

MASTER THESIS

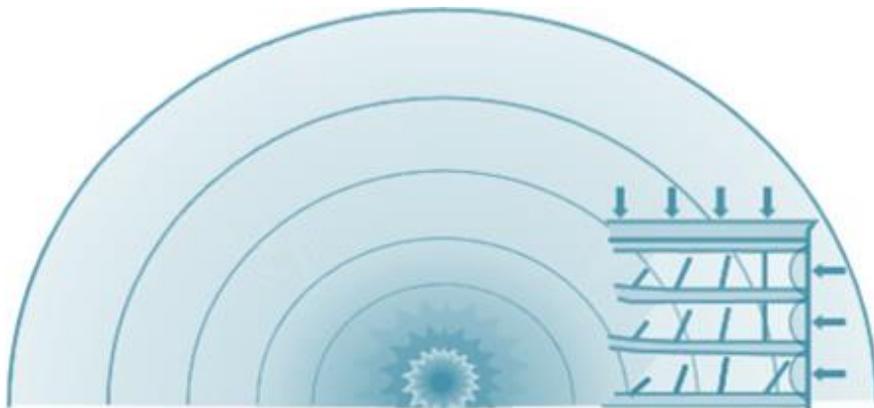
**Prediction of the nonlinear dynamic
behaviour of a concrete slab
subjected to blast load**

Appendix II – Validation experiment 2

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1 Introduction

This appendix presents the results of the experiment conducted in Woomera, Australia in 2004 (Ngo, Mendis, & Krauthammer, 2007). The goal of the experiment is to investigate the structural behaviour of concrete for heavy explosions. The explosion is captured and shown in Figure 1.1. The crater that is left behind is massive, showing the impact of such explosions.

The blast was generated by a 6 t TNT equivalent explosion with a standoff distance of 40 m. This is equivalent to the scaled distance Z of $2.3 \text{ m/kg}^{1/3}$, high enough to be considered 'far field'.



Figure 1.1: Installing panels into concrete frames (top left), Panels ready for blast (top right), Blast, equivalent to 6t of TNT (bottom left), Crater (17m diameter) caused by the blast (bottom right)

The panel of interest is shown in Figure 1.2. Conventional concrete and reinforcement are used in the panel.



Figure 1.2: Panel 4 before the blast

2 Experiment results

The obtained results in the experiment are presented in this chapter. The goal is to recreate these results in the FDM model.

2.1 Observations

There is no displacement-time history graph available for panel 4. Some observations are described in (Ngo, Mendis, & Krauthammer, 2007):

- Concrete is spalled off on the front face, which leaves a cavity of 100 mm width and 30 mm depth.
- A permanent deflection of 142 mm is measured.
- At the rear surface, an approximately 8-mm-wide crack at the midspan is observed.

The concrete panel after the blast trial is shown in Figure 2.1. Figure 2.2 is a scaled illustration of the observations. At the given permanent deflection, the support rotation is 8° .



Figure 2.1: Panel 4 after the blast

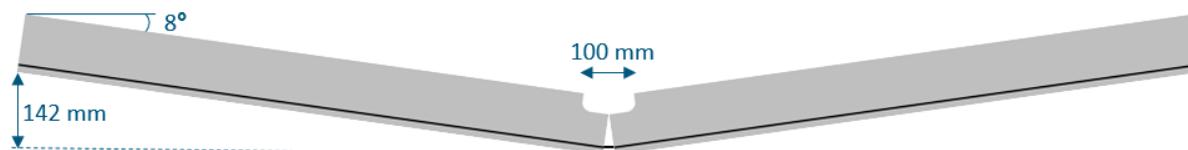


Figure 2.2: Scaled illustration of the observations

3 Parameters

The parameters in the dynamic analysis are strain rate dependant. The strain rate is extracted from the analysis. An average value for the strain rate is used according to (3.1) and (3.2), where t_E is the time to yield the reinforcement bars.

$$\dot{\epsilon}_{c,avg} = 0.002/t_E \quad (3.1)$$

$$\dot{\epsilon}_{s,avg} = f_{dy}/(E_s t_E) \quad (3.2)$$

Table 3.1: Dynamic parameters

| Parameter | Units | Panel 4 |
|---|-----------------|---------|
| Time to yield t_E | s | 0.0065 |
| Concrete strain rate $\dot{\epsilon}_{c,avg}$ | s ⁻¹ | 0.308 |
| Steel strain rate $\dot{\epsilon}_{s,avg}$ | s ⁻¹ | 0.5 |
| DIF _c | - | 1.25 |
| DIF _t | - | 1.46 |
| DIF _E | - | 1.27 |
| DIG _{GF} | - | 1.00 |
| DIF _{GC} | - | 1.25 |

The concrete properties, which are based on an element length of 41.67 mm, are included in Table 3.2. The steel reinforcement properties are provided in Table 3.3.

Table 3.2: Concrete properties

| Parameter | Units | Panel 4 |
|------------------------------------|-------------------|---------------|
| Young's modulus (static / dynamic) | MPa | 33296 / 42285 |
| Initial Poisson's ratio | - | 0 |
| Mass density | Kg/m ³ | 2400 |
| Tensile curve | - | Hordijk |
| Tensile strength (static/dynamic) | MPa | 3.01 / 4.40 |
| Fracture energy | N/m | 137 |
| Poisson's ratio reduction | - | Damage based |
| Compression curve | - | Parabolic |
| Compressive strength | MPa | 39.80 / 49.75 |
| Compressive fracture energy | N/m | 35419 / 44274 |

Table 3.3: Steel reinforcement properties

| Parameter | Units | Panel 4 |
|--|-------|-----------|
| Young's modulus | MPa | 200000 |
| Yield stress (static / dynamic) | MPa | 550 / 645 |
| Ultimate engineering stress (static / dynamic) | MPa | 594 / 691 |
| Ultimate engineering strain | - | 0.05 |

The applied concrete and reinforcement stress-strain relationships are shown in Figure 3.1 and Figure 3.2, respectively.

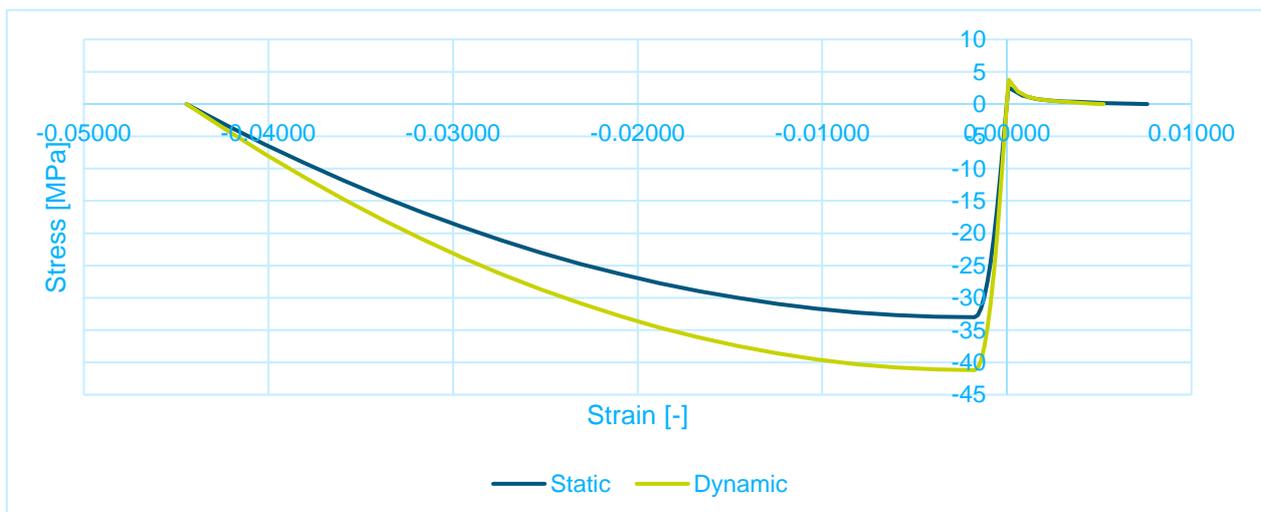


Figure 3.1: Concrete stress-strain relationship for the element length of 41.67 mm

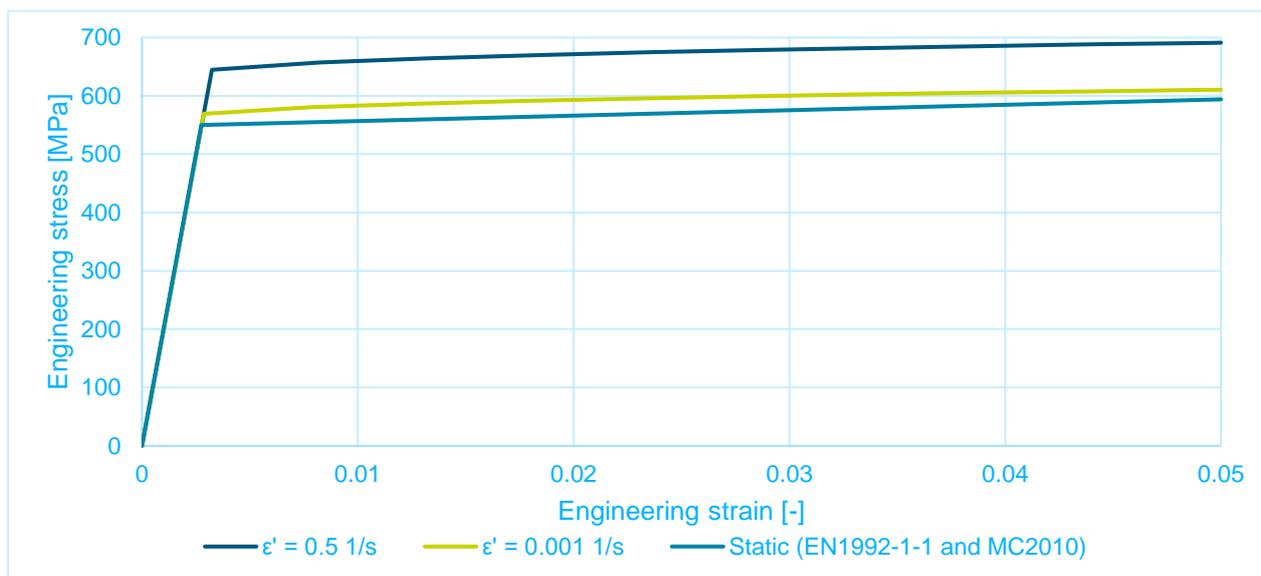


Figure 3.2: Reinforcement stress-strain relationship for panel 4

4 Applied force

The measured reflected pressure is shown in Figure 4.1. The simplification of the measured pressure is indicated in the figure and is approximated by (4.1). The approximating function is shifted by -32.5 ms in Figure 4.1.

$$DIF_t = \begin{cases} 700 - 700 \frac{t}{5.25} & \text{for } 4.5 \text{ ms} \geq t \geq 0 \\ 116 - 116 \frac{t}{32.5} & \text{for } 32.5 \text{ ms} \geq t \geq 4.5 \text{ ms} \end{cases} \quad (4.1)$$

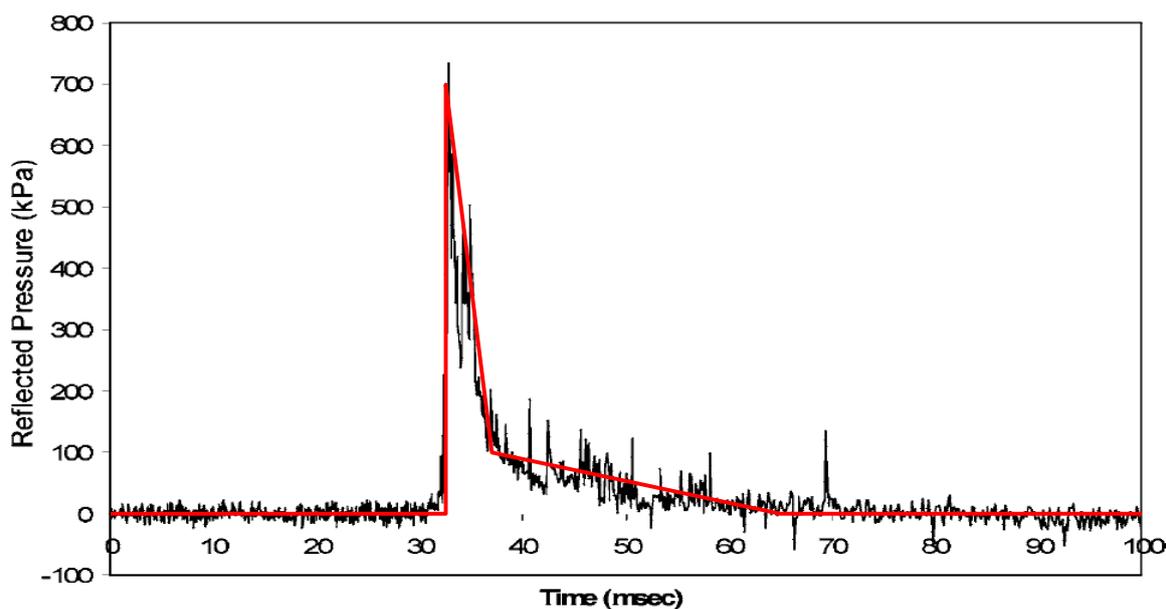


Figure 4.1: Applied pressure on Panel 4

5 Dynamic analysis with FEM comparison

In this chapter, the results of the FDM analyses are presented. A comparison is made with the FEM results.

5.1 Moment curvature relationship

The Moment-curvature (M- κ) graph is manually constructed and shown in Figure 5.1 and more specified in Table 5.1. Noticeable is that the manually constructed M- κ graph fails earlier than the M- κ graph obtained in FEM. This is because the concrete crushes before the reinforcement fails, whereas the failure mechanism in the FEM analysis is reinforcement failure. The stress state at the onset of failure (crushing) is shown in Figure 5.2. It is retrieved from the python script behind the manually constructed M- κ graph.

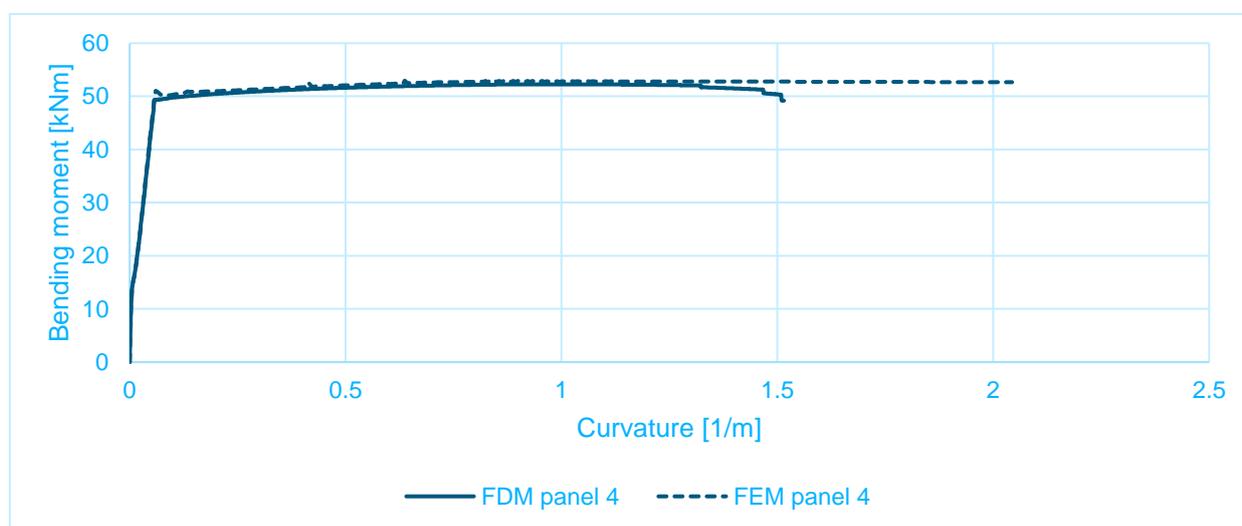


Figure 5.1: M- κ graph for panel 4

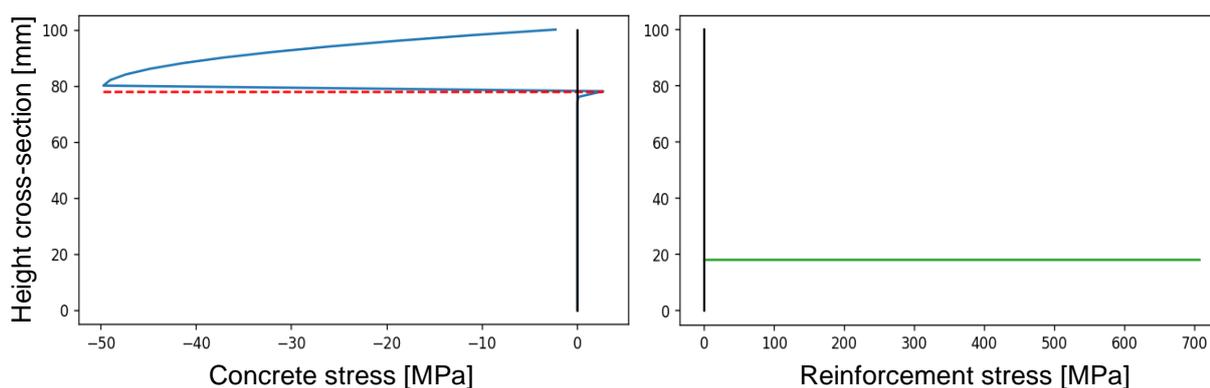


Figure 5.2: Stress state in the cross-section at the onset on failure

Table 5.1: Values for the distinct points in the M-k graph

| | Units | Panel 4 |
|-------------------------|-------|---------|
| Cracking bending moment | kNm | 7.76 |
| Cracking curvature | 1/m | 0.00208 |
| Yielding bending moment | kNm | 49.36 |
| Yielding curvature | 1/m | 0.0576 |
| Ultimate bending moment | kNm | 52.27 |
| Ultimate curvature | 1/m | 1.52 |

5.2 Force-deflection relationship

The force-deflection (F-u) is shown in Figure 5.3 and more specified in Table 5.2: Values for the distinct point in the F-u graph. The permanent deflection is 142 mm, which does not lead to failure according to the F-u graph.

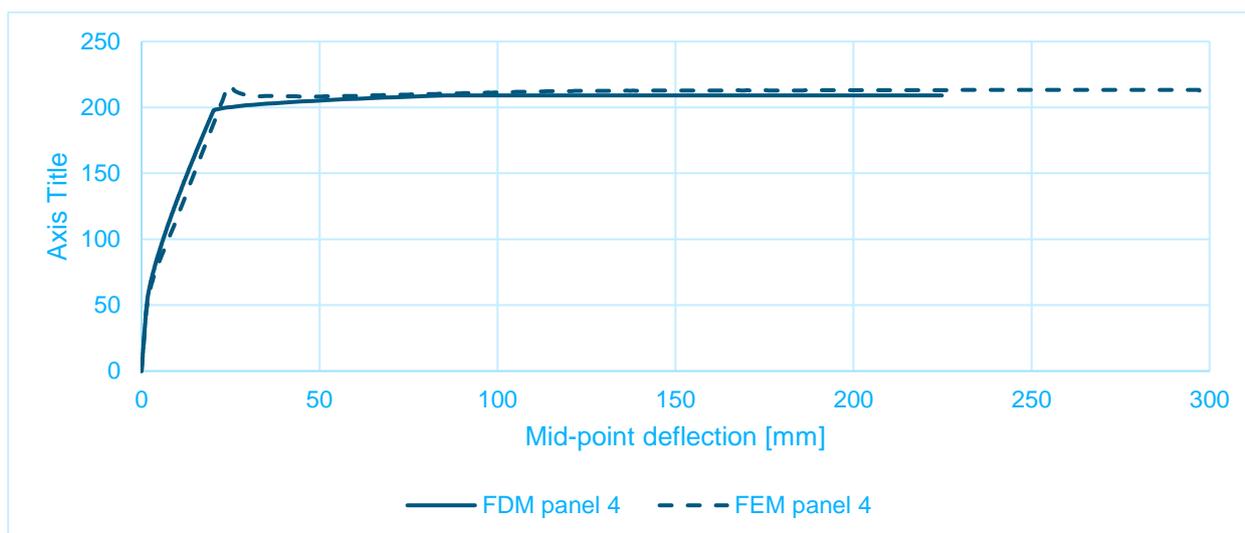


Figure 5.3: F-u graph for panel 4

Table 5.2: Values for the distinct point in the F-u graph

| | Units | Panel 4 |
|---------------------|-------|---------|
| Cracking force | kN | 31.36 |
| Cracking deflection | mm | 0.878 |
| Yielding force | kN | 197.81 |
| Yielding deflection | mm | 20.25 |
| Ultimate force | kN | 209.10 |
| Ultimate deflection | mm | 224.80 |

5.3 Single degree of freedom mass-spring system

The result of the mass-spring system analysis is shown in Figure 5.4.

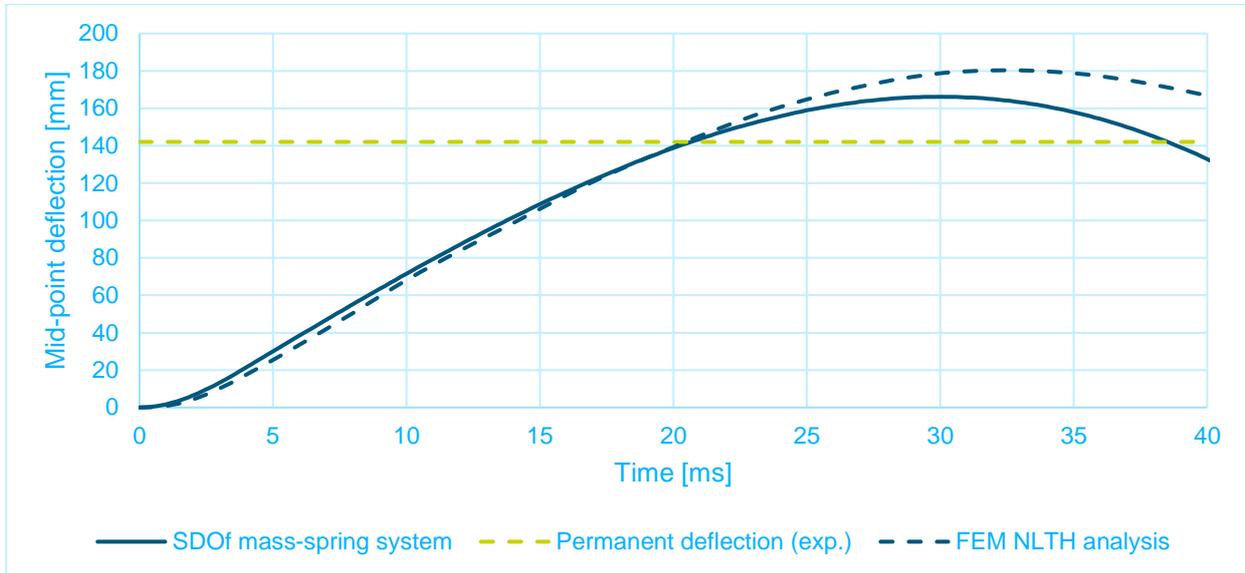


Figure 5.4: Deflection-time history graph of the mass-spring system

6 Discussion

The results of the SDOF mass-spring system are close to the results of the nonlinear time history analysis performed in DIANA. The deflection goes beyond the permanent deflection, which is as expected. Due to the inward acceleration after reaching the maximum deflection and possible effects of the negative phase of the blast (partial vacuum), the slab moves back.

UFC 3-340-02 emphasizes on multiple occasions that crushing may occur at the support rotation of 2 degrees. This experiment shows that this is a rather conservative assumption since the support rotation goes up to 8 degrees. A comprehensive study is performed by (U.S. Army Corps of Engineers, 2008) on the comparison of SDOF analysis to a large data set of experiments (Table 6.1). The referred test series in (U.S. Army Corps of Engineers, 2008) are mostly classified since they were conducted by defence departments. The study gives a good indication of the level of damage at certain support rotations. Up to 2 degrees the damage of the element could be considered moderately. Above the support rotation of 2.6 degrees the damage level is categorised as “heavy” damaged. The transition zone between 2 degrees and 2.6 degrees could lead to “moderate” damage or “heavy” damage. The crucial part of this study is that it shows the ductility of one-way elements beyond the support rotation of 2 degrees up to 6 degrees. This confirms the observations made on the ductility of one-way elements in the validation experiments.

Table 6.1: SDOF analysis on a large data set (U.S. Army Corps of Engineers, 2008)

| Test Series | Test No. | L | Thick (inch) | Depth (inch) | f _{dc} (psi) | f _{dv} (psi) | Reinf. Ratio (%) | Reinf. Index | Support | Weight (psi) | I _{eff} (in ⁴ /in) | E (psi) | M (lb-in/in) | Ru (psi) | K (psi/in) | Mass (psi-ms ² /in) | P (psi) | I (psi-ms) | Pbar | Ibar | Max. Defl. (inch) | Theta (deg) | Damage Level |
|--|-----------|-----|--------------|--------------|-----------------------|-----------------------|------------------|--------------|---------|--------------|--|---------|--------------|----------|------------|--------------------------------|---------|------------|------|------|-------------------|-------------|--------------|
| Scaled Testing, Analysis of Building Components | F1 | 250 | 7.9 | 6.7 | 8000 | 8.5e4 | 0.66 | 0.069 | Simple | 0.68 | 20.3 | 5.1e6 | 2.4e4 | 3.0 | 2.0 | 1753 | 42 | 212 | 13.8 | 0.09 | 5.2 | 2.4 | Heavy |
| | F3 | 250 | 7.9 | 6.7 | 8000 | 8.5e4 | 0.66 | 0.069 | Simple | 0.68 | 20.3 | 5.1e6 | 2.4e4 | 3.0 | 2.0 | 1753 | 15 | 140 | 4.9 | 0.06 | 2.5 | 1.2 | Moderate |
| | F4 | 250 | 7.9 | 6.7 | 8000 | 8.5e4 | 0.66 | 0.069 | Simple | 0.68 | 20.3 | 5.1e6 | 2.4e4 | 3.0 | 2.0 | 1753 | 7 | 72 | 2.3 | 0.03 | 0.8 | 0.4 | Moderate |
| | F5 | 250 | 7.9 | 6.7 | 8000 | 8.5e4 | 0.66 | 0.069 | Simple | 0.68 | 20.3 | 5.1e6 | 2.4e4 | 3.0 | 2.0 | 1753 | 166 | 350 | 54.4 | 0.16 | 7.9 | 3.6 | Heavy |
| | F6 | 250 | 7.9 | 6.7 | 8000 | 8.5e4 | 0.66 | 0.069 | Simple | 0.68 | 20.3 | 5.1e6 | 2.4e4 | 3.0 | 2.0 | 1753 | 4 | 32 | 1.1 | 0.01 | 0.3 | 0.1 | Superfcl |
| | P1-shot 1 | 250 | 5.3 | 4.5 | 8000 | 8.5e4 | 0.66 | 0.069 | Simple | 0.46 | 6.2 | 5.1e6 | 6.8e3 | 0.9 | 0.6 | 1183 | 15 | 72 | 16.6 | 0.06 | 2.4 | 1.1 | Moderate |
| | P1-shot 2 | 250 | 5.3 | 4.5 | 8000 | 8.5e4 | 0.66 | 0.069 | Simple | 0.46 | 6.2 | 5.1e6 | 6.8e3 | 0.9 | 0.6 | 1183 | 167 | 350 | 192 | 0.27 | 13.4 | 6.1 | Haz Fail |
| | P2 | 250 | 5.3 | 4.5 | 8000 | 8.5e4 | 0.66 | 0.069 | Simple | 0.46 | 6.2 | 5.1e6 | 6.8e3 | 0.9 | 0.6 | 1183 | 8 | 76 | 9.6 | 0.07 | 2.4 | 1.1 | Moderate |
| | P3 | 250 | 5.3 | 4.5 | 8000 | 8.5e4 | 0.66 | 0.069 | Simple | 0.46 | 6.2 | 5.1e6 | 6.8e3 | 0.9 | 0.6 | 1183 | 56 | 224 | 64.3 | 0.18 | 11.8 | 5.4 | Heavy |
| | P5 | 250 | 5.3 | 4.5 | 8000 | 8.5e4 | 0.66 | 0.069 | Simple | 0.46 | 6.2 | 5.1e6 | 6.8e3 | 0.9 | 0.6 | 1183 | 15 | 124 | 16.9 | 0.11 | 4.9 | 2.2 | Moderate |
| P6 | 250 | 5.3 | 4.5 | 8000 | 8.5e4 | 0.66 | 0.069 | Simple | 0.46 | 6.2 | 5.1e6 | 6.8e3 | 0.9 | 0.6 | 1183 | 3 | 36 | 3.4 | 0.03 | 0.6 | 0.3 | Superfcl | |
| Airblast Loading on Wall Panels | 150-1 | 94 | 5.9 | 5.0 | 6000 | 7.7e4 | 0.21 | 0.027 | Simple | 0.51 | 8.6 | 4.4e6 | 3.9e3 | 3.6 | 37.4 | 1316 | 62 | 116 | 17.5 | 0.09 | 1.8 | 2.2 | Moderate |
| | 150-2 | 94 | 5.9 | 5.0 | 6000 | 7.7e4 | 0.21 | 0.027 | Simple | 0.51 | 8.6 | 4.4e6 | 3.9e3 | 3.6 | 37.5 | 1317 | 234 | 227 | 65.6 | 0.19 | 4.5 | 5.4 | Heavy |
| | 200-1 | 94 | 7.9 | 7.0 | 4400 | 7.7e4 | 0.26 | 0.041 | Simple | 0.68 | 20.3 | 3.8e6 | 8.7e3 | 7.9 | 75.7 | 1753 | 1008 | 528 | 128 | 0.31 | 3.9 | 4.7 | Heavy |
| | 200-2 | 94 | 7.9 | 7.0 | 4400 | 7.7e4 | 0.26 | 0.041 | Simple | 0.68 | 20.3 | 3.8e6 | 8.7e3 | 7.9 | 75.7 | 1753 | 1008 | 528 | 128 | 0.31 | 3.6 | 4.4 | Heavy |
| | 200-3 | 94 | 7.9 | 7.0 | 4400 | 7.7e4 | 0.26 | 0.041 | Simple | 0.68 | 20.3 | 3.8e6 | 8.7e3 | 7.9 | 75.7 | 1753 | 1008 | 528 | 128 | 0.31 | 3.8 | 4.6 | Heavy |
| | 200-4 | 94 | 7.9 | 7.0 | 4400 | 7.7e4 | 0.26 | 0.041 | Simple | 0.68 | 20.3 | 3.8e6 | 8.7e3 | 7.9 | 75.7 | 1753 | 219 | 227 | 27.8 | 0.12 | 2.1 | 2.5 | Moderate |
| | 200-5 | 94 | 7.9 | 7.0 | 4400 | 7.7e4 | 0.26 | 0.041 | Simple | 0.68 | 20.3 | 3.8e6 | 8.7e3 | 7.9 | 75.7 | 1753 | 529 | 311 | 67.2 | 0.17 | 2.2 | 2.6 | Moderate |
| | 200-6 | 94 | 7.9 | 7.0 | 4400 | 7.7e4 | 0.26 | 0.041 | Simple | 0.68 | 20.3 | 3.8e6 | 8.7e3 | 7.9 | 75.7 | 1753 | 1008 | 528 | 128 | 0.31 | 3.1 | 3.8 | Heavy |
| | 200-7 | 94 | 7.9 | 7.0 | 4400 | 7.7e4 | 0.26 | 0.041 | Simple | 0.68 | 20.3 | 3.8e6 | 8.7e3 | 7.9 | 75.7 | 1753 | 1008 | 528 | 128 | 0.31 | 3.0 | 3.7 | Heavy |
| 200-8 | 94 | 7.9 | 7.0 | 4400 | 7.7e4 | 0.26 | 0.041 | Simple | 0.68 | 20.3 | 3.8e6 | 8.7e3 | 7.9 | 75.7 | 1753 | 1008 | 528 | 128 | 0.31 | 3.1 | 3.7 | Heavy | |
| 200-9 | 94 | 7.9 | 7.0 | 4400 | 7.7e4 | 0.26 | 0.041 | Simple | 0.68 | 20.3 | 3.8e6 | 8.7e3 | 7.9 | 75.7 | 1753 | 1008 | 528 | 128 | 0.31 | 3.7 | 4.5 | Heavy | |
| WES Semi - Hardened Facility Design Criteria Tests | Test I-1 | 65 | 12.8 | 11.0 | 6000 | 8.5e4 | 1.00 | 0.141 | Fixed | 1.10 | 87.3 | 4.4e6 | 9.5e4 | 360 | 6644 | 2851 | 2960 | 916 | 8.2 | 0.07 | 0.6 | 1.0 | Moderate |
| | Test I-2 | 65 | 12.8 | 11.0 | 6000 | 8.5e4 | 0.50 | 0.071 | Fixed | 1.10 | 87.3 | 4.4e6 | 5.0e4 | 188 | 6644 | 2851 | 2960 | 916 | 15.7 | 0.10 | 1.0 | 1.8 | Moderate |
| | Test I-3 | 65 | 12.8 | 11.0 | 6000 | 8.5e4 | 0.50 | 0.071 | Fixed | 1.10 | 87.3 | 4.4e6 | 5.0e4 | 188 | 6644 | 2851 | 2960 | 916 | 15.7 | 0.10 | 3.0 | 5.3 | Heavy |
| | Test I-4 | 65 | 12.8 | 11.0 | 6000 | 8.5e4 | 0.25 | 0.035 | Fixed | 1.10 | 87.3 | 4.4e6 | 2.5e4 | 96 | 6644 | 2851 | 2960 | 916 | 30.8 | 0.16 | 2.2 | 4.0 | Heavy |
| | Test I-6 | 65 | 12.8 | 11.0 | 6000 | 8.5e4 | 0.25 | 0.035 | Fixed | 1.10 | 87.3 | 4.4e6 | 2.5e4 | 96 | 6644 | 2851 | 2960 | 916 | 30.8 | 0.16 | 1.5 | 2.6 | Moderate |