2 APR. 1973 ARCHIEF Lab. v. Scheepsbouwkunde
Technische Hogeschool
H Delft

OFFICE OF NAVAL RESEARCH
DEPARTMENT OF THE NAVY

CONTRACT N00014-67-A-0094-0012

Onderatdeling heepsbouwkunde

To hinische Hogeschool, Delli

DOCUMENTATIE:

DATUM: K90-14

Cavidations Wall effect restricted flow experiment

EXPERIMENTAL VERIFICATION OF CAVITY-FLOW WALL EFFECTS AND CORRECTION RULES

BY

ARTHUR K. WHITNEY
CHRISTOPHER BRENNEN
T. YAO-TSU WU

CALIFORNIA INSTITUTE OF TECHNOLOGY

PASADENA, CALIFORNIA

Division of Engineering and Applied Science California Institute of Technology Pasadena, California

EXPERIMENTAL VERIFICATION OF CAVITY-FLOW WALL EFFECTS AND CORRECTION RULES

Contract N00014-67-A-0094-0012

by

Arthur K. Whitney Christopher Brennen T. Yao-tsu Wu

This document has been approved for public release and sale; its distribution is unlimited.

Experimental Verification of Cavity-flow Wall Effects and Correction Rules

Abstract

This report is intended as a companion to Report No. E-111A.5, "Wall Effects in Cavity Flows", by Wu, Whitney and Lin. Some simple rules for the correction of wall effect are derived from that theoretical study. Experiments designed to complement the theory and to inspect the validity of the correction rules were then carried out in the high-speed water tunnel of the Hydrodynamics Laboratory, California Institute of Technology. The measurements on a series of fully cavitating wedges at zero angle of attack suggested that of the theoretical models that due to Riabouchinsky is superior. They also confirmed the accuracy of the correction rule derived using that model and based on a measurement of the minimum pressure along the tunnel wall.



With Compliments

R. D Mathieu

Dr. Richard D. Mathieu Liaison Scientist

United States of America
Department of the Navy
OFFICE OF NAVAL RESEARCH, BRANCH OFFICE
Keysign House, 429 Oxford Street
London, W. I. England

1. Introduction

Wu, Whitney and Lin (1969) presented exact solutions for fully cavitating flows in solid wall tunnels. In particular they computed the non-lifting case of a wedge (half vertex angle, $\beta\pi$, base width, ℓ) centered in a stream limited by straight walls, h apart. Having explored the choked flow conditions in which the cavity is infinitely long and the cavitation number, σ , takes its minimum possible value, $\sigma_{\rm C}$, they then treated the general case of finite cavities and came to the following basic conclusions on the influence of the wall upon the drag on the headform:

- (i) The drag is always lower than that in unbounded flow at the same cavitation number, σ . The difference is termed the drag reduction. It is due to the somewhat increased velocity, decreased pressure coefficient, C_p , over the wetted surface of the body though the end points, $C_p = 1$ at stagnation, $C_p = -\sigma$ at separation are identical.
- (ii) At the same σ and $\lambda = l/h$ the percentage drag reduction increases with decreasing wedge angle, implying that the wall effect is more significant for thinner bodies in cavity flows.
- (iii) The drag reduction is almost insensitive to σ for a given wedge angle, β , and $\lambda = \ell/h$.

These effects were found with both the open-wake and Riabouchinsky theoretical models. Effects (i) and (iii) were also found for the re-entrant jet model for a flat plate $\left(\beta=\frac{1}{2}\right)$, although numerical results for other wedge angles are as yet unavailable. A review of the previous theoretical work is included in Wu, Whitney, Lin (1969) and will not be repeated here. Morgan (1966) reviews recent experimental studies of the wall effect in cavity flows. Investigations of "flow choking" and wall effect in nominally axisymmetric flow have been reported by Barr (1966), Dobay (1967) and Brennen (1969b) among others. Brennen also finds numerical solutions to the theoretical Riabouchinsky flows around a sphere and a disc and these furnish theoretical predictions of the wall effect in axisymmetric flow.

In another experimental endeavor, Meijer (1967) carried out a study of the wall effect upon a cavitating hydrofoil with flaps (nominally planar flow). He suggests an empirical method to correct for the influence of the walls. This involves the use of the minimum pressure on the tunnel wall, p_b , and the corresponding velocity, V, as reference rather than the tunnel "free stream" pressure and velocity, p_{∞} and U. The usual cavitation number, σ , and drag coefficient are

$$\sigma = \frac{P_{\infty}^{-P} c}{\frac{1}{2} \rho U^2} \qquad C_D = \frac{D}{\frac{1}{2} \rho U^2 \ell S}$$
 (1)

where p_c is the cavity pressure, D the drag on the body, ρ the density of the liquid and S the span. Meijer's corrected σ'' , C_D'' are thus

$$\sigma'' = \frac{P_b - P_c}{\frac{1}{2} \rho V^2} \qquad C_D''(\sigma'') = \frac{D}{\frac{1}{2} \rho V^2 \ell S} \qquad (2)$$

Meijer found that this provided a satisfactory wall correction rule for his experiments. The correction rules suggested in this report are similarly based on a measurement of the minimum pressure p_b . However both the theoretical predictions of Wu, Whitney and Lin and the present experimental results indicate that Meijer's rule generally over-corrects by an amount which can be quite large.

It is of interest to point out the different trends between the wall effects in non-separated, non-cavitating flows and those in cavity flows. In closed wind-tunnels, the lateral constraint and body thickness generally result in an increase of flow velocity and hence dynamic pressure, thus increasing lift, drag, and moment coefficients at a given angle of attack (see, e.g., Pope (1954)). In contrast, the general trend of the wall effect on cavity flows in closed tunnels have been found to decrease the drag and lift coefficients at prescribed cavitation number and incidence. These opposite trends may seem at first glance puzzling, particularly to those experienced with wind-tunnel testings. Actually, the lateral constraint in the presence of a cavity still results in an increase of flow velocity and hence a decrease of the pressure over the wetted surface of the body, consequently decreasing all the forces if referred to the same cavitation number. Furthermore, this increase in flow velocity at the cavity boundary will cause the cavity pressure $P_{\rm C}$

to be somewhat lower, and hence the cavitation number somewhat higher than in an unbounded flow with the same free stream condition. These two effects therefore reinforce each other such that the curve of drag coefficient, C_D , against σ lies below the corresponding curve for unbounded flow.

The first concern of the present report is the derivation of some simple rules for the correction of cavity wall effect. The second is the experimental verification of these rules and of the theoretical analyses of Wu, Whitney and Lin. However, at the same time the opportunity is taken to discuss some of the other problems and real fluid effects which arise during cavitation experiments in high speed water tunnels. These may be generally grouped as follows:

- (i) Viscous effects due to the boundary layer on the model being tested.
- (ii) Viscous and other effects due to the boundary layer on the tunnel walls including production of a longitudinal pressure gradient and acceleration and the possible appearance of secondary flows.
- (iii) The necessity of determining the cavity pressure, p_c ; effects which cause this to differ from p_V , the vapor pressure.
- (iv) The determination of a hypothetical "free stream" pressure, p_{∞} , equal to the remote pressure were the tunnel infinitely long.
- (v) Limitations on the range of cavitation number which can be satisfactorily covered including the effects of ''flow choking.''
- (vi) Effects due to actual cavity closure. These include the unsteady, turbulent nature of the flow in this region, the cavity filling effect of the re-entrant jet (especially when this impinges on the rear of the headform) and the viscous, turbulent wake behind the cavity.

Some discussion on these is included at the appropriate point in the sections

which follow.

2. Wall Correction Formulae

In view of the fact that the ratio $\lambda = \ell/h$ is usually small in experimental practice, an asymptotic representation, for λ small, of the exact solutions of Wu, Whitney, Lin (1969) can serve useful purposes for evaluating the wall effects and their corrections. The analysis of the asymptotic expansions is less complicated for symmetric wedges and will be carried out for two different flow models.

For the reader's convenience, expressions utilized in the derivations will be reproduced from Wu, Whitney, Lin (1969).

A. The Open-Wake Model

For this model, the drag coefficient is given by

$$C_{D}(\sigma, \lambda) = \frac{1}{\lambda U} \left(U + \frac{1}{U} - V - \frac{1}{V} \right) , \qquad (3)$$

where

$$U = (1+\sigma)^{\frac{1}{2}} \tag{4}$$

is the upstream velocity and $\,V\,$ is the downstream velocity. The cavity wall velocity has been normalized to unity. $\,V\,$ depends on $\,\sigma\,$ and $\,\lambda\,$ through the implicit relation

$$\lambda = U[F(U) - F(V)] , \qquad (5)$$

where

$$F(U) = \frac{2}{\pi} \sin \beta \pi \int_{0}^{1} \frac{\{1 + (1 - \zeta^{2})^{\frac{1}{2}}\}^{2} \zeta^{1 - 2} \beta}{\zeta^{2} + [a(U)]^{2}} d\zeta$$
 (6)

and

$$a(U) = 2[U^{-1/2\beta} - U^{1/2\beta}]^{-1}$$
 (7)

In (6) and (7), $\beta \pi$ is the half-angle of the wedge.

For fixed σ (hence U), the unbounded flow limit (λ =0) of the drag coefficient is found by letting $V \rightarrow U$ in (3) and (5), giving upon using l'Hospitol's rule

$$C_{D}(\sigma,0) = \frac{U^{-2}(U^{-2}-1)}{F^{1}(U)}$$
.

If this equation is solved for F'(U), and integrated from U to V, an alternate expression for λ is obtained, using again (5)

$$\lambda = U \int_{U}^{V} \frac{\sigma(u)(1+\sigma(u))}{C_{D}(\sigma(u),0)} du , \qquad (8)$$

where $\sigma(u) \equiv u^{-2} - 1$. For a given wedge angle, (8) determines V implicitly as a function of σ and λ .

We next seek a partial differential equation for $C_D(\sigma,\lambda)$. Partial differentiation of (3) and (8) with respect to σ and λ and elimination of terms involving V gives

$$\begin{split} & \frac{2(1+\sigma)}{\sigma} \ C_{\mathrm{D}}(\sigma,0) \ \frac{\partial C_{\mathrm{D}}(\sigma,\lambda)}{\partial \sigma} + \left[1 \ -\frac{\lambda}{\sigma} \ C_{\mathrm{D}}(\sigma,0)\right] \frac{\partial C_{\mathrm{D}}(\sigma,\lambda)}{\partial \lambda} \\ & = \frac{1}{\lambda} \ \left[\ C_{\mathrm{D}}(\sigma,0) - C_{\mathrm{D}}(\sigma,\lambda) \right] + \frac{2}{\sigma} \ C_{\mathrm{D}}(\sigma,0) C_{\mathrm{D}}(\sigma,\lambda) \quad . \end{split}$$

In the limit as $\lambda \rightarrow 0$, this equation becomes

$$\frac{\partial C_{D}(\sigma,0)}{\partial \lambda} + \frac{(1+\sigma)}{\sigma} C_{D}(\sigma,0) \frac{\partial C_{D}(\sigma,0)}{\partial \sigma} = \frac{1}{\sigma} C_{D}^{2}(\sigma,0) , \qquad (9)$$

or to the order of accuracy, $O(\lambda)$, we also have

$$\frac{\partial C_{D}(\sigma,\lambda)}{\partial \lambda} + \frac{(1+\sigma)}{\sigma} C_{D}(\sigma,\lambda) \frac{\partial C_{D}(\sigma,\lambda)}{\partial \sigma} = \frac{1}{\sigma} C_{D}^{2}(\sigma,\lambda) . \tag{10}$$

For fixed σ , (10) gives an estimate of the dependence of C_D on λ , namely $\partial C_D/\partial \lambda$; however, both C_D and $\partial C_D/\partial \sigma$ must be known. For experimental applications, the latter quantity would require estimating a derivative from experimental data, which can be rather inaccurate.

A more useful result follows by integrating (10) from σ to $\sigma' < \sigma$, corresponding to $\lambda = 0(\sigma - \sigma' = O(\lambda))$, along the mathematical characteristics

$$\frac{\mathrm{d}\hat{\sigma}}{\mathrm{d}\lambda} = \left(\frac{1+\sigma}{\sigma}\right) C_{\mathrm{D}}(\sigma,\lambda) \quad , \quad \frac{\mathrm{d}C_{\mathrm{D}}}{\mathrm{d}\sigma} = \frac{C_{\mathrm{D}}(\sigma,\lambda)}{1+\sigma} \quad ,$$

and yields

$$C_{D}(\sigma^{1}, 0) = \left(\frac{1+\sigma^{1}}{1+\sigma}\right) C_{D}(\sigma, \lambda) + O(\lambda^{2}) \tag{11}$$

where

$$\sigma^* = \sigma - \left(\frac{1+\sigma}{\sigma}\right)C_D(\sigma, \lambda)\lambda + O(\lambda^2)$$
 (12)

This two-way correction rule takes a measured drag coefficient $C_D(\sigma,\lambda)$, in a tunnel of known λ , and converts it by (11) and (12) to an estimated drag coefficient $C_D(\sigma^*,0)$ in unbounded flow $(\lambda=0)$ at a different cavitation number, σ^* , given by (12). An example of the use of this rule in estimating unbounded drag coefficients from theoretically calculated data, $C_D(\sigma,\lambda)$, is shown in Fig. 1 for $\beta\pi=15^\circ$. The agreement of predicted estimates with calculated values of $C_D(\sigma^*,0)$ is found to be excellent for all angles, with λ up to 1/6 and σ up to 1.

Another interesting consequence of Eq. (6) is that estimates of $C_D(\sigma,\lambda)$ can be obtained if good approximations of $C_D(\sigma,0)$ are known. For example, for wedges with $\beta\pi > 30^\circ$ it is known that $C_D(\sigma,0) \cong C_O(\beta)(1+\sigma)$ is a fairly good approximation as long as $\sigma < 1$. Substituting this approximation for $C_D(\sigma,0)$ into (8), we have

$$\lambda = \frac{\dot{U}}{C_o} \left\{ \frac{1}{\dot{U}} + \dot{U} - \frac{1}{\dot{V}} - \dot{V} \right\} ,$$

so that

$$C_{D}(\sigma, \lambda) = \frac{C_{O}}{U^{2}} = C_{O}(1+\sigma) = C_{D}(\sigma, 0)$$

by (3). Thus, there is no correction for wall effect if $C_D(\sigma, 0)$ obeys the linear relation exactly and it is reasonable to expect that the correction is small if $C_D(\sigma, 0)$ follows it only approximately. This is confirmed by numerical calculations.

Another important case occurs for small angle wedges ($\beta \pi \le 15^{\circ}$) and σ fairly large, in which case

$$C_D(\sigma, 0) \simeq \sigma$$

is a good approximation (see Figs. 7,8,9, Wu, Whitney, Lin (1969)). In

this case, we find

$$C_D(\sigma, \lambda) = C_D(\sigma, 0) - \frac{\lambda}{1 - \lambda}$$

which is in excellent agreement with numerical evaluations of the exact equations (3) + (7).

B. The Riabouchinsky Model

For this model, Wu, Whitney, Lin (1969) give

$$C_{D}(\sigma, \lambda) = (1+\sigma)\left[1 - \frac{I_{-}(a,b)}{I_{+}(a,b)}\right]$$
 (13)

and

$$\lambda = \frac{2U}{\pi} (\sin \beta \pi) (b^2 - a^2)^{\frac{1}{2}} I_{+}(a, b)$$
 (14)

where

$$I_{\pm}(a,b) = \int_{0}^{1} \frac{\left[1_{\pm}(1-\zeta^{2})^{\frac{1}{2}}\right]^{2\beta} \zeta^{1-2\beta}}{\left(\zeta^{2}+a^{2}\right)\left(\zeta^{2}+b^{2}\right)^{\frac{1}{2}}} d\zeta$$
 (15)

The parameters, a and b, are related to the upstream velocity, U, and the maximum wall velocity, V_{ψ} by (7) and

$$b = a(V) \tag{16}$$

respectively. In order to examine the rate-of-change of b as the 'tunnel spacing-ratio' λ is varied, and the role played by the minimum pressure p_b and the maximum velocity V on the wall, as was once investigated by Meijer (1967) (see Eq. (2)), we also introduce a new cavitation number σ^{μ} based on p_b and V as

$$\sigma^{ai} = (p_b - p_c) / (\frac{1}{2} \rho V^2) = V^{-2} - 1 = \sigma(V)$$
, (17)

where $\sigma(U)$ gives the conventional cavitation number

$$\sigma = \sigma(\mathbf{U}) = \mathbf{U}^{-2} - \mathbf{1} \tag{18}$$

The unbounded-flow limit $\lambda=0$ is reached as $b\to a$, which implies $V\to U$ and $\sigma''\to \sigma$. In order to estimate C_D for small λ , we expand $C_D(\sigma,\lambda)$ given by (13) in Taylor series for $|\sigma''-\sigma|\ll 1$,

$$\frac{C_{D}(\sigma,\lambda)}{1+\sigma} = \frac{C_{D}(\sigma,0)}{1+\sigma} + (\sigma''-\sigma) \frac{\partial}{\partial \sigma''} \frac{C_{D}(\sigma,\lambda)}{1+\sigma} \Big|_{b=a} + O(\sigma''-\sigma)^{2} . \quad (19)$$

Now, by (13), (16) and (17),

$$\left. \frac{\partial}{\partial \sigma^{\dag \dag}} \left. \frac{C_D(\sigma,\lambda)}{1+\sigma} \right|_{b=a} = - \left[\frac{\partial}{\partial b} \left. \frac{I_-(a,b)}{I_+(a,b)} \right] \frac{db}{dV} \left. \frac{dV}{d\sigma^{\dag \dag}} \right|_{b=a} \right.$$

Since the functional dependence of σ'' on b is the same as that of σ on a (see (7), (16), (17), (18)), we have

$$\frac{db}{dV} \frac{dV}{d\sigma^{\dagger\dagger}} \bigg|_{b=a} = \frac{da}{dU} \frac{dU}{d\sigma} .$$

Furthermore, from (15) it immediately follows

$$\frac{\partial}{\partial b} I_{\pm}(a,b) \Big|_{b=a} = \frac{1}{3} \frac{d}{da} I_{\pm}(a,a)$$
.

Combining these results, we have

$$\frac{\partial}{\partial \sigma^{\dagger \dagger}} \frac{C_{D}(\sigma, \lambda)}{1 + \sigma} \bigg|_{b=a} = -\frac{1}{3} \frac{d}{da} \left(\frac{I_{-}(a, a)}{I_{+}(a, a)} \right) \frac{da}{d\sigma} = \frac{1}{3} \frac{d}{d\sigma} \frac{C_{D}(\sigma, 0)}{1 + \sigma} \quad . \tag{20}$$

Upon substituting (20) in (19), the resulting equation can evidently be written as

$$\frac{C_D(\sigma,\lambda)}{1+\sigma} = \frac{C_D(\sigma^1,0)}{1+\sigma^1} + O(\lambda^2) \quad , \tag{21}$$

where

$$\sigma' = \sigma + \frac{1}{3} (\sigma'' - \sigma) = \frac{2}{3} \sigma + \frac{1}{3} \sigma''$$
, (22)

and σ'' is given by (17), which can either be calculated from (14) and (16) or be obtained by actual measurement in experiments. This correction rule has also been used to compare corrected estimates of $C_D(\sigma',0)$ with the numerical results of the exact

solution $C_D(\sigma, 0)$; the agreement is again excellent for wedges of all angles with $\lambda \le 1/6$, $\sigma \le 1$. An example is shown in Fig. 1 for $\beta \pi = 15^{\circ}$. Its application in experiments will be discussed in Sect. 5.

It is noteworthy that (21) is identical to (11); only σ^* is different in these two theoretically derived wall-correction rules. To this end, we note that σ^* in (12) is known once σ, λ , and $C_D(\sigma, \lambda)$ are measured, whereas in (22), (17), σ^* requires an additional measurement of either V or P_b .

Another point worthy of note is that although the significance of σ^{IM} has been explored earlier by Meijer (1967), its use in Meijer's empirical rule leads to an over-correction of the wall effect on drag coefficient. This is indicated in Fig. 1 for $\beta \pi = 15^{\circ}$. This is because in Meijer's rule, σ^{IM} takes the place of σ^{I} , instead of a weighted contribution as given by (22).

In the choked flow limit, $V \to I$ and $\sigma^{\parallel} \to 0$ and (22) becomes $\sigma^{\parallel} = \frac{2}{3} \sigma$

so that (21) is

$$\frac{C_{D}(\sigma,\lambda)}{1+\sigma} = \frac{C_{D}\left(\frac{2}{3}\sigma,0\right)}{1+\frac{2}{3}\sigma}$$
 (23)

This equation gives the choked flow drag coefficient if the unbounded drag coefficient as a function of σ is known, or visa versa. As an example of the use of (23) we estimate the choked flow C_D for $\beta \pi = 15^{\circ}$ in Fig. 1 and compare this with the computed value.

Finally, we observe that in these two sets of wall correction rules the body configuration has become implicitly absorbed in the drag coefficient as one of its argument (i.e. $C_D(\sigma,\lambda;\beta)$). In view of the result that these correction rules are extremely accurate over the entire range of β (0 < β < 1), it is reasonable to expect that they are also valid for bodies of arbitrary shape, at least for those with not too great curvatures of their surface profiles.

3. Experimental Arrangements

Four wedges of vertex angle $2\beta \pi = 7\frac{1}{2}^{\circ}$, 9°, 15° and 30° (chord \approx 6 in.) were tested in the high speed water tunnel at the California

Institute of Technology, utilizing the 6 in. span, two dimensional working section (Kiceniuk (1964)) whose normal height is 30 inches. However by fitting the tunnel with inserts the 9° and 30° wedges were also run with a wall spacing of 13.45 in. (see Fig. 2). The models were supported in the center of the tunnel on a three component force balance for direct measurement of total drag. At the conclusion of each set of experiments the total drag forces on the fairing plate and wedge supports were measured by replacing that plate by a blank, supporting the wedge in the same position but fastened to the opposite side-wall and measuring the drag registered under conditions identical to those of the main experiments. Subtracting this tare drag from the original drag reading yielded a measure of the force on the wedge alone.

A working section reference pressure, p_T , was measured at a point in the center of the side-wall about 7 in. upstream of the leading edge of the model using a water/mercury/air manometer (see next section). The hypothetical 'free stream' velocity in the working section, U, was inferred from the difference between p_T and the pressure upstream of the convergent section. A series of static pressure taps on the lower wall (see Fig. 2) were connected to an inverted water manometer referenced to p_T for the purpose of determining the wall pressure distribution. Since some differences were observed even with no model installed in the tunnel, values more representative of the effect of the model were obtained by using these "clear tunnel" readings as datum.

All four wedges included a base pressure tapping used to measure cavity pressure, p_c, the technique employed being a familiar one (Brennen (1969a)). The pressure line is connected through a two way push pull valve to an air supply adjusted so that the air flow keeps the line free of liquid. Activating the valve cut off this supply and connected in an air/mercury/water manometer from which, following an interval of a few seconds, the difference (p_T-p_C) could be obtained.

Two of the wedges, the 9° and 30°, were built up from the basic model used by Meijer (1967) in order to utilize the static pressure tubes distributed along one face of that model. Fifteen of these were connected to a water/mercury manometer board referred to p_T in order to obtain wetted surface pressure distributions; bleeding of these lines before every

reading was required to obtain reliable data.

For each model configuration data was obtained over a series of cavitation numbers, o, at a few selected velocities, U. However, apart from the limit imposed by flow choking (i.e. $\sigma > \sigma_c$), there were certain other physical limitations upon the range of σ which could be safely and satisfactorily covered at a particular velocity. At higher velocities (35 to 50 ft/sec depending on model size) readings could be obtained only up to a certain σ , for above this either the drag exceed that measurable by the balance (120 lbs) or the vibration of the whole structure became excessive. At lower velocities (25 to 40 ft/sec depending on model size) a minimum σ was usually imposed by the fact that an excessive number of vapor/air bubbles appeared in the pressure lines when p_T was less than about 0.45 ft. of mercury. In the case of the reduced tunnel, vibration of the inserts and oscillation of the flow around them was an added hazard. In general, however, an acceptable range of σ could be obtained by combining the results at two velocities, one in the higher range, the other in the lower.

4. Experimental Results

A recurring problem in water tunnel experiments arises in determining a hypothetical, "free stream" pressure corresponding to the remote pressure, p_{∞} of potential flow calculations which assume the working section to be infinitely long. In a tunnel of constant section a favorable longitudinal pressure gradient is produced by boundary layer growth on the walls. In the present tunnel this could be overcome by flairing the side walls (Kiceniuk (1964)). Then the longitudinal pressure gradient is given roughly by

$$\frac{\partial C_{p}}{\partial x} = \frac{2}{S} \frac{\partial S}{\partial x} - \frac{4(S+h)}{Sh} \frac{\partial \delta}{\partial x}$$
 (24)

where $\delta_{\rm D}$ is some mean boundary layer displacement thickness, x is the centerline distance and S(x) is the span or tunnel width. Under normal operational conditions the boundary layer is probably turbulent so that $\partial \delta_{\rm D}/\partial x$ may be given by 0.038(ν/xU)^{1/5}

though the effective origin of x is difficult to estimate. However both the experiments of Kiceniuk (1964) and the above formula when, say, $x^{1/5}$ is of order 1 ft $^{1/5}$ and U is between 30 and 50 ft/sec indicate that $\partial C_p/\partial x$ is roughly zero when $\partial S/\partial x$ is about 0.003. Thus the flair is set at this value. Nevertheless since pressures are to be measured on the model itself it seems wise to locate the reference pressure tap as close to the model as possible, yet far enough away for the influence of the pressure field around the model to be negligible. The choice of a tap 7 in. from the leading edge of the model (see Fig. 2) involved such compromises. Theoretical estimates indicated that the pressure field influence was less than $\Delta C_p = 0.01$ at that point. Further upstream the influence of the tunnel convergent section is felt; for example 6 in. further upstream, C_p was of the order of 0.03 higher.

It will be seen that of the theoretical models that of Riabouchinsky yields results closest to the experimental measurements. To avoid confusion by profusion comparison is made in most of the figures only with that model, whilst comments on the other model will be included in the text. Typical pressure distributions on the faces of the 9° and 30° wedges are shown in Figs. 3,4,5 where s is measured along the wetted surface from the leading edge and s = C at separation. These agree quite well with the theory though two deviations are noteworthy: (i) the lower experimental C close to the leading edge are probably due to a slight downward inclination of the incident stream since small negative lifts were also registered by the balance; (ii) near the trailing edge the experimental C are slightly above the theory, especially when the flow is close to being choked. This second effect may be partly due to the presence of small air/vapor bubbles in the tubes registering these low pressures though there may also be some contribution from the complex boundary layer flow near separation.

The coefficients of drag are plotted in Figs. 6 and 7. Graphic integration of the experimental pressure distributions yields results in excellent agreement with the Riabouchinsky model theory. The direct measurements, corrected for tare drag, showed a greater scatter and the comparison is poorer. An estimate of the skin friction component of this total drag was obtained using the Faulkner Skan solutions for the

boundary layer flow near the leading edge of a wedge. Then

$$(\Delta C_{D})_{Viscous} = \frac{2\sqrt{2(n+1)}}{(3n+1)} \frac{A^{\frac{3}{4}}}{\tan \beta \pi} f''(0) \left(\frac{\nu}{CU}\right)^{\frac{1}{2}}$$
 (25)

where $n = \beta/(1-\beta)$, A represents the strength of the leading edge singularity which is estimated from the value of $(1-C_p)\left(\frac{C}{s}\right)^n$ near that point and takes a value of about unity. In the conventional notation, f''(0) is a known function of β available in tables of Faulkner Skan solutions. The work of Ackerberg (1970) would indicate that the contribution of the rapidly accelerating flow near the trailing edge is small in comparison. Equation (25) yields respective values of 0.012 and 0.006 for the 9° and 30° wedge experiments and these are included in the figures, with, as can be seen, mixed results.

The more reliable data, namely the pressure integrated drag coefficients could also be compared with the results of the open-wake theoretical model. However it is clear from the agreement with the Riabouchinsky model and the difference between the two theoretical models (Wu, Whitney and Lin (1969)) that the experimental values will lie significantly below the open-wake theory except close to the choked condition where the theories virtually coincide in any case. The difference would be especially marked for small ℓ/h at moderate to high σ_{ℓ} Comparison could also be made with the results of the linearized theory of Cohen and Gilbert (1957). As expected the linearized theory yields values of $C_{\rm D}$ substantially greater than either the exact theory or the experiments. This is exemplified in Fig. 1 where it is seen that the linearized theoretical choked flow line is actually above the unbounded flow line for a 30° wedge. The difference is less for wedges of smaller β π_{ℓ}

Sample wall pressure distributions, referenced to clear tunnel values as mentioned in the last section, are presented in Fig. 8 for the case of the 9° wedge. Note that the cavity wake causes the experimental curves to asymptote to a non-zero C_p downstream of the cavity. Thus the actual curves correspond to a compromise on the Riabouchinsky model theory in the direction of the open-wake model (the curves for which are not shown but decrease monotonically toward a value $C_p = -\sigma$). This

deviation clearly causes a slight reduction of the minimum wall pressure below the Riabouchinsky model value. This occurred consistently as can be seen from Fig. 9 where the minimum wall pressures for all model configurations are plotted against σ . Nevertheless the agreement with theory is satisfactory.

The pressure-integrated drag on the 9° and 30° wedges are corrected for wall effect using the relations (21), (22) and the experimental values of minimum wall pressure. The results are shown with the original points and the theoretical Riabouchinsky curves in Figs. 10 and 11. Clearly the results are very satisfactory since the rule collapses the points for different ℓ/h onto a single line very close to the unbounded theoretical line. The only noticeable deviation is at low σ where the experimental points lie somewhat above that theoretical curve.

5. Concluding Remarks

The two basic conclusions to be drawn from the present work are as follows:

- (1) The experimental results agree very well with the theory which employs the Riabouchinsky model. Agreement with other models is less good.
- (2) The rules for the correction of wall effect which are based on the Riabouchinsky model and use the value of the minimum pressure on the tunnel wall are found to be eminently satisfactory. They may indeed be applicable to a much wider variety of cavitating flow.

Acknowledgment

The authors have pleasure in expressing their appreciation and gratitude to Professor Francis Clauser for invaluable encouragement, and to the Division of Engineering and Applied Science of the California Institute of Technology for the entire support to carry out the experimental investigation using the High-Speed Water Tunnel facility of the Hydrodynamics Laboratory.

The early part of the main theoretical study was carried out under the support of the Naval Ship System Command General Hydrodynamics Research Program, SR 009 0101, and Hydrofoil Advanced Development Program S 46-06, Contract N00014-67-A-0094-0007, administered by the Naval Ship Research and Development Center, with the results reported by Wu, Whitney and Lin (1969), and the latter part, with further results presented herein, under the support of the Office of Naval Research.

References

- Ackerberg, R.C. (1970) Boundary layer separation at a free streamline. Proc. of 2nd Int'l. Conf. on Numerical Methods in Fluid Mechanics, Berkeley, Calif. Sept. 15 - 19.
- Barr, R.A. (1966) An investigation of the cavity flow behind drag discs and supercavitating propellers. M.S. Thesis, Univ. of Maryland.
- Brennen, C. (1969a) Dynamic balances of dissolved air and heat in natural cavity flows. Jour. of Fluid Mechanics, 37, 1.
- Brennen, C. (1969b) A numerical solution of axisymmetric cavity flows.

 Jour. of Fluid Mechanics, 37, 1.
- Cohen, H. and Gilbert, R. (1957) Two-dimensional, steady, cavity flow about slender bodies in channels of finite bredth. J. Appl. Mech. 24, 170 176.
- Dobay, G.F. (1967) Experimental investigation of wall effect on simple cavity flows. Proc. Symp. Testing Techniques in Ship Cavitation Research. Vol. 1, 175 230, Skipsmodelltanken, Trondheim, Norway.
- Kiceniuk, T. (1964) A two-dimensional working section for the high speed water tunnel at the California Institute of Technology. ASME; Cav. Res. Fac. and Tech.
- Meijer, M.C. (1967) Pressure measurement on flapped hydrofoils in cavity flows and wake flows. J. Ship. Res. 11, 170 189.
- Morgan, W.B. (1966) The testing of hydrofoils and propellers for fully-cavitating or ventilated operation. Proc. 11th ITTC 202 218, Tokyo, Japan.
- Pope, A. (1954) Wind tunnel testing. Second Edition. John Wiley and Sons, New York.
- Whitney, A.K. (1969) A simple correction rule for wall effect in two-dimensional cavity flow. Cavitation State of Knowledge. New York: ASME.
- Wu, T.Y., Whitney, A.K. and Lin, J.D. (1969) Wall effect in cavity flows. Calif. Inst. of Tech. Rep. No. E-111A.5.

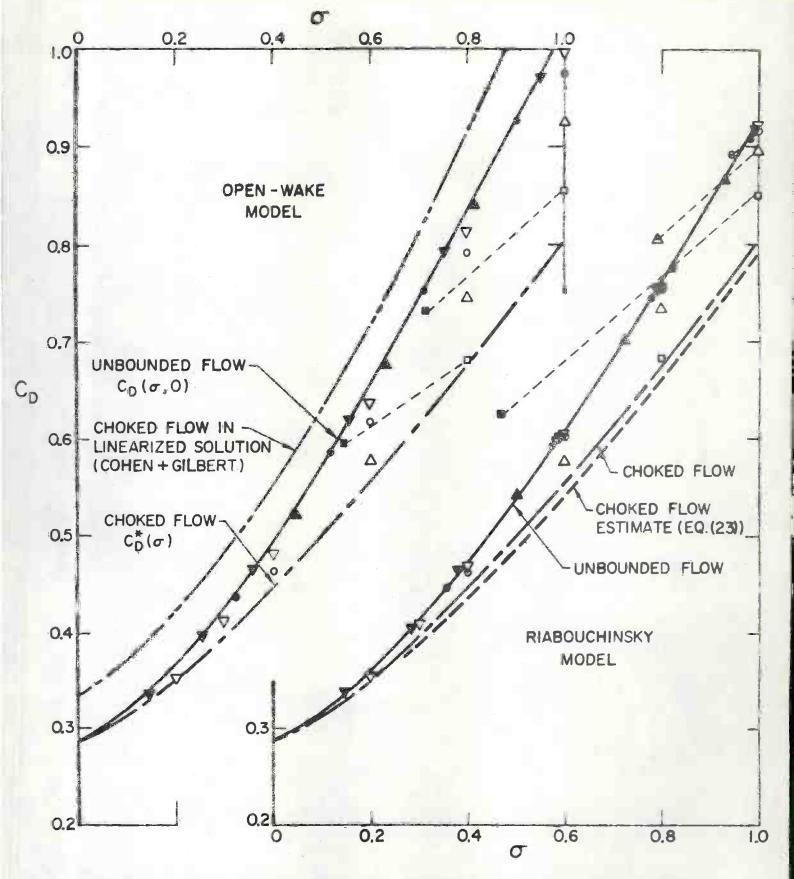


Figure 1 - Correction Rules Checked Against Theoretical Results for 30° Wedge

$\lambda = l/h$	Computed $C_D(\sigma, \lambda)$	Corrected to $C_D(\sigma, 0)$	Meijer's Corrected C'' _D (σ'')				
. 025	\triangledown	₩					
050	0	•	⊖				
.100	Δ	A	A				
.167			B				

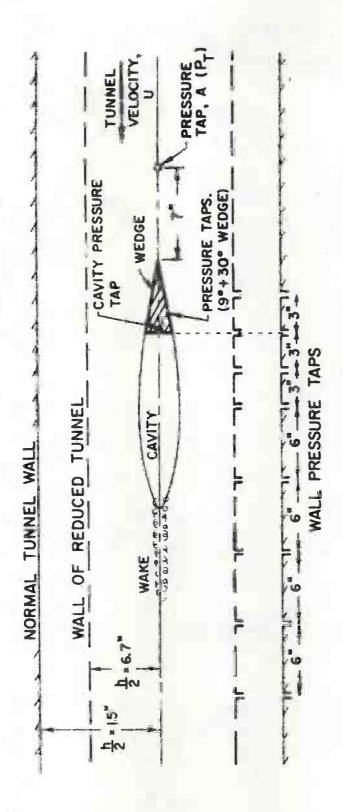


Figure 2 - Diagram of Experimental Arrangement.

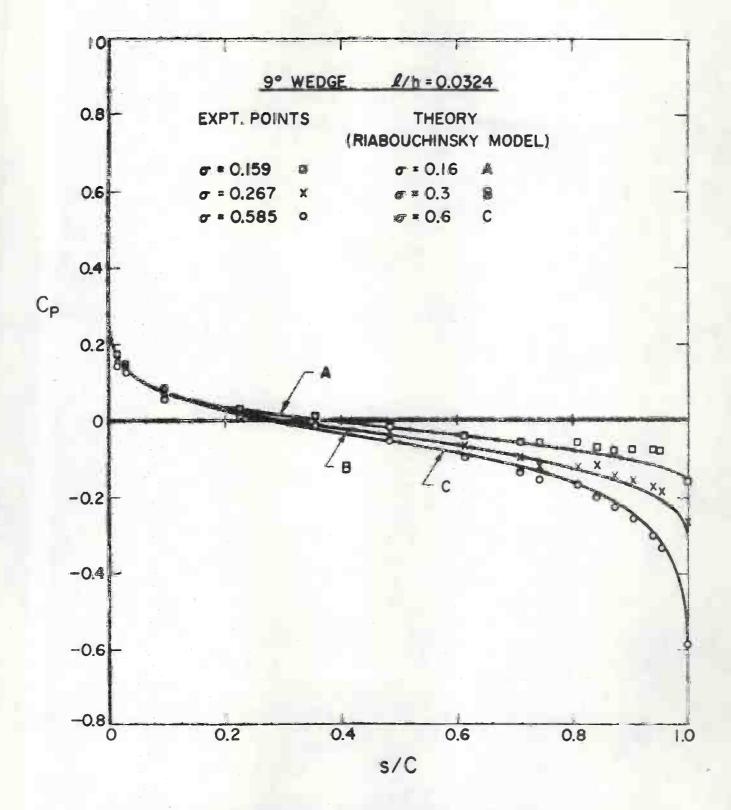


Figure 3 - Pressure Distribution on 9° Wedge in Normal Tunnel.

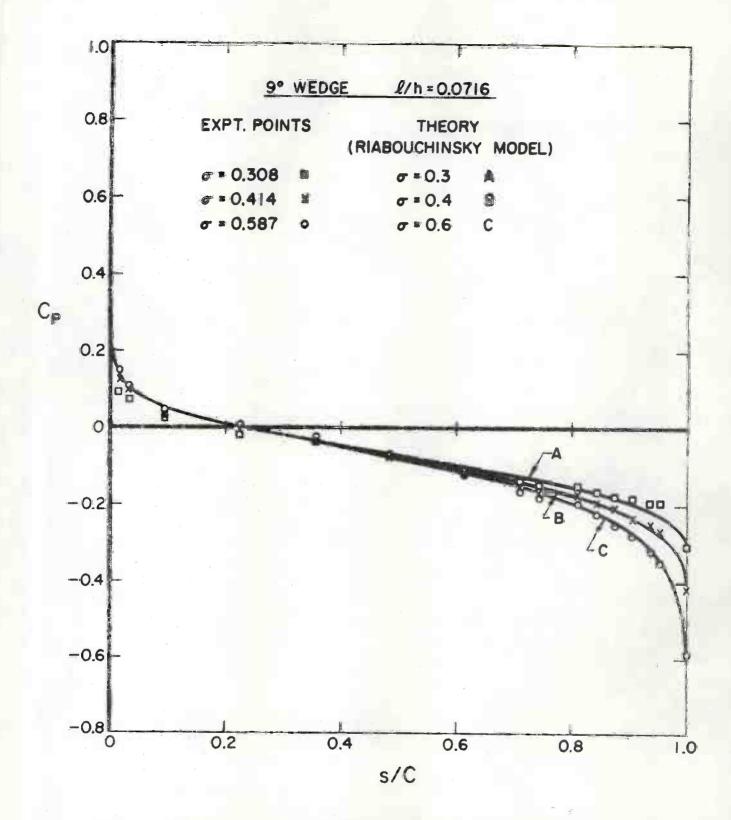


Figure 4 - Pressure Distributions on 9° Wedge in the Reduced Tunnel.

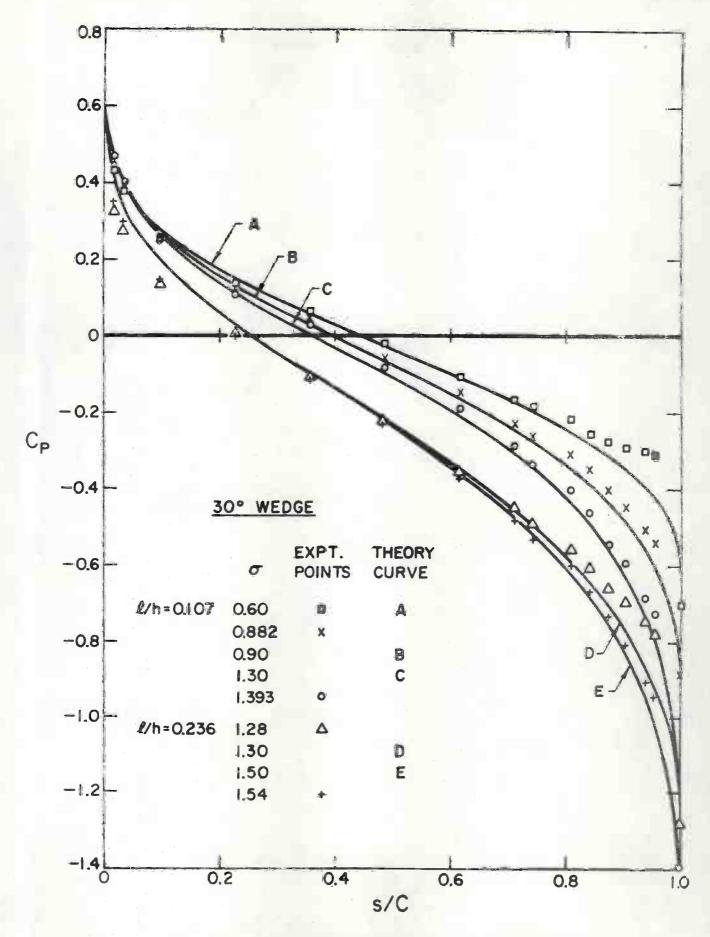


Figure 5 - Pressure Distributions on 30° Wedge.

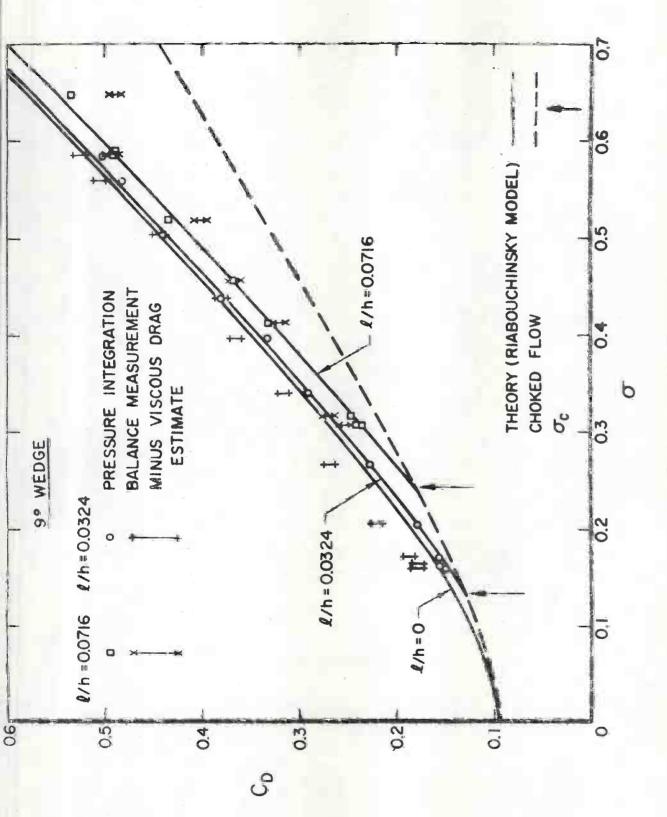


Figure 6 = Drag of 9° Wedge.

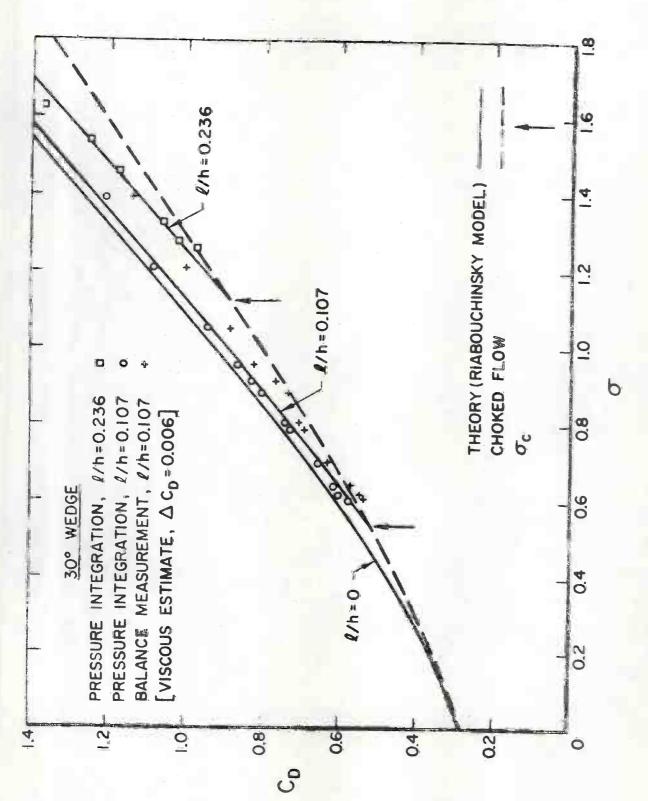


Figure 7 * Drag of 30° Wedge.

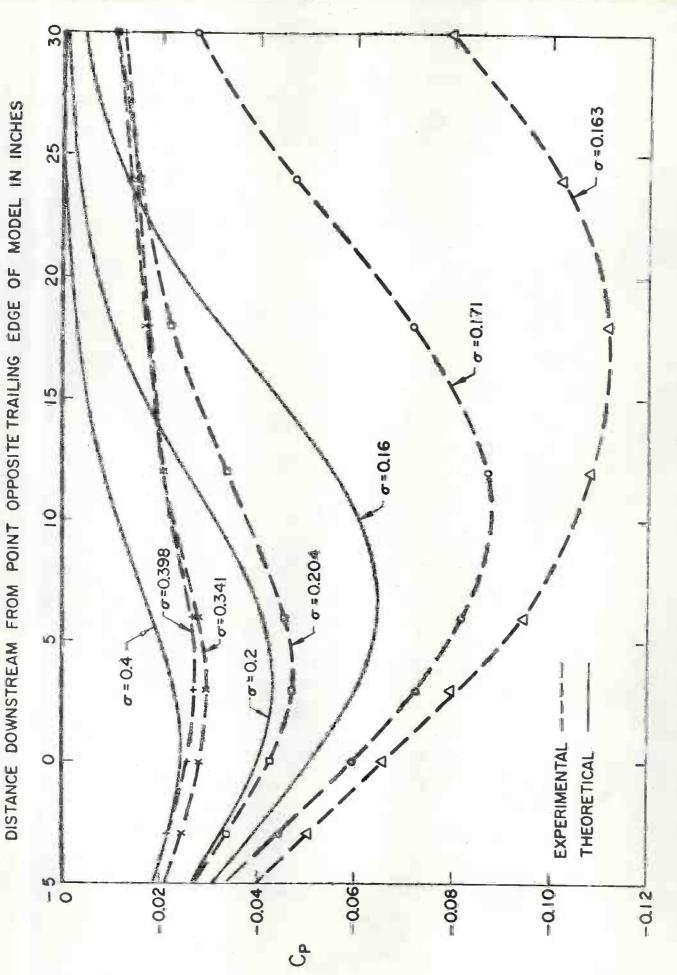


Figure 8 - Sample Wall Pressure Distributions for 2β = 9°, 1/h = 0.0324.

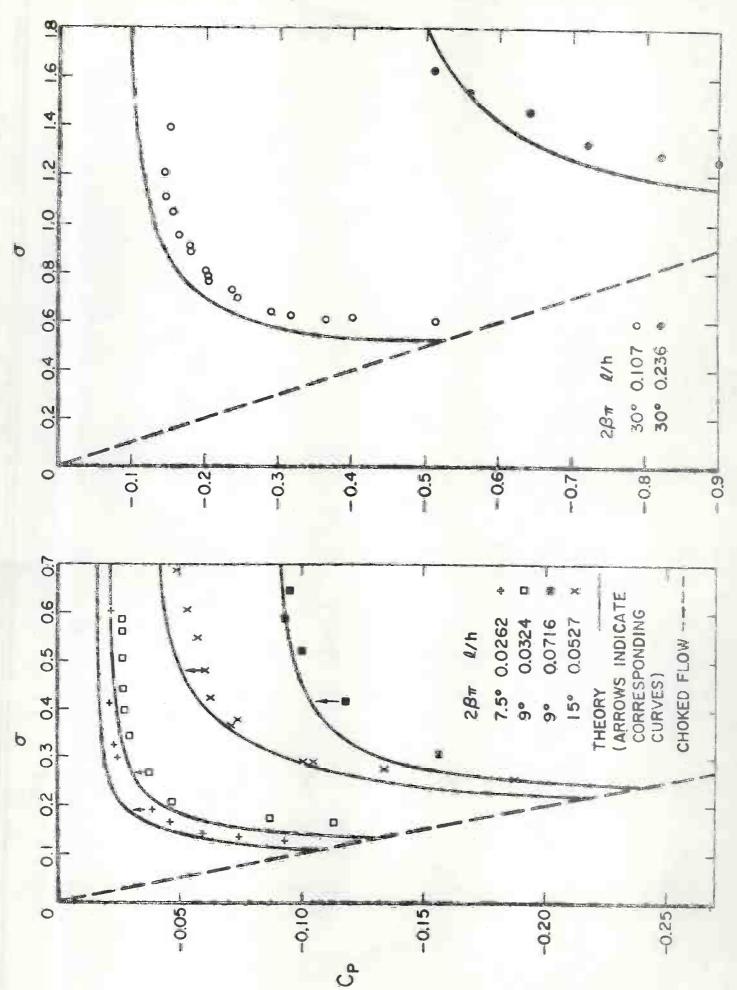


Figure 9 - Minimum Wall Pressure Versus Cavitation Number.

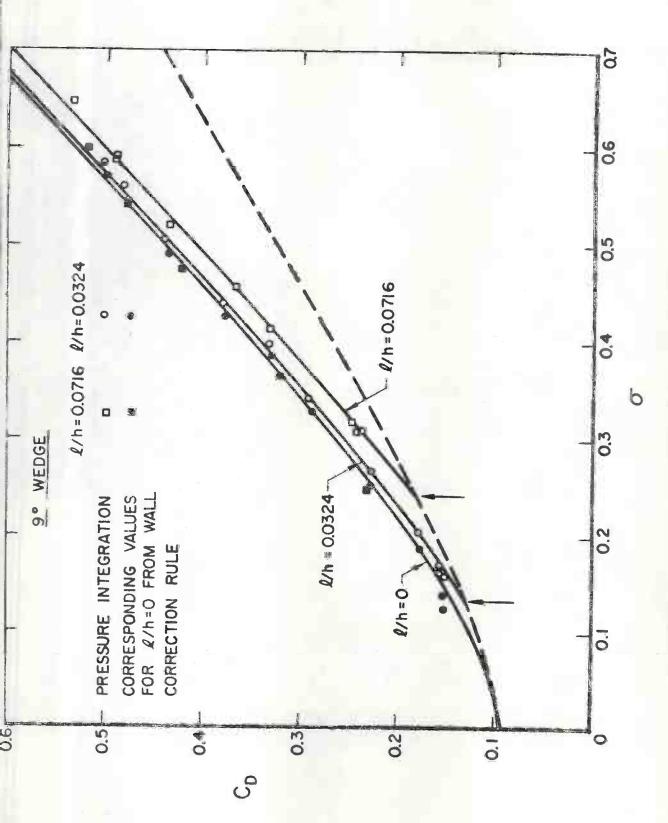


Figure 10 = Application of Wall Correction for 9° Wedge.

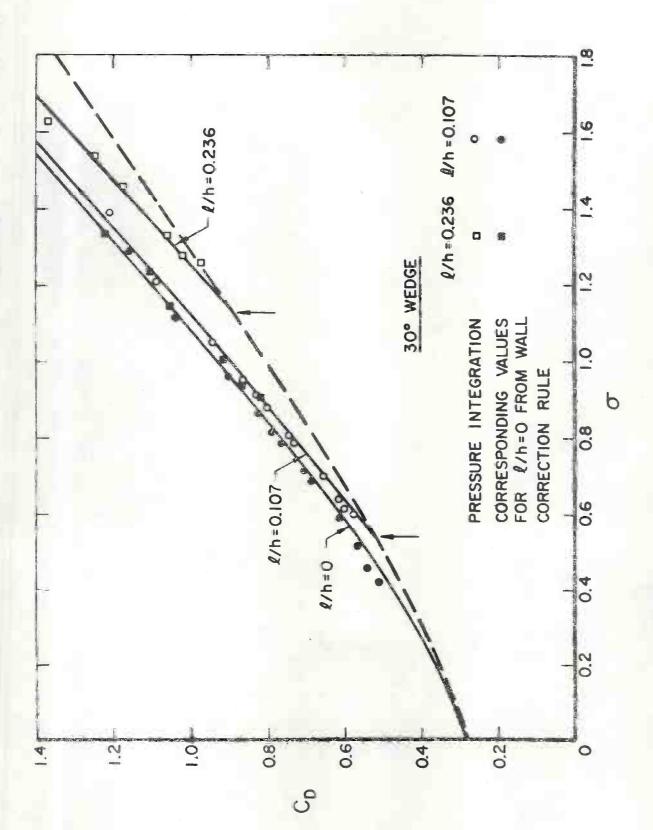


Figure 11 - Application of Wall Correction for 30° Wedge,

DISTRIBUTION LIST FOR UNCLASSIFIED TECHNICAL REPORTS ISSUED UNDER

CONTRACT N0014-67-A-0094-0012 (Single copy unless otherwise specified)

Technical Library
Building 131
Aberdeen Proving Ground, Md. 21005

Defense Documentation Center (20)
Cameron Station
Alexandria, Virginia 22314

Technical Library
Naval Ship Research and Dev. Center
Annapolis Division
Annapolis, Maryland 21402

Professor Bruce Johnson Engineering Department Naval Academy Annapolis, Maryland 21402

Library Naval Academy Annapolis, Maryland 21402

Professor W. P. Graebel
Dept. of Engineering Mechanics
The University of Michigan
College of Engineering
Ann Arbor, Michigan
48104

Professor W. R. Debler Dept. of Engineering Mechanics University of Michigan Ann Arbor, Michigan 48104

Dr. Francis Ogilvie Dept. of Naval Arch. and Marine Eng. University of Michigan Ann Arbor, Michigan 48108

Professor S. D. Sharma Dept. of Naval Arch. and Marine Eng. University of Michigan Ann Arbor, Michigan 48108

Professor W. W. Willmarth Dept. of Aerospace Engineering University of Michigan Ann Arbor, Michigan 48104

Professor Fin C. Michelsen Naval Arch. and Marine Eng. 445 West Engineering Building University of Michigan Ann Arbor, Michigan 48104

AFOSR (REM) 1400 Wilson Boulevard Arlington, Virginia 22204 Dr. J. Menkes
Institute for Defense Analyses
400 Army-Navy Drive
Arlington, Virginia 22204

Professor S. Corrsin
Mechanics Department
The Johns Hopkins University
Baltimore, Maryland 20910

Professor O. M. Phillips The Johns Hopkins University Baltimore, Maryland 20910

Professor L.S.G. Kovasznay The Johns Hopkins University Baltimore, Maryland 20910

Librarian
Department of Naval Architecture
University of California
Berkeley, California 94720

Professor P. Lieber
Department of Mechanical Engineering
University of California
Institute of Engineering Research
Berkeley, California 94720

Professor M. Holt Division of Aeronautical Sciences University of California Berkeley, California 94720

Professor J.V. Wehausen
Department of Naval Architecture
University of California
Berkeley, California 94720

Professor J.R. Paulling Department of Naval Architecture University of California Berkeley, California 94720

Professor E.V. Laitone
Department of Mechanical Engineering
University of California
Berkeley, California 94720

School of Applied Mathematics Indiana University Bloomington, Indiana 47401

Commander
Boston Naval Shipyard
Boston, Massachusetts 02129

Director, Office of Naval Research Branch Office 495 Summer Street Boston, Massachusetts 02210 Professor M. S. Uberoi Department of Aeronautical Engineering University of Colorado Boulder, Colorado 80303

Naval Applied Science Laboratory Technical Library Bldg. 1 Code 222 Flushing and Washington Avenues Brooklyn, New York 11251

Professor J. J. Foody Chairman, Engineering Department State University of New York Maritime College Bronx, New York 10465

Dr. Irving C. Statler, Head Applied Mechanics Department Cornell Aeronautical Laboratory, Inc. P. O. Box 235 Buffalo, New York, 14221

Dr. Alfred Ritter Assistant Head, Applied Mechanics Dept. Cornell Aeronautical Laboratory, Inc. Buffalo, New York 14221

Professor G. Birkhoff
Department of Mathematics
Harvard University
Cambridge, Massachusetts 02138

Commanding Officer
NROTC Naval Administrative Unit
Massachusetts Institute of Technology
Cambridge, Massachusetts 02139

Professor N. Newman
Dept. of Naval Arch. and Marine Eng.
Massachusetts Institute of Technology
Cambridge, Massachusetts 02139

Professor A. H. Shapiro
Department of Mechanical Engineering
Massachusetts Institute of Technology
Cambridge, Massachusetts 02139

Professor C. C. Lin
Department of Mathematics
Massachusetts Institute of Technology
Cambridge, Massachusetts 02139

Professor E. W. Merrill Department of Mathematics Massachusetts Institute of Technology Cambridge, Massachusetts 02139

Professor M. A. Abkowitz
Dept. of Naval Arch. and Marine Eng.
Massachusetts Institute of Technology
Cambridge, Massachusetts 02139

Professor G. H. Carrier
Dept. of Engineering and Applied Physics
Harvard University
Cambridge, Massachusetts 02139

Professor E. Mollo-Christensen Room 54-1722 Massachusetts Institute of Technology Cambridge, Massachusetts 02139 Professor A. T. Ippen Department of Civil Engineering Massachusetts Institute of Technology Cambridge, Massachusetts 02139

Commander
Charleston Naval Shipyard
U. S. Naval Base
Charleston, South Carolina 29408

A. R. Kuhlthau, Director
Research Laboratories for the
Engineering Sciences
Thorton Hall, University of Virginia
Charlottesville, Virginia 22903

Director
Office of Naval Research, Branch Office
219 Dearborn Street
Chicago, Illinois 60604

Library
Naval Weapons Center
China Lake, California 93557

Library MS 60-3 NASA Lewis Research Center 21000 Brookpark Road Cleveland, Ohio 44135

Professor J. M. Burgers
Institute of Fluid Dynamics and App. Math.
University of Maryland
College Park, Maryland 20742

Acquisition Director
NASA Scientific and Technical Information
P. O. Box 33
College Park, Maryland 20740

Professor Pai Institute for Fluid Dynamics and App. Math. University of Maryland College Park, Maryland 20740

Technical Library
Naval Weapons Laboratory
Dahlgren, Virginia 22448

Computation and Analyses Laboratory Naval Weapons Laboratory Dahlgren, Virginia 22448

Professor C. S. Wells LTV Research Center Dallas, Texas 75222

Dr. R. H. Kraichnan Dublin, New Hampshire 03444

Commanding Officer
Army Research Office
Box CM, Duke Station
Durham, North Carolina 27706

Professor A. Charnes The Technological Institute Northwestern University Evanston, Illinois 60201

Dr. Martin H. Bloom Polytechnic Institute of Brooklyn Graduate Center, Dept. of Aerospace Engineering and Applied Mechanics Farmingdale, New York 11735

Technical Documents Center Building 315 U. S. Army Mobility Equipment Research and Development Center Fort Belvoir, Virginia 22060

Professor J. E. Cermak College of Engineering Colorado State University Ft. Collins, Colorado 80521

Technical Library Webb Institute of Naval Architecture Glen Cove, Long Island, New York 11542 La Jolla, California 92037

Professor E. V. Lewis Webb Institute of Naval Architecture Glen Cove, Long Island, New York 11542

Library MS 185 NASA, Langley Research Center Langley Station Hampton, Virginia 23365

Dr. B. N. Pridmore Brown Northrop Corporation NORAIR-Div. Hawthorne, California 90250

Dr. J. P. Breslin Stevens Institute of Technology Davidson Laboratory Hoboken, New Jersey 07030

Dr. D. Savitsky Stevens Institute of Technology Davidson Laboratory Hoboken, New Jersey 07030

Mr. C. H. Henry Stevens Institute of Technology Davidson Laboratory Hoboken, New Jersey 07030

Professor J. F. Kennedy, Director Iowa Institute of Hydraulic Research State University of Iowa Iowa City, Iowa 52240

Professor L. Landweber Iowa Institute of Hydraulic Research State University of Iowa Iowa City, Iowa 52240

Professor E. L. Resler Graduate School of Aeronautical Eng. Cornell University Ithaca, New York 14851

Professor John Miles c/o I.G. P. P. University of California, San Diego La Jolla, California 92038

Director Scripps Institute of Oceanography University of California La Jolla, California 92037

Dr. B. Sternlicht Mechanical Technology Incorporated 968 Albany-Shaker Road Latham, New York 12110

Mr. P. Eisenberg, President (2) Hydronautics Pindell School Road Howard County Laurel, Maryland 20810

Professor A. Ellis University of California, San Diego Dept. of Aerospace and Mech. Eng. Sci.

Mr. Alfonso Alcedan Laboratorio Nacional De Hydraulics Antigui Cameno A. Ancon Casilla Jostal 682 Lima, PERU

Commander Long Beach Naval Shipyard Long Beach, California 90802

Professor John Laufer Dept. of Aerospace Engineering University Park Los Angeles, California 90007

Professor J. Ripkin St. Anthony Falls Hydraulic Laboratory University of Minnesota Minneapolis, Minnesota 55414

Professor J. M. Killen St. Anthony Falls Hydraulic Laboratory University of Minnesota Minneapolis, Minnesota 55414

Lorenz. G. Straub Library St. Anthony Falls Hydraulic Laboratory Mississippi River at 3rd Avenue SE Minneapolis, Minnesota 55414

Dr. E. Silberman St. Anthony Falls Hydraulic Laboratory University of Minnesota 55414 Minneapolis, Minnesota

Professor A. B. Metzner University of Delaware Newark, N. J. 19711

Superintendent
Naval Postgraduate School
Library Code 0212
Monterey, California 93940

Technical Library
USN Underwater Weapons and Research
Engineering Station
Newport, Rhode Island 02840

Technical Library Underwater Sound Laboratory Fort Trumbull New London, Connecticut 06321

Professor J. J. Stoker Institute of Mathematical Sciences New York University 251 Mercer Street New York, New York 10003

Engineering Societies Library 345 East 47th Street New York, New York 10017

Office of Naval Research New York Area Office 207 West 24th Street New York, New York 10011

Director, Naval Research Laboratory (25) Professor A. Acosta Attn: Library, Code 2029 (ONRL) Department of Mecha Washington, D.C. 20390 California Institute of

Professor H. Elrod Department of Mechanical Engineering Columbia University New York, New York 10027

Society of Naval Architects and Marine Engineering 74 Trinity Place New York, New York 10006

Professor S. A. Piascek
Department of Engineering Mechanics
University of Notre Dame
Notre Dame, Indiana 46556

United States Atomic Energy Commission Division of Tech. Information Extension P. O. Box 62 Oak Ridge, Tennessee 37830

Miss O. M. Leach, Librarian National Research Council Aeronautical Library Montreal Road Ottawa 7, Canada

Technical Library
Naval Ship Research and Dev. Center
Panama City, Florida 32401

Library
Jet Propulsion Laboratory
California Institute of Technology
4800 Oak Grove Avenue
Pasadena, California 91109

Professor H. Liepmann
Department of Aeronautics
California Institute of Technology
Pasadena, California 91109

Technical Library Naval Undersea Warfare Center 3202 E. Foothill Boulevard Pasadena, California 91107

Dr. J. W. Hoyt Naval Undersea Warfare Center 3202 E. Foothill Boulevard Pasadena, California 91107

Professor T. Y. Wu
Department of Engineering
California Institute of Technology
Pasadena, California 91109

Director, Office of Naval Research Branch Office, 1030 E. Green Street Pasadena, California 91101

Professor A. Acosta
Department of Mechanical Engineering
California Institute of Technology
Pasadena, California 91109

Naval Ship Engineering Center Philadelphia Division, Technical Library Philadelphia, Pennsylvania 19112

Technical Library (Code 249B) Philadelphia Naval Shipyard Philadelphia, Pennsylvania 19112.

Professor R. C. MacCamy Department of Mathematics Carnegie Institute of Technology Pittsburgh, Pennsylvania 15213

Dr. Paul Kaplan Oceanics, Inc. Plainview, Long Island, New York 11803

Technical Library Naval Missile Center Point Mugu, California 93441

Technical Library Naval Civil Engineering Laboratory Port Hueneme, California 93041

Commander
Portsmouth Naval Shipyard
Portsmouth, New Hampshire 03801

Commander, Norfolk Naval Shipyard Portsmouth, Virginia 23709 Professor F. E. Bisshopp Division of Engineering Brown University

Providence, Rhode Island 02912

Dr. L. L. Higgins TRW Space Technology Labs, Inc. One Space Park Redondo Beach, California 90278

Redstone Scientific Information Center Attn: Chief, Document Section Army Missile Command Redstone Arsenal, Alabama 35809

Dr. H. N. Abramson Southwest Research Institute 8500 Culebra Road San Antonio, Texas 78228

Editor, Applied Mechanics Review Southwest Research Institute 8500 Culebra Road San Antonio, Texas 78206

Naval Command Control Communications Laboratory Center San Diego, California 92152

Library and Information Services General Dynamics-Convair P. O. Box 1128 San Diego, California 92112

Commander (Code 246P) Pearly Harbor Naval Shipyard Box 400 FPO San Francisco, California 96610

Technical Library (Code H245C-3) Hunters Point Division San Francisco Bay Naval Shipyard San Francisco, California 94135

Office of Naval Research San Francisco Area Office 1076 Mission Street San Francisco, California 94103

Dr. A. May Naval Ordnance Laboratory, White Oak Silver Spring, Maryland 20910

Fenton Kennedy Document Library The Johns Hopkins University Applied Physics Laboratory 8621 Georgia Avenue Silver Spring, Maryland 20910

Librarian, Naval Ordnance Laboratory White Oak Silver Spring, Maryland 20910

Dr. Byrne Perry Department of Civil Engineering Stanford University Stanford, California 94305

Professor Milton Van Dyke Department of Aeronautical Engineering Stanford University Stanford, California 94305

Professor E. Y. Hsu Department of Civil Engineering Stanford University Stanford, California 94305

Dr. R. L. Street Department of Civil Engineering Stanford University Stanford, California 94305

Professor S. Eskinazi Department of Mechanical Engineering Syracuse University Syracuse, New York 13210

Professor R. Pfeffer Florida State University Geophysical Fluid Dynamics Institute Tallahassee, Florida 32306

Professor J. Foa Department of Aeronautical Engineering Rennsselaer Polytechnic Institute Troy, New York 12180

Professor R. C. DiPrima Department of Mathematics Rennsselaer Polytechnic Institute Troy, New York 12180

Dr. M. Sevik Ordnance Research Laboratory Pennsylvania State University University Park, Pennsylvania 16801

Professor J. Lumley Ordnance Research Laboratory Pennsylvania State University University Park, Pennsylvania 16801

Dr. J. M. Robertson Dept. of Theoretical and Applied Mechanics University of Illinois Urbana, Illinois 61803

Shipyard Technical Library Code 130L7 Building 746 San Francisco Bay Naval Shipyard Vallejo, California 94592

Code LA2, Naval Ship Res. and Dev. Ctr. Washington, D.C. 20007

Code 800, Naval Ship Res. and Dev. Ctr. 20007 Washington, D. C.

Code 2027, U. S. Naval Research Lab. (6) Washington, D. C. 20390

Code 438, Chief of Naval Research (3) Department of the Navy Washington, D.C. 20360

Code 513, Naval Ship Res. and Dev. Ctr. Washington, D.C. 20007

Science and Technology Division Library of Congress Washington, D.C. 20540

ORD 913 (Library)
Naval Ordnance Systems Command
Washington, D.C. 20360

Code 6420, Naval Ship Engineering Center Concept Design Division Washington, D.C. 20360

Code 500, Naval Ship Res. and Dev. Ctr. Washington, D.C. 20007

Code 901, Naval Ship Res. and Dev. Ctr. Washington, D.C. 20007

Code 520, Naval Ship Res. and Dev. Ctr. Washington, D.C. 20007

Code 0341, Naval Ship Systems Command Department of the Navy Washington, D.C. 20360

Mr. J. L. Schuler (Code 03412) Naval Ship Systems Command Department of the Navy Washington, D.C. 20360

Dr. J. H. Huth (Code 031) Naval Ship Systems Command Department of the Navy Washington, D.C. 20360

Code 461, Chief of Naval Research Department of the Navy Washington, D.C. 20360

Code 530, Naval Ship Res. and Dev. Ctr. Washington, D. C. 20360

Code 466, Chief of Naval Research Department of the Navy Washington, D.C. 20360

Office of Research and Development Maritime Administration 441 G Street, NW Washington, D.C. 20235

Code 463, Chief of Naval Research Department of the Navy Washington, D.C. 20360

National Science Foundation Engineering Division 1800 G Street, N.W. Washington, D.C. 20550

Dr. G. Kulin
National Bureau of Standard
Washington, D.C. 20234

Code 481, Chief of Naval Research Department of the Navy Washington, D.C. 20390 Code 421, Chief of Naval Research Department of the Navy Washington, D.C. 20360

Commander, Naval Ordnance Systems Com., Code ORD 035 Washington, D.C. 20360

Librarian Station 5-2 Coast Guard Headquarters 1300 E Street, N.W. Washington, D.C. 20226

Division of Ship Design Maritime Administration 441 G Street, N.W. Washington, D.C. 20235

HQ USAF (AFRSTD)
Room 1D 377
The Pentagon
Washington, D.C. 20330

Commander, Naval Ship Systems Comm. Code 6644C Washington, D.C. 20360

Code 525, Naval Ship Res. and Dev. Ctr. Washington, D.C. 20007

Dr. A. Powell (Code 01) Naval Ship Res. and Dev. Ctr. Washington, D.C. 20007

Director of Research Code RR National Aeronautics and Space Admin. 600 Independence Avenue, S.W. Washington, D.C. 20546

Commander, Naval Ord. Systems Comm. Code 03
Washington, D.C. 20360

Code ORD 05411
Naval Ordnance Systems Command
Washington, D.C. 20360

AIR 5301, Naval Air Systems Command Department of the Navy Washington, D.C. 20360

AIR 604, Naval Air Systems Command Department of the Navy Washington, D.C. 20360

Dr. John Craven (PM 1100)
Deep Submergence Systems Project
Department of the Navy
Washington, D.C. 20360

Code 522, Naval Ship Res. and Dev. Ctr. Washington, D.C. 20007

Commander, Naval Oceanographic Office Washington, D.C. 20390

Chief of Research and Development Office of Chief of Staff Department of the Army The Pentagon, Washington, D.C. 20310 Code 6342A, Naval Ship Systems Command Department of the Navy Washington, D.C. 20360

Code 468, Chief of Naval Research Department of the Navy Washington, D.C. 20360

Director, U. S. Naval Research Laboratory Code 6170 Washington, D.C. 20390

Code 473, Chief of Naval Research Department of the Navy Washington, D.C. 20360

Code 6100, Naval Ship Engineering Center Department of the Navy Washington, D.C. 20360

Mr. Ralph Lacey (Code 6114) Naval Ship Engineering Center Department of the Navy Washington, D.C. 20360

Dr. A. S. Iberall, President General Technical Services, Inc. 451 Penn Street Yeadon, Pennsylvania 19050

Dr. H. Cohen
IBM Research Center
P. O. Box 218
Yorktown Heights, New York 10598

Code 2052 (Technical Library) Naval Ship Systems Commany Department of the Navy Washington, D.C. 20360

Department of the Army Coastal Engineering Research Center 5201 Little Falls Road, NW Washington, D.C. 20011

Code 521 Naval Ship Res. and Dev. Ctr. Washington, D.C. 20007

	U	\mathbf{n}	\mathbf{c}	7	a	S	<u>s</u>	Ш		e	Q
Securi	tv	C	1 :1	S	si	fi	c	at	in	n	

Security Classification							
	ENT CONTROL DATA						
(Security classification of title, body of abstract	and indexing annotation mu						
California Institute of Technology	Unclassified 2b: GROUP Not applicable						
Division of Engineering and Appl							
REPORT TITLE				-			
Experimental Verification of Cav	ity-Flow Wall E	ffects and C	orrection Rules				
DESCRIPTIVE NOTES (Type of report and inclusive day Technical Report	tes)						
AUTHOR(5) (First name, middle initial, last name)				-+			
Whitney, Arthur K.							
Brennen, Christopher							
Wu, T. Yao-tsu							
REPORT DATE	78. TOTAL	NO. OF PAGES	7b. NO. OF REFS	-			
November 1970	28		12				
a. CONTRACT OR GRANT NO.	9a. ORIGINA	TOR'S REPORT NE	MBER(S)				
N00014-67-A-0094-0012	F_0	E-97A-18					
b. PROJECT NO.	15-7						
C.	IN OTHER	DE DODE WORL (An-					
	this repo	9b. OTHER REPORT NO(S) (Any other numbers that may be assigned this report)					
d							
O. DISTRIBUTION STATEMENT							
This document has been approved	for public relea	ase and sale	its distribution				
is unlimited.	Langer 4 010		7/				
1. SUPPLEMENTARY NOTES	TZ. SPONSO	RING MILITARY AC	TIVITY	7			

13. ABSTRACT

This report is intended as a companion to Report No. E-111A.5, Wall Effects in Cavity Flows", by Wu, Whitney and Lin. Some simple rules for the correction of wall effect are derived from that theoretical study. Experiments designed to complement the theory and to inspect the validity of the correction rules were then carried out in the high-speed water tunnel of the Hydrodynamics Laboratory, California Institute of Technology. The measurements on a series of fully cavitating wedges at zero angle of attack suggested that of the theoretical models that due to Riabouchinsky is superior. They also confirmed the accuracy of the correction rule derived using that model and based on a measurement of the minimum pressure along the tunnel wall.

Office of Naval Research

22217

Arlington, Va.

•	KEY WORDS	LINE		LINI	K B	LINKC	
		ROLE	WT	ROLE	WT	ROLE	WT
Cavity flow Wall effect							
Wall effect		1 1					
Wall effect co	rrection						
Water tunnel	experiments						
, and the state of		4					
				1			
				1			
						1	
		-					
		1		10			
				ħ.			
		r I		1 1			
		1		9			
				i.			
				1			
						- 1	
					1		
				5			
				Ī		970	
				- Control of the Cont			

DD FORM 1473 (BACK)
(PAGE 2)

Unclassified
Security Classification