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Modeling Thermodynamic Properties of Propane or Tetrahydrofuran Mixed with Carbon Dioxide or Methane in Structure-II Clathrate Hydrates

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Abstract

A sound knowledge of thermodynamic properties of sII hydrates is of great importance to understand the stability of sII gas hydrates in petroleum pipelines and in natural settings. Here, we report direct molecular dynamics (MD) simulations of the thermal expansion coefficient, the compressibility and the specific heat capacity of C₃H₈, or tetrahydrofuran (THF), in mixtures of CH₄ or CO₂, in sII hydrates under a wide, relevant range of pressure- and temperature conditions. The simulations were started with guest molecules positioned at the cage center of the hydrate. Annealing simulations were additionally performed for hydrates with THF. For the isobaric thermal expansion coefficient, an effective correction method was used to modify the lattice parameters, and the corrected lattice parameters were subsequently used to obtain thermal expansion coefficients in good agreement with experimental measurements. The simulations indicated that the isothermal expansion coefficient and the specific heat capacity of C₃H₈ - pure hydrates were comparable, but slightly larger than those of THF- pure hydrates, which could form Bjerrum defects. The considerable variation in the compressibility between the two, appeared to be due to crystallographic defects. However, when a second guest molecule occupied the small cages of the THF hydrate, the deviation was smaller, because the subtle guest-guest interactions can offset an unfavorable configuration of unstable THF hydrates, caused by local defects in free energy. Unlike the methane molecule, the carbon dioxide molecule, when filling the small cage, can increase the expansion coefficient and compressibility as well as decrease the heat capacity of the binary hydrate, similar to the case of sI hydrates. The calculated bulk modulus for C₃H₈ pure and binary hydrates with CH₄ or CO₂ molecule varied between 8.7 and 10.6 GPa at 287.15K between 10 and 100MPa. The results for the specific heat capacities varied from 3155 to 3750.0 J kg⁻¹ K⁻¹ for C₃H₈ pure and binary hydrates with CH₄ or CO₂ at 287.15K. These results are the first of this kind reported so far. The simulations show that the thermodynamic properties of hydrates largely depend on the enclathrated compounds. This provides a much-needed atomistic characterization of the sII hydrate properties, and gives an essential input for large-scale discoveries of hydrates and processing as a potential energy source.

Key words: mixed propane clathrate hydrate; expansion coefficient; compressibility; heat capacity
1. Introduction

Clathrate hydrates, known as non-stoichiometric inclusion compounds, are ice-like crystal hydrates in which certain compounds (they are hydrate formers) stabilize the network formed by hydrogen-bonded concomitant water molecules.\(^1\) If the hydrate formers exist in the state of a gas, the clathrate hydrates are called gas hydrates. Three typical hydrate structures (cubic sI, cubic sII and hexagonal sH)\(^2\) have been identified in the permafrost region and in deep oceans as well as in pipelines\(^3\). A conservative assessment suggests that hydrates, when considered as potential future energy resources\(^4\), represent twice the energy stored in all other fossil fuel deposits\(^5\). There are three effective recovery methods for production of CH\(_4\) from gas hydrates deposits. Replacement of methane hydrates by CO\(_2\) is one of those\(^6\). Moreover, because of the high occupancy and selectivity of clathrate hydrates, various industrial applications have been suggested, such as gas storage, seawater desalination\(^7,8\), gas sequestration and transportation\(^4,9-13\). Other significant impacts of gas hydrates relate to flow assurance\(^14\), global climate change, the carbon cycle, ecosystems, marine geohazards, etc.

In almost all of the previously mentioned applications, the understanding of thermodynamic properties such as the thermal expansion coefficient, the isothermal compressibility and the heat capacity at constant pressure of the gas hydrates are essential. As for the thermal expansion coefficient, the basic information is critical for risk assessment studies of the mechanical stability of the earth strata hosting hydrates\(^15\). Seismic waves are usually employed in order to detect natural gas hydrates in sedimentary layers, and the wave speed is connected with the elastic constants and compressibility of the media through which they propagate\(^16\). Additionally, the heat capacity is not only used for the modelling of natural gas production from hydrate-bearing sediments, but also for hazard mitigation in conventional hydrocarbon extraction\(^17\). On a global scale, thermal properties provide a key for studies of climate changes related to methane release from natural hydrates\(^17\).

Most of the thermal and mechanical properties of gas hydrates can provide insight into the properties of other compounds like ice, I\(_h\), because of the common hydrogen-bond dominated network. While most thermodynamic properties are very similar, some of them differ widely between gas hydrates and ice I\(_h\), such as thermal conductivity and thermal expansion coefficient. The thermal conductivity of clathrate hydrates is anomalously low as compared to that of ice I\(_h\) due to the vibrational coupling of guest gas and host water molecules\(^18,19\). On the other hand, the thermal expansion coefficient is much larger than that of ice I\(_h\) below 200K\(^20\). Several studies have been done to investigate these anomalous properties of hydrates. The conclusion is that thermal conductivity and thermal expansion coefficient are related to the crystal type, guest type and size, as well as the occupancy\(^19-26\).

Large quantities of experimental results exist for the thermal expansion coefficient\(^20,27-32\), compressibility\(^17,33-36\) or bulk modulus, and heat capacity\(^17,37-39\) of clathrate hydrates. Unfortunately, these experimental values are mostly available in a limited and insufficient temperature - and pressure range. In addition, to measure such properties are rather difficult, time-consuming and costly, and the results can be strongly impacted by the purity of simple\(^15,40\). Molecular dynamic simulations have been shown to be a valid tool to probe the nature of gas hydrates on a molecular scale and link the microscopic behavior to macroscopic properties\(^7,8,41\). There are many studies on clathrate hydrates using MD simulation to calculate thermal expansion coefficient, compressibility and heat capacity\(^23\). Those results were used to validate experimental reports and obtain deeper relationships between hydrates’ configurations and thermodynamic properties. So far, most of studies have focused on sI hydrates\(^40,42-44\) with fewer studies of sII and sH hydrates\(^45-46\). Although the dominant structure of gas hydrates in nature is structure I (methane hydrate), sII and sH
Hydrates are also common in several regions, such as the Gulf of Mexico, Cascadia Margin, and South China Sea. Davidson et al. estimated the gas component of the near-seafloor hydrates samples from the Gulf of Mexico. They carried out carbon-13 NMR and powder XRD measurements and confirmed the sII hydrate. The sII hydrates made up more than 80% of the water in the core materials (80.5 wt% water, 13.6 wt% gas and 5.9 wt% solid residue), and no I hydrates were detected. Therefore, to understand the properties of sII hydrates is also necessary and important to understand their behavior and evolution in natural deposits.

Cubic structure II (sII) clathrate hydrate, with a unit cell denoted as 16M 8M 8L 136H2O has 16 small pentagonal dodecahedron cages and eight hexakaidecahedron large cages. C3H8 and THF hydrates are two typical hydrates with sII crystalline phase, one is the major component of structure II hydrates in sediments and the other is a promising analog material for CO2 recovery from flue gas as well as for hydrogen storage. It was used as a prototype for all hydrates to investigate, for example, the hydrates’ thermodynamics properties. Studies have demonstrated that the guest-host hydrogen bonding in THF hydrates leads to the formation of Bjerrum defects in the THF water lattice. This may explain the fast dielectric relaxation of hydrates and the fast kinetics of stoichiometric hydrates phase formation from ice at low temperatures. The difference in thermodynamic properties of C3H8 and THF hydrates can provide evidence that those properties are characteristic for the molecule involved and help comprehend the importance of guest-host interaction under similar conditions. To date, there are few studies of isobaric expansion coefficient, isothermal compressibility and heat capacity of C3H8 and THF hydrates by MD simulation, especially under low temperature conditions.

In addition, the small cages of sII hydrates are often occupied by relative small molecules (also called secondary “help-gases”) like CH4 and CO2 molecules, which stabilize the structure II hydrate lattice and affect the clathrate structure in binary hydrates. For that reason, it may also be significant to know the thermodynamic properties of sII hydrates in the presence of small molecules (CH4 and CO2). This is relevant for the gas production process from natural gas hydrates deposits, for example, the replacement of CH4 hydrates by CO2 from the deposits. We shall therefore also report results of calculations of the thermal expansion coefficient, the isothermal compressibility and the specific heat capacity for the sII structure with C3H8, THF in the presence of CH4 and CO2, all using MD simulations. From this basis, we discuss effects caused by host-host, guest-host and guest-guest coupling interaction on thermodynamic properties of structure II hydrates.

2. Method

2.1 Simulation tool and system definition

Molecular simulations were carried out using the Gromacs package version 4.5.4. For the sII hydrates system, the cubic simulation box (34.62×34.62×34.62 Å initial dimensions, lattice parameter of a unit cell is 17.31 Å) consisted of 2×2×2 unit cells. Periodic boundary conditions were used. The positions of the water oxygen atoms of the initial hydrate configuration were taken from x-ray crystallography, and the water hydrogen atoms were inserted to adjust the orientation for yield to Bernal-Fowler rule and minimize the net unit cell dipole moment and potential energy. All guest molecules were placed at the center of the water cages, assuming that the propane and THF molecules both full occupied the large cages, and that the methane, carbon dioxide molecules fully lived in the small cages. The OPLS-AA all-atom force field was used for both methane and propane. And the rigid, non-polarizable TraPPE potential was used for CO2 and THF molecules. Water was described by TIP4P/2005 model, as this was found to
be suitable for the host-host interaction\(^4\). The particle-mesh Ewald (PME) summation method\(^6\) was used to calculate the electrostatic interactions. Van der Waals interactions were calculated using the Lennard-Jones potential with a cut-off distance of 16 Å. The leapfrog algorithm\(^8\) was employed to integrate the equation of motion with a 1 fs time step.

### 2.2 Simulation procedure

Isotropic $NPT$ ensemble simulations were carried out to determine the average lattice parameters for pure propane and propane along with methane or carbon dioxide mixtures. Temperature and pressure control were implemented using velocity rescaling with a stochastic term\(^9\) and Parrinello-Rahman extended-ensemble pressure coupling\(^10\), respectively. For C$_3$H$_8$ pure and binary hydrates with CH$_4$ or CO$_2$ molecules, simulations were performed using the initial structure constructed above since the guest-host interaction is weak. Contrarily, for the THF pure and binary hydrates with CH$_4$ or CO$_2$ molecules, longer simulation times were needed in the low temperature region because of the strong interaction between host and guest, as well as low kinetic energy. To increase the particle thermal motion and eliminate non-equilibrium states of system, a single annealing simulation was performed with 200ps to bring the clathrate hydrates to the desired volume and temperature before the MD simulation. All the simulation parameters were set as above. To simulate the temperature-dependent lattice parameter, the pressure was set to atmospheric pressure or 14.5 MPa, while the temperature varied from 5 to 270 K. To simulate the pressure-dependence of the lattice parameter, the temperature was set to the same value (287.15 K), and the pressure was varied from 10 to 100 MPa in steps of 10 MPa. This range of pressures covers most of the relevant conditions for the natural gas industry\(^7\). Afterwards, 10 ns production run simulations were performed in the $NPT$ ensemble with 1 ns equilibration time.

It is known that classical MD simulations of lattice parameters of hydrates structures cannot capture accurately reported experimental results\(^4\), particularly at temperatures below 150 K. Therefore, in order to decrease the deviation from experiments, a simple correction method developed by Costandy et al.\(^43\) was used to modify lattice constants of the fully occupied structure sI with CH$_4$ or CO$_2$ pure hydrates. The corrected lattice constants were calculated from classical molecular dynamics simulations at low temperatures using the TIP4PQ/2005 water force field\(^7\). The procedures are as follow: Step one, quantum path-integral simulation and classical simulation for empty sII structure have been performed using TIP4PQ/2005 water model\(^7\) at temperature of 77, 100 and 125K. \(^7\) Then the temperature dependence for density difference $C(T)$ ($=\rho^{\text{emp}} - \rho^{\text{mod}}$) was obtained by fitting the density deviation data of the two different simulations for the empty sII hydrates in the temperature range 77-125 K to a second degree polynomial: $C(T)=a_0+a_1T+a_2T^2$ with $a_0=0.04672, a_1=-1.68913 \times 10^{-4}, a_2=2.17391 \times 10^{-7}$. Step two, classical MD simulations for C$_3$H$_8$ or THF pure and binary sII hydrates were performed using TIP4PQ/2005 water model as well as the other guest molecular force fields described above. Once the lattice constant $a$ for a hydrates unit cell was available from classical MD simulations (CS), the hydrate density, $\rho$, was calculated through

$$\rho = \frac{n_w M_w + \sum_i \theta_i M_g}{N_A V} \quad (1)$$

where $n_w$ is the number of water molecules per hydrate unit cell, $M$ is the molecular weight of water (w) and guest gas (g), $N_A$ is the Avogadro’s number, $\theta_i$ is the fractional occupancy of cavity $i$ by the gas
guest (θᵢ = 0 or 1, propane or THF fully occupied in the large cages, CH₄ or CO₂ or empty for the small cages in structure sII), νᵢ is the number of type i cavities in the unit cell, and V = a³ is the hydrates unit cell volume. Step three, the hydrate density is corrected through the following equation: ρ \text{corr} = \rho - C(T), where C(T) was obtained in step one and superscript "corr" as a function of temperature. And then, we can substitute in Eqn. (1) the obtained value for ρ and re-solve it in order to calculate the corrected value for unit cell volume (V) and the lattice constant: \( a^\text{corr} = (V^{corr})^{1/3} \). Finally, the lattice parameters performed by a series of similar NPT simulations and corrected by Costandy’s approach were used to calculate the corresponding thermal expansion coefficients. Otherwise, the values of compressibility corresponding to different hydrates were determined by lattice parameters without Costandy’s correction at constant temperature. All simulations were performed for propane hydrate, THF hydrates and these along with binary CO₂ or CH₄ within 5-287.15K and pressure range of 10-100MPa. The properties were obtained by numerical differentiation according to the following definitions:

\[
\alpha_p = \frac{1}{V} \left( \frac{\partial V}{\partial T} \right)_p \tag{2}
\]

\[
\kappa_T = -\frac{1}{V} \left( \frac{\partial V}{\partial P} \right)_T \tag{3}
\]

Where \( \alpha_p \) is the thermal expansion coefficient, K⁻¹; \( \kappa_T \) is the isothermal compressibility coefficient, MPa⁻¹; \( T \) is the temperature, K; \( P \) is the pressure, MPa⁻¹ and \( V \) is the volume, Å³.

Furthermore, we also used the fluctuations in the NPT ensemble to calculate the thermal expansion coefficients, isothermal compressibility and heat capacity of the single-crystal sII hydrate and compared these values with the numerical differentiation method and experimental values. The equations from fluctuation theory are as follows:\(^7^4:\)

\[
\alpha_p = \frac{\left\langle V \cdot U \right\rangle - \left\langle V \right\rangle \cdot \left\langle U \right\rangle + P \left( \left\langle V^2 \right\rangle - \left\langle V \right\rangle^2 \right)}{k_B T^2 \left\langle V \right\rangle} \tag{4}
\]

\[
\kappa_T = \frac{1}{k_B T \left\langle V \right\rangle} \left( \left\langle V^2 \right\rangle - \left\langle V \right\rangle^2 \right)_{\text{NPT}} \tag{5}
\]

\[
C_p = \frac{1}{2} \left( \frac{\left\langle U^2 \right\rangle - \left\langle U \right\rangle^2}{k_B N} + \frac{1}{k_B T^2} \right) + 2P \left( \left\langle V \cdot U \right\rangle - \left\langle V \right\rangle \cdot \left\langle U \right\rangle \right) + P^2 \left( \left\langle V^2 \right\rangle - \left\langle V \right\rangle^2 \right) \left( \left\langle \left\langle V^2 \right\rangle - \left\langle V \right\rangle^2 \right)_{\text{NPT}} \tag{6}
\]

where \( k_B \) is Boltzmann’s constant and equal to 1.38×10⁻²³ J/K; \( U \) is the potential energy, J; \( C_p \) is the heat capacity at constant pressure, J/K; \( i \) is the number of degrees of freedom (\( i=3n-k \), \( n \) is sample quantity and \( k \) is the number of constrained variables); and \( N \) is the number of molecules. The first term of Eqn (6) represents the contribution from the kinetic energy, and for a C₃H₈ or CH₄ molecule, \( i = 33 \) or 15, respectively; for a rigid CO₂ molecule, \( i = 5 \); for a THF molecule, TraPPE uses fixed bond lengths, \( i=10 \). Therefore, the first term of Equation (6) can be expressed as follows:
\begin{align}
\frac{i}{2} k_B N &= \frac{i}{2} k_B N_{H,O} + \frac{15}{2} k_B N_{CH_4} + \frac{5}{2} k_B N_{CO_2} + \frac{33}{2} k_B N_{C_3H_8} \\
\frac{i}{2} k_B N &= \frac{i}{2} k_B N_{H,O} + \frac{15}{2} k_B N_{CH_4} + \frac{5}{2} k_B N_{CO_2} + \frac{10}{2} k_B N_{THF}
\end{align}

where \(i\) represents the number of degrees of freedom (DOF) of water molecules, \(N_{H_2O}\), \(N_{CH_4}\), \(N_{CO_2}\), \(N_{C_3H_8}\) and \(N_{THF}\) is the number of water molecules, methane molecules, carbon dioxide molecules, propane molecules and THF molecules, respectively. If the water molecules are fully mobile, then \(i = 6\). If the water molecules can only rotate or only translate, then \(i = 3\). If the water molecules are fully immobile, then \(i = 0\). Here, we used \(i=6\) because the water molecules can rotate and translate slightly in the hydrates structures. Usually, the heat capacity of gas hydrates is reported not in \([J/K]\) but in \([J/(\text{mol} \cdot \text{K})]\), i.e., the specific heat capacity. Here, we denote the unit of specific heat capacity by \([J/(\text{kg} \cdot \text{K})]\):

\[c_p = \frac{1000 N_A c_p}{M_n}\]  

where \(c_p\) is the specific heat capacity, and \(N_A\) is Avogadro's constant. For an MD cell that consists of 2x2x2 unit cells, 1 mol MD cell contains 64 mol \(C_3H_8\cdot17H_2O\) or \(THF\cdot17H_2O\) when the gases only fully occupy the large water cages and 64 mol \(C_3H_8\cdot2CH_4or/CO_2\cdot17H_2O\) or \(THF\cdot2CH_4or/CO_2\cdot17H_2O\) when the gases fully occupy the water cages. Thus \(n=64\). \(M\) is the molar mass (g/mol) of the gas hydrate.

3. Results and discussions

3.1 Lattice parameter and isobaric thermal expansion coefficient

In this section, we report first results of a series of simulations using TIP4P/2005 water model or TIP4Q/2005 water model as well as guest molecular potentials mentioned above to determine the lattice parameters of structure II hydrates (\(C_3H_8\) or THF pure sII hydrates and \(C_3H_8\) or THF with \(CO_2\) or \(CH_4\) binary sII hydrates) as a function of temperature at atmospheric pressure or 14.5 MPa pressure. And then, we plot in Fig.1, the lattice parameters determined by TIP4Q/2005 water model modified by Costandy’s correction. The lattice parameters determined by TIP4P/2005 water model as well as experimental values of sII clathrate hydrates are also shown in Fig.1. It is first observed that the calculated lattice parameters using the TIP4P/2005 water model vary in an almost linear manner with temperature at higher temperature (>200K). The linear variation stops below this temperature. Also, deviations between experimental\(^{20, 75-76}\) and computational values become considerable in the low temperature region (<200K). The last leads us to conclude that quantum effects can have a significant effect on lattice parameter: The classical MD simulation using TIP4P/2005 water model could hardly reproduce the configurations at low temperatures\(^{40, 43}\). In contrast, the lattice parameters calculated by TIP4Q/2005 water model and modified by Costandy’s correction showed good agreement with the experimental data, also in the low temperature region. The TIP4Q/2005 water model should therefore not be used to explain lattice constants in this temperature region. Unfortunately, this is the he region where natural gas hydrates are stable in sediments and pipelines \(^{40}\). Costandy’s methodology is found to perform well, however, for cases of sII hydrates with single cage occupancies and for guest both without (for \(C_3H_8\)) and with (for THF) strong interaction between guest and host molecules.

Fig. 1 also shows that the lattice parameters of structure II \(C_3H_8\) hydrates are smaller than structure II THF hydrate’s and the lattice parameter increased when the small cages were occupied by secondary help-gas
species CH$_4$ and CO$_2$. Furthermore, compared with binary sII hydrates with CH$_4$ and pure hydrates, the binary sII hydrates with CO$_2$ expanding similar manners, especially in the high temperature region (>150K from Fig 1. In this study).

Ordinarily, guest molecules are enclathrated within the host water cages by weak van der Waals forces, and there is no strong interaction between the guest and host molecules. The push of the larger gas molecules on the cages is dominated by van der Waals repulsion, increasing by the size of the cages and therefore the size of the lattice. The maximum van der Waals diameters of propane and THF molecules were estimated using the Winmostar program\textsuperscript{77}: 6.7Å for C$_3$H$_8$ and 6.5Å for THF. Despite the larger guest-size of C$_3$H$_8$ as compared to THF, Fig.1 shows that C$_3$H$_8$ hydrates has the smaller lattice parameters at the same temperature, which might be an evidence for the anomalous interaction between THF and host molecules in sII clathrate hydrates. In clathrate hydrates of guest with hydrophilic functional groups (THF), hydrogen bonds between the guest and the water molecules have been observed in MD simulation\textsuperscript{55, 78} (Fig.2). The usual guest-host potentials encountered in parameterized versions of the van der Waals-Platteeuw equation do not take account of interactions such as guest-host hydrogen bonding, evidence for which was encountered recently both by experiment\textsuperscript{57-58, 79} and theory\textsuperscript{55, 80-81}. Guest-host hydrogen bonding affects the guest to which the hydrogen bond is formed as well as the guests in neighboring cages which may have a Bjerrum defect in one of their cage faces. The host-guest interaction affects the structure of THF clathrate hydrate crystal and plays an important for the properties of clathrate hydrates. Figure1 also shows that the lattice parameters of hydrates with CO$_2$ in small cages were larger than those with CH$_4$ in the high temperature region (>150K in this study) under the same pressure condition. However, in the low temperature region (<150K in this study), the lattice parameters of C$_3$H$_8$ binary hydrates with CO$_2$ are much smaller than those with CH$_4$ under the same pressure condition. This is different from the result for THF binary hydrates. Those findings may imply that the lattice parameter is sensitive to the occupation of small cages and that the guest-guest interaction plays a role in the determination of the lattice parameter. Alavi’s simulations\textsuperscript{55} can be taken as support. They showed that the number and nature of the guest in the small cage affected the probability of hydrogen bonding of the tetrahydrofuran guest with the large cage water molecules. Hydrogen bonding of tetrahydrofuran in large cages occurs, despite the fact that the guests in the small cages do not themselves form hydrogen bonds with water. These results indicate that nearest neighbor guest-guest interactions (mediated through the water lattice framework) can affect the clathrate structure and stability. That is why the lattice parameter difference between THF binary hydrates with CO$_2$ and THF pure hydrates is larger than the same difference between C$_3$H$_8$ binary hydrates with CO$_2$ and C$_3$H$_8$ pure hydrates under the same temperature and pressure conditions. Overall, the host-guest interaction and guest-guest interaction both play important roles in the determination of the properties of clathrate hydrates, especially for THF pure and binary hydrate. A cautious remark in the end: It should be remembered that the simulations did only taken into account the intermolecular stretching, and not the intramolecular stretching, assuming it to be constant (both TIP4P/2005 and TIP4PQ/2005 water models are rigid water models). This may also partially explain the larger reported lattice constants in the high temperature region.
Fig. 1 Lattice parameters for sII clathrate hydrates of the C$_3$H$_8$(a/c), THF(b/d) with different second-help molecules in the small cages as a function of temperature at atmospheric pressure (a/b) or 14.5 MPa (c/d) compared with the experimental values. Results are obtained by MD simulations, with (square points) and without (triangular points) the Costandy correction. Experimental data are shown as other signs. Data from other simulation works are indicated with a reference.
Fig2. Schematic representation of H$_2$O molecule cavities occupied by non-hydrogen bond forming guest C$_3$H$_8$(a) and hydrogen bond forming guest THF(b).

The volumes of the unit cells at atmospheric pressure or 14.5MPa were fitted to second-order polynomials as a function of temperature as follows:

\[ V = B_2T^2 + B_1T + B_0 \]  

(9)

Where \( V \) is the volume of the cell of the sII hydrate, in Å$^3$; and \( T \) is the temperature, in K; \( B_2, B_1, B_0 \) are coefficients of the second-order polynomial function. Their values for the different hydrates by two water models are presented in Tables I and II.

<table>
<thead>
<tr>
<th>Table I Coefficients of polynomial function for the unit volume of sII hydrates at atmospheric pressure. (units $B_2$: Å$^3$/K$^2$; $B_1$: Å$^3$/K; $B_0$: Å$^3$)</th>
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<tr>
<td><strong>TIP4P/2005</strong></td>
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<tr>
<td>$B_2$</td>
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<tr>
<td>(\times 10^{-4})</td>
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<tr>
<td>C$_3$H$_8$</td>
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<tr>
<td>C$_3$H$_8$+CH$_4$</td>
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<th>Table II Coefficients of polynomial function for unit volume of sII hydrates at 14.5 MPa pressure. (units $B_2$: Å$^3$/K$^2$; $B_1$: Å$^3$/K; $B_0$: Å$^3$)</th>
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</tbody>
</table>
By combining those fits and eqn (2), the isobaric thermal expansion coefficient was determined as a function of temperature at atmosphere pressure or 14.5MPa pressure. Figure 3 shows the thermal expansion coefficient of the pure and binary hydrates, obtained from the numerical differentiation of eqn (9) for the two water models, compared with the value given by fluctuations in the NPT ensemble using TIP4P/2005 water model (Eqn (4)). The results from the fit to the polynomial and from the fluctuation method agree relatively well. Obviously, the value of the thermal expansion coefficient of the hydrates, calculated with the TIP4PQ/2005 water model and Costandy’s correction, shows agreement with experimental data, especially in the low temperature region (<200K). The agreement generally increases when the small cages of sII structure hydrates are occupied by guest molecules at the same temperature. Both in C3H8 and THF binary hydrates, the thermal expansion coefficient of the binary hydrates with CO2 guest molecular in small cages, is larger than when we include CH4 binary hydrates at the same temperature. This finding agrees with the simulation results from the sI structure mixture hydrate and is in contrast to an experimental report (where the sample may be hampered by impurity). Many other measurements and MD simulations indicate that the thermal expansion coefficient of the CO2 hydrate is larger than that of the Xe hydrates and that of the pure CH4 hydrates at high temperature. The agreement with experimental data, shows agreement with experimental data, indicates that the host-guest interaction can play an important role in the determination of the properties of gas hydrates. However, both sI and sII structure hydrates are ice-like crystals in which the guest molecules are encapsulated in a network formed by hydrogen-bonded water molecules, and some similarities exist in the property of mechanics and thermodynamics, for example the host-host effect on expansion coefficient. That is the reason why the expansion coefficient of the pure propane hydrates is just slightly larger than the pure THF hydrate. In addition, when we compare Fig. 2(a) and Fig. 2(c) (or Fig. 2(b) and Fig. 2(d)), we find that the thermal expansion coefficient is not only temperature dependent, but also to some degree pressure dependent. The pressure does not have a substantial effect on the thermal expansion coefficient, however, so the effect of the intermolecular interactions on the temperature-dependent expansion coefficient may be more complex, than that on the pressure-dependent compressibility.

In conclusion, the guest – host interactions and guest-guest interactions may both play a similarly important role as the host – host interactions for hydrate expansion properties, similar to what is experimentally observed for thermal expansion behavior of sII clathrate hydrates with diatomic guest molecules. This finding is in contrast to what was expected and may also explain the reason behind the difference in thermal expansion between sI and sII hydrates.
Fig 3. The isobaric thermal expansion coefficient for sII clathrate hydrates of the C$_3$H$_8$(a/c) or THF(b/d) with different guest molecular in the small cages as a function of temperature at atmospheric pressure(a/b) and 14.5MPa(c/d).

3.2 Isothermal compressibility

We used the TIP4P/2005 water model as well as guest molecular potentials described above to model the interactions at 287.15K. A series of simulations were performed to determine the isothermal compressibility as a function of hydrate compositions at various pressures (10 - 100MPa) at the same temperature. The lattice parameters obtained are plotted in Fig. 4. The figure shows that the lattice parameter decreases with increasing pressure. At the maximum pressure of the simulation (100MPa), for the propane and THF pure hydrates, the deviations of unit cell volume was 1.0 % and 1.3 % of the unit cell volume at 10MPa, respectively. The guest-host interaction and guest-guest interaction cannot vary much in this range. But, the parameters of binary THF hydrates are larger than those of binary C$_3$H$_8$ hydrates, in the presence of the same second-help molecules in small cages. Lattice parameters of propane and THF binary hydrates with CO$_2$ are furthermore larger than with CH$_4$ at the same pressure. This finding is in accordance with the results obtained above, and indicates that the lattice parameter of hydrates depends not only temperature and composition, but also on pressure.

The lattice parameters presented in Fig. 4 were fitted to second-order polynomials as follows:
Here \( V \) is the volume of the unit cell of the sII hydrate, in \( \text{Å}^3 \); and \( P \) is the pressure, in MPa. Using these expressions and eqn (3), we determined the isothermal compressibility. Figure 5 provides the values of the compressibility of the sII hydrates derived from the numerical differentiation of eqn (10) and from fluctuations in the \( NPT \) ensemble (eqn (5)). The results from the fit to the polynomial and from the fluctuation method again agree relatively well. We note that the \( \text{C}_3\text{H}_8 \) binary hydrates with \( \text{CO}_2 \) molecules in the small cages can be easier compressed than a \( \text{C}_3\text{H}_8 \) pure hydrate with small cages unoccupied. By contrast, it is more difficult to compress the \( \text{C}_3\text{H}_8 \) hydrates with \( \text{CH}_4 \) molecules filled in the small cages. We note that a gas hydrate occupied by a linear guest molecule appears to be more compressible than one occupied by a symmetric guest molecule. However, the isothermal compressibility of THF pure hydrates is relatively small due to the hydrogen-bonded framework. Defects inevitably found in real polycrystalline hydrate systems will increase compressibility. Meanwhile, the value of isothermal compressibility of the THF hydrates reduce approximately to the sI and sII structure number for small cages of hydrates crystal occupied by second-help guest molecules, such as \( \text{CH}_4 \) and \( \text{CO}_2 \). This finding shows that the so-called second-help guests could improve the stability of THF binary hydrates, even if the defect remain. Moreover, the THF binary hydrates with symmetric guest molecule (\( \text{CH}_4 \)) is more difficult to compress than THF binary hydrates with linear guest molecule (\( \text{CO}_2 \)), which however, is the same as propane binary hydrate.

The radial distribution functions (RDFs) were computed to further elucidate this point. The RDFs \( g_{oo} \) of host water are shown in Fig.6 for 14.5 MPa and 287.15 K for THF pure and binary hydrate with \( \text{CH}_4 \) or \( \text{CO}_2 \) as well as \( \text{C}_3\text{H}_8 \) pure. Those RDFs indicate that the arrangement of water molecules in \( \text{C}_3\text{H}_8 \) hydrates is more perfect than in THF hydrates. This may be attributed to the formation of crystallographic defects in THF hydrates, which could interrupt the regular pattern of symmetry or the equilibrium state of the crystal. Imperfection of the THF hydrate crystal may be a reason why it is abnormally easier to distort and compress than \( \text{C}_3\text{H}_8 \) hydrate. Interestingly, compared with \( \text{C}_3\text{H}_8 \) hydrates, THF with \( \text{CH}_4 \) binary hydrates are also present with a normal arrangement of water molecules, which is obviously different to the case of THF with \( \text{CO}_2 \) hydrates. Alavi’s simulation\(^55\) showed that the THF binary sII hydrates with \( \text{CO}_2 \) had the largest probability of hydrogen bond formation between guest THF and host water molecule. The pure THF sII hydrates with empty small cages had furthermore a greater probability of hydrogen bonding than the binary sII hydrates with \( \text{CH}_4 \). These findings may account for the distinct different arrangements of those hydrates. It was confirmed that the subtle guest-guest interaction could play an important role for the crystallographic structure and therefore affect the thermodynamic properties of hydrate crystals. Besides, THF and \( \text{CO}_2 \) binary hydrates have the largest probability to form hydrogen bonds, but they can also be stabilized by van der Waals forces between guest-host molecules and by subtle guest-guest interactions, even if THF and \( \text{CO}_2 \) binary hydrates are easier to compress than THF and \( \text{CH}_4 \) binary hydrates (which are also stabilized by second-help molecules).

\[
\begin{align*}
V_{c,\text{H}_8} &= 1.8935 \times 10^4 P^2 - 0.58 P + 5159.9018 \\
V_{c,\text{H}_8-\text{CH}_4} &= 2.1732 \times 10^4 P^2 - 0.5305 P + 5211.8002 \\
V_{c,\text{H}_8-\text{CO}_2} &= 2.1092 \times 10^4 P^2 - 0.6130 P + 5286.8328 \\
V_{\text{THF}} &= 6.9879 \times 10^4 P^2 - 0.869 P + 5219.6656 \\
V_{\text{THF-CH}_4} &= 5.2064 \times 10^4 P^2 - 0.6673 P + 5270.0361 \\
V_{\text{THF-CH}_4} &= 3.8109 \times 10^4 P^2 - 0.70134 P + 5366.2880 \\
10 &\leq P \leq 100 \text{MPa}
\end{align*}
\]
Fig. 4 Lattice parameters for sII clathrate hydrates of C$_3$H$_8$(a) and THF(b) with different guest molecules in the small cages, as a function of pressure at 287.15K.

Fig. 5 The isothermal compressibility of sII hydrates of C$_3$H$_8$(a) and THF(b) with different guest molecules in the small cages as a function of pressure at 287.15 K.

Fig. 6 Radial distribution function (RDF) for the oxygen-oxygen atoms of water at 287.15K and 14.5MPa for different pure and mixed hydrates.
The bulk modulus of clathrate hydrates is the inverse of the compressibility:

$$\beta_T = \frac{1}{\kappa_T} \quad (11)$$

The bulk modulus of the propane sII structure hydrates and propane binary hydrates with CH₄, CO₂ from this relation is approximately 8.96 GPa, 9.93 GPa and 8.70 GPa at 287.15 K and 14.5 MPa, respectively. The calculated bulk moduli of propane hydrate, pure and binary, are close to the experimental value of ice Ih and sI CH₄ hydrate; approximately 9.1 GPa at 253 – 268 K and 9.1 GPa at 271K and 0.6 MPa, respectively. The bulk modulus of the propane sII structure hydrate decreased when CO₂ occupied the small cages. The effect should be considered for CH₄ recovery processes from CH₄ hydrates in deep oceans. This applies for instance to the Shenhua area, where sII structures are found in abundance. The knowledge is also relevant for the replacement of CH₄ by CO₂ in both sI and sII structure hydrates, especially when the solid including CH₄ hydrates act as cement or have a framework support function in porous sediments. Figure 5 shows the bulk modulus of the THF sII structure from Eq. 11 is approximately 6.0 GPa at 287.15K and 14.5 MPa, which is far apart from values of other sI and sII hydrates. It reflects that pure THF hydrates under this condition are relatively soft, probably due to a defective hydrogen-bonded framework. When the small cages of THF hydrates were filled with second-help molecules CH₄ or CO₂, the bulk modulus increased to 8.1 GPa and 7.8 GPa at 287.15 K and 14.5 MPa, respectively. The results taken together indicate that small cage - guests can stabilize the structure through hydrogen binding of THF in binary structure II clathrate hydrates. Since the bulk modulus is mainly determined by the elasticity of the hydrogen-bonded water framework, the effect of small cage guests should not be neglected. Variable filling of the cavities with guest molecules also has a substantial effect on the bulk modulus, especially for hydrates with strong guest-host interaction.

3.3 Specific heat capacity at constant pressure

The specific heat capacity at constant pressure is used to compute hydrate entropy and enthalpy as a function of temperature. With information also on the enthalpies of phase transition, one can predict hydrate stability. In the permafrost region, the temperature of the hydrate deposits is normally far from the equilibrium temperature. Knowledge of the limit for stability is essential for prediction of climate gas depletion. So far, specific heat capacity has been measured for propane and tetrahydrofuran hydrates. There are limited data for sII structure binary hydrates with CH₄ and CO₂ molecules. The results and discussion above have shown that the fluctuation method can give results comparable to those calculated by the fitting method. Therefore, the fluctuation method was used to also calculate the average heat capacities of the C₃H₈ and THF sII structure pure hydrates and their binary mixtures. We calculated the constant pressure specific heat capacity of the mixed hydrates in the temperature range 5 - 287.15 K and the pressure range 10-100 MPa. The results were plotted in Fig. 7 and 8 and compared to published result for sII hydrates. We see that the different clathrate hydrates have relatively different heat capacities. The specific heat capacities of the C₃H₈ hydrates are slight larger than those of the THF hydrates. We explain that by the guest molecule property and the interaction between guest and host. Compared with the pure C₃H₈ and THF hydrates, the specific heat capacity of both C₃H₈ and THF hydrates decrease when the small cages of hydrates are occupied by CO₂ molecules and they increase when the same cages are filled with CH₄ molecules at the same temperature and pressure. That is, the effect of the CO₂ molecule can be treated as a positive contribution to the heat capacity in sII structure hydrates, while the CH₄ molecule has a negative
contribution relatively speaking. This is in accordance with the result published on sI hydrates\textsuperscript{40}. With increasing pressure, the heat capacities decrease slightly. The heat capacity of C\textsubscript{3}H\textsubscript{8} or THF pure and binary hydrates as a function of pressure at 287.15K was fitted to a line as follows:

\begin{align}
    c_{P,C,H\textsubscript{8}} &= -0.7563P + 3613.2690 \\
    c_{P,C,H\textsubscript{8}+CH\textsubscript{4}} &= -0.4813P + 3717.0008 \\
    c_{P,C,H\textsubscript{8}+CO\textsubscript{2}} &= -0.1763P + 3189.2362 \\
    c_{P,THF} &= 2.7669P + 3585.7779 \\
    c_{P,THF+CH\textsubscript{4}} &= -0.3824P + 3215.7374 \\
    c_{P,THF+CO\textsubscript{2}} &= -0.0559P + 2764.3700
\end{align}

(12)

Here \( c_p \) is the specific heat capacity at constant temperature, in J kg\textsuperscript{-1} K\textsuperscript{-1}, and \( P \) is pressure, in MPa. According to the eqn (12), the specific heats of C\textsubscript{3}H\textsubscript{8}, C\textsubscript{3}H\textsubscript{8} with CH\textsubscript{4} and C\textsubscript{3}H\textsubscript{8} with CO\textsubscript{2} hydrates are in the range of 3605-3537.6 J kg\textsuperscript{-1} K\textsuperscript{-1}, 3712-3668.8 J kg\textsuperscript{-1} K\textsuperscript{-1} and 3187-3171.6 J kg\textsuperscript{-1} K\textsuperscript{-1}, respectively, and decrease by approximately 1.9\%, 1.1\% and 0.5\% between 10 and 100 MPa, respectively. The above analyses show that the specific heat capacity of sII structure is (relatively) pressure independent. The pressure has a complicated effect on the heat capacities of the THF sII structure hydrates. As the pressure increased, the value of heat capacity of THF pure hydrates apparently increase by 6.9\%. But, when the small cages of THF hydrates are occupied by small molecules, such as CH\textsubscript{4} and CO\textsubscript{2}, the heat capacity of the binary hydrates may decrease slightly with the pressure increase. This finding may be attributed to the subtle guest-guest interaction and lattice defects, which can affect the thermal motion of atoms and then distort the specific heat capacity. Likewise, according to the eqn (12), the specific heats of THF with CH\textsubscript{4} and THF with CO\textsubscript{2} hydrates are in the range of 3211-3199.7 J Kg\textsuperscript{-1} K\textsuperscript{-1} and 2764-2766.7 J Kg\textsuperscript{-1} K\textsuperscript{-1}, respectively, and decrease by approximately 0.4\% and 0.1\% between 10 and 100MPa.

![Fig.7 Pressure dependence of the specific heat capacity at constant pressure of C\textsubscript{3}H\textsubscript{8}(a), THF(b) pure and with CH\textsubscript{4} or CO\textsubscript{2} binary hydrates at 287.15K.](image-url)
Compared with the pressure, the effect of temperature on the specific heat is larger. Handa\textsuperscript{37, 86} obtained approximately 804-2027 J kg\textsuperscript{-1} K\textsuperscript{-1} for propane sII hydrates (C\textsubscript{3}H\textsubscript{8} \cdot 17H\textsubscript{2}O refers to full occupancy of the large cages of structure II) between 85 and 279 K at 0.34 MPa and 841-2074 J kg\textsuperscript{-1} K\textsuperscript{-1} for THF pure hydrates (THF \cdot 16.9H\textsubscript{2}O) between 85 and 270 K. The capacity increased 152.1\% within this temperature range. Leaist et al.\textsuperscript{39} investigated approximately 1066-1893 J kg\textsuperscript{-1} K\textsuperscript{-1} for THF hydrate (THF \cdot 16.9H\textsubscript{2}O) between 120-260K at atmospheric pressure. The value increased 77.6\% in the temperature interval of 10 K. Yamamura et al.\textsuperscript{84} measured approximately 56.7-4025.2 J kg\textsuperscript{-1} K\textsuperscript{-1} for THF pure hydrates (THF\textsubscript{16.64}H\textsubscript{2}O) between 12-300K at atmospheric pressure. Tombari et al.\textsuperscript{85} measured and compared the heat capacity of the THF clathrate hydrates and of its components (THF \cdot 15.9H\textsubscript{2}O, THF \cdot 17.1H\textsubscript{2}O and THF \cdot 17.7H\textsubscript{2}O) against the temperature at ambient pressure. Our simulations indicated that the heat capacity of C\textsubscript{3}H\textsubscript{8} or THF - pure and binary hydrates as a function of temperature at 14.5MPa can be approximately fitted to a line as follows:

\[
\begin{align*}
    c_p^c_{\text{H}_\text{c}} &= 1.5018 T + 3071.3113 \\
    c_p^c_{\text{H}_\text{c} + \text{CH}_4} &= 0.9386 T + 3368.7513 \\
    c_p^c_{\text{H}_\text{c} + \text{CO}_2} &= 1.4115 T + 2675.4371 \\
    c_p^{\text{THF}} &= 2.1112 T + 2412.7323 \\
    c_p^{\text{THF} + \text{CH}_4} &= 1.4161 T + 2760.1949 \\
    c_p^{\text{THF} + \text{CO}_2} &= 1.9013 T + 2358.7803 \\
\end{align*}
\]

(5 \leq T \leq 270K)

Where \(c_p\) is the specific heat capacity at constant pressure, in J kg\textsuperscript{-1} K\textsuperscript{-1}, and \(T\) is the temperature in K. The average value of the heat capacity of C\textsubscript{3}H\textsubscript{8} pure hydrates increase approximately 8\% from 3261 J kg\textsuperscript{-1} K\textsuperscript{-1} at 150K to 3522 J kg\textsuperscript{-1} K\textsuperscript{-1} at 270K. The value of the heat capacity of THF pure hydrates increased approximately 15.2\% in the same temperature region. The increase rate of the heat capacity of pure THF hydrates is the largest of those hydrates mentioned in this paper. The RDFs for oxygen-oxygen of water and oxygen atom of THF with the hydrogen atom of water (HW) at 14.5MPa pressure for the THF pure sII hydrates were shown in Fig.9. The insert shows the THF-water hydrogen bonding in the THF hydrates as the area under the peak in the RDF at 1.5Å. The peak is related to the extent of THF-water hydrogen bonding in THF hydrates. The guest-host hydrogen bonding gradually degrades with increasing of temperature and decreasing activation barrier to motion of THF molecules.\textsuperscript{87-88} The water molecules of the framework become more labile and the heat capacity increases rapidly for THF hydrates after the melting temperature (287.15K).

Although the results yield similar dependencies on temperature, there is a systematic difference between the experimental values and the calculated of heat capacities of C\textsubscript{3}H\textsubscript{8} and THF pure hydrates, especially at low temperature. We have calculated the value of the specific heat capacity of liquid water at 298 K and 1 atm using the TIP4P/2005 water model. The value was 84.6 J mol\textsuperscript{-1} K\textsuperscript{-1}, approximately 12\% larger than the experimental value, 75.6 J mol\textsuperscript{-1} K\textsuperscript{-1}.\textsuperscript{40} The specific heats of C\textsubscript{3}H\textsubscript{8}, THF pure and binary hydrates in this case may be similarly overestimated (see the ESI. Compared two different fluctuation methods). Considering the systematic deviation, the calculated values were in the range of 3219-3158.0 J kg\textsuperscript{-1} K\textsuperscript{-1} for C\textsubscript{3}H\textsubscript{8} pure hydrates, 3314-3275.9 J kg\textsuperscript{-1} K\textsuperscript{-1} for C\textsubscript{3}H\textsubscript{8} binary hydrates with CH\textsubscript{4} and 2846-2831.2 J kg\textsuperscript{-1} K\textsuperscript{-1} for C\textsubscript{3}H\textsubscript{8} binary hydrates with CO\textsubscript{2} at 287.15K between 10 and 100 MPa and 2749-3104.3 J kg\textsuperscript{-1} K\textsuperscript{-1} 3011-3233.2 J kg\textsuperscript{-1} K\textsuperscript{-1} at 14.5 MPa between 5 and 270 K, respectively. Considering the temperature or pressure difference between the measurements and our simulations, the modified results are still higher than the experimental measurements at a high temperature range. The experiments may have been hampered by the impurity of the hydrates samples. Although the effect of residual ice or liquid water on the measurements can be eliminated,\textsuperscript{17, 89} the residual gas is barely removed because the samples,
whether synthesized in a laboratory or obtained in nature, contain many micro-pores.\textsuperscript{90-92} The diameter of these pores was 100 – 500 nm, sometimes even 1 \textmu m.\textsuperscript{92} In addition, it is more difficult to compress polycrystalline hydrates samples with multiple pores than polycrystalline ice with multiple pores. Therefore, the micro-pores and residual gas may greatly lower the experimental values of the specific heat of gas hydrates. Furthermore, the cages in the gas hydrates in the lab and in nature may not be fully occupied by guest molecules (sometimes water-deficient and therefore excess guest molecules). And the cage occupancy also depends upon the temperature, pressure, guest concentration and the guest and cage types. However, the cage occupancy has a complicated and weak effect on the heat capacities of hydrates at different pressure.\textsuperscript{40}

![Figure 8: Temperature dependence of specific heat capacity of C\textsubscript{3}H\textsubscript{8}(a) or THF(b) pure and binary hydrates with CH\textsubscript{4} or CO\textsubscript{2} binary hydrates at 14.5MPa.](image)

![Figure 9: Radial distribution functions for the oxygen-oxygen atom of water(a) and the oxygen atom of THF(O)](image)
with the hydrogen atom of water (HW) at 14.5MPa(b) pressure for the THF pure sII hydrates.

4. Discussion

According to our simulations, the host-host interaction, guest-host interaction and guest-guest interaction all have effects on the expansion, compressibility and heat capacity of gas hydrates. Generally, the host-host interaction plays the main role for mechanical and thermal properties of both structure I and II clathrate hydrates at lower temperatures (≤ 200K) and pressures (≤100 MPa). The relatively weaker guest-host interaction has an impact on the properties at higher temperatures and pressures. However, the guest-host and guest-guest interaction appears different for thermal and mechanical behavior of gas hydrates, especially for hydrates with hydrophilic guest molecules, in which the guests may form hydrogen bonds with the cage water (leading to the formation of a Bjerrum L-defects between two framework water molecules). The mechanical and thermal properties of hydrates with these extra hydrogen-bonded frameworks follow special patterns. While other sI and sII clathrate hydrates with hydrophobic molecules, obtain a stronger guest-host and guest-guest coupling interaction (≥260K) and obtain an extraordinarily high strength compared with other icy compounds.

Two water models, TIP4P/2005 and TIP4PQ2005, were used in our simulations. Compared with the experimental results, the lattice parameters calculated using TIP4P/2005 water model exhibit a discrepancy with the experimental values below 200K, similar to what was observed for sI and sH hydrates. Subsequently, we modified the lattice parameters using Costandy’s method, leading to a match with the experimental value at the low temperatures (Fig.1). As a result, the deviation between the calculated thermal expansion coefficient and the experimental values, which was large using TIP4P/2005 water model, could be reduced significantly. To some extent, the specific heat capacities calculated by our simulations deviate from experimental values below 260 K (Fig. 8). This behavior may imply that the rigid and non-polarizable water models and guest potentials do not describe properly the host−guest interaction. As mentioned above, the host-guest and guest-guest interactions are rather weak. Random thermal motions of the host and guest molecules are constrained under low-temperature conditions, but not at high. Hydrate proton NMR analysis and dielectric constant measurements have suggested that water molecular motion is “frozen in” at very low temperatures (<50 K) so that hydrates lattices become rigid. The reorientation of water molecules is the first-order contribution to water motion in the structure; the second-order contribution is due to translational diffusion at these low temperatures. The rate of molecular water diffusion is as much as two orders of magnitude slower in the gas hydrates than in ice.

Supplementary calculations indicated that a smaller number of degrees of freedom i(DOF) of water molecules in hydrates may be more suitable for determination of the heat capacity by the fluctuation method at lower temperatures, especially in the solid state of the water-related system. For example, above 271.15 K, i = 3 can result in a $c_P$ of water or C$_3$H$_8$ and THF pure hydrates that is closer to the experimental values. However, i = 0 may be more suitable for ice Ih or C$_3$H$_8$, THF pure hydrates at lower temperatures and can yield a $c_P$ value that is closer to the experimental values (Fig. 10).
Fig. 10 Temperature dependence of specific heat capacity of C₃H₈ (a) and THF (b) pure hydrates at 14.5MPa using DOF=0 and 3.

Experiments⁸⁹, ⁹³ have shown that polycrystalline sI hydrates are ductile and that sII hydrates exhibit an irreversible plastic-deformation-like pattern, where the expanded lattices fail to recover their original state with contraction. The tendency of thermal expansion appears to be “memorized” from previous history. Therefore, to gain a better understanding of these properties of gas hydrates, it is necessary to use more realistic intermolecular potentials and more complex approximations that consider the inharmonic effects, although such undertakings will require a substantial calculation time. A suitable description of the intermolecular interactions of the guest – guest and guest – host complexes is also important in the study of simulated properties of gas hydrates, considering the importance of the guest – host coupling interaction on the thermodynamic properties of C₃H₈ or THF hydrates. A highly accurate and explicit model for the guest – water interaction potential is required, and the use of LJ parameters fitted to the ab initio data does provide a good approach. But in our further studies, polarizable water models and ab initio-fit H₂O-C₃H₈ or THF potentials will be tested by studying the effects of temperature and occupancy on the thermal and mechanical properties of monocry stalline and polycrystalline gas hydrates, and the results will be compared to those from ab initio density functional theory.

5. Conclusions
Classical molecular simulations were performed to determine mechanical and thermodynamic properties
of structure II C$_3$H$_8$ or THF pure and binary hydrates, including thermal expansion coefficient, isothermal compressibility and heat capacity at constant pressure. For THF pure and binary hydrates, a short single annealing simulation was first done to optimize the initio configuration at low temperature, with the intention to make the initial structure more reasonable and decrease the simulation time. We found that the correction for lattice parameters of hydrates in low temperature region is significant improvement of the results compared to experimental data. This simple methodology to incorporate quantum effects is found to perform well both in C$_3$H$_8$ and THF hydrates at low temperature and achieves a balance between relatively accurate results and low computational time. Based on above operation and the correction, the lattice parameters and thermal expansion coefficients of C$_3$H$_8$ and THF hydrates are close to the experimental values. The results provide a basis for further study of the effect of temperature and guest molecule types on the expansion at low temperature by MD simulations. Our simulations also reveal that the lattice parameter at a constant pressure or a constant temperature varies as a function of the guest type and guest coupling interaction. The thermodynamic properties of THF hydrates are similar to that of C$_3$H$_8$ hydrates and CH$_4$ hydrates except for compressibility, which also provides the possibility for the application of THF hydrates instead of other hydrates in the experiment. Small molecules, such as CH$_4$ and CO$_2$, play an obvious role in the stabilization of THF hydrates structure with defect. Moreover, when the CO$_2$ molecules replace CH$_4$ molecules in the small cages of sII structure, the lattice parameters, isothermal compressibility and thermal expansion of the hydrates increase, and the bulk modulus and specific heat capacity decrease accordingly. The effect to structure II hydrates is the same as that to structure I hydrates, that is, this effect has nothing to do with crystal structure and other guest type in the hydrates. Furthermore, the effect of the hydrates volume and heat capacity variations should not be neglected during the recovery of CH$_4$ from CH$_4$ hydrates in deep oceans using CO$_2$ to replace CH$_4$, especially in the calculation of phase equilibria and mechanical stability of sediments. Although the heat capacities of C$_3$H$_8$, THF pure and binary hydrates using the fluctuation method showed a systematic deviation from the experimental values at lower temperatures, the results are still comparable with the experimental values at higher temperatures, and in reality, most natural hydrates reservoirs and petroleum industry temperatures are in the higher temperature range. The present approach, which can replace the costly and time-consuming experimental measurements and be applied to calculate the variation of mechanical and thermal properties mixture hydrates with different guest types, could potentially be applied to other complex hydrates systems, such as sI + sII hydrates; gas storage and transportation; and deep-sea sequestration of CO$_2$.

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