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# A Parameter Recognition-Based Impedance Tuning Method for SS-Compensated Wireless Power Transfer Systems

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**Abstract**—This article presents a parameter recognition-based impedance tuning method for the impedance mismatch caused by capacitance drift and coil misalignment in series-series-compensated wireless power transfer (WPT) systems. First, a parameter recognition method is proposed to identify the unknown parameters of the resonant circuits by only measuring the rms values of the coil currents. No phase detection circuits and auxiliary measurement coils are required. Furthermore, according to the recognized parameters, the reactance on both sides are minimized simultaneously by regulating the system frequency and the phase shift angles of the active rectifier. Compared with the existing methods, the proposed parameter recognition method adopts a dynamic frequency approaching strategy to avoid severe system detuning due to the bifurcation phenomenon. Moreover, based on the recognized parameters, the proposed impedance tuning method can simultaneously cope with the parameter deviations caused by capacitance drift and coil misalignment on both sides without using extra circuits and switches. Experimental results show that the unknown parameters of the resonant circuits are recognized accurately, with the average relative errors all less than 3%. Additionally, by implementing the impedance tuning method, the dc to dc efficiency of the WPT prototype is improved by 4.3%–15% in the experiments.

**Index Terms**—Capacitance drift, coil misalignment, impedance tuning, parameter recognition, wireless power transfer (WPT).

## I. INTRODUCTION

AS AN emerging technology in recent decades, wireless power transfer (WPT) enables safe, convenient, and automated charging in many industrial applications, such as portable electronics [1], underwater loads [2], implanted medical devices [3], and electric vehicles [4], [5], [6]. To obtain a higher transmission efficiency, various compensation topologies are

introduced in WPT systems to cancel the leakage inductance of the loosely coupled coils, where the most widely used one is the series-series (SS) compensation [7]. In the SS-compensated WPT system, the series capacitors are designed to be resonant with the coils at the nominal resonant frequency. However, due to the component tolerances, temperature variations and aging effects, the compensation capacitance may deviate from the nominal values [8]. Additionally, in practical WPT applications, the metallic shielding plates are usually used in the transmitter (Tx) and receiver (Rx) coils to protect human and electronic devices from the stray magnetic field, while magnetic ferrites are often employed to improve the coil coupling. As a result, the self-inductances of the coils become sensitive to the spatial displacement between the Tx and Rx pads as these metallic and magnetic materials interfere with the transmission of the magnetic flux [9]. The parameter deviations caused by the capacitance drift and coil misalignment lead to detuning of the system, which reduces the transmission efficiency and results in a lower power factor [10]. Therefore, in order to obtain better transmission performance, it is desirable for the system to consistently operate at the resonance state regardless of the capacitance drift and coil misalignment.

Many works have been done to deal with the impedance mismatch caused by parameter deviations, which can be roughly divided into three categories:

- 1) using the variable capacitors or inductors [9], [11], [12], [13], [14], [15];
- 2) tracking the resonant frequency [16], [17];
- 3) adopting the active rectifier [18], [19].

A commonly used approach for impedance tuning is to adjust the compensation impedance. In [11], a variable inductor was implemented in the secondary side to dynamically tune the receiver circuit. However, two extra conversion stages, i.e., a diode rectifier and a buck converter, are required in this method, which greatly increases the hardware costs. In [12], [13], and [14], by introducing the selectable capacitor array, the compensation capacitance is discretely regulated. Nevertheless, the use of numerous switches and capacitors increases the system volume and costs. Additionally, this method fails to continuously adjust the impedance. To reduce the number of components and realize continuous tuning, controllable capacitors were used in [9] and [15]. In [15], a voltage-controlled capacitor was proposed to achieve dynamic impedance tuning. Nevertheless,

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the analog amplifier used in this method limits the power transfer capability, and thus, it is only suitable for applications of a few watts. In [9], a pulsewidth modulation (PWM) controlled capacitor was proposed to withstand the detuning caused by the Tx inductance variation. This method enables continuous capacitance tuning and is able to cope with high-power applications. However, the introduction of additional power switches in the PWM-controlled capacitors increases the power losses and hardware costs. Additionally, the capacitance drift is not considered in this method.

Another typical method to deal with the impedance mismatch is to track the resonant frequency. In [16], a power-frequency controller was proposed, which implements the resonance tracking by synchronizing the switching signals with the resonant current. In [17], a self-oscillating switching technique was adopted, where the switching frequency of the inverter automatically tracks the resonant frequency. However, these methods can only realize zero-phase-angle (ZPA) input, whereas the reactance in the Rx side cannot be tuned.

To tune the Rx-side reactance, the active control of the rectifier was adopted in some methods. In [18] and [19], by regulating the duty cycle and the phase shift angle of the active rectifier, the equivalent load impedance was regulated to minimize the Rx-side reactance and to realize the maximum efficiency tracking. However, the active rectifier control cannot simultaneously handle the impedance mismatch on both sides.

Recently, some researchers combine the resonant frequency tracking and the active rectifier control to tune the reactance on both the Tx and Rx sides. In [20], an impedance tuning control was proposed to deal with the self-inductance variations caused by coil misalignment, where the switching frequency was controlled to realize ZPA input and a synchronous switching technique was proposed for the active rectifier to minimize the Rx-side reactance. However, the parameter deviations caused by capacitance drift were not discussed in this method. In [21], an impedance decoupling-based method was proposed to minimize the dual-side reactance caused by capacitance drift. Nevertheless, the phase detection circuits and an auxiliary measurement coil are needed to measure the reactance angles on both sides, which increases the hardware costs and complexity.

The phase detection circuits for reactance angle measurements can be avoided by parameter recognition. Dai et al. [22] presented a pulse density modulation-based parameter identification method to simultaneously estimate the self-inductance and compensation capacitance on the Rx-side. However, only the Rx-side reactance is tuned in this method. In [23], a parameter recognition-based self-tuning method was proposed to address a wide range of coupling coefficient variations, where both the mutual inductance and the self-inductances can be identified without using the phase information and auxiliary measurement coils. However, this method cannot identify the compensation capacitances.

In practice, the impedance mismatch usually involves deviations of multiple parameters, and it is challenging to tune the impedance when considering all of them. Therefore, previous studies mainly focus on parameter deviations in one specific aspect, for instance, only considering the coil misalignment [9], [20], [23], [24], [25], the capacitance drift [21], or the

impedance mismatch on just one side [22]. To simultaneously tune the dual-side impedance mismatch under capacitance drift and coil misalignment, the parameters of the whole resonant circuit are required to be identified. Although the identification of multiple parameters can be realized by the frequency-sweep-based front-end monitoring methods [26], [27], these methods generally sweep the frequency around the nominal resonant frequency, which leads to severe system detuning and significant load power ripple especially under parameter deviations.

To fill up the aforementioned research gaps, this article proposes a new parameter recognition-based impedance tuning method. First, a parameter recognition method is proposed to identify the unknown parameters of the resonant circuits, and the original features of this method are summarized as follows.

- 1) Compared to the conventional front-end parameter monitoring methods, the secondary-side information is introduced, and therefore, all of the unknown parameters of the resonant circuits, including the self-inductances, the mutual inductance, and the compensation capacitances, are recognized accurately, without using any phase detection circuits and auxiliary measurement coils.
- 2) A dynamic frequency approaching strategy is proposed to acquire the required data for parameter recognition, which avoids severe system detuning during the traditional frequency-sweep process.
- 3) The parameter recognition is implemented at pre start-up, with the rectifier output short-circuited during this process, which avoids significant load power fluctuations caused by frequency variations.
- 4) A simple yet powerful heuristic algorithm called JAYA is introduced to recognize the unknown parameters. Compared with the conventional genetic algorithm (GA) and differential evolution (DE) algorithm, which need to tune the parameters of the differential weight and the crossover rate, the JAYA algorithm is free from algorithm-specific parameters and thereby avoids the difficulty of tuning parameters [28].

Furthermore, based on the recognized parameters, the reactance on both sides are minimized simultaneously by regulating the system frequency and the phase-shift angles of the active rectifier.

The rest of this article is organized as follows. Section II introduces the configuration of the SS-compensated system and analyses the impact of the impedance mismatch caused by capacitance drift and coil misalignment. In Section III, the proposed parameter recognition method is described, and the corresponding impedance tuning method is presented. In Section IV, experimental results are given to validate this proposal. Finally, Section V concludes this article.

## II. IMPEDANCE MISMATCH CAUSED BY CAPACITANCE DRIFT AND COIL MISALIGNMENT

### A. System Configuration

As shown in Fig. 1, a typical SS-compensated WPT system is studied in this article, where an active rectifier is adopted in the

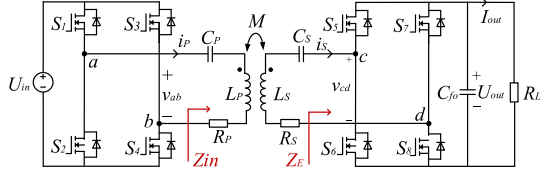


Fig. 1. Circuit diagram of the SS-compensated WPT system using the active rectifier.

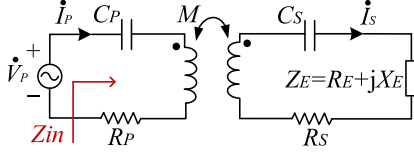


Fig. 2. Equivalent circuit model of the WPT system.

secondary side. The dc input voltage is represented by  $U_{in}$ , while the dc output voltage and current are denoted by  $U_{out}$  and  $I_{out}$ , respectively. Moreover,  $v_{ab}$  and  $v_{cd}$  are the ac voltages of the inverter and rectifier;  $i_P$  and  $i_S$  are the transmitter and receiver coil currents;  $L_P$  and  $L_S$  represent the self-inductances of the coupled coils;  $C_P$  and  $C_S$  are their corresponding compensation capacitors;  $R_P$  and  $R_S$  are the equivalent loss resistances of the primary and secondary resonant circuits; and  $R_L$  is the resistive load. The mutual inductance of the coils is denoted by  $M = k\sqrt{L_P L_S}$ , where  $k$  is the coupling coefficient. The equivalent circuit model derived by fundamental frequency approximation is further presented in Fig. 2, where  $Z_E$  is the equivalent load impedance regulated by the active rectifier;  $\dot{V}_P$ ,  $\dot{I}_P$ , and  $\dot{I}_S$  are the phasor forms of the fundamental components of  $v_{ab}$ ,  $i_P$ , and  $i_S$ , respectively. According to the Kirchhoff's voltage law, the steady-state equation of the system is given by

$$\begin{cases} \dot{V}_P = Z_P \dot{I}_P - j\omega M \dot{I}_S \\ 0 = j\omega M \dot{I}_P - (Z_S + Z_E) \dot{I}_S. \end{cases} \quad (1)$$

The equivalent impedances of primary and secondary resonant circuits  $Z_P$  and  $Z_S$  are expressed as

$$Z_i = R_i + jX_i, X_i = \omega L_i - 1/(\omega C_i) \quad (2)$$

where the subscript  $i$  indicates the primary (P) or the secondary (S) side. Moreover, the equivalent load impedance  $Z_E$  is represented by  $Z_E = R_E + jX_E$ , where  $R_E$  and  $X_E$  are the equivalent load resistance and reactance, respectively.

### B. Parameter Deviations Caused by Coil Misalignment and Capacitance Drift

Ideally, for the SS-compensated WPT system, the compensation capacitors are designed to resonate with the coupled coils at the nominal resonant frequency. Nevertheless, in practical applications, the parameters of the resonant circuits may deviate from the nominal values due to the coil misalignment and capacitance drift.

On one hand, as the aluminum shielding sheets and magnetic ferrites are generally used in the Tx and Rx pads, the coil self-inductances vary with the spatial displacement. To demonstrate the impact of coil misalignment, the measured coil

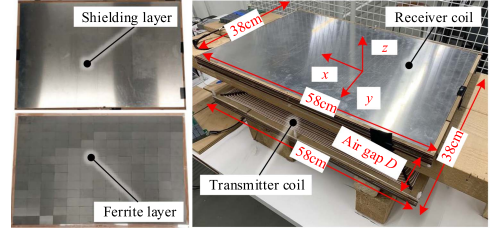


Fig. 3. Charging pads with the shielding and ferrite layers.

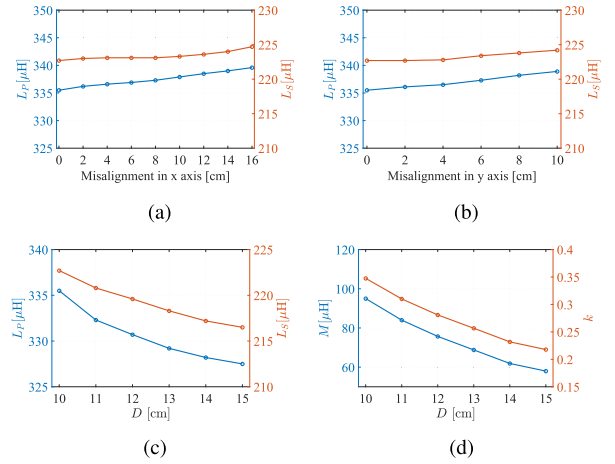


Fig. 4. Measured coil inductances under different coil misalignment directions and air gaps. (a) Self-inductance variations under the  $x$ -direction misalignment ( $D = 10$  cm). (b) Self-inductance variations under the  $y$ -direction misalignment ( $D = 10$  cm). (c) Self-inductance variations under different air gaps. (d) Variations in mutual inductance and coupling coefficient under different air gaps.

inductances under different misalignment directions and air gaps are illustrated in Fig. 4 for the charging pads shown in Fig. 3. As it can be observed from Fig. 4, the coil self-inductances slightly increase as the misalignment in the  $x$ - and  $y$ -directions increases. More significant inductance variations can be observed under different air gaps. As the air gap  $D$  increases from 10 to 15 cm, the primary self-inductance  $L_P$  drops from 335.5 to 327.5  $\mu$ H, while the secondary self-inductance  $L_S$  decreases from 222.7 to 216.5  $\mu$ H. Meanwhile, the increase in the air gap reduces the coupling coefficient  $k$  from 0.35 to 0.22. In this article, two cases, with the air gap  $D$  at 10 cm and 15 cm, are selected as cases A and B for theoretical analysis, respectively.

On the other hand, due to the ambient temperature variations, the aging effect, and the manufacturing errors, significant capacitance drift may occur in the practical applications. Therefore, it is essential to investigate the influence of the capacitance drift. In this article, both the primary and secondary capacitance deviations are considered and expressed as

$$C_P = (1 + d_P)C_{P0}, C_S = (1 + d_S)C_{S0} \quad (3)$$

where  $d_P$  and  $d_S$  indicate the degree of capacitance drift; and  $C_{P0}$  and  $C_{S0}$  are the nominal compensation capacitances. Considering component tolerances of the commercialized capacitors, the aging effects and the ambient temperature variations, the maximum degree of capacitance drift is set to  $\pm 20\%$  to ensure



TABLE I  
 SYSTEM PARAMETERS OF THE SS-COMPENSATED WPT SYSTEM

Symbol	Parameters	Value	Unit
$L_P$	Primary coil inductance	327.5 ~ 335.5	$\mu\text{H}$
$L_S$	Secondary coil inductance	216.5 ~ 222.7	$\mu\text{H}$
$k$	Coupling coefficient	0.22 ~ 0.35	/
$C_{P0}$	Nominal primary capacitance	10.45	nF
$C_{S0}$	Nominal secondary capacitance	15.74	nF
$d_P$	Degree of primary capacitance drift	-0.2~0.2	/
$d_S$	Degree of secondary capacitance drift	-0.2~0.2	/
$R_P$	Primary loss resistance	0.72	$\Omega$
$R_S$	Secondary loss resistance	0.48	$\Omega$
$R_L$	Load resistance	100	$\Omega$
$f_N$	Nominal switching frequency	85	kHz
$U_{in}$	DC input voltage	200	V

that the proposed WPT system is able to deal with the majority of the capacitance drift cases in practice. The investigated capacitance drift range follows the analysis in [21].

With the parameter deviations caused by capacitance drift and coil misalignment taken into account, the parameters of the SS-compensated system are listed in Table I.

### C. Impact of Parameter Deviations

1) *Power Transfer Capability*: According to (1), the output power of the resonant tank is derived by

$$P_{out} = |\dot{I}_S|^2 R_E = \omega^2 M^2 |\dot{V}_P|^2 R_E / D_E \quad (4)$$

where  $D_E = (X_P^2 + R_P^2)(R_{ST}^2 + X_{ST}^2) + 2\omega^2 M^2(R_P R_{ST} - X_P X_{ST}) + \omega^4 M^4$ ,  $R_{ST} = R_S + R_E$ , and  $X_{ST} = X_S + X_E$ . As illustrated in (4), the parameter deviations of the coil inductances and compensation capacitances influence the primary and secondary reactance  $X_P$  and  $X_S$ , which in turn affects the output power. Assume the equivalent load reactance  $X_E = 0$ , the output power  $P_{out}$  versus the equivalent load resistance  $R_E$  under parameter deviations is shown in Fig. 5. As it can be observed in Fig. 5(a), the output power curve has a peak point when the degree of capacitance drift is  $d_P = d_S = -0.2$ . This means that the power transfer capability of the system is limited no matter how the load resistance  $R_E$  is adjusted, and therefore, the system may not be able to reach the required output power. Similar power limitations can also be observed in Fig. 5(b). Compared with Case A, since the air gap  $D$  of Case B is increased from 10 to 15 cm, the mutual inductance is correspondingly reduced from 95 to 58  $\mu\text{H}$ , and thus, the system can reach more power. However, in some cases, the output power of the system is still limited due to the capacitance drift, for example, the case of  $d_P = 0.2, d_S = 0$ .

2) *Transfer Efficiency*: Another effect of the parameter deviations is on the transfer efficiency. Based on (1), the transmission efficiency of the resonant tank is obtained as

$$\eta = \frac{|\dot{I}_S|^2 R_E}{\text{Re}[\dot{V}_P(I_P)^*]} = \frac{\omega^2 M^2 R_E}{\omega^2 M^2 R_{ST} + R_P(R_{ST}^2 + X_{ST}^2)}. \quad (5)$$

As it can be observed in (5), the secondary lumped reactance  $X_{ST}$  that exists in the denominator degrades the transfer efficiency, whereas the primary reactance  $X_P$  does not directly

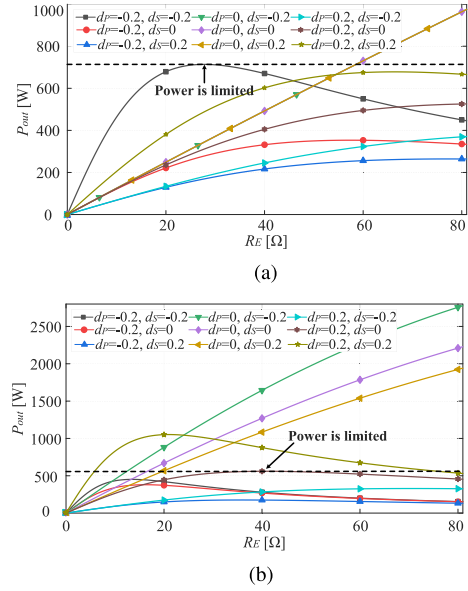


Fig. 5. Output power  $P_{out}$  versus the equivalent load resistance  $R_E$  under parameter deviations. (a) Case A. (b) Case B.

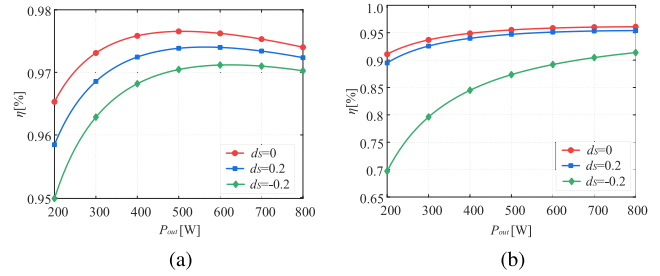


Fig. 6. Transfer efficiency  $\eta$  versus the output power  $P_{out}$  under parameter deviations. (a) Case A. (b) Case B. Herein, the equivalent load resistance  $R_E$  is adjusted to obtain the same output power under different values of  $d_S$ .

affect the efficiency. Assume  $X_E = 0$  and  $d_P = 0$ , the efficiency  $\eta$  versus the output power  $P_{out}$  under parameter deviations is shown in Fig. 6. As it can be observed in Fig. 6(a), the transfer efficiency of the resonant tank is degraded due to the capacitance drift, and the efficiency drop is more noticeable under light load conditions. Moreover, as shown in Fig. 6(b), since the air gap  $D$  is increased to 15 cm in Case B, the secondary self-inductance  $L_S$  is reduced from 222.7 to 216.5  $\mu\text{H}$ . In this case, the secondary reactance  $X_S$  becomes larger when the secondary capacitance is also decreased, and thus, remarkable efficiency reduction can be observed when  $d_S = -0.2$ .

According to the aforementioned analysis, the parameter deviations caused by coil misalignment and capacitance drift reduce the system transfer efficiency and may result in a failure to obtain the required output power. Therefore, it is desirable to cancel the dual-side reactance caused by parameter deviations so that the system can always operate at the resonance state.

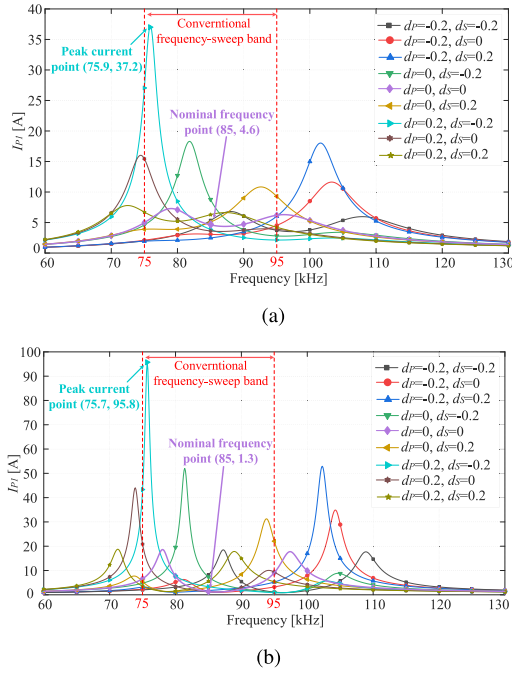


Fig. 7. Value of  $I_{P1}$  under frequency variations and parameter deviations. (a)  $R_E = 24.1 \Omega$  (Case B), where the output power at the nominal frequency point is 800 W. (b)  $R_E = 5.8 \Omega$  (Case B), where the output power at the nominal frequency point is 200 W. Herein, the DC input voltage of the system is 200 V, the nominal switching frequency is 85 kHz, and the inverter output is set to the full duty cycle.

### III. PROPOSED PARAMETER RECOGNITION-BASED IMPEDANCE TUNING METHOD

#### A. System Detuning Caused by Frequency Variations

To identify the unknown parameters, conventional parameter recognition methods generally sweep the frequency around the nominal resonant frequency [26], [27]. However, for the SS-compensated WPT system, the nominal resonant frequency may split into multiple resonant frequencies due to the parameter deviations, which is the so-called bifurcation phenomenon [29]. Since these resonant frequencies are close to the nominal frequency, the traditional frequency-sweep process causes severe system detuning under parameter deviations, which results in enormous coil currents and significant power ripple.

To demonstrate the influence of the system detuning on the coil currents, the rms value of the fundamental component of the primary coil current  $I_{P1}$  under parameter deviations and frequency variations is depicted in Fig. 7, where the frequency-sweep band is set to 75~95 kHz to ensure that sufficient frequency points can be collected [26]. In Fig. 7, the equivalent load resistance  $R_E$  is set to different values to investigate the impact of load variations, while Case B is selected as an example to demonstrate the influence of coil misalignment. Moreover, nine different capacitance drift cases are illustrated with dotted solid lines in different colors to show the influence of capacitance drift, where the maximum degree of capacitance drift is set to  $\pm 20\%$ . As illustrated in Fig. 7(a), when the equivalent load resistance  $R_E$  is 24.1  $\Omega$  under Case B, the output power at the nominal frequency point is 800 W, with the primary coil current

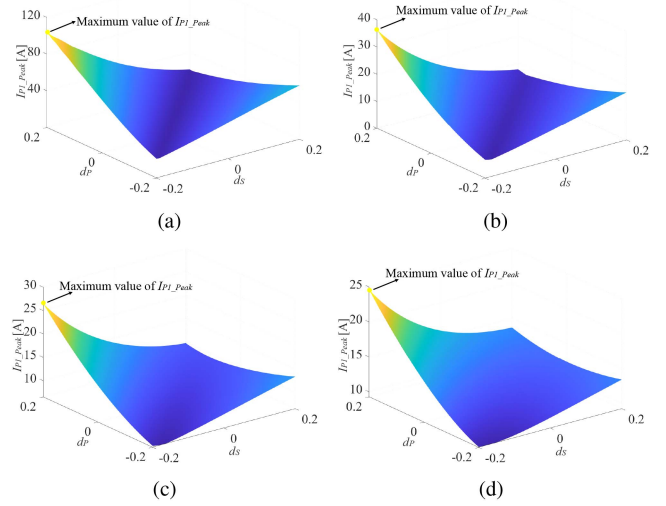


Fig. 8. Value of the peak primary coil current  $I_{P1\_Peak}$  under different values of  $R_E$  and degree of capacitance drift in Case B. (a)  $R_E = 5 \Omega$ . (b)  $R_E = 25 \Omega$ . (c)  $R_E = 45 \Omega$ . (d)  $R_E = 65 \Omega$ .

at 4.6 A. However,  $I_{P1}$  increases to 37.2 A at 75.9 kHz under  $d_P = 0.2$  and  $d_S = -0.2$ . More severe system detuning can be observed under smaller load resistances, as shown in Fig. 7(b). When the equivalent load resistance  $R_E$  is 5.8  $\Omega$  under Case B, the output power at the nominal frequency point is 200 W, with the primary coil current  $I_{P1}$  at 1.3 A. Due to the frequency variations and capacitance drift,  $I_{P1}$  dramatically increases to 95.8 A at 75.7 kHz under  $d_P = 0.2$  and  $d_S = -0.2$ . It should be noted that, in Fig. 7, the inverter output is set to the full duty cycle. Although decreasing the inverter duty cycle is able to reduce the coil currents, it results in a remarkable disparity in the current amplitudes under different cases. This poses a great challenge to the measurement accuracy of the coil currents.

Furthermore, observing the current curve in Fig. 7 reveals that the peak current point can be derived by sweeping the frequency. Take Case B as an example, by sweeping the frequency from 60 to 130 kHz, the peak value of the primary coil current  $I_{P1\_Peak}$  under different values of  $R_E$  and degree of capacitance drift is illustrated in Fig. 8. As shown in Fig. 8, the maximum value of  $I_{P1\_Peak}$ , i.e.,  $MAX\_IP1\_Peak$ , can always be found in the case of  $d_P = 0.2$  and  $d_S = -0.2$ , where the degree of the primary and secondary capacitance drift reaches the upper boundary and the lower boundary, respectively. Moreover, by sweeping the parameters of the equivalent load resistance  $R_E$  and the coil coupling coefficient  $k$ , the value of  $MAX\_IP1\_Peak$  under load variations and coupling changes is shown in Fig. 9. As it can be observed, the value of  $MAX\_IP1\_Peak$  is inversely related to both  $R_E$  and  $k$ . In other words, when  $R_E$  or  $k$  is small, more severe system detuning may occur due to the frequency variations and parameter deviations. Specifically, the worst case shown in Fig. 9 is the point A, where the value of  $MAX\_IP1\_Peak$  reaches 101.8 A when  $R_E = 5 \Omega$  and  $k = 0.22$ , while the best case is the point B, where the value of  $MAX\_IP1\_Peak$  is 11.6 A under  $R_E = 81 \Omega$  and  $k = 0.35$ .

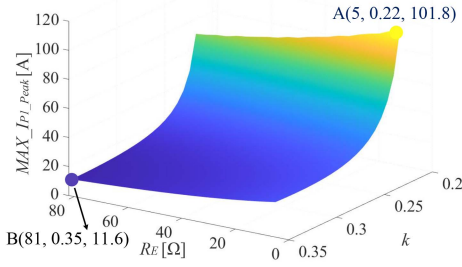


Fig. 9. Value of MAX\_IP1\_Peak under different values of  $R_E$  and  $k$ .

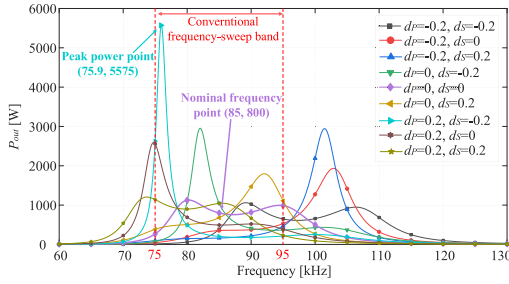


Fig. 10. System output power  $P_{out}$  under frequency variations and parameter deviations when the equivalent load resistance  $R_E$  is  $24.1 \Omega$  in Case B. Herein, the input conditions of the system are the same as those in Fig. 7.

The increased coil currents not only significantly increase the current stress of the resonant tank, but also potentially damage the semiconductor devices due to the rise of their junction temperature.

Another impact of the system detuning is on the system output power  $P_{out}$ . As shown in Fig. 10, when the equivalent load resistance  $R_E$  is  $24.1 \Omega$  under Case B, significant power ripple is observed under frequency variations and parameter deviations. In some cases, the output power of the system may considerably exceed the load tolerance, eventually causing irreparable damage to the load.

According to the aforementioned analysis, it can be concluded that the traditional frequency-sweep-based parameter recognition methods may lead to severe system detuning under parameter deviations, resulting in considerable coil currents and significant power ripple. Therefore, to ensure the safe operation of the system, it is essential to avoid wide frequency variations near the nominal resonance point.

### B. Proposed Parameter Recognition Method

This article proposes a new parameter recognition method to recognize the unknown parameters of the capacitors and coils, i.e.,  $L_P$ ,  $L_S$ ,  $C_P$ ,  $C_S$ , and  $M$ , as shown in Fig. 11. First, the parameter recognition process is carried out at pre start-up, and the rectifier output is short-circuited during this process. As a result, significant load power ripple during the conventional frequency-sweep process is avoided. It should be noted that in [30] and [31], the rectifier output is also short-circuited to implement fast mutual inductance identification. However, in this article, all the unknown parameters of the resonant circuits

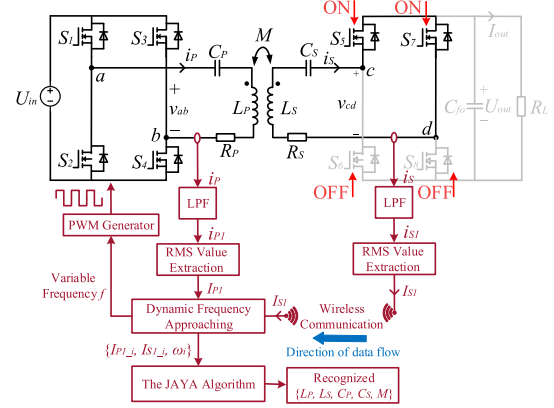


Fig. 11. Block diagram of the proposed parameter recognition method implemented at pre start-up, where the rectifier output is short-circuited during this process. Herein, the measured  $I_{S1}$  is transmitted from the secondary controller to the primary controller for parameter recognition.

are considered, and the number of unknown parameters are much larger than that in [30] and [31]. Then, the primary and secondary coil currents  $i_P$  and  $i_S$  are measured and fed to two separate low-pass filters (LPFs). With the LPFs, the fundamental components of  $i_P$  and  $i_S$ , i.e.,  $i_{P1}$  and  $i_{S1}$ , are extracted. Furthermore, the rms values of  $i_{P1}$  and  $i_{S1}$ , i.e.,  $I_{P1}$  and  $I_{S1}$ , are obtained by the rms value extraction modules. According to the values of  $I_{P1}$  and  $I_{S1}$ , a dynamic frequency approaching strategy is proposed to determine the selected frequency points. By recording the values of  $I_{P1}$  and  $I_{S1}$  at different frequency points, multiple sets of  $\{\omega_i, I_{P1_i}, I_{S1_i}\}$  are acquired. Finally, based on the acquired data, the unknown parameters are derived by the JAYA algorithm. In the following section, the implementation of the proposed method will be described in detail.

1) *Recognition Model*: When the rectifier output is short-circuited, the equivalent input impedance  $Z_{in}$  of the SS-compensated system is derived by

$$Z_{in} = R_P + j \left( \omega L_P - \frac{1}{\omega C_P} \right) + Z_R \quad (6)$$

where  $Z_R$  is the reflected impedance of the secondary resonant circuit, which can be expressed as

$$Z_R = \frac{(\omega M)^2}{R_S + j[\omega L_S - 1/(\omega C_S)]}. \quad (7)$$

The amplitude of the equivalent input impedance is denoted by  $|Z_{in}|$ . If the switching angular frequency  $\omega$  is switched to another value, a new value of  $|Z_{in}|$  can be obtained. Furthermore, by sweeping the switching frequency  $\omega$ , multiple sets of  $\{\omega_i, |Z_{in_i}|\}$  can be acquired as

$$|Z_{in_i}| = \frac{V_{P1_i}}{I_{P1_i}} = f(R_P, R_S, L_P, L_S, C_P, C_S, M, \omega_i) \quad (8)$$

where  $\omega_i$  ( $i = 1, 2, \dots, m$ ) is the  $i$ th selected frequency point;  $m$  is the number of the measured frequency points;  $V_{P1_i}$  and  $I_{P1_i}$  are the rms values of  $v_{P1}$  and  $i_{P1}$  at the  $i$ th frequency point; and  $v_{P1}$  is the fundamental component of the inverter output voltage  $v_{ab}$ . According to the analysis in [26], assuming  $R_P$  and  $R_S$  are



given,  $\{L_P, L_S, C_P, C_S, M\}$  can be estimated by multiple sets of  $\{\omega_i, |Z_{in\_i}|\}$ .

However, it is difficult to identify  $\{L_S, C_S, M\}$  accurately with only the front-end information, as there are countless sets of  $\{L_S, C_S, M\}$  that lead to an almost consistent reflected impedance  $Z_R$ . Suppose there is a new set of solution  $\{L'_S, C'_S, M'\}$  satisfying  $L'_S = \lambda L_S$ ,  $C'_S = (1/\lambda)C_S$ ,  $M' = \sqrt{\lambda}M$ , where  $\{L_S, C_S, M\}$  represents the correct solution and  $\lambda$  is any nonzero positive real number. Generally, when the switching frequency  $\omega$  is deviated from the secondary resonant frequency  $\omega_S$  ( $\omega_S = 1/\sqrt{L_S C_S}$ ),  $X_S$  is much larger than  $R_S$ . Therefore, the reflected impedance  $Z'_R$  of the new set of solution satisfies

$$Z'_R \approx \frac{(\omega M')^2}{j[\omega L'_S - 1/(\omega C'_S)]} = \frac{\lambda(\omega M)^2}{j\lambda[\omega L_S - 1/(\omega C_S)]} \approx Z_R. \quad (9)$$

Since  $\lambda$  can be any value, there are countless sets of solution  $\{L'_S, C'_S, M'\}$  such that the reflected impedance  $Z'_R$  is almost identical with the correct reflected impedance  $Z_R$ . This means that it is difficult to accurately recognize  $\{L_S, C_S, M\}$  with only the primary-side information. Therefore, in this article, the secondary coil current  $i_S$  is also measured. By introducing the secondary-side information, the relationship between  $I_{P1}$  and  $I_{S1}$  is established as

$$\frac{I_{P1}}{I_{S1}} = \sqrt{\frac{R_S^2 + [\omega L_S - 1/(\omega C_S)]^2}{(\omega M)^2}} \approx \frac{\omega L_S - 1/(\omega C_S)}{\omega M}. \quad (10)$$

Define the ratio of  $I_{P1}$  to  $I_{S1}$  as  $T_{ii}$ , i.e.,  $T_{ii} = I_{P1}/I_{S1}$ . Then, the ratio  $T'_{ii}$  of the new set of solution  $\{L'_S, C'_S, M'\}$  satisfies

$$T'_{ii} \approx \frac{\omega L'_S - 1/(\omega C'_S)}{\omega M'} = \frac{\lambda[\omega L_S - 1/(\omega C_S)]}{\sqrt{\lambda}\omega M} \approx \sqrt{\lambda}T_{ii}. \quad (11)$$

The only solution of  $\lambda$  such that (9) and (11) hold simultaneously is  $\lambda = 1$ . This means that by introducing the information of  $i_S$ , the correct solution of  $\{L_S, C_S, M\}$  is unique and all the unknown parameters can be estimated accurately.

To introduce the information of  $i_S$  into the recognition model, the equivalent gain from  $I_{S1}$  to  $V_{P1}$  is given by

$$|Z_{PS}| = \frac{V_{P1}}{I_{S1}} = \left| j\omega M - \frac{(R_P + jX_P)(R_S + jX_S)}{j\omega M} \right|. \quad (12)$$

Similarly, by sweeping the switching frequency  $\omega$ , multiple sets of  $\{\omega_i, |Z_{PS\_i}|\}$  can be obtained as

$$|Z_{PS\_i}| = \frac{V_{P1\_i}}{I_{S1\_i}} = g(R_P, R_S, L_P, L_S, C_P, C_S, M, \omega_i). \quad (13)$$

Furthermore, with the information on both sides, the recognition model for the unknown parameters is derived as

$$\min J = \|\mathbf{V}_{P1} - \mathbf{V}_{P1\text{est}}\| + \|\mathbf{V}_{P1} - \hat{\mathbf{V}}_{P1\text{est}}\| \quad (14)$$

s.t.  $\mathbf{V}_{P1\text{est}} = |\mathbf{Z}_{in}|\mathbf{I}_{P1}$ ,  $\hat{\mathbf{V}}_{P1\text{est}} = |\mathbf{Z}_{PS}|\mathbf{I}_{S1}$ ,  $L_{PL} \leq L_P \leq L_{PH}$ ,  $L_{SL} \leq L_S \leq L_{SH}$ ,  $C_{PL} \leq C_P \leq C_{PH}$ ,  $C_{SL} \leq C_S \leq C_{SH}$ , and  $M_L \leq M \leq M_H$ , where

$$|\mathbf{Z}_{in}| = \text{diag}\{|Z_{in\_i}|\} (i = 1, \dots, m)$$

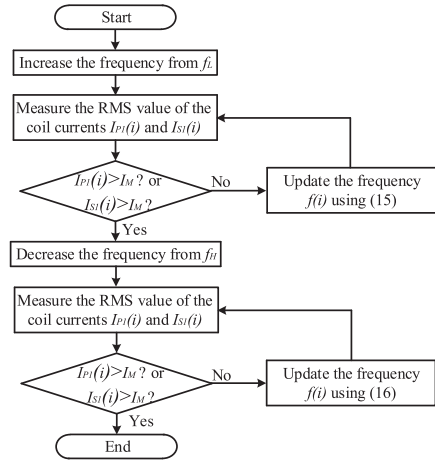


Fig. 12. Flow chart of the proposed dynamic frequency approaching strategy.

$$|\mathbf{Z}_{PS}| = \text{diag}\{|Z_{PS\_i}|\} (i = 1, \dots, m)$$

$$\mathbf{I}_{P1} = [I_{P1\_1}, I_{P1\_2}, \dots, I_{P1\_m}]$$

$$\mathbf{I}_{S1} = [I_{S1\_1}, I_{S1\_2}, \dots, I_{S1\_m}]$$

$$\mathbf{V}_{P1\text{est}} = [V_{P1\text{est\_1}}, V_{P1\text{est\_2}}, \dots, V_{P1\text{est\_m}}]$$

$$\hat{\mathbf{V}}_{P1\text{est}} = [\hat{V}_{P1\text{est\_1}}, \hat{V}_{P1\text{est\_2}}, \dots, \hat{V}_{P1\text{est\_m}}]$$

$$\mathbf{V}_{P1} = [V_{P1\_1}, V_{P1\_2}, \dots, V_{P1\_m}]$$

Herein,  $\mathbf{I}_{P1}$  is the measured rms values of  $i_{P1}$  at multiple frequency points;  $\mathbf{V}_{P1\text{est}}$  is the estimated rms values of  $v_{P1}$  derived by  $|\mathbf{Z}_{in}|\mathbf{I}_{P1}$ ;  $\mathbf{I}_{S1}$  is the measured rms values of  $i_{S1}$ ;  $\hat{\mathbf{V}}_{P1\text{est}}$  is the estimated rms values of  $v_{P1}$  derived by  $|\mathbf{Z}_{PS}|\mathbf{I}_{S1}$ ;  $\mathbf{V}_{P1}$  is the measured rms values of  $v_{P1}$ ;  $\|\mathbf{V}_{P1} - \mathbf{V}_{P1\text{est}}\|$  represents the norm of the voltage differences between  $\mathbf{V}_{P1}$  and  $\mathbf{V}_{P1\text{est}}$ ;  $\|\mathbf{V}_{P1} - \hat{\mathbf{V}}_{P1\text{est}}\|$  is the norm of the voltage differences between  $\mathbf{V}_{P1}$  and  $\hat{\mathbf{V}}_{P1\text{est}}$ . It should be noted that when the dc input voltage  $U_{in}$  and the duty cycle of the inverter ac voltage  $v_{ab}$  remain unchanged, the rms value of  $v_{P1}$  does not vary with the switching frequency. In our article, the dc input voltage is configured at 200 V, and the inverter output is fixed at the full duty cycle. This means that the measurement process for the inverter voltage can be avoided. Based on the recognition model, the unknown parameters  $\{L_P, L_S, C_P, C_S, M\}$  are searched within the empirically selected lower and upper bounds.

2) *Dynamic Frequency Approaching*: Based on the aforementioned analysis, it is essential to measure  $i_P$  and  $i_S$  at multiple frequency points for parameter recognition. However, according to the analysis in Section III-A, when the parameters of the capacitors and coils deviate from the nominal values, the frequency variations near the nominal resonance point may lead to severe system detuning, resulting in enormous coil currents. To constrain the coil currents in a safe range, a dynamic frequency approaching strategy is proposed, as shown in Fig. 12. In Fig. 12,  $f_L$ ,  $f_H$ , and  $I_M$ , as well as the update equations (15) and (16), are predesigned based on the system parameters and stored in the microcontrollers in advance. However, the values of  $I_{P1}$  and  $I_{S1}$  are updated based on the measured results in

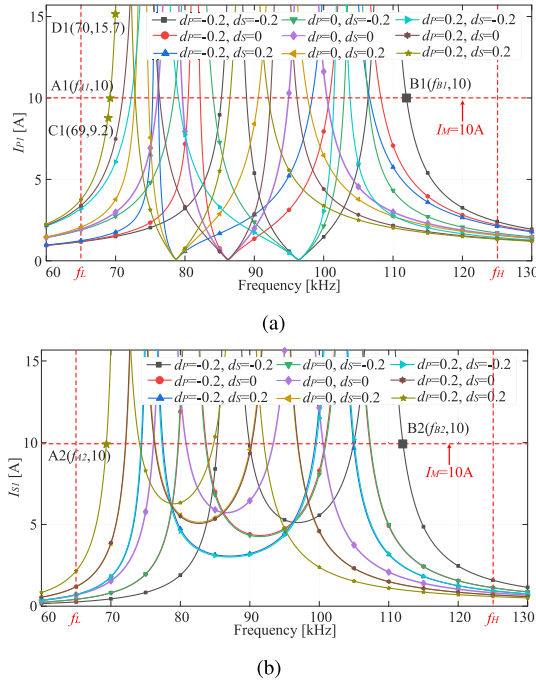


Fig. 13. Values of  $I_{P1}$  and  $I_{S1}$  when the rectifier output is short-circuited under Case B. (a)  $I_{P1}$ . (b)  $I_{S1}$ .

practical operation. The detailed steps of this strategy are as follows. First, the frequency is swept from the lower bound  $f_L$  at various frequency points, while  $I_{P1}$  and  $I_{S1}$  are measured. The frequency-sweeping process is stopped when  $I_{P1}$  or  $I_{S1}$  exceeds the threshold value  $I_M$ . Then, the frequency is swept from the upper bound  $f_H$  and is terminated when  $I_{P1}$  or  $I_{S1}$  is larger than  $I_M$  again.

In this article, the current threshold  $I_M$  is set as 10 A based on the current capability of the system, while  $f_L$  and  $f_H$  are set to 65 and 125 kHz. The basic principle of selecting  $f_L$  and  $f_H$  is to ensure that  $I_{P1}$  and  $I_{S1}$  at both  $f_L$  and  $f_H$  are lower than 10 A under any case. Take Case B as an example, the values of  $I_{P1}$  and  $I_{S1}$  when the rectifier output is short-circuited is shown in Fig. 13. As illustrated in Fig. 13(a),  $f_L$  is required to be lower than  $f_{A1}$  to ensure that the value of  $I_{P1}$  is smaller than 10 A at the frequency point  $f_L$  under any case, while  $f_H$  should be higher than  $f_{B1}$  to guarantee  $I_{P1}$  is always smaller than 10 A at  $f_H$ . Similarly, as shown in Fig. 13(b),  $f_L$  is also required to be less than  $f_{A2}$ , and  $f_H$  is needed to be greater than  $f_{B2}$  to ensure that the value of  $I_{S1}$  does not exceed the threshold. Furthermore, define  $f_{A\_min}$  as the minimum value of  $f_{A1}$  and  $f_{A2}$ ,  $f_{B\_max}$  as the maximum value of  $f_{B1}$  and  $f_{B2}$ , the values of  $f_{A\_min}$  and  $f_{B\_max}$  under different values of  $k$  when the rectifier output is short-circuited is illustrated in Fig. 14. To guarantee the coil currents at  $f_L$  and  $f_H$  are lower than 10 A under any case, as shown in Fig. 14,  $f_L$  is required to be lower than 65.1 kHz, and  $f_H$  should be larger than 121.7 kHz. Therefore,  $f_L$  and  $f_H$  are set to 65 and 125 kHz, respectively.

Moreover, the interval of the frequency points is not fixed but dynamically adjusted according to the measured current values. The motivations of the dynamic frequency interval are

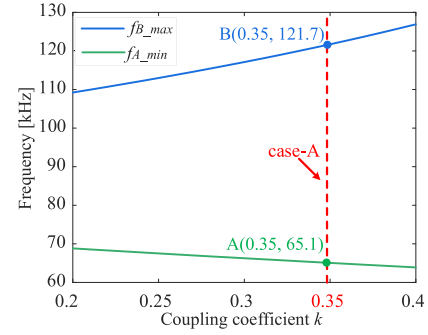


Fig. 14. Values of  $f_{A\_min}$  and  $f_{B\_max}$  under different values of  $k$  when the rectifier output is short-circuited.

as follows. On one hand, when the frequency approaches to the peak current point, the coil currents rise dramatically. Take  $d_P = d_S = 0.2$  under Case B as an example, as shown in Fig. 13(a),  $I_{P1}$  is 9.2 A when the frequency is 69 kHz, whereas it rapidly increases to 15.7 A at 70 kHz. As a result, if the frequency interval is large under the high-current frequency points, the coil currents may greatly exceed the threshold, endangering the safe operation of the system. On the other hand, when the frequency is close to  $f_L$  and  $f_H$ , as illustrated in Fig. 13(a), the coil currents might be quite small under some cases, and the measurement errors should be considered in these cases. Therefore, if the frequency interval is small under the low-current frequency points, the measurement errors might be significant in some cases. Besides, a small frequency interval will also make the frequency-sweep process time consuming. Considering the aforementioned reasons, a dynamic frequency interval is adopted in this article. When the frequency is increased from  $f_L$ , the update equation is

$$f(i+1) = f(i) + \tau \times \text{ceil}[I_M - \max(I_{P1}(i), I_{S1}(i))] \quad (15)$$

where  $\text{ceil}$  is the round-up function;  $\tau$  is a fixed factor, which is set to 0.2 to ensure that the coil current does not increase dramatically as it approaches to the threshold  $I_M$ . Similarly, when the frequency is decreased from  $f_H$ , the updated equation is

$$f(i+1) = f(i) - \tau \times \text{ceil}[I_M - \max(I_{P1}(i), I_{S1}(i))]. \quad (16)$$

As shown in (15) and (16), the frequency interval is dynamically adjusted between 0.2 and 2 kHz according to the rms values of the coil currents. Based on the aforementioned analysis, by using the proposed dynamic frequency approaching strategy, the coil currents are constrained safely, and the required data for parameter recognition is acquired efficiently.

3) *JAYA Algorithm*: After the required data are obtained, the optimization problem described in (14) is needed to be solved to recognize the unknown parameters. In this article, a heuristic algorithm called JAYA is introduced to derive the unknown parameters. Generally, there are two mainstream approaches for solving unknown parameters in the WPT systems: the least square approximation (LSA) and the heuristic algorithms. The LSA was implemented in [32] to recognize the mutual inductance and load resistance, while it was used for identifying multiple loads in [27] and the secondary-side reactance in [22]. The heuristic

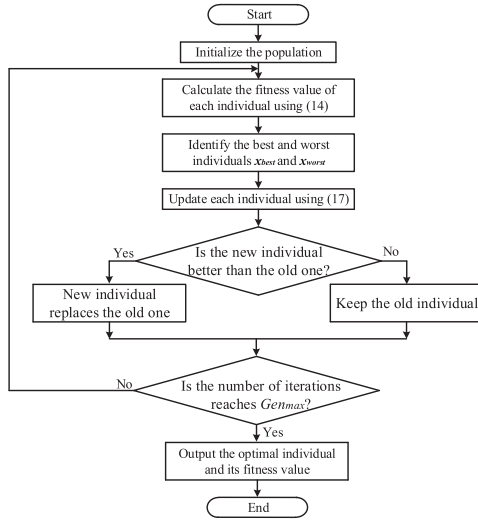


Fig. 15. Flowchart of the JAYA algorithm.

algorithms, which can find optimal solutions more efficiently than the traditional LSA for the multivariable systems [26], are also usually used, such as the GA in [33], and the adaptive differential evolution (ADE) algorithm in [26]. However, for the conventional GA algorithm and differential evolution (DE) algorithm, various algorithm-specific parameters, including the crossover and mutation rates, need to be tuned. Although the ADE algorithm avoids the difficulty of tuning parameters, the adaptive cross-over and mutation rates need to be calculated in each iteration, which increases the complexity of the algorithm. Compared with the GA and ADE algorithms, the JAYA algorithm is free from algorithm-specific parameters (except for two common parameters, i.e., the population size  $P_{size}$  and the maximum number of generations  $Gen_{max}$ ), and only one update equation is required in each generation [28]. The flowchart of the JAYA algorithm is depicted in Fig. 15, and the process is detailed as follows: *[Initialization]* First, a random population  $x$  with  $P_{size}$  individuals is generated in the search space (within the lower and upper bounds), where  $x_{p,q}$  represents the  $q$ th parameter of the  $p$ th individual ( $p = 1, 2, \dots, P_{size}; q = 1, 2, \dots, N$ ), and  $N$  is the number of the unknown parameters. Specifically, in this article,  $x$  represents the population with  $P_{size}$  ( $P_{size}=50$ ) individuals, and each individual consists of  $N$  ( $N=7$ ) unknown parameters. The unknown parameters are  $R_P, R_S, L_P, L_S, C_P, C_S$ , and  $M$ , respectively. *[Fitness]* Then, the fitness value of each individual is calculated based on the cost function described in (14). *[Update]* According to the fitness value of each individual, the best individual  $x_{best} = [x_{best,1}, x_{best,2}, \dots, x_{best,N}]$  with minimum fitness value and the worst individual  $x_{worst} = [x_{worst,1}, x_{worst,2}, \dots, x_{worst,N}]$  with maximum fitness value are selected, and the population is then updated by

$$x'_{p,q} = x_{p,q} + r_1(x_{best,q} - |x_{p,q}|) - r_2(x_{worst,q} - |x_{p,q}|) \quad (17)$$

where  $x_{best,q}$  and  $x_{worst,q}$  are the  $q$ th parameter of the best and worst individuals, respectively;  $r_1$  and  $r_2$  are two random numbers within  $[0,1]$ . In (17), the term  $r_1(x_{best,q} - |x_{p,q}|)$  reveals the tendency of approaching the best individual, whereas the

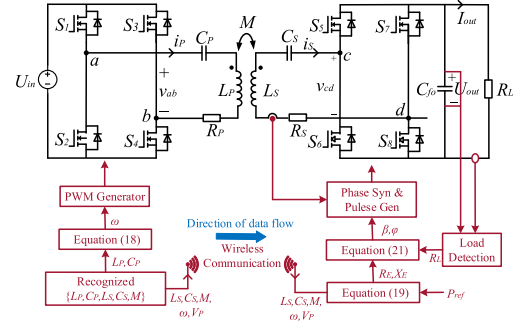


Fig. 16. Block diagram of the impedance tuning method. Herein, the parameters  $\{L_S, C_S, M, \omega, V_P\}$  are transmitted from the primary controller to the secondary controller for calculating the required phase shift angles of the active rectifier.

term  $-r_2(x_{worst,q} - |x_{p,q}|)$  indicates the tendency of escaping from the worst individual. *[Selection]* The updated individual  $x'_{p,q}$  is accepted if it gives a better fitness value. All the accepted individuals at the end of iteration are retained and become the input of the next generation. *[Termination]* The optimization process is stopped when the termination criteria is satisfied. Here, the termination criteria is the number of iterations reaches  $Gen_{max}$ .

### C. Impedance Tuning

Based on the recognized parameters, an impedance tuning method is adopted, as shown in Fig. 16. To minimize the primary reactance  $X_P$ , the switching frequency  $\omega$  of the inverter is adjusted to

$$\omega = \frac{1}{\sqrt{L_P C_P}}. \quad (18)$$

Additionally, the duty cycle of the inverter ac voltage  $v_{ab}$  is maintained at the full duty cycle. Then, the equivalent load impedance  $Z_E$  is regulated by the active rectifier to minimize the secondary reactance  $X_S$  and to obtain the required output power  $P_{ref}$ , i.e.,

$$\begin{cases} R_E = \frac{\omega^2 M^2 P_{ref}}{V_P^2} \\ X_E = -X_S = -\left(\omega L_S - \frac{1}{\omega C_S}\right). \end{cases} \quad (19)$$

Herein, it should be noted that the secondary reactance can be slightly overcompensated to realize zero-voltage-switching (ZVS) for the inverter [22]. According to [18], the equivalent load impedance provided by the active rectifier is

$$\begin{cases} R_E = \frac{4}{\pi^2} R_L \cos^2(\varphi)(1 - \cos(\beta)) \\ X_E = \frac{4}{\pi^2} R_L \sin(\varphi)\cos(\varphi)(1 - \cos(\beta)) \end{cases} \quad (20)$$

where  $\beta$  is the duty-cycle angle of the rectifier input voltage  $v_{cd}$ , and  $\varphi$  is the phase shift angle between  $\dot{V}_S$  and  $\dot{I}_S$ . Substituting (20) into (21),  $\beta$  and  $\varphi$  are derived by

$$\begin{cases} \varphi = \arctan\left(\frac{X_E}{R_E}\right) \\ \beta = \arccos\left(1 - \frac{\pi^2 X_E}{2R_L \sin(2\varphi)}\right). \end{cases} \quad (21)$$

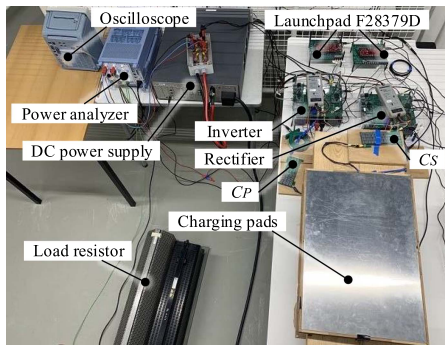


Fig. 17. Experimental setup of the SS-compensated WPT system.

TABLE II  
CASE STUDY FOR PARAMETER RECOGNITION

No.	$L_P$ [ $\mu\text{H}$ ]	$L_S$ [ $\mu\text{H}$ ]	$M$ [ $\mu\text{H}$ ]	$C_P$ [nF]	$C_S$ [nF]
A1	335.5	222.7	95	9.9	17.32
A2	335.5	222.7	95	11.53	16.5
A3	335.5	222.7	95	11.53	14.88
A4	335.5	222.7	95	9.9	13.21
A5	335.5	222.7	95	9.07	14.88
B1	327.5	216.5	58	9.9	17.32
B2	327.5	216.5	58	11.53	16.5
B3	327.5	216.5	58	11.53	14.88
B4	327.5	216.5	58	9.9	13.21
B5	327.5	216.5	58	9.07	14.88

Considering the range of  $\beta$  ( $[0, \pi]$ ) and  $\varphi$  ( $[-\pi/2, \pi/2]$ ), the maximum  $R_E$  and  $X_E$  that can be provided by the active rectifier are  $8R_L/\pi^2$  and  $\pm 4R_L/\pi^2$ , respectively.

#### IV. EXPERIMENTAL VERIFICATION

##### A. Experimental Setup

To verify the feasibility of the proposed parameter recognition-based impedance tuning method, experiments are carried out on an SS-compensated WPT prototype using the charging pads in Fig. 3, as shown in Fig. 17. A dc power supply is utilized to provide the required power, and two rheostats are connected in series as the load resistor. The impedance tuning algorithm and PWM generation are implemented in the LaunchPad F28379D. Two separate H-bridge converters are adopted as the inverter and the active rectifier, respectively. The experimental data and waveforms are recorded by an oscilloscope (YOKOGAWA DLM2054) and the dc to dc efficiency of the system is measured by a power analyzer (YOKOGAWA WT500). More details of the prototype are listed in Table II.

##### B. Parameter Recognition

The accuracy of the proposed parameter recognition method is verified in ten cases of the parameter deviations, as listed in Table II. The parameters of the coil inductances and compensation capacitances in Table III are measured by an impedance analyzer (Agilent 4294 A).

To acquire the required data for parameter recognition, the rectifier output is short-circuited and the system frequency  $f$  is regulated based on the dynamic frequency approaching strategy

TABLE III  
PARAMETERS OF THE JAYA ALGORITHM

Symbol	Value	Symbol	Value
$L_{PL}$	300 $\mu\text{H}$	$L_{PH}$	350 $\mu\text{H}$
$L_{SL}$	200 $\mu\text{H}$	$L_{SH}$	250 $\mu\text{H}$
$M_L$	50 $\mu\text{H}$	$M_H$	120 $\mu\text{H}$
$C_{PL}$	5 nF	$C_{PH}$	15 nF
$C_{SL}$	10 nF	$C_{SH}$	20 nF
$R_{PL}$	0.5 $\Omega$	$R_{PH}$	0.9 $\Omega$
$R_{SL}$	0.3 $\Omega$	$R_{SH}$	0.7 $\Omega$
$P_{\text{size}}$	50	$\text{Gen}_{\text{max}}$	5000

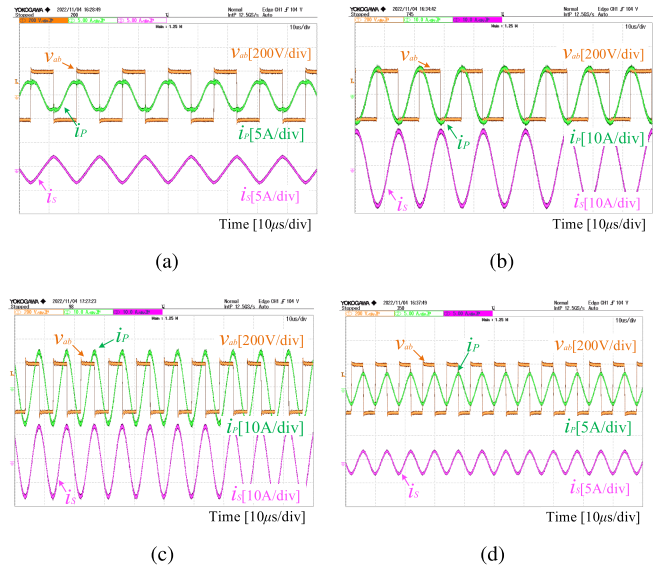


Fig. 18. Measured operating waveforms of Case A1 under different frequency points. (a) 65 kHz. (b) 70.4 kHz. (c) 107.7 kHz. (d) 125 kHz.

shown in Fig. 12. By dynamically adjusting the system frequency  $f$ , the primary and secondary coil currents  $i_P$  and  $i_S$  are measured at multiple frequency points. The measured data are recorded by the oscilloscope, and then, extracted to MATLAB for processing. Fig. 18 shows the recorded waveforms of Case A1 under different frequency points. It should be noted that when the frequency is increased from  $f_L$  (65 kHz), hard switching of the inverter power switches is inevitable due to the capacitive input impedance  $Z_{\text{in}}$ . However, since the data acquisition stage only lasts for hundreds of milliseconds (see Section IV-D), the extra switching loss caused by hard switching during this process can be ignored, and the voltage spikes at the switching transient can also be suppressed by optimizing the resistor-capacitor (RC) snubber circuits in practice [34], [35]. Another noteworthy point is that the extracted coil currents, as shown in Fig. 18(a), contain a small amount of third harmonics when the frequency is increased from  $f_L$  (65 kHz). Therefore, a digital second-order LPF is implemented to filter out the harmonic components of the coil currents when the frequency is increased from  $f_L$ , and the magnitude-frequency response of the designed LPF is illustrated in Fig. 19. It should be noted that when the frequency is decreased from  $f_H$  (125 kHz), the digital LPF is not required due to the third harmonics are well-attenuated by the high-impedance characteristics of the resonant circuits in the



TABLE IV  
COMPARISONS WITH OTHER WORKS ON IMPEDANCE TUNING

Reference	Compensation	Considered parameters	Parameter recognition	Impedance tuning	Wireless communication	Rated Power
[9]	LCC-S	$L_P$	Phase detection	SCC	No	66.8 W
[20]	LCC-S	$M, L_P, L_S$	Phase detection	Frequency tuning & semi-active rectifier	No	3.3 kW
[24]	LCC-LCC	$M, L_P, L_S$	Phase detection & the gradient descent algorithm	Two SCCs	No	3 kW
[21]	SS	$C_P, C_S$	Phase detection & auxiliary coils	Frequency tuning & semi-active rectifier	Yes	50 W
[22]	SS	$L_S, C_S$	Pulse density modulation & the LSA algorithm	Frequency tuning & active rectifier	No	145 W
This article	SS	$M, L_P, L_S, C_P, C_S$	Dynamic frequency approaching & the JAYA algorithm	Frequency tuning & active rectifier	Yes	800 W

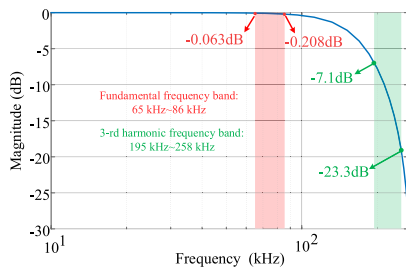


Fig. 19. Magnitude–frequency response of the designed digital LPF. Herein, the maximum frequency point that can be reached when the frequency is increased from  $f_L$  is calculated as 86 kHz based on the parameter deviation range listed in Table II.

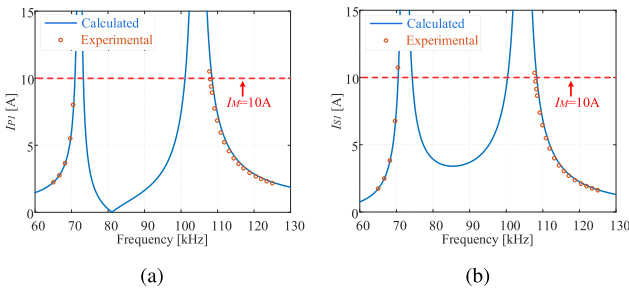


Fig. 20. Extracted rms values of  $I_{P1}$  and  $I_{S1}$  in Case A1. (a)  $I_{P1}$ . (b)  $I_{S1}$ .

high-frequency band, as it can be observed in Fig. 18(c) and (d). After the harmonics are filtered by the LPF, the rms values of the fundamental components of the coil currents, i.e.,  $I_{P1}$  and  $I_{S1}$ , are then extracted by the rms function of MATLAB. The extracted rms values of  $I_{P1}$  and  $I_{S1}$  under Case A1 are illustrated in Fig. 20. As it can be observed, by implementing the proposed dynamic frequency approaching method,  $I_{P1}$  and  $I_{S1}$  are accurately obtained under sufficient frequency points.

Furthermore, based on the values of  $I_{P1}$  and  $I_{S1}$ , the JAYA algorithm is implemented to recognize the unknown parameters of the resonant circuits. The searching constraints of the unknown parameters  $\{L_P, L_S, M, C_P, C_S\}$  for the JAYA algorithm are listed in Table IV. Since the loss resistances  $R_P$  and  $R_S$  may vary with the system operating conditions,  $R_P$  and  $R_S$  are considered as the unknown parameters as well. Additionally, the population size  $P_{size}$  and the maximum generation numbers

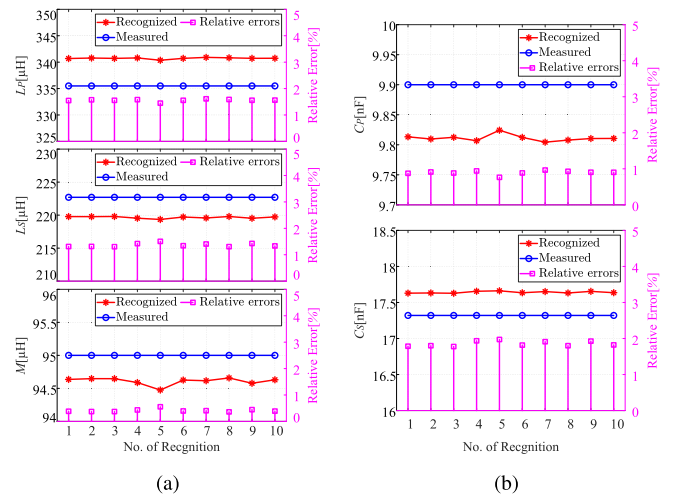


Fig. 21. Recognized results for Case A1. (a) Coil inductances  $L_P$ ,  $L_S$ , and  $M$ . (b) Compensation capacitances  $C_P$  and  $C_S$ .

$Gen_{max}$  of the JAYA algorithm are also shown in Table IV. The parameters are independently recognized by the JAYA algorithm for ten times. The JAYA algorithm is implemented in MATLAB on a computer with a Intel(R) Core(TM) i7-1185G7 CPU, and the average computation time for each recognition is 1–3 s. Fig. 21 presents the recognized parameters for Case A1 in each recognition. As shown in Fig. 21, the unknown parameters of Case A1 are recognized accurately, with the relative errors in each recognition all less than 2%. Besides, as it can be observed, the recognized results of each independent recognition are basically consistent, which validates the stability of the JAYA algorithm. Fig. 22 shows the average relative errors (AREs) of Case A1 under different numbers of frequency points. As shown in Fig. 22, the AREs are significant when the number of extracted frequency points is small. This is because when the amount of extracted data is insufficient, it becomes difficult to converge to the optimal solution in the iterative process due to inevitable measurement noise, and the results of each recognition is not stable. This phenomenon can also be observed in other similar works [22], [27]. However, the AREs converge to a stable level as the number of extracted frequency points increases. It should be noted that the number of frequency points can be tuned by



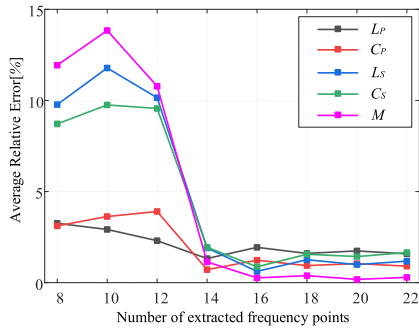


Fig. 22. AREs of Case A1 under different numbers of frequency points.

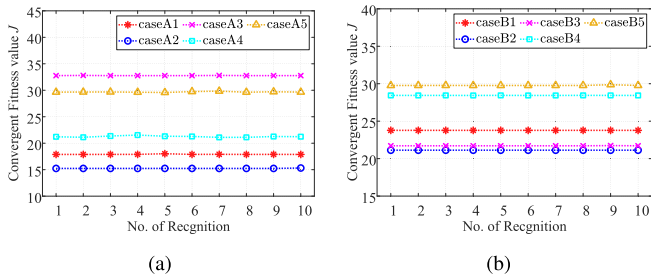


Fig. 23. Convergent fitness values for the studied ten cases. (a) Case A. (b) Case B.

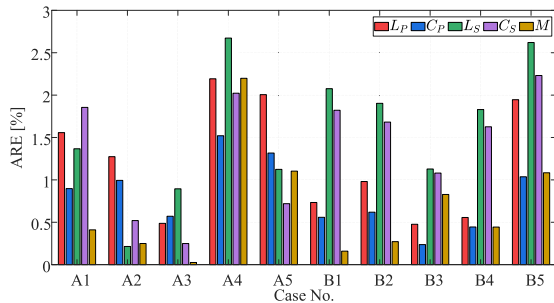


Fig. 24. AREs for the studied ten cases.

tuning the factor  $\tau$  in (15) and (16) to ensure sufficient frequency points can be obtained for accurate parameter recognition.

Moreover, all of the ten cases listed in Table III are studied. To verify the stability of the JAYA algorithm, the convergent fitness values for all of the studied ten cases are demonstrated in Fig. 23. The convergent fitness values are steady for all cases in each recognition, which validates that the JAYA algorithm can always find the global optimal solution. The AREs for the studied ten cases are then presented in Fig. 24. As shown in Fig. 24, the unknown parameters of the resonant circuits are recognized accurately, with the AREs of all cases less than 3%. Moreover, the standard deviations of the recognized results under each case are shown in Fig. 25. The standard deviations of the unknown parameters  $L_P$  and  $L_S$ ,  $C_P$ ,  $C_S$ , and  $M$  are less than  $0.5 \mu\text{H}$ ,  $0.6 \mu\text{H}$ ,  $0.012 \text{ nF}$ ,  $0.035 \text{ nF}$ , and  $0.2 \mu\text{H}$ , respectively, with the relative standard deviations all less than 0.3%.

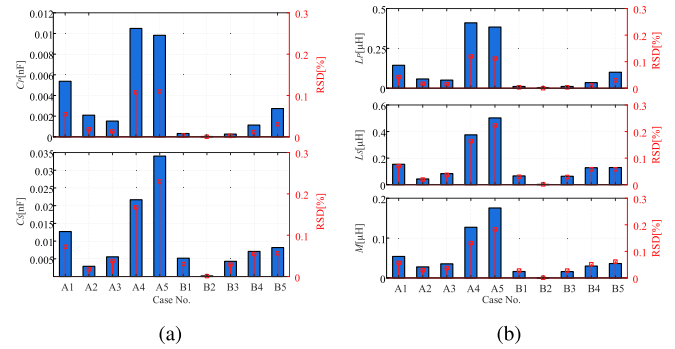
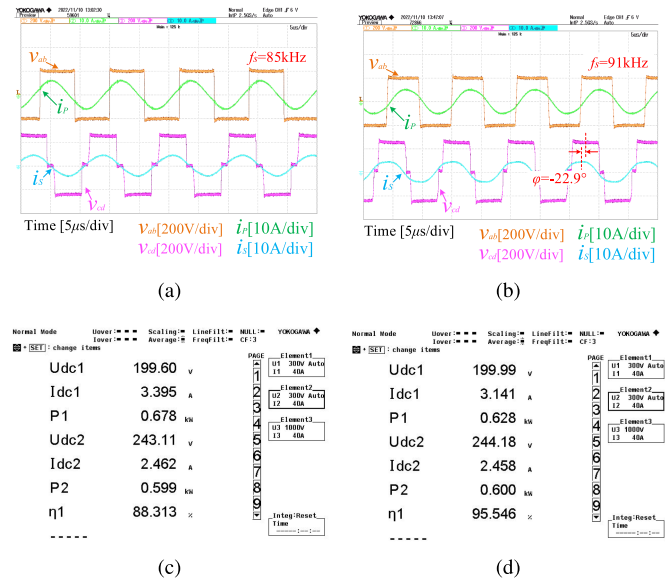

 Fig. 25. Standard deviations for the studied ten cases. (a) Coil inductances  $L_P$ ,  $L_S$ , and  $M$ . (b) Compensation capacitances  $C_P$  and  $C_S$ .


Fig. 26. Measured operating waveforms and dc-to-dc efficiency of Case A5 when delivering 600-W power. (a) Operating waveforms before tuning. (b) Operating waveforms after tuning. (c) Measured dc-to-dc efficiency before tuning. (d) Measured dc-to-dc efficiency after tuning.

### C. Impedance Tuning

After the unknown parameters are accurately recognized, the impedance tuning method is implemented to allow the system operate close to the resonance state. To demonstrate the effectiveness of the impedance tuning method, experiments are carried out in two cases of parameter deviations, i.e., Cases A5 and B5. For Cases A5 and B5, the primary and secondary compensation capacitances are  $9.07$  and  $14.88 \text{ nF}$ , with the degree of capacitance drift at  $-13.21\%$  and  $-5.46\%$ , respectively. Besides, compared with Case A5, the air gap of Case B5 is increased from  $10$  to  $15 \text{ cm}$ , and thus, the coil coupling coefficient  $k$  is decreased from  $0.35$  to  $0.22$ . Due to the aforementioned parameter deviations caused by coil misalignment and capacitance drift, both the primary and secondary resonant circuits are detuned.

Fig. 26 presents the measured operating waveforms of Case A5 when delivering  $600\text{-W}$  power. Before the impedance tuning, as shown in Fig. 26(a), the system frequency is  $85 \text{ kHz}$ , and the secondary ac voltage  $v_{cd}$  and current  $i_S$  are in phase. Moreover,

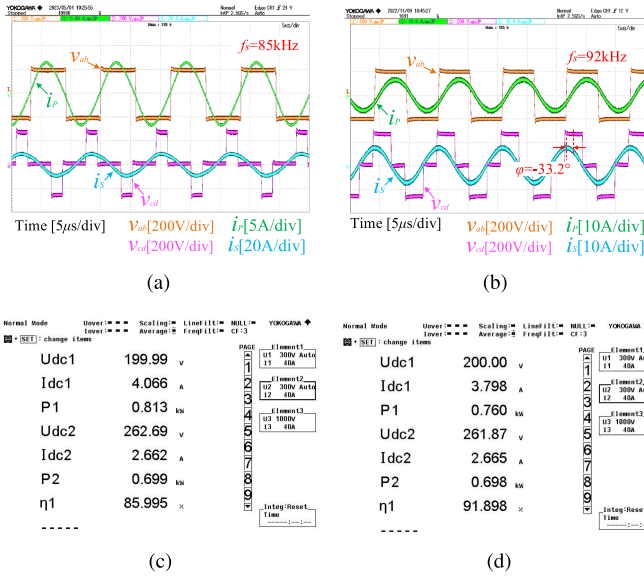


Fig. 27. Measured operating waveforms and DC-to-DC efficiency of Case B5 when delivering 700-W power. (a) Operating waveforms before tuning. (b) Operating waveforms after tuning. (c) Measured DC-to-DC efficiency before tuning. (d) Measured DC-to-DC efficiency after tuning.

due to the system detuning, the primary current  $i_P$  leads the primary ac voltage  $v_{ab}$ . By implementing the impedance tuning method based on the recognized parameters, the operating frequency is increased to 91 kHz to minimize the primary-side reactance  $X_P$ , while the phase shift angle between  $v_{cd}$  and  $i_S$ , i.e.,  $\varphi$ , is regulated to  $-22.9^\circ$  to minimize the secondary-side reactance  $X_S$ . After the impedance tuning, as illustrated in Fig. 26(b), the primary voltage  $v_{ab}$  and current  $i_P$  are almost in phase ( $i_P$  slightly lags behind  $v_{ab}$  to realize ZVS for the inverter). To illustrate the effectiveness of the impedance tuning, the measured dc-to-dc efficiency of Case A5 before and after tuning is further presented in Fig. 26(c) and (d). As it can be observed, when delivering 600 W in Case A5, the dc-to-dc efficiency of the WPT system is increased from 88.3% to 95.5%. The measured operating waveforms and efficiency of Case B5 when delivering 700-W power are then demonstrated in Fig. 27. Based on the identified parameters and carrying out the impedance tuning, as shown in Fig. 27(a) and (b), the system frequency is increased from 85 to 92 kHz, and the phase shift angle  $\varphi$  is adjusted to  $-33.2^\circ$ . The reactance on both sides are minimized simultaneously, and therefore, the dc-to-dc efficiency of the system is improved from 86% to 91.9%.

Furthermore, the measured dc-to-dc efficiency of Cases A5 and B5 under different output power points is shown in Fig. 28. By implementing the impedance tuning method, the dc-to-dc efficiency is significantly improved. As shown in Fig. 28(a), the efficiency is improved by 4.3%–7.7% after achieving impedance tuning in Case A5. More significant efficiency optimization can be observed under Case B5, as illustrated in Fig. 28(b), the efficiency improvement after tuning ranges from 5.9% to 15%.

It should be noted that due to the parameter deviations in Cases A5 and B5, the output power of the system is limited, as illustrated in Fig. 29. Therefore, Fig. 28 only presents the

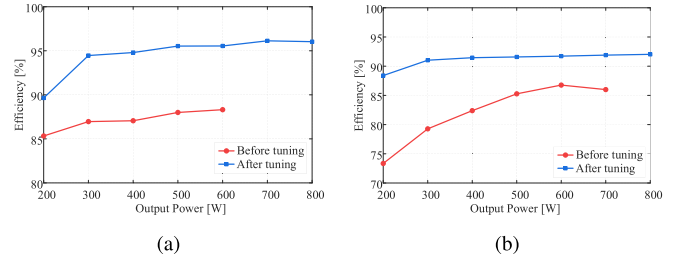


Fig. 28. Measured dc-to-dc efficiency of Cases A5 and B5 under different power points. (a) Case A5. (b) Case B5.

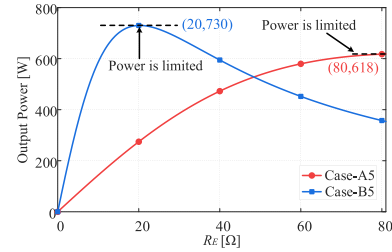


Fig. 29. Illustration of the limited output power due to the parameter deviations under Cases A5 and B5.

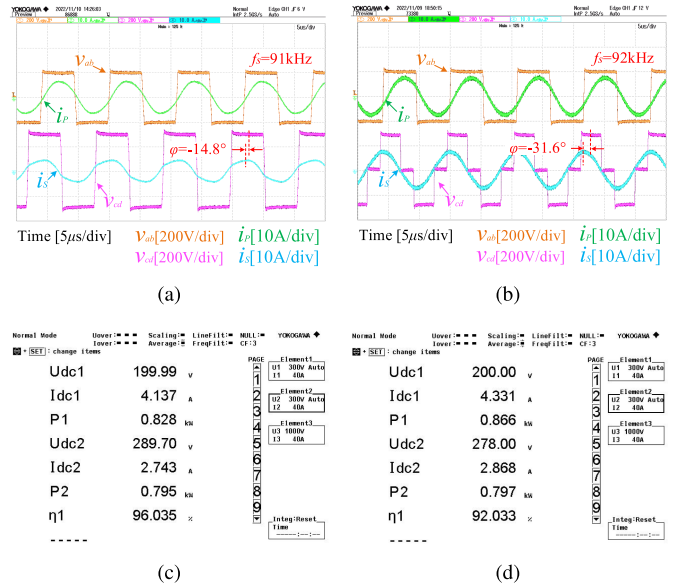


Fig. 30. Measured operating waveforms and DC-to-DC efficiency of Cases A5 and B5 when delivering 800-W power. (a) Operating waveforms after tuning in Case A5. (b) Operating waveforms after tuning in Case B5. (c) Measured DC-to-DC efficiency after tuning in Case A5. (d) Measured DC-to-DC efficiency after tuning in Case B5.

measured efficiency in the power range of 200–600 W before tuning in Case A5, and the measured efficiency in the power range of 200–700 W before tuning in Case B5. Nevertheless, by implementing the impedance tuning method, the system can reach the rated power (800 W) under both Cases A5 and B5, as shown in Fig. 30. As it can be observed, by regulating the system frequency and the phase shift angles of the active rectifier according to the recognized parameters, the system is able to

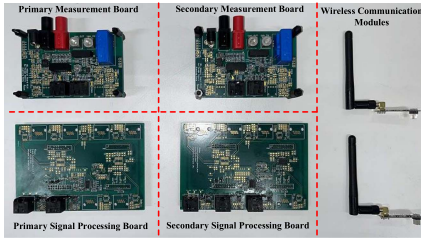


Fig. 31. Hardware modules for the close-loop experiments.

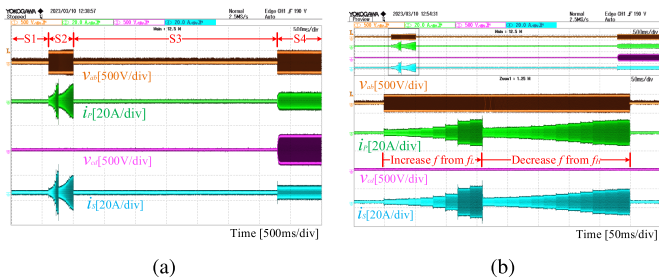


Fig. 32. Experimental results of the close-loop experiments under Case A5. (a) Complete implementation of the proposed method. (b) Enlarged view of the data acquisition stage.

reach 800-W output power, with the dc-to-dc efficiency at 96% under Case A5 and 92% under Case B5, respectively.

#### D. Close-Loop Verification

To further verify the feasibility of the proposed method in practice, the close-loop recognition and tuning process is implemented in the TMS320F28379D microcontrollers. Two measurement boards and two signal processing boards, as shown in Fig. 31, are utilized to measure the primary and secondary coil currents, respectively, where the measurement boards are connected to the resonant circuits and the signal processing boards are installed on top of the LaunchPads. Additionally, the NRF24L01+ modules shown in Fig. 31 are employed for the dual-side wireless communication. According to [36], the adopted module takes 339  $\mu$ s for a single-byte payload to complete a transmission and acknowledgment between the transmitter and the receiver. It is worth noting that the proposed method only requires the measurement of steady-state rms values of the coil currents, and the communication latency does not affect the accurate measurement of these values. Based on the aforementioned hardware modules, the close-loop experiments are carried out under Case A5, where the experimental results are demonstrated in Fig. 32.

As shown in Fig. 32(a), the complete implementation of the proposed method includes four different stages, where S1, S2, S3, and S4 represent the pre start-up stage, the data acquisition stage, the JAYA algorithm execution stage, and the normal charging stage, respectively. After the system starts, it first enters the data acquisition stage, where the rectifier output is short-circuited and the inverter frequency is adjusted based on the proposed dynamic frequency approaching strategy. During this stage, as shown in Fig. 32(b), the inverter frequency  $f$  is first increased from  $f_L$ , and then, it is decreased from  $f_H$  after the

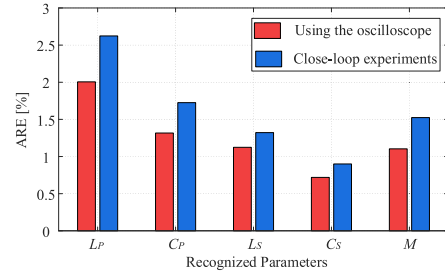


Fig. 33. Comparisons on the recognized results in the close-loop experiments and those using the oscilloscope.

coil currents exceed the threshold  $I_M$ . The data acquisition stage stops when the coil currents exceed the threshold again. In the experiments, 20 different frequency points are extracted with the time for each frequency point configured at 20 ms, and therefore, the total time for the whole data acquisition stage is 400 ms. After the data acquisition, the JAYA algorithm is implemented to solve the unknown parameters, which takes around 3.2 s in the experiments. In the close-loop tests, the maximum ARE of the recognized results for Case A5 is 2.6%, which is slightly larger than that of using the oscilloscope. The recognition results in the closed-loop experiments are compared with those using the oscilloscope in Fig. 33. The discrepancy in estimated results is attributed to the difference in measurement errors. In the close-loop experiments, the current transducer (LAH 50-P) is adopted to measure the coil currents, with the frequency bandwidth at 200 kHz, and the sampling rate of the DSP is configured at 1 MHz. Compared with the 50-MHz bandwidth of the current probe (KEYSIGHT N2782B) and the 12.5-GHz sampling rate of the oscilloscope, the measurement errors in the close-loop experiments are increased due to the limited bandwidth of the adopted measurement system. Consequently, the recognition errors in the close-loop experiments are slightly larger than that of using the oscilloscope. In practice, the current sensor with high bandwidth and the analog-to-digital converter with high sampling rate can be employed to further minimize the measurement errors, thereby achieving a higher recognition accuracy. Finally, based on the recognized parameters, the system frequency as well as the phase shift angles of the rectifier are regulated to realize the impedance tuning, and the system enters the normal charging stage.

#### E. Comparison With Other Works

To illustrate the difference between the proposed method and other existing impedance tuning methods, detailed comparisons are summarized in Table IV.

Compared with other reported methods, the main contribution of the proposed method is all parameters of the resonant circuits are recognized simultaneously, without using extra phase detection circuits and auxiliary coils. Based on these identified parameters, the proposed method is able to simultaneously deal with a wide range of parameter deviations caused by capacitance drift and coil misalignment on both sides. In this article, the primary-side reactance is tuned by regulating the inverter frequency, while the secondary-side reactance is tuned by the



TABLE V  
COMPARISONS WITH OTHER WORKS ON PARAMETER RECOGNITION

Ref.	Recognized parameters	Data Acquisition & Algorithm	Max. Error	Time
[27]	Multiple loads	Traditional frequency sweeping and LSA	/ <sup>1</sup>	/
[32]	$M, R_E$	Traditional frequency sweeping and LSA	/	/
[26]	$M, R_E, C_S, L_S$	Traditional frequency sweeping and ADE	< 3 %	17.95 s
[22]	$C_S, L_S$	Pulse density modulation and LSA	< 5 %	2 ~ 5 s
[37]	$M, R_E$	Harmonic detection and calculation	6.9 %	7 ms
This article	$M, L_P, L_S, C_P, C_S$	Dynamic frequency approaching and JAYA	< 3 %	≈ 3.6 s

<sup>1</sup> The symbol “/” indicates the relevant details are not provided in the reference.

active rectifier. Compared with those methods using SCCs, the proposed method avoids the extra power losses caused by SCCs. Since all parameters of the resonant circuits are considered, the proposed method requires the secondary-side information to accurately identify  $L_S$ ,  $C_S$ , and  $M$ . Therefore, the wireless communication is needed in this article.

Moreover, the proposed method is compared with other existing parameter monitoring methods in Table V. For multi-parameter estimation, it is of great importance to measure the coil currents at various frequency points. The existing methods mainly acquire this information from two distinct perspectives: frequency sweeping [26], [27], [32] and harmonic detection [22], [35]. However, for the harmonic-detection-based methods, the number of parameters that these methods can accurately estimate is restricted by the limited harmonic frequency points. On the other hand, the traditional frequency-sweeping-based methods are susceptible to severe system detuning and load power ripple under wide-range parameter deviations. To this end, a dynamic frequency approaching strategy is proposed in this article, with the rectifier output short-circuited during the parameter recognition process. This approach avoids significant load power ripple, and is able to efficiently and safely measure the coil currents under a sufficient number of frequency points. As shown in Table V, the maximum estimation error of the proposed method is comparable to other existing works. Additionally, the estimation time of the proposed method is around 3.6 s, which is also fast enough for the stationary charging applications.

## V. CONCLUSION

In this article, a parameter recognition-based impedance tuning method is proposed for the SS-compensated WPT systems. The proposed parameter recognition method is implemented at pre start-up, with the rectifier output short-circuited during this process. Therefore, the proposed method is more suitable for stationary applications, whereas it is not desirable to be used in the dynamic wireless charging cases. Notably, as the proposed method is load-independent and the total time for the entire process is only several seconds, it can also be repeated during

the charging process to deal with some abnormal behaviors, for instance, a sudden movement of the receiver coil or significant variation in operating temperature. Compared with the existing methods, the proposed parameter recognition method avoids severe system detuning and significant load power ripple, and is able to accurately identify all of the unknown parameters of the resonant circuits. The accuracy of the parameter recognition is experimentally validated in ten cases of parameter deviations, with the relative average errors of the recognized results all less than 3%. Thanks to the pre start-up parameter recognition, the parameter deviations caused by coil misalignment and capacitance drift on both the primary and secondary sides can be addressed without adding any extra switches and circuits, which is the main contribution of this proposal. Based on the recognized parameters, an impedance tuning method is carried out to cope with the impedance mismatch caused by parameter deviations. By regulating the system frequency and the phase shift angles of the active rectifier, the reactance on both sides are minimized, and therefore, the dc-to-dc efficiency of the WPT prototype is enhanced by 4.3–15% in the experiments. Close-loop verification is also implemented to further verify the feasibility of the proposed method in practice, with the time consumption for the whole parameter recognition process at around 3.6 s in the experiments.

It is worth mentioning that this article only presents the application in the typical and widely used SS compensation network. However, in recent years, hybrid compensation structures, such as LCC-S, LCC-LCC, etc., are gaining more and more attention. For these hybrid networks, since the number of passive elements is much greater than that of the SS compensation, the implementation of parameter identification is more difficult, and additional information is required to be measured. Considering the increasing popularity of these hybrid structures, the research on how to further extend the proposed method to the hybrid compensation will be regarded as our future work. Another noteworthy point is that, in addition to its application for active impedance tuning, the proposed parameter recognition strategy also shows promise in optimal power flow control and foreign object detection. These potential applications will also be considered as part of our future work.

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