Universality of electron correlations in conducting carbon nanotubes

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An effective low-energy Hamiltonian of interacting electrons in conducting single-wall carbon nanotubes with arbitrary chirality is derived from the microscopic lattice model. The parameters of the Hamiltonian show very weak dependence on the chiral angle, which makes the low-energy properties of conducting chiral nanotubes universal. The strongest Mott-like electron instability at half filling is investigated within the self-consistent harmonic approximation. The energy gaps occur in all modes of elementary excitations and estimate at 0.01–0.1 eV. [S0163-1829(99)50616-4]

Single-wall carbon nanotubes (SWNT's) are linear macromolecules whose individual properties can be studied by methods of nanophysics.¹ A recent demonstration of electron transport through single² and multiple³ SWNT's has been followed by remarkable observations of atomic structure,^{4,5} one-dimensional van Hove singularities,⁴ standing electron waves⁶ and, possibly, electron correlations⁷ in these systems. Moreover, the first prototype of a functional device—the nanotube field effect transistor working at room temperature—has been fabricated recently.⁸

Structurally uniform SWNT's can be characterized by the wrapping vector $\vec{w} = N_1 \vec{a}_+ + N_2 \vec{a}_-$ given by the linear combination of primitive lattice vectors $\vec{a}_\pm = (\pm 1, \sqrt{3})a/2$, with $a \approx 0.246$ nm (Fig. 1). It is natural to separate nonchiral armchair ($N_1 = N_2$) and zigzag ($N_1 = -N_2$) nanotubes from their chiral counterparts. A recent scanning tunneling microscopy study⁴ has revealed that individual SWNT's are generally chiral. According to the single-particle model, the nanotubes with $N_1 - N_2 = 0 \bmod 3$ have gapless energy spectrum⁹ and are therefore conducting; otherwise, the energy spectrum is gapped and SWNT's are insulating. Therefore, on the level of noninteracting electrons, physical properties of SWNT's are determined by their geometry.

The Coulomb interaction in one-dimensional SWNT's should result in a variety of correlation effects due to the non-Fermi-liquid ground state of the system. In particular, metallic armchair SWNT's are predicted to be Mott insulating at half-filling.^{10–13} Upon doping the nanotubes become conducting but still display density wave instabilities in three modes of elementary excitations with neutral total charge.^{13,14}

Experimental observation of electron correlations still remains challenging since their signatures are usually masked by charging effects. Two recent transport spectroscopy experiments on an individual conducting SWNT (Ref. 7) and a rope of SWNT's (Ref. 15) produced contradicting results. The data by Tans *et al.*⁷ assumes spin-polarized tunneling into a nanotube, which in turn suggests the interpretation in

terms of electron correlations. On the other hand, the data by Cobden *et al.*¹⁵ fits the constant interaction model remarkably well and shows no signatures of exotic correlation effects. Since the atomic structure of particular SWNT's studied in these experiments is not known, it might be appealing to interpret the discrepancy in the results in terms of geometry-dependent *many-particle* properties of conducting SWNT's.

Unfortunately, a consistent theory of interacting electrons in chiral SWNT's is lacking, although such a theory has been recently developed for armchair nanotubes.^{12–14} In this work we establish an effective low-energy model for conducting chiral SWNT's and evaluate its parameters (scattering amplitudes) from the microscopic theory. We found very weak dependence of the dominant scattering amplitudes on the chiral angle. This allows us to introduce a *universal* low-energy Hamiltonian of conducting SWNT's. According to the results of the renormalization group analysis¹³ the strongest Mott-like electron instability occurs at half-filling. We investigate this instability using the self-consistent harmonic approximation. Substantial energy gaps are found in all modes of elementary excitations. The conditions for experimental observation of the gaps are briefly discussed.

We start from the standard kinetic term $H_k = \sum_{s,\vec{k}} \xi(\vec{k}) a_{-s}^\dagger(\vec{k}) a_{+s}(\vec{k}) + \text{H.c.}$ of the tight-binding Hamiltonian for p_z electrons of a graphite sheet.¹⁶ Here

FIG. 1. The graphite lattice consists of two atomic sublattices $p = +, -$ denoted by filled and open circles. SWNT at the angle χ to the x axis can be formed by wrapping the graphite sheet along $\vec{w} = \vec{OO}'$ vector.

$a_{p,s}(\vec{k})$ are the Fermi operators for electrons with the spin $s = \pm$ at the sublattice $p = \pm$ (Fig. 1). The matrix elements are given by $\xi(\vec{k}) = -t(e^{-ik_y a/\sqrt{3}} + 2e^{ik_y a/2\sqrt{3}} \cos k_x a/2)$, t being the hopping amplitude between neighboring atoms. The eigenvalues of the Hamiltonian vanish at two Fermi points of the Brillouin zone, $\alpha\vec{K}$ with $\alpha = \pm$ and $\vec{K} = (K, 0)$, $K = 4\pi/3a$.

We consider conducting chiral (N_1, N_2) SWNT of the radius $R = (a/2\pi)\sqrt{N_1^2 + N_1N_2 + N_2^2}$ whose axis x' forms the angle $\chi = \arctan[(N_2 - N_1)/\sqrt{3}(N_1 + N_2)]$ with the direction of chains of carbon atoms (x axis in Fig. 1). Expanding H_k near the Fermi points to the lowest order in $\vec{q} = \vec{k} - \alpha\vec{K} = q(\cos\chi, \sin\chi)$ and introducing slowly varying Fermi fields $\psi_{pas}(x') = L^{-1/2} \sum_{q=2\pi n/L} e^{iqx'} a_{pas}(\vec{q} + \alpha\vec{K})$, we obtain

$$H_k = -iv \sum_{pas} a e^{-ip\alpha\chi} \int dx' \psi_{pas}^\dagger \partial_{x'} \psi_{-pas}, \quad (1)$$

with the Fermi velocity $v = \sqrt{3}ta/2 \approx 8.1 \times 10^5$ m/s. The kinetic term can be diagonalized by the unitary transformation

$$\psi_{pas} = \frac{1}{\sqrt{2}} e^{-ip\alpha\chi/2} \sum_{r=\pm} (r\alpha)^{(1-p)/2} \varphi_{ras} \quad (2)$$

to the basis φ_{ras} of left ($r = -$) and right ($r = +$) movers.

The Coulomb interaction has the form

$$H_{int} = \frac{1}{2} \sum_{pp', \{\alpha_i\}, ss'} V_{pp'}(2\bar{\alpha}K) \times \int dx' \psi_{p\alpha_1 s}^\dagger \psi_{p'\alpha_2 s'}^\dagger \psi_{p'\alpha_3 s'} \psi_{p\alpha_4 s}, \quad (3)$$

with the matrix elements

$$V_{pp'}(2\bar{\alpha}K) = \frac{1}{\rho} \sum_{\vec{r}_p} U(\vec{r}_p - \vec{r}_{p'}) \exp[-2i\bar{\alpha}\vec{K}(\vec{r}_p - \vec{r}_{p'})], \quad (4)$$

corresponding to the amplitudes of intra- ($p = p'$) and inter- ($p = -p'$) sublattice forward ($\bar{\alpha} = 0$) and backward ($\bar{\alpha} = \pm 1$) scattering¹⁷ (the sum is taken over the nodes of the sublattice p of SWNT). Here $U(\vec{r}) = e^2 / \{\kappa \sqrt{a_0^2 + (x')^2 + 4R^2 \sin^2(y'/2R)}\}$ is the Coulomb interaction with a short-distance cutoff $a_0 \sim a$, $\rho = 4\pi R / \sqrt{3}a^2$ is a linear density of sublattice nodes along SWNT, and $\bar{\alpha} = (\alpha_1 - \alpha_4)/2 = (\alpha_3 - \alpha_2)/2$. We will choose the parameter a_0 from the requirement that the on-site interaction in the original tight-binding model corresponds to the difference between the ionization potential and electron affinity of sp^2 hybridized carbon.¹⁸ This procedure gives $a_0 = 0.526a$.

The forward-scattering part H_F [terms with $\bar{\alpha} = 0$ in Eq. (3)] of the Hamiltonian H_{int} can be separated into the Luttinger model-like term H_ρ and the term H_f related to the difference $\Delta V(0) = V_{pp}(0) - V_{p-p}(0)$ between intra- and intersublattice amplitudes,

$$H_\rho = \frac{V_{pp}(0)}{2} \int dx' \rho^2(x'), \quad (5)$$

$$H_f = -\frac{\Delta V(0)}{2} \sum_{p\alpha s s'} \int dx' \psi_{pas}^\dagger \psi_{-p\alpha' s'}^\dagger \psi_{-p\alpha' s'} \psi_{pas}, \quad (6)$$

where $\rho = \sum_{pas} \psi_{pas}^\dagger \psi_{pas}$ is the total electron density. The backscattering Hamiltonian H_B [terms with $\bar{\alpha} = \pm 1$ in Eq.

TABLE I. Scattering amplitudes $\Delta V(0)$, $V_{pp}(2K)$, $V_{p-p}(2K)$ in units $ae^2/2\pi\kappa R$ for all chiral SWNT's with radii R in the range $2R/a = 4-7$.

a_0/a	$\Delta V(0)$	$V_{pp}(2K)$	$ V_{p-p}(2K) $
0.4	0.44265–0.44274	0.97060–0.97095	$0.6-2.2 \times 10^{-3}$
0.526	0.17378–0.17395	0.53549–0.53561	$0.5-1.6 \times 10^{-3}$
0.7	0.04880–0.04895	0.24778–0.24797	$0.3-1.5 \times 10^{-3}$

(3)] can be subdivided into the intrasublattice $H_b^{(+)}$ ($p = p'$) and intersublattice $H_b^{(-)}$ ($p = -p'$) parts.

The dominant contribution to the forward-scattering amplitudes $V_{pp'}(0)$ comes from the long range component of the Coulomb interaction, $V_{pp}(0) = (2e^2/\kappa) \ln(R_s/R)$, where $R_s \approx \min(L, D)$ characterizes the screening of the interaction due to a finite length L of the SWNT and/or the presence of metallic electrodes at a distance D .¹² The forward-scattering differential part $\Delta V(0)$ and the intrasublattice backscattering amplitude $V_{pp}(2K)$ can be estimated from Eq. (4) as follows, $\Delta V(0), V_{pp}(2K) \sim ae^2/\kappa R$ (for $a_0 \sim a$). Despite the amplitudes $\Delta V(0), V_{pp}(2K)$ are much smaller than $V_{pp}(0)$, they produce essentially non-Luttinger terms in the low-energy Hamiltonian which will be important in further analysis.

We evaluated the matrix elements (4) numerically for chiral SWNT's with radii R in the range $2R/a = 4-7$ [$2R/a = 5.5$ for (10,10) SWNT's]. We found that dimensionless amplitudes $2\pi\kappa R[\Delta V(0), V_{pp}(2K)]/ae^2$ show very weak dependence on the radius of SWNT and its chiral angle (see Table I). The results are sensitive to the value of the cutoff parameter a_0 .

The intersublattice backscattering amplitude $V_{p-p}(2K)$ is almost three orders of magnitude smaller than $\Delta V(0)$, $V_{pp}(2K)$. This is due to the C_3 symmetry of a graphite lattice, which leads to an exact cancellation of the terms (4) contributing to $V_{p-p}(2K)$ in the case of a plane graphite sheet. The matrix elements $V_{p-p}(2K)$ are generally complex due to asymmetry of effective one-dimensional (1D) intersublattice interaction potential (the matrix elements are real for symmetric zigzag and armchair SWNT's). Let us note that after the unitary transformation (2) of the Hamiltonian $H = H_k + H_{int}$, the chiral angle χ enters *only* to the intersublattice backscattering matrix elements.¹⁹ Due to the smallness of these matrix elements, the low-energy properties of chiral SWNT's are expected to be virtually independent of the chiral angle.

Neglecting the intersublattice backscattering we arrive to the universal low-energy model of conducting SWNT's given by the Hamiltonian $H = H_k + H_F + H_b^{(+)}$. The latter can be bosonized along the lines of Refs. 14 and 13. We introduce bosonic representation of the Fermi fields,

$$\varphi_{ras} = \frac{\eta_{ras}}{\sqrt{2\pi\tilde{a}}} \exp[irq_F x' + i(\theta_{as} + r\phi_{as})], \quad (7)$$

and decompose the phase variables θ_{as}, ϕ_{as} into symmetric $\delta = +$ and antisymmetric $\delta = -$ modes of the charge ρ and spin σ excitations, $\theta_{as} = (\theta_{\rho+} + s\theta_{\sigma+} + \alpha\theta_{\rho-} + \alpha s\theta_{\sigma-})/2$ and $\phi_{as} = (\phi_{\rho+} + s\phi_{\sigma+} + \alpha\phi_{\rho-} + \alpha s\phi_{\sigma-})/2$. The bosonic

fields satisfy the commutation relation, $[\theta_{j\delta}(x_1), \phi_{j'\delta'}(x_2)] = i(\pi/2)\text{sign}(x_1 - x_2)\delta_{jj'}\delta_{\delta\delta'}$. The Majorana fermions $\eta_{r\alpha s}$ are introduced¹⁴ to ensure correct anticommutation rules for different species r, α, s of electrons, and satisfy $[\eta_{r\alpha s}, \eta_{r'\alpha's'}]_+ = 2\delta_{rr'}\delta_{\alpha\alpha'}\delta_{ss'}$. The quantity $q_F = \pi n/4$ is

related to the deviation n of the average electron density from half-filling, and $\tilde{a} \sim a$ is the parameter of the standard exponential ultraviolet cutoff.

The universal low-energy Hamiltonian of conducting SWNT's has the following bosonized form,²⁰

$$H = \sum_{j=\rho,\sigma} \sum_{\delta=\pm} \frac{v_{j\delta}}{2\pi} \int dx' \{K_{j\delta}^{-1}(\partial_{x'}\theta_{j\delta})^2 + K_{j\delta}(\partial_{x'}\phi_{j\delta})^2\} + \frac{1}{2(\pi\tilde{a})^2} \int dx' \{[\Delta V(0) - V_{pp}(2K)] \\ \times [\cos(4q_F x' + 2\theta_{\rho+})\cos 2\theta_{\sigma+} - \cos 2\theta_{\rho-}\cos 2\theta_{\sigma-}] - \Delta V(0)\cos(4q_F x' + 2\theta_{\rho+})\cos 2\theta_{\rho-} \\ + \Delta V(0)\cos(4q_F x' + 2\theta_{\rho+})\cos 2\theta_{\sigma-} - \Delta V(0)\cos 2\theta_{\sigma+}\cos 2\theta_{\rho-} + \Delta V(0)\cos 2\theta_{\sigma+}\cos 2\theta_{\sigma-} \\ - V_{pp}(2K)\cos(4q_F x' + 2\theta_{\rho+})\cos 2\phi_{\sigma-} + V_{pp}(2K)\cos 2\theta_{\sigma+}\cos 2\phi_{\sigma-} \\ + V_{pp}(2K)\cos 2\theta_{\rho-}\cos 2\phi_{\sigma-} + V_{pp}(2K)\cos 2\theta_{\sigma-}\cos 2\phi_{\sigma-}\}, \quad (8)$$

$v_{j\delta} = v\sqrt{A_{j\delta}B_{j\delta}}$ and $K_{j\delta} = \sqrt{B_{j\delta}/A_{j\delta}}$ being the velocities of excitations and exponents for the modes j, δ . The parameters $A_{j\delta}, B_{j\delta}$ are given by

$$A_{\rho+} = 1 + \frac{4\bar{V}(0)}{\pi v} - \frac{\Delta V(0)}{4\pi v} - \frac{V_{pp}(2K)}{2\pi v}, \quad (9)$$

$$A_{\nu\delta} = 1 - \frac{\Delta V(0)}{4\pi v} - \delta \frac{V_{pp}(2K)}{2\pi v}, \quad (10)$$

$$B_{\nu\delta} = 1 + \frac{\Delta V(0)}{4\pi v}, \quad (11)$$

with $\bar{V}(0) = [V_{pp}(0) + V_{p-p}(0)]/2$.

Since $\bar{V}(0)/v \sim \ln(R_s/R) \gg 1$ and $\Delta V(0)/v, V_{pp}(2K)/v \sim a/R \ll 1$, the renormalization of the parameters $K_{j\delta}, v_{j\delta}$ by the Coulomb interaction is the strongest in $\rho+$ mode. Assuming $\kappa = 1.4$ (Ref. 14) and $R_s = 100$ nm we obtain $K_{\rho+} \approx 0.2, v_{\rho+} \approx v/K_{\rho+}$ for generic SWNT's with $R \sim 0.7$ nm.¹² The interaction in the other modes is weak: $v_{j\delta} = v, K_{j\delta} = 1$, up to a factor $1 + O(a/R)$.

The renormalization group analysis of armchair SWNT's with long-range Coulomb interaction has been performed in Refs. 12–14. The modification of the parameters of the Hamiltonian (8) by the neglected small term $V_{p-p}(2K)$ should not change the results qualitatively.²¹ The most relevant perturbation is the umklapp scattering at half-filling. In this case the nonlinear terms of the Hamiltonian (8), which do not contain $\cos 2\theta_{\sigma-}$ scale to strong coupling and the phases $\theta_{\rho+}, \theta_{\sigma+}, \theta_{\rho-}, \phi_{\sigma-}$ get locked at $(\theta_{\rho+}^{(m)}, \theta_{\sigma+}^{(m)}, \theta_{\rho-}^{(m)}, \phi_{\sigma-}^{(m)}) = (0, 0, 0, 0)$ or $(\pi/2, \pi/2, \pi/2, \pi/2)$. Therefore, the ground state of half-filled SWNT is the Mott insulator with all kinds of the excitations gapped.

To estimate the gaps quantitatively, we will employ the self-consistent harmonic approximation which follows from Feynman's variational principle.²² We consider trial harmonic Hamiltonian of the form:

$$H_0 = \sum_{j\delta} \frac{v_{j\delta}}{2\pi} \int dx' \{K_{j\delta}^{-1}[(\partial_{x'}\theta_{j\delta})^2 + (1 - \delta_{j\sigma}\delta_{\delta-})q_{j\delta}^2\theta_{j\delta}^2] \\ + K_{j\delta}[(\partial_{x'}\phi_{j\delta})^2 + \delta_{j\sigma}\delta_{\delta-}q_{j\delta}^2\phi_{j\delta}^2]\}, \quad (12)$$

$q_{j\delta}$ being variational parameters. By minimizing the upper estimate for the free energy $F^* = F_0 + \langle H - H_0 \rangle_0$,²² one obtains the following self-consistent equations:

$$q_{\rho+}^2 = \frac{2K_{\rho+}}{\pi\tilde{a}^2 v_{\rho+}} c_{\rho+} \{ [V_{pp}(2K) - \Delta V(0)]c_{\sigma+} + \Delta V(0)c_{\rho-} \\ + V_{pp}(2K)d_{\sigma-} \}, \quad (13)$$

$$q_{\rho-}^2 = \frac{2K_{\rho-}}{\pi\tilde{a}^2 v_{\rho-}} c_{\rho-} \{ \Delta V(0)c_{\rho+} + \Delta V(0)c_{\sigma+} \\ - V_{pp}(2K)d_{\sigma-} \}, \quad (14)$$

$$q_{\sigma+}^2 = \frac{2K_{\sigma+}}{\pi\tilde{a}^2 v_{\sigma+}} c_{\sigma+} \{ [V_{pp}(2K) - \Delta V(0)]c_{\rho+} + \Delta V(0)c_{\rho-} \\ - V_{pp}(2K)d_{\sigma-} \}, \quad (15)$$

$$q_{\sigma-}^2 = \frac{2}{\pi\tilde{a}^2 K_{\sigma-} v_{\sigma-}} d_{\sigma-} V_{pp}(2K) \{ c_{\rho+} - c_{\sigma+} - c_{\rho-} \}, \quad (16)$$

where $c_{j\delta} = \langle \cos 2\theta_{j\delta} \rangle_0 = \cos 2\theta_{j\delta}^{(m)} (\gamma\tilde{a}q_{j\delta})^{K_{j\delta}}, d_{\sigma-} = \langle \cos 2\phi_{\sigma-} \rangle_0 = \cos 2\phi_{\sigma-}^{(m)} (\gamma\tilde{a}q_{\sigma-})^{1/K_{\sigma-}}, \langle \dots \rangle_0$ denotes averaging with respect to the trial Hamiltonian (12), and $\gamma \approx 0.890$. Note that $\langle \cos 2\theta_{\sigma-} \rangle_0 = 0$, so that only the terms of the Hamiltonian (8) that scale to the strong coupling contribute to Eqs. (13)–(16).

In the limiting case of interest, $|\Delta V(0)|, |V_{pp}(2K)| \ll v$ and $K_{\rho+} \ll 1$, the solution of Eqs. (13)–(16) can be found in a closed form, giving rise to the following estimates for the gaps $\Delta_{j\delta} = v_{j\delta}q_{j\delta}$ in the energy spectra:

$$\Delta_{\rho+} = \frac{v_{\rho+}}{\gamma\tilde{a}} \left(\frac{2\gamma^2 V_{\rho+}}{\pi v_{\rho+}} \right)^{1/(1-K_{\rho+})}, \quad (17)$$

$$\Delta_{\rho-} = \frac{|\Delta V(0)|}{V_{\rho+}} \Delta_{\rho+}, \quad (18)$$

$$\Delta_{\sigma+} = \frac{|V_{pp}(2K_0) - \Delta V(0)|}{V_{\rho+}} \Delta_{\rho+}, \quad (19)$$

FIG. 2. The energy gaps $\Delta_{j\delta}$ for the modes $\rho+$, $\sigma-$, $\sigma+$, $\rho-$ at $a_0=0.526a$ (lines marked by crosses, from top to bottom) and for the mode $\rho+$ at $a_0=0.4a$ (triangles) and at $a_0=0.7a$ (squares). The energy is in units $\hbar v/\tilde{a} \approx 2.16$ eV for $\tilde{a}=a$.

$$\Delta_{\sigma-} = \frac{|V_{pp}(2K_0)|}{V_{\rho+}} \Delta_{\rho+}, \quad (20)$$

with $V_{\rho+} = \{[\Delta V(0) - V_{pp}(2K)]^2 + [\Delta V(0)]^2 + [V_{pp}(2K)]^2\}^{1/2}$. In the above expressions we used the approximation, $v_0/v_{\rho+} = K_{\rho+}$ and $v_0/v_{j\delta} = K_{j\delta} = 1$ for $\sigma\pm$ and $\rho-$ modes. The formulas (17)–(20) indicate that the largest gap occurs in $\rho+$ mode, albeit all four gaps are of the same order for realistic values of the matrix elements (see Table I). The gaps decrease as $\Delta_{j\delta} \propto (1/R)^{1/(1-K_{\rho+})} \approx (1/R)^{5/4}$ with the tube radius. This should be contrasted to the $1/R$ dependence of wide semiconductor gaps and $1/R^2$ dependence of narrow deformation induced gaps²³ expected from the single-particle picture.

In Fig. 2 we present numerical results for the gaps $\Delta_{j\delta}$ for the cutoff parameter $a_0=0.526a$. The data for somewhat larger and somewhat smaller values of a_0 indicate possible variation of the gap $\Delta_{\rho+}$ due to uncertainty in the short-distance cutoff of the Coulomb interaction. The gaps can be loosely estimated at $\Delta_{j\delta} \sim 0.01$ – 0.1 eV for typical SWNT's with $R \approx 0.7$ nm. Due to the gaps in the spectrum of bosonic elementary excitations, the electronic density of states should disappear in the subgap region and display features at the gap frequencies and their harmonics. Both signatures should be observable by means of the tunneling spectroscopy.

Why have the gaps not been observed in the experiments?^{4,7,15} This might be due to the effect of metallic electrodes. The difference in the work functions of the electrodes (Au, Pt) and the nanotube results in a downward shift of the Fermi level of the nanotube by a few tenths of an eV.⁴ This causes substantial deviation $\Delta n = 4q_F/\pi \sim 1$ nm⁻¹ of the electron density in SWNT from half-filling, at least in the vicinity of the electrodes. Therefore, we expect the gap features to be observable in the layouts with well separated source and drain contacts. The piece of nanotube between them should be well isolated from any conductor.

In conclusion, we have developed an effective low-energy theory of conducting chiral SWNT's with long-range Coulomb interaction. The many-particle properties of SWNT's are found to be virtually independent of the chiral angle. The universal Hamiltonian (8) of conducting SWNT's is introduced. The Mott-like energy gaps in the range of 0.01–0.1 eV should be observable at half-filling.

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¹⁹The transformed matrix elements $V_{p-p}(2\bar{\alpha}K)e^{2i\bar{\alpha}p\chi}$ are invariant under $\pi n/3$ rotations in chiral angle $\chi_n = \chi_0 + \pi n/3$, which correspond to equivalent representations of a nanotube.

²⁰Equation (8) has the same form as the phase Hamiltonian for a two-leg Hubbard-type ladder [H. Lin *et al.*, Phys. Rev. B **58**, 1794 (1998)], provided that the difference in definitions of the fields θ_{j-} and ϕ_{j-} ($j=\rho, \sigma$) in terms of densities of right and left movers in two energy bands is taken into account.

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