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## Article

# The Mechanical Properties and Elastic Anisotropy of $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn Intermetallic Compounds

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**Abstract:** Full intermetallic compound (IMC) solder joints present fascinating advantages in high-temperature applications. In this study, the mechanical properties and elastic anisotropy of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn intermetallic compounds were investigated using first-principles calculations. The values of single-crystal elastic constants, the elastic ( $E$ ), shear ( $G$ ), and bulk ( $B$ ) moduli, and Poisson's ratio ( $\nu$ ) were identified. In addition, the two values of  $G/B$  and  $\nu$  indicated that the two IMCs were ductile materials. The elastic anisotropy of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> was found to be higher than Cu<sub>3</sub>Sn by calculating the universal anisotropic index. Furthermore, an interesting discovery was that the above two types of monocrystalline IMC exhibited mechanical anisotropic behavior. Specifically, the anisotropic degree of  $E$  and  $B$  complied with the following relationship:  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> > Cu<sub>3</sub>Sn; however, the relationship was Cu<sub>3</sub>Sn >  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> for the  $G$ . It is noted that the anisotropic degree of  $E$  and  $G$  was similar for the two IMCs. In addition, the anisotropy of the  $B$  was higher than the  $G$  and  $E$ , respectively, for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub>; however, in the case of Cu<sub>3</sub>Sn, the anisotropic degree of  $B$ ,  $G$ , and  $E$  was similar.

**Keywords:** mechanical properties; elastic anisotropy; intermetallic compounds; first-principles calculates

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## 1. Introduction

The application of high-powered electronic equipment and third-generation semiconductor power devices is currently widespread and requires high service temperatures (>250 °C) for solder joints [1,2]. The two common tin-based intermetallic compounds (IMCs) are Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn, the melting point of which is 415 and 676 °C, respectively [3], and both have excellent thermodynamic and kinetic stability [1,4,5]. As such, full IMC solder joints have fascinating advantages in high-temperature application fields. Concurrently, the volume and mass of these solder joints are reduced due to high-density packaging, which enables increasing the proportion of IMCs in solder joints and creating a full IMC solder matrix. Several studies have shown that the tensile and shear strength of solder joints will be influenced by the thickness of the IMC layer [6–8]. Furthermore, hundred-micron solder joints only include a small number of grains; this will cause the solder joints to exhibit obvious anisotropic mechanical properties [9]. It follows that the mechanical properties of materials, based on large-scale specimens, will not accurately characterize the mechanical behavior of microscale solder joints. Domestic and foreign research

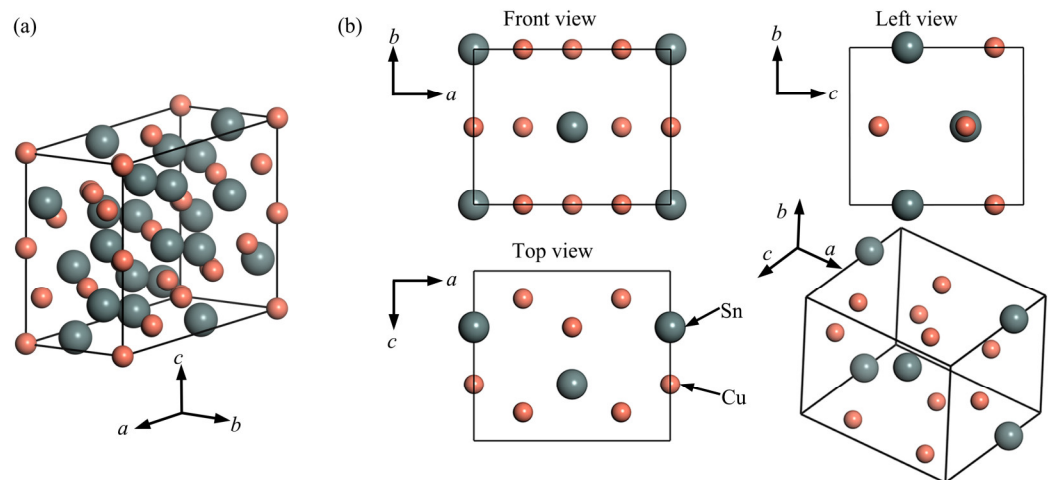
both present studies on the mechanical properties of  $\text{Cu}_6\text{Sn}_5$  and  $\text{Cu}_3\text{Sn}$ . The Young's modulus ( $E$ ) and hardness ( $H$ ) of  $\text{Cu}_3\text{Sn}$  and  $\text{Cu}_6\text{Sn}_5$  were measured by nanoindentation experiments [10–13]. Ghosh et al. [14] identified the values of  $E$ , shear modulus ( $G$ ), bulk modulus ( $B$ ), and Poisson's ratio ( $\nu$ ) using the pulse-echo method. However, due to the influence of experimental methods, sample manufacturing processes, and mechanical anisotropy, different experimental results were reported. For example, An et al. [15] studied  $E$  anisotropy of  $\text{Cu}_3\text{Sn}$  using the first-principles method, and the results showed that the experimental results of mechanical properties will be influenced by mechanical anisotropy. Mu et al. [16] found that  $\text{Cu}_6\text{Sn}_5$  and  $(\text{Cu, Ni})_6\text{Sn}_5$  reflected high anisotropy in  $E$  and for  $H$ . Moreover, because bulk single-crystal IMCs are difficult to prepare using the current experimental devices and methods, few reports exist on directly obtaining anisotropic mechanical properties through experiments. Choudhury et al. [17] investigated anisotropic mechanical properties for single-grain  $\text{Cu}_6\text{Sn}_5$  using nanoindentation and electron back-scattered diffraction. However, information about anisotropic mechanical properties that were obtained through experimental methods is limited because it is difficult to obtain this information from all directions.

It is noted that first-principles methods have in recent years been applied for investigating the mechanical properties of materials, including predicting the properties of metallic systems subjected to doping [18–22]; this has, to an extent, compensated for the shortcomings of experimental methods. In addition,  $\text{Cu}_6\text{Sn}_5$  can exist in a variety of crystal structures, i.e.,  $\eta$ ,  $\eta'$ ,  $\eta^6$ ,  $\eta^8$ ,  $\eta^{4+1}$ , and  $\eta''$ , and the  $\eta^8$  and  $\eta^{4+1}$  superstructures are approximant structures of the incommensurate  $\eta''$  phase [23]. Importantly,  $\eta'$ - $\text{Cu}_6\text{Sn}_5$  and  $\text{Cu}_3\text{Sn}$  are the most common phase during the service of solder joints [24]; therefore, they have a significant effect on the mechanical behavior of microscale solder joints. Although the anisotropic mechanical properties of  $\text{Cu}_3\text{Sn}$  were investigated by first-principles method, the anisotropy of  $B$  and  $G$  have typically been neglected. Furthermore, simulations for detecting the anisotropic mechanical properties of  $\eta'$ - $\text{Cu}_6\text{Sn}_5$  are rare. Actually,  $E$ ,  $B$ , and  $G$  represent the resistance to uniaxial stretching, volume deformation, and plastic deformation capacity, respectively. Elastic anisotropy is related to the generation of microcracks. As such, there is a need for systematically analyzing the mechanical properties and elastic anisotropy of  $\eta'$ - $\text{Cu}_6\text{Sn}_5$  and  $\text{Cu}_3\text{Sn}$ , further contributing to improving the durability of solder joints.

In this paper, the elastic constants of monocrystalline  $\eta'$ - $\text{Cu}_6\text{Sn}_5$  and  $\text{Cu}_3\text{Sn}$  were calculated based on the first-principles method. Then, according to the Voigt–Reuss–Hill approximation, the  $E$ ,  $B$ ,  $G$ , and  $\nu$  of polycrystalline could be obtained. Finally, the directional dependence and anisotropic degree of  $E$ ,  $B$ , and  $G$  were investigated.

## 2. Computational Methods and Details

In this study, a first-principles approach, based on density functional theory integrated with the CASTEP code [25] in the Materials Studio software [26], was employed to calculate the elastic constants of single crystals. The  $\text{Cu}_3\text{Sn}$  is a large one-dimensional long-period superstructure based on a *hcp* unit cell. In order to improve computational efficiency, the crystal model established by Burkhardt et al. [27] was employed in first-principles calculations. The  $\eta'$ - $\text{Cu}_6\text{Sn}_5$  and  $\text{Cu}_3\text{Sn}$  are monoclinic and orthorhombic systems, respectively [27,28]. The atomic site parameters and lattice constants of these two IMCs is presented in existing research [27,28]. The crystal models of  $\eta'$ - $\text{Cu}_6\text{Sn}_5$  and  $\text{Cu}_3\text{Sn}$  were created as shown in Figure 1a, b, respectively.



**Figure 1.** Crystal structures: (a) unit cell of monoclinic  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub>; (b) three views of unit cell of orthorhombic Cu<sub>3</sub>Sn.

The exchange-correlation energy was described by the generalized gradient approximation (GGA) with the Perdew and Wang (PW91) [29] functional for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn. The ultrasoft pseudopotentials [30] was used to describe ionic cores for the two IMC. The Monkhorst–Pack k-points meshes were  $8 \times 8 \times 10$  and  $8 \times 10 \times 9$  for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn, respectively. The two IMCs employed all plane-wave cutoff energy of 550 eV. The self-consistent field tolerance was set as  $5.0 \times 10^{-7}$  eV/atom. Once the geometric optimizations were completed, the lattice constants and the atom coordinates of the unit cells were completely relaxed, and the forces on atoms were less than 0.01 eV/Å.

### 3. Results and Discussion

#### 3.1. Structural Properties

Following geometric optimization, the structural information of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn was summarized (see Table 1). The calculated results, obtained using the GGA, showed good agreement with the experimental value. For  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn, the lattice constant errors were lower than 2.2% and 1.8%, respectively; the volume errors of unit cells were 4.4% and 1.6%, respectively. Based on the error analysis, the results of geometry optimization were reasonable.

**Table 1.** The lattice constants of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn.

Structure	Method	Lattice Constants			
		$a_0$ (Å)	$b_0$ (Å)	$c_0$ (Å)	$V_0$ (Å <sup>3</sup> )
$\eta'$ -Cu <sub>6</sub> Sn <sub>5</sub>	GGA	11.160	7.445	9.901	813.466
	Expt. [31]	11.022	7.282	9.827	779.368
	GGA [32]	11.370	7.510	10.020	846.019
Cu <sub>3</sub> Sn	GGA	5.391	4.278	4.795	110.586
	Expt. [15]	5.490	4.320	4.740	112.418
	GGA [33]	5.537	4.344	4.781	114.996

### 3.2. Elastic Properties

#### 3.2.1. The Elastic Constants of Single Crystals

Due to the presence of anisotropy, elastic constants  $C_{ij}$  (the elastic stiffness matrix) and the elastic compliance matrix  $S_{ij}$  were important for describing the relationships between stress and strain in a single crystal. Based on the crystal symmetry,  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn had 13 and 9 independent elastic constants, respectively. The  $(C_{ij})$  is an inverse matrix of,  $(S_{ij})$ , i.e.,  $(C_{ij}) = (S_{ij})^{-1}$ . In this paper, elastic constants  $C_{ij}$  and  $S_{ij}$  of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn were calculated as shown in Tables 2 and 3. The calculated  $C_{ij}$  was in good agreement with previously calculated values and demonstrated the reasonability of the results in the present work. To ensure stable  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn crystal structures,  $C_{ij}$  should comply with the corresponding mechanical stability criteria given by Equations (1) and (2) [34], respectively. By substituting the data of Table 2 into Equations (1) and (2), the above two crystal structures were shown to be mechanically stable.

$$\begin{aligned}
 &C_{11} > 0, C_{22} > 0, C_{33} > 0, C_{44} > 0, C_{55} > 0, C_{66} > 0, [C_{11} + C_{22} + C_{33} + 2(C_{12} + C_{13} + C_{23})] > 0, \\
 &(C_{33}C_{55} - C_{35}^2) > 0, (C_{44}C_{66} - C_{46}^2) > 0, (C_{22} + C_{33} - 2C_{23}) > 0, \\
 &[C_{22}(C_{33}C_{55} - C_{35}^2) + 2C_{23}C_{25}C_{35} - C_{23}^2C_{55} - C_{25}^2C_{33}] > 0, \\
 &\{2[C_{15}C_{25}(C_{33}C_{12} - C_{13}C_{23}) + C_{15}C_{35}(C_{22}C_{13} - C_{12}C_{23}) + C_{25}C_{35}(C_{11}C_{23} - C_{12}C_{13})] \\
 &\quad - [C_{15}^2(C_{22}C_{33} - C_{23}^2) + C_{25}^2(C_{11}C_{33} - C_{13}^2) + C_{35}^2(C_{11}C_{22} - C_{12}^2)] + C_{55}g\} > 0 \\
 &g = C_{11}C_{22}C_{33} - C_{11}C_{23}^2 - C_{22}C_{13}^2 - C_{33}C_{12}^2 + 2C_{12}C_{13}C_{23}.
 \end{aligned} \tag{1}$$

$$\begin{aligned}
 &C_{11} > 0, C_{44} > 0, C_{55} > 0, C_{66} > 0, C_{11}C_{22} > C_{12}^2, \\
 &C_{11}C_{22}C_{33} + 2C_{12}C_{13}C_{23} - C_{11}C_{23}^2 - C_{22}C_{13}^2 - C_{33}C_{12}^2 > 0.
 \end{aligned} \tag{2}$$

**Table 2.** The  $C_{ij}$  of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn (GPa).

Structure	$C_{11}$	$C_{22}$	$C_{33}$	$C_{44}$	$C_{55}$	$C_{66}$	$C_{12}$	$C_{13}$	$C_{15}$	$C_{23}$	$C_{25}$	$C_{35}$	$C_{46}$	Note
$\eta'$ -Cu <sub>6</sub> Sn <sub>5</sub>	136.2	164.5	146.3	38.2	44.1	44.2	65.8	58.3	-10.6	63.0	0.4	-3.0	1.1	Present
	156.4	165.2	155.8	42.3	51.9	48.0	62.2	69.4	-	60.6	-	-	-	Theo. [32]
Cu <sub>3</sub> Sn	213.6	218.6	185.0	54.2	52.3	63.1	96.8	99.4	-	108.1	-	-	-	Present
	154.6	173.7	148.2	50.2	44.2	55.0	78.9	76.5	-	95.1	-	-	-	Theo. [35]
	207.0	226.0	194.0	58.0	47.0	57.0	93.0	94.0	-	94.0	-	-	-	Theo. [15]

**Table 3.** The  $S_{ij}$  of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn ( $\times 10^{-3}$ , GPa<sup>-1</sup>).

Structure	$S_{11}$	$S_{22}$	$S_{33}$	$S_{44}$	$S_{55}$	$S_{66}$	$S_{12}$	$S_{13}$	$S_{15}$	$S_{23}$	$S_{25}$	$S_{35}$	$S_{46}$
$\eta'$ -Cu <sub>6</sub> Sn <sub>5</sub>	10.13	8.19	8.92	26.20	23.20	22.63	-3.03	-2.69	2.27	-2.34	-0.95	-0.02	-0.66
Cu <sub>3</sub> Sn	6.64	6.85	8.62	18.45	19.13	15.85	-1.65	-2.60	-	-3.11	-	-	-

### 3.2.2. Elastic Constants for Polycrystalline Aggregates

Mechanical properties of polycrystalline aggregate, such as  $B$  and  $G$  could be obtained by Voigt–Reuss–Hill approximation [36, 37]. The Voigt, Reuss, and Hill approximations obtain the maximum, minimum, and average value of  $B$  and  $G$ , respectively. Voigt bulk modulus  $B_V$ , Voigt shear modulus  $G_V$ , Reuss bulk modulus  $B_R$ , and Reuss shear modulus  $G_R$  can be calculated by Equations (3)–(6) [38].

$$B_V = \frac{1}{9}(C_{11} + C_{22} + C_{33}) + \frac{2}{9}(C_{12} + C_{13} + C_{23}) \quad (3)$$

$$G_V = \frac{1}{15}(C_{11} + C_{22} + C_{33} - C_{12} - C_{13} - C_{23}) + \frac{1}{5}(C_{44} + C_{55} + C_{66}) \quad (4)$$

$$B_R = [(S_{11} + S_{22} + S_{33}) + 2(S_{12} + S_{13} + S_{23})]^{-1} \quad (5)$$

$$G_R = 15[4(S_{11} + S_{22} + S_{33}) - 4(S_{12} + S_{13} + S_{23}) + 3(S_{44} + S_{55} + S_{66})]^{-1} \quad (6)$$

According to empirical formulas proposed by Hill [39], the  $B$  and  $G$  of polycrystalline aggregates satisfy Equations (7) and (8), respectively.

$$B = (B_V + B_R) / 2 \quad (7)$$

$$G = (G_V + G_R) / 2. \quad (8)$$

The  $E$  and  $\nu$  of polycrystalline aggregates are defined as:

$$E = 9BG / (3B + G) \quad (9)$$

$$\nu = (3B - 2G) / (6B + 2G). \quad (10)$$

The theoretical results of  $E$ ,  $G$ ,  $B$ , and  $\nu$  for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn are summarized in Table 4. The theoretical values and the reported experimental results showed excellent consistency for Cu<sub>3</sub>Sn. Although reports on experimental results are rare for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub>, the present work is supported by previously computed values (see Table 4). Therefore, in this paper, the results calculated using the first-principles method is reasonable.

**Table 4.** The  $E$  (GPa),  $G$  (GPa),  $B$  (GPa),  $\nu$ , and  $G/B$  of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn.

Structure	$E$	$G_V$	$G_R$	$G$	$B_V$	$B_R$	$B$	$\nu$	$G/B$	Note
$\eta'$ -Cu <sub>6</sub> Sn <sub>5</sub>	109.8	42.6	42.0	42.3	91.2	90.0	90.6	0.30	0.47	Present
	94.4	-	-	35.9	-	-	84.4	0.31	0.43	Expt. [14]
	116.7	-	-	45.0	-	-	95.5	-	0.47	Theo. [32]
	107.9	-	-	42.4	-	-	79.4	0.27	0.53	Theo. [20]
Cu <sub>3</sub> Sn	143.9	54.8	53.9	54.4	136.2	135.6	135.9	0.32	0.40	Present
	123.2	-	-	46.7	-	-	113.8	0.32	0.41	Expt. [14]
	143.0	-	-	-	-	-	-	-	-	Expt. [10,40]
	147.0	-	-	56.0	-	-	132.0	0.32	0.42	Theo. [15,41]

Generally,  $G/B$  and  $\nu$  [19] are employed to evaluate the brittleness of materials. If  $G/B > 0.57$  and  $\nu < 0.26$ , the materials will be brittle, or, alternatively, will show ductility. Table 4 shows that  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn all conformed to the following criterion:  $G/B < 0.57$ ,  $\nu > 0.26$ ; as such, they were ductile materials.

### 3.3. Elastic Anisotropy

Elastic anisotropy is related to the generation of microcracks; it also causes poor consistency in the results of tests reviewing the mechanical properties of materials. Therefore, the investigation of elastic anisotropy related to  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn is favorable for better understanding the failure behaviors in these materials and, accordingly, improving their mechanical durability. In this paper, three anisotropic indexes were applied to assess the elastic anisotropy of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn, i.e., universal anisotropic index  $A^U$ , as well as the anisotropic percentage in the compression ( $A_{\text{comp}}$ ) and shear ( $A_{\text{shear}}$ ) modes [36]. The three anisotropic indexes can be expressed as follows:

$$A^U = 5G_V / G_R + B_V / B_R - 6 \quad (11)$$

$$A_{\text{comp}} = (B_V - B_R) / (B_V + B_R) \quad (12)$$

$$A_{\text{shear}} = (G_V - G_R) / (G_V + G_R) \quad (13)$$

Furthermore, shear anisotropy in different crystal planes can be evaluated by shear anisotropy factors, i.e.,  $A_1$ ,  $A_2$ , and  $A_3$  denote the anisotropic degree in the (100), (010), and (001) crystal planes, respectively [33]. The three shear anisotropy factors for the monoclinic, and orthorhombic structures can be defined as follows [33,42]:

$$A_1 = 4C_{44} / (C_{11} + C_{33} - 2C_{13}) \quad (14)$$

$$A_2 = 4C_{55} / (C_{22} + C_{33} - 2C_{23}) \quad (15)$$

$$A_3 = 4C_{66} / (C_{11} + C_{22} - 2C_{12}) \quad (16)$$

Generally,  $A^U = A_{\text{comp}} = A_{\text{shear}} = 0$ , and  $A_1 = A_2 = A_3 = 1$ , which represent isotropy; otherwise,  $A^U \neq 0$ ,  $A_{\text{comp}} \neq 0$ ,  $A_{\text{shear}} \neq 0$ ,  $A_1 \neq 1$ ,  $A_2 \neq 1$ , and  $A_3 \neq 1$ , which represent anisotropy. For  $A^U$ ,  $A_{\text{comp}}$ , and  $A_{\text{shear}}$ , the deviation between 0 and actual values was used to describe the anisotropic degree. For  $A_1$ ,  $A_2$ , and  $A_3$ , the deviation of from 1 represent the anisotropic degree. The calculated  $A^U$ ,  $A_{\text{comp}}$ ,  $A_{\text{shear}}$ ,  $A_1$ ,  $A_2$ , and  $A_3$  of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn are summarized in Table 5. The values of  $A^U$  were 0.0848 and 0.0838 for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn, respectively, which showed that the elastic anisotropy of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> was higher. Meanwhile, the  $A_{\text{comp}}$  of Cu<sub>3</sub>Sn were all close to 0; this indicated modest compression anisotropy. It is worth noting that the  $A_{\text{shear}}$  of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn were 0.0071 and 0.0079, respectively, and the shear anisotropy of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> was lower. Moreover, according to the calculated values of  $A_1$ ,  $A_2$ , and  $A_3$ , the shear anisotropy of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> was low and similar in three crystal planes and was the highest and lowest in the (010) and (001) planes for Cu<sub>3</sub>Sn, respectively.

**Table 5.** The anisotropic indexes of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn.

Structure	$A^U$	$A_{\text{comp}}$	$A_{\text{shear}}$	$A_1$	$A_2$	$A_3$
$\eta'$ -Cu <sub>6</sub> Sn <sub>5</sub>	0.0848	0.0066	0.0071	0.9210	0.9545	1.0455
Cu <sub>3</sub> Sn	0.0838	0.0022	0.0079	1.0847	1.1164	1.0574

To reveal the elastic anisotropy more concretely, the directional dependences of  $E$ ,  $B$ , and  $G$  were obtained, and the results are exhibited as three-dimensional (3D) surfaces in Cartesian coordinates. Furthermore, the deviation between the 3D surfaces and the sphere shape denotes the degree of anisotropy. The 3D surfaces of  $E$  can be obtained by Equation (17) [43] as follows:

$$\begin{aligned}
1/E(\mathbf{n}) = & S_{11}n_1^4 + S_{22}n_2^4 + S_{33}n_3^4 + (S_{44} + 2S_{23})n_2^2n_3^2 + (S_{55} + 2S_{31})n_3^2n_1^2 + (S_{66} + 2S_{12})n_1^2n_2^2 \\
& + 2n_2n_3[(S_{14} + S_{56})n_1^2 + S_{24}n_2^2 + S_{34}n_3^2] + 2n_3n_1[S_{15}n_1^2 + (S_{25} + S_{46})n_2^2 + S_{35}n_3^2] \\
& + 2n_1n_2[S_{16}n_1^2 + S_{26}n_2^2 + (S_{36} + S_{45})n_3^2]
\end{aligned} \quad (17)$$

where  $n_1$ ,  $n_2$ , and  $n_3$  denote the directional cosines of loading-direction  $\mathbf{n}$  with three principal directions. For the two IMCs, the 3D surfaces and their cross-sections of  $E$  are illustrated in Figures 2 and 3, respectively. In this study, anisotropy ratio  $E_{\max}/E_{\min}$  was employed to quantify the amount of anisotropy; the larger the anisotropy ratio, the higher the anisotropy [44]. For  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub>,  $E_{\max} = 124.6$  GPa,  $E_{\min} = 89.5$  GPa, and the anisotropy ratio was 1.39. The directions of  $E_{\max}$  and  $E_{\min}$  were (1, 0, -0.76) and (1, 0, 0.42), respectively. The anisotropic ratios, maximum and minimum values of  $E$  is listed Table 6 for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn. Obviously,  $E$  anisotropy in the  $xz$  plane was the highest for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub>. For Cu<sub>3</sub>Sn, the results showed that the 3D plot of  $E$  was non-spherical (see Figure 2b); moreover,  $E_{\max}$  and  $E_{\min}$  were 153.9 GPa and 116.0 GPa, respectively. The anisotropy ratio was 1.33, and the directions of  $E_{\max}$  and  $E_{\min}$  were (1, 0.84, 0) and (0, 0, 1), respectively. It is noted that  $E$  anisotropy of the  $yz$  and  $xz$  planes was similar for Cu<sub>3</sub>Sn. Overall, the anisotropy ratio of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> was higher, which showed that  $E$  anisotropy of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> was higher. This conclusion is also supported by the  $A^U$  values shown in Table 5. Furthermore, the 3D surfaces of  $G$  could be obtained by the following formula [43]:

$$\begin{aligned}
1/G(\mathbf{n}, \mathbf{m}) = & 4[2S_{12} - (S_{11} + S_{22} - S_{66})]n_1m_1n_2m_2 + 4[2S_{23} - (S_{22} + S_{33} - S_{44})]n_2m_2n_3m_3 \\
& + 4[2S_{31} - (S_{33} + S_{11} - S_{55})]n_3m_3n_1m_1 + 4(n_1m_2 + n_2m_1)[(S_{16} - S_{36})n_1m_1 + (S_{26} - S_{36})n_2m_2] \\
& + 4(n_2m_3 + n_3m_2)[(S_{24} - S_{14})n_2m_2 + (S_{34} - S_{14})n_3m_3] \\
& + 4(n_3m_1 + n_1m_3)[(S_{35} - S_{25})n_3m_3 + (S_{15} - S_{25})n_1m_1] \\
& + S_{44}(n_2m_3 - n_3m_2)^2 + S_{55}(n_3m_1 - n_1m_3)^2 + S_{66}(n_1m_2 - n_2m_1)^2 \\
& + 2S_{45}(n_2m_3 + n_3m_2)(n_3m_1 + n_1m_3) \\
& + 2S_{56}(n_3m_1 + n_1m_3)(n_1m_2 + n_2m_1) + 2S_{64}(n_1m_2 + n_2m_1)(n_2m_3 + n_3m_2)
\end{aligned} \quad (18)$$

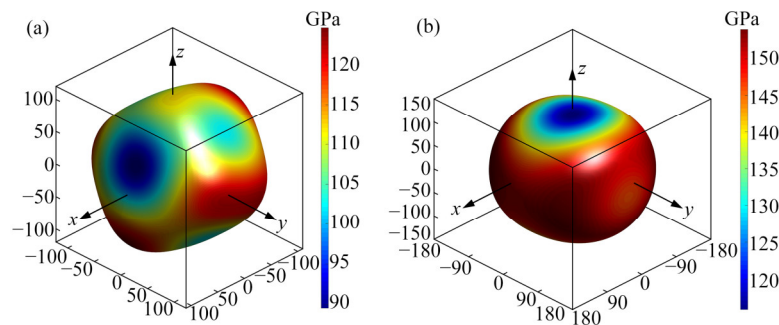


Figure 2. The 3D directional dependence of  $E$  for (a)  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub>, (b) Cu<sub>3</sub>Sn.

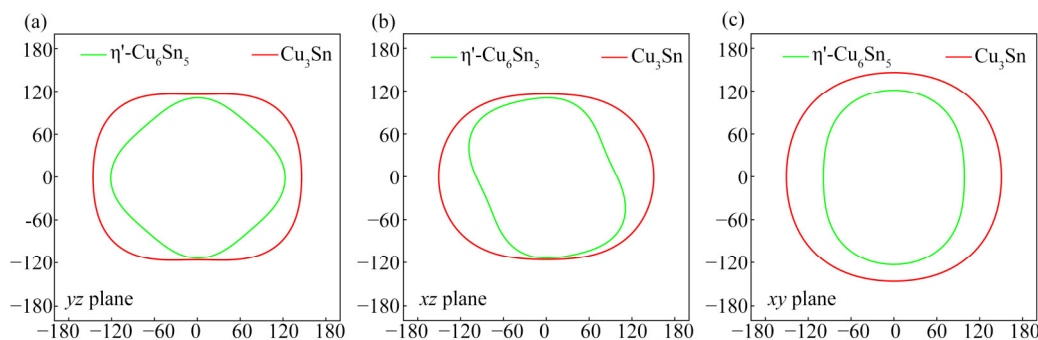


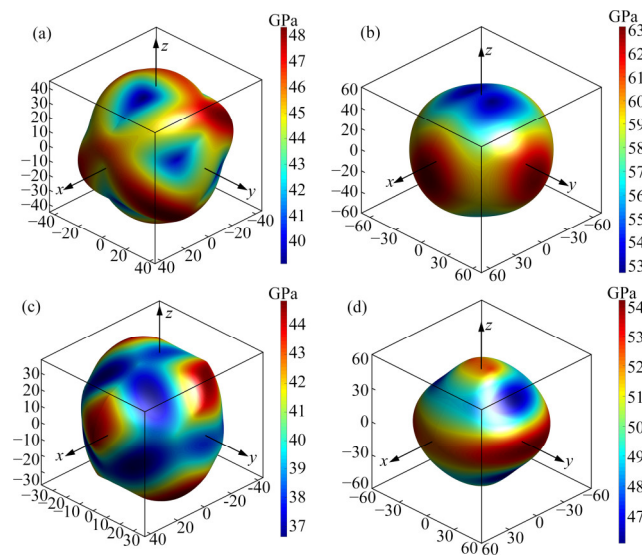
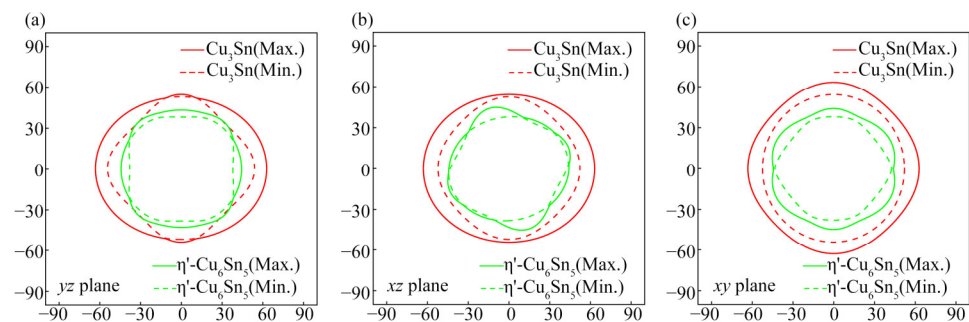
Figure 3. Cross-sections of  $E$  in the  $yz$ ,  $xz$ , and  $xy$  planes for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn: (a) the  $yz$  plane; (b) the  $xz$  plane; (c) the  $xy$  plane. The green and red lines denote the cross-sections for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn, respectively.



**Table 6.** The anisotropic ratios, maximum and minimum values of  $E$  for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn.

	$\eta'$ -Cu <sub>6</sub> Sn <sub>5</sub>				Cu <sub>3</sub> Sn			
	Whole	$yz$	$xz$	$xy$	Whole	$yz$	$xz$	$xy$
$E_{\max}$ (GPa)	124.6	122.1	124.6	122.1	153.9	149.7	150.6	177.8
$E_{\min}$ (GPa)	89.5	103.2	89.5	98.7	116.0	116.0	116.0	125.1
Anisotropic ratios	1.39	1.18	1.39	1.24	1.33	1.29	1.30	1.42

where  $m_1$ ,  $m_2$ , and  $m_3$  are the directional cosines of measurement direction  $\mathbf{m}$ , and  $\mathbf{m}$  is perpendicular to  $\mathbf{n}$ . In a particular direction  $\mathbf{n}$ ,  $G$  will be changed with a change in  $\mathbf{m}$ . For the two IMCs, the directional dependences of maximum and minimum  $G$  are plotted in Figure 4. In addition, the cross-sections of maximum and minimum  $G$  in the  $yz$ ,  $xz$ , and  $xy$  planes are shown in Figure 5. In this study, anisotropy ratio  $G_{\max}/G_{\min}$  was employed to describe the anisotropic degree of  $G$ . For  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub>, the directions of  $G_{\max} = 48.3$  GPa and  $G_{\min} = 36.6$  GPa were  $(0.71, 1, -0.71)$  and  $(-0.67, 0.60, -1)$ , respectively; hence, the anisotropy ratio was 1.32. The anisotropic ratios, maximum and minimum values of  $G$  is listed Table 7 for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn. The anisotropic degree of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> was similar in the  $yz$ ,  $xz$ , and  $xy$  planes. For Cu<sub>3</sub>Sn,  $G_{\max} = 63.1$  GPa,  $G_{\min} = 46.1$  GPa, and the  $G_{\max}/G_{\min}$  was 1.37 for Cu<sub>3</sub>Sn. The directions of  $G_{\max}$  and  $G_{\min}$  were  $(0, 1, 0)$  and  $(0, 1, 1)$ , respectively. Obviously,  $G$  anisotropy of the  $yz$ ,  $xz$ , and  $xy$  planes was similar for Cu<sub>3</sub>Sn.

**Figure 4.** The 3D directional dependence of  $G$ : (a) the maximum  $G$  of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub>; (b) the maximum  $G$  of Cu<sub>3</sub>Sn; (c) the minimum  $G$  of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub>; (d) the minimum  $G$  of Cu<sub>3</sub>Sn.**Figure 5.** Cross-sections of  $G$  in the  $yz$ ,  $xz$ , and  $xy$  planes for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn: (a) the  $yz$  plane; (b) the  $xz$  plane; (c) the  $xy$  plane. The solid and dotted lines denote the maximum and minimum values, respectively. The green and red lines denote the cross-sections for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn, respectively.

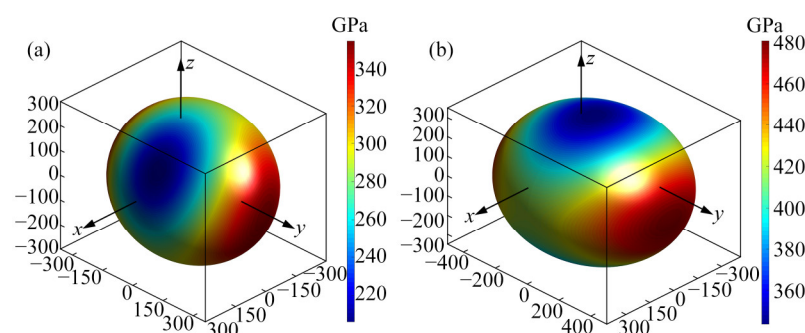
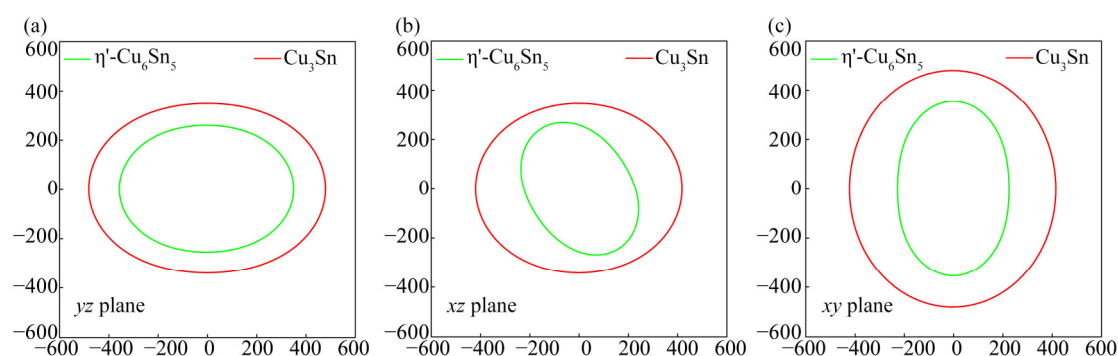
**Table 7.** The anisotropic ratios, maximum and minimum values of  $G$  for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn.

	$\eta'$ -Cu <sub>6</sub> Sn <sub>5</sub>				Cu <sub>3</sub> Sn			
	Whole	$yz$	$xz$	$xy$	Whole	$yz$	$xz$	$xy$
$G_{\max}$ (GPa)	48.3	46.6	46.6	47.0	63.1	63.1	63.1	63.1
$G_{\min}$ (GPa)	36.6	38.0	38.0	37.2	46.1	48.9	48.9	52.3
Anisotropic ratios	1.32	1.23	1.23	1.26	1.37	1.29	1.29	1.21

In summary, for the two IMCs,  $G$  anisotropy of Cu<sub>3</sub>Sn was higher. This conclusion is also supported by the  $A_{\text{shear}}$  values shown in Table 5. Finally, the directional dependences of  $B$  are described by formula (19) [45].

$$\begin{aligned}
 1/B(\mathbf{n}) = & (S_{11} + S_{12} + S_{13})n_1^2 + (S_{16} + S_{26} + S_{36})n_1n_2 + (S_{15} + S_{25} + S_{35})n_3n_1 \\
 & + (S_{12} + S_{22} + S_{23})n_2^2 + (S_{14} + S_{24} + S_{34})n_2n_3 \\
 & + (S_{13} + S_{23} + S_{33})n_3^2
 \end{aligned} \quad (19)$$

The directional dependence of  $B$  is shown in Figure 6. The cross-sections of  $B$  in the  $yz$ ,  $xz$ , and  $xy$  planes are shown in Figure 7. Anisotropy ratio  $B_{\max}/B_{\min}$  was performed to describe the anisotropic degree of  $B$ . For  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub>,  $B_{\max} = 354.2$  GPa was located on the  $yz$  and  $xy$  planes, and the  $B_{\min} = 206.1$  GPa was located on the  $xz$  planes. The anisotropy ratio was 1.72, and the directions of  $B_{\max}$  and  $B_{\min}$  were  $(0, 1, 0)$  and  $(1, 0, 0.67)$ , respectively. The anisotropic ratios, maximum and minimum values of  $B$  is listed Table 8 for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn. The  $B$  anisotropy of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> was found to be the highest in the  $xy$  plane. For Cu<sub>3</sub>Sn,  $B_{\max} = 480.7$  GPa,  $B_{\min} = 343.9$  GPa, and the anisotropy ratio was 1.40. The directions of  $B_{\max}$  and  $B_{\min}$  were  $(0, 1, 0)$  and  $(0, 0, 1)$ , respectively. The anisotropic degree of  $B$  was highest in the  $yz$  plane of Cu<sub>3</sub>Sn. It is noted that  $B$  anisotropy of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> was higher than Cu<sub>3</sub>Sn, which can be confirmed by  $A_{\text{comp}}$  (see Table 5).

**Figure 6.** The 3D directional dependence of  $B$ : (a)  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub>; (b) Cu<sub>3</sub>Sn.**Figure 7.** Cross-sections of  $B$  in the  $yz$ ,  $xz$ , and  $xy$  planes for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn: (a) the  $yz$  plane; (b) the  $xz$  plane; (c) the  $xy$  plane. The green and red lines denote the cross-sections of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn, respectively.

**Table 8.** The anisotropic ratios, maximum and minimum values of  $B$  for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn.

	$\eta'$ -Cu <sub>6</sub> Sn <sub>5</sub>				Cu <sub>3</sub> Sn			
	Whole	$yz$	$xz$	$xy$	Whole	$yz$	$xz$	$xy$
$B_{\max}$ (GPa)	354.2	354.2	289.9	354.2	480.7	480.7	419.0	480.7
$B_{\min}$ (GPa)	206.1	257.3	206.1	226.4	343.9	343.9	343.9	418.9
Anisotropic ratios	1.72	1.38	1.41	1.56	1.40	1.40	1.22	1.15

#### 4. Conclusions

Clarifying the mechanical properties of IMCs is helpful to provide basic material properties for finite element analysis and improve the reliability of microscale solder joints. In this work, the mechanical properties and elastic anisotropies of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn were investigated using the first-principles calculations method. The conclusions of the present work are as follows.

1. For  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn, the elastic constants of single crystals and polycrystalline aggregates were obtained using first-principles calculations. Accordingly,  $E$ ,  $G$ ,  $B$ , and  $\nu$  of the two IMCs all exhibited the following relationship: Cu<sub>3</sub>Sn >  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub>. Moreover, the values of  $G/B$  and  $\nu$  showed that the two IMCs were ductile materials.
2. The directional dependence analysis of  $E$  had anisotropy ratios of 1.39 and 1.33 for monocrystalline  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn, respectively. The  $E$  anisotropy reflected the following relationship:  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> > Cu<sub>3</sub>Sn.
3. The two monocrystalline IMCs exhibited evident anisotropy of  $G$ ; the anisotropy ratios were 1.32 and 1.37 for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub>, and Cu<sub>3</sub>Sn, respectively. Accordingly,  $G$  anisotropy abided by the following relationship: Cu<sub>3</sub>Sn >  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub>. In addition, the anisotropic degree of  $E$  and  $G$  was similar for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> and Cu<sub>3</sub>Sn.
4. For  $B$  of the two monocrystalline IMCs, the anisotropy ratio of  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> was higher, reaching 1.72. For Cu<sub>3</sub>Sn, the anisotropy ratios were 1.40. The relationship for  $B$  anisotropy was  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub> > Cu<sub>3</sub>Sn. Furthermore, the anisotropy of  $B$  was higher compared with  $G$  and  $E$  for  $\eta'$ -Cu<sub>6</sub>Sn<sub>5</sub>; however, in the case of Cu<sub>3</sub>Sn, the anisotropic degree of  $B$ ,  $G$ , and  $E$  was similar.

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