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When MAML Learns Quickly, Does It Generalize Well?

O. Taylan Turan¹, David M.J. Tax¹, and Marco Loog¹

Delft University of Technology, Van Mourik Broekmanweg 6, Delft 2628 XE, The Netherlands

Abstract. Model-Agnostic Meta-Learning is a meta-learning method that achieved state-of-the-art performance on few-shot image classification benchmarks at the time of its introduction. MAML’s strength is its ability to quickly adapt to a new task in time-critical settings, while still being general enough for any gradient-based model. Although there is no need for quick adaptation in most of the few-shot learning benchmarks, often MAML is utilized as a benchmark in this context. We investigate the benefit of limiting the adaptation steps of MAML in settings where quick adaptation is not required by the problem. In this initial study, the expected performance of MAML is compared to some conventional base learners for synthetic linear and nonlinear regression problems. Our experimental results show that limited gradient descent steps only improve generalization performance when faced with small task variance.

Keywords: meta-learning · expected performance · model-agnostic meta-learning

1 Introduction

Learning to learn, also referred to as meta-learning, treats the training of a machine learning model as a learning problem in itself. In this setting, there exist multiple learning problems and they are treated together. A machine learning model is "learning to learn" if the performance on each task improves with training experience obtained from the other tasks [18]. A major use of meta-learning is to tackle few-shot learning problems, where there is little data available from the learning task that is of prime interest, whereas there is an abundance of data from other, yet similar tasks.

Early works on the learning-to-learn paradigm relied upon two different models working together, where one model tries to improve performance on the specific task and the other tries to improve performance over the observed tasks together [18]. MAML (Model-Agnostic Meta-Learning) [6] provides an algorithm that circumvents the need for multiple models. This method tackles meta-learning by providing a model initialization (which is always required for models that are optimized with Stochastic Gradient Descent) that facilitates quick adaptation and good generalization.

Since it is model and problem independent, MAML finds a wide application area in the context of few-shot meta-learning. Specifically, for supervised and

reinforcement learning problems under that paradigm. Moreover, MAML also aims to improve a specific task performance quickly (with a few gradient steps). This is an additional important aspect of meta-learning.

The quick adaptation feature can prove useful in certain settings, for instance, in robotics applications, where the reaction/adaptation time of the agents in dynamic environments imposes time limitations. However, this limitation is not present in supervised learning problems, where MAML or its variants are utilized as a baseline (*e.g.* [8,15,17,3,10]). Most supervised problems are benchmarked with an image classification problem, where N -way K -shot classification problem (N different classes with K labeled training data) is tackled, where memory or time limitations do not constitute a major issue.

The main aim of this paper is to investigate MAML in settings where quick adaptation is not needed, and where most of the applications and variants of this method are benchmarked. This will be achieved by looking at the expected performance of MAML under two synthetic regression scenarios, and comparing its performance to conventional base learners (*e.g.* Linear Regression, Ridge Regression, Kernel Ridge Regression, etc.). By doing this we aim to investigate the effect of the limited adaptation step, and whether or not there is a benefit to this limitation. The code for all experiments is available at github.com/taylanot/EE_MAML.git.

2 Model-Agnostic Meta-Learning (MAML)

MAML aims to obtain an intermediate model $\mathcal{M}(\bar{\mathbf{w}}_{\text{meta}})$ that can generalize well after adaptation with gradient descent to a dataset $\mathcal{Z}$ observed from a new and unseen task $\mathcal{T}$ drawn from $p_{\mathcal{T}}$ where the number of training points N and the number of iterations n_{iter} is limited.

In order to obtain $\bar{\mathbf{w}}_{\text{meta}}$ first, a batch of tasks $\{\mathcal{T}_i\}_{i=1}^M$ from $p_{\mathcal{T}}$ is observed with each having a corresponding dataset $\{\mathcal{Z}_i\}_{i=1}^M$. Then, the future gradients concerning each task are observed and gradient descent is utilized to get possible parameters $\bar{\mathbf{w}}'$ for each task and a gradient descent iteration is made by collecting all the possible parameters from an observed batch of tasks for the real parameter update. The general procedure for supervised learning problems is given in Algorithm 1. Authors of [6] indicate that by using this procedure the model $\mathcal{M}(\bar{\mathbf{w}}_{\text{meta}})$ requires few gradient updates from a specific task, achieving good generalization performance. Examples of the intermediate model $\mathcal{M}(\bar{\mathbf{w}}_{\text{meta}})$ prediction with the observed tasks on the background can be seen in Figures 1a and 1b.

3 Related Work

MAML received multiple developments that followed the same approach of finding a warm initialization for all the tasks coming from a certain task distribution. Subsequent works highlight some of its limitations. Authors in [8,3] improved on

Data: $p_{\mathcal{T}}, \alpha, \beta$
Result: Intermediate Model $\mathcal{M}(\bar{\mathbf{w}}_{meta})$
 initialize $\bar{\mathbf{w}}$ randomly;
while *not done* **do**
 sample a batch of tasks $\mathcal{T}_i$ from $p_{\mathcal{T}}$
 forall $\mathcal{T}_i$ **do**
 Obtain future gradients: $\nabla_{\bar{\mathbf{w}}} \mathcal{L}_{\mathcal{T}_i}(\mathcal{M}(\bar{\mathbf{w}}))$ wrt. $\mathcal{Z}_i$
 Possible future parameters: $\bar{\mathbf{w}}'_i = \bar{\mathbf{w}}_i - \alpha \nabla_{\bar{\mathbf{w}}} \mathcal{L}_{\mathcal{T}_i}(\mathcal{M}(\bar{\mathbf{w}}))$
 end
 Update: $\bar{\mathbf{w}} \leftarrow \bar{\mathbf{w}} - \beta \nabla_{\bar{\mathbf{w}}} \sum \mathcal{L}_{\mathcal{T}_i}(\mathcal{M}(\bar{\mathbf{w}}'_i))$
end

Algorithm 1: MAML[6] Algorithm

MAML’s need for task similarity making the meta-learning more task family robust. The sensitivity of MAML to architectural details is noted and circumvented in [1]. The need for a second order term in MAML is questioned and shown that first order approximations can give equally good results in [15]. Deeper changes to the MAML method are presented in [9] to convert it to a method of probabilistic inference. Moreover, a continual learning extension where tasks are introduced sequentially is proposed in [7,17].

Besides most of the above-mentioned developments, some of the attention went to improving the quick adaptation stage from the learned initialization. In [12] not just the initialization, but also the update direction and the learning rate are optimized. Moreover, in [2] the learning rate for the adaptation is learned with hypergradient descent. Both methods aim to limit the adaptation steps needed.

Therefore, MAML’s developments also focus on quick adaptation. However, the above-mentioned articles use the Omniglot dataset [11] as a supervised classification benchmark with MAML as the baseline and some of the works recreate the sinusoidal regression task as shown in the original MAML paper [6]. Both of these settings where MAML and its variants are tested do not have the time or memory restrictions as few-shot learning problems. Yet, quick adaptation methods are still being benchmarked with these datasets.

4 Experimental Setting

Throughout this work uppercase bold letters (*e.g.* $\mathbf{X}$), lowercase bold letters (*e.g.* $\mathbf{x}$), and lowercase letters (*e.g.* x) are used for matrices, vectors, and scalars respectively. Moreover, the vectors are assumed to be stored in columns. Finally, the $\mathbf{I}_D$ represents a $D \times D$ identity matrix, the $\mathbf{1}_D$ and $\mathbf{0}_D$ represents $D \times 1$ vector of ones and zeros respectively.

4.1 Learning Problems

In this work, two families of regression tasks are considered; a linear and a nonlinear regression task family.

Consider the conventional linear regression problem

$$y = \mathbf{x}^T \mathbf{a} + \varepsilon, \quad (1)$$

where $y \in \mathbb{R}$, $\mathbf{x} \in \mathbb{R}^D$, $\mathbf{a} \in \mathbb{R}^D$ and $\varepsilon \sim \mathcal{N}(0, \sigma^2)$. Each realization of the slope $\mathbf{a}$ corresponds to a task $\mathcal{T}$.

For the nonlinear problem family, the regression function is defined as a weighted combination of sinusoidal functions:

$$y = \sin(\mathbf{x} + \boldsymbol{\phi})^T \mathbf{a} + \varepsilon, \quad (2)$$

where $y \in \mathbb{R}$, $\mathbf{x} \in \mathbb{R}^D$, $\mathbf{a} \in \mathbb{R}^D$ and $\varepsilon \sim \mathcal{N}(0, \sigma^2)$. Assuming that each realization of scale term $\mathbf{a}$ and $\boldsymbol{\phi}$ corresponds to a task observed in the environment $\mathcal{T}$.

For both learning problems each set of observed N input ($\mathbf{x}$) and its corresponding label (y) is denoted by a dataset $\mathcal{Z} := \{(\mathbf{x}_i, y_i)\}_{i=1}^N$.

A model parameterized by $\bar{\mathbf{w}}$ is denoted by $\mathcal{M}(\mathbf{x}, \bar{\mathbf{w}}) : \mathbf{x} \rightarrow y$. A model $\mathcal{M}(\mathbf{x}, \bar{\mathbf{w}})$ that is trained with $\mathcal{Z}$ obtained from task $\mathcal{T}$ is denoted by $\hat{\mathcal{M}}(\mathbf{x})$. Noting that $\hat{\mathcal{M}}(\mathbf{x})$ for a base learner is only exposed to a single task $\mathcal{T}$ and a single dataset $\mathcal{Z}$, whereas a meta learner, in this case, MAML, are exposed to multiple tasks from $p_{\mathcal{T}}$ and multiple datasets $\mathcal{Z}$ in the meta-learning stage and then the adaptation is done as in the case of a base learner with just a single task $\mathcal{T}$ and a single dataset $\mathcal{Z}$. The discrepancy between the prediction of the estimator $\hat{\mathcal{M}}$ and y is measured in terms of squared loss $\mathcal{L} := (\hat{\mathcal{M}}(\mathbf{x}) - y)^2$. Ultimately the loss that this paper investigates is the *Expected Squared Loss* of an estimator $\hat{\mathcal{M}}$ over the $p_{\mathcal{T}}$;

$$\mathcal{E} := \iiint (\hat{\mathcal{M}}(\mathbf{x}) - y)^2 p(\mathbf{x}, y) p_{\mathcal{Z}} p_{\mathcal{T}} d\mathbf{x} dy d\mathcal{T}. \quad (3)$$

This performance measure gives rise to the *Bayes Error* to be given by σ^2 that is coming from the noise term, which represents a model that is the perfect estimator, referred to as oracle in some of the meta-learning literature.

For all the problems the input distribution is given by $p_{\mathbf{x}} \sim \mathcal{N}(0, k\mathbf{I})$ where k is a parameter for the variance of the inputs. For the linear problem the $p_{\mathcal{T}} := p(\mathbf{a}) \sim \mathcal{N}(m\mathbf{1}_D, c\mathbf{I}_D)$ and for nonlinear problem the task distribution takes the form of a joint distribution $p_{\mathcal{T}} := p(\mathbf{a}, \boldsymbol{\phi})$ where $p_{\mathbf{a}} \sim \mathcal{N}(\mathbf{1}_D, c_1\mathbf{I}_D)$ and $p_{\boldsymbol{\phi}} \sim \mathcal{N}(\mathbf{0}_D, c_2\mathbf{I}_D)$

4.2 Models

For the linear problems $\mathcal{M}(\mathbf{x}, \bar{\mathbf{w}}) := \bar{\mathbf{x}}\bar{\mathbf{w}}$ with $\bar{\mathbf{x}} \in \mathbb{R}^{1 \times D+1}$ and $\bar{\mathbf{w}} \in \mathbb{R}^{D+1 \times 1}$ where $\bar{\mathbf{w}} := [\mathbf{w}, b]^T$ and $\bar{\mathbf{x}} := [\mathbf{x}, 1]$ is utilized. The optimum parameters ($\hat{\bar{\mathbf{w}}}$) for different linear models are obtained as follows:

Linear Estimator is given by the least-squares solution, $\hat{\bar{\mathbf{w}}} := (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T \mathbf{y}$, where $\mathbf{X} \in \mathbb{R}^{N \times D}$ is the design matrix where the observed input data is stored in rows.

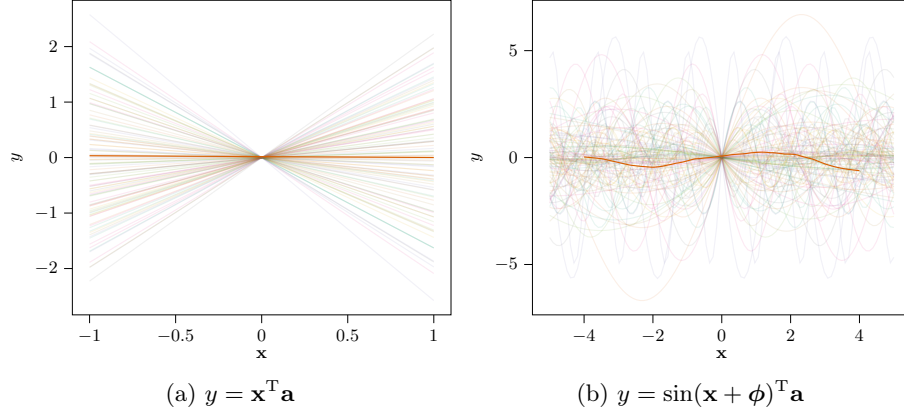


Fig. 1: 100 sample tasks drawn from $p_{\mathcal{T}}$ for both linear ($m = 0$ and $c = 1$) and nonlinear ($c_1 = 1$ and $c_2 = 1$) problems with low opacity and the intermediate models for MAML trained with respective $p_{\mathcal{T}}$.

Ridge Estimator is given by $\hat{\mathbf{w}} := (\mathbf{X}^T \mathbf{X} + \lambda \mathbf{I}_D)^{-1} \mathbf{X}^T \mathbf{y}$ which is obtained by minimizing the squared loss with the additional term of $\lambda \|\bar{\mathbf{w}}\|_2^2$.

Kernel Ridge Estimator is given by $\hat{\mathbf{w}} = \mathbf{X}^T \boldsymbol{\alpha}$ where $\boldsymbol{\alpha} := (\mathbf{K} + \lambda \mathbf{I}_N)^{-1} \mathbf{y}$ where $\mathbf{K} \in \mathbb{R}^{N \times N}$ is the *Gram Matrix* obtained by replacing $\mathbf{X}^T \mathbf{X}$ inner product by a kernel $\kappa(\mathbf{X}, \mathbf{X})$. Then, the prediction of the estimator takes the form $\mathcal{M}(\mathbf{x}^*, \bar{\mathbf{w}}) = \boldsymbol{\alpha}^T \kappa(\mathbf{x}^*, \mathbf{X})$ where $\mathbf{x}^* \in \mathbb{R}^{D \times 1}$.

For both linear and nonlinear models, gradient descent can be utilized to update the parameters of a model $\mathcal{M}$. Then,

Gradient Descent for any given model $\mathcal{M}(\mathbf{x}, \bar{\mathbf{w}})$ and a given number of iterations n_{iter} the gradient descent estimator is given by $\{\bar{\mathbf{w}}_{j+1} = \bar{\mathbf{w}}_j - \eta \nabla_{\bar{\mathbf{w}}_j} \sum_{i=1}^N (\mathcal{M}(\mathbf{x}_i, \bar{\mathbf{w}}_j) - y_i)^2\}_{j=0}^{n_{iter}}$. In other words for any given value of $\bar{\mathbf{w}}$ one gradient update is given by the gradient with respect to $\bar{\mathbf{w}}$ with a scaling parameter η .

All the models investigated can be divided into two sub-categories the models that have information regarding the task space and the ones that have not. The labels used in Section 5 of the models that have information regarding the task space are as follows:

- **MAML** (for linear problem): corresponds to gradient descent with n_{iter} with the adjustable parameters obtained from the mean of the tasks $\mathbb{E}[p_{\mathcal{T}}]$ with small perturbation $\delta \sim \mathcal{N}(\mathbf{0}, 0.1\mathbf{I})$ since the MAML procedure for a linear model goes to the mean of the task distribution.
- **MAML** (for nonlinear problem): an intermediate model trained with the network and meta-learning procedure given in [6] for the sinusoidal regression problem. After which gradient descent with n_{iter} is used for adaptation to a certain task.

Finally, the following model labels have information from a single task:

- **Linear**: standard least squares solution.
- **Ridge**: standard least squares solution with L_2 – *regularization*.
- **random GD**: gradient descent with n_{iter} with the adjustable parameters starting from random initialization.
- **Kernel Ridge**: kernelized (with Radial Basis Function Kernel)

For the linear problem setting, it should be noted that the optimum can always be reached when the gradient descent is utilized with an infinitely small learning rate and an infinite number of gradient steps. Thus, allowing us to investigate the difference between taking limited steps or allowing the model to go towards the optimum directly.

It should be noted that the hyper-parameters of the utilized models if there are any, are selected with a simple grid search with 20 different values, and only the one with the lowest mean expected error over the parameter under investigation are presented in the results.

5 Results and Discussion

This section is dedicated to the expected performance results of a meta-learning model after adaptation and conventional base learners (*e.g.* Linear, Ridge, and Kernel Ridge Regression models), to see their performance differences under certain scenarios induced by the experimental assumptions (*e.g.* task variance, input variance, noise, and dimensionality).

Linear Problem The linear problem introduced in Section 4 is characterized by the dimensionality D , number of training samples N , number of gradient steps n_{iter} , the task variance c and task mean m , and the variance of the input samples k . For the sake of brevity, only some of the parameters are discussed in this section. Unless the parameter in the configuration is under investigation, the default values are utilized. And, the default values for the experimentation $\sigma = 1$, $m = 0$, $k = 1$, $c = 1$, $n_{iter} = 1$. Moreover, the number of tasks drawn ($N_{\mathcal{T}}$), and dataset draws ($N_{\mathcal{Z}}$) for approximating the expected error given in Equation 3 are taken to be 100 each. Finally, the test set size is taken as 1000.

Effect of Number of Gradient Steps n_{iter} : It can be observed from Figure 2a that for a low number of training samples the gradient steps taken have little to no influence. But as the number of training samples increases for a given problem dimensionality the effect n_{iter} on the expected error gets much more prominent. It is evident that MAML decreases the number of gradient steps needed for convergence. Moreover, for $D = N$ case it even improves generalization after convergence too (see Figures 2d and 2a). Overall, it can be observed that the increasing n_{iter} converges towards the Ridge model variants with the exception of the $D = 1$ and $N = 1$ cases.

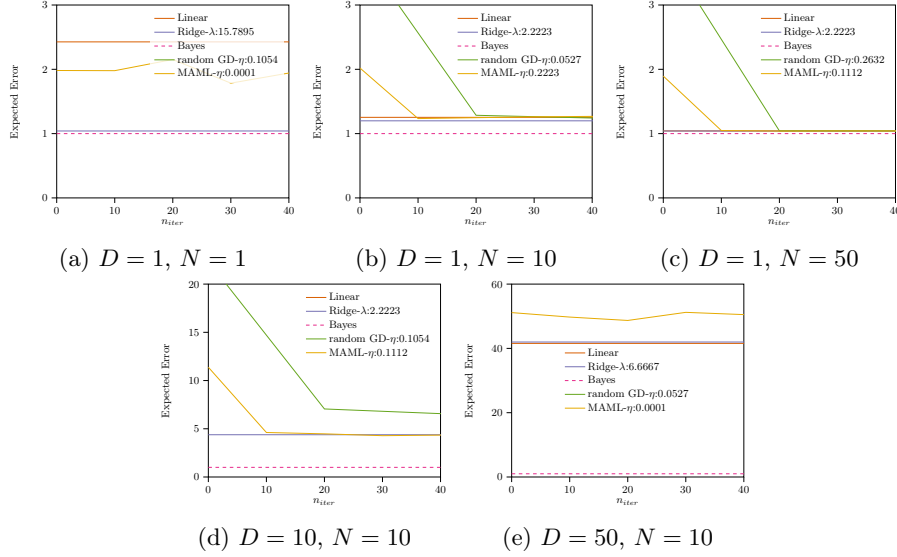


Fig. 2: The expected error for the increasing number of gradient steps n_{iter} used for adaptation when changing the number of training samples for various problems of different dimensions.

Effect of the Number of Training Samples N : Results of this experiment can be found in Figure 3 for increasing problem dimensionality. It can be seen that the Linear model suffers from singularities. For instance, in Figure 3b when the number of samples equals dimensionality $N = D$. However, it is able to have comparable error over all the selected problem dimensionalities. For the increasing training samples case, the Ridge model performs much better as all the cases converge towards the Bayes error. However, MAML is unable to converge towards the Bayes error. This can be attributed to the regularizing effect of the limited gradient steps (n_{iter}) allowed for the models. Overall, the improvement that the additional task-related information brings to the gradient-based models is not visible, as the random GD model is orders of magnitude higher in expected error. It is evident that although task information provides gain over random initialization, the expected performance is hindered for the gradient-based models.

Effect of Task Variance c : The results of increasing task variance for various problem dimensions and various numbers of training samples can be found in Figure 4. The most obvious observation is that for all the models that utilize gradient descent, expected error increases, whereas the Linear model and the Ridge model are only affected by this phenomenon for problem dimensionality $D \geq N$.

In light of this observation, another important result is that for $N \geq D$ and for small task variance the gradient descent variants (except the randomly initialized model) have lower expected error than the Ridge model. However,

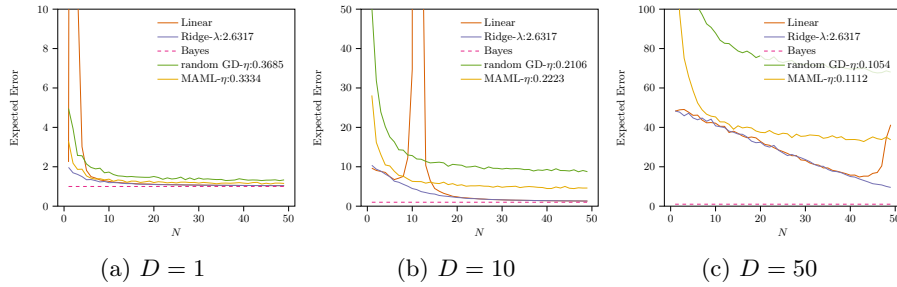


Fig. 3: The expected error for the increasing number of training samples and problem dimensionality.

this performance diminishes with increasing problem dimensionality and the increasing number of training points. It is interesting to see a better performance from just one gradient step.

That is why an additional mini-experimentation is done for the GD and MAML models to investigate if there is an improvement with the additional gradient steps. The results of this experimentation are given in Table 1. It is observed from the table that there exists a point at which the gradient steps are hurting the expected performance one would get in this range after the second gradient step. Then, it can be conjectured that the number of gradient steps has a regularizing effect on the task distributions with small variance. Despite, the surprising results of MAML-like algorithms, the Ridge model is much more stable and performs better than gradient-based methods for $N \geq D$.

Table 1: Mean expected error for the range $c : [0, 1]$ range with various gradient steps for the MAML and GD models with $\eta = 0.3234$. Note that only $D = 1$, $N = 10$ case (see Figure 4b) is presented.

	n_{iter}									
	1	2	3	4	5	6	7	8	9	10
MAML	1.2132	1.1938	1.2067	1.2171	1.2318	1.2476	1.2773	1.3330	1.4622	1.7556

Effect of Task Mean m : The results can be seen in Figure 5. The most important observation from this experimentation is that the Ridge model has an increasing expected error for the cases of $N \leq D$ cases (see Figures 5a, 5d and 5e) and mostly the best λ from the trials is found to be the lowest value, which makes the Ridge model behave similar to the Linear model. Furthermore, other models which have prior task information do not seem to be affected by the task mean shifting in the task space, as expected. Again, the superiority of including information from the task space is evident as the conventional regularization cannot deal with the changing task distribution mean for $N \leq D$.

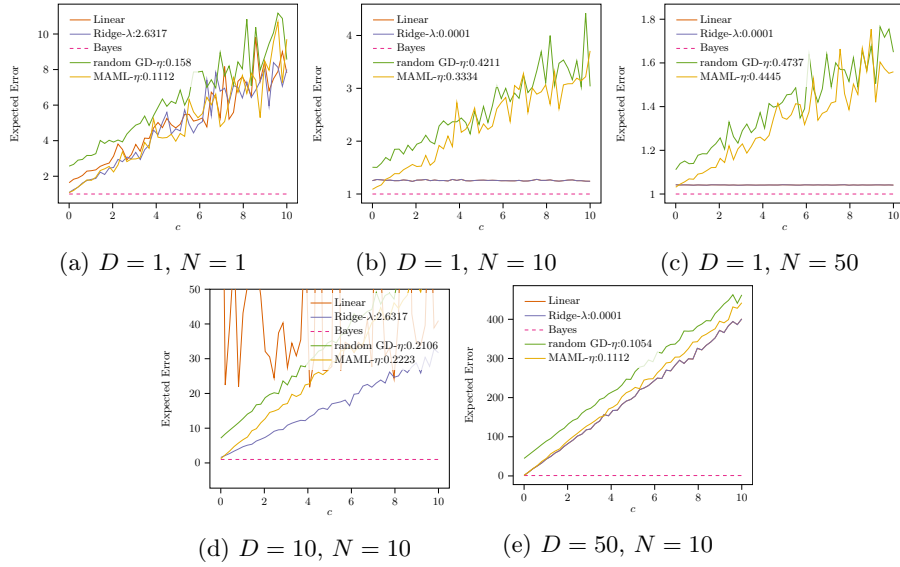


Fig. 4: The expected error for increasing task variance c when changing the number of training samples for various problems of different dimensions.

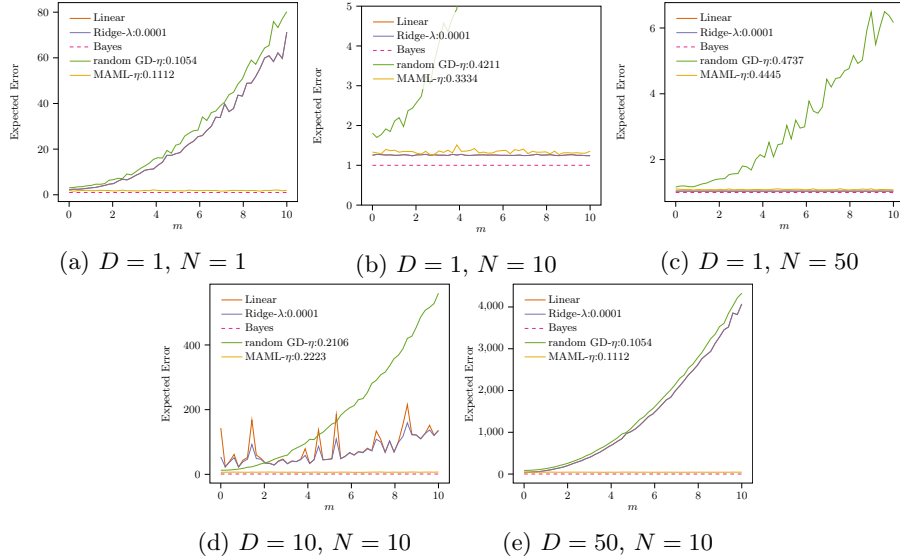


Fig. 5: The expected error for increasing task mean m when changing the number of training samples for various problems of different dimensions.

Nonlinear Problem The nonlinear problem introduced in Section 4 has parameters controlling the dimensionality D , number of training samples N , number

of gradient steps n_{iter} , the task variances and means m_1 and m_2 , c_1 and c_2 , and the variance of the input samples k . Note that only some of the parameters are discussed in this section. Unless the parameter in the configuration is under investigation, the default values are utilized. And, the default values are given as $\sigma = 1$, $m_1 = 1$, $m_2 = 0$, $c_1 = 2$, $c_2 = 2$, $k = 1$, $n_{iter} = 10$. Moreover, the number of tasks drawn ($N_{\mathcal{T}}$), and dataset draws ($N_{\mathcal{Z}}$) for approximating the expected error given in Equation 3 are taken to be 50 each. Finally, the test set size is taken as 1000.

Effect of Number of Gradient Steps n_{iter} : It can be seen from Figure 6a that a single realization of the Kernel Ridge model can have a lower expected error for an extreme value of 1 training sample for the 1-dimensional problem. However, as the number of training samples increases for a given problem dimensionality MAML model starts showing a lower expected error (see Figure 6b). Moreover, the further increase in training samples to 50 lowers the difference in expected error for given models. Another interesting observation is, that for $N \leq D$ Kernel Ridge model can achieve a lower expected error, and for all the other cases one might find a better MAML model given that sufficient gradient steps are allowed. Moreover, it can be observed that the difference between random GD and MAML is low in terms of expected error for most of the presented problems. Finally, in cases where MAML outperforms Kernel Ridge the number of gradient steps required to get a lower expected error is low.

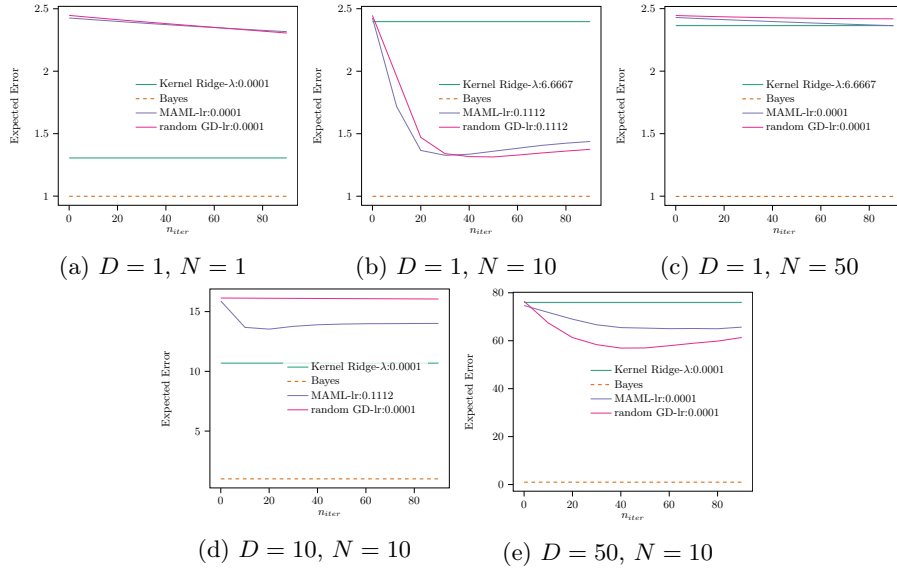


Fig. 6: The expected error for the increasing number of gradient steps n_{iter} used for adaptation when changing the number of training samples for various problems of different dimensions.

Effect of Number of Training Samples N : By looking at Figure 7 it can be seen that for all the given dimensionalities there exists a training sample amount where the expected error of the Kernel Ridge model is higher than MAML. Another observation is that the randomly initialized model average performance is stable over all number of training samples.

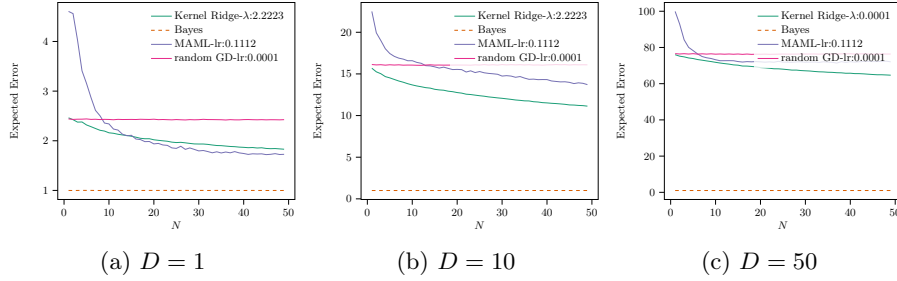


Fig. 7: The expected error for the increasing number of training samples and problem dimensionality.

Effect of Phase Task Variance c_2 : Remembering that the task variance effect for the linear problem had some interesting properties where even a single gradient step resulted in a lower expected error. One might wonder if that is the case for the nonlinear problem as well. As can be seen in Figure 8b a similar effect is observed for the nonlinear problem. However, for this case, the decreased expected error of MAML is only better than a randomly initialized model. This indicates that a better performance can be achieved with a regularization-based conventional learner. The only clear advantage of utilizing MAML is seen in the case where there is only 1 training sample. However, even the randomly initialized model performs better than the Kernel Ridge model for that case and what MAML adds is just a slight improvement.

Additional experimentation results for σ for linear and nonlinear problems can be found in the Appendix, it is observed that increasing noise has similar behavior with single task learning models. Moreover, the effect of input variance is investigated and found that the gradient descent based methods perform poorer for the linear problem.

5.1 Discussion

Upon our investigation, it is found empirically that meta-information about the task space can help the generalization performance in linear and nonlinear problem settings even with limited gradient steps. Increased generalization performance of MAML compared to single task learning models on expectation when the tasks that are in consideration are close to each other is observed, where the same

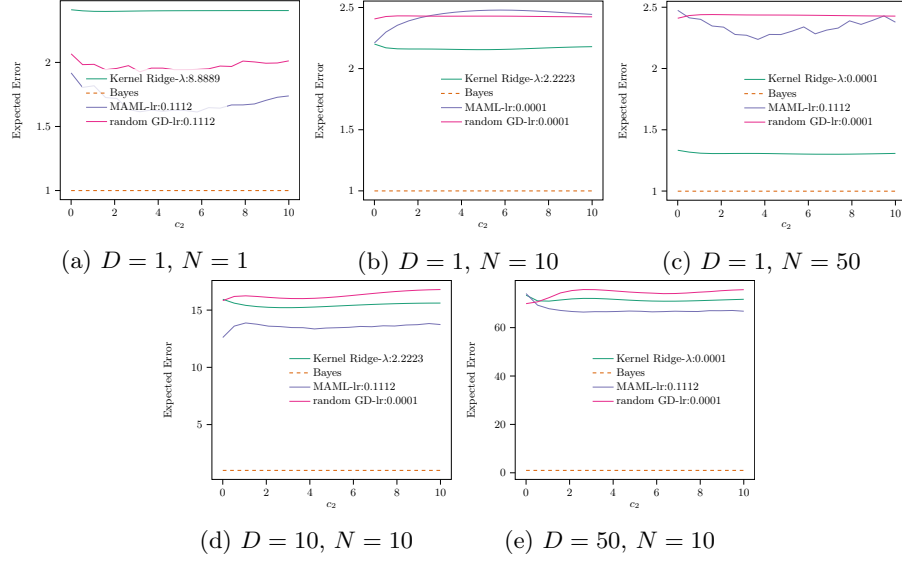


Fig. 8: The expected error for increasing task variance for phase c_2 used for adaptation when changing the number of training samples for various problems of different dimensions.

observation is made theoretically in [5]. This observation suggests that there is a regularizing effect of limiting the gradient steps used for adaptation. We conjecture that after the meta-learning stage intermediate model parameters $\bar{\mathbf{w}}$ are closer to the test set optimum compared to the proximity of train and test set optimums. This type of behavior is investigated in [14] as well, where the large learning rate in the training phase acts as a regularizer due to the discrepancy between train and test loss landscapes.

This limitation of adaptation steps is noted in [2,13] that tries to improve the MAML adaptation step so that the adaptation is limited to fewer gradient steps, preferably one. Our findings suggest that the expected performance of these methods should be investigated as well since some of the generalization power of MAML might be coming from the regularization induced by not optimizing the training loss perfectly. This hypothesis is supported by the findings of [16] which concludes that the performance gain of MAML is about feature reuse instead of rapid learning.

6 Conclusion

Upon our investigation, we observed that single-task learners are able to compete with MAML when a limited number of gradient steps are allowed. We show that even in the case of general regularization, and when there is enough data, a single-task learner can outperform on expectation of a meta learner. Especially

when the tasks observed start to deviate from each other. It indicates that the regularization-based meta-learners similar to the ones presented in [4], can be competitive and robust enough for much wider task variance. However, it also should be suitable for nonlinear problem settings. Moreover, regularization-based methods similar to the ones presented in [10] for MAML can prove useful to extend the generalization performance of MAML to wider task variances.

This study only utilizes synthetic data, since the computational burden of expected error analysis is high. Thus, more in-depth expected performance should be done for the Omniglot dataset and other widely used supervised few-shot learning benchmark datasets with improvements introduced on top of MAML. We believe that understanding all the contributing factors to generalization performance is key to correct use cases of meta-learning methods.

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7 Appendix

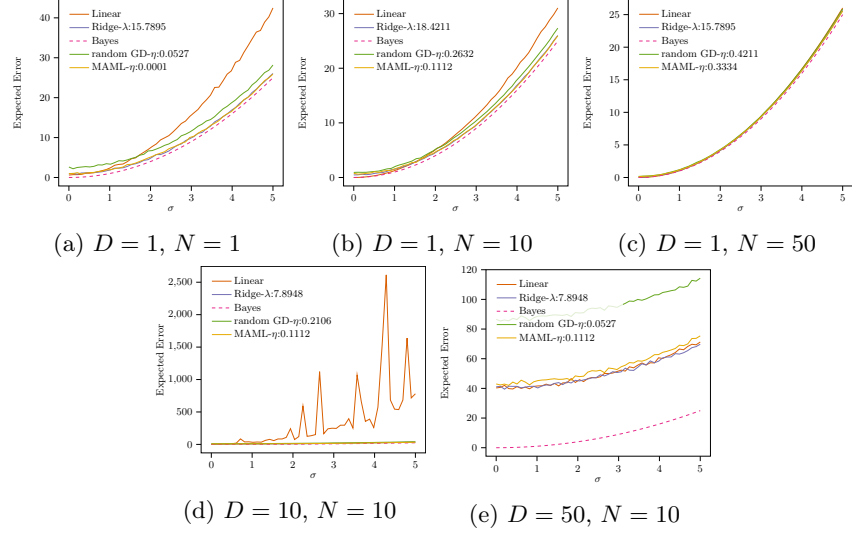


Fig. 9: **[Linear Problem]**: The expected error for increasing noise standard deviation σ when changing the number of training samples for various problems of different dimensions.

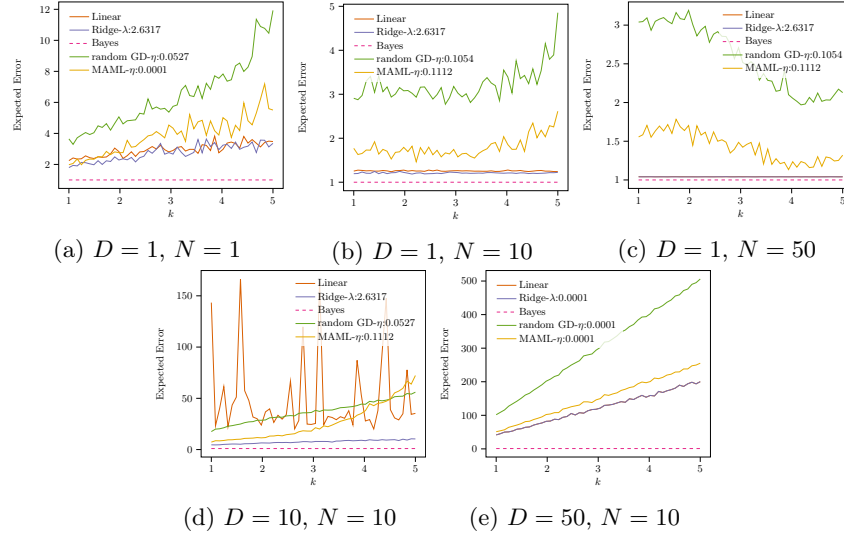


Fig. 10: **[Linear Problem]**: The expected error for increasing input variance k when changing the number of training samples for various problems of different dimensions.

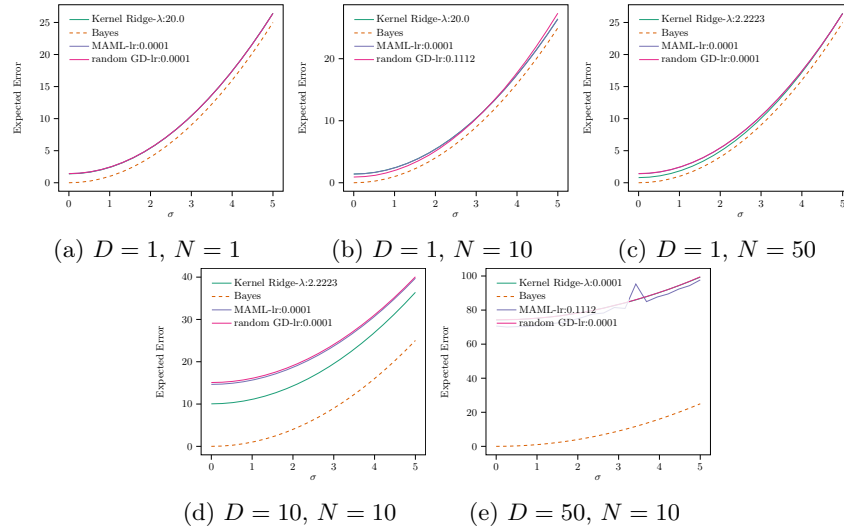


Fig. 11: **[Nonlinear Problem]**: The expected error for increasing noise standard deviation σ when changing the number of training samples for various problems of different dimensions.