Integrated Approach to Variable Speed Limits & Ramp Metering

extension of COSCAL v2 algorithm with ramp metering and ramp queue constraints

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Integrated Approach to Variable Speed Limits & Ramp Metering
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Traffic congestion continues to remain a serious problem in most countries, with significant economic and environmental losses. ‘Intelligent Transport Systems (ITS)’ that utilize advanced information and communication technology for managing road infrastructure, including vehicles and users, have shown great potential in dealing with this problem. However, most current traffic management measures, like route guidance, ramp metering and variable speed limits are designed and implemented independently. Potentially counter-productive when deployed simultaneously, integration of these measures can benefit from synergic effects.

The aim of this work is to integrate a near-future variable speed control strategy with ramp metering, to operate efficiently at a freeway merging section. From a policy perspective, this is a challenge because freeways and urban network are managed by different authorities. Currently, a spillback of ramp queue to the urban network results in a deactivation of ramp metering, and an abrupt release of on-ramp vehicles onto the freeway. This is undesirable for the freeway control measure. Therefore, the development of the integrated strategy considers both, an improvement in freeway efficiency, and at the same time queue regulation at the on-ramp.

The research arch is initiated by conducting a literature survey, wherein the theoretical and control aspects of available speed control approaches are studied first. Subsequently, different queue management approaches used in current ramp metering strategies are reviewed to identify the desirable features for a queue controller. Finally, integration approaches for combining ramp metering with variable speed limits are looked at.

It is seen that optimization-based integration strategies may offer huge potential to improve freeway efficiency but these strategies are computationally complex for systems available in practice. Therefore, a sophisticated reactive variable speed limits strategy - COoperative Speed Control ALgorithm (COSCAL v2) is chosen for integration with ramp metering. COSCAL v2 is a counteractive control strategy that resolves moving jams to recover loss in efficiency from capacity drop. It uses shockwave theory concepts to speed limit the exact the number of vehicles required to first resolve a jam, and next, to stabilize the traffic while recovering traffic throughput.

The theory development is conducted in two stages from a simplistic to a more advanced approach that relaxes some of the initial assumptions. The basic strategy is developed to guarantee jam resolution under the condition of a constant ramp metering flow during the activation of COSCAL v2. Additionally, ramp queue constraints are not included, which implies that in order to prevent a spillback, a sufficiently high metering flow must be chosen. The theoretical formulation to determine when and how many vehicles must be speed-limited, as in COoperative Speed Control ALgorithm (COSCAL) v2, is preserved here.
The core principle involves instantaneously speed-limiting the vehicles entering the moving jam. In this way, the inflow into the jam is reduced as compared to the flow exiting the jam, resulting in jam resolution. In the integrated strategy, the theory to determine the most upstream speed-limited vehicle that resolves the jam, given a constant ramp metering flow, is formulated. Similarly, the theory for determining the last vehicle speed-limited for stabilization is extended for the additional ramp flow. For this, COSCAL v2 checks for a maximum (average) density in the speed-limited area to ensure traffic stability. The value of the target density determines the freeway flow arriving at the on-ramp. Then, the integrated approach determines reduced target densities required to accommodate the ramp flow. It is also described how these densities can be implemented in practice, and how errors its realization can be compensated within the feedback structure of the scheme.

However, this approach is not feasible for time-dependent ramp metering flows. This is essentially because accommodating a varying ramp flow will require implementing different densities in space-time, which is both difficult to determine and implement in the COSCAL v2 algorithm. Therefore, in the advanced strategy the theory of COSCAL v2 is extended for compatibility to a more sophisticated ramp metering approach. In the new approach, rather than regulating density the flow arriving at the on-ramp is directly controlled by determining when and where vehicles should enter and exit speed-limits. This additionally improves the effectiveness of COSCAL v2. Further, a new ramp metering strategy using cumulative curves is developed to include: queue-length constraints; policy restrictions on ramp metering flows; and limitations on the minimum freeway flow that can be achieved with speed limits given the traffic state measurements. One of the main advantages of the advanced strategy is its responsiveness to changing ramp flows, and the utilization of freeway speed-limitation to prevent a queue spillback on the ramp.

Following the development of the two integration strategies, the advanced approach is translated to an algorithm. This step ensures that a controller can be designed to realize traffic behaviour according to the developed theory. Here, the complete strategy is divided into five modules that together determine the spatial extent of speed limits at any given time. Similarly to the algorithmic formulation of COSCAL v2, unique driving modes for the different detection and actuation tasks of the algorithm are used to communicate the control scheme for implementation.

The control strategy thus developed is tested by means of simulation. Of the five modules, three modules related to the speed control strategy are implemented in this work. Simulation runs under different demand conditions are performed to verify the behavioural performance of the approach. Jam waves - that otherwise occur when ramp metering and COSCAL v2 are implemented independently - are prevented in the integrated approach. The results offer an initial indication of potential improvement from the strategy. However, a more comprehensive quantitative evaluation is recommended. Furthermore, some critical developments to the approach following the simulation study are identified.

In conclusion, this work demonstrates two ways in which COSCAL v2 can be integrated with ramp metering (RM); how cumulative curves can be used for integration of control measures; and how efficiency gains on the freeway and urban network can be balanced. The simulations offer a proof of concept for the working of the advanced integrated strategy. However, the basic strategy should be both implemented and tested further.
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Chapter 1
Introduction

The functional characteristic of freeway infrastructure is to transport high volumes of people and goods at high speeds. However, there is a trade-off between maximizing supply and maintaining highest efficiency. With growing mobility and traffic demand, providing sufficient infrastructural capacity has become a limitation. This makes a traffic breakdown increasingly likely when traffic intensity peaks spatio-temporally. As a result, freeway congestion continues to remain a serious problem in most countries, with many adverse effects - from lost vehicle hours, energy consumption to emissions.

This research aims to develop an ‘intelligent’ traffic management system that addresses the problem of freeway congestion. In this chapter, the main goal is to identify the research objectives, the approach that will be adopted, focus areas and the scope of the research.

1-1 Research Motivation

In order to arrive at the relevant research questions, three intriguing questions are answered in this section:

How does traffic congestion deteriorate freeway efficiency?

The most undesirable consequence of congestion is the result of the difference in driver behaviour while entering and leaving a congestion. It is observed that drivers maintain a larger headway when exiting a congestion than before breakdown; in other words, for the same distance headways, drivers prefer a lower speed and take longer during acceleration than that during deceleration (Hoogendoorn & Knoop, 2012). This difference in the microscopic behaviour, characteristic of a state transition, i.e. from congestion to free flow or free flow to congestion is referred to as traffic hysteresis. It is this non-equilibrium transition process that results in a capacity drop - a flow reduction of about 10-30% - characteristic of a traffic breakdown (Kerner & Rehborn, 1996). Such a capacity drop is often observed at freeway merging sections, upon activation of on-ramp bottlenecks. The drop in capacity from a congestion also implies a lower queue discharge flow, which further worsens the resolution of the congested state. Therefore, the mechanism of traffic breakdown, capacity drop, and resulting slower resolution of congestion, results in a substantial loss of freeway efficiency.

The potential of advanced application of information and communication technologies (ICT) in the field of road transport, including infrastructure, vehicles and users, and in traffic management, has been recognized in meeting the growing challenge of road congestion. Such ‘Intelligent Transport Systems (ITS)’ have
enabled better information provision, safer, more coordinated and smarter use of transport networks (Directive 2010/40/EU). Most advanced traffic management systems, such as, ramp metering (RM), dynamic route guidance, dynamic lane use etcetera have been designed to eliminate the causes leading to congestion. This thesis focuses on variable speed limits as a dynamic traffic management approach for freeways, which is motivated next.

Why would we want to regulate freeway traffic with variable speed limits (VSL)?

In practice, congestion is a common occurrence during high traffic load conditions, in spite of control systems that aim to manage road use. However, these strategies tend to regulate traffic on the sub-network in order to ensure an increased throughput on the freeways. In the early 80’s, researchers envisioned VSL as an innovative approach that could regulate the mainstream traffic. The full potential of VSL remains in its immediate response to the actual traffic situation on the freeway, to weather and daylight setting, and any other real-time circumstance. The three main advantages of speed control systems are:

1. VSL allow immediate intervention that can influence dynamics of the traffic nearest to the problem location
2. traffic can be managed while avoiding diverting or restricting access for unrelated streams of traffic
3. benefits from VSL can be realized at both microscopic and macroscopic levels - the harmonization effects on traffic speeds have shown to dampen disturbances from individual driver behaviour, and controlled application of speed limits is being explored to prevent and resolve congestion.

Even so, the only common application of VSL has been seen in incident management and near temporary road-works, and static speed limits remain the most widespread means of informing how fast users can drive on the road. Clearly, the potential of VSL to improve freeway efficiency is yet to be realized in practice.

What are the policy and practice related challenges in the adoption of VSL control measures?

The challenges in the widespread adoption of VSL systems are both technical and policy related. First major technical hurdle is the lack of generalized VSL strategies that are independent of specific infrastructure configuration and traffic scenarios. For instance, a recent approach is designed exclusively for stationary jams at infrastructural bottlenecks (Carlson et al., 2011). The transferability of such approaches to practice is then limited by the occurrence of the specific conditions, and the efficiency gains thereof.

Another important deterrent is the lack of complementarity of VSL approaches to the existing control systems. This means that different control measures are designed independently, which can deteriorate overall performance when these measures are deployed simultaneously.

RM is the most popular control measure used to regulate the traffic entering a freeway. On-ramp infrastructure offers access to traffic from the sub-network to enter the freeway at specific locations. RM control allows to restrict this additional flow from on-ramps to prevent traffic deterioration on the freeway. At the same time, on-ramp merging sections are potential bottlenecks; merging disruptions at ramp section can induce queueing in the shoulder lane as on-ramp demand increases (Cassidy & Rudjanakanoknad, 2005). These disturbances can propagate forward to result in a congestion downstream of the on-ramp. Therefore, on-ramps with RM are critical locations for potential activation of VSL systems as well.

Therefore, to facilitate the adoption of VSL approaches in the near future, their integration with other more commonly implemented control measures, and the validation of benefits from their synergic effects are crucial. Some recent works have demonstrated that integration of RM and VSL strategies can enhance the overall performance of the freeway (Carlson et al., 2010, Kotsialos & Papageorgiou, 2004, Van de Weg et al., 2014). However, no such integrated systems have been tested in the field yet. This is also due to their
computational complexity, given the capacity of the available systems.

Finally, a crucial policy-specific difficulty in using current integrated control systems is about achieving a compromise between regional benefits (dis-benefits) and large network-level gains. The consequence of RM measure is a faster growth rate of the on-ramp queue. Under peak traffic loads, this situation results in spillback of ramp queues onto the surface roads. While freeways are most commonly maintained centrally, the performance of surface roads and the adjacent lower network is managed by local (municipal) agencies. This explains that a spillback of on-ramp queues is highly undesirable for the local traffic managers. Since sub-networks commonly lack sophisticated traffic management systems, congestion aggravates faster, leading to a deteriorated performance and in a worse case, a network gridlock. For this reason, current traffic management policies in the Netherlands allow deactivation of RM under such conditions.

However, this policy can have adverse effects on an integrated control strategy involving RM. This is because a sudden deactivation of RM results in an abrupt flux of vehicles which may disrupt the control strategy active on the freeway. Therefore, the work attempts to investigate an integrated VSL and RM approach that can also prevent spillback of on-ramp queues to the surface roads. Such an approach will ensure improved efficiency on the freeway and the sub-network.

1-2 Research Scope

The scope and the context of this research is explained with the help of traffic flow deterioration process, illustrated in Figure 1-1. When the traffic intensity (flow) is near to the infrastructure capacity, the traffic state is meta-stable, such that traffic stability is ensured as long as a disturbance does not result in a breakdown. If a disturbance results in a congestion, two main adverse phenomenon deteriorate the freeway efficiency - capacity drop and queue spillback (Schakel & van Arem, 2013). Capacity drop implies a sub-optimal performance of the freeway, and a queue spillback on the freeway or at the on-ramp can block unrelated traffic streams. Both these effects aggravate the congestion, and increase travel time delays.

The integrated VSL and RM strategy will intervene directly at three operational points in the traffic deterioration process:

(1) RM control measure will regulate the entry of additional traffic from the sub-network, and hence, influence the total intensity on the freeway.

(2) the intended role of the VSL measure is to improve freeway efficiency.

VSL strategies can be preventive, such that speed-limitation avoids a potential traffic breakdown. Alternately, there are counter-active VSL strategies that aim at resolving a congestion that has already occurred.

In this research, a counter-active VSL approach will be employed that intervenes after a congestion is detected.
from a policy viewpoint, controlling the spillback of on-ramp queues to the surface roads was identified as important for practical suitability of VSL systems. Therefore, queue constraints will be additionally incorporated in the integrated strategy that will intervene to prevent spillback.

1-2-1 Focus Areas

With an understanding of the problem situation and the intended intervention with an integrated control strategy, the focus areas are described in further detail. This will help define the research boundaries within each of the research areas: VSL, RM and queue management, which are themselves extensive areas of research.

1-2-1-1 Macroscopic VSL measures

Speed control systems can be macroscopic or microscopic. Most current microscopic systems, like adaptive cruise control (ACC) and cooperative adaptive cruise control (CACC), aim to improve car-following tasks and safety. In such systems, each individual vehicle employs radar sensing, and additionally vehicle-to-vehicle communication in CACC, to locate the leader and adjust speed and acceleration accordingly. On the contrary, macroscopic systems use the aggregate traffic flow characteristics, like average flow, density and speed, to generate control advice. The control advice is typically displayed via variable message signs (VMS) mounted over roadside gantries in this case.

The scope of this work is restricted to macroscopic speed control measures. One major reason is the difficulty to implement microscopic traffic control strategies in practice. The limitations include the practical problem of insufficient penetration of in-car technologies, and the theoretical complexity of incorporating lane-changing behaviour in the design of traffic management systems.

1-2-1-2 Near-future implementation

The suitability of the designed approach for near-future field testing is an important consideration in this work. Therefore, the focus will be on developing systems that are computationally and technologically comparable to the existing traffic systems.

1-2-1-3 Local RM with queue regulation

Sophisticated approaches for RM consider coordination of multiple on-ramps to utilize the additional capacity and distribute delays effectively. However, the scope here is limited to local RM approaches at a single on-ramp merging section. Integration of coordinated RM strategies with VSL could be potential future extensions to this work.

The integration of RM control with VSL will focus on on-ramp queue regulation. This is because of the hierarchical management of freeway and urban networks that entails deactivation of RM control when the on-ramp queue spills back to the surface road. The subsequent release of the on-ramp queues substantially deteriorates the performance of the VSL system and therefore, the freeway.

1-2-1-4 Efficiency improvement for freeway and the sub-network

The objective of a control strategy can vary from improving safety, travel time, travel time reliability, or environmental impact. The goal of the integration strategy here is to improve the freeway efficiency while preventing performance degradation of the secondary network. The focus on on-ramp queue regulation is in line with this. The indicators used for measuring efficiency will be discussed in Section 1-4.
1-2-1-5 Simple test network

The test network will consider a simple merging section with a single lane on-ramp and a two-lane freeway section. This simple network is only a representation of more complex networks in reality. The focus of the evaluation will be to validate the expected behaviour of the control design which can be sufficiently examined with the proposed network. However, evaluating network effects of the integrated control measure requires a larger and more realistic network. Network effects will therefore not be considered.

1-2-2 Relevance

Most traffic control measures are typically designed and implemented stand-alone. However, managing traffic disruptions at a local level is not always the most efficient at a higher network-level. At the same time, various control strategies deployed locally can be mutually counter-productive. This gap is recognised in the concept of network-wide traffic regulation. The concept aims to benefit from utilization of storage capacity at locations other than the point of disruption, distribution of delays over a larger network, and the synergic effects from more coordinated control measures. This drives the network towards a system optimum. However, the first step towards realizing such a concept is the integration of the different traffic management measures currently being used or being designed for near-future implementation. The work in this thesis thus demonstrates how a widely-used traffic management measure, RM, can be integrated with a VSL strategy.

1-3 Research Objective

The potential of VSL to improve freeway efficiency, and the current barriers in the practical implementation of these systems motivate this research. We recognized that freeway on-ramp locations are bottlenecks where VSL can be beneficial in improving traffic efficiency. At the same time, RM is a more commonly deployed control measure at on-ramps. Therefore, integration of VSL strategy with RM is an opportunity to improve the practical suitability of VSL systems.

In this work, an integrated VSL and RM strategy will be developed and implemented in a traffic simulator. The aim is to test the functional performance of critical design aspects, and to inform design improvements from practical considerations. To that end, the main research question that guides the final outcome is: Can COoperative Speed Control ALogrithm (COSCAL v2) be integrated with ramp metering, in a way suitable for roadside and near-future implementation, to improve freeway efficiency and regulate on-ramp queues?

In order to answer this research question, the following objectives have been formulated for this research:

1. Explore the different theoretical and control approaches for variable speed limits systems, and for on-ramp queue control.
2. Develop an integrated VSL and RM strategy that improves freeway efficiency and prevents spillback of on-ramp queues.
3. Verify the functional correctness of the developed strategy by means of simulation.

1-4 Research Approach

The research approach involves three parts - a literature survey, theoretical development and simulation-based testing:
The literature survey is conducted for two main purposes. First, to understand the theoretical underpinnings of VSL from the available control approaches and second, to identify the desirable characteristics for the design of an integrated VSL and RM strategy. The focus areas identified in Section 1-2-1 guide the boundaries of the literature survey, which further informs of the design process.

In the theory development part, COoperative Speed Control ALgorithm (COSCAL) v2 algorithm for VSL will be adapted and extended to be integrated with a suitable RM approach. Compatibility of the theoretical approach to COSCAL v2 will therefore be important throughout the design process.

**COSCAL v2 algorithm for VSL**

COSCAL v2 is a macroscopic speed control approach based on shockwave theory, to resolve moving jams and hence, improve freeway efficiency. It is suitable for roadside deployment, and designed for multi-lane, heterogeneous traffic conditions. Additionally, COSCAL v2 and its microscopic counterpart COSCAL v1 are designed with transition to cooperative systems in mind. Both versions of the algorithm are compatible for roadside and in-car detection as well. This offers the advantage of leveraging faster and more accurate sensing via in-car technology, regardless of the penetration rates.

The theory will be built from a simplistic approach to a more sophisticated approach that relaxes some of its design assumptions. Two different approaches for integrating RM with VSL are proposed in the process:

**Basic approach for RM with COSCAL v2**

The theoretical formulation of the approach is macroscopic, with the simplifying design choice of constant RM flow during the activation of the VSL scheme. In this case, the approach does not explicitly consider any constraints for queue-length on the on-ramp. Thus, the RM rate must be the highest outflow required to prevent a queue spillback at any time.

In a situation that the VSL scheme crosses the on-ramp section, the adapted approach must ensure that the freeway flows arriving at the on-ramp section are reduced to accommodate the additional ramp flow. In other words, the higher the desired RM flow, the more stringent the VSL scheme must be to sufficiently reduce mainstream flow arriving at the ramp section. In effect, such a conservative integrated strategy reduces the efficiency of the VSL scheme. This is a major drawback of the basic approach, that is addressed in the advanced approach.

**Advanced approach for RM with COSCAL v2**

In the advanced approach, the goal is to design and integrate a more sophisticated RM approach with the VSL strategy. The RM strategy should dynamically respond to changing on-ramp demand, while ensuring a maximum queue-length limit to prevent spillback. The advantage here is that the on-ramp storage is better utilized, requiring less conservative RM rate.

For the integration of the VSL scheme with time-dependent RM flows, a predictive approach is considered desirable. In this case, RM flows are available over a prediction horizon and anticipatory decisions can be determined to (1) adapt VSL, and (2) ensure all necessary constraints are met in the future.

In the final part of this research, specific design aspects of the developed approaches are evaluated in VISSIM micro-simulation package. This mainly entails a qualitative analysis of the control behaviour observed as compared to that expected based theoretically.
1-5 Overview of the Report

Table 1-1 summaries how chapters are organized in this report; the third column provides the essence of the content in each chapter.

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Chapter 2

Literature Survey

Research studies in traffic management systems have shown novel ways to intervene at different operational levels with advanced controls, such as, route information systems, ramp metering (RM), variable speed limits (VSL), and individual lane guidance. These systems allow to manage road usage and improve the capacity of the network. In practice, they are often implemented stand-alone with the common goal to ease local traffic deterioration. However, the potential of integrated traffic control measures for improved traffic efficiency has been discussed in theory and practice (Papageorgiou et al., 2003). This chapter discusses the literature on freeway traffic control with three main objectives:

1. to survey the principle design and control approaches for dynamic speed control. The insights from this part are used to understand and apply traffic flow theory to the VSL strategy.

2. to review RM strategies with a focus on queue-management; the goal is to understand desirable features for an on-ramp queue regulator that can be integrated with COoperative Speed Control ALgorithm (COSCAL) v2.

3. to identify the most important considerations for integration of RM with VSL strategies, and specifically COSCAL v2

2-1 Introduction and Overview

VSL offer a responsive and flexible way to influence traffic dynamics, almost instantaneously. This is an important reason why speed control for improving freeway efficiency has received growing attention in the recent years. The additional advantage of speed control systems is the growing availability of variable message signs (VMS) on freeways, which offer ready infrastructure for deployment. Moreover, technological advances towards in-car systems offer the potential of even more precise implementation, and a richer data source which has been pointed out in some recent studies (Grumert & Tapani, 2012, Van de Weg et al., 2014). However, the full potential of speed limits has not been utilized in practice yet.

On the other hand, RM is considered as the most direct and efficient control measure to upgrade freeway performance (Papageorgiou et al., 2003). However, in keeping flow from entering the freeway, the queue on the on-ramp grows faster, i.e. RM and queue management are essentially counteracting. The propagation of the resulting ramp congestion to its sub-networks is usually prevented by deactivation of RM and discharge of the entire queue. The subsequent uncoordinated release of on-ramp flows can disrupt any mainstream
speed control. This stands as an obstacle in the implementation of other control strategies, as well as their integration with RM.

The Literature Survey is used to understand the challenges and the opportunities in the two control approaches, which then helps to identify the desirable characteristics for the integrated strategy. While conducting the Literature Survey, the following main considerations are central: resolving congestion, improving freeway efficiency, preventing a spillback of on-ramp queues to surface streets, compatibility of the RM and VSL approach, and suitability for implementation in practice.

This Chapter is structured as follows; first, VSL approaches are reviewed from two different standpoints - traffic flow theory related in Section 2-2 and systems control related in Section 2-3. While the theoretical aspects helps understand the design choices and their realised impacts, the control strategy is crucial for realizing expected performance in the field. Next, in Section 2-4, different queue management approaches are discussed. Further, different schemes for the integration of RM with VSL are presented in Section 2-5 and finally, the main conclusions important for the theoretical design of the control approach are presented in Section 2-6.

2-2 Theoretical Aspects of Freeway Speed Control

The direct impact of speed control on the freeway is reduced speeds. However, there are additional macroscopic effects like cumulative flow and density changes, speed and flow differences between lanes, and microscopic effects like speed differences between consecutive vehicles. These effects are the consequence of not only the magnitude of speed decrease, but also the dynamics of the control procedure. When developing a speed based traffic regulator, two dynamic choices have to be made: (1) the spatial extent over which the control is applied and changed over time, and (2) the value of applied speed limits. As an example, variable speed limit values could be applied over a fixed length of freeway in one case or a fixed speed limit over varying segments in another. The impacts of these choices are non-trivial for the achieved efficiency and are the focus in this section.

In the earliest works on traffic control using VSL, Smulders (1990) explains two possibilities to avoid congestion, either by removing the sources of disturbances (increasing homogeneity) or by reducing shorter headway (increasing stability). Hegyi et al. (2008) later embodied these principles into two analytically different approaches towards speed limitation: one utilizing the homogenization effects from decreased speeds, and the other using flow reduction for preventing traffic breakdown or resolving a prevailing jam. The approaches are detailed in the following sections.

2-2-1 Speed Homogenization Approach

If the speed limits used are above the critical speed, i.e. the speed at the critical density with maximum flow, speed limitation is understood to have a homogenization effect (Smulders, 1990). The fundamental principle involves slowing down the faster driving vehicles without limiting the speed of the slower traffic. This reduces speed differences, and the need for acceleration and braking manoeuvres. Hence, by keeping the speed above the critical speed, lower than the free flow speed and only slightly lesser than the average speed, speeds are better homogenized (Hegyi et al., 2008).

Smulders (1990) used this approach, founded on contemporary work by van Toorenburg (1983), in a macroscopic traffic flow model based optimization that maximized time to congestion and traffic throughput to determine the switching time for control. The work attributes the reduction of small time headways (<1s) in the faster lane as most important to the homogenizing effect. Alessandri et al. (1999) used the same speed regulator, maximizing a flow cost function based on an alternate traffic model and optimization technique to demonstrate a slight improvement in efficiency. The improvement was theoretically attributed to the increased critical density at lower average speed.
2-2-2 Flow Reduction Approach

The flow reduction approach is central to improving freeway efficiency. This follows from the understanding of how a jam is resolved; when the inflow into the jam reduces below its outflow the jam state diminishes over time. Similarly, if the flow into a bottleneck is reduced sufficiently, a capacity drop can be prevented at the bottleneck. Therefore, by using speed limitation to achieve lower flows a maximum capacity flow can be maintained on the freeway.

Flow reduction from speed limitation can be achieved in different ways, depending on the value of the applied speed limits. For speeds lower than the critical speed, reduction effects additionally depend on the traffic demand. These mechanisms will be summarised after a discussion on the fundamental impacts of how speed limits are imposed:

- **Stationary speed limits.** Holds for over-critical VSL in all inflow conditions, and for under-critical VSL in low inflow conditions.
- **Instantaneous speed limits.** Direct flow reduction in all inflow conditions.
- **Time-varying outflow from VSL over a freeway length and time interval.** Holds in low inflow conditions. Gating effects result in different flow reduction mechanism in high inflow conditions.

**Figure 2-1:** Effects of VSL application dynamics, value of speed limits and inflow condition
2-2-2-1 Dynamics of Imposing Speed Limits

The dynamics used in the SPEed Controlling ALgorIdhm using Shockwave Theory (SPECIALIST) algorithm emphasize on how the application of the speed limits - regardless of the value of the speed limit itself - influences the traffic flow dynamics (Hegyi et al., 2008). This difference is exploited in this algorithm to serve two main objectives with speed control. The first is employed for jam resolution, while the second is used to create an additional buffer space on the freeway that can store the speed limiting vehicles at a higher density than achievable without control. Essentially, the differences translate to unique flow and density consequences for the outflow from the speed-limited area.

The different possibilities for application of VSL can be categorised between the two extreme cases, namely instantaneous and stationary application of speed limits. Moving fronts, wherein the head and the tail of the speed limited area are continuously changed over time, at a chosen speed, comprise all intermediate possibilities. Their impact on the traffic state can be more easily understood by visualizing one vehicle following the other at the same speed, maintaining a fixed headway. With this hypothetical scenario as the basis of the explanation, the three possibilities: instantaneous application, stationary speed limits and moving fronts for the control area are detailed.

- Instantaneous application of speed limits
  In the case that the two vehicles are subjected to speed limitation at the same time, both would simultaneously adjust to this lower speed, from their original free flow speed, without changing the spacing between them. The implication is that there’s no impact on the density from application of speed limits itself. However, since the speed is reduced, these vehicles would take longer to cross an arbitrary downstream location as compared to the case without speed limitation. The result is a reduced flow, as illustrated in Figure 2-1b. On the fundamental diagram, this can be understood with a vertical line, corresponding to a given density. Now, this density line crosses the speed limit line (a line from the origin at a slope equal to the applied speed limit) at a lower flow value compared to the free flow branch, indicating a reduction of flow Figure 2-1b.

- Stationary speed limits
  Stationary speed limits refers to point implementation of speed control, e.g. at a single gantry, for a given time interval. In keeping the location fixed over time, a time difference between when the vehicles enter speed limits is effectuated. This is because a following vehicle would cross a fixed location at a later time than the leader. This time difference in the application of speed limits on consecutive vehicles, results in a change (increase) in density downstream of the controlled area. The important consequence of stationary speed limits is that flow is conserved at the boundary. However, Papageorgiou et al. (2008) hypothesizes a VSL triggered temporary reduction in flow, during the period of transition to the new, higher density state. This can be understood from Figure 2-1a and is the theoretical reasoning utilized in modelling the control approach (Carlson et al., 2011) under low arrival demand conditions.

  The author understands that when VSL below the critical speed are applied, the resultant free flow branch crosses the congested arm of the fundamental diagram. In this case, the flow reduction is not indirect always, and is conditional on the demand flow. For higher inflows, above the flow at the cross-over point, the reduction effect is direct. The flow in this case is reduced to the flow value at the congested state for the applied speed limits. For lower inflows, the flow reduction is indirect.

- Moving fronts for application or release of speed limits
  Time varying location of the head and tail of the speed control area are referred to as moving fronts. By changing the speed of these fronts over time, the speed limited section can be leveraged to regulate traffic flow and density. When the tail of the control section propagates upstream, the speed limits apply to the following vehicle at a later time compared to its leader. In doing so, the following vehicle drives at a higher speed while the leader is already speed limited. This diminishes the spacing between the two vehicles to achieve a higher density in the process of speed control. The time lag in
speed limit application to the vehicles determines the realized density; the higher the lag, the greater the resultant density. Just as time difference in speed limitation can be exploited to achieve different densities inside the controlled area, a similar logic can be translated to the vehicles leaving this area. The head of the controlled section can be allowed to propagate upstream at varying speeds; the faster the propagation speed (more negative), the higher is the resultant flow downstream, i.e. flow leaving the section.

2-2-2-2 Implication of VSL Dynamics for Flow Reduction Approaches

The mechanism of flow reduction differs based on the dynamics of imposed speed limits, and was differentiated as direct and indirect flow reduction. Direct flow reduction results when the density is conserved in the new traffic state on application of VSL; a reduced speed then results in a lower flow. Indirect flow reduction occurs from a flow inefficiency, typically attributed to the transition period, wherein traffic state changes to a higher density state at the same flow value when speed-limits are applied; the phenomenon becomes clear in Figure 2-1a.

Further, it is understood that flow reduction can be achieved directly with instantaneous application of speed limits, for all speed limit values above and below critical speed. Alternately, stationary speed limits result in an indirect reduction in flow in most cases. This is true when speed limits are applied (1) at over-critical speeds, and (2) at under-critical speed-limits in low demand condition (lower than the congestion flows at that speed). While moving fronts for application and release of speed-limits can result in both an increase or decrease in traffic flow based on the speed of head, tail and the state of traffic under speed-limitation; this flow variation is essentially direct due to changes in traffic density. Stationary speed limits can also result in a direct flow reduction, only when applied with sufficiently low speed limit values. These are VSL values that induce a capacity flow lower than the average freeway demand. When this holds, the speed limited area holds up the excess, to allow only the capacity flow to exit downstream. Hegyi (2014) refers this approach as ‘gating’ and Carlson et al. (2011) uses this aspect to create a controlled congestion upstream of a fixed bottleneck. Additionally, the author recognises that in case of speed limits, as low as 40 km/h to 20 km/h, any gain in critical density (and hence, capacity) is likely to be exceeded by the reduction in flow from a lower speed. Therefore, the resulting outflow is lower than without speed control for such cases.

![Figure 2-2: Effects of VSL dynamics on the fundamental diagram.](image-url)
2-2-3 Fundamental Diagram and Effects of VSL

A well-founded understanding of the effects of VSL control on the fundamental diagram (FD) is important for selection of appropriate speed limits, and for heuristic approaches that are otherwise based on arbitrary desired values of traffic state variables. It also helps to develop more effective control strategies whose impacts can be anticipated qualitative without simulation-based-analysis.

The impact of VSL on aggregate traffic flow, and most importantly the critical values in the macroscopic FD: critical density and capacity flow, are not well evidenced in empirical data. This is because of: (1) the difficulty to ensure comparable conditions for with (after) and without VSL(data used in ex-post analysis, (2) the difficulty to obtain sufficient speed-flow data across all occupancies under VSL and (3) difficulty to validate that the observed impacts are from speed control, independent of local infrastructure and driving characteristics.

Papageorgiou et al. (2008) in their important work to empirically validate the effects of VSL, presented some evidence for an increase in critical occupancy for under-critical speed limits. However, they confirmed no conclusive impact on the flow-capacity (this aspect is used in Alessandri et al. (1999) to motivate an increased efficiency from homogenization approach). The work also surveys some of the more influencing notions of aggregate traffic behaviour under speed control.

A general hypothesis based on the literature surveyed and the author’s understanding is summarised below and will be considered while formulating the control strategy in this research:

- When speed limits are applied on free flowing traffic, the free flow branch shifts to a slope equivalent to the effective (average) speed from speed control. The effective speed can be lower or higher than the applied speed limits depending on whether the speed limits are mandatory or advisory, respectively, and on the level of enforcement. Jonkers et al. (2011) report a difference in applied and realized average speed from a VSL field-test results. In addition, this phenomenon is being studied in simulation as varying levels of compliance (Hellinga & Mandelzys, 2011).

- Papageorgiou et al. (2008) hypothesizes a positive shift in the critical density from speed limitation. The work proposes that FD under speed limitation crosses that without control, close to or at a slightly higher density than the critical density of the original flow-density curve. This was validated with some empirical evidence.

- Reduction in flow is indirect during state transition to a higher density—when stationary speed limits are imposed at over-critical speeds (Figure 2-1a). The flow drop is proportional to the magnitude of speed reduction; the higher the reduction in speed, the greater is the flow reduction and the longer it takes for the state transition.

- When stationary speed limits below the critical speed are applied, the resultant free flow branch crosses the congested arm of the original curve. The flow reduction is therefore, not indirect in all cases and is conditional on the demand flow. For inflows above the flow at the cross-over point, the flow reduction is direct due to gating effects. For lower inflows, the reduction is indirect.

- Flow reduction from instantaneous application are achieved from the time of application to the time that the last speed limited vehicle leaves a given downstream location, illustrated in Figure 2-1b. The reduction is proportional to the decrease in speeds but is observed for any speed-limit values.

2-3 VSL Control Approaches

The objective of this section is to identify the desirable properties of a speed control system for this research. The surveyed literature on available VSL approaches can be classified into three main categories:
heuristic, regulatory, and optimization based controls. The categorization highlights the trade-off between effectiveness (optimality) and the computation and data requirements of different approaches. It also highlights the lack of effective and easily implementable non-heuristic speed control approaches in practice.

### 2-3-1 Heuristic Strategies

Heuristic strategies use occupancy, speed, flow values or a combination, as threshold for activation and deactivation of control. More advanced heuristic approaches employ decision-tree based thresholds, and are understood as effective for field implementation (Allaby et al., 2007, Waller et al., 2009, Li et al., 2014a).

Such approaches can be offline or online. Offline approaches use historical time and day data (Waller et al., 2009). This consists of demand profile and aggregated speed and flow data, collected over considerable time for the control area. The data serves as a proxy for the actual traffic situation on which control decisions are based. Such an approach is an option for fixed infrastructural bottlenecks and daily peak-hour condition but is seldom used in practice. This is because of the obvious drawback that such a system cannot respond to real-time occurrences and factors like weather, incidents and driver-induced disturbances. Hence, they cannot be designed to respond to non-recurrent congestion.

Control decisions in online strategies are based on real-time data, collected from traffic sensors like loop detectors, video based recordings, and more recently, from in-car devices. Waller et al. (2009) evaluated an online and offline algorithm in a simulation-based study. The results showed an improvement in safety but non-significant increase in throughput from speed control.

In their work, Papageorgiou et al. (2008) critique the ad-hoc nature of speed and occupancy thresholds used in heuristic control approaches. Not just do these approaches necessitate location based tuning, but also, frequent online tuning for both seasonal and long-term changes in traffic patterns. However, the ease of implementation, makes heuristic strategies most common in practice. VSL strategies applied on the E4 motorway in Stockholm (Nissan & Koutsopoulosb, 2011), M25 motorway in the UK (dep, 2006) and German Autobahns (Weikl et al., 2013) are all heuristic. Field-results of these approaches concur on safety improvements from VSL strategies. However, no significant improvement in flow-capacity is evidenced. In fact, Weikl et al. (2013) report a higher capacity drop with VSL than without, and conclude that there is a trade-off between capacity gains and speed homogenization effects. In summary, heuristic approaches are easily implementable but efficiency improvements from these strategies are not sufficiently known.

### 2-3-2 Regulatory Strategies

Regulatory strategies are designed to achieve a predetermined traffic state, by using desired values for flow, occupancy or speed as design parameters. The variation of the measured traffic data from these design values or set-points, is used to determine the speed control decisions. These set-points are chosen to drive the system to an optimal performance. However, to ensure maximum efficiency they usually require fine-tuning post-implementation.

These strategies can be feed-forward, in which case the freeway state measurements are used to generate a one-time control scheme that does not consider the response of the system to the control (Hegyi et al., 2008). Alternately, in more sophisticated feedback approaches, the control scheme is calculated repeatedly based on the divergence of the online measurements from the target state. MTFC-VSL (Carlson et al., 2011) and COSCAL v2 (Hegyi, 2013) are two such recent approaches that have been designed to improve freeway efficiency. Additionally, these approaches are computationally suitable for practical implementation with significantly positive results in simulation (Weg & Hegyi, 2014, Carlson et al., 2014).

For the direct relevance of these approaches to the research objective, the Mainstream Traffic Flow Control (MTFC)-VSL and COSCAL-v2 are studied in detail.
2-3-2-1 Mainstream Traffic Flow Control (MTFC)-VSL

Mainstream Traffic Flow Control via Variable Speed Limits (MTFC-VSL) has been an influential control approach in the recent years. First designed as a sophisticated optimal controller (Carlson et al., 2010), it was later reformulated to a simpler feedback approach because of the practical limitations of implementing it in the field. MTFC works on the principle of regulating mainstream flow upstream of a bottleneck, by creating a ‘controlled congestion’ that can achieve an outflow equal to the flow capacity of the bottleneck. The design principle uses the controlled congestion to prevent an uncontrolled congestion that would have otherwise resulted in a capacity drop at the bottleneck. Therefore, the approach derives throughput improvement from three main aspects: (1) preventing a capacity drop, (2) limiting the spatial-temporal extent of uncontrolled congestion, and (3) speed improvement within the controlled congestion; with speeds above jam speeds.

 Principally, MTFC-VSL uses a cascade control approach, with two controller loops arranged such that the primary (outer) loop controls the set-point of the secondary (inner) loop. Here, the secondary loop regulates the outflow from the controlled congestion area towards a desired flow value provided by the primary loop. An integral controller achieves this by determining suitably low speed limits, using the error in the achieved outflow as a feedback input. Further, the primary loop uses a proportional-integral (PI) controller, in which the fluctuation of the bottleneck density from a predetermined critical value provides a feedback input. In short, the primary loop monitors the density fluctuations at the bottleneck to provide the desired outflow value from the controlled congestion area. The secondary loop then determines the appropriate VSL value based on the divergence of the actual outflow from this desired value. From control engineering fundamentals, a proportional control is a linear feedback that responds proportionally to an error, while an integral controller reacts proportionally to the integral of the error term (add wiki ref).

Note, the critical density or occupancy is reflective of the bottleneck capacity. Densities near capacity drop are empirically known to show little variation as compared to flow (Chung et al., 2007). Hence, the author concludes that the primary loop should have a stabilizing effect on the secondary.

2-3-2-2 COoperative Speed Control ALgorithm (COSCAL) v2

Hegyi et al. (2008) in their work used shockwave theory to design a theoretical approach to resolve jam waves (1-2 km long travelling congestion that propagate upstream). The approach uses moving fronts for application and release of speed limits, and applies a fixed speed limit value over a dynamically changing length of freeway. In spite of conclusive results of its effectiveness in a field-experiment in the Netherlands (Hegyi & Hoogendoorn, 2010), the algorithm had an inherent drawback from a feed-forward structure. With the growing potential of cooperative systems (based on in-car detection and actuation), the conceptual framework of SPECIALIST was developed to a feedback, fully cooperative system - with assumptions of 100% penetration, single lane with no overtaking behaviour and single vehicle class - at TU Delft in cooperation with UC Berkeley (Hegyi et al., 2013). Most recently, a more realistic version of this algorithm, COSCAL v2, which considers low penetration rates of in-car devices, combined roadside and in-car deployment, multiple lanes and user class has been formulated (Hegyi, 2013).

The design objective of COSCAL v2 is to resolve a moving jam by reducing the flow entering it below the outflow from it. Once the jam is resolved, the head and tail fronts of the speed-limited area are manipulated in a way that a desired flow is recovered after. These moving fronts enable a compaction mechanism, such that the freeway itself is utilized as a buffer space to hold vehicles at a high but stable density. Essentially, this allows to lower the flow entering the jam without creating another jam upstream of it.

2-3-2-3 Discussion on MTFC-VSL and COSCAL v2

In this part, the author contrasts the two strategies and highlights the takeaways relevant for this research. Both, MTFC-VSL and COSCAL v2, are non-heuristic approaches suitable for practical implementation
that stress on the effectiveness of VSL to improve freeway efficiency. The functional similarity is that both approaches use a flow reduction aspect of VSL.

However, MTFC-VSL uses flow reduction to prevent a capacity drop from congestion, and COSCAL v2 is a counter-active measure deployed when a jam is detected. The author would like to add here that COSCAL v2 could be adapted to prevent breakdown at an infrastructural bottleneck. This would require an alternate actuation mechanism (than jam detection) and suitable tuning of the controller parameters. Moreover, a primary control loop similar to MTFC-VSL could be employed to regulate this desired flow in real-time.

The flow reduction approach used in these strategies also differs. MTFC-VSL primarily uses a gating technique, as discussed under stationary speed control measures in Section 2-2-2-1. In addition, fundamentals of temporary flow reduction are used for low demand conditions. On the other hand, COSCAL v2 uses instantaneous application of speed limits to reduce the flow entering a jam. The downside of the former approach is the state of the speed-limited area, referred to as a ‘controlled congestion’; gating approach creates a congested state within this area, even though it is limited in extent. In contrast, the dynamics of speed-limitation are leveraged in COSCAL v2 to ensure a free flow condition before and after the jam is resolved. The author recommends that this aspect is favourable from the point of view of efficiency, and safety as well.

Overall, the limitation of either approaches is their specific use case - while one prevents capacity drop at an infrastructural bottleneck, the other resolves moving jams in particular. A generalised solution for using VSL to prevent or resolve congestion on the freeway remains a challenge for such simpler strategies that do not use elaborate traffic models.

2-4 Ramp Metering (RM) - Queue Management

RM is used as access control for the freeway, the underlying objective being to improve freeway efficiency by limiting the entry of vehicles from the secondary access points. The impetus to integrate RM with VSL strategies is to avoid degenerative effects from uncoordinated implementation of the control measures. One of the main reasons is the result of limited storage capacity of ramp infrastructure. The spillover of on-ramp queues to the surface streets necessitates queue control measures that adversely affect VSL strategies. Therefore, this section focuses particularly on the current state of queue management approaches used in RM strategies, in practice and in research. Before that, the different RM strategies themselves are discussed briefly in the next paragraphs.

Papageorgiou & Kotsialos (2000) and Zhang et al. (2001) offer a complete overview and categorization of the available RM strategies. The former distinguishes the approaches from a control and effectiveness perspective as, fixed-time, reactive and optimal ramp-metering. While, the latter categorizes them from an implementation standpoint as, isolated and coordinated strategies.

Papageorgiou & Kotsialos (2000) identifies the use of historical data for demand estimation as the main drawback of fixed-time strategies. In doing so, the demand is assumed constant, when in reality it varies within the time of a day, and between days. Hence, they cannot predict non-recurrent disturbances and long term changes in demand.

Reactive strategies are described as a tactical control measure based on real-time traffic measurements. Their aim is to keep the freeway traffic state at prescribed target values. Two such principal approaches - demand-capacity and Asservissement linéaire d’entrée autoroutière (ALINEA) - are discussed in detail in (Smaragdis & Papageorgiou, 2003). However, both of these are local strategies, using only the traffic measurements closely downstream of the on-ramp as control input. This is addressed in METALINE RM approach by using all available freeway measurements, to calculate RM rates for all adjacent controllable ramps. The control formulation is based on ALINEA local RM approach and hence, can be understood as its generalization (Papageorgiou & Kotsialos, 2000).
The most sophisticated control strategies are proactive and use forecasting models to predict freeway traffic conditions and disturbance propagation. The advantage of these type of controls is that they allow optimal coordination and strategic allocation of infrastructure, with the knowledge of traffic evolution over a sufficiently long time horizon. In spite of the explicit advantage of these strategies to dramatically improve freeway efficiency, they cannot yet be implemented in practice because of real-time computational demand. Also, practical effectiveness in such controls is contingent on performance deterioration from prediction errors, and more fundamental model-versus-reality mismatches (Papamichail & Papageorgiou, 2008).

### 2-4-1 Rule-based Queue Management

When the freeway condition aggravates due to increasing traffic demand, fixed-time RM strategies fail and reactive RM strategies tend to lower the metering rates. At the same time, it is realistic that when the traffic on freeway is at a peak, the demand at the on-ramp is high as well. Then, the intensified RM makes the on-ramp queues grow faster, making queue management necessary. Such growing queues are mostly detected by a queue detector placed at the entrance of the on-ramp.

In a rudimentary queue management strategy, the occupancy measurement from the queue detector is used as a measure of the queue length on the on-ramp. The strategy entails deactivation of the local RM in order to disperse the on-ramp queue when a pre-set occupancy threshold is reached (Gordon, 1996). This approach is also referred to as the ‘queue-flush’ strategy and is commonly employed in practice.

In a nutshell, a higher freeway flow orders a lower ramp outflow, which in turn fastens the queue growth leading to a breach of the control threshold, and a subsequent activation of the queue-flush policy. Since the freeway state is likely to be near critical when this happens, a traffic breakdown is probable. Therefore, the author would like to argue that the outcome of this policy is conflicting with the primary objective of RM itself. Moreover, it appears that RM and queue management are intrinsically competitive which can lead to oscillatory switching between the two measures. Besides, the fundamental downside in this approach is that on-ramp demand or occupancy give only a rough approximation of queue dynamics. Additionally, counting errors from loop detectors would make such strategies sub-optimal.

In another rule-based approach, Jiang et al. (2012) uses a queue-length threshold that activates and deactivates to the same threshold value. Upon activation, the strategy proposes incrementing the metering-rate proportional to the amount by which the queue overshoots its target length. Moreover, it uses a minimum speed threshold of 45 km/h for the freeway; when the average speed is measured below this value, the freeway performance is given priority by switching off the queue regulator. The work demonstrates that any queue-management strategy, sophisticated or simply heuristic, would not deactivate by itself in dense traffic conditions. Therefore, a deactivation strategy for queue-management strategies is required, all the more when RM is integrated with another mainstream control. A complementary control approach that can improve the buffer space on the freeway can also be effective in increasing the duration of queue control, without deteriorating freeway performance.

### 2-4-2 ALINEA/Q and PI-ALINEA/Q

One of the variants of a local RM strategy ALINEA, called ALINEA/Q, incorporates queue management (Smaragdis & Papageorgiou, 2003). The controller uses the vehicle conservation equation describing queue dynamics in order to determine the ramp outflow required to achieve a desired queue-length in the next time step (in control theory called a dead-beat controller that drives the system to steady state in smallest number of time steps). The queue regulator overrides the RM control only if the ramp flow it requests is higher than that estimated by the RM control. This queue-override policy allows optimal utilization of the freeway under free flow - low demand conditions. To elaborate, when the freeway demand is low, RM orders a large RM rate while the queue regulator order a low ramp flow, in order to achieve the desired queue length. Since the greater of the two flows apply, RM decision supersedes to maximize freeway performance.

In order to define the queue dynamics in a subsequent time step, the on-ramp inflow in that time step must be known. ALINEA/Q overcomes this issue by using the inflow in the previous step as an approximation.
for the following. Alternately, Spiliopoulou et al. (2010) uses the same queue-management approach with PI-ALINEA and employs a one-step demand forecast using linear exponential smoothing. PI-ALINEA is an extension of ALINEA designed for distant bottlenecks (Wang et al., 2010). Essentially, the usefulness of this queue-management methodology is its compatibility to most local RM approaches and easy implementability in practice.

### 2-4-3 Queue Management Aspects in Comprehensive Controls

Rule-based coordination strategy HEuristic Ramp-metering coOrdination (HERO) coordinates multiple on-ramps that use ALINEA algorithm for local RM. In this algorithm, the higher level coordination between ramps, when necessary, is achieved by considering a minimum queue condition for on-ramps (called slave ramps) upstream of the critical merge area (Papamichail & Papageorgiou, 2008). The coordination decision itself is based on a relative queue ratio (actual queue length divided by the maximum desired length) for the master (critical) on-ramp, and the freeway density measurements at a downstream segment. The coordination is activated when the relative queue exceeds a threshold and the freeway density is close to critical. Therefore, by maintaining a minimum queue at multiple on-ramps, more space is made available on the freeway. Then, this allows more vehicles to enter from the master ramp. Additionally, to ensure equity, comparable queue lengths are kept on the slave ramps. This is achieved by updating the minimum desired queue length for every ramp in each control cycle.

Based on Papamichail & Papageorgiou (2008), two core insights relevant for this research have been identified below:

- Maximum efficiency benefits can be achieved by enlarging the storage space nearest to the critical location where freeway deterioration initiates. In this work, the storage space on multiple slave ramps is used to allow a longer metering time for the master ramp closest to the bottleneck.

- Typical queue-management strategies can lead to under-utilization of the ramp infrastructure. This unused storage could otherwise be distributed for better network efficiency.

Another network-wide RM approach, Advanced Motorway Optimal Control (AMOC), provides an ideal open-loop solution using a macroscopic model-based optimization. The approach is formulated under the assumption of known ramp demand and off-ramp exit profiles. The application of the control approach on the Amsterdam ring network, in simulation, demonstrated high levels of efficiency improvements (Kotsialos & Papageorgiou, 2004). The results highlight the potential of optimal predictive control, attributable to the timely prognosis of congestion and anticipatory activation of control in these approaches. The optimization uses a minimization criteria for total time spent (TTS), including the waiting times on the on-ramp. Additionally, a penalty (quadratic term) for the fluctuations in the control output and another for the queue length itself (to maintain a minimum queue when desired) are used.

This approach meets the favourable aspects of the HERO algorithm and above that, distributes delays over on-ramps and the freeway equitably. The results also suggest a significant improvement in TTS from increasing the on-ramp storage (nearly 10 percent decrease in travel time from increasing ramp storage from 40 to 80 vehicles).

The desirable characteristics of AMOC can be pointed out as:

- The assumption of a known demand and turning-ratios for the ramps can be useful for developing an anticipatory control approach. Such an approach can predict a traffic disruption well in advance, and initiate control suitably.

- Efficiency of AMOC was found to be sensitive to the on-ramp storage capacity. The author understands this as an important infrastructural aspect that is often limited by spatial design specific to different locations. Hence, sensitivity of the designed strategy to the ramp storage is an important evaluation criterion for implementing an approach in practice.
2-5 Integration of VSL and RM

This section focuses on the coordination of a VSL strategy with RM and a queue regulator. First, three different strategies are discussed here and the most relevant aspects are identified for each. The insights are later used to identify the desirable design characteristics for such systems.

Carlson et al. (2012) integrate MTFC-VSL with PI-ALINEA ramp metering control using a split range controller. In this approach, the controller output of combined flow, from the speed limited area and the on-ramp, is used to determine the input for both the control measures. The design policy prioritizes RM as the preceding control, such that the VSL system is activated either upon the activation of ramp queue-management or when RM orders a flow value below its lower limit. The latter situation occurs when the freeway condition is so dense that the metering rate requested is lower than the minimum required.

The design choices of RM as the first control measure and the actuation criteria for VSL have some implications. First, if the freeway demand increases after the start of the queue-management strategy (and hence after VSL), then the speed limit value would continue to decrease to keep the queue regulated. Essentially, this could necessitate extremely low (near-zero) VSL values. Second, there is likely to be a cumulative demand (freeway plus on-ramp) for which the integrated control is not sufficient to prevent a capacity drop at the bottleneck or a queue spillback. With the knowledge of these extreme conditions, over-ruling activation and deactivation decisions can be specified. Both these considerations can improve the design of an integrated control strategy.

In an alternate coordination approach, Lu et al. (2011) combines a similar VSL logic with a Coordinated Ramp Metering (CRM) strategy. The VSL approach creates a regulated speed limited area upstream of the discharge section of an infrastructural bottleneck. The discharge section allows for the necessary acceleration required for the vehicles to be able to achieve a desired speed before they arrive at the bottleneck. Further, the design policy is to estimate the VSL control before evaluating the on-ramp flows. In each time step, first the VSL value in the control area is chosen such that the discharge section flow matches the downstream bottleneck capacity. The VSL value is based on the freeway flow, the on-ramp demand and storage space, and the variations in speed allowable for safety considerations. Subsequently, a Model Predictive Control (MPC) is used to compute ramp flows that minimize the difference of total travel time and total travel distance; this objective function improves the throughput until the margin cost of adding more vehicles does not exceed the additional travel time gain from them.

The advantage of employing an MPC is that it can optimize the system by coordinating the ramps, given the VSL scheme. Additionally, it can consider the state over a larger freeway state and hence, compatible for a network level control. However, the approach does not explicitly include queue constraints for the on-ramp.

Similarly to the previous two methods, Li et al. (2014b) proposes an approach to prevent capacity drop at a downstream bottleneck section. The approach uses reactive strategies for both, VSL and RM. RM flows are first determined with X-ALINEA/Q, after which, a logic tree type VSL algorithm, based on real-time bottleneck flow and occupancy measurements, determines the speed limits. Meanwhile, queue length is checked at each time step, which if exceeds its prescribed value, the queue regulator is switched on. In the case that the queue regulator orders a flow higher than the ramp controller, the queue control overrides and the VSL scheme is recalculated for this increased ramp outflow.

The rule-based formulation of the VSL strategy makes it possible to recalculate the scheme when necessitated by the queue regulator. This brings forth an important consideration for the integration of VSL and RM with queue management. Integrated strategies in which the VSL scheme is generated before the RM, the queue management decisions require the VSL scheme to be adapted in the case of a queue-length violation. However, this may not very feasible for more sophisticated approaches.
2-5-1 Advantages of an Integrated Control Strategy

From the discussion in this chapter so far, the following core advantages of integrating RM and VSL have been understood:

- Integration of RM and VSL is expected to improve the performance of speed control against disruption from ramp flows.
- Integration of control measures increases useful storage capacity of the network that can be allocated more effectively.
- VSL control on the freeway can improve RM performance - by regulating freeway traffic with VSL, higher flows can be allowed from the on-ramp. Then, higher ramp flows can prevent a spillback for a higher range of total on-ramp and freeway demand. In the case of COSCAL v2, jam waves are resolved to restore a capacity drop, that allows for higher RM flows.
- Additional consideration of ramp queue constraints can prevent employment of a ‘queue-flush’ strategy in practice while VSL control is still active.

2-5-2 Recommendations for the Design of an Integrated Strategy

Given the advantage of integrating RM with VSL control, some recommendations for the design of an integrated strategy are assimilated. The desirable characteristics are identified for coordination of the control strategy with a queue regulator:

- On-ramp queue control ensures that the queue does not exceed a desired maximum value. At the same time, it should not result in an under-utilization of ramp storage space. Therefore, a minimum queue criteria should be included in the design of the queue regulator.
- Using two control measures to regulate the freeway state offers an additional degree of freedom. This requires making design choices such as: (1) the conditions under which the control measures are activated, (2) the restrictions that result in their deactivated, and (3) condition for reactivation when one of the controls is deactivated temporarily.
- A queue regulator should include deactivation criteria that depends on the freeway condition. In the situation that preventing a spillback on the urban network deteriorates the performance of the freeway traffic, the trade-off should be considered.
- In typical feedback controllers, when the input variable overshoots its desired set-value by a large magnitude, a significant error accumulates in a given direction. The control output continues to be driven in that direction, for a significant amount of time, until the error is compensated (unwound) in the opposite direction. The resulting lag in response, due to the slow unwinding process, is referred to as "wind-up effect". This should be avoided by bounding the control variables within a maximum and minimum value.

2-6 Summary and Discussion

In this literature survey, two freeway control measures, namely variable speed limits (VSL) and ramp metering (RM) were studied. The research objective was to integrate RM with COSCAL v2 to improve freeway efficiency, for which "resolving congestion, improving freeway efficiency; preventing a spillback of on-ramp queues to surface streets, compatibility of the RM and VSL approach, and suitability for implementation in practice" were the key criteria. Three main objectives were identified for the literature review,
which are briefly answered here.

The first objective was to survey the principle design and control approach for VSL. Speed homogenization and flow reduction were identified as the two main theoretical approaches to designing VSL strategies. Flow reduction approaches were found to be more suitable for improving freeway efficiency. Further, two main dynamic choices - the spatial extent and the value of applied speed limits, and their implication on the realized traffic state were discussed elaborately in Section 2-2-2-1. This offers a framework to anticipate the effect of the design of the VSL strategy on the traffic state.

From a control perspective, reactive controllers have the advantage of straightforward implementation, computational affordability in view of present day control systems, and near-optimal effectiveness if designed properly. Since these controllers are largely regulatory, i.e. the control is determined to drive the system towards a pre-determined desirable state; the choice of the pre-set parameters is found important to achieve desired performance. In comparison, the advantage of model-based optimization methods is not just solution optimality, but also, the possibility of superior coordination at the network level. Currently deployed reactive systems are therefore limited because of their stand-alone design. In order to improve reactive control strategies, integration of different control systems in a way that advantages from their synergic effects is required.

Further, COSCAL v2 was compared to a contemporary reactive VSL strategy – MTFC-VSL, in Section 2-3-2. While COSCAL v2 employs speed limits to resolve a jam and recover capacity drop, MTFC-VSL uses it to prevent capacity drop at infrastructural bottlenecks. Even though both approaches improve freeway efficiency, the theoretical principle used differs. A downside of the MTFC-VSL approach is that in order to sufficiently reduce outflow, it creates a congested traffic state in the speed-limited area. Alternately, the unique attribute of COSCAL v2 to resolve moving jams, and to maintain free-flow condition before and after jam resolution is considered more desirable.

The second objective required to identify the desirable characteristics of an on-ramp queue controller for COSCAL v2. For this, RM approaches and some comprehensive strategies were reviewed. ALINEA/Q strategy is a reactive approach with ramp queue regulation that is suitable for near-future implementation. From a control systems perspective, ALINEA/Q was found to be compatible with COSCAL v2. However, theoretically adapting COSCAL v2 for real-time responsiveness to changing on-ramp flows is a challenge. The HERO coordinated RM approach focused on the under-utilization of ramp storage, when RM flows are so high to even keep a minimum queue length. In such a situation, freeway efficiency is needlessly decreased due to the high ramp flows. Therefore, a minimum queue length criteria is desirable for the queue controller. Additionally, when the ramp queue can no longer be managed without deteriorating the performance of the freeway, the trade-off between the efficiency of the urban network and the freeway must be considered. Hence, the control design should result in deactivation of the ramp queue management if the trade-off is not balanced. Over and above, minimal tuning parameters and a generic formulation are attractive characteristics.

The third objective related to the integration of VSL and RM strategies. The integration of RM and VSL is recognized as beneficial for both the systems, and can improve their combined operating efficiency. On the one hand, integration with RM improves the effectiveness of VSL when speed limits are active at the on-ramp section, and on the other, the possibility to regulate freeway flows with VSL can allow higher RM flows. Over and above, an integrated strategy can ensure that the freeway traffic is effectively regulated even when ramp queue restriction is reached. On surveying various integrated strategies, three main approaches to integration were highlighted. These can be generalized as: (1) inputs of one control measure are used to determine the output of the other, (2) output of one is used to determine output of the other, and (3) inputs to both measures together determine outputs (in model based approaches). Furthermore, the conditions for activation and deactivation of RM and VSL are understood to offer a degree of freedom, since two flow streams are regulated to control the freeway traffic state. Hence, these must be carefully specified in the design of the integrated strategy. Finally, it was observed that based on the integration approach, on-
ramp queue regulation may require re-estimation of the control scheme. This is not so desirable for more complex and computationally demanding strategies.

In this process, some core insights into VSL strategies, their integration with RM approaches and ramp queue management have been gained. These insights will be used in the theory development phase.
Chapter 3

Basic Approach for Ramp Metering with COSCAL v2

The literature survey identified some desirable characteristics for an integrated ramp metering (RM) and variable speed limits (VSL) strategy with ramp queue regulation. In this chapter, the theory for extension of a macroscopic speed control algorithm, COoperative Speed Control ALgorithm (COSCAL) v2 in Hegyi (2013) is developed. The extension is made for a basic RM strategy that considers a constant RM rate, without any constraints on the ramp queue; this is a simplification of practice. However, it is the first step to understanding the functional workings of an integrated strategy. The theory is further developed in Chapter 4, for an advanced RM strategy with time-varying ramp flows and ramp queue constraints.

The work in this Chapter is influenced by a recent work that adapts the microscopic counterpart of COSCAL v2 for a constant RM rate (Van de Weg et al., 2014). To remain consistent with the original work and for ease of understanding, parts of the original algorithm in Hegyi (2013) are reproduced before presenting its extension. The new theoretical contributions in this chapter include:

- Section 3-4-2: extension of jam resolution task in COSCAL v2 for RM flows
- Section 3-5-2-3: adaptation of stabilization task in COSCAL v2 for RM flows
- Section 3-5-3: correction for difference in actual density and the target (design) density in the area speed-limited for stabilization

3-1 Introduction

Cooperative speed control algorithms – COSCAL v1 and COSCAL v2 – are more sophisticated feedback strategies based on the conceptual framework of SPEed Controlling ALgorIthm using Shockwave Theory (SPECIALIST) (Hegyi et al., 2008). These algorithms are based in shockwave theory and aim to improve freeway efficiency by resolving jam waves. The basics of SPECIALIST useful to this research will be discussed in Section 3-1-1. The fundamental principle in all these algorithms is to speed limit the minimum number of vehicles required for two main purposes: (1) to resolve a moving jam, and (2) for stabilizing traffic further upstream such that an increased outflow is achieved after the jam is resolved.

The development of COSCAL v2 was preceded by a microscopic algorithm, COSCAL v1 that used sensing and actuation capability of vehicles for both detection and actuation processes. However, due to low
penetration rate of cooperative vehicles, detector loops and roadside speed limit gantries need to be used in combination with in-car capabilities. Additionally, from the Dynamax in-car project (Netten et al., 2013) it became clear that the main advantage of cooperative systems over a purely roadside system came from the improved jam detection accuracy and the faster jam detection. Consequently, COSCAL v2 does not exploit the possibility to actuate in-car. For higher penetration rates, roughly 10–20%, a combination of the two algorithms remains an interesting opportunity.

The other important considerations made in COSCAL v2 compared to COSCAL v1 include:

- **Multi-lane and heterogeneous traffic** – In a multi-lane setting, the vehicle type distributions may be different over the lanes which may lead to different macroscopic traffic dynamics. This difference will not lead to difficulties as long as the assumptions of the theory hold, i.e. as long as the jam head is (roughly) at the same location on all lanes and the jam is created or resolved roughly at the same location on all lanes. It is expected that the microscopic traffic dynamics ensures that this assumption holds. This is because it is expected that vehicles will change lanes when one lane is jammed and a neighbouring lane is in free flow. Hence, it is assumed that there is no significant difference between the jam locations on different lanes.

- **Lane changing and overtaking** – On a multi-lane freeway vehicles can change lanes and can overtake. While this complicates the algorithm formulation on vehicle level, COSCAL v2 is less sensitive (or insensitive) to these behaviours. The theory of COSCAL v2 holds on road section level; the number of vehicles to be speed-limited is determined based on actuation segments (i.e. gantry locations) which typically contain tens of vehicles. The rounding error made in the process is much larger than the number of vehicles that may overtake during one time period. Furthermore, the feedback mechanism compensates for errors caused by overtaking in the determination of the necessary length of the speed-limited stretch.

### 3-1-1 Overview of the roadside-cooperative algorithm

The development of the cooperative speed control algorithm qualitatively follows the same steps as taken in the SPECIALIST and COSCAL v1 algorithms. However, due to the different methods for the measurement and actuation, the mathematical formulation differs. The qualititative steps can be summarized as four main tasks:

1. **Task 1:** Moving jam detection. The jam should be detected.

2. **Task 2:** Speed-limitation for jam resolution. As soon as the jam is detected and the jam is assessed to be resolvable or not. If resolvable, the vehicles directly upstream of the jam are slowed down to the lowest admissible speed. The length of the speed-limited stretch (and hence, the number of slowed down vehicles) should be just enough to resolve the jam.

3. **Task 3:** Speed-limitation for traffic flow stabilization. The traffic joining the speed-limited vehicles at the tail, are also slowed down, in order to stabilize the traffic flow. These vehicles do not only maintain the speed, but also realize a given target density (on the average). This continues as long as there are speed-limited vehicles on the freeway.

4. **Task 4:** Release of speed limits. After the jam has been resolved, the speed limits can be released, starting at the head of the speed-limited stretch (which consists by then only of the stabilized area), until the head of the speed-limited area meets its tail.

### 3-1-2 Overview of the chapter

For the development of the theory for integrated RM with COSCAL v2, the basic assumptions and starting points are first given in Section 3-2. Following this, each of the Sections 3-3, 3-4, 3-5 and 3-6 detail the
core tasks in COSCAL v2. The jam detection and the release of speed limits (task 1 & task 4 respectively) remain the same as in the original work, and are given in Section 3-3 and Section 3-6. The remaining two tasks are detailed in Sections 3-4-2 and 3-5-2-3; here the original formulation of the tasks is discussed before the integration approach.

Further, Section 3-7 describes how the algorithm determines a jam as resolvable, which is based essentially on the physical limitation of infrastructure over which speed limits can be applied. Another important implementation issue is regarding the detection of multiple jams while speed limits are active. How the algorithm is restricted to resolve a single jam in one complete scheme is discussed in Section 3-8. Finally, the conclusions from the theory development in this chapter will be given in Section 3-9.

3-2 Assumptions and design parameters

3-2-1 Notation

We assume that the freeway stretch is partitioned into detection segments, and also partitioned into actuation segments, where the segment boundaries physically correspond to the loop detector and speed limit gantry locations respectively. The detection and actuation segment boundaries do not need to be aligned.

We denote the segment index of the detection segments with $i_{det}$, $i_{det} \in \{1, 2, \ldots, I_{det}\}$ and the gantry index with $i_{act}$, $i_{act} \in \{1, 2, \ldots, I_{act}\}$, where $i_{det}(i_{act})$ is the detection segment index of the segment in which gantry $i_{act}$ is positioned. The typical segment length is 100m (determined by the available detectors: induction loops, floating car, video based monitoring), while the typical distance between gantries is about 500–600m (determined by the available speed limit gantries). We also assume that the speed limit gantry of actuation segment $i_{act}$ is at the upstream end of the segment, and the loop detector of segment $i_{det}$ is at the downstream end of detection segment $i_{det}$. The segment indices increase in the flow direction.

We refer to the the upstream and downstream end of the actuation segment $i_{act}$ by $x_{u}^{i_{act}}$ and $x_{d}^{i_{act}}$ respectively, and likewise for detection segment $i_{det}$ by $x_{u}^{i_{det}}$ and $x_{d}^{i_{det}}$.

In the description below, we will use vehicle index $i_{veh}$ to refer to individual vehicles, where the more downstream vehicle has a lower index. We also will use the discrete time index $k$, referring to the time period $t \in [kT, (k+1)T)$, where $T$ (h) is the discrete time step size of the roadside detection and actuation system. Time step $T$ will be typically in the range around 5-30s.

3-2-2 Assumptions related to the jam characteristics

- The jam head has a known, constant propagation speed $v_{jam-h}$ (km/h) (for jam waves, this is about -18 km/h, for jams at on-ramps this is zero).
- The flow $q^{[1]}$ (veh/h) and the density $\rho^{[1]}$ (veh/km/lane) downstream of the jam after the traffic has reached its free-flow speed, are also known and constant. (The superscript [1] also refers to the corresponding traffic state in SPECIALIST.) For moving jams this flow equals the queue discharge rate, and is around 70% of the normal free-flow capacity, for jams at on-ramps this is usually around 90-95% of the freeway capacity.
- The average speed $v^{[2]}$ and density $\rho^{[2]}$ inside the jam are assumed to be known from historical data. Typically, the jam speed should be close to zero and the jam density near about 100 veh/km/lane.

These assumptions are not very limiting, since there are many empirical observations that support them. The last two assumptions entail the first.
3-3 TASK 1: Jam detection

While in the case of 100% penetration rate in COSCAL v1 the jam is detected by measurements from individual vehicles, for low penetration rates the jam has to be detected by fusing the individual vehicle data with other data sources, such as inductive loop data or VBM. The result of the data fusion is a state estimate (speed and density) for each detection segment $i^{\text{det}}$.

The structure of the jam detection algorithm is similar to the individual vehicle based formulation: a jam is detected if the speed $v_i^{\text{det}}(k)$ of segment $i^{\text{det}}$ drops below a certain threshold $v^{\text{th}}$ by a sufficient amount and for a sufficient time (i.e., for very low speeds a shorter detection time is sufficient). Similarly, the detected jam state is restored to free flow if the speed is above the threshold for a sufficiently long time. In order to determine what is sufficiently long, the time integral detected jam state is restored to free flow if the speed is above the threshold for a sufficiently long time. In order to determine what is sufficiently long, the time integral $z_i^{\text{det}}(k)$ is taken of $v_i^{\text{det}}(k) - v^{\text{th}}$ as long as the speed $v_i(k)$ remains continuously above or continuously below $v^{\text{th}}$, and the integral is compared with thresholds $z^{\text{ff}}$ (free flow) and $z^{\text{jam}}$ (jam), with $z^{\text{jam}} < 0 < z^{\text{ff}}$ according to

\[
\begin{align*}
\bar{z}_i^{\text{det}}(k) &= \begin{cases} 
    z_i^{\text{det}}(k-1) + T(v_i^{\text{det}}(k) - v^{\text{th}}) 
    & \text{if } (z_i^{\text{det}}(k-1) \geq 0 \land v_i^{\text{det}}(k) > v^{\text{th}}) \lor (z_i^{\text{det}}(k-1) \leq 0 \land v_i^{\text{det}}(k) < v^{\text{th}}) \\
    (v_i^{\text{det}}(k) - v^{\text{th}}) & \text{otherwise} 
    \end{cases} \\
    z_i^{\text{det}}(k) &= \min\{2z^{\text{ff}}, \max\{2z^{\text{jam}}, \bar{z}_i^{\text{det}}(k)\}\} \\
j_i^{\text{det}}(k) &= \begin{cases} 
    1 & \text{if } z_i^{\text{det}}(k) \leq z^{\text{jam}} \\
    0 & \text{if } z_i^{\text{det}}(k) \geq z^{\text{ff}} \\
    j_i^{\text{det}}(k-1) & \text{otherwise} 
    \end{cases}
\end{align*}
\]

(3-1)

(3-2)

(3-3)

where $\bar{z}_i^{\text{det}}(k)$ is truncated in (3-2) to prevent that $z_i^{\text{det}}(k)$ grows to plus or minus infinity (to prevent numerical problems), and $j_i^{\text{det}}(k)$ indicates the jam state of vehicle $i$, where 1 means jam and 0 means free flow. The integration and thresholding prevents the chattering of the jams state, for the case when the speed closely fluctuates around $v^{\text{th}}$.

If the measurement $v_i^{\text{det}}(k)$ is not available (e.g. due to no vehicles in the segment), then it is assumed that $z_i^{\text{det}}(k) = z_i^{\text{det}}(k-1)$ and $j_i^{\text{det}}(k) = j_i^{\text{det}}(k-1)$. It is also assumed that in the first time step $v_i^{\text{det}}(0)$ is available for all segments.

If one or more segments detect a jam, then the location of the jam head location $x_i^{\text{jam-h}}$ is determined by the location $x_i^{\text{jam-h}}$ of the downstream end of detection segment $j_i^{\text{jam-h}}$, where $j_i^{\text{jam-h}}$ refers to the most downstream segment in jam state.

3-4 TASK 2: Initial speed limitation and jam resolution

The second task involves the start the of the speed limit scheme following the jam detection. Jam resolution task uses instantaneous speed-limitation for flow reduction in order to resolve a moving jam. The principle is to reduce the inflow into the jam below the discharge flow at the jam-head. Hence, when extra vehicles from the on-ramp enter, the spatio-temporal extent of speed-limitation for this task is under-estimated in the original algorithm. Therefore, there is a need to adapt the original algorithm.

3-4-1 Initial speed limitation for jam resolution - variable speed limits only

After the jam has been detected in one or more detection segments, the vehicles in and upstream of the detection segment containing the jam head should reduce their speed according to the effective speed limit $v^{\text{eff}}$. The effective value of the speed limit is defined as the speed that vehicles will drive at when the speed limits are on (displaying a speed $v^{\text{disp}}$ (km/h)), including possible non-compliance.
In this step, it is determined which actuation segment is the last segment that needs to be slowed down in order to resolve the jam. To determine the last segment the following reasoning is used.

Let us consider a vehicle that is slowed down and that will join the queue at some point before the jam is resolved. An example of a trajectory of such a vehicle is shown by the blue dashed line in Figure 3-1.

Based on these assumptions the flow that crosses the head of the jam can be calculated, using the same reasoning as Lighthill and Whitham citeLighthill used for the derivation of front speeds. A moving observer who moves parallel with the head of the jam will see not only a flow \( q^1 \) (or \( q^2 \), depending on on which side of the front he is looking), but also the vehicles that he is passing due to his own speed. The total flow \( q^{jam-h} \) he sees is given by

\[
q^{jam-h} = q^1 - v^{jam-h} \rho^1, \tag{3-4}
\]

or equivalently by,

\[
q^{jam-h} = q^2 - v^{jam-h} \rho^2. \tag{3-5}
\]

This means that for vehicle \( i^veh \) upstream of the jam head, the time \( t_{exit}^i \) when it will exit the queue, can be calculated, using the number of vehicles \( N_{i^veh}(k) \) (veh) between the first (most downstream) vehicle in the queue and vehicle \( i^veh \). The exit time is given by:

\[
t_{exit}^i(k) = N_{i^veh}(k) / q^{jam-h}. \tag{3-6}
\]

This time implicitly includes a partial free-flow travel (up to the tail of the queue) and a queuing part, as indicated by the dashed blue line in Figure 3-1. This equation holds as long as vehicle \( i^veh \) can join the queue before it exits the queue.

Note that (3-6) implies that the exact trajectory of the vehicle is irrelevant as long as the vehicle will join the queue at least for a moment. (After the jam has been resolved, the outflow calculation doesn’t hold anymore.) This simplifies the calculations compared to the original SPECIALIST, since states 2, and 6 do not have to be determined explicitly.

Now, if vehicle \( i^veh \) slows down earlier (by speed limitation), and slows down sufficiently, such that it does not have to join queue, this is equivalent to saying that the queue has resolved downstream of vehicle \( i \). Not joining the queue means that the vehicle crosses the imaginary head of the queue later than it would do so based on (3-6) (like the green dashed line crosses the black dotted line in Figure 3-1).

If we now assume that vehicle \( i^veh \) will travel at speed \( v^{eff} \) after it has been slowed down, then the time \( t_{sl}^i \) when its trajectory will cross the (imaginary) trajectory of the queue front is given by:

\[
t_{sl}^i(k) = x^{jam-h}(k) - x^{i^veh}(k) + v^{eff}, \tag{3-7}
\]

where \( x^{jam-h}(k) \) is the location of the jam head at time step \( k \). The corresponding trajectory for the blue vehicle is indicated by the blue dotted line.

For vehicles that will join the queue, it holds that

\[
t_{exit}^i(k) > t_{sl}^i(k), \tag{3-8}
\]
**Figure 3-1:** Different vehicle trajectories and the corresponding times \( t_{\text{exit}} \) and \( t_{\text{sl}} \). The blue vehicle (blue dashed line) has to join the queue even if it is slowed down. Therefore, its average speed will be lower than the effective speed limit. The blue dotted line is the trajectory if the vehicle would be able to maintain a speed equal to \( v_{\text{eff}} \). The red vehicle (both dashed and dotted) arrives at the head of the queue exactly while it maintains a speed equal to \( v_{\text{eff}} \) without having to slow down (i.e., without joining the queue). The green vehicle avoids the queue if it maintains \( v_{\text{eff}} \) (dotted). In fact it could even travel somewhat faster to cross the line of the imaginary jam head at the time based on (3-6). The last vehicle that should be slowed down is the red one (Hegyi, 2013).
such as the blue vehicle in Figure 3-1. For the vehicle that joins the queue at the moment that the queue is being resolved (red vehicle in Figure 3-1), it holds that
\[ t_{\text{exit}}^{\text{veh}}(k) = t_{\text{sl}}^{\text{veh}}(k), \quad (3-9) \]
and for the vehicles that will not join the queue anymore (green vehicle), it holds that
\[ t_{\text{exit}}^{\text{veh}}(k) < t_{\text{sl}}^{\text{veh}}(k) \quad (3-10) \]
Using this, the last vehicle that should be slowed down in order to resolve the jam, is the first (counting from \( i = 1, 2, \ldots \)) for which holds that
\[ t_{\text{exit}}^{\text{veh}}(k) \leq t_{\text{sl}}^{\text{veh}}(k) \quad (3-11) \]
In this case, this is the red vehicle.

Now, since detection segments are the fundamental units of the measurements, (3-11) is evaluated for each detection segment, using the upstream end \( x_{\text{u, det}} \) of the segment as the location of the most upstream vehicle in that segment. If inequality 3-11 holds for the upstream end of a certain detector segment, then the gantry that is at the same location or just upstream of it, is the most upstream one that is needed for jam resolution.

So, for the evaluation of the time \( t_{\text{sl}}^{\text{veh}}(k) \) in (3-7), the vehicle location \( x_{\text{veh}}^{\text{veh}}(k) \) is replaced by the location of the upstream end \( x_{\text{u, det}} \) of the detector segment \( i_{\text{det}} \). For the evaluation of the time \( t_{\text{exit}}^{\text{veh}}(k) \) in (3-6) the number of vehicles between the jam head and the upstream end of the detection segment under consideration is determined based on the densities of the segments between the jam head and the current detection segment:
\[ N_{i_{\text{det}}}(k) = \sum_{j = j_{\text{jam-h}}}^{j_{\text{det}}} L_j \lambda_j \rho_j(k) \quad (3-12) \]
where \( j_{\text{jam-h}} \) is the detector index of the detector segment containing the jam head, and \( L_j, \rho_j(k), \lambda_j \) are respectively the link length, the density, and the number of lanes of segment \( j \). If \( j_{\text{det}} \) is the detector segment index of the jam head and if \( j_{\text{det}} \) is the first detector index for which (3-11) holds (the first when going from downstream into the upstream direction), then the speed limits will be activated on the actuation segments that include detection segments \( j_{\text{det}}, \ldots, j_{\text{jam-h}} \). The range of actuation segments goes from \( j_{\text{act}}^{\text{det}}, \ldots, j_{\text{act}}^{\text{jam-h}} \), where \( x_{\text{act}}^{\text{det}} > x_{\text{act}}^{\text{det}} \geq x_{\text{act}}^{\text{det}} \text{ and } x_{\text{act}}^{\text{jam-h}} \geq x_{\text{act}}^{\text{jam-h}} > x_{\text{act}}^{\text{det}} \). Important to note is that the data from a given time step, \( k \) is used for activation in the following time step, \( k + 1 \).

Equation (3-11) can then be rewritten as:
\[ t_{\text{exit}}^{\text{det}}(k) \leq t_{\text{sl}}^{\text{det}}(k) \quad (3-13) \]
where,
\[ t_{\text{sl}}^{\text{det}}(k) = \frac{N_{i_{\text{det}}}(k)}{q_{\text{jam-h}}}, \quad (3-14) \]
\[ t_{\text{sl}}^{\text{act}}(k) = \frac{x_{\text{jam-h}}(k) - x_{\text{u, det}}}{v_{\text{eff}}} \quad (3-15) \]

### 3-4-2 Initial speed limitation for jam resolution - variable speed limits and ramp metering

If the last vehicle that must be slowed down to resolve the jam crosses an on-ramp location \( x_{\text{ramp}} \), equation (3-13) must be adapted for ramp flows. For roadside control, this corresponds to a case when the most
upstream segment used for resolving the jam is upstream of the on-ramp segment, including the detection segment $t_{ramp}$ that contains the on-ramp and satisfies $x_{u,\text{det}} < x_{ramp} \leq x_{d,\text{det}}$. In the absence of such modification, the vehicles from the on-ramp entering the jam before the last vehicle on the detector segment that satisfies equation (3-13) are not included. This leads to an underestimation of $t_{\text{exit}}(k)$, and hence the vehicles speed-limited would not be sufficient to resolve the jam.

Therefore, theory is developed to determine the additional ramp vehicles that enter the jam before its resolution. An iterative approach has been adopted for this. At each time step, iterations are performed in space - moving upstream from the first detection segment where a jam is detected. For ease of execution and understanding, the spatial iterations are identified within three broad cases, as illustrated in Figure 3-4. These cases differ in how merging flows influence jam resolution. For better clarity, the variables used for the important time intervals, estimated either relative to the start of the control scheme or the current time step, are plotted in Figure 3-2.

### 3-4-2-1 Assumptions for merging flow during jam resolution

- The on-ramp flows merging onto the freeway can take known constant values - $q_{\text{ramp}}$, $q_{\text{metered}}$ or $q_{\text{congested}}$. Here, $q_{\text{ramp}}$ equals the on-ramp demand and occurs when RM is switched off; $q_{\text{metered}}$ is the metered flow when RM is active; $q_{\text{congested}}$ is the ramp flow realized when vehicles merge into a congested state on the freeway.

- The RM starts simultaneously with the VSL scheme at time $k_{\text{start}}T$, when a jam is detected downstream of the on-ramp.

- There is a considerable delay between the time when the RM is turned on and the time when the metered flow enters the freeway merging area. This delay is because of the vehicles on the merging lane (between the stop line of the ramp signal and the entry point on the freeway) when RM starts. These vehicles must clear before the RM flow can enter the freeway.

The length of the merging segment is taken as $x^r$ and the average speed on the merging segment as $v^r$. The total delay from the start of the scheme is given by the extreme situation of a vehicle crossing the stop line just before the RM is switched on. The time it takes this vehicle to enter the freeway gives an estimate of the total delay $t_{\text{delay}}(k_{\text{start}})$.

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Therefore, demand flow $q^{\text{ramp}}$ merges into the freeway from the start of the scheme for a time interval of $t_{\text{delay}}(k^{\text{start}})$. The delay remainder at a time instant $kT$, later than the start of the control scheme at $k^{\text{start}}T$, is given by:

$$t_{\text{delay}}(k) = \max(t_{\text{delay}}(k^{\text{start}}) - (k - k^{\text{start}})T, 0)$$  \hspace{1cm} (3-17)

- After the elapse of $t_{\text{delay}}(k)$, until the tail of the jam crosses the on-ramp, $q^{\text{metered}}$ flow enters the freeway. The time beyond the current time that it takes the tail of the jam to cross the ramp is denoted as $t_{\text{ramp}} jam_{-h}(k)$. The calculation of this time is detailed in (3-36).

- If the tail of the jam crosses the on-ramp before $t_{\text{delay}}(k)$ expires, $q^{\text{ramp}}$ flow merges until the $t_{\text{ramp}} jam_{-h}(k)$ and metered flow $q^{\text{metered}}$ is not observed. This is because the crossing jam results in a merging flow $q^{\text{congested}}$ after the jam tail crosses.

- Finally, during the time the freeway is in congested state, i.e between the time the tail and the head of the jam pass the on-ramp, the flow equals $q^{\text{congested}}$. In reality, this can cause queueing on the ramp resulting in a reduced merging even if RM is active. It is thus assumed that $q^{\text{congested}} \leq q^{\text{metered}}$. The time, $t_{\text{ramp}} jam_{-h}(k)$, it takes from the current time instant for the jam head to pass the ramp location can be calculated using the jam head velocity:

$$t_{\text{ramp}} jam_{-h}(k) = \frac{x_{\text{jam-h}}(k) - x_{\text{ramp}}}{\rho_{\text{jam}}}$$  \hspace{1cm} (3-18)

- After the head of the jam crosses the on-ramp, the on-ramp flow merges into the free-flowing freeway traffic downstream of the jam head (state [5A]). The merging mechanism here does not influence jam resolution and hence, RM flows need not be accounted for.

### 3-4-2-2 Calculation of merging flow from on-ramp

We have discussed so far that the on-ramp flow is time dependent and may change during the jam resolution task. At any given time, the effective accumulation between the jam head and the most upstream jam resolving segment, given by $N_{\text{eff}}^{\text{plot}}(k)$, is equal to or greater than the actual accumulation $N_{\text{plot}}^{\text{plot}}(k)$ over these segments. This is considered by calculating the additional merging vehicles that would cross the head of the jam, $N_{\text{merge}}^{\text{plot}}(k)$, between the current time step till the time the jam is resolved.

$$N_{\text{eff}}^{\text{plot}}(k) = N_{\text{plot}}^{\text{plot}}(k) + N_{\text{merge}}^{\text{plot}}(k)$$  \hspace{1cm} (3-19)

where,

$$N_{\text{plot}}^{\text{plot}}(k) = \sum_{j=\text{plot}(k)}^{j=\text{jam-h}(k)} L_j \lambda_j \rho_j(k)$$  \hspace{1cm} (3-20)

The estimate of $N_{\text{merge}}^{\text{plot}}(k)$ depends on one, the on-ramp flow profile, second, the time that the jam arrives at the on-ramp and thirdly, the time it takes for the most upstream speed-limited vehicle used in jam
resolution to reach the on-ramp. For each detection segment this is a hypothetical vehicle that enters the most upstream segment used in jam resolution when speed limits activate. This vehicle would be the last vehicle to enter the jam, and hence, its trajectory is the shockwave between the initial speed-limited area and the stabilization area, in other words the tail of the initial speed-limited area, called the R-tail line.

If we consider any speed-limited vehicle upstream of the on-ramp at time $kT$, it will take this vehicle time $t_{ramp}^{veh}(k)$ to pass the ramp location and can be estimated as:

$$t_{ramp}^{veh}(k) = \frac{x_{ramp} - x_{veh}(k)}{v_{eff}}$$ (3-21)

Given discrete detection segments, the time estimate $t_{ramp}^{i_{det}}$ for the most upstream vehicle on a detection segment $i_{det}$ becomes:

$$t_{ramp}^{i_{det}}(k) = \frac{x_{ramp} - x_{u, det}^{i_{det}}(k)}{v_{eff}}$$ (3-22)

The number of vehicles that will merge between the jam head and the most upstream speed-limited vehicle by the time it crosses the on-ramp can be calculated by integrating the merging on-ramp flow $q^{merge}$, that can take values $q^{ramp}$, $q^{metered}$ or $q^{congested}$.

$$N^{merge}_{i_{det}}(k) = \int_{kT}^{kT + t_{ramp}^{i_{det}}(k)} q^{merge}(t) \, dt$$ (3-23)

The time $t_{ramp}^{i_{det}}(k)$ that the most upstream speed-limited vehicle crosses the on-ramp, compared to the jam-head determines $N^{merge}_{i_{det}}(k)$, given as:

$$N^{merge}_{i_{det}}(k) = \begin{cases} 0 & \text{if } t_{ramp}^{i_{det}}(k) \leq 0 \\ q^{ramp} & \text{if } 0 < t_{ramp}^{i_{det}}(k) \leq t_{delay}^{i_{det}}(k) \\ c1 + q_{metered} & \text{if } t_{delay}^{i_{det}}(k) < t_{ramp}^{i_{det}}(k) \leq t_{ramp}^{i_{det}}(k) \\ c2 & \text{if } t_{ramp}^{i_{det}}(k) > t_{ramp}^{i_{det}}(k) \\ \end{cases}$$ (3-24)
where,

\[ c_1 = q^{\text{ramp}} r^{\text{delay}}(k) \]

\[ c_2 = c_1 + q^{\text{metered}} \max \{ t^{\text{ramp}}_{\text{jam} - t}(k) - r^{\text{delay}}(k), 0 \} + q^{\text{congested}} (t^{\text{ramp}}_{\text{jam} - h}(k) - t^{\text{ramp}}_{\text{jam} - t}(k)) \]  

(3-25)

(3-26)

The constant value for \( N^{\text{merge}}_{\text{det}}(k) \) after the jam tail crosses the on-ramp is a simplification. Once the tail of the jam has crossed the on-ramp, the jam can only be resolved upstream of the ramp. In other words, no vehicle that crosses the on-ramp in congestion can resolve it. Since, the vehicles merging after the head of the jam crosses the ramp do not affect jam propagation, the constant accounts for the total number of vehicles merging until \( t^{\text{ramp}}_{\text{jam} - h}(k) \).

Now, the predicted number for the vehicles merging between the jam head and the most upstream jam resolving vehicle, \( N^{\text{merge}}(k) \) can be substituted in equation (3-19) to adapt equation (3-13), which now becomes:

\[ t^{\text{exit}}_{\text{det}}(k) \leq t^{\text{sl}}_{\text{det}}(k) \]  

(3-27)

where,

\[ t^{\text{exit}}_{\text{det}}(k) = \frac{N^{\text{eff}}(k)}{q^{\text{jam-h}}} \]  

(3-28)

\[ t^{\text{sl}}_{\text{det}}(k) = \frac{x^{\text{jam-h}}(k) - x^{\text{u.det}}_{\text{det}}}{v_{\text{jam-h}} + v^{\text{eff}}} \]  

(3-29)

3-4-2-3 Guiding cases and the iterative control approach

The different jam resolving scenarios that may occur when a jam is detected downstream of the ramp can be identified within three broad cases, as illustrated in Figure 3-4. These cases should guide the control scheme - the determination of \( N^{\text{merge}}_{\text{det}}(k) \), and the choice of \( q^{\text{metered}} \) for more efficient integration of RM with VSL. Two critical cases are used to identify the applicable situation. In essence, the classification is based on whether the jam can be resolved downstream of the on-ramp or not, and if the last jam resolving vehicle is downstream or otherwise.

An understanding of the cases also explains the iterative approach; iterations are performed over detection segments (in space) at every time step. The iterations are continued in time till the last jam resolving segment is found.

At any given time \( kT \), \( N^{\text{merge}}_{\text{det}}(k) \) is determined for a detector segment \( i^{\text{det}} \), upstream of the segment containing the jam head, i.e. \( i^{\text{jam-h}} \). The time \( t^{\text{ramp}}_{\text{det}}(k) \) it takes a hypothetical vehicle that enters \( i^{\text{det}} \) when speed limits are activated decides \( N^{\text{merge}}_{\text{det}}(k) \) (refer Figure 3-3). \( N^{\text{merge}}_{\text{det}} \) reflects in \( N^{\text{eff}} \) and the condition in equation (3-27) that must be satisfied by the most upstream jam resolving segment. This iterations start at detector segment \( i^{\text{jam-h}} \) - 1; if the condition is not met here, the next upstream segment is checked similarly till the condition holds for some detection segment. If no detector segment (within the length of actuation infrastructure) satisfies the condition, the jam is considered as unresolvable. This is discussed in more detail in Section 3-7. The guiding cases are detailed next:

- **Case a:** When a jam is detected downstream of the on-ramp, the iterations begin by assuming **Case a**. This scenario occurs when the detected jam can be resolved by a detection segment downstream of the on-ramp (more specifically, the vehicle that enters this detection segment just when the speed limits are activated). The ramp flows do not impact the jam resolution area in this case and hence,
**Case a:** Jam is resolved downstream of the ramp by a downstream vehicle.  
*Critical case is when the jam is resolved by the first vehicle downstream of the ramp when the scheme activates.*

**Case b:** Jam is resolved downstream of the ramp, by a vehicle that is upstream of the ramp at the start of scheme.  
*Critical case arises when the jam is resolved at the ramp by an upstream vehicle.*

**Case c:** Jam crosses the on-ramp location and is resolved at an upstream location by a vehicle further upstream at the start of the scheme.

*Case a* does not hold, iterations are continued further upstream. It is now checked if the jam can be resolved by a detection segment upstream of $i_{\text{det},\text{crit}}$. The jam may still be resolved downstream of the ramp, such that $t_{\text{ramp}}^{\text{jam}}(k) \leq t_{\text{ramp}}^{\text{jam} - 1} \leq t_{\text{ramp}}^{\text{jam} - h}(k)$ holds. This also implies that the congestion does not cross the ramp, and therefore, $q_{\text{congested}}$ is not observed.

However, as we proceed upstream of $i_{\text{det},\text{crit}}$, every segment that does not satisfy (3-27) must be additionally checked to determine if the jam-tail crosses the on-ramp before the associated R-tail line (indication of *Case c*). This step adds to the advantage of a case-based approach by detecting sooner if jam may not be resolved downstream of the ramp.

Figure 3-5 illustrates how an approach in accordance with that used to find the most upstream jam resolving speed-limited segment can be used to predict the time $t_{\text{ramp}}^\text{jam} - (k)$ that the jam-tail crosses the on-ramp. It is also clear from the figure that to proceed we need to calculate the time $t_{\text{enter}}(k)$ when a hypothetical R-tail vehicle would join the queue. The method is detailed below.

We first assume that *Case b* holds, concurrently implying that the R-tail line enters the jam before

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**Figure 3-4:** Cases for jam resolution based on on-ramp location
the jam tail reaches the on-ramp. The $N_{\text{eff}}$ estimate under this assumption is used to first calculate a make-do estimate of $t_{\text{exit}}$. To estimate $t_{\text{exit}}(k)$ we use the average velocity of vehicles in the jam $v_{\text{jam}}$. This velocity can be calculated off-line from historical data, avoiding the estimation of flow and density inside and downstream of the jam.

For any speed-limited vehicle that joins the queue its trajectory comprises of two parts; it travels under free flow with $v_{\text{eff}}$ till it enters the queue, and under queue condition with a speed $v_{\text{jam}}$ after, until it exits the queue. Thus, the intersection of the R-tail line and a line at $v_{\text{jam}}$ slope gives the time that the associated vehicle enters the jam.
The two parts of the trajectory then give:

\[ x_{\text{enter}}^\text{i\_det}(k) = x_{\text{exit}}^\text{i\_det}(k) + v_{\text{jam}}(x_{\text{exit}}^\text{i\_det}(k) - t_{\text{exit}}^\text{i\_det}(k)) \]  

(3-30)

where \( x_{\text{exit}}^\text{i\_det}(k) \) is known from the evolution of the jam head,

\[ x_{\text{exit}}^\text{i\_det}(k) = x_{\text{d\_det}}^\text{i\_det}(k) + v_{\text{jam-h}}^\text{i\_det}(k) \]  

(3-31)

and

\[ x_{\text{enter}}^\text{i\_det}(k) = x_{\text{u\_det}}^\text{i\_det}(k) + v_{\text{eff}}^\text{i\_det}(k) \]  

(3-32)

Eliminating \( x_{\text{enter}}^\text{i\_det} \) results in:

\[ t_{\text{enter}}^\text{i\_det}(k) = \frac{x_{\text{d\_det}}^\text{i\_det}(k) - x_{\text{u\_det}}^\text{i\_det}(k)}{v_{\text{eff}} - v_{\text{jam}}} + \frac{v_{\text{jam-h}}^\text{i\_det}(k) - v_{\text{eff}}^\text{i\_det}(k)}{v_{\text{eff}} - v_{\text{jam}}^\text{i\_det}(k)} \]  

(3-33)

Finally, substituting equation (3-14) gives:

\[ t_{\text{enter}}^\text{i\_det}(k) = \frac{v_{\text{eff}} - v_{\text{jam-h}}^\text{i\_det}(k)}{v_{\text{eff}} - v_{\text{jam}}} t^\text{ramp}_{\text{jam-t}}^\text{i\_det}(k) + \frac{v_{\text{jam-h}}^\text{i\_det}(k) - v_{\text{eff}}^\text{i\_det}(k)}{v_{\text{eff}} - v_{\text{jam}}^\text{i\_det}(k)} \]  

(3-34)

With the prescribed approach, \( t^\text{ramp}_{\text{jam-t}}^\text{i\_det}(k) \) can be calculated from the first detector segment for which the following condition holds:

\[ t^\text{ramp}_{\text{jam-t}}^\text{i\_det}(k) = \frac{v_{\text{eff}} - v_{\text{jam}}}{} \]  

(3-35)

This implies that the vehicle has crossed the on-ramp in congestion and the time the tail crosses the on-ramp can then be given as:

\[ t^\text{ramp}_{\text{jam-t}}^\text{i\_det}(k) = \frac{v_{\text{eff}} - v_{\text{jam}}}{} \]  

(3-36)

In performing the two checks iteratively, we will either detect a jam resolving segment or find the time the tail of the jam crosses the on-ramp. The latter is an indication that \textit{Case c} holds.

The critical situation occurs when the jam is resolved exactly at the on-ramp location \( x^\text{ramp}_{\text{jam-t}} \). The corresponding detector segment \( i^\text{det, crit2} \) that resolves the jam would be further upstream. \( i^\text{det, crit2} \) is determined by tracking the trajectory of the speed-limited vehicle that crosses the on-ramp at the same time as the jam head. Then, the time it takes for the jam head in the current time step to reach the on-ramp will be equal to the time it takes this vehicle to reach the on-ramp. The location of the last speed limited vehicle \( x_{\text{veh}} \), at the current time step can be found:

\[ \frac{x^\text{ramp} - x_{\text{veh}}}{v_{\text{eff}}} = \frac{x_{\text{d\_det}}^\text{i\_det}(k) - x^\text{ramp}_{\text{jam-h}}}{v_{\text{jam-h}}} \]  

(3-37)

and thus

\[ x_{\text{veh}} = \frac{x^\text{ramp} - x_{\text{veh}}}{v_{\text{eff}}} x_{\text{d\_det}}^\text{i\_det}(k) - x^\text{ramp}_{\text{jam-h}}}{v_{\text{jam-h}}} \]  

(3-38)

The critical detector segment \( i^\text{det, crit2} \) then will satisfy \( x_{\text{u\_det}}^\text{i\_det, crit2}(k) \geq x_{\text{veh}} < x_{\text{d\_det}}^\text{i\_det, crit2}(k) \).
• **Case c**: In this case, the jam crosses the on-ramp and is therefore resolved upstream of the on-ramp by a detection segment upstream of \( t_{\text{det,crit}}^2 \). Here, for the most upstream jam-resolving vehicle \( t_{\text{det}}^i(k) > t_{\text{jam}}^i-h(k) \) holds and all three flows \( q_{\text{ramp}}, q_{\text{metered}}, q_{\text{congested}} \) may be observed.

From the iterative approach used, if Case c holds, the time \( t_{\text{ramp}}^i \) will already be known. However, in this case the starting assumption that the most upstream jam-resolving vehicle crosses the on-ramp before the jam tail does not hold, and so we have wrongly calculated \( N_{\text{merge}}^i \) using \( q_{\text{metered}} \) instead of \( q_{\text{congested}} \). Since \( q_{\text{congested}} < q_{\text{metered}} \), \( N_{\text{merge}}^i \) and hence, \( t_{\text{exit}}^i \) are over-estimated. In doing so, \( t_{\text{enter}}^i \) is under-estimated as can be understood from Figure 3-5. Because for a vehicle crossing the on-ramp in jam \( t_{\text{enter}}^i \leq t_{\text{ramp}}^i \) should hold, the under-estimation would still satisfy the condition in equation (3-36). Therefore, when \( t_{\text{ramp}}^i \) is known, the assumption is relaxed to recalculate \( N_{\text{merge}}^i \) as the constant \( c_2 \) in equation (3-26).

With the correct estimate of \( N_{\text{merge}}^i \) and hence, \( N_{\text{eff}}^i \), the iterations are continued upstream to check equation (3-27) in order to find the most upstream jam resolving segment.

### 3-5 TASK 3: Speed limitation for stabilization

The goal of this task is to achieve a desired efficiency (that ensures traffic flow stability) of the flow leaving the stabilization area after the jam is resolved. For this, vehicles upstream of those used for resolving the jam are also speed-limited. These vehicles are controlled towards a target density \( \bar{\rho} \) in addition to their target speed \( v_{\text{eff}} \). This target density should be higher than the free flow density but low enough to ensure stable traffic flow at \( v_{\text{eff}} \) speed. A high density in this stabilisation area accumulates vehicles, and allows recovery to a traffic state with flow higher than the queue discharge flow. It is from this mechanism that an improvement in efficiency is achieved.

Since the aim is to maximize efficiency, the target density is chosen to ensure maximum stable flow in the stabilization area. This implies that when extra ramp flows enter, the traffic flow becomes metastable, and is prone to a traffic breakdown at the on-ramp section. Therefore, both the task must be adapted for integration with RM. First, the VSL only strategy will be presented in Section 3-5-1. This is extended to include ramp flows in the subsequent Section 3-5-2.

#### 3-5-1 Speed limitation for stabilization - variable speed limits only

In the SPECIALIST algorithm, the target density was on the average achieved by determining the fixed slope (in the time-space plane) of the front between the upstream free-flow area and the stabilizing region under the speed limits. The slope was determined by shock wave theory, based on a single measurement of the traffic state upstream of the jam and on the pre-defined state (speed and density) of the stabilization area under the speed limits. Using a single measurement was sufficient for the feed-forward algorithm, however, COSCAL v2 has a feedback structure, and therefore the slope is not fixed anymore, and is adjusted based on the updated measurements every time step.

In the COSCAL v1 algorithm, S-tail lines were used to determine the target trajectory for each individual vehicle. Each vehicle was slowed down at the right moment based on its S-tail line and its speed and deceleration characteristics. Since for COSCAL v2 a basic assumption is that the penetration rate is low, there are many vehicles of which the deceleration will be controlled by roadside speed limit gantries instead of the S-tail lines. Therefore, their location and start time of the deceleration cannot be controlled at such a detail.

The approach is based on the location of the region where vehicles will accumulate if the speed at a speed limit gantry is reduced. The basic idea is to extend the speed-limited area in the upstream direction until the target density is reached in the accumulation region. However, in some cases the upstream traffic may
have such a low flow that the tail of the speed-limited stretch can (and thus should) be shortened, without exceeding the target density. This approach has a homogenizing effect on the density in the stabilization area.

The stabilisation area is demarcated by the R-tail or S-head shockwave on the downstream end depending if the jam has been resolved, and the S-tail line on the upstream side. The downstream end of the stabilization area is at the upstream end of the jam resolving area, called the R-tail line, if the jam has not been resolved yet, or at the S-head line (defined in Section 3-6) once the jam is resolved. The R-tail line represents the most upstream vehicle that was ever used to resolve the jam. Due to the feedback structure, this vehicle may change over time. Therefore, it is the line that goes through the point of time step $k$ and location $x^{R,t}_{\text{act}}(k)$, where segment $i^{\text{act}}$ is the most upstream actuation segment used for jam resolution in the current time step. The index of the detector segment that the R-tail line crosses in the next time step can be given as $i^{R,t}(k + 1)$. The slope of the R-tail line equals the speed $v_{\text{eff}}$ of the speed-limited vehicles. The R-tail line is retained until the jam is resolved, unless at some moment a new R-tail line follows from the most upstream resolving actuation segment, that is more upstream than the current R-tail line. In that case, the new R-tail line is used in the subsequent steps.

So, let us denote the detection segment index that contains the R-tail or S-head line, by $i^{d,\text{det}}$, such that $x^{d,\text{det}}_{\text{u}} < x^{S\text{-line},\text{ds}}(k + 1) \leq x^{d,\text{det}}_{\text{L}}$, where $x^{S\text{-line},\text{ds}}(k + 1)$ denotes the location of the R-tail or S-head line in the current time step (whichever will be active then).

The estimation of the most upstream segment in the stabilization area, $i^{\text{det}}$ will be explained using Figure 3-6. If a vehicle passes the speed limit gantry exactly when the speed limit becomes activated, it should create the density $\bar{\rho}$ (veh/km/lane) required for stabilization when it has reached its target speed $v_{\text{eff}}$. In the figure the black dash-dotted line represents the vehicle trajectory and the blue dashed line its target trajectory. If the speed limit gantry is actuated later, then the vehicle will slow down later, and it will create a higher density. If the gantry is activated earlier, then the target density may not be reached.

Let us denote the number of vehicles between the R-tail line (or S-head, if that is active) and an upstream stabilisation segment by $N$ and the distance between the target trajectory line and $x^{S\text{-line},\text{ds}}(k)$ by $\Delta x$, and let denote the time and distance that the vehicle needs to decelerate by $t_{\text{dec}}$ (h) and $x_{\text{dec}}$ respectively (where $v_{\text{det}} = (v_{\text{eff}} - v_{\text{det}})/a_{\text{dec}}$, and $x_{\text{dec}} = t_{\text{dec}}(v_{\text{eff}} + v_{\text{det}})/2$) and $a_{\text{dec}}$ (km/h²) is the nominal deceleration rate. Now for every detection segment $i^{\text{det}} = i^{d,\text{det}}, i^{d,\text{det}} + 1, \ldots$ the following expression is evaluated:

$$\frac{N}{\Delta x} \leq \bar{\rho},$$

(3-39)

where

$$N = \sum_{i^{d,\text{det}}} \rho_i(k) \lambda_i L_i,$$

(3-40)

$$\Delta x = \sum_{i^{d,\text{det}}} L_i = (x_{\text{dec}} - t_{\text{dec}} v_{\text{eff}})$$

(3-41)

If expression (3-39) does not hold, then the density is too high and the next upstream detector segment has to be evaluated. If the expression holds then the first detection segment for which it holds is the most upstream detection segment that needs speed limits (first in the direction from downstream to upstream), and this part of the procedure can stop.

In an idealized situation the above procedure would lead to a homogeneous density in the stabilization area, but in practice the area may become inhomogeneous over time, due to differences in the individual vehicle speeds. If this inhomogeneity means that at the tail of the stabilization area the density is close to or above the critical value, then the upstream speed limits should be extended at a faster rate to prevent too high densities there, even if the average density in the complete stabilization area is below $\bar{\rho}$. For this reason, the above procedure is repeated starting at all detector segment locations in the current stabilization area plus a (negative) offset $d_{\text{stab}}$ (km) in the upstream direction. This offset helps to prevent too high densities just

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Figure 3-6: Illustration of the stabilization approach. The thick solid horizontal lines represent the gantry locations, the thin dotted lines the detector locations. In the red areas the speed limits are active for jam resolution, in the yellow areas for stabilization (Hegyi, 2013).
upstream of the speed-limited area. For all starting locations the detection segment is determined that needs speed limits. The overall detection segment that needs speed limits will be the most upstream one among these. The speed limits that will be activated for stabilization, will correspond to the actuation segments that include the detection segments from the most upstream one that needs speed limits to $\bar{\rho}_{\text{det}}$.

### 3-5-2 Speed limitation for stabilization - variable speed limits with ramp metering

The approach that has just been presented to realize stable traffic has to be extended when the moving jam is propagating near an on-ramp. The difference with the approach presented in the previous section is that a different density must be achieved at different locations depending on the location of the on-ramp. This section will calculate these different densities and in what situation they must be applied.

Figure 3-7 shows the different situations that a vehicle which is speed-limited for stabilization can encounter. These states are labelled as 4A, 4B, and 4C. The density in area 4A, downstream of the on-ramp is equal to the design density for the stabilisation area, $\bar{\rho}$ (veh/km/lane). $\bar{\rho}$ is the maximum possible density that ensures stability at velocity $v_{\text{eff}}$. Vehicles driving in area 4B and 4C, however, must maintain different densities. First, it is explained what these densities must be, in Sections 3-5-2-1 and 3-5-2-2. This theory is reproduced from the extension of COSCAL v1 with RM, by Van de Weg (2013). Following which it is explained how these densities are imposed in the macroscopic formulation of COSCAL v2.
### 3-5-2-1 Target density of vehicles in area 4B

Vehicles driving in area 4B are upstream of the on-ramp and should create extra space for traffic from the on-ramp. These vehicles will be passing the on-ramp while they are speed-limited thus they should have lower density to accommodate the on-ramp flow, such that downstream of the on-ramp the density is $\bar{\rho}$ on an average.

Note that the flow $q_{[4A]}$ (veh/h) downstream of the on-ramp in the stabilization area can be derived from the density $\bar{\rho}_{[4A]}$, assuming stationary traffic conditions:

$$q_{[4A]} = \bar{\rho}_{[4A]} v_{\text{eff}}$$  \hspace{1cm} (3-42)

The flow $q_{[4B]}$ (veh/h) upstream of the on-ramp in stabilization area 4B is then given by:

$$q_{[4B]} = q_{[4A]} - q_{\text{metered}}$$  \hspace{1cm} (3-43)

The target density $\bar{\rho}_{[4B]}$ (veh/km/lane) upstream of the on-ramp in the stabilization area 4B is given by:

$$\bar{\rho}_{[4B]} = \frac{q_{[4A]} - q_{\text{metered}}}{v_{\text{eff}}}$$  \hspace{1cm} (3-44)

$$\bar{\rho}_{[4B]} = \bar{\rho}_{[4A]} - \frac{q_{\text{metered}}}{v_{\text{eff}}}$$  \hspace{1cm} (3-45)

### 3-5-2-2 Target density of vehicles in area 4C

Now that the density in area 4B has been determined, the target density $\bar{\rho}_{[4C]}$ (km) in area 4C can be determined. The goal of realizing this headway distance in area 4C is to stabilize traffic. Note that the flow $q_{[5C]}$ (veh/h) in area 5C is realized by releasing vehicles from the speed limits from area 4C. Therefore, the flow in area 5C is higher or equal to the flow in area 4C:

$$q_{[5C]} \geq q_{[4C]}$$  \hspace{1cm} (3-46)

Furthermore, the flow $q_{[5B]}$ (veh/h) in area 5B is equal to the flow in area 5C plus the on-ramp flow:

$$q_{[5C]} + q_{\text{metered}} = q_{[5B]}$$  \hspace{1cm} (3-47)

thus, it holds that:

$$q_{[5B]} \geq q_{[5C]} \geq q_{[4C]}$$  \hspace{1cm} (3-48)

This implies that realizing a stable flow in area 5B means that the flow in area 5C and 4C will be stable as well. Choosing the flow $q_{[5B]}$ equal to the flow $q_{[5A]}$ in area 5A will result in stable traffic in area 5B as well. The reason for this is that the S-head line has been tuned to realize a stable flow in area 5A. Note that this only holds when the speed in area 5A equals the speed in area 5B, which is a reasonable assumption since the flows are equal. The flow $q_{[5A]}$ is computed using shock wave theory with the speed $v_{[4A-5A]}$ (km/h) of the S-head line, downstream of the on-ramp, between areas 5A and 5B, the free-flow speed $v_{\text{ff}}$ (km/h) of vehicles in area 5A. The speed of the S-head line is given by:

$$v_{[4A-5A]} = \frac{v_{\text{ff}} - \bar{\rho}_{[4A]} v_{\text{eff}}}{\bar{\rho}_{[4A]}}$$  \hspace{1cm} (3-49)

$$v_{[4A-5A]} = \frac{q_{[5A]} - \bar{\rho}_{[4A]} v_{\text{ff}}}{q_{[5A]} - \bar{\rho}_{[4A]} v_{\text{eff}}}$$  \hspace{1cm} (3-50)
this can be rewritten to give the flow $q^{[5A]}$:

$$q^{[5A]} = \bar{\rho}^{[4A]} v_{ff}^{[4A-5A]} - \bar{v}_{ff}^{[4A-5A]} \cdot (3-51)$$

Now choosing the flow $q^{[5B]}$ in area 5B equal to the flow $q^{[5A]}$ in area 5A will result in stable traffic.

From the flow $q^{[5B]}$ in area 5B the flow $q^{[5C]}$ in area 5C can be determined:

$$q^{[5C]} = q^{[5B]} - q_{metered} \cdot (3-52)$$

The flow $q^{[5C]}$ is realized by traffic that has driven from area 1US through area 4C to area 5C. By tuning the density in area 4C and the speed $v^{[4C-5C]}$ (km/h) of the S-head line between areas 4C and 5C the flow $q^{[5C]}$ is realized. Using shock wave theory, the speed $v^{[4C-5C]}$ of the S-head line upstream of the on-ramp can be given as:

$$v^{[4C-5C]} = \frac{q^{[5C]} - \bar{\rho}^{[4C]} v_{eff}^{[4C-5C]}}{q^{[5C]} / v^{[5C]} - \bar{\rho}^{[4C]} \cdot (3-53)}$$

Thus, the speed $v^{[4C-5C]}$ can be expressed as a function of the density $\rho^{[4C]}$.

How is the density $\bar{\rho}^{[4C]}$ chosen? Consider the fundamental diagram on the right of Figure 3-7. This figure shows, among other things, the states of areas 1US, 5C, and 4C. The slope of the line connecting states 5C and 4C in this figure has speed $v^{[4C-5C]}$ (km/h). The slope of the line connecting states 1US and 4C has speed $v^{[4C-1US]}$ (km/h) which is given by:

$$v^{[4C-1US]} = \frac{\bar{\rho}^{[4C]} v_{eff}^{[4C]} - q^{[1US]}}{\bar{\rho}^{[4C]} - \rho^{[1US]} \cdot (3-54)}$$

Hence, by tuning the density $\bar{\rho}^{[4C]}$, the slopes of these two lines can be changed. Note that in Figure 3-7 a minimum density $\rho^{[5C]}$ and a maximum density $\rho^{[4C]}$ have been indicated. The density in area 4C should not be chosen lower than the minimum density which is given by:

$$\rho^{min} = \rho^{[5C]} \cdot (3-55)$$

Additionally, the density $\bar{\rho}^{[4C]}$ should not exceed the maximum density given by:

$$\rho^{max} = \frac{q^{[5C]}}{v_{eff}} \cdot (3-56)$$

These extreme densities ensure that the stabilisation area 4C is bound and not increasing in size over time. So, when exceeding the maximum density, the S-head line will propagate downstream making the area in the state grow larger in time; this is undesirable from the point of view of implementation. However, this maximum density $\rho^{max}$ does not guarantee stable traffic. The density $\bar{\rho}^{[4A]}$ in area 4A has been tuned to realize stable traffic and exceeding this density can result in unstable traffic. Therefore, the density $\bar{\rho}^{[4C]}$ should be chosen in the following interval:

$$\rho^{min} \leq \bar{\rho}^{[4C]} \leq \max \left(\rho^{[4A]}, \rho^{max} \right) \cdot (3-57)$$

Now that the bounds in which the density $\bar{\rho}^{[4C]}$ can be chosen have been defined, the value of the density should be chosen. Note that the speed with which the stabilization area 4C is propagating upstream
decreases with increasing density $\rho_{4C}$. Reducing this speed will help to limit the length of the freeway stretch over which vehicles have to be speed-limited. This is beneficial when implementing this approach in practice. Therefore, the density $\rho_{4C}$ should be chosen as large as possible:

$$\rho_{4C} = \max \left( \rho_{4A}, \rho_{\text{max}} \right).$$  (3-58)

### 3-5-2-3 Imposing desired densities

In the previous section, we calculated the desired density in the different states in the stabilization area identified as 4A, 4B and 4C. The subsequent task is it to be able to identify when that specific density should be applied. Let’s refer back to the different cases for the control scheme illustrated in Figure 3-4.

It can be observed that the need for adjusting the stabilization area would arise in Case a and Case b; in Case c the stabilization area will be entirely upstream of the on-ramp.

Figure 3-7 identifies the theoretical traffic states in a space-time plot. States 4A and 4B are separated at the ramp location, while states 4B and 4C are separated by a shock wave propagating upstream at speed $v_{\text{eff}}$. This shock wave starts at the time when the S-head line reaches the on-ramp location. Therefore, the head and the tail location in state 4B is known at any given time. However, it must be determined when vehicles drive into state 4C.

**Identifying the upstream boundary of area 4A:**

The downstream location of the detector segment containing the on-ramp, $x_{d, \text{det}}$, demarcates the upstream boundary of traffic state 4A. Upstream of this location a lower density, $\rho_{4B}$, is applied. This ensures that the extra merging vehicles from the ramp do not cause instability in traffic of state 4A, which is set to achieve the maximum stable density achievable for flow at $v_{\text{eff}}$ speed.

**Identifying the upstream boundary of area 4B:**

There are two possibilities that can occur when imposing speed limits over density state 4B: the first is for high freeway volumes such that speed limitation must be extended over area 4C for traffic flow stability, and the second is in the case of low freeway inflow, in which case speed limitation in 4B is sufficient to stabilize the traffic.

In case of low flow condition, typically the S-head shock wave will terminate downstream of the on-ramp. If state 4C must exist, the S-head line will cross the on-ramp at the same time as the shock wave between states 4B and 4C. The shock wave speed is equal to the $v_{\text{eff}}$ since both these states are under speed limitation. Therefore, an estimate of the trajectory of the shockwave 4B-4C is useful to identify when state 4C is applicable upstream of the boundary of area 4B. This is achieved by determining the trajectory of the S-head line, the time it reaches the ramp, and finally, the upstream boundary of area 4B. These steps have been mathematically formulated below:

- The time when speed limits are released is the start location of S-head line. In COSCAL v2, it is determined by the last detection segment that changes from jam state to free flow state (Section 3-6). This detector index is known in real-time, after the speed release starts at $t_{S-h}$. Therefore, the exact trajectory of shock wave 4B-4C is not available before that time. To overcome this, the jam head (propagating at design speed $v_{\text{jam-h}}$) and the most recent R-tail line (propagating at $v_{\text{eff}}$) are used to predict the location of the start of the S-head shockwave. The intersection of the two fronts gives this desired time estimate.

With $i_{\text{jam-h}}(k)$ and $i_{\text{R-t}}(k)$ as the indices of the detector segments with the jam head and the R-tail line at the start of the current time step, the time $t_{S-h}^\text{start}(k)$ it would take for the start of speed release (S-head line) can be given as:

$$t_{S-h}^\text{start}(k) = \frac{x_{d, \text{det}}(k) - x_{u, \text{det}}(k)}{v_{\text{eff}} - v_{\text{jam-h}}}$$  (3-59)
The location of the start of speed release then becomes:
\[ x^{\text{start}}_{S-h}(k) = x^{u,\text{det}}_{S-h}(k) + v^{\text{eff}} t^{\text{start}}_{S-h}(k) \] (3-60)

This gives an interim estimate of the associated detector segment \( S-h^{\text{start}} \), where \( x^{u,\text{det}}(S-h^{\text{start}}) < x^{\text{start}}_{S-h}(k) \leq x^{d,\text{det}}(S-h^{\text{start}}) \) holds. The estimate is replaced once the actual detector segment where the jam is resolved is located.

- Under the assumption that the S-head line is not terminated before it crosses the on-ramp, the hypothetical time \( t^{\text{ramp}}(S-h)(k) \) is calculated to check if density 4C applies. The location of the start of S-head line and its slope gives:
\[ t^{\text{ramp}}(S-h)(k) = t^{\text{start}}_{S-h}(k) + \frac{x^{\text{start}}_{S-h}(k) - x^{\text{ramp}}_{S-h}(k)}{v(S-h)(k)} \] (3-61)

- With the time when the S-head line reaches the on-ramp known, the equation of the shockwave 4B-4C can be determined. In the event that state 4C occurs, it will necessarily be upstream of shockwave 4B-4C. Therefore, the location of the most upstream detector segment \( i^{\text{det}} \), that achieves an average density \( \bar{\rho}^{[4B]} \) between \( v^{\text{eff}} \) and \( v^{\text{det}} \), is of interest. If \( v^{\text{det}} \) lies upstream of the estimated location of the shockwave, \( x^{[4B-4C]}(k) \) at a given time, state 4C exists. Then, \( x^{[4B-4C]}(k) \) defines the boundary of area 4B. To include the time it takes the first vehicle that arrives at \( v^{\text{det}} \) when speed-limitation starts to decelerate to \( v^{\text{eff}} \), an additional deceleration time \( t^{\text{dec}} \) and distance \( x^{\text{dec}} \) are added.

The shockwave 4B-4C trajectory can be given as:
\[ x^{[4B-4C]}(kT + t^{\text{dec}}) = x^{\text{ramp}} - v^{\text{eff}}(t^{\text{ramp}}(S-h)(k) - t^{\text{dec}}) \] (3-62)

Then, the condition to check for state 4C becomes \( x^{u,\text{det}} + x^{\text{dec}} < x^{[4B-4C]}(kT + t^{\text{dec}}) \); if it holds the \( x^{[4B-4C]}(kT) \) defines the upstream boundary of state 4B, and target density in state 4C, \( \bar{\rho}^{[4C]} \) must be applied upstream of it.

The assumption of S-head crossing the on-ramp does not affect the outcome if it terminates downstream of the ramp. In this case the above condition will not hold and \( \bar{\rho}^{[4B]} \) will be correctly applied.

The core principle used in estimating the most upstream detection segment \( i^{\text{det}} \) of the stabilisation area remains the same, given in equation (3-39). However, with three different densities in the stabilization area, the scheme first checks for the most upstream stabilization state. Then the target density is applied accordingly. To ensure that the appropriate density is applied \( i^{\text{det}} \) is checked for the cases below:

\[ \bar{\rho}(k) = \begin{cases} \bar{\rho}^{[4A]} & \text{if } x^{\text{d,ran}} \leq x^{u,\text{det}}(k) + x^{\text{dec}} \\ \bar{\rho}^{[4B]} & \text{if } x^{[4B-4C]}(kT + t^{\text{dec}}) \leq x^{u,\text{det}}(k) + x^{\text{dec}} < x^{\text{d,ran}} \\ \bar{\rho}^{[4C]} & \text{otherwise} \end{cases} \] (3-63)

This check ensures that density \( \bar{\rho}^{[4A]} \) is applied downstream of the ramp, \( \bar{\rho}^{[4B]} \) is applied between the on-ramp and the extreme 4B-4C boundary, and \( \bar{\rho}^{[4C]} \) upstream of this boundary.

Finally, in addition to the choice of desired density based on the \( i^{\text{det}} \) location, the downstream segment \( i^{\text{d,ran}} \) of the stabilization state in consideration also changes. Here, \( i^{S-h} \) is the index of the detection segment containing the R-tail or S-head line depending on whether the jam has been resolved or not, respectively. Further, \( i^{[4B-4C]} \) is the detection segment containing the shockwave 4B-4C. The most downstream segment of the most upstream stabilisation state is therefore given as:
\[
i_{d,\text{det}} = \begin{cases} 
\text{i-\text{line}} & \text{if } x_{i_{\text{ramp}}}^{\text{d, det}} \leq x_{i_{\text{det}}}^{\text{u, det}}(k) + x_{\text{dec}} \\
\text{i-\text{Ramp}} & \text{if } x_{i_{\text{4B-4C}}}^{\text{4B-4C}}(k + t_{\text{dec}}) \leq x_{i_{\text{det}}}^{\text{u, det}}(k) + x_{\text{dec}} < x_{i_{\text{ramp}}}^{\text{d, det}} \\
\text{i-\text{4B-4C}} & \text{otherwise}
\end{cases}
\] (3-64)

It is important to note that once a new upstream state is identified (state 4B or 4C), the density in the downstream stabilization states is no longer checked, and \(i_{d,\text{det}}\) is updated as per the above equation. \(N\) is then accumulation in the most upstream stabilization state. It equals the total number of vehicles between \(i_{d,\text{det}}\) and an upstream detection segment \(i_{\text{det}}\). The effective distance \(\Delta x\) used to check for the appropriate density therefore is the length of the freeway between \(i_{d,\text{det}}\) and \(i_{\text{det}}\). The condition \(N \Delta x \leq \bar{\rho}\) to find the most upstream segment \(i_{\text{det}}\), given in equation (3-39), is adapted such that \(\bar{\rho}(k)\) and \(i_{d,\text{det}}\) are now determined using equations (3-63) and (3-64).

### 3-5-3 Correction for density errors in downstream stabilization states

When making a transition from state 4A to 4B or 4B to 4C, the actual density achieved in the downstream state may not be equal to the desired density. Therefore, when locating the most upstream segment of the most upstream stabilization state, the actual density error in the downstream stabilization states is accounted for. While a positive density error, where the actual density is higher than the desired density, is accommodated by suitably increasing the stabilization area, a negative error would then mean reducing the freeway length over which speed limits are applied. The latter can, however, cause a local spike in density leading to a breakdown even if the average density in the complete stabilization area is below the desired value. Therefore, only a negative density error will result in a correction.

We now discuss the procedure to adjust the upstream stabilization area according to the achieved density in downstream stabilization states, denoted by \(\rho_{\text{state,ds}}\) compared to their desired values, \(\bar{\rho}_{\text{state,ds}}\). Firstly, at any given time instant, the spatial extent of the different stabilization states in the following time step must be calculated. The effective length in each of the stabilization states at any given time, cumulated over all lanes, is estimated based on the location of \(i_{\text{det}}\) relative to the extreme location of the shockwaves 4A-4B and 4B-4C. The lengths can be given as:

\[
L_{\text{4A}}^{(k)} = \sum_{i=\text{max}(i_{\text{det}},i_{\text{ramp}}+1)}^{\text{i-\text{line}}} L_i \lambda_i \\
L_{\text{4B}}^{(k)} = \sum_{i=\text{min}(i_{\text{ramp}}+1,\text{max}(i_{\text{det}},i_{\text{4B-4C}})+1)}^{i_{\text{ramp}}} L_i \lambda_i \\
L_{\text{4C}}^{(k)} = \sum_{i=\text{min}(i_{\text{4B-4C}}+1,i_{\text{det}})}^{i_{\text{4B-4C}}} L_i \lambda_i
\] (3-65)

The compensation scheme is designed to provide as much surplus gaps in the most upstream state as required for the number of surplus vehicles downstream. The extra number of vehicles are the difference of the actual accumulation and that desirable to achieve the densities calculated in Section 3-5-2, over their lengths of actuation calculated in the preceding equation (3-65). The surplus accumulation \(N_{\text{sur}}(k)\) can then be given as below, where D is the set of all downstream stabilization states:

\[
N_{\text{sur}}(k) = \sum_{d \in D} \max(\rho_{\text{state,ds}} - \bar{\rho}_{\text{state,ds}}, 0) L_{\text{state,ds}}^{(k)}(k)
\] (3-66)
To ensure space for the surplus vehicles, the actual accumulation on a given freeway segment plus the additional \( N_{\text{sur}}(k) \) vehicles, should meet the desired density. The governing condition to locate the most upstream speed limited detector segment \( \frac{N}{\Delta x} \leq \rho \) then becomes:

\[
\frac{N + N_{\text{sur}}}{\Delta x} \leq \rho^{\text{[state,us]}}
\]

(3-67)

where

\[
N = \sum_{i} L_i \lambda_i,
\]

\[
\Delta x = \sum_{i} L_i
\]

3-6 TASK 4: Speed limit release

Since the speed in the stabilization area is constant and the density is more or less homogeneous, the speed limits can be released along a straight line in the time-space plane, from downstream to upstream, similarly to SPECIALIST and COSCAL v1. Let us call this line the S-head line. After releasing the speed limit along the S-head line, the vehicles will accelerate to a free-flow state with a lower density than in the stabilization area. The S-head line should begin at the point when and where the last vehicle in the jam leaves the jam (corresponding to point D in the SPECIALIST scheme). In case of COSCAL v2 this is defined as the head of the last detection segment that has changed from jam state to free flow state. The same S-head line should apply for all vehicles in the stabilization area. The slope of the S-head line \( v^{[A-,A]} \) is a tuning variable, and the more steep it is (more negative) the higher the resulting flow will be.

3-7 Resolvability of jam

Some jams cannot be resolved, and for these jams intervening with speed control measures is not meaningful. For the COSCAL v2 algorithm a jam cannot be resolved when the most upstream vehicle that has to be slowed down is physically outside (upstream) of the stretch that can be controlled by speed limits. In such a case it makes no sense to reduce the speed of the other vehicles, because the jam will not be resolved and the associated capacity drop will not be removed. Since the algorithm has a feedback structure, the vehicle in question may vary, and consequently the resolvability of the jam may fluctuate when in one case the resolving vehicle is within the speed-limited stretch, and in the other case it is not. This would mean that the algorithm decides in one time step to set the speed limits, and in the next time step to remove them. This is undesired, and therefore the initial tail location of the resolving actuation segments should be such that it remains within the physically available stretch, including the fluctuations. For this reason the algorithm may only be activated if the initial tail location \( x^u_{\text{act},i} \) of the most upstream actuation segment \( i^{\text{act}} \) (including the lead-in) is downstream of the pre-defined location \( x^{\text{act},\text{min}} \):

\[
x^u_{\text{act},i} \geq x^{\text{act},\text{min}},
\]

(3-68)

where \( x^{\text{act},\text{min}} \) should be sufficiently downstream of the upstream end of the stretch equipped with dynamic speed limits to make sure that all fluctuations remain within the controllable area.

Once the algorithm activated the speed limits, the threshold \( x^{\text{act},\text{min}} \) is ignored, in order to allow fluctuations that are within the physically available space (but are possibly upstream of \( x^{\text{act},\text{min}} \)).
In addition, there is another case when the complete speed limit scheme will not fit on the physically available stretch, namely when the stabilization area grows out (upstream) of the available area. In this case the jam can be resolved, but the stability of the upstream traffic cannot be guaranteed. Since in this case the jam can be resolved, and at least a temporal flow improvement can be achieved, one may decide to accept the risk that a new jam will occur. However, if this type of breakdown has to be prevented $x_{\text{act.min}}$ can be chosen even more downstream.

### 3-8 Limiting the algorithm to a single jam

In the development of the algorithm it is implicitly assumed that there is only one jam on the freeway. However, in a real situation there may be more than one jam at the same time, and it could lead to unpredictable behavior when the speed limits are active for one jam, but another jam requires speed limits at an overlapping stretch. For this reason the algorithm is limited to activate for a single jam and will not try to solve another jam until all speed limits are deactivated.

To achieve this, after a jam has been detected and the speed limits are activated to resolve it (i.e., the jam is considered to be resolvable) the jam head is tracked until it has been resolved. The tracking of the jam head ensures that the speed limits will be activated only due to this specific jam, and not to others that possibly appear during operation. Furthermore, new jams are ignored until all speed limits have been released, including the speed limits for traffic flow stabilization. This is necessary, because after the jam has been resolved, there will be remaining active speed limits in the stabilization region. These speed limits should not be disturbed by speed limits due to a new jam. Therefore, new jams are ignored until all speed limits have been resolved.

The jam is tracked by tracking its head propagation over time. Since the jam head speed $v_{\text{jam-h}}$ is limited, the jam head location from time step $k$ to $k+1$ may be between the two locations what can be expected based on the minimum and maximum jam head propagation speed. This speed is assumed to be $v_{\text{jam-h}}$, but due to measurement errors and the discretization of time and space, the measured jam head may propagate somewhat slower or faster then $v_{\text{jam-h}}$ and therefore the fastest propagation speed is assumed to be $v_{\text{jam-h, max}}$ (km/h), such that $v_{\text{jam-h, max}} < v_{\text{jam-h}}$ (more negative), and the slowest jam head propagation speed is assumed to be zero. If the jam head location in time step $k$ was $x_{\text{jam-h}}(k)$, then for time step $k+1$ the jam head is required to be at a segment between $x_{\text{jam-h}}(k)$ and $x_{\text{jam-h}}(k) + T v_{\text{jam-h, max}}$. The most downstream segment that is in jam state and satisfies this condition, is taken as the new jam head.

Since the detection of a new jam should be postponed not only for the duration of an already existing jam, but also for the duration of the release of the stabilizing speed limits after the jam has been resolved, the following steps are taken:

- If there is a jam detected, but there was no jam in the previous time step and the speed limits were not activated in the previous time step then the detected jam is a new jam and the speed limits may be activated.
- If there is a jam detected, but there was no jam in the previous time step and the speed limits were active in previous time step (for stabilization), then no jam location is passed to the rest of the algorithm.
- If there is a jam detected, and there was a jam in the previous time step, the jam is tracked according to the constraints above. If the same jam still exists in the current measurement then only this jam is passed to the rest of the algorithm as jam location. Otherwise, the jam under consideration has been resolved, and the currently measured jam is a new one, that should be ignored until all speed limits are resolved.
- If no jam is detected, then the algorithm should either continue with the already active speed limits (for stabilization) or do nothing, depending on the stabilization part of the algorithm.
Summary and Discussion

In this chapter, the COoperative Speed Control ALgorithm (COSCAL) v2 in Hegyi (2013) was extended for integration with ramp metering (RM). The macroscopic algorithm uses VSL in four main tasks to resolve a moving jam, and subsequently stabilize the traffic flow while it recovers from the capacity drop. For the integration of RM and VSL strategy, two of these tasks, namely, (1) jam detection, and (2) speed-limitation for stabilization were modified. The traffic theoretic principles used in the original algorithm were utilized for this.

Jam detection task in COSCAL v2 uses instantaneous speed-limitation for flow reduction in order to resolve a moving jam, whereby the inflow into the jam is reduced below the outflow at the jam-head. Hence, when extra vehicles from the on-ramp enter onto the freeway, the spatio-temporal extent of speed-limitation required for this task is under-estimated. In the modified algorithm, the excess vehicles from RM were estimated to determine the freeway length necessary to be speed-limited for jam resolution.

In the stabilization task, vehicles upstream of the ones used for resolving the jam are speed-limited to achieve a maximum flow efficiency (that ensures traffic flow stability) after the jam is resolved. Likewise, ramp flows can disrupt the stabilization area where the traffic state is likely to become metastable. Therefore, in order to prevent a traffic breakdown from the RM flow, the algorithm was adapted to determine lower target densities for the speed-limited area upstream of the on-ramp. These densities are chosen and implemented in a way that the flow arriving at the ramp section is appropriately reduced to accommodate the additional ramp flow.

Most parameters used in the COSCAL v2 algorithm can be interpreted as a traffic flow variable or a physical attribute of the infrastructure. For the extension of the VSL algorithm, a few additional parameters were considered:

Ramp infrastructure related
- the location \( x^{\text{ramp}} \) of the on-ramp
- the merging length \( x^r \) and the average speed \( \bar{v}^r \) on the merging segment

RM strategy related
- the RM flow \( q^{\text{metered}} \)
- the ramp flow \( q^{\text{congested}} \) merging into freeway flow in congestion

Freeway traffic related
- the average speed \( v^{\text{jam}} \) in moving jam state
- the average free-flow speed \( v^{\text{ff}} \) of vehicles in state [5A]

All of the above parameters, except RM flow \( q^{\text{metered}} \) can be tuned using off-line or on-line traffic data. Based on the desirable characteristics for a ramp controller, the RM flow \( q^{\text{metered}} \) must be chosen to prevent both, a queue spillback and underutilization of the on-ramp storage capacity. Additionally, a low RM rate should theoretically improve the effectiveness of the VSL approach.

The above discussion highlights the caveat in the developed strategy. Even though the simple RM strategy is suitable for field-implementation, it is not as sophisticated as reactive RM strategies. Moreover, it lacks responsiveness to how queue on the on-ramp grows. If queue length constraint is indirectly considered by selecting a high enough RM flow that ensures that the queue-length does not exceed a maximum value, it will be the most restricting value. Hence, at the cost of the effectiveness of the VSL scheme.
In order to incorporate a more advanced RM strategy, which responds to the traffic state on the freeway and queue length on the ramp, a more advanced adaptation for the VSL strategy is required. As opposed to the macroscopic adaptation in this chapter, where density criteria for the speed-limited area is used to limit the freeway flows arriving at the on-ramp section, an advanced strategy will require microscopic traffic flow concepts to control freeway flows directly according to time-dependent RM flows. Accordingly, an advanced RM and VSL strategy is developed in the next chapter.
Chapter 4

Advanced Approach for Ramp Metering with COSCAL v2

4-1 Introduction

In the previous sections, we first discussed the basic formulation of stand-alone speed control for road-side implementation. Subsequently, this control approach was adapted for additional flow from an on-ramp infrastructure, which may disrupt implementation of speed limits. The assumption of a constant outflow from ramp metering (RM) was made for this extension. Lastly, a corrective feedback for realised densities in the stabilization areas that are higher than their design values was incorporated.

In this section, an advanced RM strategy integrable with the speed control approach is presented. The most important considerations for the RM strategy have been: responsiveness to limitation of storage space on the on-ramp, and at the same time limitation on reducing main stream flow with the variable speed limits (VSL) approach.

In a very rudimentary understanding, a few fewer vehicles from the main traffic stream would allow a few more to merge from the on-ramp. This explains the trade-off between any measurable performance criteria - total time spent (TTS) or waiting times between the two streams. On one hand, a lower metering rate means higher waiting times for the on-ramp traffic, on the other hand, it improves the supply on the freeway and its corresponding travel times. Hence, the design goal is to formulate and integrate a RM strategy that maximizes the performance of the VSL strategy, while ensuring that at no time during the control scheme the on-ramp queue spills over to the surface streets.

4-2 Assumptions and design parameters

4-2-1 Notations and notions

The notations for detection and actuation segments are in line with those used for the basic ramp metering strategy, detailed in Section 3-2-1. To simplify the theoretical explanation, three traffic streams are identified as: (1) freeway main stream flow: \( q_{fw} \) (2) on-ramp flow \( q_{rm} \) and, (3) combined flow \( q_{comb} \) at the on-ramp section. All traffic characteristics related to each of these traffic streams are denoted by a subscript ‘\( f\)’, ‘\( r\)’ or ‘\( m\)’ depending if the ramp flow is metered or not, and ‘\( comb\)’, respectively. Cumulative vehicle curves - derived from plotting the number of vehicles that have crossed a specific location at a given
time instant - are used extensively and follow the same labelling convention. Additionally, a ‘max’, ‘min’, ‘max,adm’ or ‘min,adm’ superscript specifies when the curve forms an admissible or limiting boundary condition (detailed later in the chapter). In general, cumulative curves are calculated at the merged freeway section, just downstream of the on-ramp.

4-2-2 Assumptions related to on-ramp flows

- A single lane on-ramp infrastructure is assumed for the ease of control formulation. The choice does not have an impact on the formulation of the integrated strategy.

- The on-ramp demand $q_{in}^r(k)$ (veh/h) is known over the time duration of speed control, and the control itself does not affect this demand from re-routing.

  The assumption allows to develop an anticipatory control that can adapt RM and VSL strategies based on the knowledge of future ramp demand.

- The storage capacity on the on-ramp is limited to a maximum of $s_{max}^r$ (veh/lane). However, the queue controller is designed to not exceed a desired queue length $s_{des}^r$ (veh/lane) ≤ $s_{max}^r$ at any time. $s_{des}^r$ has practical relevance; it is a tuning parameter that can compensate for inaccuracies in counts from loop detectors, demand prediction, and queue length estimation.

- A minimum on-ramp queue $s_{min}^r$ (veh/lane) is assumed. In the integrated control approach, $s_{min}^r$ is strategically used to keep a minimum queue at the on-ramp at all times.

  Additionally, $s_{min}^r$ gives a generic formulation which allows changing the minimum utilization of the ramp storage, if so required by a higher-level network control.

- A ruling threshold $[q_{min}^rm, q_{max}^rm]$ (veh/s/lane) is assumed for RM. This follows from the minimum and maximum cycle time constraints for the traffic signal at the ramp exit.

- The effects of merging efficiency and lane distribution on the freeway are not included theoretically in the integration of the scheme.

In the following sections, the details of the RM strategy and its integration with COoperative Speed Control ALgorithm (COSCAL) v2 are presented. There are two possibilities for disruption of speed control scheme from ramp flows: (1) when the ramp flow merges into the jam-resolving area, i.e. TASK 2, and (2) when the ramp flows joins the traffic speed-limited for stabilization, i.e. TASK 3. In this chapter, the focus remains on TASK 3 which requires developing a more advanced approach for the VSL strategy. Adaptation of TASK 2 follows similarly as in Chapter 3, and is therefore not included.

4-3 RM integration with TASK 3 of COSCAL v2 - speed limitation for stabilization

Principally, the TASK 3 of COSCAL v2 is designed to recover a desired free flow state after resolving a moving jam. The area speed-limited for stabilization is bound between shockwaves R-tail and S-tail until the jam is resolved and between S-head and S-tail after that, as shown in Figure 3-7. The speed of the S-head shockwave is a design parameter that can be varied to adjust the flow exiting the speed limited area. Additionally, the propagation speed of the S-tail front, i.e. the speed at which speed-limits are extended upstream, can control the main stream flow entering speed-limitation.

As discussed earlier in Section 4-2, $q_{fw}$ and $q_{rm}$ traffic streams combine to enter the merged freeway section resulting in $q_{comb}^r$. To achieve a particular $q_{comb}^r$ at this section, either $q_{fw}$ or $q_{rm}$ may be regulated. This requires some design choices to be made in the integrated control strategy. To that end, the different situations that may occur at the on-ramp section, depending on a VSL activation downstream of it, offers a starting point to understand what is desirable for the system. These are discussed before elaborating on the design principle for the RM strategy.
4-3-1 Scenarios of stabilization scheme at the merged freeway section

The location where the jam is detected compared to the on-ramp location, and the freeway demand profile determine the development of the speed-limitation scheme at the on-ramp section. The different scenarios that may occur are essentially based on the time the S-tail and S-head fronts of the stabilization area cross this location. Figure 4-1 illustrates three possible scenarios; each scenario shows the base case that assumes zero ramp flow and the influence of an additional constant RM flow. Assuming a constant RM flow allows a clear understanding of the core mechanisms that can then guide the design choices for the advanced RM strategy. The traffic states notation used in the basic RM formulation is used here.

In contrast to a base case with zero RM flow, any additional inflow increases the propagation speed of the S-tail shockwave. This is because, in order to realize the target density for a higher inflow requires extension of speed-limits further upstream than in the base case. Microscopically, the faster the tail propagates upstream, the lesser is the time difference between the application of speed limits on any consecutive vehicles. This results in a lower compaction, as desired for the higher flow.

The relevance of identifying these scenarios relates to the flow capacity at the on-ramp section. The capacity at the on-ramp section varies depending on whether the merged traffic stream \( q_{\text{comb}} \) is in free flow or under speed-limitation. In this work, we assume that the free flow capacity of the on-ramp section is higher than the flow in the stabilization state, i.e. \( q_{\text{comb}}^{4A} = \rho 4A v_{\text{eff}} \). Now, the scenarios will be briefly discussed.

(a) Scenario 1: Task 3 ends downstream of the on-ramp in both the base case and with RM.

(b) Scenario 2: Task 3 ends downstream of the on-ramp in the base case but crosses the on-ramp with RM.

(c) Scenario 3: Task 3 ends upstream of the on-ramp in both the base case and with RM.

**Figure 4-1:** Three possible scenarios of the stabilization scheme at the on-ramp. For each case, the base case without any on-ramp flows is contrasted with the expected progression of speed-limitation with constant ramp metering. The capacity at the on-ramp section is \( q_{\text{comb}}^{\text{free}} \) when the freeway traffic is in free flow condition, and \( q_{\text{comb}}^{\text{sl}} \) when the flow is speed-limited. This is indicated over time intervals with ‘ff’ and ‘sl’ symbols, respectively.

In the first scenario speed limitation finishes downstream of the on-ramp, both in the base case as well as with additional \( q_{\text{rm}} \) flow. However, one can notice in Figure 4-1a that due to the faster propagation of S-tail...
shockwave with RM, the scheme ends at a later time than in the base case. Clearly, the capacity of the on-ramp section in this scenario corresponds to its free flow capacity at all times.

In the second scenario, the S-tail does not pass the on-ramp in the base case but does with additional ramp flows. Once the S-tail passes the on-ramp, the on-ramp section is under speed limitation until the S-head passes at a later time. For the on-ramp vehicles to merge under speed-limitation, the freeway flow \( q_{fw} \) arriving from the upstream side must keep a lower density than before. This results in an even faster propagation of the S-tail upstream of the on-ramp, referred as S-tail2 in Figure 4-1b. The S-tail2 trajectory continues until the last main stream vehicle that enters the on-ramp section under speed-limitation regime is speed limited. An important remark here is that in order to provide an acceptable headway for \( q_{rm} \) flow at the on-ramp section, the density within the entire upstream state 4B must be decreased. This creates an inefficient region in this area. After the S-head passes the on-ramp location, free flow state is resumed at the on-ramp section.

In the third scenario, the S-tail crosses the ramp location with and without \( q_{rm} \) flows. The speed-limitation regime at the on-ramp section follows similarly to the previous scenario. The regime at the on-ramp section has been specified accordingly in Figure 4-1c. Similarly to the S-tail above, the S-head (labelled S-head2) front propagates faster to achieve a lower flow in state 5B. This is necessary so that the flow in state 5A and the ramp flow together can achieve the desired flow in downstream state 5A. Furthermore, based on the chosen density in traffic state 4C, the scheme resolves at a later time than in the base case.

From the above discussion, the importance of the time after the start of the control scheme that the S-tail and the S-head fronts cross the on-ramp section becomes evident. Since the speed of the S-head is a design variable, its corresponding crossing time \( t_{S-h}^{ramp} \) is easily computable. However, the time \( t_{S-t}^{ramp} \) when the S-tail crosses, is influenced by the freeway state and the RM strategy adopted. The next section details the methodology to estimate these time instants.

### 4-3-2 Calculation of the time S-head and S-tail cross the on-ramp section

The time when the S-head and S-tail shockwaves cross the ramp location determine the flow capacity profile at the on-ramp section. Therefore, a prediction of these times is necessary for determining the RM strategy.

The notation \( t_{ramp}^{S-h} \) denotes the time when a vehicle or shockwave crosses the on-ramp section. In line with it, \( t_{S-t}^{ramp} \) and \( t_{S-t}^{S-h} \) are respectively the times that the S-head and S-tail are predicted to reach the on-ramp.

Using the predicted location of the start of S-head shockwave, the location of the on-ramp and the propagation speed of S-head, \( t_{S-t}^{amp} \) can be determined easily, as derived in equation (3-61). Further, COSCAL v2 determines the extent of speed-limitation by checking for a target density within the controlled area. Ensuing, at time \( t_{S-t}^{ramp} \), the density downstream of this section should be the target density in state 4A: \( \rho_{[4A]} \).

The accumulation over the freeway sections between the S-tail (i.e. the most upstream segment under speed limits) and the on-ramp section is available from the most recent sensor data; lets denote it as \( N(k) \) (veh). Let \( i_{S-t}^{S-t} \) and \( i_{ramp}^{ramp} \) denote the detector segment indices containing the S-tail line and the on-ramp, respectively. Then, \( N(k) \) can be calculated directly from the available density measurements; here \( L \) denotes the length of the detector segment, \( \lambda \) the corresponding number of lanes, and \( \rho \) the average density on it. The estimate can be be given as:

\[
N(k) = \sum_{j=i_{ramp}^{ramp}}^{i_{S-t}^{S-t}} L_j \lambda_j \rho_j(k) \tag{4-1}
\]

The accumulation \( N(\tilde{k}) \) (veh) at any future prediction time is the result of two fluxes: (1) the inflows \( q_{rm} \) and \( q_{fw} \) arriving at the on-ramp section, and (2) the outflow at its head during the same interval. These
fluxes have been indicated in Figure 4-2. Note, $\tilde{k}$ is the index of a future time step for which the prediction is made based on real-time data available at the current time step $k$.

Now, for the S-tail to cross the on-ramp section, the average density over the total length $L$ (refer to Figure 4-2) should be $\bar{\rho}[4A]$. Then, the difference of the measured accumulation $N(k)$ from the target accumulation required to achieve this density must be compensated by the two fluxes. The deficit in the desired number of vehicles over length $L$, $N^{def}(k)$, can be given as below:

$$N^{def}(k) = \bar{\rho}[4A] \left( \sum_{j=\hat{t}}^{\tilde{k}} L_j \lambda_j \right) - N(k)$$  \hspace{1cm} (4-2)

The inflow flux is the combined freeway and RM flow that arrives at the on-ramp section, between time $kT$ and $\tilde{k}T$. However, this should not exceed the free flow capacity $q_{cap,ff,comb}^{in}$ (veh/h) at the on-ramp section. Therefore, the cumulative influx can be given as the minimum of the two demands: the sum of $q_{in}^{in}$ from the on-ramp and $q_{in,ramp}^{in,comb}$ arriving in free flow, and the free flow capacity at the on-ramp section:

$$N^{in}(\tilde{k}|k) = \min \left( \sum_{j=k}^{\tilde{k}} \left( q_{in}^{in}(j) + q_{in,ramp}^{in,ramp}(j) \right), q_{cap,ff,comb}^{in} \right)$$  \hspace{1cm} (4-3)

The cumulative outflow flux follows from the flow in the speed-limited state 4A, $q_{4A}$, and can be given as:

$$N^{out}(\tilde{k}|k) = q_{4A} \times (\tilde{k} - k)T$$

$$= v_{eff}^{4A} \bar{\rho}[4A] \lambda \times (\tilde{k} - k)T$$  \hspace{1cm} (4-5)
Then, the S-tail crosses the on-ramp when the net of the two fluxes compensates for the deficit $N^{\text{def}}(k)$. The S-tail crosses the on-ramp location at the earliest time that this condition is satisfied:

$$N^{\text{in}}(\hat{k}|k) \geq N^{\text{def}}(k) + N^{\text{out}}(\hat{k}|k),$$

then

$$k_{S-t}^{\text{ramp}}(k) = \hat{k}$$

### 4-3-3 Constraints and design choices for the ramp metering strategy

In the integrated VSL and RM strategy, moving fronts of the speed-limited area are leveraged to regulate the $q_{fw}$ traffic stream, and RM to ensure controlled flow $q_{rm}$ from the on-ramp. However, the design of the RM strategy is limited by some constraints from the infrastructure, traffic flow dynamics and the control approach itself.

The constraints for each of the three traffic streams: $q_{fw}$, $q_{rm}$ and $q_{\text{comb}}$ are discussed individually. All constraints are described as cumulative vehicle curves that would finally determine a feasible solution space for the RM strategy. First, the origin of these constraints and their cumulative curve notation is given; the curves computable directly from the available data are given in bold, others involve more vigorous calculation. In the subsequent section, the calculation methodology of the cumulative curves will be presented.

#### 4-3-3-1 Constraints on the freeway main stream flow

The $q_{fw}$ arriving at the on-ramp section can be either in free flow or under speed limitation when it arrives at the on-ramp location. Given the two flow regimes, for every vehicle there is a time window within which it arrives at the on-ramp location. The bounds of the time window are given by the first two constraints. The third constraint follows from microscopic traffic flow dynamics.

- **FW1 – $N_{fw}^{\text{max}}(k)$ (veh): maximum number of freeway vehicles that can arrive at the on-ramp section before time $kT$**

  The earliest time when a vehicle may arrive at the ramp is determined by its current location and free flow speed $v_{ff}$. The earlier the vehicles arrive, the higher the number of vehicles that enter the on-ramp section. Therefore, a plot of these values in the $N_{fw} - t$ plane corresponds to the upper cumulative bound for the $q_{fw}$ flows.

- **FW2 – $N_{fw}^{\text{min}}(k)$ (veh): minimum number of freeway vehicles that can arrive at the on-ramp section before time $kT$**

  Similarly, the latest time when a freeway vehicle may arrive at the on-ramp section is when it is speed limited maximally. The corresponding $N_{fw} - t$ curve gives the lower cumulative bound for the $q_{fw}$ flows.

- **FW3 – Leader-follower dependency**

  The arrival time of the follower vehicle is dependent on the actual time that a leader vehicle arrives at the on-ramp section, illustrated in Figure 4-6.
Figure 4-3: Relation of the different constraints as cumulative curves (determined at the on-ramp section) on the freeway plane \( N_{fw} - t \) and the ramp plane \( N_{rm} - t \). The arrows in blue indicate the translation of cumulative curves on \( N_{fw} - t \) plane to \( N_{rm} - t \). The activation of the VSL scheme influences the capacity flow at the on-ramp section, and thereby the translation.

4-3-3-2 Constraints on the on-ramp flow

The primary constraints on the on-ramp flows follow from the queue restrictions on the on-ramp and overarching policy restrictions on the RM rates.

- **RM1** \( N_{rm}^{\text{max}}(k) \) (veh): maximum number of vehicles that can enter the on-ramp section from the on-ramp before time \( kT \)

  This cumulative curve in the \( N_{rm} - t \) plane follows from the on-ramp demand. The outflow from the on-ramp can be no more than its inflow. Therefore, \( N_{rm}^{\text{max}}(k) \) follows directly from the cumulative \( q_{rm}^m(k) \) profile and minimum queue-length condition.

  It should be mentioned here that it costs an incoming vehicle some travel time over the length of the on-ramp, before it merges onto the freeway. This translates to an equivalent delay between the inflow and the outflow curve for the on-ramp traffic. However, we have ignored this delay when considering the inflow profile as the maximum outflow curve.

- **RM2** \( N_{rm}^{\text{min}}(k) \) (veh): minimum number of vehicles that must enter the on-ramp section from the on-ramp before time \( kT \)

  The lower bound for the RM outflow is governed by the maximum queue-length assumption. The minimum cumulative ramp outflow curve must ensure that the queue on the on-ramp never exceeds its maximum design value. This curve can be determined directly from the cumulative \( q_{rm}^m(k) \) profile and the \( s_{rm}^{\text{max}} \) value.

- **RM3** \( N_{rm}^{\text{max},p}(k) \) (veh): policy constraint on the maximum RM rate
These constraints follow from the maximum cycle time for the ramp signal. It is often regulated by the traffic network managers due to policy considerations.

- RM4 – $N_{rm}^{max,p}(k)$ (veh): policy constraint on the minimum RM rate

Similarly to RM3, it follows from the minimum cycle time for the ramp signal.

4-3-3-3 Constraints on the combined flow at the on-ramp section

The constraints on the $q_{comb}$ traffic stream follow from the variations in flow capacity based on the evolution of the stabilization scheme itself. The time intervals where $q_{cap,ff}^{comb}$ and $q_{cap,al}^{comb}$ apply are illustrated in Figure 4-1. Essentially, $q_{cap,al}^{comb}$ applies when the freeway flow arriving at the on-ramp and the combined flow downstream of it are speed-limited. At all other times, when the freeway flow arriving at the on-ramp flow is in free flow regime, the free flow capacity $q_{cap,ff}^{comb}$ holds. Then, the prevailing capacity $q_{cap}^{comb}(k|k)$ at any time in the prediction horizon can be given as:

$$q_{cap}^{comb}(k|k) = \begin{cases} q_{cap,ff}^{comb}, & \text{if } kT < t_{ramp}^{S-h}(k) \\ q_{cap,al}^{comb} = q_{r}^{[iA]} \lambda v_{eff}, & \text{if } t_{ramp}^{S-h}(k) \leq kT < t_{ramp}^{S-h}(k) \end{cases}$$  \hspace{1cm} (4-8)

Given this total flow capacity of the combined flows $q_{rm}$ plus $q_{fw}$, all constraints on the freeway flow $q_{fw}$ translate to additional constraints for ramp flow $q_{rm}$, and vice versa. These additional constraints are given as admissible cumulative curves and are defined below.

- C1 – $N_{rm}^{min,adm}(k)$ (veh): minimum number of vehicles admissible from the on-ramp before time $kT$, to achieve the capacity flow at the on-ramp section, when traffic stream $q_{fw}$ arrives in free flow (maximal main flow)

It is the minimum admissible flow required to achieve capacity flow for the combined stream, when the main stream flow is at its maximum, corresponding to $N_{fw}^{max}$. Then, the cumulative curve is obtained directly as the difference of the prevailing capacity at the on-ramp section and the $N_{fw}^{max}(k)$ curve:

$$N_{rm}^{min,adm}(k) = T \sum_{k} q_{cap}^{(k)} - N_{fw}^{max}(k)$$  \hspace{1cm} (4-9)

- C2 – $N_{rm}^{max,adm}(k)$ (veh): maximum number of vehicles admissible from the on-ramp before time $kT$, to achieve the capacity flow at the on-ramp section, when the traffic stream $q_{fw}$ is speed-limited (minimal main flow)

The cumulative curve is obtained directly as the difference of the prevailing capacity at the on-ramp section and the $N_{fw}^{min}(k)$ curve:

$$N_{rm}^{max,adm}(k) = T \sum_{k} q_{cap}^{(k)} - N_{fw}^{min}(k)$$  \hspace{1cm} (4-10)

- C3 – $N_{rm}^{max,adm}(k)$ (veh): maximum number of vehicles admissible from the main stream when the ramp metering flow is minimal

The cumulative curve is obtained directly as the difference of the capacity of the on-ramp section and the $N_{rm}^{min}(k)$ curve.
4-3-4 Determining the feasible solution space for ramp metering

When all the constraints presented in the previous section are superimposed on the $N_{rm}$-t plane, we obtain a set of possible cumulative ramp flow values at each time step. A choice of cumulative outflow at each control time step, from within this range, then determines the RM rate at any given time. To that end, in this section we discuss how each constraint translates to a corresponding condition in the $N_{rm}$-t plane. The feasible solution space is defined as a region in the $N_{rm}$-t plane such that, from any given point at least one feasible RM trajectory exists until the end of the prediction horizon. The end goal is to determine the upper: $U(\tilde{k}|k)$ and the lower: $L(\tilde{k}|k)$ bounds of this feasible region; here $\tilde{k}$ is the index of a future time step for which the prediction is made based on real-time data available at the current time step $k$. The calculations are presented procedurally, depending on which inputs are known and which become available in successive steps.

4-3-4-1 Unregulated freeway flow upstream of the on-ramp

The freeway flow $q_{fw}$ is in free flow when the traffic stream is unregulated. Since vehicles can drive fastest in free flow, they arrive at the on-ramp section earliest in this regime. Recall that the $N_{fw}^{max}(i_{det}, \tilde{k}|k)$ curve (constraint FW1) is the cumulative vehicle count at the on-ramp section when flow $q_{fw}$ arrives in free flow regime. A point $(N_{fw}, \tilde{k})$ on this curve implies that a total of $N_{fw}$ mainstream vehicles can cross the on-ramp section at the earliest by time $\tilde{k}T$.

In order to determine the cumulative curve, it is assumed that the traffic stream is travelling at an average free flow speed $v_{ff}$, which is known. In practice, it could be determined as a moving average of speeds on detector segments further upstream of the VSL scheme.

The earliest time $t_{ramp, min}(i_{det})$ when the most upstream vehicle in each detector segment $i_{det}$ (according to the density measurements at time $kT$) segment passes the on-ramp section can then be given as:

$$t_{ramp, min}(i_{det}) = x_{ramp} - x_{u, det}$$

The cumulative number of vehicles that will cross before time $t_{ramp, min}(i_{det})$ is calculated below. Here, $\rho_j$ is as available from the traffic data at time step $k$.

$$N_{fw}(i_{det}, \tilde{k}|k) = \sum_{j=u, det}^{ramp} L_j \lambda_j \rho_j(k),$$

Ensuing, a plot of $(N_{fw}(i_{det}, \tilde{k}|k), t_{ramp, min}(i_{det}))$ in the $N_{fw}$-t plane gives the cumulative curve $N_{fw}^{max}(\tilde{k}|k)$.

The capacity at the on-ramp section is time-dependent and was expressed in equation (4-8). A capacity flow constraint necessitates that when the total unregulated demand at the on-ramp section exceeds the capacity flow $q_{cap}^{comb}(\tilde{k}|k)$ at that time, either $q_{rm}$ or $q_{fw}$ flow should be reduced. Further, notice in Figure 4-1 that the flow $q_{fw}$ is unregulated until the S-tail crosses, and must be speed-limited to be reduced.
Therefore, a design choice is made here, that the controller prefers to limit $q_{rm}$ over $q_{fw}$ until the S-tail shockwave has crossed the on-ramp. The rationale is that an increase in RM flow requires a proportional reduction of the freeway flow arriving at the on-ramp section. In order to achieve a lower freeway flow in the future requires speed-limiting vehicles upstream of the on-ramp before they arrive at the on-ramp. Hence, the stabilization area upstream of the on-ramp becomes less efficient in order to accommodate ramp flows. The higher the RM flows, the lower is the efficiency of the upstream speed-limited states (state 4B and 4C in the basic strategy).

Thus, the choice entails that the freeway traffic stream $q_{fw}$ is unregulated, i.e. follows the $N_{max}^{fw} (\tilde{k}|k)$ curve, for as long as possible (at this point, this is the time $t_{S-t}^{ramp} (k)$ that the S-tail is predicted to cross the on-ramp). Consequently, the RM strategy must not allow flows more than the difference of the arriving unregulated flow from the capacity at the on-ramp section.

The appropriate RM flows in this duration are determined by translating the $N_{max}^{fw} (\tilde{k}|k)$ curve to the $N_{rm}$-t plane. This gives the minimum admissible cumulative RM flow, $N_{rm, adm}^{min} (\tilde{k}|k)$ (constraint C2), and represents the ramp flow required to fully utilize the on-ramp section capacity. Since higher on-ramp flows can be allowed when the freeway traffic is speed-limited, the label minimum admissible signifies that the RM flows are more restrictive in this case. The translation is given below:

$$N_{rm, adm}^{min} (\tilde{k}|k) = q_{cap, comb}^{max} (\tilde{k}|k) T - N_{rm}^{max} (\tilde{k})$$

(4-13)

### 4-3-4-2 Formulation of the primary RM constraints in the $N_{rm}$-t plane

Next, the primary constraints for RM given in Section 4-3-3-2 are expressed as cumulative curves on the $N_{rm}$-t plane.

When the RM rate is maximum, the queue on the on-ramp will be minimum. Then, $N_{rm}^{max} (\tilde{k})$ curve (constraint RM1) can be calculated with the on-ramp demand, on-ramp queue $s_r (k)$ at the current time step, and the minimum desired queue length as:

$$N_{rm}^{max} (\tilde{k}|k) = \max \left( s_r (k) + T \sum_{j=k}^{\tilde{k}} q_{in}^{r} (j) - s_{min}^{r}, 0 \right)$$

(4-14)

Similarly, offsetting the cumulative $q_{in}^{r}$ profile by the maximum desired queue length $s_{des}^{r}$ gives the lower bound $N_{rm}^{min} (\tilde{k})$ (constraint RM2) for RM flows:

$$N_{rm}^{min} (\tilde{k}|k) = \max \left( s_r (k) + T \sum_{j=k}^{\tilde{k}} q_{in}^{r} (j) - s_{des}^{r}, 0 \right)$$

(4-15)

In addition to the queue regulation, the minimum and maximum allowed ramp outflow $[q_{rm}^{min}, q_{rm}^{max}]$ apply due to policy considerations (constraints RM3 and RM4). The corresponding cumulative curves $N_{rm}^{min, p} (\tilde{k}|k)$ and $N_{rm}^{max, p} (\tilde{k}|k)$ assume $q_{rm}^{min}$ and $q_{rm}^{max}$, respectively at all future times. The two curves can be given as:

$$N_{rm}^{max, p} (\tilde{k}|k) = q_{rm}^{max} (\tilde{k} - k) T$$

(4-16)
and

\[ N_{rm}^{min.p}(\tilde{k}|k) = q_{rm}^{min}(\tilde{k} - k) T \]  \hspace{1cm} (4-17)

Together, constraints RM1, RM2, RM3 and RM4 provide an ad-hoc upper and lower bound of the feasible area: \([U_{rm}(\tilde{k}|k), L_{rm}(\tilde{k}|k)]\).

\[ U_{rm}(\tilde{k}|k) = \min \left( N_{rm}^{max}(\tilde{k}|k), N_{rm}^{max,p}(\tilde{k}|k) \right) \]  \hspace{1cm} (4-18)

and

\[ L_{rm}(\tilde{k}|k) = \max \left( N_{rm}^{min}(\tilde{k}|k), N_{rm}^{min,p}(\tilde{k}|k) \right) \]

**Figure 4-4:** Plot of cumulative curves from primary ramp metering constraints for a simple ramp demand profile. An initial queue length of 50 veh; a policy maximum and minimum RM rate of 600 veh/h and 200 veh/h is assumed in this illustration. The red shaded area in \( N_{rm} - t \) plane then gives the feasible RM solution due to policy restrictions, and the grey shaded area gives the feasible RM solution from queue length constraints. The overlap of the two areas (hatched) is the resultant feasible solution space.
4-3-4-3 Adapting S-tail when total demand exceeds the capacity flow at the on-ramp

At this point, we have three curves in the $N_{\text{rm}}-t$ plane - the upper and lower bounds $[U_{\text{rm}}(\bar{k}|k), L_{\text{rm}}(\bar{k}|k)]$ from the primary RM constraints, and the $N_{\text{rm}}^{\text{min,adm}}(\bar{k}|k)$ cumulative curve. While the lower bound $L_{\text{rm}}(\bar{k}|k)$ corresponds to the minimum ramp flows required by the RM strategy, $N_{\text{rm}}^{\text{min,adm}}(\bar{k}|k)$ gives the maximum ramp flow allowable when the freeway flows are unregulated. Now, if the required RM flows are larger than the allowable, the freeway and the ramp flows together will exceed the capacity at the ramp section.

Therefore, if the lower bound $L_{\text{rm}}(\bar{k}|k)$ exceeds $N_{\text{rm}}^{\text{min,adm}}(\bar{k}|k)$ at some time $\bar{k}T$, it implies that even the minimum possible RM flow determined by the ramp controller is too high to satisfy the capacity constraint, if the freeway flow is not speed-limited. Consequently, the main stream flow $q_{\text{fw}}$ must be regulated, for which speed limits should have crossed the on-ramp before such a situation arises.

In other words, the S-tail must have crossed the on-ramp before the time that the $L_{\text{rm}}(\bar{k}|k)$ curve exceeds the curve $N_{\text{rm}}^{\text{min,adm}}(\bar{k}|k)$; we denote this cross-over time as $k_{\text{S-t}}^{\text{ramp,ext}}(\bar{k}|k)T$ (s). If this is not true and $k_{\text{S-t}}^{\text{ramp,ext}}(\bar{k}|k) < k_{\text{S-t}}^{\text{ramp,min}}(\bar{k}|k)$, calculated in equation (4-6), then the propagation of the S-tail shockwave must be adapted to cross the on-ramp sooner. Lets denote the smaller of the two time steps as $k_{\text{S-t}}^{\text{ramp,min}}(\bar{k}|k) = \min(k_{\text{S-t}}^{\text{ramp,ext}}(\bar{k}|k), k_{\text{S-t}}^{\text{ramp,min}}(\bar{k}|k))$.

If $k_{\text{S-t}}^{\text{ramp,min}}(\bar{k}|k) = k_{\text{S-t}}^{\text{ramp,ext}}(\bar{k}|k)$, then regardless of the S-tail position determined by the procedure described later in Section 4-3-6-2, the freeway flow must be controlled after time $k_{\text{S-t}}^{\text{ramp,min}}(\bar{k}|k)T$. This is achieved by enforcing VSL up on the on-ramp segment. Now, between time $k_{\text{S-t}}^{\text{ramp,min}}(\bar{k}|k)$ and the time that the S-head crosses the ramp location, the freeway flow $q_{\text{fw}}$ arriving at the on-ramp is speed-limited.

4-3-4-4 Regulated freeway flow upstream of the on-ramp

When the freeway flow upstream of the on-ramp is speed-limited, it implies that the vehicles can arrive at the on-ramp section later than in free flow regime. The cumulative curves related to the freeway mainstream flows under speed limits are of interest now.

We consider the most extreme case of speed-limitation. Here, the freeway segments upstream of the on-ramp are speed-limited simultaneously at the time $k_{\text{S-t}}^{\text{ramp,min}}(\bar{k}|k)T$, i.e. the time when the S-tail is determined to cross the on-ramp as per the prediction of the control scheme at time $\bar{k}T$ (or at the current time $kT$ if the S-tail has already crossed the on-ramp). This situation gives the latest time (equivalently, the lowest possible flows) that the mainstream vehicles can arrive at the on-ramp section. The cumulative curve $N_{\text{fw}}^{\text{min}}(\bar{k}|k)$ (constraint FW2) captures this restriction, and its formulation is described next.

The number of vehicles on a typical detection segment of a few hundred metres length, is of the order of magnitude 1-2. Due to the lack of traffic information about individual vehicles on a detection segment, a theoretical simplification is made here. We consider homogeneous traffic condition within a single detection segment. Further, the upstream end of each detection segment is assumed to be the rear bumper of the most upstream vehicle on it. Then, all vehicles on a segment, ahead of this vehicle, will arrive at the ramp section earlier than the vehicle itself.

From the density measurements over the detection segments at time $kT$, the location of the last vehicle on a detector segment $x_{\text{det}}^\text{m}$, at the time that it is speed-limited can be given as:

$$x_{\text{det}} = x_{\text{det}}^\text{u} + v_{\text{eff}} \max (k_{\text{S-t}}^{\text{ramp,min}}(\bar{k}|k) - k, 0) T$$

(4-19)

The time that this vehicle then arrives at the on-ramp section can be calculated using location $x_{\text{det}}$ and the effective speed under speed limits as:

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Figure 4-5: An illustration of the minimum admissible on-ramp flows (a cumulative function of the difference between freeway capacity and demand, 400 veh/h in this case) and the feasible RM solution from primary ramp flow constraints. The minimum desired RM flows (lower bound of the feasible area) exceeds the minimum admissible cumulative flow at a time earlier than the prediction of the time of arrival of the S-tail shockwave at the ramp location. S-tail shockwave is proactively adapted to cross the on-ramp at the time the curves cross-over.
\[ t_{ramp, \text{max}}(i_{\text{det}}) = \frac{x_{d, \text{det}} - x_{i_{\text{det}}}}{v_{\text{eff}}} \] (4-20)

The cumulative number of vehicles \( N_{fw}(i_{\text{det}}) \) that would cross before time \( t_{ramp, \text{max}}(i_{\text{det}}) \) is calculated in equation (4-12). Then upon interpolation, the \( N_{fw}-t \) curve: \( (N_{fw}(i_{\text{det}}), t_{ramp, \text{max}}(i_{\text{det}})) \) gives the \( N_{fw}^{\min}(\tilde{k}|k) \) cumulative curve.

Hence, at any time after \( k_{S}^{t_{ramp, \text{min}}}(k)T \), the feasible region in the \( N_{fw}-t \) plane lies between two extreme cumulative curves: \( N_{fw}^{\max}(\tilde{k}|k) \) and the revised \( N_{fw}^{\min}(\tilde{k}|k) \) (constraints FW1 and FW2). The former corresponding to \( q_{fw} \) is in free flow regime, and the latter to \( q_{fw} \) in speed-limited regime.

### 4-3-4-5 Formulation of the Leader-Follower constraint

We determined that the cumulative curves \( N_{fw}^{\max}(\tilde{k}|k) \) and \( N_{fw}^{\min}(\tilde{k}|k) \) in the \( N_{fw}-t \) plane enclose the feasible freeway flow curves. However, not all curves (flows) in this area can be realized. The reason is that some curves may correspond to very high or low flows that cannot be produced given the current vehicle spacing on the freeway, and for vehicle speeds between \( v_{eff} \) and \( v_{ff} \). This has been illustrated in Figure 4-6. Here, given a headway of \( \Delta x \) between two consecutive vehicles \( i \) and \( i+1 \), the following vehicle \( i+1 \) can not arrive, at the given location, sooner than its arrival time in free-flow. At the same time, it can not arrive later than its arrival time under speed-limitation.

![Figure 4-6: Arrival time dependency between a leader and follower due to car-following (microscopic) behaviour](image)

Therefore, to incorporate the leader-follower dependency (constraint FW3), some additional conditions must be checked. In essence, this constraint entails a dependency of the arrival time of a following vehicle, at a pre-specified location (on-ramp section in this case), on its leader’s arrival time.

However, this arrival time dependency does not include any restrictions on the value of \( \Delta x \), and the resulting density achieved inside the speed-limited (stabilization) area. In order to ensure that the density upstream of the on-ramp is not arbitrarily too high, we must also check if the resulting density is higher.
than the desired density \( \bar{\rho}_{\text{LA}} \). The corresponding maximal flow for this density is \( q_{\text{max}}^{\text{LA}} = \frac{v_{\text{eff}}}{\bar{\rho}_{\text{LA}}} \), and

then the minimum acceptable headway becomes \( \frac{1}{q_{\text{max}}} \). Hence, \( \Delta x \) should not be smaller than \( \frac{1}{\bar{q}_{\text{LA}}} \) at any time.

Then, the arrival time dependency for the leader-follower pair with an additional criteria for density can be given as:

\[
t_i + \max \left( \frac{\Delta x}{\bar{q}_{\text{LA}}}, \frac{1}{q_{\text{max}}} \right) \leq t_{i+1} \leq t_i + \max \left( \frac{\Delta x}{\bar{q}_{\text{LA}}}, \frac{1}{q_{\text{max}}} \right)
\]

The condition may be re-written as:

\[
t_{i+1} - \max \left( \frac{\Delta x}{\bar{q}_{\text{LA}}}, \frac{1}{q_{\text{max}}} \right) \leq t_i \leq t_{i+1} - \max \left( \frac{\Delta x}{\bar{q}_{\text{LA}}}, \frac{1}{q_{\text{max}}} \right)
\]

The above equation expresses the time \( t_i \) a leader must arrive at a given section for a follower to arrive there at a desired time \( t_{i+1} \). The formulation of the condition in the latter form is desirable because, the integrated strategy is predictive such that anticipatory decisions ensure a desired traffic state in the future. Then, a leader (arriving earlier) constitutes the flow at an earlier time than its follower. Hence, the microscopic formulation in equation (4-22) allows for anticipatory control of traffic.

Next, these microscopic car-following constraints need to be converted to mesoscopic conditions suitable for the discrete formulation of COSCAL v2. For this, the condition in equation (4-22) is applied to each detection segment. For any detection segment \( t_{\text{det}} \), the most upstream vehicle on segment \( t_{\text{det}} + 1 \) is taken as a leader, and the most upstream vehicle on segment \( t_{\text{det}} \) as its mesoscopic follower.

Then, accumulation \( N_{\text{FW}}(t_{\text{det}} + 1) \) according to equation (4-12), gives the cumulative vehicle count of the representative leader for segment \( t_{\text{det}} \). Likewise, accumulation \( N_{\text{FW}}(t_{\text{det}}) \) gives the cumulative vehicle count of its mesoscopic follower. \( \Delta x \), the hypothetical headway between these mesoscopic leader-follower pair is approximated as the length of detection segment \( t_{\text{det}} \).

### 4-3-4-6 Adapting freeway cumulative curves for the Leader-Follower constraint

As per the original cumulative curve \( N_{\text{FW}}^{\text{max}} \); a follower \( N_{\text{FW}}(t_{\text{det}}) \) could at the earliest arrive at \( t_{\text{ramp}, \text{min}}(t_{\text{det}}) \), and likewise its leader \( N_{\text{FW}}(t_{\text{det}} + 1) \) at \( t_{\text{ramp}, \text{min}}(t_{\text{det}} + 1) \), as determined in equations (4-11) and (4-12). These variables have been identified in Figure 4-7.

Further, the arrival time of the leader as per the leader-follower condition in equation (4-22) is determined in the equation below. The desired arrival time based on the leader-follower criteria is denoted as \( t_{\text{ramp}, \text{min}}(t_{\text{det}}) \).

\[
t_{\text{ramp}, \text{min}}(t_{\text{det}} + 1) \geq t_{\text{ramp}, \text{min}}(t_{\text{det}}) - \max \left( \frac{L_{\text{det}}}{v_{\text{eff}}}, \frac{\rho_{\text{det}} \lambda_{\text{det}} L_{\text{det}}}{q_{\text{max}}} \right)
\]

The additional constraint requires the leader \( N_{\text{FW}}(t_{\text{det}} + 1) \) to arrive no later than time \( t_{\text{ramp}, \text{min}}(t_{\text{det}} + 1) \). Therefore, the more restrictive of the two times, i.e. \( \max \left( t_{\text{ramp}, \text{min}}(t_{\text{det}} + 1), t_{\text{ramp}, \text{min}}(t_{\text{det}} + 1) \right) \) gives the earliest time for \( N_{\text{FW}}(t_{\text{det}} + 1) \) vehicles to have crossed the on-ramp section. The adapted \( N_{\text{FW}}^{\text{max}} \) curve gives the revised upper bound in the \( N_{\text{FW}} \)-t plane.

Let's denote it as \( U_{\text{FW}} : \left( N_{\text{FW}}(t_{\text{det}}), \max \left( t_{\text{ramp}, \text{min}}(t_{\text{det}}), t_{\text{ramp}, \text{min}}(t_{\text{det}}) \right) \right) \).
Figure 4-7: Mesoscopic translation of the arrival time dependency between a leader and follower due to car-following behaviour. The red dashed lines in the on the $N_{fw}$-t plane represent the function for this constraint, and the red shaded area the reduction of the feasible freeway flows thereof.

Additionally, the flow capacity of the on-ramp section is $q_{cap,sl}^\text{comb}$ when the freeway flow upstream of the on-ramp is regulated. Hence, the cumulative curve $N_{fw}^{\text{min,adm}}(k)$ as calculated in equation (4-13) is revised beyond time $k_{S-t}^{\text{ramp,min}}(k)T$. With the flow capacity $q_{cap,sl}^\text{comb}$ under speed limits, the cumulative curve can be revised as:

$$N_{rm}^{\text{min,adm}}(k|k) = q_{cap,sl}^\text{comb} \left[ kT - k_{S-t}^{\text{ramp,min}}(k)T \right] - U_{fw}(\tilde{k}), \quad \forall \tilde{k} \geq k_{S-t}^{\text{ramp,min}}(k)$$

(4-24)

Similarly to the leader-follower constraints for the upper boundary in $N_{fw}$-t plane, the $N_{fw}^{\text{min}}$ curve is also adapted. The latest time for $N_{fw}(i_{det}+1)$ vehicles to cross at the on-ramp section due to the leader-follower constraint can be given as:

$$t_{ramp,max}(i_{det}+1) \leq t_{ramp,min}(i_{det}) = \max \left( \frac{L_{i_{det}}}{q_{cap,sl}^\text{comb} \cdot \rho_{i_{det}} \cdot \lambda_{i_{det}}}, \frac{L_{i_{det}}}{q_{max}} \right)$$

(4-25)
Then, \( \min \left( t_{\text{ramp, max}}(i_{\text{det}} + 1), t_{\text{ramp, max}}(i_{\text{det}}) \right) \) is more restrictive and gives the latest time for \( N_{\text{fw}}(i_{\text{det}}) \) vehicles to have crossed the on-ramp section. Now the revised lower bound in the \( N_{\text{fw}}-t \) plane can be given as \( L_{\text{fw}} : \left( N_{\text{fw}}(i_{\text{det}}), \min \left( t_{\text{ramp, max}}(i_{\text{det}}), t_{\text{ramp, max}}(i_{\text{det}}) \right) \right) \).

### 4-3-4-7 Translating freeway curves to the \( N_{\text{rm}}-t \) plane and the feasible ramp flows

The upper \( U_{\text{fw}} \) and lower bound \( L_{\text{fw}} \) for the freeway flows, determined in the previous section, can be translated to the \( N_{\text{rm}}-t \) plane similarly to equation (4-24). Then, the new curve \( N_{\text{rm}}^{\text{max, adm}}(\tilde{k}|k) \) gives the maximum admissible RM flow that ensures that the prevailing capacity at the on-ramp section \( q_{\text{comb}}^{\text{cap, sl}} \) not exceeded. The formulation of constraint \( C1 \) then becomes:

\[
N_{\text{rm}}^{\text{max, adm}}(\tilde{k}|k) = q_{\text{comb}}^{\text{cap, sl}} \left( \tilde{k}T - k_{\text{ramp, min}}^T \right) - L_{\text{fw}}(\tilde{k}), \quad \forall \tilde{k} \geq k_{\text{ramp, min}}^T \quad (4-26)
\]

At this point, we have a feasible area in the \( N_{\text{rm}}-t \) plane from the primary RM constraints. This region comprises of all discrete \( N_{\text{rm}} \) values between the curves \( U_{\text{rm}} \) and \( L_{\text{rm}} \). Additionally, we have similar curves \( U_{\text{fw}} \) and \( L_{\text{fw}} \) on the \( N_{\text{fw}}-t \). These were translated to the \( N_{\text{rm}}-t \) plane as \( N_{\text{rm}}^{\text{max, adm}} \) and \( N_{\text{rm}}^{\text{min, adm}} \) respectively. Therefore, the resulting feasible set is given by the superimposition of \([U_{\text{rm}}, L_{\text{rm}}]\) and \([N_{\text{rm}}^{\text{max, adm}}, N_{\text{rm}}^{\text{min, adm}}]\) on the \( N_{\text{rm}}-t \) plane:

\[
U(\tilde{k}|k) = \min \left( U_{\text{rm}}(\tilde{k}|k), N_{\text{rm}}^{\text{max, adm}}(\tilde{k}|k) \right) \quad (4-27)
\]

and

\[
L(\tilde{k}|k) = \max \left( L_{\text{rm}}(\tilde{k}|k), N_{\text{rm}}^{\text{min, adm}}(\tilde{k}|k) \right)
\]

Lastly, one final check must be performed to ensure that a feasible solution space has been found in accordance with its starting definition, i.e., at any given time at least one feasible RM path is possible till the final prediction time. This entails a backcasting approach to check for the cumulative ramp outflow value at time \((\tilde{k} - 1)T\) which can realize the desired outflow \( U(\tilde{k}) \) at the minimum RM rate \( q_{\text{rm}}^{\text{min}} \). This backcasted \( N_{\text{rm}} \) is denoted as \( U'(\tilde{k} - 1) \) and is mathematically given as:

\[
U'(\tilde{k} - 1|k) = U(\tilde{k}|k) - q_{\text{rm}}^{\text{min}} T \quad (4-28)
\]

Then the effective upper bound at time step \( \tilde{k} \) is \( \min \left( U(\tilde{k} - 1|k), U'(\tilde{k} - 1|k) \right) \).

Likewise, for the lower bound \( L(\tilde{k}|k) \) the backcasting approach checks for the minimum \( L'(\tilde{k} - 1) \) that can realise \( L(\tilde{k}) \) in the subsequent time step at a maximum RM rate \( q_{\text{rm}}^{\text{max}} \). \( L'(\tilde{k} - 1) \) can be given as:

\[
L'(\tilde{k} - 1|k) = L(\tilde{k}|k) - q_{\text{rm}}^{\text{max}} T \quad (4-29)
\]

Then, the effective lower bound at time step \( \tilde{k} \) is \( \max \left( L(\tilde{k} - 1|k), L'(\tilde{k} - 1|k) \right) \). Together, the effective upper and lower bound curves for all \( \tilde{k} > k \), gives the feasible RM flow values.
4-3-5 Selecting a feasible ramp flow trajectory

The previous section detailed the method to predict a set of feasible ramp outflow values at every future time step in the prediction horizon. Ideally, the possibility to pick any one value from this set for a subsequent time step is most desirable. However, in the current formulation of COSCAL v2 the profile of the RM flow in the future affects VSL implementation at earlier times. In other words, to accommodate a high RM outflow in a future time step may require extending speed limits further upstream in the most current time step.

Hence, selecting a complete RM trajectory, once COSCAL v2 scheme is initiated, is necessary. At each time step, the RM controller selects a trajectory that is closest to the previously chosen trajectory, and at the same time, feasible based on the current measurements and prediction.

Essentially, two criteria are used to determine the desired RM trajectory. First is the desired queue length at time $t_{S-h}$ when the S-head crosses the on-ramp location; this is when $q_{uw}$ flow recovers to free flow condition, i.e. the capacity of the on-ramp section is $c_{comb}$ once again. Here, we may chose to keep the queue at a fixed percentage of its maximum capacity $s_{H}^{max}$, where $0 < K \leq 1$. While selecting the value of the parameter $K$, the consequence of a high or low parameter value must be understood. A higher $K$ value improves VSL performance (reduces area under speed limits), however, offers lesser flexibility to adapt RM flows in the future if required for queue management. Additionally, a moderate on-ramp queue at time $t_{S-h}$ when the S-head crosses the on-ramp, increases the likelihood that the stabilization area after that time reduces in space-time regardless of a drastic spike in on-ramp demand.

The second criteria relates to the efficiency of the speed-limited area upstream of the on-ramp (state 4B). Consider, the RM flow is first high and then lowered to arrive at some end cumulative outflow value. Alternately, the same cumulative outflow could be achieved by keeping the RM flow low initially and increasing it later. In spite of the same cumulative outflow finally, the former strategy would result in a less efficient state 4B than the latter. For this reason, the RM flow trajectory is kept as low as possible, for as long as possible, and subsequently increased to achieve the set ramp storage capacity at time $t_{S-h}$.

However, the above criteria do not determine the RM trajectory beyond time $t_{S-h}$. The integrated strategy after $t_{S-h}$ poses a design choice; the on-ramp queue may either be released while the VSL scheme is still active or after the stabilization area is resolved. It is chosen to release the on-ramp queue while the freeway flow is speed-limited. The argument here is that the VSL scheme offers more flexibility to achieve the higher ramp flows desirable for releasing the entire ramp queue. At the same time, it does imply that the freeway vehicles further upstream of the problem area may be speed-limited for this. However, it is understood as more reliable to achieve the end goal.

Let’s denote the selected RM flow trajectory as $N_{s}^{Rm}(\tilde{k}|k)$, such that the desired RM rate at a future time $kT$ becomes $\frac{N_{s}^{Rm}(\tilde{k}+1) - N_{s}^{Rm}(\tilde{k})}{T}$.

4-3-6 Implementation of variable speed limits in the stabilization area

In general, any vehicle that is speed-limited, even for the shortest interval of time, enters speed-limitation at the S-tail shockwave and exits at the S-head. Further, the freeway flow $q_{uw}$ arrives at the on-ramp section in different regimes - the flow is in free flow before time $t_{S-t}$, under speed-limitation between time $t_{S-t}$ and $t_{S-h}$, and again in free flow after time $t_{S-h}$. Note that the location of the S-tail and the S-head shockwaves is uniquely determined in each case.

The freeway vehicles entering the merging location before time $t_{S-t}$, enter and exit speed-limitation downstream of the on-ramp, i.e shockwaves S-tail and S-head are both downstream of the on-ramp. For the freeway vehicles merging between time $t_{S-t}$ and $t_{S-h}$ the S-tail is located upstream of the on-ramp and the S-head downstream of it. And for vehicles entering the on-ramp section after $t_{S-h}$, both S-tail and S-head are upstream of the on-ramp location. This is illustrated with three unique vehicle trajectories in Figure 4-1c.
Now, when the S-head and S-tail shockwaves lie upstream of the on-ramp section, their propagation can be dynamically regulated in order to accommodate the on-ramp flow. The chosen RM trajectory \( N_{\text{sel}}(\tilde{k}|k) \) provides the number of vehicles that must be allowed to merge from the on-ramp in a given time step. Then, speed-limitation must ensure an appropriate density of the freeway traffic arriving at the on-ramp section in that time step. An appropriate density is low enough to offer sufficient gaps for the ramp vehicles and to achieve the desired density downstream of the on-ramp section. Therefore, by dynamically managing the propagation of the S-head and S-tail shockwaves, RM and VSL strategies are integrated.

The methodology to determine the desired location of the S-head and S-tail in the integrated control approach is detailed in the next two sections.

### 4-3-6-1 Calculating the S-head position

The location of the S-head downstream of the on-ramp section (labelled S-head \(_1\) in Figure 4-1c) depends on its design speed \( v^{S-h} \). Thus, it can be calculated from an estimate of time and location of the start of S-head shockwave, as determined in equations (3-59) and (3-60), respectively.

The S-head shockwave upstream of the on-ramp section is labelled as S-head \(_2\) in Figure 4-1c. Observe the vehicle trajectory 3 in the same figure. The location of the S-head determines when the vehicle exits speed-limitation and hence, the time that it arrives at the on-ramp section; all vehicle that exit S-head \(_2\) arrive after the S-head \(_1\) crosses the on-ramp at \( t^{\text{ramp}}_{S-h} \). Therefore, these arrival times and hence, the speed of S-head shockwave determine the flow in state 5C at any given time.

The flow in state 5C, \( q^{[5C]} \) together with the RM flow \( q_{\text{rm}} \) gives the design free flow in state 5B. Therefore, in order to maintain the desired flow \( q^{[5B]} \) while the RM flow varies in each time step, the flow in state 5C must change as below:

\[
q^{[5C]}(\tilde{k}) = q^{[5B]} - q_{\text{rm}}(\tilde{k})
\]

Further, the target value of density in state 4C is the same as that established for basic RM strategy in Section 3-5-2-2. Then, using shockwave theory the desired speed of S-head shockwave between states 4C and 5C can be determined from the flow and density in these states as:

\[
v^{[4C-5C]}(\tilde{k}) = \frac{q^{[5C]}(\tilde{k}) - q^{[4C]}(\tilde{k})}{\bar{\rho}^{[5C]}(\tilde{k}) - \bar{\rho}^{[4C]}(\tilde{k})} \lambda
\]

Notice in Figure ?? the hypothetical vehicle \( n_k \) that arrives at the on-ramp at time \( (\tilde{k} + 1)T \), travels in free flow velocity after it exits the S-head. Therefore, a ray at \( v^{ff} \) slope from X-t point \((x^{\text{ramp}}, (\tilde{k} + 1)T)\) will intersect the S-head ray, at slope \( v^{[4C-5C]}(\tilde{k}) \), in a point where vehicle \( n_k \) exits speed limits. Similar iterations for all time steps after time \( t^{\text{ramp}}_{S-h} \) gives the desired trajectory of the S-head shockwave upstream of the on-ramp. Let's denote the S-head trajectory as \((x_{\text{head}}(\tilde{k}), t_{\text{head}}(\tilde{k}))\). Then, the equations of the two rays can be given as:

\[
x_{\text{head}}(\tilde{k}) = x^{\text{ramp}} - v^{ff} \times ((\tilde{k} + 1)T - t_{\text{head}}(\tilde{k}))
\]

and

\[
x_{\text{head}}(\tilde{k}) = x_{\text{head}}(\tilde{k} - 1) + v^{[4C-5C]} \times (t_{\text{head}}(\tilde{k}) - t_{\text{head}}(\tilde{k} - 1))
\]
Subtracting equation (4-33) from equation (4-32) gives the time coordinate \( t_{\text{head}}(\tilde{k}) \) of the S-head trajectory:

\[
t_{\text{head}}(\tilde{k}) = \frac{x_{\text{head}}(\tilde{k} - 1) - x_{\text{ramp}}}{v_{\text{ff}} - v^{[4C-5C]}} + \frac{v_{\text{ff}} \times (\tilde{k} + 1) T - v^{[4C-5C]}(\tilde{k}) \times t_{\text{head}}(\tilde{k} - 1)}{v_{\text{ff}} - v^{[4C-5C]}} \tag{4-34}
\]

then the corresponding location becomes,

\[
x_{\text{head}}(\tilde{k}) = \frac{x_{\text{head}}(\tilde{k} - 1) + x_{\text{ramp}}}{2} - \frac{v^{[4C-5C]}(\tilde{k}) \times t_{\text{head}}(\tilde{k} - 1) + v_{\text{ff}} \times (\tilde{k} + 1) T}{2} + \frac{v_{\text{ff}} + v^{[4C-5C]}(\tilde{k})}{2} \times t_{\text{head}}(\tilde{k}) \tag{4-35}
\]

In a nutshell, the freeway flow desired at the on-ramp section in a time step determines the desired S-head speed \( v^{[4C-5C]}(\tilde{k}) \), given in equation (4-31). Subsequently, it is determined when a vehicle that exits at the on-ramp, at the free flow speed, at the end of the next prediction time step should leave the S-head.

### 4-3-6-2 Calculating the S-tail position

The propagation of the S-tail shockwave is identified as three distinct parts in Figure 4-1b. S-tail\(_1\) determines when the merged flow \( q_{\text{comb}} \) enters speed-limitation downstream of the on-ramp. S-tail\(_2\) determines when the freeway flow \( q_{\text{fw}} \) enters speed-limitation, to merge with the ramp flow between the time Stail\(_1\) and S-head\(_1\) cross the on-ramp. Finally, S-tail\(_3\) determines when the freeway flow \( q_{\text{fw}} \) enters speed-limitation, to exit at S-head\(_2\) and arrive at the on-ramp after the S-head\(_1\) has crossed it.

The goal of speed-limitation is to create a homogeneous flow at a desired density within the control area. This homogeneous state then ensures a desired outflow at a downstream shockwave. To that end, the core principle to determine the location of the S-tail parts entails matching the number of vehicles that enter speed-limitation to the desired outflow at a downstream shockwave.

#### Determining S-tail\(_1\)

Vehicles entering at the S-tail\(_1\) shockwave, exit at the S-head\(_1\) shockwave downstream of the on-ramp. Hence, the exact prediction of the S-tail\(_1\) trajectory does not influence the determination of a feasible ramp flow trajectory and its integration with the VSL scheme. In fact, the methodology used to determine the most upstream segment in the stabilization area (refer to Section 3-5-1), in the original formulation of COSCAL v2, will adjust the S-tail\(_1\) according to the on-ramp flows.

The most upstream speed-limited segment determined here applies until the time \( t_{S_{2-1}}^{\text{ramp,min}}(k) \) that the S-tail is predicted to cross the on-ramp. Beyond this time, the trajectory of S-tail\(_2\) is adjusted to accommodate flows at the on-ramp. The prediction of the S-tail\(_1\) is vital for the integration of VSL with RM, and is discussed next.

#### Determining S-tail\(_2\)

The part of the S-tail trajectory after the S-tail\(_1\) shockwave crosses the on-ramp is called S-tail\(_2\). The vehicles that enter speed-limitation at the S-tail\(_2\) shockwave, merge with the on-ramp vehicles at the on-ramp location. The total outflow downstream of the on-ramp, from the design of the integrated strategy, is \( q^{[4A]} \).

To achieve this desired flow, given the selected RM trajectory \( \Lambda_{\text{ramp}}^{\text{ramp}}(\tilde{k}|k) \), the number of freeway vehicles that should arrive in a future time step \( \tilde{k} \) can be given as below:
A more conservative design, detector segment upstream detector segment to be speed-limited in order to realise the outflow at the on-ramp is found. For equating the location at the point of intersection gives:

\[
N_{\text{ramp}}^\text{out}(\bar{k}|k) = q^{[4A]}T - \left( N_{\text{rm}}^\text{sel}(\bar{k} + 1|k) - N_{\text{rm}}^\text{sel}^-(\bar{k}|k) \right)
\]

\[
= \rho^{[4A]} \lambda v_{\text{eff}}T - \left( N_{\text{rm}}^\text{sel}(\bar{k} + 1|k) - N_{\text{rm}}^\text{sel}^-(\bar{k}|k) \right)
\]

Now, the location of the S-tail \(2\) should be such that the above cumulative outflow is matched by speed-limiting the exact number of vehicles at an appropriate time.

Let denote the last detector segment for which the S-tail location is determined as \(i^\text{tail,us}\) and any detector segment upstream of it as \(i^\text{det}\). Then the cumulative inflow \(N_{\text{tail}}^\text{in}(i^\text{det})\) of vehicles towards the S-tail, from all detection segments between \(i^\text{tail,us}\) and \(i^\text{det}\), can be calculated as below:

\[
N_{\text{tail}}^\text{in}(i^\text{det}) = \sum_{j=i^\text{det}}^{i^\text{tail,us}-1} L_j \lambda_j \rho_j(k)
\]

When \(N_{\text{tail}}^\text{in}(i^\text{det})\) just suffices the desired outflow \(N_{\text{ramp}}^\text{out}(\bar{k}|k)\), i.e. \(N_{\text{tail}}^\text{in}(i^\text{det}) > N_{\text{ramp}}^\text{out}(\bar{k}|k)\), the most upstream detector segment to be speed-limited in order to realise the outflow at the on-ramp is found. For a more conservative design, detector segment \(i^\text{det}+1\) is speed-limited to realise the outflow in time \(\hat{k}T\).

Let assume vehicle \(n_i\) is the last vehicle on detection segment \(i^\text{det}+1\). Now, the part of its trajectory under speed limits will intersect with the part in free flow at the time that it should be speed-limited, i.e. location of the S-tail \(2\) shockwave. This implies that a ray at slope \(v_f\) from the upstream end of detector \(i^\text{det}+1\) will intersect a ray at slope \(v_{\text{eff}}\) from X-t point \((x_{\text{ramp}}, (\bar{k} + 1)T)\) in the location of the S-tail shockwave. Equating the location at the point of intersection gives:

\[
x_{\text{det}+1}^\text{u} + v_{\text{eff}} \left( t_{\text{tail}}(i^\text{det}+1) - (k + 1)T \right) = x_{\text{ramp}} - v_{\text{eff}} \left( (\bar{k} + 1)T - t_{\text{tail}}(i^\text{det}+1) \right)
\]

On rearranging, we get the desired time that the last vehicle \(n_i\) on segment \(i^\text{det}+1\) is speed-limited:

\[
t_{\text{tail}}(i^\text{det}+1) = \frac{x_{\text{ramp}} - x_{\text{det}+1}^\text{u}}{v_{\text{eff}} - v_{\text{eff}}} + \frac{v_{\text{eff}} \times (k + 1)T - v_{\text{eff}} \times (\bar{k} + 1)T}{v_{\text{eff}} - v_{\text{eff}}}
\]

and the corresponding location of the S-tail is:

\[
x_{\text{tail}}(i^\text{det}+1) = x_{\text{ramp}} - v_{\text{eff}} \left( (\bar{k} + 1)T - t_{\text{tail}}(i^\text{det}+1) \right)
\]

S-tail \(2\) applies until the last vehicle that exits at the on-ramp at time \(t_{\text{ramp}}(i^\text{det}+1)\) is speed-limited. Vehicles further upstream are speed-limited to exit into free flow at the S-head \(2\). How this part of the S-tail is calculated is detailed next.

**Determining S-tail \(3\)**

Let denote the last detector segment for which the S-tail location is determined as \(i^\text{tail,us}\). For the first prediction for S-tail \(3\), this will be given by the last detection segment that is speed-limited as per S-tail \(2\), and exits speed-limitation at the on-ramp location. The freeway vehicles upstream of this detection segment, enter speed-limitation at the S-tail \(3\) shockwave and leave the stabilization area at the S-head \(3\) shockwave.
In Section 4-3-6-1, the desired flow in state 5C that should arrive at the on-ramp in a given time step was determined by equation (4-30). Now, the number of freeway vehicles that cross the on-ramp, say in time step $\tilde{k}T$ equals the number of vehicles that leave the S-head between the points $(x_{\text{head}}(\tilde{k}), t_{\text{head}}(\tilde{k}))$ and $(x_{\text{head}}(\tilde{k} + 1), t_{\text{head}}(\tilde{k} + 1))$ on its trajectory. This cumulative outflow $N_{\text{head}}^{\text{out}}(\tilde{k}|k)$ at the S-head is given below; the independent variable $\tilde{k}$ in its notation represents that these vehicles cross the S-head to arrive at the on-ramp in time step $\tilde{k}T$.

$$N_{\text{head}}^{\text{out}}(\tilde{k}|k) = q^{\left[5C\right]}(\tilde{k})T$$  \hspace{1cm} (4-41)

The cumulative inflow $N_{\text{tail}}^{\text{in}}(i_{\text{det}})$ of vehicles towards the S-tail, from detection segments between $i_{\text{tail},us}(k)$ and an upstream detector $i_{\text{det}}$ can be calculated as below:

$$N_{\text{tail}}^{\text{in}}(i_{\text{det}}) = \sum_{j=i_{\text{det}}}^{i_{\text{tail},us}-1} L_j \lambda_j \rho_j(k)$$  \hspace{1cm} (4-42)

When $N_{\text{tail}}^{\text{in}}(i_{\text{det}})$ just suffices the desired outflow $N_{\text{head}}^{\text{out}}(\tilde{k}|k)$, i.e. $N_{\text{tail}}^{\text{in}}(i_{\text{det}}) > N_{\text{head}}^{\text{out}}(\tilde{k}|k)$, the most upstream detector segment to be speed-limited in order to realise the outflow at S-head is found. Similarly to the calculations for S-tail, for a conservative design, S-tail is located for the accumulation upto the detector segment just downstream of $i_{\text{det}}$.

This implies that a ray at slope $v^{\text{eff}}$ from the upper edge of segment $i_{\text{det}} + 1$ at time $kT$ will intersect a ray at slope $v^{\text{eff}}$ from S-head point $(x_{\text{head}}(\tilde{k} + 1), t_{\text{head}}(\tilde{k} + 1))$. Corresponding to equations (4-39) and (4-40), the coordinates of the S-tail for freeway vehicles arriving at the on-ramp at time $kT$ are:

$$t_{\text{tail}}(i_{\text{det}} + 1) = \frac{x_{\text{head}}(\tilde{k} + 1) - x_{\text{tail},us}(i_{\text{det}} + 1)}{v^{\text{eff}} - v^{\text{eff}}} + \frac{v^{\text{eff}} \times (\tilde{k} + 1)T - v^{\text{eff}} \times t_{\text{head}}(\tilde{k} + 1)}{v^{\text{eff}} - v^{\text{eff}}}$$  \hspace{1cm} (4-43)

and

$$x_{\text{tail}}(i_{\text{det}} + 1) = x_{\text{head}}(\tilde{k} + 1) - v^{\text{eff}} \left( (\tilde{k} + 1)T - t_{\text{tail}}(i_{\text{det}} + 1) \right)$$  \hspace{1cm} (4-44)

### 4-4 Summary and Discussion

COSCAL v2 was extended with an advanced RM and VSL approach, to overcome some of the limitations of the basic integrated approach in Chapter 3. A predictive approach with feedback is used for both the control measures. In the case of RM, the queue-length on the ramp and the most recent freeway traffic measurements are used to predict a set of feasible ramp flows in the future. The feasible solution space ensures that (1) the ramp queue is always between a maximum and minimum queue-length (2) the RM rate is always between the maximum and minimum policy dictated RM rates, and (3) the freeway flow can be regulated to accommodate the desired RM flow.

In the advanced VSL strategy, if the scheme crosses a ramp location, an approach different from the original algorithm is required to appropriately (as per the RM flow at any time) reduce the freeway flows arriving at the ramp section. In the new approach, the propagation of the S-head and S-tail shockwave is controlled. The underlying microscopic concept was to determine the trajectory of each vehicle, and the time when it enters and exits speed limits, to ensure a desired flow profile at the ramp section. This concept was converted to a macroscopic formulation in terms of the accumulation measured over detection segments.
It must be mentioned here that the original COSCAL v2 and COSCAL v1 algorithms were designed with a transition towards cooperative systems in mind, and have the capacity for in-car detection and actuation. Given the microscopic conceptualization of the new VSL approach, this capacity can be further utilized. Since equipped vehicles can be regulated more accurately, they can be used to create gaps for the additional vehicles to merge from the on-ramp. A similar RM strategy using in-car communication technologies was proposed in a recent work (Scarinci et al., 2013), which could be a very useful extension to the proposed theory. Besides, in-car actuation capability can in itself help in realising the shockwave trajectories more accurately.

In developing these advanced approaches for RM and VSL, some additional parameters were considered other than the tuning parameters in COSCAL v2:

**Ramp infrastructure related**

- the location $x^{ramp}$ of the on-ramp

**RM strategy related**

- on-ramp demand flow $q^{in}(k)$
- the maximum $s^{max}$ and minimum $s^{min}$ on-ramp queue length
- the maximum $q^{max}_{rm}$ and minimum $q^{min}_{rm}$ RM flow
- parameter $K$ for the desired queue-length $Ks^{max}$ on the on-ramp at time $t^{ramp}_{S-h}$ when the S-head shockwave crosses the on-ramp

**Freeway traffic related**

- the average speed $v^{jam}$ in moving jam state
- the average free-flow speed $v^{ff}$ of vehicles

In comparison to the RM strategy used in the basic approach, the advanced RM requires a prediction for the demand on the on-ramp. Since the present demand prediction algorithms are not very accurate, the parameters related to the RM strategy should be tuned to compensate for it in practice. However, the performance sensitivity of the integrated strategy to the accuracy of the demand prediction should be tested in simulation before field-testing.

At the same time, the VSL strategy uses the freeway traffic measurements at any time to predict the evolution of the VSL scheme. The prediction horizon in the approach extends till the time the most upstream vehicle that enters speed-limitation has crossed the on-ramp location. Therefore, the duration of the prediction horizon depends on the detection location of the jam, and the traffic condition on the freeway. The longer the prediction horizon gets, traffic data from detection segments even further upstream is required for the prediction of the VSL scheme. For instance, for a prediction horizon of 15 min and an average free-flow speed of 100 km/h, freeway measurements 25 km upstream of the on-ramp should be available. This is practically not feasible. Hence, alternative approaches to prediction of the VSL scheme should be explored. One possibility is to assume constant traffic variables upstream of the most upstream detector measurements available.

Lastly, the entire approach was detailed for the case that the area speed-limited for stabilization crosses the on-ramp. However, as was discussed in Section 3-4-2, the on-ramp flows can also merge into the jam resolving area. This scenario should be treated similarly to the basic approach, by accounting for the additional vehicles from the on-ramp while determining the total number of vehicles to be speed-limited for resolving the jam. The exact formulation of the scenario is excluded here for lack of time.
Chapter 5

Algorithm Development

Two different theoretical strategies for integration of COoperative Speed Control ALgorithm (COSCAL) v2 with ramp metering (RM) strategy were developed in Chapters 3 and 4. In this chapter, the objective is to formulate an algorithm that enables the controller to achieve the traffic behaviour in accordance with the theoretical scheme.

The algorithmic formulation of COSCAL v2 (Hegyi, 2013) is used as the basis of extension for the new theory. Relevant parts of the algorithm will therefore be briefly reproduced.

5-1 Introduction

The algorithmic development is focused on the advanced integrated strategy in Chapter 4. The choice is made due to time limitation; for the same reason, only the advanced strategy is evaluated in a simulation based study.

For the ease of implementation, the entire strategy is identified in five unique modules. A modular approach allows for a more methodical evaluation procedure, and a clearer schematization of the control scheme. A description of the identified modules can be found in Table 5-1.

<table>
<thead>
<tr>
<th>Module label</th>
<th>Module description</th>
<th>Reference to theory</th>
</tr>
</thead>
<tbody>
<tr>
<td>VSL related</td>
<td>Module 1 adaptation of the trajectory of S-head shockwave for RM flows</td>
<td>Section 4-3-6-1</td>
</tr>
<tr>
<td></td>
<td>Module 2 prediction of the time that S-tail shockwave crosses the on-ramp location</td>
<td>Section 4-3-2</td>
</tr>
<tr>
<td></td>
<td>Module 3 adaptation of the trajectory of S-tail shockwave according to the RM flows</td>
<td>Section 4-3-6-2</td>
</tr>
<tr>
<td>RM related</td>
<td>Module 4 prediction of feasible RM rates, for the duration of the VSL scheme, such that there is no queue spillback</td>
<td>Section 4-3-4</td>
</tr>
<tr>
<td></td>
<td>Module 5 selection of a RM rate at each time step from the feasible flows determined in Module 4</td>
<td>Section 4-3-5</td>
</tr>
</tbody>
</table>
In the following sections, first the algorithmic formulation of COSCAL v2 is revisited. Then, the intervention of the new theory is understood within the original algorithm. Finally, flow diagrams are used to describe the algorithm development for the new modules.

5-2 Modes and Mode Transitions in COSCAL v2

In the original COSCAL v2, different driving modes are identified for detection and actuation segments that have different roles, and use different speed limits. Specifically, modes for the detection segments relate to traffic state estimation, including jam detection. Modes for the actuation segments are used for the actuation of speed limits, to keep track of their roles, and hence to determine future roles and modes.

The different modes in the control scheme are identified in Figure 5-1. A resemblance to the functional traffic states in COSCAL v2 is evident here.

5-2-1 Detection segment modes

The detection segments can be in two modes only, a jam mode (mode DJ) and a free-flow mode (mode DF) depending on whether or not there is a jam in the segment.

The detection segment modes serve to keep track of the jam location, and can be in mode DJ (jam) or mode DF (free flow, no jam). The first letter (D) of the jam mode refers to the fact that these modes are related to detection segments.

- **Mode DF: free driving**
  By default, the detection segments are in mode DF, which means that the vehicles are not in a jam.

- **Mode DJ: the vehicle in the jam**
  If for a detection segment it is determined that there is a jam on it, then the segment is in mode DJ. The role of the segments in mode DJ is to keep track of the jam head location, i.e. the most downstream detection segment in mode DJ.
5-2-2 Actuation segment modes

The actuation segment modes serve to keep track of the speed limit location and role (resolving or stabilizing), and can be in mode AA (autonomous, no speed limit), mode AR (resolving, speed limit active), mode AS (stabilizing, speed limit active).

- **Mode AA: autonomous driving**
  By default, the actuation segments are in mode AA, which means that the vehicles in these segments drive according to their own car-following rules. Autonomous in this context does not mean driverless, or fully automated, but that there is no intervention from the system in the default driving behaviour of the vehicle or driver, i.e., there is no active speed limit.

- **Mode AR: vehicles that resolve the jam**
  The actuation segments in mode AR carry the vehicles directly upstream of the jam head that have to be slowed down to resolve the jam according to equation (3-11). Therefore, the speed limit is \( v_{\text{eff}} \).
  In general, most vehicles on an actuation segment in mode AR will enter the jam at some point and will have to reduce their speed. However, before they enter the jam, they will travel at speed \( v_{\text{eff}} \). In this situation, the headway distances are typically larger than critical headways for the target speed. So, the traffic in mode AR is stable.

- **Mode AS: vehicles that stabilize the traffic flow**
  The actuation segments in mode AS contain the vehicles in the stabilization area, which is created upstream of the vehicles in mode AR. These vehicles have been slowed down or are being slowed down, using a speed limit \( v_{\text{eff}} \) according to the procedure described in Section 3-5.

5-2-3 Mode Transitions

During the application of the algorithm, the modes of the detection and actuation segments will change. Mode changes may occur due to changes in the traffic state, such as a creation or resolution of a traffic jam, or to the speed limit controller actions in response to the most recently measured traffic state.
The mode transitions for the detection segments are straight-forward and depend on the creation and the resolution of moving jams. The mode changes for the actuation segments have different triggers, which are summarized in Figure 5-2.

5-3 Algorithmic formulation for the developed theory

In the integrated strategy, the additional RM flows influence the desired trajectory of the S-head and S-tail shockwaves. In adjusting their location, the freeway flows arriving at the on-ramp are sufficiently lowered. Therefore, the integrated strategy intervenes in the original algorithm at the mode transitions between Mode AS and Mode AA. In Figure 5-2, these transitions make-up the outermost loop.

In the original algorithm, the trigger for initiating a Mode AA to Mode AS is determined by the requirement for an additional segment to achieve the desired stabilization density. Correspondingly, a Mode AS to Mode AA transition is triggered if the segment lies downstream of the S-head location in that time step.

Recall that the COSCAL v2 algorithm makes a one time step prediction for the next time step \( k + 1 \) based on the traffic measurement data and modes information in time step \( k \). In contrast, the new strategy predicts the entire (remaining) scheme at each time step, to adapt control decisions in the next time step. Therefore, prediction of S-head and S-tail shockwaves, and the appropriate RM flow trajectory constitute additional algorithmic steps that influence the earlier mentioned mode changes.

Figure 5-3 and Figure 5-4 illustrate the flow diagrams with the algorithmic steps involved in the determination of the most upstream and most downstream segments in speed-limitation, in the new strategy. Hence, the mode transitions from Mode AA to Mode AS, and vice versa, are triggered under the following conditions:

- **Mode AA → Mode AS**: If the threshold density has not been reached in the stabilization area, according to the theory in Section 3-4-1, an additional speed limit gantry will be activated to stabilize the traffic. If the most upstream gantry is upstream of the on-ramp location, the predicted trajectory of the S-tail shockwave in the new strategy determines the most upstream actuation segment in Mode AS. In other words, the actuation segments downstream of the S-tail shockwave, and upstream of the R-tail or S-head shockwave change mode from AA to AS.

- **Mode AS → Mode AA**: If the S-head shockwave in the next time step, as determined by the original algorithm, is downstream of the on-ramp, current segments in mode AS that lie downstream of it change mode to AA. However, if the shockwave is predicted to cross the downstream end of the on-ramp segment, then the trajectory of the S-head shockwave determined by the new strategy applies. Correspondingly, segments downstream of the new S-head location change mode to AA.
**Figure 5-3:** Algorithm for determining the most downstream actuation segment in speed-limitation (Mode AS) with the new VSL strategy.
Figure 5-4: Algorithm for determining the most upstream actuation segment in speed-limitation (Mode AS) with the new VSL strategy.
5-4 Pseudo-Algorithm for the Modules

The pseudo-algorithm for the five modules in the integrated strategy will ensure implementation of the controller in simulation. The algorithm for each Module defines its inputs, output and the procedural steps involved in its implementation.

**Input:**
1. desired RM flows from Module 5
2. flow capacity profile at the ramp section
3. time $t_{S-h}^r (k)$ when the S-head shockwave is predicted to or already has crossed the on-ramp location
4. freeway density estimates from loop detector measurements at time $kT$

**Output:** Desired location of the S-head shockwave (most downstream segments in Mode AS) upstream of the on-ramp

**Algorithm 1:** Procedure in Module 1

```
if jam is detected according to equation (3-3) then
    get RM flows after time $t_{S-h}^r (k)$;
    get freeway capacity at the ramp section using equation (4-8);
    calculate the freeway flows desired at the ramp section using equation (4-30);
    calculate the adapted S-head trajectory $(x_{head},t_{head})$ with equations (4-35) and (4-34);
    get the position of the adapted S-head shockwave in the next time step;
    if most downstream segment in Mode AS has crossed the on-ramp then
        set mode of actuation segments downstream of adapted S-head position to Mode AA;
    else
        set mode of actuation segments downstream of the original S-head position (as determined by COSCAL v2) to Mode AA;
end
```

**Algorithm 2:** Procedure in Module 2

```
Input:
1. desired RM flows from Module 5
2. freeway density estimates from loop detector data at time $kT$
3. actuation modes in the previous time step

Output: A prediction of time $t_{S-t}^r (k)$ when the S-tail shockwave will cross the on-ramp location

if any actuation segments in Mode AR or Mode AS are found in the previous time step then
    get the most upstream segment in Mode AR or Mode AS;
    determine total cumulative freeway plus on-ramp flows arriving at the ramp section using equation (4-3);
    calculate the additional number of vehicles, over the detection segments between the most upstream speed-limited segment and the on-ramp, required to achieve the target density in the speed-limited area, with equations (4-4) and (4-2);
    if condition in equation (4-6) holds then
        update $t_{S-t}^r (k-1)$ prediction from the previous time step;
    else
        keep $t_{S-t}^r (k-1)$;
end
```

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Input:
1. desired RM flows from Module 5
2. flow capacity profile at the ramp section
3. time $t_{S-t}^{ramp}(k)$ when the S-tail shockwave is predicted to cross the on-ramp location
4. adapted S-head trajectory from Module 1
5. freeway density estimates from loop detector measurements at time $kT$

Output: Desired location of the S-tail shockwave (most upstream segments in Mode AS) upstream of the on-ramp

if jam is detected according to equation (3-3) then
get RM flows;
get freeway capacity profile at the ramp section using equation (4-8);
if most upstream Mode AS segment is downstream of the on-ramp then
    the first detection segment $i_{det}$ used in S-tail calculation is determined by back-calculating the detection segment where the vehicle that will cross the ramp at $t_{S-t}^{ramp}(k)$ is located in the current time step;
else
    the first detection segment $i_{det}$ used in S-tail calculation is the most upstream segment in Mode AS
end
while speed-limited vehicles are predicted to cross the on-ramp before $t_{S-h}^{ramp}(k)$ do
    check detection segments upstream of $i_{det}$ to calculate the adapted S-tail trajectory $(x_{tail}, t_{tail})$ using equations (4-40) and (4-39);
end
while $x_{tail}(\hat{k})$ is upstream of $x_{head}(\hat{k})$ do
    calculate the adapted S-tail trajectory $(x_{tail}, t_{tail})$ using equations (4-44) and (4-43)
end
get the position of the adapted S-head shockwave in the next time step;
if most upstream segment and downstream segments in Mode AS have crossed the on-ramp then
    set mode of actuation segments between adapted S-tail and adapted S-head position to Mode AS;
    set most of actuation segments upstream of adapted S-tail position to Mode AA;
else if most upstream segment in Mode AS has crossed the on-ramp and the most downstream segment in Mode AS has not then
    set mode of actuation segments between the original S-head or R-tail line in COSCAL v2 and the adapted S-tail position to Mode AS;
    set most of actuation segments upstream of adapted S-tail position to Mode AA;
else
    set mode of actuation segments upstream of original S-head or R-tail line in COSCAL v2 to Mode AS, as per equation (3-39);
    set mode of actuation segments of the needed stabilization area to Mode AA;
end

Algorithm 3: Procedure in Module 3
**Input:**

1. On-ramp demand profile \( q_{in} \)
2. Flow capacity profile at the ramp section
3. Freeway density estimates from loop detector data at time \( kT \)
4. Time \( t_{S-t}^{ramp}(k) \) when the S-tail shockwave passes the on-ramp
5. Time \( t_{S-h}^{ramp}(k) \) when the S-head shockwave passes the on-ramp

**Output:** Prediction of feasible RM cumulative flows

while prediction time step \( \tilde{k} \) is less than the time when the last speed-limited vehicle will cross the on-ramp

- define feasible range of cumulative RM flows for queue-length and policy constraints in Section 4-3-4-2 to get the initial upper and lower bounds of the area, \( U_{rm}(\tilde{k}|k) \) and \( L_{rm}(\tilde{k}|k) \);
- determine the minimum and maximum admissible RM cumulative curves - \( N_{rm}^{min,adm}(\tilde{k}|k) \) and \( N_{rm}^{max,adm}(\tilde{k}|k) \) for maximum freeway flows and free-flow capacity at the ramp section, according to Section 4-3-4-1;
- check if an early crossing of S-tail shockwave is required according to the condition in Section 4-3-4-3;
- revise maximum and minimum admissible RM flow curves with ramp section capacity under speed-limitation for \( \tilde{k} \) after the desired time for S-tail crossing, according to Section 4-3-4-4;
- get the feasible RM flows from the overlap of areas between \( U_{rm}(\tilde{k}|k) \) and \( L_{rm}(\tilde{k}|k) \), and \( N_{rm}^{min,adm}(\tilde{k}|k) \) and \( N_{rm}^{max,adm}(\tilde{k}|k) \);
- revise the feasible area for leader-follower dependency according to Section 4-3-4-6;

Algorithm 4: Procedure in Module 4

Module 5 is used to select RM rates from the feasible range of cumulative RM flows determined in Module 4; the input to the module includes the feasible cumulative RM flows determined in Module 4, and the desired queue-length at the time \( t_{S-h}^{ramp} \) when the S-head shockwave is expected to cross the on-ramp. Any RM rate, between the maximum and minimum policy defined RM rates, that ensures cumulative flow within the feasible area can be chosen at each time step. Therefore, any additional requirements can be defined by the traffic controller. A possible criteria for the selection was proposed in Section 4-3-5.
Chapter 6

Simulation Design and Evaluation

In the previous chapter, the theory for the advanced approach for integration of ramp metering (RM) with variable speed limits (VSL) was translated to an algorithmic formulation. The next step involves verification of this algorithm, i.e. to test if the different modules accurately implement the theoretically desired control behaviour. In other words, the simulations should demonstrate that the controller does what it has been built to do. Hence, the simulations are performed in a microscopic simulation environment, and the results thereof are presented here.

6-1 Introduction

The objective of a simulation based evaluation is to offer a proof of concept for the developed theory. Of the two integration approaches for combining RM with VSL, the advanced strategy was translated to five algorithmic modules in Chapter 5. First three of the five modules are implemented in the simulation environment. Contour plots for spatio-temporal variations of flow, speed, density, actuation segment modes, detection segment modes and speed limit value are used to analyse the performance of the algorithm.

To that end, aspects relating to the simulation set-up prior to the implementation of the control algorithm are discussed in Section 6-2. These include the network layout and the traffic characteristics to achieve the test traffic behaviour, parametric tuning of the original COoperative Speed Control ALgorithm (COSCAL) v2 algorithm, and quantitative criteria for analysing the results. Section 6-3 discusses the simulation results for different scenarios - from the no control situation to complete implementation of the VSL related modules in the advanced strategy. Finally, a summary of the key finding from the simulations is presented in Section 6-4.

6-2 Simulation Set-up

The integrated control strategy is evaluated in version 5.40 of VISSIM - a traffic microsimulation software, and MATLAB software. VISSIM simulates traffic behaviour, while the controller itself is designed in MATLAB. The two software communicate via the COM interface; VISSIM communicates relevant traffic state measurements to the controller in MATLAB, which based on this data communicates back the appropriate control action to be implemented in the subsequent time step. A systematic simulation set-up is crucial for the accuracy of the simulation results. Hence, in the following sections, the simulation set-up is discussed.
6-2-1 Network Characteristics

A freeway merging section of a total length of 20.3 km, comprising of a 10 km long freeway section upstream of the on-ramp, a 0.3 km long freeway section with an additional merging lane, and a 10 km long freeway section downstream of the on-ramp is chosen. The length of the network is suitable for visualizing the spatial extent of a COSCAL v2 scheme in which the stabilization area crosses the ramp location. The freeway has 2 lanes, while the on-ramp section has a single lane - each lane is 3.5 m wide. Loop detectors are placed every 100 m and VSL gantries every 500 m, such that the gantry locations coincide with a loop detector location. Although in practice these infrastructures are typically less dense, this configuration allows for more accurate implementation and evaluation of the control system. Furthermore, the on-ramp is metered with a traffic signal located 100 m upstream of the upstream end of the merging area.

6-2-2 Traffic Characteristics

The simulations are performed for homogeneous traffic condition, with a mandatory speed limit of 120 km/h when the VSL scheme is not active. The speed distributions curve for cars defined in VISSIM realizes an average free-flow speed of 100 km/h in free-flow regime. When VSL scheme is activated, speed limits of 60 km/h are displayed at the appropriate gantries and an effective speed of nearly 68 km/h is achieved.

Further, VISSIM uses the Wiedamann 99 car following model that consists of ten calibration parameters to control the driving behaviour of individual vehicles in the simulation model. These parameters relate to car-following behaviour, lane changing distances, and lane changing behaviour. The tuning of these parameters is hugely important to simulate realistic traffic situations; in our case, these are (1) efficient merging condition at the on-ramp, and (2) a capacity drop from a moving jam. The used values of the Wiedemann 99 parameters are summarized in Table 6-1. These settings result in a freeway capacity of about 2060 veh/h/lane in simulation.

<table>
<thead>
<tr>
<th>VisSim Code</th>
<th>Parameter</th>
<th>Default Value</th>
<th>Used Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>CC0</td>
<td>Standstill distance</td>
<td>1.5 m</td>
<td>2 m</td>
</tr>
<tr>
<td>CC1</td>
<td>Headway time</td>
<td>0.90 s</td>
<td>0.70 s</td>
</tr>
<tr>
<td>CC2</td>
<td>Following Variation</td>
<td>4 m</td>
<td>6 m</td>
</tr>
<tr>
<td>CC3</td>
<td>Threshold for entering 'Following' state</td>
<td>-8 s</td>
<td>-8 s</td>
</tr>
<tr>
<td>CC4</td>
<td>Negative 'Following' Threshold</td>
<td>-0.35</td>
<td>-0.1</td>
</tr>
<tr>
<td>CC5</td>
<td>Positive 'Following' Threshold</td>
<td>0.35</td>
<td>0.1</td>
</tr>
<tr>
<td>CC6</td>
<td>Speed dependency of oscillation</td>
<td>11.44</td>
<td>6</td>
</tr>
<tr>
<td>CC7</td>
<td>Oscillation acceleration</td>
<td>0.25 m/s²</td>
<td>0.25 m/s²</td>
</tr>
<tr>
<td>CC8</td>
<td>Standstill acceleration</td>
<td>3.5 m/s²</td>
<td>0.5 m/s²</td>
</tr>
<tr>
<td>CC9</td>
<td>Acceleration at 80 km/h</td>
<td>1.5 m/s²</td>
<td>1.5 m/s²</td>
</tr>
</tbody>
</table>

The two main parameters important to generate desirable traffic situation are the standstill distance (CC0) and standstill acceleration (CC8). Standstill distance is the desirable spacing between vehicles when they are at rest. The inverse of this distance gives the density in jam state; the higher the standstill distance, the lower the jam density. As a result, it also determines the slope of the congestion branch in the fundamental diagram. A higher value than its default setting of 1.5 m ensures the typical propagation velocity of moving jams in real traffic. Similarly, the setting of the standstill acceleration parameter is crucial to create a capacity drop from a jam. With a low value of the parameter is chosen, vehicles take longer to accelerate to free-flow speed after leaving a jam. Hence, a low queue-discharge flow is realized in simulation.
6-2-3 Tuning Control Parameters

COSCAL v2 uses several control parameters that must be tuned to appropriate values for the algorithm to perform desirably, i.e. to resolve moving jams and improve freeway efficiency. Values of some of these parameters are chosen based on off-line traffic data, while others must be fine tuned to real-traffic measurements. Details about the tuning process and appropriate values of all the parameters can be found in (Hegyi, 2013). The used settings of the tuning parameters in COSCAL v2 are tabulated in Table 6-2.

<table>
<thead>
<tr>
<th>Related task</th>
<th>COSCAL Parameter</th>
<th>Description</th>
<th>Used Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Jam detection</td>
<td>$v^{th}$</td>
<td>speed threshold for jam detection</td>
<td>30 km/h</td>
</tr>
<tr>
<td></td>
<td>$z^{ff}$</td>
<td>hysteresis parameter for transition from free-flow to jam state</td>
<td>100 km/h*s</td>
</tr>
<tr>
<td></td>
<td>$z^{jam}$</td>
<td>hysteresis parameter for transition from jam to free-flow state</td>
<td>-40 km/h*s</td>
</tr>
<tr>
<td>Jam resolution</td>
<td>$v^{eff}$</td>
<td>effective speed limit</td>
<td>70 km/h</td>
</tr>
<tr>
<td></td>
<td>$v^{jam-h}$</td>
<td>jam head propagation speed</td>
<td>-5.5 km/h</td>
</tr>
<tr>
<td></td>
<td>$q^{jam-h}$</td>
<td>flow that crosses the jam head</td>
<td>3350 veh/h</td>
</tr>
<tr>
<td>Stabilization</td>
<td>$\bar{\rho}$</td>
<td>target density in stabilization area</td>
<td>29 veh/km/lane</td>
</tr>
<tr>
<td></td>
<td>$d^{stab}$</td>
<td>offset to check for too high densities</td>
<td>2 km</td>
</tr>
<tr>
<td></td>
<td>$a^{dec}$</td>
<td>nominal deceleration of vehicles</td>
<td>-3 m/s²</td>
</tr>
<tr>
<td>Speed limits release</td>
<td>$v^{[4A-5A]}$</td>
<td>speed of the S-head shockwave</td>
<td>-21 km/h</td>
</tr>
<tr>
<td>Resolvability</td>
<td>$x^{act, min}$</td>
<td>offset for most upstream point initial speed limit location</td>
<td>2 km</td>
</tr>
<tr>
<td>Jam head tracking</td>
<td>$v^{jam-h, max}$</td>
<td>maximum upstream propagation speed of jam</td>
<td>-72 km/h</td>
</tr>
</tbody>
</table>

Two parameters related to the stabilization scheme have been changed from the original setting, namely, the propagation speed of the S-head (under zero RM flow condition) and target density in the speed-limited stabilization area. The S-head speed is changed from its original value of -18 km/h to -21 km/h, and the stabilization density from 18 veh/km/h to 29 veh/km/lane. The values have been chosen such that the outflow from the stabilization area is closest to the free-flow capacity, and at the same time, the speed-limited flow is stable at the set target density. In the current setting, theoretically an outflow of 2181 veh/h/lane (4362 veh/h for 2 lanes) should be realized. Additionally, choosing a faster (more negative) propagation speed for the S-head offers a higher range of (negative) speeds for the S-head upstream of the on-ramp. This range determines the admissible range of RM flows for which the S-head shockwave does not propagate downstream (with a positive slope); the larger the range of negative S-head speeds, the higher the admissible RM flows can be.
6-3 Simulation Results

Multiple simulations for different boundary conditions were performed to verify the functioning of the developed algorithm. Select results from these runs are presented to discuss the control performance and potential improvements to the algorithm.

6-3-1 Base Case

The base case defines the ‘no control’ situation against which an improvement in traffic performance under different control scenarios can be evaluated. In this study, the no control situation is a moving jam that results in a capacity drop on the freeway. To that end, a slow moving bottleneck is created by slowing down vehicle to a speed of 10 km/h in space-time area of 1.1 km and 110 s. This results in a moving jam as shown in Figure 6-1. The queue discharge flow is about 1802 veh/h/lane (3604 veh/h for two-lane freeway), resulting in a capacity drop of nearly 12.5%.

![Figure 6-1: Contour plots of the base case showing a moving jam with a queue discharge rate of approximately 1810 veh/h/lane.](image)

6-3-2 COSCAL v2 without RM

If no additional RM flows disrupt the VSL scheme, the algorithm performs as per the chosen tuning parameters in Section 6-2-3. As can be observed in Figure 6-2, the moving jam is resolved with speed-limits, after which the stabilization area (further upstream) ensures an improvement in efficiency. However, it must be noted that the traffic simulator realizes an average density of 27.5 veh/km/lane for a target density of 29 veh/km/lane. This results in flow of 4022 veh/h after the jam is resolved. Although this flow is higher than the queue-discharge flow of 3604 veh/h, it is 7.8% lower than its theoretically expected value of 4362 veh/h (given the target stabilization density and speed of S-head shockwave).
6-3 Simulation Results

Figure 6-2: Contour plots of COSCAL v2 scheme for freeway demand of 1860 veh/h/lane.

6-3-3 COSCAL v2 with stand-alone RM

An important postulate in this work was that when RM and VSL strategies are implemented stand-alone, the effectiveness of COSCAL v2, as well as overall freeway efficiency are reduced. For this reason, the performance of COSCAL v2 algorithm with different RM flows was tested.

In order to achieve maximum efficiency improvement, the target density inside the stabilization is set to its critical value. Its value can be critical due to two possible reasons - either it is the maximum stable density achievable under speed-limits or it results in a capacity flow downstream of the stabilization area (state [5A]). Depending on which criteria holds and the value of RM flows, a congestion can be triggered at the ramp section inside the stabilization area and/or after the S-head shockwave crosses the on-ramp location.

In Figure 6-3, it can be seen that the merging flow initiates a congestion inside the stabilization area just downstream of the on-ramp. Such a situation is unfavourable since the implementation of COSCAL v2 is limited to a single jam. As a result, the algorithm does not adapt to a jam that occur while the scheme is active. Furthermore, the unresolved congestion blocks the RM flows, and reduces the flow exiting the stabilization area. This results in gain of total time spent (TTS). Furthermore, as the freeway demand increases, even a low value of RM flow can result in the onset of congestion. This is illustrated in Figure ??, wherein a RM flow of 50 veh/h triggers jam waves inside as well as downstream of the stabilization area.

The performance of the algorithm is found to be sensitive to the tuning of the jam resolving parameters. TTS gains were noted, especially when the tuning parameters underestimate the number of vehicles required for jam resolution. The outcome is similar to the situation when RM is active and the jam resolving
area crosses the on-ramp. In such a case, the jam resolving task does not account for the additional merging vehicles. This leads to intermediate increase in the length of freeway speed-limited for jam resolution, and hence a lowered effectiveness of the algorithm. For this reason, for all cases with RM flow higher than 100 veh/h, the flow is set to 50 veh/h in the first 1000s to ensure that the jam resolution area does not cross the on-ramp.

![Figure 6-3: Congestion onset in COSCAL v2 scheme with 200 veh/h RM flow & 1860 veh/h/lane freeway demand.](image-url)
6-3 Simulation Results

Figure 6-4: Congestion onset in COSCAL v2 scheme with 50 veh/h RM flow & 1880 veh/h/lane freeway demand.

6-3-4 Advanced strategy for integrated RM with COSCAL v2

Module 1, 2 and 3 of the advanced strategy were implemented in simulation. These modules relate to the adaptation of the S-head and S-tail shockwaves upstream of the on-ramp, and prediction of the time when the S-tail will cross the on-ramp. The shockwave trajectories are estimated based on the RM flow which should merge onto the freeway at any time.

Theoretically, it is expected that as the RM flow increases, the S-head shockwave should become less steep (less negative slope) and the S-tail shockwave should propagate faster upstream (more negative slope). The adaptation of S-head reduces the freeway flow arriving after the stabilization area has crossed the ramp section, and of the S-tail reduces the flow arriving while speed-limitation is active at the location. The difference in the slope of the S-head shockwave becomes clear on comparing the contour plots in Figures 6-5 and 6-7. In the latter case, the RM flow is lower and hence the slope of the S-head is more steep.

The propagation of the S-tail shockwave in Figure 6-5 is determined as per Module 3 of the advanced strategy. The flow and density profile at the on-ramp section for this case are plotted to analyse its performance. The graphs reflect an increase in density and a decrease in flow between the time the S-tail and the S-head shockwaves cross the ramp section, i.e during the time speed limits are active at the on-ramp. Additionally, a few important aspects in the implementation of the module were discovered from the tests related to the S-tail propagation. These are discussed next:
Figure 6-5: Contour plots of the integrated approach for 100 veh/h RM flow & 1860 veh/h/lane freeway demand.

Figure 6-6: Flow and density profiles at the ramp section for integrated approach with RM flow of 100 veh/h and freeway demand of 1860 veh/h/lane. The vertical lines in either plots indicates the time instants when the S-tail and S-head shockwaves crossed the ramp location.
- **Multiple crossing of the S-tail shockwave over ramp location**: during theoretical development, the presumption is that if the S-tail shockwave crosses the ramp location it propagates upstream until the VSL scheme is resolved upstream of the on-ramp. However, this may not always hold. When the S-tail shockwave crosses the on-ramp but the freeway demand and the RM flow are not sufficiently high, S-tail tends to oscillate about the ramp section. This is problematic for two reasons - (1) the freeway capacity at the section varies in free-flow and under speed limits; so the freeway flow that is allowed to arrive at the ramp section does not account for these fluctuations in capacity, and (2) the oscillations can result in vehicles driving in and out of speed-limited area multiple times in a short interval of time (undesirable from a driving comfort and safety perspective). Such a situation can be seen in Figure 6-7, where the S-tail tends to oscillate about the on-ramp and as a result propagates disturbances which lead to a downstream congestion.

![Figure 6-7: Contour plots showing oscillations of S-tail shockwave at the ramp section in the integrated approach; boundary condition include RM flow of 200 veh/h and freeway demand of 1865 veh/h/lane.](image)

- **Fast downstream propagation of S-tail shockwave**: the theory specifically does not include a criteria for the maximum positive propagation speed of the S-tail shockwave. However, it is found in simulation that when the speed-limits are released sharply, i.e. the forward propagating speed of the shockwave is too high it leads to sudden increase in traffic density that may trigger jam waves. Hence, speed-limits should not be deactivated too fast. Further testing should be performed to determine the maximum release speed based on local traffic characteristics. Simulation results in Figure 6-8 exemplify such a situation.
• **Downstream propagating S-head shockwave**: to lower the mainstream flow according to the additional RM flows, the speed of the S-head shockwave upstream of the on-ramp is adjusted. Theoretically, it was understood that the higher the RM flows, the higher (less negative) is the required propagation speed of the S-head.

However, the situation of a downstream propagating S-head shockwave was not anticipated. In simulation, this was found to be a common occurrence for high RM flows - flows higher than about 350 veh/h/lane (refer to Figure 6-9). A downstream propagating S-head has consequence for the design of the strategy. In current strategy, the flow capacity at the on-ramp section after the S-head crosses the on-ramp is taken as the free-flow capacity of the freeway section. However, this capacity does not hold if the shockwave propagates downstream with a positive slope.

In order to avoid this situation, the original COSCAL v2 parameters were re-tuned, and RM flows were chosen from within a correspondingly suitable range of values. However, from an implementation perspective this is restrictive for the RM strategy and can deteriorate the performance of the queue controller. Therefore, the theory must be adapted to predict such a situation, and to consider the capacity flow accordingly.

**Figure 6-8**: Contour plots showing jam waves from steep downstream propagating S-tail shockwave in the integrated approach; boundary condition include 100 veh/h RM flow & 1870 veh/h/lane freeway demand.
6-3 Simulation Results

Figure 6-9: Scenario showing forward propagating S-head shockwave; boundary condition include 800 veh/h RM flow & 1860 veh/h/lane freeway demand.

6-3-5 Quantitative evaluation

Total time spent (TTS) is the total time spent by all the vehicle in a network in a given control time interval. A TTS decrease is indicative of efficiency improvement for similar network inflow profiles in the compared scenarios. This can be used as the quantitative criteria for measuring improvement in freeway efficiency. The TTS in the network over a time horizon $K$, can be theoretically determined as in the equation below. Here, $N(k)$ are the total number of vehicles in the network in time step $k$.

$$TTS = T \sum_{k=0}^{K} N(k) \quad (6-1)$$

A desirable control strategy should then minimize the TTS. The minimization of the TTS is mathematically equivalent to maximization of the time-weighted freeway outflows in that time horizon. The proof for their equivalence can be found in Papageorgiou et al. (2003). Lets denote the time-weighted flow as TWF, which can be formulated as:

$$TWF = T^2 \sum_{k=0}^{K-1} (K - k)q_{out}^k \quad (6-2)$$
here, $q^{\text{out}}(k)$ is the flow exiting at the downstream end of the network at time step $k$.

Furthermore, TTS can alternately be determined from an estimate of TWF. In its formulation below, $N(k)$ is the total number of vehicles on the network and $q^{\text{in}}(k)$ the freeway demand at time step $k$:

$$
\text{TTS} = T \sum_{k=0}^{K} \left( N(0) + \sum_{\kappa=0}^{k-1} q^{\text{in}}(\kappa) \right) - \text{TWF}
$$

$$
= TK N(0) + T^2 \sum_{k=0}^{K-1} (K - k) q^{\text{in}}(k) - \text{TWF}
$$

The advantage of formulating TTS in terms of TWF is that it does not require individual vehicle data or density measurements over the freeway length which are typically less accurate. Therefore, the above macroscopic formulation of TTS is suitable for the formulation of COSCAL v2 and its extensions.

The criteria is used to get a rough estimate of the impact of the developed strategy on freeway efficiency. However, initial results with the above criteria were not very conclusive. A TTS of 575.7 veh*h is reported for the base case in Figure 6-1. Only a 2.3% improvement in TTS was found when COSCAL v2 is implemented without RM (Figure 6-2). This is unrealistic since the jam is resolved and capacity drop of about 12.5% is recovered. Likewise, for the advanced strategy with 100 veh/h RM flows the TTS is 569.9 veh*h - not reflective to the improvement observable from its contour plot in Figure 6-5. It is therefore recommended that the implementation of the criteria and other possible reasons for conflicting results should be further investigated.

### 6-4 Summary

Simulation results in this chapter offer some evidence for the feasibility of the developed integration strategy in Chapter 4. Contour plots for select traffic and control variables for the no-control case, COSCAL v2 without RM, COSCAL v2 with RM, and COSCAL v2 integrated with RM were compared to demonstrate the potential improvements from the developed approach; these include -

- In COSCAL v2, congestion aggravates as RM flow increases. The integrated strategy can regulate the freeway flows arriving at the ramp to prevent such breakdown.

- Jam resolution parameters of COSCAL v2 require fine-tuning such that the number of speed-limited vehicles required for jam resolution are not under-estimated. An identical undesirable effect occurs when RM is not integrated with VSL. This is because the additional merging vehicles are not included in the prediction of the jam resolution area, and the feedback structure of COSCAL v2 responds by abruptly extending speed-limits at some future time instants. Such under-estimation of the jam resolution area can have a huge effect on the overall VSL performance.

- The integrated strategy is currently suitable for a range of RM flows based on the chosen stabilization parameters of COSCAL v2. The restriction follows from downstream propagation of the S-head shockwave for higher ramp flows.

Learnings from the simulations that should guide some additional considerations for the integrated strategy include -

- The capacity function at the ramp section is crucial to the prediction of the VSL scheme in the integrated strategy. This function should be responsive to the actual propagation of the S-head and S-tail shockwaves, in a way it not currently implemented. However, the feedback structure of the algorithm is suitable for necessary development.
• A slow moving vehicle due to the merging mechanism at the ramp section can result in disturbances in the stabilization area. These were typically observed as widening downstream propagating gaps in simulation tests. A possible reasoning could be that the high density stabilization area is prone to moving bottlenecks, easily triggered for even slightly lower speeds than the effective speed limits value. Alternately, it could possibly be due to unrealistic driving behaviour in Vissim.

• Multiple crossings of the S-tail shockwave can be dealt with a responsive capacity function. However, an alternative could be to prevent such an occurrence by suitable selection of RM rate in Module 5 of the advanced strategy. An increased RM rate would necessitate a lower freeway flow at the ramp section, and hence extension of speed-limits further upstream.
Variable speed limits (VSL) strategies have been found to be effective as a preventive and counter-active traffic control measures. A macroscopic speed control algorithm, COoperative Speed Control ALgornithm v2 (Hegyi, 2013), was specifically studied in this work. The research objective was to adapt and extend the algorithm for integration with ramp metering (RM) control measure. To that end, the key focus remained on theoretical advancement and its functional verification in simulation.

In this chapter, first, the motivations and main contributions are broadly presented in Section 7-1. Next, Section 7-2 describes how the three main research objectives were met. Subsequently, practical and policy recommendations for further development, and field implementation of the control system are made in Section 7-3.

7-1 Motivation and contributions

This research was motivated by a practical difficulty in implementing COSCAL v2. On-ramp sections are potential bottlenecks for activation of the variable speed limits (VSL) strategy. However, ramp flows are not included in the design of the algorithm. This deteriorates the effectiveness of the algorithm at these merging sections. Simulation results in Chapter 6 demonstrated how additional flows at a freeway merging section can result in jam waves while the VSL scheme is still active. This is an undesirable situation that can result in increased total time spent (TTS) on the freeway, reduced merging flows and hence, faster growing queues at the on-ramp.

Furthermore, RM measure on the one hand can improve: the efficiency on the freeway, and the effectiveness of COSCAL v2, on the other, it can result in deteriorated performance of the sub-network. This is because RM and ramp queue control are inherently competitive - the lower the RM flows, the faster the queue on the on-ramp grows. However, the situation gets problematic for the VSL strategy if the ramp queue spills over to the sub-network. When this happens, RM control is switched off to release the on-ramp queue and restore traffic deterioration of the lower network. The abrupt influx from the on-ramp can disrupt the VSL scheme deteriorating freeway performance. This trade-off between efficiency improvement for the freeway and the urban network - in implementing two traffic control measures - offers a research opportunity.

Therefore, two possible theoretical extensions to the COoperative Speed Control ALgornithm (COSCAL) v2 algorithm for integration with RM were developed in this work:

- A basic integration approach that can resolve moving jams to improve freeway efficiency, given a constant RM flow. The extension fits with the reactive formulation of the original algorithm, and
uses a similar feedback structure to generate the VSL scheme at each time step based on traffic measurements in the previous. This approach can prevent a spillback of on-ramp queue as long as a suitably high RM flow is chosen that the VSL strategy can be adapted for (given its controller parameters).

- An advanced integrated strategy that balances efficiency improvement on the freeway with deterioration of urban network from ramp queue spillback. The advantage in this strategy is derived from its integration approach that uses cumulative curves to combine RM, VSL and queue control. Cumulative curves are applied to determine a range of feasible RM flows that consider: queue-length constraints, policy restrictions on maximum and minimum RM rates, the VSL approach and the freeway state. Further, COSCAL v2 is extended to guarantee jam resolution while RM flows are chosen from within this feasible range. Both RM and VSL approaches are anticipatory, and predict the scheme in the future to determine optimal control decisions in the current time step. Therefore, queue spillback on-ramp and freeway breakdown - while speed-limits are active - are pro-actively prevented in this approach.

The exploration of two different extensions to COSCAL v2 has highlighted the advantage of anticipatory traffic control for higher responsiveness. In the predictive formulation of the advanced RM strategy, proactive decisions can be made for a deteriorating traffic condition on the freeway or on the on-ramp at a later time.

The advanced strategy was therefore developed to an algorithmic version that can implemented to a controller. Due to time constraints, only a few algorithmic modules of the advanced strategy could be evaluated in simulation. The insights from the simulation study are used to recommend further improvements to the developed theory.

7.2 Findings and recommendations

The main findings and the recommendations thereof are presented in this section, by addressing the research objectives that were designed to answer the main research question, restated below -

"Can a macroscopic variable speed control strategy integrated with ramp metering improve freeway efficiency, while managing queues at a merging section?"

7.2.1 Research Objective 1: Learnings from literature survey

The literature survey was conducted with three main objectives: (1) to identify different traffic flow theoretic and different control approaches to dynamic speed limits, (2) to understand the desirable features for an on-ramp queue controller, and (3) to find the most important considerations for integration of COSCAL v2 with RM.

To that end, first VSL approaches were differentiated as those resulting in traffic homogenization, and those resulting in flow reduction. The importance of the implementation dynamics for flow reduction based approaches was presented. Here, the flow reduction approaches were further classified on the basis of implementation mechanics as: instantaneous speed limits applied over a length of freeway at the same time; stationary speed limits applied at a fixed freeway section for a considerable time interval; and speed limits with moving fronts which include all intermediate scenarios between instantaneous and stationary implementation of VSL. Regulating the fronts (shockwaves) of the speed-limited area allow to create traffic states with desired flow and density conditions. Further, VSL were understood from a control perspective. Here, regulatory strategies were found to be a middle ground between the low responsiveness of heuristic approaches and high computational demand of model-based optimization approaches.

Next, various queue management approaches were surveyed to identify some design guidelines for a queue controller. The most important requisite was found to be that the queue controller should not result in
underutilization of the on-ramp storage capacity. Therefore, a minimum ramp queue length requirement was recommended. Also, the triggers for override of control decisions from the queue controller should be well-defined. It was identified that the performance of the queue management approach can be sensitive to the length (storage capacity) of the on-ramp. This is an important consideration for field implementation and should be tested for. Lastly, it was suggested that the criteria for deactivation of queue management - when the freeway is in a congested traffic state - should be identified in the design of the controller.

Lastly, a key advantage of integrating control measures is that the traffic can be continued to be managed, even when restrictions for one of the measures are reached. For the integration of RM with VSL control measure, ramp queue violation was understood as important. The response of the integrated strategy to queue restrictions being reached on the on-ramp can be limited by its complexity and computational demand.

7-2-2 Research Objective 2: Development of COSCAL v2 for integration with ramp metering

The second research objective entailed development of an integrated VSL and RM strategy that improves freeway efficiency and prevents spillback of on-ramp queues.

To achieve this goal, COSCAL v2 algorithm was used as the test bed for an integrated control strategy. Some theoretical assumptions and simplifications were made while developing the new theory. In order to ensure the functional correctness of the algorithm, these assumptions must be recognised.

The validity of these assumptions determines how realistically the traffic behaviour is represented, and how well the desired behaviour can be achieved from application of the control strategy in practice. While some of these assumptions can relaxed by tuning the controller parameters, others should be relaxed for desired performance. The main assumptions are summarised below:

7-2-2-1 Theoretical assumptions

(1) A constant average free flow speed. Traffic information in free flow regime is assumed to propagate forward, in the direction of the traffic, at this speed; free flow speed of 100 km/h was used in the simulation study.

(2) A constant effective speed under speed limits. This assumes requisite compliance to the displayed speed limit value; an effective speed of 70 km/h for displayed speed limits of 60 km/h was used in the simulation study.

(3) Homogeneous traffic flow conditions within the length of each detection segment; a regular detection segment length of 100 m was used in simulation.

(4) A known on-ramp demand profile for the duration of the VSL scheme.

(5) Constant capacity of the freeway on-ramp section in free-flow condition and under speed limits.

7-2-2-2 Basic and advanced integrated VSL and RM strategies

Two alternative integrated strategies were developed, as mentioned earlier. The main characteristics, advantages and shortcomings of the two strategies are concluded here. The theoretical development was initiated with a basic extension of COSCAL v2 that is compatible with its current formulation. The core principle employed in this strategy is to lower the density in the area upstream of the on-ramp that is speed-limited for stabilization. The reduced density is chosen to sufficiently decrease the flow arriving at the on-ramp. This is theoretically possible, since the speed within the controlled freeway stretch is the effective speed under speed-limitation. Then, lowering the density achieves a lower flow. This is understood from the
fundamental relationship between traffic flow variables - flow $q(k)$, density $\rho(k)$ and space-mean speed $v(k)$:

$$q(k) = \rho(k) \times v(k) \quad (7-1)$$

However, there are some limitations to the basic RM strategy which were addressed in the advanced RM strategy. In the basic strategy, a desired density criterion determines the most upstream speed-limited segment, i.e. the tail of the stabilization area. This is less desirable because in order to reduce the flow at the ramp section, the target density in the entire stabilization area upstream of the on-ramp must be lowered. A lower target density also implies an increase in the spatio-temporal area that should be speed-limited and hence, an increase in TTS. This is also why the strategy holds only for a constant RM flow rate. A varying RM flow requires a varying desired freeway flow at the on-ramp section. In turn, to achieve this, a variable target density is needed over the freeway segments at any given time. The density distribution thus required is one, hard to estimate, and second, hard to implement given how target density is realized in COSCAL v2. The requirement of a constant RM rate leads to another limitation from this strategy. If the integrated strategy is to prevent a queue spillback at the on-ramp, the ramp controller must enforce the least restrictive (highest) RM rate, which is not optimal for freeway efficiency.

In an alternate methodology, the VSL approach in the advanced strategy was extended to be compatible with time-varying RM flows. The approach used for this regulates the propagation of the upstream and downstream fronts of the speed-limited area. In doing so, a desired freeway flow - based on the RM flows and the capacity at the ramp section - can be achieved at any given time. This extension required translation of microscopic traffic flow concepts to a macroscopic formulation compatible with COSCAL v2.

Additionally, a cumulative curves based approach was used for the design of a new RM strategy, and for its integration with the extended VSL approach. The approach can determine a range of feasible RM flows, given a known on-ramp demand profile. A unique advantage of the approach is that it includes queue-length restrictions on the on-ramp, and the most restrictive implementation of speed-limits, to determine the achievable ramp flows. Furthermore, both RM and VSL use a predictive approach wherein the control scheme is determined over a prediction horizon at each time step. Therefore, both control measures pro-actively determine control based on traffic predictions in the future, making it more suitable for on-ramp queue management. In other words, the integrated strategy pro-actively prevents a queue-spillback at the on-ramp. The advantages of the advanced strategy were interesting for testing in simulation. The main insights from the simulation study are presented next.

### 7-2-3 Research Objective 3: Verification of the algorithm

The third research objective is to check for the functional correctness of the developed strategy by means of simulation.

To achieve this objective, the advanced integrated strategy was translated to an algorithm that enables the controller to achieve the desired control behaviour. The algorithmic formulation of COSCAL v2 was used as a basis for this - using unique driving modes to identify the different detection and actuation states in its implementation. Furthermore, the developed integration strategy was identified into five unique modules, three relating to the VSL measure and two to RM. Pseudo-algorithms for all of these modules were detailed. However, only modules related to the VSL approach were implemented in Vissim micro-simulation environment. The simulations performed for different traffic scenarios suggest a potential improvement in freeway efficiency from the approach. Jam waves that otherwise occur from independent implementation of VSL and RM were prevented by the adaptation of the S-head and S-tail shockwaves in the advanced strategy.

Some critical design limitations were highlighted in the evaluation process. Firstly, the capacity profile at the on-ramp section is based on the prediction of the first time that the S-head and the S-tail shockwaves
cross the on-ramp (while propagating upstream). It is assumed that the arriving flows at this section are speed-limited between these time instants. However, depending on the freeway demand, fluctuations in RM flow can cause the shockwaves to cross the on-ramp multiple times. A higher flow arrives at free flow speed each time the S-tail propagates downstream over the on-ramp, triggering disturbances at the location. Therefore, if the capacity function is responsive to the actual propagation of these shockwaves, these disturbances can be avoided. The capacity profile is determining in the estimation of these shockwave trajectories, and hence, this very relevant for implementation of the strategy in practice.

Secondly, when the ramp controller orders high RM flow (after the S-head crosses the on-ramp), the desired S-head trajectory propagates downstream of the on-ramp. This situation was not anticipated during theoretical development. Simulation tests were therefore restricted to suitable range of RM values. However, this restriction could be relaxed with some modifications to Module 3 of the algorithm.

Finally, the VSL strategy uses the freeway traffic measurements at any time to predict the evolution of the VSL scheme. The prediction horizon in the approach extends till the time the most upstream vehicle that enters speed-limitation has crossed the on-ramp location. Therefore, the duration of the prediction horizon depends on the detection location of the jam, and the traffic condition on the freeway. The longer the prediction horizon gets, traffic data from detection segments even further upstream is required for the prediction of the VSL scheme. In simulation, traffic data further upstream of the network boundary was required. This was resolved by assuming constant values of the traffic flow variables upstream of the first detection segment. Since detector measurements over extremely long freeway lengths is a practical limitation as well, the inaccuracy of the assumption should be validated with real traffic data.

This work has in part demonstrated the conceptual validity of the tested integrated strategy. Therefore, there is substantial potential and need for further evaluation - in terms of correctness and performance - of the developed theory. Subsequent research steps should be performed for a complete evaluation. These include: (1) implementation of the RM related modules, (2) testing the complete strategy with more dynamic RM flow profile, and (3) exhaustive quantitative analysis of efficiency improvement from the approach for the advanced integrated strategy. The basic strategy must be translated to an algorithmic formulation first, and then verified and evaluated for performance.

### 7-3 Future work and practical implications

In this section, a discussion on the future research and practical implications of the performed research is presented. Suggestions for theoretical modules that directly complement the developed theory are made first. Then, the most important considerations for testing the strategy in a field-test, and supporting decision-making are discussed.

### 7-3-1 Recommendations for further theoretical development

This research initiated theory development towards addressing a practical problem that faces the implementation of COSCAL v2 at freeway merging sections. In the process, some theoretical bottlenecks, and some useful extension possibilities have come forth. Theoretical directions, in addition to the ones that followed from the simulation-based evaluation, are recommended here.

1. **Adjusting the speed of the S-head shockwave downstream of the on-ramp:** the integration strategy was based on controlling the propagation of the S-head and S-tail shockwaves upstream of the on-ramp location. In doing so, the mainstream flows arriving at the on-ramp could be regulated desirably. The same theoretical principle can be useful to dynamically control the outflow from the S-head shockwave downstream of the on-ramp.

   In an interesting application, the S-head speed could be adapted to counteract inefficiencies, created as a result of the control strategy or measured otherwise. As an example, consider the situation when

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the combined freeway and RM flows exceed the capacity at the on-ramp section. If this occurs before speed-limits cross the on-ramp, the designed response is to instantaneously apply speed-limits till the on-ramp location, at the earliest time of capacity overshoot (Section 4-3-4-3). However, doing so creates a downstream propagating low flow gap, of the size of the time difference between the time that the capacity overshoots and the time that the speed-limits would have otherwise crossed the on-ramp. The gap is the case of an inefficiency that is a result of the control strategy itself. Such an inefficiency can be eliminated by appropriate and timely adjustment of the S-head shockwave.

(2) Relaxing the assumption of known on-ramp demand: in the developed strategy, especially the queue controller, depends crucially on the prediction of on-ramp demand flow profile for the duration of the VSL scheme. This function is assumed as a known in the current formulation. However, present-day systems do not allow for sufficiently accurate demand forecasts. Relaxation of this assumption therefore is an important theoretical development for testing the algorithm in practice.

Aside from the readiness of better prediction models in the future, a potential solution could be to use more restrictive thresholds for the control parameters. For instance, the desired maximum queue length in the queue controller could be set to an appropriate fraction of its maximum possible value such that inaccuracies in the demand forecast are compensated. Alternately, it could be explored how to adapt the strategy to be independent of the on-ramp demand profile.

7-3-2 Considerations for field implementation

(1) Detection-actuation and communication delays: In the developed control strategy, measurements at each time step are used to predict the control scheme for the remaining duration of the scheme. This informs the control action in the subsequent time step. However, depending on the size of the control time step, a variation in the delays between (1) when traffic measurements are available, (2) the computation time of the control algorithm, and (3) the time it takes for the generated scheme to be displayed on the speed limit gantries, is likely. Depending on the magnitude of these delays, the performance of the algorithm may be affected.

Hence, from an implementation point of view, it is important to estimate these delays and to compensate for them in the control algorithm.

(2) Estimation of $v_f$ speed: The prediction methodology in the advanced integrated strategy uses an estimate of the average free-flow speed. This value however is dependent on multiple factors - road design, flow rates, traffic composition (e.g. higher truck percentage would result in a lower $v_f$), and external time-dependent factors (e.g. day-light, weather condition etcetera). Therefore, accuracy of the prediction model may require time to time on-line tuning of the free-flow speed.

(3) Length of the detection segments: Even though the developed theory is suitable for varying detection segment lengths, it has not been tested for the same. This is considered important because, the prediction of the control scheme in each time step assumes homogeneous traffic condition in each segment. If the length of the segment gets too long, the assumption may not be valid.

Overall, the control scheme prediction translates measurements from the detection segments to cumulative curves at the on-ramp location. This implies that the density/scarcity of loop detectors on the freeway can influence the accuracy of the predictions.

7-3-3 Policy implications

One of the hurdles in the implementation of new traffic control measures is their compatibility with more widely used control measures. Lack of coordination between multiple measures deployed simultaneously can compromise benefits from either strategies. By developing approaches to integrate a sophisticated VSL approach with RM measure, an advance has been made in this regard. The contributions in this work will enable a more smooth implementation of the VSL strategy in practice.
Specifically, the integration of a control measure with RM raises a policy concern. The current policy is designed to balance losses from congestion on freeways (managed centrally), and queuing on ramps and subsequent performance deterioration on the urban network (managed regionally). The directive is to deactivate RM if the ramp queue spills-back onto a lower network. Consideration for a sudden surge in merging RM flow must be made when integrating RM with another measure. Adding queue-length constraints to a RM strategy prevents queue-spillback, and hence the occurrence of such a situation. In the design of the advanced integrated strategy, queue-length constraints were additionally incorporated for this reason.

Additionally, simulation tests revealed some safety concerns in implementing the advanced strategy. A high variation in the RM flows can result in a significant fluctuation in the estimated propagation of the S-tail shockwave. Multiple simultaneous fluctuations would imply that vehicles drive in and out of speed-limits more than once in a fairly short interval of time, which is undesirable from driving safety perspective. Therefore, policy directive should guide development of a smoothing module that dampens over-fluctuations to ensure vehicles drive into speed-limits once in a VSL scheme. Furthermore, large values of positive slopes (fast downstream propagation) of the S-tail shockwave can destabilize traffic to trigger jam waves. Therefore, a suitable maximum value of the S-tail shockwave must be determined. This also leads to an understanding that VSL scheme should not be deactivated abruptly from another conflicting policy.

The potential of vehicle-to-vehicle and vehicle-to-infrastructure communication is increasingly being explored for traffic management. In that regard, the VSL approach is forward-looking; while COSCAL v2 algorithm uses vehicle-to-infrastructure communication in the detection tasks, COSCAL v1 is compatible for both, in-car detection and actuation. The benefits of vehicular intelligence for COSCAL v2 include faster jam detection, better jam tracking and more accurate traffic state estimation. The advanced integration approach can additionally benefit from in-car technology - (1) infrastructure-to-vehicle communication can improve compliance to speed limits, (2) speed-limits can be communicated more timely resulting in a more accurate realization of the desired trajectories of the stabilization fronts, and (3) vehicle-to-vehicle communication can facilitate assisted merging; thereby, more homogeneous flow can be achieved at the ramp section.


Glossary

List of Acronyms

VSL  variable speed limits
VMS  variable message signs
RM   ramp metering
SPECIALIST  SPEed Controlling ALgorItm using Shockwave Theory
COSCAL  COoperative Speed Control ALgorithm
TTS   total time spent
TWF   time weighted flow
FD    fundamental diagram
ALINEA Asservissement linéaire d’entrée autoroutière
MTFC  Mainstream Traffic Flow Control
HERO  HEuristic Ramp-metering coOrdination
AMOC  Advanced Motorway Optimal Control
CRM   Coordinated Ramp Metering
AMOC  Advanced Motorway Optimal Control
MPC   Model Predictive Control