq	dfe	adj	rms	a0	a1	b1	sse	rsq	dfe	adj	rms	a0	a1	b1	sse	rsq	dfe	adj	rms
-0.5	1	0.17654	2.506	0.468934	0.289	0.301	0.112	Test 1	0.0166	0.1207	-0.2437	2.48	187.2	0.597	7496	0.5969	0.158	0.05087	0.1685	-0.1843	161.6	0.591	7496	0.591	0.1468	0.026	0.0765	0.0398	2.695	0.912	7496	0.912	0.019
1.5	1	0.17654	2.506	0.468934	0.271	0.349	0.112	Test 2	0.00384	0.1058	0.2452	2.48	331.8	0.446	7496	0.4461	0.2104	0.09354	0.003173	0.2552	422.8	0.366	7496	0.366	0.2375	0.0268	-0.08	0.0288	2.7833	0.907	7496	0.907	0.019
3.5	1	0.17654	2.506	0.468934	0.352	0.287	0.110	Test 3	-0.00572	0.08935	0.3345	2.48	233.2	0.658	7496	0.6582	0.1764	0.03868	-0.03866	0.2451	3744	0.058	7496	0.058	0.7067	0.0267	-0.081	0.0202	2.8576	0.9	7496	0.9	0.02
5.5	1	0.17654	2.506	0.468934	0.395	0.507	0.108	Test 4	0.00817	-0.3777	0.08494	2.48	291.6	0.658	7496	0.6583	0.1972	0.06789	-0.4383	0.0263	179	0.802	7496	0.801	0.1545	0.027	-0.033	-0.074	2.9544	0.893	7496	0.893	0.02
7.5	1	0.17654	2.506	0.468934	0.465	0.485	0.106	Test 5	0.00124	0.1391	0.4426	2.48	271.7	0.748	7496	0.7481	0.1904	0.02647	0.1272	0.4407	426.1	0.649	7496	0.649	0.2384	0.0272	-0.069	0.038	3.0116	0.885	7496	0.884	0.02
9.5	1	0.17654	2.506	0.468934	0.404	0.362	0.104	Test 6	-0.1402	-0.2482	0.08813	2.48	461.3	0.361	7496	0.3603	0.2481	-0.09121	-0.2634	0.0633	432.4	0.389	7496	0.389	0.2402	0.0275	-0.027	-0.071	3.0854	0.876	7496	0.876	0.02
11.5	1	0.17654	2.506	0.468934	0.408	0.368	0.102	Test 7	-0.1612	-0.2462	0.01987	2.48	422.2	0.351	7496	0.3511	0.2373	-0.1397	-0.2268	0.0271	432.3	0.312	7496	0.311	0.2401	0.0277	-0.012	-0.073	3.1877	0.866	7496	0.866	0.021
13.5	1	0.17654	2.506	0.468934	0.394	0.361	0.100	Test 8	-0.1793	-0.0187	0.2135	2.48	454.3	0.275	7496	0.2746	0.2462	-0.1711	0.000126	0.1894	446.5	0.232	7496	0.231	0.2441	0.0279	-0.071	0.0103	3.3641	0.852	7496	0.852	0.021
15.5	1	0.17654	2.506	0.468934	0.361	0.339	0.098	Test 9	-0.1878	0.1649	0.05432	2.48	517.2	0.179	7496	0.1791	0.2627	-0.18	0.1584	0.0167	475.5	0.167	7496	0.166	0.2519	0.0281	0.0099	0.0694	3.524	0.84	7496	0.84	0.022
17.5	1	0.17654	2.506	0.468934	0.308	0.290	0.096	Test 10	-0.1739	0.05912	-0.1207	2.48	616.9	0.099	7496	0.0987	0.2869	-0.1591	0.04403	-0.1234	591.5	0.098	7496	0.098	0.2809	0.0282	0.0657	-0.018	3.6901	0.826	7496	0.826	0.022
25.5	1	0.17654	2.506	0.468934	0.127	0.100	0.089	Test 11	-0.06314	-0.0123	-0.0627	2.48	818.5	0.018	7496	0.018	0.3305	-0.04638	0.03504	-0.0411	692.9	0.016	7496	0.015	0.304	0.0286	-0.014	-0.058	4.1612	0.765	7496	0.765	0.024
25.5	3	0.17654	2.506	0.468934	0.486	0.452	0.088	Test 12	-0.03127	0.2967	0.3441	2.48	91.15	0.895	7496	0.8946	0.1103	0.007677	0.3176	0.3104	76.24	0.907	7496	0.907	0.1009	0.0286	0.0054	0.0596	4.1485	0.764	7496	0.764	0.024
17.5	3	0.17654	2.506	0.468934	0.516	0.484	0.096	Test 13	-0.01778	-0.3854	0.3154	2.48	133.5	0.875	7496	0.8744	0.1334	0.01113	-0.3608	0.3051	191.4	0.814	7496	0.814	0.1598	0.0282	-0.067	-0.013	3.6876	0.826	7496	0.825	0.022
13.5	3	0.17654	2.506	0.468934	0.526	0.509	0.100	Test 14	0.01416	0.5085	0.05869	2.48	260.1	0.791	7496	0.7905	0.1863	0.02095	0.4882	0.0092	227.7	0.797	7496	0.797	0.1743	0.0277	0.0375	0.0617	3.3343	0.854	7496	0.854	0.021
11.5	3	0.17654	2.506	0.468934	0.537	0.527	0.102	Test 15	0.02241	-0.4774	0.1917	2.48	174.5	0.851	7496	0.8504	0.1526	0.04051	-0.4531	0.1769	155.9	0.851	7496	0.851	0.1442	0.0275	-0.061	-0.042	3.2008	0.866	7496	0.866	0.021
9.5	3	0.17654	2.506	0.468934	0.561	0.536	0.104	Test 16	0.04827	-0.2841	-0.4273	2.48	215.2	0.821	7496	0.821	0.1694	0.05485	-0.2594	-0.4052	154.7	0.849	7496	0.849	0.1437	0.0273	0.0351	-0.068	3.0623	0.877	7496	0.877	0.02
5.5	3	0.17654	2.506	0.468934	0.539	0.396	0.108	Test 17	0.06295	-0.0605	-0.4724	2.48	238.8	0.781	7496	0.7807	0.1785	0.06653	-0.03103	-0.3282	1982	0.171	7496	0.17	0.5142	0.0268	0.0676	-0.045	2.9174	0.894	7496	0.894	0.02
3.5	3	0.17654	2.506	0.468934	0.509	0.512	0.110	Test 18	0.07989	0.2476	0.351	2.48	903	0.434	7496	0.4336	0.3471	0.08502	0.2033	0.3758	140.1	0.83	7496	0.83	0.1367	0.0268	-0.047	0.0685	2.8495	0.901	7496	0.901	0.02
-0.5	3	0.17654	2.506	0.468934	0.412	0.396	0.113	Test 19	0.06446	0.08684	-0.337	2.48	188.5	0.707	7496	0.7065	0.1586	0.06821	0.09														

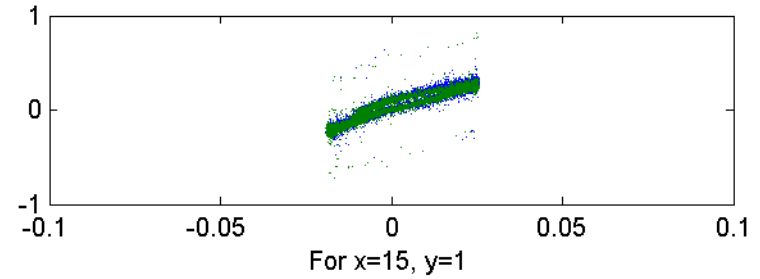
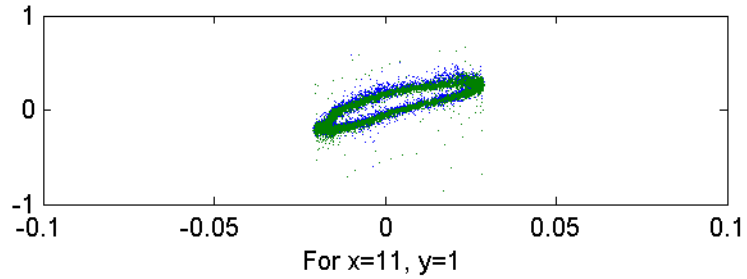
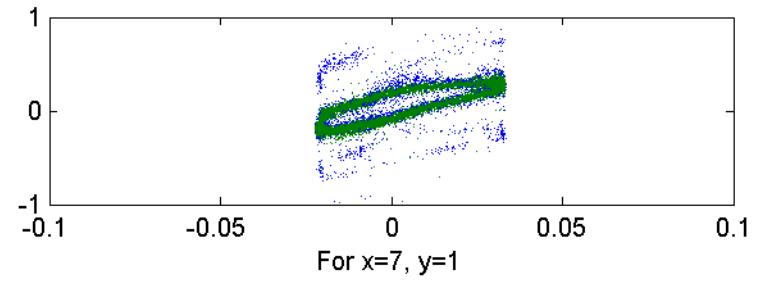
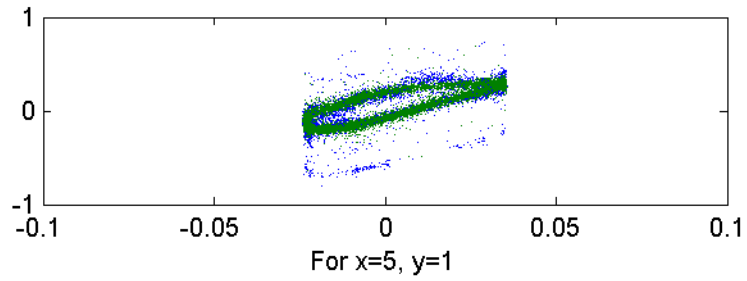
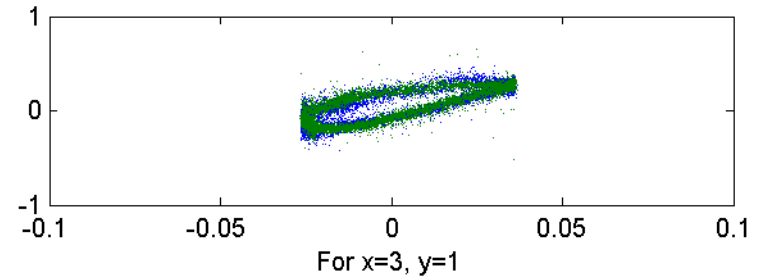
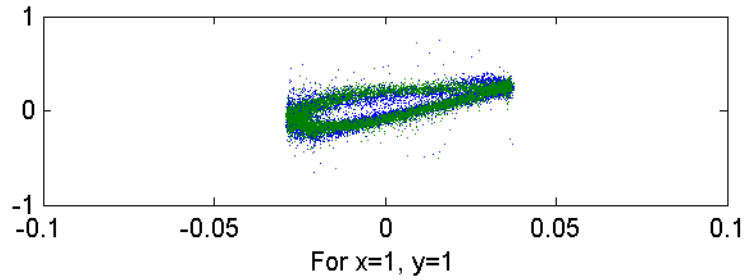
Appendix B - Tables of Results

Location		Loading Parameters			Resultant Max.			Test Coefficient for Vx1					Goodness of fit parameters					Coefficient for Vx2					Goodness of fit parameters					Coefficient for WL			Goodness of fit parameters										
X	Y	Hm0	Tp	U0	R - Vx1	R - Vx2	R - WL	R037	a0	a1	b1	w	sse	rsq	dfe	adj	rms	a0	a1	b1	sse	rsq	dfe	adj	rms	a0	a1	b1	sse	rsq	dfe	adj	rms	a0	a1	b1	sse	rsq	dfe	adj	rms
-0.5	1	0.09615	1.769	0.302018	0.346	0.379	0.117	Test 1	0.05075	0.2616	0.1371	3.51	100.6	0.765	7496	0.7646	0.1158	0.09237	0.2701	0.0956	52.28	0.855	7496	0.855	0.0835	-0.069	0.0088	0.047	0.5301	0.942	7496	0.942	0.008								
1.5	1	0.09615	1.769	0.302018	0.415	0.416	0.116	Test 2	0.05963	0.04071	-0.3531	3.51	79.48	0.856	7496	0.8562	0.103	0.0811	0.01753	-0.3343	48.61	0.896	7496	0.896	0.0805	-0.069	0.0405	-0.023	0.5416	0.937	7496	0.937	0.009								
3.5	1	0.09615	1.769	0.302018	0.451	0.396	0.113	Test 3	0.0578	-0.346	0.1876	3.51	83.94	0.874	7496	0.8737	0.1058	0.03477	-0.314	0.179	299.4	0.621	7496	0.621	0.1999	-0.069	-0.041	-0.015	0.5596	0.928	7496	0.928	0.009								
5.5	1	0.09615	1.769	0.302018	0.447	0.418	0.112	Test 4	0.04276	0.3717	0.1589	3.51	70.14	0.897	7496	0.8973	0.0967	-0.02057	0.3847	0.0992	1154	0.339	7496	0.339	0.3923	-0.069	0.0123	0.0405	0.5788	0.921	7496	0.921	0.009								
7.5	1	0.09615	1.769	0.302018	0.438	0.414	0.110	Test 5	0.0239	0.4142	-0.0154	3.51	281.5	0.696	7496	0.6959	0.1938	0.03438	0.3794	0.0017	110	0.831	7496	0.831	0.1212	-0.069	0.0301	0.0267	0.596	0.91	7496	0.91	0.009								
9.5	1	0.09615	1.769	0.302018	0.419	0.428	0.108	Test 6	0.00636	0.00141	0.4127	3.51	444.8	0.59	7496	0.5894	0.2436	-0.05088	0.04044	0.3754	572.7	0.483	7496	0.483	0.2764	-0.07	-0.027	0.0272	0.6108	0.9	7496	0.9	0.009								
11.5	1	0.09615	1.769	0.302018	0.408	0.430	0.106	Test 7	0.0002	0.3735	0.1633	3.51	69.82	0.899	7496	0.8992	0.0965	0.06154	0.3379	0.1463	741.1	0.407	7496	0.407	0.3144	-0.07	0.0194	0.0308	0.6474	0.885	7496	0.885	0.009								
13.5	1	0.09615	1.769	0.302018	0.395	0.374	0.104	Test 8	0.00041	0.3884	0.0685	3.51	391.9	0.598	7496	0.5978	0.2286	0.01123	0.355	0.0742	484	0.505	7496	0.504	0.2541	-0.07	0.0252	0.0237	0.6315	0.877	7496	0.877	0.009								
15.5	1	0.09615	1.769	0.302018	0.419	0.428	0.102	Test 9	-0.01715	0.2718	-0.2957	3.51	832.3	0.421	7496	0.4208	0.3332	-0.04471	0.2604	-0.281	1755	0.239	7496	0.239	0.4839	-0.07	0.0314	0.009	0.6974	0.851	7496	0.851	0.01								
17.5	1	0.09615	1.769	0.302018	0.412	0.366	0.100	Test 10	-0.01743	-0.1129	-0.3785	3.51	52.49	0.918	7496	0.9177	0.0837	-0.03244	-0.107	-0.3162	1413	0.228	7496	0.228	0.4342	-0.07	0.0068	-0.03	0.7117	0.834	7496	0.834	0.01								
25.5	1	0.09615	1.769	0.302018	0.390	0.353	0.094	Test 11	-0.02511	-0.1661	-0.3254	3.51	17.39	0.966	7496	0.9664	0.0482	0.004408	-0.1586	-0.3103	12.07	0.974	7496	0.974	0.0401	-0.069	0.0037	-0.025	0.7679	0.757	7496	0.757	0.01								
25.5	3	0.09615	1.769	0.302018	0.409	0.358	0.094	Test 12	-0.04214	-0.3565	0.08554	3.51	24.17	0.954	7496	0.9542	0.0568	0.001366	-0.3478	0.0785	25.17	0.95	7496	0.95	0.0579	-0.069	-0.025	-0.002	0.7697	0.757	7496	0.757	0.01								
17.5	3	0.09615	1.769	0.302018	0.447	0.386	0.101	Test 13	-0.03538	-0.2889	0.2935	3.51	27.52	0.959	7496	0.9585	0.0606	0.001272	-0.2548	0.2888	18.65	0.968	7496	0.968	0.0499	-0.07	-0.029	0.0112	0.7335	0.83	7496	0.83	0.01								
11.5	3	0.09615	1.769	0.302018	0.437	0.383	0.106	Test 14	-0.03639	-0.4	-0.0214	3.51	81.88	0.88	7496	0.8802	0.1045	0.005291	-0.3773	0.0013	21.9	0.961	7496	0.961	0.054	-0.07	-0.029	-0.022	0.6436	0.886	7496	0.886	0.009								
9.5	3	0.09615	1.769	0.302018	0.425	0.372	0.108	Test 15	-0.02818	-0.3174	0.2382	3.51	50.35	0.921	7496	0.9214	0.082	-0.00028	-0.28	0.2452	22.09	0.959	7496	0.959	0.0543	-0.07	-0.038	0.0003	0.6209	0.899	7496	0.899	0.009								
5.5	3	0.09615	1.769	0.302018	0.392	0.376	0.112	Test 16	-0.00115	-0.1808	0.3464	3.51	53.74	0.914	7496	0.9141	0.0847	0.01588	-0.1472	0.3286	91.08	0.842	7496	0.842	0.1102	-0.069	-0.039	0.0156	0.5799	0.921	7496	0.921	0.009								
-0.5	3	0.09615	1.769	0.302018	0.390	0.358	0.117	Test 17	0.03793	-0.1521	0.3176	3.51	67.55	0.873	7496	0.8731	0.0949	0.02869	-0.1153	0.3087	360.5	0.53	7496	0.53	0.2193	-0.07	-0.045	0.0136	0.5393	0.94	7496	0.94	0.009								
-0.5	1	0.10152	1.217	0.28772	0.390	0.341	0.102	Test 1	0.05696	-0.1076	0.3151	4.97	56.5	0.88	7496	0.8803	0.0868	0.06746	-0.05183	0.2687	55.76	0.834	7496	0.834	0.0862	-0.069	-0.027	0.0185	0.302	0.931	7496	0.931	0.006								
1.5	1	0.10152	1.217	0.28772	0.411	0.338	0.102	Test 2	0.05528	0.1739	-0.3099	4.96	58.63	0.89	7496	0.8898	0.0884	0.04213	0.1459	-0.2571	25.8	0.927	7496	0.927	0.0587	-0.069	0.0293	-0.013	0.2815	0.932	7496	0.932	0.006								
3.5	1	0.10152	1.217	0.28772	0.408	0.332	0.098	Test 3	0.04498	0.171	-0.3201	4.97	39.47	0.926	7496	0.926	0.0726	0.02346	0.133	-0.278	73.97	0.828	7496	0.828	0.0993	-0.069	0.0241	-0.016	0.2658	0.923	7496	0.923	0.006								
5.5	1	0.10152	1.217	0.28772	0.394	0.331	0.097	Test 4	0.02701	0.2981	-0.2139	4.97	37.16	0.931	7496	0.9314	0.0704	0.01768	0.245	-0.1961	281	0.568	7496	0.568	0.1936	-0.069	0.0261	0.0079	0.2864	0.907	7496	0.907	0.006								
7.5	1	0.10152	1.217	0.28772	0.383	0.335	0.095	Test 5	0.01408	-0.2454	-0.2753	4.97	56.87	0.9	7496	0.8997	0.0871	0.01643	-0.2286	-0.2223	81.33	0.824	7496	0.824	0.1042	-0.069	-0.013	-0.022	0.2879	0.898	7496	0.898	0.006								
9.5	1	0.10152	1.217	0.28772	0.361	0.319	0.094	Test 6	0.0046	0.2817	-0.2176	4.97	25.8	0.949	7496	0.9485	0.0587	0.002424	0.2417	-0.2038	38.56	0.907	7496	0.907	0.0717	-0.07	0.022	-0.011	0.3482	0.865	7496	0.865	0.007								
11.5	1	0.10152	1.217	0.28772	0.370	0.324	0.093	Test 7	-0.01914	-0.0157	0.351	4.97	62.06	0.882	7496	0.8818	0.091	0.02146	-0.01104	0.3023	621.1	0.356	7496	0.356	0.2879	-0.07	0.0005	0.0233	0.2447	0.893	7496	0.893	0.006								
13.5	1	0.10152	1.217	0.28772	0.365	0.334	0.093	Test 8	-0.01576	0.3488	-0.0234	4.97	53.48	0.896	7496	0.8955	0.0845	0.01574	0.3165	-0.0306	59.54	0.864	7496	0.864	0.0891	-0.07	0.0226	-0.003	0.1858	0.913	7496	0.913	0.005								
15.5	1	0.10152	1.217	0.28772	0.363	0.328	0.093	Test 9	-0.01663	0.08364	-0.3365	4.97	18.27	0.961	7496	0.961	0.0494	0.007158	0.04257	-0.3178	181.9	0.679	7496	0.679	0.1558	-0.07	-0.001	-0.023	0.1691	0.921	7496	0.921	0.00								
17.5	1	0.10152	1.217	0.28772	0.355	0.319	0.093	Test 10	-0.01528	0.2363	-0.2435	4.97	10.96	0.975	7496	0.9752	0.0382	0.007844	0.2011	-0.2379	24.78	0.936	7496	0.936	0.0575	-0.07	0.0075	-0.022	0.1785	0.921	7496	0.921	0.00								
25.5	1	0.10152	1.217	0.28772	0.285	0.271	0.098	Test 11	0.00705	-0.0608	-0.2713	4.97	8.14	0.973	7496	0.9727	0.033	0.01269	-0.06222	-0.251	7.104	0.972	7496	0.972	0.0308	-0.068	-0.025	-0.017	0.2122	0.941	7496	0.94	0.005								
25.5	3	0.10152	1.217	0.28772	0.325	0.275	0.098	Test 12	-0.03504	-0.2279	0.18	4.97	7.148	0.978	7496	0.9779	0.0309	0.002291	-0.2112	0.1718	27.33	0.91	7496	0.91	0.0604	-0.068	0.0075	0.029	0.2152	0.94	7496	0.94	0.005								
17.5	3	0.10152	1.217	0.28772	0.371	0.324	0.093	Test 13	-0.0216	0.2056	-0.283	4.97	14.75	0.969	7496	0.9688	0.0444	0.001461	0.1851	-0.2642	13.24	0.967	7496	0.967	0.042	-0.07	0.0058	-0.023	0.1738	0.923	7496	0.923	0.00								
11.5	3	0.10152	1.217	0.28772	0.400	0.337	0.094	Test 14	-0.04023	0.2082	0.2929	4.97	36.1	0.931	7496	0.9306	0.0694	0.004347	0.1957	0.2695	14.76	0.966	7496	0.966	0.0444	-0.07	0.0137	0.0192	0.214	0.907	7496	0.907	0.005								
9.5	3	0.10152	1.217	0.28772	0.379	0.336	0.094	Test 15	-0.02794	0.1264	0.3272	4.97	24.49	0.95	7496	0.9496	0.0572	0.003949	0.1389	0.3012	27.25	0.938	7496	0.938	0.0603	-0.07	0.0056	0.0237	0.3388	0.868	7496	0.868	0.007								
5.5	3	0.10152	1.217	0.28772	0.354	0.329	0.097	Test 16	-0.01675	-0.1974	-0.2732	4.96	14.21	0.968	7496	0.9677	0.0435	0.006971	-0.1923	-0.258	25.91	0.937	7496	0.937	0.0588	-0.07	0.0056	-0.027	0.2938	0.904	7496	0.904	0.006								
-0.5	3	0.10152	1.217	0.28772	0.368	0.331	0.103	Test 17	0.04792	-0.2602	-0.1866	4.97	40.08	0.906	7496	0.9056	0.0731	0.02382	-0.2717	-0.1433	54.9	0.866	7496	0.866	0.0856	-0.07	-0.012	-0.031	0.2682	0.939	7496	0.939	0.006								

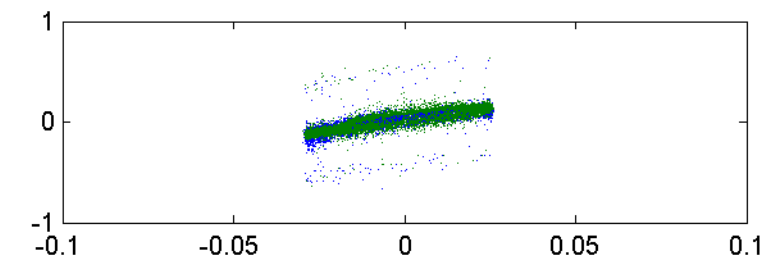
Appendix B - Tables of Results

Location	Loading Parameters			Resultant Max.			Test Coefficient for Vx1				Goodness of fit parameters				Coefficient for Vx2				Goodness of fit parameters				Coefficient for WL			Goodness of fit parameters							
1.5	1	0.15159	1.549	0.464677	0.504	0.555	0.128	Test 2	0.02083	-0.0686	0.4781	4.05	280.6	0.757	7496	0.7571	0.1935	0.1035	0.000966	0.4519	121.8	0.863	7496	0.863	0.1275	-0.073	-0.045	0.0326	2.0429	0.848	7496	0.848	0.017
3.5	1	0.15159	1.549	0.464677	0.580	0.579	0.127	Test 3	0.03539	0.243	0.4875	4.05	244.1	0.82	7496	0.8201	0.1804	0.06738	0.2564	0.4424	153.5	0.865	7496	0.865	0.1431	-0.074	-0.01	0.0524	2.1062	0.835	7496	0.835	0.017
5.5	1	0.15159	1.549	0.464677	0.625	0.612	0.124	Test 4	0.03311	0.2295	0.5454	4.05	268.9	0.83	7496	0.83	0.1894	0.06707	0.2133	0.5011	411.1	0.73	7496	0.73	0.2342	-0.074	-0.014	0.0484	2.3126	0.804	7496	0.804	0.018
7.5	1	0.15159	1.549	0.464677	0.655	0.580	0.121	Test 5	0.02552	0.4896	0.3964	4.05	221.3	0.871	7496	0.8705	0.1718	0.02567	0.4197	0.3614	129	0.899	7496	0.899	0.1312	-0.074	0.0083	0.0465	2.375	0.779	7496	0.779	0.018
9.5	1	0.15159	1.549	0.464677	0.632	0.552	0.118	Test 6	-0.00672	-0.2072	0.5895	4.05	287.1	0.836	7496	0.836	0.1957	0.004968	-0.1746	0.5183	144.3	0.886	7496	0.886	0.1387	-0.074	-0.035	0.0272	2.3862	0.752	7496	0.752	0.018
11.5	1	0.15159	1.549	0.464677	0.652	0.553	0.116	Test 7	-0.01756	-0.4803	0.4151	4.05	181.5	0.893	7496	0.8927	0.1556	0.007671	-0.4108	0.3588	242.3	0.822	7496	0.822	0.1798	-0.074	-0.041	0.0074	2.398	0.733	7496	0.733	0.018
13.5	1	0.15159	1.549	0.464677	0.652	0.548	0.114	Test 8	-0.04059	0.227	0.5677	4.05	251.5	0.848	7496	0.8478	0.1832	-0.00891	0.2014	0.4998	123.7	0.898	7496	0.898	0.1285	-0.074	0.0026	0.0401	2.4429	0.713	7496	0.713	0.018
13	1	0.15159	1.549	0.464677	0.651	0.543	0.112	Test 9	-0.05095	-0.0653	-0.5963	4.05	292.5	0.822	7496	0.8217	0.1975	-0.03885	-0.0559	-0.5014	537.6	0.64	7496	0.64	0.2678	-0.073	0.0055	-0.039	2.5037	0.695	7496	0.695	0.018
17.5	1	0.15159	1.549	0.464677	0.645	0.543	0.111	Test 10	-0.06786	0.175	0.5504	4.05	122.5	0.911	7496	0.9107	0.1279	-0.02945	0.1614	0.4875	108.4	0.901	7496	0.901	0.1203	-0.073	0.0034	0.0379	2.5085	0.684	7496	0.684	0.018
25.5	1	0.15159	1.549	0.464677	0.559	0.455	0.106	Test 11	-0.06783	0.3205	0.3718	4.05	75.02	0.923	7496	0.9233	0.1	0.03363	0.2868	0.3085	557.8	0.544	7496	0.544	0.2728	-0.073	0.026	0.0207	1.7658	0.701	7496	0.701	0.015

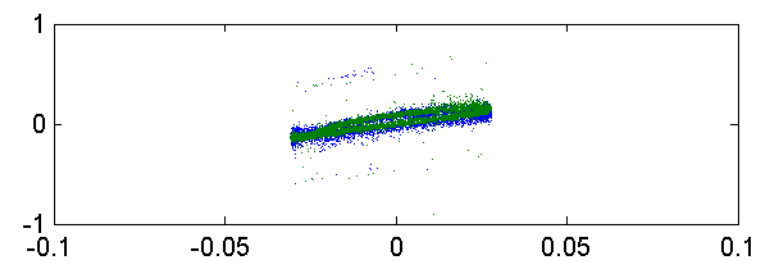
Experiment R001, Lissajous curve of x =waterlevel [m] y =measured x-velocity, blue Vx1, green Vx2 [m/s]



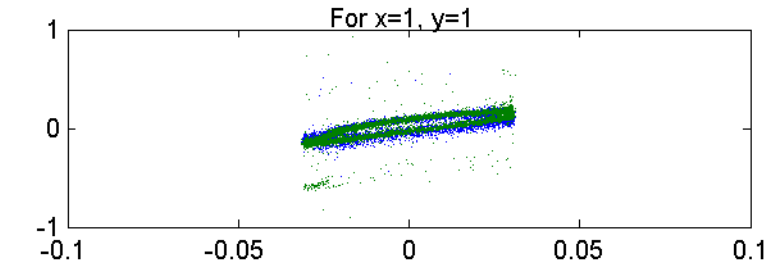
Experiment R002, Lissajous curve of x =waterlevel [m] y =measured x -velocity, blue V_{x1} , green V_{x2} [m/s]



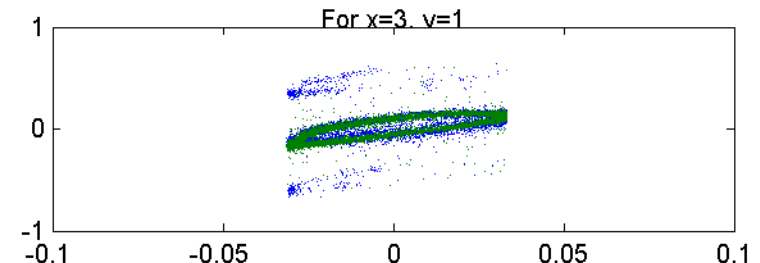
For $x=1, y=1$



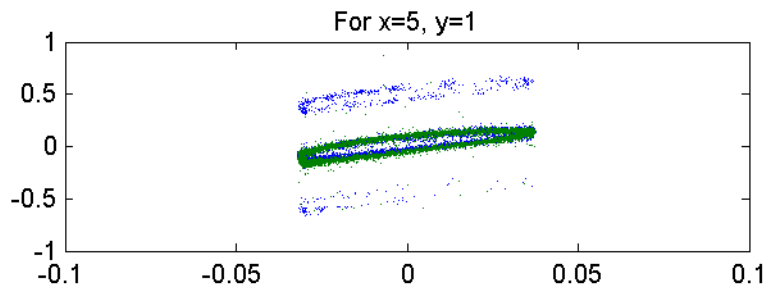
For $x=3, y=1$



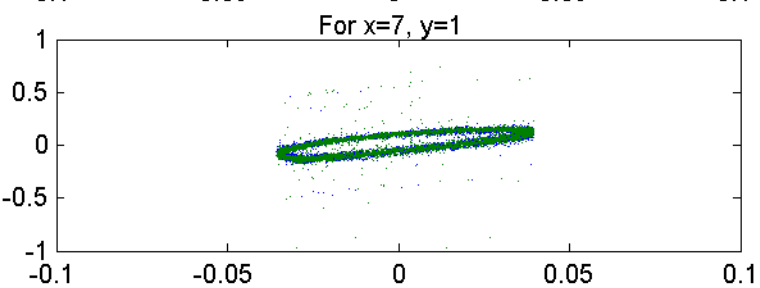
For $x=5, y=1$



For $x=7, y=1$

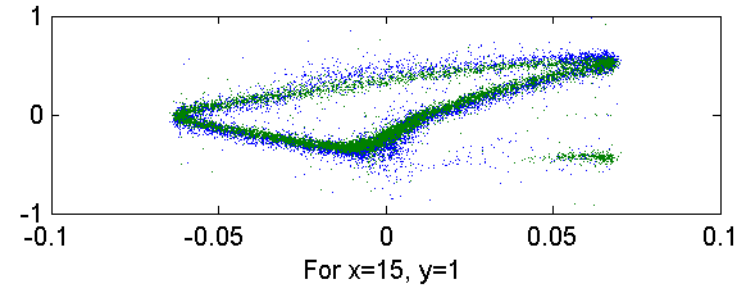
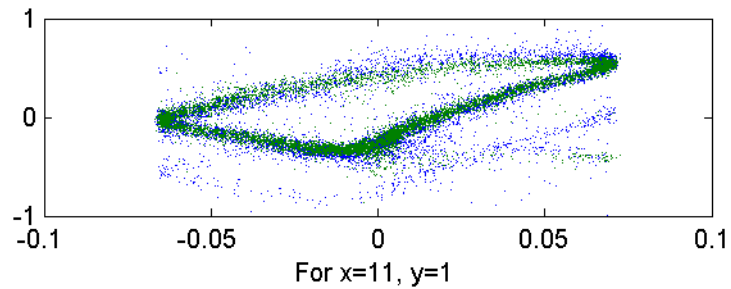
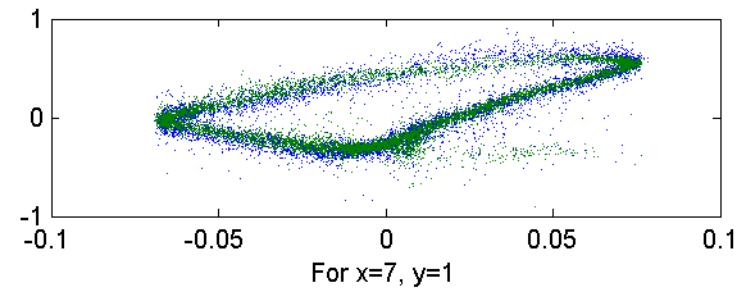
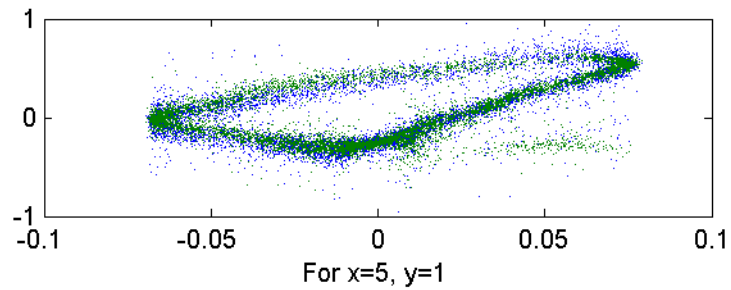
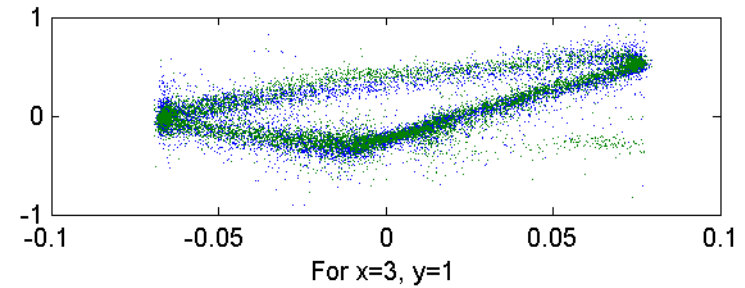
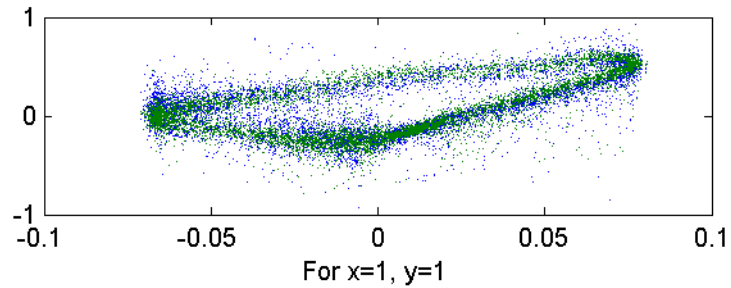


For $x=11, y=1$

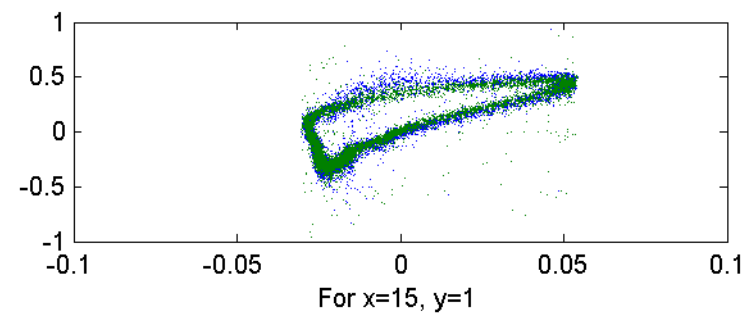
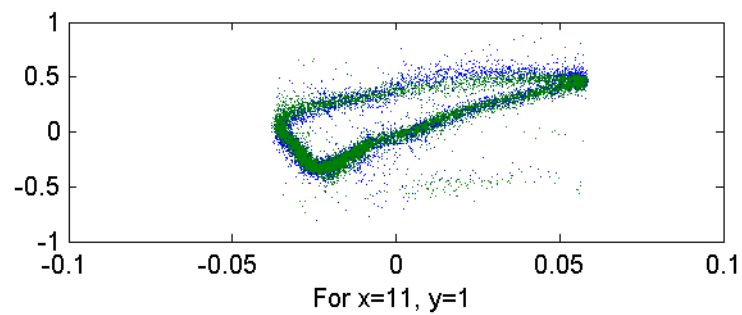
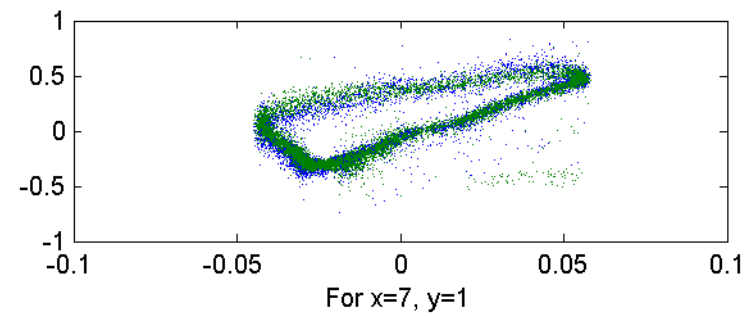
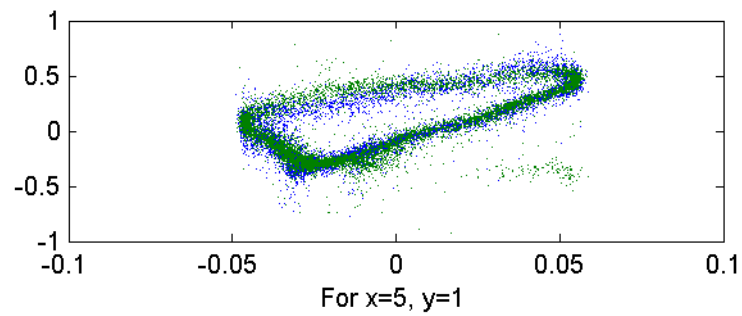
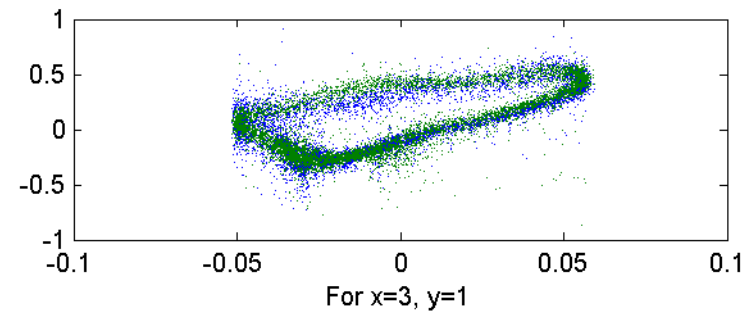
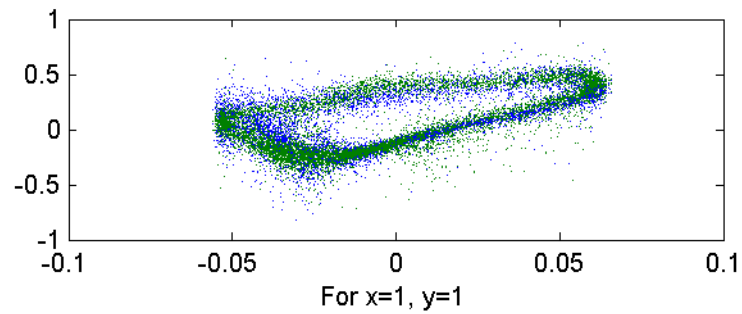


For $x=15, y=1$

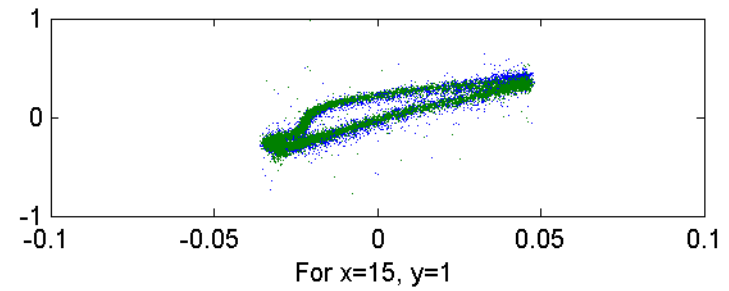
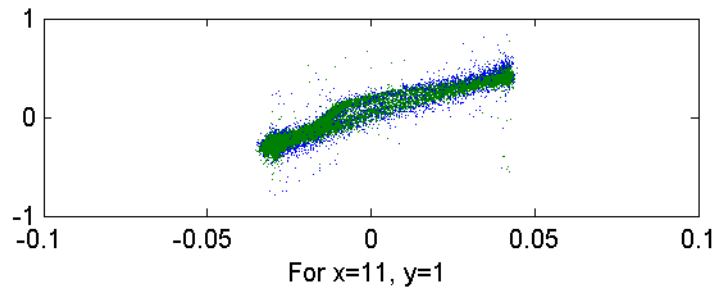
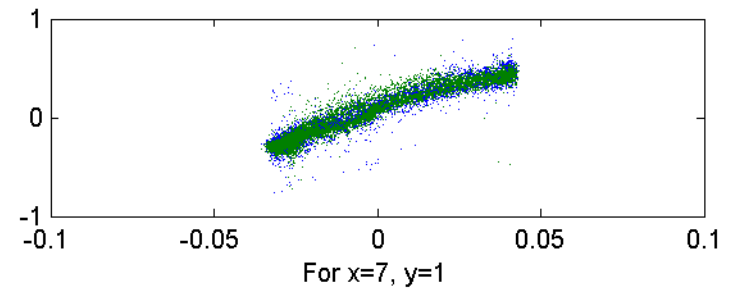
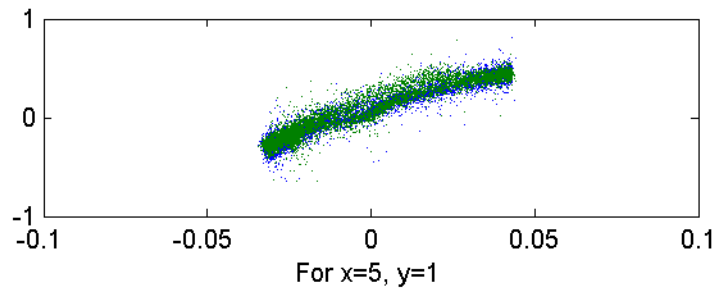
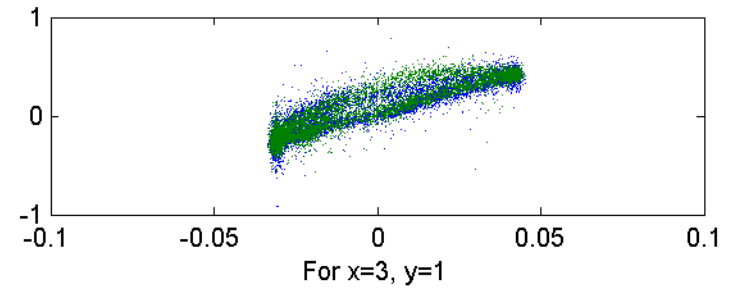
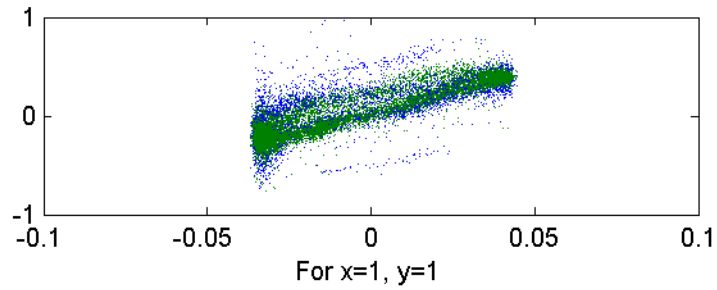
Experiment R003, Lissajous curve of x =waterlevel [m] y =measured x -velocity, blue V_{x1} , green V_{x2} [m/s]



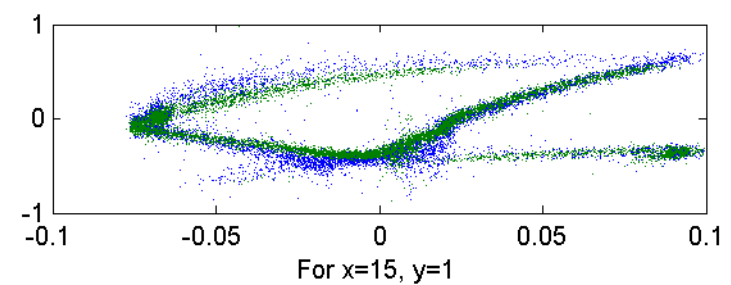
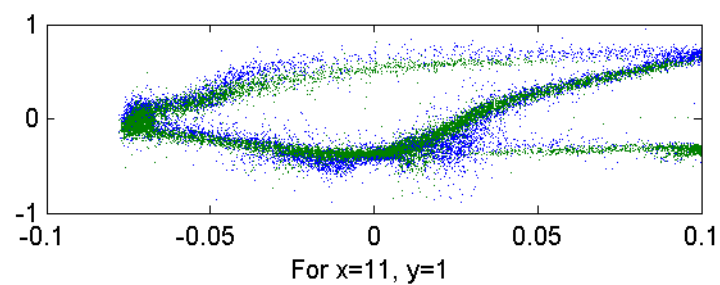
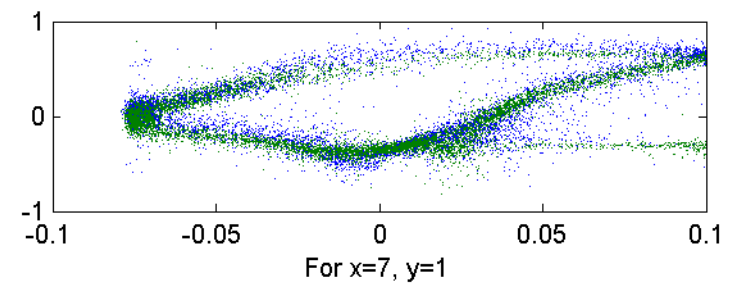
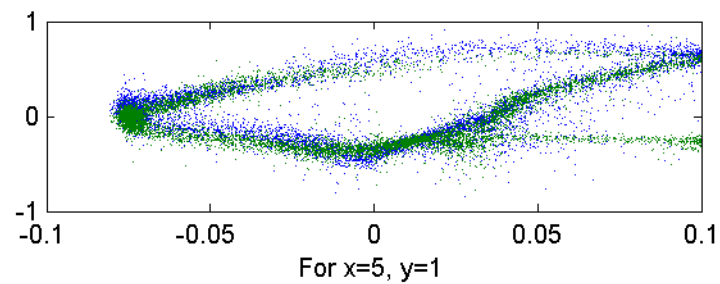
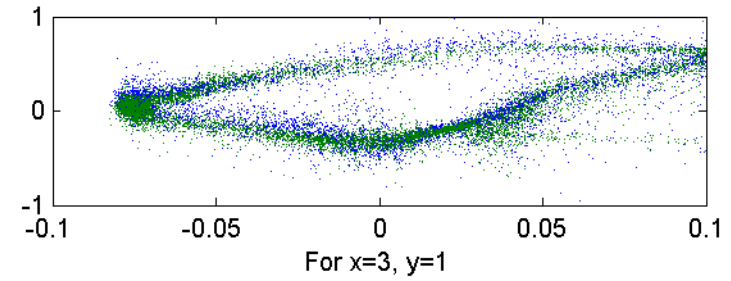
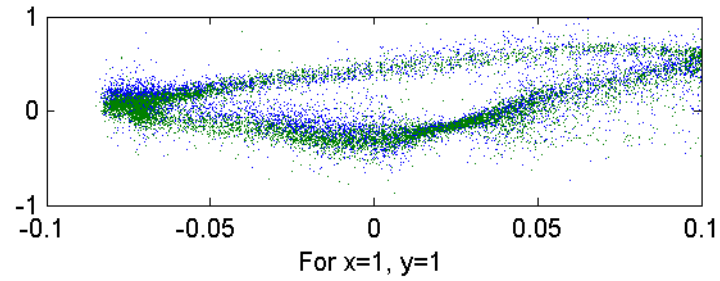
Experiment R004, Lissajous curve of x =waterlevel [m] y =measured x -velocity, blue V_{x1} , green V_{x2} [m/s]



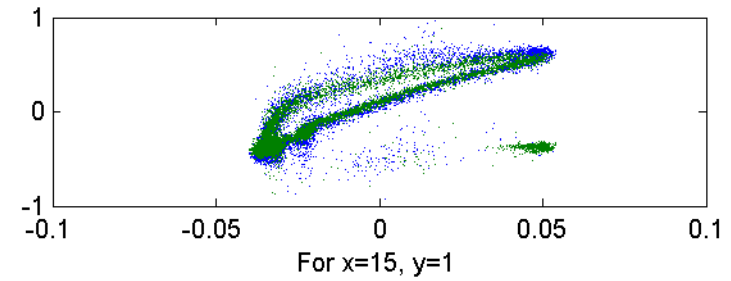
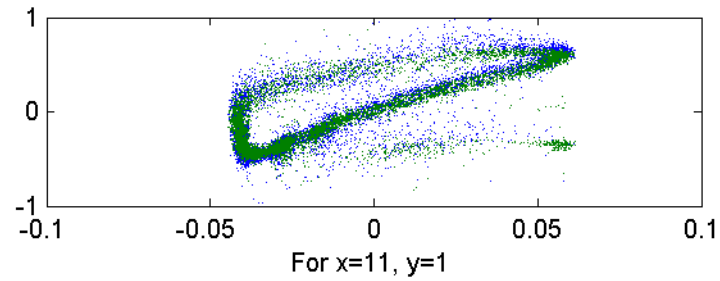
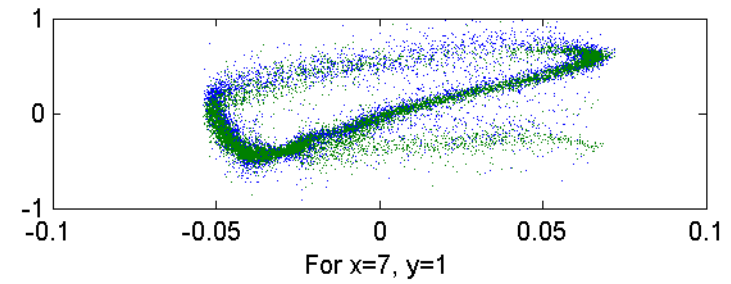
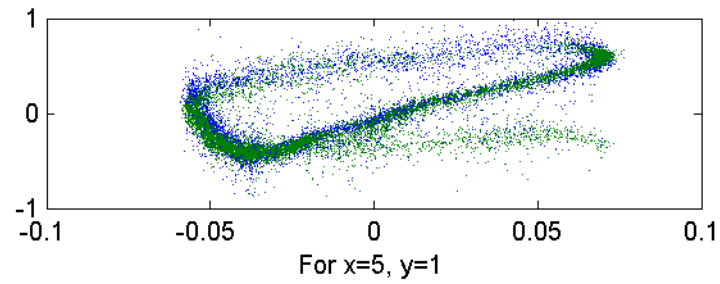
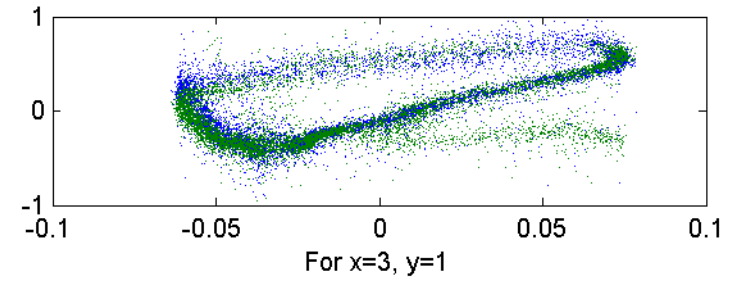
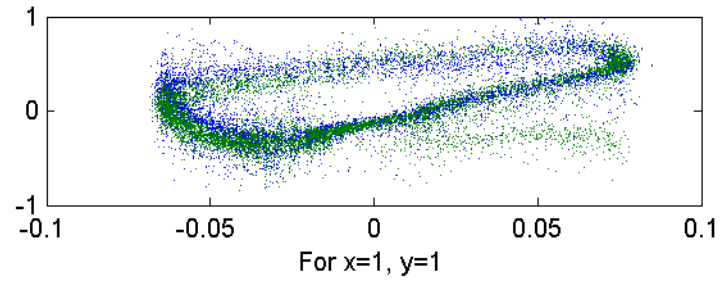
Experiment R005, Lissajous curve of x =waterlevel [m] y =measured x-velocity, blue Vx1, green Vx2 [m/s]



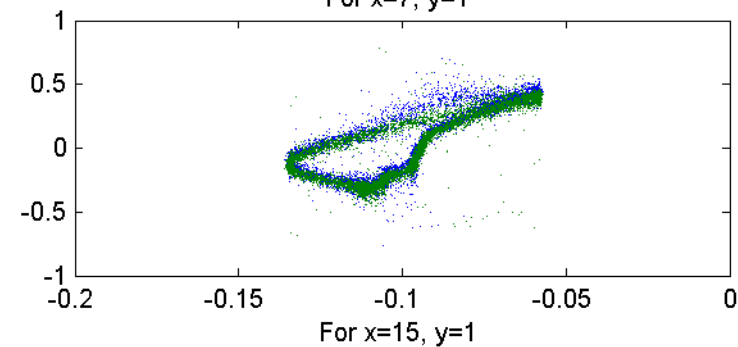
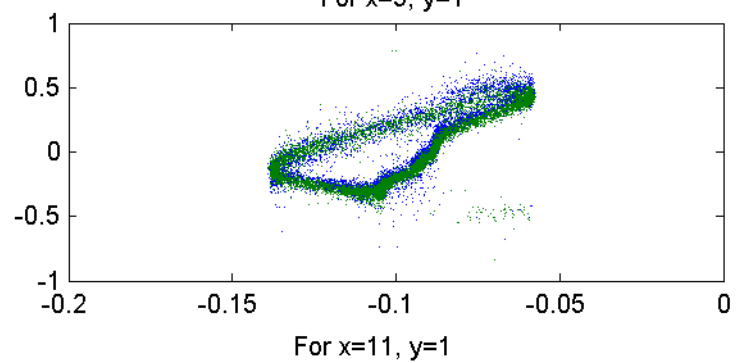
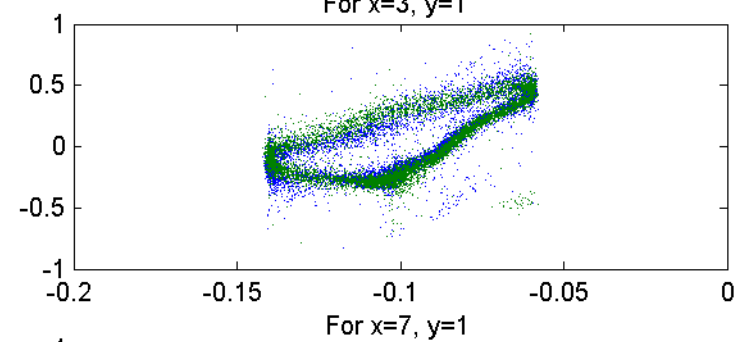
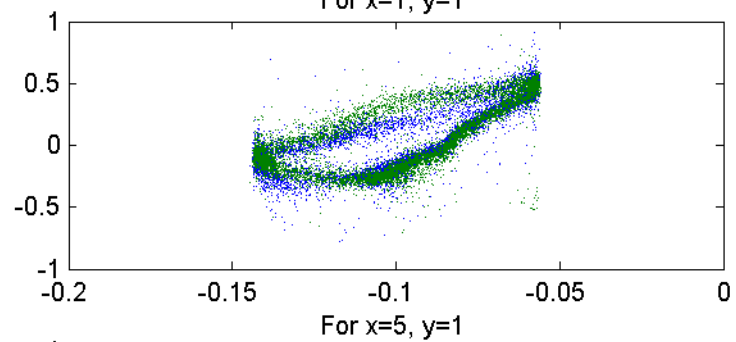
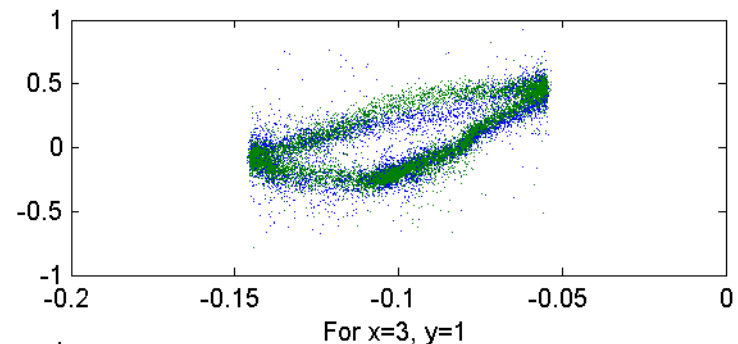
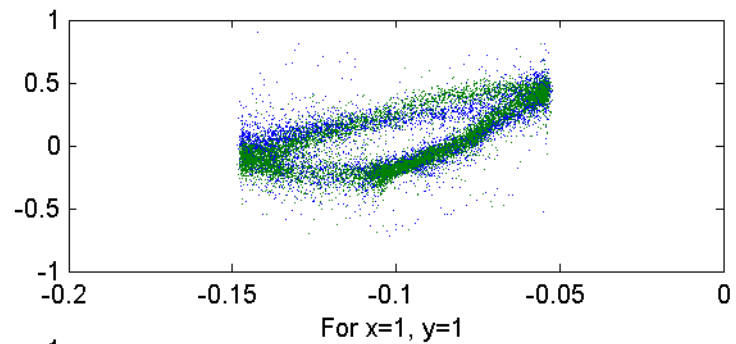
Experiment R006, Lissajous curve of x =waterlevel [m] y =measured x -velocity, blue V_{x1} , green V_{x2} [m/s]



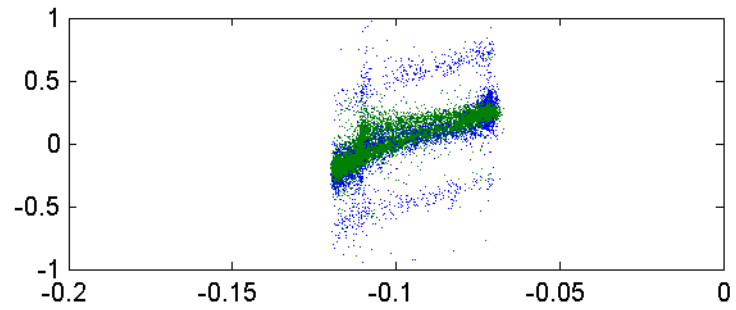
Experiment R007, Lissajous curve of x =waterlevel [m] y =measured x -velocity, blue V_{x1} , green V_{x2} [m/s]



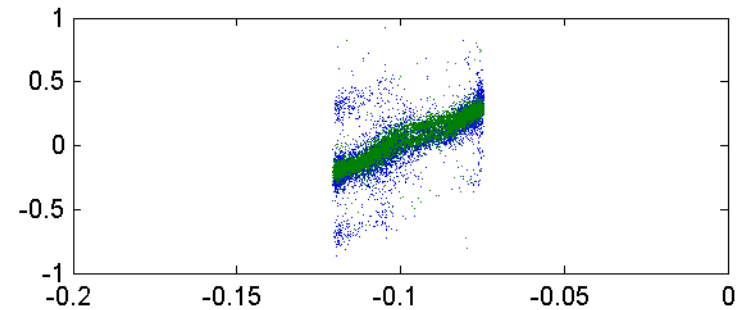
Experiment R008, Lissajous curve of x =waterlevel [m] y =measured x -velocity, blue V_{x1} , green V_{x2} [m/s]



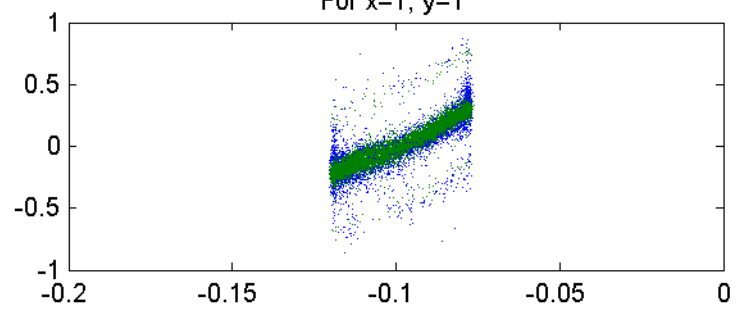
Experiment R009, Lissajous curve of x =waterlevel [m] y =measured x-velocity, blue V_{x1} , green V_{x2} [m/s]



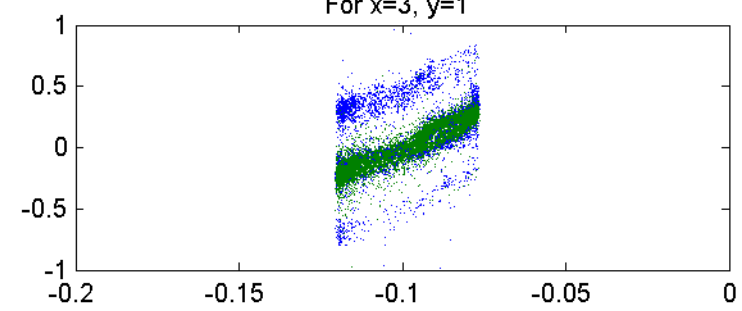
For $x=1, y=1$



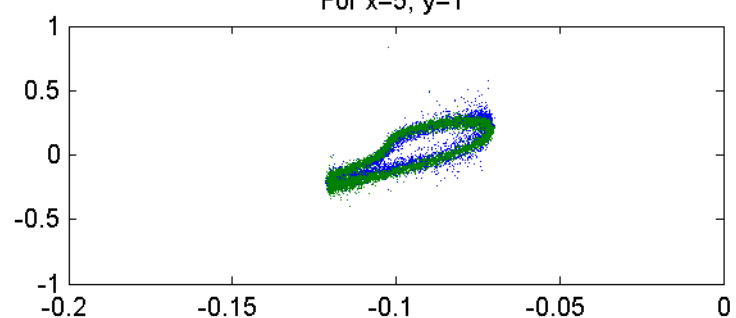
For $x=3, y=1$



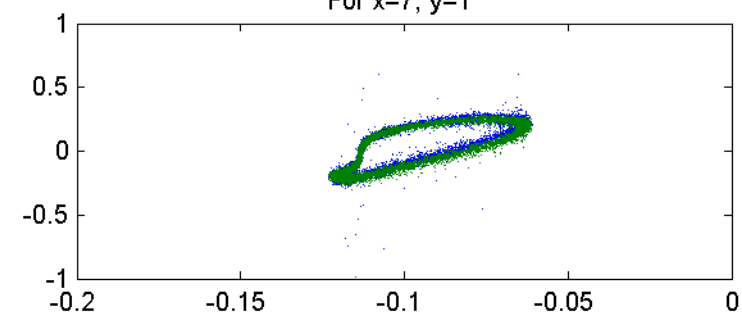
For $x=5, y=1$



For $x=7, y=1$

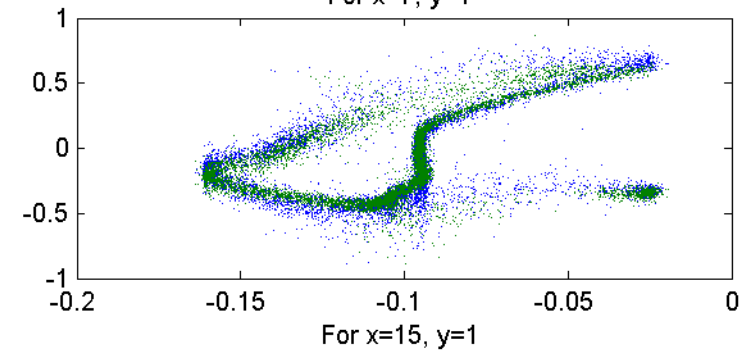
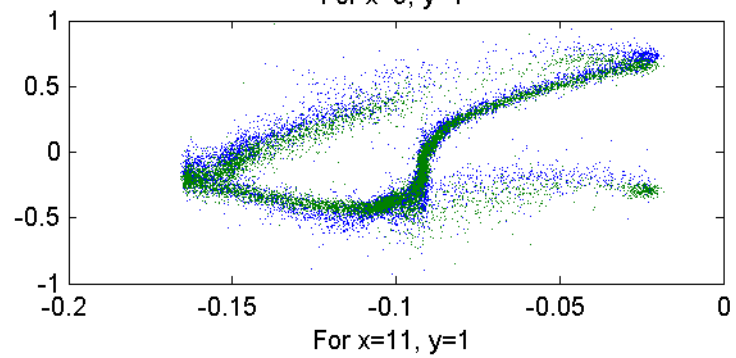
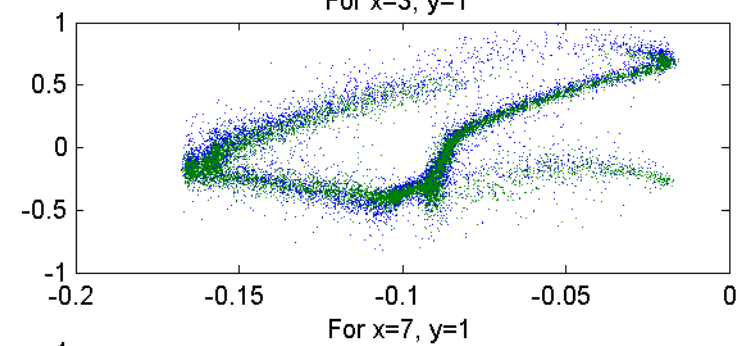
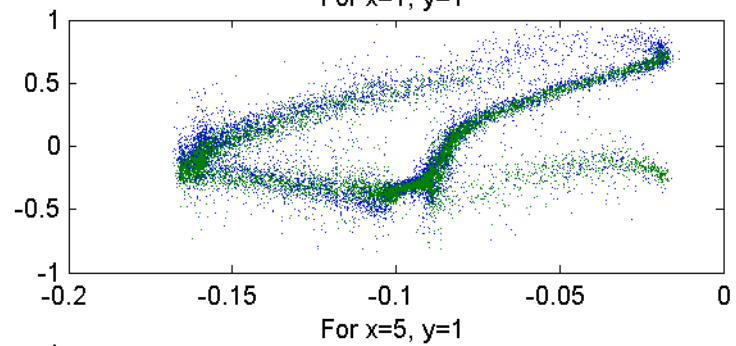
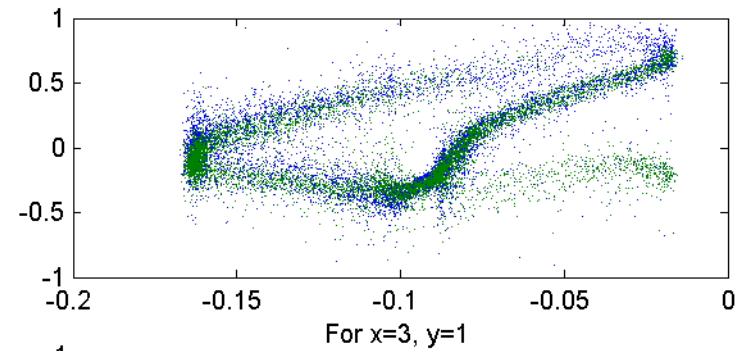
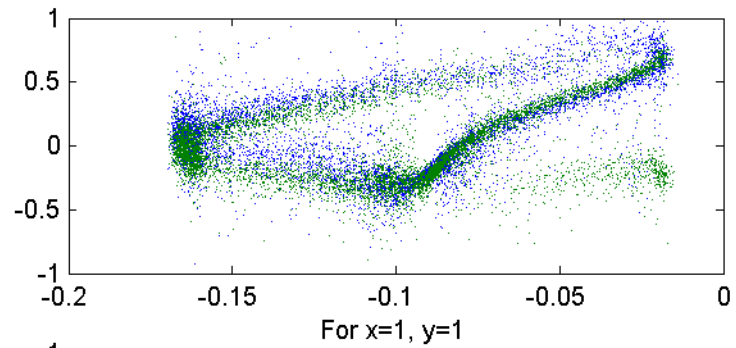


For $x=11, y=1$

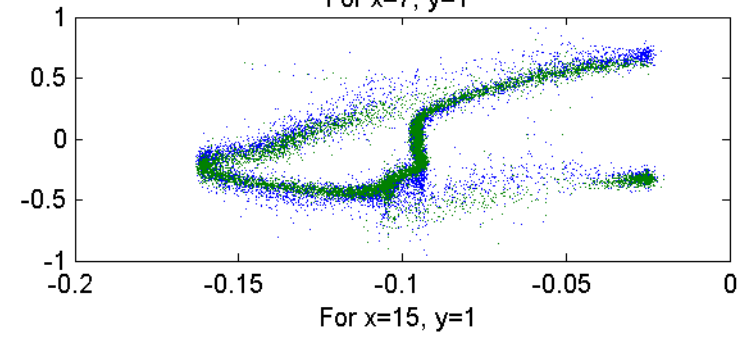
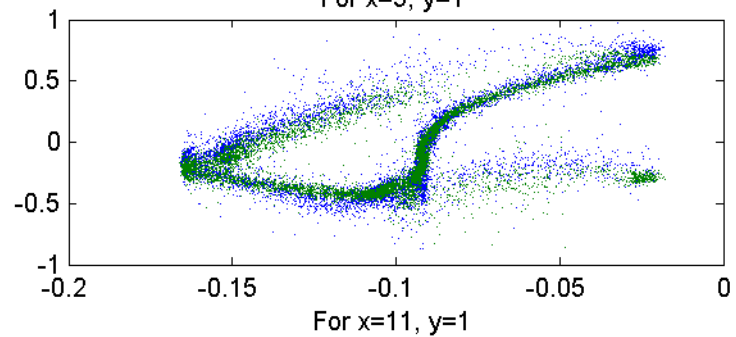
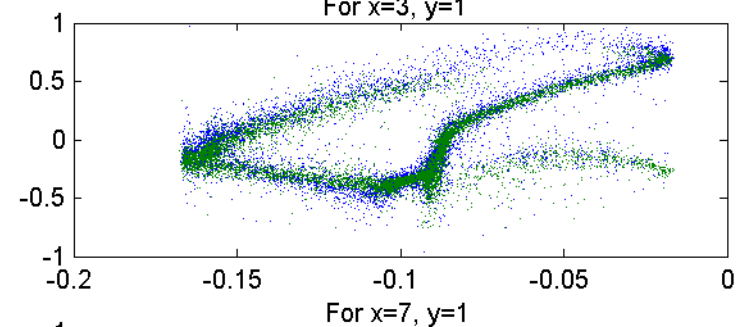
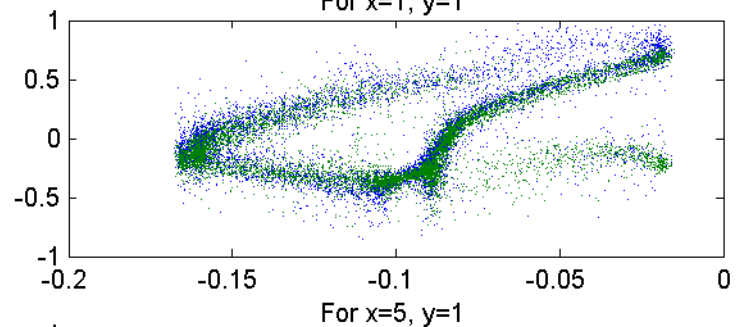
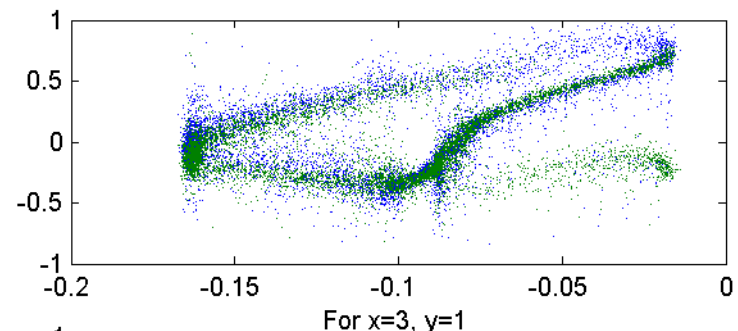
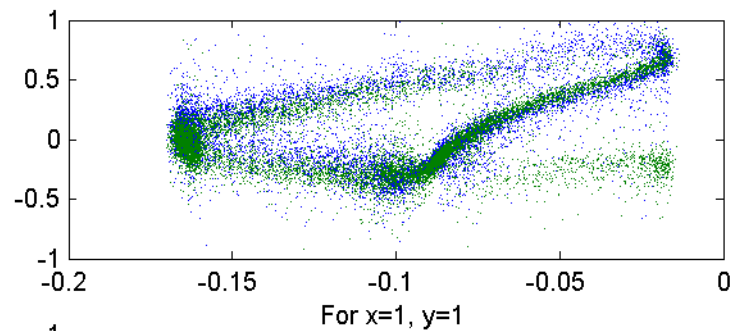


For $x=15, y=1$

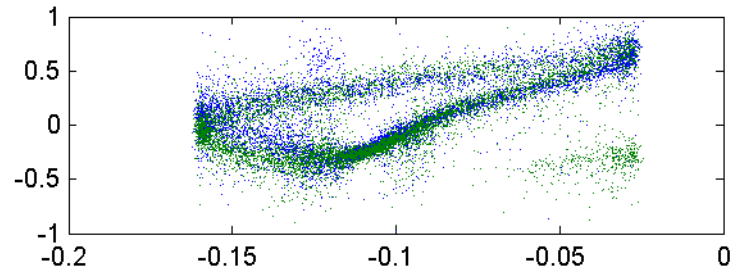
Experiment R010, Lissajous curve of x =waterlevel [m] y =measured x -velocity, blue V_{x1} , green V_{x2} [m/s]



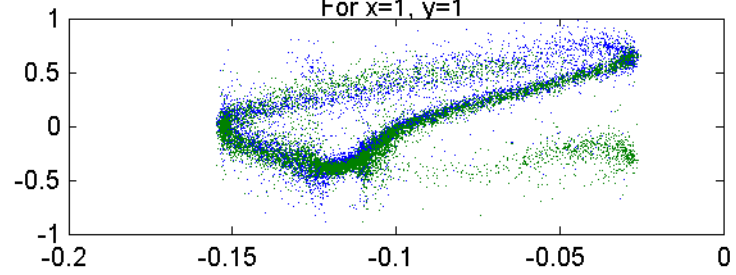
Experiment R011, Lissajous curve of x =waterlevel [m] y =measured x -velocity, blue V_{x1} , green V_{x2} [m/s]



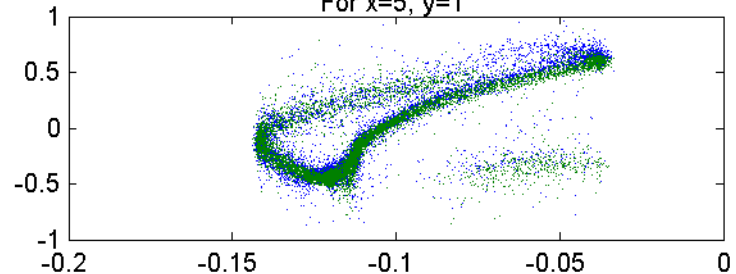
Experiment R012, Lissajous curve of x =waterlevel [m] y =measured x-velocity, blue V_{x1} , green V_{x2} [m/s]



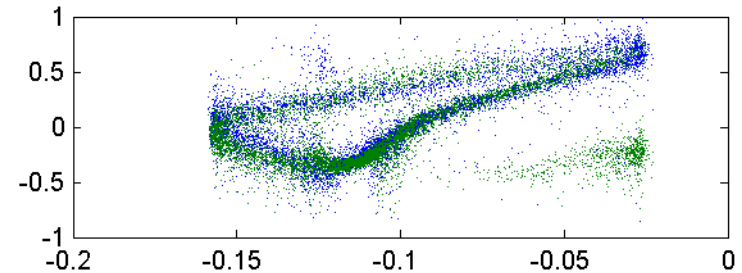
For $x=1, y=1$



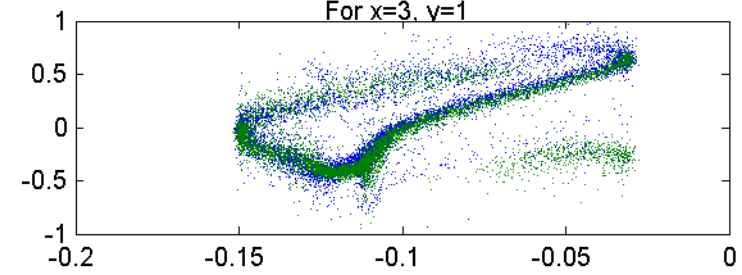
For $x=5, y=1$



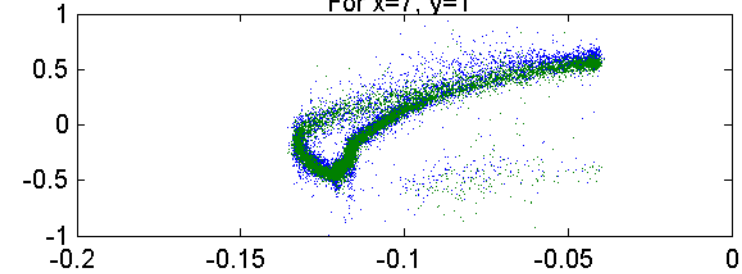
For $x=11, y=1$



For $x=3, y=1$

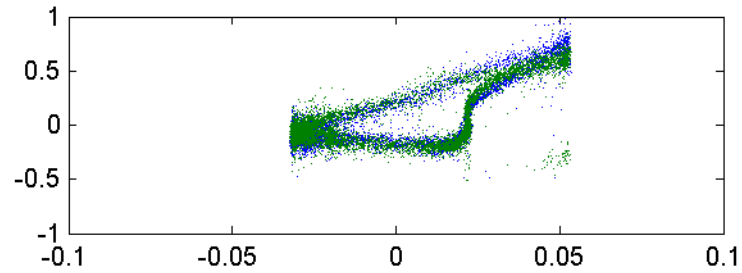


For $x=7, y=1$

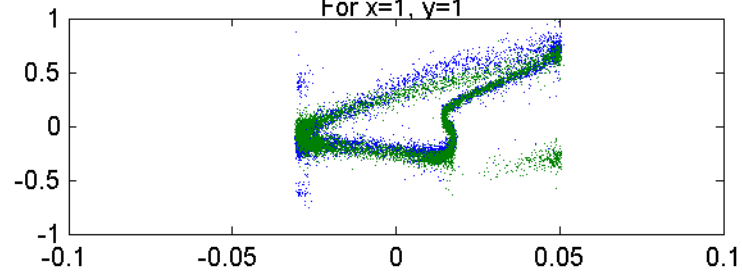


For $x=15, y=1$

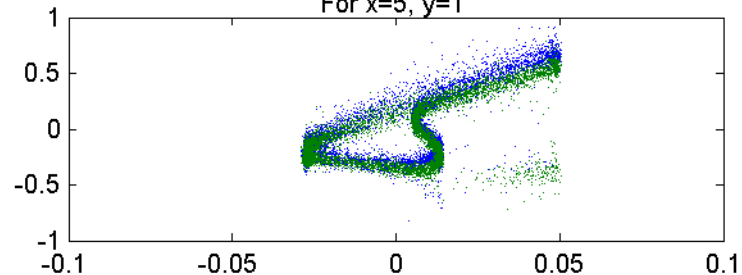
Experiment R015, Lissajous curve of x =waterlevel [m] y =measured x-velocity, blue Vx1, green Vx2 [m/s]



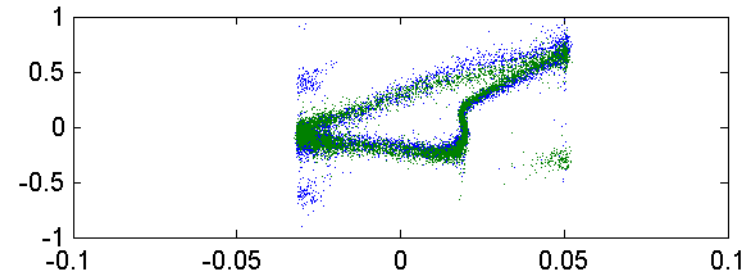
For $x=1, y=1$



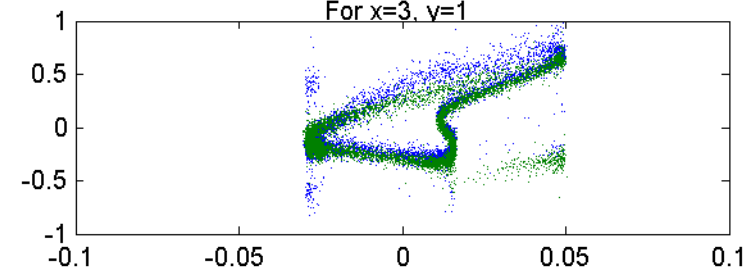
For $x=5, y=1$



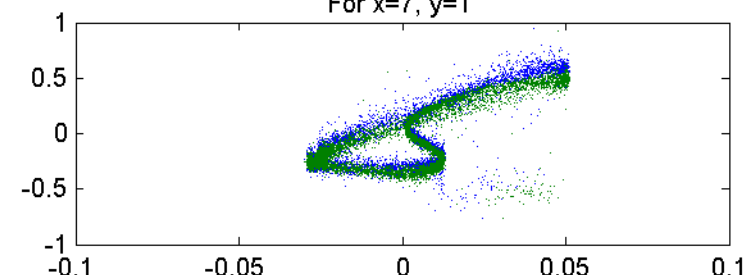
For $x=11, y=1$



For $x=3, y=1$

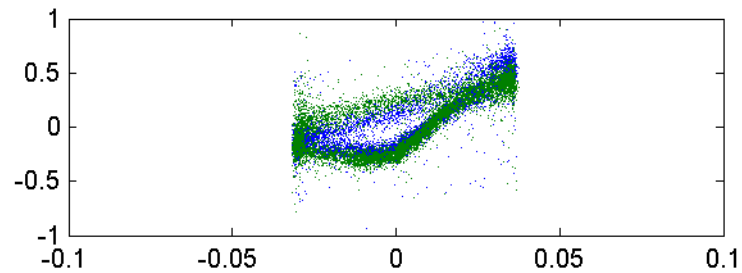


For $x=7, y=1$

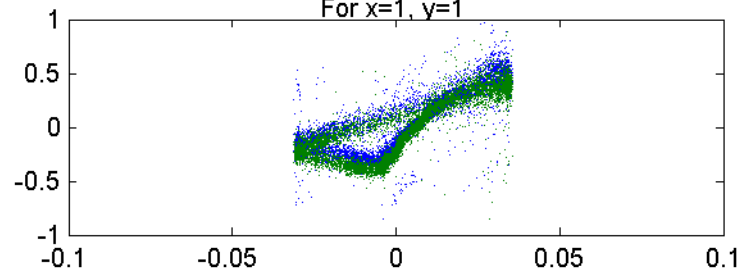


For $x=15, y=1$

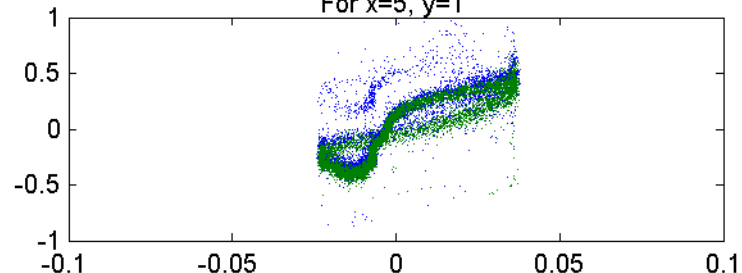
Experiment R016, Lissajous curve of x =waterlevel [m] y =measured x-velocity, blue V_{x1} , green V_{x2} [m/s]



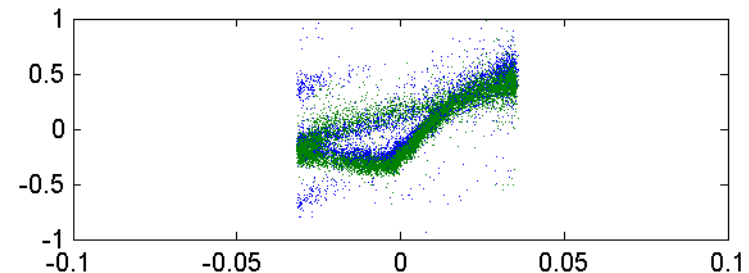
For $x=1, y=1$



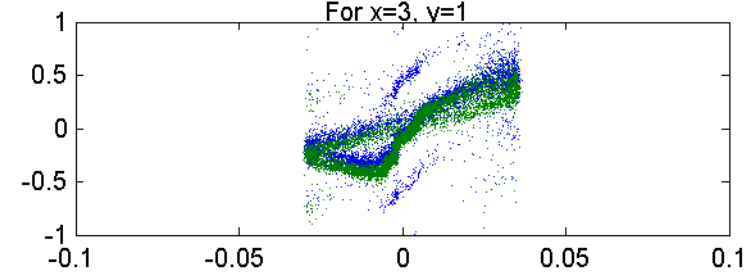
For $x=5, y=1$



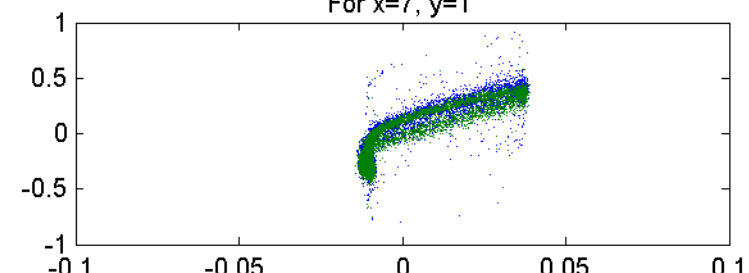
For $x=11, y=1$



For $x=3, y=1$

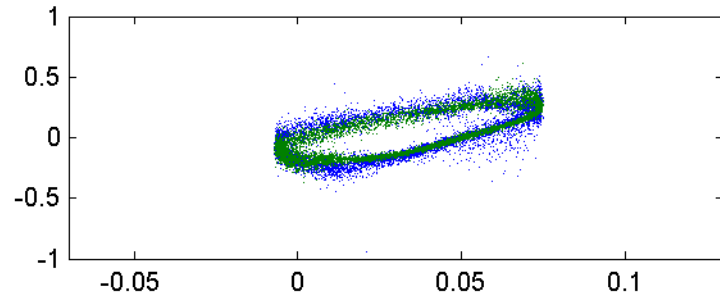


For $x=7, y=1$

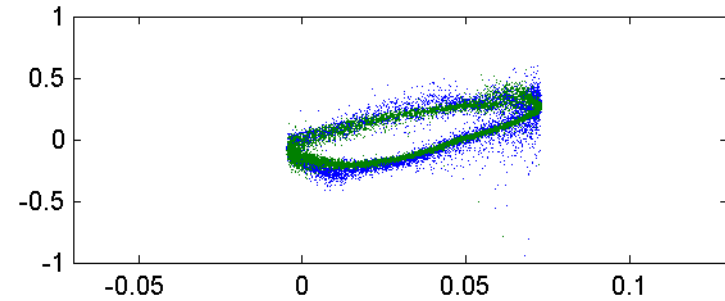


For $x=15, y=1$

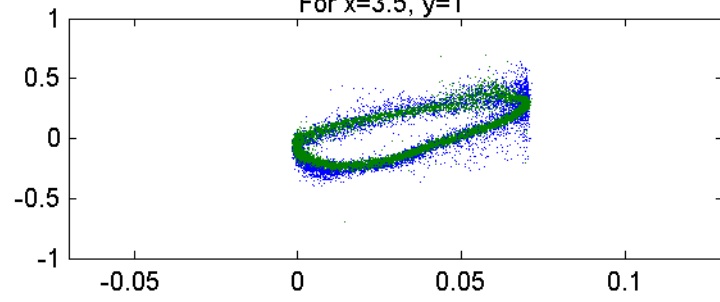
Experiment R030, Lissajous curve of x =waterlevel [m] y =measured x -velocity, blue V_{x1} , green V_{x2} [m/s]



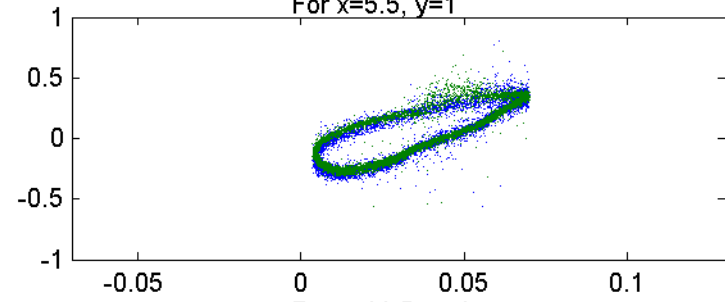
For $x=3.5, y=1$



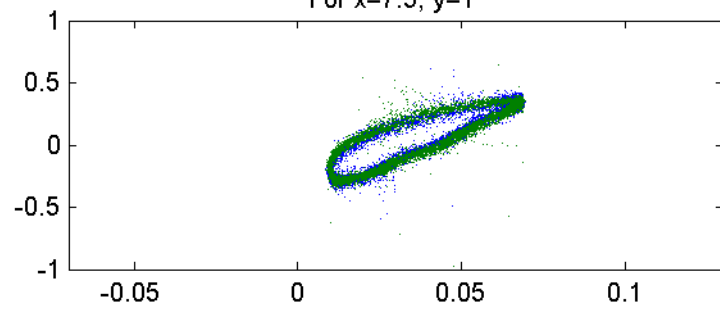
For $x=5.5, y=1$



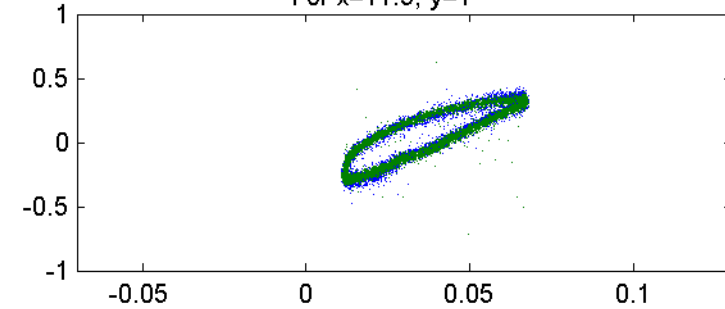
For $x=7.5, y=1$



For $x=11.5, y=1$

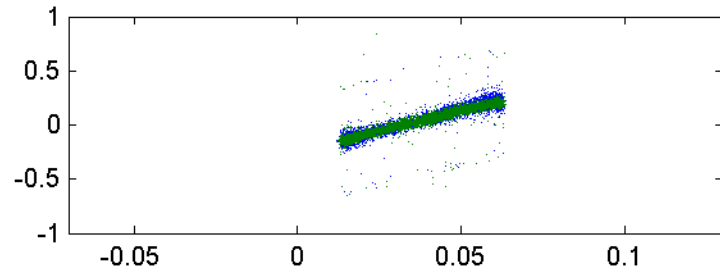


For $x=15.5, y=1$

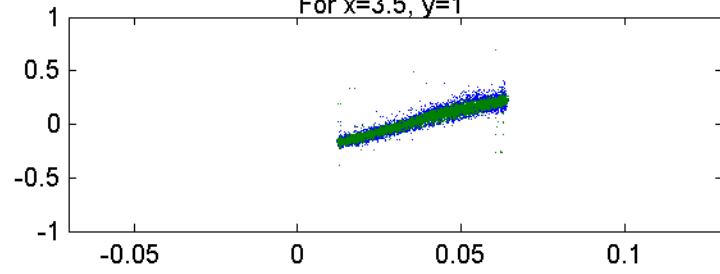


For $x=17.5, y=1$

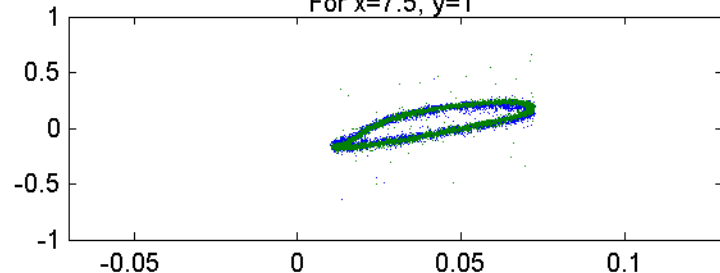
Experiment R031, Lissajous curve of x =waterlevel [m] y =measured x-velocity, blue V_{x1} , green V_{x2} [m/s]



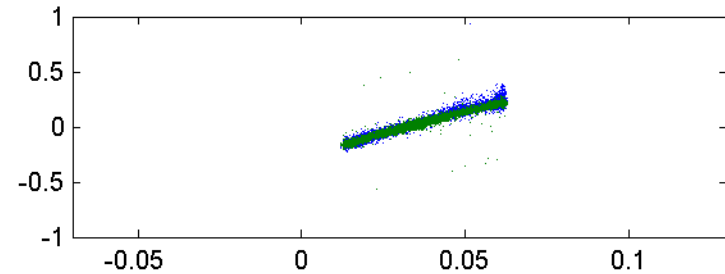
For $x=3.5, y=1$



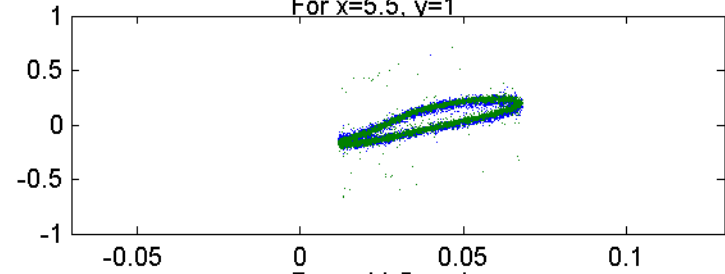
For $x=7.5, y=1$



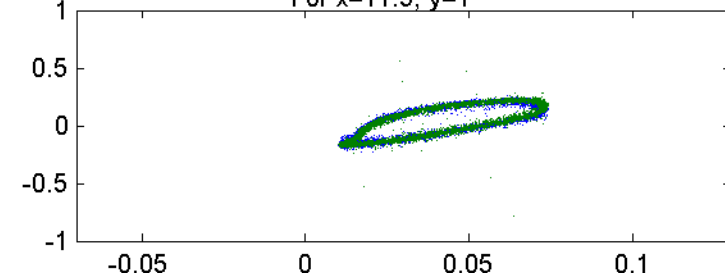
For $x=15.5, y=1$



For $x=5.5, y=1$

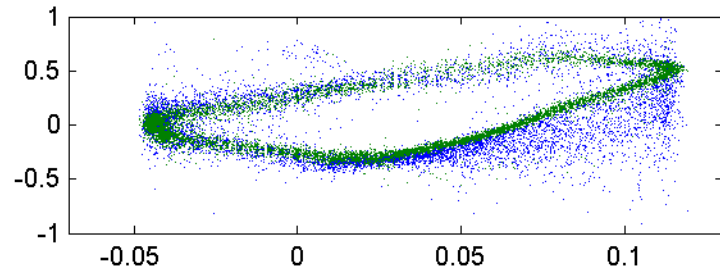


For $x=11.5, y=1$

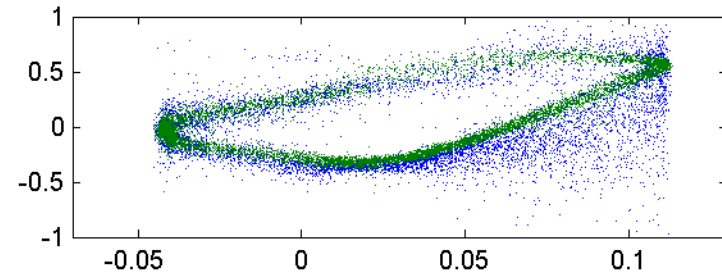


For $x=17.5, y=1$

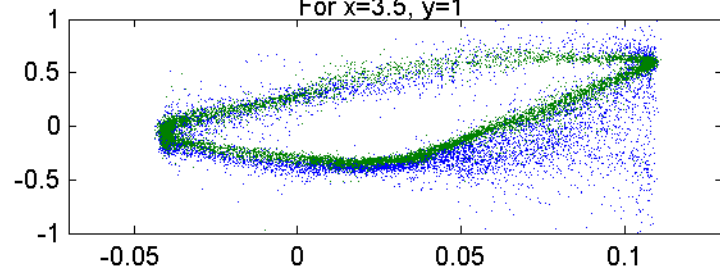
Experiment R032, Lissajous curve of x =waterlevel [m] y =measured x -velocity, blue V_{x1} , green V_{x2} [m/s]



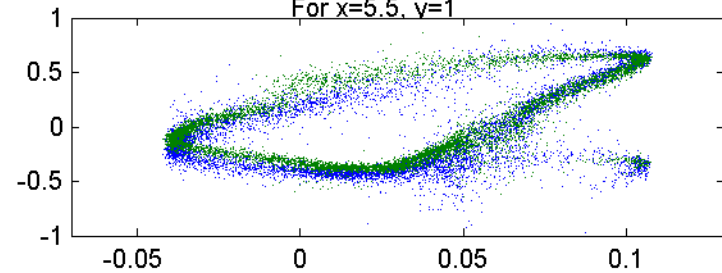
For $x=3.5, y=1$



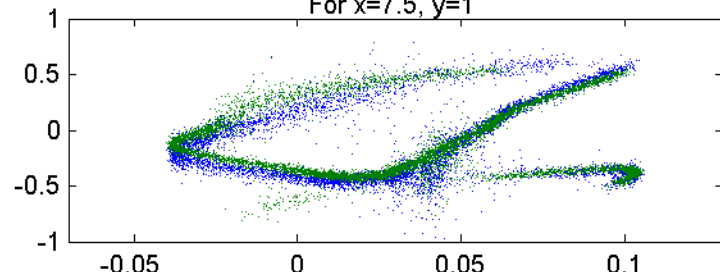
For $x=5.5, y=1$



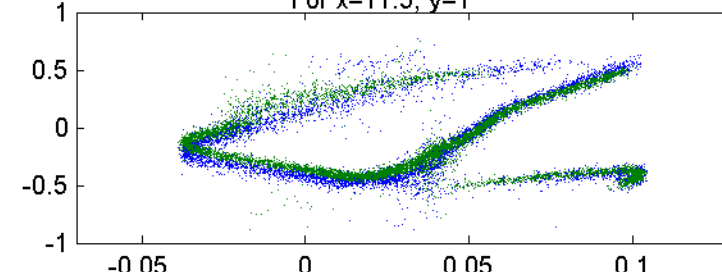
For $x=7.5, y=1$



For $x=11.5, y=1$

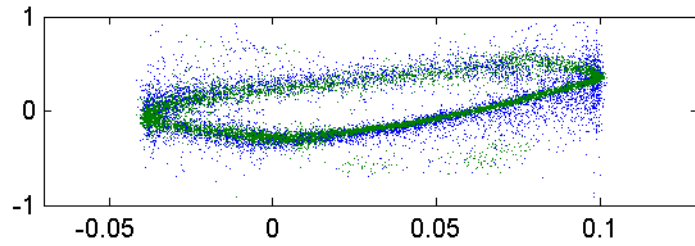


For $x=15.5, y=1$

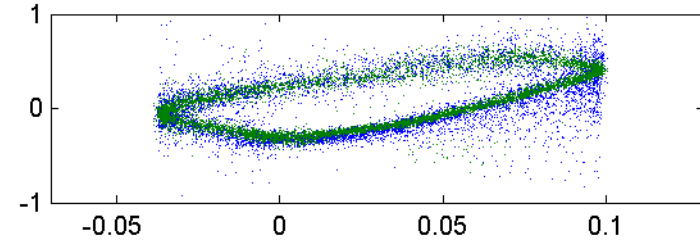


For $x=17.5, y=1$

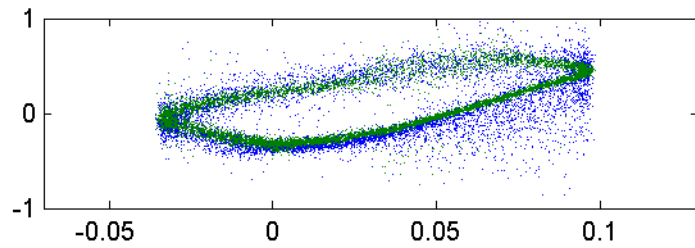
Experiment R033, Lissajous curve of x =waterlevel [m] y =measured x-velocity, blue V_{x1} , green V_{x2} [m/s]



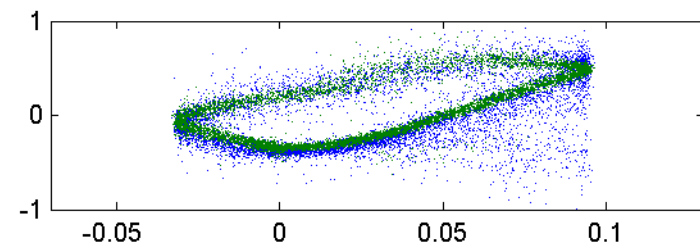
For $x=1.5, y=1$



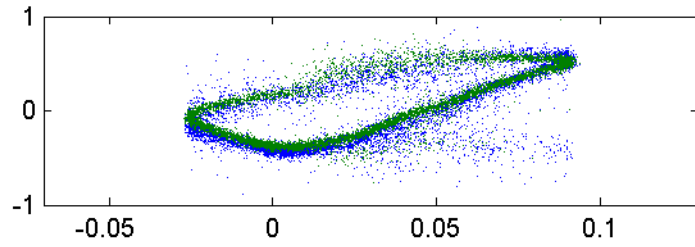
For $x=3.5, y=1$



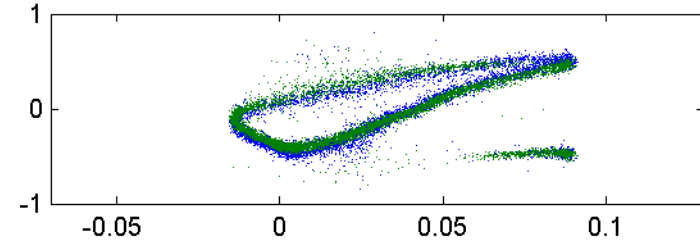
For $x=5.5, y=1$



For $x=7.5, y=1$

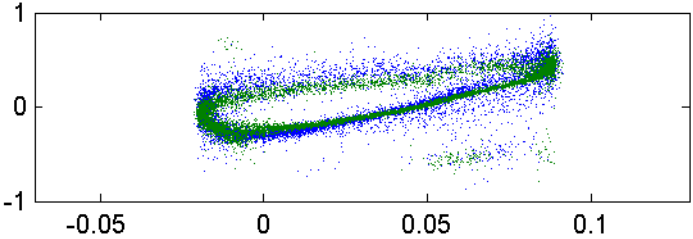


For $x=11.5, y=1$

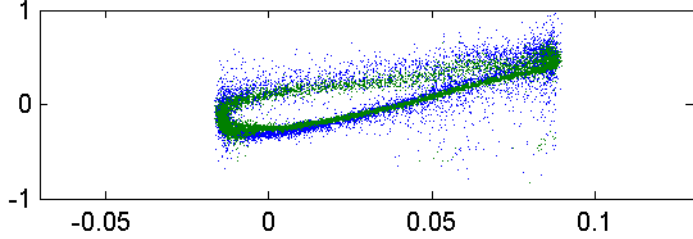


For $x=17.5, y=1$

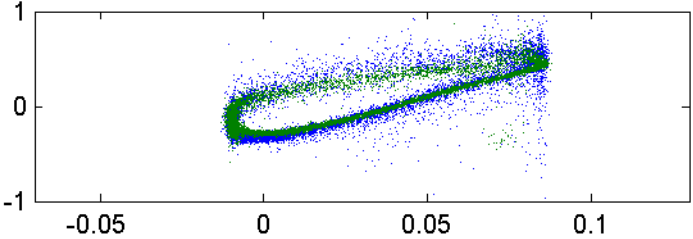
Experiment R034, Lissajous curve of x =waterlevel [m] y =measured x-velocity, blue V_{x1} , green V_{x2} [m/s]



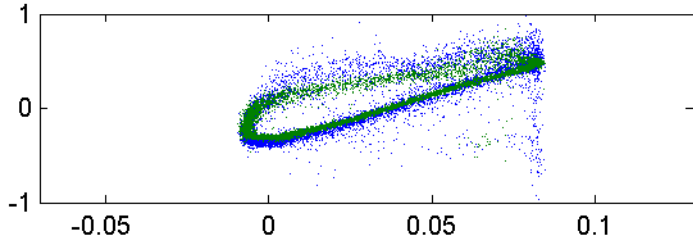
For $x=1.5, y=1$



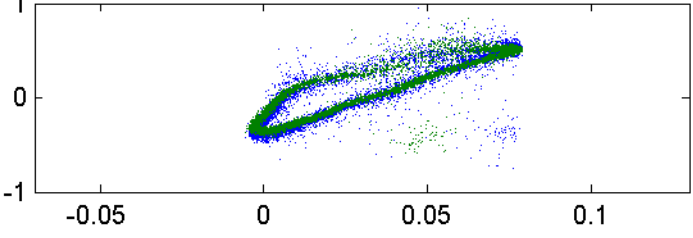
For $x=3.5, y=1$



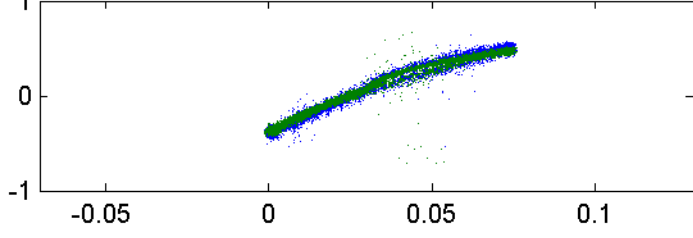
For $x=5.5, y=1$



For $x=7.5, y=1$

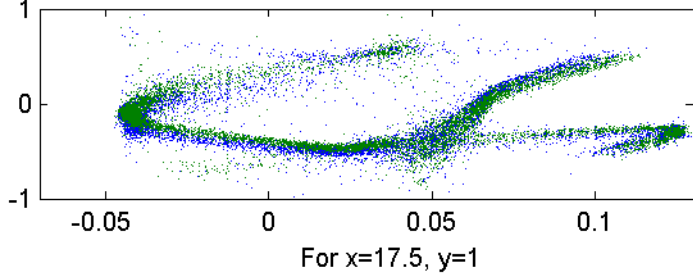
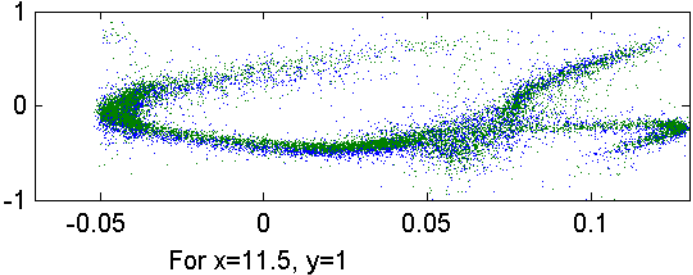
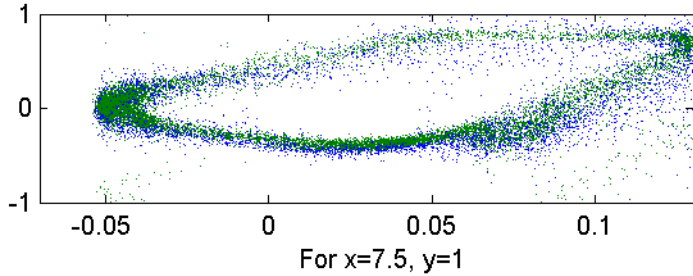
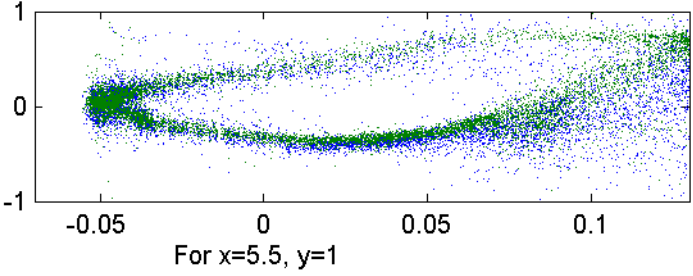
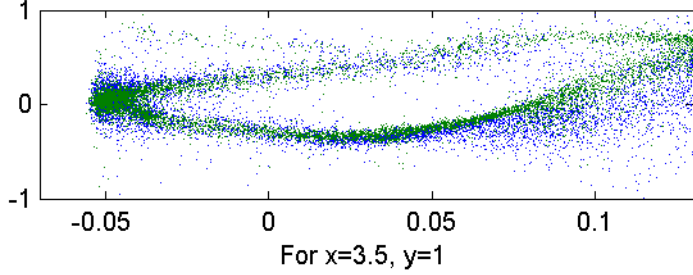
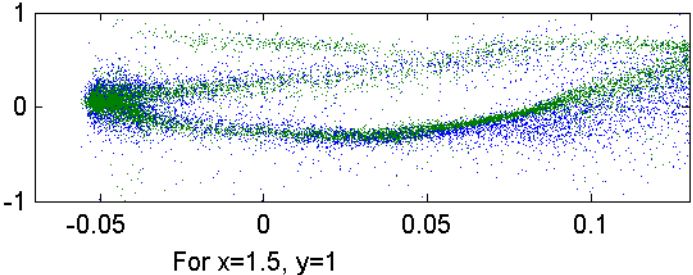


For $x=11.5, y=1$

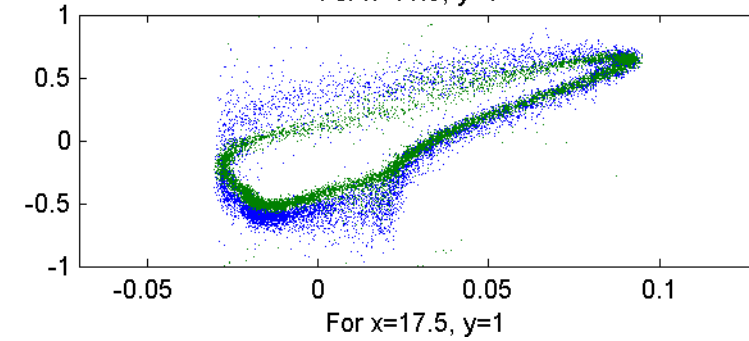
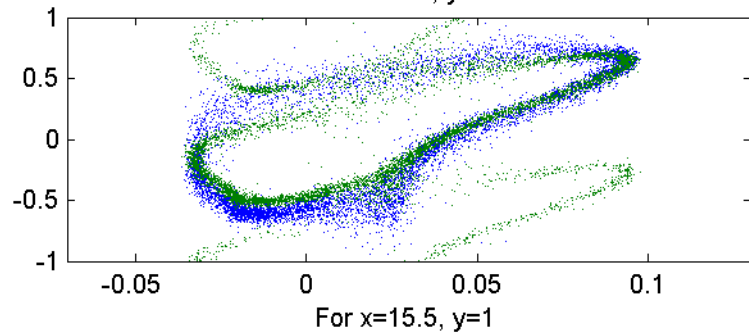
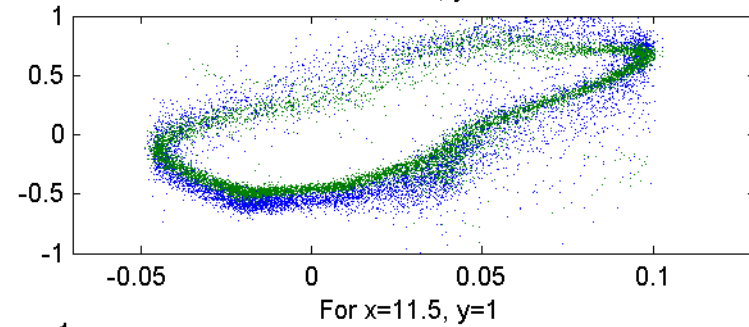
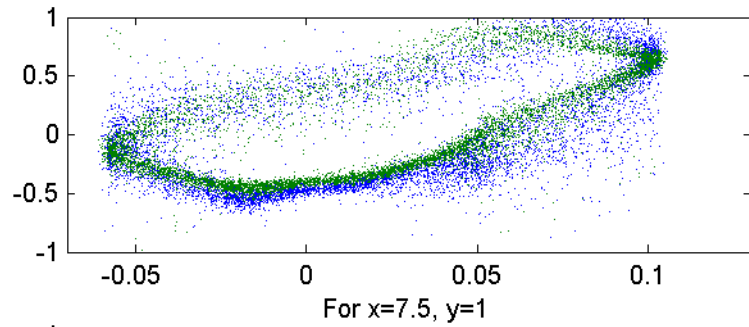
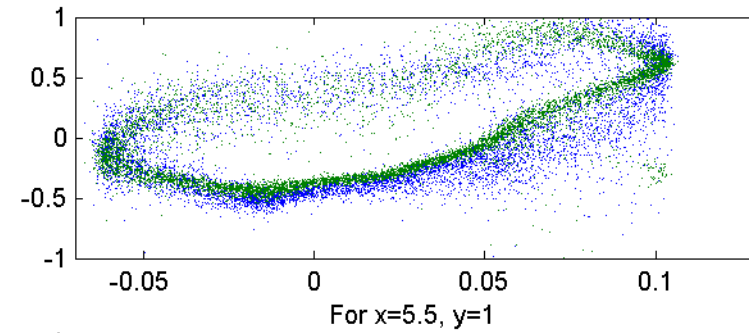
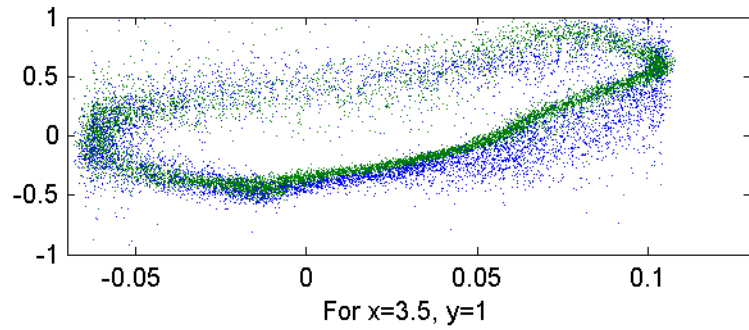


For $x=17.5, y=1$

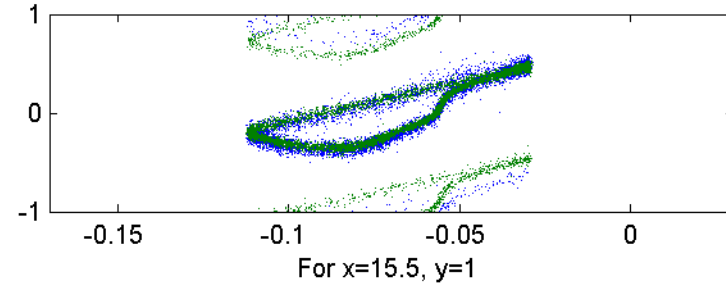
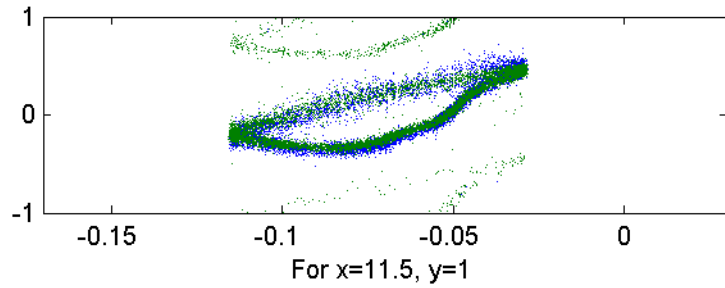
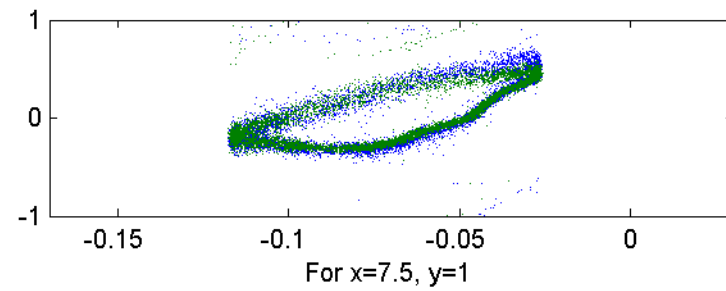
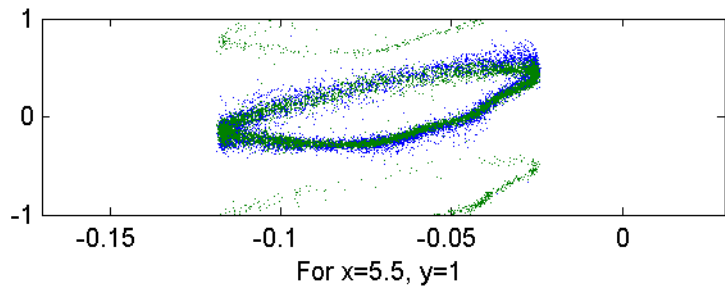
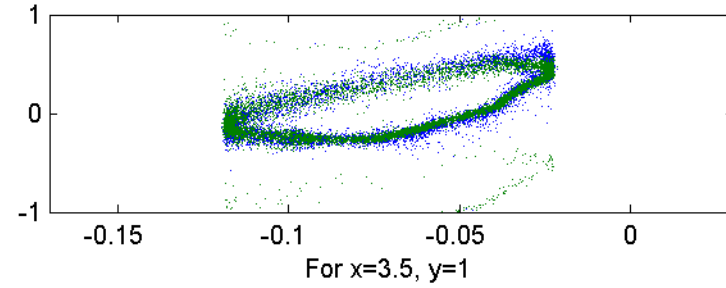
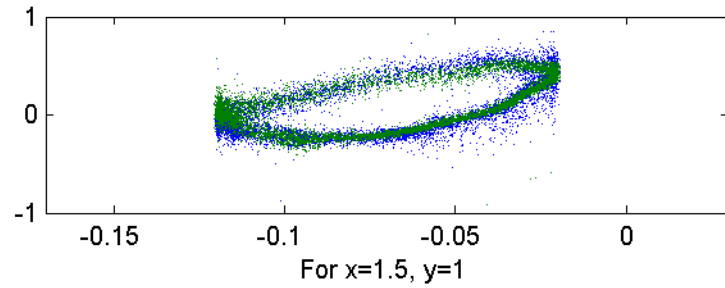
Experiment R035, Lissajous curve of x =waterlevel [m] y =measured x -velocity, blue V_{x1} , green V_{x2} [m/s]



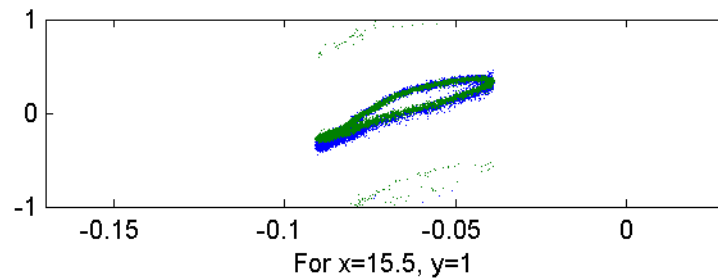
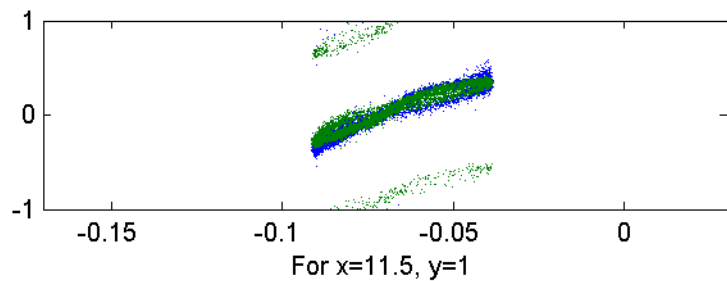
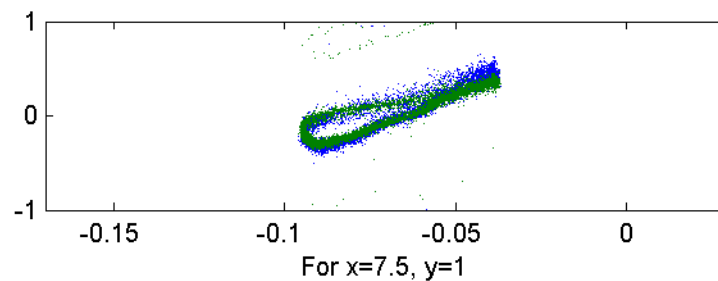
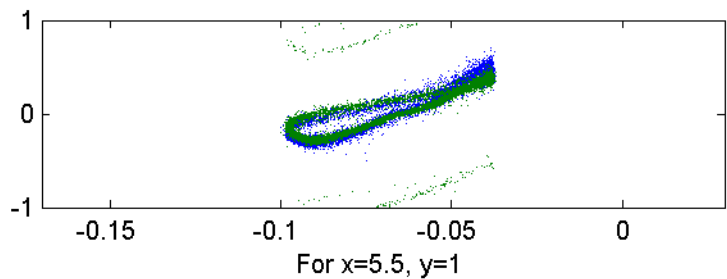
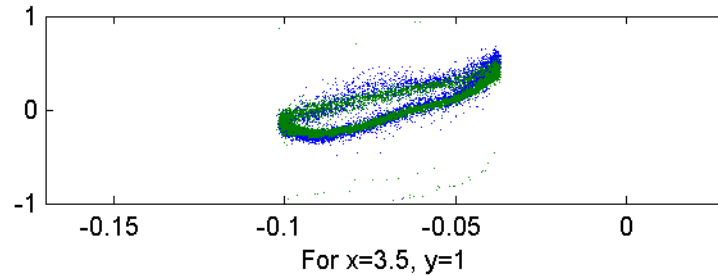
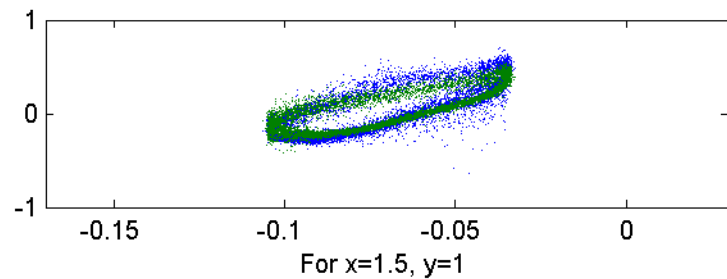
Experiment R036, Lissajous curve of x =waterlevel [m] y =measured x -velocity, blue V_{x1} , green V_{x2} [m/s]



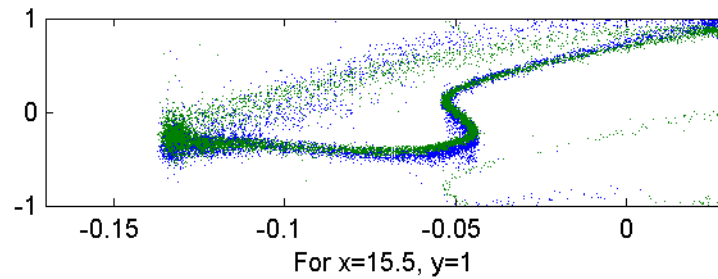
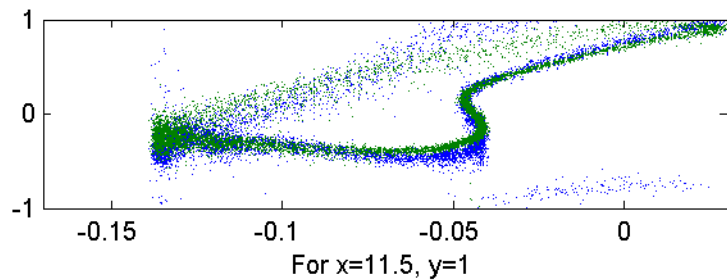
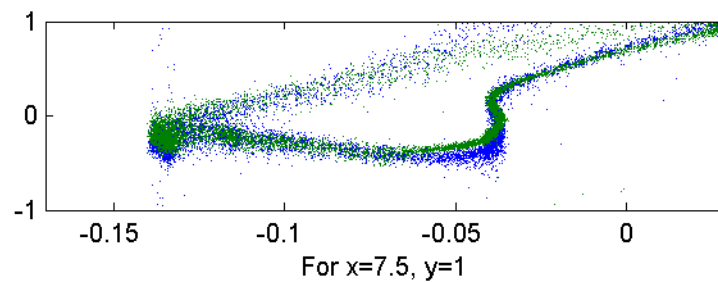
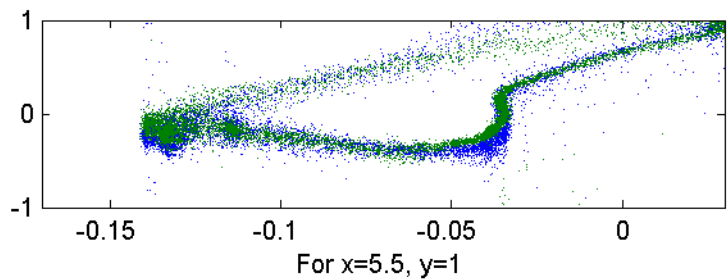
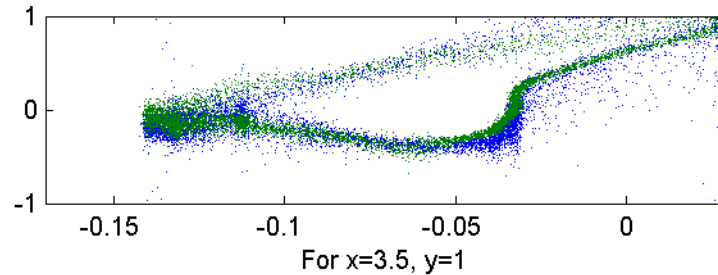
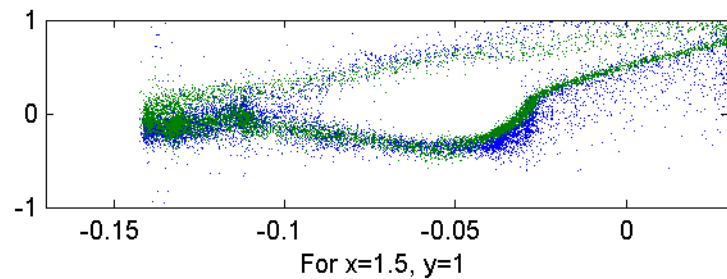
Experiment R037, Lissajous curve of x =waterlevel [m] y =measured x -velocity, blue V_{x1} , green V_{x2} [m/s]



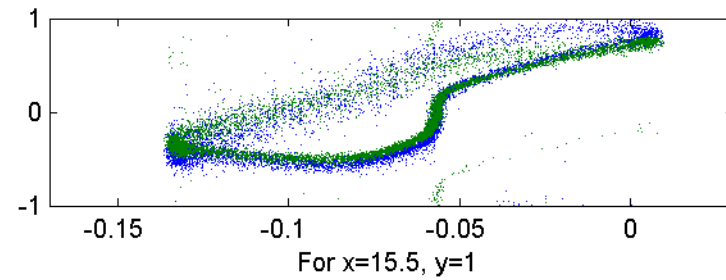
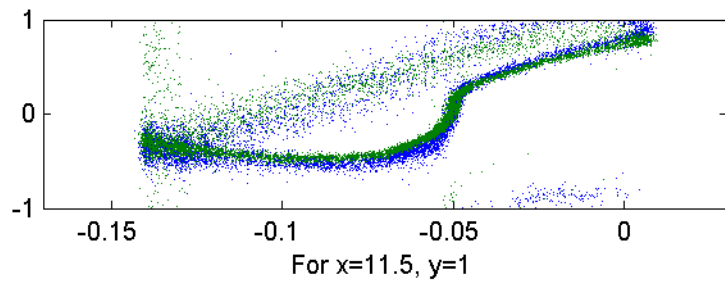
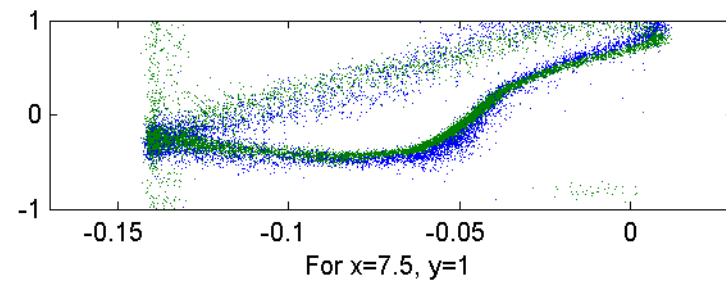
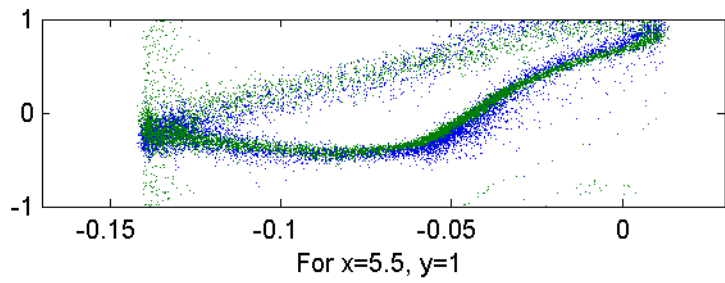
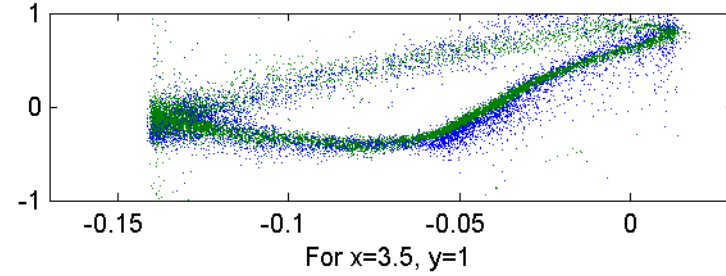
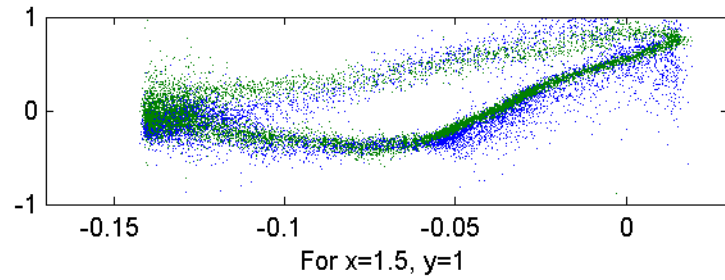
Experiment R038, Lissajous curve of x =waterlevel [m] y =measured x-velocity, blue V_{x1} , green V_{x2} [m/s]



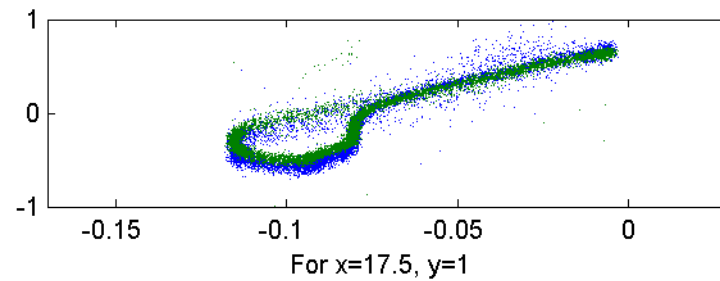
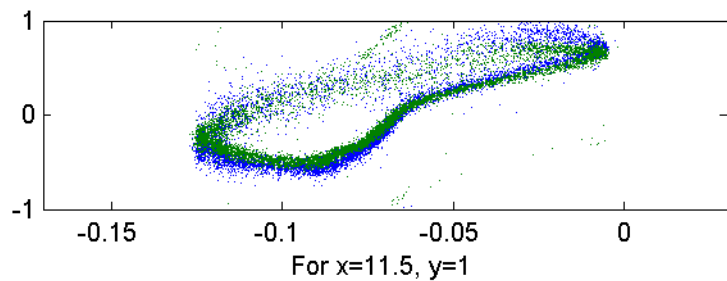
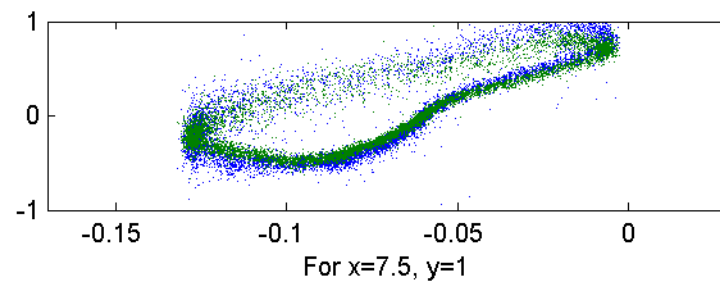
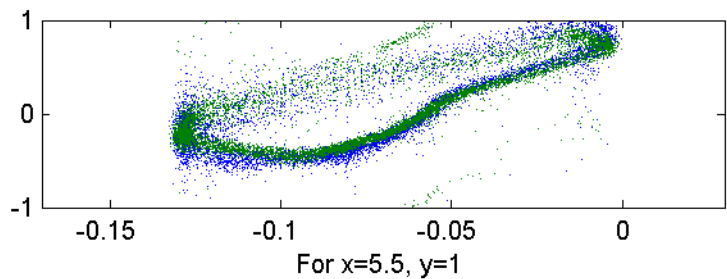
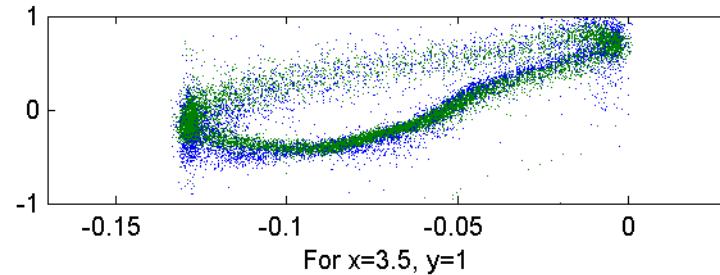
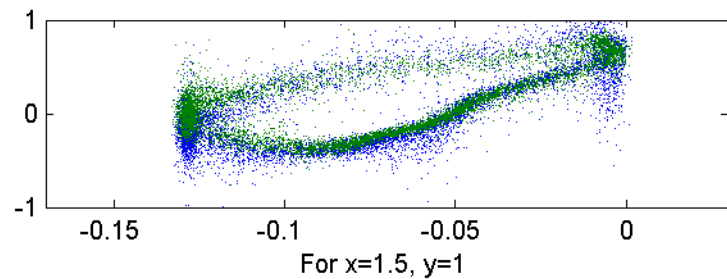
Experiment R039, Lissajous curve of x =waterlevel [m] y =measured x -velocity, blue V_{x1} , green V_{x2} [m/s]



Experiment R040, Lissajous curve of x =waterlevel [m] y =measured x -velocity, blue V_{x1} , green V_{x2} [m/s]



Experiment R041, Lissajous curve of x =waterlevel [m] y =measured x-velocity, blue V_{x1} , green V_{x2} [m/s]



Appendix D – Maximum Velocity Distribution Plots

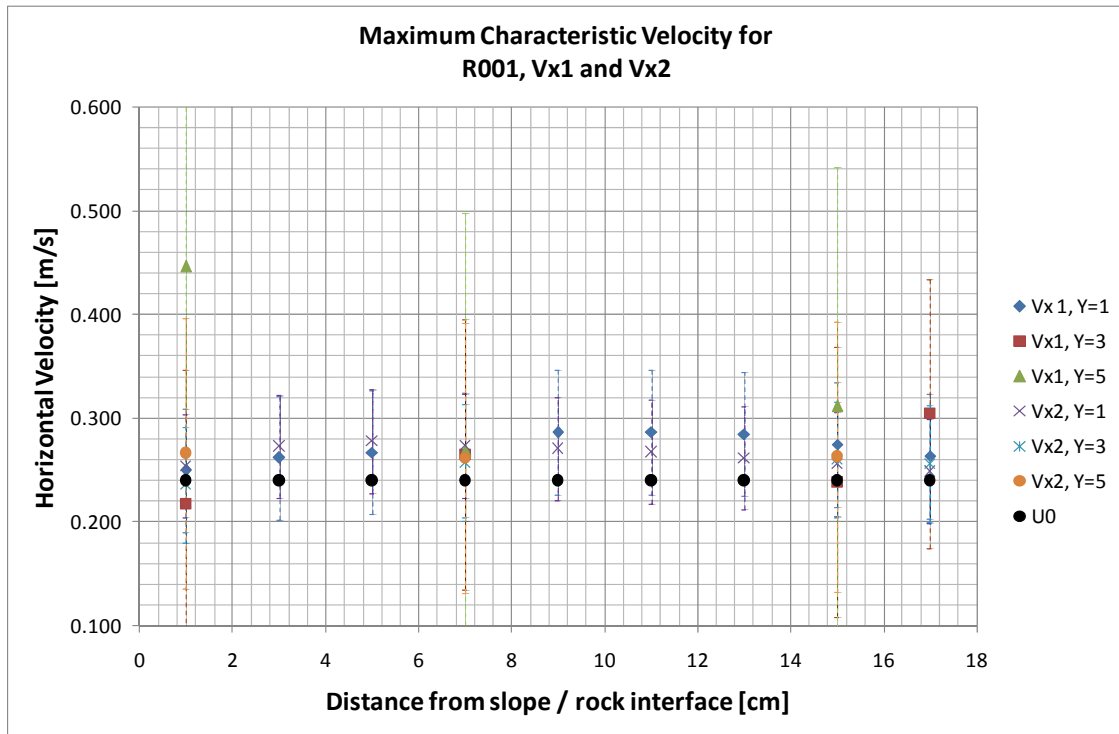


FIGURE 1 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R001

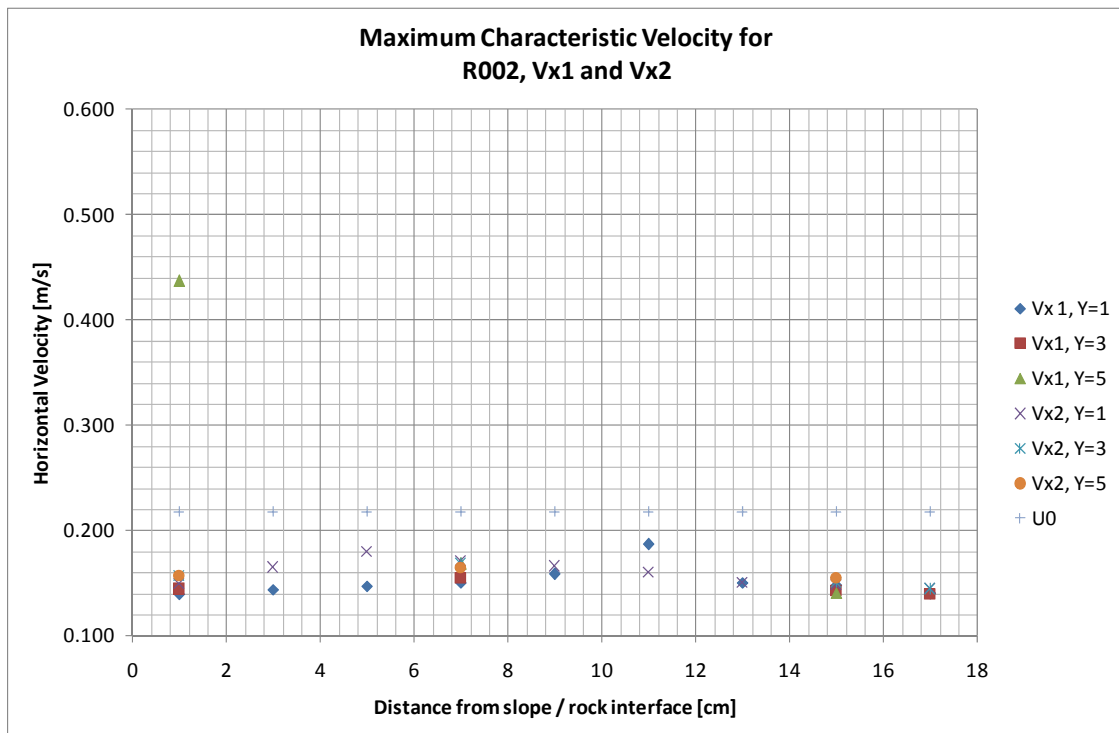


FIGURE 2 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R002

Appendix D – Maximum Velocity Distribution Plots

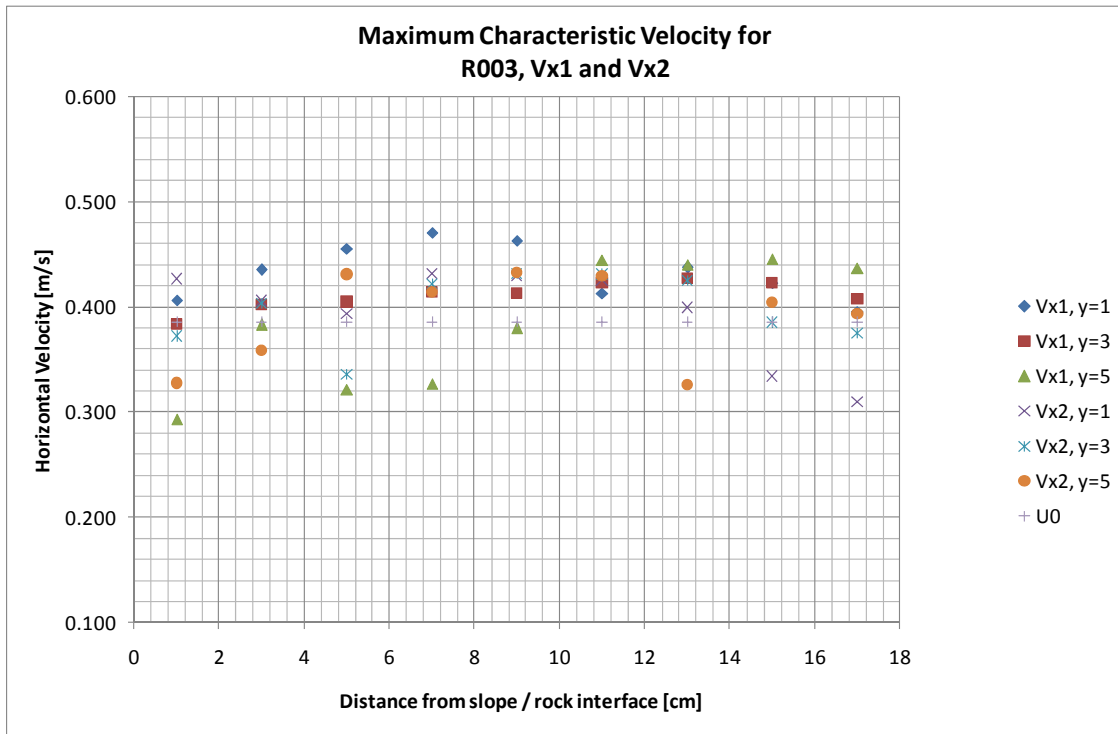


FIGURE 3 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R003

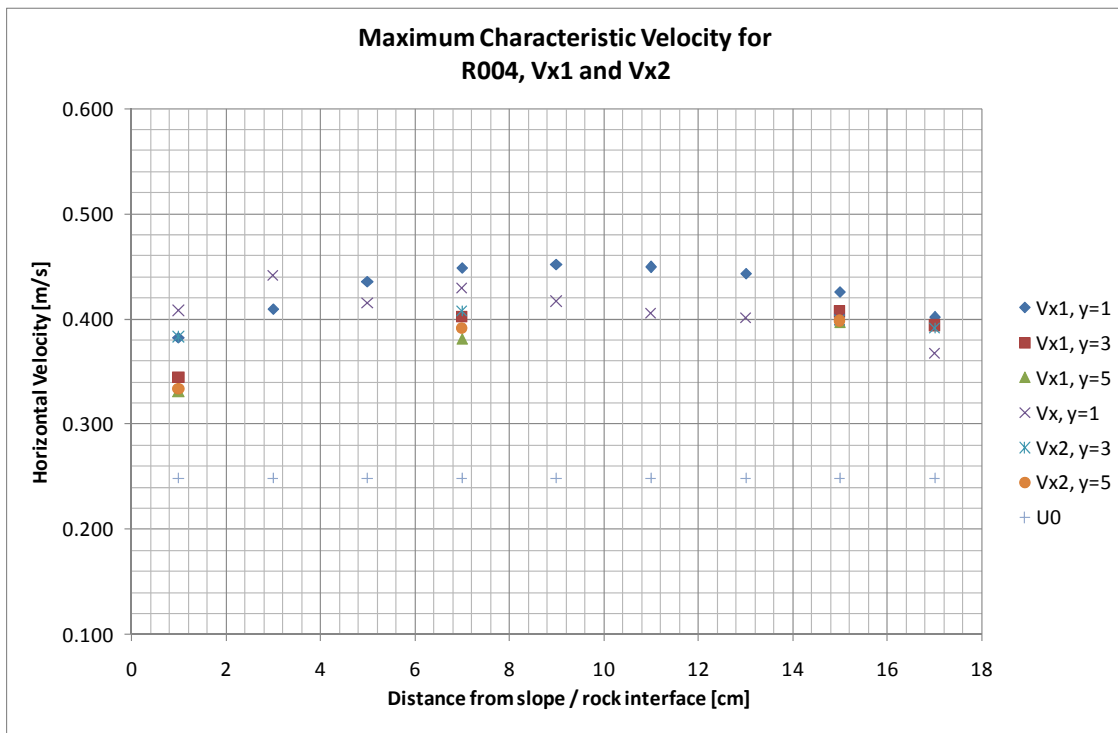


FIGURE 4 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R004

Appendix D – Maximum Velocity Distribution Plots

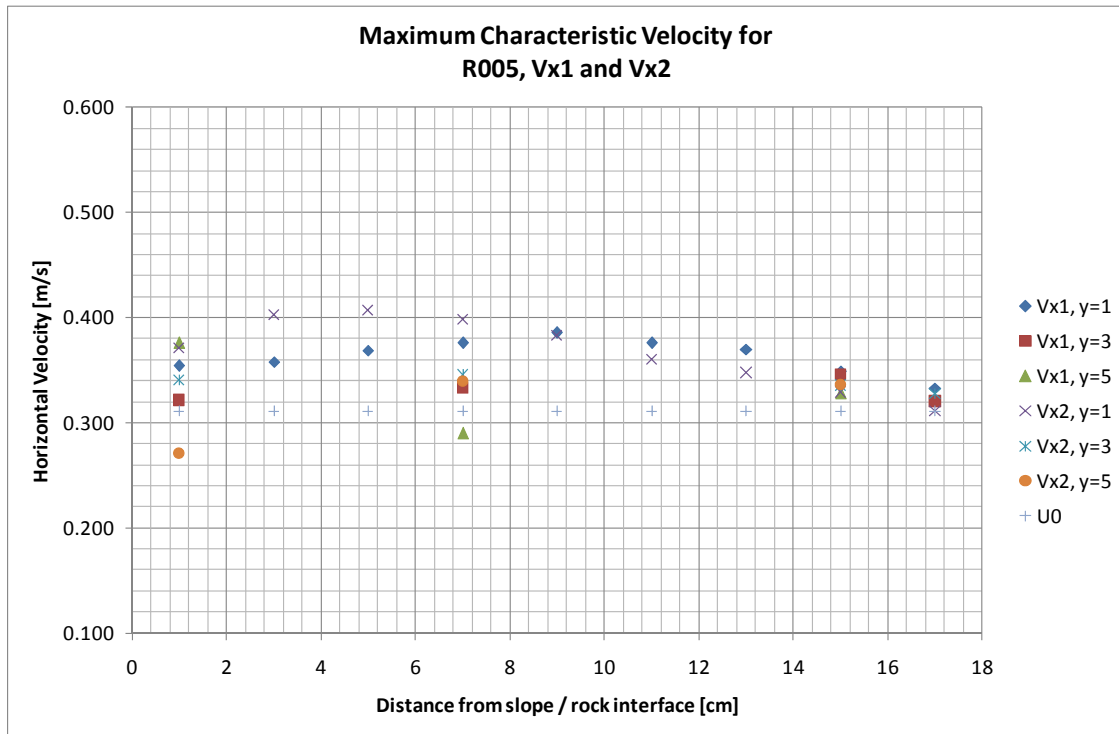


FIGURE 5 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R005

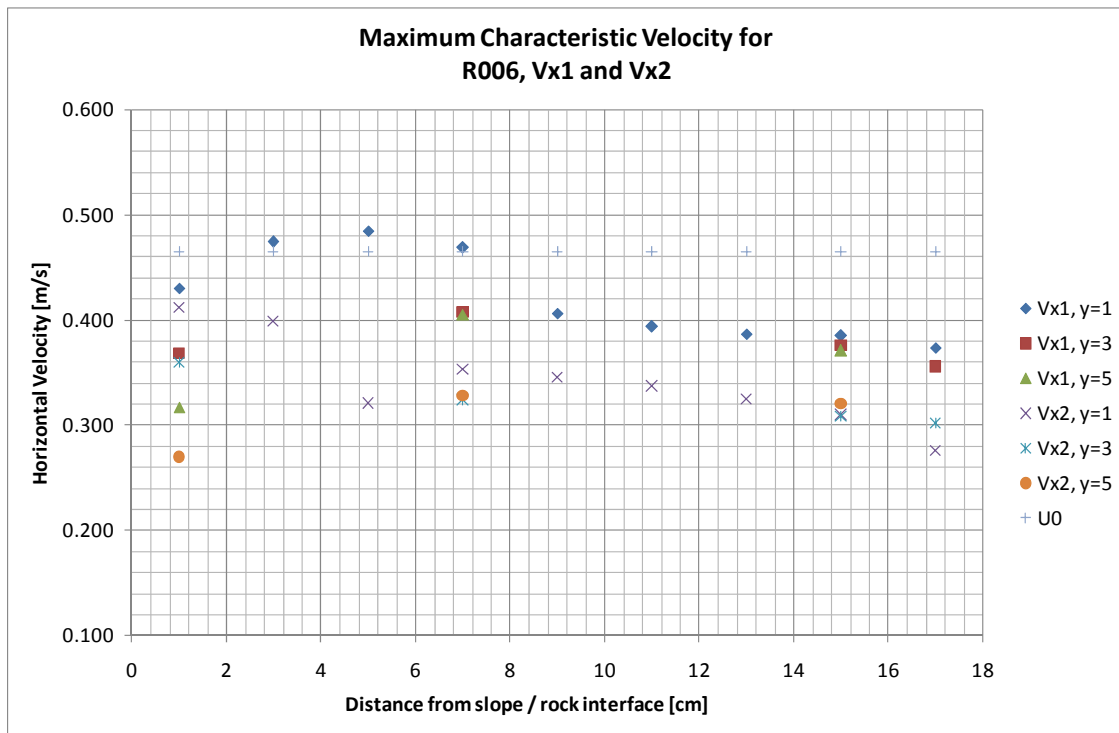


FIGURE 6 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R006

Appendix D – Maximum Velocity Distribution Plots

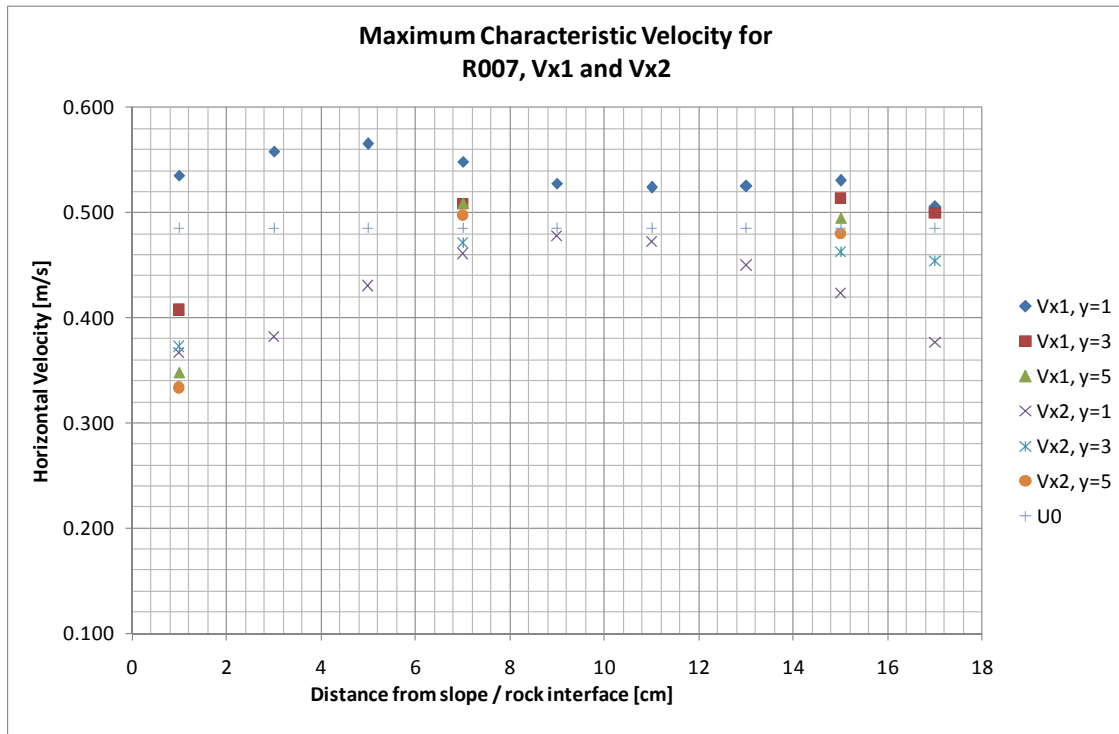


FIGURE 7 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R007

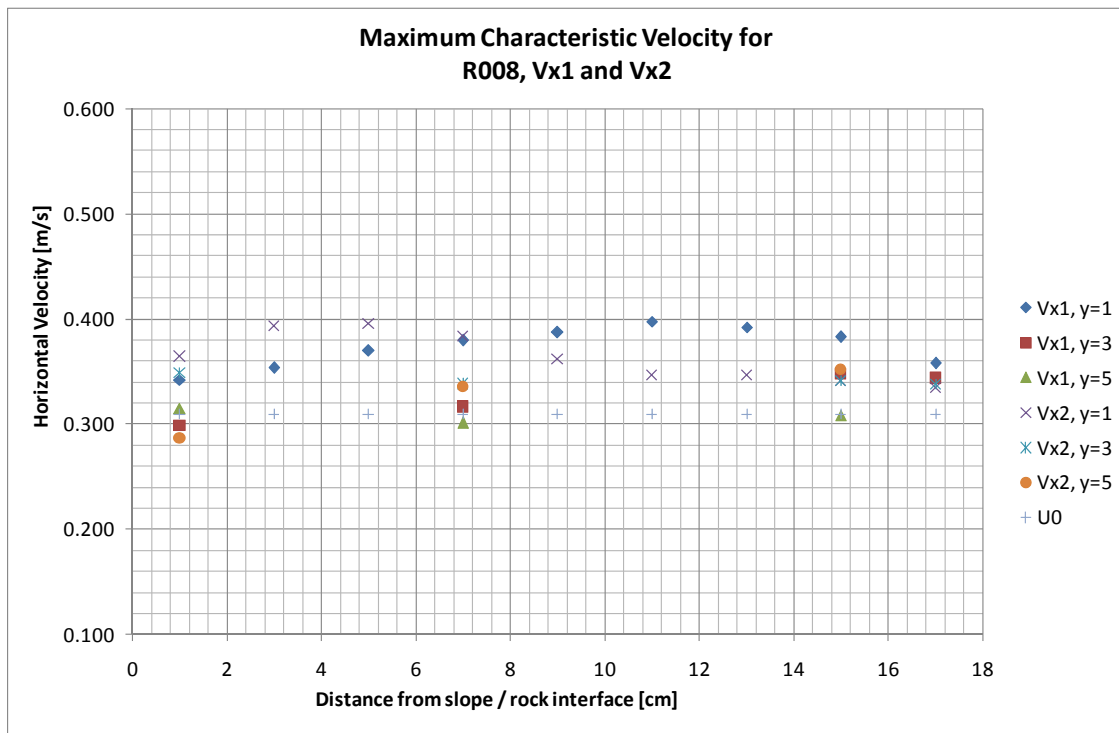


FIGURE 8 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R008

Appendix D – Maximum Velocity Distribution Plots

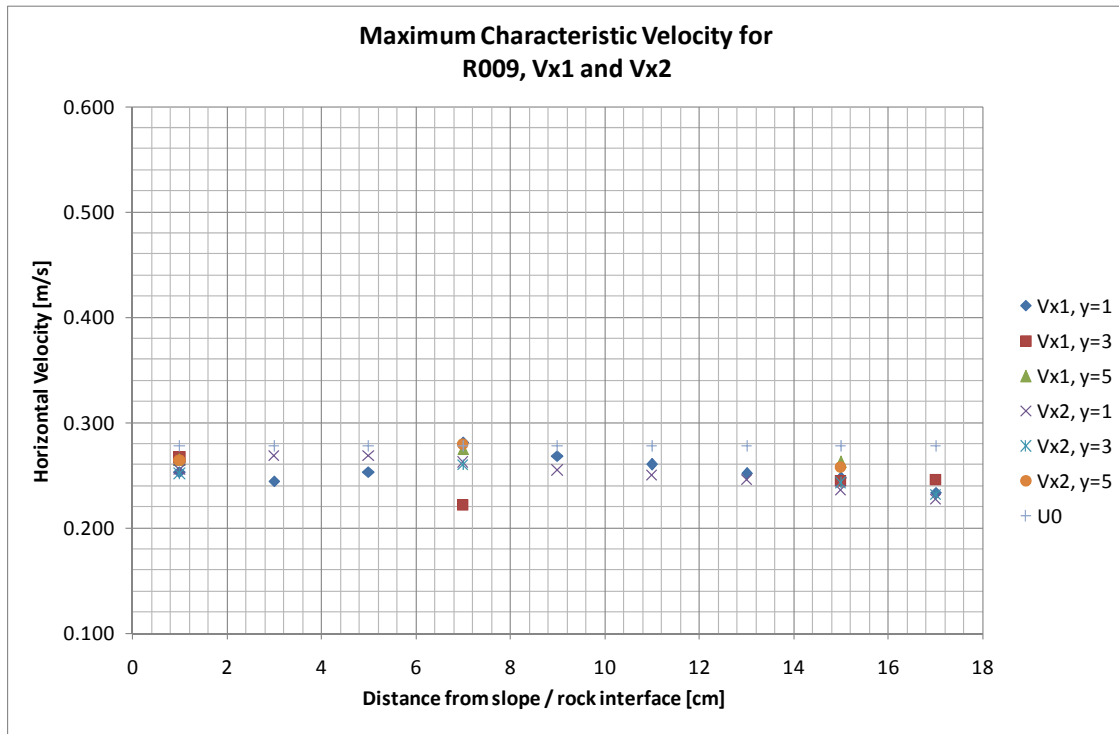


FIGURE 9 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R009

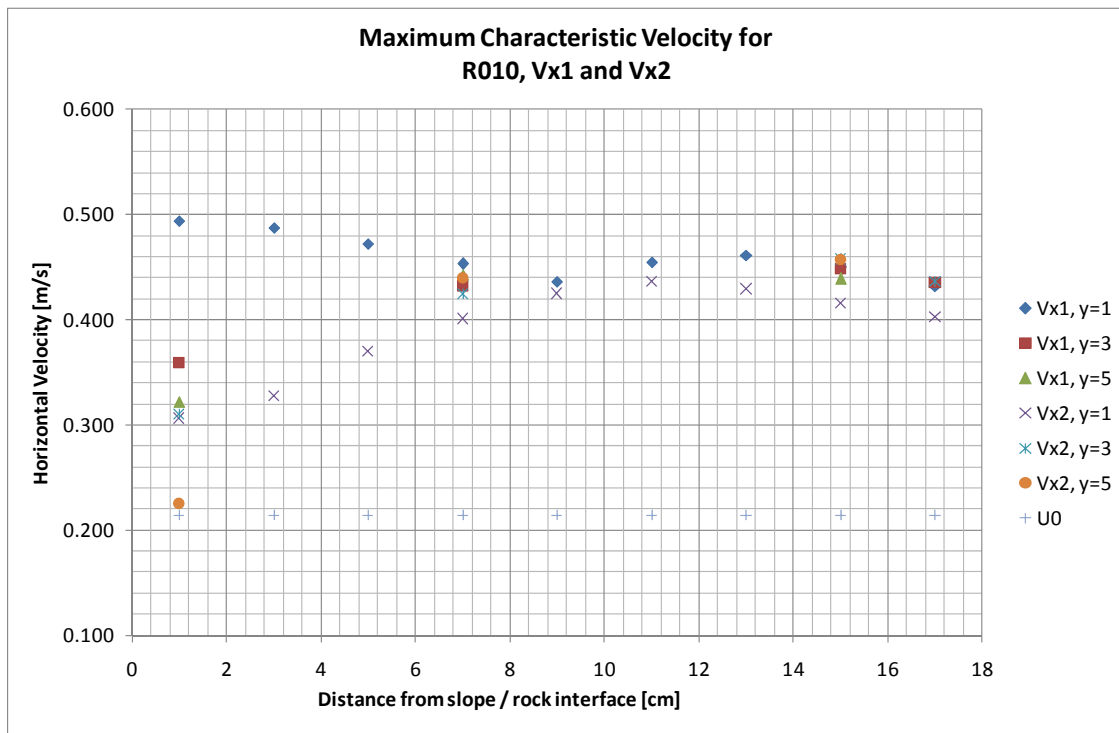


FIGURE 10 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R010

Appendix D – Maximum Velocity Distribution Plots

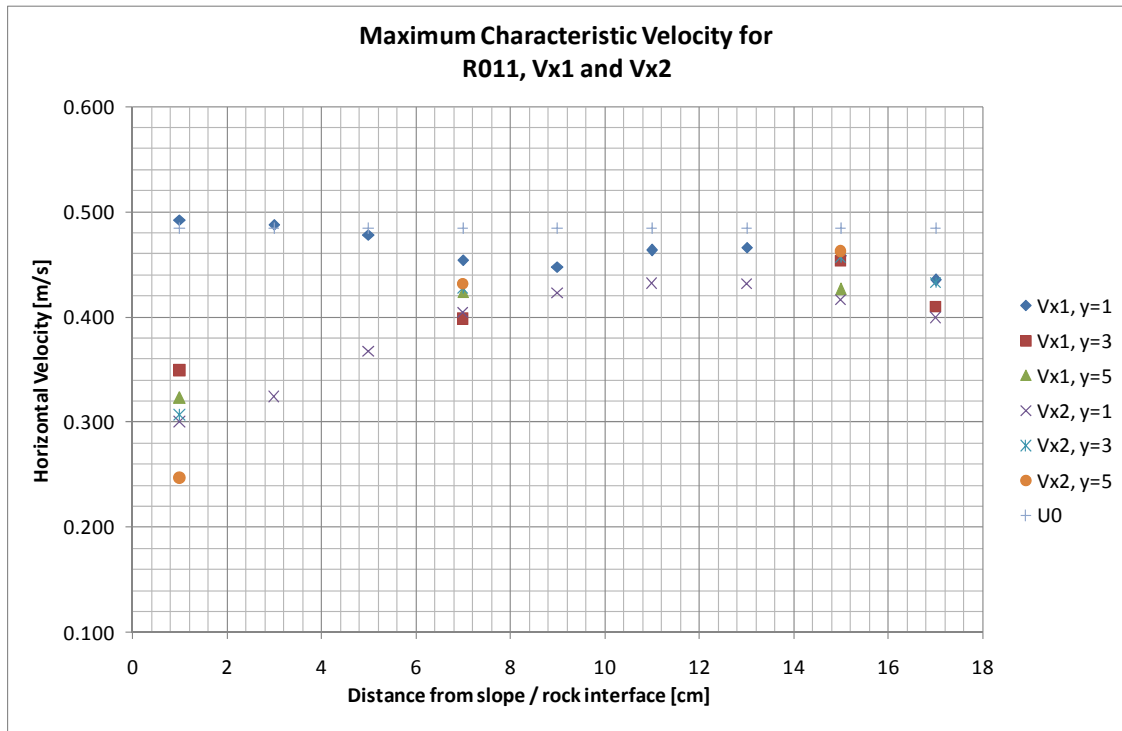


FIGURE 11 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R011

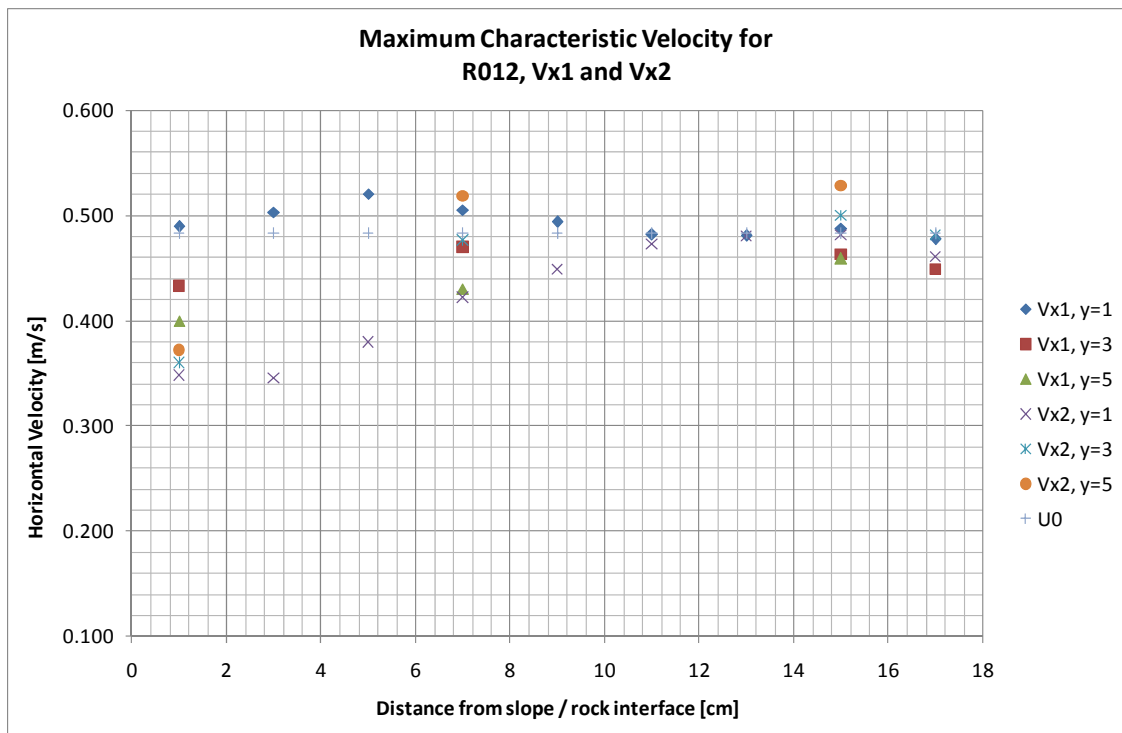


FIGURE 12 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R012

Appendix D – Maximum Velocity Distribution Plots

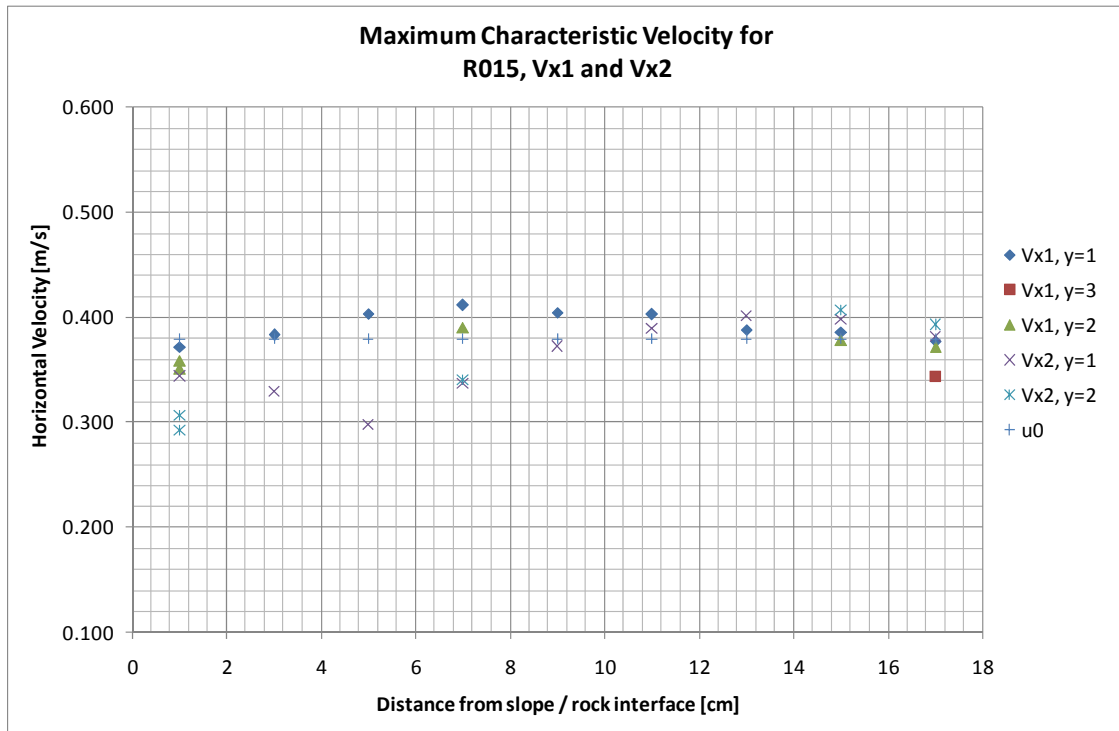


FIGURE 13 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R015

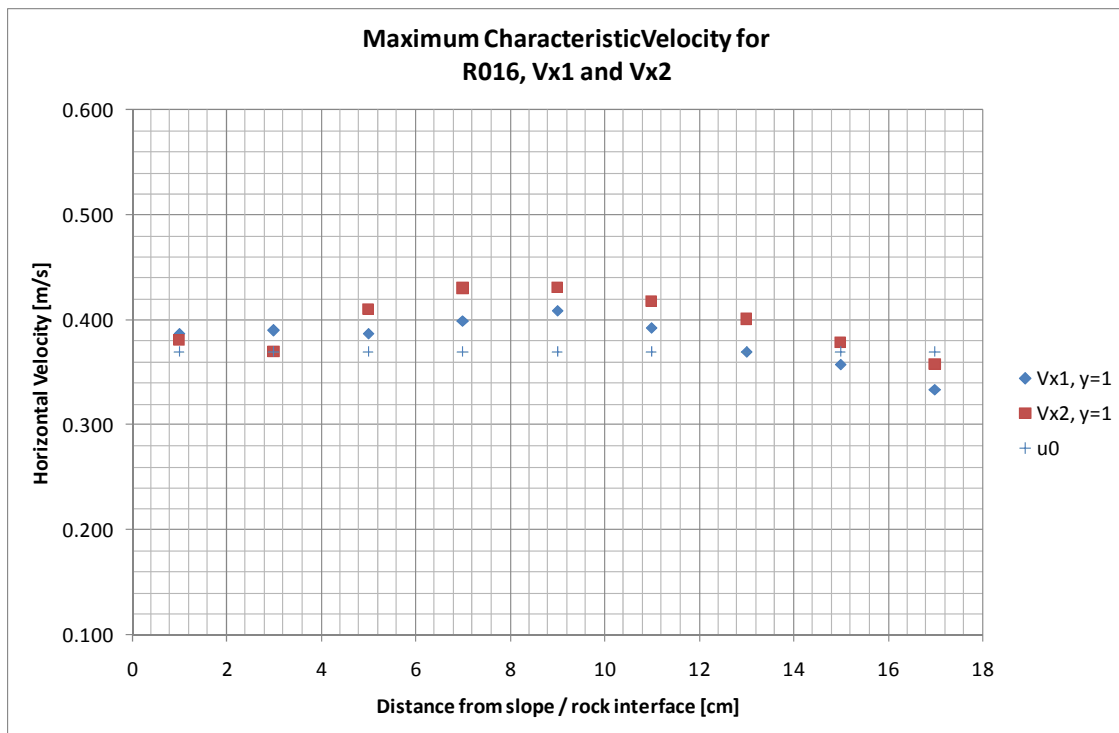


FIGURE 14 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R016

Appendix D – Maximum Velocity Distribution Plots

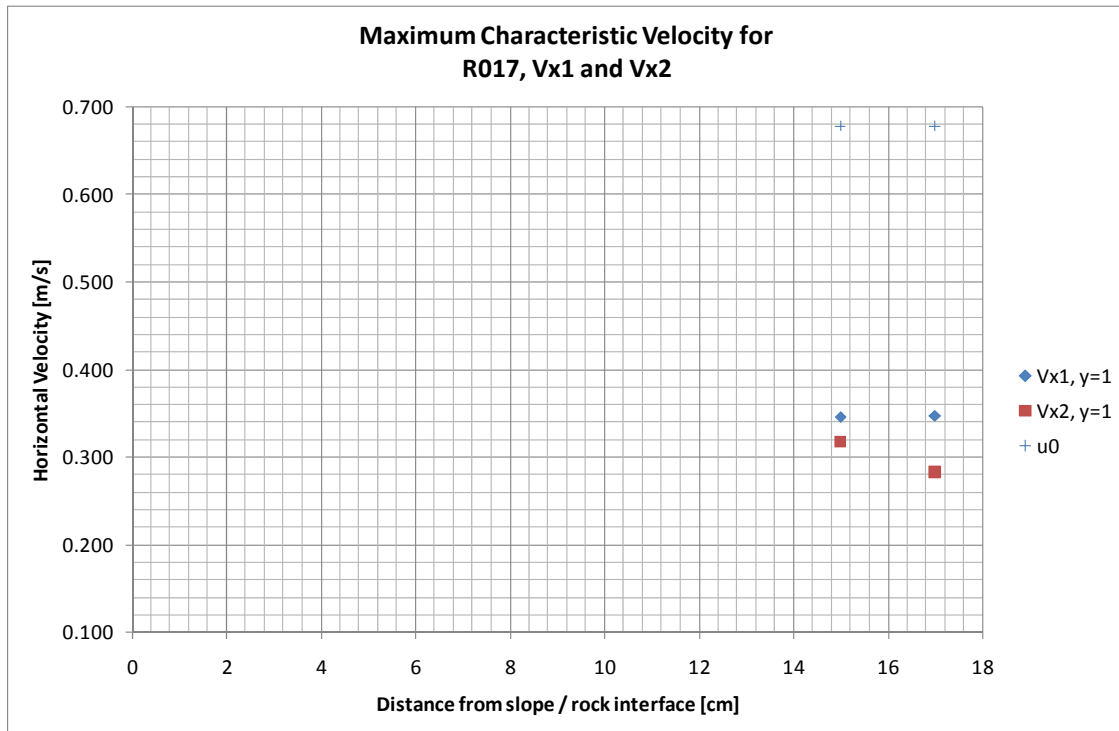


FIGURE 15 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R017

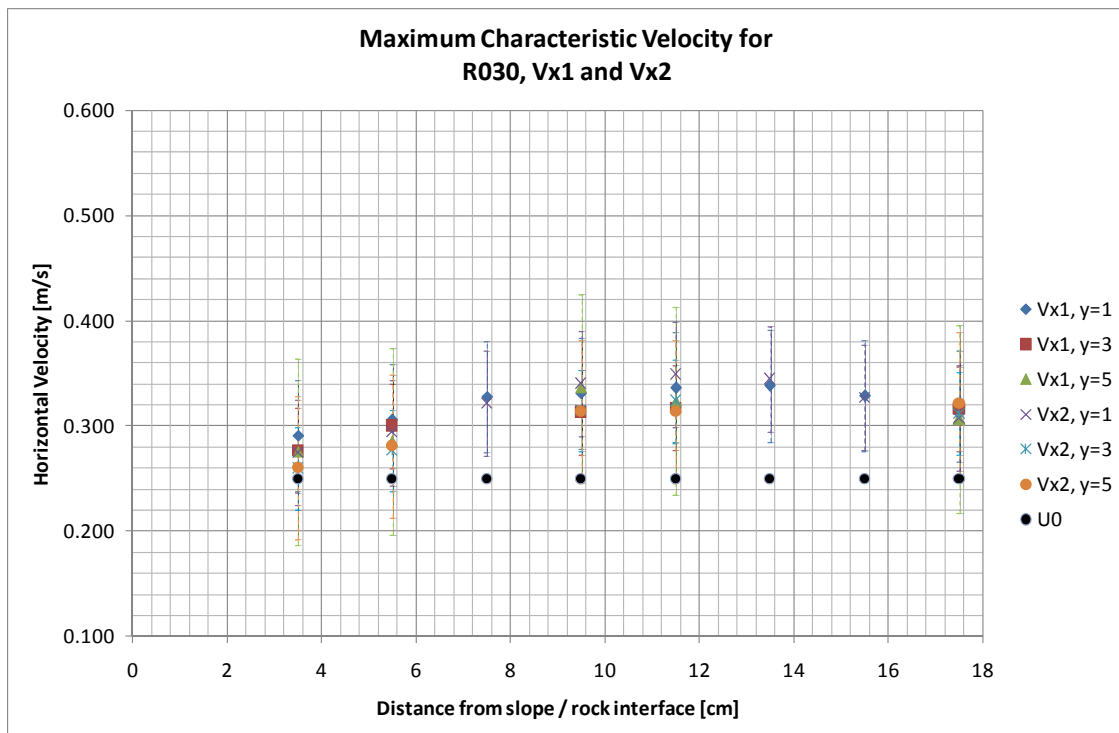


FIGURE 16 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R030

Appendix D – Maximum Velocity Distribution Plots

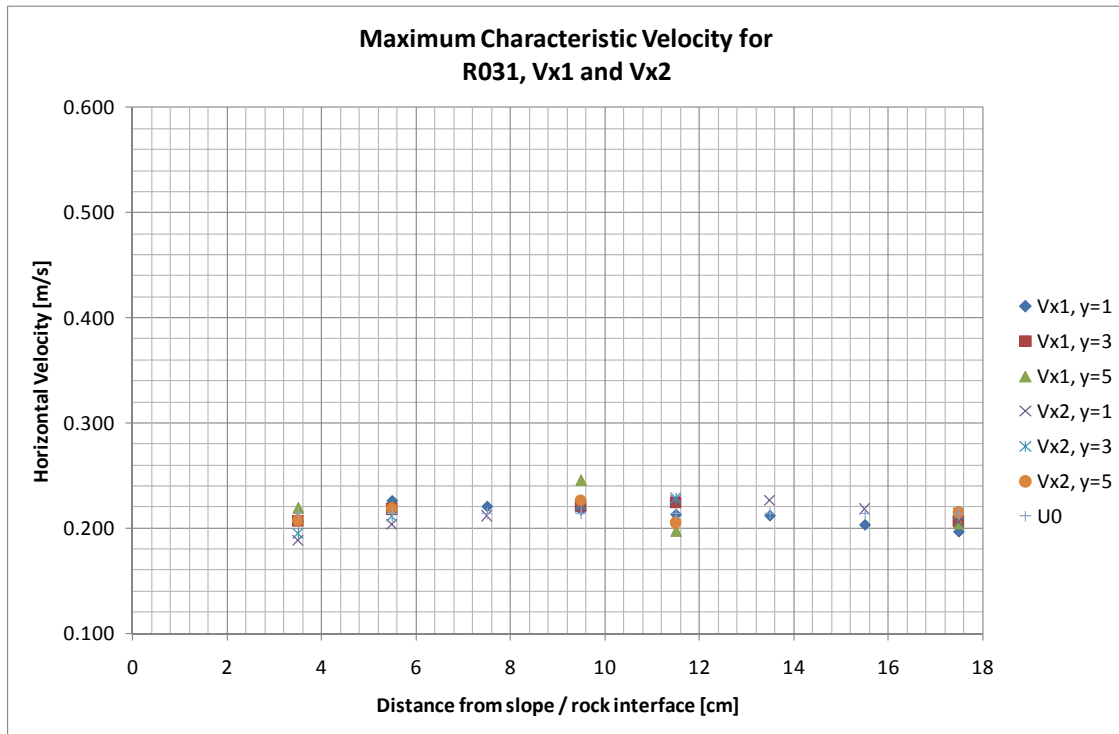


FIGURE 17 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R031

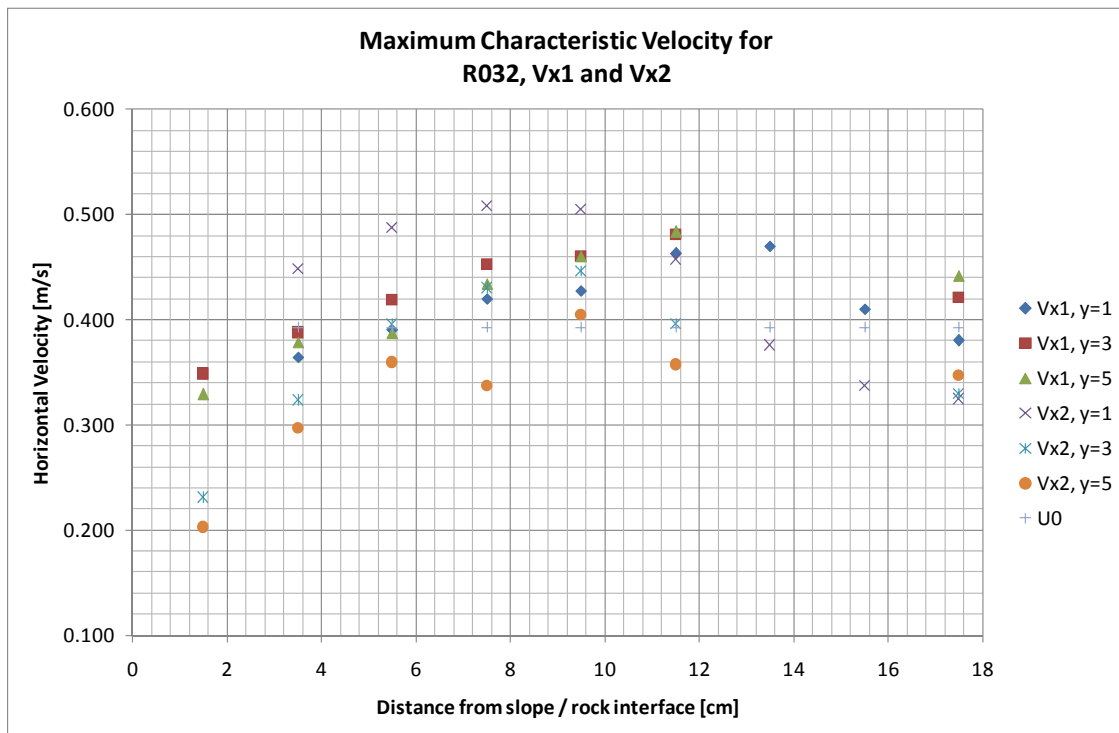


FIGURE 18 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R032

Appendix D – Maximum Velocity Distribution Plots

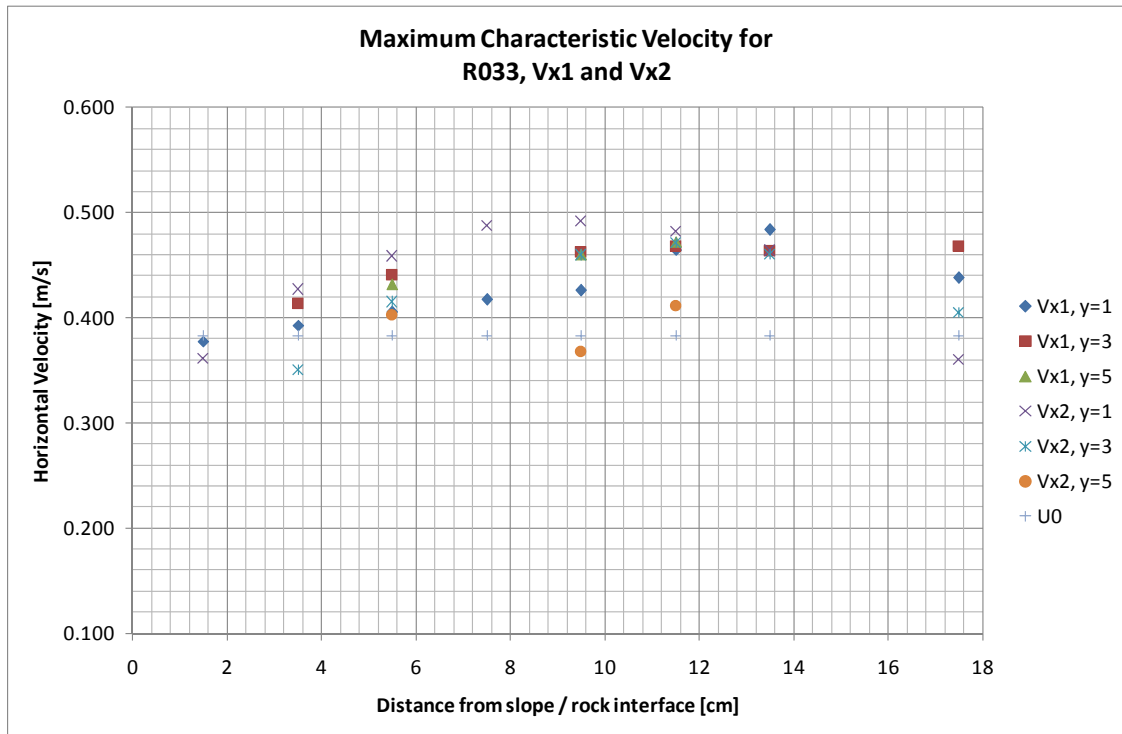


FIGURE 19 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R033

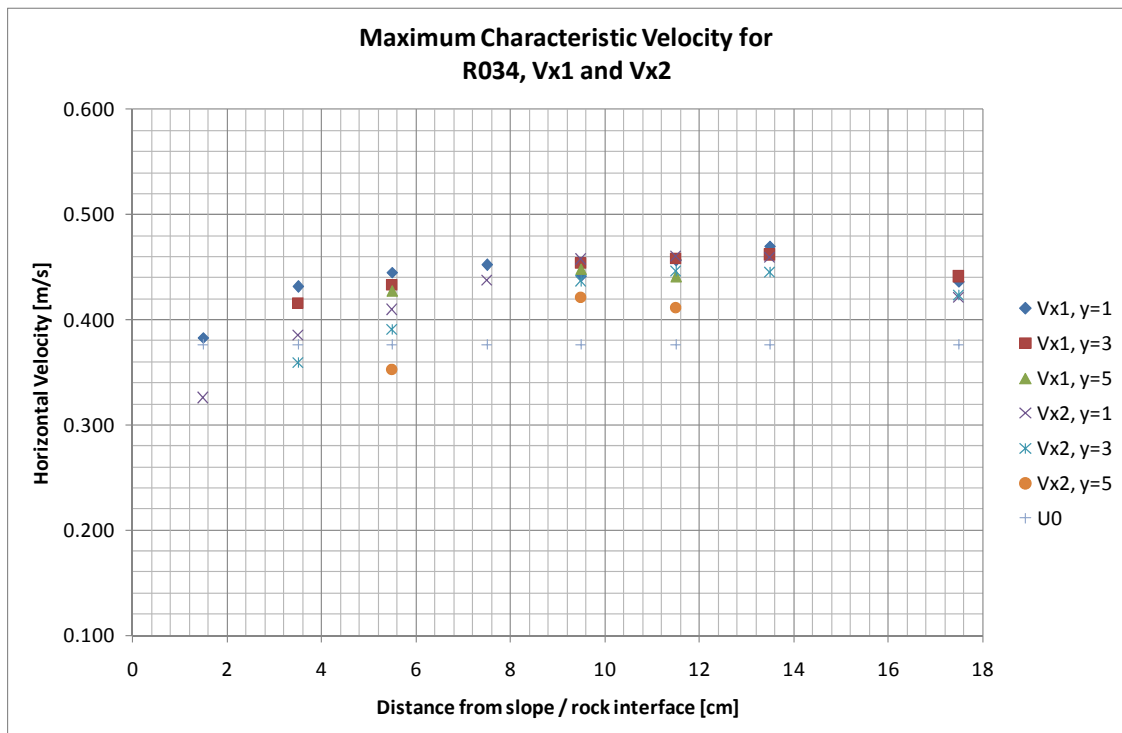


FIGURE 20 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R034

Appendix D – Maximum Velocity Distribution Plots

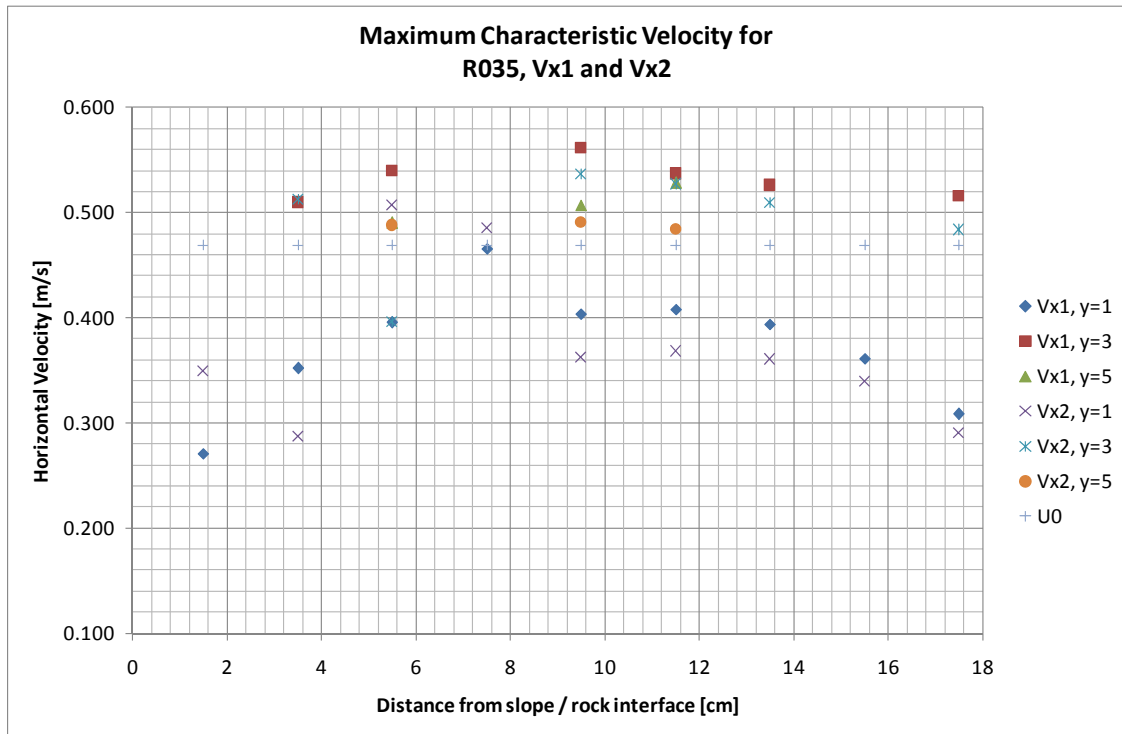


FIGURE 21 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R035

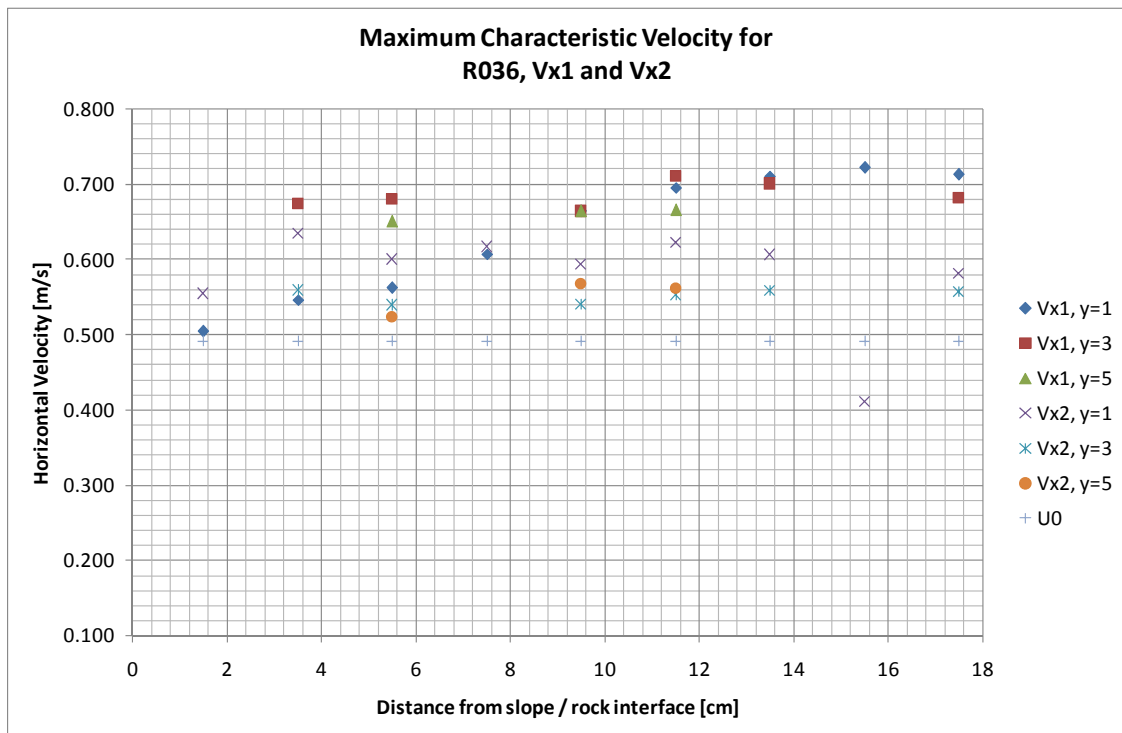


FIGURE 22 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R036

Appendix D – Maximum Velocity Distribution Plots

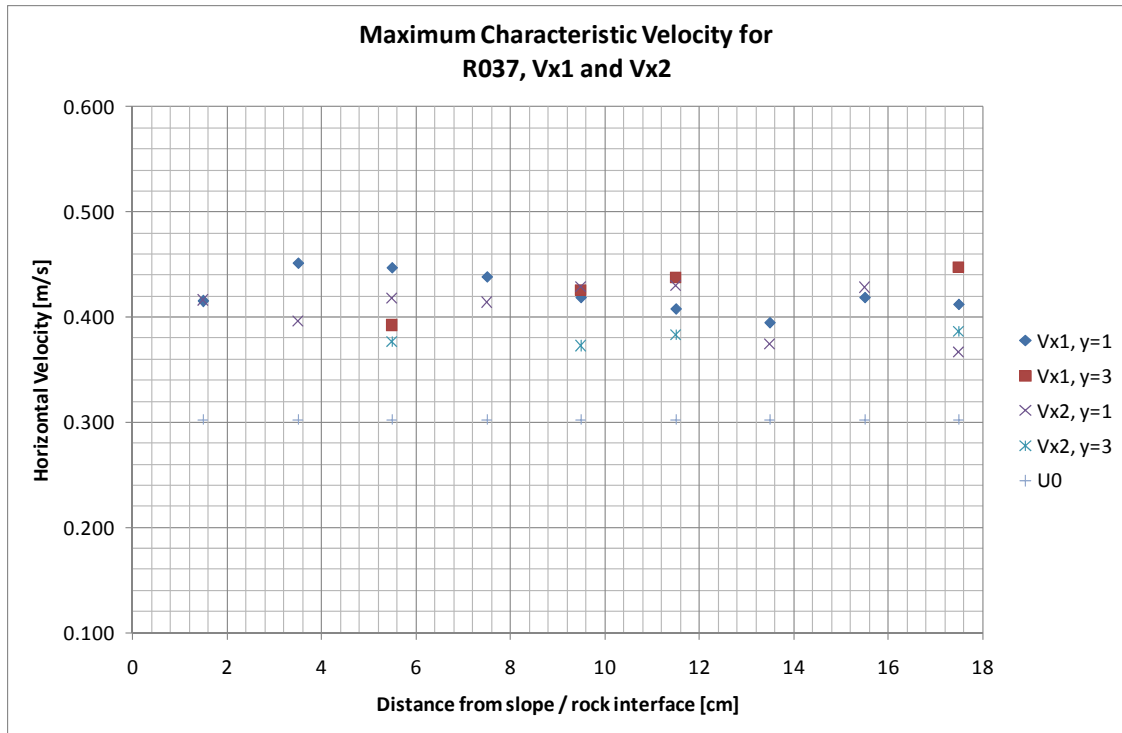


FIGURE 23 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R037

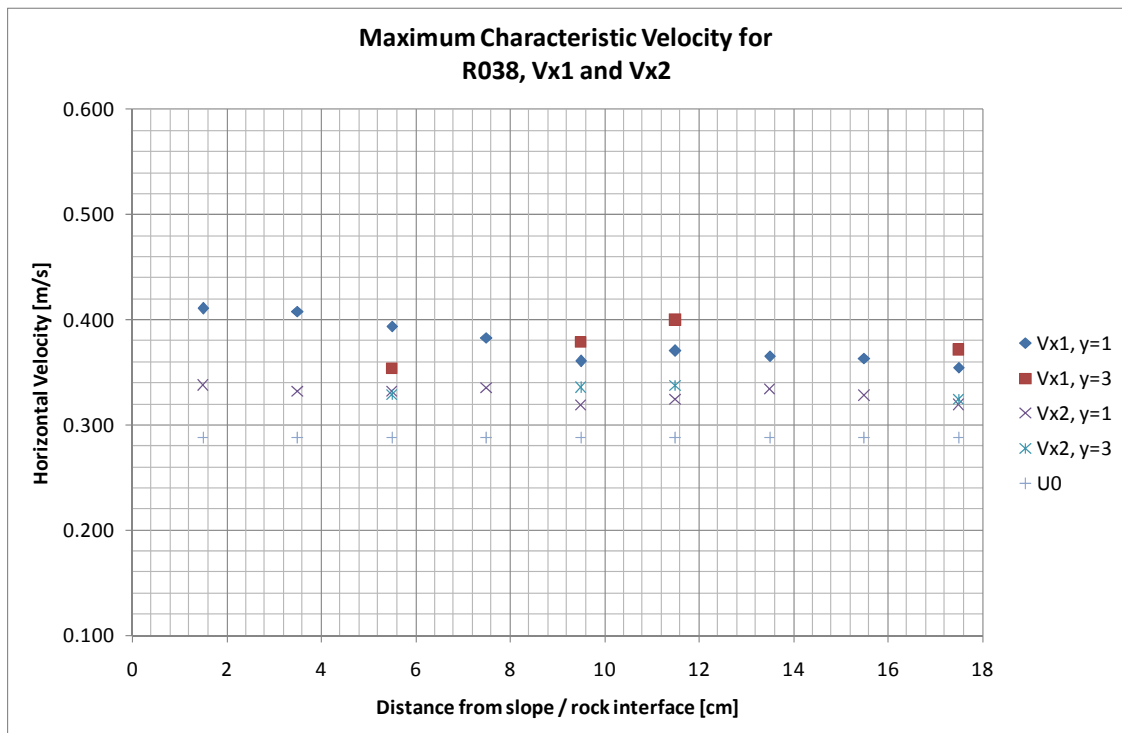


FIGURE 24 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R038

Appendix D – Maximum Velocity Distribution Plots

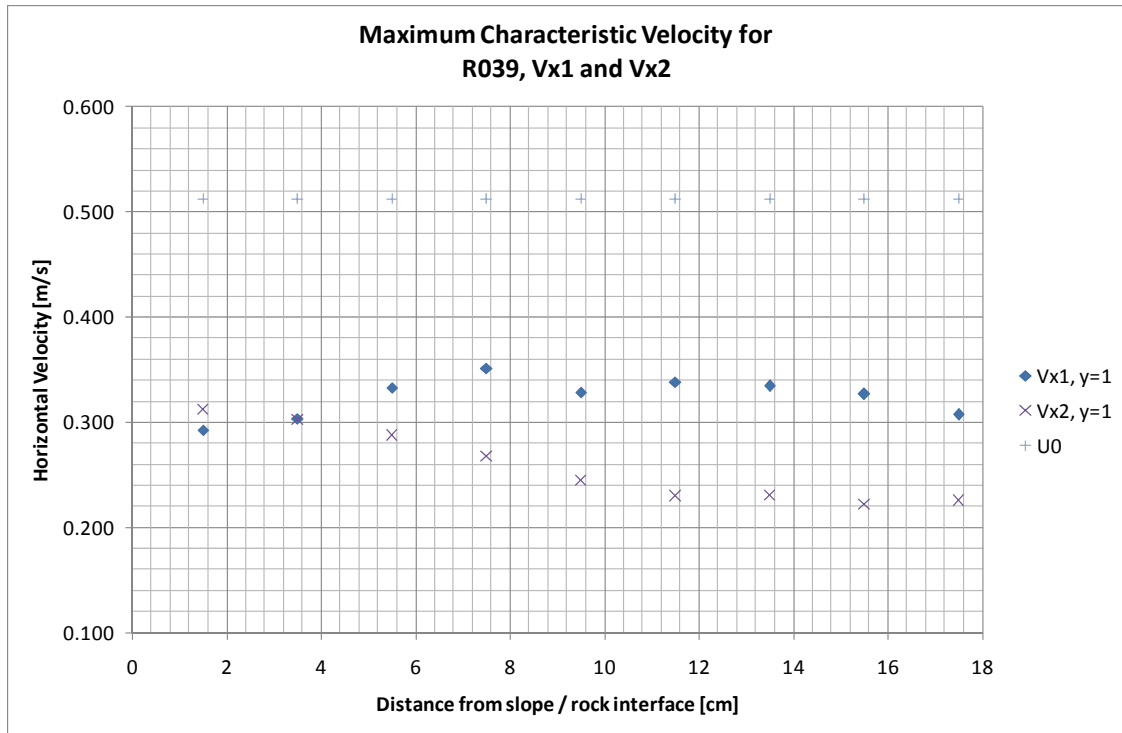


FIGURE 25 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R039

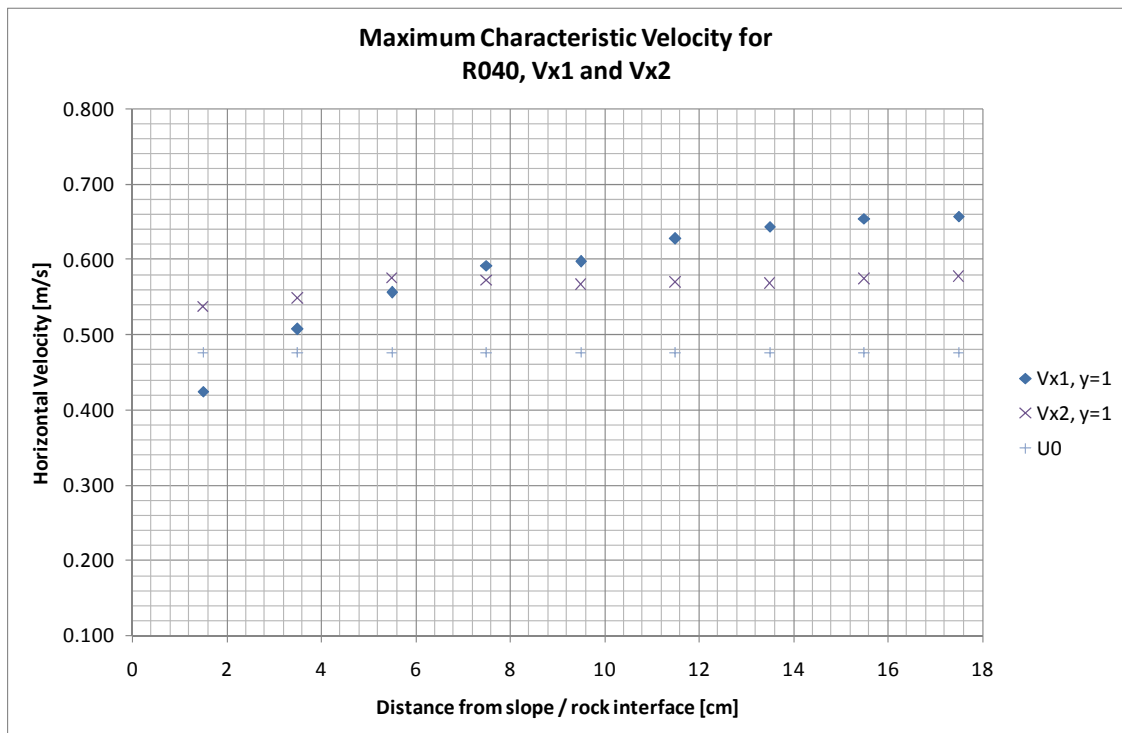


FIGURE 26 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R040

Appendix D – Maximum Velocity Distribution Plots

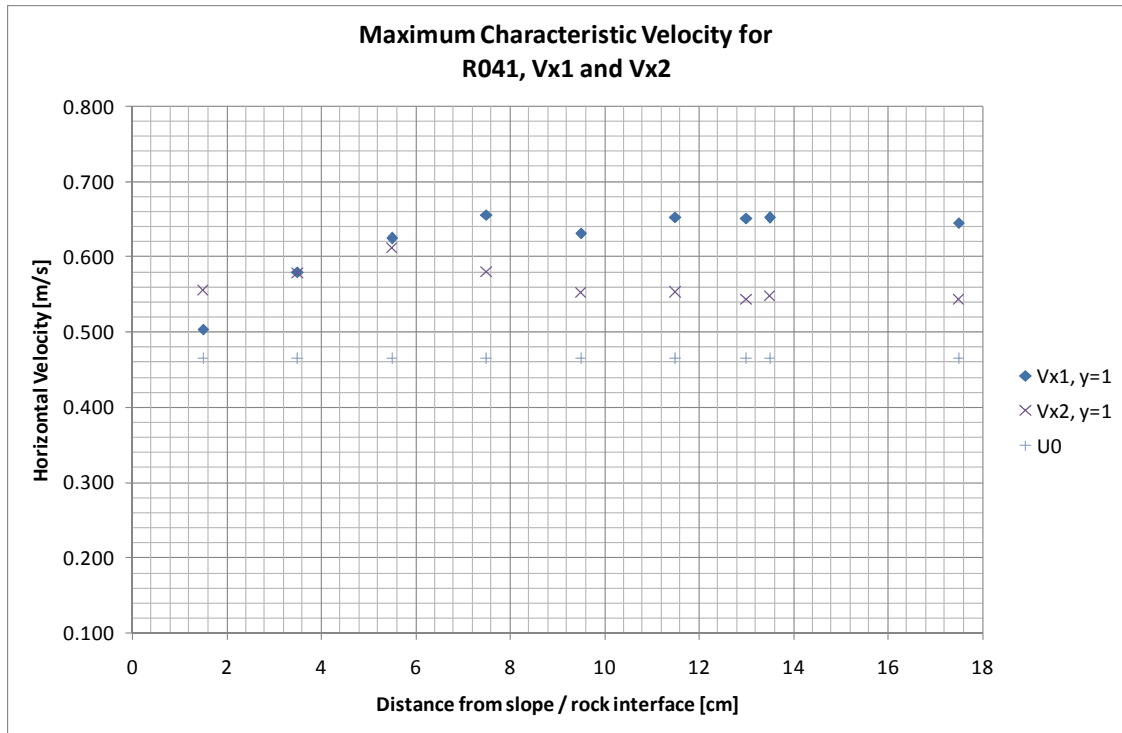


FIGURE 27 - PLOT OF MAXIMUM VELOCITY DISTRIBUTION AT TOE FOR EXPERIMENT R041