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Vision-Based Nonlinear Incremental Control for a Morphing Wing With Mechanical Imperfections

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Morphing structures have acquired much attention in the aerospace community because they enable an aircraft to actively adapt its shape during flight, leading to fewer emissions and fuel consumption. Researchers have designed, manufactured, and tested a morphing wing named SmartX-Alpha, which can actively alleviate loads while achieving the optimal lift distribution. However, the widely existing mechanical imperfections can degrade the performance of the morphing wing and even lead to instabilities. To tackle these issues, this article proposes a vision-based adaptive control approach to actively compensate for mechanical imperfections. In this approach, an incremental model is constructed online to identify the system dynamics using servo commands and vision measurements, and then, nonlinear dynamic inversion control is applied based on the identified model. This data-driven control approach with visual feedback has been validated by real-world experiments on the SmartX-Alpha. The results demonstrate that the vision-based system combined with the proposed control methodology can actively compensate for mechanical imperfections with minimal adjustments to the actual system design. Compared to a controller that only uses a feedforward input-output mapping, this proposed approach improves the system performance and decreases the tracking errors by more than 62% despite disturbances. The results collectively demonstrate the effectiveness of the proposed control system, which sets a foundation for realizing morphing in next-generation aircraft.

I. INTRODUCTION

Active morphing can bring several benefits to conventional wing designs. Morphing wings have the potential to improve aircraft performance across the full flight envelope, by actively adapting the shape. Due to conflicting requirements [1], conventional wing designs generally can only be optimized for one single flight condition, such as cruise. To assess the benefits of morphing wings, the SmartX project [2] was initiated at the Delft University of Technology. An overactuated and oversensed wing prototype was developed for this project, named SmartX-Alpha, capable of seamless active wing morphing with six distributed translation-induced camber (TRIC) morphing modules [3]. Coupled with advanced nonlinear control methods, this wing has demonstrated the capability to actively reduce gust loads while actively maintaining an optimal lift distribution in a recent wind tunnel study [4].

However, due to the mechanical complexity and manufacturing imperfections, mechanical imperfections generally exist in aerospace systems, such as input saturation [5], friction [6], dead zone [7], and disturbances. These nonlinearities can largely degrade the system performance and lead to undesirable phenomena such as limit-cycle oscillations, flutter, and even divergence [7], [8]. Apart from these, backlash hysteresis is also observed in both wind tunnel tests and a design validation assessment with a digital image correlation (DIC) setup [4], which is caused by the nature of the morphing mechanism. This backlash effect diminishes the achievable morphing range and consequently reduces the aerodynamic control effectiveness of the wing. Instead of perfecting hardware, which is costly and nonadaptive, an alternative is to actively compensate for these hardware imperfections via software algorithms. However, as depicted in Fig. 1, the backlash output $u$ is a function of not only the input $u_c$, but also its derivative $u_c'$, which is fundamentally different from the other common nonlinearities that act directly on the actuation output. Consequently, the time-dependent hysteresis effect makes backlash compensation a challenging problem.

Conventional linear control methods, paired with the gain-scheduling technique, are not suitable for this task because the closed-loop stability and performance cannot be guaranteed in between the operational points [9]. For example, classic proportional-derivative control has been observed to result in limit-cycle oscillations in the presence of backlash [10]. There are also some adaptive control approaches designed for backlash such as [11] that employs an observer with adjustable parameters. However, they often rely on fixed structures and are limited for complex and variant nonlinearities [11]. Alternatively, some articles

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The main contributions of this article are summarized as follows:

1) The methodology and real-world implementation techniques for the proposed vision-based IM-NDI to actively compensate for mechanical imperfections (particularly for backlash hysteresis) are validated in morphing wing experiments.
sufficiently small sampling interval $\Delta t$, errors caused by linearization and discretization can be bounded within a small vicinity of zero:

**Assumption 1 ([24])** The sampling frequency is sufficiently high, and the system dynamics are relatively slow time-varying.

With a sampling frequency of 100 Hz, Assumption 1 holds in aerospace applications [9], [35]. Experimental results have shown that 60 Hz is sufficient for this morphing wing control problem.

Before discretization, we first assume that the system is first-order continuous with respect to time, and therefore, we can approximately linearize the system dynamics (1) at around a time instant $t_0$, by taking the first-order Taylor series expansion as follows:

$$\begin{align*}
\dot{x}(t) &= \dot{x}(t_0) + F[x(t_0), u(t_0)]\Delta x + G[x(t_0), u(t_0)]\Delta u + O(\Delta x^2, \Delta u^2) \\
y(t) &= y(t_0) + H[x(t_0)]\Delta x + O(\Delta x^2) \quad (2)
\end{align*}$$

where $F[x(t_0), u(t_0)] = \frac{\partial f(x(t_0), u(t_0))}{\partial x} | x(t_0), u(t_0) \in \mathbb{R}^{n \times n}$, $G[x(t_0), u(t_0)] = \frac{\partial f(x(t_0), u(t_0))}{\partial u} | x(t_0), u(t_0) \in \mathbb{R}^{n \times m}$, and $H[x(t_0)] = \frac{\partial y(t_0)}{\partial x} | x(t_0) \in \mathbb{R}^{p \times n}$ are bounded due to the Lipschitz continuity of $f$ and $h$ in (1), respectively. $\Delta x = x(t) - x(t_0)$, $\Delta u = u(t) - u(t_0)$. $O(\Delta x^2)$ and $O(\Delta u^2)$ denote higher-order terms.

Since the controller is designed based on the identified dynamics, the higher order terms can perturb the closed-loop performance. Nevertheless, as claimed in [9], these higher order terms satisfy

$$\begin{align*}
\lim_{\Delta t \to 0} \| O(\Delta x^2, \Delta u^2) \|_2 &= 0 \quad \forall x \in \mathbb{R}^n \quad \forall u \in \mathbb{R}^m \\
\lim_{\Delta t \to 0} \| O(\Delta x^2) \|_2 &= 0 \quad \forall x \in \mathbb{R}^n \quad (3)
\end{align*}$$

where $\Delta t = t - t_0$ is the sampling interval. As demonstrated in (3), the norm values of the higher order terms approach zero under Assumption 1. Besides, (3) also implies that $\forall \tilde{O} > 0$, $\exists \Delta t > 0$ such that for all $0 < \Delta t \leq \Delta t$, $\forall x \in \mathbb{R}^n \quad \forall u \in \mathbb{R}^m \quad \forall t \geq t_0$, $\| O(\Delta x^2, \Delta u^2) \|_2 \leq \tilde{O}$ and $\| O(\Delta x^2) \|_2 \leq \tilde{O}$, i.e., there exists a $\Delta t$ that guarantees the boundedness of the higher-order terms. Furthermore, the IM adopts a local linearization technique such that the linearization errors will not accumulate. Consequently, the two higher order terms in (2) are omitted hereafter in the control design process for convenience.

Then, an IM can be utilized to approximately represent (2) using the Euler method accordingly:

$$\begin{align*}
\Delta x_{t+1} &\approx (I_n + F_{t-1}\Delta t)\Delta x_t + G_{t-1}\Delta t\Delta u_t \\
\Delta y_{t+1} &\approx H_t\Delta x_{t+1} \quad (4)
\end{align*}$$

where the subscript $t$ stands for the current sampling time instant and $I_n$ denotes an $n$-dimensional identity matrix. $F_{t-1} = \frac{\partial f(x(t), u(t))}{\partial x} | x_{t-1}, u_{t-1} \in \mathbb{R}^{n \times n}$, $G_{t-1} = \frac{\partial f(x(t), u(t))}{\partial u} | x_{t-1}, u_{t-1} \in \mathbb{R}^{n \times m}$, and $H_t = \frac{\partial y(t)}{\partial x} | x_{t} \in \mathbb{R}^{p \times n}$, respectively, denote the system transition matrix, the input distribution...
matrix, and the observation matrix of the discretized system. For simplicity, we denote $A_{i-1} \triangleq I_n + F_{i-1} \Delta t$ and $B_{i-1} \triangleq G_{i-1} \Delta t$ hereafter.

Inspired by the work in [24], [25], and [36], the incremental dynamics at the current time instant $t$ can be represented using previous data sequences on a time horizon $[t - N, t - 1]$ as

$$\Delta x_t \approx \tilde{A}_{t-1, t-1-N} \Delta x_{t-N} + U_N \Delta u_{t-1,N}$$

$$\Delta y_{t,N} \approx V_N \Delta x_{t-N} + T_N \Delta u_{t-1,N}$$

(5)

where $\Delta u_{t-1,N} = [\Delta u_{t-1}^T, \Delta u_{t-2}^T, \ldots, \Delta u_{t-N}^T]^T \in \mathbb{R}^{N \times m}$, $\Delta y_{t,N} = [\Delta y_{t-1}^T, \Delta y_{t-2}^T, \ldots, \Delta y_{t-N+1}^T]^T \in \mathbb{R}^{N \times p}$, $A_{i} = \prod_{\alpha=1}^{i} A_{\alpha}$, The controllability matrix is $U_N = [B_{t-2}, A_{t-2}B_{t-3}, \ldots, A_{i-2,N-1}B_{t-N-1}] \in \mathbb{R}^{N \times mN}$ while $V_N = [(H_{t-1}A_{t-2}, t - N - 1)^T, (H_{t-2}A_{t-3,N-1})^T, \ldots, (H_{t-N}A_{t-1,N})^T]^T \in \mathbb{R}^{PN \times N}$ is the observability matrix.

$$T_N = \begin{bmatrix} 
H_{t-1}B_{t-2} & H_{t-1}A_{t-2}B_{t-3} & \cdots & H_{t-1}A_{t-1,N-1}B_{t-1-N} \\
0 & H_{t-2}B_{t-3} & \cdots & H_{t-2}A_{t-2,N-1}B_{t-1-N} \\
0 & 0 & \cdots & H_{t-1}A_{t-1,N-1} 
\end{bmatrix} \in \mathbb{R}^{N \times mN}.$$ 

For OPFB scenarios, only the output $y_t$ instead of the full state $x_t$ can be measured. To determine system transitions with input-output observations, the following assumptions are required.

**ASSUMPTION 2** ([35]) The linearization and discretization do not change the property of controllability and observability of the original system described by (1), i.e., $(A_{i-1}, B_{i-1})$ is controllable and $(A_{i-1}, H_i)$ is observable.

**ASSUMPTION 3** ([35]) The deduced system (4) can be regarded deterministic within the range of $M$ time steps, where $M \geq n/p$.

**ASSUMPTION 4** During the identification and control process, the persistent excitation (PE) condition [37] is always satisfied.

Assumptions 2 and 3 are proposed based on Assumption 1. Both of them are necessary for the fidelity of the identified local model. According to Assumptions 2–4, the system is observable, locally deterministic, and persistently excited. Therefore, there must exist an observability index $K$, such that the column rank of the observability matrix $V_N$ satisfies $\text{rank}(V_N) < n$, $\forall N < K$, and $\text{rank}(V_N) = n$, $\forall N \geq K$. Note that $K$ satisfies $n/p \leq K \leq M$.

Let $N \leq K \leq M$, and there exists a matrix $\tilde{N} \in \mathbb{R}^{N \times pN}$ such that

$$\tilde{A}_{i-2,i-1-N-1} = \tilde{N} V_N.$$ 

(6)

Since $V_N$ has a full column rank, thus we can obtain its left inverse $V_N^+$ by

$$V_N^+ = (V_N^T V_N)^{-1} V_N^T$$

(7)

so that

$$\tilde{N} = \tilde{A}_{t-2,i-1-N-1} V_N^+ + Z(U_N - V_N V_N^+) \equiv \tilde{N}_0 + \tilde{N}_1$$

(8)

holds for any matrix $Z$, with $\tilde{N}_0$ denoting the minimum norm operator and $P(R^N \setminus V_N) = I_N - V_N V_N^+$ being the projection onto a range perpendicular to $V_N$ [36].

Inspired by [25], the following lemma is proposed to demonstrate how to reconstruct the unmeasurable system states from the input-output data:

**LEMMA 1** Given Assumptions 2–4, the unmeasurable internal states $x_t$ can be reconstructed uniquely in terms of the previous input-output sequences by

$$\Delta x_t \approx \tilde{N}_0 \Delta y_{t,N} + (U_N - \tilde{N}_0 T_N) \Delta u_{t-1,N}$$

(9)

where $N$ satisfies $n/p \leq K \leq M$.

**PROOF** See Appendix A. 

Lemma 1 provides a deterministic relationship between the previous measured data and unmeasured states over a long-enough time horizon, which illustrates the rationality and validity of the IM. However, the matrices representing the system dynamics ($A_{i-1}, B_{i-1}, H_i$, etc.) have to be known.

Therefore, in the next step, a direct mapping from the previous input-output data to the future output data regardless of the inner state is constructed based on the IM. This model utilizing the stored data sequences is named as the extended IM, and is presented in the following theorem.

**THEOREM 1** Under Assumptions 2–4, then given the measured input-output data over a long-enough time horizon, $[t - N + 1, t]$, $N \geq n/p$, the output increment $\Delta y_{t+1}$ can uniquely be determined as follows:

$$\Delta y_{t+1} \approx \bar{F}_T \Delta y_{t,N} + \bar{G}_T \Delta u_{t,N}$$

(10)

where $\bar{F}_T \in \mathbb{R}^{p \times NP}$ and $\bar{G}_T \in \mathbb{R}^{p \times Nm}$, respectively, denotes the transition matrix and the input distribution matrix of this extended discrete system.

**PROOF** The following proof is adapted from [25]. According to (5), the following approximation holds:

$$\Delta y_{t-1,N} \approx \tilde{V}_N \Delta x_{t-N} + \tilde{T}_N \Delta u_{t-1,N}$$

(11)

where $\tilde{V}_N = [(H_{t-2}A_{t-3,N-1})^T, (H_{t-3}A_{t-4,N-1})^T, \ldots, H_{t-N}B_{t-N-1}]^T \in \mathbb{R}^{PN \times N}$ and

$$\tilde{T}_N = \begin{bmatrix} 
0 & H_{t-2}B_{t-3} & H_{t-2}A_{t-3,B_{t-4}} & \cdots & H_{t-2}A_{t-1,N-1}B_{t-1-N} \\
0 & 0 & H_{t-3}B_{t-4} & \cdots & H_{t-3}A_{t-2,N-1}B_{t-1-N} \\
0 & 0 & 0 & \cdots & H_{t-1}B_{t-N-1} 
\end{bmatrix} \in \mathbb{R}^{N \times mN}.$$ 

Since the system is fully observable, when $N \geq n/p$, $\tilde{V}_N$ also has a full column rank, and its left inverse is given by:

$$\tilde{V}_N^+ = (\tilde{V}_N^T \tilde{V}_N)^{-1} \tilde{V}_N^T$$

(12)

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By left-multiplying $\hat{V}_N^+$ to (11) and substituting the resulted $\Delta x_{-N}$ into (5) and then the resulted $\Delta x_i$ into (4), the dynamics that maps the previous measured data to the output can be obtained:

$$
\Delta y_i \approx H_i - 1 \hat{A}_{t-2:N-1} \hat{V}_{N}^+ \Delta Y_{t-1:N} + (H_i - 1) U_N - H_i - 1 \hat{A}_{t-2:N-1} \hat{V}_{N}^+ \hat{Y}_N) \Delta u_{t-1:N} = F_{t-1} \Delta Y_{t-1:N} + G_{t-1} \Delta u_{t-1:N}. \tag{13}
$$

By comparing (10) and (13), it can be found that they have the same representation but are for different time instants. This completes the proof.

In this way, the original nonlinear continuous system is approximately transformed into a new locally linear discrete system. The $\hat{F}_t$ and $\hat{G}_t$, in the extended incremental model (10) will be identified online using the RLS algorithm presented in the next section.

B. Online Identification With the RLS Algorithm

An RLS algorithm is introduced in this section. Rewrite (10) in a row-by-row form as follows:

$$
\Delta Y_{t+1}^T \approx \begin{bmatrix} \Delta Y_{t, N}^T & \Delta u_{t, N}^T \end{bmatrix} \begin{bmatrix} F_t^T \\ G_t^T \end{bmatrix}. \tag{14}
$$

Denote $\tau_t = [\Delta Y_{t, N}^T, \Delta u_{t, N}^T] \in \mathbb{R}^{N(p+m) \times 1}$ as the input information of the extended IM identification, and $\Theta_t = [F_t, G_t]^T \in \mathbb{R}^{N(p+m) \times p}$ as the matrix to be determined.

According to Lemma 1 and Theorem 1, data sequences from at least $n/p$ time instants are required. Hence, a sliding window technique [24], [35] is employed to store sufficient measured data for online identification, with the data window width $N$ satisfying $N \geq n/p$.

The main procedure of the RLS algorithm is presented as follows [35], [38]:

$$
\begin{align*}
\Delta Y_{t+1}^T &= \tau_t^T \hat{\Theta}_t \\
\epsilon_t &= \Delta y_{t+1} - \Delta Y_{t+1} \\
\hat{\Theta}_{t+1} &= \hat{\Theta}_t + \frac{\epsilon_t}{\gamma_{RLS} + \tau_t^T \text{Cov}_{\tau_t} \tau_t} \\
\text{Cov}_{\tau_{t+1}} &= \frac{1}{\gamma_{RLS}} \left( \text{Cov}_{\tau_t} - \frac{\tau_t \tau_t^T \text{Cov}_{\tau_t}}{\gamma_{RLS} + \tau_t^T \text{Cov}_{\tau_t} \tau_t} \right)
\end{align*} \tag{15-18}
$$

where $\hat{Y}_{t+1}$ and $\hat{\Theta}_t$ denote the estimated and approximated values of $y_{t+1}$ and $\Theta_t$, respectively; $\epsilon_t \in \mathbb{R}^p$ is the prediction error; $\text{Cov}_{\tau_t} \in \mathbb{R}^{(p+m) \times (p+m)}$ denotes the symmetric and positive definite estimation covariance matrix; $\gamma_{RLS} \in (0, 1]$ is the forgetting factor.

Assumptions 1 and 3 imply that in a certain time horizon $\mathcal{H} = [t_0, t]$, where $N \leq t - t_0 \leq M < \infty$. The slowly varying extended system dynamics can be approximated by a linear model with constant pending parameters. Hence, based on the following assumption, the locally approximate convergence of the RLS algorithm is analyzed.

**Assumption 5** (24]) For the locally linear system (10), in the local domain $\mathcal{H}$, the measured data $\tau_{t_0}, \ldots, \tau_t$ constitute the samples of an ergodic process, such that the time average is valid. The unmodeled dynamics noises within one sliding window are formulated as a zero-mean white noise vector as

$$
\Delta y_{t+1}^T = \zeta_t^T \hat{\Theta}_t + e_{o,t} \tag{19}
$$

where $\zeta_t$ is the locally optimal matrix, and $e_{o,t}$ is the equivalent plant noise independent of the samples $\tau_t$.

**Theorem 2** If Assumptions 1–5 hold, and the RLS algorithm is conducted obeying (15)–(18), then the approximate augmented matrix $\hat{\Theta}_t$ shows the trend of converging to the locally optimal matrix $\hat{\Theta}_t$.

**Proof** See Appendix B. \hfill $\square$

C. NDI Control

It is noteworthy that the identification is conducted online such that the IM can adapt to the variations and therefore reflect the system dynamics in real time. The following NDI controller is designed based on the adaptive IM and consequently has the capability to adapt online.

Define $e = y - y_{ref}$ as the tracking error between the system output $y$ and the reference signal $y_{ref}$. It is clear that given a Lyapunov function $J = e^2$, the tracking error dynamics is stable, when the following equation holds:

$$
\dot{e} = y - y_{ref} = -k_p e - k_d \dot{e} \tag{20}
$$

where $k_p > 0$ and $k_d > 0$ are control parameters.

Discretizing (20) in the same way of (4) yields

$$
\frac{\Delta e_{t+1}}{\Delta t} = \frac{\Delta y_{t+1} - \Delta y_{t+1}^{ref}}{\Delta t} = -k_p e_t - k_d \dot{e}_t - e_{t-1}. \tag{21}
$$

The derivative of the reference signal is assumed to be slow-varying, i.e., $\Delta y_{t+1}^{ref} / \Delta t \approx 0$. Substituting the incremental model (10) yields

$$
\hat{F}_t \Delta Y_{t, N} + \hat{G}_t \Delta u_{t, N} - \Delta y_{t+1}^{ref} \approx -k_p \Delta e_t - k_d \Delta e_t. \tag{22}
$$

With the identified system matrices $\hat{F}_t$ and $\hat{G}_t$, the control law is derived from (22) as

$$
\begin{align*}
u_t &\approx \Delta u_{t-1} + \hat{G}_{1, t}^{-1} \left( \hat{F}_t \Delta Y_{t, N} - \hat{G}_{1, t} \Delta u_{t, N} - k_p \Delta e_t - k_d \Delta e_t \right)
\end{align*} \tag{23}
$$

where $\hat{G}_{1, t} \in \mathbb{R}^{p \times m}$ and $\hat{G}_{1, t} \in \mathbb{R}^{p \times (N-1) \times m}$ are partitioned matrices from $\hat{G}_t$.

**Remark 1** Satisfying the PE condition is essential for both theoretical deduction and experimental implementation. A common approach to ensure the satisfaction of the PE condition is adding exploration noise to the control command [24], [25], such that even at a steady status, there is small vibration that does not affect the performance in general but can excite the system. In practice, it could be easier to satisfy the PE condition because there always exist noises and disturbances in the real world, which actually play the same role as the exploration noise.
Remark 2 Although Assumption 4 and Remark 1 are given, in some practical situations, some elements of $G_{11,1}$ can have too small values. Therefore, for the real-world implementation, lower bounds are set for these elements to guarantee the invertibility of $G_{11,1}$ and to avoid aggressive control increments.

Remark 3 Input constraints are imposed on the $u_i$ calculated by (23). It is also feasible to explicitly consider input constraints while solving (22) following our previous research in [4].

It is noteworthy that the proposed IM-NDI is fundamentally different from the well-known incremental control (including incremental NDI, incremental backstepping, incremental sliding model control) in the literature [9], [16], [39]. First of all, the state-of-the-art incremental control methods only depend on the information (state derivatives and control input) of the previous single time step, whereas IM-NDI can make use of the information of previous $N$ time steps. Consequently, IM-NDI is more applicable for solving hysteresis effects and is more robust. Second, the state-of-the-art incremental control methods normally neglect the state variation related term [9], whereas this neglection is abandoned in IM-NDI, further enhancing its robustness. Third, prior knowledge of the control effectiveness is normally required in the state-of-the-art incremental control methods, while the proposed IM-NDI method does not need any prior knowledge of system dynamics. This simplifies the experimental implementation and empowers IM-NDI with swift online adaptation ability.

III. VISION-BASED CONTROL

A crucial aspect of implementing a control strategy to compensate for mechanical imperfections is an accurate knowledge of the morphing wings’ shape. In particular, the variable of interest to the controller is the local vertical displacement of the wing trailing-edge with respect to a body-fixed coordinate system. In a previous study, a morphing wing concept, utilizing the distributed TRIC has been described [3]. This design has a relatively stiff wing box and a flexible morphing trailing edge. A body-fixed coordinate system $\mathcal{F}_B$ is chosen to be near the root of the wing in the wing box section, with an origin $O_B$. The displacement of the trailing edge, denoted as $z = [z_1, z_2, \ldots, z_{12}]^T$ along 12 stations of the span is reconstructed in the $\mathcal{F}_B$ frame, from a camera-fixed frame $\mathcal{F}_C$ in real time, by means of vision-based tracking. Two locations in each of the six modules are tracked and fed back to the controller. The experimental setup is shown in Fig. 3. A concise overview of the vision-based tracking pipeline is shown in Fig. 4 and explained in the following sections.

A. Apparatus

The experimental apparatus is shown in Fig. 3. The system consists of a morphing wing with six distributed TRIC morphing modules placed in the Open Jet Facility (OJF) wind tunnel facility of the Delft University of Technology. Each module is actuated by two embedded servos [3]. An array of IR light-emitting diodes (LEDs) are installed on the wing bottom surface, in the nonmorphing wing-box and the morphing trailing-edge modules. Four IR markers per module (24 in total) with another three markers defining the body-fixed reference frame are tracked by five Prime41 4.1 megapixel IR cameras at a frame rate of 250 frames per second (FPS) [41]. The deflections of the morphing flaps are reconstructed in real time with a reconstruction algorithm.

The intensity of IR has been adjusted to approximately 20 % and tuned to the obtain best tracking performance. Image segmentation and filtering are applied to further improve the tracking, which will be discussed in Section III-B.

B. Processing Framework

A 3-D reconstruction procedure is required to transform the measured marker correspondence $x_1, x_2, \ldots, x_n$ detected in the image frame, $u, v$, to a 3-D world coordinates defined in the camera fixed reference frame, $\mathcal{F}_C$. Segmentation and filtering are applied to the raw images in order to obtain the binary mask with marker locations in the image frames for each individual camera. The filtering consists of image threshold filtering and morphological image transformations [42] to improve the segmentation of distinct LED markers. An example of similar segmentation and filtering approach is presented in [28]. Active adjustment of the IR brightness was needed to prevent two or more markers from merging into a single blob for far away camera views.

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In a previous study in OJF, a 3-D reconstruction approach with a stereo-camera setup was developed, which showed sensitivity to camera calibration due to the adverse environmental condition in the wind tunnel (flow conditions and mechanical vibrations) [28]. A generally suitable approach to improve the tracking accuracy and add redundancy to the tracking system is a multicamera (>2) setup [43]. Therefore, to improve robustness against calibration drift developed over time, a five-camera setup was used in this study.

The n-view 3-D reconstruction problem is concerned with finding the optimal estimation of an object $\hat{X}$ in a 3-D global coordinate frame (i.e., locations in the $x$-, $y$-, and $z$-axes), which is observable in noisy $\tilde{x}_1, \tilde{x}_2, \ldots, \tilde{x}_n$ points correspondence in $n$ camera views. The point correspondences $\tilde{x}_i$ are generally defined by markers in $u, v$ coordinates of a 2-D image plane. Back-projecting the 3-D point onto the respective camera views, a minimization problem can be defined to find the reprojection error, $E = \sum_{k=1}^n ||x_k - \tilde{x}_k||^2$, and solved by an expanded linear system of equations similar to singular value decomposition in a direct linear transform (DLT) procedure [44]. Global optimization methods can be applied, such as algebraic, matrix inequality, and the $L_\infty$ approach [45]. The development of a particular $n$-view triangulation method is not considered in this study. To perform the 3-D point cloud reconstruction in real time, a proprietary reconstruction engine is used by OptiTrack API [46]. All the applications for processing, reconstructing, and accessing the data are written in low-level C++ programming language for best performance. Multicamera calibration is performed by wandering process, resulting in an average calibration error of 0.25 mm for all cameras. The accuracy of a similar setup has been verified in [47]. It is noteworthy that the OptiTrack setup is not ready for onboard in-flight operation yet. Instead, our previous research has developed a fuselage/wing-mounted non-IR based camera tracking setup, whose effectiveness has been verified by wind tunnel experiments and real-world flight tests [28]. Nevertheless, the wing shape algorithms (including filtering, 3-D reconstruction, and coordination transformations) for these two setups are analogous.

The final step in the vision-based tracking pipeline is a coordinate system transformation from the global camera-fixed coordinate system, $F_C$ with an origin $O_C$, to the body-fixed coordinate system, $F_B$ with an origin $O_B$. This transformation is needed to express the relative deflections of the trailing-edge modules $z_i$ with respect to the baseline unmorphed shape. The coordinate frames and their respective origins, located at approximately 2 m away, are connected by a vector $r_{BC}$, as shown in Fig. 3. The transformation $F_C \rightarrow F_B$ is achieved by a translation, followed by three-axis rotations in pitch, roll, and yaw axes ($\theta, \phi, \psi$). The transformations are performed continuously as the morphing may continuously exhibits motions relative to the frame $F_B$. The average total processing latency was found to be in the range of 5–7 ms, which is smaller than the sampling interval (16.67 ms).

IV. EXPERIMENTAL RESULTS AND DISCUSSIONS

Finally, we verify the effectiveness of the proposed control approach through real-world experiments on the morphing wing system described in the preceding sections. According to Section III, the system consists of six modules and each of them is driven by two embedded actuators [3]. Without loss of generality, Module 2 is chosen for validation and its adjacent modules are used to produce disturbances. The two control channels of Module 2 are indexed by subscripts 3 and 4, respectively. It is noted that these two channels are identified together, leading to a 2-input-2-output system. The control command and vision feedback data are transmitted at 60 Hz between the host computer (Dell Optiplex 7400 i5-8500 3.0 GHz Processor) and the physical system, while the identifier and the controller work in a host computer at 500 Hz.

First of all, the online identification performance of the incremental model with the RLS algorithm is evaluated. The width of the sliding window is set as $N = 50$, which means 50 previous datasets stored in the host computer is utilized, rather than 50 real samples. The forgetting factor $\gamma_{RLS}$ is set to be 0.99995 such that the more recent data set has more dominant weight, $E_r$, $C_r$, and $C_{xy}$ are initialized as $F_0 = [I_2, 0_{2\times98}], G_0 = [I_2, 0_{2\times98}]$, and $C_{xy} = 10^3 \cdot I_{200}$, respectively, where $0_{2\times98}$ denotes the 2-row-98-column matrix with all zero elements.

The identification effectiveness of the incremental model is validated in an open-loop manner using the sinusoidal control input signal, with an amplitude of $A_3 = 20$ deg, and an angular frequency $\omega_3$ sweeps from 0.2$\pi$ to 4$\pi$ rad/s. The identification is activated 1.5 s after the open-loop control process begins. As illustrated in Fig. 5, the predicted displacements converge quickly to their values measured by the vision system as the identification is activated. The identification errors reach the minimum values at around $r = 3$ s, and after that keep increasing as the angular frequency increases. Overall, despite some disturbances and outliers, the identification errors, which are mainly caused by delays, can be bounded within ±2 deg. The experiment results verify the effectiveness of the incremental model, which makes it suitable for closed-loop control purposes.

Owing to the morphing wing shape sensory limitations reviewed in Section I, feedforward (FF) control currently is and will continue being the mainstream for morphing wings in the near future [48]. Moreover, mechanical imperfections (especially backlash hysteresis) lead to the ineffectiveness of the existing control methods. Therefore, the closed-loop control performance of the IM-NDI control method is evaluated and is compared to the FF control method in the experiment. DIC static measurements are conducted on the top and bottom surface of the morphing modules to assess the capability of the wing demonstrator to attain the static target morphing shapes [49]. A $2 \times 2$ FF mapping matrix between the servo angular inputs and the corresponding trailing-edge displacements can accordingly
be identified. Furthermore, this work extends the result of [49] by measuring the shape-changing caused by discrepant actuator commands within one morphing module such that the nondiagonal elements of the mapping matrix can also be obtained. Then, this mapping matrix is used to directly convert the morphing displacement commands to the servo commands in the FF control cases. For IM-NDI, we experimentally choose $k_p = 22.5$ and $k_d = 1.5$. These gains are tuned considering the tradeoff between tracking error reduction and noise attenuation. The experiments are conducted to track a sinusoidal signal with the same amplitude $A_m = 4$ mm but different angular frequencies. Specifically, the angular frequency $\omega$ respectively equals to 3, 6, 9, and 12 rad/s. As representatives, we illustrate the results for $\omega = 3$ rad/s and $\omega = 12$ rad/s in Figs. 6 and 7, respectively. As can be observed, both IM-NDI and FF can successfully track the reference, but IM-NDI has smaller lags and reduced tracking errors.

In Figs. 6 and 7, the control command is the direct output of the IM-NDI controller, while the “measurement” denotes the real angle feedback from the servo. Although small oscillations occur, the actuator shows desirable performance for command tracking. Coping with mechanical imperfections is one of the most challenging issues in this task. Among all mechanical imperfections, backlash is the most dominate and influential nonlinearity in this system, which
is also the primary cause for the tracking lag. As illustrated in subfigure (c), the ideal tracking curve is a line segment defined on $[-4, 4]$ mm with a slope of 1. Owing to backlash, the sinusoidal reference and the real measurement make up of a circle curve. It is clear that IM-NDI outperforms the FF controller in handling backlash nonlinearity because the curve of IM-NDI is closer to the ideal tracking line.

To intuitively compare the two methods, we define two tracking performance metrics regarding the width and length of backlash circle, as presented in Fig. 8. The left plot in Fig. 8 illustrates the standard backlash nonlinearity whose width is 2 mm. The width measurement $W_b$ is defined as the length of the horizontal segment that starts and ends at the backlash curve while passing through the origin. The ideal tracking is denoted by the black dashed line whose endpoints are marked as stars. The backlash curve splits the ideal tracking segment and the length of the middle part is defined as the length measurement $L_b$. Normally, the width $W_b$ is more widely used for describing backlash than $L_b$.

However, as can be observed from the right subplot of Fig. 8, the real-world nonlinearity is complex and does not exactly obey the mathematical representation of the standard backlash in [20]. Therefore, both $W_b$ and $L_b$ are used as for assessment in this article. The width measurement $W_b$ intends to describe the lagging property when changing the command direction, and a smaller $W_b$ represents better performance. Moreover, the length measurement $L_b$ can reflect the magnitude shrinking effect, and a larger $L_b$ indicates better performance. Fig. 8 shows that as compared to the standard backlash nonlinearity, the effect caused by the real-world backlash nonlinearity is mainly reflected on the $W_b$, whereas the magnitude shrinking phenomenon is less severe. The control performance comparison regarding different angular frequencies is summarized in Table I, and the data represent the average value of the two actuation channels. It can be observed that thanks to the active compensation, IM-NDI outperforms FF in both $W_b$ and $L_b$ for all angular frequencies, and even the worst case of IM-NDI is better than the best one of FF.

Finally, the robustness of the proposed IM-NDI to external disturbances is verified. Regarding this seamless morphing wing system, all the distributed morphing modules are connected sequentially via elastomeric skin to reduce drag in flight [4]. Consequently, the morphing modules are not purely independent; deflections of one module have impacts on its adjacent modules. Therefore, without changing the settings of Module 2, we will test the robustness of the controller to the disturbances injected by Modules 1 and 3.

In the experiments, Modules 1 and 3 were actuated in an open-loop manner with sinusoidal inputs. In specific, we design an amplitude of 20 deg, an angular frequency of 5 rad/s and a zero phase for Module 1, as well as an amplitude of 25 deg, an angular frequency of 10 rad/s, and a phase of $\phi = \frac{\pi}{2}$ rad for Module 3. The tracking performance is depicted in Figs. 9–12, where the shadowed area stands for the period that the external disturbances are injected. It is clear that with such large disturbances, the control performance of both methods degrade to certain extents. Nevertheless, through Figs. 9–12, it can be observed that IM-NDI in general manages to track the given reference in spite of disturbances by adjusting its control inputs accordingly whereas the FF controller suffers more from the disturbances because it lacks the ability to adapt. For more quantitative comparisons, the root mean square (rms) of the tracking errors in different situations are presented in Table II. Note that Module 2 has two servos; thus, the numbers presented in Table II are the mean values of the two control channels. It is shown that in all situations, IM-NDI outperforms the FF controller in the rms of tracking errors by more than 62%. For both FF and IM-NDI, the rms of tracking errors is larger when disturbances are injected. Nevertheless, although the rms of tracking errors grows as the angular frequency of the reference signal increases, no matter if disturbances exist or not, IM-NDI manages to constrain the rms of tracking errors to within 0.9 deg.

![Fig. 8. Illustrative example of the performance metrics for the backlash nonlinearity.](image)

![Fig. 9. Disturbance rejection performance when tracking a sinusoidal signal with $\omega = 3$ rad/s and $A_m = 4$ mm. The shaded area denotes the disturbance injection phase. a) Tracking performance. (b) Control input of IM-NDI.](image)
TABLE II

<table>
<thead>
<tr>
<th>ω [rad/s]</th>
<th>3</th>
<th>6</th>
<th>9</th>
<th>12</th>
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<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Disturbed</td>
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<td>Yes</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>FF</td>
<td>1.17</td>
<td>1.76</td>
<td>1.55</td>
<td>2.19</td>
</tr>
<tr>
<td>IM-NDI</td>
<td>0.34</td>
<td>0.62</td>
<td>0.55</td>
<td>0.74</td>
</tr>
<tr>
<td>Improvement</td>
<td>71.06%</td>
<td>64.78%</td>
<td>64.40%</td>
<td>66.34%</td>
</tr>
</tbody>
</table>

Comparision of the RMS of Tracking Errors, [deg]

Fig. 10. Disturbance rejection performance when tracking a sinusoidal signal with \( \omega = 6 \) rad/s and \( A_m = 4 \) mm. The shaded area denotes the disturbance injection phase. (a) Tracking performance. (b) Control input of IM-NDI.

Fig. 11. Disturbance rejection performance when tracking a sinusoidal signal with \( \omega = 9 \) rad/s and \( A_m = 4 \) mm. The shaded area denotes the disturbance injection phase. (a) Tracking performance. (b) Control input of IM-NDI.

Fig. 12. Disturbance rejection performance when tracking a sinusoidal signal with \( \omega = 12 \) rad/s and \( A_m = 4 \) mm. The shaded area denotes the disturbance injection phase. (a) Tracking performance. (b) Control input of IM-NDI.

Furthermore, the distributions of tracking errors under different conditions are illustrated in Fig. 13. It can be observed that because of the physically limited servo bandwidth, for both FF and IM-NDI, the standard deviation of tracking errors is increasing as the angular frequency of the reference signal increases. In spite of this, IM-NDI always shows a more clustering property around 0 as compared to FF. When disturbances exist, both methods present a more scattered distribution, but FF shows a more disturbed distribution, which is compatible with the results shown in Figs. 9–12 and Table II. Besides, the mean values of the tracking errors for FF have values further away from 0, whereas IM-NDI still has almost 0 mean values. Magnifying the control gains of IM-NDI (\( k_p, k_d \)) can potentially further reduce the data spreads, which however will amplify measurement noise as a side effect. Overall, the results collectively validate the better robustness of the IM-NDI method towards external disturbances.

V. CONCLUSION

Targeting for handling the mechanical imperfections in a seamless active morphing wing, this article develops a data-driven IM-NDI control approach by integrating an online identified IM and the NDI control technique. The system dynamics is identified online merely using the stored input-output data without a prior-known model. Then, an NDI controller is developed based on the identified dynamics.

A crucial aspect of improving these imperfections is an accurate knowledge of the morphing wings’ shape. A vision-based control system was developed, which has shown to be adequately effective for this task, given its robustness, high frame rates (250 FPS), and good calibration accuracy (average 0.25 mm). To evaluate the proposed method, a real-world experiment is conducted based on...
computer vision feedback. The experimental results demonstrate that by applying the IM-NDI, the morphing wing can track reference signals with different frequencies in spite of external disturbances. Under FF control, the morphing wing suffers from mechanical imperfections, reflected by the lagging and magnitude shrinking phenomena in the tracking responses. The performance of FF control also degrades in the presence of external disturbances. By contrast, experimental results show that IM-NDI can effectively decrease the tracking errors by more than 62% despite disturbances. Furthermore, the proposed vision-based system combined with the control methodology demonstrates the ability to compensate for mechanical imperfections without changing the morphing hardware. All results collectively illustrate the effectiveness of the proposed IM-NDI in dealing with mechanical imperfections existing in the morphing wing system.

APPENDIX A

PROOF OF LEMMA 1

Recalling (5) and (6), the following approximation holds:
\[ \hat{\Theta}_{t-2,t-N-1} \Delta x_{t-N} = \hat{N}_V \Delta x_{t-N} \approx \hat{N} \Delta \hat{y}_{t-N} - \hat{N} T_N \Delta u_{t-1,N}. \] (24)
Substituting (8) into (24) yields
\[ (\hat{N}_0 + \hat{N}_1)V_N \Delta x_{t-N} \approx (\hat{N}_0 + \hat{N}_1)\Delta \hat{y}_{t-N} - (\hat{N}_0 + \hat{N}_1)T_N \Delta u_{t-1,N}. \] (25)

It is noted that \( \hat{N}_1 V_N = 0 \), and therefore, \( \hat{N} \Delta y_{t-N} = \hat{N}_0 V_N \Delta x_{t-N} \). Consequently,
\[ \hat{A}_{t-2,t-N-1} \Delta x_{t-N} = \hat{N}_0 V_N \Delta x_{t-N} \approx \hat{N}_0 \Delta \hat{y}_{t-N} - \hat{N}_0 T_N \Delta u_{t-1,N} \] (26)

independently of \( \hat{N}_1 \).

By substituting (26) into (5), it can be obtained that
\[ \Delta x_t \approx \hat{N}_0 \Delta \hat{y}_{t-N} + (U_N - \hat{M}_0 T_N) \Delta u_{t-1,N} \] (27)

which expresses the incremental state in terms of past input-output data. This completes the proof.

APPENDIX B

PROOF OF THEOREM 2

Since the optimal matrix \( \Theta \) is valid over \( A^T \), the previous measurements can uniformly be written as
\[ \Delta Y_{t+1} = Z_t^T \Theta + E_{t+1} \] (28)
where \( \Delta Y_{t+1} = [\Delta y_{t+1}, \ldots, \Delta y_{t+1}] \in \mathbb{R}^{P \times (t-b)} \), \( Z_t = [z_t, \ldots, z_t] \), and \( E_{t+1} = [e_{a,b}, \ldots, e_{o,t}] \). If Assumption 4 holds, \( Z_t Z_t^T \) is guaranteed positive definite and the estimation covariance matrix \( \text{Cov} \) is invertible as \( \text{Cov}^{-1} = Z_t \Gamma_z Z_t^T \), where \( \Gamma_z = \text{diag}(\gamma_{RLS}^{(t-b+1)}, \ldots, 1) \), and \( \text{diag}(\cdot) \) reshapes the vector to a diagonal matrix. The approximate matrix \( \hat{\Theta} \) can accordingly be represented as [38]
\[ \hat{\Theta} = \Theta + \hat{\Theta} = \Theta + \text{Cov} Z_t \Gamma_z E_{t+1} \] (29)
where \( \hat{\Theta} \) denotes the approximation error.

Therefore, the aim of the RLS algorithm is to let the following approximate error correlation matrix converge to 0:
\[ \hat{L}_t = E(\hat{\Theta} \hat{\Theta}^T) \] (30)

where \( E(\cdot) \) is the expectation operation. By substituting (29) into (30), and noticing that both \( \text{Cov} \) and \( \Gamma_z \) are symmetrical matrices, we attain
\[ \hat{L}_t = E \left( \text{Cov} Z_t \Gamma_z E_{t+1} \Gamma_z^T \text{Cov} \right) \] (31)

According to Assumption 5, \( e_{a,t} \) is the white noise independent of \( \Xi_t \) such that (31) continues as
\[ \hat{L}_t = E \left( \text{Cov} \hat{X}_t \Gamma_z E_{t+1} \Gamma_z^T \text{Cov} \right) \] (32)

where \( \sigma_e^2 \) is the variance of \( e_{a,t} \), and \( \text{Cov}^{-1} = \Xi_t \Gamma_z^T \Xi_t^T \).

Considering the difficulty in the rigorous evaluation of (32), we approximately evaluate \( \hat{L}_t \) with the facilitation of Assumption 5. By noticing that \( \text{Cov}^{-1} \) is a weighted sum of the outer products \( \Xi_t^T \Xi_t \), the following approximation holds in terms of Assumption 5:
\[ \text{Cov}^{-1} \approx \frac{1 - \gamma_{RLS}^{(t-b+1)}}{1 - \gamma_{RLS}} E_o \] (33)

where \( E_o = E(\Xi_t^T \Xi_t) \) is the correlation matrix of measurements. Based on Assumption 4, \( \Xi_t^T \Xi_t \) is positive definite and \( E_o \) is invertible.

Substituting (33) into (32) yields
\[ \hat{L}_t \approx \sigma_e^2 \left( \frac{1 - \gamma_{RLS}^{(t-b+1)}}{1 - \gamma_{RLS}} \right)^2 \frac{1 - \gamma_{RLS}^{(t-b+1)}}{1 - \gamma_{RLS}} E_o^{-1} \]
\[ = \sigma_e^2 \frac{1 - \gamma_{RLS}}{1 + \gamma_{RLS}} E_o^{-1} \] (34)

In the steady domain, i.e., \( t \rightarrow M \rightarrow \infty \), we obtain that
\[ \hat{L}_M = \sigma_e^2 \frac{1 - \gamma_{RLS}}{1 + \gamma_{RLS}} E_o^{-1}. \] (35)

It can be observed that if \( \gamma_{RLS} \) is very close to 1, then \( \hat{L}_M \rightarrow 0 \), indicating that the approximate extended matrix converges to the optimal matrix, which ends the proof.

REFERENCES

[1] T. A. Weisshaar
Morphing aircraft systems: Historical perspectives and future challenges

Overview of the SmartX wing technology integrator submitted for publication.
Design of a smart morphing wing using integrated and distributed trailing edge camber morphing

Seamless active morphing wing simultaneous gust and maneuver load alleviation

Finite-time fault-tolerant attitude stabilization for spacecraft with actuator saturation

TS fuzzy model-based controller design for a class of nonlinear systems including nonsmooth functions

Vibration control of a flexible spacecraft system with input backlash

[8] L. Sanches, T. A. Guimaraes, and F. D. Marques
Aerelastic tailoring of nonlinear typical section using the method of multiple scales to predict post-flutter stable LCOs

[9] X. Wang, E.-J. van Kampen, Q. Chu, and F. Lu
Stability analysis for incremental nonlinear dynamic inversion control

Neural net backlash compensation with Hebbian tuning using dynamic inversion

Adaptive backlash compensation in upper limb soft wearable exoskeletons

Robust control design for mechanisms with backlash

Robust controller design for feedback systems with uncertain backlash and plant uncertainties subject to inputs satisfying bounding conditions

Adaptive learning-based observer with dynamic inversion for the autonomous flight of an unmanned helicopter

Output-redefinition-based dynamic inversion control for a nonminimum phase hypersonic vehicle

[16] Y. Huang, D. M. Pool, O. Strooisma, and Q. Chu
Long-stroke hydraulic robot motion control with incremental nonlinear dynamic inversion

Backlash compensation by smooth backlash inverse for haptic master device using cable-conduit

Adaptive control approach for improving control systems with unknown backlash

[19] A. Adeleke and J. Mattila
Adaptive backlash inverse augmented virtual decomposition control of a hydraulic manipulator

Backlash compensation in nonlinear systems using dynamic inversion by neural networks

Adaptive fuzzy tracking control of nonlinear systems with asymmetric actuator backlash based on a new smooth inverse

[22] A. Roudbari and F. Saghaei
Generalization of ANN-based aircraft dynamics identification techniques into the entire flight envelope

[23] S. A. Emami and A. Roudbari
Multimodel ELM-based identification of an aircraft dynamics in the entire flight envelope

[24] B. Sun and E.-J. van Kampen
Intelligent adaptive optimal control using incremental model-based global dual heuristic programming subject to partial observability

Nonlinear adaptive flight control using incremental approximate dynamic programming and output feedback

[26] B. Sun and E.-J. van Kampen
Incremental model-based heuristic dynamic programming with output feedback applied to aerospace system identification and control

[27] B. S. Alhayami et al.
Visual sensor intelligent module based image transmission in industrial manufacturing for monitoring and manipulation problems

Adaptive real-time clustering method for dynamic visual tracking of very flexible wings

[29] E. Pan, X. Liang, and W. Xu
Development of vision stabilizing system for a large-scale flappping-wing robotic bird

Obstacle avoidance strategy using onboard stereo vision on a flapping wing MAV

[31] P. Serra, R. Cunha, T. Hamel, C. Silvestre, and F. Le Bras
Nonlinear image-based visual servo controller for the flare maneuver of fixed-wing aircraft using optical flow

SUN ET AL.: VISION-BASED NONLINEAR INCREMENTAL CONTROL FOR A MORPHING WING 5517
A novel actuator controller: Delivering a practical solution to realization of active-truss-based morphing wings

3-D reconstruction and measurement system based on multi-mobile robot machine vision

[34] Y. Wang, M. Shan, Y. Yue, and D. Wang
Vision-based flexible leader-follower formation tracking of multiple nonholonomic mobile robots in unknown obstacle environments

[35] B. Sun and E.-J. van Kampen
Reinforcement learning-based adaptive optimal flight control with output feedback and input constraints

[36] F. L. Lewis and K. G. Vamvoudakis
Reinforcement learning for partially observable dynamic processes: Adaptive dynamic programming using measured output data

[37] N. T. Nguyen

[38] B. Farhang-Boroujeny

Incremental sliding-mode fault-tolerant flight control

[40] QT Brightek
QBLP670-IR3 3528 PLCC2 IR LED
2021.

[41] OptiTrack Primex 41—In depth

[42] R. Acharya

[43] B. Fu et al.
High-precision multicamera-assisted Camera-IMU calibration: Theory and method

[44] K. Kanatani, Y. Sugaya, and Y. Kanazawa


[46] OptiTrack Motive API NaturalPoint product documentation ver 2.2

Accuracy map of an optical motion capture system with 42 or 21 cameras in a large measurement volume

[48] D. Li et al.
A review of modelling and analysis of morphing wings


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