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# Multi-twist polarization ribbon topologies in highly-confined optical fields 

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#### Abstract

Electromagnetic plane waves, solutions to Maxwell's equations, are said to be 'transverse' in vacuum. Namely, the waves' oscillatory electric and magnetic fields are confined within a plane transverse to the waves' propagation direction. Under tight-focusing conditions however, the field can exhibit longitudinal electric or magnetic components, transverse spin angular momentum, or non-trivial topologies such as Möbius strips. Here, we show that when a suitably spatially structured beam is tightly focused, a three-dimensional polarization topology in the form of a ribbon with two full twists appears in the focal volume. We study experimentally the stability and dynamics of the observed polarization ribbon by exploring its topological structure for various radii upon focusing and for different propagation planes.


## 1. Introduction

Since the inception of electromagnetic theory, the polarization of light, i.e. the oscillation direction of the electric field vector, has been a central concept to our understanding of optics, giving rise to countless applications [1]. For plane waves and in paraxial beams, the polarization has been recognized as a transverse quantity and, hence, it can be represented by a set of two orthogonal basis vectors. For instance, in the linear and circular bases, the polarization of an optical beam can be represented by superpositions of linearly horizontally and linearly vertically, or circularly-left and circularly-right polarized beams, respectively. The ratio and the relative phase between the two polarization components define the oscillations of the electric field vector's tip upon propagation or in time, and its trajectory in the plane transverse to its propagation direction, typically given by an ellipse [1]. This description of the light field by a so-called polarization ellipse at each point in space is even valid in highly confined fields exhibiting out-of-plane field components, as long as the field itself is monochromatic. In two different cases, this ellipse becomes singular [2-4]: (i) the ellipse's major and minor axes are undefined, resulting in circular polarization (C-point); (ii) the minor axis of the ellipse is zero and its surface normal is undefined, and thus the polarization is linear (L-line). These so-called polarization singularities in general arise in light fields with spatially inhomogeneous polarization distributions, which we refer to as spacevarying polarized light beams. They have recently received great attention owing to their peculiar optical features and applications [5-7]. Vector vortex beams [5]-space-varying linearly-polarized beams-and Poincaré beams [8]-optical beams containing all types of polarization-are among this class of spatially inhomogeneously


Figure 1. Creation of a full Poincaré beam and subsequent optical polarization ribbon with twist index -2 under tight focusing. (a) A left-handed circularly polarized Gaussian beam is converted into a full Poincaré beam by means of a space-variant birefringent plate ( $q$-plate) with topological charge $q=-1$ (see sketch for the orientation of its fast axes) and optical retardation of $\delta=2.92$ rad. The resulting polarization ellipse at each point in the transverse plane of the beam is superimposed in white. (b) Twisted ribbon with 2 twists and its projection onto the transverse plane, created by tight focusing of the beam shown in (a) and tracing the major axis $\alpha$ of the polarization ellipse (see inset for a sketch with the definition of its parameters) on a circle with $\rho=150 \mathrm{~nm}$ around the optical axis.
polarized beams. These beams are interesting both at the fundamental and applied levels. For instance, they can be used to enhance measurement sensitivity [ 9,10 ], to transport high-power in nonlinear media [11], or to generate exotic optical beams with peculiar topological structures [12, 13]. In particular, spatially structured light fields with field components along the propagation direction were predicted by Freund to show so-called optical polarization Möbius strips and twisted ribbons [14, 15], with the former recently confirmed experimentally in tightly focused fields [16] as well as in the originally proposed scheme of crossing beams [17], and numerically in the scattering from dielectric spheres [18]. Here, we will experimentally demonstrate the generation and stability of the latter in highly confined fields, specifically looking at the dynamics of the twisted ribbon when propagating through the focal volume of a tailored space-varying polarized light beam.

## 2. Space-varying polarized beams under tight focusing

There are several different methods to generate optical beams possessing inhomogeneous polarization distributions in their transverse plane. For instance, phase-only spatial light modulators [19-21], non-unitary polarization transformation [22], and spatially structured birefringent plates [8,23] have so far been used to generate Poincaré or vector vortex beams. In this article, we use the latter technique to generate full Poincaré beams [8] by means of a spatially structured liquid crystal device, referred to as $q$-plate [24]. The $q$-plate couples spin to orbital angular momentum, and thus allows for generating certain classes of space-varying optical beams when it is fed with an elliptically polarized input beam. Choosing a left-handed circularly polarized Gaussian beam, $\hat{\mathbf{e}}_{\mathrm{L}}$, as input, the $q$-plate coherently transforms this field distribution into

$$
\begin{equation*}
\mathrm{E}(\mathbf{r}) \approx\left(\cos \left(\frac{\delta}{2}\right) E_{\mathrm{L}}(\rho, z) \hat{\mathbf{e}}_{\mathrm{L}}+\mathrm{i} \sin \left(\frac{\delta}{2}\right) E_{\mathrm{R}}(\rho, z) \mathrm{e}^{2 \mathrm{i} q \phi} \hat{\mathbf{e}}_{\mathrm{R}}\right) \tag{1}
\end{equation*}
$$

where $\delta$ is the chosen optical retardation of the $q$-plate, $\rho, \phi, z$ are cylindrical coordinates, $q$ is the $q$-plate's topological charge, $\hat{\mathbf{e}}_{\mathrm{L}}$ and $\hat{\mathbf{e}}_{\mathrm{R}}$ are the left- and right-handed polarization unit vectors, and $E_{\mathrm{L}}(\rho, z)$ and $E_{\mathrm{R}}(\rho, z)$ are the beam profiles of the left- and right-handed circularly polarized beams, respectively [25]. The orientation of liquid crystal molecules in the transverse plane of a given $q$-plate with topological charge of $q=-1$ is shown in figure 1(a). Adjusting the optical retardation $\delta$ of the plate changes the superposition ratio, and thus the polarization topology. For instance, when (i) $\delta=0,2 \pi$, the plate will not change the initial state of the beam and the beam polarization remains left-handed circular; (ii) $\delta=\pi$, the plate works as a structured half-wave plate and converts the Gaussian beam into a right-handed circularly polarized doughnut beam possessing orbital angular momentum of $2 q$; (iii) $\delta=\pi / 2$ the plate generates a coherent superposition of (i) and (ii). In the latter case (iii), the beam exhibits a point of circular polarization on the optical axis (C-point) and an azimuthal polarization structure with polarization topological charge of $\eta=q$. An example of such polarization topology


Figure 2. Sketch of the experimental setup. (a) Distribution of the local fast axis of the liquid crystal molecules in the transverse plane of the employed $q=1$-plate. (b) Experimentally generated intensity distribution of the resulting full-Poincare beam that is subsequently focused. Note that a half-wave plate is used to transform the output polarisation topology into that of a $q=-1$-plate. (c) SEM-image of the utilized gold nano-sphere with a diameter of 80 nm . (d) Sketch of the experimental setup utilized to reconstruct the full vectorial focal field distribution of the tightly focused full Poincaré beam.
is shown in figure 1 (a). Note that the polarization topology shown in figure 1 (a) corresponds to that resulting from a $q=-1$-plate. The action of $a q=-1$-plate can be entirely reproduced using a $q=1$-plate sandwiched between two half-wave plates oriented at $\pi / 4$. Thus, for practical reasons, we use a $q=1$-plate followed by a half-wave plate in the experiment to mimic the $q=-1$-plate topology, where the input circular polarization is flipped (see figure 2).

Upon tight focusing, strong (longitudinal) $z$-components of the incoming transversely polarized beam described by equation (1) emerge. Using vectorial diffraction theory [26], one can show that the total electric field at the focus will have the following form [27]

$$
\begin{equation*}
\mathbf{E}_{\text {focus }}(\mathbf{r})=\left(\widetilde{E}_{\mathrm{L}}(\rho, z ; \delta) \hat{\mathbf{e}}_{\mathrm{L}}+\widetilde{E}_{\mathrm{R}}(\rho, z ; \delta) \mathrm{e}^{2 \mathrm{i} q \phi} \hat{\mathbf{e}}_{\mathrm{R}}\right)+\left(\widetilde{E}_{\mathrm{L}}^{z}(\rho, z ; \delta) \mathrm{e}^{\mathrm{i} \phi}+\widetilde{E}_{\mathrm{R}}^{z}(\rho, z ; \delta) \mathrm{e}^{\mathrm{i}(2 q-1) \phi}\right) \hat{\mathbf{e}}_{\mathrm{e}}, \tag{2}
\end{equation*}
$$

where $\widetilde{E}_{\mathrm{L}}$ and $\widetilde{E}_{\mathrm{R}}$ are the components of the transverse electric field (including the weight factors) at the focus, and $\widetilde{E}_{\mathrm{L}}^{z}$ and $\widetilde{E}_{\mathrm{R}}^{z}$ are the associated $z$-components. The exact form for these amplitudes, i.e. $\widetilde{E}_{\mathrm{L}}, \widetilde{E}_{\mathrm{R}}, \widetilde{E}_{\mathrm{L}}^{z}$ and $\widetilde{E}_{\mathrm{R}}^{z}$, can be found in [27]. The last term in equation (2) corresponds to spin-orbit coupling amplified by tight focusing with a high-numerical aperture (NA) lens [28], which renders the polarization vector in threedimensional space, with its amplitude depending on the NA of the focusing lens. However, the polarization ellipse traced by the tip of the electric field vector in time remains in a two-dimensional plane for any given point in space. Nevertheless, the spatial distribution of the polarization ellipse forms a specific topology in threedimensional space, which is dictated by the topological charge of the $q$-plate. Without loss of generality, we consider a radial position $\rho=\rho_{0}$ where the amplitude of the contributions of the initial right- and left-circular polarization components to the longitudinal focal field component are equal, i.e. $\widetilde{E}_{\mathrm{L}}^{z}\left(\rho_{0}\right)=\widetilde{E}_{\mathrm{R}}^{z}\left(\rho_{0}\right)$. The $z-$ component of the electric field, apart from a phase $\exp (\mathrm{i} q \phi)$, will now be proportional to $\cos [(q-1) \phi]$. The electric field intensity of the $z$-component will then be proportional to $|\cos [(q-1) \phi]|^{2}$, which results in a $2|q-1|$-fold symmetry. This $z$-component of the electric field turns the two-dimensional into a threedimensional polarization topology. The structure of the polarization topology can be studied by evaluating the spatial dependence of either the major or minor axes of the polarization ellipse. Tracing the focal field on a closed loop around the on-axis C-point, the major axis of the polarization ellipse oscillates $|q-1|$ times through the transverse plane. In the three-dimensional perspective, the major (or the minor) axis of the polarization ellipse, depending on the value of $q$, forms a Möbius or a ribbon topology with $|q-1|$ twists. While the existence of polarization Möbius strips with $3 / 2$-twists and $5 / 2$-twists, for the case of $q=-1 / 2$ and $-3 / 2$, respectively, has been experimentally demonstrated recently [16], we here will look at the case of ribbons with integer twists for integer values of $q$. In particular, we consider the case of $q \neq+1$ to avoid the trivial case of ribbons with no twists.

## 3. Experimental realization

To determine the polarization ellipse, and consequently its major and minor axes in three dimensions, it is necessary to measure amplitude and phase of the full complex vectorial light field in the plane of observation. This can be achieved by employing a probe as a local field sensor and utilizing the angularly resolved far-field scattering by this probe while point-wise scanning the latter relative to the field distribution. This technique, named Mie-scattering nano-interferometry (see [29] for more details on the technique), was shown to achieve deep sub-wavelength spatial resolution in the experimental study of vectorial focal fields. The Mie-scattering nano-interferometry has previously allowed for the experimental verification of optical polarization Möbius strips in both, tailored light fields [16] and in the focal region of a tightly focused linearly polarized beam around points of transversely spinning fields [30]. The general experimental concept will be discussed in the following, while details are discussed in [29].

The custom-built experimental setup is shown in figure 2 [29]. As a nano-probe, a single gold sphere with a transverse diameter of $d=80 \mathrm{~nm}$ and a height of $h=86 \mathrm{~nm}$ (see scanning electron micrograph in figure 2(c)) on a glass substrate is utilized. For the measurement, it is moved through the investigated field distribution via a three-dimensional piezo stage. The angularly resolved detection of the interference between the light scattered by the probe into the lower half-space forward direction and the directly transmitted light in this region is realized by collecting the light via an oil-immersion microscope objective ( $\mathrm{NA}=1.3$ ) and imaging its back focal plane onto a CCD camera (see figure 2(d)). This interferometric information for each position of the probe relative to the investigated field is equivalent to an observation of the scattering process from various directions. Thus, it allows for a retrieval of the relative phase information of the distributions under study from the far-field [29]. The highly confined field distribution containing a twisted ribbon formed by tracing the major axis of the polarization ellipse along a closed loop around the optical axis is created in the shown setup by sending an initially right-handed circularly polarized Gaussian beam onto a $q=1$-plate [24] (see sketch of its structure in figure 2(a)) and a subsequent half-wave plate.

As discussed in the previous section, this combination results effectively in the operation of a $q=-1$-plate. By adjusting the voltage applied to the liquid-crystal-based $q$-plate [25,31], a coaxial superposition of the initial right-handed circular polarized Gaussian beam $\left(\operatorname{HyGG}_{0,0}(\rho, \phi, z) \hat{\mathbf{e}}_{\mathrm{R}}\right)$ and a left-handed circularly polarized hypergeometric Gauss beam $\left(\operatorname{HyGG}_{-2,2}(\rho, \phi, z) \hat{\mathbf{e}}_{\mathrm{L}}\right)$ is generated [32,33] with the Hypergeometric Gauss modes $\operatorname{HyGG}_{p, \ell}(\rho, \phi, z)$ having the radial and azimuthal indices of $p$ and $\ell$, respectively. The resulting full Poincaré beam [8,25] is filtered spatially with a pinhole to obtain the lowest radial order of both constituting beams in the Laguerre Gauss basis, i.e. $\operatorname{LG}_{0,0}(\rho, \phi, z) \hat{\mathbf{e}}_{\mathrm{R}}$ and $\operatorname{LG}_{0,2}(\rho, \phi, z) \hat{\mathbf{e}}_{\mathrm{L}}$ (see figure 2(b) for the experimentally achieved intensity distribution). The spatially filtered beam is then transmitted through two orthogonally oriented non-polarizing beamsplitters to redirect part of the incoming beam and the light reflected from the sample onto corresponding photodetectors. By using two orthogonally aligned beamsplitters, the remaining weak polarizing effect of non-polarizing beamsplitters can be compensated for. Finally, the generated beam is focused by a microscope objective with an NA of 0.9 , resulting in the complex focal field distribution under study, shown in figure 3(a).

Scanning the described nano-probe through this focal field and applying the reconstruction algorithm [29] to the collected far-field intensity information results in the experimentally reconstructed focal field distributions shown in figure 3(b). Here, the excitation wavelength was chosen to be $\lambda=530 \mathrm{~nm}$, with an experimentally determined relative permittivity of the utilized nano-probe of $\epsilon=-3.1+2.5 i$. The total electric energy density (depicted on the left side of figure 3(b)) strongly resembles the numerically simulated field distributions calculated via vectorial diffraction theory (figure 3(a)) [26, 34]. The energy density distributions of the individual electric field components (right side of figure 3(b)) show minor deviations specifically in the transverse field components, where the skewing of the field structure can be traced back to a residual $\mathrm{LG}_{0,-2} \hat{\mathbf{e}}_{\mathrm{L}}$ beam, which might be present as a result of the generation of the field via a cascaded $q$-plate and half-wave plate. The resulting phase distributions are also shown as insets. The phase distribution of the transverse components of the electric field at the focus exhibit two singularities of topological charge $\pm 1$, both displaced (vertically or horizontally) away from the optical axis. Due to spin-orbit coupling, the $z$-component of the electric field under tight focusing gains extra phase singularity points, in this case five singular points that are shown in figure 3. The $z$-component of the electric field now reaches amplitudes comparable to that of the transverse components (see the scale bar in figure 3(b)), and thus breaks the cylindrical symmetry into a four-fold symmetric pattern.

The major and minor semi-axes of the polarization ellipse $\boldsymbol{\alpha}(\mathbf{r}), \boldsymbol{\beta}(\mathbf{r})$ as well as the normal to the polarization ellipse $\gamma(\mathbf{r})$ for the electric field $\mathbf{E}$ at any point of $\mathbf{r}$ can be calculated (see [3,35]) using the terminology of [36]


Figure 3. Electric energy density distributions of a tightly focused structured beam. (a) Numerically calculated focal field distribution for a tightly focused composite beam generated from a coherent superposition of $\mathrm{LG}_{0,0}(\rho, \phi, z) \hat{\mathbf{e}}_{\mathrm{R}}$ and $\mathrm{LG}_{0,2}(\rho, \phi, z) \hat{\mathbf{e}}_{\mathrm{L}}$. The total electric energy density distribution is plotted on the left, while the individual Cartesian components as well as their relative phase distribution are depicted on the right. (b) Experimentally reconstructed focal field distribution of the same input field used in (a), showing the very good overlap between experiment and calculation. All distributions are normalized to the maximum value of the corresponding total electric energy density distribution.


Figure 4. Experimentally reconstructed major axes of the polarization ellipses in the focal volume. Experimentally reconstructed distribution of the major axis of the polarization ellipse traced around the optical axis in the focal plane of the tightly focused structured beam as well as one wavelength before and after the focus. (a) The resulting polarization ribbon with twist number of -2 and (b) its projection onto the transverse plane are depicted for a trace radius of $\rho=150 \mathrm{~nm}$, shown as a red solid line in the semitransparent focal plane.

$$
\begin{align*}
\alpha(\mathbf{r}) & =\frac{1}{|\sqrt{\mathbf{E} \cdot \mathbf{E}}|} \mathfrak{R}\left(\mathbf{E} \sqrt{\mathbf{E}^{*} \cdot \mathbf{E}^{*}}\right), \\
\boldsymbol{\beta}(\mathbf{r}) & =\frac{1}{|\sqrt{\mathbf{E} \cdot \mathbf{E}}|} \Im\left(\mathbf{I} \sqrt{\mathbf{E}^{*} \cdot \mathbf{E}^{*}}\right), \\
\gamma(\mathbf{r}) & =\mathfrak{I}\left(\mathbf{E}^{*} \times \mathbf{E}\right), \tag{3}
\end{align*}
$$

where $\mathfrak{R}(u), \Im(u)$ and $u^{*}$ represent the real and imaginary parts of $u$, and its complex conjugate, respectively. With these equations, we calculated the local polarization ellipse in the focal plane, $z=0$, from the experimental field data at each point on a circular trace with radius $\rho=150 \mathrm{~nm}$ around the optical axis (shown in figure 3(b) as a black dashed circle). The major axes of the polarization ellipses for these points in three-dimensional space are shown in the central row of figure 4. In order to see the three-dimensional topological structure, the semiaxes are colored in blue and green, revealing a twisted ribbon with twist index -2 . Note that the number of twists is given by $|q-1|$, which for the above case is $|-1-1|=2$ (the minus sign indicates that the direction of the twists is clockwise). The projection of the major axis onto the transverse plane is shown next to the ribbon in figure 4(b). Following the major axes of the ellipses around the C-point also shows the two-dimensional polarization topology with the polarization topological index of -1 in the transverse plane. We observe the same
three-dimensional (ribbon with two twists) and two-dimensional (polarization topological index of -1 ) topologies for different radii around the C-point (not shown here). However, for radii, $\rho \gg 500 \mathrm{~nm}$, the field amplitudes drop quickly due to the strong spatial confinement of the focal field, resulting in a low signal-tonoise ratio.

In a next step, we also studied the behavior of the observed ribbon topology in other planes parallel to the focal plane within the focal volume. In order to observe the evolution of the three-dimensional polarization topology, we retrieve the electric field components and their relative phases one wavelength before and after the focus, i.e. $z= \pm \lambda= \pm 530 \mathrm{~nm}$ from the reconstructed focal data. Again, the major axes of the polarization ellipses are retrieved for a given radius, i.e. $\rho=150 \mathrm{~nm}$, and plotted in three-dimensional space. Figure 4 shows the evolution of the major axes of the polarization ellipses upon free-space propagation when it passes through the focal plane. The three-dimensional polarization topology, i.e. ribbon with -2 twists, as well as the twodimensional polarization topology, shown in figure $4(\mathrm{~b})$ as a projection onto the corresponding planes, are conserved upon propagation through the focus. However, two main effects can be observed. First, the magnitude of the $z$-component of electric field is weaker outside the focal plane. Second, the topological structure rotates while traversing the focal plane. The latter effect is more visible in the projection shown in figure 4(b) as two-dimensional topology, and was previously observed for the two-dimensional case [25]. Such a rotation in the three-dimensional and two-dimensional polarization topologies is caused by the difference in Gouy phases for $\mathrm{LG}_{0,0}(\rho, \phi, z)$ and $\mathrm{LG}_{0,-2}(\rho, \phi, z)$ beams. This propagation distance-dependent phase equals $-(2 p+|\ell|+1) \arctan \left(z / z_{\mathrm{R}}\right)$ for $\mathrm{LG}_{p, \ell}(\rho, \phi, z)$, where $z_{\mathrm{R}}$ is the Rayleigh range. Thus, one expects a relative accumulated phase when propagating from $-z$ to the focal plane (with $|z|>z_{\mathrm{R}}$ ), and, hence, a rotation of $\pi / 2$ of the polarization topology.

## 4. Conclusion

In summary, we studied the topological structure of an optical beam possessing a transverse polarization topological charge of -1 in the tight focusing regime. When such a structured beam is tightly focused, the longitudinal component of the electric field is enhanced, and the polarization structure forms a threedimensional topology. We utilized a recently introduced nanoscopic field reconstruction technique to measure all three components of the electric field as well as their relative phases. Calculating the major axes of the polarization ellipses from the measured data in three-dimensional space reveals a ribbon-type topology with two twists when following a circular trace around the optical axis. We also observed the evolution of the multitwisted polarization ribbon upon propagation through the focus.

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