Origin of Predominance of Cementite among Iron Carbides in Steel at Elevated Temperature

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A long-standing challenge in physics is to understand why cementite is the predominant carbide in steel. Here we show that the prevalent formation of cementite can be explained only by considering its stability at elevated temperature. A systematic highly accurate quantum mechanical study was conducted on the stability of binary iron carbides. The calculations show that all the iron carbides are unstable relative to the elemental solids, α-Fe and graphite. Apart from a cubic Fe23C6 phase, the energetically most favorable carbides exhibit hexagonal close-packed Fe sublattices. Finite-temperature analysis showed that contributions from lattice vibration and anomalous Curie-Weis magnetic ordering, rather than from the conventional lattice mismatch with the matrix, are the origin of the predominance of cementite during steel fabrication processes.

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Despite the fact that steel is one of the most commonly used materials in both old and modern times, the physical understanding of the formation and stability of iron and iron carbide phases is still in a premature state [1–5].

In the early 1950s, Hofer and Cohn investigated the formation of iron carbide precipitates in quenched steels [1,2]. They observed that the first stage of carbide formation occurs at temperatures between 370 and 470 K, where ε-Fe2C forms first. The second stage occurs at around 550 K, where the retained austenite decomposes into ferrite and η-Fe2C. In the third stage (470 to 720 K), θ-Fe3C and χ-Fe5C2 phases precipitate. Above 720 K only θ-Fe3C, cementite, is formed. Slowly cooling steels contain mainly ferrite and cementite [2]. θ-Fe3C was also found during carburization of iron [6]. Recent work shows that θ-Fe3C may play an important role in Earth’s core as well [7]. It was shown that cementite, as a weak magnet, shows almost no thermal expansion (Invar behavior) at the temperature below its Curie temperature [8,9]. Notwithstanding many theoretical efforts, very basic questions on steel remain unanswered [3–5,10]. One prominent question is why the cementite phase is observed much more frequently than other carbide phases in steel.

Iron carbides exhibit a rich variety of crystal structures and physical properties. Up to now, about a dozen structural models for binary iron carbides have been obtained or proposed by experimentalists, covering a wide variety of crystal structures [2,11–14].

To explain the predominance of cementite in steel, theoretical approaches, especially the electronic density-functional theory (DFT) techniques, can provide essential insights. Here we present a systematic DFT study on the formation and stability of binary iron carbides within the generalized gradient approximation, with details in Refs. [15,16]. Various structural models and magnetic orderings are examined for, in total, 17 carbide phases, and the factors that are considered to be important for the stability are discussed. Finally, we address the changes in the relative stability caused by lattice vibrations and magnetic ordering at elevated temperatures, which turn out to be of major importance to the formation of carbides.

We first performed total energy calculations for the elemental solids α-Fe and diamond. α-Fe has a bcc structure [15,16]. The calculations give a lattice parameter $a = 2.831$ Å and local moment $M = 2.21 \mu_B$/Fe which agree well with the experimental values ($a = 2.866$ Å and $M = 2.12 \mu_B$/atom). We performed calculations for diamond and added a correction term ($-17$ meV/C) in order to obtain the enthalpy for graphite [16] The calculated diamond lattice parameter is $3.5713$ Å, which agrees with the experimental value ($3.5668$ Å at $300$ K).

Taking the calculated energies of the elemental solids, we can obtain the formation enthalpy ($\Delta H_f$) of Fe$n$C$m$ at $T = 0$ K and $P = 0$ Pa, using the following formula whereby the zero-point vibration contribution is ignored:

$$\Delta H_f = [E(Fe^nC^m) - (nE(Fe) + mE(C))]/(n + m). \quad (1)$$

Figure 1 shows the calculated formation enthalpies for the iron carbides with $\Delta H_f < 150$ meV/at. The formation enthalpies for all the iron carbides are positive. This indicates that at $T = 0$ K and $P = 0$ Pa, none of the iron carbides are stable relative to the elemental solids (graphite and α-Fe), in agreement with experiments [2].

As shown in Fig. 1, the formation enthalpies of $\eta$-Fe2C (17.3 meV/at), $\chi$-Fe2C2 (18.6 meV/at), and θ-Fe3C (20.6 meV/at) are among the lowest. All three compounds have similar hexagonal close-packed (hcp-type) Fe sublattices [14]. The calculations also show that the orthorhombic $\eta$-Fe2C phase is the most stable carbide, while the hexagonal form ($\epsilon$-)Fe2C within a simple hcp
lattice as proposed by Jack in 1948 has a much higher formation enthalpy (~120 meV/atom) [17]. A hexagonal lattice $e$-Fe$_x$C was calculated to be slightly less stable than $\theta$-Fe$_x$C ($\Delta H_f = 25.1$ meV/atom vs $20.6$ meV/atom) [1,2,11]. Another relatively stable carbide is Fe$_3$C$_6$, which has a formation enthalpy comparable to that of $\theta$-Fe$_x$C (19.5 meV/atom vs 20.6 meV/atom). This carbide does not have a hcp-type Fe sublattice and has been discussed elsewhere [16].

As shown in Fig. 1, the calculations also show a trend of stability, $-\Delta H_f$, from high to low: $-\Delta H_f(\eta$-$Fe_2C) > -\Delta H_f(\chi$-$Fe_3C_2) > -\Delta H_f(\theta$-$Fe_2C)$. However, experimentally cementite is formed much more frequently in carbon steels than $\eta$-$Fe_2C$ or $\chi$-$Fe_3C_2$.

Conventionally, one of the most important factors stabilizing the $\theta$-$Fe_2C$ phase in steels is considered to be the interfacial energy between $\theta$-$Fe_2C$ and ferrite [2]. The interfacial energies are influenced, not only by the lattice matching as discussed by many experimentalists, but also by the chemical bonding at the interfaces. Fe$_2$C$_6$ has a small lattice mismatch with austenite [16], but is rarely observed in unalloyed steels. Analysis suggests that the high carbon solubility in austenite, the Fe vacancies needed for nucleation, and the distortion of the Fe planes at the metal-carbide interface are the culprits.

A careful analysis of the lattice matches between the iron carbides of the hcp family to the ferrite matrix has revealed that these carbides all have similar mismatches because their crystal structures are so similar. Hence it is unlikely that the lattice mismatch can explain the prevalence of cementite relative to $\eta$-$Fe_2C$ and $\chi$-$Fe_3C_2$.

Magnetism plays an important role in Fe and the iron carbides. Our calculations show that most of the iron carbides, including all the members of the hcp family, exhibit ferromagnetism, in spite of the fact that the ground state of a pure hcp-Fe crystal has a spiral magnetic ordering with a small local moment [18]. Below we discuss the influence of magnetism and lattice vibration on the stability of iron carbides of the hcp family.

Figure 1 shows that two iron carbides have lower formation enthalpies than that of cementite: $\eta$-$Fe_2C$ and $\chi$-$Fe_3C_2$. $\eta$-$Fe_2C$ is the most observed iron carbide at low temperature, while $\chi$-$Fe_3C_2$ is less commonly observed in steel, and its Curie temperature is not known. Therefore, we only compare the temperature-dependent relative stability of $\eta$-$Fe_2C$ and $\theta$-$Fe_2C$. Hofer and Cohen [1] reported that cementite is formed from $\eta$-$Fe_2C$ and $\alpha$-Fe:

$$\eta$-$Fe_2C + \alpha$-Fe $\leftrightarrow \theta$-$Fe_2C.$

In order to determine the relative stability of $\theta$-$Fe_2C$ with respect to $\eta$-$Fe_2C$ and $\alpha$-Fe, we have calculated both the magnetic contribution and the lattice vibration contribution (including zero-point vibrations) to the stability of these three phases. The Gibbs energy can be separated into two contributions [19], as

$$G_{total}(T) = G_{nonmagn}(T) + G_{magn}(T).$$

The nonmagnetic terms include contributions from lattice vibrations and electronic excitations. The lattice vi-

![FIG. 1. Formation enthalpies, $\Delta H_f$ [see Eq. (1)], for iron carbides ($Fe_xC_m$) with respect to the elemental solids (graphite and $\alpha$-Fe) from first-principles calculations. For clarity, the data for hexagonal $e$-Fe$_x$C ($x = 2, 3$) are not included.](image-url)
... and theoretically [24–26]. The thermodynamic properties of cementite were studied as well [27]. For the sake of a systematic study, we performed phonon calculations for \( \alpha \)-Fe, \( \eta \)-Fe\(_2\)C, and \( \theta \)-Fe\(_2\)C employing the harmonic approximation [28] with the force constants obtained using the DFT–generalized-gradient-approximation method. The calculated results of the phonon spectra and phonon density of states are very close to those in the literature for \( \alpha \)-Fe [24,25] and \( \theta \)-Fe\(_2\)C [26]. The calculated phonon spectrum of \( \eta \)-Fe\(_2\)C, being similar to that of \( \theta \)-Fe\(_2\)C, consists of three separated parts: the low energy part (0 to 40 meV) from Fe contribution, and two rather narrow bands at high energies of C contributions. Details of the...
calculations and phonon spectra of the phases will be discussed elsewhere.

Figures 2(a)–2(c) show the computed specific heat of θ-Fe₂C, η-Fe₂C, and α-Fe, respectively. The magnetic contribution to the specific heat was obtained using Eq. (5) with the parameters in Table I. The free energy of an iron carbide is obtained from the computed specific heat.

The free energy difference \[ \Delta G^{\text{Fe}_3\text{C}}(T)_{\text{total}} \] between Fe₃C and \{η-Fe₂C + Fe\} can now be evaluated by substituting all values into Eqs. (3) and (4). The result is displayed in Fig. 2(d). The vibrational contribution to \[ \Delta G^{\text{Fe}_3\text{C}}(T)_{\text{total}} \] is \(-0.50 \text{ kJ/mol} \) at \( T = 0 \text{ K} \) because of the zero-point vibration contributions, and then decreases gradually with increasing temperature. On the other hand, the contribution from magnetic ordering (Curie-Weiss behavior) is zero at \( T = 0 \text{ K} \), remains nearly zero up to 300 K, and then starts to decrease significantly. Considering the total energy difference [black solid curve in Fig. 2(d)], it is clear that η-Fe₂C is more stable at low temperatures. With increasing temperature, the energy difference between η-Fe₂C and θ-Fe₃C becomes smaller, and above 330 K, θ-Fe₃C is more stable than η-Fe₂C.

Figures 1 and 2(d), show that, at low temperature, nucleation and crystal growth of iron carbide precipitates will occur with initial formation of η-Fe₂C, due to its low formation enthalpy. During heating, contributions from lattice vibrations and magnetism increase the stability of θ-Fe₃C. When the temperature is high enough to overcome the transformation barrier, η-Fe₂C transforms to θ-Fe₃C. On the other hand, for slow-cooling processes at elevated temperatures θ-Fe₃C is formed without η-Fe₂C as an intermediary. Recently, Schneider and Inden found that the activation energy barrier for carbon diffusion in cementite is about 1.79 eV/atom [29]. The activation energy barriers will prevent transformation to other phases, such as η-Fe₂C and/or η-Fe₂C₂ at low temperature. This clarifies the experimental observation of preferential θ-Fe₃C formation during steel fabrication processes.

Furthermore, it can be concluded that in comparison with other materials, the stability of iron carbides is rather subtle and that magnetism can have a determining influence. Therefore, a careful assessment of temperature-dependent energetics is required for making reliable stability predictions.

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[15] All calculations were carried out using the vasp code employing the density-functional theory within the projector-augmented wave method. The generalized gradient approximation by J. P. Perdew, K. Burke, and M. Ernzerhof, Phys. Rev. Lett. 77, 3865 (1996) was employed for the exchange and correlation energy terms. The cutoff energy of the wave functions was 500 eV. Dense k meshes were used, e.g., a 12 × 12 × 12 grid with 84 k points in the irreducible Brillouin zone of θ-Fe₃C using the H. J. Monkhorst and J. D. Pack method, Phys. Rev. B 13, 5188 (1976). Details of settings are described in Ref. [16].