

Prepared for:

Dutch Ministry of Transport, Public Works and  
Water Management, Tidal Waters Division

The importance of internal waves for  
mixing in a stratified estuarine tidal flow

Part two: tables and figures

November 1993

# The importance of internal waves for mixing in a stratified estuarine tidal flow

Part two: tables and figures

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**delft hydraulics**

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Table 1. Mean values for Rotterdam Waterway (day 156) and Caland channel (day 157).

Data derived from Table 2.

Mean values for day 156, Rotterdam Waterway:

Lower estimate/tot KE	[·]	0.74
Upper estimate/tot KE	[·]	1.02
$\int (G_{\partial u \partial u} + \chi  Q _{\rho u}) / \langle u'^2 \rangle$	[·]	0.55
$\chi  Q _{\rho v} / \langle v'^2 \rangle$	[·]	1.10
$\chi  Q _{\rho w} / \langle w'^2 \rangle$	[·]	1.29
$\alpha$	[·]	0.43
Br	[mm <sup>2</sup> /s <sup>3</sup> ]	310.

Mean values for day 157, Caland channel:

Lower estimate/tot KE	[·]	0.42
Upper estimate/tot KE	[·]	0.60
$\int (G_{\partial u \partial u} + \chi  Q _{\rho u}) / \langle u'^2 \rangle$	[·]	0.39
$\chi  Q _{\rho v} / \langle v'^2 \rangle$	[·]	1.01
$\chi  Q _{\rho w} / \langle w'^2 \rangle$	[·]	0.90
$\alpha$	[·]	0.47
Br	[mm <sup>2</sup> /s <sup>3</sup> ]	5.

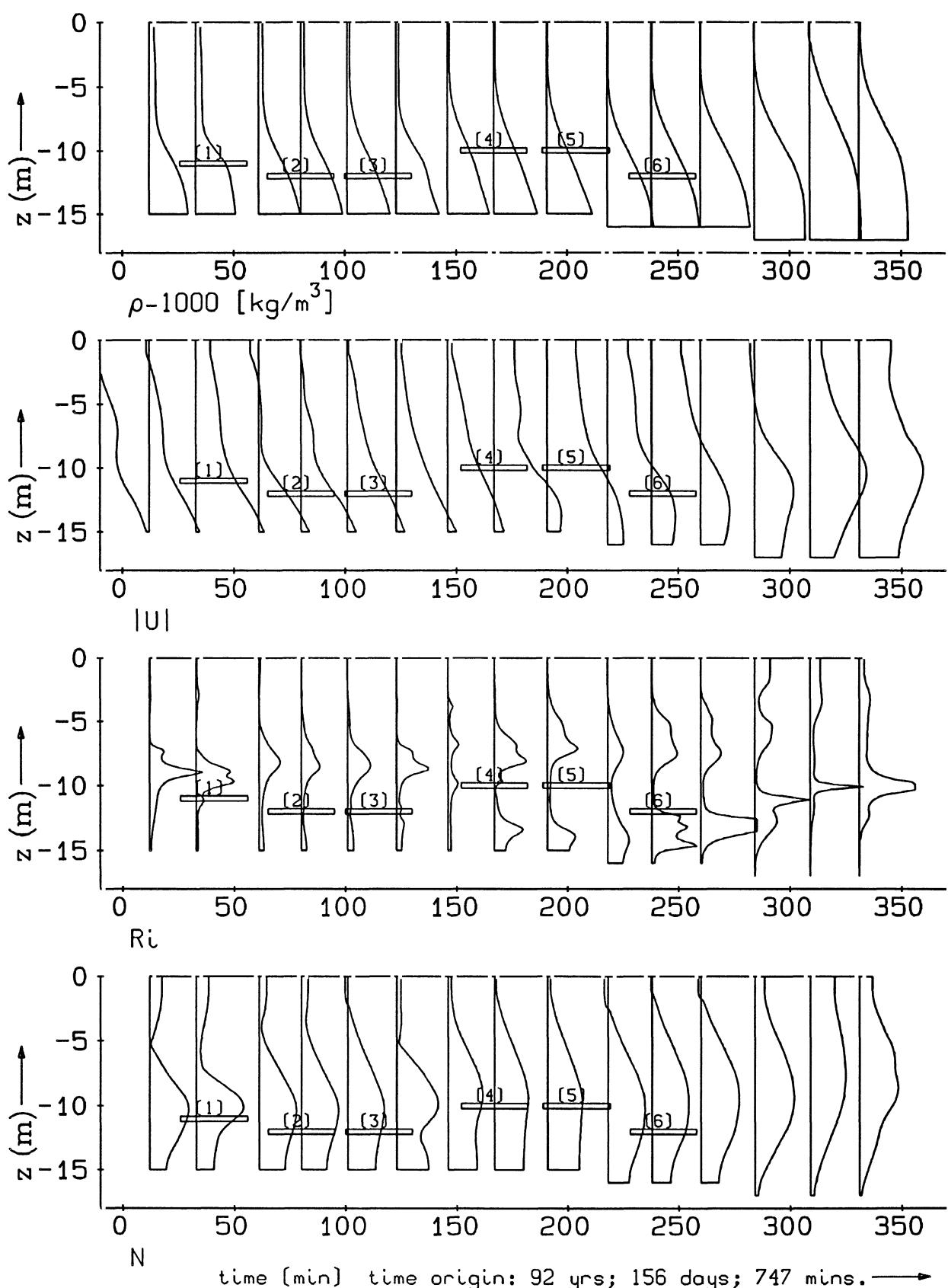
Table 2. Summary of platform data per time series measurement of 30 minutes.

Data averaged from Table 3.

Reference number M.E.T time/Julian day		1 [h:min/d]	2 12:53/156	3 13:32/156	4 14:07/156	5 14:59/156	6 15:36/156	7 16:15/156	8 09:13/157	9 09:53/157	10 10:35/157	11 11:11/157
Total KE: $\frac{1}{2}\langle \mathbf{u}' \cdot \mathbf{u}' \rangle$	[mm <sup>2</sup> /s <sup>2</sup> ]	2211	1560	1992	2878	992	977	452	833	1076	682.	
Upper estimate KIWE	[mm <sup>2</sup> /s <sup>2</sup> ]	2342	885	1915	3720	2129	117	281	390	870	345	
Lower estimate KIWE	[mm <sup>2</sup> /s <sup>2</sup> ]	1666	1308	1946	1915	1029	189	235	368	634	97.	
Lower estimate/tot KE	[-]	0.75	0.84	0.98	0.67	1.04	0.19	0.52	0.44	0.59	0.14	
Upper estimate/tot KE	[-]	1.06	0.57	0.96	1.29	2.15	0.12	0.62	0.47	0.81	0.51	
$\int (G_{\partial u / \partial u} + \chi  Q _{\rho u}) / \langle u'^2 \rangle$	[-]	0.55	0.56	0.61	0.68	0.72	0.16	0.47	0.41	0.54	0.16	
$\chi  Q _{\rho v} / \langle v'^2 \rangle$	[-]	1.53	1.18	1.40	0.73	1.38	0.37	1.51	1.24	1.07	0.23	
$\chi  Q _{\rho w} / \langle w'^2 \rangle$	[-]	1.47	0.96	1.27	0.85	2.21	0.98	0.79	0.97	1.54	0.30	
L <sub>E</sub>	[mm]	569	297	494	761	469	138	499	643	1094	786	
L <sub>E</sub> from $\int ( Q _{\rho u_i}  Q _{\rho u_i})^{1/4}$	[mm]	480	361	498	546	326	175	456	625	933	416	
L <sub>C</sub>	[mm]	200	110	60	70	50	70	30	20	30	50	
$\alpha$ from L <sub>E</sub>	[-]	0.54	0.26	0.48	0.72	0.47	0.13	0.31	0.42	0.68	0.46	
W	[-]	2	2	17	30	22	1	69	259	332	62.	
Br	[mm <sup>2</sup> /s <sup>3</sup> ]	692	328	236	306	260	38	5	3	7	4.	

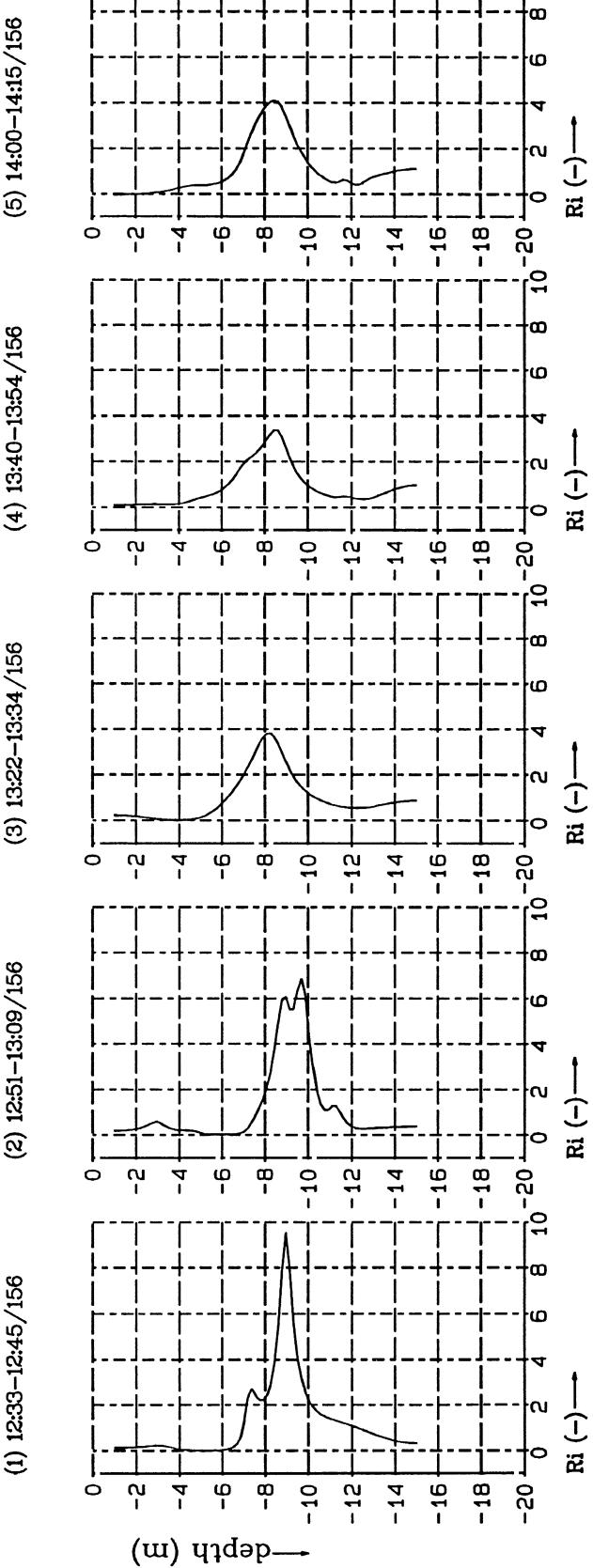
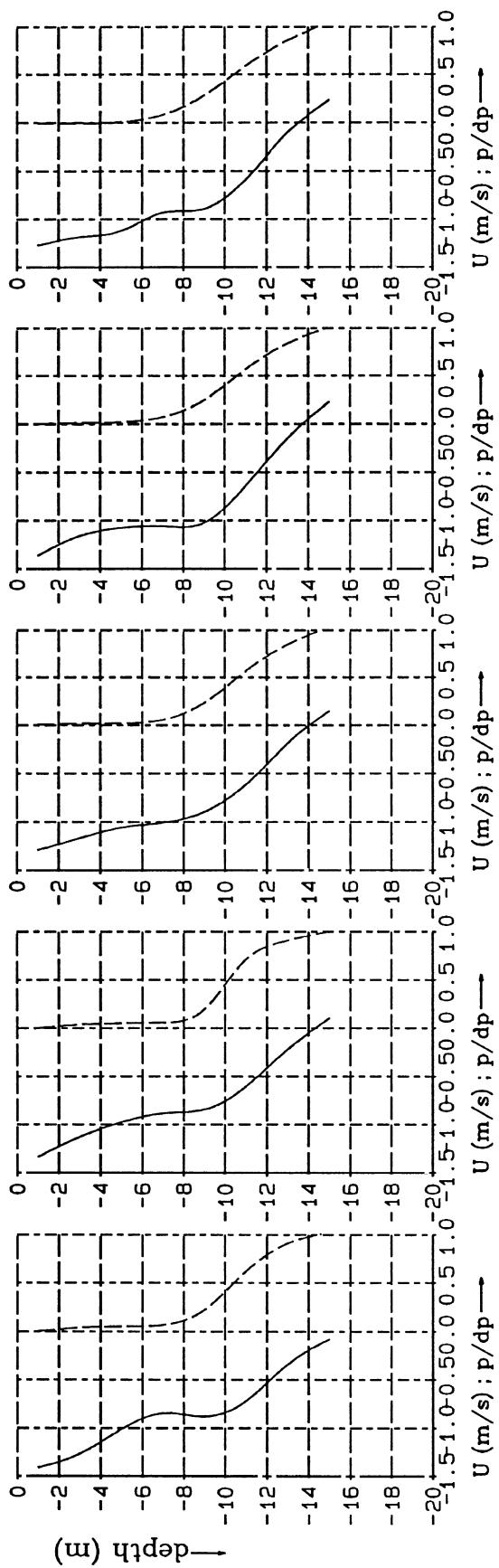
Table 3. Summary of microstructure and finescale observations at platform level.

Reference number	1	2	3	4	5	6	7	8	9	10
M.E.T time/Julian day	12:53/156	13:32/156	14:07/156	14:59/156	15:36/156	16:15/156	09:13/157	09:53/157	10:35/157	11:11/157
Depth [m]	11	12	12	10	10	12	6	6	6	9
Start after ref time [min]	26	65	100	152	189	228	19	59	101	137
End after ref time [min]	56	95	130	182	219	258	49	89	131	167
Finescale profile [-]	1+2	3+4	5+6	7+8	9+10	11+12	16	17+18	19+20	21
$-\langle \partial p / \partial z \rangle$ [kg/m <sup>4</sup> ]	3.14	2.35	1.46	3.02	2.81	3.21	0.70	0.65	0.41	0.39
dU/dz [1/s]	0.17	0.24	0.22	0.15	0.22	-0.13	0.048	0.036	0.043	0.025
U [mm/s]	604	389	272	444	286	693	165	263	253	61
Ri [-]	1.18	0.43	0.55	0.48	0.63	2.20	4.90	0.85	3.85	3.59
N [rad/s]	0.17	0.15	0.12	0.17	0.17	0.18	0.082	0.079	0.063	0.062
$\langle \rho'^2 \rangle$ [kg <sup>2</sup> /m <sup>6</sup> ]	0.799	0.122	0.130	1.32	0.435	0.0489	0.0305	0.0437	0.0503	0.0235
$\langle u'^2 \rangle$ [mm <sup>2</sup> /s <sup>2</sup> ]	3298	2520	3361	3708	1509	1613	477	1096	1601	696
$\langle v'^2 \rangle$ [mm <sup>2</sup> /s <sup>2</sup> ]	675	390	378	1217	361	270	85.7	303	276	523
$\langle w'^2 \rangle$ [mm <sup>2</sup> /s <sup>2</sup> ]	449	209	245	831	114	71.8	341	266	274	145
$\langle \rho' u' \rangle$ [kg.mm/s.m <sup>3</sup> ]	-29.5	-9.93	-13.3	-38.5	-12.4	1.62	0.773	-1.31	-0.347	0.0879
$\langle \rho' v' \rangle$ [kg.mm/s.m <sup>3</sup> ]	14.5	-0.941	-1.45	11.8	3.68	0.606	-0.264	0.448	-0.486	0.247
$\langle \rho' w' \rangle$ [kg.mm/s.m <sup>3</sup> ]	1.58	0.282	0.204	3.0	-0.0625	0.275	-0.0273	-0.172	0.426	-0.0164
$ Q _{\rho u}$ [kg.mm/s.m <sup>3</sup> ]	18.96	7.818	7.349	30.54	7.754	3.630	1.420	3.159	4.358	0.5989
$ Q _{\rho v}$ [kg.mm/s.m <sup>3</sup> ]	19.03	7.230	6.458	15.77	8.231	1.804	1.106	3.083	1.923	0.7593
$ Q _{\rho w}$ [kg.mm/s.m <sup>3</sup> ]	12.23	3.136	3.787	12.60	4.156	1.253	2.307	2.129	2.750	0.2765
$\int ( Q _{\rho u_i}  Q _{\rho u_i})^{1/4}$ [kg.mm/s.m <sup>3</sup> ]	30.77	11.51	10.86	38.25	12.72	4.430	2.990	5.008	5.626	1.046
$\langle u' w' \rangle$ [mm <sup>2</sup> /s <sup>2</sup> ]	-18.7	6.36	-68.0	34.8	-16.3	-49.9	-34.4	96.4	140	31.7
L <sub>c</sub> [mm]	200	110	60	70	50	70	30	20	30	50
H [m]	6	8	8	8	8	8	15	15	15	15



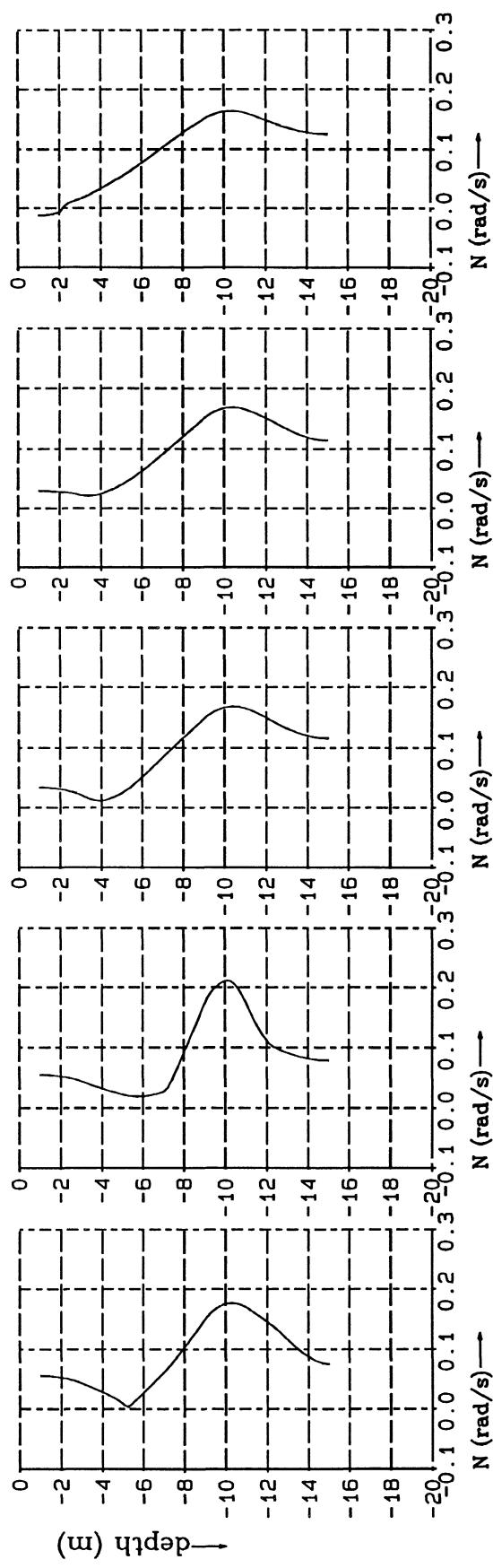
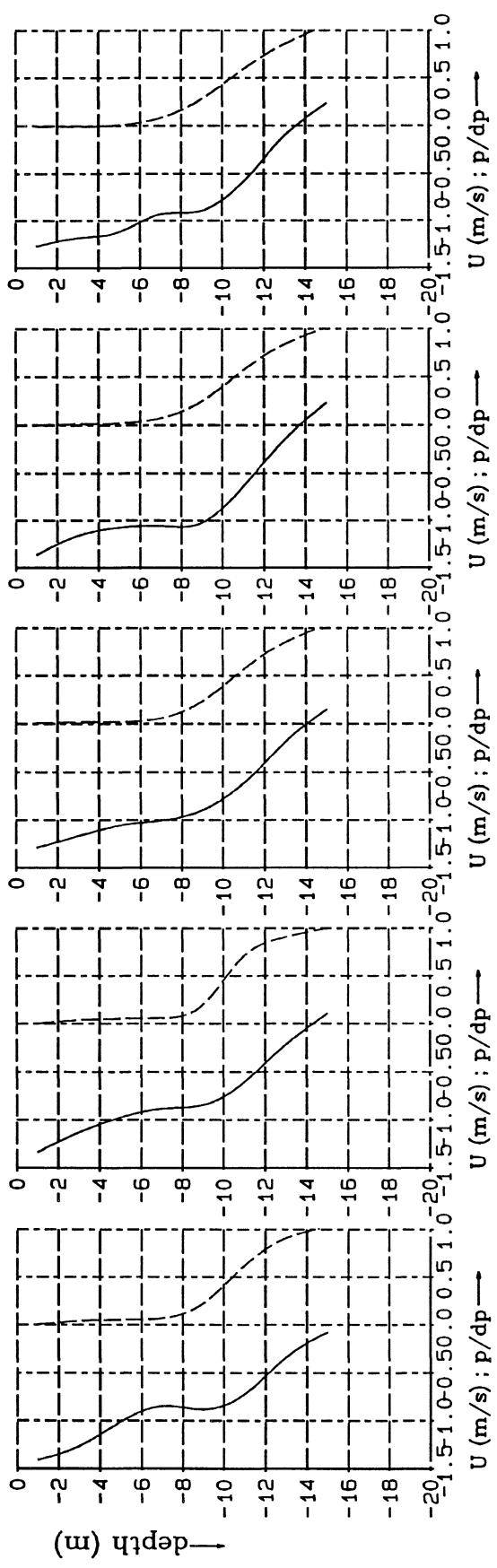
Density, vel. magnitude, Ri-number and buoyancy freq.  
 Rotterdam Waterway; day 156 [RWS].

day.156



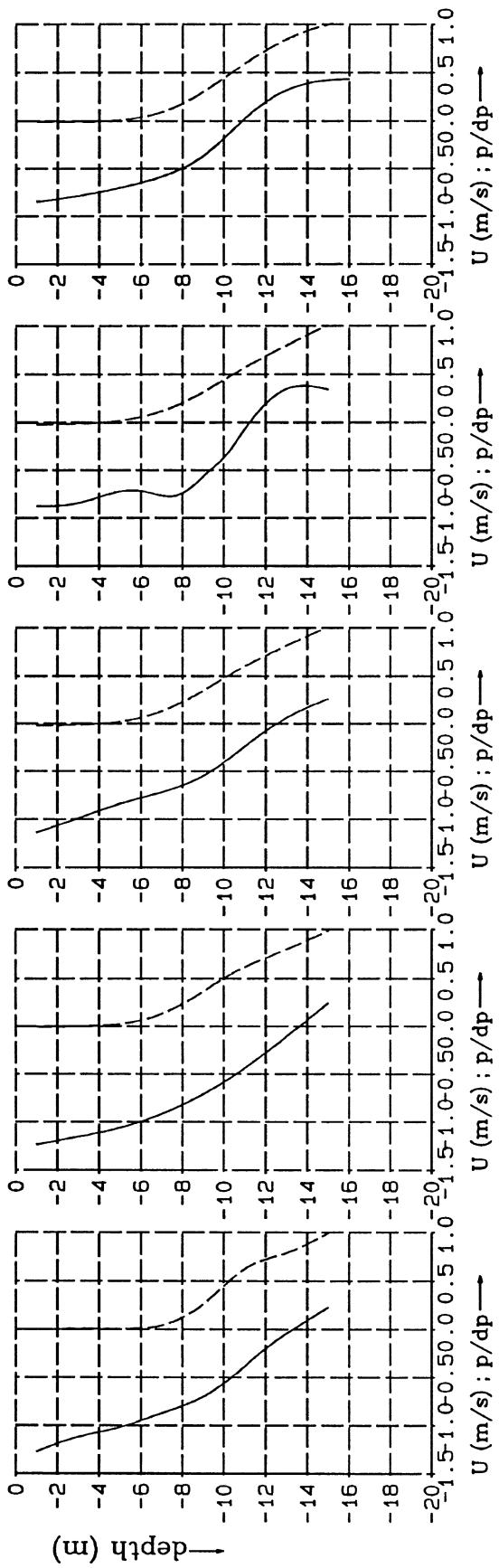
Vertical finescale profiles of  $|U|$ , rel. density and  
Richardson number (RWS).

Profiles 1-5  
Ri1-5.inv

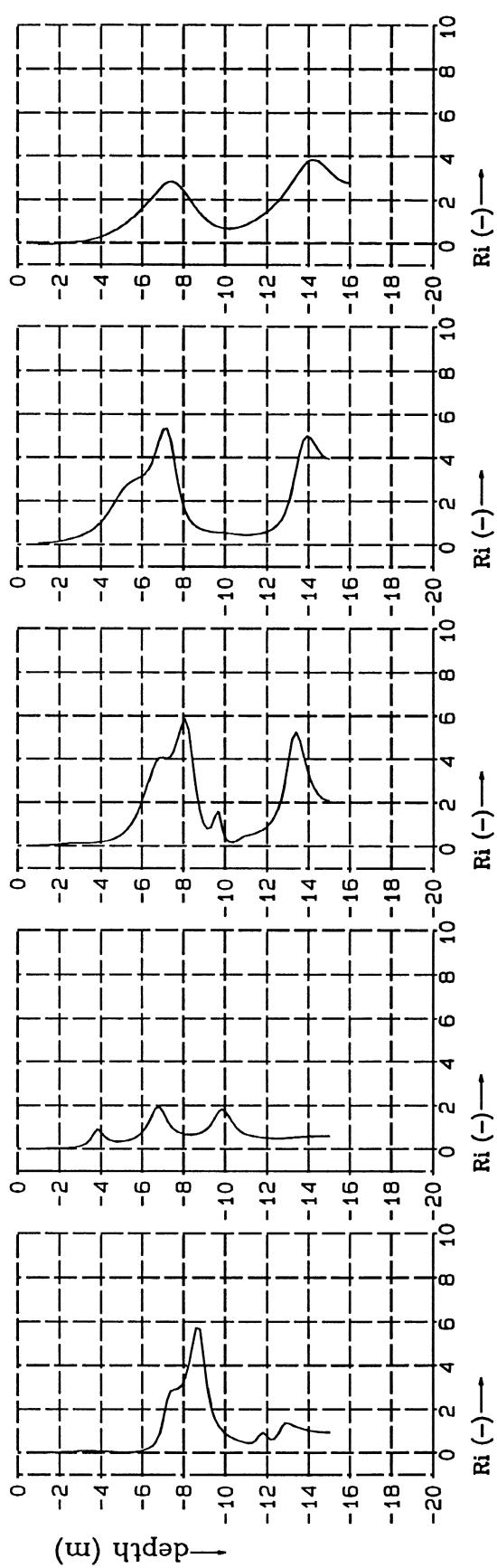


Vertical finescale profiles of  $|U|$ , rel. density and  
Brunt-Vaisala freq. [RWS].

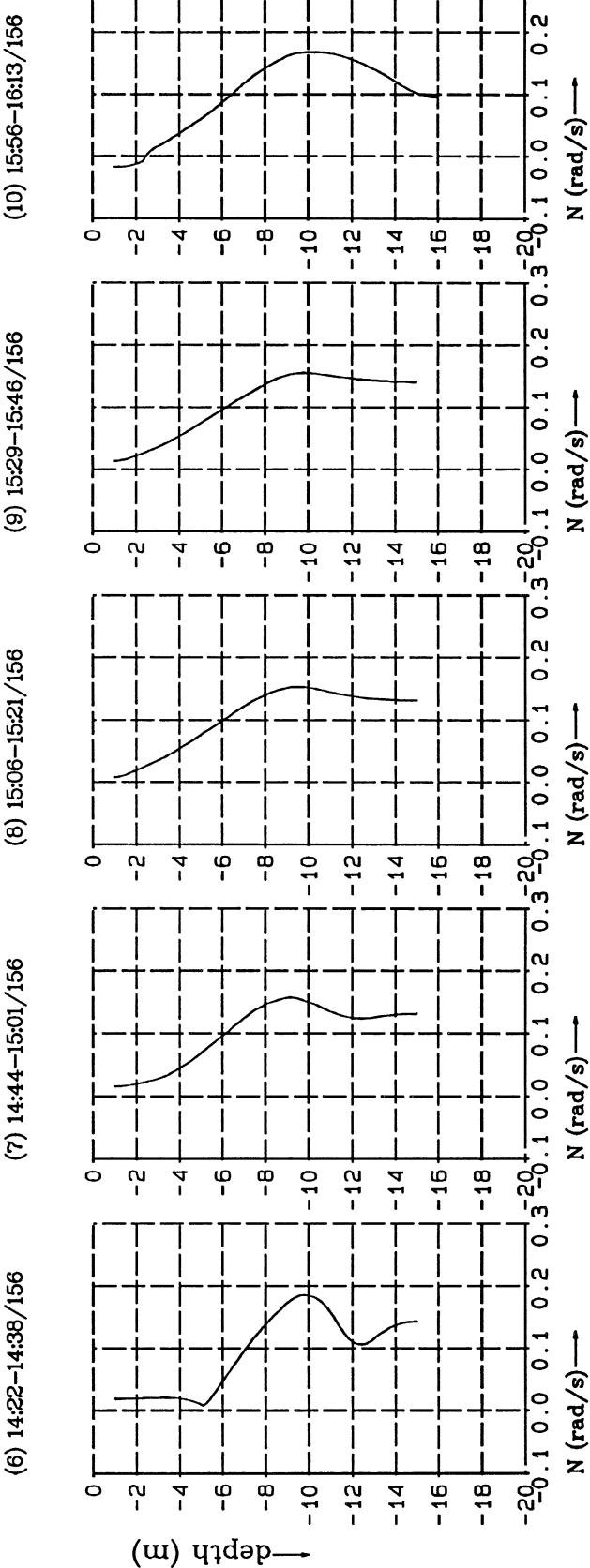
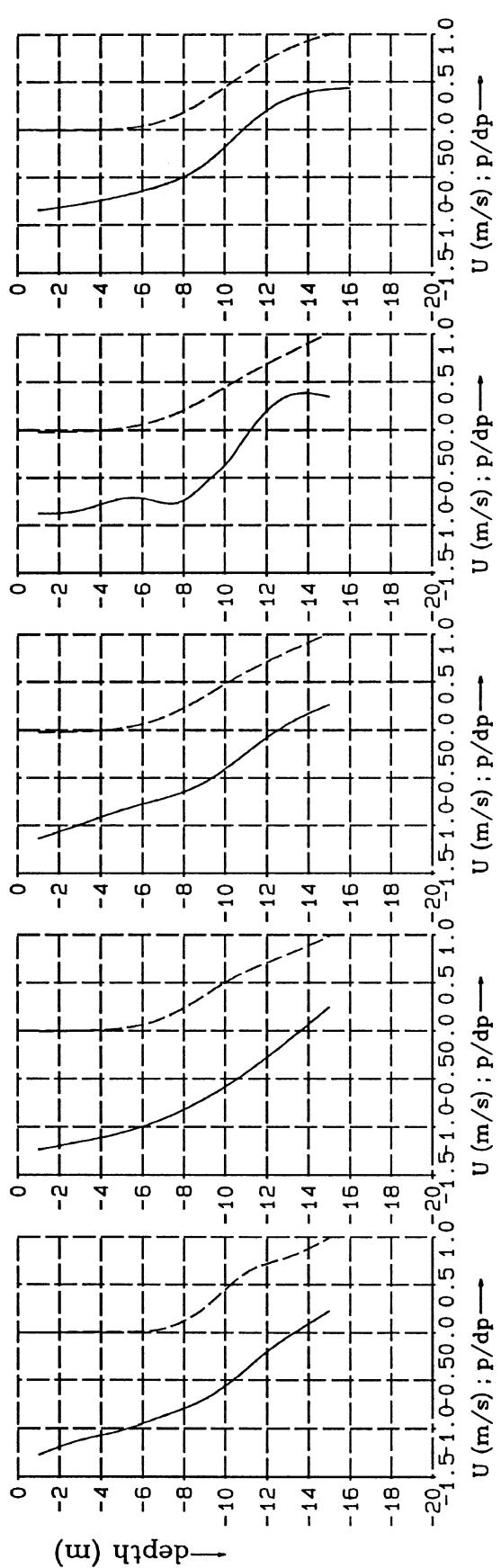
Profiles 1-5  
bv1-5.inv



Vertical finescale profiles of  $|U|$ , rel. density and  
Richardson number (RWS).



Profiles 6-10  
Ri6-10.inv



Vertical finescale profiles of  $|U|$ , rel. density and  
Brunt-Väisälä freq. [RWS].

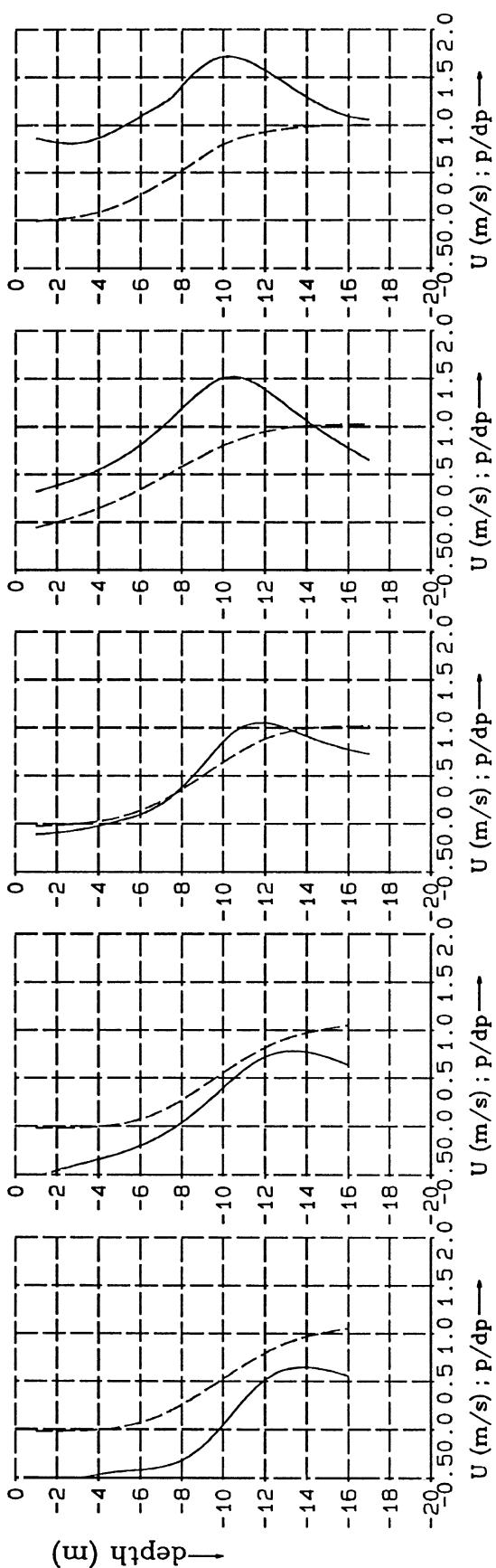
Profiles 6-10

bv6-10.inv

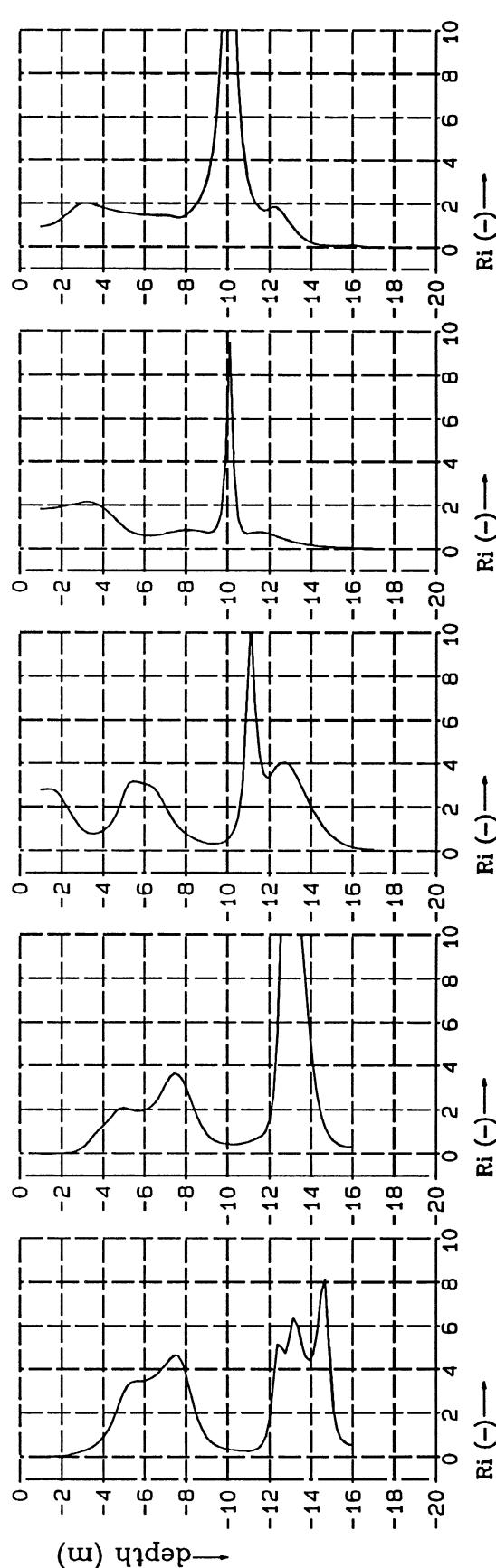
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Fig. 1<sup>e</sup>

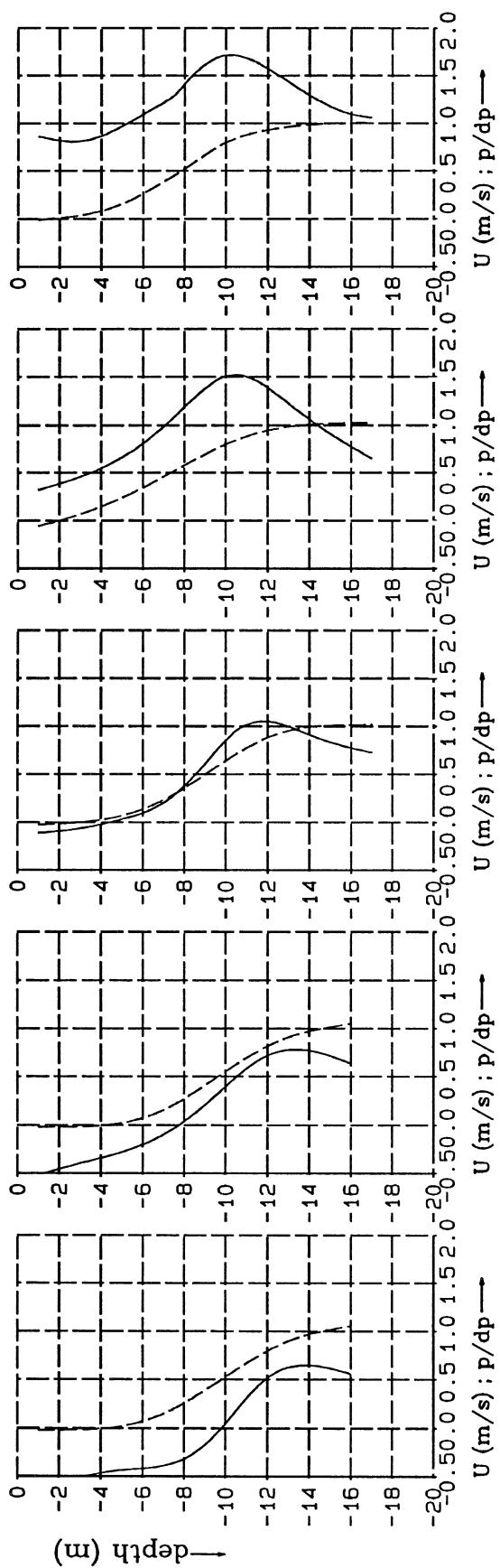


(11) 16:17-16:33/156 (12) 16:38-16:56/156 (13) 17:01-17:20/156 (14) 17:25-17:46/156 (15) 17:50-18:06/156



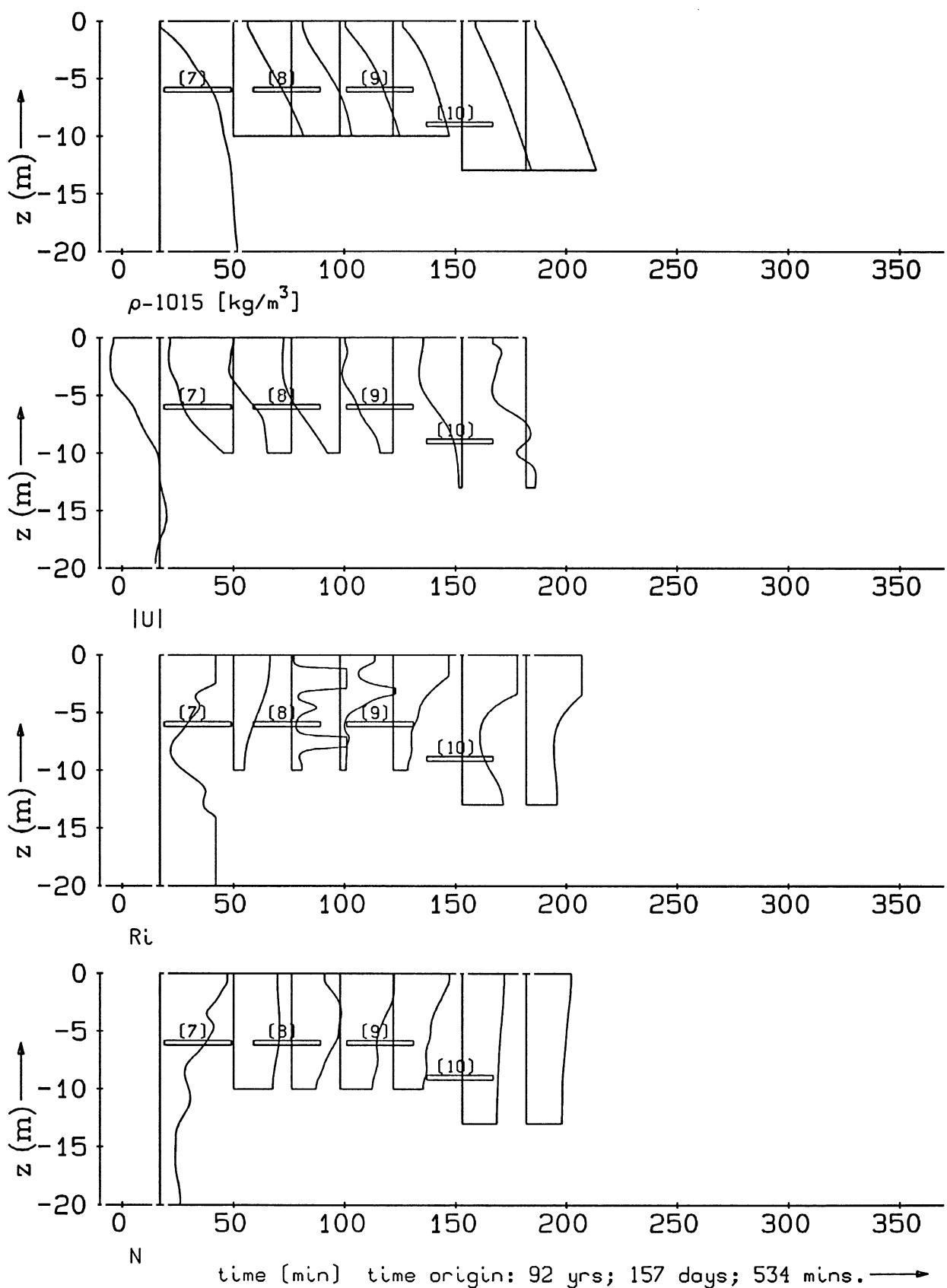
Vertical finescale profiles of  $|U|$ , rel. density and  
Richardson number (RWS).

Profiles 11-15	
$Ri_{11-15}.inv$	



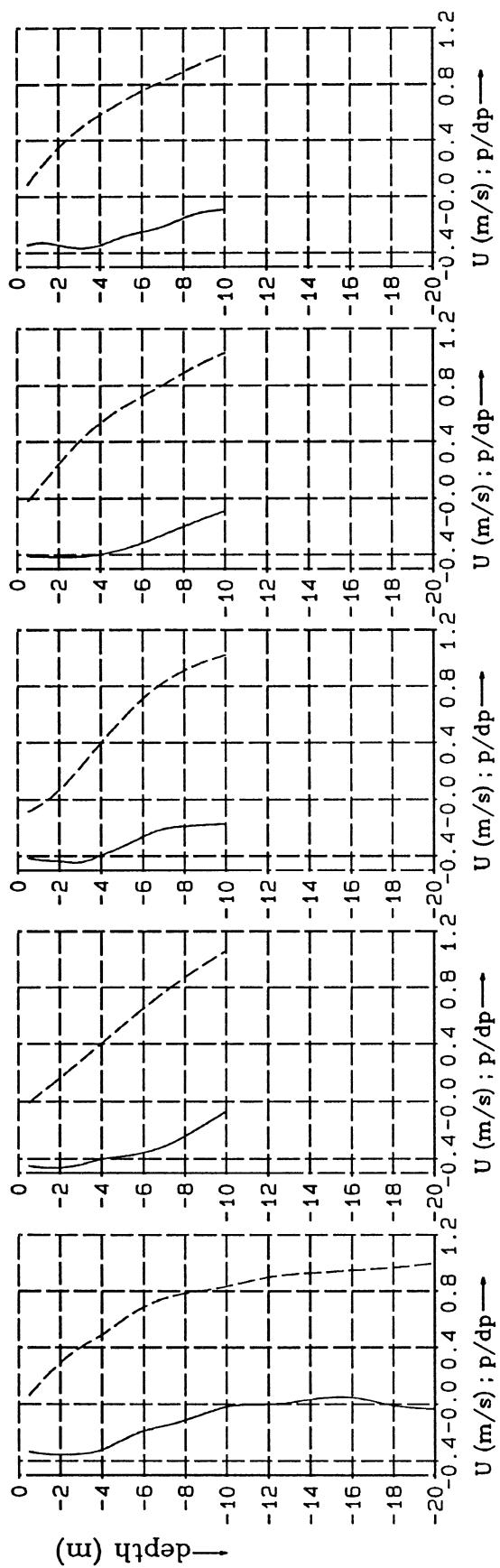
Vertical finescale profiles of  $|U|$ , rel. density and  
Brunt-Vaisala freq. [RWS].

Profiles 11-15  
bv11-15.inv

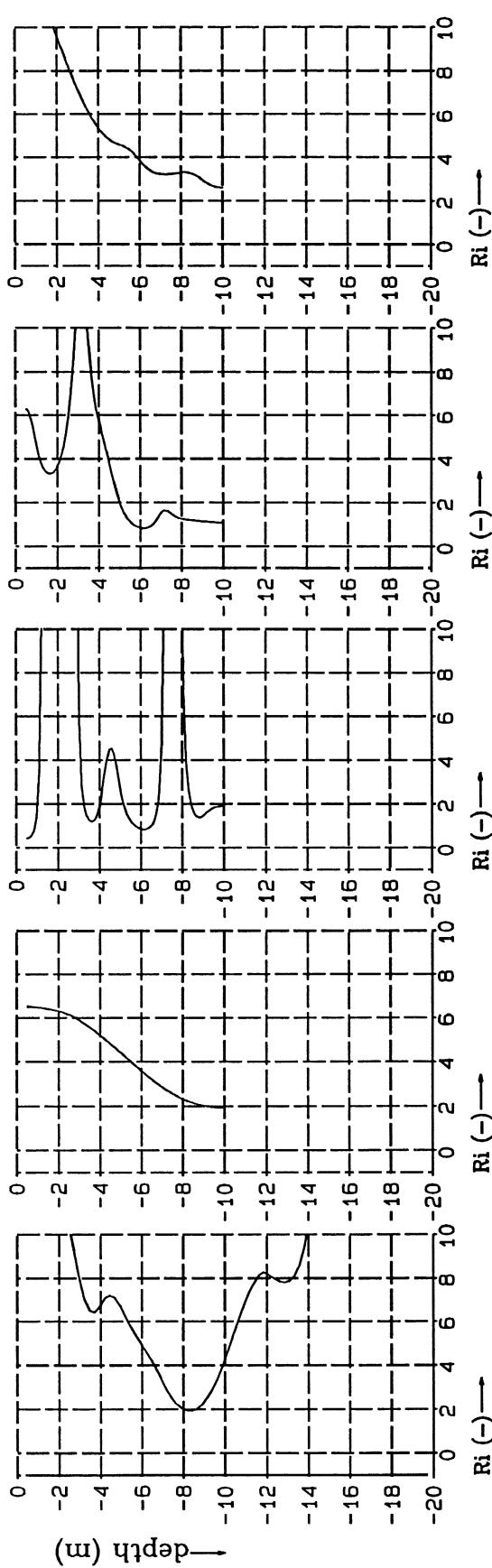


Density, vel. magnitude, Ri-number and buoyancy freq.  
 Caland channel; day 157 [RWS].

day.157

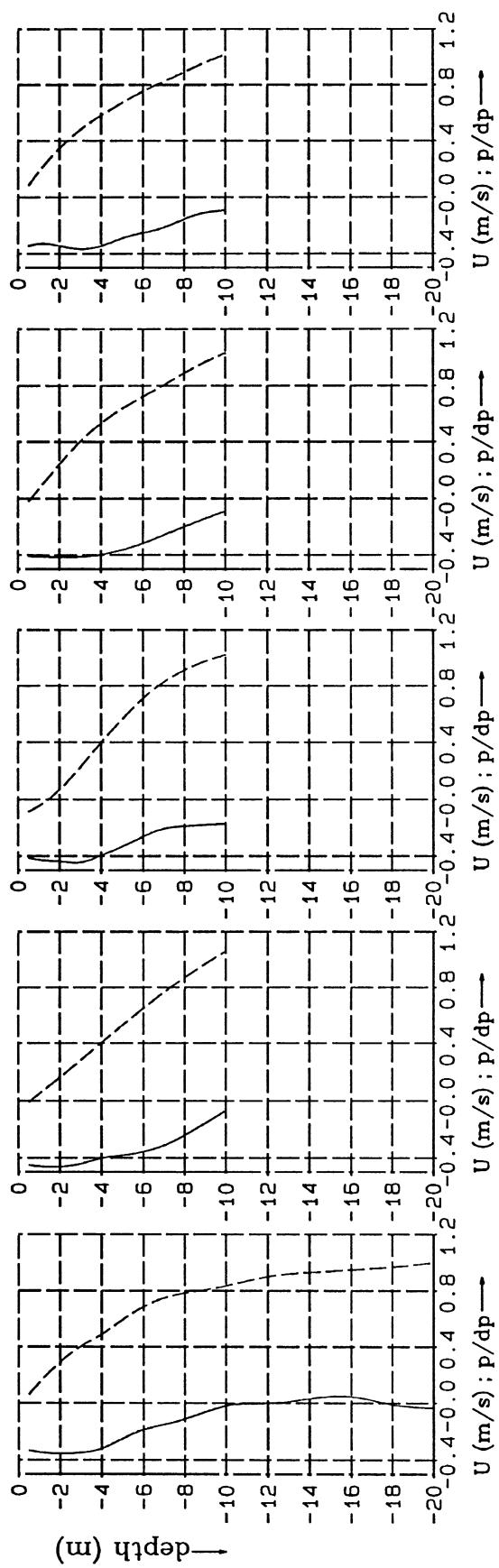


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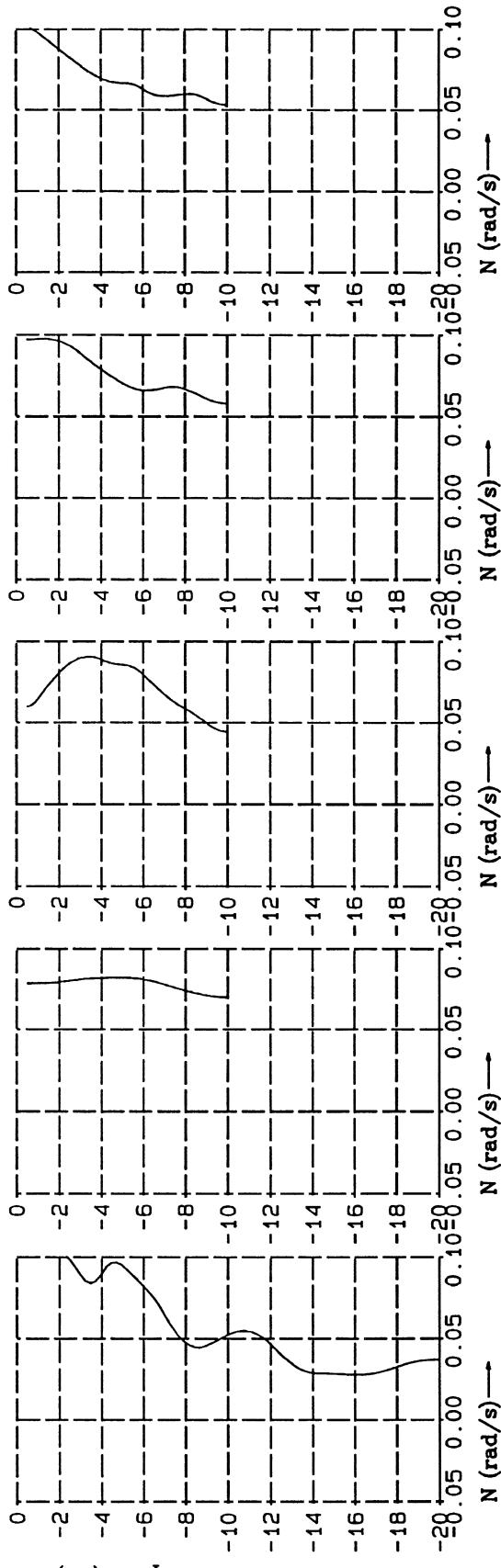
Vertical finescale profiles of  $|U|$ , rel. density and  
Richardson number (RWS).

Profiles 16-20  
Ri16-20.inv



Vertical finescale profiles of  $|U|$ , rel. density and  
Brunt-Väisälä freq. [RWS].

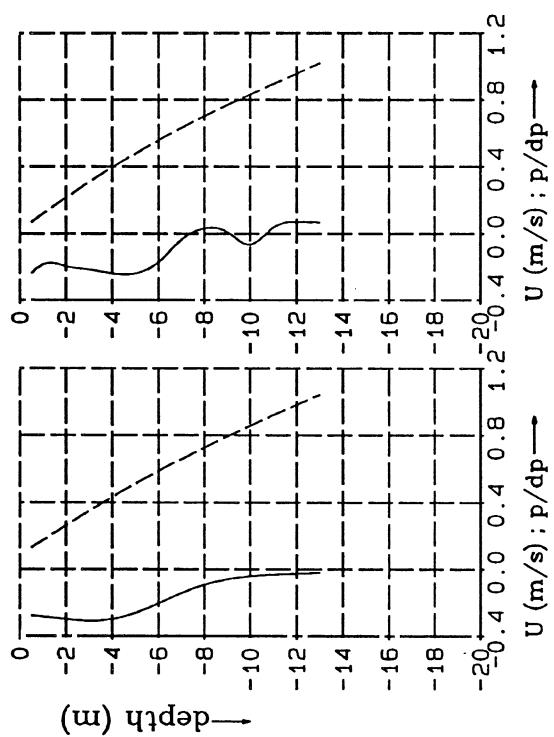
DELFT HYDRAULICS



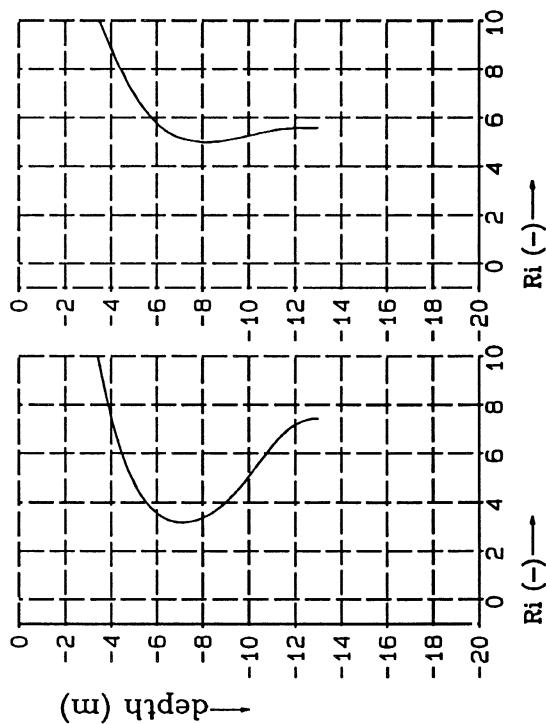
Profiles 16-20  
bv16-20.inv

Z694

Fig. 2<sup>c</sup>



(21) 11:12-11:41/157



(22) 11:45-12:07/157

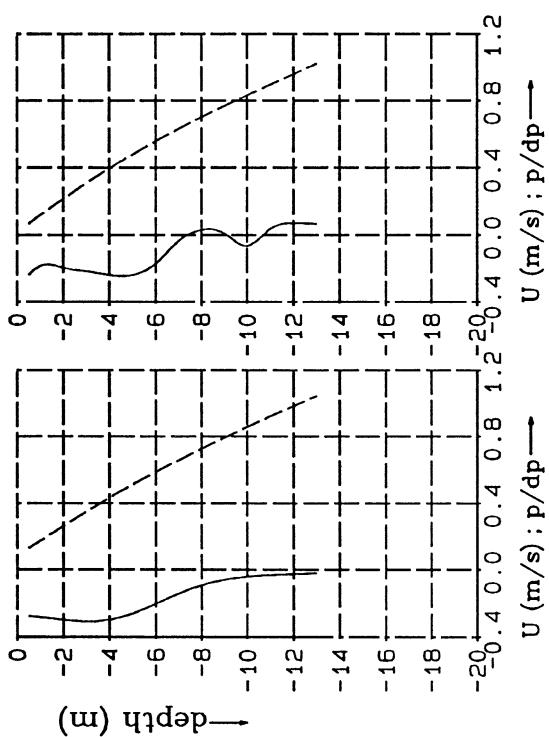
Vertical finescale profiles of  $|U|$ , rel. density and Richardson number (RWS).

Profiles 21-22

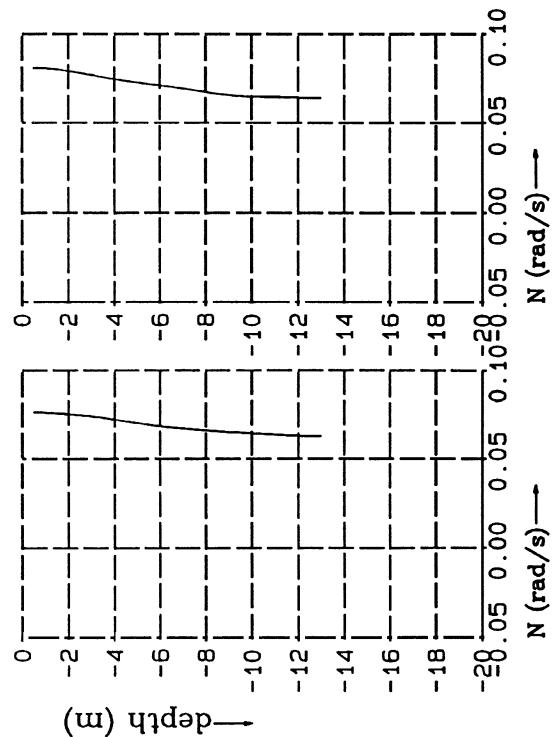
Ri21-22.inv

Z694

Fig.2<sup>d</sup>



(21) 11:12-11:41/157

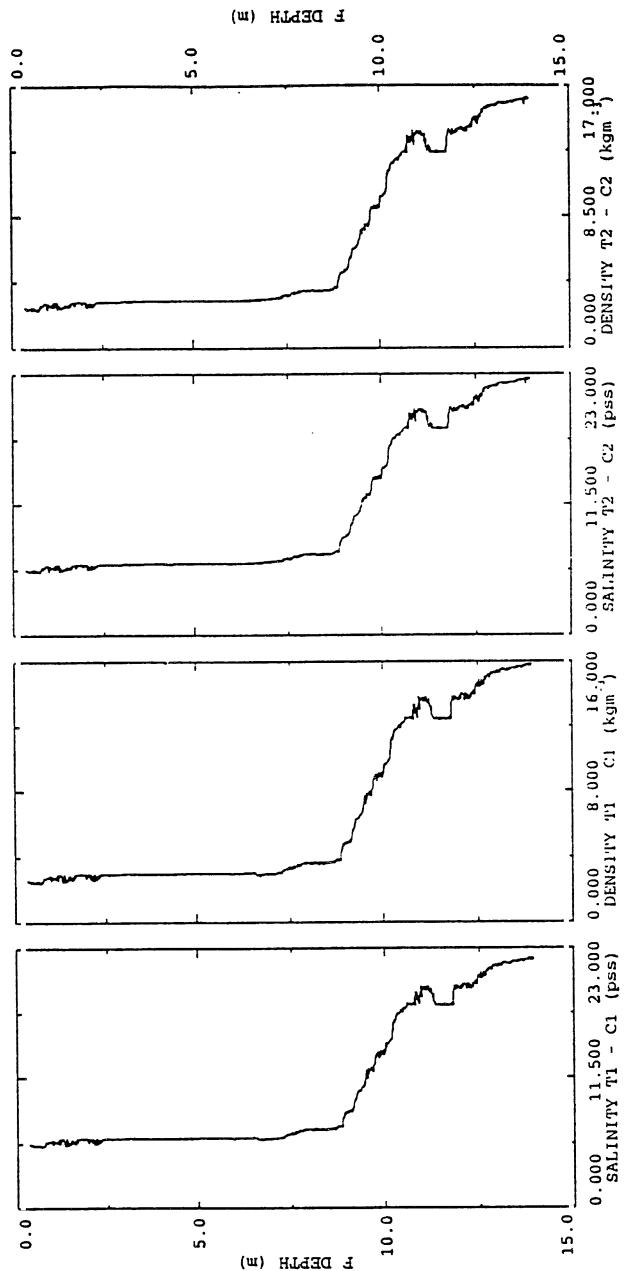


(22) 11:45-12:07/157

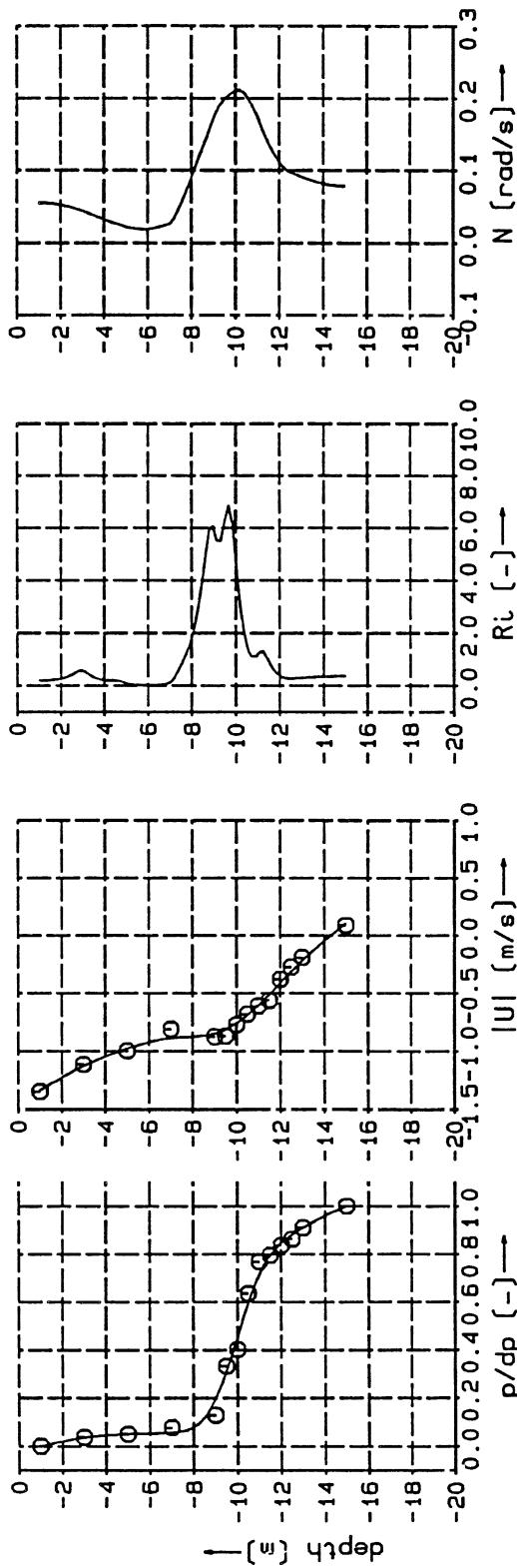
Vertical finescale profiles of  $|U|$ , rel. density and  
Brunt-Vaisala freq. (RWS).

Profiles 21-22

bv21-22.inv



a) Microstructure density profile [CWR]



b) Vertical finescale observations [RWS]

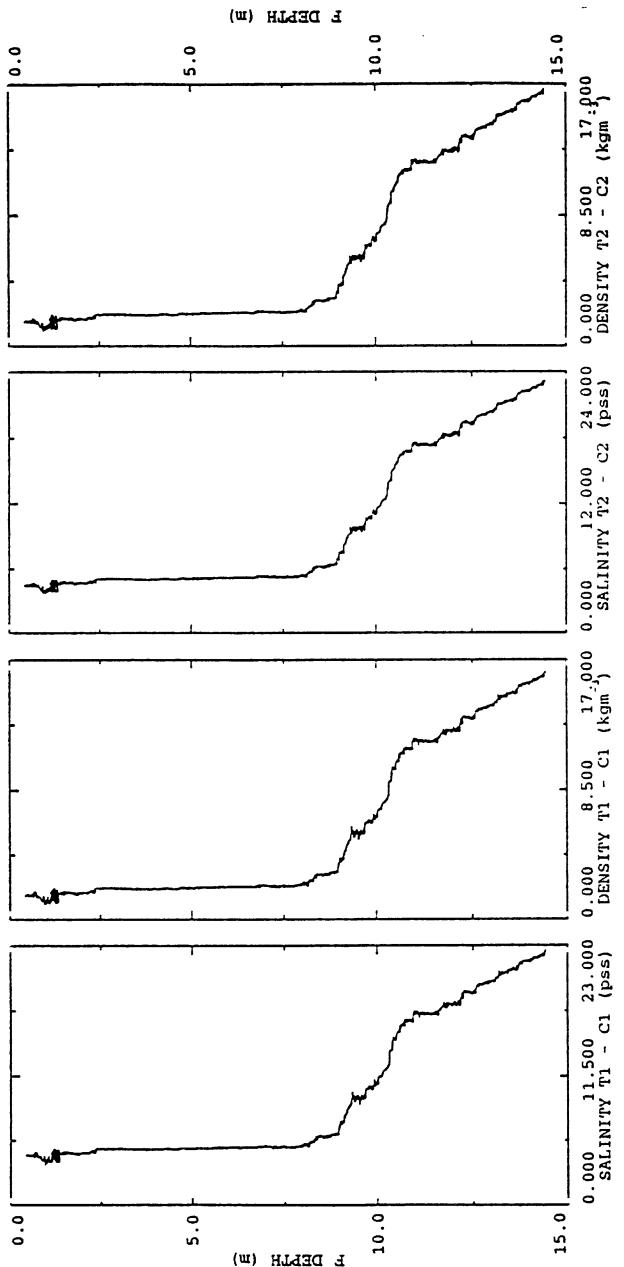
Microstructure density profile in the Rotterdam Waterway and vertical finescale structure.

12:51/156

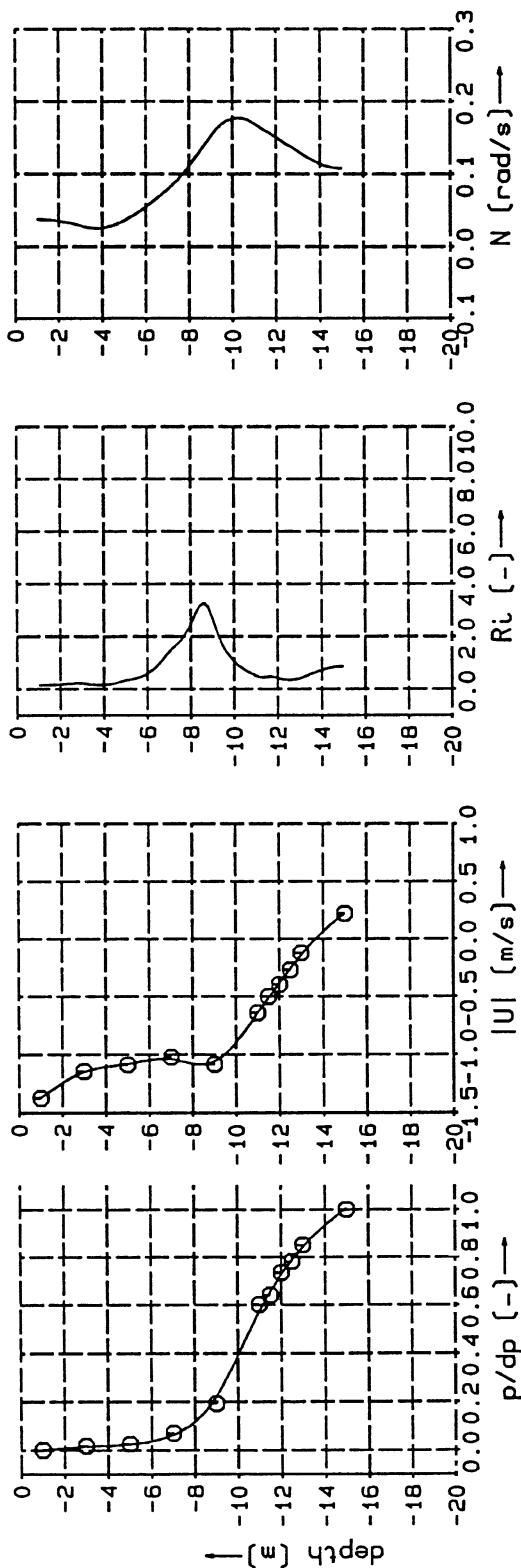
prof 2

Z 694

Fig. 3



a) Microstructure density profile [CWR]



b) Vertical finescale observations [RWS]

Microstructure density profile in the Rotterdam Waterway and vertical finescale structure.

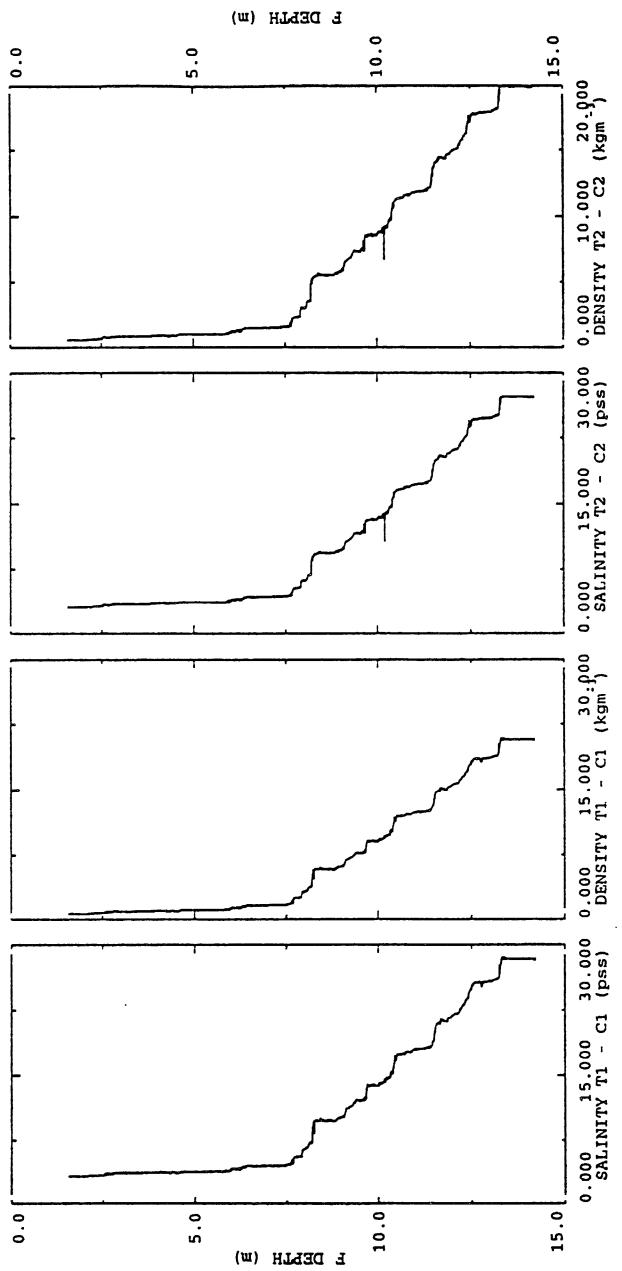
13:50/156

prof 4

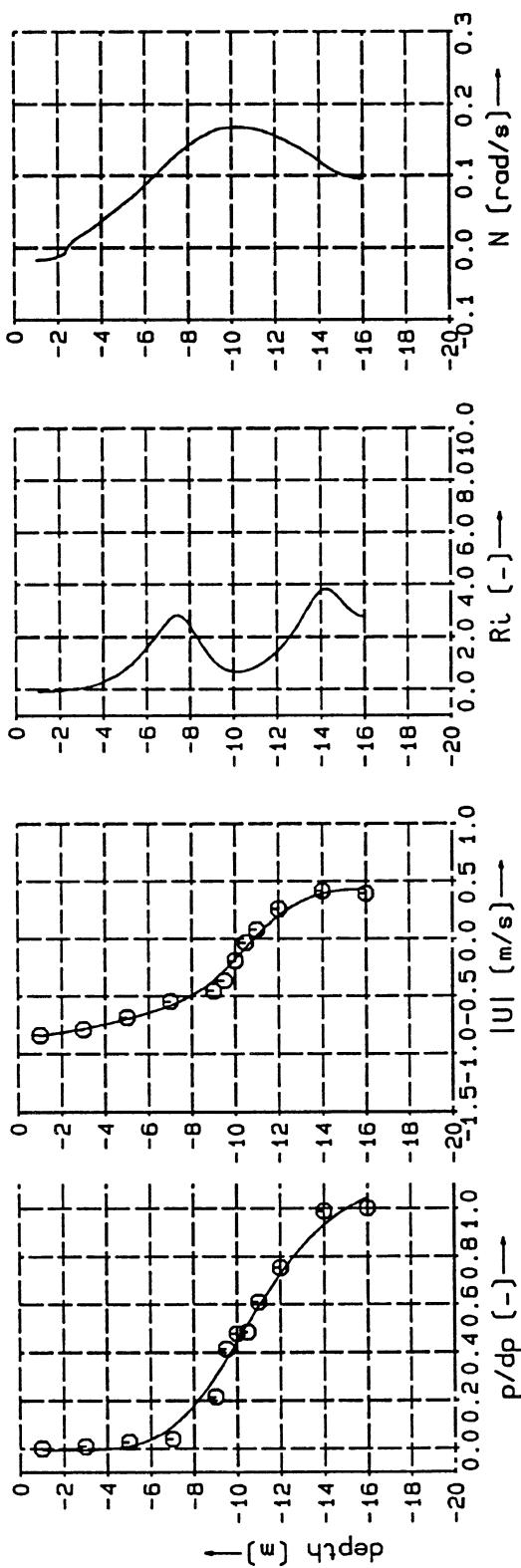
DELFT HYDRAULICS

Z 694

Fig. 4



a) Microstructure density profile [CWR]

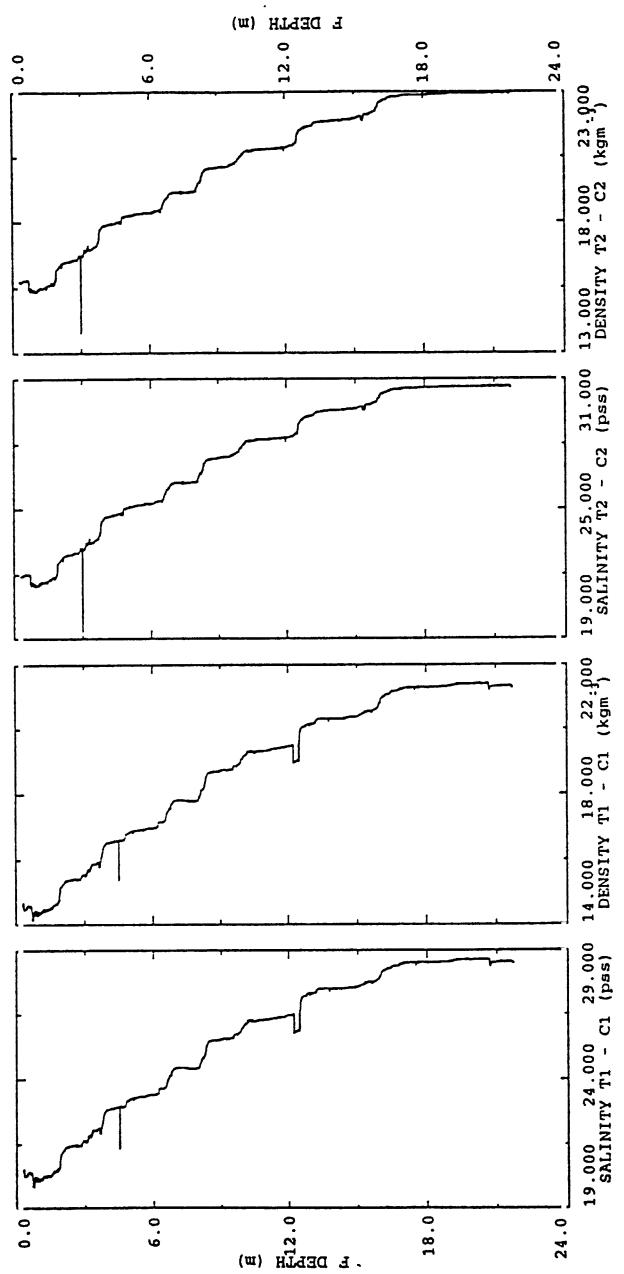


b) Vertical finescale observations [RWS]

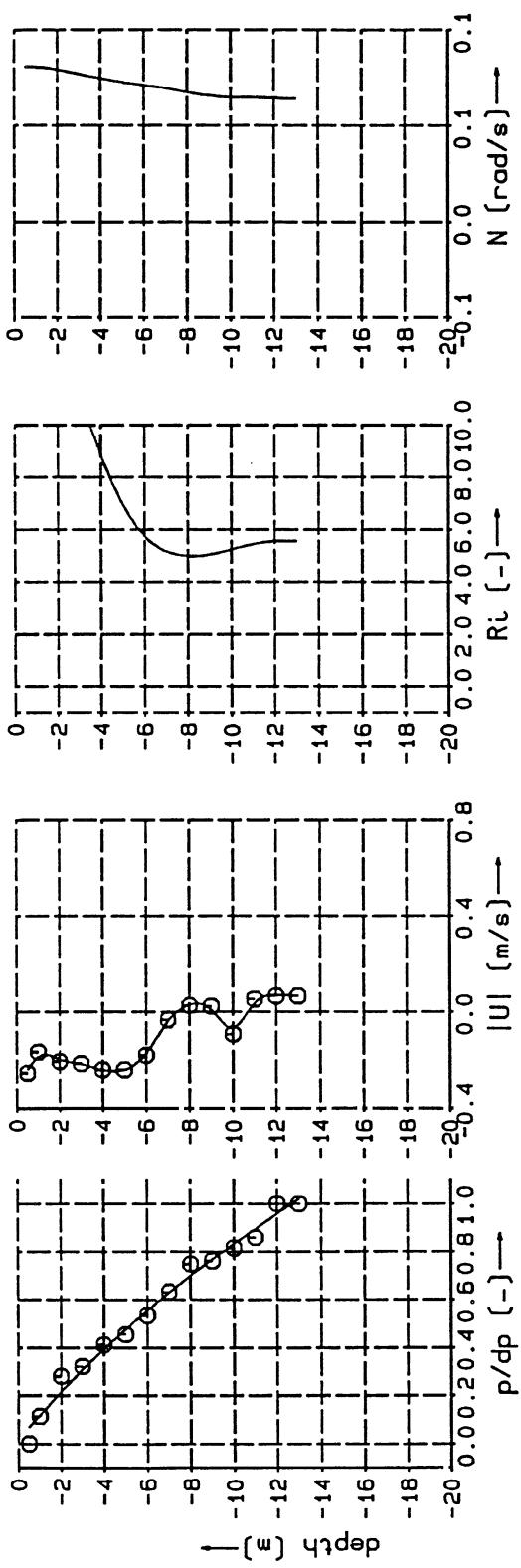
Microstructure density profile in the Rotterdam  
Waterway and vertical finescale structure.

16:13/156

prof 10



a) Microstructure density profile (CWR)



b) Vertical finescale observations (RWS)

Microstructure density profile in the Rotterdam Waterway and vertical finescale structure.

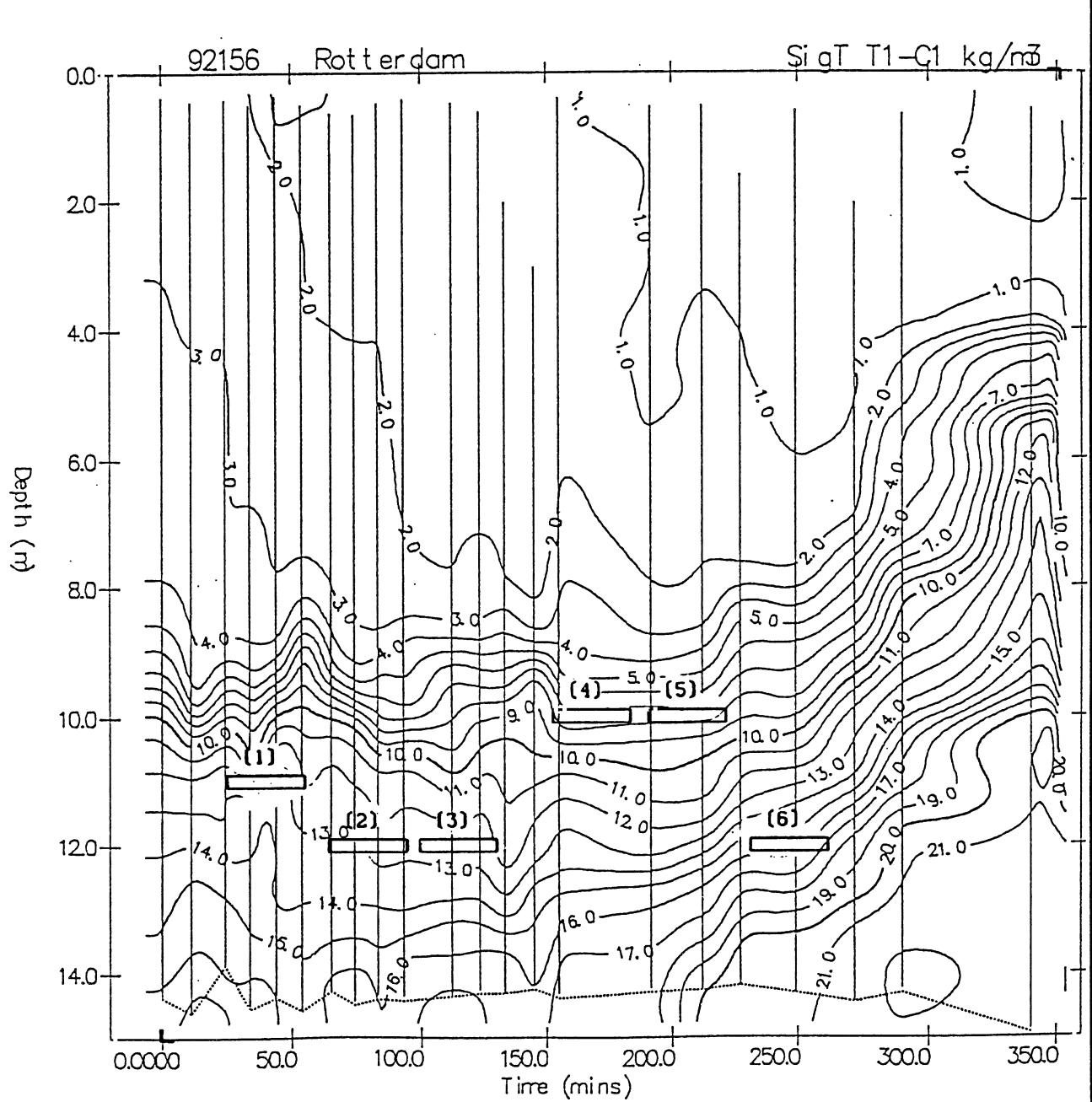
11:46/157

prof 22

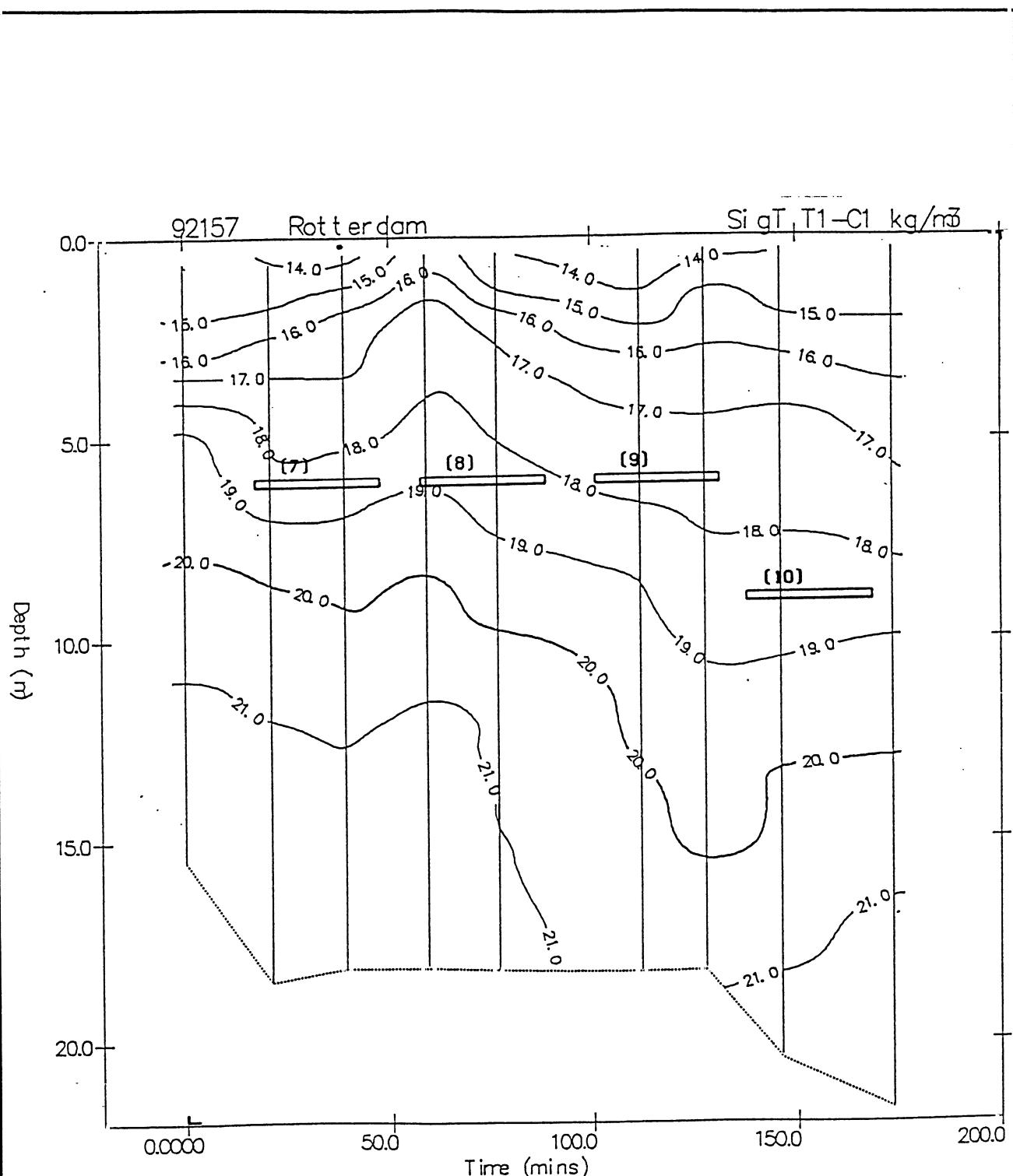
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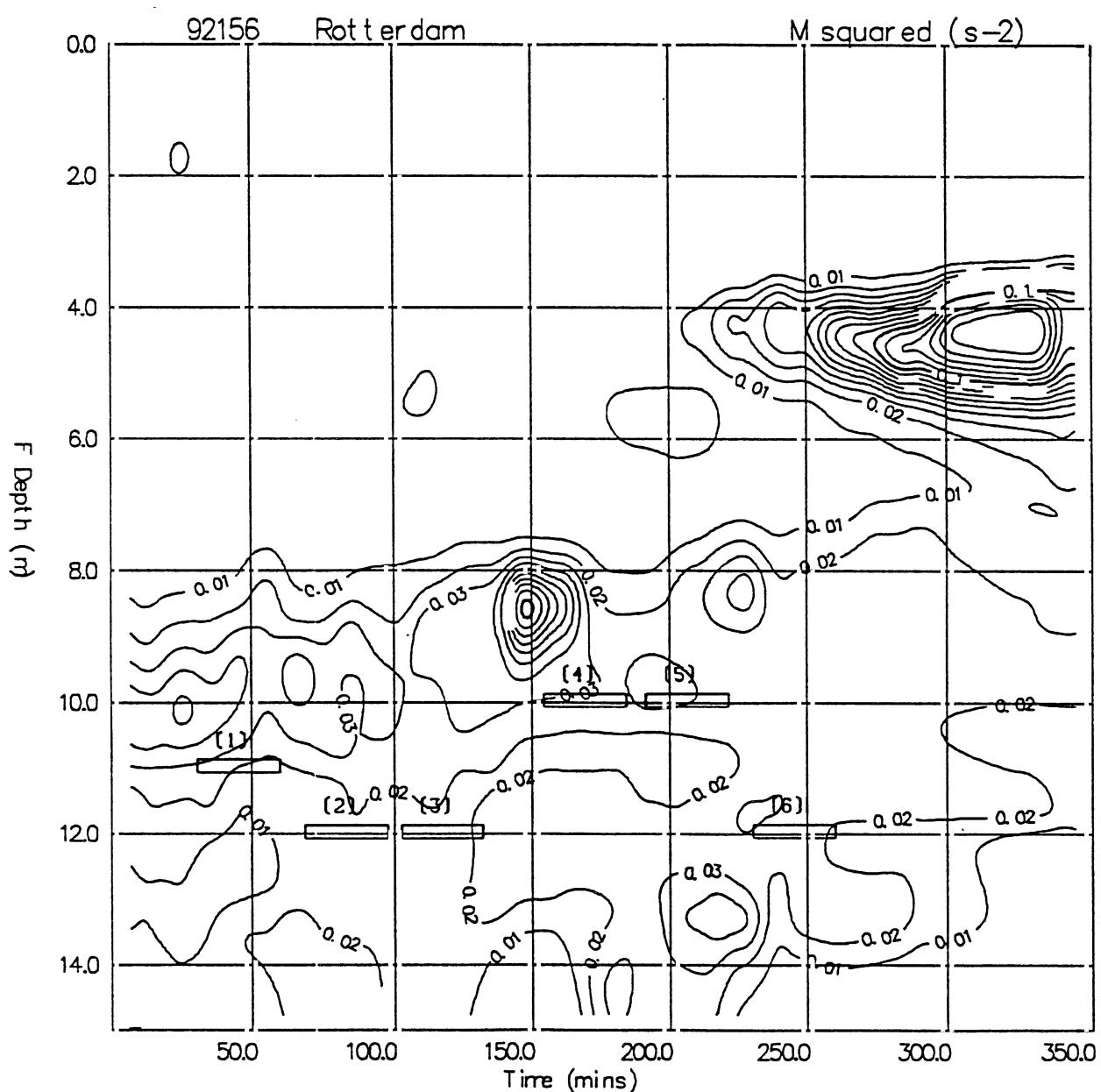
Fig. 6



Density isolines. Rotterdam Waterway (CWR)  
on day 156.

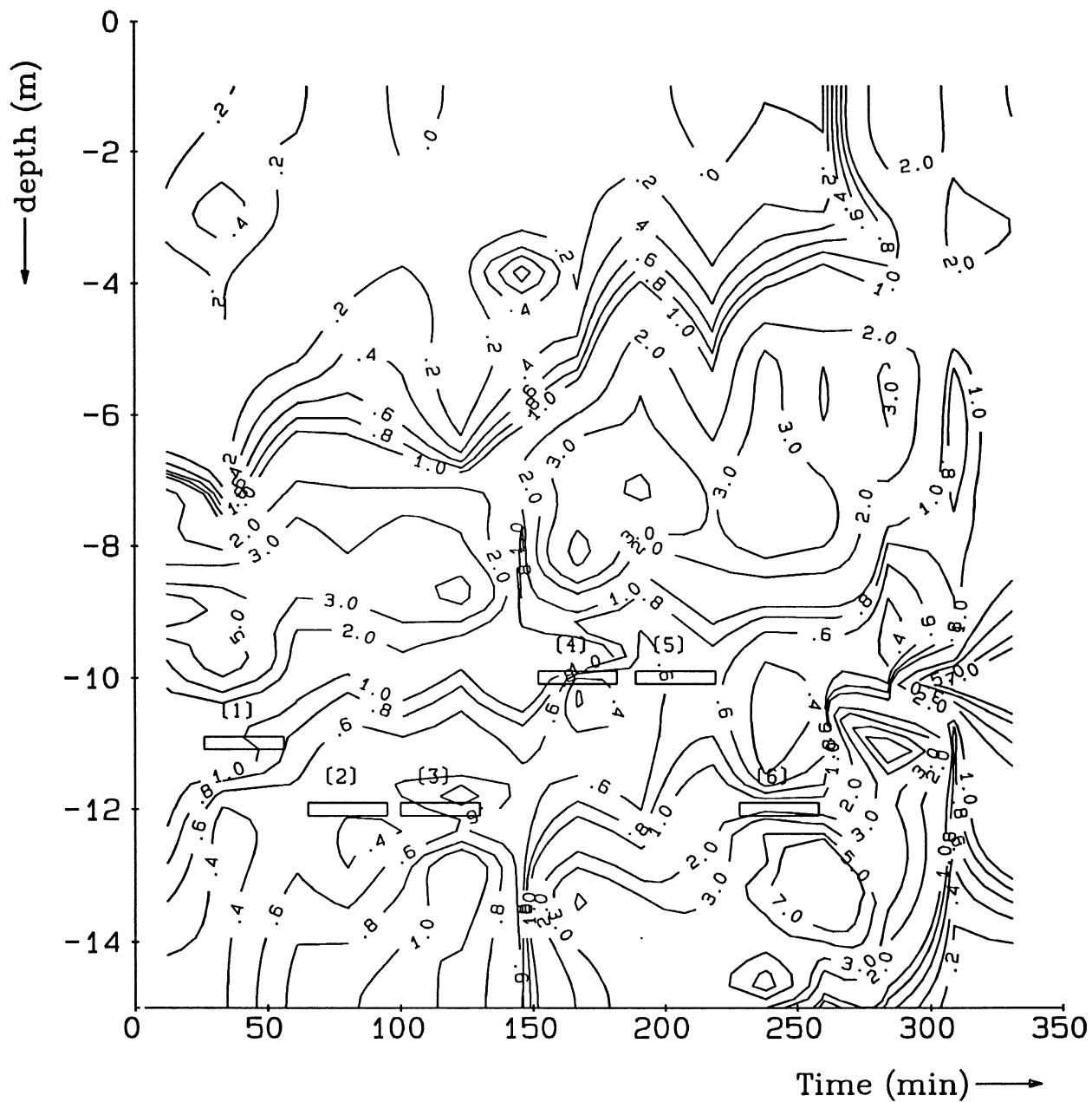


Density isolines. Catand channel (CWR)  
on day 157.



Buoyancy frequency squared. Rotterdam Waterway  
on day 156 [CWR].

Time origin: 92 yrs; 156 days; 746 mins.  
 $R_i$  [-]



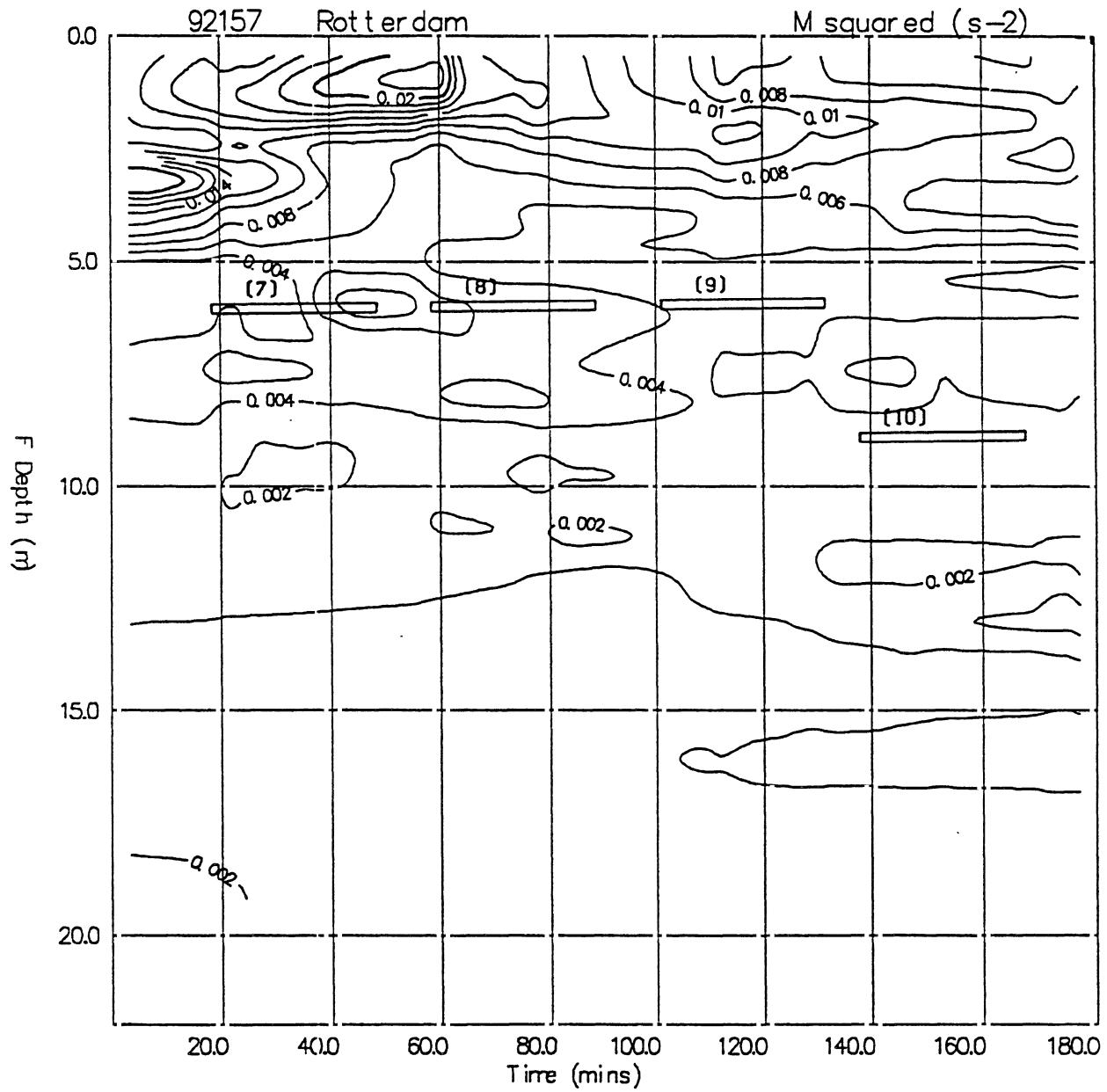
Gradient Richardson number. Rotterdam  
Waterway on day 156 [RWS].

ri156.iso

DELFT HYDRAULICS

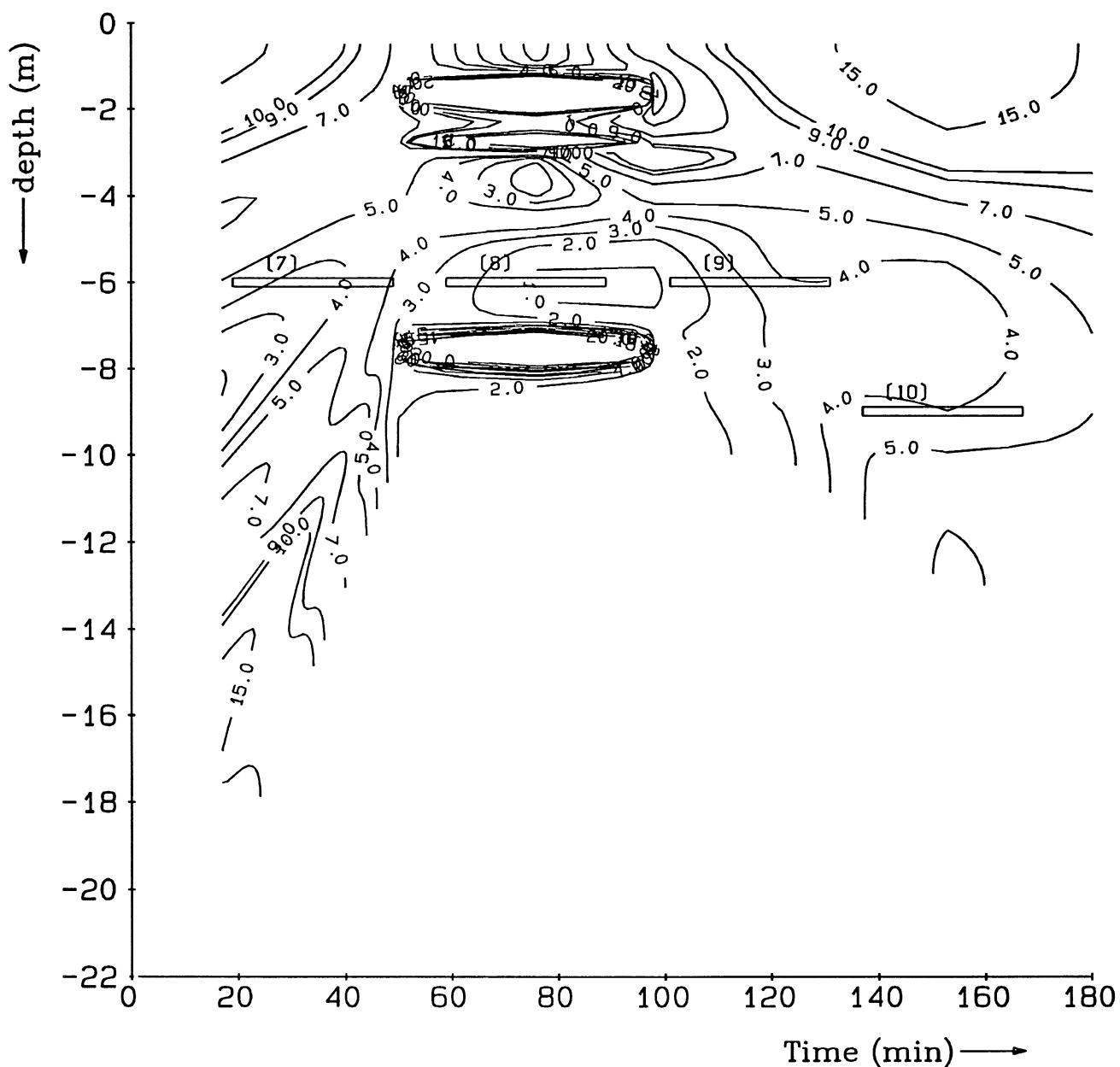
Z 694

Fig. 9<sup>b</sup>



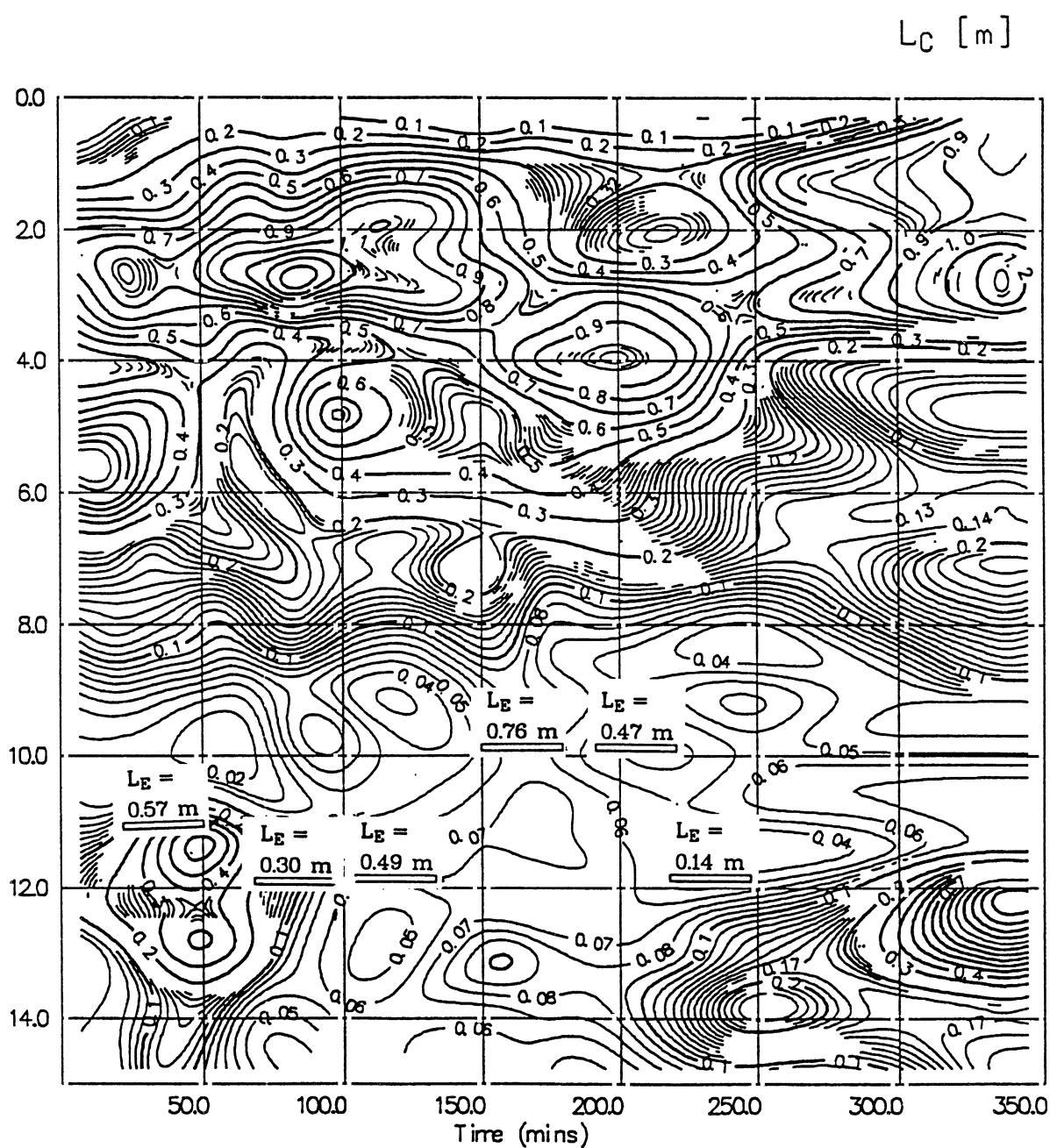
Buoyancy frequency squared. Coland channel  
on day 157 [CWR].

time origin: 92 yrs; 157 days; 534 mins.  
Ri [-]

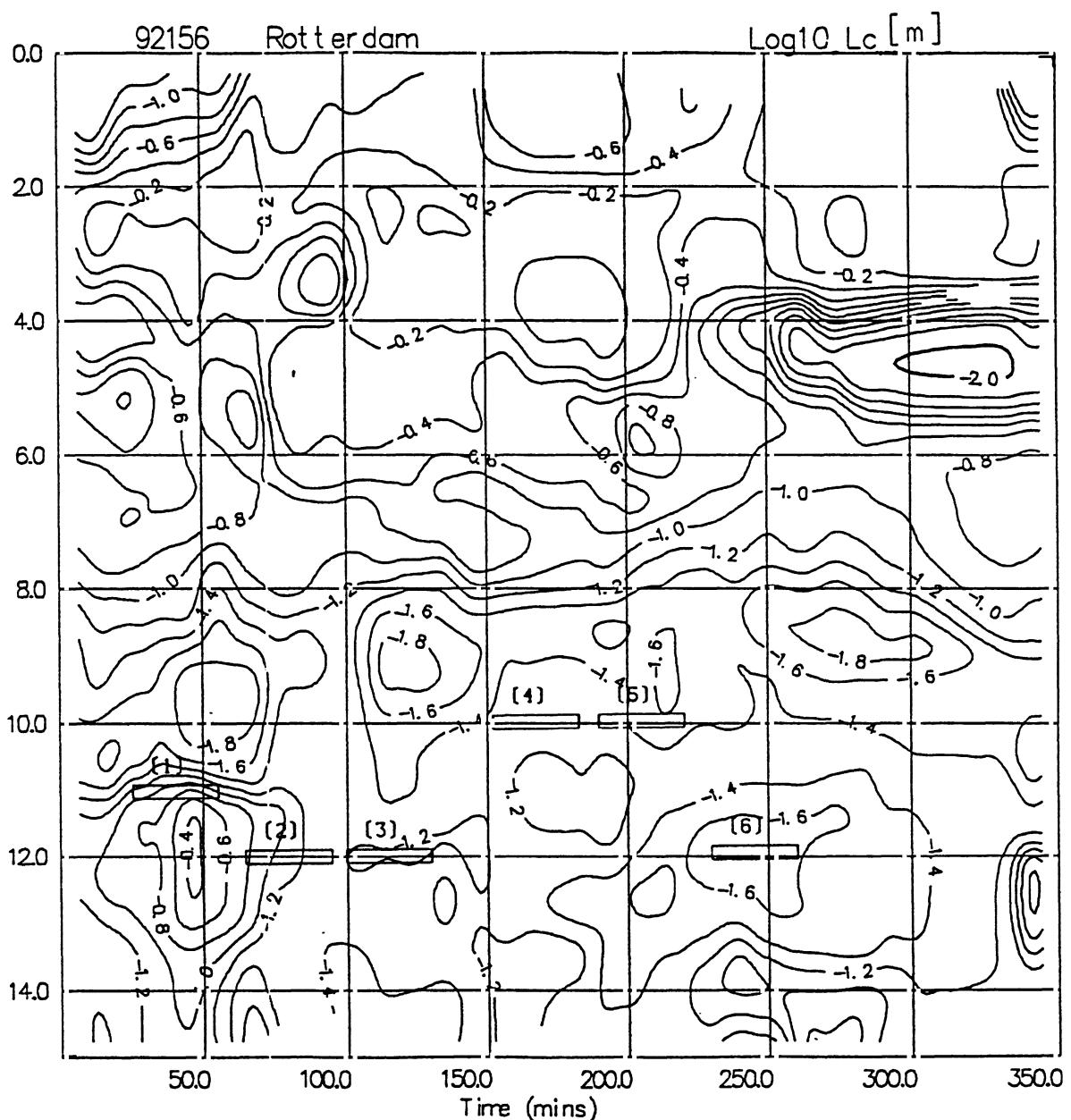


Gradient Richardson number. Caland channel  
on day 157 [RWS].

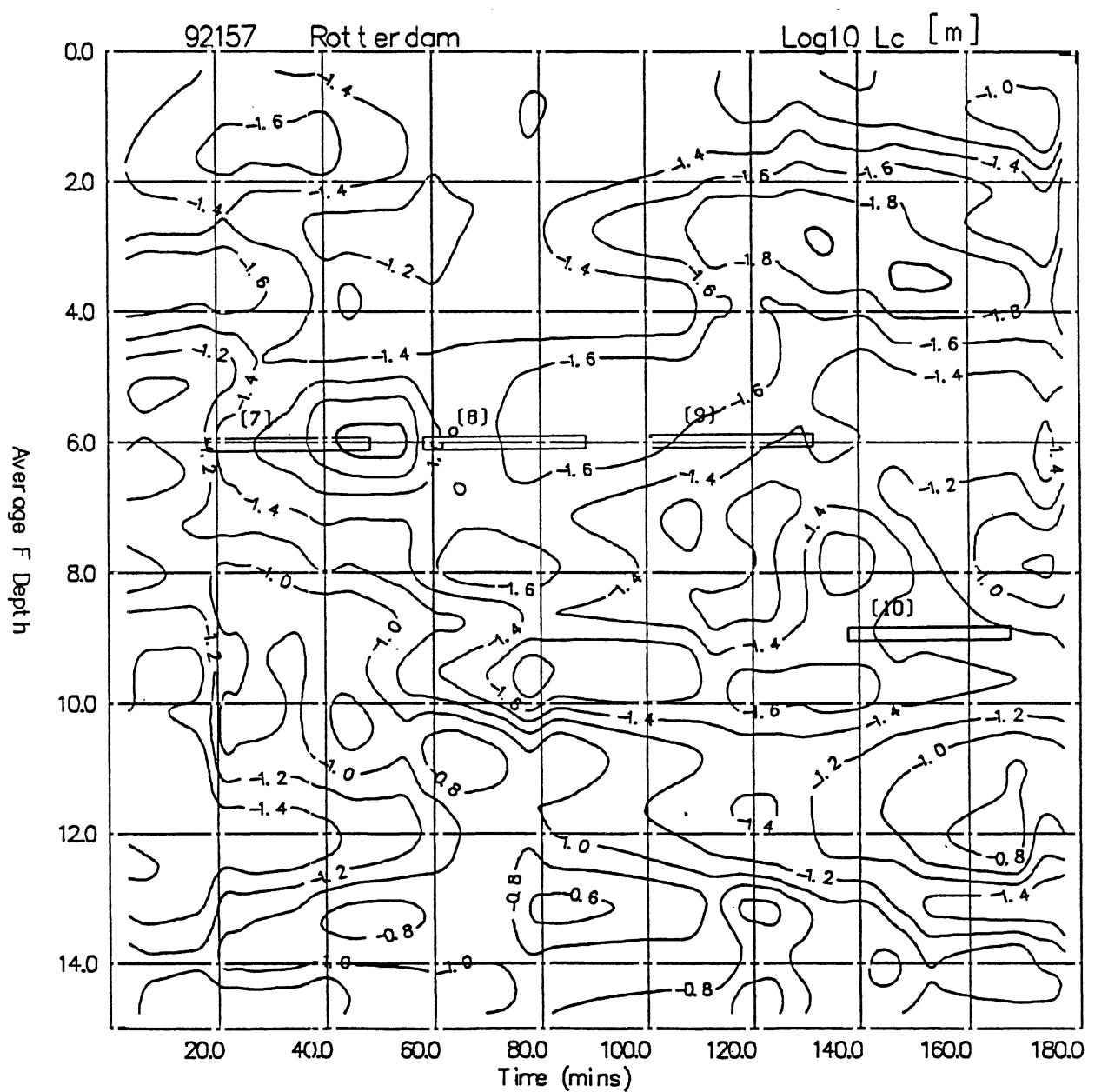
ri157.iso



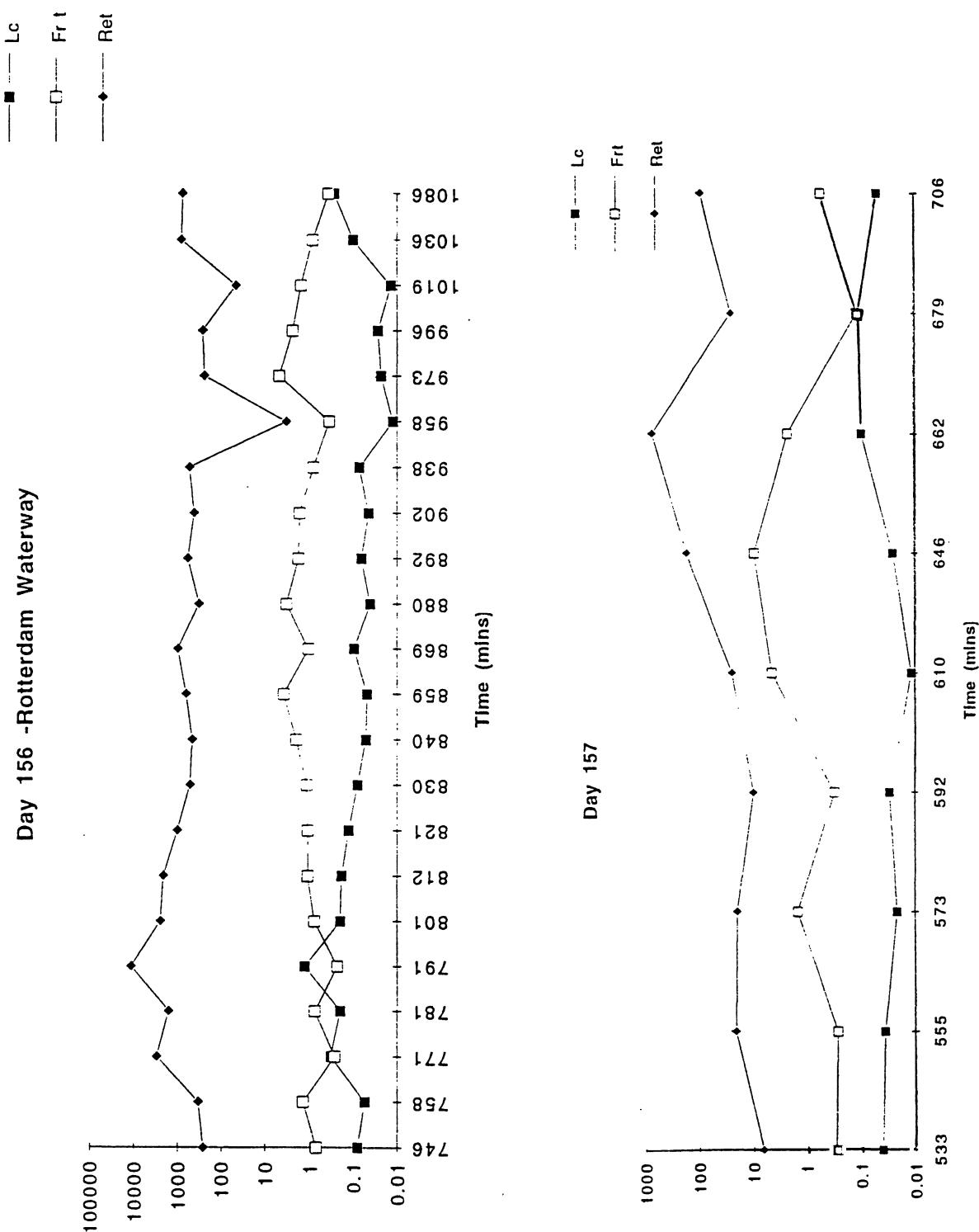
Centered displacement scale  $L_C$ . Rotterdam  
Waterway on day 156 [CWR].



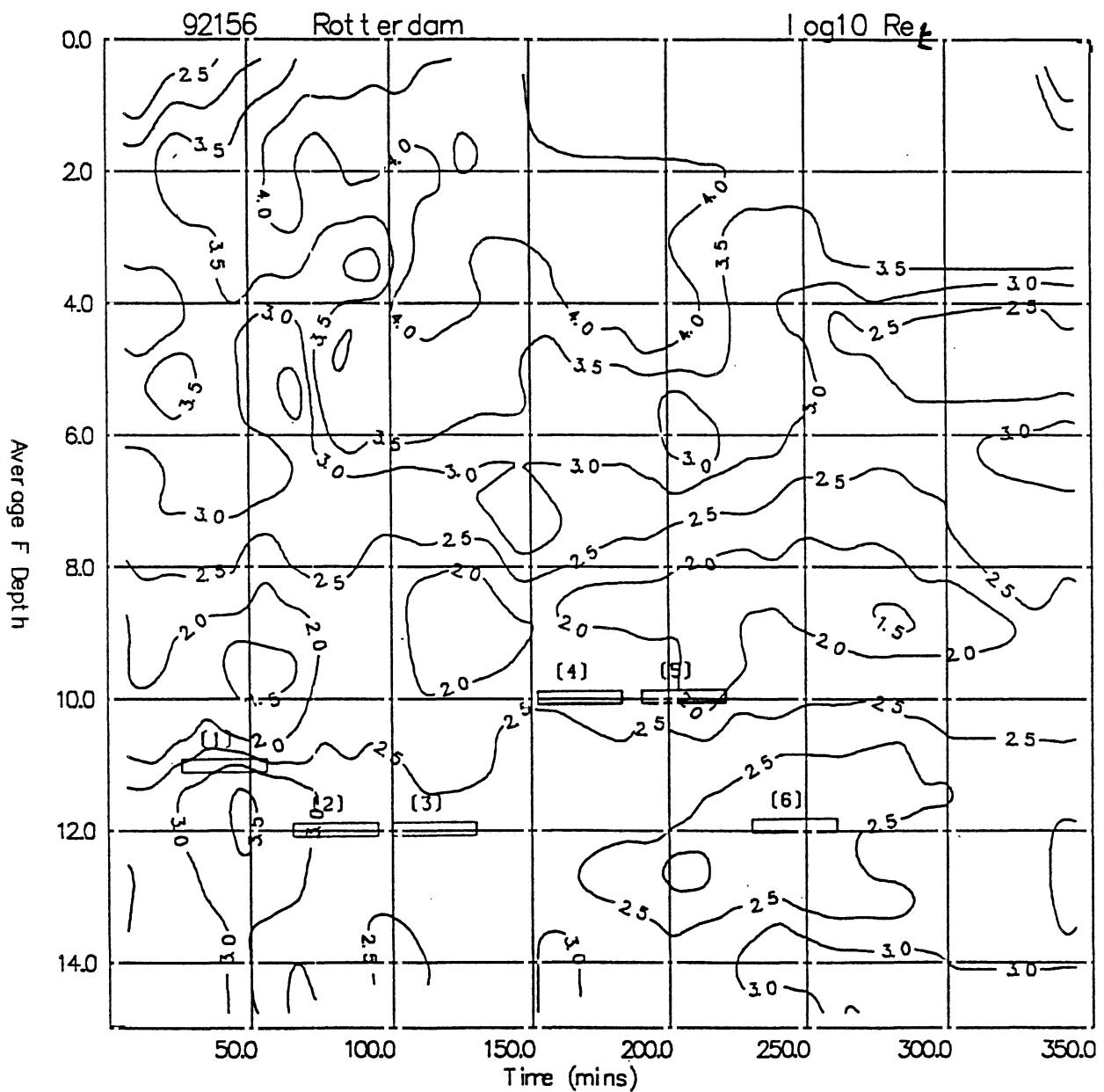
Centered displacement scale  $L_c$ . Rotterdam  
Waterway on day 156 [CWR].



Centered displacement scale  $L_c$ . Caland  
channel on day 157 [CWR].



L<sub>c</sub>, L<sub>E</sub>, Fr<sub>t</sub> and Ret at or near the platform.  
Rotterdam Waterway and Caland channel (CWR).



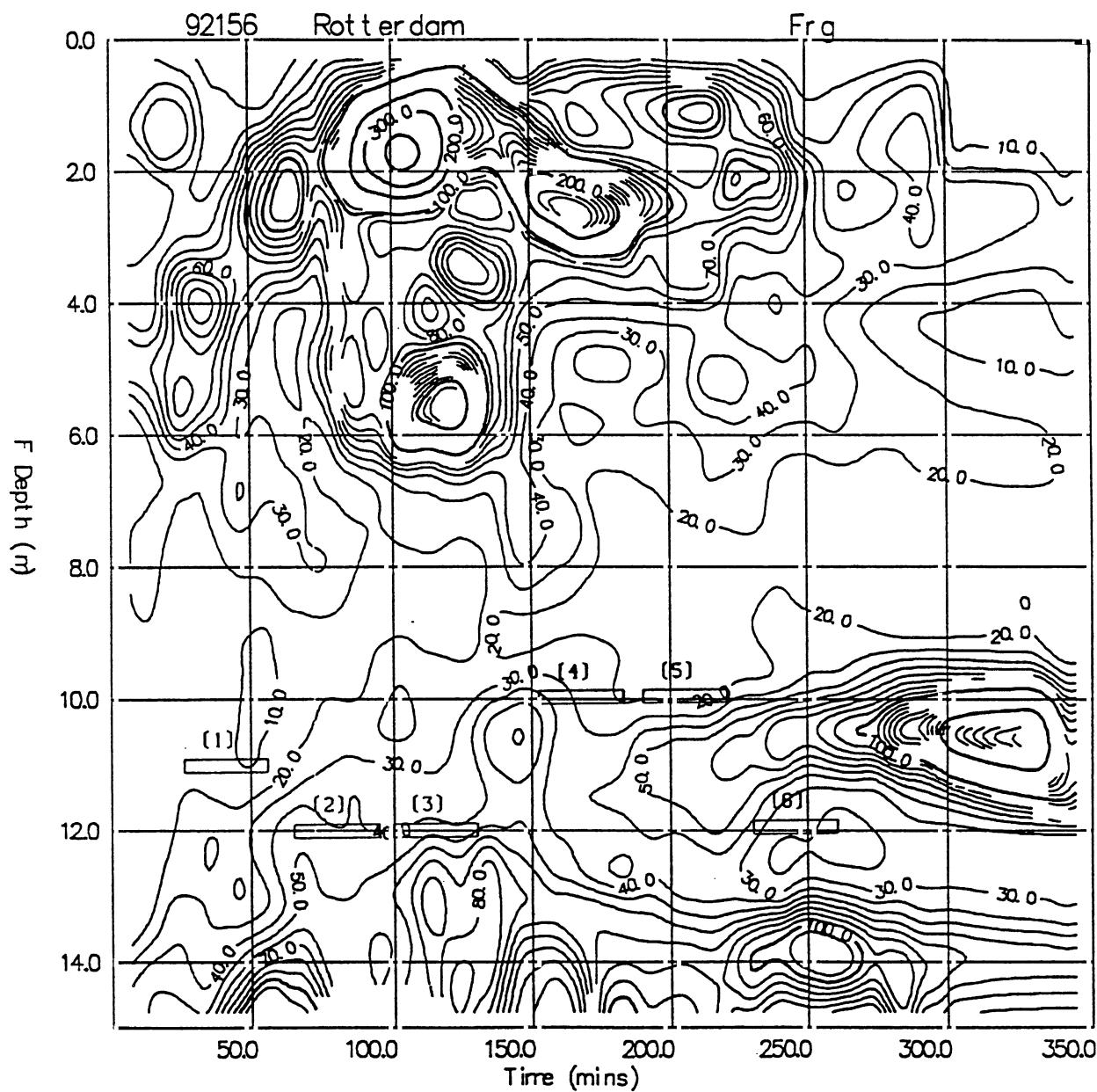
Turbulent Reynolds number  $Re_f$ .

Rotterdam Waterway [CWR].

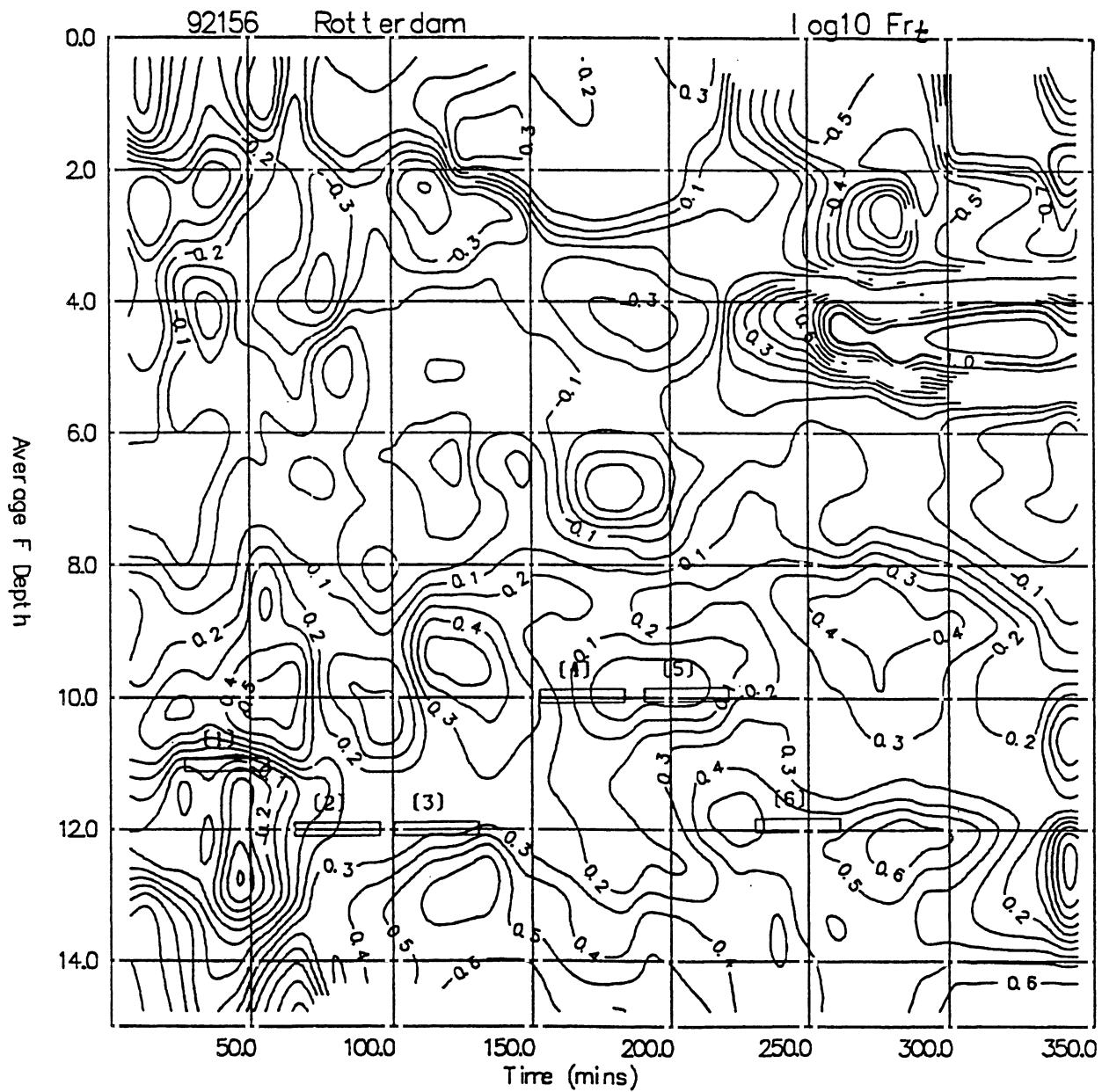
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Z 694

Fig. 15



Small-scale Froude number  $Frg$ .  
Rotterdam Waterway [CWR].

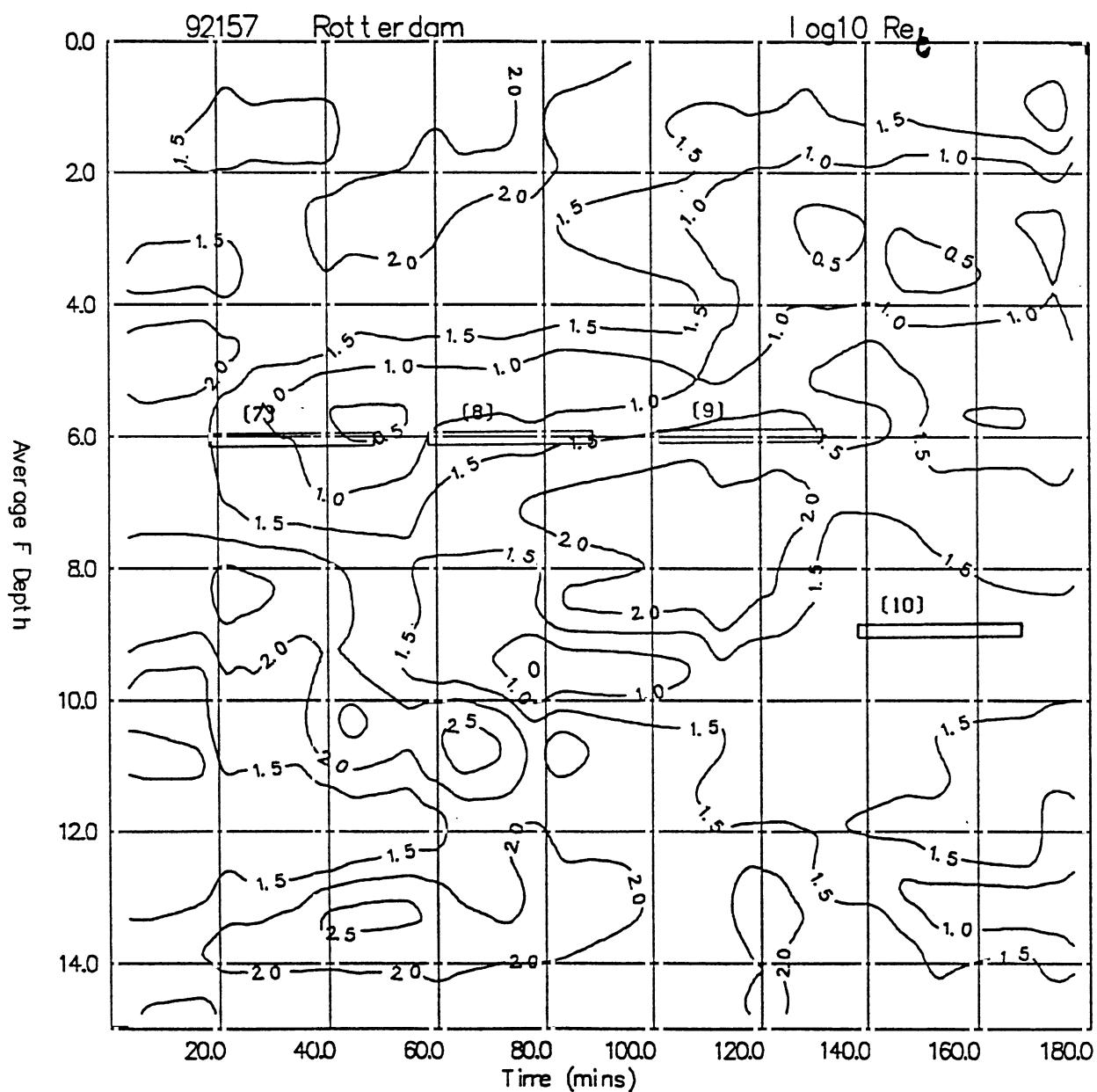


Turbulent Froude number  $Fr_t$ .  
Rotterdam Waterway [CWR].

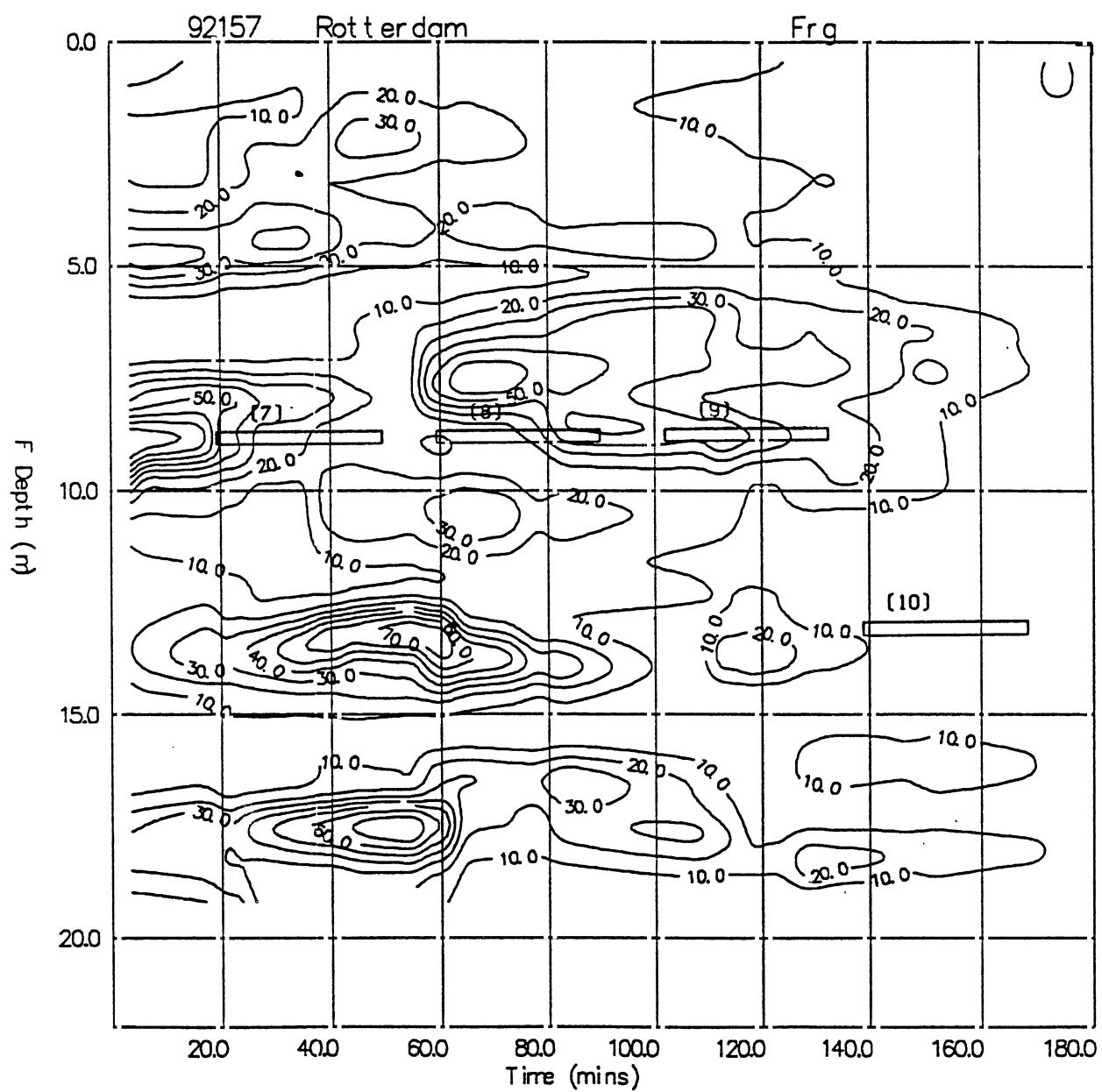
DELFT HYDRAULICS

Z 694

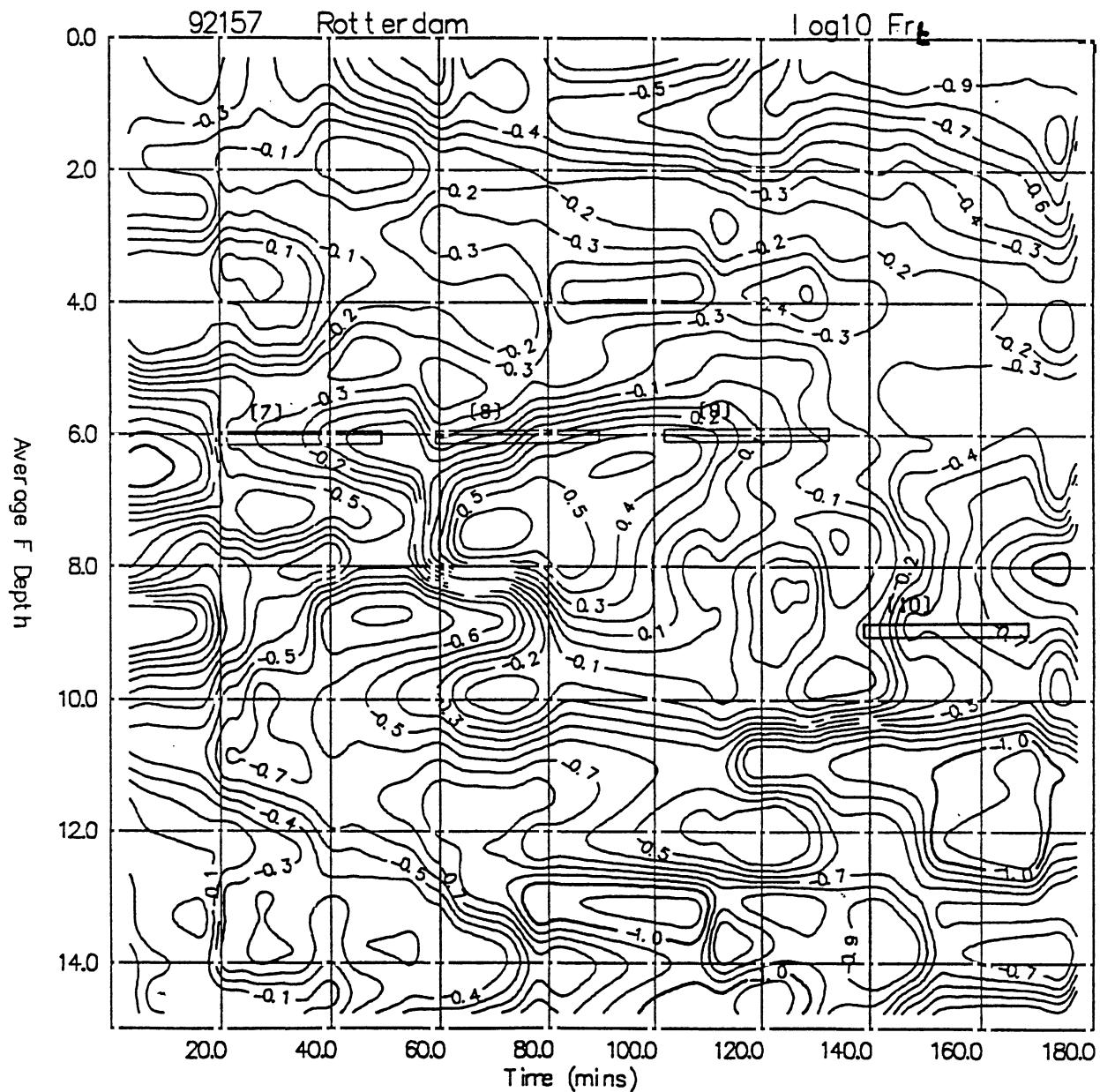
Fig. 17



Turbulent Reynolds number  $Re_t$ .  
Caland channel [CWR].

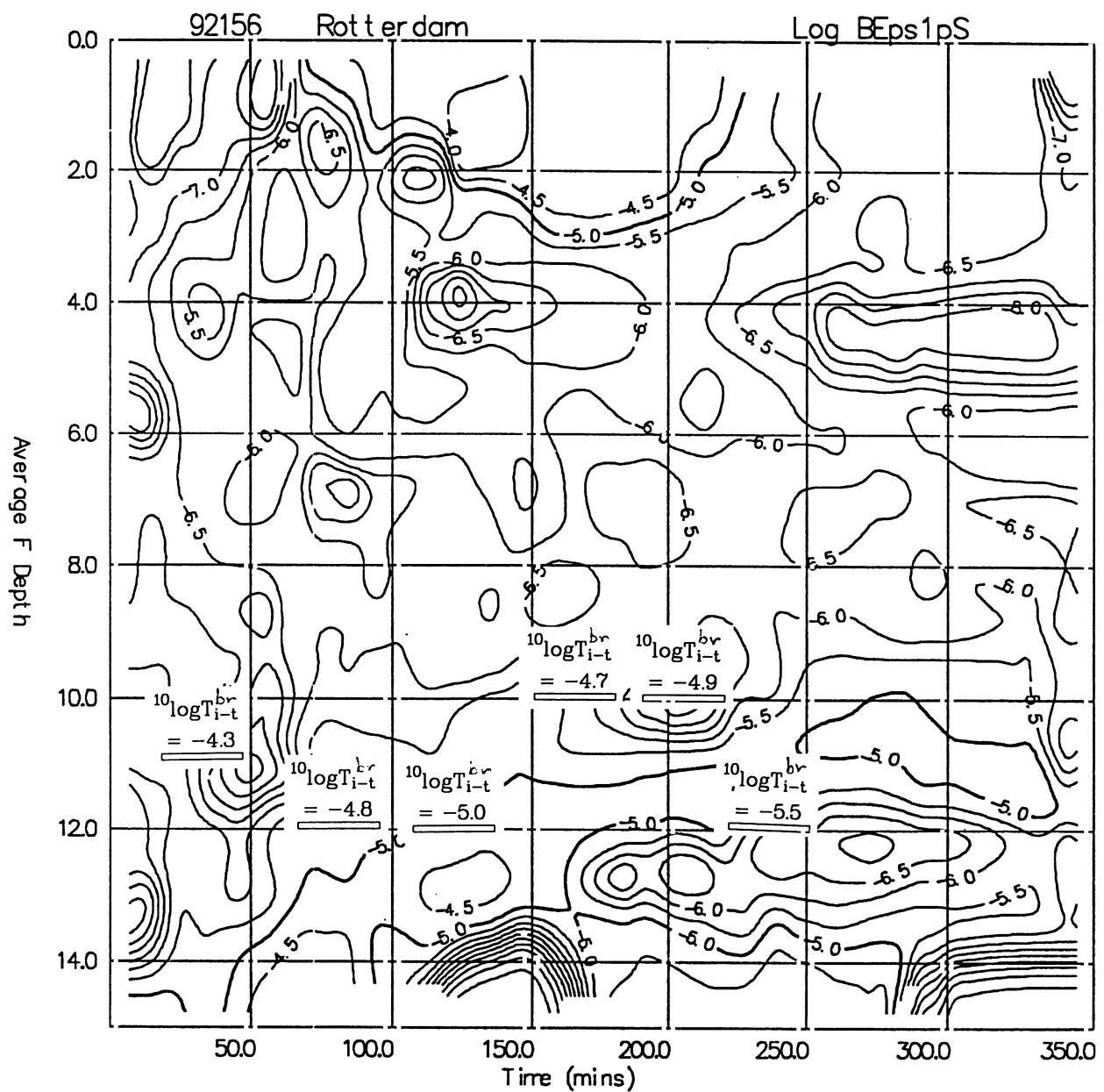


Small-scale Froude number  $F_{rg}$ .  
Caland channel [CWR].

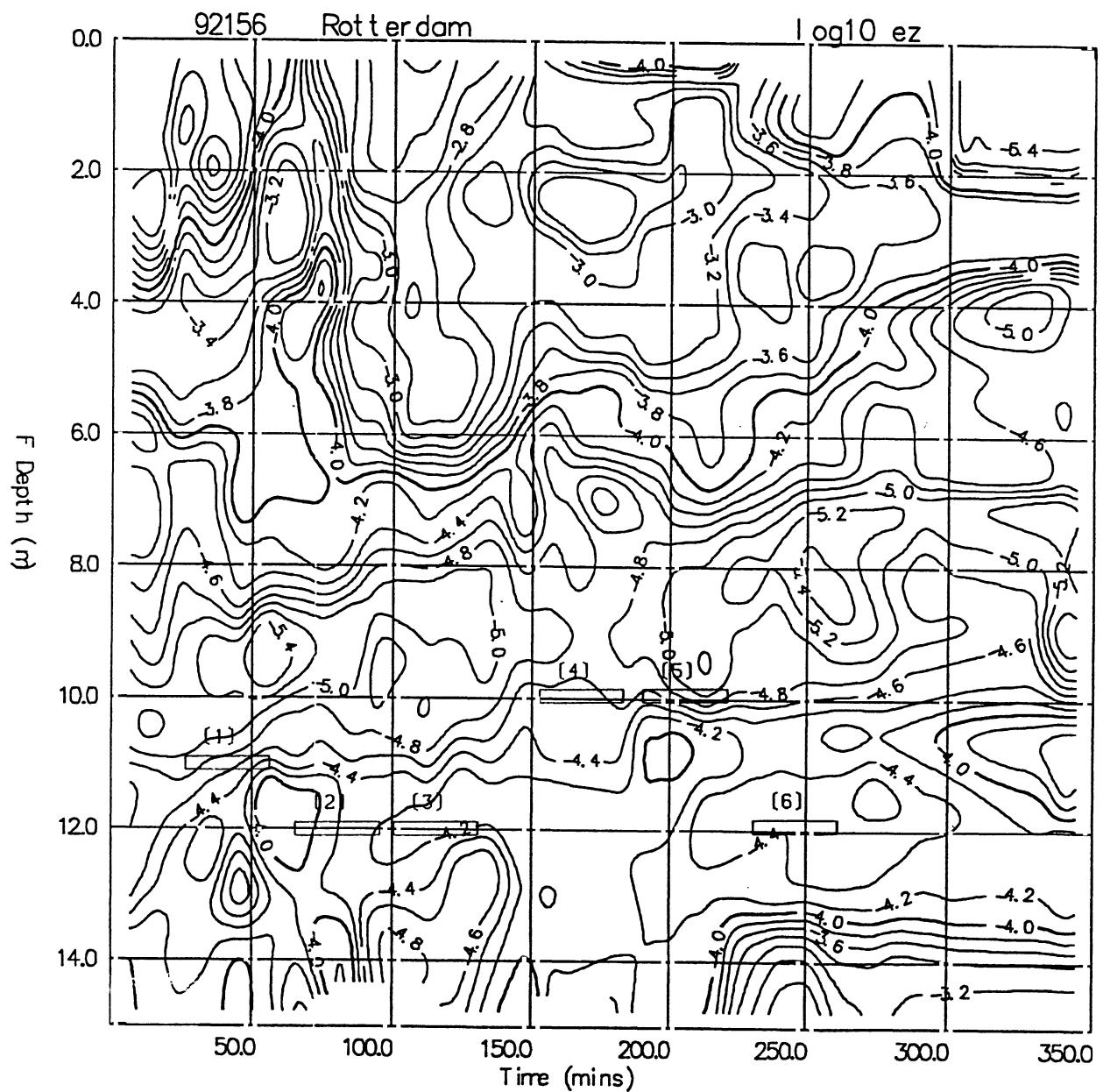


Turbulent Froude number  $Fr_t$ .

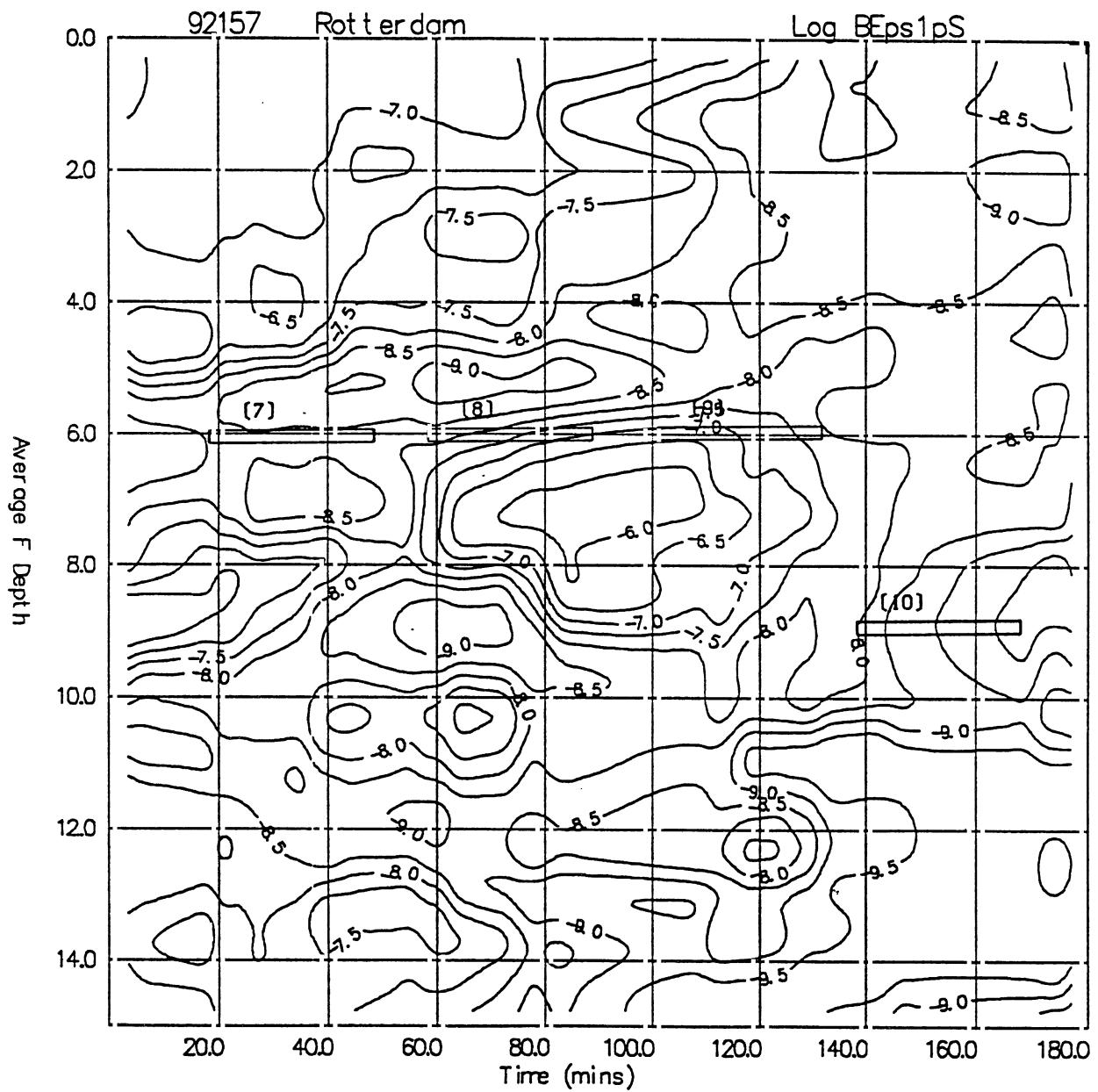
Caland channel [CWR].



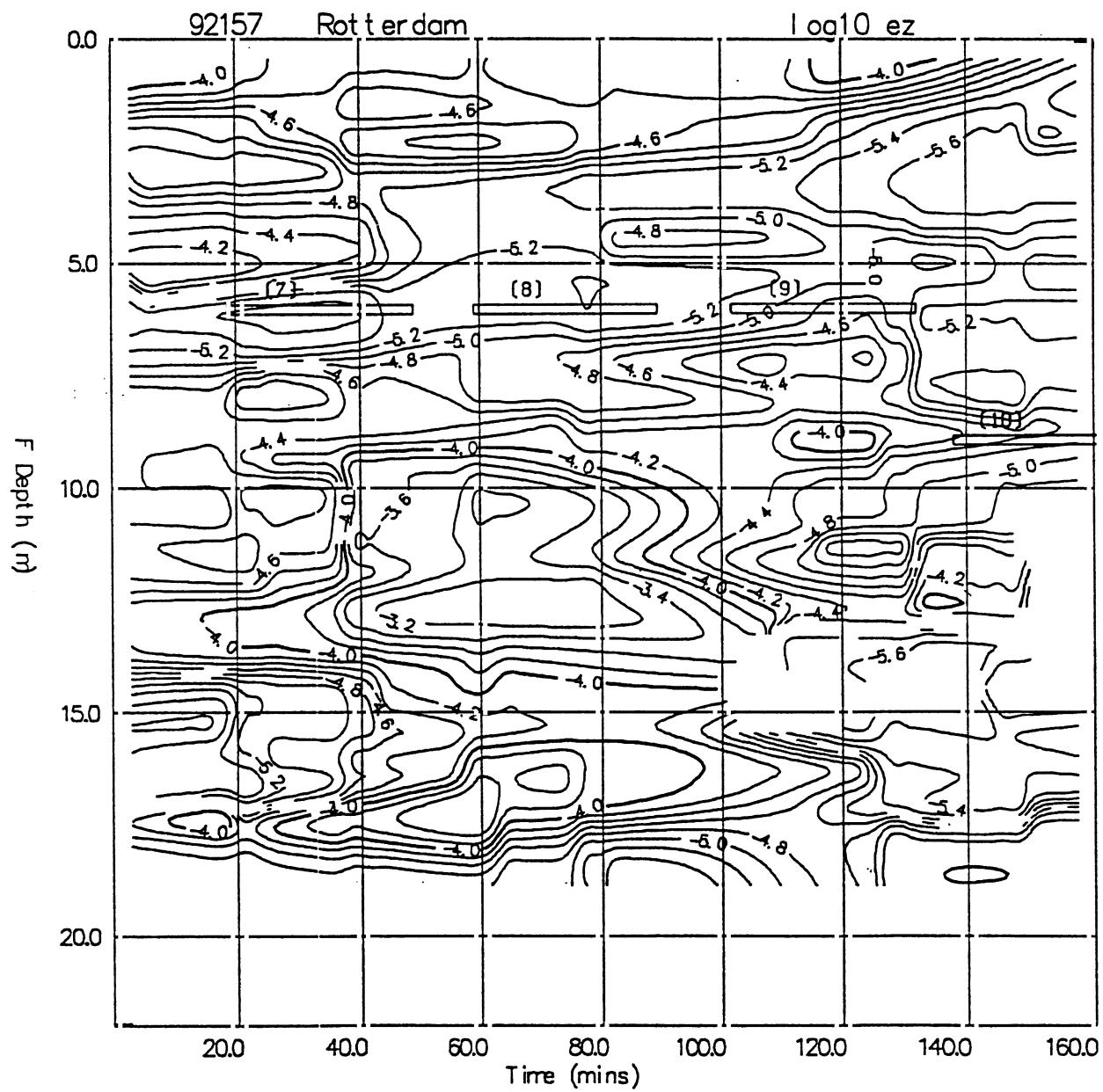
Energy dissipation rate from Batchelor spectra.  
Rotterdam Waterway, day 156 [CWR].



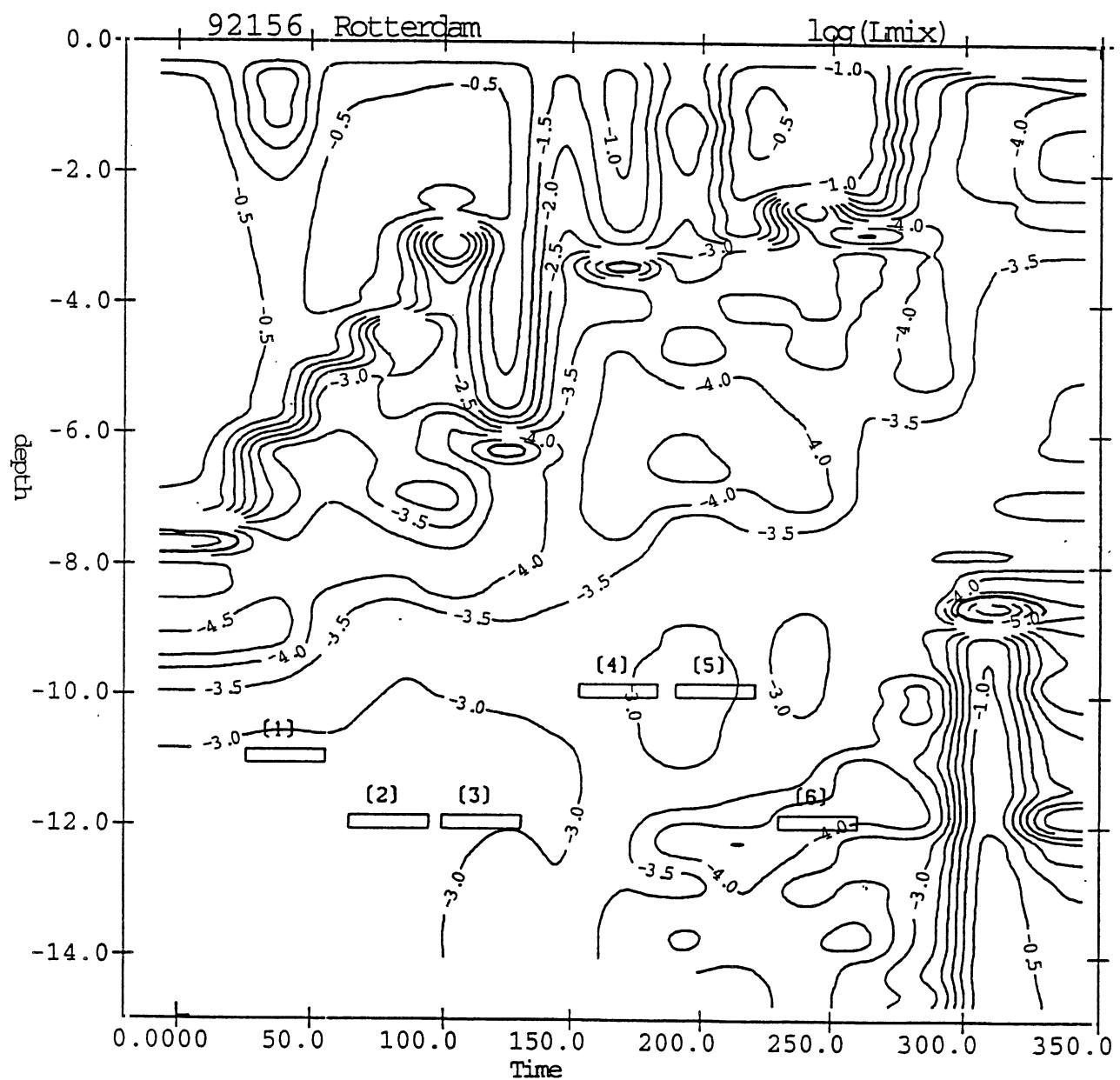
Eddy diffusivity.  
Rotterdam Waterway, day 156 [CWR].



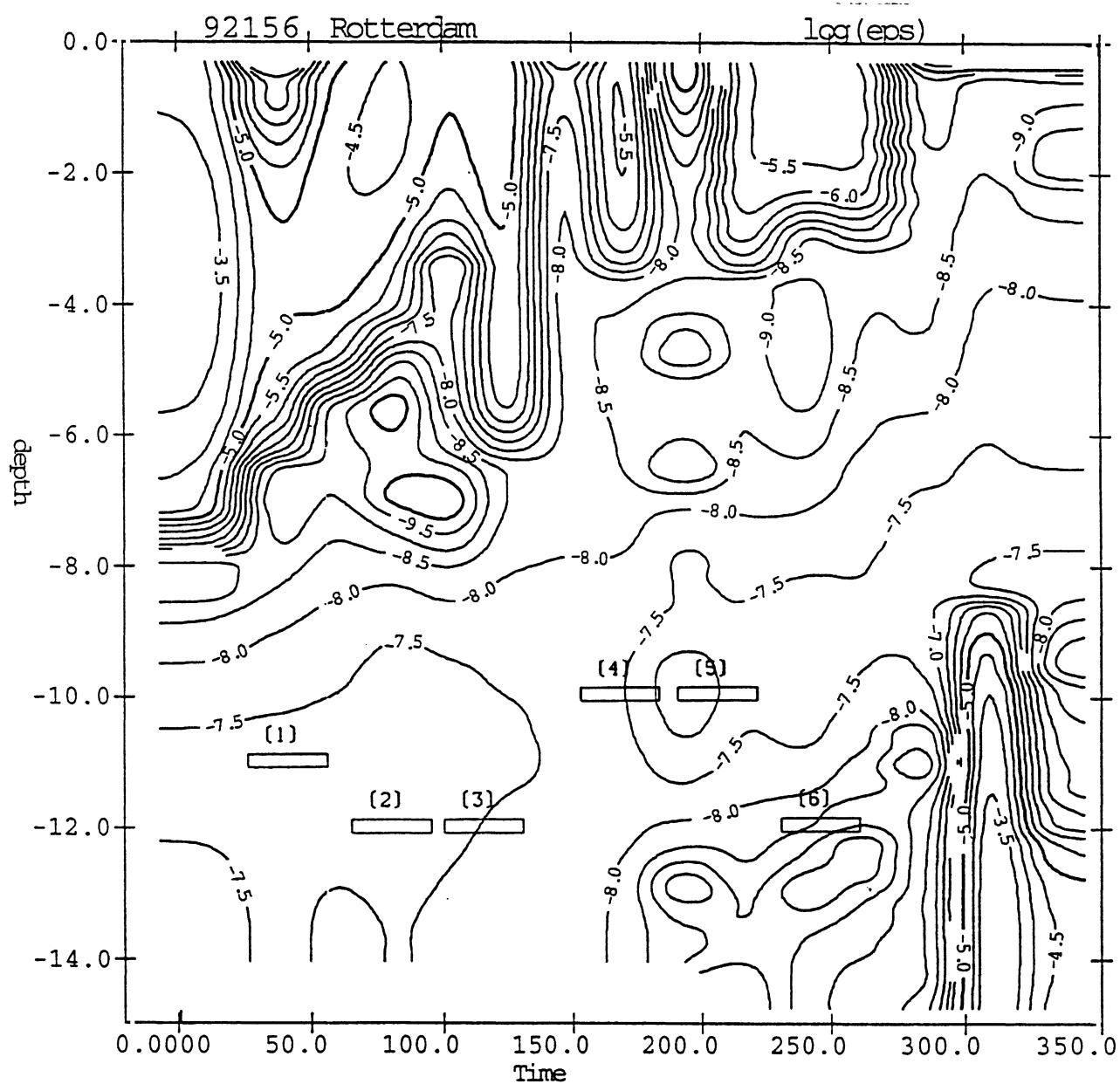
Energy dissipation rate from Batchelor spectra.  
Caland channel, day 157 [CWR].



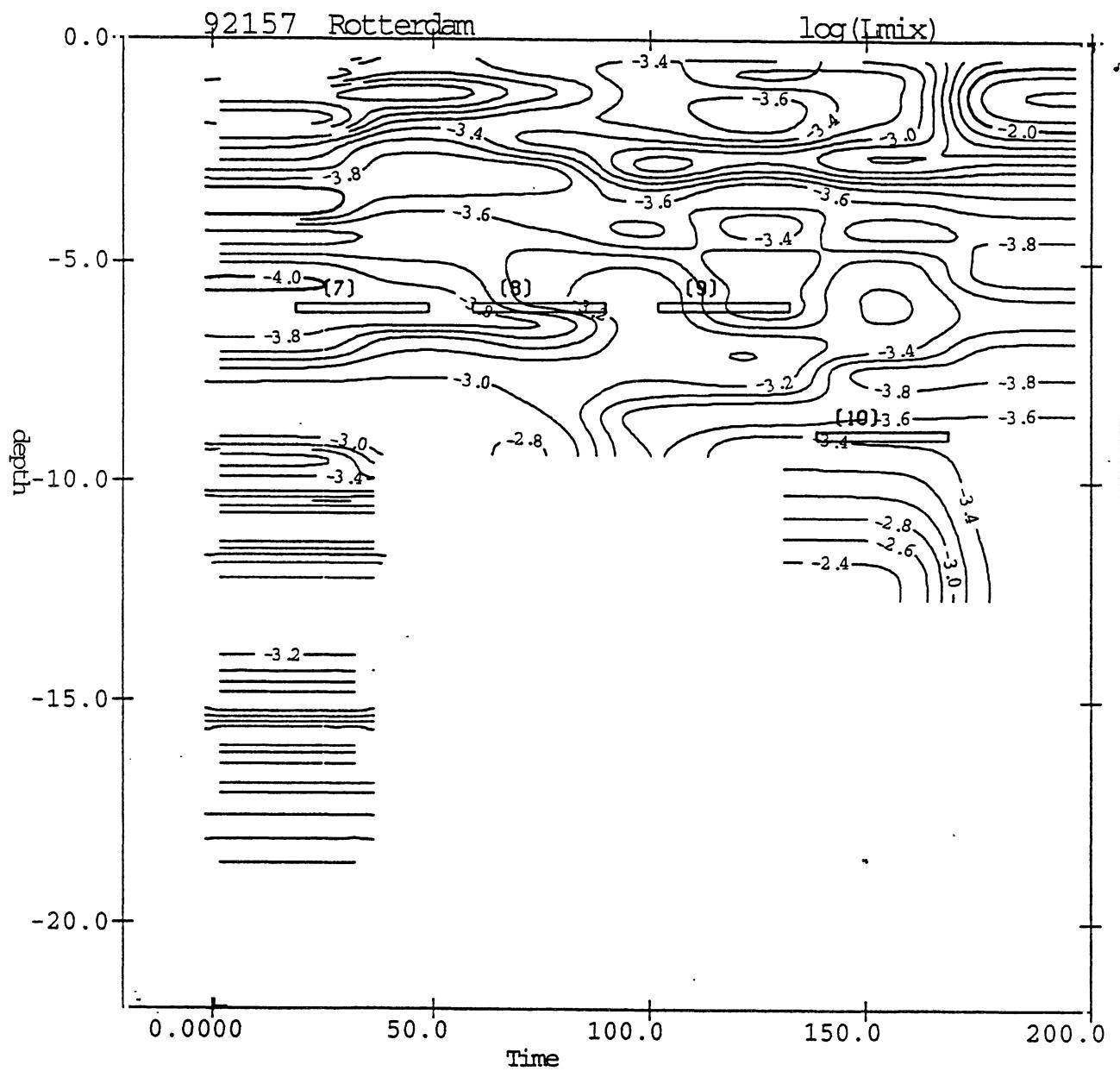
Eddy diffusivity.  
Caland channel, day 157 [CWR].



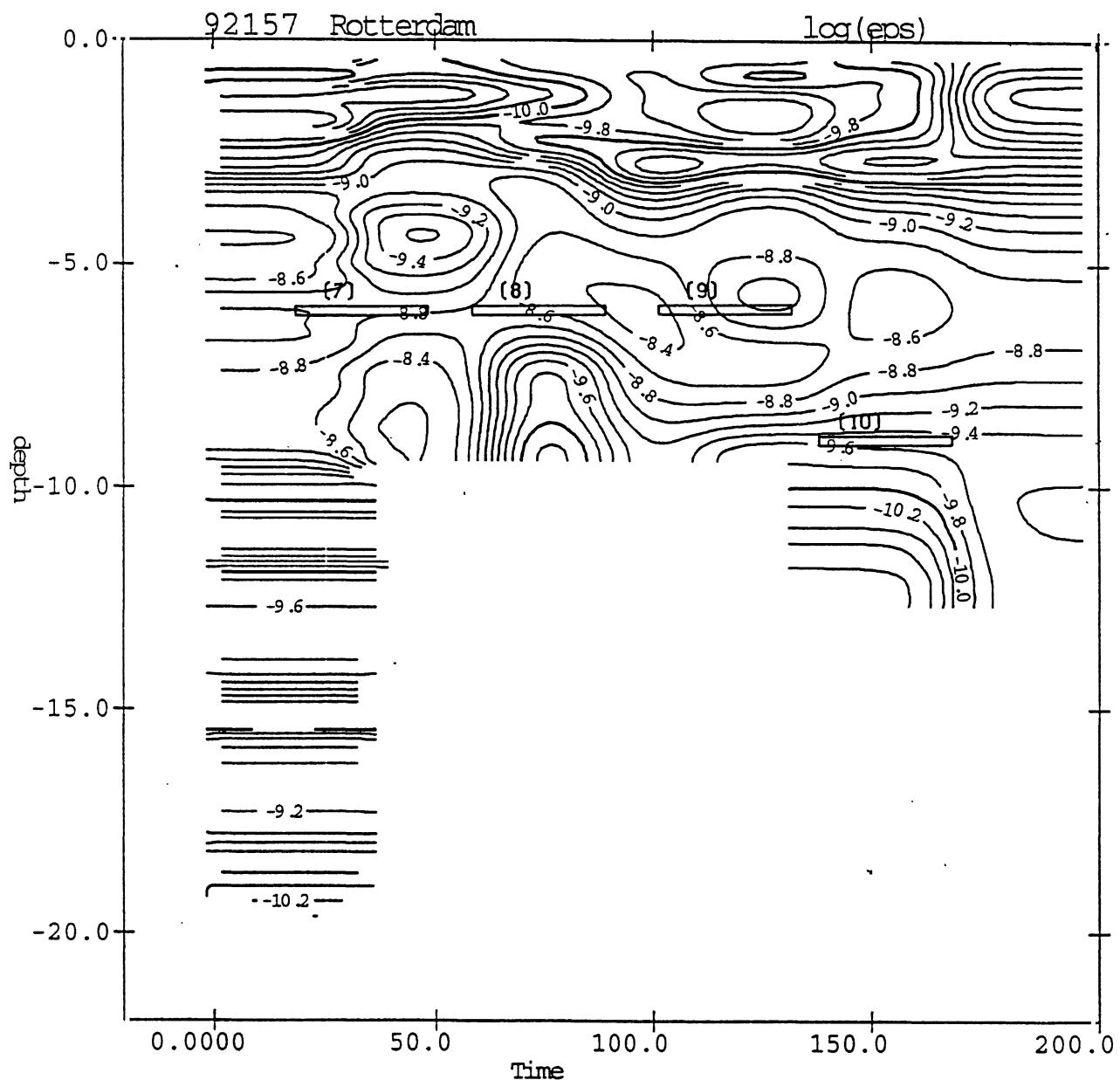
Mixing length ; 1DV  $q^2-\varepsilon$  turbulence model.  
Rotterdam Waterway, day 156.



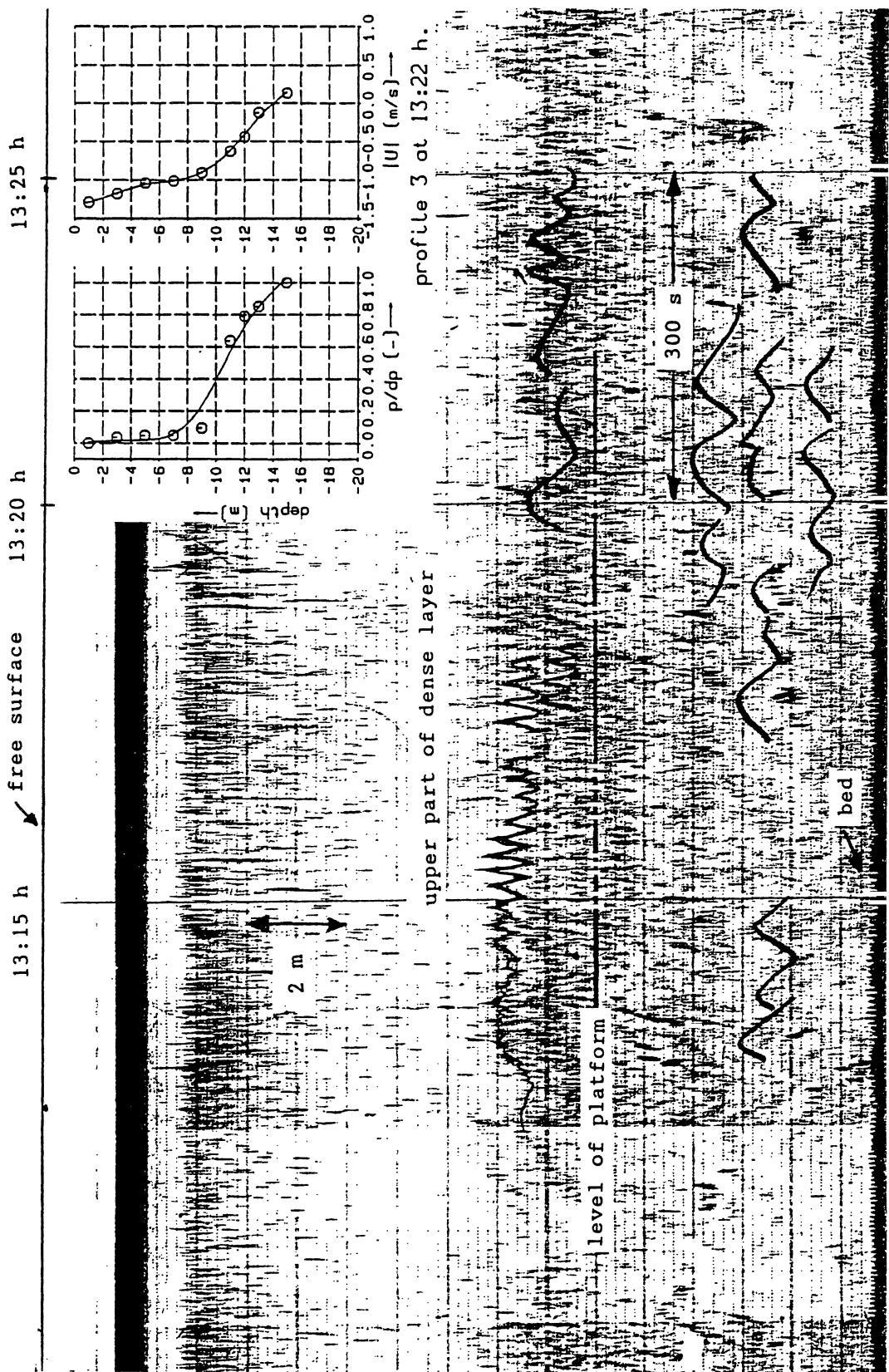
Energy dissipation ; 1DV  $q^2-\varepsilon$  turbulence model.  
Rotterdam Waterway, day 156.



Mixing length ; 1DV  $q^2 - \varepsilon$  turbulence model.  
 Caland channel, day 157.



Energy dissipation ; 1DV  $q^2-\epsilon$  turbulence model.  
Caland channel, day 157.

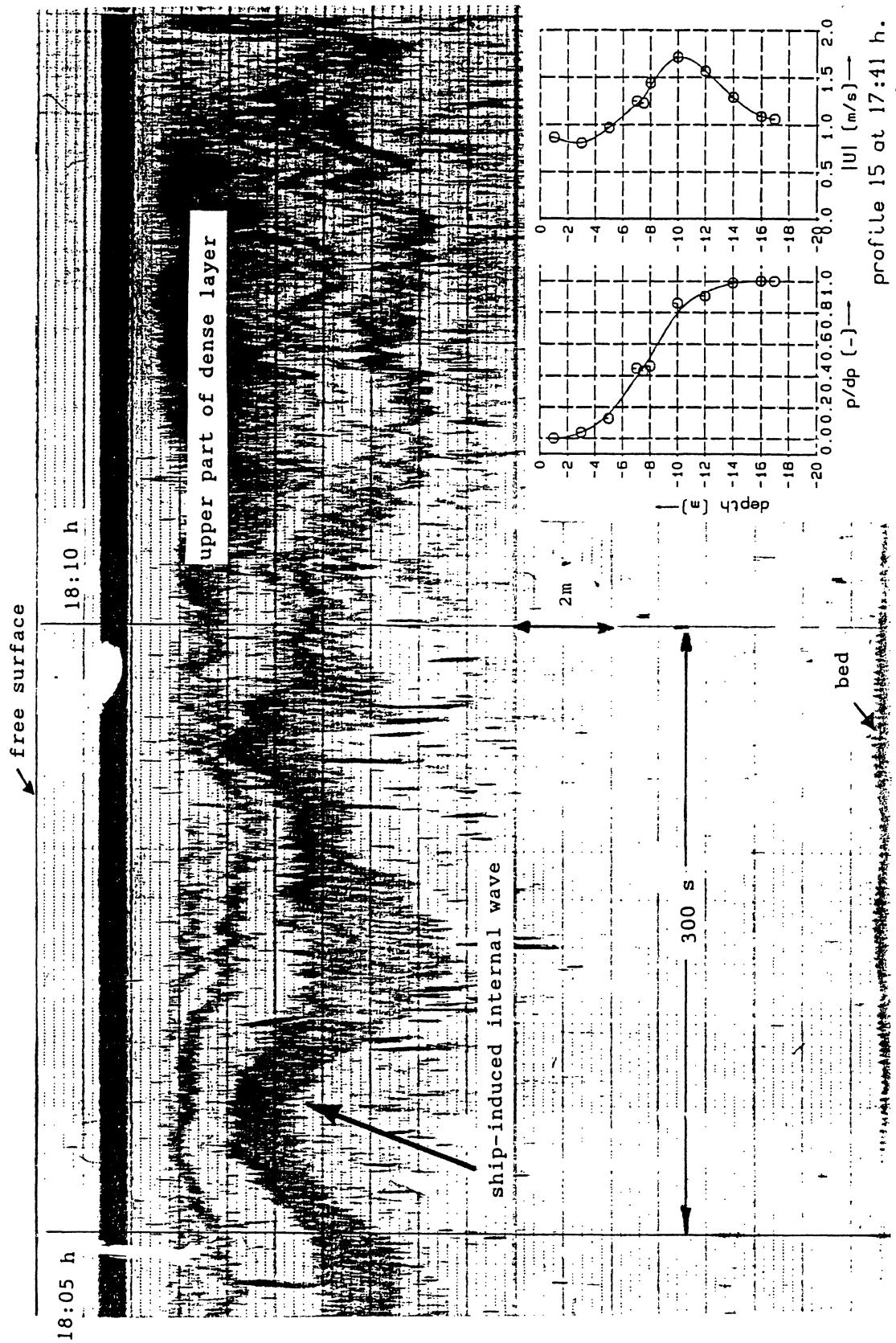


Echosounder observations from the anchored  
Pavo. Rotterdam Waterway on day 156.

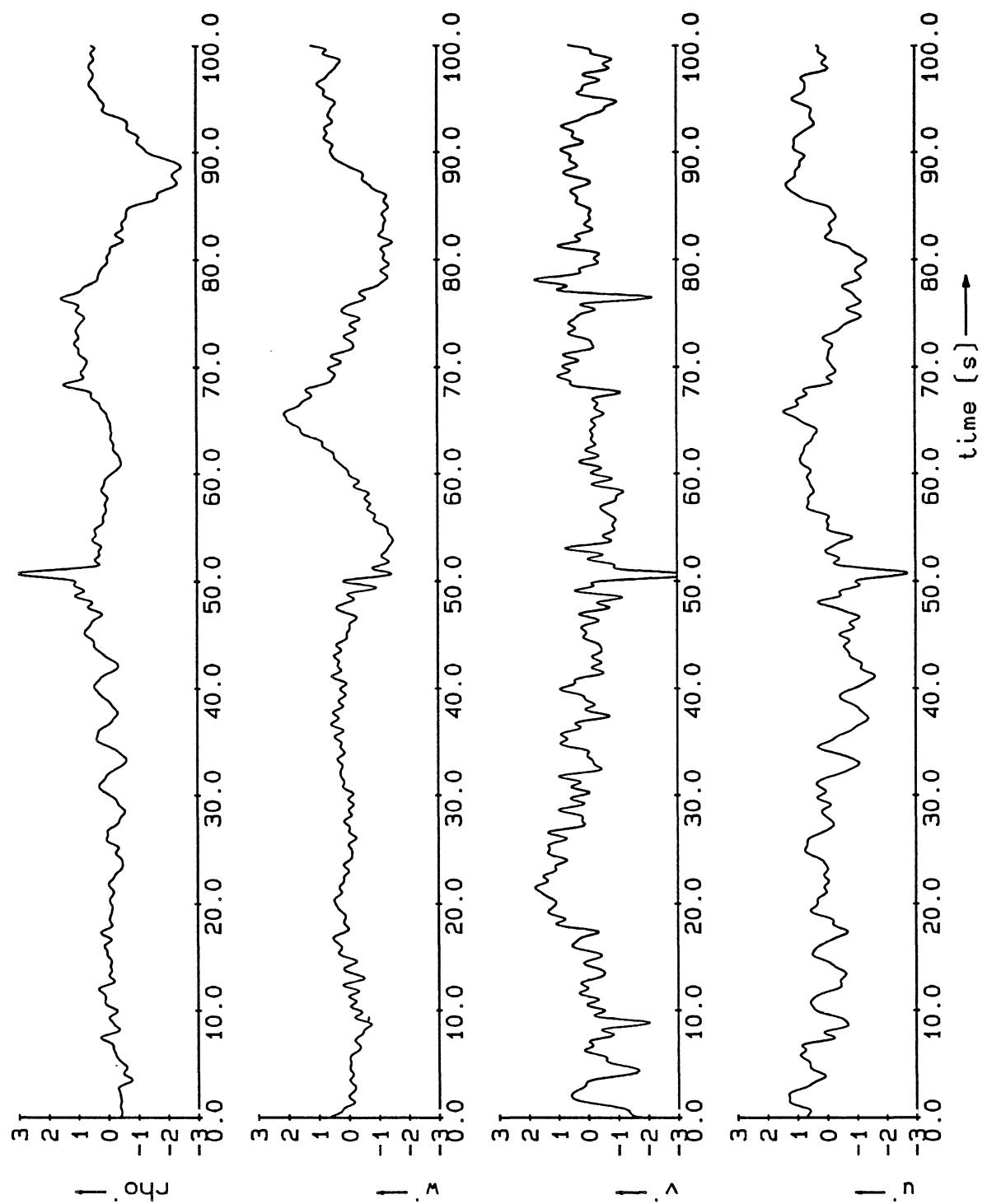
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Z 694

Fig.29



Echosounder recording of a ship-induced internal wave. Rotterdam Waterway on day 156.



Filtered velocity and density signals; normalised,  
corrected for trend and for platform motions.

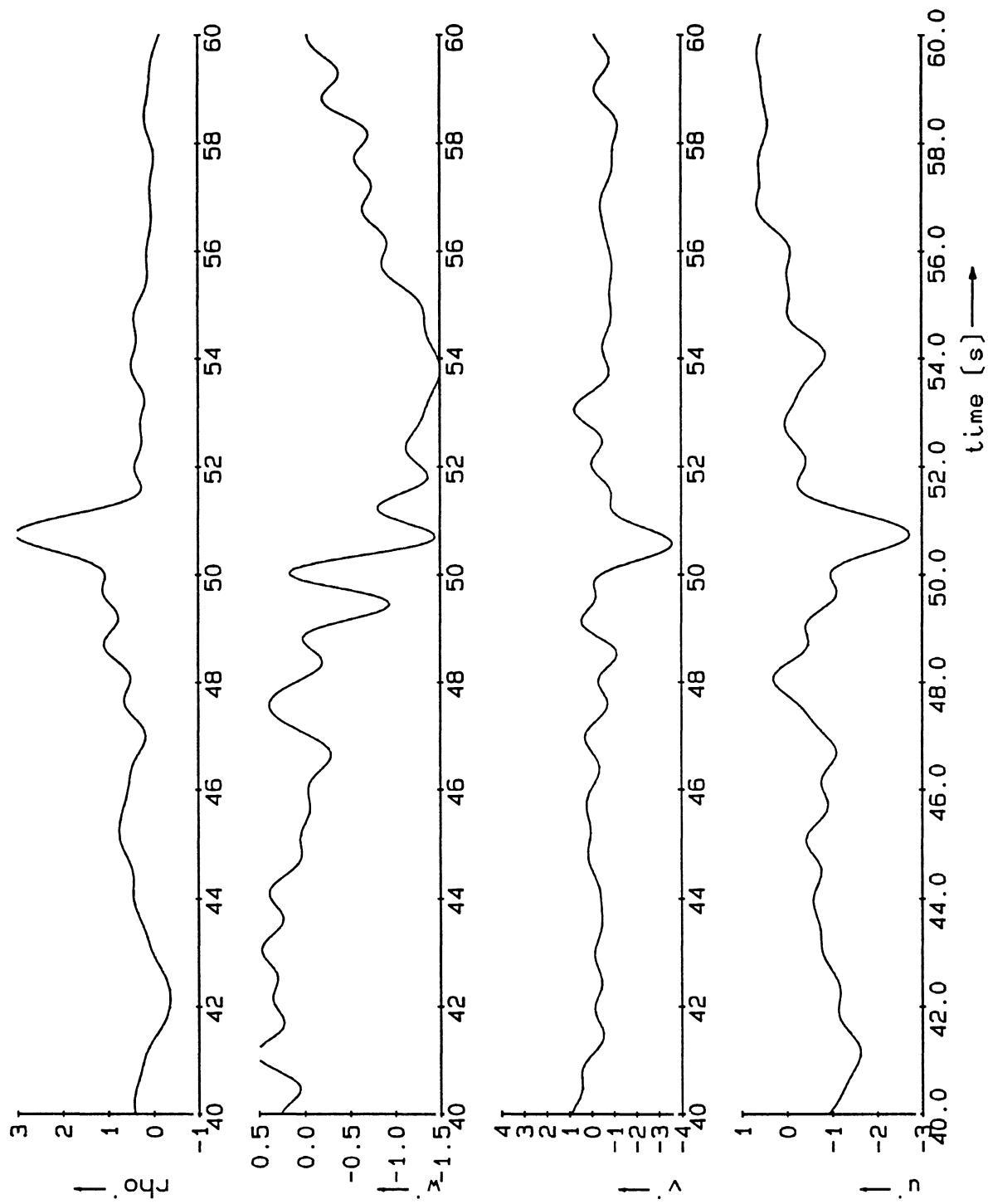
12:53/156 [0;100]

inspect.inv

DELFT HYDRAULICS

Z 694

Fig. 31



Filtered velocity and density signals; normalised,  
corrected for linear trend and for platform motions.

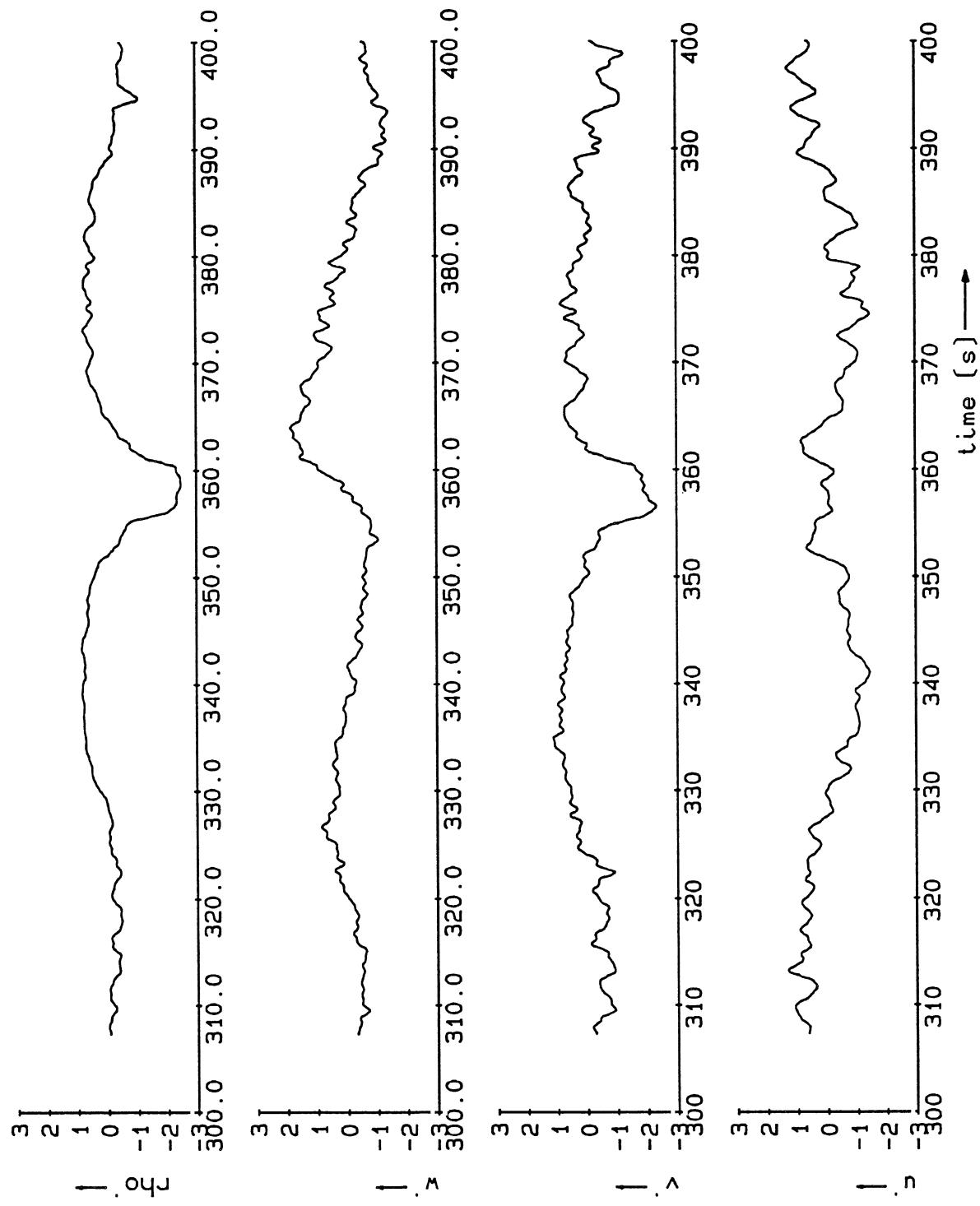
12:53/156 [0;100]

break.inv

DELFT HYDRAULICS

Z 694

Fig. 32



Filtered velocity and density signals; normalised,  
corrected for trend and for platform motions.

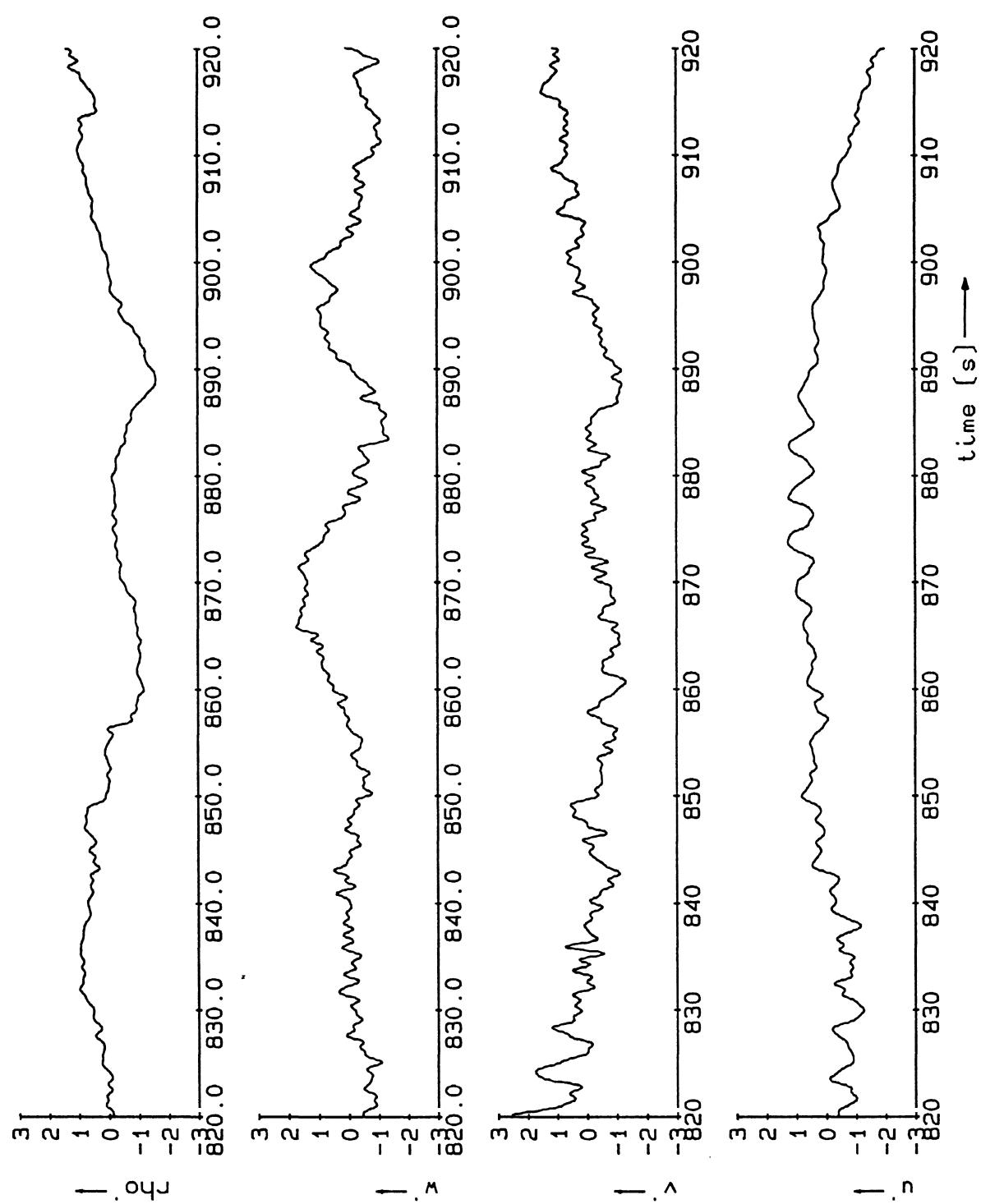
12:53/156 [0;100]

inspt.inv

DELFT HYDRAULICS

Z 694

Fig.33



Filtered velocity and density signals; normalised,  
corrected for trend and for platform motions.

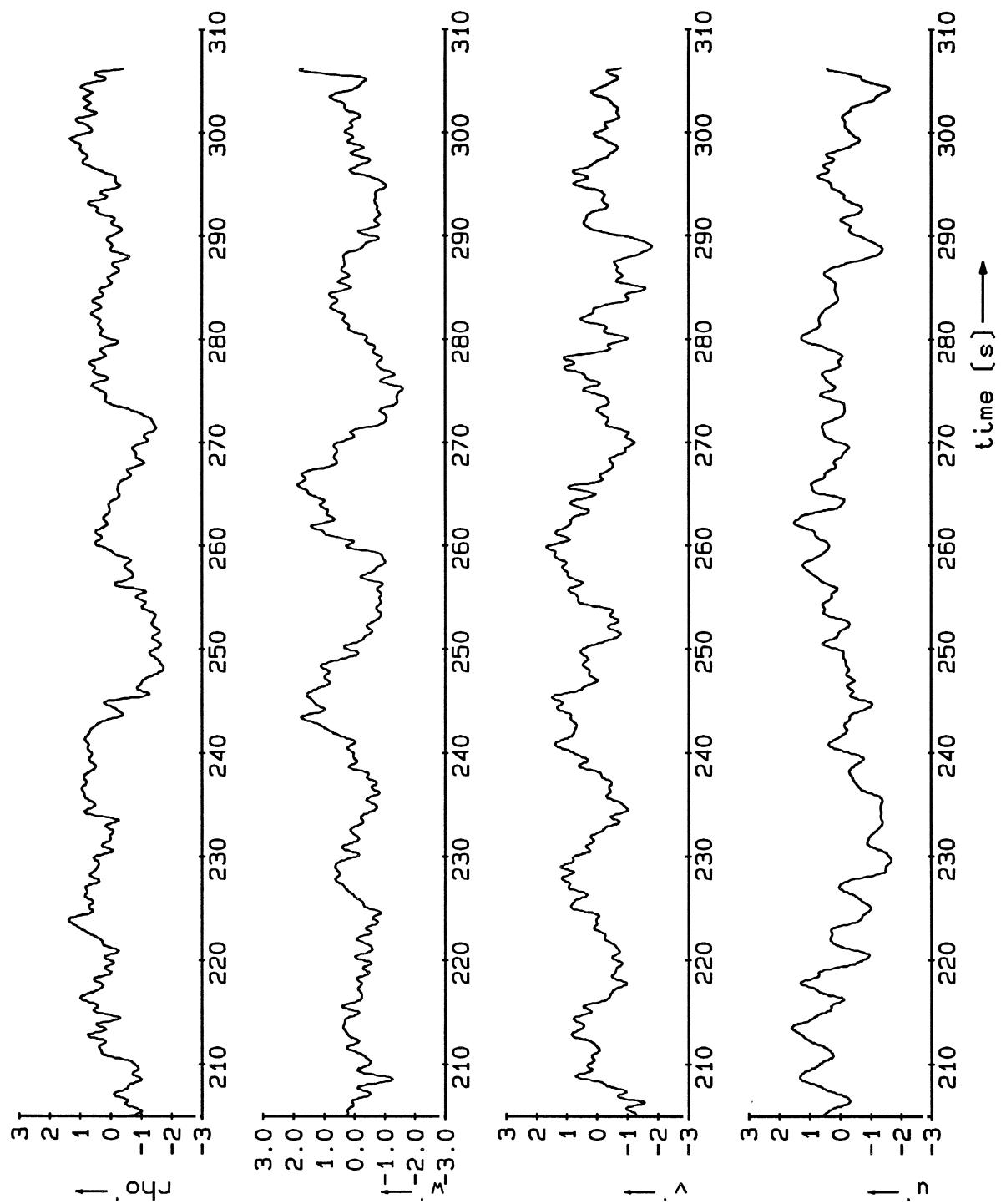
12:53/156 [0;100]

Inspect.inv

DELFT HYDRAULICS

Z 694

Fig.34



Filtered velocity and density signals; normalised,  
corrected for trend and for platform motions.

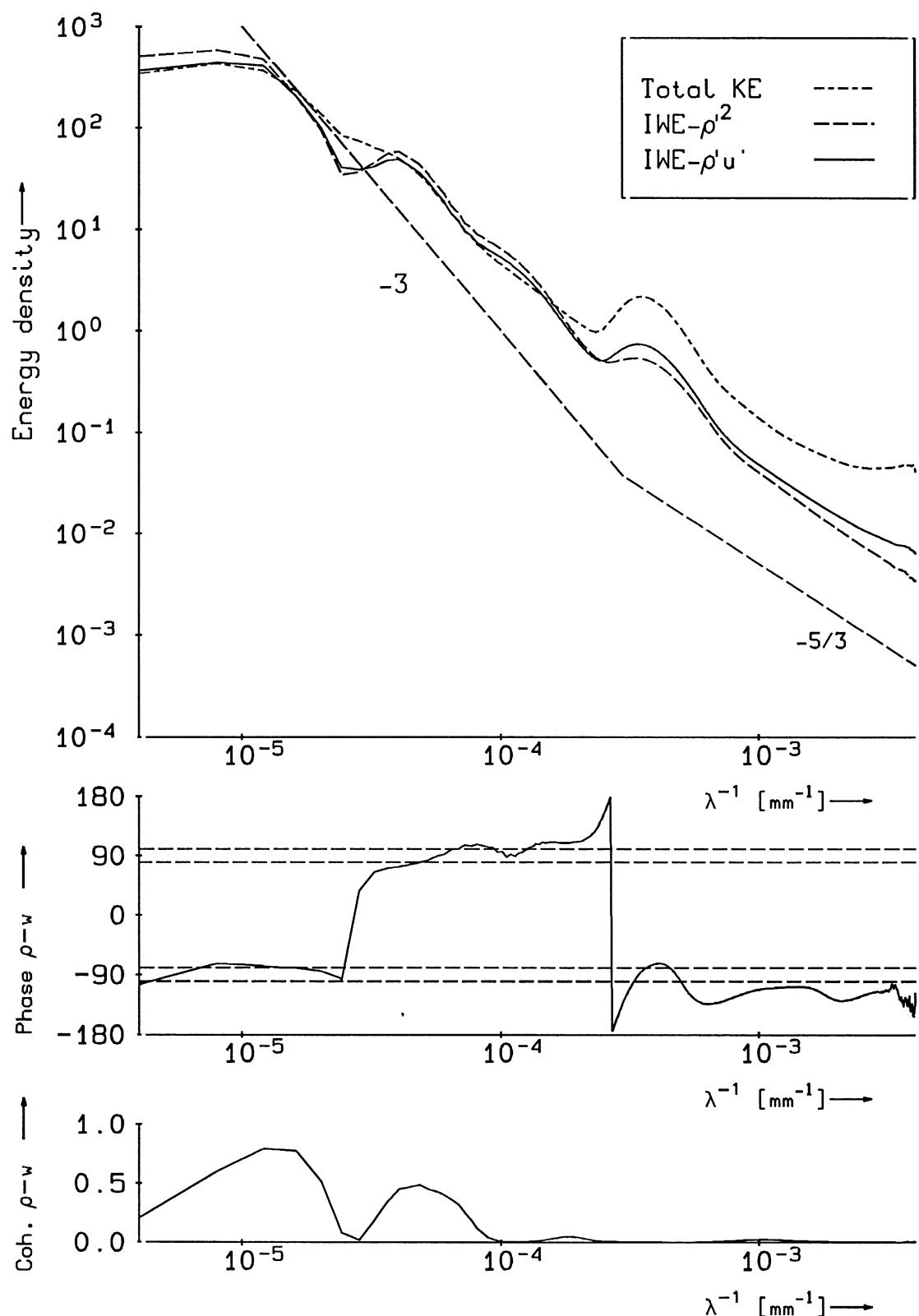
13:32/156 [0;100]

inspect.inv

DELFT HYDRAULICS

Z 694

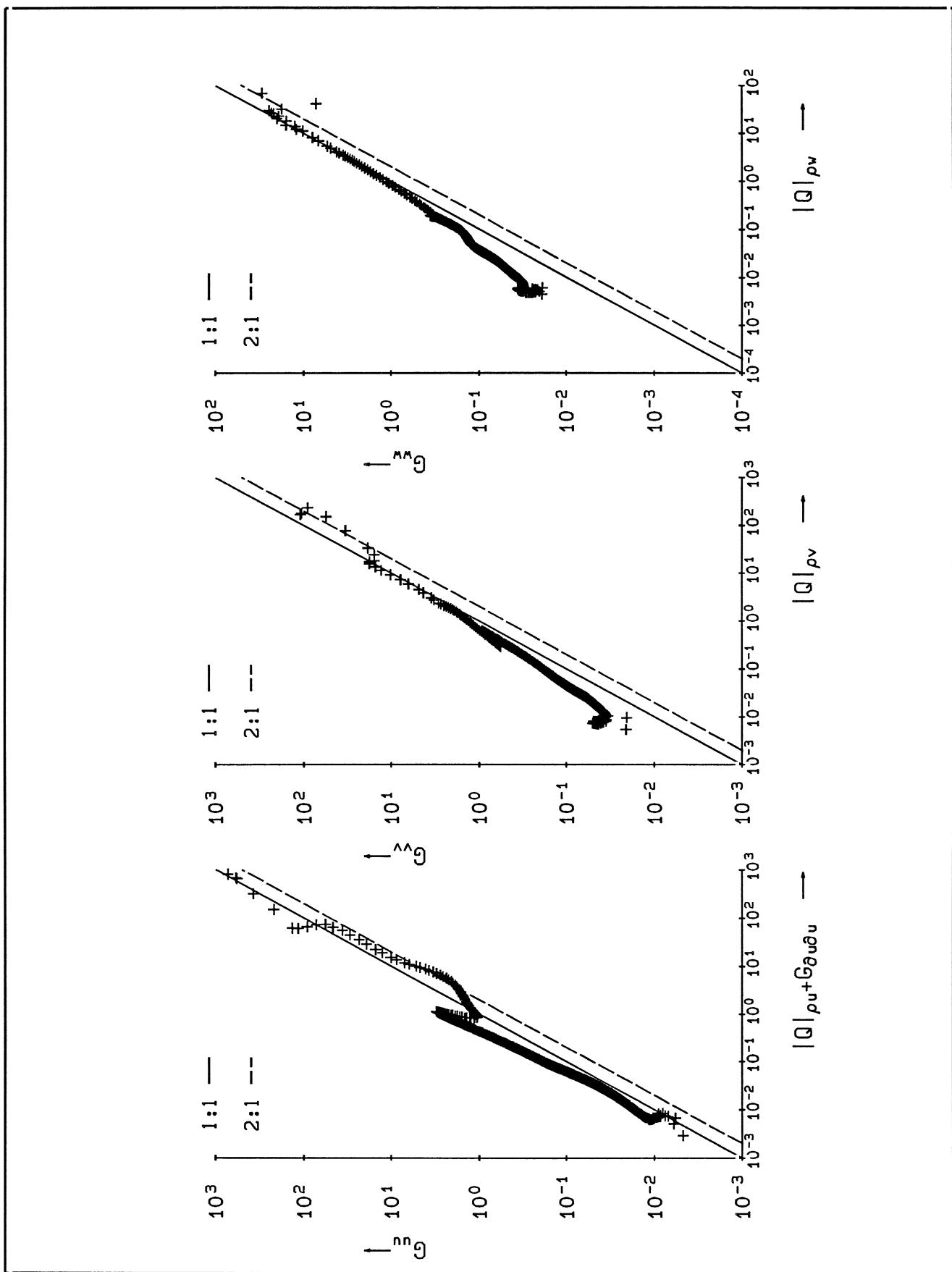
Fig.35



TKE-IWE decomposition. Field measurements  
in Rotterdam Waterway ( $R_i=1.2$ ;  $N=0.17$  rad/s).

06.04.12:53|25-56 min

iwefield.125



Absolute quad spectra compared with power spectra of velocity components  $u$ ,  $v$ , and  $w$ .

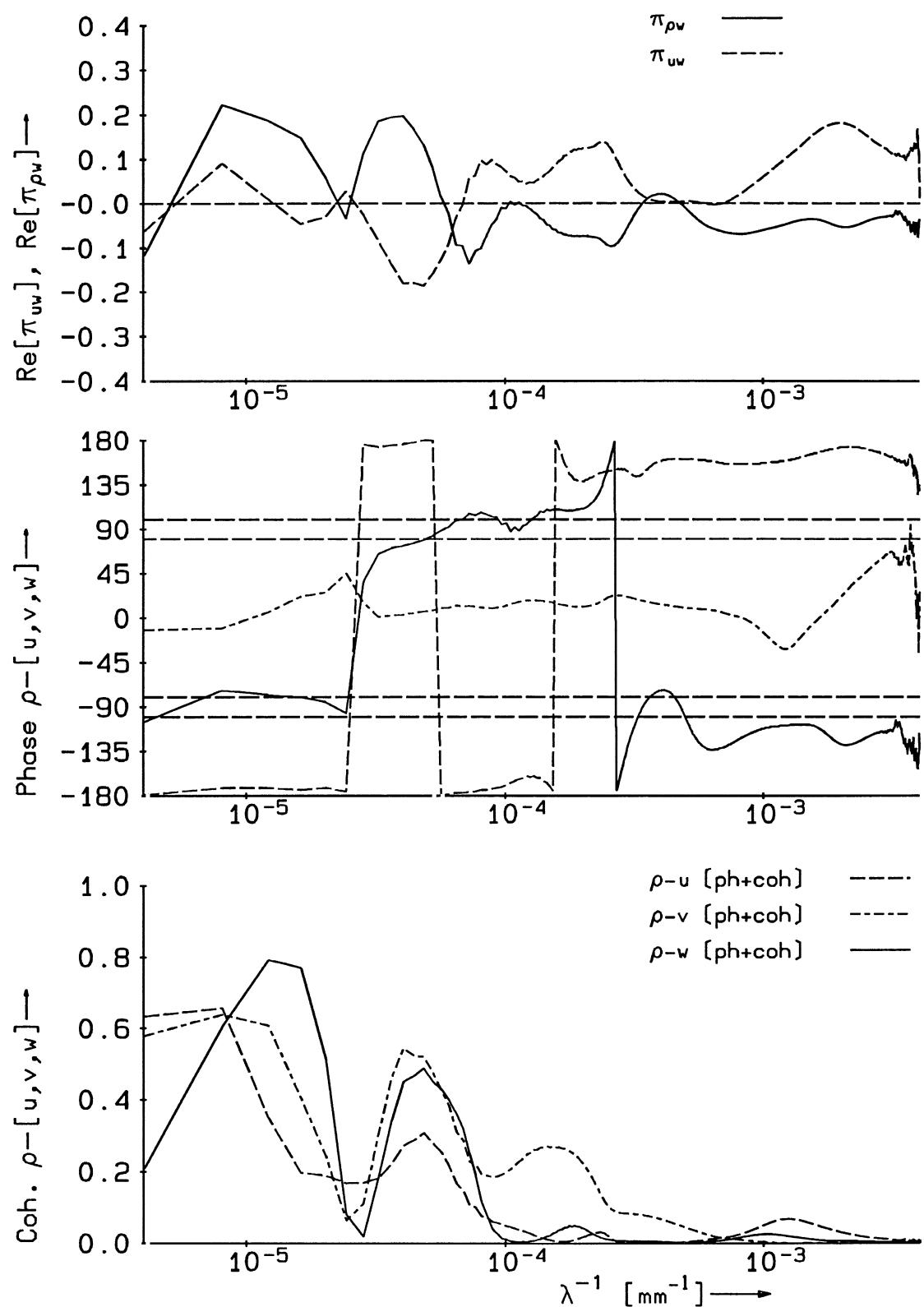
06.04.12:53|26-56 min

tet125.inv

DELFT HYDRAULICS

Z 722

Fig. 36<sup>b</sup>



Phase, coherence, momentum and buoyancy fluxes.

06.04.12:53|26-56 min

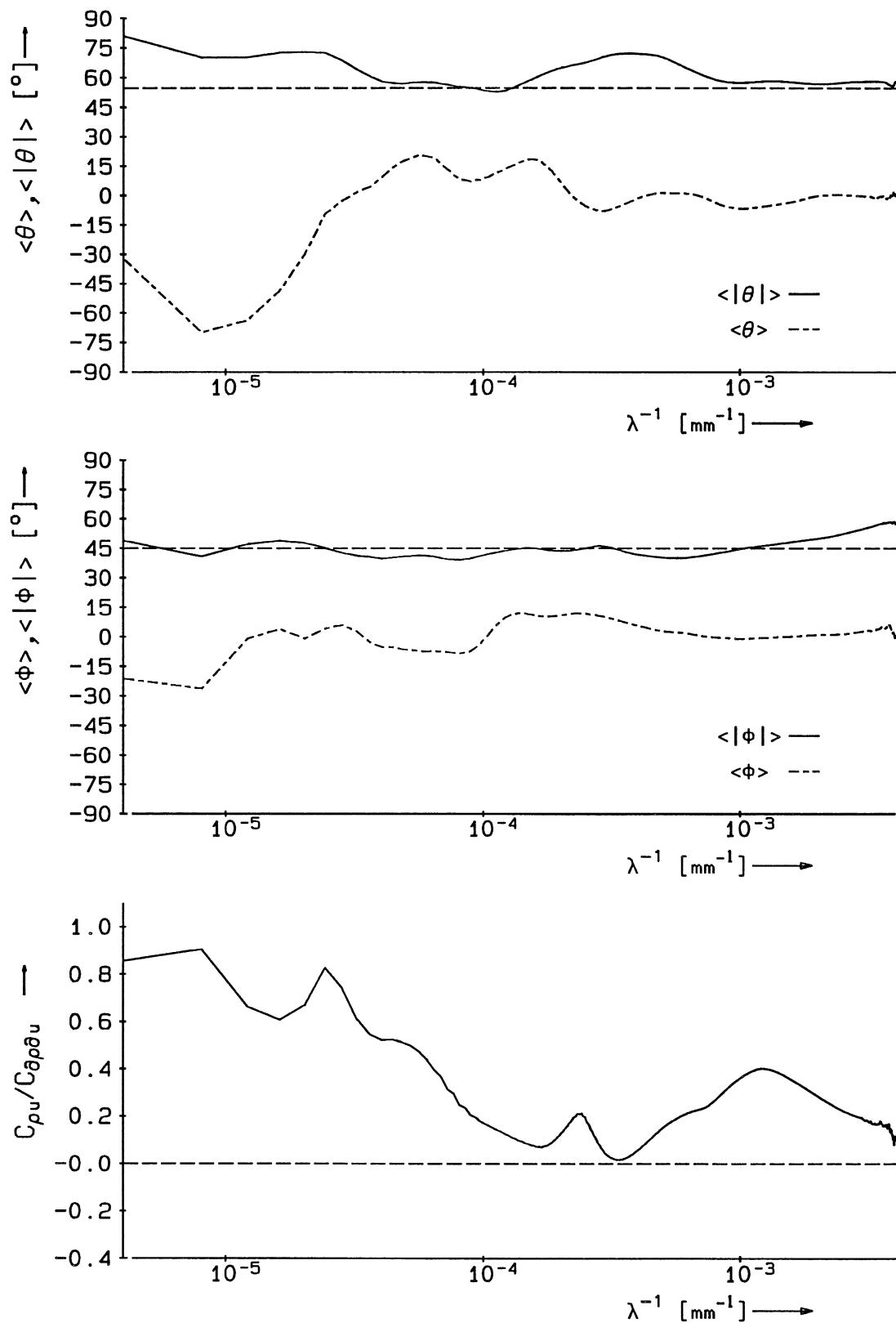
Rotterdam Waterway [ $Ri=1.2; N=0.17 \text{ rad/s}$ ].

iwe125.inv

DELFT HYDRAULICS

Z 722

Fig. 36c



Normalized Stokes mass drift and IW angles.

Rotterdam Waterway [ $Ri=1.2$ ;  $N=0.17$  rad/s].

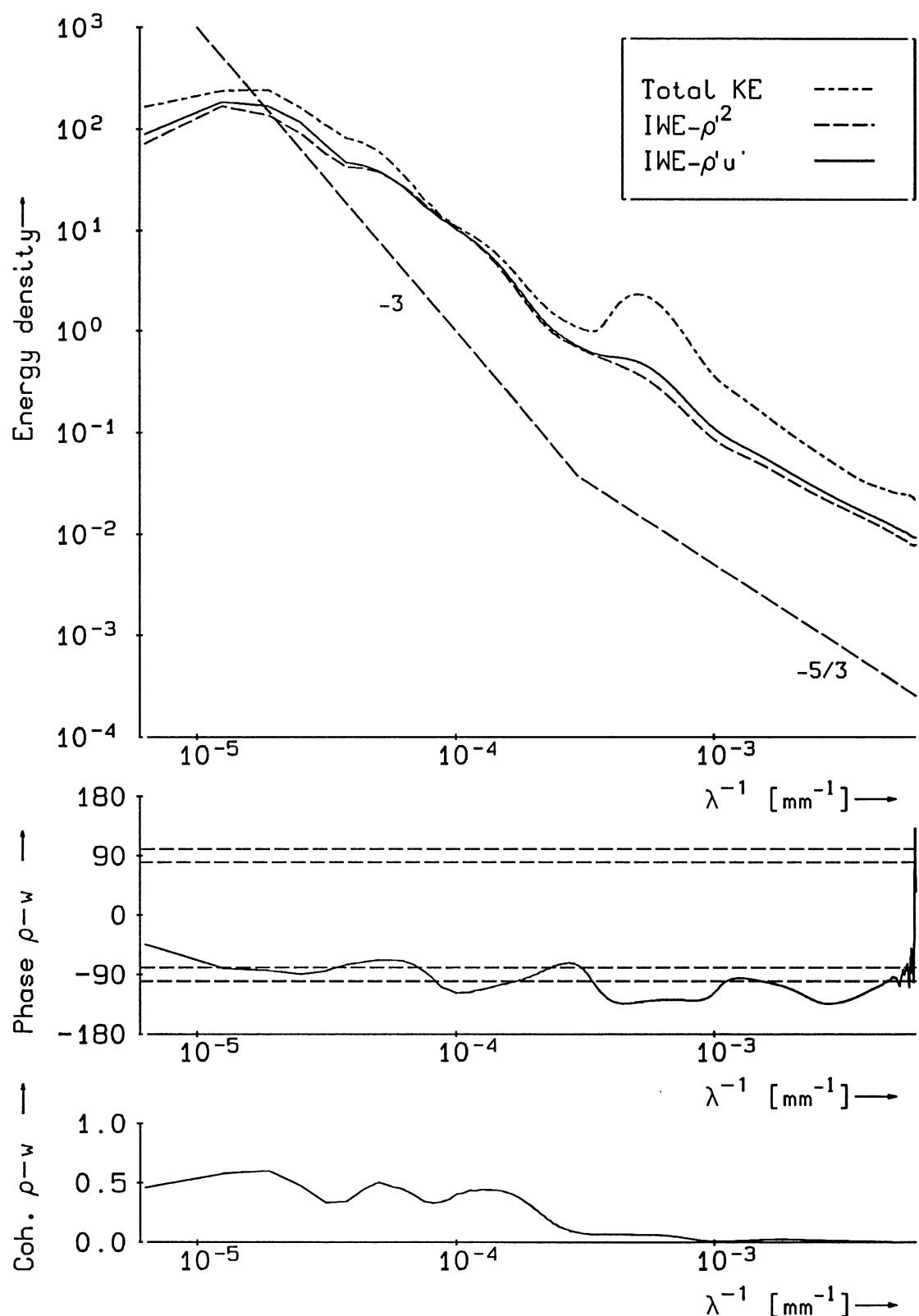
06.04.12:53|26-56 min

stok125.inv

DELFT HYDRAULICS

Z 722

Fig. 36d



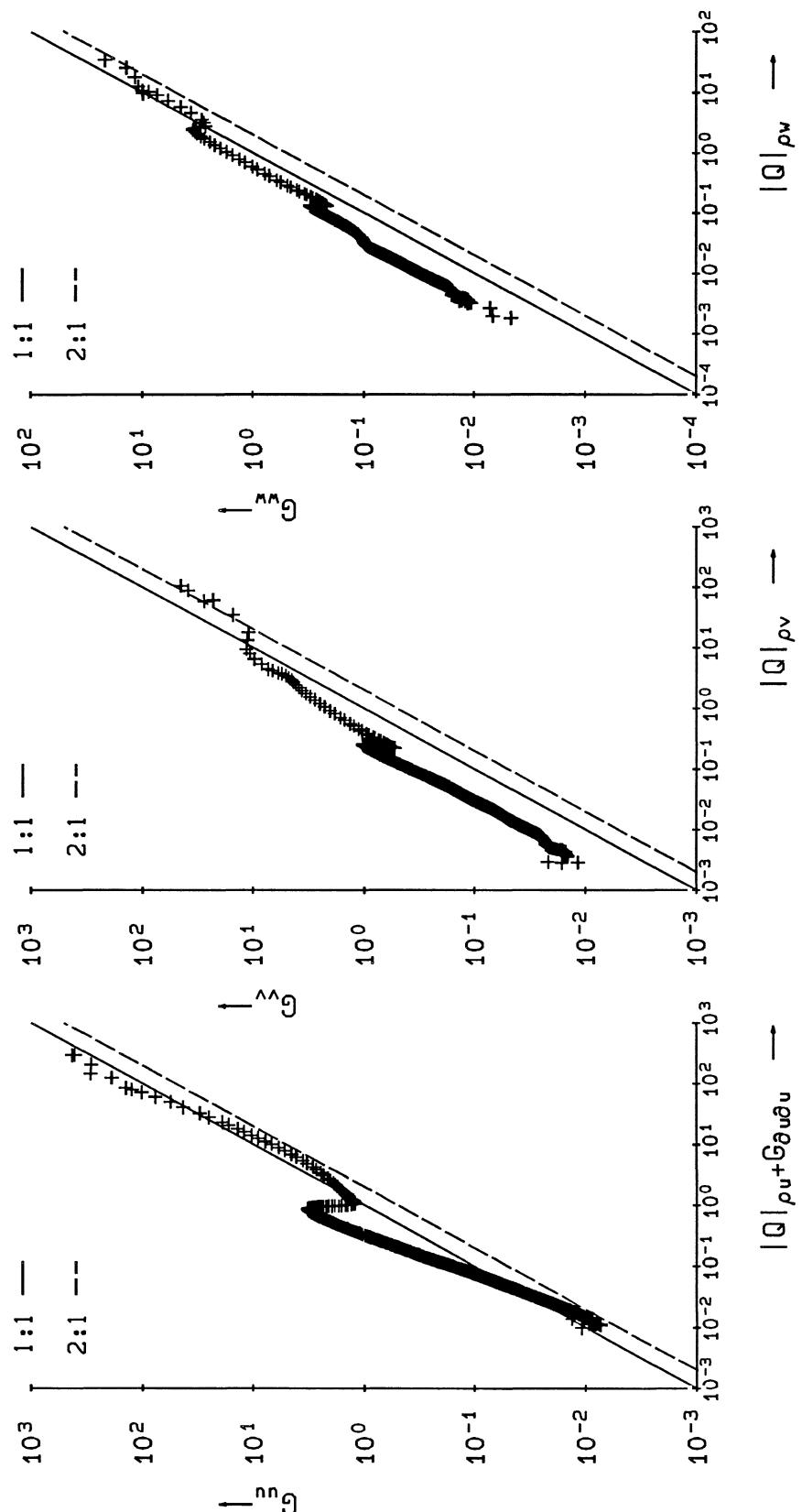
TKE-IWE decomposition. Field measurements  
in Rotterdam Waterway ( $Ri=0.43; N=0.15 \text{ rad/s}$ ).  
DELFT HYDRAULICS

06.04.13:32|65-95 min

iwefield.133

Z 722

Fig.37<sup>a</sup>



Absolute quad spectra compared with power spectra of velocity components  $u$ ,  $v$ , and  $w$ .

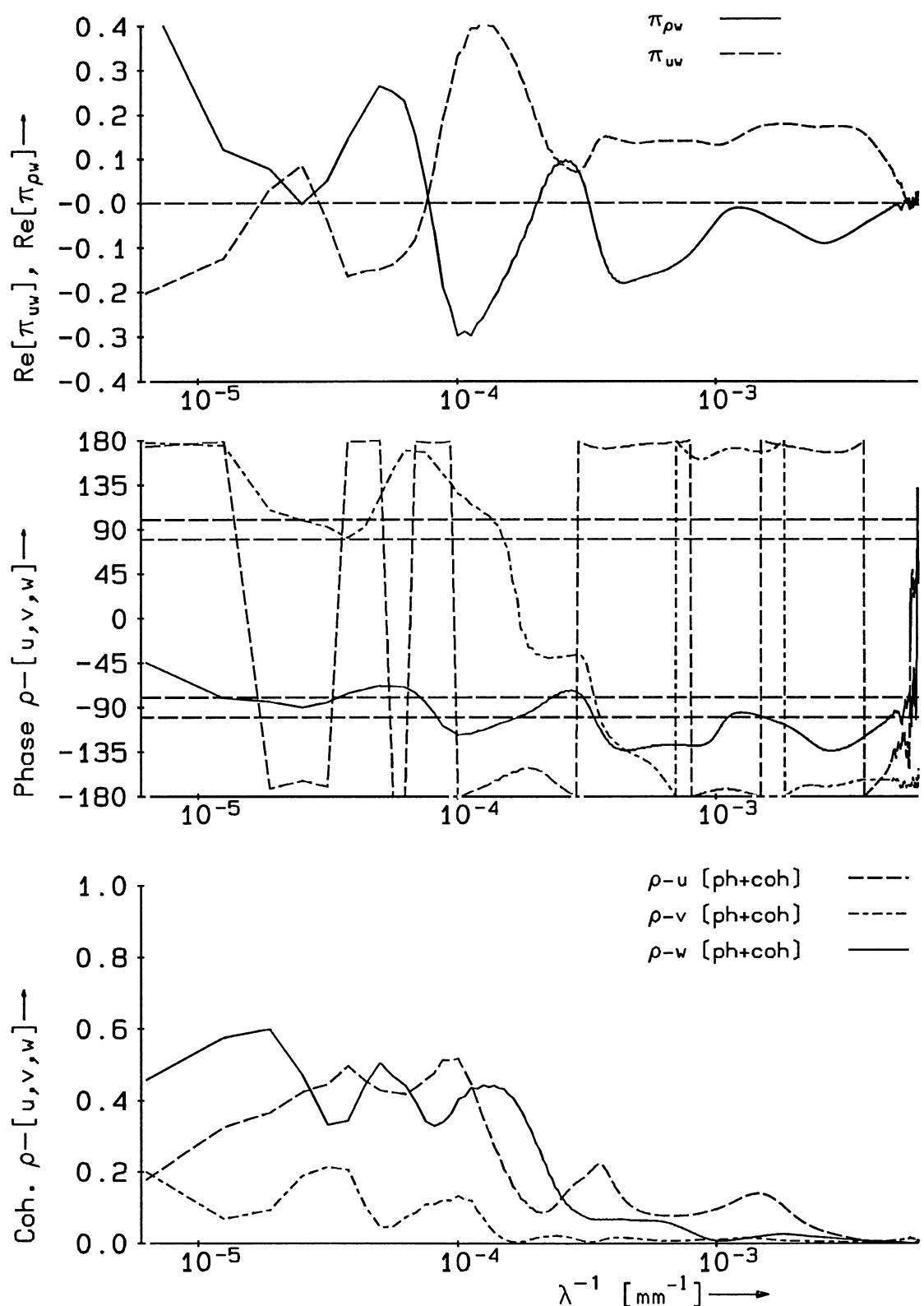
06.04.13:32|65-95 min

tet133.inv

DELFT HYDRAULICS

Z 722

Fig. 37<sup>b</sup>

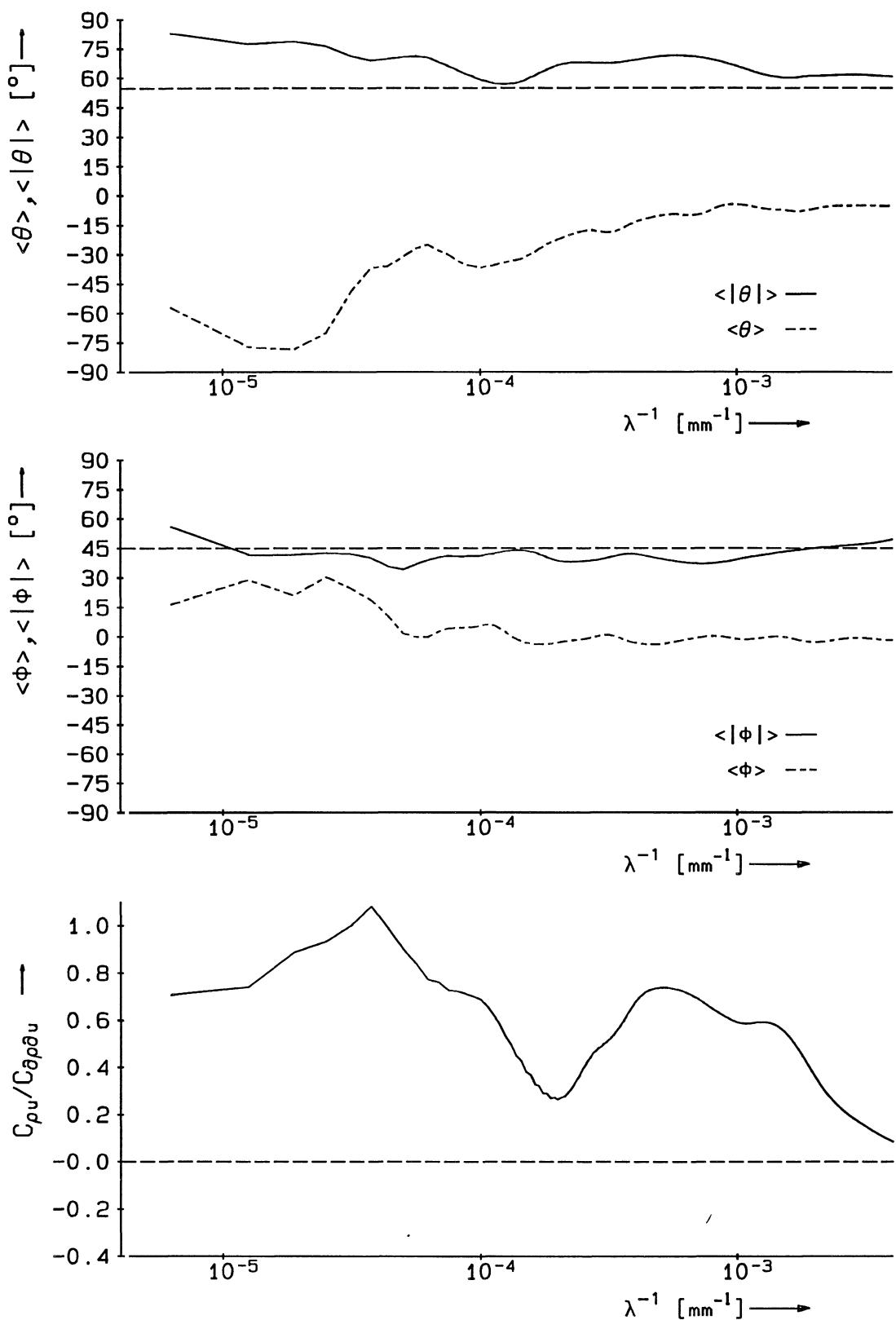


Phase, coherence, momentum and buoyancy fluxes.

Rotterdam Waterway [ $Ri=0.43; N=0.15 \text{ rad/s}$ ].

06.04.13:32|65-95 min

iwe133.inv



Normalized Stokes mass drift and IW angles.

06.04.13:32|65-95 min

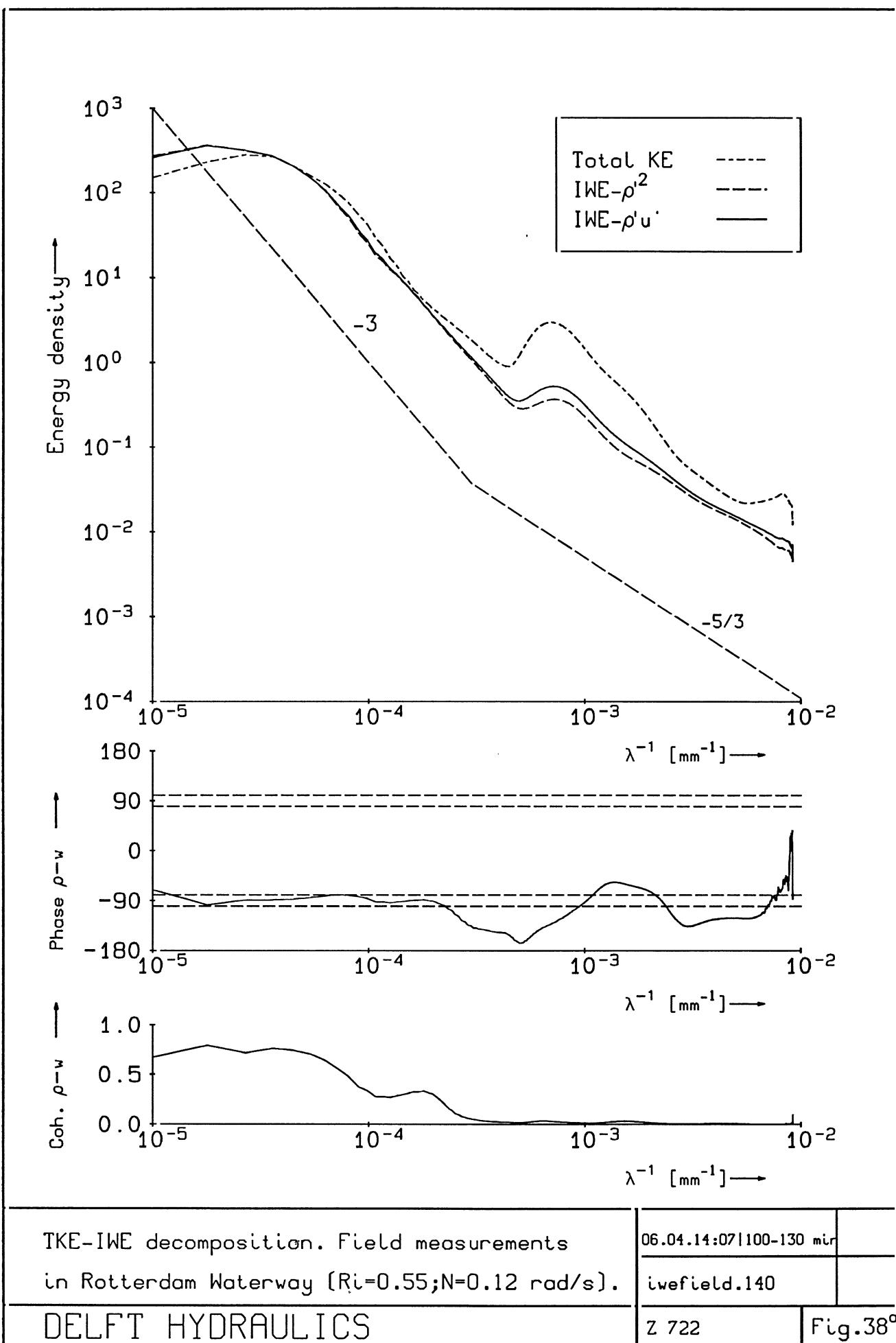
Rotterdam Waterway [ $Ri=0.43$ ;  $N=0.15$  rad/s].

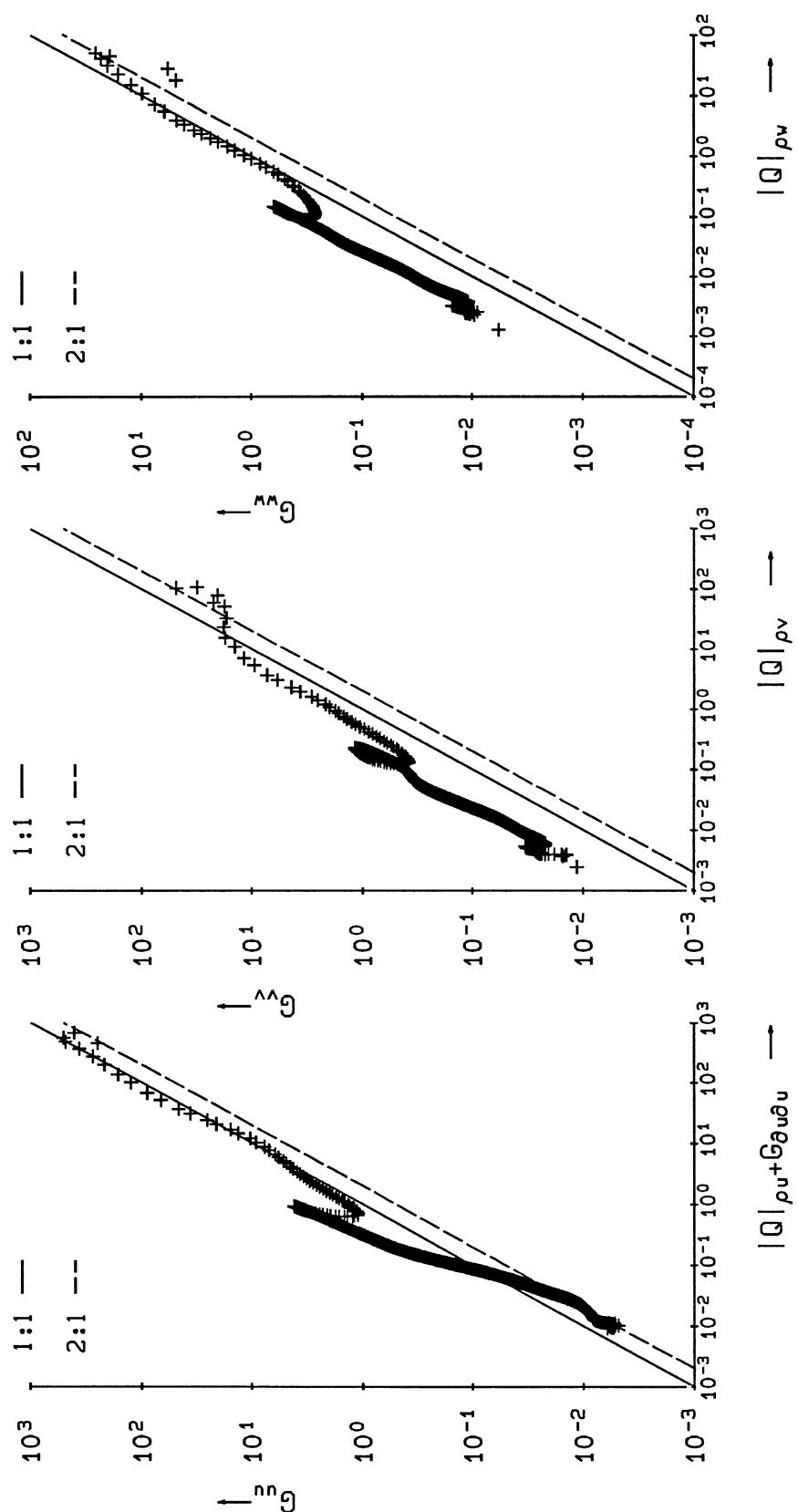
stok133.inv

DELFT HYDRAULICS

Z 722

Fig. 37d





Absolute quad spectra compared with power spectra of velocity components  $u$ ,  $v$ , and  $w$ .

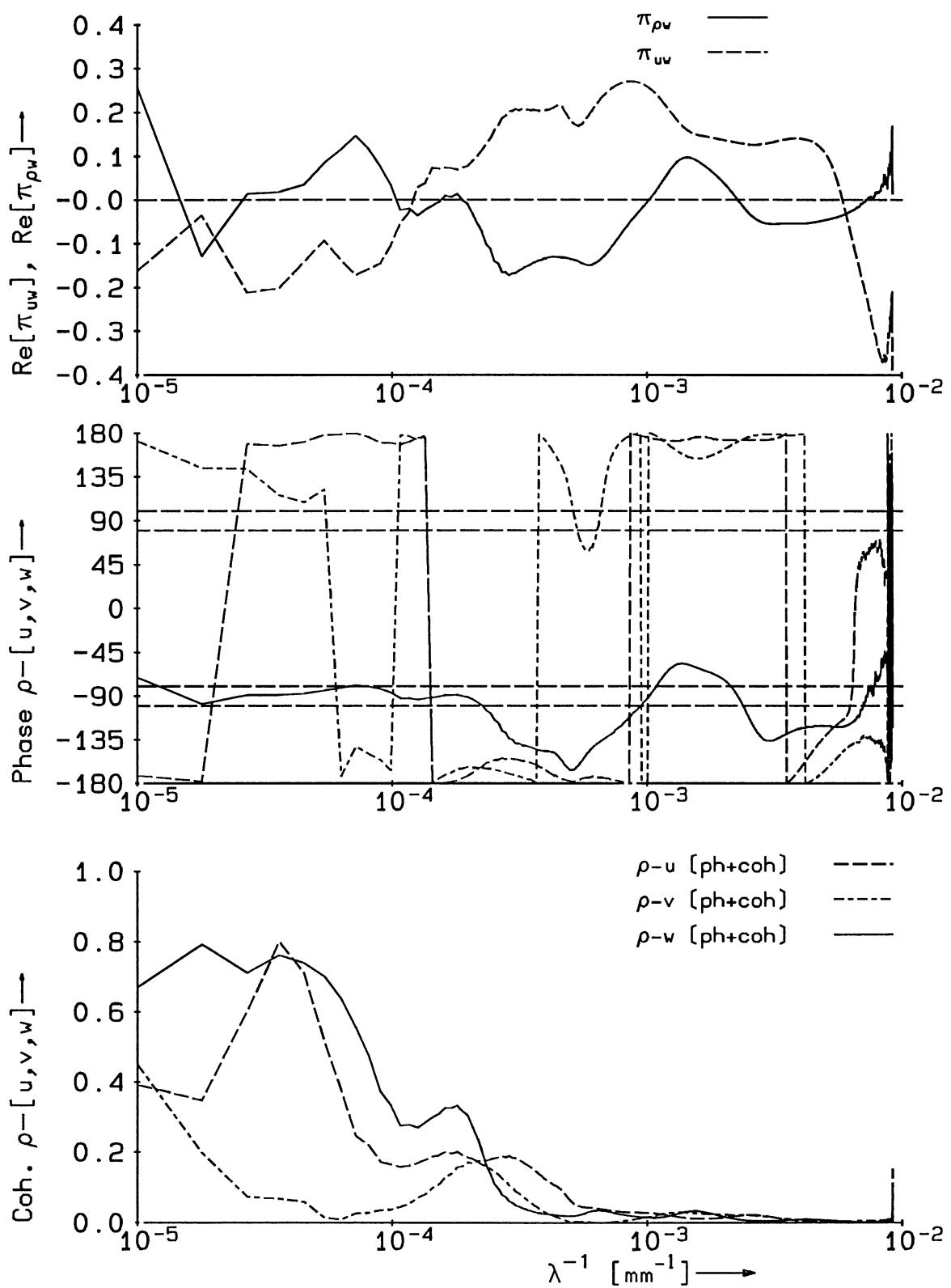
06.04.14:07|100-130 min

tet140.inv

DELFT HYDRAULICS

Z 722

Fig. 38<sup>b</sup>



Phase, coherence, momentum and buoyancy fluxes.

06.04.14:07 | 100-130 min

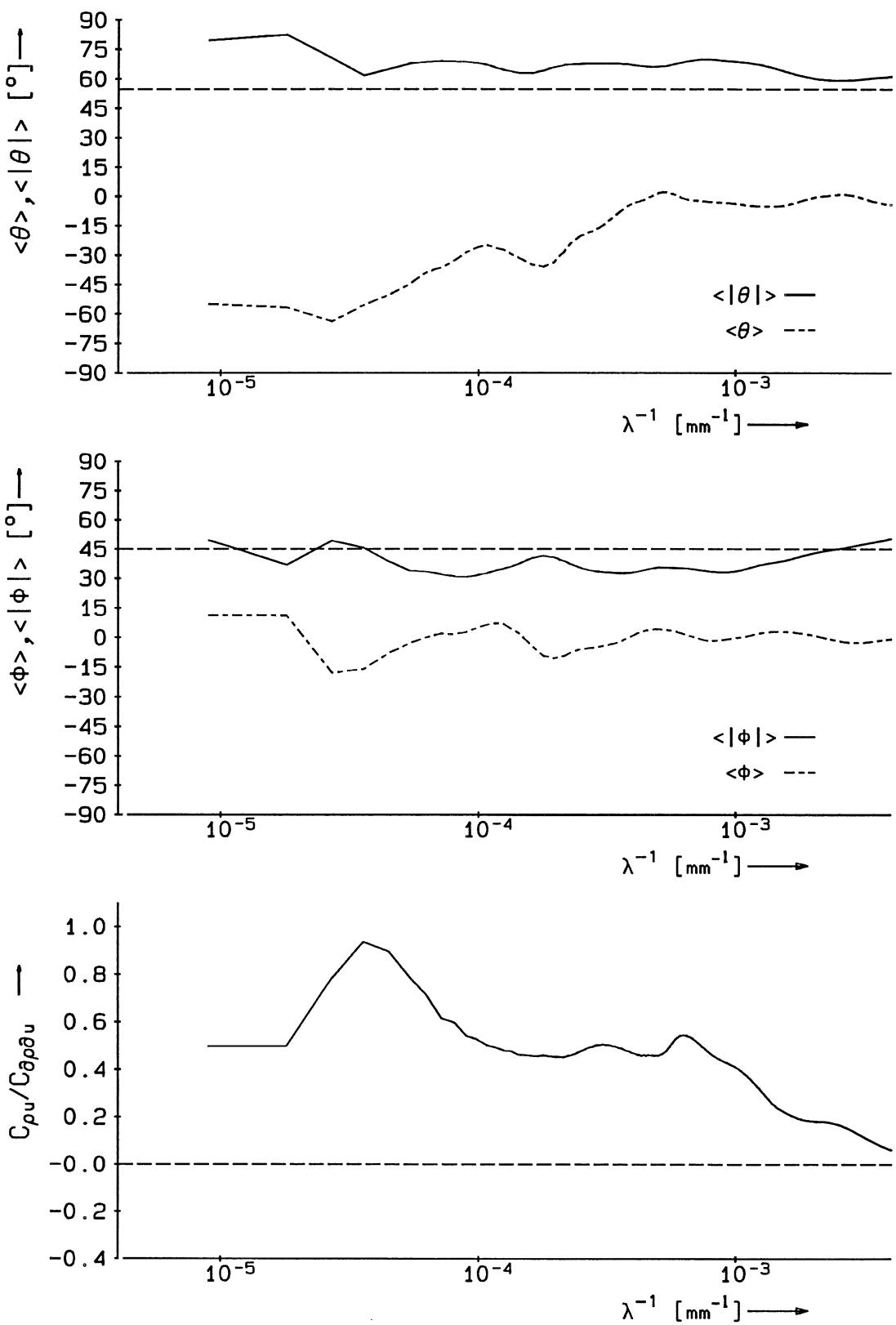
Rotterdam Waterway ( $Ri=0.55$ ;  $N=0.12$  rad/s).

iwe140.inv

DELFT HYDRAULICS

Z 722

Fig. 38c



Normalized Stokes mass drift and IW angles.

Rotterdam Waterway ( $Ri=0.55$ ;  $N=0.12$  rad/s).

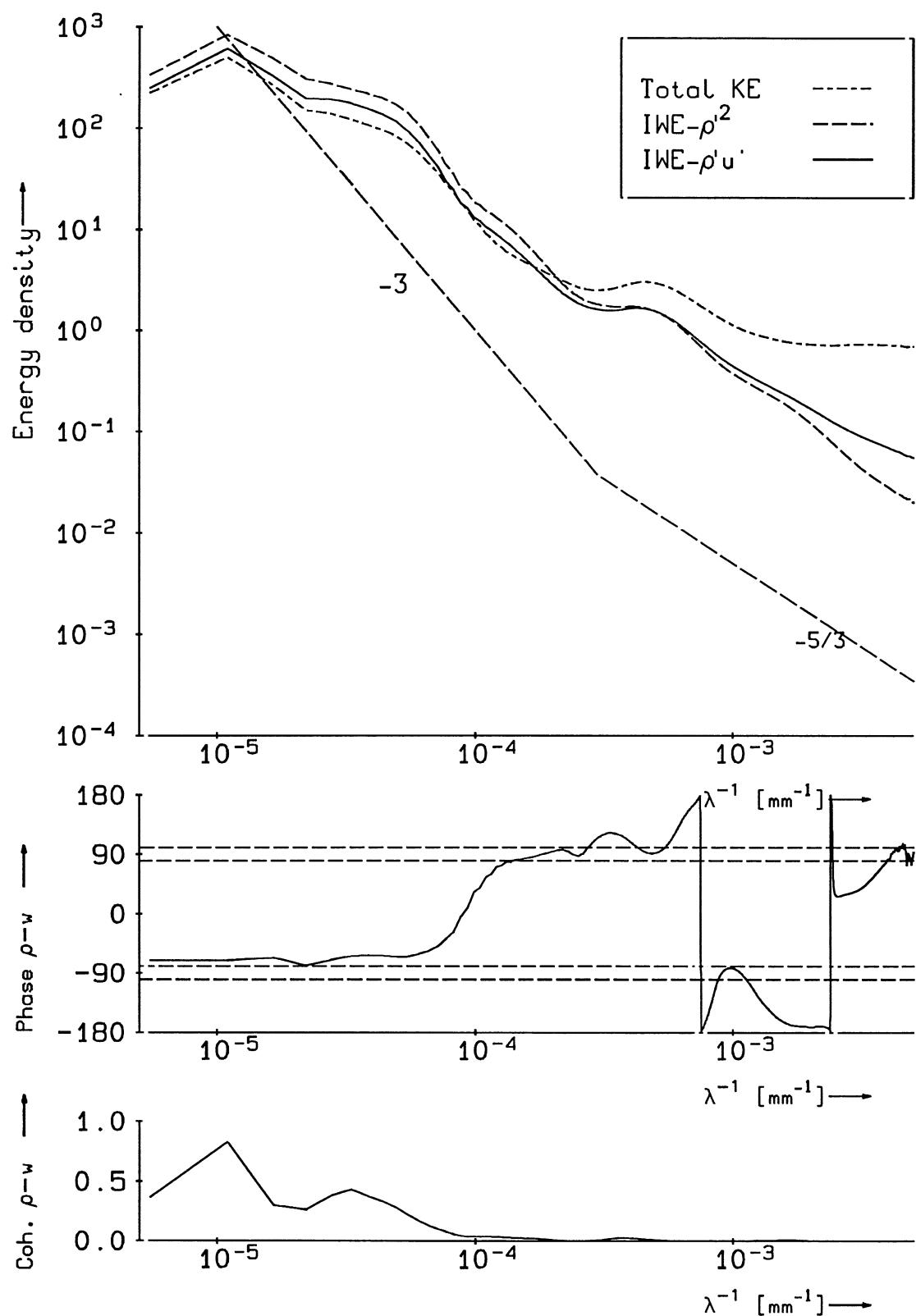
06.04.14:07 | 100-130 min

stok140.inv

DELFT HYDRAULICS

Z 722

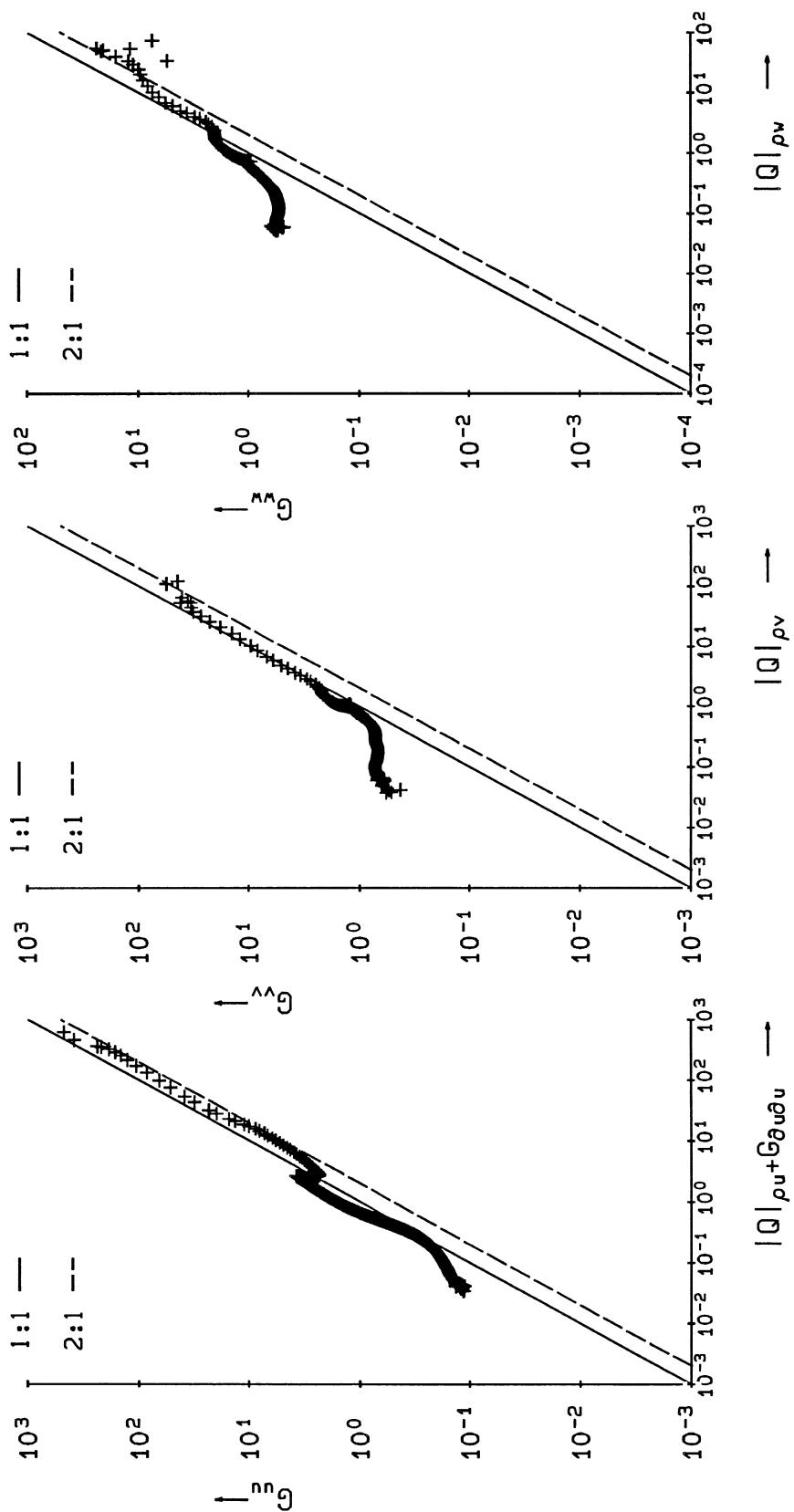
Fig. 38<sup>d</sup>



TKE-IWE decomposition. Field measurements  
in Rotterdam Waterway [ $Ri=0.48$ ;  $N=0.17$  rad/s].

06.04.14:59|152-182 min

iwefield.145



Absolute quad spectra compared with power spectra of velocity components  $u$ ,  $v$ , and  $w$ .

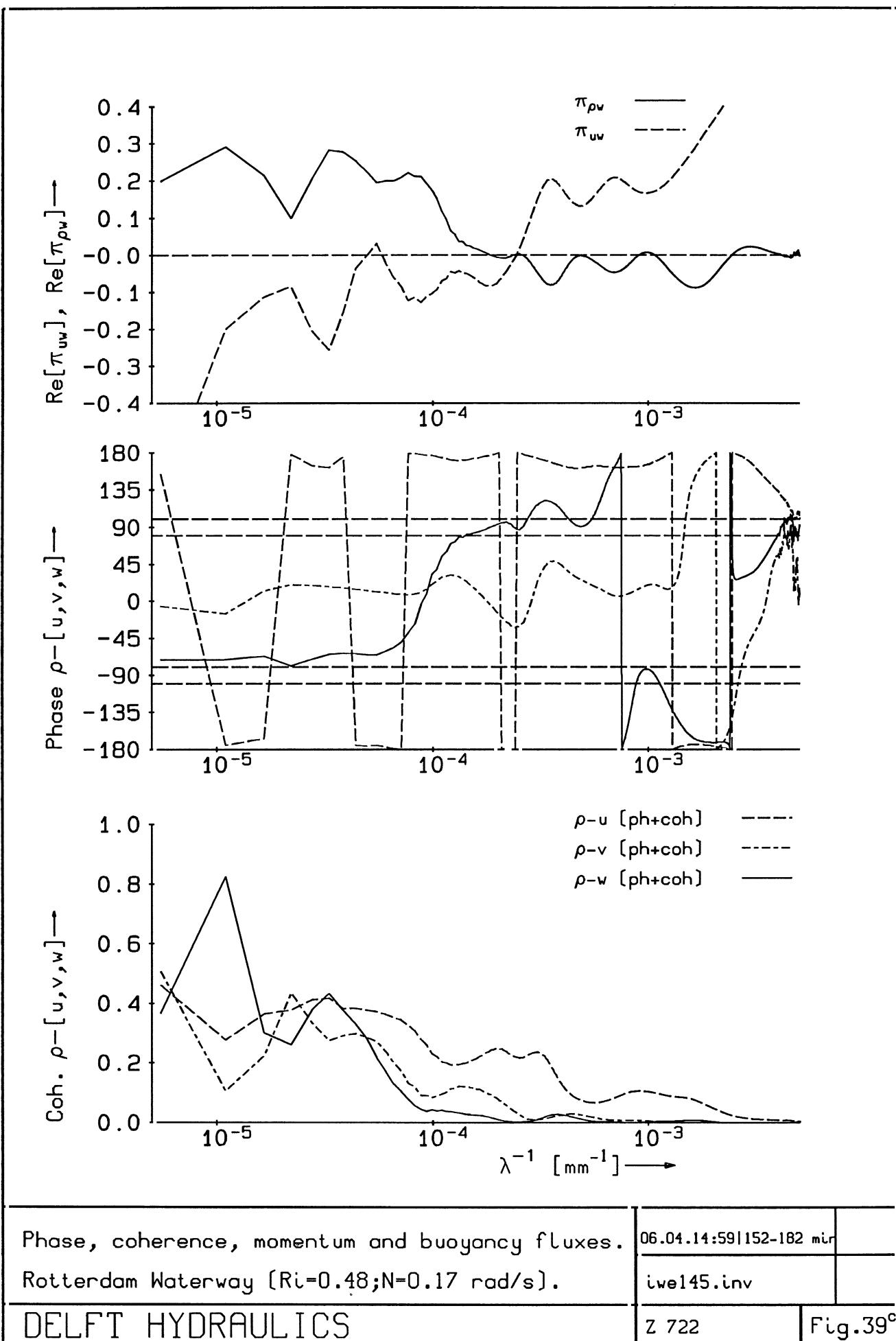
06.04.14:59|152-182 min

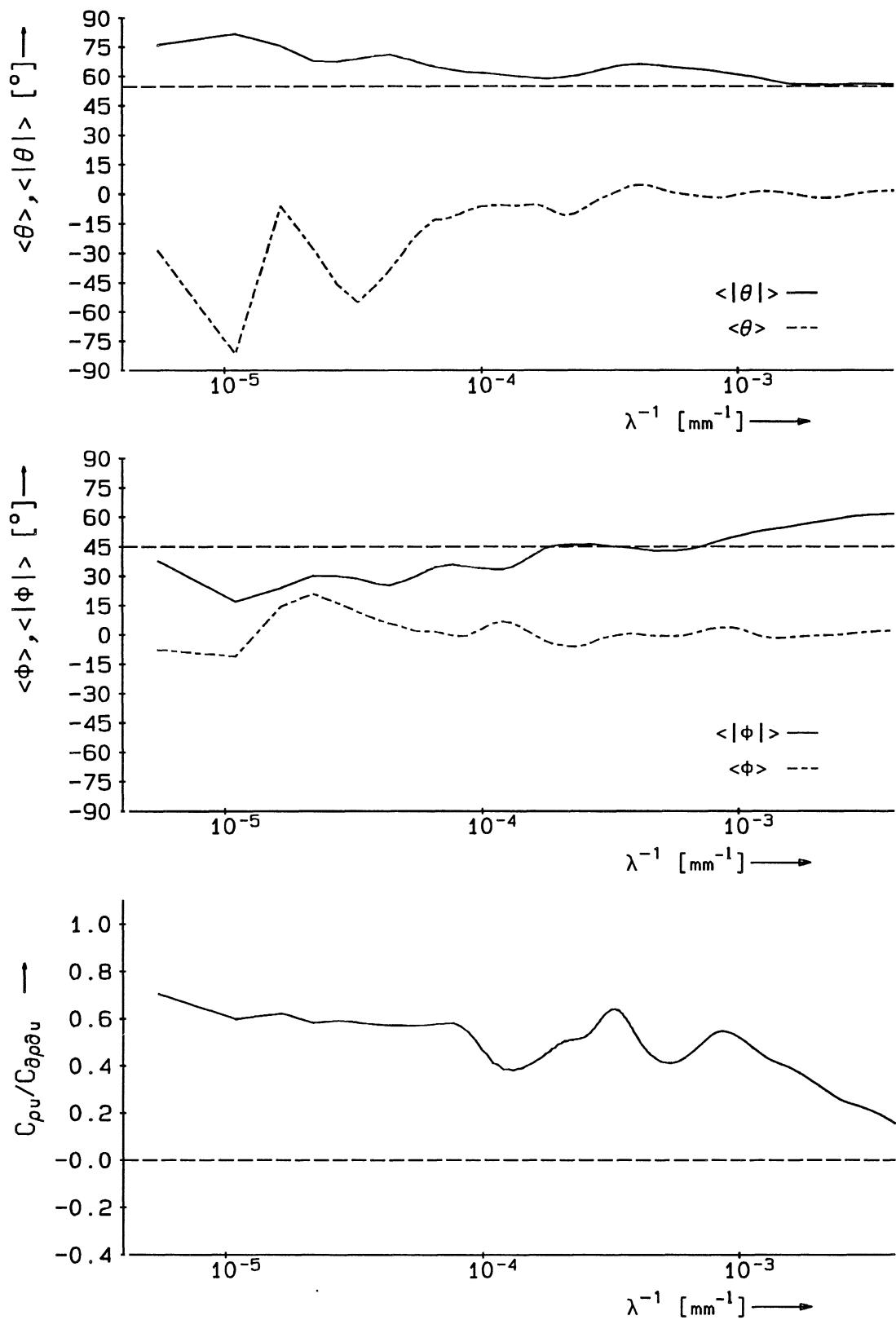
tet145.inv

DELFT HYDRAULICS

Z 722

Fig. 39<sup>b</sup>





Normalized Stokes mass drift and IW angles.

Rotterdam Waterway [ $Ri=0.48; N=0.17 \text{ rad/s}$ ].

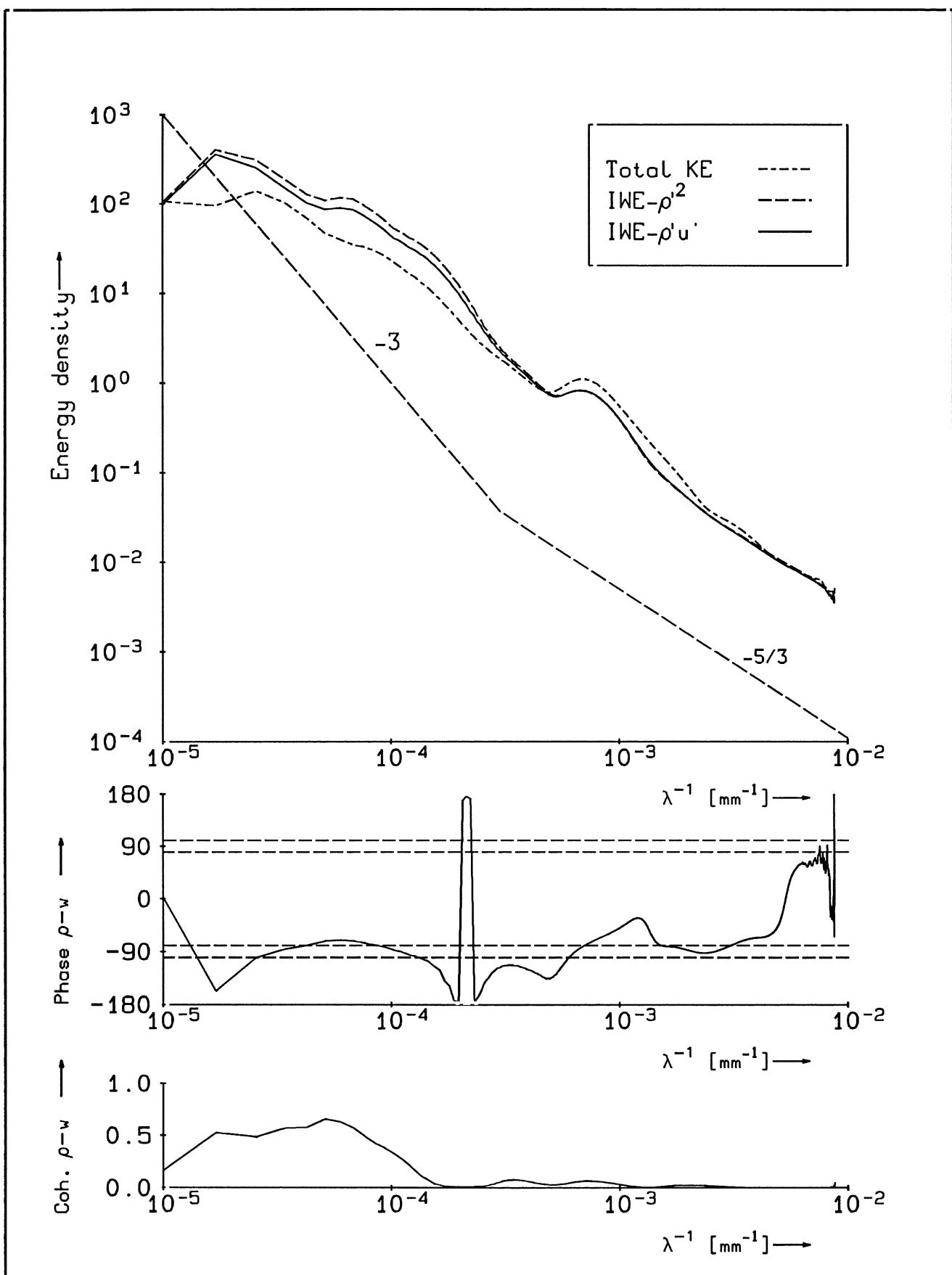
DELFT HYDRAULICS

06.04.14:59|152-182.mir

stok145.inv

Z 722

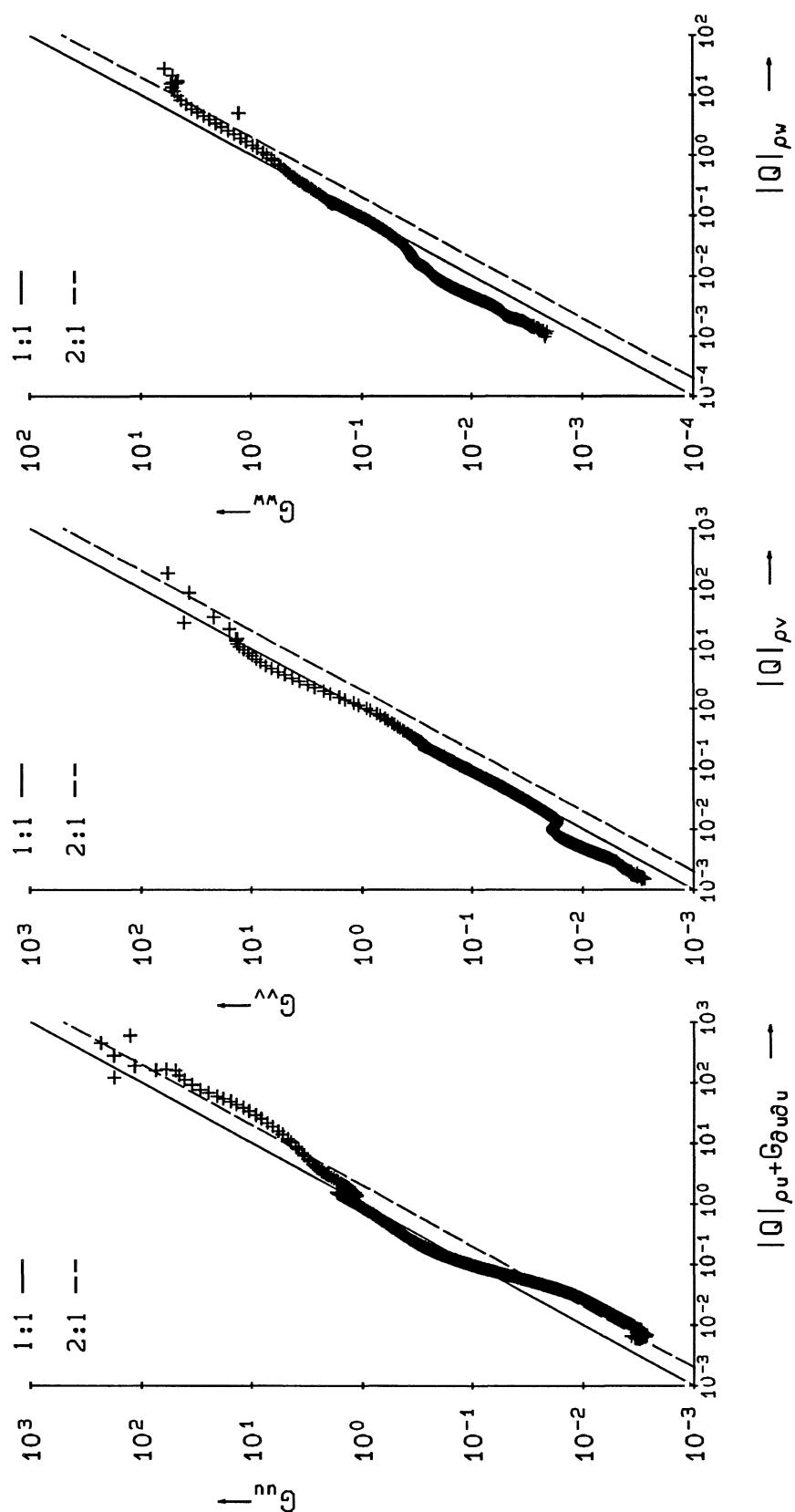
Fig.39d



TKE-IWE decomposition. Field measurements  
in Rotterdam Waterway ( $Ri=0.63; N=0.17$  rad/s).

06.04.15:36|189-219 min

iwefield.153



Absolute quad spectra compared with power  
spectra of velocity components  $u$ ,  $v$ , and  $w$ .

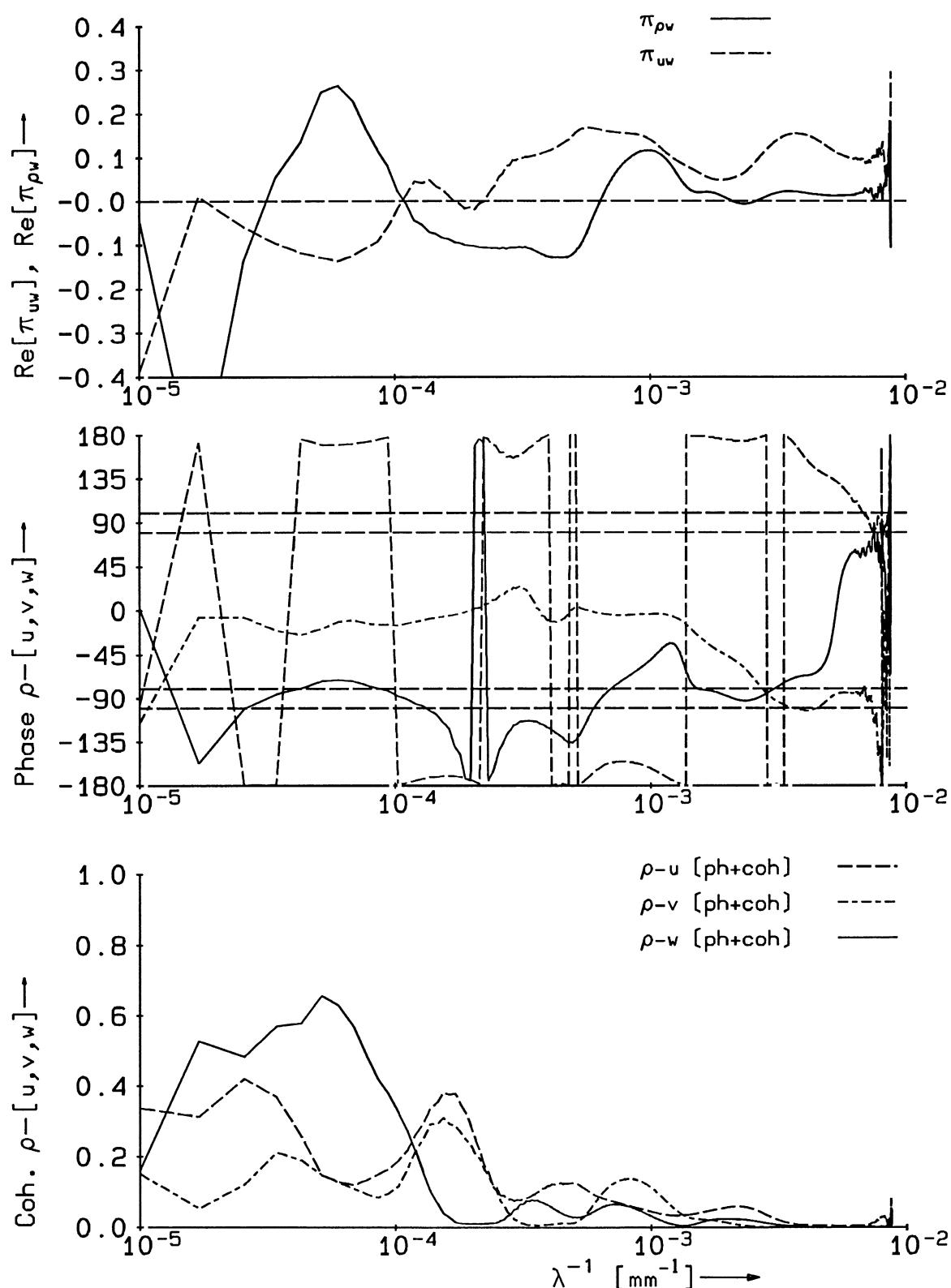
06.04.15:36 | 189-219 min

tet153.inv

DELFT HYDRAULICS

Z 722

Fig. 40<sup>b</sup>

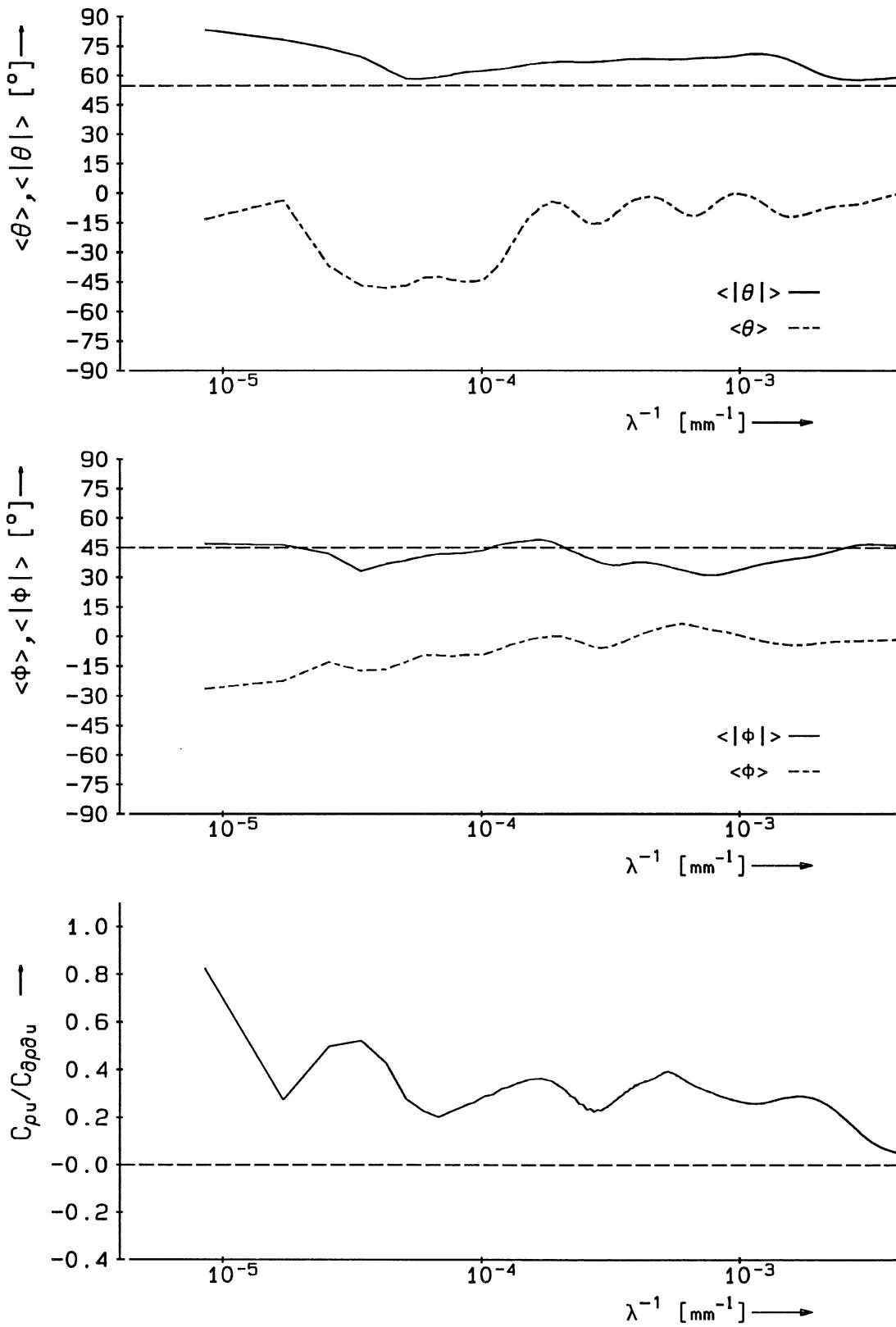


Phase, coherence, momentum and buoyancy fluxes.

06.04.15:36|189-219 min

Rotterdam Waterway [ $Ri=0.63; N=0.17 \text{ rad/s}$ ].

iwe153.inv



Normalized Stokes mass drift and IW angles.

Rotterdam Waterway [ $Ri=0.63; N=0.17 \text{ rad/s}$ ].

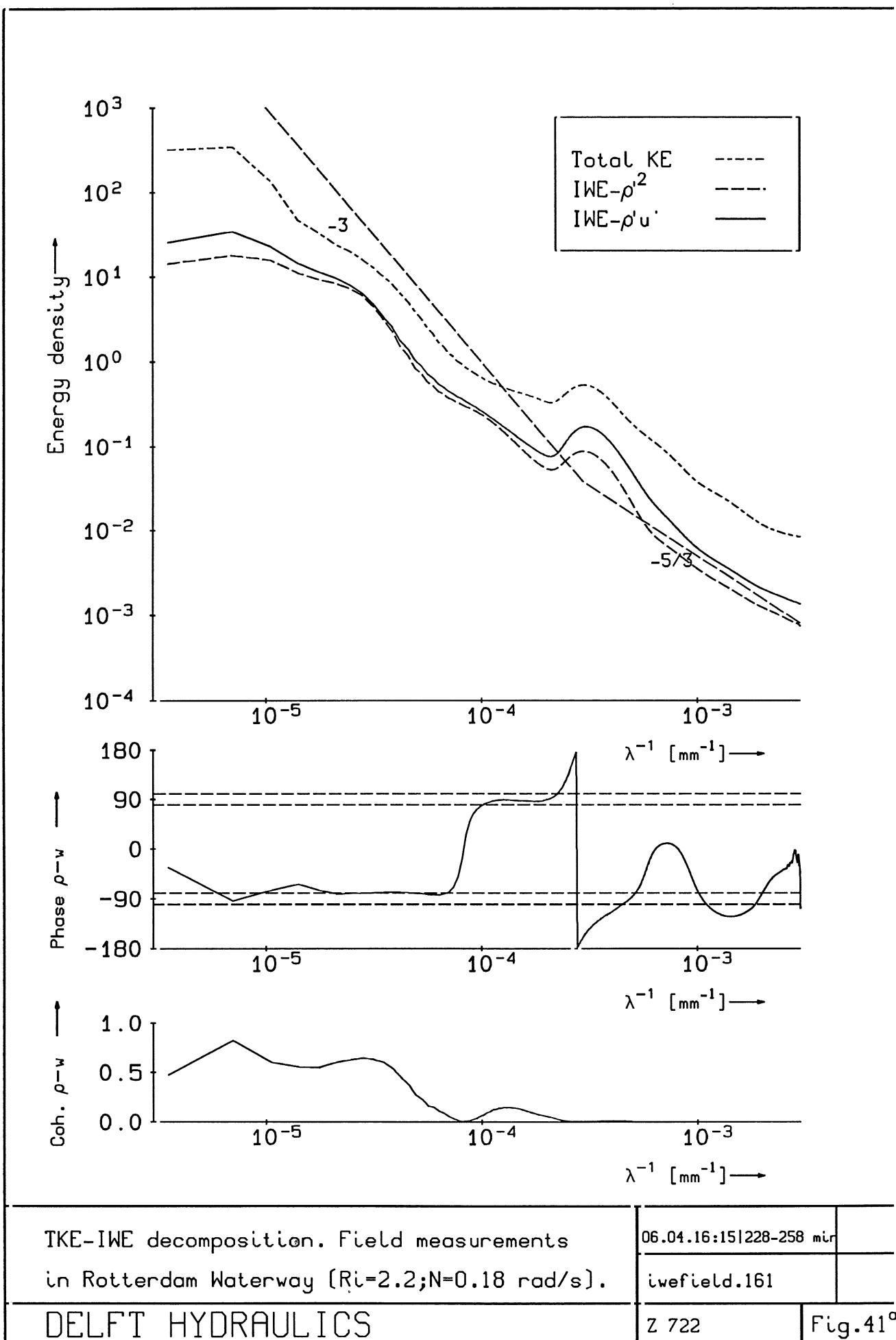
DELFT HYDRAULICS

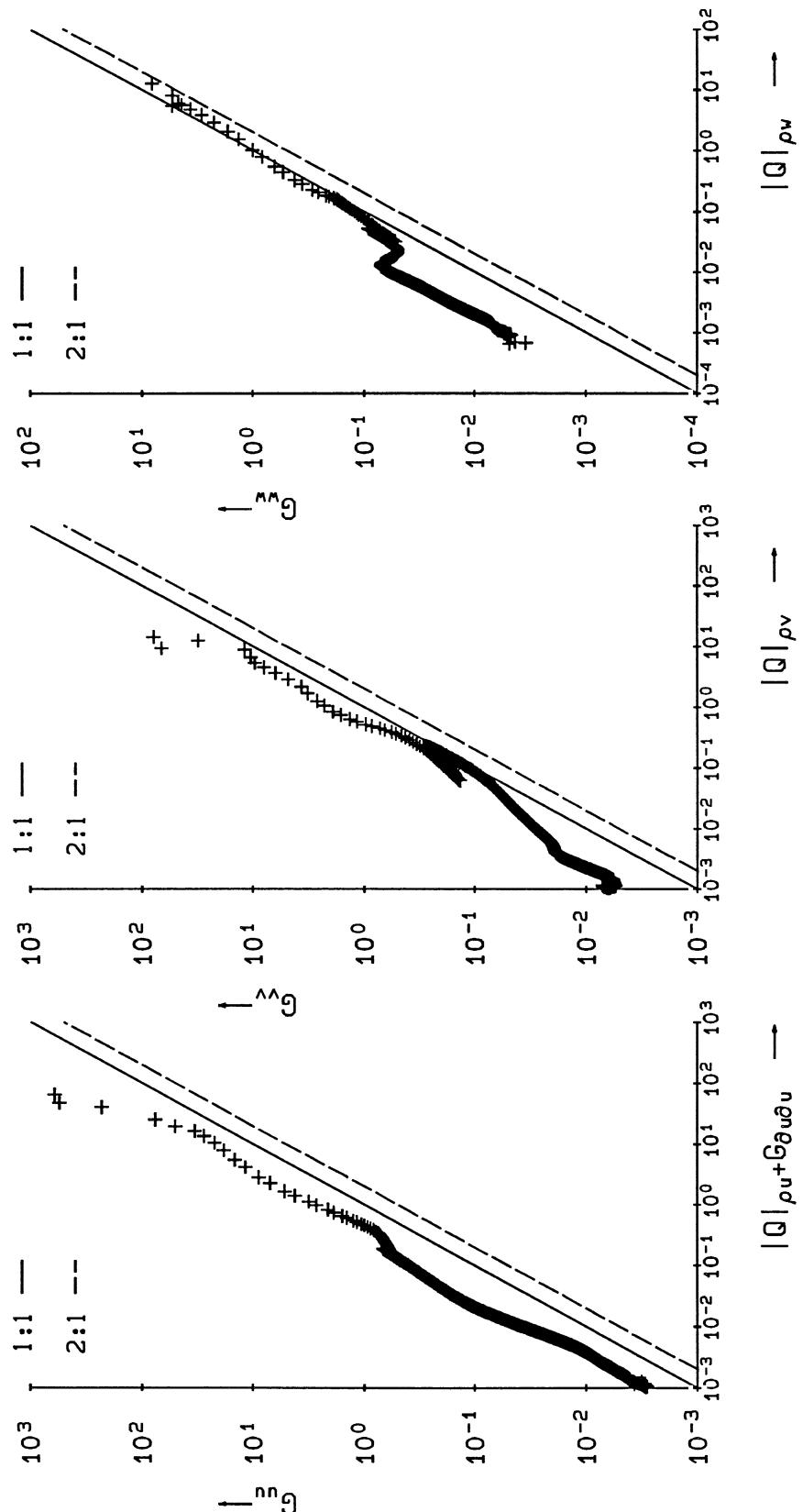
06.04.15:36|189-219 min

stok153.inv

Z 722

Fig. 40d





Absolute quad spectra compared with power spectra of velocity components  $u$ ,  $v$ , and  $w$ .

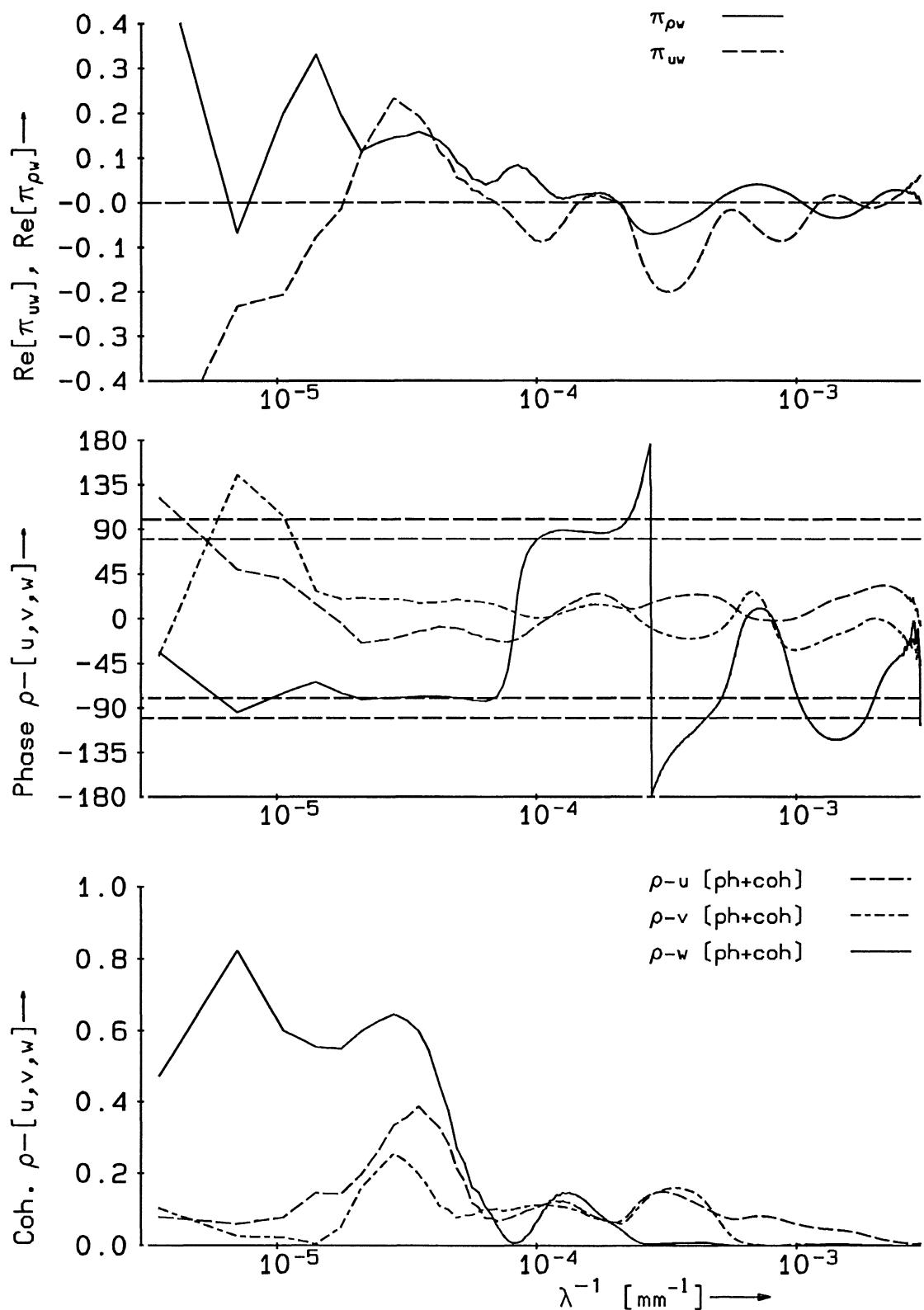
06.04.16:15 | 228-258 min

tet161.inv

DELFT HYDRAULICS

Z 722

Fig. 41<sup>b</sup>

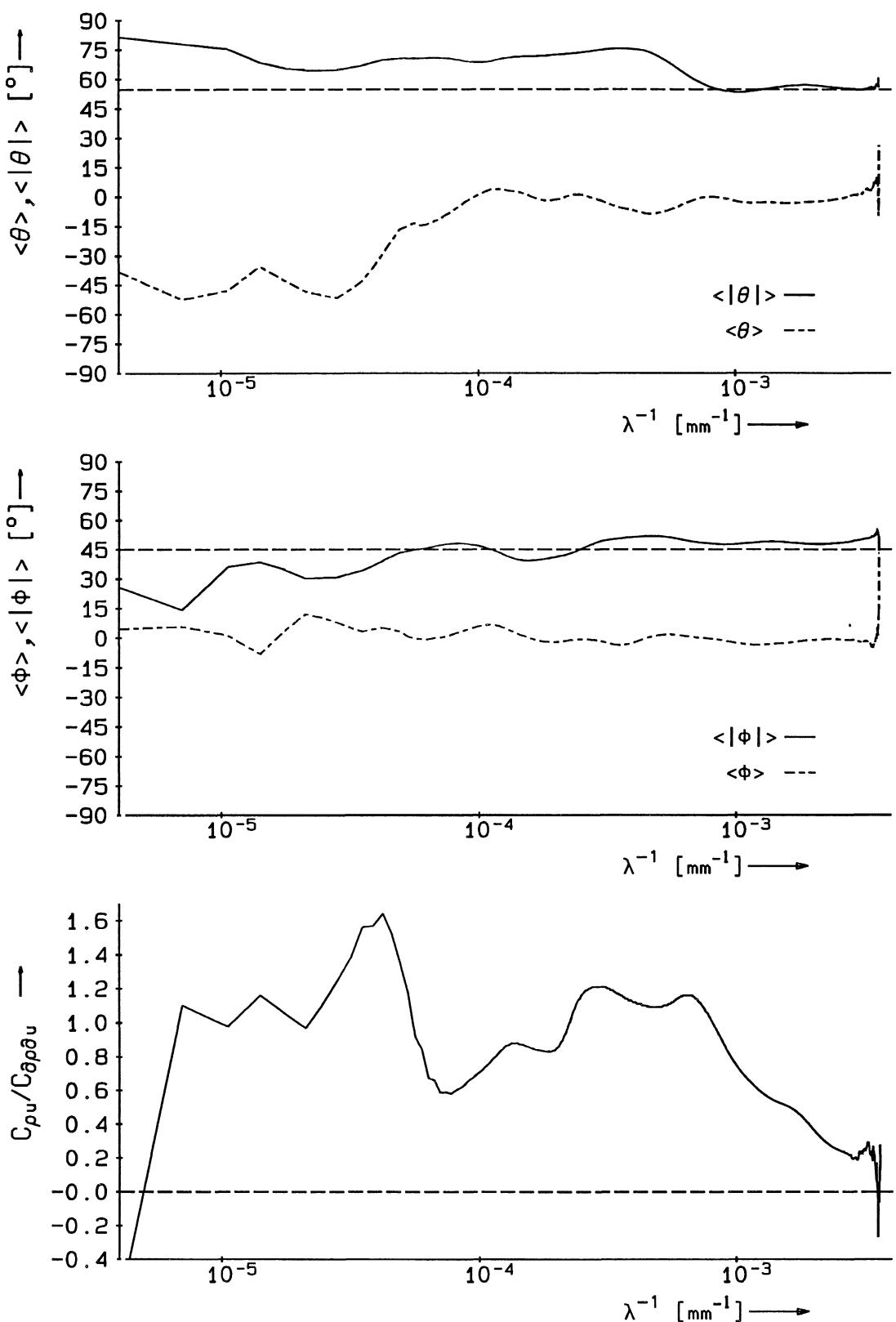


Phase, coherence, momentum and buoyancy fluxes.

06.04.16:15 | 228-258 mir

Rotterdam Waterway [ $Ri=2.2; N=0.18 \text{ rad/s}$ ].

iwe161.inv



Normalized Stokes mass drift and IW angles.

Rotterdam Waterway [ $Ri=2.2; N=0.18 \text{ rad/s}$ ].

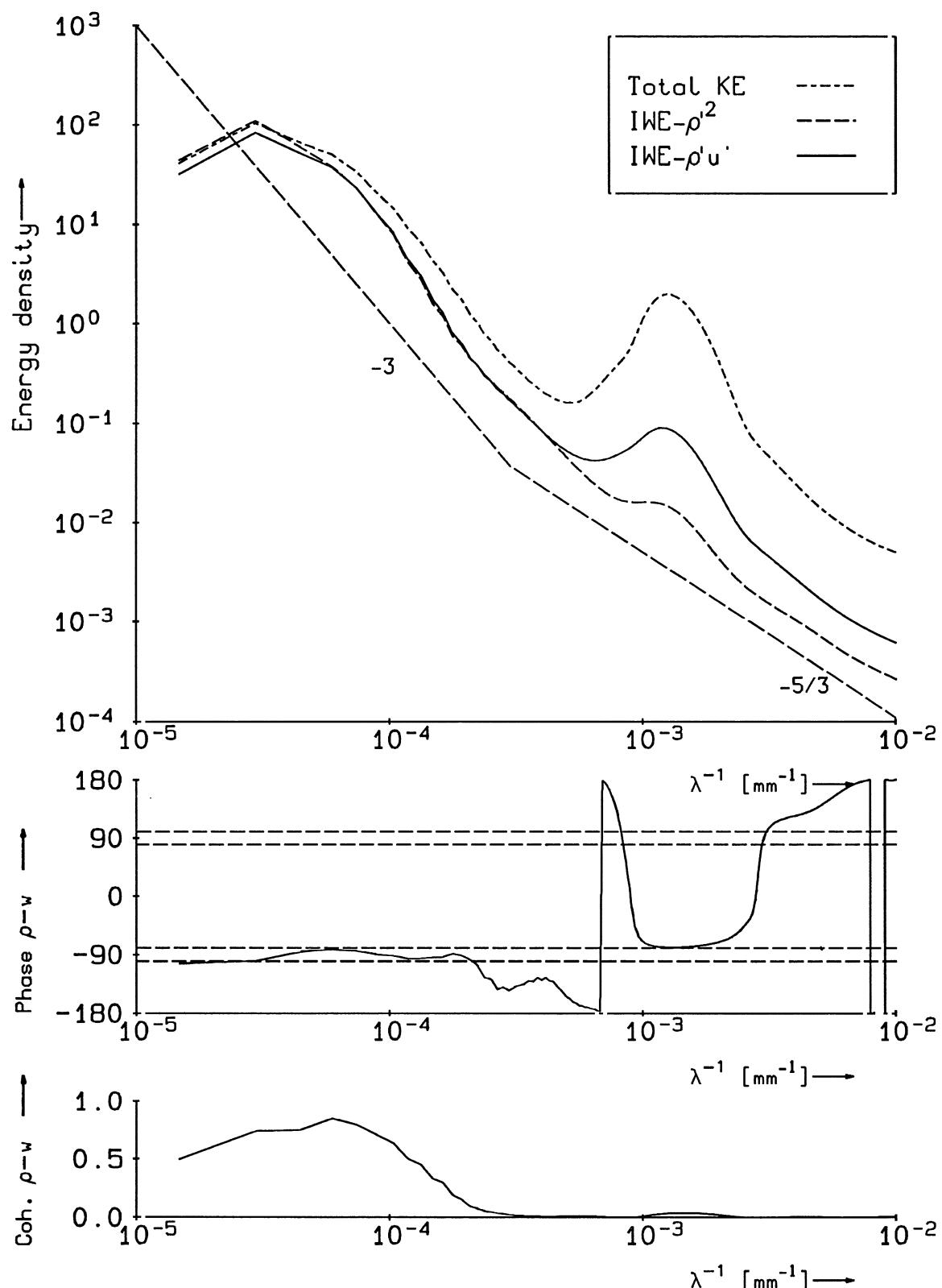
06.04.16:15 | 228-258 min

stok161.inv

DELFT HYDRAULICS

Z 722

Fig. 41d



TKE-IWE decomposition. Field measurements  
in Caland channel [ $Ri=4.9; N=0.082 \text{ rad/s}$ ].

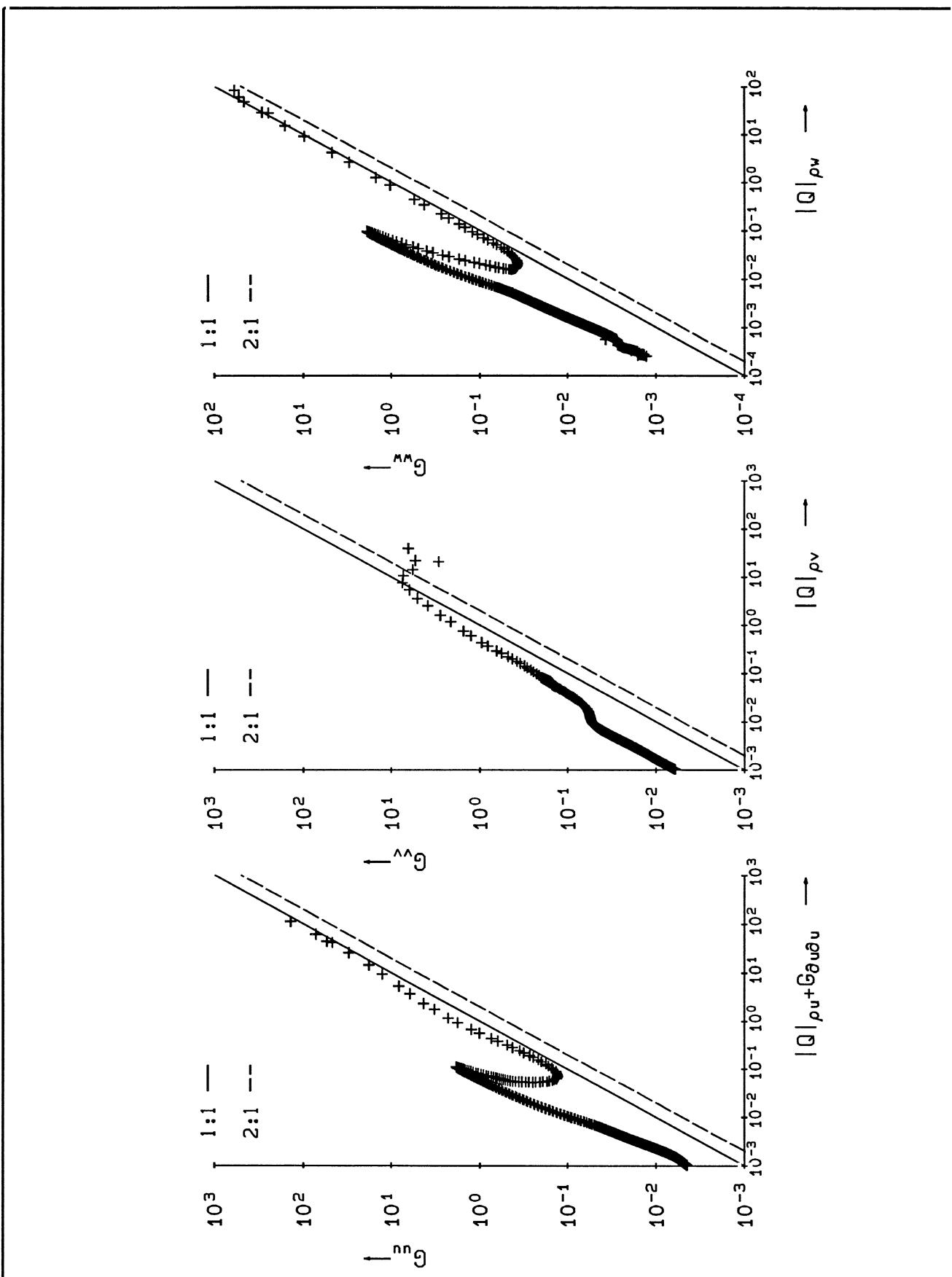
06.05.09:13|19-49 min

iwefield.913

DELFTHYDRAULICS

Z 722

Fig. 42<sup>a</sup>



Absolute quad spectra compared with power spectra of velocity components  $u$ ,  $v$ , and  $w$ .

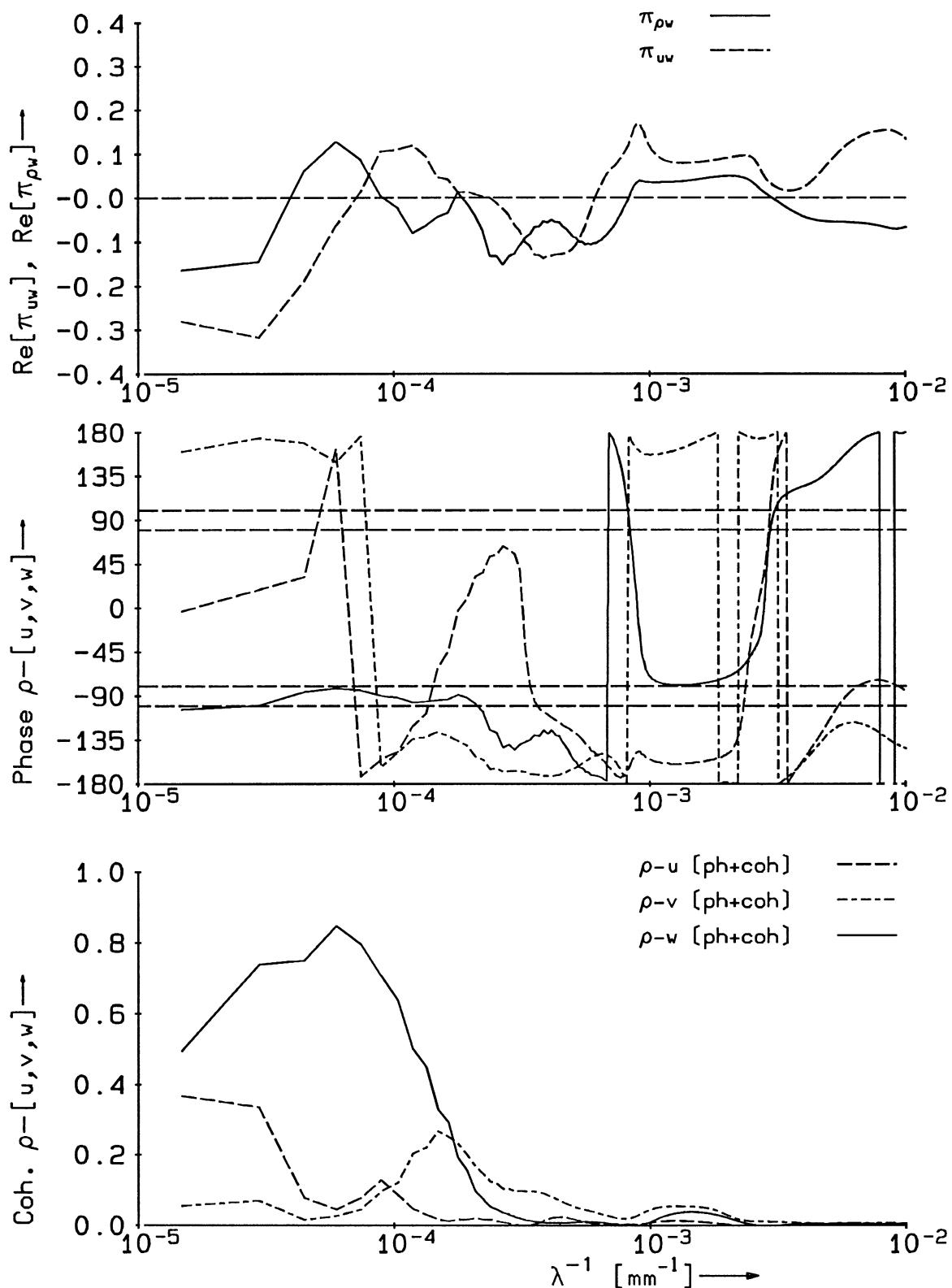
06.05.09:13|19-49 min

tet913.inv

DELFT HYDRAULICS

Z 722

Fig. 42<sup>b</sup>

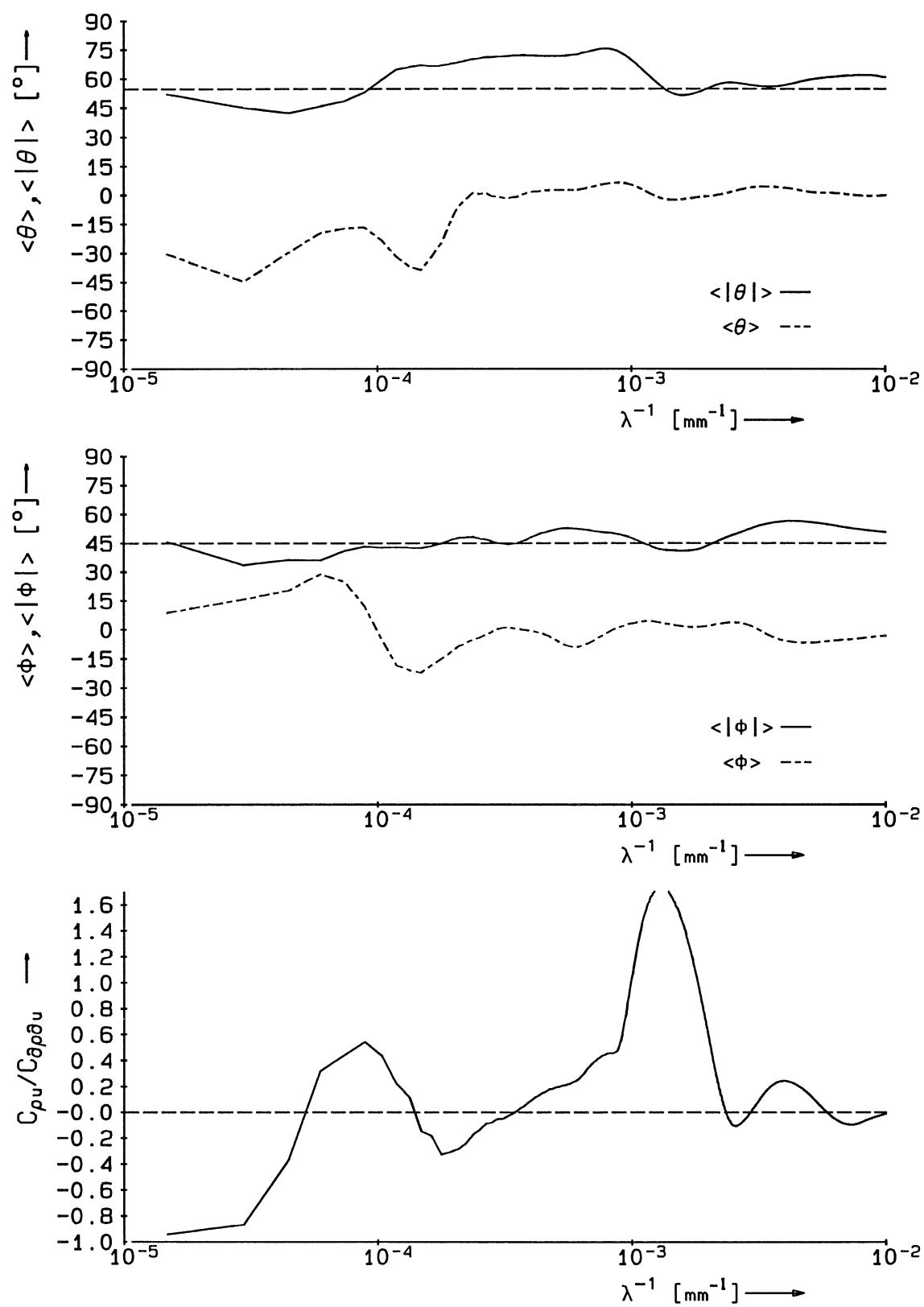


Phase, coherence, momentum and buoyancy fluxes.

06.05.09:13|19-49 min

Caland channel ( $Ri=4.9; N=0.082 \text{ rad/s}$ ).

iwe913.inv



Normalized Stokes mass drift and IW angles.

06.05.09:13|19-49 min

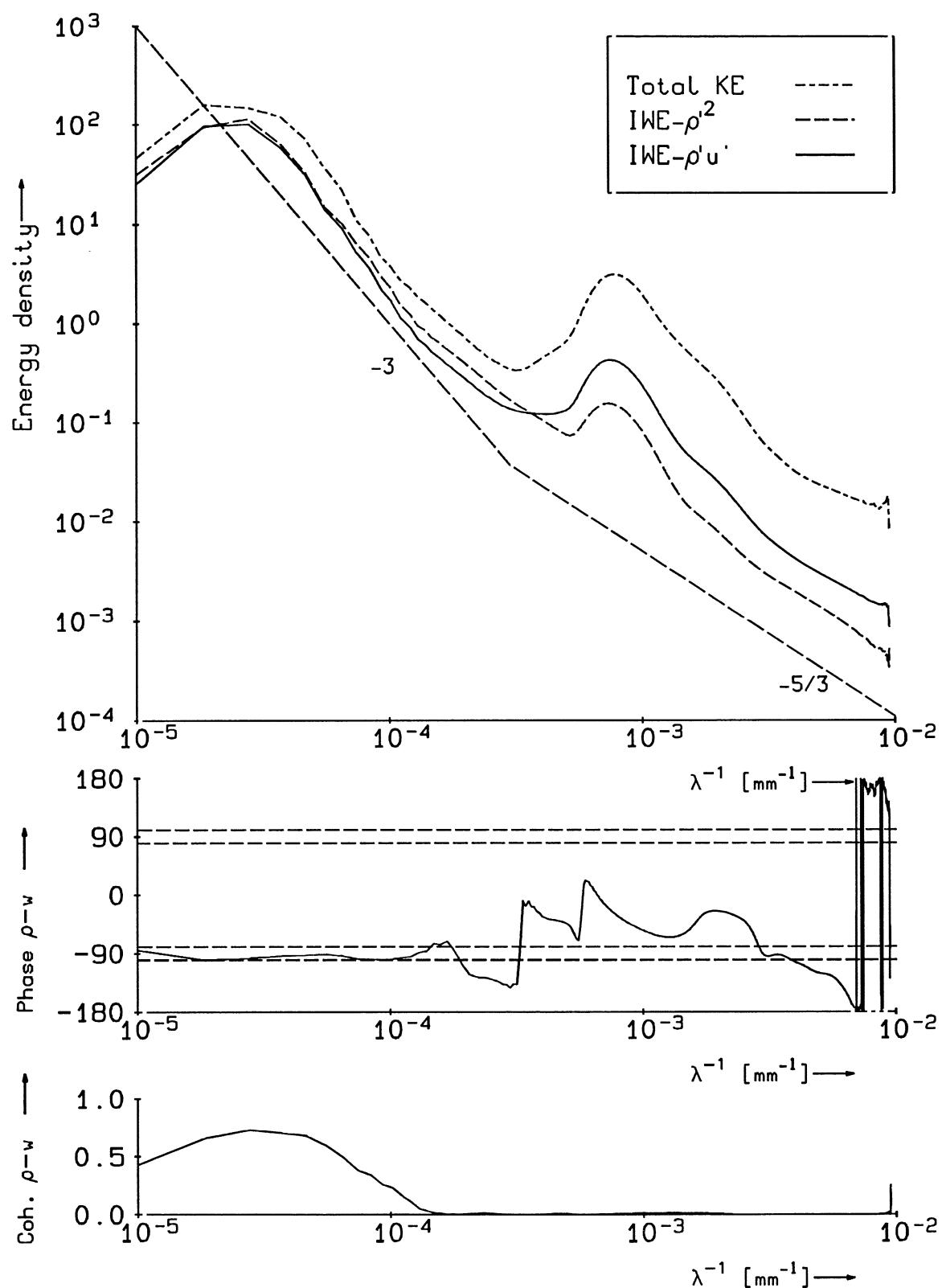
Rotterdam Waterway ( $Ri=4.9; N=0.082 \text{ rad/s}$ ).

stok913.inv

DELFTHYDRAULICS

Z 722

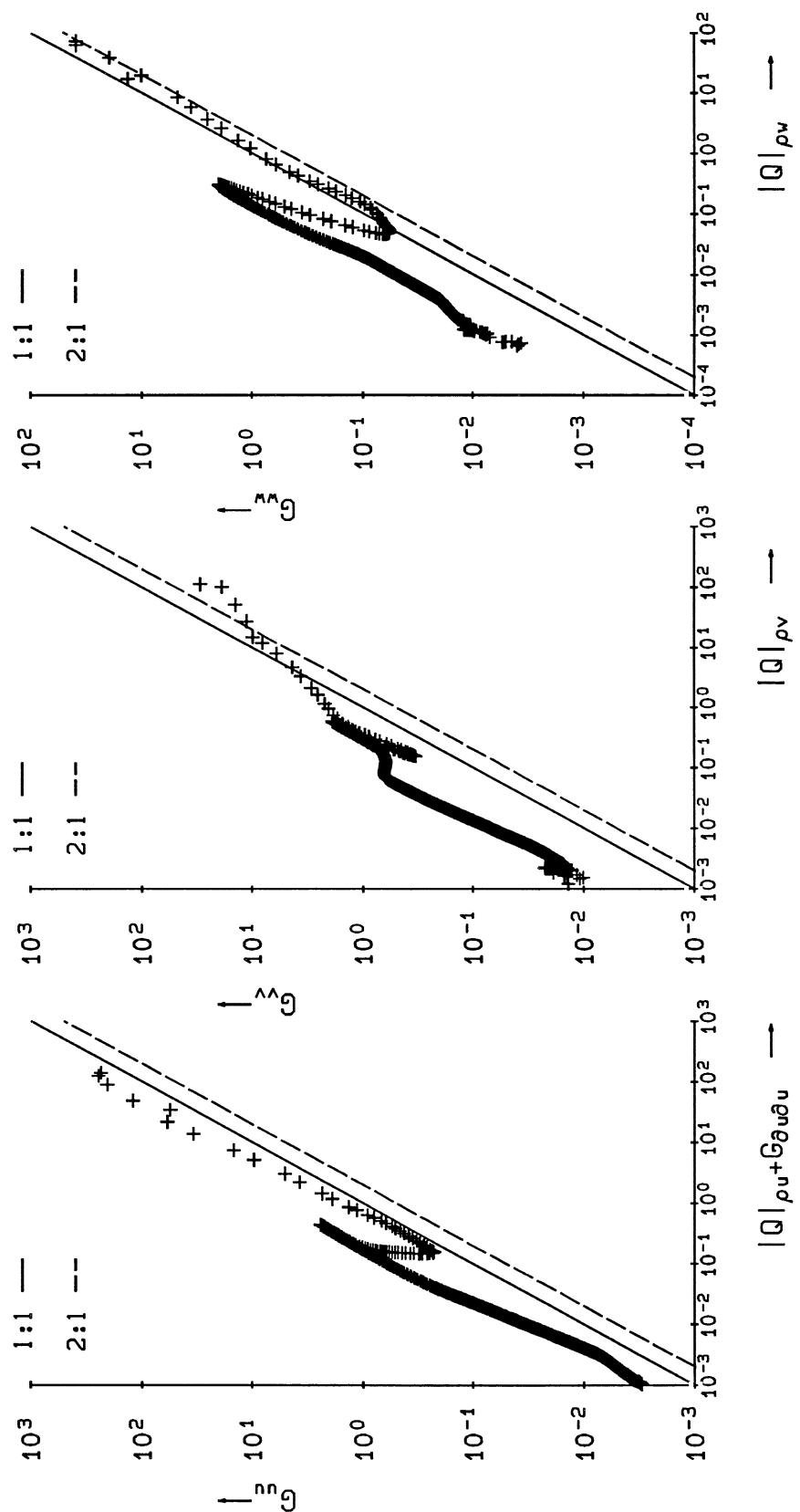
Fig. 42<sup>d</sup>



TKE-IWE decomposition. Field measurements  
in Caland channel [ $Ri=0.85; N=0.079 \text{ rad/s}$ ].

06.05.09:53|59-89 min

iwefield.953



Absolute quad spectra compared with power spectra of velocity components  $u$ ,  $v$ , and  $w$ .

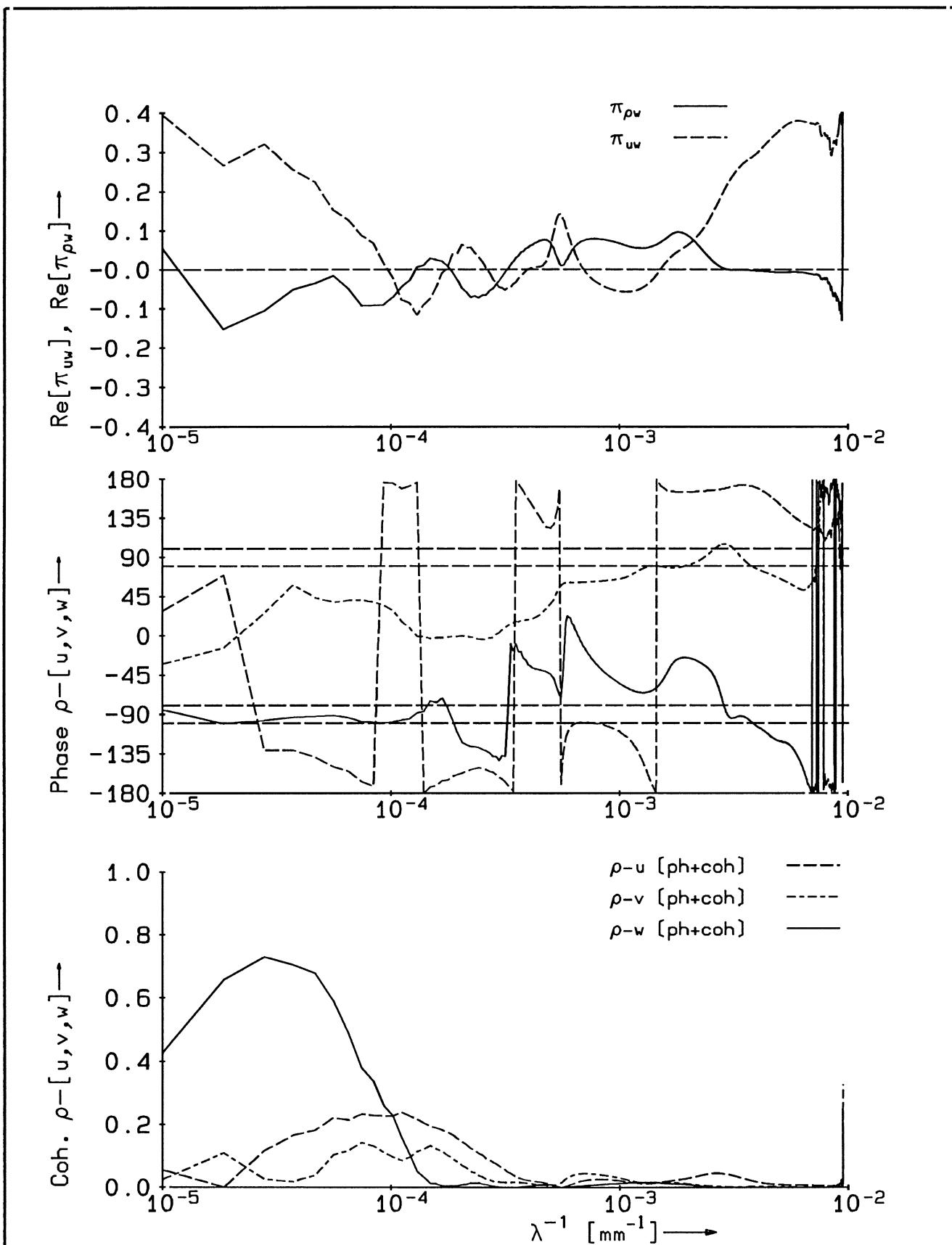
06.05.09:53|59-89 min

tet953.inv

DELFIT HYDRAULICS

Z 722

Fig. 43<sup>b</sup>

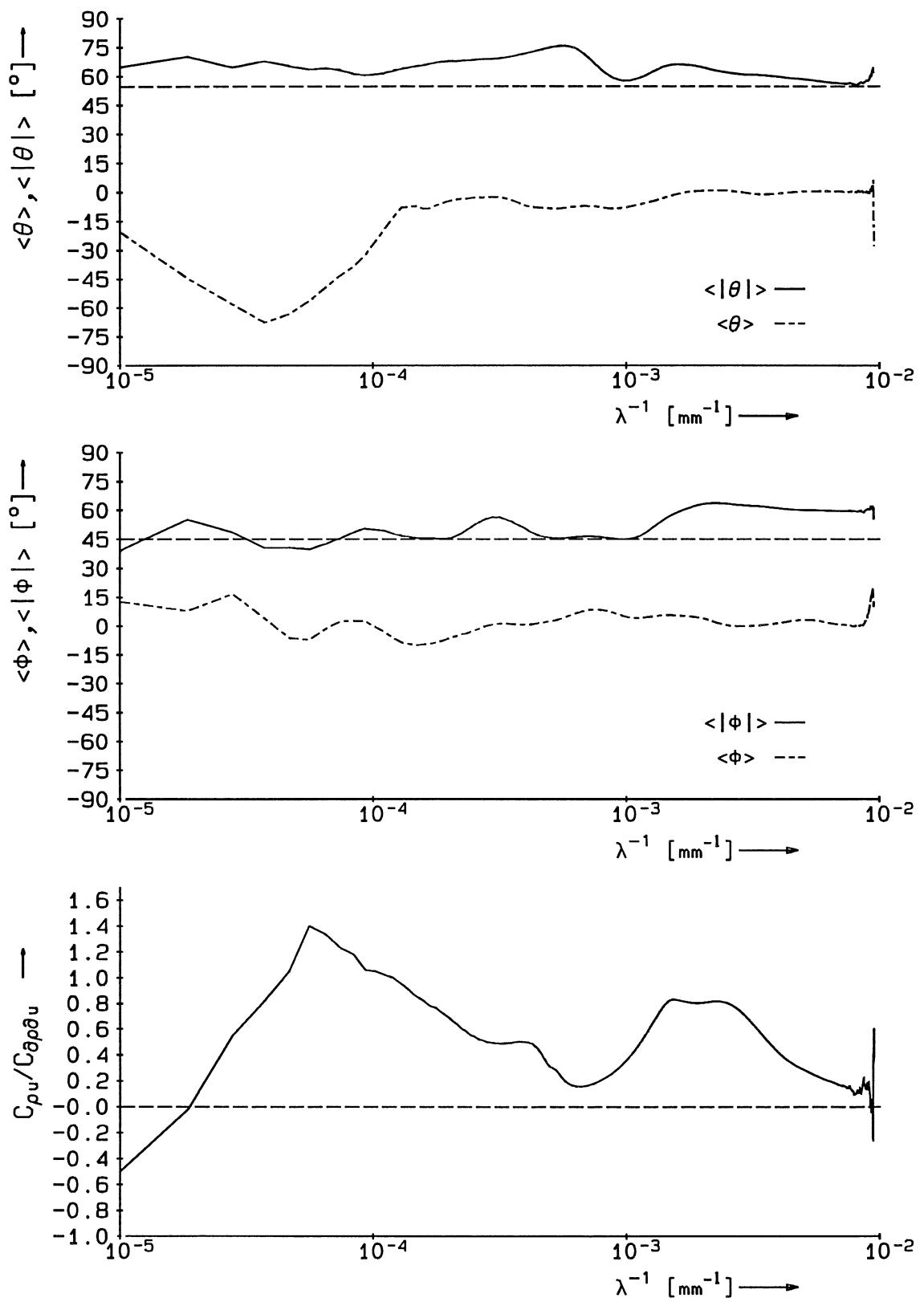


Phase, coherence, momentum and buoyancy fluxes.

Caland channel ( $Ri=0.85; N=0.079 \text{ rad/s}$ ).

06.05.09:53|59-89 min

iwe953.inv



Normalized Stokes mass drift and IW angles.

Rotterdam Waterway ( $Ri=0.85; N=0.079 \text{ rad/s}$ ).

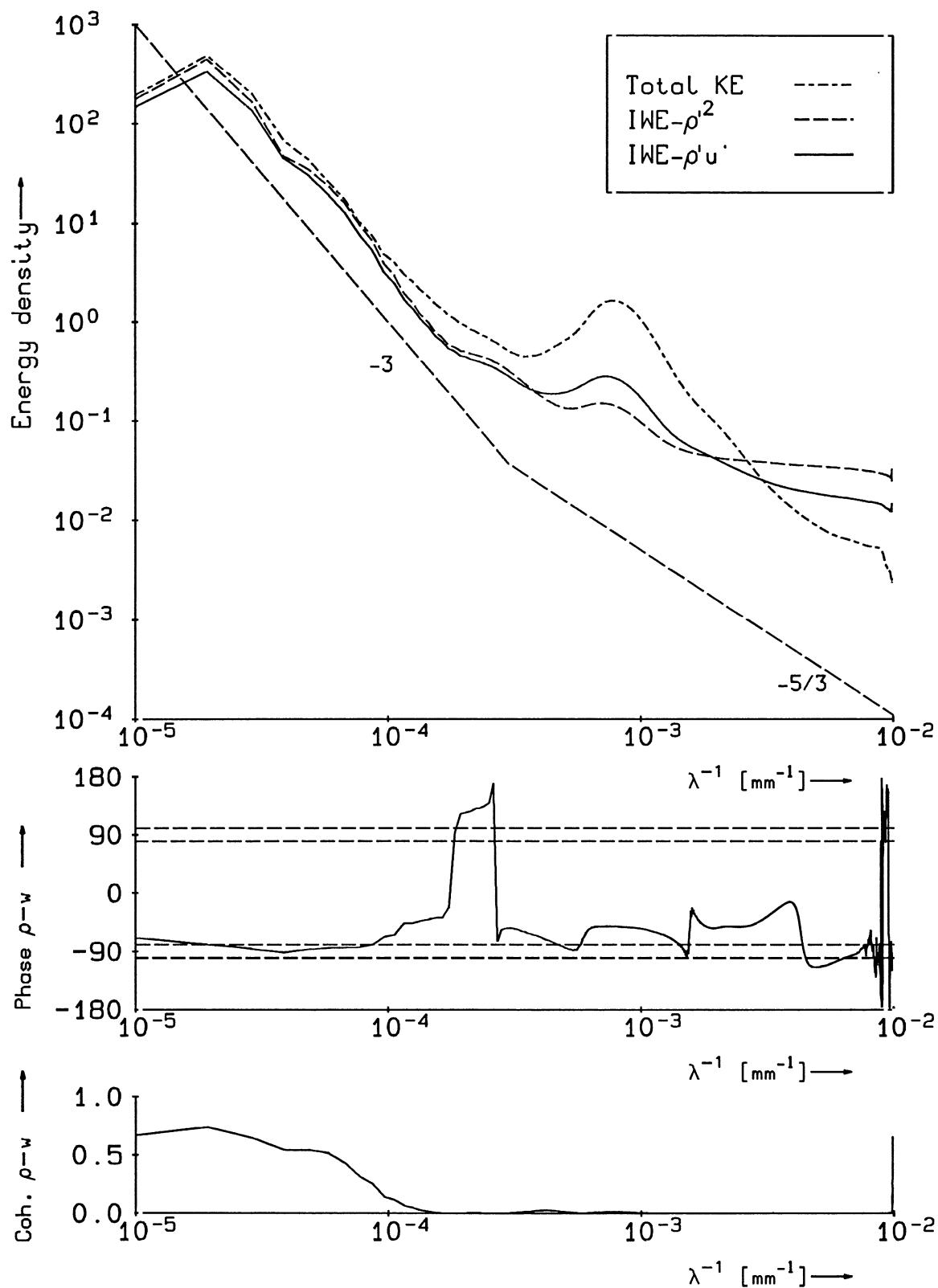
06.05.09:53|59-89 min

stok953.inv

DELFT HYDRAULICS

Z 722

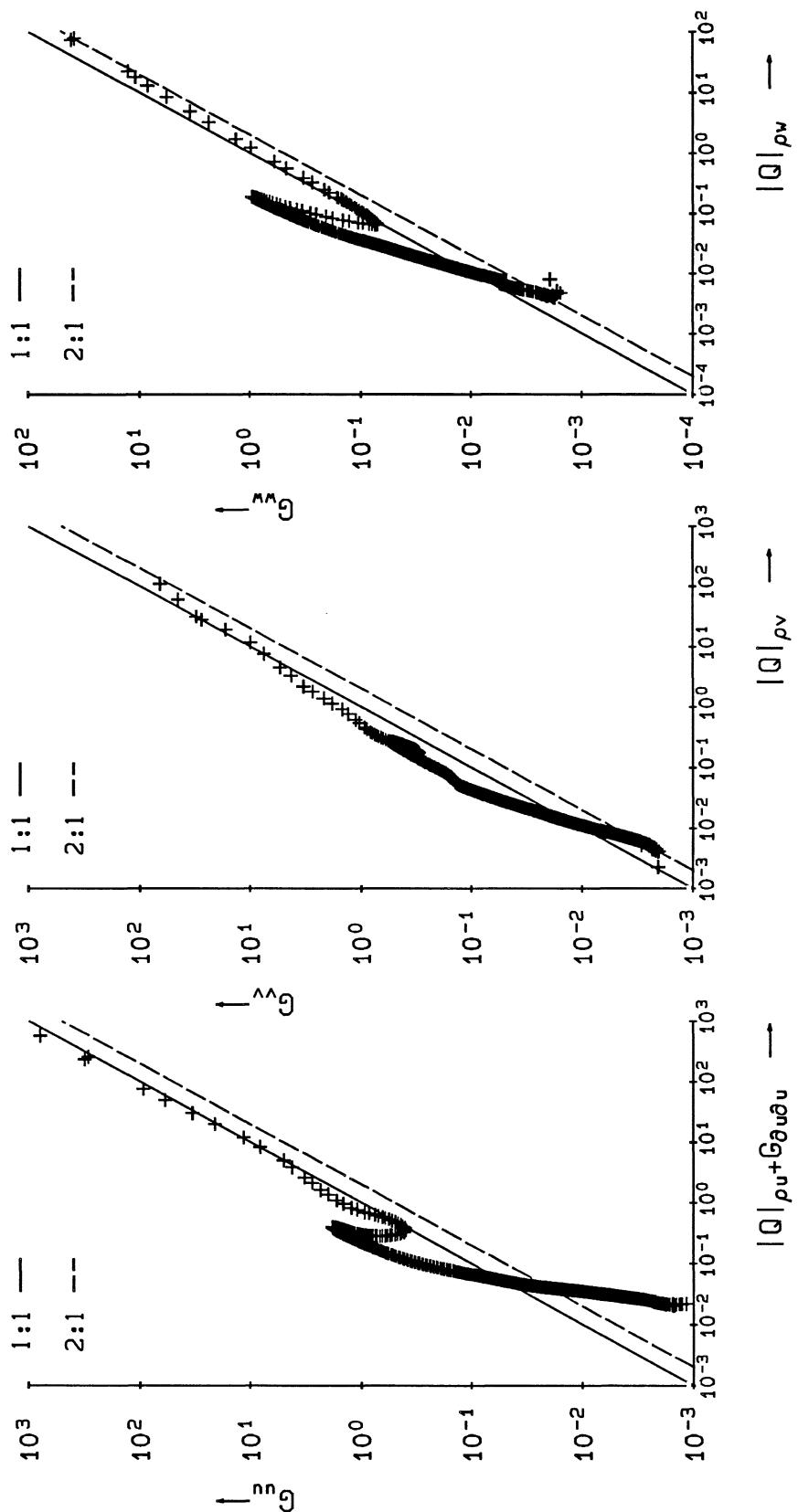
Fig. 43d



TKE-IWE decomposition. Field measurements  
in Caland channel ( $Ri=3.9; N=0.063 \text{ rad/s}$ ).

06.05.10:35|101-131 min

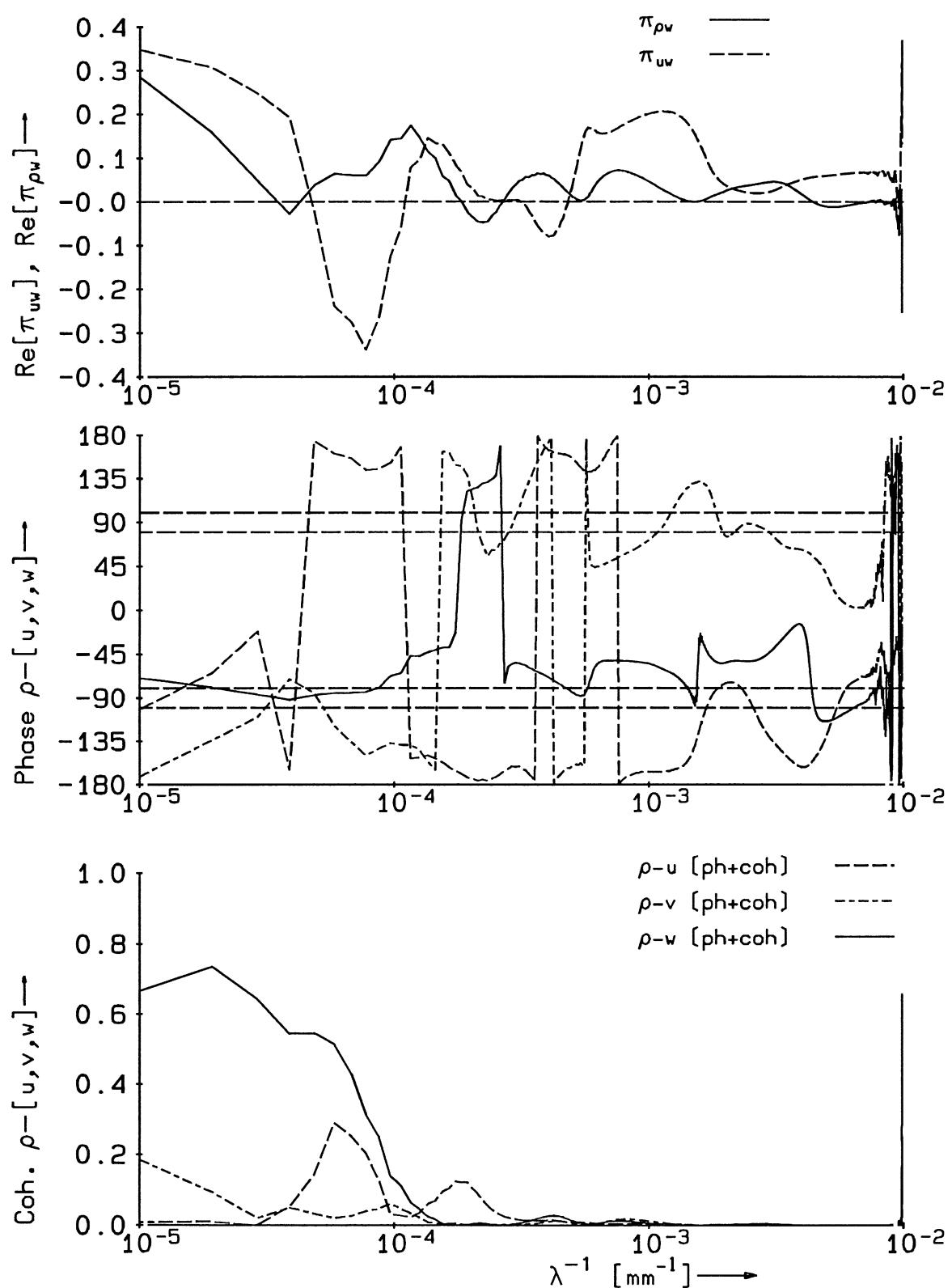
iwefield.103



Absolute quad spectra compared with power spectra of velocity components  $u$ ,  $v$ , and  $w$ .

06.05.10:35|101-131 min

tet103.inv



Phase, coherence, momentum and buoyancy fluxes.

06.05.10:35|101-131 min

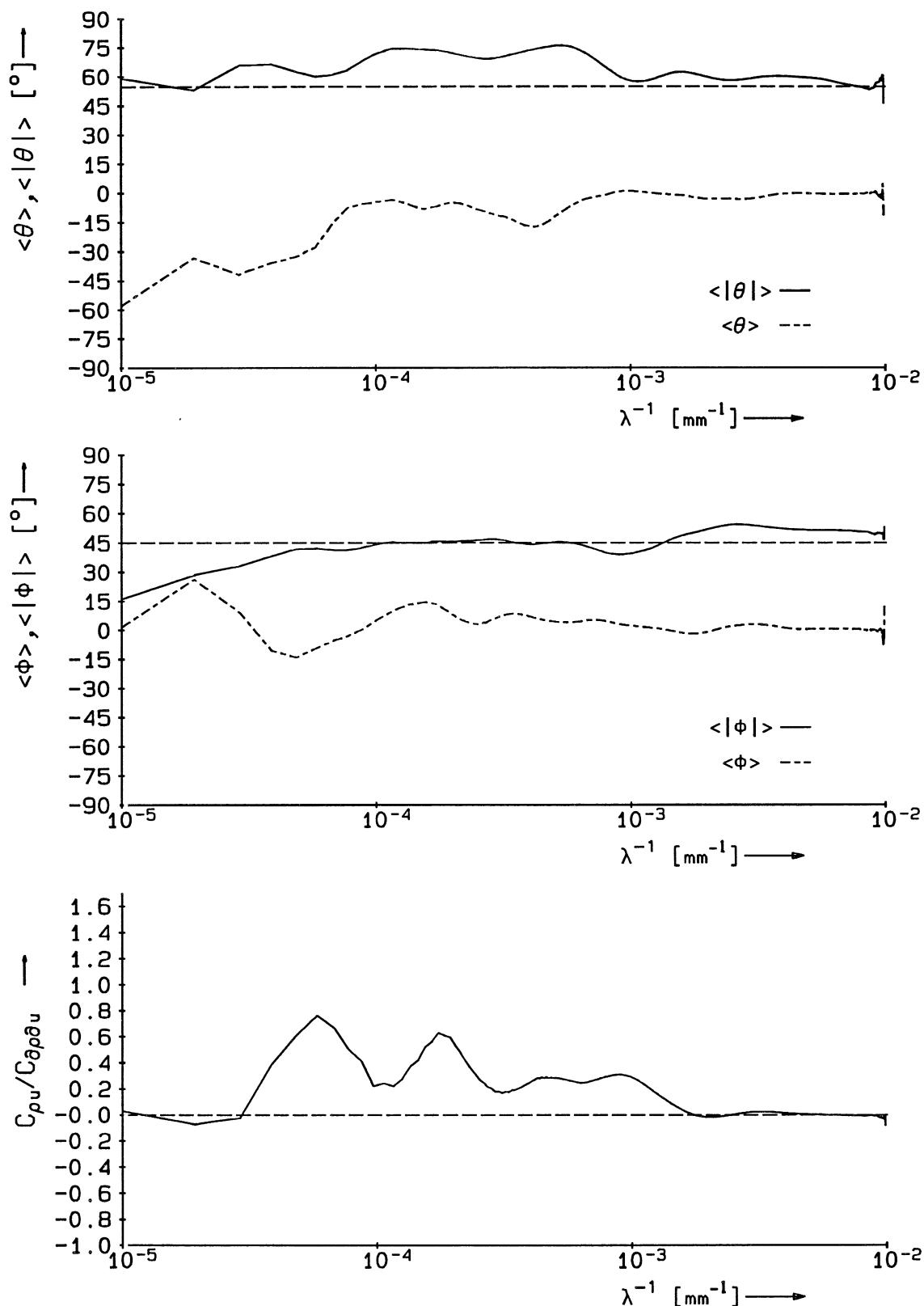
Caland channel ( $Ri=3.9; N=0.063 \text{ rad/s}$ ).

iwe103.inv

DELFT HYDRAULICS

Z 722

Fig.44<sup>c</sup>



Normalized Stokes mass drift and IW angles.

Rotterdam Waterway ( $Ri=3.9; N=0.063 \text{ rad/s}$ ).

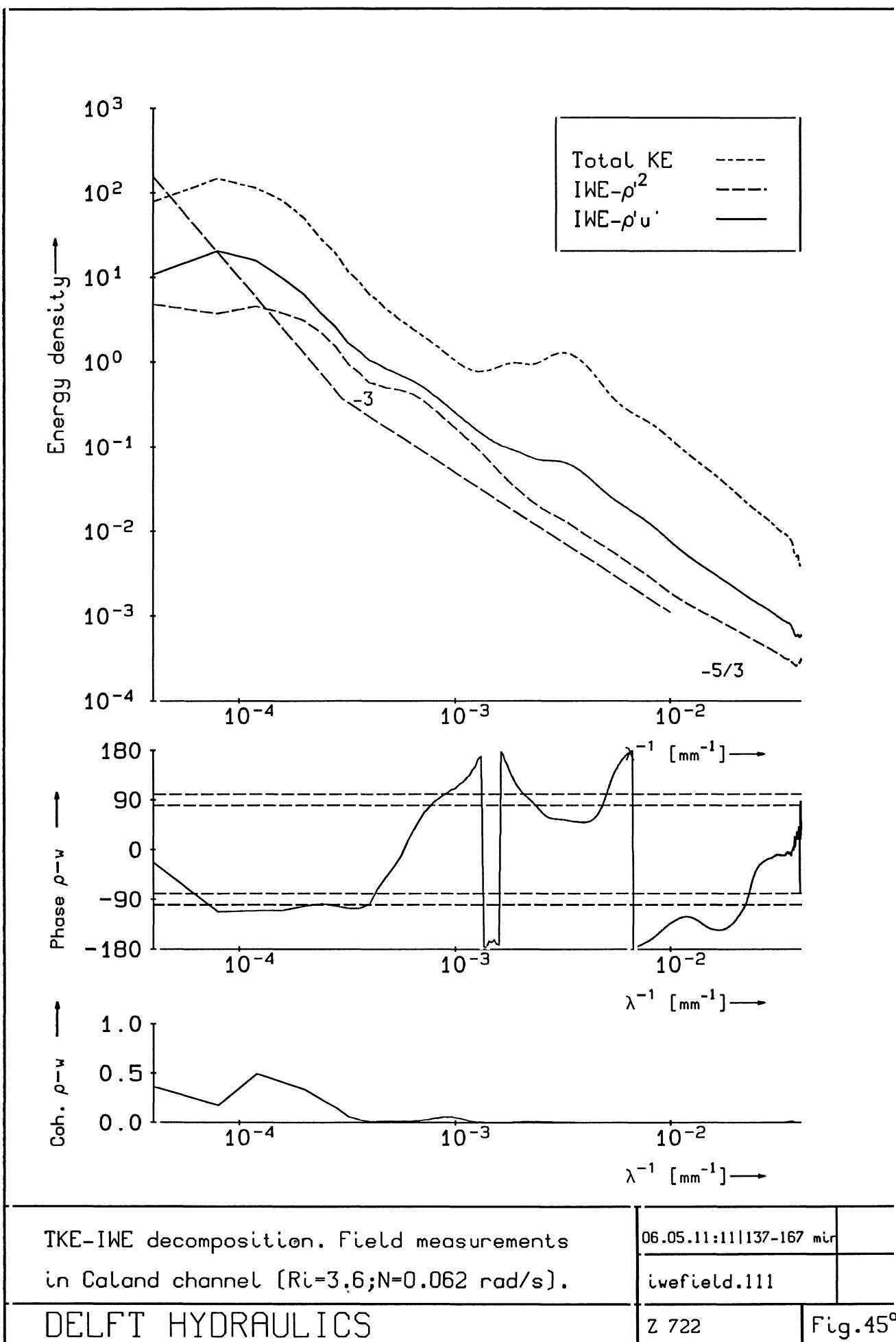
06.05.10:35|101-131 min

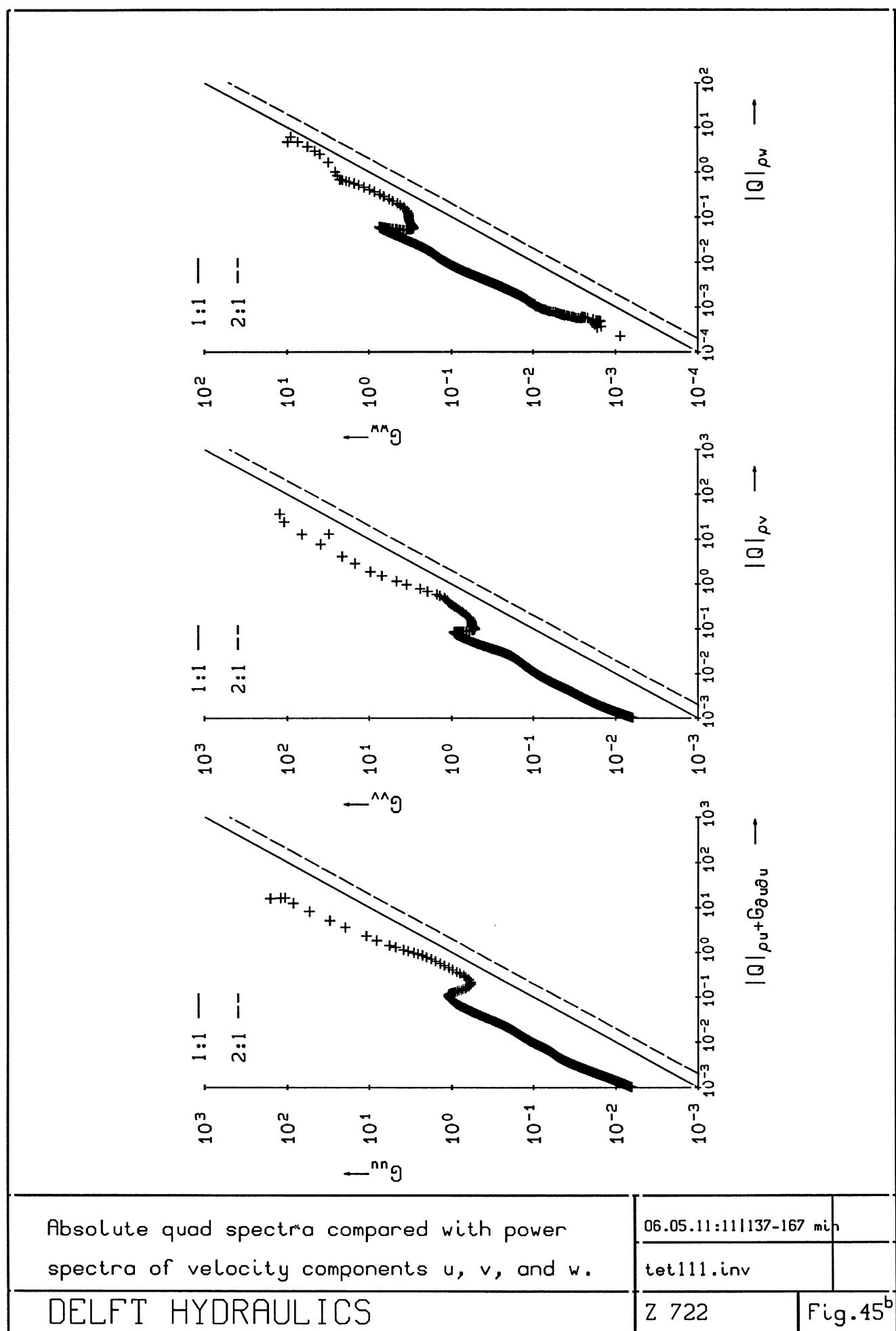
stok103.inv

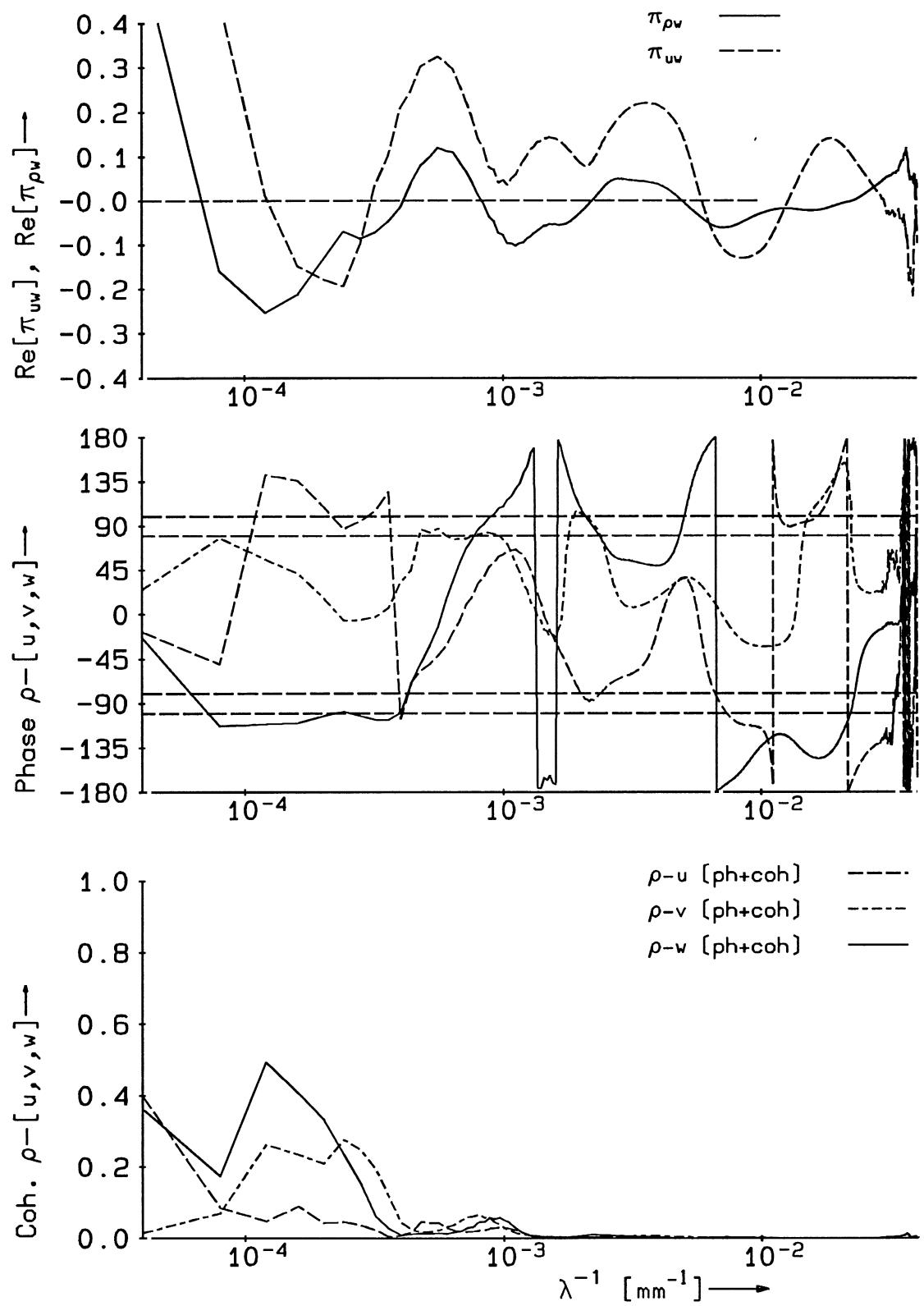
DELFT HYDRAULICS

Z 722

Fig. 44d





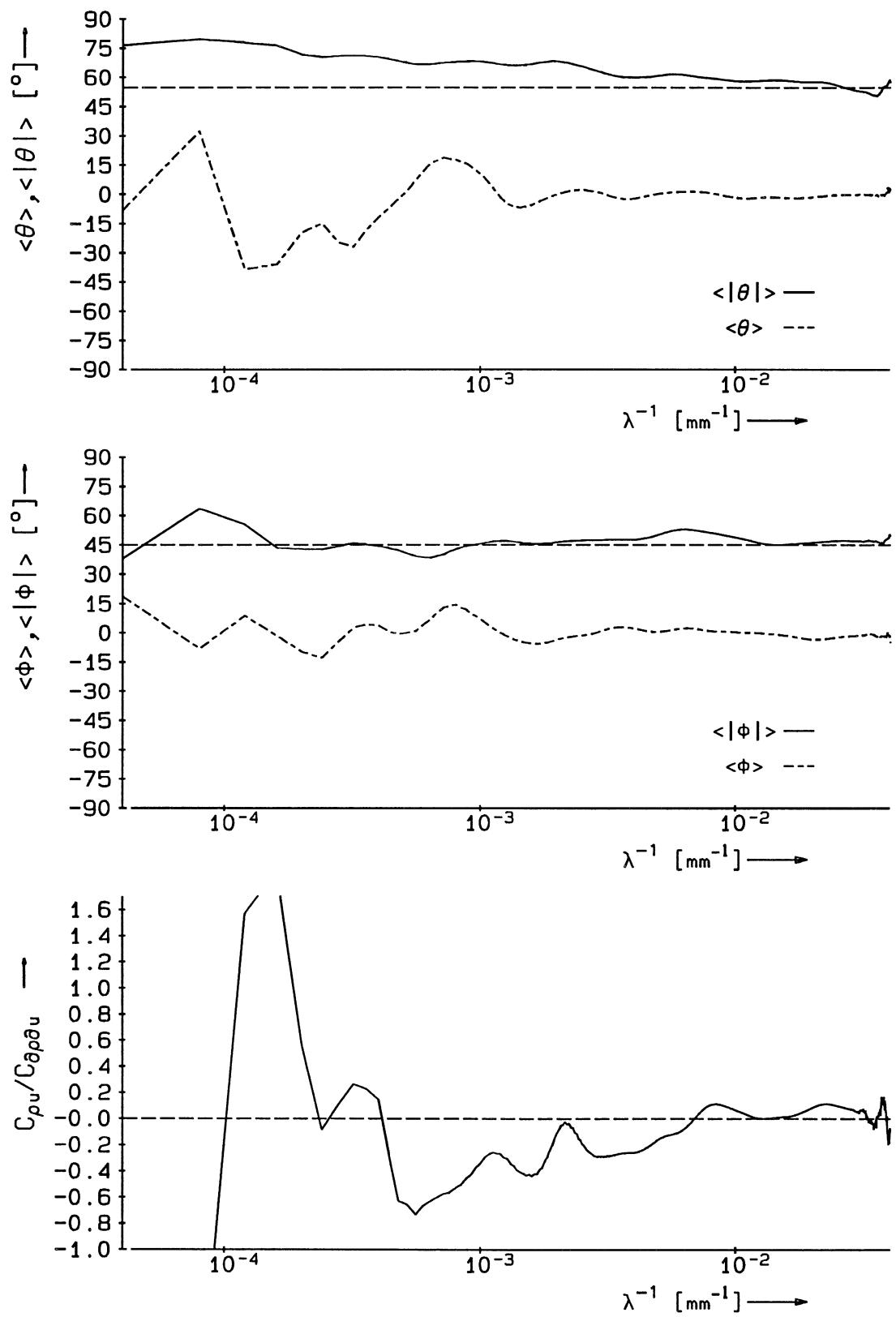


Phase, coherence, momentum and buoyancy fluxes.

06.05.11:11|137-167 min

Caland channel ( $Ri=3.6; N=0.062 \text{ rad/s}$ ).

iwe111.inv



Normalized Stokes mass drift and IW angles.

Rotterdam Waterway ( $Ri=3.6$ ;  $N=0.062$  rad/s).

06.05.11:11|137-167 mir

stok111.inv

DELFT HYDRAULICS

Z 722

Fig. 45d