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Experimental and Theoretical Studies of the Site Occupancy and Luminescence of Ce^{3+} in $LiSr_4(BO_3)_3$ for Potential X-ray Detecting Applications

Yunlin Yang, Bibo Lou, Yiyi Ou, Fang Su, Chong-Geng Ma, Chang-Kui Duan, Pieter Dorenbos, and Hongbin Liang*



measurements, respectively. This shows that concentration quenching does not occur in the investigated doping range, but inhomogeneous broadening exists in the concentrated samples. With the estimated thermal quenching activation energy, the discussions on the thermal quenching mechanisms suggest that the thermal-ionization process of the 5d electron is a dominant channel for thermal quenching of Ce^{3+} luminescence, despite the fact that thermally activated concentration quenching cannot be excluded for the highly doped samples. Finally, the X-ray excited luminescence measurement demonstrates the promising applications of the phosphors in X-ray detection.

1. INTRODUCTION

The investigation of the luminescence of Ce³⁺ in various host compounds has always been a fascinating field because of its fundamental significance and wide application.^{1,2} From the viewpoint of basic research, the Ce3+ ion shows typical 4f-5d transitions. Due to the simplest 4f¹ and 5d¹ electronic configurations of a Ce³⁺ ion in the ground and excited states, the energies of f-d transitions of Ce^{3+} in a host compound can provide a key reference to those of lanthanide ions such as Eu²⁺ and Pr³⁺ in the same lattice sites of the same host compounds.³ In addition, the luminescence of Ce³⁺ is also important for actual applications, and Ce3+-doped materials have been utilized in different fields after years of continuous efforts. For example, Y₃Al₅O₁₂:Ce³⁺ is well-known as a yellowemitting phosphor in phosphor-converted light-emitting diodes (pc-LEDs). The scintillators Lu₂SiO₅:Ce³⁺, LuA- $1O_3:Ce^{3+}$, and $LnX_3:Ce^{3+}$ (Ln = La, and X = Cl or Br; Ln = Lu, and X = I have been used commercially to detect ionizing radiation.^{1,4}

systematically investigated by luminescence intensity and lifetime

Because the crystal field strength has a strong influence on the outer 5d orbital of Ce^{3+} , the 4f–5d transition energies of Ce^{3+} may present remarkable variations in different coordination surroundings. Such a structural factor, which is controlled

by site occupancy, directly governs the various aspects of the luminescence properties.^{5–7} Apparently, a clear understanding of the site occupancy of Ce^{3+} in the host compound is crucial for the development of novel lanthanide ion-doped luminescent materials with f–d transitions. To the best of our knowledge, a systematic analysis of the crystal field splitting (CFS) and centroid of Ce^{3+} 5d energy levels is a good approach for gaining insight into the site occupancies of the doping Ce^{3+} ions experimentally.^{8,9} Furthermore, the firstprinciples calculations of the energies of f–d transitions corroborate the site occupancies, and those on the formation and transition energies of Ce^{3+} ions in different sites give an explanation for the preferential occupancies theoretically.^{10,11}

 $LiSr_4(BO_3)_3$ is an efficient host compound for luminescence of lanthanide ions, which has two Sr^{2+} sites in six- and eight-

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fold coordination, respectively.¹² In this paper, the vacuum ultraviolet–ultraviolet–visible (VUV–UV–vis) spectra of Ce^{3+} -doped $LiSr_4(BO_3)_3$ are first investigated at cryogenic temperatures in detail to understand the bandgap of the host compound, the site occupancy, and the 4f-5d transition energies of Ce³⁺ in this site experimentally. Then the firstprinciples calculations on the f-d transition energies and the formation and transition energies of Ce³⁺ ions in different sites confirm and explain the preferential site occupations theoretically. In addition, the concentration- and temperature-dependent luminescence characteristics are discussed in terms of the luminescence intensity and lifetime, respectively. The possible application of the phosphor for X-ray detection is demonstrated. This work provides a systematic method for understanding the preferential site occupancies through a combination of experiments and theoretical calculations. It is conducive to the design of novel luminescent materials.

2. METHODOLOGY

2.1. Experimental Details. A series of $\text{Li}_{1+x}\text{Sr}_{4-2x}\text{Ce}_x(\text{BO}_3)_3$ (x = 0, 0.001, 0.005, 0.01, or 0.03) samples were prepared by a traditional high-temperature solid-state reaction method using Li_2CO_3 [analytical reagent (A.R.)], SrCO₃ (A.R.), CeO₂ (99.99%), and H₃BO₃ (A.R.) as raw materials. After stoichiometrically weighed, thoroughly mixed, and ground, all reactants were transferred to the crucibles and sintered in a muffle furnace at 850 °C for 8 h in a N₂-H₂ reducing gas ambience. When the product cooled to room temperature (RT) naturally, it was ground for subsequent characterizations.

The phase purity and crystal structure of typical samples were characterized by powder X-ray diffraction (XRD) measurements on a Bruker D8 ADVANCE instrument with Cu K α radiation (λ = 1.5418 Å) at 35 kV and 35 mA. The data were collected over a 2θ range from 10° to 80° with a scanning speed of 10° /min. The high-quality XRD data for structural Rietveld refinements were recorded over a 2θ range from 10° to 100° with an interval of 0.02° , and the refinements were performed by using TOPAS Academic software.¹³ The VUV–UV–vis excitation and emission spectra were recorded on beamline 4B8 of the Beijing Synchrotron Radiation Facility (BSRF) under normal operating conditions by using the spectrum of sodium salicylate (o-C₆H₄OHCOONa) as a reference. The UV-vis emission and excitation spectra as well as the luminescence decay curves were recorded on an Edinburgh FLS1000 spectrometer. A 450 W Xe lamp was used as the excitation source for steady-state spectra, and a lightemitting diode laser with a pulse width of 736.7 ps and a pulse repetition rate of 2000 kHz was used for luminescence decay measurements. A model PET 980 detector was used to accept the signal. The temperature-variable spectroscopy test was carried out using an Oxford model Optistat DN cryostat and controlled by a Mercury model iTC temperature controller. The X-ray excitation luminescence (XEL) measurement was carried out on a Philips PW2253/20 X-ray tube at Delft University of Technology.

2.2. Computational Details. To better understand the origin of the measured excitation and emission spectra, we performed firstprinciples calculations on the formation energies and transition energies of Ce^{3+} at two different Sr^{2+} sites in $LiSr_4(BO_3)_3$. One of the Sr^{2+} ions in the 1 × 1 × 1 supercell containing 272 atoms was replaced with Ce³⁺, and structural optimization was carried out under the framework of density functional theory (DFT) utilizing the Perdew-Burke-Ernzerof exchange-correlation functional.¹⁵ A Hubbard U of 2.5 eV was adopted for the 4f orbitals of the Ce ion. To improve the description of bandgaps and Ce³⁺-related energy levels, a modified PBE0 with 31% Hartree-Fock exchange was determined by the inverse of the calculated value of the optical dielectric constant, $1/\varepsilon_{\infty}$. By applying the constrained occupancy method, we obtained the equilibrium structure of the lowest excited state of $LiSr_4(BO_3)_3$:Ce³⁺ in which one electron on the 4f Kohn-Sham (KS) orbital was excited to the lowest 5d KS orbital. Thermodynamic charge transition level $\epsilon(\mathrm{Ce}^{3\mathrm{+}/4\mathrm{+}})$ is defined as the electron Fermi level to equate the

formation energies of Ce3+ and Ce4+ dopants calculated at their corresponding equilibrium supercells. Relative to the valence band maximum (VBM), $\epsilon(Ce^{3+/4+}) = E_{tot}(Ce^{3+}) - E_{tot}(Ce^{4+}) - \epsilon_{VBM}$ where $E_{\rm tot}$ is the total energy of the relaxed structure of the $\text{LiSr}_4(\text{BO}_3)_3$ supercell containing Ce^{3+} or Ce^{4+} and ϵ_{VBM} is the position of the valence band maximum obtained by employing modified PBE0 with a Hatree–Fock mixing parameter α of 0.31. The 4f-5d excitation energies were obtained from the differences in the generalized KS eigenvalues calculated at the equilibrium geometric structure of the Ce³⁺ supercell. More details about the calculation procedures and their justifications can be found in ref 16 and are not elaborated here. The relative formation energies of Ce³⁺ between two sites are calculated with 4f-in-core pseudopotentials, and their relative concentration was estimated by the term $\omega \exp(-\Delta E_{\rm f}/k_{\rm B}T)$, where ω , $\Delta E_{\rm fr}$ k_B, and T are the ratio of sites to be occupied, the difference in formation energy, the Boltzmann constant, and the temperature of sample preparation, respectively.

3. RESULTS AND DISCUSSION

3.1. X-ray Diffraction (XRD), Structural Refinement, and Crystal Structure. To verify the phase purity and check the crystal structure, the high-quality XRD pattern of the host compound $\text{LiSr}_4(\text{BO}_3)_3$ was collected and the Rietveld refinement was carried out by using the cubic structure as the original model as shown in Figure 1a. The values of R_{wp}



Figure 1. (a) Rietveld refinement result of XRD data of the $\text{LiSr}_4(\text{BO}_3)_3$ compound at RT. The orange-point line represents the fitting curve, the black line the experimental data, and the blue line the difference between the experimental data and fitting curve, and the purple bars are the Bragg positions. The inset shows the schematic coordination surroundings of two Sr^{2+} sites in the host lattice. (b) Concentration-dependent XRD patterns of $\text{Li}_{1+x}\text{Sr}_{4-2x}\text{Ce}_x(\text{BO}_3)_3$ (x = 0, 0.001, 0.005, 0.01, or 0.03). The bottom simulated pattern of $\text{LiSr}_4(\text{BO}_3)_3$ was calculated by the VESTA program based on its Crystallographic Information Framework (CIF) file.¹⁷

(~5.98%), R_p (~3.91%), and R_B (~7.87%) all mean a fine fitting result, implying reliable refined indicators for proving LiSr₄(BO₃)₃ was free of impurities. The refined lattice parameters are as follows: a = b = c = 14.949 Å, V =3340.484 Å³, and Z = 16. The detailed structural parameters are listed in Table 1. The compound LiSr₄(BO₃)₃ crystallizes in a cubic structure with space group *Ia*3*d*, in which Sr²⁺ ions occupy two diverse lattice sites.¹² The schematic coordination surroundings of these two Sr²⁺ ions are shown as insets in the top right corner of Figure 1a. Sr²⁺(1) ions are six-fold coordinated to form distorted octahedral [Sr(1)O₆] at the 16a Wyckoff position with S₆ symmetry, while Sr²⁺(2) ions are eight-fold coordinated in two-capped trigonal prisms

Table 1. Refined Structural Parameters of $LiSr_4(BO_3)_3$ at Room Temperature

atom	Wyckoff position	x	у	z	occupation	B _{eq}
Sr1	16a	0	0	0	1	1.48
Sr2	48f	0	0.25	-0.001	1	0.84
Li	16b	0.125	0.125	0.125	1	1.60
В	96h	0.163	0.352	0.125	1	0.24
01	96h	-0.020	0.272	0.041	1	0.55
02	96h	0.264	0.365	0.125	1	1.89

 $[Sr(2)O_8]$ at the 48f Wyckoff position with C_2 symmetry. The average Sr–O bond distances for $[Sr(1)O_6]$ and $[Sr(2)O_8]$ polyhedra are 2.536 and 2.630 Å, respectively. The nearest $Sr^{2+}(1)-Sr^{2+}(1)$, $Sr^{2+}(2)-Sr^{2+}(2)$, and $Sr^{2+}(1)-Sr^{2+}(2)$ distances are approximately 6.474, 3.665, and 3.738 Å, respectively.

The XRD patterns of Ce³⁺-doped Li_{1+x}Sr_{4-2x}Ce_x(BO₃)₃ (x = 0, 0.001, 0.005, 0.01, or 0.03) samples were further measured as presented in Figure 1b. Since the standard XRD card of $LiSr_4(BO_3)_3$ was not found in the powder diffraction files (PDF) database, the simulated pattern of $LiSr_4(BO_3)_3$ at the bottom of the graph was obtained using VESTA program according to its CIF file.¹⁷ For the samples with different doping contents, their XRD patterns are identical to the simulated one and all diffraction peaks can be indexed to the simulated pattern, indicating that these Ce3+-doped samples are without impurities; this can be further confirmed by the luminescence spectra in section 3.2. In addition, the observations imply that the doping Ce³⁺ ions do not clearly affect the crystal structure of the $LiSr_4(BO_3)_3$ host. Considering the similar ionic radii of Ce³⁺ and Sr²⁺ [for a coordination number (CN) of 6, $r(Ce^{3+}) = 1.01$ Å and $r(Sr^{2+})$ = 1.18 Å; for a CN of 8, $r(Ce^{3+}) = 1.14$ Å and $r(Sr^{2+}) = 1.26$ Å],¹⁸ Ce³⁺ ions are assumed to enter Sr²⁺ sites. In sections 3.2-3.3, we will discuss the site occupancy through experimental luminescence spectra and theoretical calculations in detail.

3.2. Excitation and Emission Wavelength Dependencies of the Luminescence of Li_{1.001}Sr_{3.998}Ce_{0.001}(BO₃)₃. Figure 2a displays the highest height-normalized excitation $(\lambda_{\rm em}$ = 390, 400, 418, 420, 450, 470, and 485 nm) and emission (λ_{ex} = 268, 286, and 332 nm) spectra of the $Li_{1.001}Sr_{3.998}Ce_{0.001}(BO_3)_3$ sample at RT for comparison. Herein, wavelengths of 268, 286, and 332 nm are close to the peaks of three bands in the excitation spectra, and wavelengths of 390, 400, 418, 420, 450, 470, and 485 nm are near 35%, 65%, 100%, 100%, 80%, 55%, and 30% of the emission peak, respectively. Under varied wavelength excitation, three emission curves almost overlap with one another. Meanwhile, seven normalized excitation spectra also nearly overlap by monitoring the selected emission wavelengths. The observations suggest that the sample does not contain any impurity that affects the luminescence in this spectral range, and Ce³⁺ ions occupy only one kind of site in this sample.

Upon 320 nm excitation, the luminescence decay curves of $Li_{1.001}Sr_{3.998}Ce_{0.001}(BO_3)_3$ of different wavelength emission are shown in Figure 2b. All curves overlap, and the luminescence lifetime of $Li_{1.001}Sr_{3.998}Ce_{0.001}(BO_3)_3$ is exponentially fitted to be approximately ~41.3 ns at 78 K. The observation further illustrates the existence of only a single kind of Ce^{3+} luminescence center in the host compound, and the



Figure 2. (a) Highest height-normalized excitation ($\lambda_{em} = 390, 400, 418, 420, 450, 470, and 485 nm$) and emission ($\lambda_{ex} = 268, 286, and 332 nm$) spectra of the Li_{1.001}Sr_{3.998}Ce_{0.001}(BO₃)₃ sample at room temperature. (b) Luminescence decay curves ($\lambda_{ex} = 320$ nm, and $\lambda_{em} = 402, 420, 450, and 473$ nm) of the Li_{1.001}Sr_{3.998}Ce_{0.001}(BO₃)₃ sample at 78 K.

Time (ns)

inhomogeneous broadening effect is not pronounced in this diluted $Li_{1.001}Sr_{3.998}Ce_{0.001}(BO_3)_3$ sample.¹⁹

3.3. VUV - UV - vis Luminescence of Li_{1.001}Sr_{3.998}Ce_{0.001}(BO₃)₃ at Cryogenic Temperatures and Site Occupancy of Ce³⁺. To clarify the site occupancy and the 5d energies of Ce³⁺ in this host compound, the VUV-UV-vis luminescence spectra of Li_{1.001}Sr_{3.998}Ce_{0.001}(BO₃)₃ are recorded at cryogenic temperatures. The purple line in Figure 3a presents the UV excitation ($\lambda_{em} = 420$ nm) spectrum of this



Figure 3. (a) Lab UV excitation ($\lambda_{em} = 420$ nm) and UV-vis emission ($\lambda_{ex} = 332$ nm) spectra of Li_{1.001}Sr_{3.998}Ce_{0.001}(BO₃)₃ at 78 K. (b) Synchrotron radiation VUV-UV excitation spectrum ($\lambda_{em} = 420$ nm) of Li_{1.001}Sr_{3.998}Ce_{0.001}(BO₃)₃ at 11 K. (c and d) Calculated 4f-5d_j (j = 1-5) transition energies of Ce³⁺ ions in two Sr²⁺ sites of LiSr₄(BO₃)₃.

sample using an Edinburgh FLS1000 spectrometer at 78 K. Three distinct broad bands are seen with maxima at ~30.2 \times 10³ cm⁻¹ (331 nm, 3.74 eV), ~35.0 \times 10³ cm⁻¹ (286 nm, 4.33 eV), and ~37.4 \times 10³ cm⁻¹ (267 nm, 4.64 eV). The lowest 4f– 5d excitation band of Ce³⁺ in LiSr₄(BO₃)₃ has been reported around the range of 340–356 nm, which are largely in agreement with the value observed in Figure 3a.^{20–22} The

deviation may be the result of different measurement instruments, temperatures, etc.

The black line in Figure 3a shows the emission spectrum of Li_{1.001}Sr_{3.998}Ce_{0.001}(BO₃)₃ upon 332 nm excitation at 78 K. The band position is consistent with that in Figure 2a, but the spectral resolution is better due to the low-temperature condition. It consists of a main band and a shoulder band at the shorter wavenumber side. The spectrum can be well-fitted with a sum of two Gaussian functions. Accordingly, two band peaks are estimated at $\sim 22.2 \times 10^3$ cm⁻¹ (peak A, 450 nm, 2.75 eV) and \sim 24.1 × 10³ cm⁻¹ (peak B, 415 nm, 2.99 eV). Their energy separation (~ 1.90×10^3 cm⁻¹, 0.24 eV) corresponds to typical values of $^2F_{5/2}$ and $^2F_{7/2}$ spin–orbit split 4f ground states of Ce³⁺. From the energy difference between the band maxima of the ${}^{2}F_{5/2}$ -5d₁ transition in excitation (3.74 eV) and emission (2.99 eV) spectra, the Stokes shift of Ce^{3+} in $LiSr_4(BO_3)_3$ is evaluated to be 0.75 eV, indicating that the 5d electrons of Ce^{3+} in $LiSr_4(BO_3)_3$ experience a strong effect of electron-phonon interaction with the coordination environment.³

Figure 3b exhibits the synchrotron radiation VUV-UV excitation ($\lambda_{em} = 420$ nm) spectrum of $\rm Li_{1.001}Sr_{3.998}Ce_{0.001}(BO_3)_3$ recorded on beamline 4B8 of the Beijing Synchrotron Radiation Facility (BSRF) at 11 K. The whole excitation profile includes the host-related absorption with an energy above $\sim 52.2 \times 10^3$ cm⁻¹ and the 4f-5d transitions of Ce3+ ions below this wavenumber. First, the bandgap of host compound $LiSr_4(BO_3)_3$ is evaluated according to the spectrum in Figure 3b. The host exciton creation energy (E^{ex}) is found to be ~56.8 × 10³ cm⁻¹ (~7.04 eV, 176 nm). This assignment can be further confirmed by the synchrotron radiation VUV-UV excitation spectrum of the Li_{1.001}Sr_{3.998}Gd_{0.001}(BO₃)₃ sample in Figure S1, in which an evident excitonic absorption band with a maximum at ~175 nm can be observed when the 312 nm emission of the Gd³⁺ ${}^{6}\mathrm{P}_{7/2}$ \rightarrow ${}^{8}\mathrm{S}_{7/2}$ transition is monitored. In addition, a conspicuous host-related band has been observed near ${\sim}7$ eV of isomorphic compound NaSr₄(BO₃)₃.²³ Considering the electron transfer from the upper valence band to the conduction band bottom, the optical bandgap value of the host compound should add the electron-hole binding energy of an exciton to the host exciton creation absorption energy $(E^{\rm ex})$. The binding energy can be estimated to be 0.008 \times $(E^{ex})^{2}$ ²⁴ In our case, upon addition of the electron-hole binding energy to the exciton creation energy, the bandgap energy of the $LiSr_4(BO_3)_3$ compound between the upper valence band and conduction band bottom is calculated to be ~7.44 eV.

Then, we discuss the 4f–5d excitation bands of Ce³⁺ ions in Figure 3b. As mentioned in section 3.2, Ce³⁺ ions enter only one type of Sr²⁺ site in LiSr₄(BO₃)₃. Hence, at most five 4f–5d transition bands might occur in the excitation spectrum. This is exactly what we find in the range of 28.6×10^3 to 52.2×10^3 cm⁻¹ of the spectrum at 11 K, which contains a strong band (I), two medium bands (II and III), and two very weak overlapping bands. The positions and profiles of three obvious low-energy bands (I–III) are consistent with those in Figure 3a. To better evaluate these excitation peaks, a sum of five Gaussian functions is adopted to fit the curve at this range. The peak maxima of these bands are estimated to be ~30.2 × 10³ cm⁻¹ (band II, 3.74 eV, 331 nm), ~34.9 × 10³ cm⁻¹ (band II, 4.64 eV, 267 nm), ~45.2 × 10³ cm⁻¹ (band IV, 5.61 eV, 221 nm), and

~48.5 × 10³ cm⁻¹ (band V, 6.01 eV, 206 nm), which are attributed to the Ce³⁺ transitions from the 4f ground state to the first to fifth 5d (5d₁₋₅) excitation states, respectively. The different intensity distributions of five excitation bands may relate to the energy separation between the conduction band minimum (CBM) and the 5d₁₋₅ multiplets as shown in Figure 7 (vide infra). 5d₁ is fairly below the CBM in energy, so the 4f–5d₁ excitation band is strong; the 5d_{2,3} energy levels are close to the CBM. Hence, the 4f–5d_{2,3} excitation bands are with medium intensities, but the 5d_{4,5} levels are evidently higher than the CBM; therefore, the 4f–5d_{4,5} excitation bands are very weak due to autoionization processes.³

Herein, the centroid energy of Ce3+ ion 5d states in $LiSr_4(BO_3)_3$ is estimated to be ~4.87 eV by calculating the arithmetic average energy of five 4f-5d excitation bands, which is larger than that of borate LiCaBO₃ [4.46 eV, C_1 point symmetry (CaO₇) polyhedron with a mean bond length of 2.428 Å], close to that of LaBO₃ [4.92 eV, C_s point symmetry (LaO_9) polyhedron with an average bond distance of 2.602 Å], but smaller than those of $NaSr_4(BO_3)_3$ [5.15 eV, C_2 point symmetry (SrO_8) polyhedron with a mean bond length of 2.687 Å] and Li_{6} Y(BO₃)₃ [5.01 eV, C_1 point symmetry (YO₈) polyhedron with an average bond distance of 2.376 Å].^{8,23,25,26} The centroid energy is related to the nephelauxetic effect, the covalency between O^{2-} anions and Ce^{3+} cations, and/or the spectroscopic polarizability of O^{2-} anions in the first coordination sphere of Ce^{3+} cations. The comparisons presented above indicate that Ce³⁺ ions possess a moderate spectroscopic polarizability, covalency, and nephelauxetic effect in host compound $\text{LiSr}_4(\text{BO}_3)_3$.

In terms of the energy difference between the first 5d (5d₁) and the fifth 5d (5d₅) states in Ce³⁺ ions, the crystal field splitting energy (E_{cfs}) is calculated to be ~2.27 eV (18.3 × 10³ cm⁻¹), which is affected by the shape and size of the first anion coordination polyhedron around Ce³⁺ cations. Generally, the smaller coordination number and the shorter bond length will lead to a larger E_{cfs} . For the Ce³⁺ occupying six-coordinated sites in some host compounds, the E_{cfs} values are in the range of 18.6 × 10³ to 23.3 × 10³ cm⁻¹ with an arithmetic average value of 20.1 × 10³ cm⁻¹, whereas for Ce³⁺ ions at eight-fold sites in some host compounds, the E_{cfs} values have been reported to be in the range from 16.2 × 10³ to 19.6 × 10³ cm⁻¹ with a mean value of ~17.8 × 10³ cm⁻¹.^{8,27} The latter average value is closer to that in our case (18.1 × 10³ cm⁻¹), which implies that the spectral data we obtained above may relate to the Ce³⁺ ions in eight-fold coordinated C_2 symmetry Sr²⁺ sites in LiSr₄(BO₃)₃.

The viewpoint described above can be further verified by the theoretical simulations of $4f-5d_j$ (j = 1-5) transitions of Ce^{3+} ions. Panels c and d of Figure 3 show the calculated $4f-5d_j$ (j = 1-5) transition energies of Ce^{3+} ions in Sr^{2+} sites when the CN of Sr^{2+} is eight and that of $LiSr_4(BO_3)_3$ is six. The calculated and experimental results are also listed in Table 2 for comparison. It is obvious that the experimental excitation spectrum can be attributed to the 4f-5d transitions of Ce^{3+} ions in eight-coordinated Sr^{2+} sites, indicating that the Ce^{3+} ions preferentially occupy eight-coordinated rather than six-coordinated Sr^{2+} sites.

The calculation of the relative formation energy can provide an explanation for the preferential occupancy of Ce^{3+} in two Sr^{2+} sites. The formation energy of Ce^{3+} ions at $[Sr(1)O_6]$ sites is higher than that at $[Sr(2)O_8]$ sites by 0.51 eV, from which it is estimated that the concentration of the latter is higher than

Table 2. Calculated and Experimental $4f-5d_j$ (j = 1-5)Transition Energies of Ce³⁺ Ions

5d multiplet	six-coordinated	eight-coordinated	experimental (eV)
5d ₁	3.57	3.84	3.74
5d ₂	3.57	4.42	4.33
5d ₃	3.87	4.62	4.64
5d ₄	6.03	5.52	5.61
5d ₅	6.03	5.96	6.01

the former by >2 orders of magnitude, in agreement with the assignment determined from the excitation spectrum in Figure 3.

3.4. Concentration-Dependent Luminescence of LiSr₄(BO₃)₃:Ce³⁺. The highest height-normalized excitation spectra of Li_{1+x}Sr_{4-2x}Ce_x(BO₃)₃ (x = 0.001, 0.005, 0.01, or 0.03) samples are shown in the left-hand inset of Figure 4. It



Figure 4. Highest height-normalized emission ($\lambda_{ex} = 340 \text{ nm}$) and excitation ($\lambda_{em} = 420 \text{ nm}$) spectra of $\text{Li}_{1+x}\text{Sr}_{4-2x}\text{Ce}_x(\text{BO}_3)_3$ (x = 0.001, 0.005, 0.01, or 0.03) at RT. The insets show the integrated intensity of emission spectra and the fluorescence decay curves ($\lambda_{ex} = 320 \text{ nm}$, and $\lambda_{em} = 420 \text{ nm}$) of $\text{Li}_{1+x}\text{Sr}_{4-2x}\text{Ce}_x(\text{BO}_3)_3$.

can be found that the peak positions of the $4f-5d_j$ (j = 2 or 3) excitation bands remain stable for samples with different doping concentrations, but that of the lowest 4f-5d excitation band gradually shifts to the long wavelength side. We assume that this phenomenon is mainly related to the slight increase in the 5d crystal field splitting (CFS) of Ce³⁺ ions, as the smaller radius of Ce³⁺ compared to that of Sr²⁺ results in the contraction of the local coordination environment around Ce³⁺ with increasing doping contents. The right-hand inset of Figure 4 displays the emission spectra of Li_{1+x}Sr_{4-2x}Ce_x(BO₃)₃ (x = 0.001, 0.005, 0.01, or 0.03) samples under 340 nm excitation. One can see that all spectral profiles are almost identical, but they slightly move in the long wavelength direction with an increase in Ce³⁺ content, as a consequence of the larger CFS of the Ce³⁺ 5d state at a higher doping level.

The inset in the top left corner of Figure 4 presents the integrated emission intensity in the range of 350-560 nm as a function of doping concentration, showing that the intensity increases first, reaches maximum at x = 0.005, and then decreases with an increase in concentration. Furthermore, the luminescence decay curves of $\text{Li}_{1+x}\text{Sr}_{4-2x}\text{Ce}_x(\text{BO}_3)_3$ (x = 0.001, 0.005, 0.01, or 0.03) all overlap as presented at the top right

corner of Figure 4, and they can be well fitted with an exponential function with a lifetime of \sim 37.9 ns. This value measured at RT is slightly smaller than that (\sim 41.3 ns) collected at a low temperature of 78 K in Figure 2, due to thermal quenching as discussed in detail in Figure 6 (vide infra). Although the intensity-dependent luminescence and decay-dependent luminescence are somewhat inconsistent, the decay curves may provide better evidence because many experimental factors influence the spectral measurement results.²⁸ In other words, no concentration quenching occurs in the investigated doping contents.

Figure 2 has illustrated that the inhomogeneous broadening effect is not pronounced in the diluted $Li_{1.001}Sr_{3.998}Ce_{0.001}(BO_3)_3$ sample as mentioned in section 3.2. Further assessing the inhomogeneous broadening in a concentrated sample to gain insight into the influence of doping content on the inhomogeneous broadening effect is worthwhile. Therefore, the excitation and emission spectra as well as the luminescence decay curves of $Li_{1.03}Sr_{3.94}Ce_{0.03}(BO_3)_3$, which has a Ce^{3+} doping concentration 30 times higher than that of $Li_{1.001}Sr_{3.998}Ce_{0.001}(BO_3)_3$, are shown in Figure 5. One can observe that the highest height-



Figure 5. (a) Emission (λ_{ex} = 311 and 358 nm) and excitation spectra (λ_{em} = 418 and 450 nm) of Li_{1.03}Sr_{3.94}Ce_{0.03}(BO₃)₃ at RT. (b) Luminescence decay curves (λ_{ex} = 320 nm, and λ_{em} = 402, 450, and 500 nm) of Li_{1.03}Sr_{3.94}Ce_{0.03}(BO₃)₃ at RT.

normalized first f–d excitation band $(4f-5d_1)$ is almost invariable when different emission wavelengths of 418 and 450 nm are monitored, but the emission band shifts slightly in the long wavelength direction as the excitation wavelength moves from the left side (311 nm) to the right side (358 nm) across the first f–d excitation peak (Figure 5a). One of the possible reasons for the observations may be that the inhomogeneous broadening effect is somewhat enhanced in this concentrated Li_{1.03}Sr_{3.94}Ce_{0.03}(BO₃)₃ sample in comparison to that in the diluted Li_{1.001}Sr_{3.998}Ce_{0.001}(BO₃)₃ sample.^{29,30}

The existence of inhomogeneous broadening in this concentrated sample can be further corroborated by the fluorescence decay curves under 320 nm excitation and different wavelength emission. When the monitored emission wavelength shifts from 500 nm to 450 and 402 nm, the decay of Ce^{3+} luminescence accelerates gradually and the lifetime is shorter steadily as shown in Figure 5b. The shorter the monitored emission wavelength, the faster the luminescence decay and the shorter the luminescence lifetime. There are

some unevenly distributed disturbed Ce^{3+} sites in the highly doping samples, and the 4f–5d transition energies of these ions are slightly different, individually. The successive site-to-site energy transfer provides a channel for changing the luminescence lifetime; therefore, the decay time changes with detection wavelength across the emission band, and the luminescence decay curve deviates from the exponential form more or less.^{31–33}

3.5. Luminescence of $Li_{1.001}Sr_{3.998}Ce_{0.001}(BO_3)_3$ at Different Temperatures. Upon 335 nm excitation, the temperature-dependent emission spectra of the $Li_{1.001}Sr_{3.998}Ce_{0.001}(BO_3)_3$ sample are measured in the range of 100–500 K as shown in Figure 6a. With an increase in



Figure 6. (a) Normalized emission spectra ($\lambda_{ex} = 335 \text{ nm}$) and (b) luminescence decay curves ($\lambda_{ex} = 320 \text{ nm}$, and $\lambda_{em} = 420 \text{ nm}$) of $\text{Li}_{1.001}\text{Sr}_{3.998}\text{Ce}_{0.001}(\text{BO}_3)_3$ at 100–500 K. The insets show the integrated intensity or lifetime as a function of temperature and their fitting results using eqs 1 and 2, respectively.

temperature, the typical double emission peaks of Ce^{3+} ions gradually merged into a single peak gradually like normal cases. The inset shows that the integrated emission intensity remains almost stable below 300 K and then decreases with an increase in temperature, indicating that the thermal quenching of Ce^{3+} luminescence occurs in $LiSr_4(BO_3)_3$. The thermal quenching can be also confirmed by the temperature-dependent luminescence decay curves of the $Li_{1.001}Sr_{3.998}Ce_{0.001}(BO_3)_3$ sample. As shown in Figure 6b, three fluorescence decay curves almost overlap with each other in the temperature range of 100–300 K. Then, the decay begins to accelerate above 300 K.

According to the temperature-dependent intensity or lifetime in the insets of Figure 6, the thermal quenching activation energy of Ce^{3+} f-d emission in $LiSr_4(BO_3)_3$ can be evaluated by the single-barrier quenching model derived in eqs 1 and 2.

$$I(T) = \frac{I_0}{1 + \left(\frac{\Gamma_0}{\Gamma_\nu}\right) \exp[-E_{(a,I)}/kT]}$$
(1)

$$\tau(T) = \frac{\frac{1}{\Gamma_{\nu}}}{1 + \frac{\Gamma_{0}}{\Gamma_{\nu}} \exp[-E_{(a,\tau)}/kT]}$$
(2)

where I(T) and $\tau(T)$ are the integrated emission intensity and lifetime at temperature *T*, respectively, Γ_0 and Γ_v are the thermal quenching rate at $T = \infty$ (attempt rate) and the radiative Ce³⁺ 5d \rightarrow 4f transition rate, respectively, $E_{(a,I)}$ and $E_{(a,\tau)}$ represent the activation energies for thermal quenching of Ce³⁺ luminescence deduced by intensity and lifetime, respectively, and k is the Boltzmann constant (8.62 $\times 10^{-5}$ eV K⁻¹). Therefore, the values of $E_{(a,I)}$ and $E_{(a,\tau)}$ are simulated to be ~0.19 and ~0.27 eV, respectively, for this diluted Li_{1.001}Sr_{3.998}Ce_{0.001}(BO₃)₃ sample.

The luminescence of 4f-5d transitions of Ce³⁺ and/or Eu²⁺ ions may be thermally quenched by different nonradiative channels.^{28,34-37} Three mechanisms were proposed to explain the thermal quenching characteristics of Ce³⁺-doped phosphors.

Initially, the nonradiation $5d \rightarrow 4f$ crossover relaxation via electron-phonon coupling is thought to be responsible for the thermal quenching of Ce³⁺ luminescence. In terms of this viewpoint, the activation energy of thermal quenching corresponds to the energy barrier ($E_{\rm fd}$) between the lowest point of the excited-state 5d parabola and the intersection point of 4f and 5d parabolas in the configurational coordinate diagram. Accordingly, the energy barrier ($E_{\rm fd}$) in this case is estimated according to eq 3.³⁵

$$E_{\rm fd} = \frac{E_{\rm em}^2}{4E_{\rm FC}} \tag{3}$$

where $E_{\rm em}$ is the emission energy [2.99 eV (415 nm)] in our case and $E_{\rm FC}$ is the Franck–Condon shift (0.38 eV), which is approximately equal to half of the Stokes shift (~0.75 eV).³⁸ Therefore, the value of $E_{\rm fd}$ is 5.88 eV in the ${\rm Li}_{1.001}{\rm Sr}_{3.998}{\rm Ce}_{0.001}({\rm BO}_3)_3$ sample. Apparently, the crossing energy barrier is so large that the 5d \rightarrow 4f crossover mechanism is unlikely to cause the thermal quenching of ${\rm Ce}^{3+}$ emission in the ${\rm LiSr}_4({\rm BO}_3)_3$ host compound.

Latterly, the thermal ionization of the 5d electrons of Ce³⁺ ions into the conduction band of the host compound has been considered to be the channel resulting in the thermal quenching of Ce³⁺. In this scenario, the activation energy of thermal quenching should be close to the energy barrier (E_{dc}) between the lowest 5d energy level of Ce³⁺ and the conduction band minimum of the host compound. To derive this energy barrier (E_{dc}) in the LiSr₄(BO₃)₃ host compound, the vacuum referred binding energy (VRBE) scheme is constructed as depicted in Figure 7.3 The adopted experimental data for the construction include the bandgap energy (\sim 7.44 eV) of $LiSr_4(BO_3)_3$, the energies (3.74, 4.33, 4.64, 5.61, and 6.01 eV) of the Ce³⁺ 4f-5d transitions, and the exchange splitting energy (0.84 eV) of Tb^{3+} electron transitions between the low spin and high spin in the $LiSr_4(BO_3)_3$ host as displayed in Figure S2. The additional empirical datum involves a Coulomb interaction U_c value of 6.89 eV, which corresponds to the energy difference between the 4f ground states of Eu²⁺ and Eu³⁺ ions and calculated from the chemical shift model.³ The VRBE scheme reveals the $E_{\rm dc}$ value of Ce³⁺ is 0.29 eV, which is near the experimental fitting values (~0.19 and 0.27 eV, with a mean value of $0.23 \pm 0.04 \text{ eV}$) from the temperaturedependent intensity or lifetime in the insets of Figure 7. Several factors such as the relaxation of the 4f-5d transition, the construction of the VRBE scheme, the fitting of the thermal quenching activation energy, etc., would impose influences on this difference. Regardless, the values are enough to explain the thermal quenching mechanism we developed here. Hence, we assume that the electron thermal-ionization process provides an important channel for Ce³⁺ thermal quenching in



Figure 7. Vacuum referred binding energy (VRBE) scheme of trivalent lanthanide ions in $\text{LiSr}_4(\text{BO}_3)_3$. The top and bottom black solid lines are the conduction band minimum (CBM) and the valence band maximum (VBM), respectively. The distance between the purple line and the top black solid line corresponds to the electron–hole binding energy. The green triangles and orange circles represent the lowest Sd states and 4f ground states of Ln^{3+} , respectively.

Li_{1.001}Sr_{3.998}Ce_{0.001}(BO₃)₃. In addition, the thermally activated concentration quenching may also contribute to the thermal quenching. In this process, nonradiative energy migration happens among doping luminescence centers and finally to killer centers like oxygen vacancies or holes in materials^{28,35,37} with an increase in temperature, closely related to the resonance energy transfer process.³⁹ With an increase in doping concentration, the spectral overlap between the excitation band and emission band usually increases. Consequently, the energy transfer probability between doping ions and that to the quenching centers increases, which eventually results in a decrease in the thermal quenching temperature and the thermal quenching activation energy.

To assess the influence of this factor on the thermal quenching, the temperature-dependent emission spectra and luminescence decay curves of a concentrated $\text{Li}_{1.03}\text{Sr}_{3.94}\text{Ce}_{0.03}(\text{BO}_3)_3$ sample are measured at 100–500 K as shown in Figure S3. The fitted values of $E_{(a,I)}$ and $E_{(a,r)}$ are ~0.15 and ~0.18 eV, respectively. The values are slightly smaller than the corresponding values of the diluted $\text{Li}_{1.001}\text{Sr}_{3.998}\text{Ce}_{0.001}(\text{BO}_3)_3$ sample. It seems that the thermally activated concentration quenching partially contributes to the thermal quenching of the luminescence of Ce^{3+} in $\text{LiSr}_4(\text{BO}_3)_3$.

3.6. X-ray Excited Luminescence of $Li_{1.01}Sr_{3.98}Ce_{0.01}(BO_3)_3$. The X-ray excitation luminescence (XEL) measurement of the $Li_{1.01}Sr_{3.98}Ce_{0.01}(BO_3)_3$ sample is performed to evaluate the potential detecting application. The XEL spectra of the $Li_{1.01}Sr_{3.98}Ce_{0.01}(BO_3)_3$ compound and BaF₂ reference single crystal at RT are shown in Figure 8. The emission spectrum of the $Li_{1.01}Sr_{3.98}Ce_{0.01}(BO_3)_3$ sample exhibits a broad band in the range of 350–550 nm, which is consistent with that under UV light excitation. The emission curve of a BaF₂ reference single crystal is in agreement with that in ref 14. Upon calculation of the ratio of the integrated intensity of two samples, the photon yield of the $Li_{1.01}Sr_{3.98}Ce_{0.01}(BO_3)_3$ sample is estimated to be ~12.0 ×



Figure 8. X-ray excited luminescence (XEL) spectra of the BaF_2 crystal and the $Li_{1.01}Sr_{3.98}Ce_{0.01}(BO_3)_3$ sample at RT.

 10^3 photons/MeV using the photon yield of 8800 photons/ MeV of the BaF₂ reference crystal. This value is also higher than that of commercial Bi₄Ge₃O₁₂ powder (8200 photons/ MeV).⁴⁰ The Li_{1.01}Sr_{3.98}Ce_{0.01}(BO₃)₃ powder is worth further optimization as a potential X-ray detecting material.

4. CONCLUSIONS

In this paper, the site occupancy, VUV-UV-vis photoluminescence, and X-ray radio-luminescence of Ce³⁺ ions doped in $LiSr_4(BO_3)_3$ are systematically studied, after the sample preparation by a traditional high-temperature solidstate reaction approach and the phase purity and structure characterization by the high-resolution XRD Rietveld refinement. First, the bandgap energy of the host compound is estimated to be \sim 7.44 eV according to the synchrotron radiation VUV-UV excitation spectra of Ce3+- and Gd3+doped $\text{LiSr}_4(\text{BO}_3)_3$. In addition, the excitation bands of Ce^{3+} ions in LiSr₄(BO₃)₃ are observed around 331, 286, 267, 221, and 206 nm and attributed to the transitions to the five 5d crystal field states of Ce3+ ions located at the eight-fold coordinated Sr^{2+} sites with C_2 symmetry, not those six-fold coordinated sites. Second, the preferential occupancy of Ce³⁺ ions is further confirmed by the calculated $4f-5d_i$ (i = 1-5)transition energies of Ce³⁺ ions located at both of two sites in the first-principles framework, as there is good agreement between the experimental results and the calculated ones for the eight-fold coordinated case $(31.0 \times 10^3, 35.7 \times 10^3, 37.3 \times 10$ 10^3 , 44.5×10^3 , and 48.1×10^3 cm⁻¹), and a large mismatch with the six-fold coordinated case $(28.8 \times 10^3, 28.8 \times 10^3, 31.2)$ \times 10³, 48.6 \times 10³, and 48.6 \times 10³ cm⁻¹). Moreover, the preferential occupancy can be explained by the calculated relative defect formation energies (0.51 and 0.00 eV) of Ce^{3+} located at $[Sr(1)O_6]$ and $[Sr(2)O_8]$ sites, respectively. Third, the doping concentration-dependent luminescence and temperature-dependent luminescence are investigated by the luminescence spectra and decay curves, respectively. There is no concentration quenching for the studied doping concentration range, but the inhomogeneous broadening effect is observed. Upon systematic analysis of the thermal quenching activation energies fitted from the experimental spectroscopic data using three kinds of thermal quenching mechanism models, the thermal-ionization mechanism from the 5d states to the host's conduction band bottom is thought to be predominately responsible for the observed thermal quenching

effect, although the potential contribution of the thermally activated concentration quenching is not completely ignored. Finally, the photon yield of ${\sim}12.0 \times 10^3$ photons/MeV of the Li_{1.01}Sr_{3.98}Ce_{0.01}(BO_3)_3 sample estimated from XEL measurement demonstrates its potential applications in X-ray detection.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.inorgchem.2c01016.

VUV–UV excitation and emission spectra of $Li_{1.001}Sr_{3.998}Gd_{0.001}(BO_3)_3$, VUV excitation spectrum of $Li_{1.001}Sr_{3.998}Tb_{0.001}(BO_3)_3$ at 11 K, normalized emission spectra and luminescence decay curves of a concentrated $Li_{1.03}Sr_{3.94}Ce_{0.03}(BO_3)_3$ sample at 100–500 K, and fitting results of the integrated intensity and lifetime as a function of temperature (PDF)

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Notes

The authors declare no competing financial interest.

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