

A Phenomenological and Numerical Model for Scaling the Flow Aggressiveness in Cavitation Erosion

R. Fortes - Patella (*LEGI – INPG*)

JL. Reboud (*LEMD – UJF*)

L. Briançon - Marjollet (*DGA-BEC*)

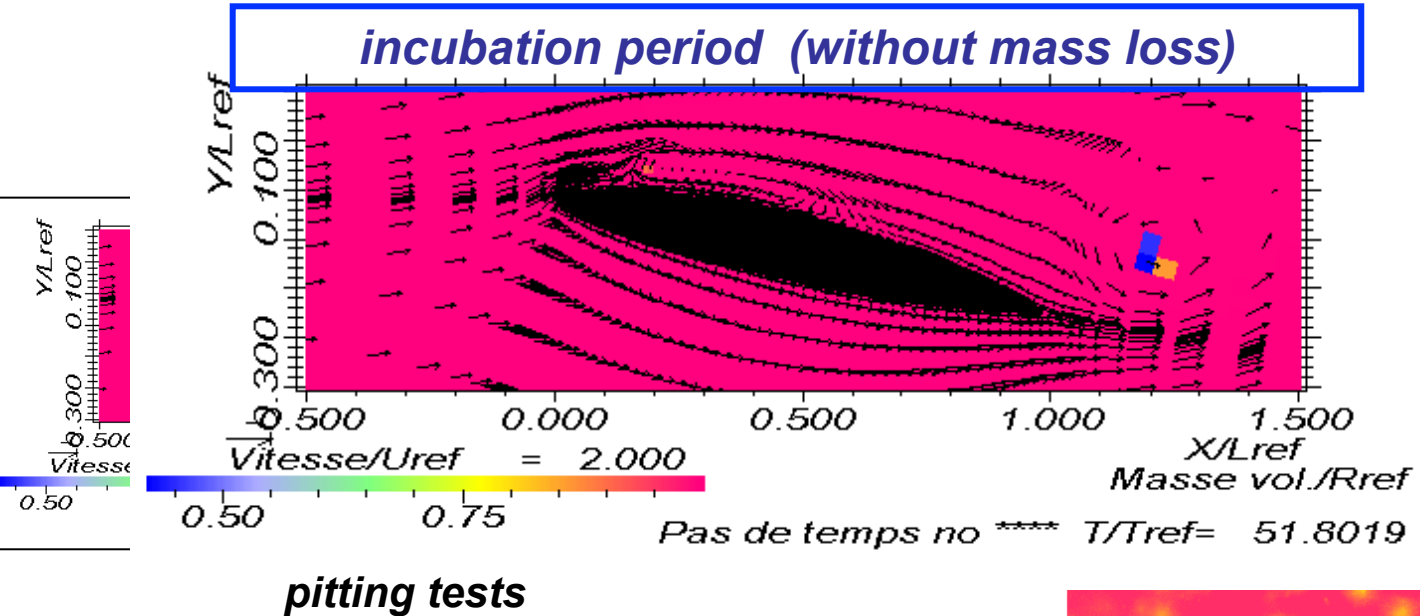
France



I. Targets

- evaluation of cavitation aggressiveness
- characterization
- prediction model

experimental and numerical studies



II.a - Physical Scenario

Mechanism : Pressure Wave

[Fujikawa and Akamatsu, 80 ; Tomita and Shima, 89]

[Avellan and Farhat, 89 ; Fortes-Patella, 94]

⇒ amplitude ~ 1GPa

⇒ celerity: 1500 m/s – 2000 m/s

⇒ duration: 10 ns up to 1 μ s

⇒ indentation size: R ~ 100 μ m ; h ~ 1 to 10 μ m

⇒ collapses of vapour structures:

spherical bubbles

vortex

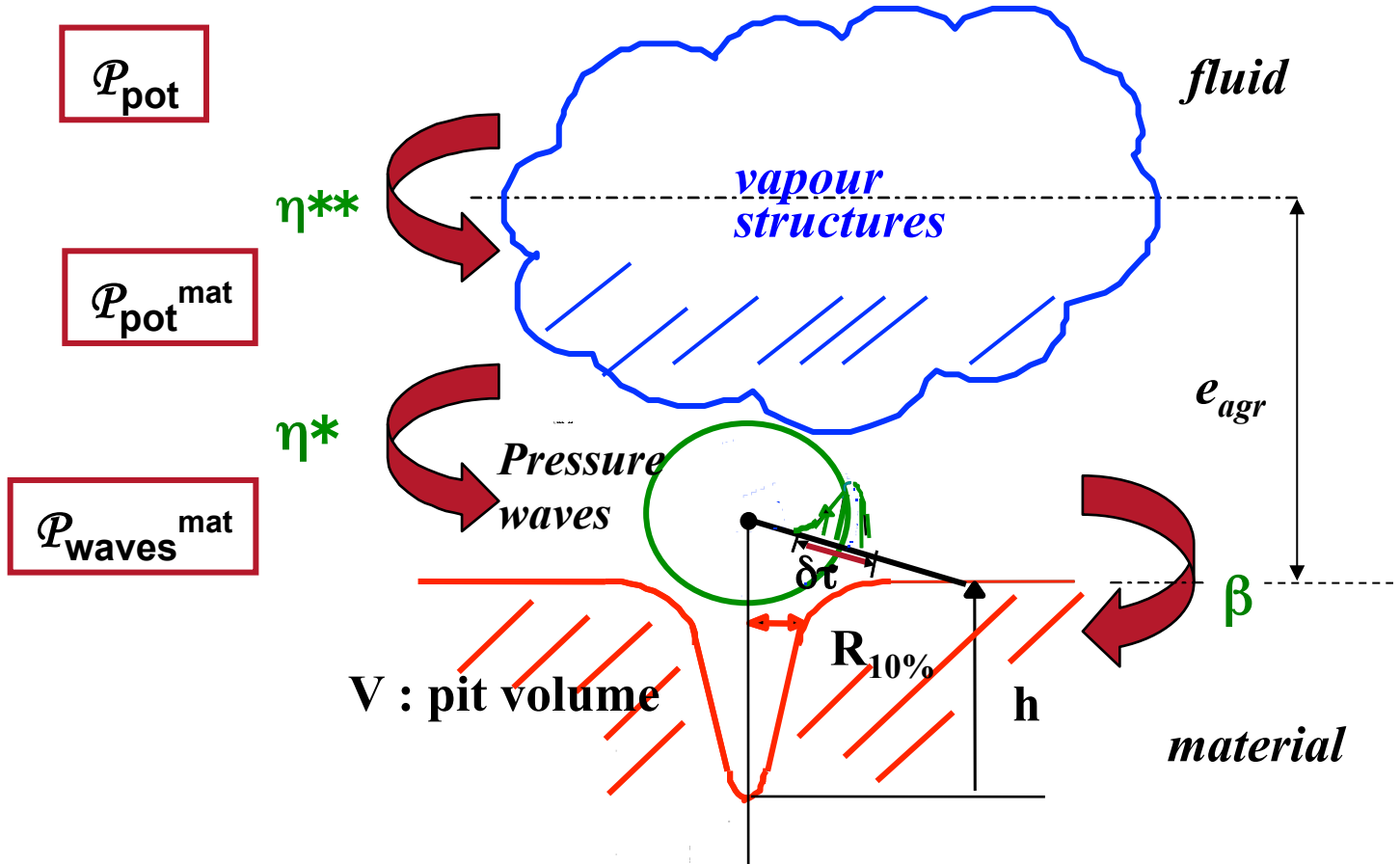
microjet

} *[Vogel et al., 89 ;
Ward et al., 90]*

[Phillip et al., 95]

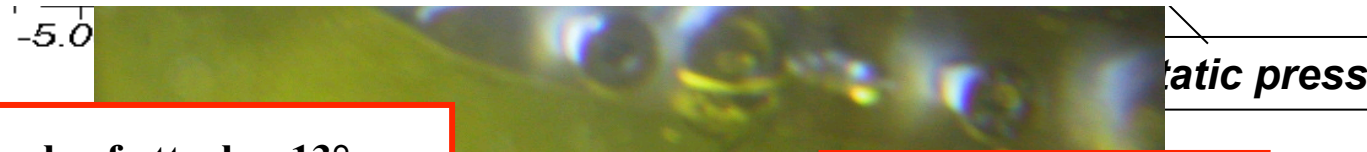
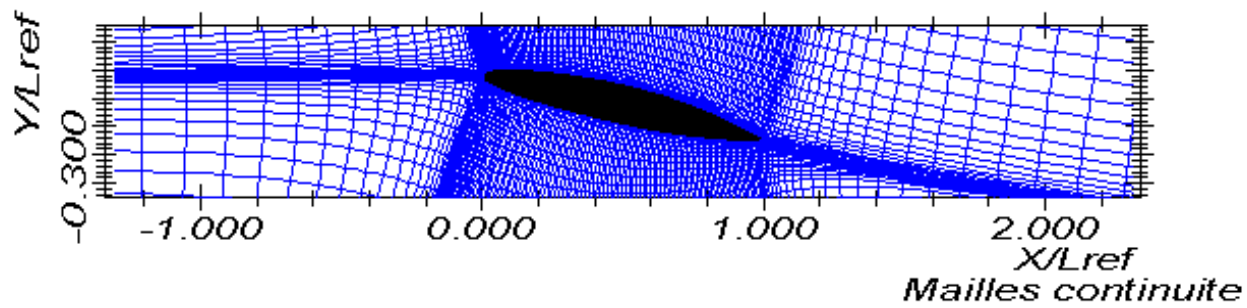
II.b – Physical Scenario

Energy Balance



III.a - Flow Aggressiveness

- numerical calculation of unsteady cavitating flows : « IZ »
(developed with the support of the French Space Agency CNES)
- 2D approach : hydrofoil geometry



Angle of attack = 13°
 $U_{ref} = 9.4 \text{ m/s}$ $T_{ref} = 16 \text{ ms}$
 $\sigma_{upstream} = 1.85$

$L_{ref} = 150 \text{ mm}$

of the wall
experimental study (BEC – DGA)

III.b – Physical Modelling: Barotropic Approach

RANS equations :

mass :

$$\partial\rho/\partial t + \text{div } \rho\mathbf{U} = 0$$

momentum :

$$\rho d\mathbf{U}/dt = -\nabla P + \nabla\tau$$

- Finite volume method :

**curvilinear orthogonal staggered
meshes**

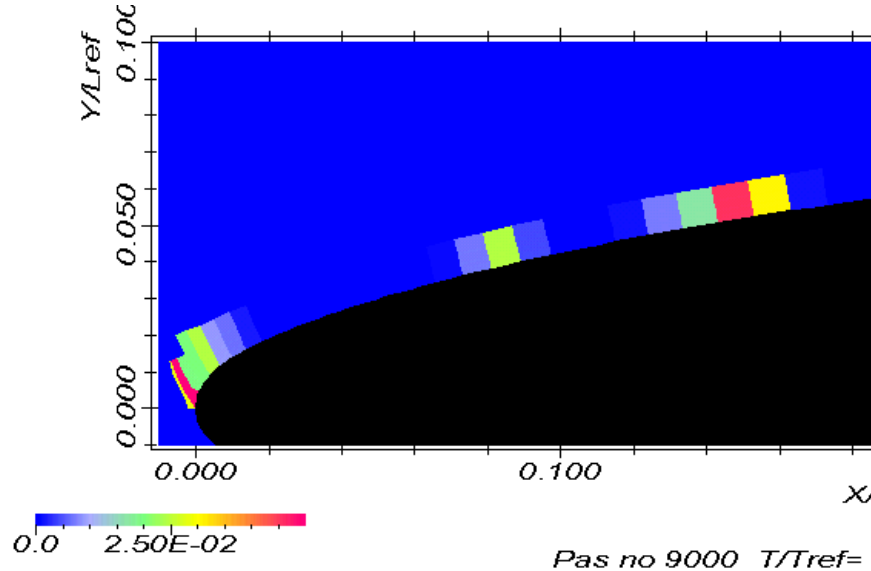
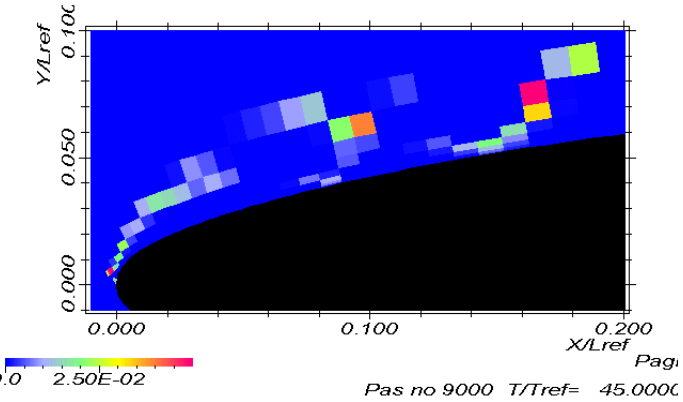
- **implicit method** :

SIMPLE algorithm

Turbulence model : modified k- ϵ

(C_μ reduced when $0 < \alpha < 1$)

III.c - Flow Aggressiveness Potential Power $\mathcal{P}_{\text{pot}}^{\text{mat}}$



initial study:

large mesh, few events (statistic representation)

results:

- more aggressive zone at the cavity closure

- $\mathcal{P}_{\text{pot}}^{\text{mat}}/\Delta S \propto V^3$

- non relevant influence of σ (erosion zone displacement)

IV.a – Pressure Wave Power $\mathcal{P}_{\text{waves}}^{\text{mat}}$

[Challier et al., 2000 ; Fortes-Patella et al., 1999]

Bubble dynamics: Keller's Model [Prosperetti and Lezzi, 86]

- fluid compressibility

- viscous effects

- surface tension

- adiabatic non-condensable gas

- thermal effects are not taken into account

Pressure Wave:

- Tait equation [Cole, 48]

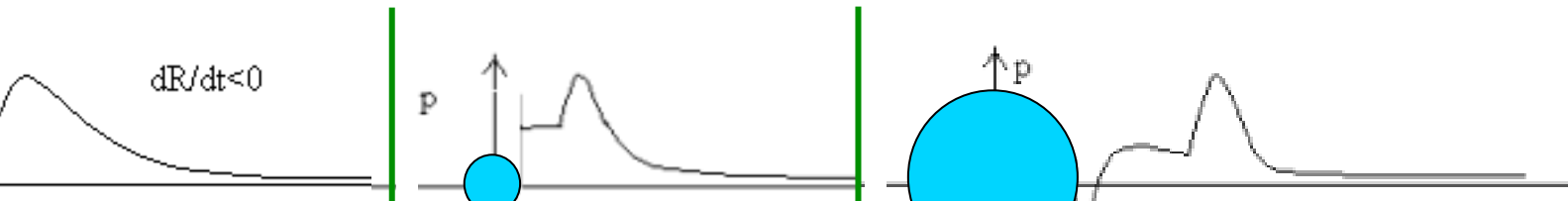
- 1st velocity potential approximation [Fujikawa and Akamatsu, 80]



simulation code: P_{∞} , P_{g0} , R_0



$P(r,t)$, δt , $R(t)$, E_{wave}



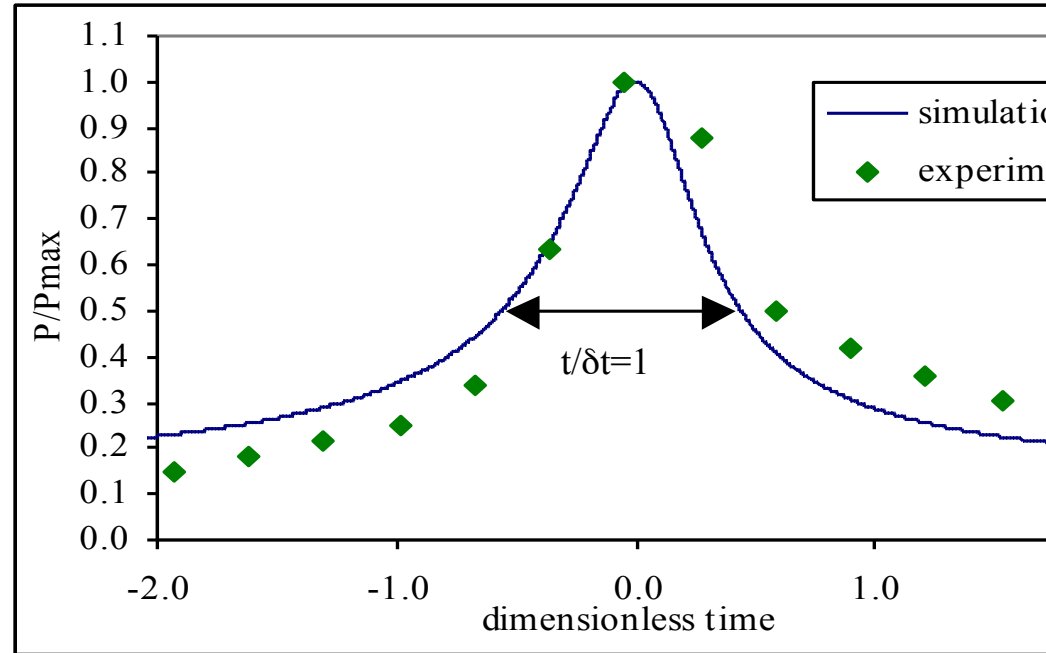
IV.b – Pressure Wave Simulation

1 Dimensional Pressure Signal

Acoustic Energy Approach:

$$\approx \frac{45\pi P_{\max}^2 r^2}{\rho C_{\infty}} \delta t$$

$$P \sim 1/r$$



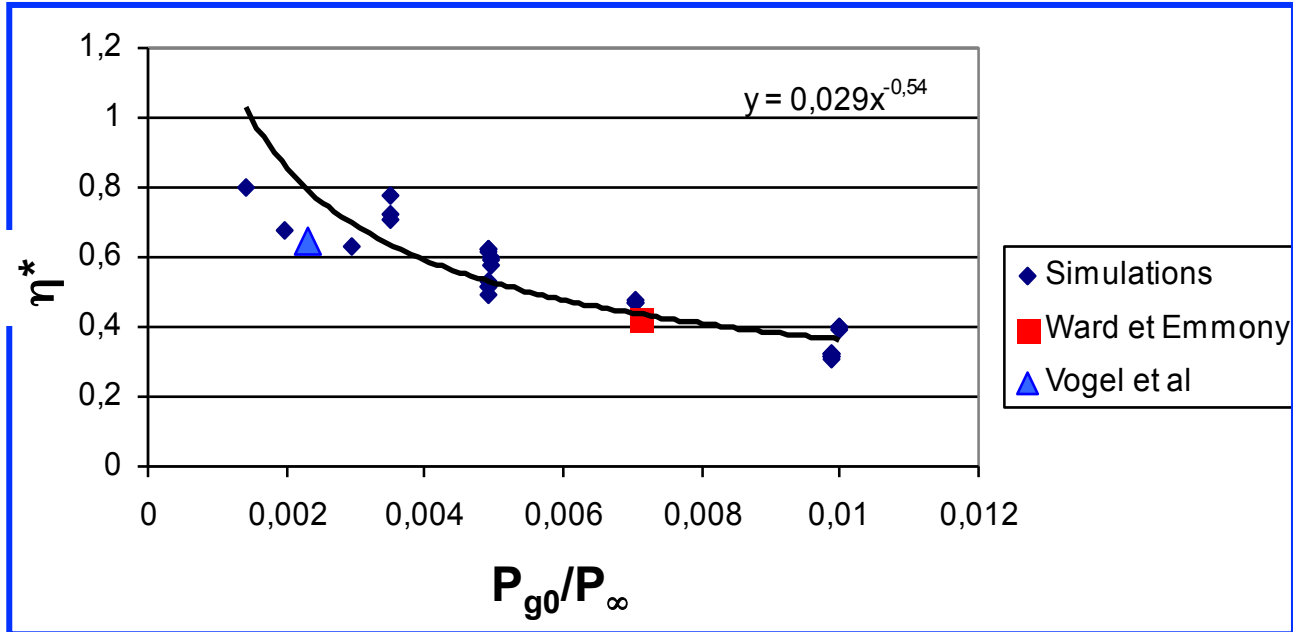
Time distribution of the pressure signal at a given radius "r".

δt : wave passage time.

[Isselin et al., 1998] : pressure signal measured by a PVDF

IV.c – Collapse Efficiency η^*

$$\eta^* = \frac{E_{\text{wave}}}{E_{\text{pot}}} = \frac{P_{\text{waves}}^{\text{mat}}}{P_{\text{pot}}^{\text{mat}}}$$



$P_{g0} \propto$ air contents [Kato et al., 1996]

“Solid” Code [Reboud, 1987]

Pressure waves
Implicit, 2D Cylindrical Axisymmetric
Numerical Code

Continuum Mechanics

elastoplastic Constitutive Equation

$E, \nu, S_0, C_L(E, \rho)$
(strain hardening)

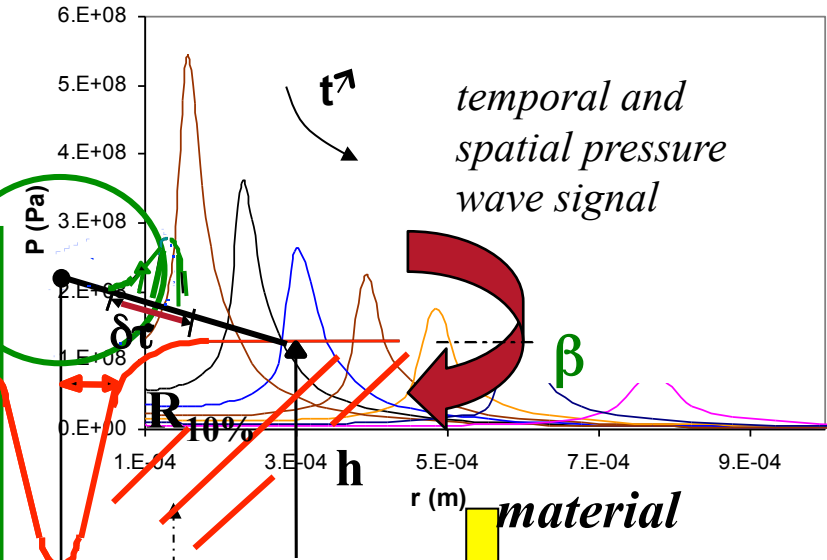
Finite-Elements Method

Incubation period

(no fracture, no mass loss)

Pressure wave

V : pit volume



temporal and spatial pressure wave signal

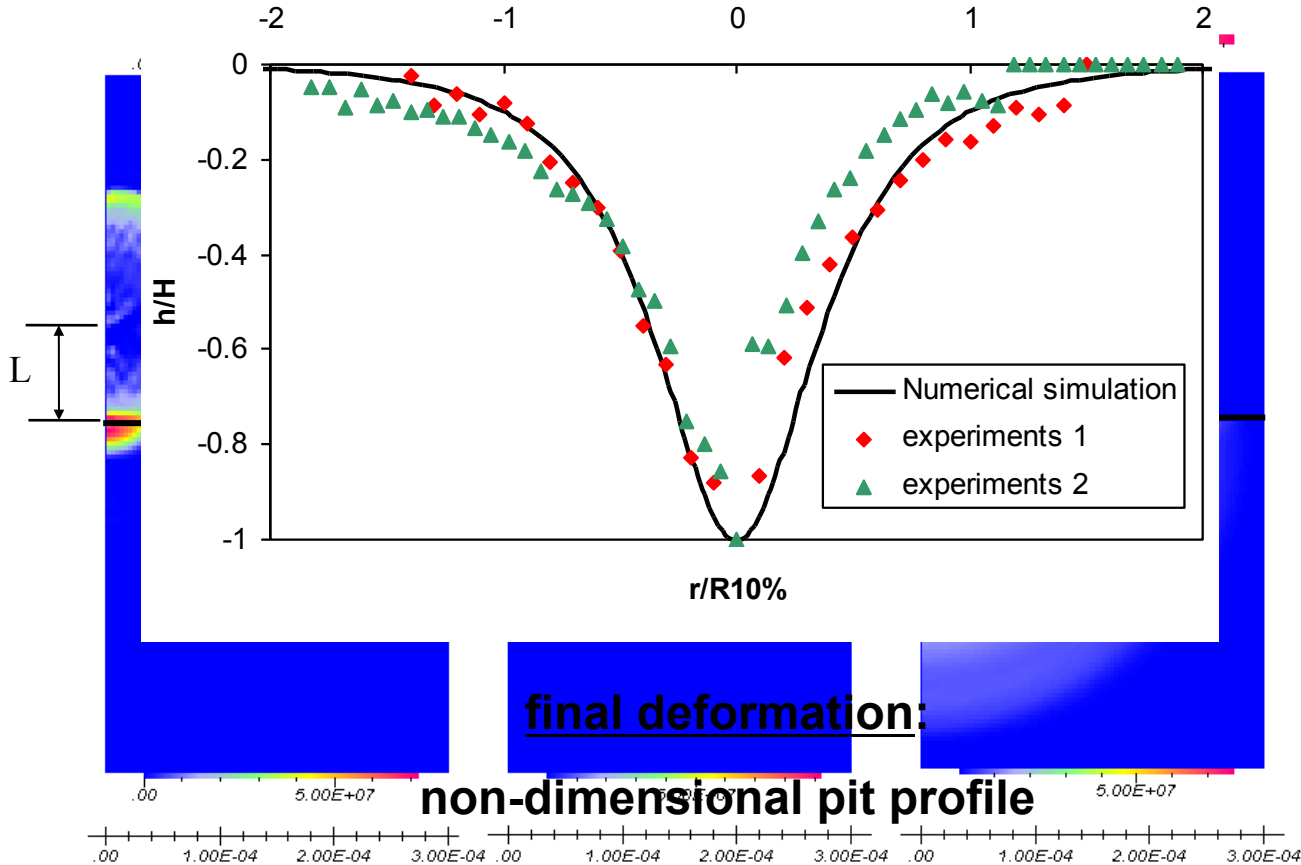
material

wetted material surface

Solid domain



Pressure wave characteristics : $P \sim 0.6$ GPa ; $dt \sim 30$ ns ; $L \sim 0.1$ m



Pressure f
in the water

Clig ~ 1500

final deformation:

non-dimensional pit profile

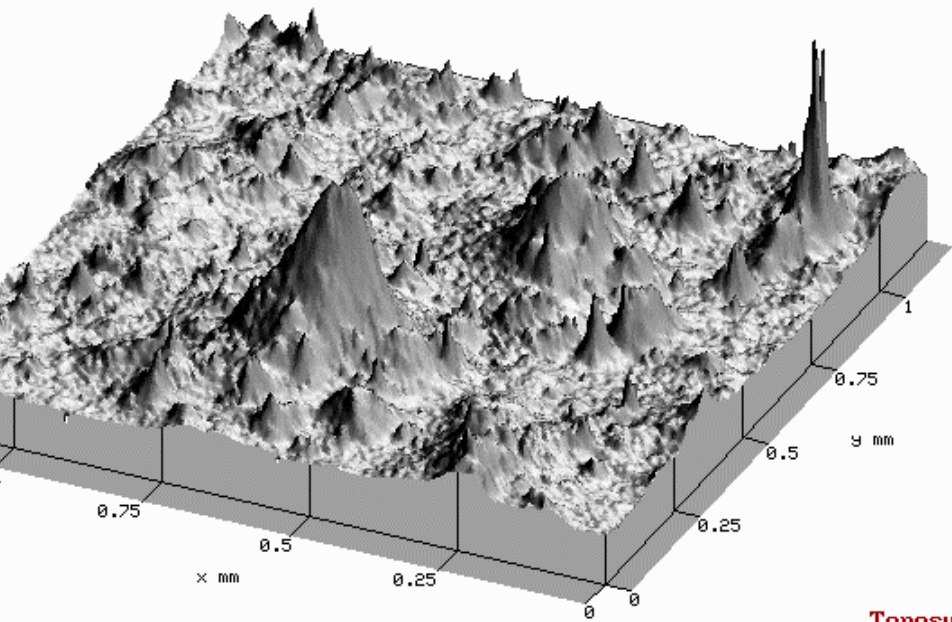
3D profilometer (EDF)

transient stress field in the material

V · B · H



VIC – Fluid-Material Interaction



Toposurf

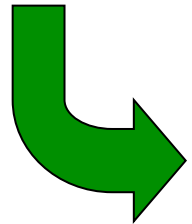
$$\beta_{\text{aluminum}} \sim 4 (\pm 0.4) \text{ J/mm}^3$$

$$\beta_{\text{copper}} \sim 20 (\pm 3) \text{ J/mm}^3$$

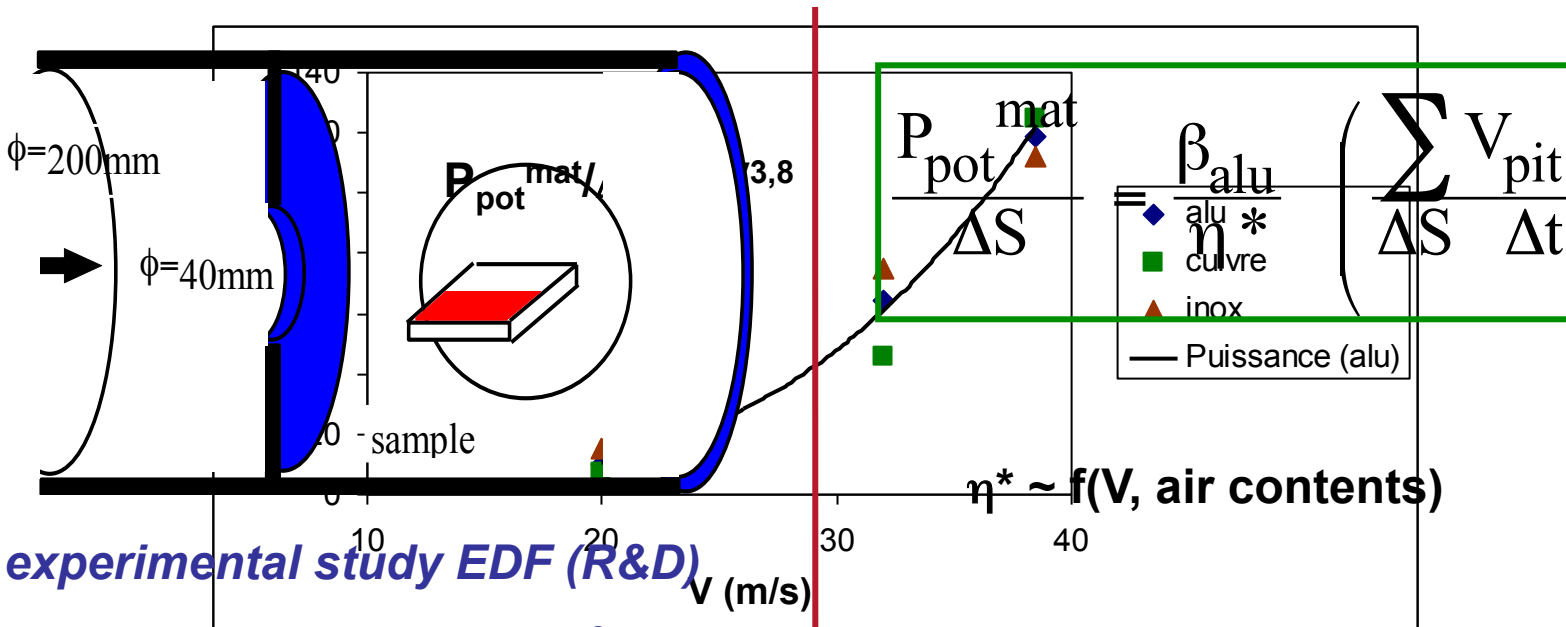
$$\beta_{\text{SS}} \sim 30 (\pm 2) \text{ J/mm}^3$$

$$E_{\text{wave}} = \beta_{\text{material}} V_p$$

Local point of view



$\frac{P_{\text{pot}}^{\text{mat}}}{\Delta S} = \frac{P_{\text{waves}}}{\Delta S \eta}$	$\frac{S_0^{\text{mat}}}{E} = \frac{\beta_{\text{material}}}{\eta E}$	Alu	Copper	S. S.
	$\frac{S_0^{\text{mat}}}{E} = \frac{\beta_{\text{material}}}{\eta E}$	100	$\sum 2V_{\text{pit}}$	200-380
	$\frac{S_0^{\text{mat}}}{E} = \frac{\beta_{\text{material}}}{\eta E}$	$\eta \cdot 50$	$\frac{\sum 2V_{\text{pit}}}{\Delta S_{120} \Delta t}$	strain hardening
	$\frac{S_0^{\text{mat}}}{E} = \frac{\beta_{\text{material}}}{\eta E}$	$\eta \cdot 50$		200
	$\frac{S_0^{\text{mat}}}{E} = \frac{\beta_{\text{material}}}{\eta E}$	$\eta \cdot 50$		200
	C_L (m/s)	5000	4700	5800
	ν	0.3	0.33	0.3



$\sigma = 0.7 ; \Delta S = 100 \text{ mm}^2$

For a given cavitating flow

- $P_{pot}^{mat} / \Delta S \Rightarrow$ flow aggressiveness
- samples: aluminum
- $P_{pot}^{mat} / \Delta S \propto V^3$ (numerical simulation)
- copper
- influence of flow velocity, geometric scale [Lecoffre, 95], and material
- SS 316L

V
 η^*
 P_{pot}^{mat} } cons

Reference test:
 $20 \text{ m/s} \leq V \leq 38.5 \text{ m/s}$



Damage:

Improvements:

- spherical bubbles collapses: simple model
- modelling of the influence of air contents
- evaluation of the vapour structures distance to the wall (e_{agr})
-

Originality:

- proposition and exploitation of a complete physical scenario:
cavitating flow \Rightarrow material
- energetical approach: experimental and numerical study
- numerical simulation of the pressure wave/material interaction
- test methodology (EDF), analysis and treatment procedure [Choffat et al.]



Complete prediction model based on simulations

Application to different geometries and materials

Tool for design, maintenance and monitoring

modelling:

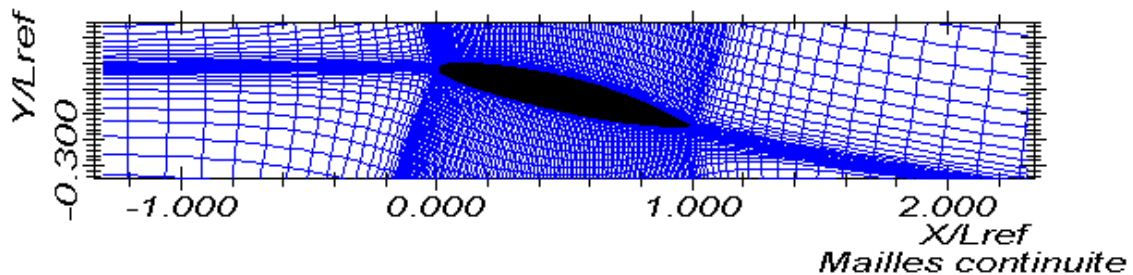
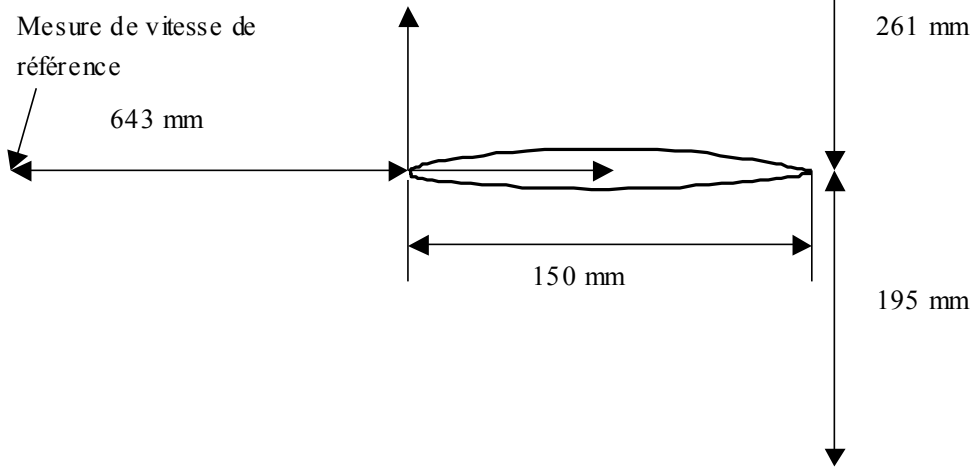
development of mass loss model

validation and improvement of proposed physical models

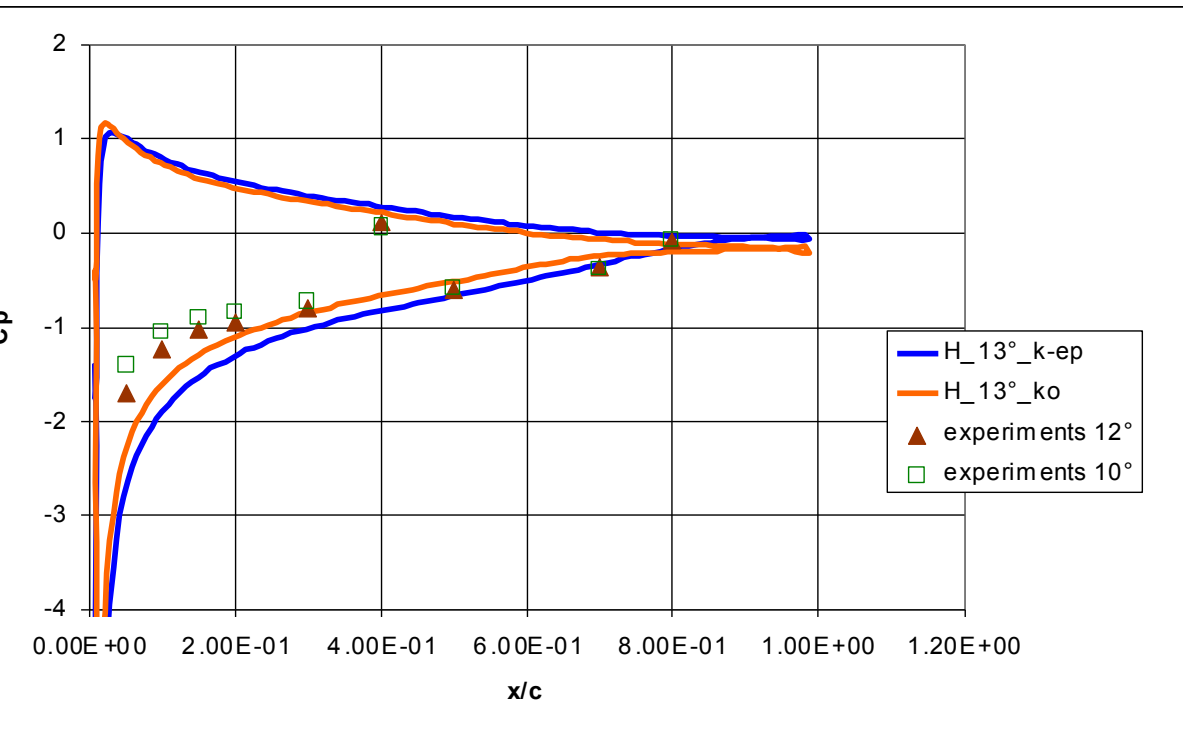
application : ship propellers, Diesel injectors, pumps

development of a 3D simulation code

metallurgical and dynamic characterization of materials (LTC 5M)

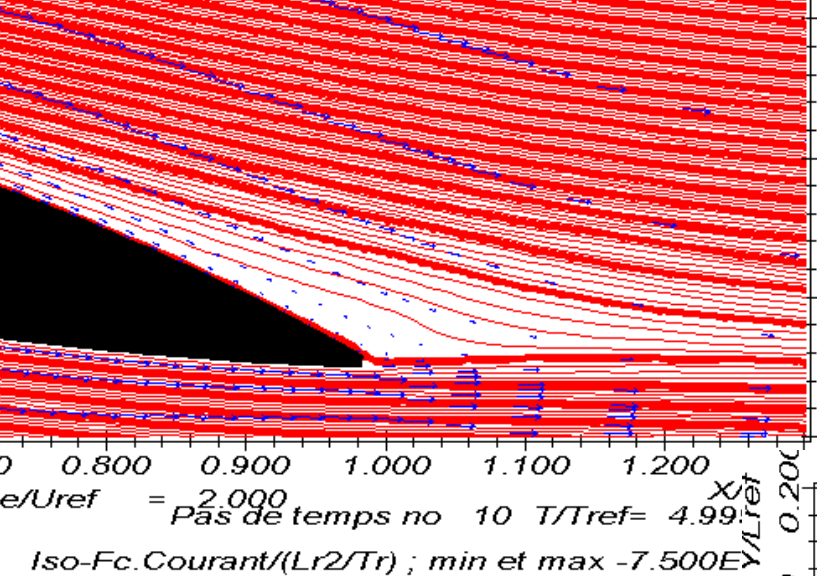


a) H Meshing: 180 x 73 nodes



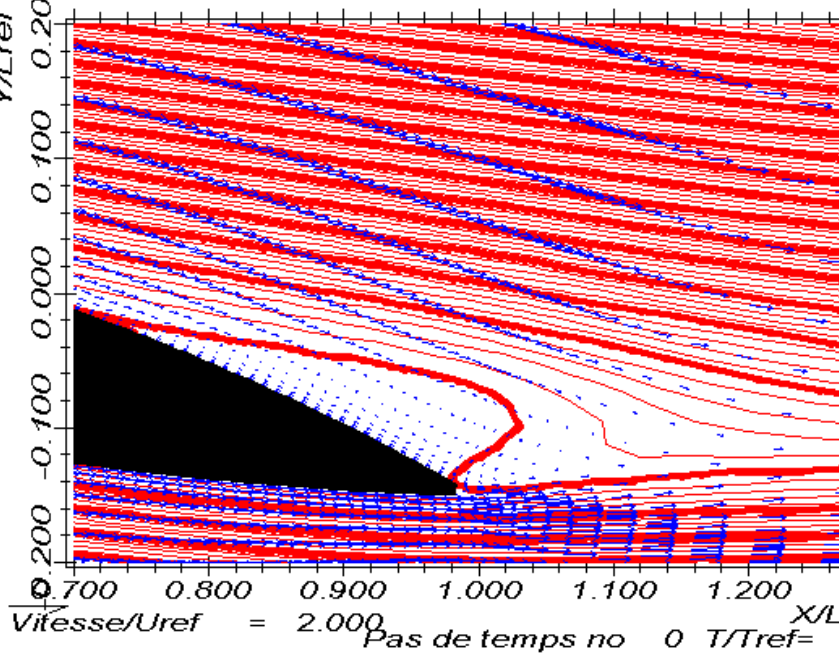
$$C_p = \frac{P - P_{down}}{\frac{1}{2}\rho U^2}$$

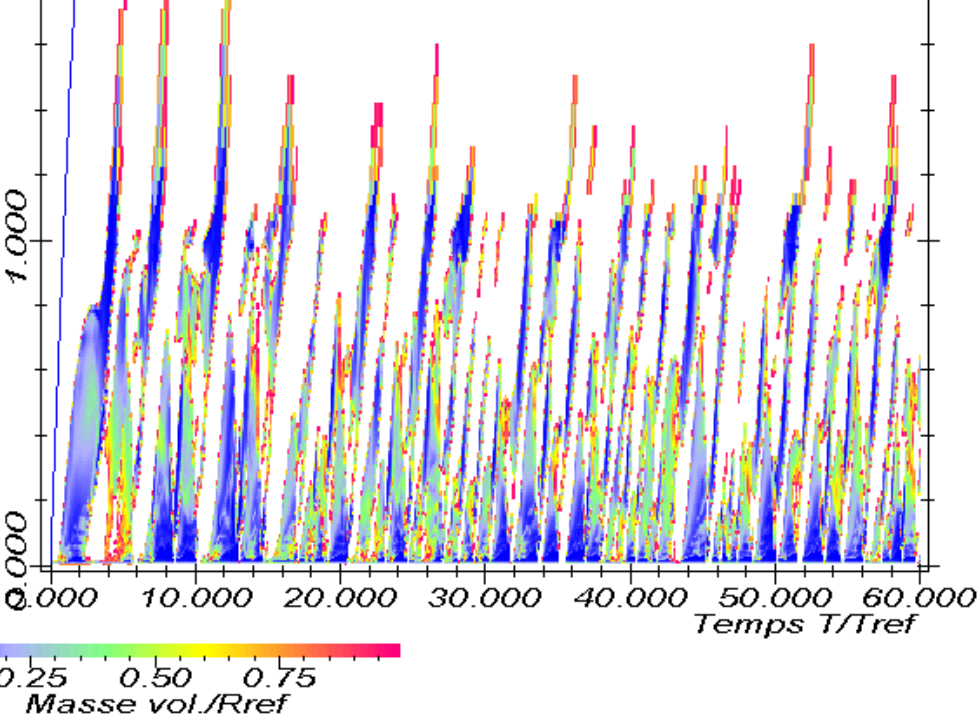
	13°_k-ε	13°_k-ω	12° exp	10° exp
lift	0.57	0.47	0.42	0.38
drag	0.054	0.07	0.059	0.054



→ Streamlines at the trailing edge

k- ω model



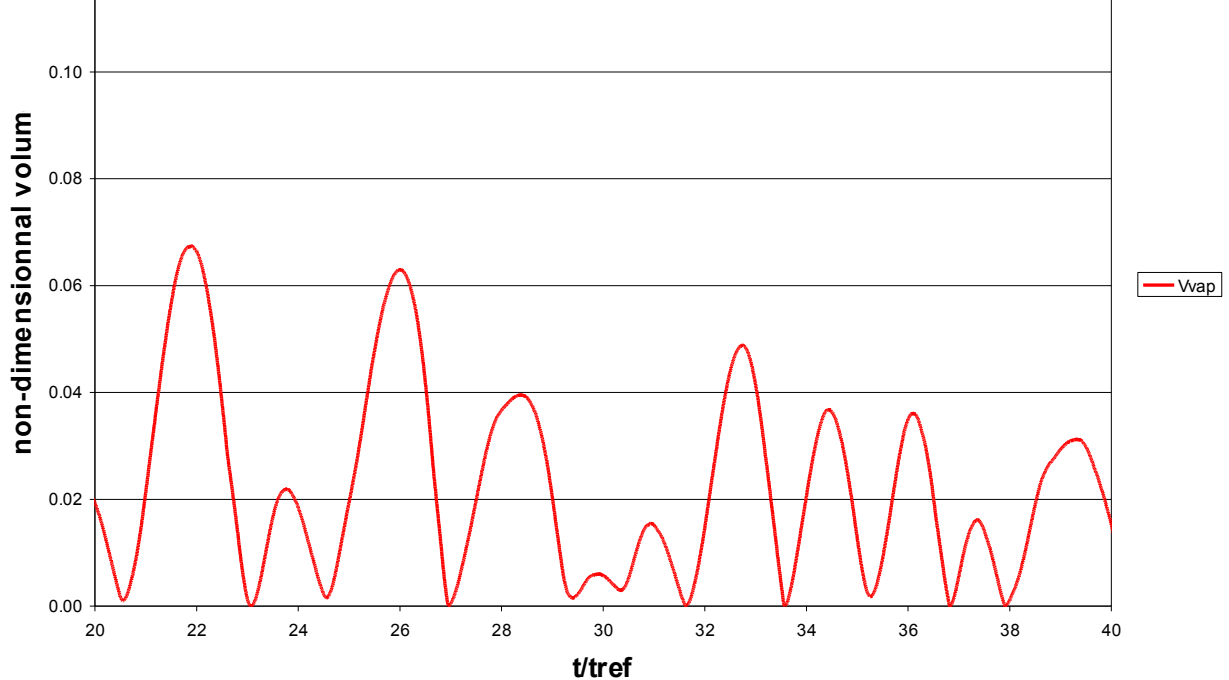


*Time evolution
of the cavity length.*

The time is reported in abscissa, and the X position in the tunnel of invitation is graduated in ordinate.

The colors represent the density values: white for the pure liquid one and from red to dark blue for the vapor one.

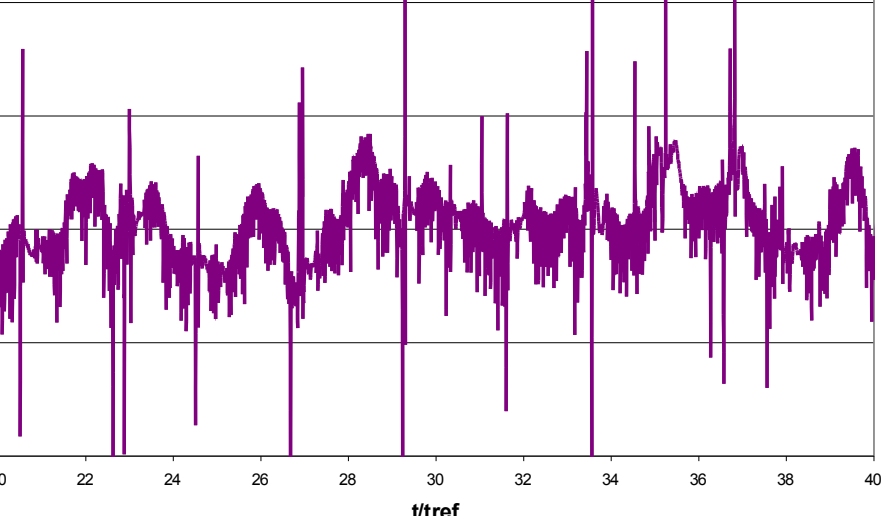
At a given point in time and position, the color indicates the minimum density in the corresponding cross section of the



Time evolution of the vapour volume

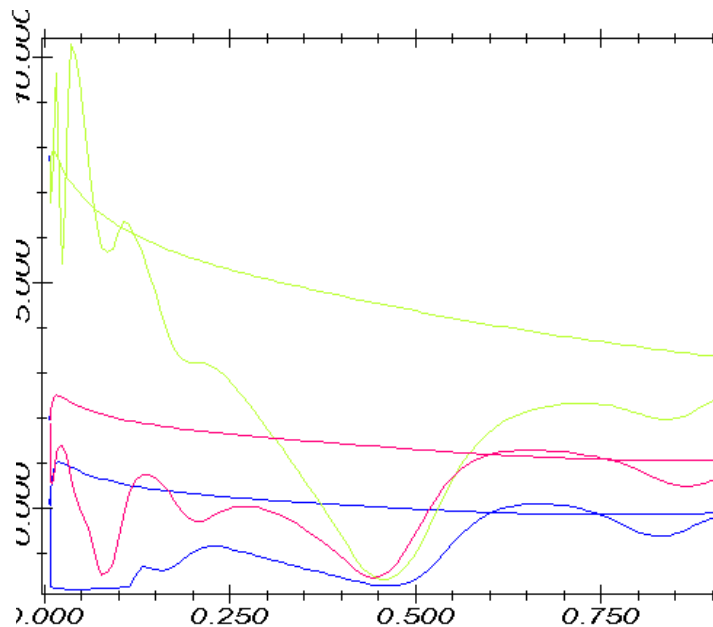
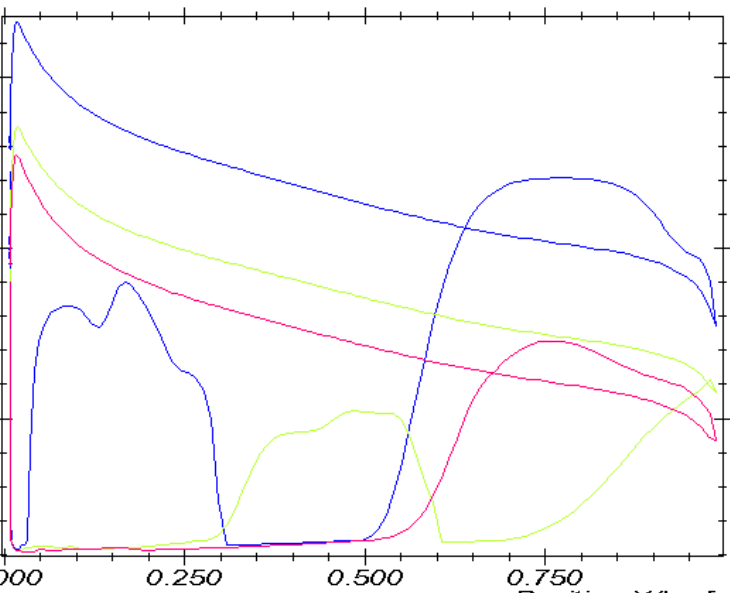
**$L_{cav} \sim 70$ mm
 $f \sim 30$ à 35 Hz**

Strouhal = $f \cdot L_{cav} / U_{ref} \sim 0.2$ to 0.25



⇒ **time evolution of the lift coefficient**

mean lift
coefficient =
0.47



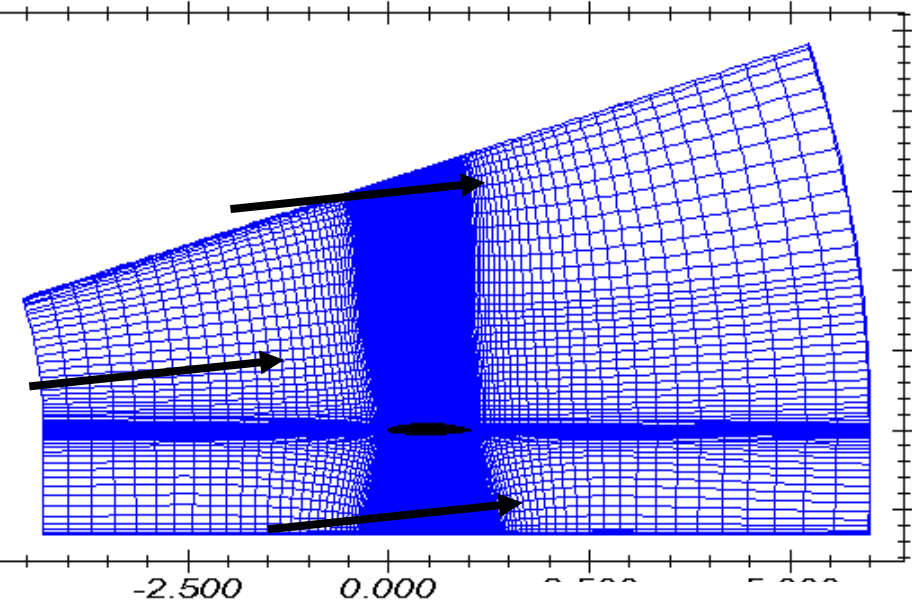
$$\sigma_{\text{upstream}} \sim 1.9$$

$$U_{\text{ref}} = 9.4 \text{ m/s} \quad T_{\text{ref}} = 16 \text{ ms}$$

turbulence model : $\kappa - \varepsilon$ RNG

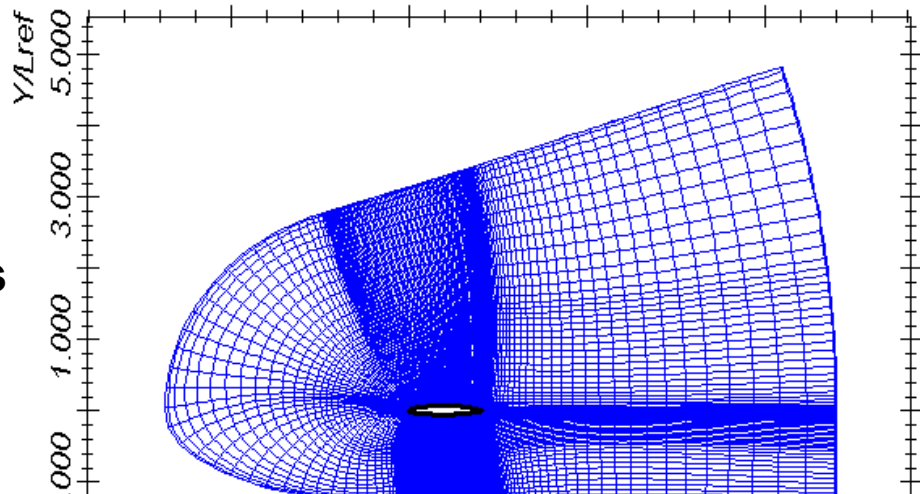
H meshing

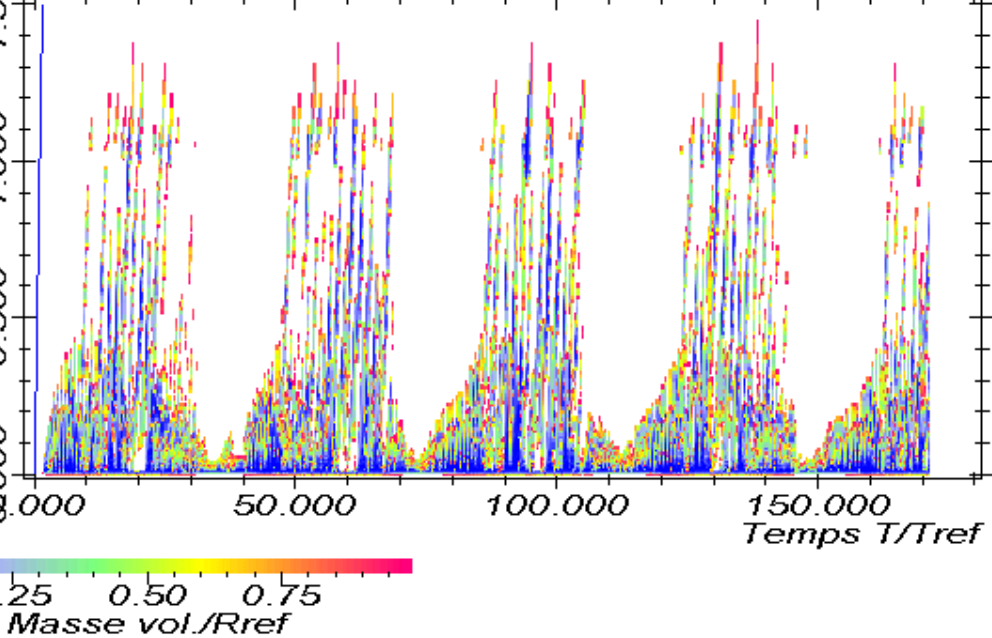
oscillating frequency: 0.6 s



a) H Meshing: 170 x 75 nodes

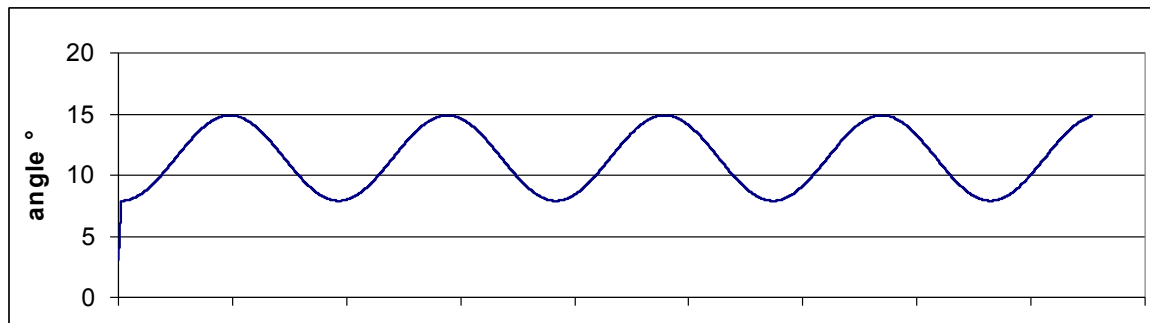
C Meshing: 270 x 44 nodes

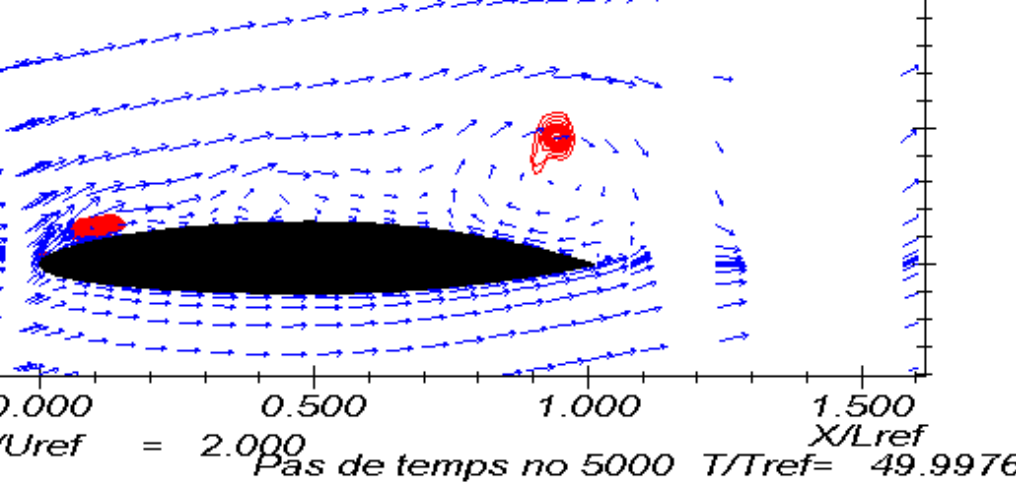




**⇒cavitating unsteady
behaviour**

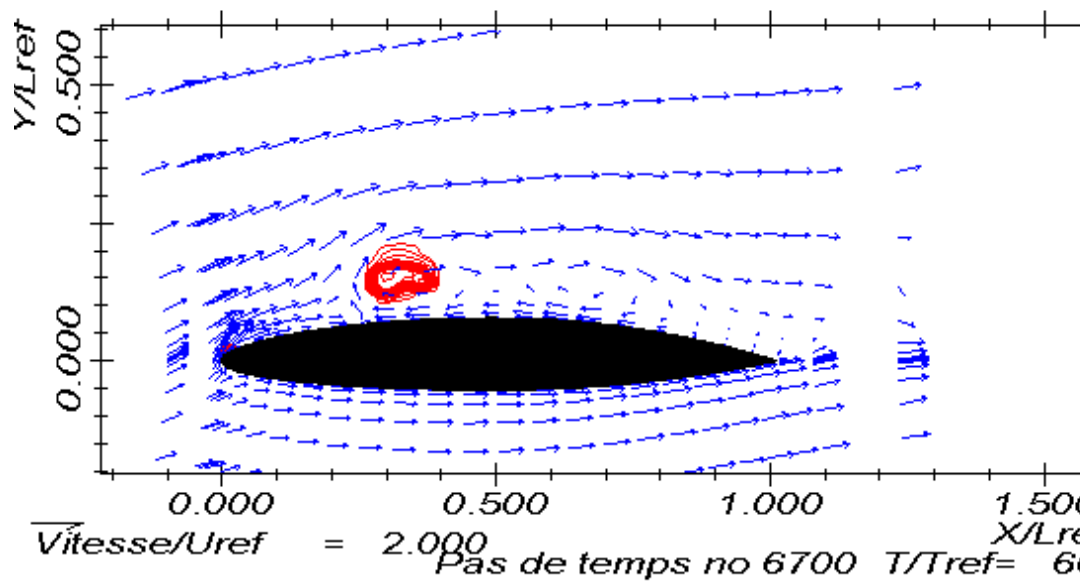
variation of the angle of attack



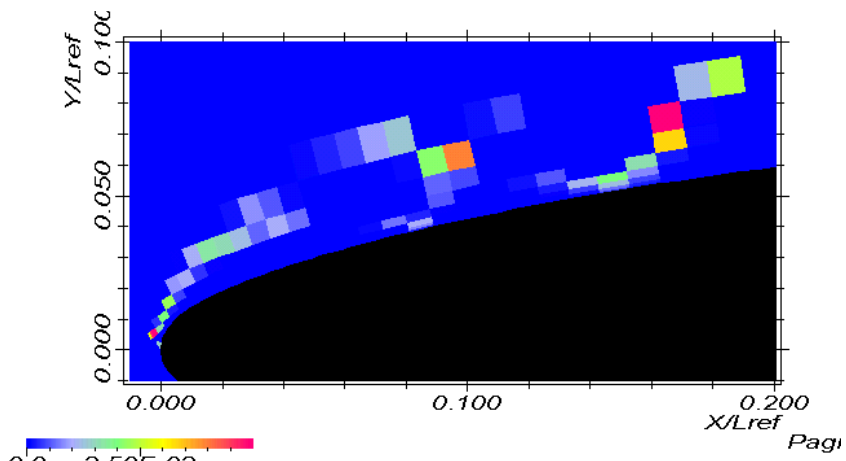
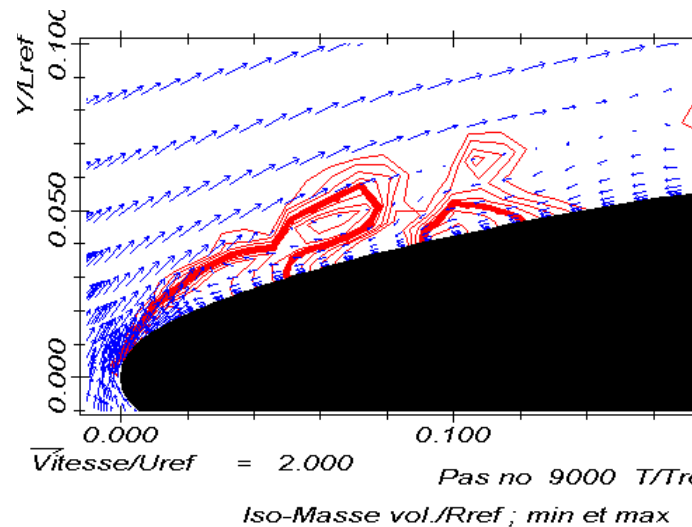
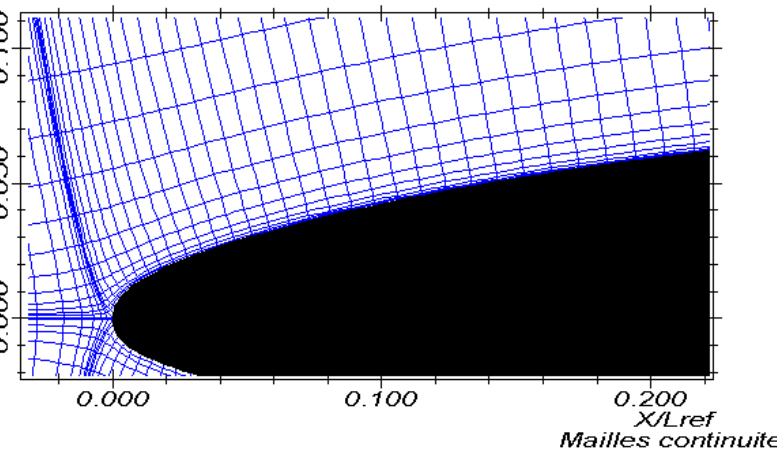


evolution of the
 cavitation structures
 between 40 and 50 T_{ref}
 weak angle of attack

evolution of the
 cavitation structures
 between 60 and 67 T_{ref}
 high angle of attack

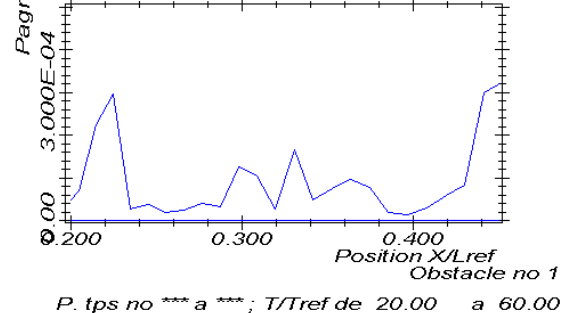


Flow Aggressiveness

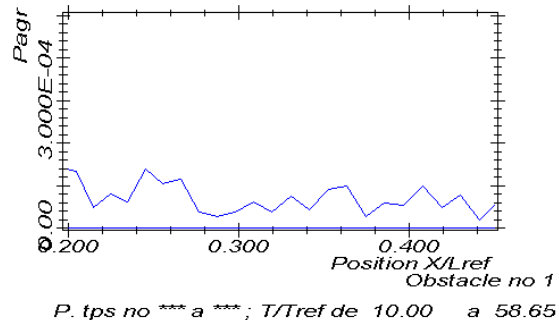


σ_{amont}	$e_{\text{agr}}/L_{\text{ref}}$
2.0	0.0011
1.9	0.0012
1.85	0.0014
1.75	0.00144

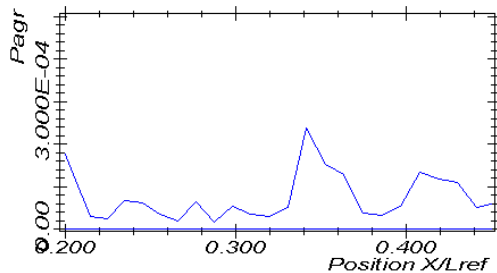
$\sigma_{\text{ot}}^{\text{mat}}/\Delta S \propto 0.5 \text{ à } 3 \cdot 10^{-4} (0.5 \rho V^3)$



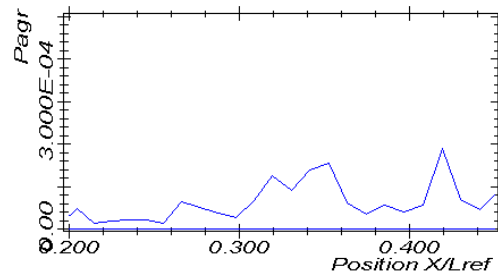
pth5m1.75_13°_v9.4_resm_amin021



pth5m1.8_13°_v9.4_resm_amin021



pth5m1.9_13°_v9.4_resm_amin021



hydrofoil in a channel , numerical simulation)

- $P_{pot}^{mat}/\Delta S \propto 2 \cdot 10^{-5} (0.5 \rho V^3)$

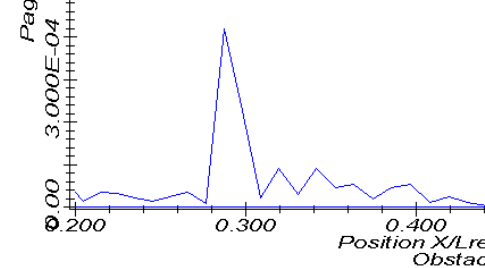
(hydrofoil « non-confined » , simulation)

- $P_{pot}^{mat}/\Delta S \propto 4 \cdot 10^{-4} (0.5 \rho V^3)$

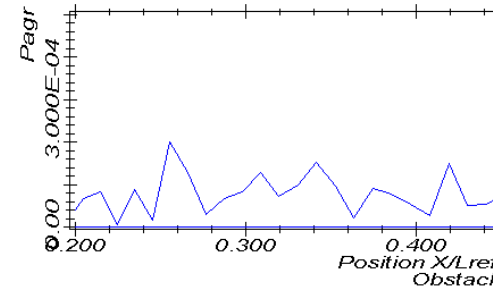
(hydrofoil with oscillating angle of attack)

- $P_{pot}^{mat}/\Delta S (MODULAB) \propto 3 \cdot 10^{-6} (0.5 \rho V^3)$

(MODULAB , experimental results)



P. tps no *** a ***; T/Tref de 20.00 a



P. tps no *** a ***; T/Tref de 20.00 a

hydrofoil in a channel : 13°

constant
variable

