CONTROL DESIGN FOR
TWO-BLADED WIND TURBINES
CONTROL DESIGN FOR TWO-BLADED WIND TURBINES

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In the past decades, wind energy has evolved into a reliable source of sustainable energy. It offers a potential to reduce carbon emissions as well as advantages at political and economic levels. In order to further strengthen the position of wind energy, manufacturers, designers, and researchers are continuously looking for ways to drive down the costs of wind energy. With the gradual increase of installing wind energy at offshore locations, an interesting and attractive opportunity is found in two-bladed wind turbines. At offshore locations, several drawbacks, which have long hindered the development of two-bladed wind turbines, cease to exist. Moreover, with the use of advanced control methods, the increased fatigue loads associated with two-bladed rotors can be mitigated. This makes that two-bladed wind turbines with advanced control could provide a significant reduction of the cost of wind energy.

The introduction of this thesis is organized as follows. In Section 1.1, three important factors influencing the cost of wind energy and the role of offshore wind energy are discussed. In order to further drive down the cost of wind energy, Section 1.2 motivates why two-bladed wind turbines potentially offer a big step forward. The performance of wind turbines is heavily dependent on the various wind turbine controllers and is therefore discussed in Section 1.3. The advantages and challenges of designing controllers for wind turbines with a fixed structure are outlined in Section 1.4. Finally, the thesis goal and outline are given in Section 1.5.

By the end of 2014, the world’s cumulative installed wind energy capacity reached nearly 370GW (Global Wind Energy Council, 2015). In the same year, Denmark set the world record for wind production by providing 39.1% of its total electricity needs from wind power. In Germany 9% of the total electricity consumption is generated from wind energy and in the USA this is roughly 5%. The majority of the wind energy is produced at onshore locations. Looking at offshore wind capacity, the UK has the largest offshore wind energy capacity in Europe with nearly 4.5GW of installed offshore wind energy. Denmark has just over 1.25GW offshore wind power and Germany doubled its offshore installed wind capacity in 2014 to 1.05GW.
The goal set by the Dutch government is to have 4.45 GW of operational offshore wind energy by the year 2023 (Ministerie van Infrastructuur en Milieu, 2013). The Netherlands had a total installed capacity of 2.81 GW by the end of 2014, of which nearly 247 MW was deployed offshore. This means that by taking into account the already existing offshore wind farms and the wind farms in preparation, a wind energy capacity of 3.45 GW will be required from 2015 onwards. In realizing the desired capacity, the cost-effectiveness of offshore wind energy plays an important role. While the cost-effectiveness of onshore wind energy has become competitive to fossil fuel powered energy, this is not yet the case for offshore wind energy, which is roughly two to three times more expensive (Kost et al., 2013; Energy Information Administration, 2014; Siemens AG, 2014). For that reason, much effort is put into decreasing the costs of offshore wind energy to strengthen the business case.

1.1. Cost of Wind Energy

The cost of energy of wind turbines and wind farms is an important characteristic for the competitiveness of wind energy. A number of factors which determine the cost of energy of a single wind turbine can be pointed out (Moné et al., 2015):

**Annual Energy Production (AEP):** The AEP is determined by the available wind, the wind turbine rating, and the number of operating hours in full and partial load. It is therefore important to design reliable wind energy conversion systems, because failures and maintenance contribute to a decreased AEP.

**Installed capital costs:** The components of the wind turbine, including the tower, rotor, and drivetrain, determine the capital costs. A review report on cost of energy (Moné et al., 2015) states that the turbine components make up 68% of the capital costs of onshore turbines, and an estimated 32% of the capital costs of offshore turbines. The reasons for this difference include the increased costs at offshore locations related to the substructure and foundation, assembly and installation, and electrical infrastructure.

**Annual operating costs:** Land-lease costs, operation and maintenance, and replacement costs determine the annual operating costs. Operation and maintenance costs include wage and material costs known beforehand, but also unplanned maintenance and other costs that depend on the amount of electricity generated.

Besides the factors at an individual turbine level, additional factors arise when considering the cost of energy at a wind farm level. It is well known that grouping wind turbines closely has some beneficial impacts on installation, maintenance and cable lengths, but aerodynamic interaction (due to turbine wakes) negatively affects the total power output (Gebraad et al., 2014).

So far, the cost of energy has been steadily reduced by increasing the size of wind turbines. This is a very effective way to increase the AEP, because by doubling the rotor size, the rotor swept area increases by four times and hence the power output. An illustration of the increase in size of wind turbines is depicted in Figure 1.1. In the early nineties of the previous century, the largest rotor diameter was 40 m and the rated power
output 500 kW. In 2000, the rotor size was already doubled to 80 m with a rated power of 800 kW. Currently, the largest commercially available turbine has a rotor diameter of 164 m and a rated power of 8 MW (Windpower monthly, 2015). It is predicted that the size and thereby the power output of wind turbines will exceed the 10 MW frontier in the coming years.

Reducing the cost of energy can also be achieved by decreasing the capital costs associated with wind turbines. This can, for example, be realized by designing the wind turbine with less material, which typically leads to a lighter turbine and thus cost savings. As a consequence of the increased flexibility however, the bending stresses due to the wind will increase and negatively affect the turbine fatigue loads. The negative effect of bending stresses can be (partly) compensated for by using active control methodologies (see Section 1.3).

The cost of wind energy heavily depends on the location of deployment, as already briefly discussed above. Onshore locations have the benefit of being easily accessible and therefore cheaper in terms of infrastructure, construction, grid connection, and maintenance. However, the available locations for onshore locations are becoming scarce (Gebraad, 2014) and onshore wind energy often faces social resistance. In particular, large wind turbines are considered undesirable near populated areas due to visual and noise impacts. For these reasons, a gradual increase of offshore installed wind energy is taking place (Global Wind Energy Council, 2015).

Offshore locations have some favorable properties compared to onshore locations (Hau, 2006). At offshore locations, more wind resources are generally available year-round, benefiting the AEP. For example, it is known that the average European onshore wind turbine annually extracts 24% of its theoretical maximum power, whereas the average European offshore wind turbine extracts 41% of its theoretical maximum (Europower, 2015).
This discrepancy in extracted power between onshore and offshore is mainly caused by the more persistent wind speeds at offshore locations (Pryor and Barthelmie, 2001, 2002).

Another advantage of offshore wind is that the surface roughness of the sea is typically much lower than that of land, which means that the wind speed above sea increases more rapidly with height than on land. Hence, tower heights can be lowered while maintaining the same power output compared with land based locations.

Finally, turbulence intensity levels for offshore locations are lower. Whereas turbulence levels onshore are typically between 10% and 20%, four years of wind speed measurements at an open sea location showed that turbulence levels of less than 10% were measured at a height of 50 m above the sea level (Türk and Emeis, 2010). The reduced wind turbulence levels at offshore areas also positively affect the wind turbine fatigue loads. On the other hand, the lower turbulence also causes the wakes in a wind farm to recover more slowly because there is less mixing of the air (Hansen et al., 2012), which might lead to an increase in the turbine spacing.

In the ongoing process of reducing the cost of energy, much effort has been devoted to the development of three-bladed wind turbines. However, with the gradually changing focus towards offshore wind energy, new wind turbine concepts are being (re)considered, explored and developed.

1.2. RENEWED INTEREST IN TWO-BLADED WIND TURBINES

Although the wind energy market is nowadays dominated by three-bladed wind turbines, numerous two-bladed turbines have been developed and built in the past (see for example Hau (2006) and Spera (2009) for a historical overview of wind turbines). Already in the forties of the last century, two-bladed wind turbines were built by the company F. L. Smidth (Westh, 1981). Their first design was a two-bladed turbine with a rotor diameter of 17.5 m and a rated power output of 50 kW (see Figure 1.2a). Twelve of these turbines were built in total, with both lattice steel towers and concrete towers.

Due to problems with the dynamic characteristics of the two-bladed rotor, their second design consisted of three blades. In the same period, the world’s first large1 two-bladed wind turbine, i.e., the Smith-Putnam wind turbine (Putnam, 1948), was built. This turbine had a rotor diameter of 53.3 m, a tower height of 35.6 m, and a rated power output of 1.25 MW (see Figure 1.2b). The rotor was positioned downwind from the lattice tower and blade flapping hinges were used to reduce the dynamic loading. Speed control was provided by hydraulic pitching2 of the blades. After roughly four years of operation, the turbine was disassembled because of a fracture in one of the blades.

During the 1970s and 1980s, large subsidized programs were carried out to develop large wind turbines (Hau, 2006). This led to, among others, the experimental MOD-0 to MOD-5 wind turbines in the United States. These wind turbines were developed and built by large companies such as Boeing, General Electric and Westinghouse. The MOD-1, built by General Electric, had a lattice tower, a two-bladed rotor with a diameter of 61 m, and a power output of 2 MW. Succeeding the MOD-1, the MOD-2 built by Boeing

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1 In this context ‘large’ means larger than 1 MW.
2 Pitching a blade means rotating the blade along its longitudinal axis so as to change the aerodynamics, also see Figure 1.3.
1.2. Renewed Interest in Two-Bladed Wind Turbines

Figure 1.2: Two-bladed wind turbine designs in the previous century (photographs from Hau (2006)).
in 1980 (Boeing Engineering & Construction Company, 1979; Linscott et al., 1981), featured a monopile support structure, a two-bladed rotor with a diameter of 91 m, and a power output of 2.5 MW (see Figure 1.2c). Finally, General Electric designed the MOD-5A two-bladed wind turbine (General Electric Company, 1984); it was not completed, but replaced by the MOD-5B, which was based on the MOD-2 and could be implemented more rapidly. The MOD-5A was designed to have a rated power output of 7.3 MW and a rotor diameter of 122 m. The MOD-5B (Lowe and Wiesner, 1983), built by Boeing in 1987, had a two-bladed rotor diameter of 97 m and power output of 3.2 MW (see Figure 1.2d).

Despite these extensive developments of two-bladed wind turbines in the previous century, three-bladed wind turbines became the favored choice in the years after. In general, it can be stated that two-bladed wind turbines suffer from a number of drawbacks (Hau, 2006):

**Visual impact:** The rotor of a two-bladed wind turbine has a beam-like structure. The passing of the blades of such a structure causes a restless view. A three-bladed rotor gives a much more ‘steady’ view.

**Noise impact:** In order for a two-bladed wind turbine to operate at maximal power output, higher rotational speeds are required. The increased rotor speed causes increased noise emission levels.

**Challenging dynamics:** The dynamics of a two-bladed wind turbine are considered to be more challenging. In every revolution, the beam-like rotor is in a vertical position twice. This means that twice per revolution, there is a large difference between both blade loads caused by wind shear. Moreover, the inertia of the two-bladed rotor is dependent on the rotor position, which means that asymmetric wind flows can cause large yawing moments\(^3\). The latter effects account for increased fatigue loading of a two-bladed wind turbine.

The above mentioned disadvantages have largely contributed to the dominant position of three-bladed wind turbines in the current wind energy market. However, citing from (Hau, 2006), the outlook for two-bladed wind turbines may well change in the future:

“As the size of the wind turbines increases, however, and their field of application is extended (offshore wind farms), the two-bladed rotor may quite easily become attractive again. The choice of the optimum number of rotor blades is, therefore, not only a question of aerodynamic power differences, but rather requires integrated consideration of the wind turbine and the conditions under which it is used as a total system.”

Two-bladed wind turbines offer a number of distinct advantages over three-bladed wind turbines. The first is the major advantage of having a reduced number of blades (and pitch drives). Although this will be partly compensated for by the other two blades, the rotor weight (and therefore material) is approximately equal to 70% of the rotor weight of a comparable three-bladed rotor (Aerodyn engineering GmbH, 2014). Moreover, as two-bladed rotors operate at a higher rotational speed, the torque on the shaft is

---

\(^3\) A yaw moment causes the rotor to rotate around the support structure, see also Figure 1.3.
lower and consequently the drivetrain and nacelle (which houses for instance the generator and drivetrain) are lighter. Another advantage can be found during transportation and construction: a two-bladed rotor can be transported fully preassembled and pretested on a ship’s deck to the wind farm site (De Vries, 2011). Finally, extreme loads can be considerably reduced by using horizontal parking of the rotor (Aerodyn engineering GmbH, 2014). Due to reduced extreme loads, the tower and foundation can be designed lighter.

The increased fatigue loads of a two-bladed rotor can largely be overcome in two different ways. Considering that the wind flow is asymmetric due to for example wind shear (i.e., the wind speed increases with height above the surface), it makes sense to allow the rotor to have a teetering motion about the shaft. This can be achieved by connecting the blades to a teetering hinge. The resulting dynamics are then comparable to a three-bladed turbine (Hau, 2006). Another way of compensating the increased fatigue loadings is to use advanced control methods. More specifically, by changing the aerodynamic lift of the blades over one revolution of the rotor, the dominant cyclic loads can be removed (see Section 1.3 and Bossanyi et al. (2013)).

At the time of writing this thesis, a number of companies have begun developing and building two-bladed wind turbines (Schorbach and Dalhoff, 2012; Clover and Snieckus, 2014). This renewed interest in two-bladed wind turbines is mainly motivated by the increased focus on offshore wind energy. At offshore locations, the noise and visual aspects discussed earlier in this section automatically disappear. Furthermore, with a teetering hinge or active control methods, the challenging dynamics causing higher fatigue loads can be compensated for. Finally, in Shikha et al. (2005) a cost of energy reduction of 10 – 12% is stated and in Clover and Snieckus (2014) a 20% reduction, on paper, is mentioned for two-bladed wind turbines. Combining these facts and the potential cost of energy reduction and it can be concluded that two-bladed turbines are an interesting opportunity which manufactures are actively exploring.

In the remainder of this section, a number of recent designs of two-bladed wind turbine are briefly discussed. The purpose of this overview is to give an impression of the variety of two-bladed wind turbine designs, each having its own advantages and features. It should be stressed that the overview is far from complete, but covers a number of interesting designs. For a more complete overview of two-bladed turbine designs, refer to Schorbach and Dalhoff (2012). The rated power and rotor diameter of the turbine designs covered below are listed in Table 1.1. Because certain details of the recent designs require some understanding of wind turbine yaw and blade pitching, Figure 1.3 visualizes the meaning of these concepts.

<table>
<thead>
<tr>
<th>Manufacturer</th>
<th>Rated power [MW]</th>
<th>Rotor diameter [m]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aerodyn/Ming Yang</td>
<td>6.0</td>
<td>140</td>
</tr>
<tr>
<td>Condor Wind Energy</td>
<td>6.1</td>
<td>125</td>
</tr>
<tr>
<td>Envision</td>
<td>3.6</td>
<td>128</td>
</tr>
<tr>
<td>2-B Energy</td>
<td>6.0</td>
<td>140.6</td>
</tr>
</tbody>
</table>
1. INTRODUCTION

**Blade pitch**

**Yaw**

Figure 1.3: Downwind configured wind turbine with blade pitch and yaw degrees of freedom

**AERODYN/MING YANG**

The German company aerodyn has been developing wind turbine systems since 1983 for manufacturers all over the world. Since 2010, a 3 MW downwind two-bladed wind turbine, has been in operation and, more recently, a prototype of the 6 MW downwind two-bladed turbine (built by the Chinese manufacturer Ming Yang) was connected to the Chinese grid. The “SCD advanced”, as the 6 MW turbine is called, has a rotor diameter of 140 m and a hub height of 100 m (Aerodyn engineering GmbH, 2014). A photograph of the turbine at the coast of China is shown in Figure 1.4a.

An important characteristic of the 6 MW SCD advanced turbine is the use of redundant components. For example, the turbine has three 3.0 MW inverters and a surplus of hydraulic pumps and other components. In case of failures, simply switching to a redundant component increases the level of reliability. Moreover, during a typhoon, the rotor is parked in horizontal position and the hydraulic yaw brakes are released such that the rotor-nacelle assembly can freely rotate. The advantage is that a downwind rotor naturally aligns with the wind and can follow rapid wind direction changes. Due to the horizontal position of the rotor, structural loads are minimized during extreme winds.

Aerodyn also has an 8 MW two-bladed downwind turbine on the drawing board. This turbine can either be supported with a fixed jacket support structure or a floating support structure (called “SCD nezzy”).

**CONDOR WIND ENERGY**

In November 2010, the UK-based company Condor Wind Energy was established. Condor Wind Energy is developing a two-bladed 2 MW onshore turbine and a two-bladed 6.1 MW offshore turbine (Condor Wind Energy, 2015), called the Condor 6 (see Figure 1.4c for an artist impression). The Condor 6 is the successor of the Condor 5 design (De Vries, 2011). One of the main innovations of the Condor 6 design is the
1.2. Renewed interest in two-bladed wind turbines

(a) Photograph of the aerodyn 6 MW turbine off the coast in China (photograph from aerodyn engineering GmbH, 2014).

(b) Photograph of the Envision 3.6 MW wind turbine (photograph from Envision, 2015).

(c) Artist impression of the Condor 6 (illustration from De Vries, 2011).

(d) Illustration of the 2B6 wind turbine designed by 2-B Energy (2-B Energy, 2015).

Figure 1.4: Photographs and illustrations of recent two-bladed wind turbine designs.
power regulation. Whereas power control in above-rated winds is typically achieved by pitching the blades out of the wind, the Condor 6 uses active yaw control. In below-rated operating conditions, the rotor is kept in the wind; in above-rated operating conditions, the yaw drives are used to yaw the turbine from the wind to control the rotor speed. An elastomeric teetering hinge (for which a patent has been filed (Caruso et al., 2014)) is used to ‘filter’ out most of the asymmetric loads coming from the wind (Condor Wind Energy, 2015). Moreover, it dramatically reduces the yaw moments, even at high yawing accelerations.

In a study by Wilkinson et al. (2010), it was found that one of the most occurring failures in a wind turbine is the pitch drives. Therefore, the Condor 6, which regulates the power by actively yawing the rotor, has a major advantage of not requiring a pitch mechanism. Furthermore, Garrad Hassan, the leading consultancy company within the wind industry, demonstrated that the fatigue drivetrain loads of the Condor 6 are reduced by 80% compared to three-bladed turbines due to the specific turbine design. This is another advantage, because the gearbox is another major contributor to wind turbine failures (Wilkinson et al., 2010).

**ENVISION**

Another interesting two-bladed wind turbine is developed by Envision (Envision, 2015). This is a 3.6MW downwind turbine design which has as key innovation partially pitchable blades. This enables the turbine to pitch the outer section of the blades such that extreme loads can be reduced (Kim et al., 2014b,a). Especially in case of large errors between the wind direction and the rotor position, the extreme loads can be substantially reduced. This is of particular importance at locations where typhoons occur. The partial pitch turbine also has the ability to be customized to the clients’ needs at a specific location by adjusting the inner blade section. A photograph of the wind turbine is shown in Figure 1.4b, from which the partial pitch can clearly be observed.

**2-B ENERGY**

Another novel two-bladed wind turbine design, called the 2B6 wind turbine (2-B Energy, 2015) is being developed by 2-B Energy in the Netherlands. The turbine has a rated power of 6MW and a rotor diameter of 140.6m. The rotor blades are rigidly connected to the hub and blade pitching is used for load control. The major novelties of the full modular two-bladed 2B6 wind turbine are:

1. a downwind rotor configuration;
2. a damped free-yaw system;
3. a full three-leg jacket support structure;
4. a service life of 40 years.

Moreover, the 2B6 has a helicopter deck on top of the nacelle for ease of access and has the possibility to include a transformer deck in the jacket support structure. An illustration of the turbine is shown in Figure 1.4d. The first 2B6 wind turbine should be fully operational in 2015.
A model of the 2B6 is used in Chapter 4 for a study of the impact of yaw damping and controller strategies on the turbine loads for a two-bladed (damped) free yaw wind turbine.

At the start of this section it was stated that nowadays the wind energy market is dominated by three-bladed wind turbines. It is unlikely to expect that this will change dramatically soon; however, it can be expected that two-bladed wind turbines will gradually obtain a larger market share, especially considering the potentially lower costs and the increased deployment of wind energy at offshore locations. Moreover, more advanced control techniques are becoming available, which are able to compensate for the increased fatigue loadings of two-bladed wind turbines, this could then further accelerate the reduction of the cost of energy and increase the market share of two-bladed wind turbines.

1.3. Control of wind turbines

Wind turbines are subjected to a three-dimensional, time-varying turbulent wind field. The continuous changing wind field therefore requires wind turbines to be actively controlled. Two control objectives for wind turbines can be identified. First, the wind turbine should be regulated such that it extracts the maximum available power from the wind. Second, the loads on the wind turbine should be kept as low as possible to reduce fatigue. The control system of a wind turbine can therefore be decomposed into two layers. A high-level supervisory controller enables several lower-level controllers depending on the current wind and turbine conditions. More specifically, the supervisory controller enables the specific controllers designed for start-up conditions, normal operating conditions, cut-out conditions, and emergency events.

A wind turbine has a number of control degrees-of-freedom, cf. Figure 1.3, which schematically shows a downwind turbine. The three most important degrees of freedom are the generator torque (not shown in Figure 1.3), the blade pitch, and the turbine yaw. The generator torque directly influences the rotor speed in below-rated wind conditions. The blade pitch (i.e., the angular rotation of the blade along its longitudinal axis) is used to alter the aerodynamic lift of the blade and makes it possible to control the rotor speed in above-rated wind conditions. The turbine yaw needs to be regularly adjusted such that the rotor is aligned with the wind and maximum energy is extracted from the wind.

During normal operating conditions of a wind turbine, two types of controllers are active (Bossanyi, 2000), i.e., power controllers and load reduction controllers. Typically, two different power controllers are used, which are activated depending on the operating condition of the turbine. The operating conditions can roughly be divided into two operating conditions: below-rated and above-rated. In the former, the wind speed is lower than the rated wind speed of the turbine and the generator torque is regulated such that the power output is maximized and the rotor speed varies. In the latter, the wind speed is rated or higher such that the turbine reaches its rated power output. In this case, the generator torque is fixed while regulating the blade pitch angles to keep the power output and rotor speed at rated values. The controller regulating the generator torque is often called the torque controller and the controller regulating the blade pitch angles is called the Collective Pitch Control (CPC) (because all blades have the same (collective) pitch angle). Switching logic or saturation techniques can be used to hand over the control
between both controllers around rated operating conditions.

The second type of controllers which are active during normal operating conditions actively reduce the wind turbine loads. Wind turbine loads arise from different effects and include wind shear, tower shadow, yaw misalignments, and ‘sampling’ the turbulent wind field. A typical spectral plot of the blade loads and the tower loads is shown in Figure 1.5 for the two-bladed NREL CART2 wind turbine for a wind speed of 18 m s\(^{-1}\) and turbulence intensity of 6%.

The blades have dominant periodic loads at harmonic frequencies of the rotor speed (i.e., \(1P, 2P, \ldots\), where \(nP\) stands for the \(n\) times-per-revolution occurring load) and the tower load is dominated by the first structural tower mode. By using sensor measurements, estimation techniques or a combination of both, controllers can be designed and implemented which minimize the loads on the various components of the turbine.

One such controller which is often employed is a drivetrain damper. It is well-known that for variable speed operating turbines the drivetrain mode is very lightly damped and can therefore lead to large torque oscillations (Bossanyi, 2000). The large oscillations can be prevented by superimposing a small periodic torque on the generator torque, effectively damping the drivetrain mode. Moreover, turbine manufactures often include a feedback loop providing damping for the forward-afterwards (fore-aft) motion of the tower. The fore-aft motion is caused by excitation of the first tower mode yielding large bending moments. Damping can be provided for the tower in the fore-aft direction by actively regulating the aerodynamic thrust moment of the turbine by collectively pitching the blades.

The aforementioned power and load controllers can be applied without significant differences to three-bladed or two-bladed wind turbines. A schematic representation of a wind turbine control system is shown in Figure 1.6. It should be noted that most

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\(4\) The NREL CART2 wind turbine is a two-bladed research turbine on which (advanced) control algorithms can easily be implemented and validated. The CART2 is used in Chapter 2 and Chapter 3 to evaluate control algorithms for two-bladed wind turbines.
of the control loops can be decomposed into separate and almost decoupled single-input single-out control loops (Bossanyi et al., 2009) and can be designed according to Bossanyi (2000).

In Figure 1.6, besides the CPC, also a feedback loop denoted by Individual Pitch Control (IPC) is shown. IPC is different from CPC in that it provides individual setpoints for each blade pitch angle (Bossanyi, 2003). Typically, the IPC angles are 120° phase shifted for three-bladed rotors and 180° for two-bladed rotors. IPC can be used to remove dominant periodic turbine loads, such as wind shear and tower shadow. Hence, it provides a way to remove asymmetric loads, which become increasingly dominant with increasing rotor size.

IPC can play an important role in reducing the cost of energy of wind turbines. Since they are capable of removing large cyclic loads, wind turbine structures can be designed to be more flexible. That is, the wind turbine structure can be designed with less material, which would normally lead to increased bending; however, by using IPC, this consequence is reduced. While load reduction controllers have been thoroughly analyzed for three-bladed wind turbines in the past, only very little attention in this context has been devoted to two-bladed wind turbines. To the best of our knowledge, the only literature considering IPC for two-bladed wind turbines can be found in Larsen et al. (2007), Bossanyi and Wright (2009), Bossanyi et al. (2010), and Bossanyi et al. (2013).

The working principle of IPC can be explained as follows. The rotor dynamics can be regarded as a periodic system (every revolution of the rotor is a period). Designing a controller for such a system would also require to be periodic. However, as the controller design for Linear Time-Invariant (LTI) systems is well-known and more straightforward, a coordinate transformation is used to transform the periodic wind turbine system to a linear system. This transformation, called the Multi-Blade Coordinate (MBC) transformation (Bir, 2008), takes the blade root moments measured in the rotating system as input and transforms these to fixed non-rotating moments. These moments are in fact the tilt and yaw moment of the rotor and have the appealing property of (almost) being decoupled (Bir, 2008; Bossanyi, 2003). Thus, the controllers in the non-rotating frame can be designed with LTI techniques. Finally, by reverse transforming the outputs of the controllers, periodic blade pitch signals are obtained which reduce the blade loads and consequently also other turbine loads.

In the previous paragraphs, various power and load controllers for wind turbine control have been discussed. However, an important controller which has only briefly been mentioned so far is the yaw controller. The yaw controller ensures the rotor-nacelle assembly faces the wind, such that extracted power from the wind is maximal. Typically, the yaw controller activates the yaw drives every five minutes for example, or when the measured yaw misalignment exceeds a certain threshold, to rotate (yaw) the rotor-nacelle assembly in the wind. In such a case, the hydraulic yaw brakes are released and the yaw drives enabled to yaw the rotor perpendicular to the wind direction. The yaw controller impacts the power output mainly in below-rated and to a lesser extent in above-rated conditions. The yaw controller also affects the turbine loads, because of gyroscopic effects due to yawing the turbine, hence, the yaw rotation is kept at very low rates.

In the case of a free yawing wind turbine such as the 2-B Energy 2B6, the use of the
Figure 1.6: Schematic block diagram of a wind turbine control system with the torque controller (active in the below-rated region), the CPC (active in the above-rated region) and the load reducing controllers.
yaw drives can be greatly reduced by using yaw-by-IPC. This means that IPC is used to create periodic individual blade pitch setpoints such that an aerodynamic moment around the tower can be created. This aerodynamic moment causes the rotor-nacelle assembly to rotate accordingly and, hence, can be used to face the rotor in the wind.

The design and tuning of the aforementioned controllers is a critical process. A properly designed and tuned controller maximizes the power output and at the same time keeps the loads as low as possible. In this thesis, a specific type of controllers, well-suited for industrial application, is considered, which is discussed next.

1.4. STRUCTURED CONTROL FOR WIND TURBINES

The deployment rate of industrial applications involving control systems is, among others, determined by the ease of fine-tuning the controllers. For example, the dynamics of wind turbines can be predicted reasonably well by software packages using first-principle models, but will never exactly match the real-world built wind turbine due to many factors (van der Veen et al., 2013b). It is therefore important to have the ability to quickly update or fine-tune the controllers on the real-world turbine, without requiring a full redesign of the controller. A possibly even better approach would be to directly design the controller based on measurements obtained from the system. This is supported by a recent study in which a data-driven controller design outperforms a model-based controller design (Formentin et al., 2014).

Classical optimal and robust control design techniques lead to high order controllers (e.g., as high as the order of the model (plant) used for designing the controller, see Zhou et al. (1996) and Skogestad and Postlethwaite (2006)). The controllers obtained with these design techniques are very hard to modify, because they consist of many parameters without a direct interpretation. Moreover, Proportional Integral Derivative (PID) controllers, notch filters, low-pass filters, and other types of filters are still widely applied to high-end applications in industry (e.g., see Butler (2011)). This also applies to wind turbines, where the majority of the controllers consist of PID controllers, low-pass filters, and notch filters (Bossanyi, 2000).

Controllers with these building blocks belong to the class of fixed-structure controllers. Since the controller structure is fully fixed a priori, only the tunable parameters need to be chosen such that the performance specifications are met. Such controllers can be tuned with the help of plant models and can later on easily be fine-tuned by engineers in the field. However, unlike well-known solutions to unstructured control synthesis problems (e.g., using Riccati equations (Doyle et al., 1989) or Linear Matrix Inequality (LMI) techniques (Gahinet and Apkarian, 1994; Iwasaki and Skelton, 1994)), the main problem that arises when imposing constraints on the controller structure is that the resulting optimization problem is no longer convex and is in general considered to be hard (Nemirovskii, 1993; Blondel and Tsitsiklis, 1997).

In the control theory community, the synthesis and design of fixed-order and fixed-structure controllers have been a research topic of interest for many years. Over the years, many methods to design such controllers have been proposed (Apkarian and Noll, 2006; Maruta et al., 2009; Rubió-Massegú et al., 2013). However, a drawback of the majority of the previously mentioned techniques is that they do not directly compute controllers based on, for example, measured data from the plant, effectively meaning that
either a first-principle model or an intermediate system identification step is required before one can use these techniques and tools. On the other hand, controller synthesis methods using measurements of the plant have several times been proposed in the past (Guardabassi and Savaresi, 2000; Campi et al., 2002; Karimi et al., 2008; den Hamer et al., 2009; Galdos et al., 2010; Khadraoui et al., 2013), but generally require solving complex non-convex optimization problems.

In an ideal scenario, one would be able to directly use input-output measurements from a wind turbine and tune fixed-structure controllers using convex optimization. This could increase the controller performance and speed up the implementation of the controller on the final design.

1.5. Thesis Goal and Outline

As mentioned before, a significant reduction in the cost of energy would strengthen the business case of offshore wind energy. The Far and Large Offshore Wind (FLOW) program (FLOW, 2010) is a research program consisting of 13 Dutch companies and research institutes working together with the aim to drive down the costs of offshore wind energy. The main goals are to increase the reliability, to accelerate the rate of development, and to reduce the risks of wind farms. The FLOW program is subdivided in five themes:

1. Wind farm design;
2. Support structures;
3. Electrical systems and integration;
4. **Turbine development** (this thesis);
5. Societal.

By the end of the project in the year 2015, the combined contributions of the five themes should drive down the costs of offshore wind farms by 20% compared to the year 2010. The FLOW program is followed up by the TKI Wind op Zee program (van Zuijlen et al., 2014), which has the goal to reduce the costs of offshore wind power, compared to 2010, with 40% by the year 2020. This is a significant reduction of the cost of wind energy.

This thesis is part of the FLOW theme 4 research program and focuses on control design for two-bladed wind turbines (FLOW, 2010). More specifically, it focuses on the design of controllers that mitigate the (periodic) wind turbine loads, with the ultimate goal to reduce the cost of energy of wind turbines. Sections 1.1 and 1.2 motivated why two-bladed wind turbines may accelerate the reduction of the cost of energy of wind turbines. Moreover, sections 1.2 and 1.3 motivated that active control, if tuned correctly, can be used to compensate for increased fatigue loads of two-bladed wind turbines and that only few effort has been devoted to control design of two-bladed turbines. Finally, Section 1.4 motivated that structured control design plays an important role in the design and deployment of wind turbine controllers. Therefore, the goal of this thesis is formulated as follows.

**Thesis goal:** Develop structured control architectures and tuning methods for two-bladed wind turbines.
1.5. Thesis Goal and Outline

To achieve this goal, in Chapter 2-4 the control architectures for two-bladed wind turbines with a rigid and free yaw configuration are developed. The controllers are designed such that their structure can be fixed on beforehand and only the tunable controller parameters need to be found. These parameters are then obtained with the use of available design techniques from literature. The focus of this part is on the development of the control architecture rather than on the fine-tuning of the controllers. The latter is left to the turbine manufacturers and designers as this involves many tradeoffs. In Chapter 5, a fixed-structure controller design method is developed. With this method, the structured controllers in the former chapters of the thesis can be tuned.

The thesis consists of six chapters, which can be read independently from each other. As each chapter stands on its own, some overlap between the different chapters exists. A short outline of the chapter contents and publications are given below.

Chapter 2
In Chapter 2, the conventional nonlinear MBC transformation based IPC strategy is analyzed. Based on this analysis, a linear coordinate transformation is considered, and subsequently a novel Linear Individual Pitch Control (LIPC) strategy exploiting this transformation is introduced. It is demonstrated that LIPC can be designed with structured controllers.

The chapter is based on the following publications:


Chapter 3
The LIPC strategy proposed in Chapter 2 is validated by means of field tests on the two-bladed National Renewable Energy Laboratory CART2. In order to do so, the LIPC is scheduled on the rotor speed of the wind turbine, so that the LIPC strategy can be compared to the conventional IPC strategy for below-rated and above-rated operating conditions.

The chapter is based on the following publication:

CHAPTER 4
In Chapter 4, the control architecture for the state-of-the-art 2-B Energy 2B6 two-bladed downwind damped free-yaw turbine is presented. It is shown that the controllers and the amount of yaw damping supplied by the yaw system have a large impact on the turbine loads and impose a design tradeoff for the designer.

The chapter is based on the following publication:


CHAPTER 5
Chapter 5 presents a data-driven fixed-structure controller tuning method. This method exploits the Generalized Nyquist stability criterion and fixed-structure controllers can directly be designed using measurements of the plant. Fixed-structure controllers are experimentally designed for an experimental setup which has dynamics similar to the drivetrain of a wind turbine.

The chapter is based on the following publications:

van Solingen, E., van Wingerden, J. W., and Oomen, T. Data-Driven Optimization of Linear Parameterizable \( \mathcal{H}_\infty \) Controllers in the Frequency Domain. In submitted to Special Issue of International Journal of Robust and Nonlinear Control, 2015d

van Solingen, E., van Wingerden, J. W., De Breuker, R., and Verhaegen, M. Optimization of Linear Parameterizable \( \mathcal{H}_\infty \) Controllers in the Frequency Domain. In 19th IFAC World Congress, Capetown, South-Africa, 2014a

Finally, in the last chapter the conclusions drawn throughout this thesis are summarized and recommendations for future work are given.
In this chapter, the conventional Individual Pitch Control (IPC) strategy for wind turbines is reviewed and a Linear Individual Pitch Control (LIPC) strategy for two-bladed wind turbines is proposed. The typical approach of IPC for three-bladed rotors involves a Multi-Blade Coordinate (MBC) transformation which transforms measured blade load signals, i.e., signals measured in a rotating frame of reference, to signals in a fixed non-rotating frame of reference. The fixed non-rotating signals, in the so-called yaw and tilt direction, are decoupled by the MBC transformation, such that Single-Input Single-Output (SISO) control design is possible. Then, SISO controllers designed for the yaw and tilt directions provide pitch signals in the non-rotating frame of reference, which are then reverse transformed to the rotating frame of reference so as to obtain the desired pitch actuator signals. For three-bladed rotors, the aforementioned method is a proven strategy to significantly reduce fatigue loadings on pitch controlled wind turbines. The same MBC transformation and approach can be applied to two-bladed rotors, which also results in significant load reductions. However, for two-bladed rotors, it is shown that this MBC transformation is singular and therefore not uniquely defined. For that reason, a linear non-singular coordinate transformation is proposed for IPC of two-bladed wind turbines. This transformation only requires a single control loop to reduce the once-per-revolution rotating blade loads (1P’ loads). Moreover, all harmonics (1P, 2P, 3P,...) of the rotating blade loads can be accounted for with only two control loops. As in the case of the MBC transformation, also the linear coordinate transformation decouples the control loops to allow for SISO control design. A high fidelity simulation study on a two-bladed wind turbine without a teetering hub shows the efficacy of the LIPC strategy. The simulation study indicates that LIPC provides similar load reductions and requires similar pitch actuation compared to the conventional IPC strategy.
2.1. INTRODUCTION

The current trend in wind energy is to install wind turbines at offshore locations. It is expected that by the end of 2020 a total amount of 75 GW of offshore wind energy will be installed worldwide (BTM Consult, 2010). Compared to the end of 2011, when offshore wind farms had a total installed capacity of 3.16 GW, this is a tremendous increase. Despite the ongoing shift from onshore to offshore wind energy, the latter still has some disadvantages. To mention a few, installation, assembly and maintenance are more difficult and, above all, more costly at offshore locations. In order to decrease the cost of wind turbines, one could consider to reduce the amount of required material. In this respect, two-bladed wind turbines can be considered as a very interesting opportunity. However, in the past, two-bladed turbines have long been overlooked, partly because of their visual and noise impact. Whereas three-bladed rotors have a symmetrical rotation, providing a visually steady motion, two-bladed rotors do not have symmetrical rotation. Furthermore, two-bladed wind turbines typically operate at slightly higher rotational speeds compared to three-bladed turbines (Manwell et al., 2002), resulting in a higher noise impact. The aforementioned aspects cease to be important for offshore locations and, hence, two-bladed turbines are an interesting opportunity to increase the cost effectiveness.

Besides the visual and noise impacts, two-bladed rotors also require a more complex mounting system in order to connect the rotor to the shaft. The asymmetry of a two-bladed rotor plane causes the load distribution to be strongly dependent on the azimuth. When these azimuth-varying loads are transferred to the main shaft they cause large variations in the shaft bending moments, additional to those due to gravity and inertia. Three-bladed rotors on the other hand, have a rather symmetric load distribution from the blades to the shaft over the azimuth and, hence, do not have this problem. For two-bladed rotors the asymmetric load transfer can be accounted for by connecting the blades through a teeter hinge to the shaft. By mounting the axis of the hinge perpendicular to both the shaft and the blade axes, the blades are able to teeter and the load transfer from the blades to the shaft is reduced (Burton et al., 2001).

While a teeter hinge is one option to mitigate the load, also active load reduction mechanisms are widely applied in commercial wind turbines to reduce (fatigue) loads (Burton et al., 2001; Bossanyi, 2000, 2003, 2005; Bossanyi et al., 2013). This is, for example, motivated by the fact that due to the increasing size of wind turbines, the load differences across the rotor plane increase. In order to handle these loads, the blades are pitched such that the loads in the blades (and other parts of the wind turbine) are reduced. Moreover, it is demonstrated in Bossanyi et al. (2013; Bossanyi and Wright (2009); Bossanyi et al. (2010) that Individual Pitch Control (IPC) can be used as an alternative to a mechanical teeter hinge.

The typical IPC approach to reduce the loads in wind turbines (Bossanyi, 2003, 2005) is to transform the measured blade loads to two decoupled SISO control loops, subsequently apply control action and reverse transform the obtained control signals so as to obtain the individual pitch demands. The underlying transformations map the measured blade loads from a rotating frame of reference to a fixed non-rotating frame of reference and vice versa. The reason to include these transformations is that the non-rotating signals are decoupled and, this makes control design relatively simple. The
transformations are also used in electrical machine theory (Park, 1929), where the non-rotating frame of reference is a two-axis system called the d-q axis (the so-called ‘direct’ and ‘quadrature’ axes), and in helicopter theory (Coleman and Feingold, 1958; Johnson, 1994). More recently, the transformations are applied in wind turbine control (Bossanyi, 2003, 2005; Bir, 2008).

In the past decade, a considerable amount of articles have appeared on IPC, of which the work in Bossanyi (2003, 2005); Bossanyi et al. (2013); Bossanyi and Wright (2009); Bossanyi et al. (2010) has already been mentioned. To mention a few, in Kanev and van Engelen (2009), IPC is extended to compensate for rotor imbalances due to blade imperfections (i.e., aerodynamic and mass imbalances) and higher harmonics pitch control is presented in van Engelen (2009). Moreover, anti-windup elements are added so as to deal with blade pitch actuator limitations (Kanev and van Engelen, 2009). A two degree of freedom approach including feedback and feedforward control has been applied to IPC in Selvam et al. (2009). The feedforward controller is based on a wind speed estimator to provide load reduction caused by low-frequency components of the wind. The feedback loop consists of a Linear Quadratic Controller (LQR) minimizing the yaw and tilt moments. Another two degree of freedom approach involving learning control is presented in Houtzager et al. (2013). In this latter reference, deterministic blade loads, i.e., loads due to wind shear and tower shadow, are reduced by means of a repetitive feedforward controller. The stochastic loads are reduced by a typical feedback loop. A multi-objective IPC approach is outlined in Geyler and Caselitz (2008) where an $H_{\infty}$ control optimization problem is formulated. Finally, in Wright et al. (2009); Wright and Stol (2010); Wright et al. (2011) a multi-input multi-output controller has been designed using advanced state-space control methods in order to mitigate wind turbine loads. The latter controller has been implemented and tested on a two-bladed wind turbine.

To a large extent, the previous citations in the context of IPC either directly or indirectly address three-bladed wind turbines. Although the techniques and transformations used for three-bladed rotors can be generalized to a rotor having any number of blades (Bossanyi and Wright, 2009; Bir, 2008), this chapter focuses mainly on IPC for two-bladed wind turbines. More specifically, the contribution of this chapter is fourfold:

1. An overview of the fundamental MBC transformation for IPC of two- and three-bladed wind turbines is given;
2. It is shown that if the MBC transformation used for IPC of three-bladed wind turbines is applied to two-bladed wind turbines, the transformation is singular;
3. A linear and non-singular coordinate transformation for Linear Individual Pitch Control (LIPC) of two-bladed wind turbines is proposed;
4. The controller design for LIPC of two-bladed wind turbines with the linear coordinate transform is outlined.

The last contribution is motivated by the fact that the linear non-singular coordinate transformation requires a different control design compared to the control design with the conventional coordinate transformation.

The chapter is organized as follows. In Section 2.2, the typical IPC approach is reviewed. The MBC transformation is investigated both in its general form as well as the
special cases of three-bladed and two-bladed rotors. Also, the distribution of the signal harmonics in the rotating and non-rotating frames of reference due to the MBC transformations are listed. Then, in Section 2.3 the linear coordinate transformation for LIPC of two-bladed rotors is presented. Subsequently, the simulation environment and the description of a two-bladed wind turbine, which are used to evaluate the IPC based on the proposed coordinate transformation, are described in Section 2.4. In this section the controller design for IPC with the linear coordinate transformation is also outlined. Finally, the performance of the LIPC for two-bladed wind turbines is compared to the conventional IPC approach by means of a simulation study in Section 2.5. The conclusions are formulated in Section 2.6.

2.2. CONVENTIONAL INDIVIDUAL PITCH CONTROL

The control system of a commercial wind turbine typically consists of a number of independent feedback loops. First of all, in the below-rated operating region, a torque controller is active to regulate the generator torque $T_{\text{gen}}$, thereby changing the rotor speed in order to maximize the power output. In the above-rated operating region, Collective Pitch Control (CPC) makes sure that the rated rotational speed $\Omega_{\text{gen, rated}}$ is maintained by collectively pitching the blades. Furthermore, IPC takes the measured out-of-plane blade root moments ($M_{y,1}, M_{y,2}, M_{y,3}$) as inputs and generates individual pitch demands ($\theta_1, \theta_2, \theta_3$) in order to reduce the blade loads. The collective pitch angle $\theta_{\text{col}}$ is added to these individual pitch demands to obtain the final blade pitch angles ($\Theta_1, \Theta_2, \Theta_3$). The typical block scheme of a wind turbine control system is depicted in Figure 2.1. In addition to the aforementioned controllers, drivetrain damping and tower damping in the fore-aft and side-side directions could be added. However, as we are mainly interested in IPC in this thesis, we do not further consider these controllers.

The conventional approach for IPC of three-bladed rotors is to transform the blade root moments, measured in a rotating frame of reference, to a non-rotating frame of reference. To generate individual pitch demands, controllers are designed in the non-rotating frame and the resulting non-rotating pitch demands are reverse transformed to the rotating frame where they are sent to the pitch actuators. The involved coordinate transformation is often referred to as the Multi-Blade Coordinate transformation (Bir, 2008; Hohenemser and Yin, 1972), the Coleman transformation (Coleman and Feingold, 1958), the Fourier Coordinate Transform (Johnson, 1994) and the Park transformation (Park, 1929). From here on we will use “MBC transformation” to refer to these transformations. The interested reader is referred to Stol et al. (2009) for a comparison between MBC transformations and direct periodic techniques for wind turbine control. Finally, note that in Figure 2.1 the IPC block includes the forward and reverse coordinate transformations.

In the subsequent part of this section, IPC for both three-bladed and two-bladed rotors is reviewed. More specifically, first the MBC for any number of blades is discussed in Section 2.2.1, the typical IPC approach is described in Section 2.2.2 and then the special cases for three-bladed and two-bladed rotors are analysed in Section 2.2.3 and Section 2.2.4, respectively.
2.2.1. MULTI-BLADE COORDINATE TRANSFORMATION

As mentioned before, IPC of wind turbines involves a coordinate transformation that brings the measured blade loads from a rotating frame of reference to a fixed non-rotating frame of reference. This signal transformation involves the following identity (Johnson, 1994)

\[
q_0 = \frac{1}{B} \sum_{b=1}^{B} q^{(b)}, \\
q_{nc} = \frac{2}{B} \sum_{b=1}^{B} q^{(b)} \cos(n\psi_b), \\
q_{ns} = \frac{2}{B} \sum_{b=1}^{B} q^{(b)} \sin(n\psi_b), \\
q_{B/2} = \frac{1}{B} \sum_{b=1}^{B} q^{(b)} (-1)^b, \quad \text{(only for } B \text{ even)}
\]

with \( B \) the total number of blades, \( b \) the blade number, \( q^{(b)} \) the rotating signals (e.g., the measured blade root moments), \( \psi_b \) the blade azimuth angle, and \( n \) the harmonic number. The reverse transformation, to go from the fixed non-rotating frame of reference...
back to the rotating frame of reference, involves

\[ q^{(b)} = q_0 + \sum_{n} (q_{nc} \cos(n\psi_b) + q_{ns} \sin(n\psi_b)) + q_{B/2}(-1)^b, \tag{2.5} \]

where the summation goes from \( n = 1 \) to \( n = (B - 1)/2 \) for \( B \) odd and from \( n = 1 \) to \( n = (B - 2)/2 \) for \( B \) even.

The variable \( q^{(b)} \) represents the motion of an individual blade \( b \) in the rotating frame, whereas the variables \((q_0, q_{nc}, q_{ns}, \ldots, q_{B/2})\) describe the motion of the rotor in the non-rotating frame (Johnson, 1994) as a whole. The interested reader is referred to Johnson (1994) for more details and proofs.

### 2.2.2. Individual Pitch Control

In IPC, the measured blade loads \((M_{y1}, M_{y2}, \ldots, M_{yB})\) are transformed from the rotating domain to the non-rotating domain by using (2.1)-(2.4), which can alternatively be written in matrix form

\[
\begin{bmatrix}
M_0 \\
M_{nc} \\
M_{ns} \\
M_{B/2}
\end{bmatrix} = \frac{2}{B} \begin{bmatrix}
1/2 & 1/2 & \cdots & 1/2 \\
\cos(n\psi_1) & \cos(n\psi_2) & \cdots & \cos(n\psi_B) \\
\sin(n\psi_1) & \sin(n\psi_2) & \cdots & \sin(n\psi_B) \\
-1/2 & 1/2 & \cdots & (-1)^{B/2}
\end{bmatrix} \begin{bmatrix}
M_{y1} \\
M_{y2} \\
\vdots \\
M_{yB}
\end{bmatrix}, \tag{2.6}
\]

where in the notation \( q \) is replaced by \( M \). By rewriting the azimuths of each blade into the azimuth angle \( \psi \) of the rotor, i.e., \( \psi_b = \psi + 2\pi(b - 1)/B \), (2.6) becomes

\[
\begin{bmatrix}
M_0 \\
M_{nc} \\
M_{ns} \\
M_{B/2}
\end{bmatrix} = \frac{2}{B} \begin{bmatrix}
1/2 & 1/2 & \cdots & 1/2 \\
\cos(n\psi) & \cos(n[\psi + 2\pi/B]) & \cdots & \cos(n[\psi + 2\pi(B - 1)/B]) \\
\sin(n\psi) & \sin(n[\psi + 2\pi/B]) & \cdots & \sin(n[\psi + 2\pi(B - 1)/B]) \\
-1/2 & 1/2 & \cdots & (-1)^{B/2}
\end{bmatrix} \begin{bmatrix}
M_{y1} \\
M_{y2} \\
\vdots \\
M_{yB}
\end{bmatrix}. \tag{2.7}
\]

After transforming the measured signals \((M_{y1}, M_{y2}, \ldots, M_{yB})\) to the fixed non-rotating domain, the next step is to apply a PI controller (e.g., by using loop shaping techniques) to each of the cyclic modes \((M_{nc}, M_{ns})\) in order to obtain the pitch angles \((\theta_{nc}^*, \theta_{ns}^*)\) in the non-rotating domain. Then, the pitch signals \((\theta_{nc}^*, \theta_{ns}^*)\) are reverse transformed to obtain the pitch signals \((\theta_1, \theta_2, \ldots, \theta_B)\) in the rotating domain by applying the reverse transformation

\[
\begin{bmatrix}
\theta_1 \\
\theta_2 \\
\vdots \\
\theta_B
\end{bmatrix} = \begin{bmatrix}
1 & \cos(n\psi) & \sin(n\psi) & -1 \\
1 & \cos(n[\psi + 2\pi/B]) & \sin(n[\psi + 2\pi/B]) & 1 & \theta_0^* \\
\vdots & \cdots & \cdots & \cdots & \cdots & \cdots & \theta_{nc}^* \\
1 & \cos(n[\psi + 2\pi(B - 1)/B]) & \sin(n[\psi + 2\pi(B - 1)/B]) & (-1)^B & \theta_{ns}^* \\
\end{bmatrix}, \tag{2.8}
\]

which is obtained from (2.5). The aforementioned approach is schematically shown in Figure 2.2.

In the above equations, the harmonic number \( n \) is directly related to the periodic loadings present in a wind turbine. For example, a rotor blade experiences a load increase due to passing the turbine tower (i.e., tower shadow). As a result, the measured
load signals contain a once-per-revolution load (1P load). Likewise, the turbine tower itself experiences an \( nP \) load, where \( n \) is determined by the number of blades due to each blade passing the tower. From here on, we will frequently use the notation \( nP \) to indicate periodic frequencies. Due to the transformations of (2.7) and (2.8), the pitch signals in the rotating domain have dominant activity at the \( nP \) component. Note that sometimes the measured blade loads \( (M_{y,1}, M_{y,2}, \ldots, M_{y,B}) \) are first passed through a pre-filter to filter the \( n' \)th harmonic frequency (Houtzager et al., 2013). Another approach is to filter unwanted harmonics from the fixed non-rotating reference frame by extending the PI controller with notch filters. Furthermore, to eliminate any high frequent activity to be passed on to the pitch actuators, a low-pass filter (denoted by \( \mathcal{L} \) in Figure 2.2) is applied to each pitch signal after the reverse transformation.

The above outlined approach should be carried out for every desired \( nP \) load that one wants to reduce. Then, for every harmonic number \( n \), the blade pitches are obtained and added to the collective pitch angle so as to obtain the final pitch demands for the pitch actuators (see Figure 2.1).

### 2.2.3. MBC for Three-bladed Rotors

For IPC typically the modes \( q_0 \) and \( q_{B/2} \) (where the mode \( q_{B/2} \) is only present for \( B \) even) are discarded and only the cyclic modes \( (q_{nc}, q_{ns}) \) are considered. Hence, neglecting the modes \( M_0 \) and \( M_{B/2} \) in (2.7) and (2.8), gives the forward MBC transformation for three-bladed rotors

\[
\begin{bmatrix}
  M_{nc} \\
  M_{ns}
\end{bmatrix} = \frac{2}{3} \begin{bmatrix}
  \cos(n\psi) & \cos(n[\psi + 2\pi/3]) & \cos(n[\psi + 4\pi/3]) \\
  \sin(n\psi) & \sin(n[\psi + 2\pi/3]) & \sin(n[\psi + 4\pi/3])
\end{bmatrix} \begin{bmatrix}
  M_{y,1} \\
  M_{y,2} \\
  M_{y,3}
\end{bmatrix}
\]

and its corresponding reverse MBC transformation

\[
\begin{bmatrix}
  \theta_1 \\
  \theta_2 \\
  \theta_3
\end{bmatrix} = \begin{bmatrix}
  \cos(n\psi) & \sin(n\psi) \\
  \cos(n[\psi + 2\pi/3]) & \sin(n[\psi + 2\pi/3]) \\
  \cos(n[\psi + 4\pi/3]) & \sin(n[\psi + 4\pi/3])
\end{bmatrix} \begin{bmatrix}
  \theta_{nc}^* \\
  \theta_{ns}^*
\end{bmatrix}.
\]

To see how the periodic frequencies in the signals are transferred from the rotating frame of reference to the non-rotating frame of reference and vice versa, consider Table 2.1. In
this table the periodic frequency distributions are shown for the 1P and 2P transformations, i.e., the transformation matrices in (2.9) and (2.10) with \( n = 1 \) and \( n = 2 \). The results are obtained by considering the following rotating artificial sinusoidal signals

\[
M_{y1} = M_a \left[ \cos(j \psi) + \sin(j \psi) \right], \\
M_{y2} = M_b \left[ \cos(2j \psi + 2\pi/3) + \sin(j \psi + 2\pi/3) \right], \\
M_{y3} = M_c \left[ \cos(j \psi + 4\pi/3) + \sin(j \psi + 4\pi/3) \right],
\]

which are linear combinations of a sine and a cosine, effectively yielding a sine with a certain amplitude and phase. The forward transformation in (2.9) with \( n = 1, 2 \) is then used to map the signals of (2.11)-(2.13) for \( j = 0, \ldots, 4 \) to the fixed non-rotating system. The analysis is carried out for the case in which \( M_a = M_b = M_c \) and for the case in which \( M_a \neq M_b \neq M_c \). To analyse the frequency mappings from the non-rotating domain to the rotating domain, consider the following artificial non-rotating signals

\[
\theta^*_{jc} = \theta_a \left[ \cos(j \psi) + \sin(j \psi) \right], \\
\theta^*_{js} = \theta_b \left[ \sin(j \psi) - \cos(j \psi) \right],
\]

and

\[
\theta^*_{jc} = \theta_a \left[ \cos(j \psi) + \sin(j \psi) \right], \\
\theta^*_{js} = \theta_b \left[ \cos(j \psi) - \sin(j \psi) \right],
\]

which were found in the analysis of the forward transformation described above. The signals of each pair, i.e., (2.14)-(2.15) and (2.16)-(2.17), have a phase difference of 90° and as a consequence of the phase difference between (2.15) and (2.17), the signal pairs (assuming \( \theta_a = \theta_b \)) appear at different harmonic frequencies after applying the reverse MBC transformation of (2.10). More specifically, the signal pair (2.14)-(2.15) is transformed to the \( j - n \) frequency and the signal pair (2.16)-(2.17) is transformed to the \( j + n \) frequency in the rotating frame of reference. The analysis of the reverse transformation is carried out for the case in which \( \theta_a = \theta_b \) and for the case in which \( \theta_a \neq \theta_b \).

Considering the viewpoint of a single blade, the tower passing frequency is 1P; hence, due to tower shadow and wind shear, it is well-known that a peak around the 1P frequency is observed in the blade load signals. From Table 2.1 it is seen that passing such a signal through the 1P forward MBC transformation of (2.9), results in dominant 0P signal components in the non-rotating frame. Therefore, applying proportional and integral action on the 0P frequencies in the non-rotating domain, i.e., on the static signal component, results after passing through the reverse MBC transformation of (2.10) in 1P pitch action in the rotating frame.

### 2.2.4. MBC for Two-bladed Rotors

According to Johnson (1994), the only mathematically sound coordinate transformation for two-bladed rotors is determined by the modes \( M_0 \) and \( M_1 \) in (2.7)-(2.8). Despite this, the typical approach of IPC for two-bladed wind turbines (e.g., see Bossanyi et al. (2013); Bossanyi and Wright (2009); Bossanyi et al. (2010)) involves the cyclic modes \( M_{nc} \)
Table 2.1: Harmonic frequency mappings of the MBC transformation for $B = 3$. A ‘-’ indicates that the signal component disappears after the transformation, a ‘+’ indicates that the signal component appears at the indicated frequencies and a ‘/’ indicates that the signal component appears on either of the indicated frequencies depending on the signals defined in (2.14)-(2.15) (left of ‘/’) and (2.16)-(2.17) (right of ‘/’).

<table>
<thead>
<tr>
<th>Transformation</th>
<th>Load balance</th>
<th>Signal component: ( j P ) load</th>
</tr>
</thead>
<tbody>
<tr>
<td>Forward 1P (rotating to non-rotating)</td>
<td>( M_a = M_b = M_c )</td>
<td>0P</td>
</tr>
<tr>
<td>Forward 1P (rotating to non-rotating)</td>
<td>( M_a \neq M_b \neq M_c )</td>
<td>1P</td>
</tr>
<tr>
<td>Reverse 1P (non-rotating to rotating)</td>
<td>( \theta_a = \theta_b )</td>
<td>1P</td>
</tr>
<tr>
<td>Reverse 1P (non-rotating to rotating)</td>
<td>( \theta_a \neq \theta_b )</td>
<td>1P</td>
</tr>
<tr>
<td>Forward 2P (rotating to non-rotating)</td>
<td>( M_a = M_b = M_c )</td>
<td>-</td>
</tr>
<tr>
<td>Forward 2P (rotating to non-rotating)</td>
<td>( M_a \neq M_b \neq M_c )</td>
<td>2P</td>
</tr>
<tr>
<td>Reverse 2P (non-rotating to rotating)</td>
<td>( \theta_a = \theta_b )</td>
<td>2P</td>
</tr>
<tr>
<td>Reverse 2P (non-rotating to rotating)</td>
<td>( \theta_a \neq \theta_b )</td>
<td>2P</td>
</tr>
</tbody>
</table>

and \( M_{ns} \). For that reason, an analysis of the typically used MBC transformation for two-bladed rotors is given here.

Considering (2.7) and (2.8) for two blades, this translates to the following forward transformation

\[
\begin{bmatrix}
M_0 \\
M_{nc} \\
M_{ns} \\
M_1 
\end{bmatrix}
= 
\begin{bmatrix}
\frac{1}{2} & \frac{1}{2} \\
\cos(n\psi) & \cos(n(\psi + \pi)) \\
\sin(n\psi) & \sin(n(\psi + \pi)) \\
-\frac{1}{2} & \frac{1}{2} 
\end{bmatrix}
\begin{bmatrix}
M_{y,1} \\
M_{y,2} 
\end{bmatrix}
\]

and reverse transformation

\[
\begin{bmatrix}
\theta_1 \\
\theta_2 
\end{bmatrix}
= 
\begin{bmatrix}
1 & \cos(n\psi) & \sin(n\psi) & -1 \\
1 & \cos(n(\psi + \pi)) & \sin(n(\psi + \pi)) & 1 
\end{bmatrix}
\begin{bmatrix}
\theta^*_0 \\
\theta^*_{nc} \\
\theta^*_{ns} \\
\theta^*_1 
\end{bmatrix}.
\]

Neglecting the modes \( M_0 \) and \( M_1 \) gives the forward MBC transformation for two-bladed rotors

\[
\begin{bmatrix}
M_{nc} \\
M_{ns} 
\end{bmatrix}
= 
\begin{bmatrix}
\cos(n\psi) & \cos(n(\psi + \pi)) \\
\sin(n\psi) & \sin(n(\psi + \pi)) 
\end{bmatrix}
\begin{bmatrix}
M_{y,1} \\
M_{y,2} 
\end{bmatrix}
\]

(2.18)

and the corresponding reverse MBC transformation

\[
\begin{bmatrix}
\theta_1 \\
\theta_2 
\end{bmatrix}
= 
\begin{bmatrix}
\cos(n\psi) & \sin(n\psi) \\
\cos(n(\psi + \pi)) & \sin(n(\psi + \pi)) 
\end{bmatrix}
\begin{bmatrix}
\theta^*_{nc} \\
\theta^*_{ns} 
\end{bmatrix}.
\]

(2.19)

In (2.18) the non-rotating cyclic modes \( M_{nc} \) and \( M_{ns} \) are determined, however these modes do not uniquely exist for two-bladed rotors\(^1\). To see this, consider the transformation matrix in (2.18) for \( n = 1 \), i.e.,

\[
\begin{bmatrix}
\cos(n\psi) & \cos(n(\psi + \pi)) \\
\sin(n\psi) & \sin(n(\psi + \pi)) 
\end{bmatrix}
= 
\begin{bmatrix}
\cos(\psi) & -\cos(\psi) \\
\sin(\psi) & -\sin(\psi) 
\end{bmatrix}.
\]

(2.20)

\(^1\)This also occurs for the transformation of three-bladed rotors in (2.9)-(2.10) for \( n = 3 \).
From (2.20), one readily observes that this matrix is singular. Also, the reverse transformation matrix in (2.19) for \( n = 1 \), i.e.,

\[
\begin{bmatrix}
\cos(n\psi) & \sin(n\psi) \\
\cos(n(\psi + \pi)) & \sin(n(\psi + \pi))
\end{bmatrix}
= \begin{bmatrix}
\cos(\psi) & \sin(\psi) \\
-\cos(\psi) & -\sin(\psi)
\end{bmatrix},
\]

is singular. This means that the two linear combinations determined from the measured signals in (2.18) do not provide extra information to describe the motion of the rotor in the non-rotating frame compared with the information that one would obtain with only one of the linear combinations. In other words, instead of having two SISO controllers as in Bossanyi and Wright (2009), only one SISO controller can achieve the same. For that reason, in Section 2.3 a non-singular coordinate transformation for two-bladed rotors is proposed.

For completeness, we have included, as was previously done for the three-bladed case, an analysis of the frequency content mapping from the rotating frame of reference to the non-rotating frame of reference and vice versa. For the rotating signals, consider the following artificial sinusoidal signals representing the blade loads of a two-bladed rotor

\[
M_{y,1} = M_a \left[ \sin(j\psi) + \cos(j\psi) \right],
\]

\[
M_{y,2} = M_b \left[ \sin(j(\psi + \pi)) + \cos(j(\psi + \pi)) \right].
\]

To obtain the signals in the non-rotating frame of reference, (2.22)-(2.23) are multiplied by the transformation given in (2.18). The rotating signals are considered for the harmonic number \( j = 0, \ldots, 4 \) and the 1P and 2P transformations of (2.18) are considered by choosing \( n = 1 \) and \( n = 2 \), respectively. The cases in which \( M_a = M_b \) and \( M_a \neq M_b \) are separately considered. To obtain the results for the reverse transformation, i.e., to go from the non-rotating frame of reference to the rotating frame of reference, the following artificial signals are considered

\[
\theta_0^* = \theta_a \left[ \cos(j\psi) + \sin(j\psi) \right],
\]

\[
\theta_1^* = \theta_b \left[ \cos(j\psi) - \sin(j\psi) \right],
\]

which have a phase difference of 90°. The latter phase difference was found by observing the results from transforming the rotating signals (2.22)-(2.23) to the non-rotating frame of reference. Furthermore, also the non-rotating signals

\[
\theta_0^* = \theta_a \left[ \cos(j\psi) - \sin(j\psi) \right],
\]

\[
\theta_1^* = \theta_b \left[ \cos(j\psi) + \sin(j\psi) \right],
\]

were found in the above analysis. The difference between (2.24)-(2.25) and (2.26)-(2.27), with the assumption of \( \theta_a = \theta_b \), is that after transforming with (2.19), the signal pairs either appear at the \( j + n \) or \( j - n \) harmonic, respectively. Because of this difference, both signal pairs are included in the analysis. The non-rotating signals in (2.24)-(2.27) are considered for the harmonic numbers \( j = 0, \ldots, 4 \), both the 1P and 2P reverse transformations are considered by respectively setting \( n = 1 \) and \( n = 2 \) in (2.20)-(2.21) and the cases of \( \theta_a = \theta_b \) and \( \theta_a \neq \theta_b \) are considered. The results are outlined in Table 2.2.
Table 2.2: Harmonic frequency mappings of the MBC transformation for $B = 2$. A ‘−’ indicates that the signal component disappears after the transformation, a ‘+’ indicates that the signal component appears at the indicated frequencies and a ‘/’ indicates that the signal component appears on either of the indicated frequencies depending on the signals defined in (2.24)-(2.25) (left of ‘/’) and (2.26)-(2.27) (right of ‘/’).

<table>
<thead>
<tr>
<th>Transformation</th>
<th>Load balance</th>
<th>Signal component: $jP$ load</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0P</td>
<td>1P</td>
</tr>
<tr>
<td>Forward 1P (rotating to non-rotating)</td>
<td>$M_a = M_b$</td>
<td>- 0P+2P</td>
</tr>
<tr>
<td>Forward 1P (rotating to non-rotating)</td>
<td>$M_a \neq M_b$</td>
<td>1P 0P+2P 1P+3P 2P+4P 3P+5P</td>
</tr>
<tr>
<td>Reverse 1P (non-rotating to rotating)</td>
<td>$\theta_a = \theta_b$</td>
<td>1P 2P / 0P 3P / 1P 4P / 2P 5P / 3P</td>
</tr>
<tr>
<td>Reverse 1P (non-rotating to rotating)</td>
<td>$\theta_a \neq \theta_b$</td>
<td>1P 0P+2P 1P+3P 2P+4P 3P+5P</td>
</tr>
<tr>
<td>Forward 2P (rotating to non-rotating)</td>
<td>$M_a = M_b$</td>
<td>2P - 0P+4P - 2P+6P</td>
</tr>
<tr>
<td>Forward 2P (rotating to non-rotating)</td>
<td>$M_a \neq M_b$</td>
<td>2P 1P+3P 0P+4P 1P+5P 2P+6P</td>
</tr>
<tr>
<td>Reverse 2P (non-rotating to rotating)</td>
<td>$\theta_a = \theta_b$</td>
<td>2P 3P / 1P 4P / 0P 5P / 1P 6P / 2P</td>
</tr>
<tr>
<td>Reverse 2P (non-rotating to rotating)</td>
<td>$\theta_a \neq \theta_b$</td>
<td>2P 1P+3P 0P+4P 1P+5P 2P+6P</td>
</tr>
</tbody>
</table>

### 2.3. Linear Individual Pitch Control

In the previous section, the conventional IPC approach is reviewed and the important frequency mappings for the loads at different periodic frequencies between the non-rotating and rotating domains are given. These mappings provide valuable insight to design appropriate controllers for both two- and three-bladed wind turbines. However, it is observed that the transformation matrices in (2.18) and (2.21) have a singularity and therefore the non-rotating signals $M_{nc}$ and $M_{ns}$ are not uniquely defined. In this section a linear non-singular coordinate transformation for two-bladed rotors is considered.

In Johnson (1994) it is stated that the reactionless mode $q_{B/2}$ of (2.4) replaces the cyclic modes $q_{nc}$ and $q_{ns}$ and couples with the fixed system. This means that the set of (2.1)-(2.4) reduces to (2.1) and (2.4). Rewriting the latter two equations into vector notation (and using $M$ instead of $q$) yields

$$\begin{bmatrix} M_0 \\ M_1 \end{bmatrix} = \begin{bmatrix} 1/2 & 1/2 \\ -1/2 & 1/2 \end{bmatrix} \begin{bmatrix} M_{y,1} \\ M_{y,2} \end{bmatrix}. \quad (2.28)$$

So, for two-bladed rotors we have a collective mode $M_0$ (coning mode) and a reactionless differential mode $M_1$ (teetering mode). Consequently, the corresponding reverse transformation is given by

$$\begin{bmatrix} \theta_1 \\ \theta_2 \end{bmatrix} = \begin{bmatrix} 1 & -1 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} \theta_0^* \\ \theta_1^* \end{bmatrix}. \quad (2.29)$$

Note that this coordinate transformation is uniquely defined and independent of the rotor azimuth angle. The non-rotating signals are obtained purely by summation and subtraction of the measured blade load signals. Further analysis of the transformation matrices in (2.28) and (2.29) shows the following interesting property. Consider the blade load signals of (2.22) and (2.23) with $j = 1$

$$M_{y,1} = M_a \left[ \cos(\psi) + \sin(\psi) \right],$$

$$M_{y,2} = M_b \left[ \cos(\psi + \pi) + \sin(\psi + \pi) \right] = -M_b \left[ \cos(\psi) + \sin(\psi) \right],$$
with the assumption that $M_a = M_b$. Transforming these load signals to the non-rotating domain by (2.28) gives

$$
\begin{bmatrix}
M_0 \\
M_1
\end{bmatrix} =
\begin{bmatrix}
1/2 & 1/2 \\
-1/2 & 1/2
\end{bmatrix}
\begin{bmatrix}
\cos(\psi) + \sin(\psi) \\
-\cos(\psi) - \sin(\psi)
\end{bmatrix} =
\begin{bmatrix}
0 \\
-\cos(\psi) - \sin(\psi)
\end{bmatrix}.
$$

From (2.30) it is recognized that the 1P load only appears in the differential mode $M_1$. In practice the measured blade load also contains higher order harmonics. Hence, to see how the forward transformation affects for example a 2P blade load periodic, consider again the signals of (2.22) and (2.23) with $j = 2$

$$
\begin{align*}
M_{y,1} &= M_a \left[ \cos(2\psi) + \sin(2\psi) \right], \\
M_{y,2} &= M_b \left[ \cos(2(\psi + \pi)) + \sin(2(\psi + \pi)) \right] = M_b \left[ \cos(2\psi) + \sin(2\psi) \right].
\end{align*}
$$

Similarly, transforming (2.31) and (2.32) to the non-rotating domain by (2.28) results in

$$
\begin{bmatrix}
M_0 \\
M_1
\end{bmatrix} =
\begin{bmatrix}
1/2 & 1/2 \\
-1/2 & 1/2
\end{bmatrix}
\begin{bmatrix}
\cos(2\psi) + \sin(2\psi) \\
\cos(2\psi) + \sin(2\psi)
\end{bmatrix} =
\begin{bmatrix}
\cos(2\psi) + \sin(2\psi) \\
0
\end{bmatrix}.
$$

Hence, the 2P periodic is only present in the collective mode $M_0$. Extending the previous results to higher order harmonics, i.e., by considering $jP$ for $j = 1, 2, 3, \ldots$, leads to the following observation:

- For $j$ odd, the harmonics appear in the differential mode $M_1$;
- For $j$ even, the harmonics appear in the collective mode $M_0$.

These analytical results are supported by simulations carried out in the wind turbine design software Bladed (see Section 2.4 for details of this software package). The forward transformation (2.28) is applied to the measured blade loads ($M_{y,1}, M_{y,2}$) obtained from the NREL CART2 two-bladed wind turbine\textsuperscript{2}, which is described in Section 2.4, for a turbulent wind field with mean wind speed 18 m s\textsuperscript{-1} and turbulence intensity $I_T = 6\%$. The control system of Figure 2.1 and Figure 2.2 is used, where, in the latter figure, the coordinate transformations are replaced by (2.28) and (2.29), and the inputs to the reverse transformation in Figure 2.2 are left unconnected. The signals in both the rotating and the non-rotating domains of the turbine are logged. Then, by computing the power spectral densities of the logged signals, the frequency content is analysed. In Figure 2.3a and Figure 2.3b, the power spectral densities of the rotating Out-of-Plane (OoP) blade root moments $M_{y,1}$ and $M_{y,2}$ are shown and the first six periodic frequencies are indicated by the arrows. In Figure 2.3c and Figure 2.3d, the non-rotating modes $M_0$ and $M_1$ are shown. Clearly, the odd periodic frequencies are transformed to the differential mode $M_1$ and the even periodic frequencies are transformed to the collective mode $M_0$.

To conclude this section, some interesting properties of the linear coordinate transformation are discussed. In the previous part of this section it is outlined that (2.28) maps

\textsuperscript{2}The NREL CART2 wind turbine has a rated rotational speed of 41.7 rpm, which means that the 1P loads are at 0.695 Hz.
2.4. Controller design for IPC

The conventional IPC approach involves two decoupled PI controlled SISO loops. These loops can be independently designed using classical control design tools but typically have identical control parameters. Similarly, it is shown in this section that the control
loops, determined by the linear coordinate transformation, are almost decoupled, so that again SISO design techniques can be applied. The control design requires a model of the dynamics from the individual pitch angles to the blade loads. To this end, descriptions of the software package and turbine specifications which we will use are given in Section 2.4.1. The software package, the specified wind turbine, and a baseline controller, which is described in Section 2.4.2, are required in order to deduce a model from input-output data by means of system identification. The details of the system identification procedure are briefly discussed in Section 2.4.3. Finally, the design steps for the LIPCs and the conventional IPC are outlined in Section 2.4.4 and Section 2.4.5, respectively.

2.4.1. SIMULATION ENVIRONMENT AND TWO-BLADED WIND TURBINE

To simulate the dynamics of the wind turbine in terms of individual pitch angles and blade loads, various software packages are available. We chose GH Bladed 4.00 (Garrad Hassan, 2013; Garrad Hassan & Partners Ltd, 2013), which is a certified wind turbine design software package widely used in industry and by researchers making it a representative and reliable environment. Furthermore, Bladed allows the testing of new control algorithms, i.e., controllers can be designed in MATLAB Simulink® (Mathworks, 2013) after which an automated script converts the Simulink® model to an equivalent C code and subsequently a DLL file is compiled (Houtzager, 2011). The DLL file is then read by Bladed as an external controller.

In addition to the simulation environment, a representative two-bladed wind turbine description is also required. To this end, the National Renewable Energy Laboratory (NREL) Controls Advanced Research Turbine 2 (CART2) turbine is considered. The CART2 turbine is located at NREL’s National Wind Technology Center and is specifically configured to enable field-testing of advanced control algorithms (Bossanyi et al., 2010; Fingersh and Johnson, 2004). It is a two-bladed onshore upwind turbine with a teetering hub (switched off during all simulations), variable speed and pitch control. The maximum electrical rated power output is 660 kW\(^3\). The important specifications of the turbine are listed in Table 2.3.

\(^3\)In our simulations the rated output power is set to 570 kW (Bossanyi et al., 2010).

---

<table>
<thead>
<tr>
<th>Description</th>
<th>Symbol</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rated power</td>
<td>(P_{\text{rated}})</td>
<td>660 kW</td>
</tr>
<tr>
<td>Rotor diameter</td>
<td>(d_{\text{ro}})</td>
<td>42.672 m</td>
</tr>
<tr>
<td>Hub height</td>
<td>(h_{\text{hub}})</td>
<td>36.8497 m</td>
</tr>
<tr>
<td>Cut-in wind speed</td>
<td>(v_{\text{cutin}})</td>
<td>4 m s(^{-1})</td>
</tr>
<tr>
<td>Rated wind speed</td>
<td>(v_{\text{rated}})</td>
<td>12.7 m s(^{-1})</td>
</tr>
<tr>
<td>Cut-out wind speed</td>
<td>(v_{\text{cutout}})</td>
<td>25 m s(^{-1})</td>
</tr>
<tr>
<td>Rated rotational rotor speed</td>
<td>(\Omega_{\text{ro}})</td>
<td>(2\pi 41.7/60) rad/s</td>
</tr>
<tr>
<td>Gearbox ratio</td>
<td>(\nu)</td>
<td>43.165</td>
</tr>
<tr>
<td>Pitch rate limit</td>
<td>(\theta_{\text{limit}})</td>
<td>18 deg s(^{-1})</td>
</tr>
</tbody>
</table>
2.4.2. Baseline controller

The CART2 turbine is a variable-speed pitch-controlled wind turbine and, hence, to operate properly in below- and above-rated wind conditions, it requires a torque controller and a CPC. The torque controller makes sure that in below-rated wind conditions the power is maximum and the CPC makes sure that the power is kept at its rated value in above-rated wind conditions. The combination of the torque and CPC is denoted in this chapter as the baseline controller and is schematically depicted in Figure 2.1. Note that the IPC in this diagram is not part of the baseline controller. The control design of the torque controller and the CPC follows the same procedure as is done for the well-known UPWIND 5MW reference turbine (Bossanyi and Witcher, 2009a,b). In order to switch between the below-rated and above-rated regions, logic rules are applied.

In the baseline controller design, notch filters are used to prevent certain turbine modes from being excited. That is, in both the torque controller as well as in the CPC, a notch filter is placed at the drivetrain resonance frequency to prevent heavy oscillations, which would in practice cause severe damage. Furthermore, to prevent the CPC from reacting to 2P frequencies, i.e., the blade passing frequency, also a notch filter at the 2P frequency is added. With the baseline controller a model for IPC design can be obtained, which is discussed next.

2.4.3. Obtaining a model for IPC design

Several options exist to obtain an appropriate model for control design. The main objective for a ‘good’ model for controller design is that it captures the relevant dynamics without requiring high complexity. One of the options in this particular case is system identification (van der Veen et al., 2013a). System identification is widely used and a readily accepted technique to acquire models from input-output data. In our particular case, we set up the configuration of Figure 2.4. The torque controller is not shown here, because the IPC is only designed to operate at above-rated wind conditions. The goal is to obtain a model from the individual pitch angles \( \theta^*_0, \theta^*_1 \) to the blade root moments \( M_0, M_1 \). Hence, by perturbing the individual pitch inputs \( \theta^*_i \) with appropriate excitation signals and measuring the response of the blade root moments \( M_i \), the dynamics in between can be modeled based on the measured input-output data. The system identification algorithm used here is the Optimized Predictor-Based Subspace IDentification (PBSID\textsubscript{opt}) method (van der Veen et al., 2013a).

The identification experiment is carried out in Bladed as follows. The CART2 wind turbine is subjected to a constant wind speed of 18 m s\(^{-1}\) without turbulence and all periodic loadings are switched off (e.g., gravity, wind shear, tower shadow). Note that because the wind speed is in the above-rated region, we can assume that the rotor speed is constant and that the blades have a certain pitch angle, determined by the CPC, in order to maintain the rated power. The inputs \( \theta^*_0, \theta^*_1 \) are chosen to be a Random Binary Signal (RBS), given by

\[
\theta^*_i(k) = c \cdot \text{sgn} \, w(k),
\]

where \( w(k) \) is a stochastic white noise sequence and \( c \) is a scalar which has a magnitude of 0.5°. The stochastic white noise sequence has a sample time of 0.2s. Hence, the RBS switches randomly from +0.5° to −0.5° and vice versa. To prevent high-frequent pitch
Figure 2.4: Schematic outline of the system identification scheme.

The PBSID_opt is carried out on a ten minute dataset containing 60000 samples. The Variance Accounted For (VAF) (Verhaegen and Verdult, 2007) is used as a measure to see how well the simulated outputs ($\hat{M}_0, \hat{M}_1$) of the identified model correspond to the measured outputs ($M_0, M_1$). The final selected model has an order of $n = 11$ and has a VAF of roughly 96% for the first output and roughly 93% for the second output, which is a satisfactory result. The Bode diagram of the identified system is given in Figure 2.5. In this figure also an 11th order PBSID_opt model, with approximately 95% VAF for output 1 and output 2, is shown for the case when no coordinate transformation is used, i.e., the system in Figure 2.4 from inputs ($\theta_1, \theta_2$) to outputs ($M_{y,1}, M_{y,2}$). With this figure the effect which the linear coordinate transformation has on the system can be analysed.

The most important conclusion based on the Bode diagrams shown in Figure 2.5 is that the coordinate transformation almost decouples the input-output pairs ($\theta_0^*, M_0$) and ($\theta_1^*, M_1$). This is seen from the fact that the off-diagonal transfer functions (Figure 2.5b and Figure 2.5c) have significantly lower magnitude for the case with the coordinate transformation. Quantitatively, at 0.01 Hz the difference between the diagonal and off-diagonal magnitudes is over 20 dB which is an absolute gain difference of more than 10 times. This is an important observation since it allows the controllers for the
2.4. CONTROLLER DESIGN FOR IPC

2.4.4. STRUCTURED $H_\infty$ CONTROL DESIGN FOR LINEAR IPC

The control design for IPC with the linear coordinate transformation given by (2.28) and (2.29) differs from the conventional IPC design and is therefore outlined here. It is observed in Figure 2.5 that the system is almost decoupled and, hence, the control design can be individually carried out for the odd and even harmonics. To reduce odd and even periodic loads simultaneously, the separate controllers can simply be combined. One advantage of the conventional IPC approach is that when only 0P signal components are present in the fixed non-rotating frame, this automatically yields smooth pitch activity in the rotating domain. With the LIPC approach, one has to manually make sure that only the appropriate frequencies are present in the rotating frame by using inverted notch filters.

Figure 2.5: Bode magnitude responses of the pitch angles to the blade moments. The solid lines represent the PBSIDopt model with coordinate transformation and the dashed lines represent the PBSIDopt model without coordinate transformation.

(a) From $\theta_{0}^*$ to $M_0$ (solid) and from $\theta_1$ to $M_{y,1}$ (dashed).
(b) From $\theta_{1}^*$ to $M_0$ (solid) and from $\theta_2$ to $M_{y,1}$ (dashed).
(c) From $\theta_{0}^*$ to $M_1$ (solid) and from $\theta_1$ to $M_{y,2}$ (dashed).
(d) From $\theta_{1}^*$ to $M_1$ (solid) and from $\theta_2$ to $M_{y,2}$ (dashed).

collective and differential modes to be independently designed by classical SISO loop shaping techniques.
In this chapter, three different LIPCs are designed:

- IPC for 1P loads (denoted by IPC-1P);
- IPC for 1P and 2P loads (denoted by IPC-1P-2P);
- IPC for 1P, 2P, and 3P loads (denoted by IPC-1P-2P-3P).

The IPC for the 1P loads (IPC-1P) and the IPC for the 1P and 3P loads (IPC-1P-3P) are designed using the identified transfer function from $\theta_1^*$ to $M_1$ (see Figure 2.5d). The IPC for 2P loads (IPC-2P) is designed using the identified transfer function from $\theta_0^*$ to $M_0$ (see Figure 2.5a).

As stated above, the designed controllers should only be active at the desired $nP$ frequencies. Such a controller design can be conducted in different ways. One way is to use classical loop shaping techniques (Skogestad and Postlethwaite, 2006) as was previously done in van Solingen and van Wingerden (2015). Another way to design the controller is to synthesize a full-order controller (Skogestad and Postlethwaite, 2006) with norm-based techniques. The disadvantage of such a design approach is that the obtained controller is of high order and the physical interpretation of the controller is lost. The latter makes the controller therefore difficult to fine-tune in the field. A third approach is to fix the structure of the controller on beforehand by using basic control blocks. These control blocks include low-pass filters, high-pass filters, and notch filters. Only the tunable controller parameters of these elements are then optimized to realize the objectives. For the purpose of LIPC, the control blocks as depicted in Figure 2.6 can be considered. This approach has previously been taken in van Solingen et al. (2014b); van Solingen and van Wingerden (2014) and is discussed in the next paragraphs.

The design of the IPC-1P-2P, consisting of the IPC-1P controller for the differential mode $M_1$ and the IPC-2P for the collective mode $M_0$, is outlined here. First of all, the IPC-1P involves a proportional gain $K_{1P}$ which reduces the magnitude of the open-loop system. Second, an inverted notch filter

$$NF_{\text{inv},1P}(s) = \frac{s^2 + 2\omega_{1P} \zeta_{1P} s + \omega_{1P}^2}{s^2 + 2\omega_{1P} \beta_{1P} s + \omega_{1P}^2}$$

is placed at the 1P frequency to amplify the 1P measured loads. Additionally, a ‘normal’
2.4. Controller design for IPC

Notch filter

\[ \text{NF}_{3P}(s) = \frac{s^2 + 2\omega_{3P}\beta_{3P}s + \omega_{3P}^2}{s^2 + 2\omega_{3P}\zeta_{3P}s + \omega_{3P}^2} \]

is placed at the 3P frequency to prevent from unwanted 3P pitch activity. A second-order high-pass filter parameterized by

\[ \mathcal{H}_{1P}(s) = \frac{s^2 + 2\omega\beta_{1P}s + \omega_{1P}^2}{s^2 + 2\omega\zeta_{1P}s + \omega_{1P}^2} \]

is used to attenuate pitch activity below the 1P frequency. Note that typically for a high-pass filter only \( s^2 \) in the numerator is required. However, here it is chosen to also include the lower order numerator coefficients to allow for some additional freedom in the controller design. Finally, a second-order low-pass filter given by

\[ \mathcal{L}_{1P}(s) = \frac{\omega_{1P}^2}{s^2 + 2\omega\beta_{1P}s + \omega_{1P}^2} \]

is included to provide roll off at higher frequencies. The combination of the low-pass filter and high-pass filter can be thought of as a bandpass filter. The resulting structure of the IPC-1P controller is given by

\[ C_{1P}(s) = \frac{K_{1P} \text{ Gain}}{s^2 + 2\omega\beta_{1P}s + \omega_{1P}^2} \times \frac{s^2 + 2\omega\beta_{1P,2}s + \omega_{1P,2}^2}{s^2 + 2\omega\zeta_{1P}s + \omega_{1P}^2} \times \frac{\omega_{1P}^2}{s^2 + 2\omega\beta_{1P}s + \omega_{1P}^2} \]

Some of the parameters in the above equation can directly be assigned to certain values (for instance \( \omega_{1P} \) and \( \omega_{3P} \), respectively the 1P and 3P frequencies), the remaining parameters are the degrees of freedom in the optimization process of the controller.

The design of the IPC-2P for the collective mode \( M_0 \) follows a similar approach. A proportional gain \( K_{2P} \), an inverted notch at the 2P frequency, a high-pass filter \( \mathcal{H}_{2P}(s) \), and a low-pass filter \( \mathcal{L}_{2P}(s) \) are used. From experiments it was clear that no additional notch was required at higher harmonic frequencies, so that the IPC-2P amounts to

\[ C_{2P}(s) = \frac{K_{2P} \text{ Gain}}{s^2 + 2\omega\beta_{2P}s + \omega_{2P}^2} \times \frac{s^2 + 2\omega\beta_{2P,2}s + \omega_{2P,2}^2}{s^2 + 2\omega\zeta_{2P} s + \omega_{2P}^2} \times \frac{\omega_{2P}^2}{s^2 + 2\omega\beta_{2P}s + \omega_{2P}^2} \]
Applying the IPC-1P of (2.34) to the differential mode \( M_1 \) and the IPC-2P of (2.35) to the collective mode \( M_0 \) yields the IPC-1P-2P controller.

The IPC-1P and the IPC-1P-2P-3P controller cases are obtained as follows. For the IPC-1P case, only the 1P frequency in the differential mode \( M_1 \) needs to be considered and is thus directly given by (2.34). In the IPC-1P-2P-3P case, the controller should provide control action at the 1P and 3P frequencies of the differential mode \( M_1 \) and is therefore denoted by IPC-1P-3P. To obtain this controller, the notch filter at the 3P frequency in (2.34) is replaced by an inverted notch filter at the 3P frequency given by

\[
NF_{\text{inv,3P}}(s) = \frac{s^2 + 2\omega_3p\zeta_3ps + \omega_{3P}^2}{s^2 + 2\omega_3p\beta_3ps + \omega_{3P}^2}
\]

Thus, the IPC-1P-3P controller is given by

\[
C_{1P3P}(s) = K_{1P3P} \times \frac{s^2 + 2\omega_{1P}\zeta_{1P}s + \omega_{1P}^2}{s^2 + 2\omega_{1P}\beta_{1P}s + \omega_{1P}^2} \times \frac{s^2 + 2\omega_{1P}\zeta_{1P}s + \omega_{1P}^2}{s^2 + 2\omega_{1P}\beta_{1P}s + \omega_{1P}^2} \times \frac{s^2 + 2\omega_{3P}\zeta_{3P}s + \omega_{3P}^2}{s^2 + 2\omega_{3P}\beta_{3P}s + \omega_{3P}^2} \times \frac{s^2 + 2\omega_{3P}\zeta_{3P}s + \omega_{3P}^2}{s^2 + 2\omega_{3P}\beta_{3P}s + \omega_{3P}^2} \times \frac{\omega_{L_{1P3P}}^2}{s^2 + 2\omega_{L_{1P3P}}\beta_{L_{1P3P}}s + \omega_{L_{1P3P}}^2} \times \frac{\omega_{L_{1P3P}}^2}{s^2 + 2\omega_{L_{1P3P}}\beta_{L_{1P3P}}s + \omega_{L_{1P3P}}^2}.
\]

The IPC-1P-2P-3P controller is then realized by applying the IPC-1P-3P of (2.36) to the differential mode \( M_1 \) and the IPC-2P of (2.35) to the collective mode \( M_0 \).

To find the parameters of the fixed-structure controllers in (2.34)-(2.36), the controller design is formulated into a mixed-sensitivity control problem. The block scheme representation of the generalized plant is shown in Figure 2.7. The mixed-sensitivity problem is given by

\[
\min \left\| \begin{array}{c}
W_p S \\
W_u KS \\
W_i T
\end{array} \right\|_\infty,
\]

where \( S \) is the sensitivity function, \( KS \) is the controller times sensitivity function, and \( T \) is the complementary sensitivity function. The performance weight \( W_p \) is chosen such that the sensitivity at the desired \( nP \) frequencies is small. The weighting function \( W_u \) is used to penalize the controller to be active at low and high frequencies, and possibly at other frequencies to avoid higher harmonics pitch action. The third weight \( W_i \) is included to account for unmodeled dynamics.

For the IPC-1P controller, the weighting filters were chosen as follows. The performance weight \( W_{p,1P}(s) \) on the sensitivity function includes an inverted notch filter at the 1P frequency and a small gain such that the transfer function of \( W_{p,1P}(s) \) is given by

\[
W_{p,1P}(s) = \frac{0.7s^2 + 1.22s + 13.35}{s^2 + 1.31 \cdot 10^{-2}s + 19.07}.
\]

The input weighting function \( W_u \) on the controller times sensitivity function is chosen as an inverse bandpass filter. Hence, the controller is designed to be active in the bandpass
region and low-frequency and high-frequency pitch action is penalized. The filter $W_u$ is constructed by a large gain multiplied with a second-order low-pass filter and a second-order high-pass filter such that the complete weight $W_{u,1P}(s)$ is given by

$$W_{u,1P}(s) = \frac{1.25 \cdot 10^{12} s^4 + 2.64 \cdot 10^{13} s^3 + 2.83 \cdot 10^{14} s^2 + 8.33 \cdot 10^{14} s + 1.25 \cdot 10^{15}}{s^4 + 8.80 \cdot 10^3 s^3 + 3.95 \cdot 10^7 s^2 + 1.39 \cdot 10^5 s + 2.49 \cdot 10^2}. \quad (2.39)$$

Finally, the weight $W_t(s)$ for unmodeled dynamics is chosen to be of the form (see Skogestad and Postlethwaite (2006))

$$W_t(s) = \frac{0.16s + 0.01}{7.96 \cdot 10^{-3}s + 1}. \quad (2.40)$$

Minimizing (2.37) for the mixed-sensitivity problem shown in Figure 2.7 with the above mentioned weights (2.38)-(2.40) and the controller structure in (2.34) then gives the desired fixed-structure IPC-1P controller.

The weighting filters of the IPC-2P controller are chosen in a similar way. The performance weight $W_{p,2P}(s)$ involves an inverted notch filter at the 2P frequency and a small gain such that

$$W_{p,2P}(s) = \frac{0.7s^2 + 1.22s + 53.39}{s^2 + 0.17s + 76.28}. \quad (2.38)$$

The filter $W_{u,2P}(s)$ giving a bound on the controller times sensitivity function is composed of the same filters (with different parameter values) as in (2.39) and is given by

$$W_{u,2P}(s) = \frac{2.22 \cdot 10^{11} s^4 + 5.47 \cdot 10^{12} s^3 + 6.81 \cdot 10^{13} s^2 + 4.21 \cdot 10^{14} s + 1.32 \cdot 10^{15}}{s^4 + 8.80 \cdot 10^3 s^3 + 3.95 \cdot 10^7 s^2 + 1.39 \cdot 10^5 s + 2.49 \cdot 10^2}. \quad (2.40)$$

The weight $W_t(s)$ for the IPC-2P is identical to (2.40). Again, minimizing (2.37) with the mentioned weights and the controller structure in (2.35) yields the desired fixed-structure IPC-2P controller.
For the IPC-1P-3P controller, the weighting filters were chosen as follows. The performance weight \( W_{p,1P3P}(s) \) on the sensitivity function now includes inverted notch filters at the 1P and 3P frequencies and a small gain, such that the weight \( W_{p,1P3P}(s) \) is given by

\[
W_{p,1P3P}(s) = \frac{0.7s^4 + 3.06s^3 + 1.37 \cdot 10^2 s^2 + 2.45 \cdot 10^2 s + 2.29 \cdot 10^3}{s^4 + 0.66s^3 + 1.91 \cdot 10^2 s^2 + 1.35 \cdot 10^1 s + 3.27 \cdot 10^3}.
\]

The filters \( W_u(s) \) and \( W_f(s) \) for the IPC-1P-3P controller are given by (2.39) and (2.40), respectively. Finally, the IPC-1P-3P controller is obtained by minimizing (2.37) for the given weights.

The optimization of the controllers was carried out with the use of a nonsmooth \( H_\infty \) optimization solver (Apkarian and Noll, 2006; Gahinet and Apkarian, 2011a), available in MATLAB. The final obtained parameter values of (2.34)-(2.36) are listed in Table 2.4. The values in bold indicate optimized parameters, the remaining parameter values are user defined. The Bode diagrams of the tuned LIPC\(_s\) are shown in Figure 2.8. The plots in Figure 2.9 also show the sensitivity functions and their inverse weights for the IPC-1P case.

For comparison, the same controllers were also designed without a pre-defined order or structure using unstructured controller synthesis. By using the same weighting functions for the sensitivity function \( S \), the controller times sensitivity function \( KS \), and the complementary sensitivity function \( T \), this resulted in 18\(^{th}\) order IPC-1P and IPC-1P-3P controllers and a 20\(^{th}\) order IPC-2P controller. These orders and corresponding norms of the controllers have been tabulated in Table 2.5. It should be noted that the optimization algorithms used to obtain the \( H_\infty \) controllers are different. In the structured case the mentioned nonsmooth \( H_\infty \) solver is used and in the unstructured case the two-Riccati formulae (Doyle et al., 1989) is used. The comparison indicates that with a fixed structure (and order) of the controller very similar results are obtained, while it remains suitable for practical applications.

The above controller designs are based on an identified system excluding periodic effects. Although the closed-loop systems of the identified system with each of the designed IPC\(_s\) are stable, no statements can be made about the stability of the closed-loop systems when applied to the fully non-linear wind turbine model including periodic effects and subjected to turbulent wind. However, for all considered simulation scenarios (see Section 2.5) the closed-loop system remained stable. The interested reader is referred to Stol et al. (2009) for a direct periodic controller approach and to Geyler and Caselitz (2008) for a robust multivariable controller approach.

### 2.4.5. Conventional IPC Design

In the next section, the performance of the LIPC strategy is analysed and compared to the conventional IPC approach. Therefore, in this section an IPC according to the conventional approach is designed. Inherently, the conventional IPC design uses the MBC transformation given in (2.18) and (2.19). This controller is considered for the 1P loads only and is referred to as: IPC-1P-MBC.

Two identical integral controllers are used in parallel to the decoupled cyclic modes \( q_1c \) and \( q_1s \) (see Section 2.2.4), i.e., the tilt and yaw moments. The integral control parameter \( K_{I-MBC} \) is experimentally chosen to give the best results. Further-
Table 2.4: Controller parameters of the structured LIPCs (the values in bold are optimized).

<table>
<thead>
<tr>
<th>Description</th>
<th>Symbol</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>IPC-1P</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Proportional gain</td>
<td>$K_{1P}$</td>
<td>$1.69 \cdot 10^{-7}$</td>
</tr>
<tr>
<td>Inverse notch filter 1P frequency</td>
<td>$\omega_{1P}$</td>
<td>$2\pi 41.7/60 \text{ rad s}^{-1}$ ($= 0.695 \text{ Hz}$)</td>
</tr>
<tr>
<td>Inverse notch filter 1P parameter #1</td>
<td>$\zeta_{1P}$</td>
<td>1.30</td>
</tr>
<tr>
<td>Inverse notch filter 1P parameter #2</td>
<td>$\beta_{1P}$</td>
<td>$1.50 \cdot 10^{-3}$</td>
</tr>
<tr>
<td>Low-pass filter frequency #1</td>
<td>$\omega_{L1P}$</td>
<td>$2.77 \cdot 2\pi \text{ rad s}^{-1}$</td>
</tr>
<tr>
<td>Low-pass filter frequency #2</td>
<td>$\omega_{L1P,2}$</td>
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</tr>
<tr>
<td>Low-pass filter parameter</td>
<td>$\beta_{L1P}$</td>
<td>0.53</td>
</tr>
<tr>
<td>High-pass filter frequency #1</td>
<td>$\omega_{H1P}$</td>
<td>$3.65 \cdot 10^{-4} \cdot 2\pi \text{ rad s}^{-1}$</td>
</tr>
<tr>
<td>High-pass filter frequency #2</td>
<td>$\omega_{H1P,2}$</td>
<td>$0.46 \cdot 2\pi \text{ rad s}^{-1}$</td>
</tr>
<tr>
<td>High-pass filter parameter #1</td>
<td>$\beta_{H1P}$</td>
<td>$-6.41$</td>
</tr>
<tr>
<td>High-pass filter parameter #2</td>
<td>$\beta_{H1P,2}$</td>
<td>0.48</td>
</tr>
<tr>
<td>Notch filter 3P frequency</td>
<td>$\omega_{3P}$</td>
<td>$3 \cdot 2\pi 41.7/60 \text{ rad s}^{-1}$ ($= 2.085 \text{ Hz}$)</td>
</tr>
<tr>
<td>Notch filter 3P parameter #1</td>
<td>$\zeta_{3P}$</td>
<td>0.45</td>
</tr>
<tr>
<td>Notch filter 3P parameter #2</td>
<td>$\beta_{3P}$</td>
<td>$9 \cdot 10^{-3}$</td>
</tr>
<tr>
<td><strong>IPC-1P-3P</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Proportional gain</td>
<td>$K_{1P3P}$</td>
<td>$4.92 \cdot 10^{-10}$</td>
</tr>
<tr>
<td>Inverse notch filter 1P frequency</td>
<td>$\omega_{1P}$</td>
<td>$2\pi 41.7/60 \text{ rad s}^{-1}$ ($= 0.695 \text{ Hz}$)</td>
</tr>
<tr>
<td>Inverse notch filter 1P parameter #1</td>
<td>$\zeta_{1P}$</td>
<td>$3.35 \cdot 10^{3}$</td>
</tr>
<tr>
<td>Inverse notch filter 1P parameter #2</td>
<td>$\beta_{1P}$</td>
<td>$2.23 \cdot 10^{-3}$</td>
</tr>
<tr>
<td>Inverse notch filter 3P frequency</td>
<td>$\omega_{3P}$</td>
<td>$3 \cdot 2\pi 41.7/60 \text{ rad s}^{-1}$ ($= 2.085 \text{ Hz}$)</td>
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<tr>
<td>Inverse notch filter 3P parameter #1</td>
<td>$\zeta_{3P}$</td>
<td>13.13</td>
</tr>
<tr>
<td>Inverse notch filter 3P parameter #2</td>
<td>$\beta_{3P}$</td>
<td>$2.40 \cdot 10^{-2}$</td>
</tr>
<tr>
<td>Low-pass filter frequency #1</td>
<td>$\omega_{L1P3P}$</td>
<td>$4.69 \cdot 2\pi \text{ rad s}^{-1}$</td>
</tr>
<tr>
<td>Low-pass filter frequency #2</td>
<td>$\omega_{L1P3P,2}$</td>
<td>$51.12 \cdot 2\pi \text{ rad s}^{-1}$</td>
</tr>
<tr>
<td>Low-pass filter parameter</td>
<td>$\beta_{L1P3P}$</td>
<td>$2.72 \cdot 10^{2}$</td>
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<tr>
<td>High-pass filter frequency #1</td>
<td>$\omega_{H1P3P}$</td>
<td>$6.15 \cdot 10^{-2} \cdot 2\pi \text{ rad s}^{-1}$</td>
</tr>
<tr>
<td>High-pass filter frequency #2</td>
<td>$\omega_{H1P3P,2}$</td>
<td>$0.74 \cdot 2\pi \text{ rad s}^{-1}$</td>
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<tr>
<td>High-pass filter parameter #1</td>
<td>$\beta_{H1P3P}$</td>
<td>19.53</td>
</tr>
<tr>
<td>High-pass filter parameter #2</td>
<td>$\beta_{H1P3P,2}$</td>
<td>0.51</td>
</tr>
<tr>
<td><strong>IPC-2P</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Proportional gain</td>
<td>$K_{2P}$</td>
<td>$3.51 \cdot 10^{-9}$</td>
</tr>
<tr>
<td>Inverse notch filter 2P frequency</td>
<td>$\omega_{2P}$</td>
<td>$2 \cdot 2\pi 41.7/60 \text{ rad s}^{-1}$ ($= 1.39 \text{ Hz}$)</td>
</tr>
<tr>
<td>Inverse notch filter 2P parameter #1</td>
<td>$\zeta_{2P}$</td>
<td>0.77</td>
</tr>
<tr>
<td>Inverse notch filter 2P parameter #2</td>
<td>$\beta_{2P}$</td>
<td>$1.02 \cdot 10^{-2}$</td>
</tr>
<tr>
<td>Low-pass filter frequency</td>
<td>$\omega_{L2P}$</td>
<td>$2 \cdot 2\pi 41.7/60 \text{ rad s}^{-1}$</td>
</tr>
<tr>
<td>Low-pass filter parameter</td>
<td>$\beta_{L2P}$</td>
<td>0.10</td>
</tr>
<tr>
<td>High-pass filter frequency #1</td>
<td>$\omega_{H2P}$</td>
<td>$1.3 \cdot 2\pi \text{ rad s}^{-1}$</td>
</tr>
<tr>
<td>High-pass filter frequency #2</td>
<td>$\omega_{H2P,2}$</td>
<td>$4 \cdot 10^{-4} \cdot 2\pi \text{ rad s}^{-1}$</td>
</tr>
<tr>
<td>High-pass filter parameter #1</td>
<td>$\beta_{H2P}$</td>
<td>$-5.64 \cdot 10^{2}$</td>
</tr>
<tr>
<td>High-pass filter parameter #2</td>
<td>$\beta_{H2P,2}$</td>
<td>0.16</td>
</tr>
</tbody>
</table>
Table 2.5: Comparison of orders and $\mathcal{H}_\infty$ norms for structured and unstructured controller design

<table>
<thead>
<tr>
<th>Type</th>
<th>Order</th>
<th>$\mathcal{H}_\infty$-norm</th>
</tr>
</thead>
<tbody>
<tr>
<td>Structured IPC-1P</td>
<td>8</td>
<td>1.99</td>
</tr>
<tr>
<td>Unstructured IPC-1P</td>
<td>18</td>
<td>1.96</td>
</tr>
<tr>
<td>Structured IPC-2P</td>
<td>8</td>
<td>1.56</td>
</tr>
<tr>
<td>Unstructured IPC-2P</td>
<td>20</td>
<td>1.39</td>
</tr>
<tr>
<td>Structured IPC-1P-3P</td>
<td>8</td>
<td>2.03</td>
</tr>
<tr>
<td>Unstructured IPC-1P-3P</td>
<td>18</td>
<td>2.02</td>
</tr>
</tbody>
</table>

Figure 2.8: Bode diagrams of the optimized structured LIPCs.

more, the integral controllers are extended with two notch filters to filter the 2P and 4P frequencies from the cyclic modes. The latter frequencies are present due to the rotating 1P and 3P loads, which are transformed to the fixed non-rotating frame by the MBC according to Table 2.2. The notch filters are given by

$$\text{NF}_{\text{2P-MBC}}(s) = \frac{s^2 + 2\omega_{\text{2P}}\beta_{\text{2P-MBC}} s + \omega_{\text{2P}}^2}{s^2 + 2\omega_{\text{2P}}\zeta_{\text{2P-MBC}} s + \omega_{\text{2P}}^2},$$

$$\text{NF}_{\text{4P-MBC}}(s) = \frac{s^2 + 2\omega_{\text{4P}}\beta_{\text{4P-MBC}} s + \omega_{\text{4P}}^2}{s^2 + 2\omega_{\text{4P}}\zeta_{\text{4P-MBC}} s + \omega_{\text{4P}}^2},$$

respectively. If one does not filter these frequencies, they are reverse transformed to the rotating domain and appear as unwanted 3P and 5P frequencies in the pitch signal.
The reverse MBC transformation can be modified such that phase losses can be accounted for. This is outlined in Bossanyi and Witcher (2009b) and in Houtzager et al. (2013) and can be achieved by adding an offset to the azimuth angle of the reverse MBC transformation, i.e.,

\[
\begin{bmatrix}
    \theta_1 \\
    \theta_2
\end{bmatrix} = \begin{bmatrix}
    \cos(\psi + \delta_{1P}) & \sin(\psi + \delta_{1P}) \\
    \cos(\psi + \pi + \delta_{1P}) & \sin(\psi + \pi + \delta_{1P})
\end{bmatrix} \begin{bmatrix}
    \theta_{1c}^* \\
    \theta_{1s}^*
\end{bmatrix}, \tag{2.41}
\]

where \(\delta_{1P}\) is the azimuth angle offset. The value of \(\delta_{1P}\) was obtained by inspection of the phase loss at the 1P frequency of the identified differential mode \(M_1\) and was experimentally verified.

The final obtained controller parameters of the IPC-MBC controller are listed in Table 2.6. The performance of the baseline controller and the IPC-1P-MBC is in accordance with the performance shown in Bossanyi and Wright (2009). In the next section the performance of the aforementioned IPC designs is evaluated.

### 2.5. RESULTS

The performance of the LIPCs is compared to the conventional IPC design and to a baseline controller configuration without IPC. The evaluation is based on a number
of simulation studies obtained by using the Bladed software package and the CART2 wind turbine description (see Section 2.4), where the teetering hub was switched off in all simulations. As previously indicated, only above-rated wind speeds are considered. Two different wind speeds are considered: \( v_0 = 18 \, \text{m/s} \) and \( v_0 = 22 \, \text{m/s} \). Turbulent wind fields are generated by using the von Karman model with three components. For both wind speeds, five different wind turbulence intensities are considered, i.e., \( I_T \in \{0\%, 6\%, 10\%, 14\%, 18\%\} \). So, in total 10 different simulation cases are considered. For each wind case, five different control configurations are subjected to the previously mentioned wind fields, i.e.:

- The baseline configuration without IPC (Baseline);
- The baseline configuration with conventional IPC for 1P (IPC-1P-MBC);
- The baseline configuration with LIPC for the 1P loads (IPC-1P);
- The baseline configuration with LIPC for the 1P and 2P loads (IPC-1P-2P);
- The baseline configuration with LIPC for the 1P, 2P and 3P loads (IPC-1P-2P-3P).

The simulation runs are each 10 minutes long. Note the abbreviations as they will be used to refer to the different controllers in the results.

The important wind turbine fatigue loads are the blade root bending moments \((M_{y,1}, M_{y,2})\), the rotating hub moment \(M_{hub,y}\), the yaw bearing moment \(M_{yaw,z}\) and the tower base moment \(M_{tow,y}\). The fatigue loads are quantified by computing the Damage Equivalent Load (DEL)\( s \) (Freebury and Musial, 2000), where the slope of the S-N curve was set to \( m = 10 \) (SN10) for the blades and to \( m = 4 \) (SN4) for the other components. The results are structured as follows:

- The baseline controller results are listed as the computed DELs;
- The obtained DELs of the IPCs are listed as percent reduction of the baseline results.

The results of the blade root bending moments \((M_{y,1}, M_{y,2})\) are shown as the average of \(M_{y,1}\) and \(M_{y,2}\). Furthermore, to quantify the pitch activity, four different measures are

### Table 2.6: Controller parameters of IPC-MBC-1P

<table>
<thead>
<tr>
<th>Description</th>
<th>Symbol</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Integral gain</td>
<td>( K_{I-MBC} )</td>
<td>( 4 \times 10^{-7} )</td>
</tr>
<tr>
<td>Reverse azimuth angle offset</td>
<td>( \delta_{1P} )</td>
<td>( 30^\circ )</td>
</tr>
<tr>
<td>Notch filter 2P frequency</td>
<td>( \omega_{2P} )</td>
<td>( 2 \cdot 2\pi 41.7/60 , \text{rad/s} ) (( = 1.39 , \text{Hz} ))</td>
</tr>
<tr>
<td>Notch filter 2P parameter #1</td>
<td>( \zeta_{2P-MBC} )</td>
<td>0.5</td>
</tr>
<tr>
<td>Notch filter 2P parameter #2</td>
<td>( \beta_{2P-MBC} )</td>
<td>0.005</td>
</tr>
<tr>
<td>Notch filter 4P frequency</td>
<td>( \omega_{4P} )</td>
<td>( 4 \cdot 2\pi 41.7/60 , \text{rad/s} ) (( = 2.78 , \text{Hz} ))</td>
</tr>
<tr>
<td>Notch filter 4P parameter #1</td>
<td>( \zeta_{4P-MBC} )</td>
<td>0.5</td>
</tr>
<tr>
<td>Notch filter 4P parameter #2</td>
<td>( \beta_{4P-MBC} )</td>
<td>0.01</td>
</tr>
</tbody>
</table>
The first two measures are the standard deviations of the blade pitch angle and the blade pitch rate angle. The third measure is the cumulative distance traveled by the pitch system, which is computed by

\[ \theta_{\text{tot}} = \sum_k |\Delta \theta_1(k)| + |\Delta \theta_2(k)|, \]

where \( \Delta \theta_b(k) = \theta_b(k) - \theta_b(k-1) \). That is, \( \Delta \theta_b(k) \) is the difference between two consecutive measured pitch angle samples for blade number \( b \). The fourth measure is the number of direction reversals of the pitch system. The number of direction reversals by the pitch actuators is an important measure for the life-time of the bearings, which is a typical problem for IPC. The results of the different controllers subjected to the indicated wind fields are given in Table 2.7 and Table 2.8. For brevity, only a selection of the spectral densities and time domain signals are shown in Figure 2.10 and Figure 2.11. The figures illustrate the results for the case in which the wind speed is \( v_0 = 22 \text{ m s}^{-1} \) and turbulence intensity is \( I_T = 10\% \).

To analyse the results, first the IPC-1P and the IPC-1P-MBC controllers are compared. In general one could say that the performance is rather similar. One observes in Figure 2.10 that both IPCs significantly reduce the rotating 1P loads. The IPC-1P-MBC achieves a slightly higher reduction of the 1P blade root moment. It should be noted that this difference can easily be the result of tuning. It can also be seen that by using IPC to reduce 1P loads, the 3P loads in the blade root moments (\( M_{y,1}, M_{y,2} \)) are increased. A very important observation, regarding two-bladed wind turbines, is the removal of the 1P rotating hub moment \( M_{\text{hub},y} \). This means that by using IPC to reduce rotating 1P loads, the load transfer from the blades to the shaft are reduced, such that it is a useful alternative to a mechanical teeter hinge as stated in Bossanyi et al. (2013); Bossanyi and Wright (2009). Furthermore, as a result of applying 1P load reduction in the rotating reference frame, the 2P loads in the fixed frame of reference are reduced, which is observed in the yaw bearing moment \( M_{\text{yaw},z} \) and the tower base moment \( M_{\text{tow},y} \).

From Figure 2.10, one observes that IPC-1P-2P and IPC-1P-2P-3P respectively remove the 1P, 2P loads and the 1P, 2P, 3P loads in the blade root bending moments (\( M_{y,1}, M_{y,2} \)). The most important reduction due to IPC-2P is the further reduction of the 2P load in the tower base moment \( M_{\text{tow},y} \) (not shown). Moreover, the most important reductions due to IPC-3P are the removal of the 3P loads in the rotating moments, further reductions of the 2P loads in the yaw bearing \( M_{\text{yaw},z} \) and tower base moments \( M_{\text{tow},y} \), and removing the 4P loads in the fixed non-rotating components. These additional load reductions typically also yield lower DELs, as can be seen in Table 2.7.

When comparing the time domain blade pitch signals in the lower part of Figure 2.11, one observes smooth pitch signals for all IPCs. One can observe a 2P signal component in the pitch signal of the IPC-1P-2P controller and 2P and 3P signal components for the IPC-1P-2P-3P controller. It is remarked that the IPC-1P and IPC-1P-2P contain some variations in the pitch rates, which might be considered to be undesired. These variations could be removed by including additional roll-off in the specific controllers. This can also be seen from the spectral plots in Figure 2.11, which show that the IPC-1P and IPC-1P-2P have less roll-off at higher frequencies. The IPC-1P-2P-3P includes higher roll-off due to the specific tuning of the two inverted notch filters in (2.36).
The previous observations are supported by the pitch measures in Table 2.8. The cumulative distance traveled by the pitch system and the number of pitch direction reversals increase for every added harmonic, which seems to be a logical consequence.

**2.6. Conclusions**

In this chapter, the typical IPC strategy for both three-bladed and two-bladed wind turbines is analysed and a linear coordinate transform for IPC of two-bladed wind turbines is proposed. The strategy taken for three-bladed turbines is to transform load signals, measured in a rotating frame of reference, to a fixed non-rotating frame of reference, by using a so-called MBC transformation. The main advantage of the MBC transformation is that it decouples the signals in the non-rotating frame of reference, allowing for SISO control design. After applying control action in the non-rotating frame, the signals are reverse transformed to the rotating frame and sent to the pitch actuators. As a consequence of the MBC transformation, frequency content in the rotating frame is distributed to different frequencies in the fixed non-rotating frame and vice versa for the reverse transformation. The frequency mappings, for both three-bladed rotors and two-bladed rotors, are summarized in this chapter.

Analysis of the MBC transformation for two-bladed rotors reveals that it contains a singularity. For that reason, a linear and non-singular coordinate transformation for IPC is proposed, which is the main contribution of this chapter. The proposed transformation does not require the rotor azimuth position and consists of only simple additions and subtractions. As with the MBC, the linear coordinate transformation also decouples the non-rotating signals, so that SISO loop shaping techniques can be used to design the IPC. The main advantage of using the linear transformation is that only a single control loop is required to be able to account for the odd harmonic frequencies (1P, 3P, etc.) of the measured rotating signals. By including a second control loop, all even harmonic frequencies (2P, 4P, etc.) in the measured rotating signals can also be accounted for. To achieve this, only simple control blocks, such as gains, low-pass and high-pass filters, and notch filters are required as is the case with conventional IPC.

It has been shown that the controller structure of the LIPC can be fixed on beforehand such that only the tunable controller parameters need to be tuned. The performance of three LIPCs (i.e., with 1P, 1P-2P and 1P-2P-3P load reduction capabilities) is evaluated on a two-bladed wind turbine without a teetering hub by means of a simulation study. The results are compared to a baseline controller without IPC and to the conventional IPC strategy. The results show that LIPC gives similar load reductions compared to conventional IPC. However, it is shown that by using the linear coordinate transformation, IPC for two-bladed turbines is relatively easily extended to reduce higher order harmonics of the fatigue loads. Hence, LIPC can arguably be a valuable addition to the control system of a two-bladed wind turbine.
Figure 2.10: Power spectral densities of the fatigue inducing loads resulting from the different IPCs for the NREL CART2 turbine. The results are shown for a wind speed of $v_0 = 22 \text{ m s}^{-1}$ and a turbulence intensity of $I_T = 10\%$. 
Figure 2.11: Power spectral densities and time domain plots of the first blade pitch angle resulting from the different IPCs for the NREL CART2 turbine. The results are shown for a wind speed of $v_0 = 22 \text{ m s}^{-1}$ and a turbulence intensity of $I_T = 10\%$. The legends of the lower two plots are identical.
Table 2.7: DELs and percent load reductions for the different IPCs.

<table>
<thead>
<tr>
<th></th>
<th>( v_0 ) [m s(^{-1})]</th>
<th>0</th>
<th>6</th>
<th>10</th>
<th>18</th>
<th>22</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>I(_T) [%]</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Baseline [Nm]</td>
<td>1.57 \times 10^5</td>
<td>2.40 \times 10^5</td>
<td>3.05 \times 10^5</td>
<td>4.03 \times 10^5</td>
<td>4.54 \times 10^5</td>
<td>1.85 \times 10^5</td>
</tr>
<tr>
<td>IPC-1P [%]</td>
<td>58.5</td>
<td>32.9</td>
<td>16.8</td>
<td>10.1</td>
<td>8.6</td>
<td>64.9</td>
</tr>
<tr>
<td>IPC-1P-MBC [%]</td>
<td>58.5</td>
<td>32.2</td>
<td>20.0</td>
<td>6.0</td>
<td>8.8</td>
<td>64.9</td>
</tr>
<tr>
<td>IPC-1P-2P [%]</td>
<td>81.9</td>
<td>36.5</td>
<td>23.6</td>
<td>9.6</td>
<td>9.4</td>
<td>84.5</td>
</tr>
<tr>
<td>IPC-1P-2P-3P [%]</td>
<td>82.5</td>
<td>35.5</td>
<td>24.2</td>
<td>12.3</td>
<td>9.7</td>
<td>85.2</td>
</tr>
</tbody>
</table>

**Averaged DEL (SN10) of blade 1&2 OoP root bending moments (DEL(\( M_{y,1} \)) + DEL(\( M_{y,2} \))) / 2**

<p>| | | | | | | | | | | |</p>
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<th></th>
<th></th>
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<th></th>
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</tr>
</thead>
<tbody>
<tr>
<td>Baseline [Nm]</td>
<td>3.52 \times 10^5</td>
<td>3.83 \times 10^5</td>
<td>4.19 \times 10^5</td>
<td>4.61 \times 10^5</td>
<td>5.12 \times 10^5</td>
<td>3.52 \times 10^5</td>
<td>4.31 \times 10^5</td>
<td>4.82 \times 10^5</td>
<td>5.34 \times 10^5</td>
<td>5.87 \times 10^5</td>
</tr>
<tr>
<td>IPC-1P [%]</td>
<td>70.8</td>
<td>59.4</td>
<td>50.3</td>
<td>43.4</td>
<td>37.1</td>
<td>70.7</td>
<td>57.0</td>
<td>48.3</td>
<td>41.9</td>
<td>34.8</td>
</tr>
<tr>
<td>IPC-1P-MBC [%]</td>
<td>71.1</td>
<td>60.5</td>
<td>51.9</td>
<td>45.8</td>
<td>39.0</td>
<td>70.7</td>
<td>58.0</td>
<td>49.7</td>
<td>44.0</td>
<td>37.7</td>
</tr>
<tr>
<td>IPC-1P-2P [%]</td>
<td>71.0</td>
<td>59.6</td>
<td>50.5</td>
<td>43.6</td>
<td>37.3</td>
<td>70.7</td>
<td>57.2</td>
<td>48.7</td>
<td>42.0</td>
<td>34.8</td>
</tr>
<tr>
<td>IPC-1P-2P-3P [%]</td>
<td>82.2</td>
<td>62.1</td>
<td>51.6</td>
<td>44.1</td>
<td>37.6</td>
<td>82.2</td>
<td>59.4</td>
<td>49.1</td>
<td>42.3</td>
<td>34.1</td>
</tr>
</tbody>
</table>

**DEL (SN4) of rotating hub moment \( M_{hub,y} \)**

<p>| | | | | | | | | | | |</p>
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<th></th>
<th></th>
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<th></th>
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<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Baseline [Nm]</td>
<td>1.71 \times 10^5</td>
<td>2.24 \times 10^5</td>
<td>2.66 \times 10^5</td>
<td>3.06 \times 10^5</td>
<td>3.51 \times 10^5</td>
<td>2.19 \times 10^5</td>
<td>2.62 \times 10^5</td>
<td>3.11 \times 10^5</td>
<td>3.54 \times 10^5</td>
<td>4.05 \times 10^5</td>
</tr>
<tr>
<td>IPC-1P [%]</td>
<td>61.9</td>
<td>39.0</td>
<td>31.8</td>
<td>25.5</td>
<td>18.6</td>
<td>69.9</td>
<td>37.5</td>
<td>27.2</td>
<td>21.2</td>
<td>16.3</td>
</tr>
<tr>
<td>IPC-1P-MBC [%]</td>
<td>61.9</td>
<td>40.1</td>
<td>32.7</td>
<td>27.0</td>
<td>20.6</td>
<td>69.8</td>
<td>37.9</td>
<td>29.0</td>
<td>22.9</td>
<td>18.1</td>
</tr>
<tr>
<td>IPC-1P-2P [%]</td>
<td>61.9</td>
<td>39.4</td>
<td>32.4</td>
<td>25.8</td>
<td>18.5</td>
<td>69.9</td>
<td>37.6</td>
<td>27.6</td>
<td>21.3</td>
<td>16.4</td>
</tr>
<tr>
<td>IPC-1P-2P-3P [%]</td>
<td>77.8</td>
<td>43.7</td>
<td>34.1</td>
<td>28.0</td>
<td>20.1</td>
<td>81.7</td>
<td>41.9</td>
<td>29.5</td>
<td>23.2</td>
<td>17.1</td>
</tr>
</tbody>
</table>

**DEL (SN4) of yaw bearing moment \( M_{yaw,z} \)**

<p>| | | | | | | | | | | |</p>
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<th></th>
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</tr>
</thead>
<tbody>
<tr>
<td>Baseline [Nm]</td>
<td>2.09 \times 10^5</td>
<td>7.15 \times 10^5</td>
<td>1.00 \times 10^6</td>
<td>1.31 \times 10^6</td>
<td>1.58 \times 10^6</td>
<td>2.32 \times 10^5</td>
<td>9.57 \times 10^5</td>
<td>1.21 \times 10^6</td>
<td>1.55 \times 10^6</td>
<td>1.91 \times 10^6</td>
</tr>
<tr>
<td>IPC-1P [%]</td>
<td>-16.5</td>
<td>4.0</td>
<td>2.8</td>
<td>-1.1</td>
<td>1.6</td>
<td>-3.2</td>
<td>3.8</td>
<td>2.3</td>
<td>0.3</td>
<td>2.0</td>
</tr>
<tr>
<td>IPC-1P-MBC [%]</td>
<td>-17.5</td>
<td>3.7</td>
<td>2.8</td>
<td>0.7</td>
<td>0.2</td>
<td>-5.7</td>
<td>3.3</td>
<td>2.5</td>
<td>0.5</td>
<td>0.3</td>
</tr>
<tr>
<td>IPC-1P-2P [%]</td>
<td>-16.6</td>
<td>8.6</td>
<td>4.5</td>
<td>-1.8</td>
<td>1.8</td>
<td>-6.2</td>
<td>5.0</td>
<td>1.9</td>
<td>1.2</td>
<td>1.1</td>
</tr>
<tr>
<td>IPC-1P-2P-3P [%]</td>
<td>-21.8</td>
<td>7.7</td>
<td>4.7</td>
<td>-2.8</td>
<td>1.6</td>
<td>-10.3</td>
<td>6.3</td>
<td>2.6</td>
<td>1.8</td>
<td>1.1</td>
</tr>
</tbody>
</table>
Table 2.8: Pitch angle measures for the different IPCs.

<table>
<thead>
<tr>
<th>$v_0$ [m s$^{-1}$]</th>
<th>0</th>
<th>6</th>
<th>10</th>
<th>14</th>
<th>18</th>
<th>0</th>
<th>6</th>
<th>10</th>
<th>14</th>
<th>18</th>
</tr>
</thead>
<tbody>
<tr>
<td>$I_T$ [%]</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>IPC-1P [deg]</td>
<td>0.94</td>
<td>1.00</td>
<td>1.06</td>
<td>1.10</td>
<td>1.15</td>
<td>1.10</td>
<td>1.14</td>
<td>1.22</td>
<td>1.28</td>
<td>1.34</td>
</tr>
<tr>
<td>IPC-1P-MBC [deg]</td>
<td>0.95</td>
<td>1.00</td>
<td>1.07</td>
<td>1.11</td>
<td>1.16</td>
<td>1.10</td>
<td>1.15</td>
<td>1.23</td>
<td>1.29</td>
<td>1.35</td>
</tr>
<tr>
<td>IPC-1P-2P [deg]</td>
<td>0.96</td>
<td>1.02</td>
<td>1.09</td>
<td>1.14</td>
<td>1.19</td>
<td>1.12</td>
<td>1.17</td>
<td>1.25</td>
<td>1.32</td>
<td>1.40</td>
</tr>
<tr>
<td>IPC-1P-2P-3P [deg]</td>
<td>0.95</td>
<td>1.02</td>
<td>1.09</td>
<td>1.14</td>
<td>1.20</td>
<td>1.11</td>
<td>1.17</td>
<td>1.25</td>
<td>1.32</td>
<td>1.40</td>
</tr>
</tbody>
</table>

Standard deviation of blade 1 pitch angle $\theta_1$

| IPC-1P [deg]        | 4.11 | 4.38 | 4.67 | 4.89 | 5.15 | 4.80 | 5.02 | 5.40 | 5.69 | 6.04 |
| IPC-1P-MBC [deg]    | 4.13 | 4.39 | 4.68 | 4.88 | 5.15 | 4.82 | 5.03 | 5.40 | 5.68 | 6.01 |
| IPC-1P-2P [deg]     | 4.33 | 4.78 | 5.17 | 5.54 | 5.93 | 5.06 | 5.45 | 6.00 | 6.45 | 6.97 |
| IPC-1P-2P-3P [deg]  | 4.36 | 4.85 | 5.27 | 5.68 | 6.12 | 5.10 | 5.53 | 6.12 | 6.59 | 7.15 |

Standard deviation of blade 1 pitch angle rate $\dot{\theta}_1$

| IPC-1P [deg s$^{-1}$] | $4.45 \times 10^3$ | $4.61 \times 10^3$ | $4.80 \times 10^3$ | $4.86 \times 10^3$ | $4.99 \times 10^3$ | $5.19 \times 10^3$ | $5.29 \times 10^3$ | $5.58 \times 10^3$ | $5.79 \times 10^3$ | $5.99 \times 10^3$ |
| IPC-1P-MBC [deg s$^{-1}$] | $4.47 \times 10^3$ | $4.63 \times 10^3$ | $4.81 \times 10^3$ | $4.86 \times 10^3$ | $5.01 \times 10^3$ | $5.22 \times 10^3$ | $5.31 \times 10^3$ | $5.60 \times 10^3$ | $5.79 \times 10^3$ | $5.96 \times 10^3$ |
| IPC-1P-2P [deg s$^{-1}$] | $4.46 \times 10^3$ | $4.82 \times 10^3$ | $5.14 \times 10^3$ | $5.38 \times 10^3$ | $5.64 \times 10^3$ | $5.23 \times 10^3$ | $5.52 \times 10^3$ | $5.99 \times 10^3$ | $6.39 \times 10^3$ | $6.77 \times 10^3$ |
| IPC-1P-2P-3P [deg s$^{-1}$] | $4.66 \times 10^3$ | $4.95 \times 10^3$ | $5.25 \times 10^3$ | $5.50 \times 10^3$ | $5.81 \times 10^3$ | $5.46 \times 10^3$ | $5.68 \times 10^3$ | $6.14 \times 10^3$ | $6.54 \times 10^3$ | $6.94 \times 10^3$ |

Number of direction reversals of blade 1 pitch angle $\theta_1$

| IPC-1P           | 834  | 834  | 856  | 910  | 944  | 834  | 834  | 842  | 874  | 934  |
| IPC-1P-MBC       | 834  | 834  | 838  | 882  | 919  | 834  | 834  | 836  | 844  | 868  |
| IPC-1P-2P        | 834  | 926  | 996  | 1132 | 1182 | 834  | 912  | 1022 | 1087 | 1196 |
| IPC-1P-2P-3P     | 834  | 902  | 1012 | 1180 | 1260 | 834  | 910  | 1038 | 1133 | 1210 |
Chapter 3

FIELD TESTING OF LINEAR INDIVIDUAL PITCH CONTROL ON THE NREL CART2

This chapter presents the results of field tests using Linear Individual Pitch Control (LIPC) on the two-bladed Controls Advanced Research Turbine 2 (CART2) at the National Renewable Energy Laboratory (NREL). LIPC has recently been introduced as an alternative to the conventional Individual Pitch Control (IPC) strategy for two-bladed wind turbines. The main advantage of LIPC over conventional IPC is that it requires, at most, only two feedback loops to potentially reduce the periodic blade loads. In previous work, LIPC was designed to implement blade pitch angles at a fixed frequency (e.g., the once-per-revolution (1P) frequency), which made it only applicable in above-rated wind turbine operating conditions. In this study, LIPC is extended to below-rated operating conditions by gain scheduling the controller on the rotor speed. With this extension, LIPC and conventional IPC are successfully applied to the NREL CART2 wind turbine. The field-test results obtained during the measurement campaign indicate that LIPC significantly reduces the wind turbine loads for both below-rated and above-rated operation.

3.1. INTRODUCTION

Over the past decades, the rotor diameter of wind turbines have vastly increased. With current rotor diameters exceeding 150 meters, the loads across the rotor plane have become increasingly asymmetric (Burton et al., 2001). To mitigate these asymmetric loads, active load mitigation methodologies can be applied. One such methodology is Individual Pitch Control (IPC) (Bossanyi, 2003, 2005), in which the blades are pitched cyclically along their longitudinal axis. Experiments have demonstrated (Bossanyi et al., 2013, 2010) that IPC is able to remove the once-per-revolution (or 1P) blade loadings (Bossanyi et al., 2013), caused by, wind shear, tower shadow and other factors. In addition to reducing the 1P loads on the rotating part of the machine, the 2P loads (for two-bladed wind turbines) and the 3P loads (for three-bladed wind turbines) on the non-rotating components are reduced.
The working principle of conventional IPC is to transform the blade root moments, measured in a rotating frame of reference, to a fixed non-rotating yaw and tilt moment. Specifically, the coordinate transformation maps the 1P frequencies in the rotating reference frame to a static yaw and tilt component. The controller, implemented in the non-rotating frame of reference, is then simplified to only require integral controllers for the yaw and tilt moment. By reverse transformation of the integrated yaw and tilt components, blade pitch setpoints at the 1P frequency in the rotating frame of reference are obtained. The coordinate transformations involved are the Coleman or Multi-Blade Coordinate (MBC) transformation (Bir, 2008; Stol et al., 2009), which are adapted from electrical machine theory (Park, 1929) and helicopter theory (Coleman and Feingold, 1958; Johnson, 1994). IPC has seen many extensions and applications over the past years, such as compensation for rotor imbalances and dealing with actuation limits Kanev and van Engelen (2009), higher harmonics load control (van Engelen, 2009), two degree of freedom control approaches (Selvam et al., 2009; Houtzager et al., 2013), and multiple-input multiple-output state-space control state-space control methods (Wright et al., 2009; Wright and Stol, 2010; Wright et al., 2011).

More recently, a new IPC strategy specifically for two-bladed wind turbines has been introduced (van Solingen and van Wingerden, 2015). The main motivation for developing this new strategy is that the coordinate transformation as previously applied for IPC (Bossanyi et al., 2010; Bossanyi and Wright, 2009) of two-bladed wind turbines is not mathematically sound (i.e., the transformation is singular (van Solingen and van Wingerden, 2015)). The new Linear Individual Pitch Control (LIPC) strategy involves a, mathematically sound, linear coordinate transformation, which transforms the rotating blade root moments to two new coordinates: a collective mode and a differential mode (van Solingen and van Wingerden, 2015). In the collective mode all even periodic blade load harmonics are contained, and in the differential mode, all odd periodic blade load harmonics are contained. This means that in order to reduce the 1P blade loads, only a single feedback loop (and thus only a single controller) is required. Ultimately, at most, only two controllers are required to potentially reduce the periodic blade loads. Furthermore, the linear coordinate transformation allows for fixed-structure $H_{\infty}$ controller design (van Solingen and van Wingerden, 2014), such that optimization techniques can be used to find the optimal controller parameters. Recently, LIPC has been experimentally tested in a wind tunnel on a small-scale two-bladed wind turbine (van Solingen et al., 2014b).

In the previous cited work (van Solingen and van Wingerden, 2015, 2014; van Solingen et al., 2014b), LIPC was only considered for above-rated operating conditions. In such operating conditions the rotor speed is approximately constant and LIPC has shown to give the same load reductions as conventional IPC. In above-rated operating conditions, the rotor speed is approximately constant, and the LIPC controller can be designed to implement blade pitch angles at fixed frequencies (i.e., 1P, 2P, ...). However, in below-rated operating conditions, the rotor speed varies and so do the 1P, 2P, ... frequencies, which means that a LIPC designed for a fixed 1P frequency is no longer effective. Therefore, in this work, LIPC is extended to below-rated operating conditions by gain scheduling the controller on the rotor speed. The latter extension gives the ability to assess the performance of LIPC over the whole operating range.
Prior to this study, only simulation studies (van Solingen and van Wingerden, 2015, 2014) and an experimental study (van Solingen et al., 2014b) had been conducted. For this study, the performance of LIPC is assessed using the two-bladed National Renewable Energy Laboratory (NREL) Controls Advanced Research Turbine 2 (CART2) at the National Wind Technology Center (NWTC) (see Figure 3.1). This chapter describes the results of the LIPC CART2 study and includes:

- Gain-scheduling LIPC on the rotor speed, such that it can be applied in below-rated operating conditions;

- Field-test validation of LIPC on the NREL CART2 two-bladed wind turbine. The LIPC strategy is compared to conventional IPC and to the case without IPC;

- Several practical issues encountered during the measurement campaign.

Section 3.2 provides the details of the NREL CART2 along with some details of the (supervisory) control system implemented on the CART2. Section 3.2, also lists the signals used by the controllers and the signals to evaluate the performance of the controllers. In Section 3.3, both the conventional IPC approach and the LIPC approach are described. The controller design and gain scheduling of LIPC on the rotor speed are discussed in Section 3.4. The results of the measurement campaign on the NREL CART2 are given in Section 3.5 and the chapter is concluded in Section 3.6.
3.2. NREL CART2 Wind Turbine and Control System

The CART2 at the NWTC (see Figure 3.1) has a 42 m rotor diameter. It is a variable speed and variable pitch controlled wind turbine with a rated electrical power output of 570 kW (rated wind speed is \( v = 12.7 \text{ m s}^{-1} \)). The wind turbine is equipped with a variety of sensors, of which the blade root strain gauges are of vital importance in this study. The pitch actuators are fast and thus suitable for IPC. The two blades are connected to the shaft through a teetered hub, which, in this measurement campaign, remained locked by means of a hydraulic brake at all times. A dedicated mast, located upwind of the wind turbine in the dominant wind direction, provides meteorological information such as wind speed and wind direction at heights of 15 m, 36.6 m, and 58.2 m.

The control system of the CART2 is such that (advanced) control concepts can easily be implemented and validated. The power production of the wind turbine is regulated by a torque controller in below-rated operating conditions and by Collective Pitch Control (CPC) in above-rated operating conditions. The torque controller and CPC incorporate a drive-train torsional notch filter, such that the drivetrain mode is prevented from being excited. In the measurement campaign no other active load reduction algorithms other than IPC were used.

A supervisory controller system monitors the wind turbine operating conditions and shuts the turbine down in case of any errors or faults. It also manages the start-up of the wind turbine and automatically cycles between different control algorithms. The following cycle of controllers is considered:

1. IPC based on the linear coordinate transformation: LIPC;
2. IPC based on the MBC coordinate transformation: IPC-MBC;
3. No IPC: Baseline.

The duration of each cycle is 300 s and the outputs of the IPC controllers are limited to \( \pm 3^\circ \) to prevent the pitch actuators from overheating. During the experiments, the following signals were used by the IPC algorithms:

- Blade 1 and 2 Out-of-Plane (OoP) root bending moments \( (M_{y,1}, M_{y,2}) \);
- Blade 1 and 2 pitch angles \( (\theta_1, \theta_2) \);
- The rotor speed \( \omega \);
- Azimuth angle \( \psi \) of the rotor.

The blade OoP root bending moments \( (M_{y,1}, M_{y,2}) \) are not directly available by sensor measurements and therefore need to be calculated from the strain gauge measurements in the blade roots. The strain gauges measure the blade root strains in both the flapping and edgewise directions and can be converted to the blade OoP root bending moments \( (M_{y,1}, M_{y,2}) \) by using the following relation

\[
\begin{align*}
M_{y,1} &= M_{\text{flap},1} \cos \theta_1 - M_{\text{edge},1} \sin \theta_1, \\
M_{y,2} &= M_{\text{flap},2} \cos \theta_2 - M_{\text{edge},2} \sin \theta_2,
\end{align*}
\]
for which also the blade pitch angles \((\theta_1, \theta_2)\) are used. For the performance analysis of the controllers, the following signals are also considered:

- Wind speeds measured by the met mast at 15 m, 36.6 m, and 58.2 m;
- Wind direction measured by the met mast;
- Nacelle fore-aft acceleration \(a_{nac,fa}\);
- Nacelle side-side acceleration \(a_{nac,sa}\);
- Teeter angle;
- Electrical power output.

In addition to the aforementioned signals, the control system internally logs various signals of the supervisory controller and the IPC controllers discussed in this chapter. These signals were mainly used for analysis and debugging throughout the measurement campaign. All signals were logged at a sampling frequency of 400 Hz, which is also the sampling frequency of the controllers.

### 3.3. IPC METHODS

Typically, the main purpose of applying IPC is to reduce the blade loads as well as other loads on the wind turbine. To obtain the pitch setpoints that mitigate blade loads, often the structure in Figure 3.2 is applied. The blade root moments \((M_{y,1}, M_{y,2})\) are measured in a rotating frame of reference and a change of coordinates is applied to obtain the non-rotating moments \((M_{y,1}^*, M_{y,2}^*)\). The transformed signals \((M_{y,1}^*, M_{y,2}^*)\) serve as input to the controller, which generate the pitch angle setpoints \((\theta_1^*, \theta_2^*)\) in the non-rotating frame of reference. The coordinate transformations are such that the non-rotating moments are decoupled from each other and Single-Input Single-Output (SISO) Linear Time-Invariant (LTI) controllers can be designed. Finally, to obtain pitch setpoints \((\theta_1, \theta_2)\) in the rotating frame of reference, the coordinates are reverse transformed. Because it is important to keep the stresses on the pitch system small (no high-frequency activity), a low-pass filter \(\mathcal{L}\) can be used to filter unwanted high frequency content from the control signals. The details of two IPC strategies and their main advantages are (briefly) discussed next.

#### 3.3.1. CONVENTIONAL IPC

The conventional IPC (Bossanyi, 2003, 2005; Bossanyi et al., 2013) strategy relies on the use of the MBC transformation (or Coleman transformation) (Bir, 2008). The nonlinear transformation maps the blade root moments \((M_{y,1}, M_{y,2})\) measured in the rotating frame of reference to a non-rotating frame of reference. In fact, the measured blade root moments \((M_{y,1}, M_{y,2})\) are transformed to yaw and tilt moments. Moreover, the yaw and tilt moments are decoupled from each other such that two independent controllers can be designed using SISO techniques. Typically, the controllers that are used for conventional IPC are integral controllers.
The forward MBC transformation is given by

\[
\begin{bmatrix}
M_{nc} \\
M_{ns}
\end{bmatrix} = \begin{bmatrix}
\cos(n\psi) & \cos(n[\psi + \pi]) \\
\sin(n\psi) & \sin(n[\psi + \pi])
\end{bmatrix} \begin{bmatrix}
M_{y,1} \\
M_{y,2}
\end{bmatrix}
\]

(3.1)

and the corresponding reverse MBC transformation by

\[
\begin{bmatrix}
\theta_1 \\
\theta_2
\end{bmatrix} = \begin{bmatrix}
\cos(n\psi) & \sin(n\psi) \\
\cos(n[\psi + \pi]) & \sin(n[\psi + \pi])
\end{bmatrix} \begin{bmatrix}
\theta_{nc} \\
\theta_{ns}
\end{bmatrix},
\]

(3.2)

where \(\psi\) is the rotor azimuth angle and \(n\) is the \(n\)'th blade load harmonic (e.g., 1P, 2P, 3P, etc.). Because the rotor azimuth angle \(\psi\) is inherited in the coordinate transformation matrices, the IPC-MBC strategy automatically accounts for rotor speed variations, such that it is directly applicable in both below-rated and above-rated operating conditions.

The main working principle of the IPC-MBC strategy is as follows. The blade load harmonics in rotating frame of reference are mapped to different frequencies in the non-rotating frame of reference. The key idea of the MBC transformation implemented for the \(n\)'th harmonic is that the \(n\)'th blade load harmonic is mapped to a static component (0P) in the non-rotating frame of reference. By integrating the static component and passing it through the reverse transformation, the 0P is mapped to an \(n\)P pitch signal. An overview of the frequency mappings between the rotating and non-rotating frame of reference is given in van Solingen and van Wingerden (2015).

### 3.3.2. Linear IPC

The recently introduced LIPC (van Solingen and van Wingerden, 2015, 2014; van Solingen et al., 2014b) strategy for two-bladed wind turbines follows a strategy similar to IPC-MBC. The key difference of the LIPC strategy is the use of a linear coordinate transformation instead of the MBC transformation. The LIPC is detailed in van Solingen and van Wingerden (2015) and briefly addressed here.

The forward coordinate transformation (Johnson, 1994; van Solingen and van Wingerden, 2015) of LIPC is given by

\[
\begin{bmatrix}
M_0 \\
M_1
\end{bmatrix} = \begin{bmatrix}
1/2 & 1/2 \\
-1/2 & 1/2
\end{bmatrix} \begin{bmatrix}
M_{y,1} \\
M_{y,2}
\end{bmatrix}
\]

(3.3)
and the reverse coordinate transformation by

$$\begin{bmatrix} \theta_1 \\ \theta_2 \end{bmatrix} = \begin{bmatrix} 1 & -1 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} \theta_0^* \\ \theta_1^* \end{bmatrix}. \quad (3.4)$$

It can be (analytically) shown (van Solingen and van Wingerden, 2015) that the even and odd blade load harmonics are separately contained in the linear combinations \((M_0, M_1)\) of the blade root moments \((M_{y1}, M_{y2})\). All even harmonics are mapped to the collective mode \(M_0\) and all odd harmonics are mapped to the differential mode \(M_1\). Similar to the MBC transformation, the collective mode \(M_0\) and the differential mode \(M_1\) are decoupled from each other.

The main advantage of the linear coordinate transformation is that a reduced amount of controllers is required. In the case of MBC-IPC two controllers need to be implemented for each blade load harmonic that one wants to reduce, whereas for LIPC, at least one controller is required and at most two. The latter is schematically depicted in Figure 3.3. Another advantage of LIPC is that it directly allows for (fixed-structure) \(H_\infty\) controller design (van Solingen and van Wingerden, 2014).

### 3.4. Control Design

The IPC strategies outlined in the previous section require the design of LTI controllers, and therefore, a linear model of the wind turbine system. To be more specific, a linear model of the dynamics from pitch actuator setpoints to the blade root moment responses at different operating conditions is required. Through the use of system identification techniques (van der Veen et al., 2013a), such models can be obtained. Both the system identification procedure to obtain linear models and the controller design are discussed in this section.
3.4.1. System Identification

To obtain a model for controller design, offline system identification was applied to data obtained from a high-fidelity model of the CART2 using FAST (Jonkman and Buhl Jr., 2005). To do so, in Figure 3.2, the linear coordinate transformations were used and the blade pitch angles ($\theta_1^*, \theta_2^*$) were excited by a random signal. The response caused by the blade pitch excitation was measured in the transformed blade root moments ($M_{y,1}^*, M_{y,2}^*$). Then, system identification techniques (van der Veen et al., 2013a) were used to model the dynamics$^1$ between the excited pitch inputs ($\theta_1^*, \theta_2^*$) and the measured moments ($M_{y,1}^*, M_{y,2}^*$). The system identification procedure was repeated for different wind speeds to obtain the dynamics for a range of operating conditions of the wind turbine.

The pitch excitations were chosen to be a Random Binary Signal (RBS) and are generated by

$$\theta_i^*(k) = c \cdot \text{sgn} \, w(k),$$

where $w(k)$ is a stochastic white noise sequence and $c$ is a scalar that has a magnitude of 0.5°. The stochastic white noise sequence has a sampling time of 0.2s. Hence, the RBS switches randomly from $+0.5^\circ$ to $-0.5^\circ$ and vice versa. To prevent high-frequent pitch activity in the inputs ($\theta_1^*, \theta_2^*$), a low-pass filter $L$ is used with a cutoff frequency at 10Hz. A notch filter at the drivetrain frequency is used to prevent exciting the drivetrain mode (3.2Hz). Constant wind speeds are considered between $v = 6 \text{ m s}^{-1}$ to $v = 18 \text{ m s}^{-1}$.

The Optimized Predictor-Based Subspace IDentification (van der Veen et al., 2013a) is applied to ten minute data sets containing 240,000 samples (sampling frequency of 400Hz) and the Variance Accounted For (VAF) (Verhaegen and Verdult, 2007) serves as a measure to see how well the simulated outputs ($\hat{M}_{y,1}^*, \hat{M}_{y,2}^*$) of the identified models correspond to the measured outputs ($M_{y,1}^*, M_{y,2}^*$). The final selected models have an order between $n = 20$ and $n = 25$ and all outputs have a VAF exceeding 90%. The Bode diagrams of the identified systems are given in Figure 3.4. The Bode diagrams only show the identified models from pitch input $\theta_2^*$ to blade moment output $M_{y,2}^*$ (see Figure 3.2, where the linear coordinate transformations (3.3) and (3.4) were used). In other words, the dynamics between the differential pitch component $\theta_2^*$ (excitation input) to the differential blade root moment $M_{y,2}^*$ (measured output) are shown. It can be observed that for increasing wind speed, the gain from pitch input to blade moment response increases, which means that to have the same effect on the blade root moments over the whole operating range, smaller pitch angles are required with increasing wind speeds (or the control authority is lower at lower wind speeds). Furthermore, notice the dip in the Bode magnitude at the drivetrain frequency, which is due to the notch filter removing excitation around the drivetrain frequency. Moreover, the phase loss due to the low-pass filter, notch filters, and actuator at the 1P frequency is roughly 70°. For IPC it is important to account for this in the controller such that the blade pitch angles have the right phase. The phase loss found here is in accordance with the values reported in Bossanyi et al. (2013).

\footnote{The dynamics of the linear transformed system are non-linear and time-varying. However, it was found in van Solingen and van Wingerden (2015) that an LTI identified model can sufficiently well approximate the dynamics of the transformed system such that it can be used for controller design.}
Figure 3.4: Identified models of the differential mode (from differential pitch $\theta_{2}^{*}$ to differential blade mode $M_{y,2}^{*}$) for wind speeds between $v = 8 \text{ m s}^{-1}$ and $v = 18 \text{ m s}^{-1}$).

### 3.4.2. **Conventional IPC Design**

The IPC-MBC strategy requires the design of two identical integral controllers (Bossanyi, 2003). The order of magnitude of the integral gains can be observed from e.g., the identified models (see Figure 3.4). The gains were further fine-tuned by trial and error using FAST (Jonkman and Buhl Jr., 2005) simulations with various wind conditions. The MBC transformation can incorporate any phase delays by including an offset in the azimuth position $\psi$ of the reverse MBC transformation (3.2). A value of 60° was found to give the best performance in simulations. Moreover, to compensate for unwanted frequencies in the non-rotating frame of reference, notch filters were placed at the 2P and 4P frequencies. Finally, because the MBC transformations are dependent on the azimuth position $\psi$ of the rotor, IPC-MBC can be directly applied in both above-rated and below-rated operating conditions.

### 3.4.3. **Linear IPC Design**

The IPC field measurement campaign focused on 1P blade load reduction only, which means that for LIPC only a single controller is required. Compared to previous work (van Solingen and van Wingerden, 2015, 2014), the control blocks are chosen slightly different in the sense that the inverted notch filter is chosen such that it by default incorporates roll-off at low and high frequencies. The transfer function of this inverted notch filter is given by

$$NF_{1P}(s) = \frac{ks}{s^2 + 2\omega_{1P}\beta s + \omega_{1P}^2},$$

(3.5)
where $\omega_{1P}$ is the 1P frequency, $k$ is the gain, and $\beta$ simultaneously controls the width and height of the notch. This is a very simple and low-order controller that can easily be tuned with $k$ and $\beta$. Additionally, a lead compensator is used to compensate for the phase loss of the actuator and filters in the feedback loop. The lead compensator is given by

$$LC(s) = \frac{s + \tau_1}{s + \tau_2},$$

where the amount of phase lead and frequency range can be controlled by $\tau_1$ and $\tau_2$. The lead compensator was designed to have roughly $60^\circ$ of phase around the 1P frequency.

### 3.4.4. Gain-scheduling Linear IPC

The LIPC methodology, as it is described thus far, implements pitch action only at the frequency determined by the inverted notch filter. This frequency is typically the 1P load frequency and possibly higher order harmonics such as the 2P and 3P frequencies. These frequencies remain (approximately) constant for above-rated operating conditions of the wind turbine. However, for below-rated operating conditions, the frequencies vary with rotor speed. Moreover, the current form of LIPC always implements the pitch action at fixed frequencies regardless of the rotor speed (see (3.5)), which clearly results in incorrect blade pitch frequencies for varying rotor speed. A solution to overcome this problem is to gain schedule the inverted notch filter on the rotor speed. To this end, the following continuous-time state-space implementation of (3.5) was considered

$$A(\omega) = \begin{bmatrix} 0 & 1 \\ -\omega^2 & -2\omega \end{bmatrix}, \quad B = \begin{bmatrix} 0 \\ 1 \end{bmatrix}, \quad C = [0 \quad k], \quad D = 0.$$
3.4. CONTROL DESIGN

The controller is low-pass filtered by

$$\mathcal{L}_\omega(s) = \frac{1}{\tau_{\text{LPF}} s + 1},$$

with crossover frequency at 5Hz. A block diagram representation of the gain-scheduled LIPC controller is shown in Figure 3.5, where the filter $\mathcal{L}(s)$ represents the drivetrain notch filter and an additional low-pass filter. The final gain-scheduled LIPC controller incorporating the drivetrain notch and additional low-pass filter is shown in Figure 3.6 for three different rotor speeds.

It was observed in Figure 3.4 that for lower wind speeds, the gain from pitch to blade root moments becomes smaller. This effectively means that by designing a controller for 16 m s$^{-1}$, and by scheduling on the rotor speed, the controller becomes less aggressive for lower wind speeds. From a practical point of view, this is useful because at lower wind speeds, typically the loads are lower and would require larger pitch actions (because of lower control authority). Hence, this implementation provides a mechanism to limit the pitch activity at lower wind speeds. For higher wind speeds, the gains only marginally increase, as can be seen from Figure 3.4. Hence, a controller designed for a wind speed of 16 m s$^{-1}$ becomes less aggressive at lower wind speeds and becomes only marginally more aggressive at higher wind speeds.

Figure 3.6: Bode diagrams of the LIPC controller for three different rotor speeds: 20rpm, 30rpm, and rated rpm.
3.5. Results

The results of the IPC field measurement campaign on the NREL CART2 are divided into three parts. The first part shows that the proposed extension of LIPC to below-rated operating conditions (see Section 3.4.4) by gain scheduling the controller on the rotor speed results in the desired response. In the second part, the performance of the IPC algorithms is assessed by means of power spectral densities based on individual 300 s runs. In the third part, the performance is analyzed by splitting measurement data of many cycles into smaller data sets (bins). The bins with matching characteristics (i.e., met mast wind speed at hub height) are combined such that over a wide range of measurements the performance can be assessed.

All results are based on post-processed data, and the following post-processing steps have been carried out:

1. The sampling frequency of the control system is 400 Hz, which is much higher than the frequency range of interest, and therefore, all data is resampled to 20 Hz.

2. The first 30 s and last 30 s of each data set are removed. These parts of the data contain switching transients between the different controllers. That is, the supervisory controller repeatedly switches every 300 s to the next controller and continues to do so as long as there are no faults, sufficient wind, and the operator does not manually terminate power production. The transitions between the controllers are achieved by ramping an enabling signal of the next controller from 0 (off) to 1 (on) in 5 s and ramping the enabling signal of the current controller from 1 to 0 also in 5 s. By removing the first 30 s and last 30 s of the data, the effects of the switching are removed.

3. An automated script checks for saturation of the pitch angles\(^2\) and removes the ‘saturated’ data.

4. Data in which the yaw misalignment is larger than 30\(^\circ\) is removed.

Finally, in addition to the previous steps, the nacelle accelerations are passed through a high-pass filter with cut-off frequency at 0.1 Hz, to remove the signal offsets.

3.5.1. Below-rated Linear IPC

In Section 3.4.4, gain scheduling is applied to extend LIPC to the full operating range of two-bladed wind turbines. To assess whether this implementation is successful, eight datasets obtained on April 9, 2014, were analyzed. These datasets contain measurements of both below-rated as well as above-rated operating conditions. The various rotor speeds that were measured made it possible to analyze the frequencies of the blade pitch angles (\(\theta_1, \theta_2\)), so as to determine whether the gain-scheduled LIPC worked properly. To this end, the eight datasets were split into 30 s bins, and for each bin, the average rotor speed was computed. Then, by computing the power spectral densities of the blade

\(^2\)The outputs of the IPC controllers, i.e., the individual blade pitches, are passed through a saturation block (limited at \(\pm 3\) deg) to prevent the actuators from overheating. On some occasions the individual blade pitch angles were saturated and, due to the nonsmooth saturation of the pitch angles, the loads on the wind turbine increased.
3.5. RESULTS

Figure 3.7: Spectral waterfall plots of the LIPC blade pitch angles based on eight datasets. The spectral waterfall plot is obtained by computing the power spectral densities of the blade pitch angles and plotting versus the average rotor speed. The amplitude of the power density (rad²/Hz) is indicated by the color bar on the right. The plots clearly show the 1P frequency. The 3P frequency can be very lightly observed above the 1P

pitch angles (θ₁, θ₂) for each bin, one could plot the blade pitch frequencies versus the average rotor speed. Such a plot is called a spectral waterfall plot and is shown in Figure 3.7. Rotor speeds below 22rpm were excluded from the analysis. Clearly, one can conclude from Figure 3.7 that the blade pitch angle frequency increases with rotor speed as desired. The 3P frequency can also (very lightly) be observed.

3.5.2. SINGLE DATASET RESULTS

A first performance analysis was conducted on full-length post-processed data sets. Three data sets with approximately the same operating conditions were chosen, and power spectral density plots of the important (load) signals were generated. The selected data sets³ are in above-rated wind conditions and a 10s moving average of the hub height wind speed measured at the met mast is shown in Figure 3.8. Figure 3.8 shows that the wind speeds over the complete data set are rather similar. For the selected datasets, the average wind speed and wind direction were calculated. Moreover, the wind shear exponent α (Manwell et al., 2002) using

\[ v(h) = v(h_0) \left( \frac{h}{h_0} \right)^\alpha , \]

with \( v(h) \) the wind speed at height \( h \) and \( v(h_0) \) the wind speed at a reference height \( h_0 \), was estimated from the wind speeds measured by the met mast. The turbulence intensity of the wind was calculated from the wind speed measured by the met mast at the hub height by dividing the standard deviation of the measured wind speed signal by the average wind speed. The results are listed in Table 3.1.

The power spectral densities of a number of measured signals for the aforementioned datasets are shown in Figure 3.9. The results indicate that both IPC methods perform equally well in removing the 1P blade loadings (upper two graphs). Both IPC

Table 3.1: Wind characteristics of sample datasets

<table>
<thead>
<tr>
<th></th>
<th>Average wind speed [m s(^{-1})]</th>
<th>Average wind direction [deg]</th>
<th>Estimated shear exponent</th>
<th>Turbulence intensity [%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Baseline</td>
<td>13.43</td>
<td>334.04</td>
<td>0.13</td>
<td>14.63</td>
</tr>
<tr>
<td>LIPC</td>
<td>12.48</td>
<td>34.94</td>
<td>0.15</td>
<td>14.53</td>
</tr>
<tr>
<td>IPC-MBC</td>
<td>12.36</td>
<td>336.07</td>
<td>0.14</td>
<td>13.86</td>
</tr>
</tbody>
</table>

Figure 3.8: Measured wind speed time series for the three different cases.

methods also fully remove the 1P rotating hub \(M_{hub,y}\) load, where the rotating hub moment \(M_{hub,y}\) is computed as the difference between the blade OoP bending moments \((M_{y,1}, M_{y,2})\). The removal of the rotating hub moment \(M_{hub,y}\) is important, because it makes a teeter hinge unnecessary (Bossanyi et al., 2013). The nacelle fore-aft acceleration \(a_{nac,fa}\) has some reductions around the 1P frequency and the tower mode, and the nacelle side-side acceleration \(a_{nac,ss}\) shows reductions around the 2P frequency (the blade passing frequency seen from the tower). The responses around the 1P frequency in the nacelle accelerations (most notably in the side-side acceleration \(a_{nac,ss}\)) must be caused by rotor imbalance (Bossanyi et al., 2013). The pitch activity can be observed in Figure 3.10 and it can be concluded that there is little difference between the two methods.

The power spectral densities shown in Figure 3.9 and Figure 3.10 also show the baseline controller case. That is, the case in which only the generator torque and speed are regulated and without active load reduction. Despite this, the baseline controller contributes to the 1P frequency and also to the 2P frequency (see Figure 3.10), which should ideally not be the case. The reason for the 1P and 2P frequency contributions in the collective pitch is that the CPC takes, among others, the generator speed as input. The generator speed signal consists of variations caused by rotor imbalances (1P) and variations in the aerodynamic torque (2P) of a two-bladed rotor. Because the rotor (imbalance) loads are transferred from the low-speed shaft through a gearbox to the high-speed shaft, the aforementioned loads are present in the generator speed and should ideally be filtered before inputting to the CPC. Moreover, the CPC controller is tuned rather aggressively (high bandwidth) and therefore reacts to the 1P and 2P disturbances. Simulations show that decoupling the CPC has a positive effect on the load reduction per-
3.5. Results

Figure 3.9: Power spectral densities of the fatigue inducing loads for the NREL CART2 turbine.
Another measure of load mitigation performance can be found in the teeter angle. The teeter angle of the CART2 can be locked or released with a hydraulic brake. If the pressure in the hydraulic system is high enough, the teeter angle should not vary when the teeter brake is applied. However, during the measurements the hydraulic pressure might not have been as high as desired. Therefore, dynamic loading of the rotor could result in changes in the teeter angle. Figure 3.11 shows the measured teeter angle for the three aforementioned data sets. The figure shows that the teeter angle varies significantly less when IPC is enabled, which implies its effectiveness.
3.5.3. Binned datasets results

The second performance assessment is based on many measurements obtained from April 9 to May 3, 2014. In total 153 baseline data sets (each of 300s length), 119 LIPC data sets, and 101 IPC-MBC data sets were obtained. All data sets were split into 30s data bins, and after post-processing the data according to the steps given at the start of this section, there are 1115 baseline bins, 687 LIPC bins, and 556 IPC-MBC bins left. The bins were grouped by computing the average wind speed for each bin and were distributed over the range of wind speeds according to Table 3.2. According to Table 3.2, the wind speeds that occurred most frequently during the measurement campaign were below 10 m s\(^{-1}\). This analysis included the wind speeds between 5 m s\(^{-1}\) and 15 m s\(^{-1}\) as these wind speeds had enough bins to obtain a reliable analysis. Note that the 15 m s\(^{-1}\) wind speed case of IPC-MBC must be considered with care because only 4 bins are available.

The load reduction analysis based on binned data was started by computing the Damage Equivalent Load (DEL) (Freebury and Musial, 2000) of the measured OoP blade bending moments \(M_{y,1}, M_{y,2}\). The slope of the S-N curve was set to \(m = 10\) (SN10) for the blades. Then, the average and standard deviation of all DELs per wind speed are computed and the results are plotted in Figure 3.12. The DELs of the rotating hub moment \(M_{\text{hub},y}\) are shown in the bottom figure and are computed with \(m = 4\) (SN4). The trends shown in Figure 3.12 confirm the observations from the power spectral density plots of the single data sets in Figure 3.9; both IPC methods show similar load reductions.

Despite the rotor asymmetry, the reductions in both blades seem to be on par, demonstrating that both strategies, without modification, can handle such imperfections. The DELs of the rotating hub moment \(M_{\text{hub},y}\) show a result similar to the reductions in the blade OoP bending moments \(M_{y,1}, M_{y,2}\). In Figure 3.13, the averaged standard deviations of the nacelle fore-aft acceleration \(a_{\text{nac,fa}}\) and side-side acceleration \(a_{\text{nac,ss}}\) are shown. The figure shows that the nacelle fore-aft acceleration \(a_{\text{nac,fa}}\) and side-side acceleration \(a_{\text{nac,ss}}\) are mainly reduced around rated wind conditions. The calculation results in Figure 3.12 and Figure 3.13 are backed up in Table 3.3 and Table 3.4, where the percent load reductions for both IPC methods with respect to the baseline case are listed.

<table>
<thead>
<tr>
<th>Wind speed [m s(^{-1})]</th>
<th>(\leq 4)</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
</tr>
</thead>
<tbody>
<tr>
<td>Baseline</td>
<td>111</td>
<td>153</td>
<td>179</td>
<td>128</td>
<td>136</td>
<td>121</td>
<td>76</td>
</tr>
<tr>
<td>LIPC</td>
<td>32</td>
<td>87</td>
<td>115</td>
<td>129</td>
<td>79</td>
<td>61</td>
<td>57</td>
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<td>12</td>
<td>65</td>
<td>102</td>
<td>102</td>
<td>72</td>
<td>53</td>
<td>44</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Wind speed [m s(^{-1})]</th>
<th>11</th>
<th>12</th>
<th>13</th>
<th>14</th>
<th>15</th>
<th>16</th>
<th>17</th>
</tr>
</thead>
<tbody>
<tr>
<td>Baseline</td>
<td>63</td>
<td>60</td>
<td>48</td>
<td>25</td>
<td>13</td>
<td>2</td>
<td>0</td>
</tr>
<tr>
<td>LIPC</td>
<td>46</td>
<td>34</td>
<td>27</td>
<td>7</td>
<td>10</td>
<td>3</td>
<td>0</td>
</tr>
<tr>
<td>IPC-MBC</td>
<td>37</td>
<td>26</td>
<td>24</td>
<td>12</td>
<td>4</td>
<td>2</td>
<td>1</td>
</tr>
</tbody>
</table>
3. Field Testing of Linear Individual Pitch Control on the NREL CART2

Figure 3.12: Average DELs and standard deviations of the IPC strategies for binned data.

Figure 3.13: Average standard deviations (avg. std.) of nacelle accelerations for binned data.
The remainder of this section is devoted to a number of additional results obtained from the binned data. The average standard deviation of the IPC pitch angle (where only the IPC contributed part is considered by subtracting the CPC pitch angle) is calculated for all bins and shown in the top left graph of Figure 3.14. As shown, both IPC strategies roughly required the same amount of pitch activity to achieve the load reductions. As was stated in Section 3.4.4, and shown in the top two graphs, larger pitch actions were required at low wind speeds to mitigate the blade loads (this was also discussed in Section 3.4.4), because of a lower control authority at low wind speeds. The top right graph shows the average standard deviation of the teeter angle, and it is apparent that IPC substantially reduces the amount of variations. In the lower left graph, the average electrical power output of the wind turbine is shown. Remarkably, the graphs imply that by using IPC, the power output is increased. However, because IPC in principle should not contribute to power production this requires some attention. To obtain more insight, consider the lower right graph in Figure 3.14. Here, the electrical power output is plotted for the case when the nacelle wind speed is used to create the data bins (in the other results the met mast wind speed at hub height was used). The lower right figure shows that the differences between electrical power output for the different cases disappear. These differences are most likely accounted to the differences between the wind conditions at the met mast and the wind turbine itself. By reducing the bins in time, e.g., by considering bins of 5 s length instead of 30 s, the differences (not shown) also become smaller for the case when the met mast wind speed is used. Moreover, it is assumed that by collecting more data, the differences in the lower left graph of Figure 3.14 will become smaller.

3.6. CONCLUSIONS

In this chapter, the LIPC methodology is experimentally validated through field tests on the 570 kW NREL CART2 wind turbine. The LIPC strategy for once-per revolution (1P) blade load reduction involves a single feedback loop using a simple linear coordinate transformation of the blade root moments. By gain scheduling LIPC on the rotor speed, it was successfully applied both in below-rated and above-rated operating conditions. The LIPC strategy is compared to the conventional IPC strategy, which involves the MBC transformation. Earlier work showed that simulation studies predict similar performance in terms of load reductions and pitch duty for both methods. This was confirmed in this chapter by a measurement campaign on the NREL CART2, for which both IPC methods were shown to perform on par. The field tests indicated that the LIPC strategy can readily be applied to wind turbines and achieve load reductions similar to the conventional IPC strategy.
Figure 3.14: Various performance indicators based on binned data. In the bottom right figure, the bins were obtained by using the wind speed measured at the nacelle instead of the wind speed measured at the met mast.
Table 3.3: Percent reduction of DELs and average standard deviations based on binned data ($v = 5 - 10 \text{ m s}^{-1}$).

<table>
<thead>
<tr>
<th>$v$ [m s$^{-1}$]</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
</tr>
</thead>
<tbody>
<tr>
<td>DEL: Blade 1 Out-of-Plane root bending moment $M_{y,1}$ (SN10)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Baseline [kNm]</td>
<td>$3.92 \times 10^1$</td>
<td>$5.07 \times 10^1$</td>
<td>$6.73 \times 10^1$</td>
<td>$9.23 \times 10^1$</td>
<td>$1.08 \times 10^2$</td>
<td>$1.32 \times 10^2$</td>
</tr>
<tr>
<td>LIPC [%]</td>
<td>−9.4</td>
<td>4.4</td>
<td>12.1</td>
<td>10.4</td>
<td>11.3</td>
<td>12.7</td>
</tr>
<tr>
<td>IPC-MBC [%]</td>
<td>−0.5</td>
<td>5.8</td>
<td>14.4</td>
<td>13.5</td>
<td>5.7</td>
<td>15.8</td>
</tr>
<tr>
<td>DEL: Blade 2 Out-of-Plane root bending moment $M_{y,2}$ (SN10)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Baseline [kNm]</td>
<td>$4.47 \times 10^1$</td>
<td>$5.96 \times 10^1$</td>
<td>$7.91 \times 10^1$</td>
<td>$1.12 \times 10^2$</td>
<td>$1.30 \times 10^2$</td>
<td>$1.56 \times 10^2$</td>
</tr>
<tr>
<td>LIPC [%]</td>
<td>5.1</td>
<td>12.5</td>
<td>14.3</td>
<td>11.7</td>
<td>13.2</td>
<td>11.5</td>
</tr>
<tr>
<td>IPC-MBC [%]</td>
<td>3.7</td>
<td>6.4</td>
<td>15.2</td>
<td>15.0</td>
<td>7.2</td>
<td>11.4</td>
</tr>
<tr>
<td>DEL: Rotating hub $M_{hub,y}$ (SN4)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Baseline [kNm]</td>
<td>$4.87 \times 10^1$</td>
<td>$6.31 \times 10^1$</td>
<td>$8.40 \times 10^1$</td>
<td>$1.19 \times 10^2$</td>
<td>$1.38 \times 10^2$</td>
<td>$1.60 \times 10^2$</td>
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<tr>
<td>LIPC [%]</td>
<td>5.4</td>
<td>13.4</td>
<td>18.3</td>
<td>12.0</td>
<td>14.8</td>
<td>17.1</td>
</tr>
<tr>
<td>IPC-MBC [%]</td>
<td>7.7</td>
<td>11.8</td>
<td>20.5</td>
<td>21.8</td>
<td>15.8</td>
<td>25.6</td>
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<tr>
<td>Avg. std.: Nacelle fore-aft acceleration $a_{nac,fa}$ (SN4)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>Baseline [m s$^{-2}$]</td>
<td>$4.97 \times 10^{-2}$</td>
<td>$7.75 \times 10^{-2}$</td>
<td>$1.41 \times 10^{-1}$</td>
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<td>LIPC [%]</td>
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<td>1.4</td>
<td>5.2</td>
<td>3.6</td>
<td>−13.8</td>
<td>16.7</td>
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<tr>
<td>Avg. std.: Nacelle side-side acceleration $a_{nac,ss}$ (SN4)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Baseline [m s$^{-2}$]</td>
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<td>$8.23 \times 10^{-2}$</td>
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<td>LIPC [%]</td>
<td>−30.1</td>
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<td>7.8</td>
<td>11.0</td>
<td>1.0</td>
<td>18.5</td>
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<tr>
<td>IPC-MBC [%]</td>
<td>3.2</td>
<td>−2.6</td>
<td>4.8</td>
<td>−1.9</td>
<td>−13.4</td>
<td>23.0</td>
</tr>
</tbody>
</table>
Table 3.4: Percent reduction of DELs and average standard deviations based on binned data ($v = 11 - 15 \text{ m s}^{-1}$).

<table>
<thead>
<tr>
<th>$v$ [m s$^{-1}$]</th>
<th>11</th>
<th>12</th>
<th>13</th>
<th>14</th>
<th>15</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>DEL: Blade 1 Out-of-Plane root bending moment $M_{y,1}$ (SN10)</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Baseline [kNm]</td>
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<td>$2.06 \times 10^2$</td>
<td>$2.11 \times 10^2$</td>
</tr>
<tr>
<td>LIPC [%]</td>
<td>18.3</td>
<td>18.7</td>
<td>15.1</td>
<td>15.0</td>
<td>9.4</td>
</tr>
<tr>
<td>IPC-MBC [%]</td>
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<td>17.0</td>
<td>7.0</td>
<td>11.0</td>
<td>22.0</td>
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<td><strong>DEL: Blade 2 Out-of-Plane root bending moment $M_{y,2}$ (SN10)</strong></td>
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</tr>
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<td>11.2</td>
<td>6.6</td>
</tr>
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<td>IPC-MBC [%]</td>
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<td>15.4</td>
<td>5.9</td>
<td>9.2</td>
<td>17.0</td>
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<tr>
<td><strong>DEL: Rotating hub $M_{hub,y}$ (SN4)</strong></td>
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<td>19.6</td>
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<td><strong>Avg. std.: Nacelle fore-aft acceleration $a_{nac,fa}$ (SN4)</strong></td>
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<td></td>
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<td>Baseline [m s$^{-2}$]</td>
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<td>1.4</td>
<td>$-14.8$</td>
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<td>IPC-MBC [%]</td>
<td>27.2</td>
<td>27.1</td>
<td>22.2</td>
<td>$-15.8$</td>
<td>7.6</td>
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<tr>
<td><strong>Avg. std.: Nacelle side-side acceleration $a_{nac,ss}$ (SN4)</strong></td>
<td></td>
<td></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>Baseline [m s$^{-2}$]</td>
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</tr>
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<td>14.2</td>
<td>8.6</td>
<td>$-13.6$</td>
<td>$-1.7$</td>
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</table>
4

CONTROL DESIGN FOR TWO-BLADED DOWNWIND FREE-YAW WIND WIND TURBINES

In this chapter, a control architecture for a two-bladed downwind teeterless damped free-yaw wind turbine is developed. The wind turbine features a physical yaw damper which provides damping in the yawing motion of the rotor-nacelle assembly. Individual Pitch Control (IPC) is employed to obtain yaw control so as to actively track the wind direction and to reduce the turbine loads. The objectives of the yaw-by-IPC and IPC for load reduction are conflicting and therefore two decoupling strategies are presented and compared in terms of loads, power production, and stability. The design of the different controllers and the physical yaw damping are coupled and have a large impact on the turbine loads. It is shown that the tuning of the controllers and the choice of the yaw damping value involve a tradeoff between blade loads and tower loads. All results have been obtained by high-fidelity simulations of the state-of-the-art 2-B Energy 2B6 wind turbine.

4.1. INTRODUCTION

With the goals set by the European Union for the year 2020 and 2030 (European Wind Energy Association, 2012; European Council, 2014), offshore wind energy has a bright future. Although the total amount of offshore wind power is planned to strongly increase for the next decades, offshore wind has, however, still a bottleneck: the cost of energy. To drive down the cost of (offshore) wind energy, different opportunities exist. Considering the past decades, manufactures have steadily increased the size of wind turbines. With increasing size, rated speed and power are reached at lower wind speeds yielding an increase in annual generated power and enables deployment in easier accessible areas. Moreover, with the implementation of active load reduction techniques, loads can be kept at a certain level such that a lighter design can be obtained, which means a reduced amount of material.

In the ongoing effort of reducing the cost of energy, an interesting opportunity can be found in two-bladed wind turbines. Two-bladed wind turbines have been developed
and built during the seventies and eighties of the previous century (see for example Hau (2006); Spera (2009) or refer for more details of wind turbine developments in that period to General Electric Company (1984) and Spera et al. (1977)). For different reasons, at the end of the eighties the focus completely shifted to three-bladed wind turbines, which to this day dominate the landscape. Compared to three-bladed wind turbines, two-bladed wind turbines have several advantages and disadvantages:

- Two-bladed wind turbines have the advantage of saving the material of one blade. It is estimated that the total weight of a two-bladed rotor is 70% of a three-bladed rotor (Aerodyn engineering GmbH, 2014) for equally rated capacities;

- The rotor of two-bladed wind turbines has a higher rotational speed and, hence, the torque on the shaft is lower such that the drivetrain and nacelle (which houses the generator, drivetrain, etc.) are lighter;

- Two-bladed rotors have several advantages during transportation and installation (De Vries, 2011). For example, the nacelle and a two-bladed rotor can be transported fully assembled and tested on a ship to the construction site. Moreover, the assembly can be lifted at once on top of the tower;

- Two-bladed wind turbines have the disadvantage of increased fatigue loadings. Three-bladed wind turbines have a rather uniform load transfer from the blades to the shaft, whereas the load transfer of a two-bladed wind turbine is varying with rotor azimuth causing higher shaft bending loads and yaw moments (Hau, 2006);

- Two-bladed wind turbines suffer from noise and visual impacts. The noise aspect is caused by the higher rotational speed of a two-bladed rotor and consequently increased acoustic noise levels (Madsen et al., 2007). Furthermore, it is well-known that the beam-like rotor of a two-bladed turbine gives a restless view during operation (Hau, 2006). These drawbacks disappear at offshore locations.

With the increased deployment of wind turbines in offshore locations and by overcoming the disadvantages of two-bladed rotors, two-bladed wind turbines can become an interesting choice in order to further decrease the cost of energy.

In the past couple of years, the wind energy community has renewed its interest in two-bladed wind turbines. That is, there has been a substantial number of publications regarding two-bladed wind turbines (to mention a few Larsen et al. (2007); Schorbach and Dalhoff (2012); van Solingen and van Wingerden (2015); van Solingen et al. (2015b); Bergami et al. (2014); Kim et al. (2014b); Luhmann and Cheng (2014)), but also a number of new two-bladed designs have been developed and built in recent years. An overview of two-bladed wind turbine designs since the year 2000 can for instance be found in Schorbach and Dalhoff (2012) (including the references therein) and in Snieckus (2014), of which a few will be mentioned here. An interesting two-bladed wind turbine is developed by Envision (Envision, 2015). This is a 3.6MW turbine design featuring blades with partial pitch. This enables the turbine to pitch the outer section of the blades such that extreme loads can be reduced (Kim et al., 2014b,a). Another recent two-bladed wind turbine concept with a rated power of 6.1 MW is developed by Condor Wind Energy (Condor Wind Energy, 2015). Power control in above-rated winds for this turbine is achieved
through active yaw control and a teetering hinge is used to reduce the yaw moments. A 3.5 MW two-bladed wind turbine prototype has been built by SkyWind (Luhmann and Cheng, 2014). This turbine uses a tumbling rotor and individual pitch control to reduce fatigue loadings. Finally, a floating wind turbine is being developed by Nautica Windpower (Nautica Windpower, 2015). The downwind floating turbine is able to operate in water depths over 60 metres.

Another novel two-bladed wind turbine design, called the 2B6 (2-B Energy, 2015), is being developed by 2-B Energy in the Netherlands. This is a 6 MW downwind turbine with a 140.6 m rotor diameter and a damped free-yaw system. Among others, the novelties of the full modular two-bladed 2B6 wind turbine are:

1. a downwind rotor configuration;
2. a damped free-yaw system;
3. a full three-leg jacket support structure.

Moreover, the 2B6 has a helicopter deck on top of the nacelle for ease of access and has the possibility to include a transformer deck in the jacket support structure. An illustration of the turbine is shown in Figure 4.1. An extensive description of the novelties of the 2B6 turbine is given in Section 4.2.

As mentioned above, a drawback of two-bladed wind turbines is the increased fatigue loadings due to the dynamics of a two-bladed rotor, which could possibly be overcome with active control methodologies becoming available. It is well-known within the wind energy community that wind turbine loads can be reduced by using Individual Pitch Control (IPC), which has been a topic of interest over the past decade and was
proposed in e.g., Caselitz et al. (1997). In Bossanyi (2003, 2005), IPC based on the Multi-Blade Coordinate (MBC) (Bir, 2008; Stol et al., 2009; Hohenemser and Yin, 1972) transformation is proposed. By using the MBC transformation, the blade root moments of a wind turbine can be transformed to a decoupled tilt and yaw moment. Then, by separately integrating the obtained tilt and yaw moment and reverse transforming the integrated moments, periodic blade pitch signals are obtained. A fair amount of literature has appeared on IPC, e.g., see Kanev and van Engelen (2009); van Engelen (2009); Selvam et al. (2009); Houtzager et al. (2013); Geyler and Caselitz (2008); Wright et al. (2009); Wright and Stol (2010); Wright et al. (2011); Navalkar et al. (2014b). A number of field test experiments of IPC have been performed, of which the most notable can be found in Bossanyi et al. (2013). It is expected that IPC remains effective when upscaling wind turbines to the 10 – 15 MW range (Chen and Stol, 2014).

Only few literature can be found that include IPC for two-bladed wind turbines. In Larsen et al. (2007), a study is presented in which teeter angle excursions for a two-bladed downwind rotor are reduced by using IPC. Three different IPC strategies were considered generating IPC setpoints based on measurements of the teeter angle. The results show that a controller which takes both the measured teeter angle and the teeter velocity as input, is most effective. Recently, a Linear Individual Pitch Control (LIPC) strategy specifically intended for two-bladed wind turbines was proposed in van Solingen and van Wingerden (2015). In this strategy the nonlinear MBC transformation is replaced by a linear coordinate transformation. The coordinates obtained with the linear transformation can be thought of as a collective mode and a differential mode. In the former mode, all even blade load harmonics are contained and in the latter mode all odd blade load harmonics are contained. As such, only a single feedback loop is required to reduce the dominant once-per-revolution (1P) blade loads. Moreover, at most two feedback loops are needed to potentially reduce all periodic blade loads. The LIPC strategy has been successfully demonstrated in simulations (van Solingen and van Wingerden, 2015, 2014), wind tunnel tests (van Solingen et al., 2014b), and on the NREL CART2 wind turbine (van Solingen et al., 2015b). In the latter reference it is shown that the LIPC strategy and IPC using the MBC transformation yield similar load reductions. A possible drawback of LIPC is that the transformed coordinates do no longer relate to tilt and yaw moments. Therefore, for free-yaw wind turbines one has to resort to IPC design using the MBC transformation.

A downwind damped free-yaw wind turbine offers several possibilities for wind direction tracking. A downwind free-yaw configuration will naturally track the wind with some misalignment and variations around an equilibrium yaw angle depending on the wind speed. The equilibrium yaw angle is the angle where the 1P blade tends to be minimal (Hansen, 1992) and, hence, in below-rated operating conditions not the maximum amount of energy will be extracted from the wind. In order to improve wind turbine tracking and thereby electrical power output in below-rated winds, one could use yaw-by-IPC. That is, by individually pitching the blades over a rotor revolution, a yawing moment can be generated that aligns the rotor-nacelle assembly with the wind. IPC for yaw control has been applied to wind turbines by means of periodic state-space control in Zhao and Stol (2007) and by using the MBC transformation in Navalkar et al. (2014a). These studies have demonstrated that IPC is able to keep the rotor-nacelle assembly of
three-bladed wind turbines in upwind yaw configurations aligned with the wind.

In this chapter, the controller design for a downwind two-bladed damped free-yaw wind turbine is analyzed. An important factor during the design process is the amount of yaw damping provided by the system and is therefore also investigated. Designing the controller and finding the optimal yaw damping value is an interesting case study from a mechatronics point of view, because the design of the involved controllers and the yaw damping are coupled and both significantly affect the turbine loads. Throughout the chapter, different control loops and possible control configurations are discussed and demonstrated for various yaw damping values using high-fidelity simulations. Moreover, the impact of actively adding yaw damping by means of IPC is investigated. The main contributions of this chapter are:

- Control design for a teeterless downwind two-bladed damped free-yaw wind turbine;
- Comparison and consequences for different configurations of the yaw and load reduction controllers;
- Investigation of the impact of various controllers on turbine loading;
- Investigation of the impact of passive yaw damping and active yaw-damping-by-IPC on the turbine loading;
- Analysis of the impact of an extreme wind direction change on a damped free-yaw turbine.

The chapter is organized as follows. In the section hereafter, the main properties and advantages of the novel 2-B Energy 2B6 wind turbine are described. Subsequently, in Section 4.3, the control system for power production, load control, and yaw control is outlined. In Section 4.4 the design of the yaw controller is discussed. Subject of this section are two strategies to combine the yaw controller with the conventional IPC controller, obtaining a model of the yaw dynamics and the design of the yaw controller. Furthermore, the concept of providing yaw damping to the rotor-nacelle assembly by means of IPC is introduced in Section 4.4. The results of different yaw system configurations, control strategies, and yaw damping are analyzed in Section 4.5. Finally, in Section 4.6 the chapter is concluded.

4.2. Wind Turbine Description

The controller design in this chapter is tailored to the 2-B Energy 2B6 wind turbine shown in Figure 4.1. This wind turbine has a rated output of 6MW (reached around a wind speed of 13 m s\(^{-1}\)) and the two-bladed rotor has a diameter of roughly 140 m. The most important information of the wind turbine is listed in Table 4.1. It should be noted here that some of the wind turbine details are subject to confidentiality and cannot be given for that reason. Hence, throughout this chapter some details are omitted (mainly pronounced in many figures without axes labels and the physical yaw damping values not being mentioned explicitly).

The 2B6 design has a number of unique features:
**Full three leg jacket support structure:** A jacket support structure has the advantage of a less disturbed wind flow. This is demonstrated in an experimental comparison of tower shadow for a monopile and a truss structure in Reiso et al. (2011). The findings are that a truss structure tower wake has lower turbulence intensities than a tubular tower case, indicating that loads caused by tower shadow will be lower when using a truss structure. A jacket support structure also has disadvantages (Damgaard, 2014), i.e., the welding of the tubular joints is labour intensive and the costs associated with transport and maintenance are higher.

**Downwind rotor configuration:** The rotor-nacelle assembly of the wind turbine has a downwind configuration. This means that one of the design driving properties of a wind turbine becomes less critical. That is, the tower clearance plays a larger role in an upwind configuration than in a downwind configuration. The blades can therefore also be designed to be more flexible thereby saving material.

**Damped free-yaw system:** The novel downwind rotor configuration in combination with the damped free-yaw system of the 2B6 also brings several advantages. To start off with, a recently published study by Stubkier et al. (2013) claims that the use of a soft-yaw system\(^1\) reduces the tower fatigue loads by 40% and ultimate loads by 19%, and even more in case an overload protection system in the hydraulic yaw system is introduced. Secondly, a free-yaw wind turbine can also have a positive impact on the extracted power from the wind, because it offers the possibility of continuous wind direction tracking. Furthermore, yaw misalignments for load reduction (Kragh and Hansen, 2014) can easily be incorporated and, in the context of wind farms, a free-yaw wind turbine with yaw-by-IPC could be used for wake redirection and thereby increasing the total wind farm power output (Gebraad et al., 2014). On the other hand, a challenge for a damped free-yaw rotor-nacelle assembly comes from gyroscopic effects. Although the rotor is damped in the yaw rotation, changes in the wind (direction) can cause the yaw rates to increase and thereby also the turbine loads. Moreover, the mass of inertia of a two-bladed rotor is dependent on the rotor position, which causes higher loads on the yaw system (Hau, 2006; Schorbach and Dalhoff, 2012).

**Individual Pitch Control (IPC):** The wind turbine uses IPC for load control. For a two-bladed wind turbine without a teetered hinge, IPC can be used to compensate cyclic shaft bending moments as stated in Bossanyi et al. (2013) through 1P blade load control.

The 2B6 design consists of other innovative solutions, but these are less important for the scope of this chapter and are for that reason not mentioned here. The interested reader is referred to the website of 2-B Energy (2-B Energy, 2015) for more information.

A model of the 2B6 wind turbine that describes the dynamics of the wind turbine was supplied by 2-B Energy. The wind turbine is modeled to have a small rotor mass imbalance and some aerodynamic imbalance is introduced by a 0.3° pitch offset in

\(^1\)Refer to Kim and Dalhoff (2014) for an overview of yaw systems and related patents for wind turbines, and refer to Stubkier and Pedersen (2011) for a design of a soft-yaw system for 5MW turbine.
### Table 4.1: 2-B Energy 2B6 wind turbine specifications (2-B Energy, 2015)

<table>
<thead>
<tr>
<th>Description</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rated power</td>
<td>6 MW</td>
</tr>
<tr>
<td>Rotor diameter</td>
<td>140.6 m</td>
</tr>
<tr>
<td>Hub height</td>
<td>95 m - 100 m</td>
</tr>
<tr>
<td>Orientation</td>
<td>Downwind</td>
</tr>
<tr>
<td>Support structure</td>
<td>Full 3 leg jacket</td>
</tr>
<tr>
<td>Yaw system</td>
<td>Active - soft/damped</td>
</tr>
</tbody>
</table>

blade 2 (IEC, 2005; Germanischer Lloyd, 2005). The flexible yaw configuration is modeled to include yaw friction. The software GH Bladed 4.20 (Garrad Hassan, 2014; Garrad Hassan & Partners Ltd, 2014), which is a certified and widely used wind turbine design software package in industry, is used to simulate the turbine response subject to three-dimensional turbulent wind fields throughout this chapter. The Bladed software package allows for testing of new control algorithms by compiling controllers designed in MATLAB Simulink® (Mathworks, 2013) to a DLL file (Houtzager, 2011), which is used during the simulations through a DLL interface. The 2B6 wind turbine has a full jacket structure which can be modeled with a commercially available additional package within GH Bladed. However, due to commercial reasons a monopile support structure with (almost) the same dynamics as the full jacket support structure was used during the simulations.

It should be stressed that the control architectures and involved controllers developed and tuned throughout this chapter do not reflect the control architecture and implementation of 2-B Energy.

### 4.3. CONTROL SYSTEM DESCRIPTION

The general control configuration used in this chapter is shown in Figure 4.2. The control system consists of the torque controller, which regulates the generator torque $T_{trq}$ in below-rated operating conditions and the CPC which regulates the collective blade pitch $\theta_{col}$ in above-rated operating conditions. The control system also includes a drivetrain damper preventing large oscillations in the drivetrain. The drivetrain damper typically adds a torque ripple $T_{dtd}$ to the torque setpoint $T_{trq}$ of the torque controller. The design of these controllers can be carried out according to Bossanyi (2000). Because this chapter mainly concentrates on the design of yaw and load controllers, the power production controllers are not further discussed. Moreover, the control system can be extended with tower load controllers (Bossanyi et al., 2012, 2013; Fleming et al., 2013) or aerodynamic balancing through pitch control (Duckwitz and Shan, 2014), but is not within the scope of this chapter.

In a damped free-yaw wind turbine, where IPC is used to provide wind direction tracking, an additional feedback loop for yaw control is required. The yaw controller takes as input the error $\phi$ between a reference yaw setpoint $\phi_{ref}$ and the current measured yaw error $\phi_{yaw}$, which is the error between the yaw angle position of the wind turbine and the wind direction. A Proportional Integral (PI) controller can then be used...
Figure 4.2: Schematic block diagram of a two-bladed wind turbine control system with the torque controller (active in the below-rated region), the CPC (active in the above-rated region) and the IPC and yaw controller (including the forward and reverse coordinate transformations) to reduce turbine loads and to provide yaw-by-IPC.
to regulate the individual blade pitches \((\theta_1, \theta_2)\) such that a yaw moment is created that removes the yaw error \(\phi\). Moreover, the individual blade pitches \((\theta_1, \theta_2)\) can be simultaneously used to reduce the wind turbine loads based on measurements of the Out-of-Plane (OoP) blade root bending moments \((M_{y,1}, M_{y,2})\) (refer to (Garrad Hassan & Partners Ltd, 2014) for the frame of reference). The individual blade pitch angles \((\theta_1, \theta_2)\) are summed with the collective pitch angle \(\theta_{col}\) and the resulting pitch angles \((\Theta_1, \Theta_2)\) are passed to the pitch actuators.

The typical approach for IPC is to use the MBC transformation (Bir, 2008; Stol et al., 2009) as depicted in Figure 4.3. The main principle is to transform the blade root moments \((M_{y,1}, M_{y,2})\) measured in a rotating frame of reference to a non-rotating frame of reference. In fact, the blade root moments \((M_{y,1}, M_{y,2})\) are transformed to rotor tilt \(M_{\text{tilt}}\) and yaw \(M_{\text{yaw}}\) moments. Then, an integral controller integrates the transformed moments and the result is a tilt \(\theta_{\text{tilt}}\) and yaw \(\theta_{\text{yaw}}\) pitch angle in the non-rotating frame of reference. Finally, passing \((\theta_{\text{tilt}}, \theta_{\text{yaw}})\) through the reverse MBC transformation and low-pass filtering with \(L_\theta(s)\) yields the blade pitch angles \((\theta_1, \theta_2)\) in the rotating frame of reference.

The main working principle of the MBC transformation is to map rotating frequencies to different frequencies in the non-rotating frame of reference. To see this, consider the forward MBC transformation given by

\[
\begin{bmatrix}
  M_{\text{tilt}} \\
  M_{\text{yaw}}
\end{bmatrix} =
\begin{bmatrix}
  \cos(n\psi) & \cos(n[\psi + \pi]) \\
  \sin(n\psi) & \sin(n[\psi + \pi])
\end{bmatrix}
\begin{bmatrix}
  M_{y,1} \\
  M_{y,2}
\end{bmatrix}
\]

(4.1)

and the reverse MBC transformation given by

\[
\begin{bmatrix}
  \theta_1 \\
  \theta_2
\end{bmatrix} =
\begin{bmatrix}
  \cos(n\psi) & \sin(n\psi) \\
  \cos(n[\psi + \pi]) & \sin(n[\psi + \pi])
\end{bmatrix}
\begin{bmatrix}
  \theta_{\text{tilt}} \\
  \theta_{\text{yaw}}
\end{bmatrix},
\]

(4.2)

where \(\psi\) is the rotor azimuth angle, \(n\) is the harmonic number, and \(\delta_{nP}\) is an azimuth angle offset. The phase shift of \(\pi\) in the transformation matrices indicates the \(180^\circ\) difference between the two rotor blades. It can be shown that a 1P frequency in the blade root moments \((M_{y,1}, M_{y,2})\) passed through the forward transformation is transformed to a 0P frequency (a constant) in the non-rotating frame. After integrating the 0P signal and after reverse transforming, a 1P frequency signal is obtained which is passed through the low-pass filter \(L_\theta\). Note that the integral controllers also have notch filters at the 2P and 4P frequency to remove unwanted higher harmonic frequencies. The offset \(\delta_{nP}\) is used to add phase lead to the control loop in order to overcome phase losses due to actuator dynamics and signal filtering and offers therefore an additional degree-of-freedom during controller design (Bossanyi and Witcher, 2009b).

The design of the yaw controller and IPC for load reduction is discussed in the next section.

4.4. YAW CONTROL DESIGN

The yaw-by-IPC control loop can be configured in different ways, each having its own specific advantages and disadvantages. It is beneficial to have a (control-oriented) model of the yaw dynamics, such that the yaw controller can be designed more easily.
Therefore, in the next section, a model of the yaw dynamics is obtained from an identification experiment, of which initial results are published in van Solingen et al. (2015c). Then, in the subsequent sections, two yaw control configurations and their controller designs are discussed. Finally, the impact of the yaw damping provided by the yaw system on the yaw control design is discussed.

4.4.1. Obtaining a Yaw Model

As a first step, a model of the yaw dynamics is sought such that the yaw controller can be designed using loopshaping techniques. Taking into account that the dynamics of a wind turbine are non-linear and have periodic components, a first-principles yaw model containing all these effects is likely to be of high order. For that reason, a low-order control-oriented model with the important dynamics in the frequency range of interest can be valuable. In the case of tracking the wind direction by means of IPC, the yaw controller should only provide gradual changes in the pitch setpoint (i.e., low-frequency control action). A model of the yaw dynamics should therefore accurately model the low-frequent yaw dynamics. In the work of Stubkier and Pedersen (2011) a second-order yaw model was matched with the use of simulated yaw response data. This motivated the use of a low-order model and from experiments it was found that a first-order transfer function appended with a time delay approximation is already sufficient. Therefore, consider the following parameterization of a first-order transfer function

\[ G_{yaw}(s) = \frac{\kappa}{1/(2\pi \tau) s + 1} e^{-sT_d} \]  

(4.3)

where \( \kappa \) and \( \tau \) are two parameters that respectively determine the gain and cut-off frequency of the first-order system. The time delay \( T_d \) can be modeled by a Padé approximation. To design a PI yaw controller of the form

\[ C_{yaw}(s) = K_p + \frac{K_i}{s} \]  

(4.4)

the parameters \((\kappa, \tau)\) in (4.3) need to be found. Different strategies can be pursued to find these parameters. In van Solingen et al. (2015c), the authors have used the method which is presented in Chapter 5 for this purpose.

\( \text{The Variance Accounted For (VAF) (Verhaegen and Verdult, 2007), computed for first-order and second-order identified models, were almost identical.} \)
The system identification experiment is carried out as follows. The wind turbine is excited by creating a randomly varying yaw moment for a certain wind speed. Then, by measuring the yaw misalignment of the turbine, the model parameters of (4.3) can be identified. The random yaw moment can be obtained by setting a slowly varying random signal as $\theta_{\text{yaw}}$ in Figure 4.3. Because of the free-yaw downwind turbine, which automatically aligns with the wind, no active controller is required. Thus, the loop is broken right after both integral controllers in Figure 4.3. A set of open-loop input-output data is then obtained by measuring both the yaw excitation signal $\theta_{\text{yaw}}$ and yaw misalignment response $\phi_{\text{yaw}}$, from which the model parameters can be identified. In the experiments, the measured yaw error $\phi$ was passed through a second-order low-pass filter (because we are only interested in the low-frequency dynamics) given by

$$L_{\phi} = \frac{\omega_{\text{yaw}}^2}{s^2 + 2\omega_{\text{yaw}}\beta_{\text{yaw}}s + \omega_{\text{yaw}}^2}, \quad (4.5)$$

where $\beta_{\text{yaw}} = 0.7$ and $\omega_{\text{yaw}} = 2\pi f_{\text{yaw}}$ with $f_{\text{yaw}} = 0.1$ Hz.

The identification procedure has been carried out for constant wind speeds with fixed wind direction. In total, an experiment of 90 min simulation time was considered of which 60 min was used for identification and 30 min for validation. The excitation signal $\theta_{\text{yaw}}$ was chosen to be a random binary sequence, such that the amplitude of $\theta_{\text{yaw}}$ was $\pm 1^\circ$. Then, a transfer function of the form (4.3) was identified from the input-output data. The time delay was experimentally found to be roughly 0.75 s and is modeled by a second-order Padé approximation. In Figure 4.4, the measured yaw response and the simulated yaw response are compared. It can be observed that the simulated response of the obtained model is close to the measured response. To quantify the latter result, the Variance Accounted For (VAF) (Verhaegen and Verdult, 2007) is an often used measure to indicate how close two signals are. For the result in Figure 4.4, the VAF is calculated to be roughly 93%.

The impact of different yaw damping values on the yaw dynamics was analyzed by repeating the above identification process for varying yaw damping values and wind speeds. In this chapter, five different yaw damping values are considered. Due to confidentiality reasons, the damping values cannot be given and are instead denoted by $\varnothing$ for the case of a free-yaw configuration and by I-IV for damping values varying from a
small value to a larger value. To visualize the effect of different damping values for a given wind speed, the identification procedure was repeated for each of the yaw damping values and the resulting Bode diagrams are shown in Figure 4.5. This figure shows that the cut-off frequency of the identified models decreases with increasing yaw damping. The latter observation is also expected from a physical perspective, because for increasing damping the yaw rotation is increasingly damped and, hence, responds slower to changes (excitation) of the yaw setpoint. With the obtained control-oriented models, the yaw controller can be designed, which will be the topic of the next subsections.

4.4.2. Yaw Control Strategies

The design of a yaw controller can be carried out in different ways. For example, in Zhao and Stol (2007) active yaw control using a periodic state-space IPC strategy was demonstrated on a 1.5MW three-bladed upwind wind turbine. The power extraction and speed regulation remained unaffected compared to a conventional yaw control with yaw drives, while the fatigue loads were kept in an acceptable range by using yaw brakes and other tower load controllers. Another strategy, suggested in Navalkar et al. (2014a), makes use of the MBC transformation. In this reference, the strategy is to create a yaw pitch setpoint in the non-rotating frame of reference and reverse transform this to the rotating frame of reference such that the resulting individual blade pitch setpoints create a yawing moment.

In this chapter, a similar approach to Navalkar et al. (2014a) is taken to design the yaw controller. That is, the MBC transformation will be used to transform yaw setpoint signals in the non-rotating frame of reference to the rotating frame. The main benefit of using the MBC transformation is that the yaw controllers can be LTI and, hence, classical control design methods can be used. Moreover, it can be combined with the conventional IPC strategy for load reduction as it also uses the MBC transformation.

The coupling between the yaw controller and the IPC for load reduction is an important factor in the design process. It should be stressed that the objectives of load reduction by IPC and yaw control by IPC are conflicting. More specifically, in below-rated operating conditions, the power output will be maximal if the yaw misalignment of the rotor and the wind direction is zero. However, this is not the case for the wind turbine.
loads. At every wind speed, a specific yaw misalignment will give an optimum for the wind turbine loads. Therefore, the design of the IPC controller and the yaw controller should be carefully carried out.

The yaw controller can be integrated in the control system of a wind turbine in various ways. If IPC for load reduction is not used, then the yaw controller with the reverse MBC transformation can be integrated straightforward. However, if IPC for load reduction is used, one can integrate the yaw controller and the IPC for load reduction in different ways. The two different yaw control configurations shown in Figure 4.6 can then be considered. The differences of these configurations lie in the tuning and decoupling of the different involved controllers, as well as in stability properties.

**YAW CONTROLLER CONFIGURATION #1**

In the first configuration, shown in Figure 4.6a, the yaw controller provides a setpoint for the yaw moment. The input to the yaw controller is the yaw error $\phi$ between a specified reference yaw angle $\phi_{\text{ref}}$ and the measured yaw position $\phi_{\text{yaw}}$ (see Figure 4.2). The controller is chosen to be of the PI form given in (4.4). Because the yaw controller takes as input the yaw error $\phi$, which will typically be relatively small compared with the yaw moment $M_{\text{yaw}}$, the PI gains will also be large. The advantage of this configuration is that...
the coupling between the IPC for load reduction and the yaw controller is immediately taken care of.

A model of the closed-loop system including the IPC for load reduction was not at hand. Therefore, the controller gains \((K_p, K_i)\) for this configuration were found by hand. It should be noted here that this required a bit of trial and error, but it was found that once appropriate gains were found, these could be used for the full operating range of the turbine. It should further be noted that without gain-scheduling the yaw controller gains, the yaw tracking response varies with wind speed, which might be undesired.

**Yaw controller configuration #2**

For the second configuration, the yaw controller adds a setpoint to the integrated yaw moment (as shown in Figure 4.6b). Without taking into account that the objectives of the IPC for load reduction and the yaw controller can be conflicting, this configuration would result in poor tracking of the yaw setpoint (because of coupling between both controllers). Therefore, to decouple both controllers, a high-pass filter is added to the integral controller for the yaw component. The integral controller is then given by

\[
I_{IPC} = \frac{K_{IPC}}{s} \times \frac{s^2}{s^2 + 2\omega_{IPC}\beta_{IPC}s + \omega_{IPC}^2},
\]

where \(\beta_{IPC} = 0.7\) and \(\omega_{IPC} = 2\pi f_{IPC}\). The cut-off frequency \(f_{IPC}\) provides an additional tunable parameter with which the controllers can be decoupled. Thus, the low-pass filter of the measured yaw error \(\phi\) given in (4.5) makes sure the yaw controller is active at frequencies below \(f_{yaw}\) and the high-pass filter in (4.6) makes sure the IPC load reduction controller is active at frequencies above \(f_{IPC}\).

On beforehand, it could be argued whether it would be effective to include a high-pass filter in the yaw component. Recalling that 1P blade loads are transformed to a 0P component in the non-rotating frame of reference, the resulting yaw moment is a signal with a dominant DC component. Hence, passing such a signal through a high-pass filter would almost completely remove the DC component. However, from experiments it was found that by appropriately selecting the cut-off frequency \(f_{IPC}\), additional load reductions could be achieved compared to the case where the IPC load reduction of the yaw component is removed (i.e., only IPC load reduction of the tilt component).

The yaw controller for the second configuration again has the form given in (4.4). For this case the controller gains are much smaller, because the controller takes the yaw error \(\phi\) as input and outputs a setpoint for the pitch.

**Stability of yaw configurations**

An important aspect in control design is stability of the closed-loop system. The combined yaw and IPC controllers were found to be stable for all considered load cases in this chapter. However, it was found that in the event of losing the measurements of the blade root moments, there is a difference between the yaw control configurations. To this end, consider a 600s constant wind with mean wind speed 16 m s\(^{-1}\) subjected to the two-bladed wind turbine. In the first 300s, the measurements of the blade root moments are available. Then, after 300s, it is assumed that the measurements of the blade root moments are no longer available for some reason (e.g., due to sensor failures or wiring...
4.4. YAW CONTROL DESIGN

The effect of such event on the closed-loop stability is shown for both control configurations in Figure 4.7.

From the latter figure it can be clearly observed that the first control configuration becomes unstable\(^3\). The underlying reason for this behavior is the changed closed-loop system. More specifically, after the blade root sensors become zero in the above mentioned experiment, a series interconnection of the integrator of the yaw controller and the integrator of the IPC for load reduction arises. This means that without the feedback loop from the blade moment sensors, an additional 90° phase loss occurs in the closed-loop system, which causes the instability.

The result shown in Figure 4.7 should be accounted for in the design process, for example by including fault detection algorithms. Or, a probably more reliable solution is found by choosing for the second yaw configuration, which does not rely on the blade root moment measurements. Therefore, in the remainder of this chapter, we will work with the second configuration. In Section 4.5, the performance of both control configurations in terms of load reduction and yaw tracking will be compared.

4.4.3. YAW CONTROLLER TUNING

The yaw controller as shown in Figure 4.6b and given by (4.4) can be designed according to the designer’s needs. For example, an aggressive yaw controller will accurately track the wind direction and maximize power output in below-rated operating conditions, but will at the same time generate higher yaw rates and increased loads due to gyroscopic effects. On the other hand, a slow yaw controller will lead to lower yaw rates and thus lower loads\(^4\), but not maximize the power output of the turbine. Thus, the design of the yaw controller involves a tradeoff between power output and turbine loads.

As mentioned before, this chapter considers a damped free-yaw wind turbine. The hydraulic yaw damper of the turbine provides damping of the yaw motion and interacts therefore with the yaw controller and IPC. Moreover, the yaw dynamics vary with wind speed. Hence, a yaw controller designed to yield a desired tracking behavior for a certain yaw damping value and wind speed, will result in different tracking behavior for a

---

\(^3\)Similar results are obtained when considering a turbulent wind field.

\(^4\)This holds to some extent, i.e., in case of a ‘too slow’ yaw controller very large misalignments can arise which could then lead to higher loads instead.
4. CONTROL DESIGN FOR TWO-BLADED DOWNWIND FREE-YAW WIND TURBINES

Figure 4.8: Yaw response to an initial yaw error for the five yaw damping values at 16 m s$^{-1}$.

(a) Step responses obtained for the baseline yaw controller applied to different yaw damping values.

(b) Step responses obtained for separately tuned yaw controllers for each yaw damping case so as to match the baseline response.

different yaw damping value and wind speed. Thus, for every considered yaw damping value and wind speed, the yaw controller should be tuned to have the desired tracking response (also see van Solingen et al. (2015c)). To do so, the models obtained in Section 4.4.1 for different yaw damping values and wind speeds are used to tune the yaw controllers.

In Figure 4.8a, the response of the baseline yaw controller case due to a 15° wind direction change is shown for a constant wind speed of 16 m s$^{-1}$. The baseline case involves the yaw controller (4.4) and yaw damping value III, which has been tuned to give a satisfactory performance for the 16 m s$^{-1}$ wind case. Figure 4.8a also displays the yaw responses for the same baseline controller applied to the turbines with the different yaw damping values. In Figure 4.8b, the yaw response is shown in the case that a yaw controller is tuned for every yaw damping value. It can be seen that the step responses are very similar and it can be concluded that the physical yaw damping value can be chosen as desired after which the yaw controller can be tuned accordingly.

The 16 m s$^{-1}$ wind case was extended with wind speeds of 4 m s$^{-1}$, 8 m s$^{-1}$, 10 m s$^{-1}$, and 12 m s$^{-1}$, to create a gain-scheduled yaw controller. For above-rated wind speeds the yaw dynamics remain rather constant, hence, it is sufficient to only include the 16 m s$^{-1}$ case in the gain schedule as above-rated wind speed. Extending the latter gain-scheduling to also include a gain-schedule for the yaw controller on the yaw damping gives maximum flexibility to evaluate the wind turbine performance. Thus, by doing so, the yaw tracking response is similar for all wind speeds and all yaw damping values.

4.4.4. YAW-DAMPING-BY-IPC

The physical yaw damping provided by the yaw system could be assisted by adding damping through the use of IPC. This could have the advantage of possibly reducing the amount of yaw damping provided by the yaw system such that the yaw system components could also (possibly) be reduced, which thus saves costs. Moreover, additional
damping provided by IPC could potentially further decrease the yaw rates. This is important because by keeping the yaw rates small, not only the gyroscopic loads are low, but also the loads in the yaw system.

Adding yaw damping to the system can be achieved by introducing a feedback loop using the yaw rate of the turbine. The extension of the current control configurations then becomes as schematically depicted in Figure 4.9. The yaw damping controller takes the measured yaw bearing velocity $\dot{\phi}_{yb}$ as input and outputs a yaw pitch setpoint (in the non-rotating frame of reference) to add damping to the closed-loop system. The yaw-damping-by-IPC controller has some coupling with the other IPC feedback loops. However, it is expected that this will not cause problems, because the yaw damping controller only responds to low-frequency yaw rate changes. Furthermore, the yaw damping controller does not work on the yaw position of the turbine itself, hence no significant integrator windup in the other IPC loops will occur. Thus, no decoupling procedure is considered for the yaw-damping-by-IPC controller.

The yaw damping controller is chosen to be a proportional gain $K_{yb}$ with a low-pass filter $L_{yb}$ and notch filters at the 1P and 2P frequencies. The low-pass filter $L_{yb}$ is similar to (4.5) and its cut-off frequency is set to $f_{yb} = 0.1 \text{ Hz}$.

All previously discussed controllers were tuned to give the best performance as outlined above. As mentioned before, some details of the turbine design are confidential and can therefore not be stated. This also applies to the controller parameter values and, therefore, only some of the controller details are listed in Table 4.2.

**4.5. RESULTS**

In this section, the controllers discussed throughout this chapter are evaluated in terms of wind turbine loads and power output. The results are divided in five subsections:

1. First of all, a comparison of the loads of rigid yaw and flexible yaw configurations is given in Section 4.5.1.
Table 4.2: Filter parameters of the different controllers.

<table>
<thead>
<tr>
<th>Description</th>
<th>Symbol</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Yaw controller $L_\phi$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Low-pass filter frequency</td>
<td>$f_{\text{yaw}}$</td>
<td>0.10Hz</td>
</tr>
<tr>
<td>Low-pass filter damping</td>
<td>$\beta_{\text{yaw}}$</td>
<td>0.70</td>
</tr>
<tr>
<td>Pitch controller $L_\theta$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Low-pass filter frequency</td>
<td>$f_\theta$</td>
<td>5.00Hz</td>
</tr>
<tr>
<td>Low-pass filter damping</td>
<td>$\beta_\theta$</td>
<td>0.70</td>
</tr>
<tr>
<td>IPC controller</td>
<td></td>
<td></td>
</tr>
<tr>
<td>High-pass filter frequency</td>
<td>$f_{\text{IPC}}$</td>
<td>0.05Hz</td>
</tr>
<tr>
<td>High-pass filter damping</td>
<td>$\beta_{\text{IPC}}$</td>
<td>0.70</td>
</tr>
<tr>
<td>Yaw damping controller $L_{yb}$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Low-pass filter frequency</td>
<td>$f_{yb}$</td>
<td>0.10Hz</td>
</tr>
<tr>
<td>Low-pass filter damping</td>
<td>$\beta_{yb}$</td>
<td>0.70</td>
</tr>
</tbody>
</table>

Table 4.3: Longitudinal wind turbulence intensity for the considered wind speeds.

<table>
<thead>
<tr>
<th>Wind speed [m s$^{-1}$]</th>
<th>6</th>
<th>8</th>
<th>10</th>
<th>14</th>
<th>16</th>
<th>18</th>
<th>22</th>
</tr>
</thead>
</table>

2. In Section 4.5.2 the performance of the two yaw control configurations, as described in Section 4.4.2, is compared. The loads and power output for the nominal damping case are only compared for a number of turbulent wind fields.

3. Then, in Section 4.5.3, the different controllers discussed in this chapter are compared for various turbulent wind fields.

4. The controller which gives the best performance in Section 4.5.3 is then used to evaluate the impact of the yaw damping provided by the yaw system in Section 4.5.4.

5. Finally, in Section 4.5.5 the Extreme Direction Change (EDC) extreme load case is considered. The EDC involves a turbulent wind case with an extreme change in the wind direction.

The results of the first four subsections are based on 600 s data sets in which the turbine was subjected to three-dimensional turbulent wind fields according to IEC (2005) using the software package Bladed (Garrad Hassan, 2014; Garrad Hassan & Partners Ltd, 2014). The wind turbulence intensity for each wind speed is listed in Table 4.3. As a measure for the turbine loads, the DELs (Freebury and Musial, 2000) are calculated for each data set. An overview of the loads considered in the results is given in Table 4.4.
4.5. RESULTS

Table 4.4: Description and notation of the considered loads in the results.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$M_{y,1}$</td>
<td>OoP root bending moment of blade 1 in the rotating frame of reference</td>
</tr>
<tr>
<td>$M_{x,1}$</td>
<td>IP root bending moment of blade 1 in the rotating frame of reference</td>
</tr>
<tr>
<td>$M_{bh,y}$</td>
<td>OoP hub bending moment in the rotating frame of reference</td>
</tr>
<tr>
<td>$M_{tb,z}$</td>
<td>Tower base torsional moment in the fixed frame of reference</td>
</tr>
<tr>
<td>$M_{tb,x}$</td>
<td>Tower base side-side moment in the fixed frame of reference</td>
</tr>
<tr>
<td>$M_{tb,y}$</td>
<td>Tower base fore-aft moment in the fixed frame of reference</td>
</tr>
</tbody>
</table>

4.5.1. COMPARISON OF RIGID YAW AND FREE YAW

Various yaw system types exist for wind turbines. Conventionally, most wind turbines feature an upwind rigid yaw configuration with yaw control provided by yaw drives. If a certain yaw misalignment threshold is exceeded, the yaw brakes are released and the yaw drives are enabled to align the rotor-nacelle assembly with the current wind direction. On the other hand, a free yaw configuration in a downwind fashion naturally tracks the wind. The consequence of such a free yaw turbine is that wind direction changes may cause high yaw rates and thereby gyroscopic loads. To overcome the latter, the yaw rates can be decreased by making use of a yaw system providing yaw damping. Additionally, with the use of IPC, the wind direction can be actively tracked.

Before comparing the different yaw controllers discussed in Section 4.4, first the differences between a rigid yaw and a free yaw configuration are analyzed. To this end, four different configurations are considered:

**Rigid yaw:** With this yaw configuration, the rotor-nacelle assembly is rigidly connected to the tower.

**Free yaw:** In this case, the rotor-nacelle assembly is free to rotate (except for yaw friction).

**Damped free-yaw:** In this case, the rotor-nacelle assembly is free to rotate on the tower (except for yaw friction), however damping is provided by the yaw system to limit the yaw rate. Yaw damping value III is selected for the comparison.

**Free yaw with yaw-by-IPC:** The same as the free-yaw configuration, however, extended with yaw-by-IPC to actively track the wind direction.

**Damped free-yaw with yaw-by-IPC:** The same as the damped free-yaw configuration, however, extended with yaw-by-IPC to actively track the wind direction.

The five different turbine configurations are subjected to wind speeds within the operating range of the turbine. For each wind speed and turbine configuration, the DELs, the produced energy and other measures are calculated and shown in Figure 4.10 and Figure 4.11. The term ‘flexible yaw’ is used in the remainder to indicate the cases involving free yaw, i.e., free yaw, damped free-yaw, free-yaw with yaw-by-IPC, and damped free-yaw with yaw-by-IPC.
The loads in Figure 4.10 show a number of trends for the different wind speeds. In all considered cases, the OoP blade root moment $M_{y,1}$ are larger for the flexible yaw configurations. Comparing the flexible configurations for the blade moment $M_{y,1}$, one can observe that a free-yaw configuration yields higher loads than damped free-yaw configurations. Moreover, the support of yaw-by-IPC typically reduces the blade load $M_{y,1}$. The damped free-yaw configuration with yaw control shows that the OoP blade root moments can be kept rather close to those of a rigid yaw configuration. The higher blade load $M_{y,1}$ for the free-yaw and damped free-yaw configurations can be attributed to the yaw rates and consequently higher gyroscopic loads. The In-Plane (IP) blade moment $M_{x,1}$ show a decrease mainly for the damped free-yaw configurations. This can be explained by the fact that the blade edge moments appears as a moment around the tower (Hansen, 1992). In the free-yaw configuration, this is counteracted by the increased yaw rates of the rotor-nacelle assembly. The OoP rotating hub moment $M_{th,y}$ follows the same trends as the OoP blade moments.

The major advantage of a flexible configuration can be seen in the middle left plot of Figure 4.10. The tower base torsion moment $M_{tb,z}$ is dramatically lower in the cases of the flexible yaw configurations. On the other hand, due to the yawed alignments of the turbine, the side-side tower base moment $M_{tb,x}$ and fore-aft tower base moment $M_{tb,y}$ increase, especially for the free yaw configuration without damping. Moreover, the yawing motions of the rotor-nacelle assembly of the flexible yaw configurations causes the side-side tower moment to be excited (especially in the upper portion of the tower top (Doman, 1985)). It should be noted that the increase in fore-aft tower base moment $M_{tb,y}$ is much smaller than the side-side moment $M_{tb,x}$, and in the case of the damped free-yaw configuration only marginal.

The results of Figure 4.10 also give insight in the interplay of the turbine loads for different yaw configurations. For the free-yaw configuration, the tower torsional DELs are roughly 25% to 15% of the obtained DELs for the rigid yaw configuration, whereas the calculated blade loads have substantially increased in some cases. For the damped free-yaw configuration, the blade loads are significantly lower (although still higher than the loads of the rigid yaw configuration), but the tower torsional loads are higher than the free-yaw configuration (but have still reduced by more than half compared to the rigid yaw configuration). The reduction in blade loads for the damped case is the result of reduced gyroscopic loads, because the standard deviation of the yaw rate has significantly decreased (see Figure 4.11). Adding yaw-by-IPC to the free yaw and damped free-yaw configurations has a number of impacts on the DELs. For lower wind speeds, the yaw control causes the blade loads and tower loads to increase, whereas for higher wind speeds the loads tend to be decreased (especially for the damped yaw case).

The impact of introducing yaw damping is apparent from the yaw misalignment plots in Figure 4.11. The damped free-yaw turbine configurations without yaw-by-IPC lowers the extreme yaw positions in almost all cases. Moreover, including yaw-by-IPC typically further reduces the extremes of the yaw misalignment, decreases the standard deviation of the misalignment, and also brings the mean yaw misalignment close to zero. The yaw bearing angular velocity significantly decreases for increased yaw damping and the yaw-by-IPC controller hardly affects the yaw bearing angular velocities for higher wind speeds. For lower wind speeds, the yaw controller tends to increase the yaw bearing
Table 4.5: Loads and produced energy for different downwind yaw configurations

<table>
<thead>
<tr>
<th>Yaw configuration</th>
<th>Blade $M_y$</th>
<th>Tower $M_{th,z}$</th>
<th>Tower $M_{th,y}$</th>
<th>Tower $M_{th,x}$</th>
<th>Energy</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rigid</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Free</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Damped</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Free + yaw-by-IPC</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Damped + yaw-by-IPC</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

angular velocities. Finally, the energy produced by the different turbine configurations is shown in the lower left graph in Figure 4.11. It can be observed that the free yaw and damped free-yaw configurations without yaw-by-IPC produced slightly less energy. The yaw configurations with yaw-by-IPC produce roughly the same amount as the rigid yaw configuration. Moreover, from a study by Kragh and Hansen (2015), it was concluded that with improved yaw misalignment a theoretical 0.2% annual energy production increase could be obtained compared to an (undisclosed) yaw control strategy using yaw drives. From these results and the study by Kragh and Hansen (2015), it is expected that no significant power losses or gains will be achieved with the use of a flexible yaw configuration and yaw-by-IPC.

The aforementioned results for the different downwind yaw configurations are summarized in Table 4.5. In this table, the impact of the yaw configuration on various loads is characterized. The rigid yaw configuration is considered as the reference configuration to which the other configurations are compared. It should be stressed that the results presented in Table 4.5 only hold true in general. This means that there can be ‘local’ operating conditions for which the results can be different than presented in the table.

4.5.2. COMPARISON OF YAW CONTROLLER CONFIGURATIONS

In this subsection, the loads of the two yaw control configurations, discussed in Section 4.4.2, are analyzed. The yaw controllers were tuned to give the most satisfactorily performance with respect to the loads (also see Section 4.4.3). Two wind speeds were selected to analyse the performance of both configurations. For below-rated operation, a wind speed of $8 \text{ m s}^{-1}$ is selected and for above-rated operation a wind speed of $16 \text{ m s}^{-1}$ is selected. The results are shown in Figure 4.12 and Figure 4.13. In the figures the yaw control configuration shown in Figure 4.6a is denoted by “Cfg. #1” and the yaw control configuration shown in Figure 4.6b is denoted by “Cfg. #2”. Hence, damping is only provided by the yaw system and not through the use of IPC. The controller gains for the first yaw control configuration are equal for both wind speeds, whereas the controller gains for the second configuration are gain-scheduled and thus dependent on the wind
Figure 4.10: Calculated DELs for fixed and flexible yaw configurations. The legend indicates the bar colors of the different yaw configurations.
Figure 4.11: Calculated pitch, yaw, and energy results for fixed and flexible yaw configurations. The legend indicates the bar colors of the different yaw configurations.
speed. The high-pass filter cut-off frequency of (4.6) was (only in this batch of results) set to \( f_{\text{IPC}} = 0.02 \text{Hz} \).

The results in Figure 4.12 show that the obtained DELs are rather similar for both cases. For the blade root moments \((M_{y,1,1}, M_{y,2})\) it holds that the second configuration performs better for the above-rated wind speed. On the other hand, the first configuration performs better in terms of the DELs of the tower and rotating hub moment \(M_{\text{th,y}}\). The upper row of plots shown in Figure 4.13 indicate that the pitch contributions by both strategies are rather equal. The mean yaw misalignment is lower for the first configuration in below-rated operating conditions, but higher for above-rated wind conditions. The standard deviation of the yaw bearing angular velocity is lower for the first yaw configuration in the below-rated operating condition. In terms of produced energy the differences are negligible.

In conclusion, both yaw control configurations yield on average rather similar results. The differences between both configurations can be attributed to tuning of the controllers. Thus, as outlined before, the choice for the yaw control configuration is up to the designer, but since the second configuration does not suffer from stability issues (see Section 4.4.2), we preferred this approach.

4.5.3. Controller performance for nominal yaw damping

The control system of a (damped) free-yaw turbine can be decomposed into several (decoupled) feedback loops as was discussed in Section 4.3. Here, in this subsection, the performance of the different controllers is evaluated based on a number of wind cases. The four different control systems listed in Table 4.6 are considered. With increasing subscript of \( C \), the number of included feedback loops increase. The yaw-by-IPC controller is chosen according to strategy #2 (see Figure 4.6b). The IPC-Tilt controller only reduces the tilt moment obtained by the MBC transformation. The IPC-Yaw controller provides reduction of the yaw moments (obtained by the MBC transformation) and is decoupled from the yaw controller with a high-pass filter as discussed in Section 4.4.2. Finally, controller \( C_4 \) also includes yaw-damping-by-IPC. The results are depicted in Figure 4.14 and Figure 4.15, which were obtained with the (nominal) yaw damping value III.

The DELs calculated for the different wind and controller cases indicate a number of results. The OoP blade root moment load \((M_{y,1})\) shows that the largest reductions are obtained with the IPC-Tilt controller. Consequently, the OoP rotating hub moment \(M_{\text{th,y}}\) also shows a dramatic decrease. The latter decrease makes the use of a teetered hinge redundant (Bossanyi et al., 2013). The IPC-Yaw controller and yaw-damping-by-IPC only have marginal contribution to the blade and rotating hub loads. Besides the blade loads and the rotating hub moment, the largest load reductions are obtained in the tower torsion moment \(M_{\text{th,z}}\). For the tower torsion moment \(M_{\text{th,z}}\), each extension of the controller further reduces the loads. The tower side-side moment \(M_{\text{th,x}}\) mostly benefits from the IPC-Tilt controller and the tower fore-aft moment \(M_{\text{th,y}}\) slightly increases for the IPC-Tilt controller and is again slightly reduced by the yaw-damping-by-IPC action.

In Figure 4.14, it can be observed that the obtained load reductions for the 10 m s\(^{-1}\) wind case are relatively larger than for the other wind cases. The reason for this can be found in the specific turbulence of the wind file. By generating additional 10 m s\(^{-1}\) wind files with the same characteristics, but with different turbulence seeds, load reductions
Figure 4.12: Calculated DELs for the yaw control configurations
Figure 4.13: Calculated pitch, yaw, and energy results for the yaw control configurations
4.5. RESULTS

Table 4.6: Overview of the different considered controllers

<table>
<thead>
<tr>
<th>Description</th>
<th>Yaw-by-IPC</th>
<th>IPC-Tilt</th>
<th>IPC-Yaw</th>
<th>Yaw-damping-by-IPC</th>
</tr>
</thead>
<tbody>
<tr>
<td>C₁</td>
<td>✓</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>C₂</td>
<td>✓</td>
<td>✓</td>
<td></td>
<td></td>
</tr>
<tr>
<td>C₃</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td></td>
</tr>
<tr>
<td>C₄</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
</tr>
</tbody>
</table>

following the trends of Figure 4.14 were obtained.

The impact of the different controllers on the blade pitch actuators, yaw misalignment, yaw bearing angular velocity, and energy production is shown in Figure 4.15. It can be observed from the top two figures that the blade pitch actuators are only marginally impacted by the IPC load reduction controllers for above-rated conditions in terms of the standard deviation of the blade 1 pitch angle $\theta_1$. In below-rated conditions, the blade pitch angle standard deviation roughly doubles for IPC load reduction control. The same applies to the blade pitch rate, which roughly doubles for all operating conditions with respect to yaw-by-IPC. From the mean yaw misalignment plot, it is observed that the IPC controllers slightly increase the yaw misalignment. On the other hand, the standard deviation of the yaw misalignment remains roughly unchanged except for the yaw-damping-by-IPC case, which slightly lowers the standard deviation in most cases. As was the case for the tower torsion moments $M_{tb,z}$, the standard deviation of the yaw bearing angular velocity decreases with each extension of the controller. The energy production for all controller cases are nearly identical.

4.5.4. IMPACT OF YAW DAMPING

The amount of damping provided by the yaw system has a big influence on the loads of the turbine. The impact of the yaw damping is therefore analyzed in this subsection. The five damping values introduced before are considered. For convenience, the notation and description of the yaw damping values are repeated here. The yaw damping values are denoted by $\emptyset$ for the free-yaw configuration (i.e., zero damping) and by I to IV, which indicate values from low to high damping. The controller $C_4$ (see Section 4.5.3) including yaw-by-IPC, IPC-Tilt/Yaw, and yaw-damping-by-IPC is used to generate the results for the range of wind speeds. The results are shown in Figure 4.16 and Figure 4.17.

In general, one can see a number of trends in the plots shown in Figure 4.16. The first trend is that the OoP blade root moment $M_{y,1}$, the IP blade root moment $M_{x,1}$, and the rotating hub moment $M_{rh,y}$ typically decrease with increasing yaw damping. The second trend is that the tower base torsion moment $M_{tb,z}$ decreases for decreasing yaw damping values. A third trend that can be observed is the significant decrease of the tower base side-side moment $M_{tb,x}$ with increasing yaw damping. Finally, the results for the 6 m s$^{-1}$ wind case seem to be slightly different from the other cases, which is most likely caused by the tuning of the controllers (i.e., only the yaw-by-IPC is gain scheduled).

It should be noted that the trends in the results shown here are roughly independent of the choice of the controller. Thus, any of the previous considered controllers (in Section 4.5.3) yield results with the same trends.
Figure 4.14: Calculated DELs for the different controllers
Figure 4.15: Calculated pitch, yaw, and energy results for the different controllers
Figure 4.16: Calculated DELs for the different yaw damping values
Figure 4.17: Calculated pitch, yaw, and energy results for the different yaw damping values.
Table 4.7: Wind direction change in degrees for various wind speeds of EDC.

<table>
<thead>
<tr>
<th>Wind speed [m s(^{-1})]</th>
<th>6</th>
<th>10</th>
<th>14</th>
<th>18</th>
<th>22</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wind direction change [°]</td>
<td>33.96</td>
<td>27.84</td>
<td>25.22</td>
<td>23.76</td>
<td>22.83</td>
</tr>
</tbody>
</table>

4.5.5. Extreme Wind Direction Change

In the final considered case, the response of the turbine to the EDC (IEC, 2005) load case is analyzed. In this extreme load case, the wind direction rapidly changes. In order to obtain this load case, the turbulent wind fields which were used in the previous presented results were modified to incorporate the extreme wind direction change. According to IEC (2005) the direction change occurs over 6s and the amplitude of the direction can be calculated from the turbulence intensity, wind speed at hub height, rotor diameter, and the hub height. The amplitude of the direction change for each wind speed is listed in Table 4.7. The direction change has been set to occur after 90s. After the direction change, the wind direction mean remains at the EDC amplitude. Thus, the wind direction rapidly changes to a new wind direction during the EDC and does not change back to the original wind direction.

All of the previous mentioned damping values with controller \( C_1 \) and \( C_4 \) (see Section 4.5.3) have been subjected to the EDC cases in Table 4.7. In all cases the turbine remained stable and the yaw error was compensated. Two cases have been selected from the range of load cases and are shown in Figure 4.18 and Figure 4.19. These cases involve the wind speeds 10 m s\(^{-1}\) and 22 m s\(^{-1}\) for the nominal yaw damping value (III) and the controllers \( C_1 \) and \( C_4 \). In the shown cases, the effectiveness of the controller \( C_4 \) is apparent. Overall the blade root moment \( M_{y,1} \) and the tower torsional moments \( M_{tb,z} \) are significantly decreased.

In Figure 4.18 one can observe a significant increase in the yaw bearing angular velocity due to the wind direction change. This causes the blade root moments and tower torsional loads to roughly increase by a factor two for the case without load reduction control. In the case load reduction control is enabled, the yaw bearing rates and loads remain smaller. In the 22 m s\(^{-1}\) case, the impact of the EDC on the turbine seems to be smaller.

4.6. Conclusions

This chapter presents the control design of a teeterless downwind two-bladed wind turbine with a free yaw configuration and yaw control by means of IPC. Two-bladed wind turbines currently face a renewed interest and are being developed and built by a number of companies. The motivation for two-blades can mainly be found in the potential cost reduction due to the number of blades and constructional advantages. Here a turbine, besides having a two-bladed rotor, with a free yawing rotor-nacelle assembly is considered. The major advantage of such a yaw configuration is the dramatic decrease in load transfer from the rotor to the tower. In our study, the DEL of the tower base torsional moment reduced by a factor of roughly four to six for a free yaw turbine compared to a rigid yaw turbine in the same wind conditions.
Figure 4.18: Response to the EDC at 10 m s$^{-1}$ for the nominal yaw damping case. The starting time of the EDC is indicated by the vertical dashed line. The legends for the small plots comparing the controller performance are identical and shown in the lower left plot.
Figure 4.19: Response to the EDC at 22 m s⁻¹ for the nominal yaw damping case. The starting time of the EDC is indicated by the vertical dashed line. The legends for the small plots comparing the controller performance are identical and shown in the lower left plot.
4.6. Conclusions

In order for the wind turbine with free yaw configuration to actively track the wind, a yaw controller using IPC is designed. It is shown that the yaw-by-IPC controller can be combined with the existing conventional IPC for load reduction in different ways. Two yaw controller configurations are analyzed in terms of turbine loads, power output, and stability. It can be concluded that the yaw controller, which is added after the integrator of the conventional IPC, and before the reverse MBC transformation, is favorable in terms of stability.

The yaw controller itself has a significant impact on the loads of the wind turbine. The design of the yaw controller should therefore be carefully carried out. In this study system identification techniques were used to obtain a model of the yaw dynamics and the yaw controller was designed subsequently. Moreover, in the case that a damped free-yaw configuration is used, the yaw damping provided by the yaw system imposes another degree of freedom in the design process. It is shown that the tracking performance of the yaw controller is significantly affected by the yaw damping provided by the yaw system and needs to be taken into account.

The yaw damping on its turn also has a great impact on the turbine loads. In general it can be concluded that the choice for the amount of yaw damping is a tradeoff between blade loads and tower loads. The more damping provided by the yaw system, the higher the tower torsional loads and the lower the blade and tower side-side loads. Furthermore, it is demonstrated that yaw damping can also be added to the wind turbine system by means of IPC. The results indicate that the tower base torsional moment can be decreased with roughly 5%. Finally, it remains to the designer and the specifics of the wind turbine to select the optimal yaw damping and to fine-tune the various involved controllers.
5

FREQUENCY-DOMAIN OPTIMIZATION OF LINEAR PARAMETERIZABLE $\mathcal{H}_\infty$ CONTROLLERS

In this chapter, a novel data-driven frequency-domain $\mathcal{H}_\infty$ controller design methodology is presented. The methodology considers the class of controllers which can be linearly parameterized. The tunable controller parameters are extracted into a diagonal form and by exploiting the generalized Nyquist stability criterion, a feasible solution is sought. Traditionally, the generalized Nyquist stability criterion is used to assess the stability of the closed-loop system. Here, we exploit the generalized Nyquist stability criterion to impose $\mathcal{H}_\infty$ performance specifications on the closed-loop system. Both stability and performance of the closed-loop system are obtained by constraining the Nyquist curve from encircling the origin. The constrained Nyquist curve then yields a feasibility problem with the tunable controllers parameters as decision variables. With a slight modification, the design methodology is extended to include grey-box system identification. The design methodology for controller design and grey-box system identification is demonstrated in simulation examples and using an experimental setup.

5.1. INTRODUCTION

Data-driven control design or data-driven modeling is a valuable tool in the deployment rate of industrial applications. For example, the dynamics of wind turbines can be reasonably well predicted by software packages using first-principle models, but will never exactly match the real-world built wind turbine due to many factors (van der Veen et al., 2013b). Consequently, controllers that are designed using the first-principles models will not give maximum performance when implemented. It is therefore important to be able to quickly update or fine-tune the controllers on the real-world turbine, without requiring a full redesign of the controller. Another approach would be to directly design controllers based on measurements obtained from the actual system. This is supported
by a recent study where a data-driven controller design outperforms a model-based controller design (Formentin et al., 2014).

Besides the importance of data-driven controller design, it is also important for industrial application to be able to fine-tune controllers in the field, without requiring complex optimization routines. Classical optimal and robust control design techniques lead to high order controllers (e.g., as high as the order of the plant, see Zhou et al. (1996); Skogestad and Postlethwaite (2006)). In this regard, fixed-order, fixed-structure controllers (e.g., PID controllers, notch filters and low-pass filters) are highly suitable. Since both the controller structure and order are fixed a priori, only the tunable parameters need to be found such that the performance specifications are met. Unlike well-known solutions to unstructured control synthesis problems (e.g., using Riccati equations (Doyle et al., 1989) or Linear Matrix Inequality (LMI) techniques (Gahinet and Apkarian, 1994; Iwasaki and Skelton, 1994)), the main problem that arises when imposing constraints on the controller structure is that the resulting optimization problem is no longer convex and is in general considered to be NP-hard (Nemirovskii, 1993; Blondel and Tsitsiklis, 1997).

In the past decades, fixed-structure control synthesis has received considerable attention. Numerous contributions can be found in the context of (iterative) LMIs (Scherer, 2002; Han and Skelton, 2003; Karimi et al., 2007; Scherer, 2013). However, many of these solutions are conservative or apply only to very specific controller structures. Alternatively, sum-of-squares techniques for fixed-order $H_\infty$ controller synthesis are used in Hol and Scherer (2005) and positive polynomials in Henrion et al. (2003). Furthermore, a convex-concave optimization procedure for PID controller design is outlined in Hast et al. (2013), evolutionary algorithms are used in Popov and Werner (2006), randomized algorithms are used in Maruta et al. (2009, 2013), a surrogate convex upper bound on the $H_\infty$ norm is used in Dvijotham et al. (2014), and an alternative for the Youla parameterization in Khatibi and Karimi (2010).

Arguably one of the largest impacts on fixed-structure control synthesis is the non-smooth optimization technique in Apkarian and Noll (2006); Apkarian et al. (2008); Gahinet and Apkarian (2011a,b), which is implemented in the MATLAB Robust Control Toolbox. The structure of both feedback and feedforward controllers can be fully defined by the user, and time-domain and frequency-domain multi-objective performance specifications can be set. A nonsmooth optimization solver then tunes the controller parameters in order to satisfy the specifications.

A drawback of the majority of the previously mentioned techniques is that they do not directly compute controllers based on e.g., a measured Frequency-Response Function (FRF). This effectively means that either a first-principles model or an intermediate system identification step is required before one can use these techniques and tools. As mentioned before, it is expected that a fully data-driven control design methodology will perform better than a controller designed using a model (Formentin et al., 2014). Therefore, a fully data-driven controller design method, which directly uses input-output measurements of the plant is an attractive opportunity.

Data-driven controller synthesis has seen several contributions in the past. In Guardabassi and Savaresi (2000), a direct model-reference approach to the design of linear controllers is proposed. The controller parameters are directly estimated without re-
requiring a model of the plant and can be carried out offline. The work in Campi et al. (2002) extends the previous mentioned method of Guardabassi and Savaresi (2000) to a ready-to-use technique by addressing implementation and performance issues. The former methods use time-domain data and are non-iterative (for iterative model-free controller design refer to Hjalmarsson et al. (1998); Hjalmarsson (2002) and for iterative model-based controller design refer to Karimi et al. (2004)).

A controller design method using frequency-domain data is found in den Hamer et al. (2009), where predefined fixed-structure controllers are optimized with respect to closed-loop performance specifications based on FRF data of the plant. A robust controller design method for a class of uncertainties using frequency-domain data is presented in Khadraoui et al. (2013). In Parastvand and Khosrowjerdi (2015) a subset of stabilising fixed-order controllers using a set of linear inequalities is calculated from the frequency response of the plant. The fixed-order controllers achieve some $\mathcal{H}_\infty$ norms on the (complementary) sensitivity function. The latter work is an extension to the work of Keel and Bhattacharyya (2008), in which a complete set of stabilizing Proportional Integral Derivative (PID) controllers is calculated directly from the plant FRF. The majority of the aforementioned model-free and frequency-domain based design methods require solving non-convex optimization problems.

A number of publications regarding convex optimization of linearly parameterizable controllers using frequency response data is available in Galdos et al. (2010); Karimi and Galdos (2010). In this work, it is shown that the $\mathcal{H}_\infty$ robust performance condition can be represented in the Nyquist diagram by constraints with respect to the tunable parameters of a linearly parameterized controller. The constraints are convexified by using a desired open-loop transfer function. The method can be applied to SISO systems (Karimi and Galdos, 2010) and MIMO (Galdos et al., 2010) systems. A freely available toolbox for MATLAB based on these techniques is developed by Karimi (2013). Recently, a new robust controller design method for SISO systems was presented in Karimi and Zhu (2014). The upper bound on the $\mathcal{H}_\infty$ norm of weighted frequency responses is minimized and the design includes frequency domain disk, polytopic and multimodel uncertainty.

In this chapter, a novel methodology for data-driven $\mathcal{H}_\infty$ controller design and grey-box system identification is presented. The methodology can directly use measured frequency response data obtained from the plant to find the tunable parameters of linearly parameterizable controllers. Performance specifications of the closed-loop system are imposed by weights on the (complementary) sensitivity function(s) in the frequency-domain. The methodology presented in this chapter exploits the generalized Nyquist stability criterion and yields, by constraining the Nyquist curve from certain parts of the Nyquist diagram, stability and performance of the closed-loop system. It is shown that for special control cases, the controller design results in a convex feasibility problem, but will generally result in a feasibility problem which is multilinear in the tunable controller parameters. It is shown that the methodology can also be used for grey-box system identification.

The proposed methodology can also be used for integrating the design of plant and controller. Similarly to extracting the tunable parameters of the controller, structural parameters of plant need to be extracted into a diagonal form. Thus, the diagonal controller structure is extended with structural related parameters. The inclusion of tunable struc-
The property to simultaneously design plant and controller is appealing, because it can lead to more efficient designs (see for example Grigoriadis and Wu (1997); Grigoriadis and Skelton (1998); Lu and Skelton (2000); Camino et al. (2003); Hiramoto and Grigoriadis (2005); Pang et al. (2012); van der Veen et al. (2014)).

To summarize, the main contributions of this chapter are:

- A novel data-driven fixed-structure $H_\infty$ controller synthesis method;
- A novel grey-box system identification method.

Both methods are demonstrated using measured frequency response data from an experimental setup. Since there is resemblance with the work in Galdos et al. (2010); Karimi and Galdos (2010), the differences between both methods are explicitly listed here:

- The method in this chapter does not require a desired open-loop transfer function, in contrast to the method in Galdos et al. (2010); Karimi and Galdos (2010);
- The method in this chapter automatically extends to MIMO systems, compared to Karimi and Galdos (2010) and Karimi and Zhu (2014), which only apply to SISO systems.

Other controller design methods using the Nyquist stability criterion are found in Maeda and Iwasaki (2012); Hast et al. (2013); Maeda and Iwasaki (2014), but follow different approaches.

The chapter is organized as follows. In Section 5.2 the general problem formulation is outlined. The data-driven fixed-structure controller synthesis method is subsequently presented in Section 5.3 along with some practical aspects. The extension of the methodology to a grey-box system identification method is given in Section 5.4. Section 5.5 presents the experimental setup. The methodologies are demonstrated in Section 5.6 through a simulation study and the experimental setup. The chapter is concluded in Section 5.7.

### 5.2. Problem formulation

In this section, the $H_\infty$ control design problem is defined, the class of controllers including several examples is described, and stability and performance of the closed-loop system are defined.

#### 5.2.1. Problem statement

The following partitioning of the generalized plant is considered

\[
\begin{bmatrix}
  z \\
  y 
\end{bmatrix} = \begin{bmatrix}
  P_{11}(s) & P_{12}(s) \\
  P_{21}(s) & P_{22}(s) 
\end{bmatrix} \begin{bmatrix}
  w \\
  u 
\end{bmatrix},
\]

(5.1)

with $z \in \mathbb{R}^{n_z}$, $w \in \mathbb{R}^{n_w}$, $y \in \mathbb{R}^{n_y}$, and $u \in \mathbb{R}^{n_u}$. The transfer functions $P_{11}(s)$, $P_{12}(s)$, $P_{21}(s)$, and $P_{22}(s)$ have corresponding dimensions and are all assumed to be stable. The controller parameters are real scalars, i.e., $\phi \in \mathbb{R}^{n_\phi}$. With these definitions the controller is
defined as

\[
\begin{bmatrix}
\phi_1 & 0 \\
\vdots & \ddots \\
0 & \phi_m
\end{bmatrix}
\begin{bmatrix}
y \\
k
\end{bmatrix}
\]

and the closed-loop system is obtained by

\[
T_{wz}(s) = F_l(P, K) = P_{11} + P_{12}K(I - P_{22}K)^{-1}P_{21},
\]

where \( F_l \) denotes the lower Linear Fractional Transformation (LFT). The goal is to find the controller parameters \( \phi \) that achieve \( \|T_{wz}\|_\infty < 1 \).

Note that for a freely-parameterized controller \( K \), this problem is convex (Zhou et al., 1996), but leads to a solution having the same order as the generalized plant, which is typically not desired in practical applications. On the other hand, for a fixed-structure controller, the problem is no longer convex, and advanced and sophisticated optimization routines are required to find the optimal controller (see for instance Hol (2006); Apkarian and Noll (2006)).

### 5.2.2. Linear Parameterizable Controllers

The plant and controller structure as defined in (5.1) and (5.2) for a PID controller can be obtained as follows. Let a PID controller be given by

\[
K_{\text{PID}}(s) = K_p + \frac{K_i}{s} + \frac{K_d s}{T_f s + 1},
\]

then a diagonal structure with the controller parameters \( \phi_{\text{PID}} = [K_p \ K_d \ K_i] \) as in Figure 5.2 is obtained in a straightforward manner (negative feedback is assumed). If desired, the time constant \( T_f \) can also be pulled out of the structure.
OPTIMIZATION OF LINEAR PARAMETERIZABLE $\mathcal{H}_\infty$ CONTROLLERS

Figure 5.2: Linear parameterization of a PID controller. The generalized plant is indicated by the grey box.

The diagonal controller structure as described above can be obtained from more generic parameterizations. That is, any well-posed rational function $R(b)$ can be written as an LFT (Redheffer, 1960)

$$ R(b) = F_l(M, b \otimes I), $$

with $M$ a fixed matrix and $b \otimes I$ a diagonal matrix containing the parameters which define the rational function $R(b)$ (see Gahinet and Apkarian (2011a) and Zhou and Doyle (1998) for examples). Note that repeated copies of the parameters $b$ may arise, which might complicate the optimization problem discussed in the next section.

Another choice of a linear controller parameterization is the use of basis functions (Mäkilä, 1990; Heuberger et al., 1995; Akçay and Ninness, 1999). To this end, in Karimi and Galdos (2010); Karimi and Zhu (2014) Laguerre basis functions

$$ \chi_i(s) = \frac{\sqrt{2\xi}(s - \xi)^{(i-1)}}{(s + \xi)^i} \quad \text{for } i \geq 1, \xi > 0, \chi_0(s) = 1 \quad (5.5) $$

are used. By multiplying each basis function with a scalar, e.g., $\phi_B = [\phi_i, ..., \phi_m]^T \chi$, any stable rational finite order transfer function can be approximated (for a sufficient number of basis functions). The Laguerre basis functions can be incorporated by absorbing the basis functions into the generalized plant and creating a diagonal structure similar to Figure 5.2 with the elements of $\phi_B$ on the diagonal. The tuning parameter $\xi$ and the number of bases $i$ need to be selected beforehand, and a practical guideline to select the basis functions is given in Karimi and Galdos (2010).
5.2.3. Stability and Performance

In order to find the controller parameters that result in \( \| T_{wz} \|_\infty < 1 \), consider the following approach, assuming a stable\(^1\) generalized plant \( P(s) \) and given the frequency response data of \( P(s) \) denoted by \( P(j\omega) \). By making use of the generalized Nyquist stability criterion (MacFarlane and Postlethwaite, 1977), two definitions are formulated.

**Definition 1 (Stability)** The closed-loop system \( T_{wz} \) in Figure 5.1 is asymptotically stable if for a given stable generalized plant \( P(j\omega) \), the Nyquist plot of

\[
\det \left( I - \begin{bmatrix} \phi_1 & 0 \\ \vdots & \ddots & \ddots \\ 0 & \ldots & \phi_m \end{bmatrix} P_{22}(j\omega) \right), \quad \forall \omega,
\]

(5.6)

does not encircle the origin.

This is the generalized Nyquist theorem for a positive feedback system with stable loop transfer function \( KP_{22}(j\omega) \).

**Definition 2 (Performance)** The closed-loop system \( \| T_{wz} \|_\infty \) in Figure 5.3 satisfies the performance requirement \( \| T_{wz} \|_\infty < 1 \), if for a given stable generalized plant \( P(j\omega) \), the Nyquist plot of

\[
\det \left( I - \begin{bmatrix} \Delta P(j\omega) & 0 \\ 0 & \phi_1 & 0 \\ \vdots & \ddots & \ddots \\ 0 & \ldots & \phi_m \end{bmatrix} \right), \quad \forall \omega, \forall \Delta P(j\omega),
\]

(5.7)

does not encircle the origin for any stable rational transfer function \( \Delta P \in \mathbb{C}^{n_w \times n_z} \) and \( \| \Delta P(s) \|_\infty \leq 1 \).

Note that the system in Figure 5.3 is obtained by including, in Figure 5.1, a full complex perturbation block \( \Delta P(j\omega) \) in feedback with the exogenous input \( w \) and exogenous output \( z \). The performance condition (5.7) can be deduced from robust control theory and can be found in Skogestad and Postlethwaite (2006, Theorem 8.7 and the proofs thereof). In the remainder of this chapter we refer to stability and performance as defined in (5.6) and (5.7).

5.3. Nyquist Controller Design

The procedure to find controller parameters such that \( \| T_{wz} \|_\infty < 1 \) is to constrain the Nyquist curve from encircling the origin by introducing line constraints. This procedure is outlined next.

\(^1\)In this chapter only stable generalized plants are considered, however the method can be extended to include unstable generalized plants.
5.3.1. Determinant for Stability and Performance

The determinant expression for two controller parameters (i.e., $\phi \in \mathbb{R}^2$) for closed-loop stability (5.6) is given by

$$Q(\phi, j\omega) = 1 - P_{22}^{(11)} \phi_1 - P_{22}^{(22)} \phi_2 + \left(P_{22}^{(11)} P_{22}^{(22)} - P_{22}^{(12)} P_{22}^{(21)}\right) \phi_1 \phi_2,$$  \hspace{1cm} (5.8)

where the following partitioning of $P_{22}(j\omega)$ is considered

$$P_{22}(j\omega) = \begin{bmatrix} P_{22}^{(11)}(j\omega) & P_{22}^{(12)}(j\omega) \\ P_{22}^{(21)}(j\omega) & P_{22}^{(22)}(j\omega) \end{bmatrix}.$$

Similarly, the determinant expression for two controller parameters, a single exogenous input $w$ and a single exogenous output $z$, for closed-loop performance (5.7) is given by

$$Q_\Delta(\phi, j\omega) = 1 - P_{11} \Delta_P + \left(P_{11} P_{22}^{(12)} \Delta_P - P_{12}^{(11)} P_{21}^{(11)} \Delta_P - P_{22}^{(11)} \right) \phi_1
+ \left(P_{11} P_{22}^{(22)} \Delta_P - P_{12}^{(12)} P_{21}^{(21)} \Delta_P + P_{11} P_{22}^{(22)} \right) \phi_2
+ \left(P_{11} P_{22}^{(22)} - P_{22}^{(12)} P_{22}^{(21)} - P_{11} P_{22}^{(11)} P_{22}^{(22)} \Delta_P + P_{11} P_{22}^{(12)} P_{22}^{(21)} \right) \phi_1 \phi_2,$$  \hspace{1cm} (5.9)

for which the following partitioning of the generalized plant $P(j\omega)$ is considered

$$P(j\omega) = \begin{bmatrix} P_{11}(j\omega) & P_{11}^{(11)}(j\omega) & P_{11}^{(12)}(j\omega) \\ P_{12}^{(11)}(j\omega) & P_{12}^{(11)}(j\omega) & P_{12}^{(12)}(j\omega) \\ P_{21}^{(11)}(j\omega) & P_{21}^{(12)}(j\omega) & P_{22}^{(21)}(j\omega) \end{bmatrix}.$$

From the determinant expressions in (5.8) (for stability) and (5.9) (for performance) it can be seen that the expressions are bilinear in $\phi$. For three parameters the expression is trilinear and for higher numbers of parameters the expression is multilinear.
5.3.2. **CONSTRAINTS IN THE NYQUIST DIAGRAM**

Consider the Nyquist curves of (5.6) and (5.7), respectively denoted as $Q(\phi, j\omega)$ and $Q_\Delta(\phi, j\omega)$, for a certain generalized plant $P(j\omega)$ and a parameter vector $\phi$, illustrated in Figure 5.4. In the figure, the thick solid line represents the Nyquist curve $Q(\phi, j\omega)$ (obtained with (5.8)) and the circles with centers at the solid line represent the Nyquist curve $Q_\Delta(\phi, j\omega)$ (obtained with (5.7)). Thus, the Nyquist curve $Q_\Delta(\phi, j\omega)$ with performance $\Delta_P$ forms a banded graph around the Nyquist curve of $Q(\phi, j\omega)$.

The closed-loop system $T_{wz}$ is stable if and only if the Nyquist curve $Q(\phi, j\omega)$ does not encircle the origin. Moreover, performance is achieved if and only if the Nyquist curve $Q_\Delta(\phi, j\omega)$ does not encircle the origin. The latter two definitions impose clear constraints on the Nyquist curve. Hence, considering Figure 5.4 in this context, the lines $l_1(j\omega)$ and $l_2(j\omega)$ constrain the Nyquist curve from encircling the origin. Note the different colors of the Nyquist curves $Q(\phi, j\omega)$ and $Q_\Delta(\phi, j\omega)$, and the constraint lines $l_1(j\omega)$ and $l_2(j\omega)$, illustrating the relation and frequency dependency of the constraint lines and the Nyquist curves.

The Nyquist curve $Q(\phi, j\omega)$ can be constrained above the line $l_1(j\omega)$ in Figure 5.4 by setting

\[-\text{Im}(Q(\phi, j\omega)) + \alpha_1 \text{Re}(Q(\phi, j\omega)) + c_1 < 0,
\]

(5.10)

where Re(·) and Im(·) denote the real and imaginary parts, and $\alpha_1$ and $c_1$ are the slope and offset of the constraint line $l_1(j\omega)$. Similarly, the Nyquist curve $Q(\phi, j\omega)$ can be constrained below the line $l_2(j\omega)$ in Figure 5.4 by setting

\[\text{Im}(Q(\phi, j\omega)) - \alpha_2 \text{Re}(Q(\phi, j\omega)) - c_2 < 0,
\]

(5.11)

where $\alpha_2$ and $c_2$ are the slope and offset of the constraint line $l_2(j\omega)$. In the latter two equations, $Q(\phi, j\omega)$ can be replaced by $Q_\Delta(\phi, j\omega)$ to obtain constraints for closed-loop performance. The constraints for performance are denoted by $l_\Delta(\phi, j\omega)$. 

![Nyquist diagram](image-url)

Figure 5.4: Nyquist diagram for $Q(\phi, j\omega)$ (stability) and $Q_\Delta(\phi, j\omega)$ (performance). The colors indicate which of the constraints $l_1(j\omega)$ and $l_2(j\omega)$ hold for which part of the Nyquist plots.
5.3.3. Realisation of performance $\Delta P$

The performance $\Delta P(j\omega)$ is described by $\|\Delta P(s)\|_\infty \leq 1$. To avoid evaluating an infinite number of constraints, the performance $\Delta P(j\omega)$ is realized by $n_d$ points randomly drawn from $\|\Delta P(s)\|_\infty \leq 1$. The realization of the performance $\Delta P(j\omega)$ is denoted by $\hat{\Delta}P(j\omega)$ and the determinant determined by $\hat{\Delta}P(j\omega)$ is denoted by $Q_{\hat{\Delta}}(\phi, j\omega)$. Moreover, the number of constraints in (5.11) and (5.10) is proportional to the number $n_d$ of realizations of $\Delta P$. Relevant constraints can be obtained by realizing $\Delta P(j\omega)$ with maximum singular value, i.e., $\|\Delta P(s)\|_\infty = 1$.

5.3.4. Multilinear feasibility problem

Given the frequency response data of the generalized plant $P(j\omega)$, the line constraint(s) $l(\phi, j\omega)$ for stability or $l_{\Delta P}(\phi, j\omega)$ for performance, and realizations $\hat{\Delta}P$ of the performance $\Delta P$, a feasibility problem can be formulated to obtain stability and performance of the closed-loop system. For this, it should hold that for every frequency point, the constraints should be satisfied. For stability, the following problem is obtained

Find $\phi$ such that $l(\phi, j\omega) < 0 \quad \forall \omega$ \hspace{1cm} (5.12)

and for performance, the following problem is obtained

Find $\phi$ such that $l_{\Delta P}(\phi, j\omega) < 0 \quad \forall \omega, \forall \hat{\Delta}P(j\omega)$. \hspace{1cm} (5.13)

Note that in (5.12) and (5.13), multiple constraints can be used e.g., such as in Figure 5.4, which can be assigned per frequency. Further remark that the size\(^2\) of the feasibility problem (5.12) depends on the number of frequency points and in the case of (5.13) also on the number $n_d$ of performance realizations $\hat{\Delta}P$. Hence, the feasibility problem has $N$ constraints in the former case (5.12) and $N \cdot n_d$ constraints in the latter case (5.13), with $N$ the number of frequency points considered. Finally, it is important to note that the number of constraints in the feasibility problems thus does not depend on the number of controller parameters.

5.3.5. Convex feasibility problem

In the previous sections it is shown that by extracting the tunable controller parameters into the diagonal form, the resulting feasibility problem is multilinear in the controller parameters $\phi$. However, by creating the generalized plant configuration slightly different, the feasibility problem becomes a convex feasibility problem for some special controller cases. To see this, the diagonal controller parameter matrix with the perturbation $\Delta P$ as was previously used in (5.7) is modified to

$$K_1(\phi, s) = \begin{bmatrix} \Delta P(s) & 0 \\ 0 & C_1(\phi, s) \end{bmatrix}$$ \hspace{1cm} (5.14)

where $C_1(\phi, s)$ is now the full controller including the tunable controller parameters. To do so, the generalized plant needs to be changed accordingly as well. Thus, instead of extracting the tunable parameters in a diagonal matrix gain $K$ (as was done in Figure 5.1

\(^{2}\)We assume only a single constraint $l(\phi, j\omega)$ per frequency point.
and (5.2)), the full controller is included. In the case that $C_t(\phi, s)$ in (5.14) is SISO and affine in the tunable controller parameters $\phi$, the approach results in a convex feasibility problem. This can be demonstrated by writing down the determinant expression for the SISO controller case and a scalar perturbation block $\Delta P$. The performance condition then becomes

$$
\det \left( I - K_I(\phi, j\omega) P(j\omega) \right).
$$

Substituting for $K_I$ in (5.15) gives the determinant expression

$$
(1 - \Delta P P_{11}) (1 - C_I(\phi) P_{22}) - \Delta P P_{12} C_I(\phi) P_{21},
$$

which is affine in the controller parameters $\phi$. Hence, SISO controllers including e.g., PID controllers (assuming an affine parameterization) result in a convex feasibility problem. Note that the performance $\Delta P$, which can be multidimensional, and including line constraints in the Nyquist diagram remain unchanged.

5.4. GREY-BOX SYSTEM IDENTIFICATION

The controller design methodology presented in the previous sections can be extended to a class of system identification methods. By a slight reformulation of the problem, the methodology can be used to find the parameters of a parameterized model. This approach has been used to identify a simplified control-oriented model of the yaw dynamics of a two-bladed wind turbine in van Solingen et al. (2015c).

The model matching approach is as follows. The parameters $\phi$ of a model $H(j\omega)$ which should be matched to a measured FRF are extracted into a diagonal form by an LFT, i.e., $H(j\omega) = F_I(M(j\omega), \phi)$. Then, consider the schematic block diagram in Figure 5.5. In this diagram, the measured FRF of a plant is denoted by $H_{ref}(j\omega)$, and the model $M(jw)$ with tunable model parameters $\phi$ is obtained by the previous mentioned LFT. The outputs of $M(j\omega)$ are element-wise subtracted from the outputs of the reference model $H_{ref}(j\omega)$. The output $z$ of the generalized plant $P(j\omega)$ is then given by the differenced outputs, weighted by the performance weight $W_p(j\omega)$. Similarly as before, the full perturbation block $\Delta P$ closes the loop from $z$ to $w$.

In order to find the model parameters $\phi$ such that $H(j\omega)$ is close to $H_{ref}(j\omega)$, the exact same techniques as in the previous sections can be applied. However, for the case of grey-box system identification, the stability criterion in (5.8) is rather meaningless. Therefore, only the performance condition in (5.9) is considered in this respect. Again, by constraining the Nyquist curve from encircling or crossing the origin, a feasibility problem equal to (5.13) is obtained.

In the next section, the experimental setup is described which is used to demonstrate the presented methodologies.

5.5. EXPERIMENTAL SETUP

The experimental setup considered in this chapter is a double-mass-spring-damper system (see Figure 5.6). In Figure 5.6, a force $F$ acts on the first mass $m_1$ and the angular positions $x_1$ and $x_2$ are the positions of the first mass $m_1$ and second mass $m_2$, respectively. The stiffness and damping of the system are denoted by $k$ and $d$, respectively.
A lightly damped system will show a clearly visible resonance peak in a frequency plot. The system can be described by two transfer functions. The transfer function from force input $F$ to position $x_1$ (collocated) is given by

$$\frac{x_1}{F} = \frac{m_1 s^2 + ds + k}{m_1 m_2 s^4 + (m_1 + m_2)ds^3 + (m_1 + m_2)ks^2}, \quad (5.17)$$

and the transfer function from torque input $F$ to position $x_2$ (non-collocated) is given by

$$\frac{x_2}{F} = \frac{ds + k}{m_1 m_2 s^4 + (m_1 + m_2)ds^3 + (m_1 + m_2)ks^2}. \quad (5.18)$$

The resonance frequency $\omega_r$ is at $\omega_r = \sqrt{k/m_r}$, with $m_r = m_1 m_2/(m_1 + m_2)$. A photograph of the experimental setup is shown in Figure 5.7 and the setup will be used for demonstrating the controller design methodology. The DC motor drives the first mass, which is connected to the second mass through a flexible shaft. Both the first mass and second mass have position encoders. The force actuation commands and position
readbacks are connected to a PC using a real-time connection, which is operated from MATLAB Simulink® (Mathworks, 2013). An FRF of the system is obtained by a closed-loop experiment in which the system was excited with white noise. From the closed-loop data, the open-loop response was extracted and subsequently the plant dynamics can be obtained. By averaging the results for each frequency over a number of experiments, an FRF is obtained. The FRF results for both the collocated and the non-collocated system are shown in Figure 5.8. The resonance frequency $\omega_r$ is at approximately 54.2 Hz.

5.6. RESULTS

In this section, the design methodology presented in Section 5.2-Section 5.4 is applied to two simulation examples and to three example cases using the experimental setup discussed in Section 5.5. The example cases involve non-collocated control (i.e., the force input $F$ is used to control the position of the second mass $m_2$). The following five example cases are considered:

1. Finding a PD controller that achieves certain performance requirements on a simulation example;

2. Finding a PD controller and the stiffness parameter of the system (plant/controller optimization) that achieves certain performance requirements on a simulation example;

3. Finding a PD controller without notch filter to obtain certain performance specifications on the experimental setup;

4. Finding a PD controller with notch filter to obtain certain performance specifications on the experimental setup;
5. Finding the parameters \((m_1, m_2, k, d)\) in (5.18) using the FRF of the experimental setup and the grey-box system identification method outlined in Section 5.4.

In all example cases, the dimension of \(\Delta P\) is 1 \(\times\) 1 (only a single input \(w\) and a single output \(z\)). Therefore, the perturbation \(\Delta P\) is realized by drawing \(n_d\) samples from the unit circle (i.e., \(\|\Delta P\| = 1\)). The feasibility problem obtained in each example case is solved by using YALMIP (Löfberg, 2004) with MATLAB’s fmincon solver.

5.6.1. SIMULATION RESULTS

For the simulation examples, the model in Figure 5.6 is used. The parameters of this model are fictional such that the dynamics of the simulation examples and the experimental setup are different. The simulation examples were initially presented in van Solingen et al. (2014a) and are adopted here with minor changes.

PD CONTROLLER DESIGN

In the first simulation example, the input \(F\) is used to control the position \(x_2\) of the second mass. A PD controller with negative feedback is used to obtain certain closed-loop specifications. It is assumed that the system has a time delay of \(T_d = 0.1\) s, which is modeled by a first-order Padé approximation. To this end, the transfer function in (5.18) is connected in series with the time delay approximation and is denoted by \(G(s)\). The output of the system \(G(s)\), \(y = x_2\), is connected to the PD controller given by

\[
C_{PD}(s) = \frac{K_p + K_d s}{0.01 s + 1},
\]  

(5.19)
In order to maintain a diagonal control structure with only the controller parameters on the diagonal, the fractions in (5.19) are absorbed into the plant. Then, closed-loop system performance is imposed by a bound on the sensitivity function by means of a second-order performance weight (see Skogestad and Postlethwaite (2006))

\[ W_p(s) = \frac{s^2/M_p^2 + 2\beta_p\omega_B s + \omega_B^2}{s^2 + 2\beta_p A_p \omega_B s + (A_p\omega_B)^2}, \]

where \( \beta_p = 0.3, M_p = 2, A_p = 1 \cdot 10^{-3} \) and \( \omega_B = 0.1 \). The complete generalized plant configuration for this system is shown in Figure 5.9, where also the complex perturbation \( \Delta_P \) is included. In this example, the parameter values are taken as \( m_1 = m_2 = k = 1 \) and \( d = 0.05 \).

Because the complexity of this problem is relatively low (only two controller parameters need to be found), a grid search of the controller parameters is carried out. For each combination of \( K_p \) and \( K_d \), \( \|T_{wz}\|_\infty \) was computed. Thus, the solution space can be visualized and is shown in Figure 5.10. It can be observed that there is not an obvious solution to obtain an \( \mathcal{H}_\infty \)-norm lower than 1, making it an interesting problem to evaluate the proposed controller design method. The lowest obtained \( \mathcal{H}_\infty \) norm by the grid search is \( \|T_{wz}\|_\infty = 0.884 \), which is obtained for \( K_p = 0.068 \) and \( K_d = 0.142 \). For comparison, the method in Karimi and Galdos (2010) by using the Frequency-Domain Robust Control Toolbox (FDRCT) (Karimi, 2013), is also used. As mentioned in the introduction, this method requires a desired open-loop transfer function \( L_d(s) \). Setting \( L_d(s) = W_p - 1 \) (as suggested in Karimi (2013)) gives a satisfactorily result for which \( \|T_{wz}\|_\infty = 0.861 \), \( K_p = 0.069 \), and \( K_d = 0.145 \).

In order to find controller parameters that yield performance, the feasibility problem in (5.13) is constructed. Since the generalized plant is stable, the Nyquist curve should not encircle the origin. From some trial-and-error combinations of \( K_p \) and \( K_d \), a general
Figure 5.10: Results of the grid search of $K_p$ and $K_d$ for the controlled double-mass-spring-damper system. The light grey area represents controller parameter combinations resulting in an unstable closed-loop system, the grey area represents combinations which yield a stable closed-loop system and the dark grey area represents the solutions with $H_\infty$-norm lower than 1.

The idea of the Nyquist curve was obtained (similar to Figure 5.4). With this knowledge and for $N = 400$ frequency points on a logarithmic scale in the interval $[0.1, 10]$ rad/s, two constraints in the Nyquist diagram are formulated, i.e.,

$$\text{Im}(Q_\Delta(j\omega)) + 0.2\text{Re}(Q_\Delta(j\omega)) - 0.001 < 0 \quad \text{for } \omega \leq 0.16,$$

$$-\text{Im}(Q_\Delta(j\omega)) - 5\text{Re}(Q_\Delta(j\omega)) + 0.001 < 0 \quad \text{for } \omega \geq 0.20.$$

The performance $\Delta P(j\omega)$ is for each $\omega$ realized by $n_d$ points randomly sampled on the unit circle using a uniform distribution. Finally, the feasibility problem is solved by using YALMIP (Löfberg, 2004) and MATLAB’s fmincon function. The optimization procedure is carried out for 100 Monte Carlo simulations, where for each simulation the perturbation $\Delta P$ is re-realized and the initial controller parameters are uniformly drawn from $[0, 1]$.

The obtained results for varying number $n_d$ are listed in Table 5.1, which for reference also lists the grid search result and the FDRCT result. It should be stressed, that the proposed methodology does not minimize the $H_\infty$-norm, but rather tries to find a feasible solution for which it then holds that $\|T_{wz}\|_\infty < 1$. From Table 5.1, it can be seen that for increasing $n_d$, the number of feasible solutions increases, which is to be expected. Moreover, for $n_d = 100$ realizations of $\Delta P$ all trials satisfied the performance condition. The reason for not obtaining the lowest norm (i.e., the grid search result) is twofold. First, the optimization solver quits when a feasible solution is found rather than minimizing $\|T_{wz}\|_\infty$. Second, it is possible that the constraint lines were chosen too conservative and therefore constrained from solutions which yield the lowest norm. The Nyquist curve of the plant with controller, obtained for the case with $n_d = 100$ with lowest $H_\infty$ norm ($\|T_{wz}\|_\infty = 0.913$, $K_p = 0.048$, and $K_d = 0.1474$) is shown in Figure 5.11. The graph is plotted for a densely (large $n_d$) realized complex perturbation $\Delta P$, from which it
Table 5.1: Optimization results for varying number of realizations $n_d$ of $\Delta P$.

<table>
<thead>
<tr>
<th>Description</th>
<th>$\mathcal{H}_\infty^{\text{min}}$</th>
<th>$\mathcal{H}_\infty^{\text{max}}$</th>
<th>Success [%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Grid search</td>
<td>0.884</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>FDRCT</td>
<td>0.861</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>Nyquist optim. ($n_d = 5$)</td>
<td>0.900</td>
<td>2.884</td>
<td>46</td>
</tr>
<tr>
<td>Nyquist optim. ($n_d = 10$)</td>
<td>0.913</td>
<td>2.403</td>
<td>55</td>
</tr>
<tr>
<td>Nyquist optim. ($n_d = 25$)</td>
<td>0.892</td>
<td>1.072</td>
<td>86</td>
</tr>
<tr>
<td>Nyquist optim. ($n_d = 50$)</td>
<td>0.930</td>
<td>1.058</td>
<td>98</td>
</tr>
<tr>
<td>Nyquist optim. ($n_d = 100$)</td>
<td>0.913</td>
<td>0.988</td>
<td>100</td>
</tr>
</tbody>
</table>

Figure 5.11: Resulting Nyquist plots of $Q(\phi, j\omega)$ (black) and $Q_\Delta(\phi, j\omega)$ (light grey and dark grey) for the first simulation example. The colors of the constraint lines and the Nyquist curve are matched to indicate where they hold.

It can be observed that the origin (indicated by +) is not encircled.

Simultaneous plant/control design

In the second simulation example, the simultaneous design of controller and plant parameters is considered. The goal of this example is to find PD controller parameters and the value of the stiffness parameter of the system such that a closed-loop performance specification is satisfied. To this end, the stiffness parameter $k$ in Figure 5.6 is extracted from the model by adding an external force $F_k$, which acts on both masses (see Figure 5.12). The dynamics for the modified system $G_1(s)$ are given by

$$
\begin{bmatrix}
\dot{x}_1 \\
\dot{x}_2
\end{bmatrix} = G_1(s) \begin{bmatrix}
F \\
F_k
\end{bmatrix},
$$

with $G_1(s)$ equal to

$$
\frac{1}{m_1 m_2 s^3 + (m_1 + m_2) d s^2} \begin{bmatrix}
m_2 s + d & -m_2 s \\
d & m_1 s
\end{bmatrix}.
$$
Note that by taking
\[ F_k = \kappa (x_1 - x_2), \]
and setting \( \kappa = k \), the systems in Figure 5.6 and Figure 5.12 are identical. If \( F_k \) is chosen as in (5.20), it can be regarded as adding stiffness to the system. Thus, by absorbing \( x_1 - x_2 \) into the plant, \( \kappa \) becomes a structural parameter which can be optimized. Finally, the positions \( x_1 \) and \( x_2 \) are assumed to have a time delay of 0.05 s, modeled by a first-order Padé approximation.

As with the previous case, a PD controller is used to obtain certain closed-loop specifications. In order to avoid trivial solutions (e.g., \( \kappa \) going to infinity), the performance weight \( W_p(s) \) of the previous case is modified to
\[ W_{p,1}(s) = W_p(s) \times \frac{s^2 + 2\beta_p^* A_p^* \omega_B^* s + (A_p^* \omega_B^*)^2}{s^2 / (M_p^*)^2 + 2\beta_p^* \omega_B^* s + (\omega_B^*)^2}, \]
where \( \beta_p^* = 0.7, M_p^* = 1.9, A_p^* = 0.9 \) and \( \omega_B^* = 1 \). The modification can be regarded as putting a constraint on the resonance frequency of the system. With the modified performance weight \( W_{p,1}(s) \), the generalized plant is then depicted in Figure 5.13. Similar to the previous case, a grid search of the three controller parameters is carried out in order to visualize the solution space. The results are shown in Figure 5.14.

Now the proposed method is applied to find the controller parameters \( K_p \) and \( K_d \), and the structural parameter \( \kappa \), such that the performance condition (5.7) is satisfied. The performance \( \Delta_p \) is realized by \( n_d = 100 \) points randomly sampled on the unit circle and the following constraints are applied
\[
-\text{Im}(Q_{\Delta}(j\omega)) + 0.7\text{Re}(Q_{\Delta}(j\omega)) + 0.001 < 0 \quad \text{for } \omega \leq 0.37, \\
\text{Im}(Q_{\Delta}(j\omega)) + 0.001 < 0 \quad \text{for } 0.54 \leq \omega \leq 0.57.
\]
Then, 100 Monte Carlo simulations for uniformly drawn initial parameter values in the interval \([0, 1]\) were performed. The solution with the lowest \( \mathcal{H}_\infty \) has controller parameters \( K_p = 0.0534, K_d = 0.1088, \kappa = 0.1604 \), and \( \| T_{\text{wz}} \|_\infty = 0.862 \). For completeness, with a grid search the lowest \( \mathcal{H}_\infty \) norm was found to be 0.8587.

5.6.2. Experimental results
In the experimental results, the experimental setup of Section 5.5 is used to demonstrate the controller design and grey-box system identification methods. The FRF as shown in Figure 5.8 is used to design the controllers, with 400 linearly spaced frequency points in the interval \([1.95, 391.6]\) Hz.
Figure 5.13: Configuration of the plant and controller for the simultaneous design of plant and controller.

Figure 5.14: Results of the grid search of $K_p$, $K_d$, and $\kappa$ for the double-mass-damper system. The volume within the light grey contour lines indicate the parameter combinations resulting in a stable closed-loop system and the volume within the dark grey contour lines are combinations which yield a stable closed-loop system with $\mathcal{H}_\infty$ norm lower than 1.
**PD Controller**

In the first case, the objective is to find the proportional and derivative gain of a PD controller such that certain frequency-domain performance specifications are met. The controller structure is given by

\[
C_{PD,1}(s) = \frac{K_p + K_d s}{1/(2\pi f_c) s + 1},
\]

where \( f_c = 120 \text{Hz} \) is the cut-off frequency of the low-pass filter and \((K_p, K_d)\) are the controller parameters that are sought. The performance requirement of the controlled system is a closed-loop bandwidth of 3Hz. To this end, the following second-order performance weight (Skogestad and Postlethwaite, 2006) is used

\[
W_{p,2}(s) = \frac{s^2 + 2\beta_p \omega_B s + \omega_B^2}{s^2 + 2\beta_p A_p \omega_B s + (A_p \omega_B)^2},
\]

with \( \beta_p = 0.8 \), a maximum sensitivity function gain of 6dB by setting \( M_p = 1.4 \), \( A_p = 0.05 \), and a desired bandwidth of \( \omega_B = 2\pi 2.8 \text{rad/s} \). The generalized plant configuration is therefore very similar to Figure 5.9.

It was found during the experiments that although the bandwidth of the closed-loop system was hardly affected by the proportional gain \( K_p \), the reference tracking performance was greatly influenced by \( K_p \) (i.e., \( K_p \) is mainly dominant at frequencies smaller than the closed-loop bandwidth). A low value of \( K_p \) results in poor reference tracking, whereas a larger value of \( K_p \) gives satisfactory reference tracking performance. The reason for this effect is the non-linearity of the system at low frequencies. For example, friction effects can be (partly) overcome with a higher proportional gain (with the chosen PD controller the proportional gain \( K_p \) is dominant at low frequencies). Hence, in order to have satisfactory tracking performance, it was required to maximize the proportional gain during the optimization process. Therefore, the feasibility problem (5.13) was turned into an optimization problem by maximizing the proportional gain \( K_p \) subject to the constraints (5.13). For the optimization problem, the perturbation block \( \Delta_P \) was realized by \( n_d = 100 \) points on the unit circle and two line constraints were used. The gains of the final implemented controller are \( K_p = 0.1234 \) and \( K_d = 0.0091 \), for which the \( \mathcal{H}_\infty \) norm is 0.950. The resulting sensitivity function and the inverse of the performance weight are shown in Figure 5.15, from which it can be seen that the sensitivity function remains below the inverse of the performance weight.

The results of the implemented controller on the setup are shown in Figure 5.16-5.17. The measured open-loop function of the setup is shown in Figure 5.16. It can be observed that the cross-over frequency of the loop gain crosses 0dB around 4Hz. Moreover, the step response shows decent tracking behavior. The small oscillation in the step response is caused by the resonance of the system.

**PD Controller with notch filter**

For the second controller case, the objective is to increase the bandwidth of the system. To this end, the previous controller (5.21) is extended with a notch filter,

\[
C_{PD,2}(s) = C_{PD,1}(s) \times \frac{s^2 + 2\beta_x \omega_r s + \omega_r^2}{s^2 + 2\beta_p \omega_r s + \omega_r^2},
\]
Figure 5.15: Sensitivity function obtained with the optimized controller for the first experiment. The inverse of the performance weight $W_p$ is also shown.

Figure 5.16: Measured open-loop transfer function of the first experiment

Figure 5.17: Measured step response of the first experiment
where $\omega_r$ is the resonance frequency of the experimental setup and $\beta_z$ and $\beta_p$ determine the width and deepness of the notch filter. The low-pass filter remains unchanged. Therefore, the generalized plant configuration in Figure 5.13 is modified to include an LFT of the notch filter. The bandwidth of the performance weight $W_{p,2}(s)$ in (5.22) is changed from $\omega_B = 2\pi 2.8 \text{ rad/s}$ to $\omega_B = 2\pi 6 \text{ rad/s}$. Thus, in this experiment, the controller parameters ($K_p$, $K_d$, $\beta_z$, $\beta_p$) are sought, such that the modified performance specification is satisfied. Similar to the previous case, four line constraints were used, $n_d = 50$, and an optimization problem maximizing the value of $K_p$ subject to the constraints was solved. The final obtained solution has gain $K_p = 0.6210$, $K_d = 0.0216$, $\beta_z = 0.0406$, and $\beta_p = 0.5190$. For these gains, the $H_\infty$ norm of the weighted closed-loop system is 0.8989. For this controller the sensitivity function and inverse of the performance weight are shown in Figure 5.18.

The results of the PD controller augmented with notch filter are shown in Figure 5.19-Figure 5.20. From the measured loop gain of the system it can be observed that the 0 dB line is now crossed at a frequency of roughly 10 Hz. With respect to the previous case, the bandwidth has increased by 2.5 times. The increased bandwidth can also be observed from the step response where both controller cases are compared.

**Grey-box System Identification**

The grey-box system identification method introduced in Section 5.4 can be applied to identify the parameters of the model in (5.18). To this end, the generalized plant structure as shown in Figure 5.5 is used. The model $M(s)$ is obtained by an LFT of the transfer function in (5.18), that is, the parameters ($m_1$, $m_2$, $k$, $d$) are extracted from the transfer function such that they can be put in the diagonal form used throughout this chapter.

From the step responses obtained earlier, a small time delay (approximately 0.005 s) can be observed, which was modeled by a first-order Padé approximation. Selecting the performance weight for this example case is not trivial. However, it was found that multiplying with the inverse of the plant FRF and an inverted notch filter at the resonance frequency of the system gave a satisfactorily result. The performance weight is thus given by

$$W_{p,3}(j\omega) = \frac{1}{H_{\text{ref}}(j\omega)} \times \frac{10j\omega}{(j\omega)^2 + 2\omega_r 0.01j\omega + \omega_r^2}.$$
It was also found that two constraint lines are required to constrain the Nyquist curve from crossing zero. The feasibility problem was then solved by constraining \( m_1 = m_2 \) (the masses are assumed to be of equal weight) and \( d \) to be smaller than 0.01, and \( n_d = 25 \). Note that setting \( m_1 = m_2 \) has the consequence that quadratic terms appear in the feasibility problem. The feasible solution with the lowest \( H_\infty \) norm, i.e., \( \| T_{wz} \|_\infty = 0.5151 \), is shown in Figure 5.21. For this solution the parameters are \( m_1 = m_2 = 0.0048 \), \( k = 11.4494 \), and \( d = 0.0014 \).

Figure 5.20: Measured step response of the second experiment. The measured step response of the first experiment is also shown.
5.7. CONCLUSIONS

A novel frequency-domain design methodology exploiting the generalized Nyquist stability criterion has been presented in this chapter. The methodology focuses mainly on fixed-structure controllers, of which the tunable parameters can be extracted into a diagonal form. By introducing line constraints in the Nyquist diagram, the Nyquist curve is prevented from encircling or crossing the origin, such that stability and certain performance specifications of the closed-loop system can be achieved. The line constraints result in a feasibility problem multilinear in the tunable controller parameters. However, it was shown that in special controller cases, the feasibility problem becomes convex in the tunable parameters. The methodology can directly be applied to design fixed-structure controllers using a measured FRF of the plant, but can also be used to simultaneously optimize plant and controller parameters, and for grey-box system identification. The method has been successfully demonstrated through simulation examples and on an experimental setup.

Figure 5.21: Comparison between identified model and measured FRF.
CONCLUSIONS AND RECOMMENDATIONS

Recently, two-bladed wind turbines have gained renewed interest as they potentially provide an acceleration in decreasing the cost of offshore wind energy. Wind turbines with two-bladed rotors have long remained unconsidered because of noise and visual impacts, and higher fatigue loadings compared to three-bladed rotors. However, at offshore locations the noise and visual impacts cease to exist and active control can compensate for the fatigue loads. As control design for two-bladed wind turbines has hardly been investigated in the past, structured control architectures and a tuning method for two-bladed wind turbines have been developed in this thesis. The conclusions and recommendations are given in this chapter.

6.1. CONCLUSIONS

The main conclusions of this thesis are divided into three different subjects: Linear Individual Pitch Control (LIPC), control architecture for wind turbines with free yaw, and fixed-structure control design method.

LINEAR INDIVIDUAL PITCH CONTROL

In this thesis it was shown that the Linear Individual Pitch Control (LIPC) strategy, compared to the conventional Individual Pitch Control (IPC) strategy, achieves very similar load reductions. In a simulation study it was demonstrated that the LIPC strategy, with a structured control design approach, is able to successfully remove the 1P, 2P, and 3P blade loads. A measurement campaign using the NREL-CART2, for which the 1P blade loads were targeted, confirmed that both strategies achieve identical load reduction performance.

Although it was analytically shown that the Multi-Blade Coordinate (MBC) transformation for two-bladed rotors is singular, it can without problems be used for IPC of two-bladed wind turbines. On the other hand, the singularity motivated the use of a linear coordinate transformation, borrowed from helicopter theory, and the LIPC strategy. It was
demonstrated that with the linear transformation, the blade root moments are transformed to a collective mode, containing all the even harmonic blade loads (2P, 4P, ...), and a differential mode, containing all odd harmonics (1P, 3P, ...). Therefore, only a single controller is required to decrease the 1P loads with the linear coordinate transformation, which is one less than with the conventional IPC strategy. Consequently, at most two controllers are required (one for the collective mode and one for the differential mode) to potentially reduce all blade load harmonics. It is therefore concluded that the benefit of using LIPC instead of conventional IPC mainly lies in the controller synthesis step.

CONTROL ARCHITECTURE FOR WIND TURBINES WITH FREE YAW
In this thesis, also a control architecture for a state-of-the-art wind turbine with a damped free-yaw configuration was developed. The main conclusion drawn from the results of this design study is that the tuning of the involved control loops and the choice for the yaw damping value is coupled and poses the designer a tradeoff between blade loads and tower loads. Specifically, increasing the yaw damping yields higher tower torsional loads and lower blade loads, and decreasing the damping yields lower torsional loads and higher blade loads. Thus, the choice for the ‘optimal’ yaw damping value remains up to the designer and the specifics of the wind turbine.

Furthermore, it was shown that the integration of the yaw-by-IPC controller and the IPC load reduction controller is not straightforward. Two different control configurations can be considered, where the difference of these configurations lies in where the yaw-by-IPC control loop is summed with the conventional IPC loop. This can be either right after the forward MBC transformation, or right before the reverse MBC transformation. It was shown that both configurations can be tuned so as to yield similar load reductions, however, in the event of sensor failures of the blade root moments, the latter configuration remains stable and the former causes the closed-loop system to become unstable. For that reason, it was concluded that the latter controller configuration is more suitable for practical consideration.

Finally, it was shown that (additional) yaw damping can also be supplied by means of IPC. The use of this additional controller was shown to decrease the tower torsional loads by roughly 5%, while the other turbine loads remain roughly unchanged.

FIXED-STRUCTURE CONTROL DESIGN METHOD
A novel controller design methodology was proposed for fixed-structure controller design in this thesis. The approach exploits the generalized Nyquist diagram and uses line constraints to constrain the Nyquist curve from encircling the origin so as to impose stability and performance requirements on the closed-loop system. The specific approach involves extraction of the tunable controller parameters from the controller into a diagonal matrix gain. This is a novel approach to tune the controller parameters of a fixed-structure controller. Moreover, in special controller cases a convex feasibility problem can be obtained.

It was shown, that the method can be used to simultaneously optimize plant and controller parameters. The latter is achieved by extracting both the structural and controller parameters from the plant and controller into a diagonal matrix gain. By defining the stability and performance conditions and setting the line constraints, a simultaneous design of plant and controller is achieved.
6.2. RECOMMENDATIONS

The work in this thesis has provided two control architectures for two-bladed wind turbines and a novel approach to tune the parameters of fixed-structure controllers. During the research, several opportunities for further research were identified and are outlined next.

The control architecture for a wind turbine with free-yaw configuration was designed and evaluated for normal power production conditions. However, various extreme wind conditions can occur during the lifetime of a turbine and only a load case with an Extreme Direction Change (EDC) of the wind was evaluated in this thesis. Therefore, the robustness of the controllers should be checked for other extreme load cases. Moreover, some turbine components are driven by extreme loads rather than fatigue loads. For that reason, future research should focus on control opportunities for load reduction during extreme wind conditions and the detection of such extreme events.

The controller gains of the proposed control architecture strongly depend on the operating condition of the wind turbine. Gain-scheduling techniques were used to account for the differences in dynamics between different operating conditions. Linear Parameter-Varying controllers have in this regard the potential to improve turbine stability and performance, and should for that reason be considered.

The control architecture developed for the free-yaw turbine was shown to yield good performance in a high-fidelity simulation study for below-rated and above-rated operating conditions. The next step, with taking the previous recommendations into account, is to implement the architecture on a (commercial) wind turbine and verify the performance in a practical environment.

Although the fixed-structure controller design method can be convex for special controller cases, in general it yields a multilinear feasibility problem. Moreover, defining the line constraints in the Nyquist diagram remains an issue, for which possibly other constraints, such as circle constraints, can be introduced in a more systematic approach.

The specific approach of extracting the tunable parameters from the generalized plant into a diagonal controller as presented in Chapter 5, possibly provides a new perspective on the design of fixed-structure controllers. Future research should be directed towards investigating whether the diagonal controller structure can potentially be exploited in other existing controllers synthesis methods.

Finally, future research should be devoted to develop efficient, scalable, non-conservative, and convex design methodologies. Additionally, the aim of the research should also be to develop systematic methods to simultaneously optimize plant and controller.


Aerodyn engineering GmbH. The next generation becomes reality, 2014. SCD Flyer.


6.2. Recommendations


Maeda, Y. and Iwasaki, M. A feedback controller design based on circle condition for improvement of disturbance suppression. In *Advanced Motion Control (AMC), 2012 12th IEEE International Workshop on*, pages 1–6, March 2012.


LIST OF ABBREVIATIONS

AEP  Annual Energy Production
CART2  Controls Advanced Research Turbine 2
CPC  Collective Pitch Control
DEL  Damage Equivalent Load
FAST  Fatigue, Aerodynamics, Structures, and Turbulence
FDRCT  Frequency-Domain Robust Control Toolbox
FLOW  Far and Large Offshore Wind
FRF  Frequency-Response Function
IP  In-Plane
IPC  Individual Pitch Control
LFT  Linear Fractional Transformation
LIPC  Linear Individual Pitch Control
LMI  Linear Matrix Inequality
LPV  Linear Parameter-Varying
LTI  Linear Time-Invariant
MBC  Multi-Blade Coordinate
MIMO  Multi-Input Multi-Output
NREL  National Renewable Energy Laboratory
NWTC  National Wind Technology Center
OoP  Out-of-Plane
PBSID_{opt}  Optimized Predictor-Based Subspace IDentification
PD  Proportional Derivative
PI  Proportional Integral
PID  Proportional Integral Derivative
CONCLUSIONS AND RECOMMENDATIONS

RBS  Random Binary Signal
SISO  Single-Input Single-Output
VAF  Variance Accounted For
Wind energy has evolved over the past decades into a mature source of sustainable energy. Many developments and innovations have resulted in the cost of onshore wind energy nowadays being competitive with fossil energy sources. However, as onshore wind energy faces social resistance and a limited availability of onshore locations, wind energy is increasingly deployed at offshore locations. As opposed to onshore wind power, offshore wind power still has a much higher cost of energy. Wind turbine manufacturers, designers, and researchers are therefore continuously looking for opportunities to drive down the costs associated with offshore wind energy. In this regard, two-bladed wind turbines can potentially provide a 10-20% cost reduction compared to three-bladed wind turbines with the same capacity. For that reason, manufactures have recently gained renewed interest in two-bladed wind turbines.

Wind turbines with two-bladed rotors have long remained unconsidered for a number of reasons. These reasons include a higher noise emission level because of a higher rotational speed compared to three-bladed turbines and a restless view of the beam-like rotor passing the turbine tower. Furthermore, two-bladed wind turbines have more complex dynamics compared to three-bladed turbines and thereby higher fatigue loads. However, the noise and visual drawbacks disappear for offshore deployment and the use of active control can (partly) compensate for the increased fatigue loadings. One such active control strategy is Individual Pitch Control (IPC), in which each blade is individually and partially rotated along its longitudinal axis, based on the measured loads, so as to reduce the periodic turbine loads. This method, and control design in general, have been extensively explored for three-bladed wind turbines, but has only marginally been considered for two-bladed wind turbines. Therefore, the goal of this thesis is to develop structured control architectures and a controller tuning method for two-bladed wind turbines.

In order to achieve the thesis goal, the conventional IPC approach for two-bladed wind turbines is analyzed. In the analysis it was shown that the Multi-Blade Coordinate (MBC) transformation used by the conventional IPC strategy is singular. This motivated the use of a linear coordinate transformation, replacing the non-linear MBC transformation. By exploiting the properties of this transformation, a new IPC architecture, called Linear Individual Pitch Control (LIPC), is proposed. The design of the LIPC is carried out by fixing the controller structure beforehand, and only optimizing the tunable controller parameters. Subsequently, the strategy is compared to the conventional IPC strategy by means of a simulation study, demonstrating the efficacy of LIPC. In this study, it is shown that the LIPC and the conventional IPC strategy achieve identical load reduction performance. It is also shown that LIPC can successfully remove the higher harmonic (2P 3P,...) blade loads. Finally, the performance of the LIPC method is evaluated by means of a measurement campaign on the NREL CART2. The measurement results confirm the results achieved in the simulation study and show that LIPC and conven-
tional IPC achieve similar load reductions and that the benefit of using LIPC instead of conventional IPC mainly lies in the controller synthesis step.

The above discussed LIPC architecture is developed for wind turbines with a rigid yaw configuration. For wind turbines with a free-yaw configuration making use of IPC for both yaw control\(^1\) and load control, a different control architecture is required. To this end, it is investigated for a state-of-the-art two-bladed wind turbine designed by the Dutch company 2-B Energy B.V., how the yaw-by-IPC, regulating the misalignment of the rotor with the wind direction, and the IPC for load reduction can be combined (i.e., the objectives of both control loops are conflicting). Two different control architectures are considered and analyzed in terms of load reduction, wind direction tracking, and stability. From simulation studies it can be concluded that both architectures perform very similar when it comes to regulating the yaw misalignment and reducing the turbine loads. However, only one of the control architectures is robust to sensor failures and is therefore more suitable for practical consideration. For this architecture, also the impact of yaw damping provided by the yaw system on the wind turbine is analyzed. From this analysis it is concluded that the choice for the yaw damping value is a tradeoff between blade loads and tower loads. Moreover, the yaw damping value influences the yaw dynamics and should therefore be taken into account during the controller design. Finally, it was shown that yaw damping can also be added to the system by means of IPC. It is shown that by doing so, roughly 5% of additional tower torsion reduction can be achieved.

For the control architectures discussed in the previous paragraphs, the focus was on the development of structured control architectures rather than on the specific tuning of the involved controllers. In the last part of the thesis, the focus is on the design of a tuning method for structured controllers. To this end, a frequency-domain controller design method is proposed. The starting point of the design method is to construct the generalized plant such that the tunable controller parameters form a diagonal matrix gain. The generalized Nyquist stability criterion is then exploited so as to impose stability and performance of the closed-loop system. This is achieved by constraining the Nyquist curve from certain parts of the Nyquist diagram. The constraints then result in a feasibility problem, which for feasible solutions satisfy the required conditions. Typically, the feasibility problem is multilinear in the controller parameters, but it is shown that for certain controller cases a convex feasibility problem can be obtained. The proposed method is successfully demonstrated by means of simulation examples and experiments conducted on an experimental setup. It is also shown that the method can be used to simultaneously optimize plant and controller parameters.

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\(^1\)By appropriately varying the individual blade pitch angles, a moment around the tower can be created such that the rotor-nacelle assembly can be actively aligned with the wind.
SAMENVATTING

Windenergie is de laatste jaren uitgegroeid tot een betrouwbare bron van duurzame energie. Vele ontwikkelingen en innovaties hebben er toe geleid dat de kosten van windenergie op land competitief zijn geworden met de kosten van fossiele energiebronnen. Windenergie op land heeft echter te maken met veel maatschappelijke weerstand en een gebrek aan geschikte locaties, daarom wordt er in toenemende mate windenergie op zee geïnstalleerd. In tegenstelling tot windenergie op land, heeft windenergie op zee steeds een veel hoger kostenplaatje. Windturbinefabrikanten, ontwerpers en onderzoekers zijn constant op zoek naar nieuwe mogelijkheden om de kosten omlaag te drijven. In dit opzicht bieden tweebladige windturbines een potentiële kostenreductie van 10-20% ten opzichte van driebladige windturbines. Om die reden hebben diverse windturbinefabrikanten recent (opnieuw) hun aandacht op de ontwikkeling van tweebladige windturbines gevestigd.

Er bestaan een aantal redenen waarom tweebladige windturbines lange tijd niet werden ontwikkeld. Een van de redenen is de hogere rotatiesnelheid van tweebladige windturbines wat tot hogere geluidsproducties leidt. Een andere reden is dat een turbine met twee bladen een onrustig beeld creëert voor het zicht. Daarnaast is, vergeleken met driebladige turbines, de dynamica van tweebladige turbines complexer wat er toe leidt dat tweebladige turbines meer last ondervinden van materiaalmoehed. Echter, door de recente verschuiving van windenergiewinning op land naar windenergiewinning op zee, vallen de negatieve geluids- en visuele effecten weg en door het gebruik van actieve regeltechniek kan de toegenomen materiaalvermoeiing (grotendeels) worden tegengegaan. Een dergelijke regeltechnische toepassing is het gebruik van individuele bladhoekregelingen, waarbij, op basis van de gemeten buigmomenten in de bladwortels, elk blad individueel, periodiek en gedeeltelijk rond de lengteas wordt gedraaid. Deze techniek, en regeltechniek in zijn algemeenheid, is uitgebreid onderzocht voor driebladige windturbines, maar nauwelijks voor tweebladige turbines. Het doel van dit proefschrift is daarom het ontwikkelen van gestructureerde regeltechnische architecturen en regeltechnische instellingsmethodieken voor tweebladige windturbines.

Om dit doel te bereiken is als eerste stap de conventionele individuele bladhoekregelingenmethode voor driebladige windturbines geanalyseerd. Deze analyse heeft aangetoond dat de multi-blad coördinatentransformatie, die wordt toegepast in de conventionele individuele bladhoekregeling, voor tweebladige rotors een singulariteit bevat. Dit vormde de motivatie om een lineaire coördinatentransformatie en een nieuwe regeltechnische architectuur voor tweebladige turbines te introduceren: lineaire individuele bladhoekregeling. Voor het ontwerp van deze regeling kan de structuur van de regeling volledig worden opgelegd zodat alleen de instelbare parameters hoeven te worden geoptimaliseerd. Een simulatiestudie heeft aangetoond dat de lineaire en conventionele strategiën identieke belastingreducties op de componenten van de turbine behalen. Daarnaast is gedemonstreerd dat de lineaire strategie relatief eenvoudig kan worden
uitgebreid om de hogere harmonische bladbelastingen (2P, 3P,...) te reduceren. Uiteindelijk is de lineaire regelstrategie toegepast gedurende een testcampagne op een echte windturbine: de NREL CART2 windturbine. Deze meetcampagne bevestigt de resultaten behaald in de simulatiestudie en laat zien dat de lineaire en conventionele bladhoekregelingsstrategiën identieke resultaten behalen en dat het voordeel van de lineaire strategie ligt in het ontwerp van de regeling.

De hierboven besproken lineaire bladhoekregeling kan alleen worden toegepast in tweebladige windturbines waarbij de gondel met remmen wordt vastgezet op de toren, zodat deze niet vrij kan draaien. In het geval van een turbine waarbij de gondel en de rotor vrij zijn om te draaien op de toren en waarbij een individuele bladhoekregeling wordt gebruikt om de wind te volgen\(^2\), is een andere regelstrategie vereist. Een dergelijke turbine wordt door het Nederlandse bedrijf 2-B Energy B.V. ontwikkeld. Voor deze windturbine is onderzocht hoe het actief reguleren van de gierhoek met behulp van individuele bladhoekregelingen kan worden gecombineerd met de individuele bladhoekregeling om de bladbelastingen te reduceren (de regellussen kunnen tegenstrijdig zijn met elkaar).

Twee verschillende regeltechnische architecturen zijn daarvoor geanalyseerd, waarbij de belastingreducties, het volgen van de windrichting en de stabiliteit werden vergeleken. Hieruit is geconcludeerd dat beide architecturen vrijwel identieke belastingreducties behalen en vergelijkbare resultaten opleveren voor het volgen van de windrichting. Daarentegen is maar een van de architecturen robuust tegen sensorfouten en om die reden is de methode succesvol getoetst met behulp van diverse simulatievoorbeelden en praktische experimenten. Het is ook aangetoond dat de methode kan worden gebruikt om gelijktijdig systeem- en regelparameters te optimaliseren.

\(^2\)Door het op de juiste manier variëren van de individuele bladhoeken kan een draaimoment om de toren worden gecreëerd zodanig dat de gondel en de rotor actief in de wind kunnen worden gepositioneerd.
LIST OF PUBLICATIONS

JOURNAL PAPERS


CONFERENCE PAPERS


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He attended pre-university school from 1999 to 2005 at Maerlant College in Brielle. In 2005 he started his studies in Electrical Engineering at the Delft University of Technology and obtained the Bachelor of Science degree in 2009. In September 2011 he received his Master of Science degree in Systems and Control from the Delft University of Technology. The graduation project was entitled: “Estimating the average grain diameter in the sedimentation process of hopper dredgers”.

In October 2011 he started his Ph.D. project entitled “Integrated design of far large offshore wind turbines” at the Delft Center for Systems and Control (DCSC) of the Delft University of Technology, under the supervision of dr. Jan-Willem van Wingerden, dr. Roeland De Breuker, and prof. dr. Michel Verhaegen. The Ph.D. project was funded and supported by the Far Large Offshore Wind (FLOW) project, with 2-B Energy as industrial project partner. The focus of the project was on the development of control architectures and tuning methods for two-bladed wind turbines. During his Ph.D., he conducted several wind tunnel experiments and a measurement campaign on the two-bladed Controls Advanced Research Turbine (CART2) together with the National Renewable Energy Laboratory (NREL).

Throughout his Ph.D. research he supervised several M.Sc. students, assisted in the M.Sc. course “Filtering and Identification”, and participated in various international conferences and events. He received the DISC certificate from the Dutch Institute of Systems and Control in 2014.