Magnetic fluctuations and correlations in MnSi: Evidence for a chiral skyrmion spin liquid phase

C. Pappas,1,2,4 E. Lelièvre-Berna,3 P. Bentley,3 P. Falus,3 P. Fouquet,3 and B. Farago3
1Delft University of Technology, Faculty of Applied Sciences, Meekeweg 15, NL-2629JB Delft, The Netherlands
2Helmholtz Center Berlin for Materials and Energy, Glienickerstr. 100, DE-14119 Berlin, Germany
3Institut Laue Langevin, 6, Rue Jules Horowitz, FR-38042 Grenoble, France

(Received 2 March 2011; revised manuscript received 10 April 2011; published 20 June 2011)

We present a comprehensive analysis of high-resolution neutron scattering data involving neutron spin echo spectroscopy and spherical polarimetry, which confirm the first-order nature of the helical transition in MnSi. The experiments reveal the existence of a totally chiral dynamic phase in a very narrow temperature range above $T_C$. This unconventional magnetic short-range order has a topology similar to that of a skyrmion liquid or the blue phases of liquid crystals.

DOI: 10.1103/PhysRevB.83.224405 PACS number(s): 75.25.—j, 28.20.Cz, 12.39.Dc, 75.10.Kt

I. INTRODUCTION

MnSi is one of the most investigated chiral magnets and, at least in theory, a very simple realization of chiral magnetism. The Ginzburg-Landau Hamiltonian contains three hierarchically ordered interaction terms with well-separated energy scales;1 It is therefore possible to distinguish between the different contributions to the ground state. The strongest ferromagnetic exchange interaction term fixes the spins at the crystallographic lattice. The magnetically ordered state of inversion symmetry in the crystallographic structure is at $\tau_{111}$, with $\tau = |\tau_{111}| = 0.036 \text{ Å}^{-1}$.

MnSi is a weak itinerant magnet with an ordered magnetic moment of only 0.4 $\mu_B$, a fraction of the effective magnetic moment of 1.4 $\mu_B$ determined in the paramagnetic phase.3 The strong magnetic fluctuations, which are due to the weak itinerant magnetism and the vicinity of a magnetic instability, exist not only above $T_C$,5 but also persist in the low-temperature ordered phase.9 The magnetic fluctuations lead to an enhanced effective electron mass, a broad specific heat maximum reminiscent of the specific heat of spin liquids, frustrated magnets or spin glasses,7 and broad features on thermal expansion and ultrasound measurements, which almost completely mask the helical transition.8

One intriguing feature of MnSi is that magnetic correlations above $T_C$ appear not only around the positions in reciprocal space of the helical order, but spread homogeneously over the whole surface of a sphere with radius $\tau$ emerging as a powder-diffraction-like ring on the two-dimensional small-angle neutron scattering spectra.9 If the neutron beam is polarized, the rings reduce to half-moons due to the interaction between polarized neutrons with the helical correlations as explained below.

This unconventional feature occurs in a limited temperature range above $T_C$ and is reminiscent of scattering patterns from cholesteric liquid crystals, suggesting the existence of similar textures also in magnets. However, the chiral molecules of liquid crystals are rods, whereas magnetic moments are vectors. This additional topological constraint leads to the formation of domain walls rendering domain-wall formation is minimized by higher-order skyrmionlike 2\pi disclinations.

Skyrmions were introduced in the early 1960s by Skyrme11 to bridge the gap between waves and particles in the particle-wave duality description. The existence of these solitonlike quasiparticles was alleged in semiconductors under high magnetic fields12 and their topology corresponds to that of the blue phases of liquid crystals.13 Their existence in magnets was first suggested in the late 1980s by Bogdanov and Yablonskii.14 Periodic skyrmion lattices may form under a magnetic field in the A phase of MnSi (Ref. 15) and have been directly seen by Lorentz transmission electron microscopy in Fe$_{0.5}$Co$_{0.5}$Si (Ref. 16) and FeGe.17

It has been suggested that the unconventional diffuse scattering above $T_C$ reflects the existence of skyrmion-like textures, which would form spontaneously without any structural defects or external magnetic field18 stabilized by spin stiffness. Skyrmionic textures may also emerge in other approaches, where e.g. higher order terms were introduced.19,20 As in liquid crystals, this ground state of condensed matter would occur at a very restricted temperature range just above the long-range-ordered helical phase. This was confirmed by recent numerical work, which evidences an unconventional short-range order above $T_C$ similar to that of the blue phases in liquid crystals5 and reproduce the neutron scattering patterns. In the following, we present high-resolution polarized neutron scattering experimental results, which support this hypothesis by revealing the existence of a completely chiral fluctuating phase just above $T_C$. The transition to the helical phase is of first order.

II. EXPERIMENTAL METHOD

MnSi crystallizes in the cubic P2$_1$3 (T4) structure with the Mn atoms occupying the 4a site for $x = 0.138$. The lack of inversion symmetry in the crystallographic structure is at...
the origin of the DM interaction, the chiral magnetism, and the helical magnetic structure. The experiments were done on a well-characterized single-crystalline sample with a thickness of 2 mm and a diameter of 20 mm, cut from a large single crystal grown at Ames Laboratory. The lattice constant was 4.558 Å. The sample was oriented with a (110) direction vertical, so that four 111 reflections and two 110 reflections were accessible in the horizontal scattering plane.

The polarized neutron scattering experiments were carried out with the neutron spin echo spectrometers IN11 and IN15 at the Institut Laue Langevin, Grenoble, France. On IN15, the wavelength was 8 Å and on IN11 it was 6.5 Å. At both instruments, the incoming neutron beam had a monochromatization of 15% full width at half maximum (FWHM). The XY position sensitive detectors of both spectrometers covered an angular range of \(\sim 3 \times 3 \text{ deg} \) and the resolution in momentum transfer \(Q\) was \(\sim 0.005 \text{ Å}^{-1} \text{ FWHM}.\) On IN11, the \(Q\) dependence of the relaxation and the intensity was analyzed by taking slices of the detector at constant distance from the 000 point and also from the surface of the sphere with radius \(\tau\) leading to \(-0.005 \text{ Å}^{-1} \leq q = |\vec{Q}| - \tau \leq 0.018 \text{ Å}^{-1}.\) The measurements were carried out at one of the four equivalent magnetic reflections 000 + \(\tau_{111}.\) On IN11, it was also possible to measure at a 000 + \(\tau_{110}\) point, where the correlations do not develop to a Bragg peak.

Figure 1 shows on a log-lin scale the temperature dependence of the neutron intensity at \(\tau_{111}.\) The helimagnetic phase transition is marked by an intensity jump of more than one order of magnitude within less than 0.1 deg. The data above and below \(T_C\) follow power laws similar to those found previously and which were at the origin of a long-standing controversy on the order of the transition. These power laws, however, do not account for the intensity jump, which confirms the first-order phase transition seen by specific heat.\(^{23}\)

The intensity jump defines very accurately the transition temperature \(T_C = 29.05 \pm 0.05 \text{ K}.\) These data were collected on IN15. A different cryostat and thermometer were used on IN11 and the jump was observed at \(T_C = 28.6 \pm 0.05 \text{ K}.\) In order to compare the data sets, the results will be plotted against \(T - T_C\) or the reduced temperature \(\epsilon = (T - T_C)/T_C.\)

The helical Bragg peaks are the fingerprint of the helical phase. They are elastic (energy transfer \(\hbar\omega = 0\); in the following, we will often use \(\omega\) to also designate the energy transfer without explicitly using \(\hbar\)) and have a Gaussian lineshape. In contrast, the fluctuating paramagnetic phase above \(T_C\) has finite correlations and the scattering function \(S(Q,\omega)\) is a superposition of Lorentzians.\(^{5,6}\) In the quasielastic limit, where the energy transfer is much smaller than the energies of the incoming beam and of the sample, the neutron scattering cross section becomes

\[
\frac{d^2\sigma}{dQdE} \propto S(Q,\omega) \propto \frac{C}{q^2 + \kappa^2} \frac{\Gamma}{\Gamma^2 + \omega^2} \quad (1)
\]

with \(C\) the Curie constant, \(\kappa = 1/\xi,\) where \(\xi\) is the characteristic correlation length, and \(\Gamma\) is the half width at half maximum (HWHM) energy linewidth. \(S(Q,\omega)\) is therefore the product of the static structure factor, which has the Ornstein-Zernike (OZ) form

\[
S(Q) = \int S(Q,\omega) d\omega \propto \frac{C}{q^2 + \kappa^2} \quad (2)
\]

and of the dynamic structure factor

\[
s(Q,\omega) = \frac{S(Q,\omega)}{S(Q)} \propto \frac{\Gamma}{\Gamma^2 + \omega^2}. \quad (3)
\]

The dynamic measurements were performed by neutron spin echo (NSE) spectroscopy, which uses the Larmor precession of the neutron spin in a magnetic field as a clock to measure with very high accuracy the difference in neutron velocities before and after the scattering process at the sample. The changes in the neutron energy due to inelastic scattering affect the neutron velocity and, consequently, the amplitude of the Larmor precessions. In this way, the energy transfer is measured directly by circumventing the intensity resolution limitations of the Liouville theorem. For this reason, NSE reaches very high resolutions while maintaining the high intensity advantage of a beam that is only 10%–20% monochromatic. The highest energy resolution in neutron scattering is presently reached by IN15, which accesses energies as low as some meV corresponding to motions with characteristic times reaching the \(\mu s.\)

At the quasielastic limit, which is valid in most NSE experiments, the amplitude of the NSE Larmor precessions is directly proportional to the intermediate scattering function \(I(Q,t),\) the Fourier transformation of \(s(Q,\omega).\)\(^{24}\) The comparison between NSE and inelastic neutron scattering is therefore straightforward through a Fourier transformation

\[
I(Q,t) = \frac{\int S(Q,\omega) \cos(\omega t) d\omega}{\int S(Q,\omega) d\omega} = \frac{\Re[S(Q,t)]}{S(Q)}. \quad (4)
\]

Consequently, the Lorentz function of Eq. (3) Fourier transforms to the exponential NSE decay \(\exp(-t/t_0)\) with \(t_0 = 1/\Gamma\) leading to \(t_0[\mu s] = 0.658/\Gamma[\mu eV].\) With this relation, it will be possible to compare our NSE results with the triple-axis neutron spectroscopy (TAS) measurements from the literature.\(^{5,25}\)

This so-called Larmor labeling requires polarized neutrons and some polarization analysis features are an integral part of NSE.\(^{26}\) The pulse sequence, \(\pi/2\) flip-precession-\(\pi\) flip (at the sample)-precession-\(\pi/2\) flip, is that of the classical Hahn sequence of NMR Spin Echo “Normal” paramagnetic

![FIG. 1. (Color online) Temperature dependence of the logarithm of the intensity at the position of the helical peak (\(\tau_{111} = 0.036 \text{ Å}^{-1}\)). An intensity jump of almost one order of magnitude defines the helical transition \(T_C.\)](224405-2)
scattering acts as a $\pi$ flipper and gives an echo without the otherwise obligatory $\pi$ flipper, which leads to a straightforward and unambiguous separation of the magnetic and nuclear signals. On the other hand, due to Larmor precessions, the neutron beam is depolarized at the sample with all neutron spins evenly distributed in the precession plane. For this reason, in the presence of chiral and/or nuclear-magnetic interference terms, the analysis of the experimental results is complex. The way out is the polarimetric neutron spin echo setup, a variant of intensity modulated NSE, which combines the precession field areas required for neutron spin echo spectroscopy with Cryopad.28 As shown schematically by Fig. 2, the precessions are stopped before the sample by a second additional $\pi/2$ flipper and the echo signal is recovered at the neutron detector after the analyzer.

This setup is now implemented at IN15 and can be used to observe chiral fluctuations with unprecedented accuracy and resolution both in energy (time) and momentum transfer (space). The polarimetric NSE and spherical polarimetry measurements were performed with a third-generation Cryopad, a sensitive zero-field polarimeter that controls the polarization of the incoming and the scattered beams.29,30 A combination of a soft metal and Meissner shields reduces the residual magnetic field at the sample position down to $\sim 0.1 \mu T$ and controls the direction of the polarization vectors with an accuracy of better than 1°. The beam polarization was 96% corresponding to a flipping ratio of 45.

III. POLARIZED NEUTRON FORMALISM: SPHERICAL POLARIMETRY

Before presenting in detail the experimental results, we will introduce the interaction between a polarized neutron beam and the magnetic helix of MnSi following the formalism developed almost simultaneously by Blume31 and Maleyev.32 in the early 1960s. The helix is described by two orthogonal vectors $\vec{s}_1$ and $\vec{s}_2$, which have the same amplitude and are perpendicular to the helix propagation vector $\vec{r}$. The magnetic structure factor for a reflection $\vec{Q}$ is given by

$$\hat{M}(\vec{K}) = \sum_j m_j f(\vec{K}) \exp(2i\pi \vec{K} \cdot \vec{r}_j) \quad \text{with}$$

$$m_j = \frac{1}{2} \mu (\vec{s}_1 - i\vec{s}_2) \exp(2i\pi \vec{r}_j \cdot \vec{r}_j) \exp(i\phi_j),$$

where $\mu$ is the amplitude of the Mn moments, $f(\vec{K})$ the magnetic form factor of the Mn atoms, $\vec{r}_j$ an atomic position, and $\phi_j$ an arbitrary phase angle. As the magnetic interaction vector $\hat{M}(\vec{K}) = \vec{K} \times \hat{M}(\vec{K}) \times \vec{K}$ is the projection of the magnetic structure factor onto a plane perpendicular to the scattering vector $\vec{Q} = \hat{K}$, it is convenient to choose the set of orthogonal polarization axes with $\vec{x} \parallel \vec{Q}$, $\vec{z}$ perpendicular to the scattering plane, and $\vec{y}$ completing the right-handed Cartesian set. In the geometry of the present experiment, $\vec{y} = \vec{n}$ with $\vec{n}$ the propagation vector of the incoming neutron beam. For the polarimetric measurements, the MnSi sample was oriented so that $\vec{Q} = \vec{r}_{111}$ and $\vec{z} = (1,1,0)$. For this reflection, the intensity of the diffracted beam was proportional to

$$\sigma = \hat{M} \cdot \hat{M}^* + \hat{P}^* \cdot \mathcal{S}(\hat{M} \times \hat{M}^*),$$

where $\hat{P}$ is the polarization of the incoming beam. The second term is the chiral part, which measures the degree of vector chirality characteristic of the spiral structure. This term adds to the conventional first term for $\hat{P} = \hat{Q}$, i.e., when the incident polarization is parallel to $\vec{Q}$. On the other hand, the reflection is completely extinct for $\hat{P} = -\hat{Q}$. Following Blume’s equations, the scattered polarization for MnSi is given by

$$\hat{P} \sigma = -\hat{P}^* (\hat{M} \cdot \hat{M}^*) + 2\mathcal{S} \{(\hat{P}^* \cdot \hat{M}^*) \hat{M} \} - \mathcal{S}(\hat{M} \cdot \hat{M}^*) - \mathcal{S}(\hat{M} \times \hat{M}^*).$$

The first two terms form the trivial magnetic part leading to $\hat{P} = -\hat{Q}(\hat{Q} \cdot \hat{P})$ for isotropically distributed electronic mag-
netic moments. The chiral third term creates a polarization antiparallel to \( \vec{Q} \) independently from the polarization state of the incoming beam. Both Eqs. (6) and (7) lead to the rigorous and accurate determination of the chiral component \( \Im(\vec{M}_\perp \times \vec{M}_\parallel) \) by polarized neutrons. The more general form of Eq. (7) is

\[
\vec{P} = \vec{P} \vec{P}' + \vec{P}^\dagger
\]

(8)

with \( \vec{P} \) the polarization transfer tensor and \( \vec{P}^\dagger = -\Im(\vec{M}_\perp \times \vec{M}_\parallel) \) the polarization created by the chiral sample. It is then useful to have the incident polarization along \( -\vec{x}, \vec{y}, \vec{z} \), and \( \vec{z} \) and to measure the outgoing polarization components along \( \pm\vec{x}, \pm\vec{y}, \pm\vec{z} \) for each configuration of the incident polarization, respectively. This measurement procedure is characteristic of spherical neutron polarimetry (SNP) and determines the polarization matrix

\[
\mathbb{P}_{i,j} = \frac{P_{ij}}{|P|} = \frac{\vec{P}_{i,j} \vec{P}_i^\dagger + \vec{P}_j^\dagger}{|P|} \quad \text{with} \quad (i,j) \in \{x,y,z\},
\]

(9)

where the denominator \( |\vec{P}| \) corrects for the finite efficiency of the neutron polarizer-analyzer system and the intrinsic imperfections of the experimental setup. For nuclear (coherent) scattering \( \mathbb{P}_{i,j} = \delta_{ij} \), i.e. 1 for \( i = j \) and 0 otherwise,

\[
\mathbb{P}_{nuclear} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}
\]

For an ideal paramagnet, all matrix elements are zero except \( \mathbb{P}_{xx} = -1 \):

\[
\mathbb{P}_{para} = \begin{pmatrix} -1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}
\]

In MnSi, according to Eq. (7), the scattered beam will always have a polarization antiparallel to the helix propagation vector, i.e., antiparallel to \( \vec{x} \) and \( \vec{Q} \). For this reason, the first row of the matrix will be nonzero, ideally, \( \mathbb{P}_{x,x} = -1 \), \( \mathbb{P}_{x,y} = \mathbb{P}_{x,z} = 0 \) with \( (i) \in \{x,y,z\} \). In its most general form, the chiral matrix can be written as

\[
\mathbb{P}_{chiral} = \begin{pmatrix} -1 & \eta \xi & \eta \zeta \\ 0 & 0 & 0 \\ \eta \zeta & 0 & 0 \end{pmatrix}
\]

where \( \zeta \) determines the chirality of the helix: \( \zeta = +1 \) for right-handed and \( \zeta = -1 \) for left-handed chirality. \( \eta \) measures the fraction of the dominant chiral domain: \( \eta = 1 \) for a single domain and \( \eta = 0 \) for equally populated chiral domains or for the disordered paramagnetic state, in which case \( \mathbb{P}_{chiral} \) reduces to \( \mathbb{P}_{para} \).

The polarization matrix of MnSi below \( T_C \) is that of an ideal chiral left-handed single-domain structure. At \( T_C - 4 \) K, we found

\[
\begin{pmatrix} P_{T_C - 4K} \\ 
-1.000 \pm 0.001 \\ -0.995 \pm 0.001 \\ -1.002 \pm 0.001 \\ 
-0.007 \pm 0.001 \\ 0.016 \pm 0.002 \\ -0.007 \pm 0.002 \\ 
0.054 \pm 0.003 \\ 0.055 \pm 0.002 \\ 0.062 \pm 0.002
\end{pmatrix}
\]

Just above \( T_C \), the intensity at \( \tilde{r}_{11} \) drops dramatically, which leads to higher counting times and error bars. Nevertheless, the matrix remains unaffected and is that of a perfect left-handed single-chiral domain up to \( \sim T_C + 1 \), e.g., at \( T_C + 0.4 \) K:

\[
\begin{pmatrix} P_{T_C + 0.4K} \\ 
-1.03 \pm 0.03 \\ -0.99 \pm 0.03 \\ -0.98 \pm 0.03 \\ 
-0.01 \pm 0.05 \\ -0.00 \pm 0.05 \\ -0.03 \pm 0.05 \\ 
0.07 \pm 0.05 \\ 0.04 \pm 0.01 \\ 0.07 \pm 0.05
\end{pmatrix}
\]

Above \( \sim T_C + 1 \), the nondiagonal elements decrease slowly and chirality remains finite even well above \( T_C \). For example, at \( T_C + 4 \) K, we found

\[
\begin{pmatrix} P_{T_C + 4K} \\ 
-1.02 \pm 0.01 \\ -0.4 \pm 0.1 \\ -0.3 \pm 0.1 \\ 
-0.01 \pm 0.1 \\ -0.08 \pm 0.1 \\ -0.05 \pm 0.1 \\ 
0.02 \pm 0.1 \\ 0.07 \pm 0.1 \\ -0.08 \pm 0.1
\end{pmatrix}
\]

All data have been corrected for the background determined from polarimetric measurements at 50 K. Figure 3 shows that \( \mathbb{P}_{xy} \) and \( \mathbb{P}_{xz} \) are, within the error bars, unaffected by \( T_C \) and start to decrease only above \( \sim T_C + 1 \) K. This result is confirmed by the intensity of the reflection when \( \vec{P} \parallel \pm \vec{x} \), in which case Eq. (6) becomes

\[
\sigma = N_{para} \pm N_{chiral}
\]

(10)

where the sign in front of the chiral contribution \( N_{chiral} \) depends on the direction of \( \vec{P} \) (parallel or antiparallel) with respect to \( \vec{Q} \). The intensities in the spin-flip channel are

\[
\begin{align*}
N_{x,-x} & \equiv N_{SF}^{\vec{P} \perp \vec{Q}} = N_{bck}^{\vec{P} \perp \vec{Q}} + N_{para} + N_{chiral}, \\
N_{x,-x} & \equiv N_{SF}^{\vec{P} \parallel \vec{Q}} = N_{bck}^{\vec{P} \parallel \vec{Q}} + N_{para} - N_{chiral}.
\end{align*}
\]

(11)

The chiral fraction \( N_{chiral}/(N_{chiral} + N_{para}) \) can then be deduced from the ratio \( (N_{x,-x} - N_{-x,x})/(N_{x,-x} + N_{-x,x} - 2N_{bck}^{\vec{P} \perp \vec{Q}}) \), with the background \( N_{bck}^{\vec{P} \perp \vec{Q}} \) determined at 50 K. This method minimizes the error bars and systematic errors because both \( N_{x,-x} \) and \( N_{-x,x} \) are measured under identical conditions. The deduced chiral fraction is also shown in Fig. 3 and coincides with the nondiagonal matrix elements.

Complete chirality implies complete break of time reversal symmetry. This occurs before the onset of the helical Bragg peaks at \( T_C' \sim T_C + 1 \) K. Between \( T_C' \) and \( T_C \), the isotropic

FIG. 3. (Color online) Temperature dependence of the chiral fraction determined by neutron polarimetry as explained in the text.
MAGNETIC FLUCTUATIONS AND CORRELATIONS IN

PHYSICAL REVIEW B 83, 224405 (2011)

FIG. 4. (Color online) Dynamic correlations at the position of one of the helical Bragg peaks \( \vec{\tau}_{111} \) measured by polarimetric NSE for the \( P_{z,x} \) term of the polarization matrix [Eq. (9)].

scattering at the surface of the sphere with radius \( \tau \) is observed and analysis of the dynamic and static correlations in the following sections will shed light in this unconventional and completely chiral short-range order.

IV. NEUTRON SPIN ECHO

The dynamics of MnSi was thoroughly investigated by triple-axis spectroscopy (TAS) in the mid 1980s.\textsuperscript{5} It was shown that strong magnetic correlations exist up to room temperature and that the magnetic excitation spectrum is well described by the Moriya-Kawabata theory for weak itinerant ferromagnets. The TAS measurements, however, did not have the resolution in energy transfer required to analyze the magnetic fluctuations close to \( T_C \). With neutron spin echo spectroscopy, we can reach the required resolution, follow very accurately the slowing down of the magnetic fluctuations, and complement the TAS experiments. The fact that MnSi is completely chiral above \( T_C \) was an unexpected outcome of the polarimetric measurements and also \textit{a posteriori} the justification for combining NSE and Cryopad to polarimetric NSE.

With the Cryopad on IN15, we were able to measure separately the relaxation of the diagonal \( P_{xx} \) and of the crossed chiral terms \( P_{yx} \) and \( P_{zx} \). The corresponding intermediate

FIG. 5. (Color online) Dynamic correlations at \( \vec{\tau}_{111} \) measured by classical NSE.

FIG. 6. (Color online) Dynamic correlations at \( \vec{\tau}_{110} \), where the spectra are not contaminated by the helical Bragg peaks.

FIG. 7. (Color online) Temperature dependence of the characteristic times \( t_0 \) (a) and the deduced Lorentz linewidths (b) of the fluctuations at \( \vec{\tau}_{111} \) and \( \vec{\tau}_{110} \) measured by classical (paramagnetic) and polarimetric NSE. The lines are guides to the eye.
FIG. 8. (Color online) $q$ dependence of the dynamic linewidth $\Gamma$. The open and closed symbols represent the values at $\vec{r}_{111}$ and $\vec{r}_{110}$, respectively. At the highest temperature ($\sim 31$ K), there is excellent agreement with literature (Ref. 5) and Eq. (17b) (dotted line).

scattering functions $I(q,t)$ were obtained by normalizing the spectra against the resolution measured below $T_C$, typically at 25 K. Figure 4 shows polarimetric NSE spectra for the crossed term $I_{yx}$ at $\vec{r}_{111}$.

The polarimetric NSE spectra display a purely exponential relaxation superimposed on an elastic term $I(q,t) = a \exp(-t/t_0) + (1-a)$. (12)

As seen in Fig. 4, the elastic fraction $(1-a)$ evolves from $\sim 15\%$ to $100\%$ within 0.15 K following the fast increase of the intensity displayed in Fig. 1 and masking the dynamics at $T_C$. This behavior is confirmed by standard NSE measurements (Fig. 5), which, however, do not extrapolate to 1 at $t \to 0$. The comparison with polarimetric NSE identifies this as an artifact due to the chiral magnetic scattering and not to additional dynamic components.

At $\vec{r}_{110}$, the quasielastic scattering does not develop to a Bragg peak and the NSE spectra were not contaminated by an elastic contribution. Consequently, the fluctuations could be followed even below $T_C$ (Fig. 6). The decay is exponential with the same $t_0$ and deduced $\Gamma$ as at $\vec{r}_{111}$.

All relaxation times and linewidths at $q=0$ are plotted against temperature in Fig. 7. The diagonal ($xx$) and crossed terms ($yx$ and $zx$) measured in the polarimetric NSE mode are also included. All data, even those in the closest vicinity of $T_C$, fall on the same curve. Consequently, the relevant parameter for the fluctuations is the distance from the sphere with radius $\tau$, not the Bragg peaks $\vec{r}_{111}$ of the helical phase.

We will now discuss the $q$ dependence of the relaxation (Fig. 8). Close to $T_C$, the linewidths take their lowest values at the surface of the sphere with radius $\tau$. We found that $\Gamma$ increases both for $|\vec{Q}| > \tau$ and $|\vec{Q}| < \tau$ and the low-$q$ points in Fig. 8 are the average for $q = \pm 0.03 \text{ Å}^{-1}$. However, above $\sim T_C + 1.4$ K, the $q$ dependence of $\Gamma$ flattens and it is no longer possible to identify the position of the minimum.

FIG. 9. (Color online) Magnetic signal, proportional to $S(q)$, around the $\vec{r}_{111}$. The continuous lines are the best fits: simple Gauss function at $T_C$, superposition of a fluctuating Lorentz (Orstein-Zernike), and an elastic Gaussian part at $T_C < T < T_C + 0.2$ K and a fluctuating Lorentz function above $T_C + 0.2$ K.

Close to $T_C$, $\Gamma(q=0)$ levels off at $\sim 0.64 \mu eV$, which implies that the associated correlation length does not diverge at $T_C$. The results will be discussed in the frame of dynamic scaling also after the determination of the correlation length in the following section.

V. CORRELATION LENGTH

The $Q$ dependence of the magnetic static structure factor $S(Q)$ was analyzed in the configuration $N_{x-x}$ of Eq. (11),

FIG. 10. (Color online) Comparison of the quality of fits for a simple Lorentz (dotted line), Gauss (dashed line), and the superposition of a Lorentz and a Gauss (continuous line) at $T_C + 0.05$ K and $\vec{r}_{111}$.
where the magnetic intensity is maximum and the background correction negligible for $T<30\,\text{K}$.

Figure 9 shows the scattered neutron intensity, which is proportional to $S(Q)$, around $\vec{\xi}_{111}$ in a log-lin scale. At $T_C$, the points are best fitted by a Gauss function, with $\sigma^2 = 6.11 \times 10^{-3} \pm 3 \times 10^{-5}\,\text{Å}^{-1}$ leading to $1.44 \times 10^{-2} \pm 10^{-4}\,\text{Å}^{-1}$ FWHM, i.e., significantly broader than the $Q$ resolution of the instrument. Well above $T_C$, the data are well described by the OZ function of Eq. (2) convoluted with the Gauss resolution function.

Just above $T_C$, however, neither the Gauss nor the OZ functions fit satisfactorily the experimental data. Instead, the best fit is obtained by a superposition of a fluctuating OZ and an elastic Gauss with relative weights fixed from the NSE spectra, as shown by Fig. 10. We note that all three fits in Fig. 10 involve the same number (two) of independent parameters: the total intensity and the $\sigma$ for the Gauss or $\kappa$ for the Lorentz and Gauss + Lorentz fits, respectively (in this case, the width of the Gauss was fixed to that found below $T_C$).

Similarly to the NSE spectra, the data analysis is easier at $\vec{\tau}_{110}$, where there is no contamination from Bragg peaks. At this position of the reciprocal space, a simple Lorentzian describes the scattered neutron intensity at all temperatures, even below $T_C$. All correlation lengths are plotted versus $T-T_C$ in Fig. 11 and the deduced values of $\kappa$ are in excellent agreement with previous published data (Fig. 12).

At $\vec{\tau}_{110}$, the correlation length $\xi_{110}$ levels off at about 100 Å, i.e., about half the pitch of the helix. At $\vec{\tau}_{111}$, the correlation length $\xi_{111}$ increases considerably close to $T_C$ following a power law of the reduced temperature $\epsilon$ similar to those found at second-order phase transitions and illustrated by Fig. 13. The continuous line in the figure corresponds to

$$\xi_{111} = a\,\epsilon^{-\nu} \quad \text{with} \quad a = 12 \pm 2\,\text{Å} \quad \text{and} \quad \nu = 0.5 \pm 0.2.$$  \hspace{1cm} (13)

The dotted line represents $\xi = 5.6\,\epsilon^{-0.5}\,\text{Å}$, the extrapolated curve from the high-temperature TAS data of Ishikawa et al.\textsuperscript{5} It is remarkable that this extrapolation from very high temperatures (100–300 K) is only a factor 2 off our results.

![Figure 11](image1.png)

**FIG. 11.** (Color online) Plot of the correlation lengths ($\xi_{111}$ and $\xi_{110}$) measured at $\vec{\tau}_{111}$ and $\vec{\tau}_{110}$ as a function of temperature.

![Figure 12](image2.png)

**FIG. 12.** (Color online) Plot of $\kappa$ measured at $\vec{\tau}_{111}$ and $\vec{\tau}_{110}$. The closed symbols are the present work. The open symbols are from Grigoriev et al. (Ref. 9).

**VI. DYNAMIC SCALING**

Dynamic scaling relates $\Gamma$ to $\kappa$ (or inversely $t_0$ to $\xi$) through a homogenous function

$$\Gamma(q,\epsilon) \propto \Gamma(q,\epsilon = 0) f(\kappa/q)$$  \hspace{1cm} (14)

with the dimensionless ratio $\kappa/q$ defining the critical ($\kappa/q \ll 1$) and hydrodynamic ($\kappa/q \gg 1$) regimes, respectively.\textsuperscript{34} At the critical limit, which is always reached at $\kappa=0$, the linewidth and relaxation times reflect the volume probed by the measurement

$$t_0(q,\epsilon = 0) \propto q^{-\nu} \quad \text{and} \quad \Gamma(q,\epsilon = 0) \propto q^z$$  \hspace{1cm} (15a)

$$\Gamma(q,\epsilon = 0) \propto q^{-\nu} \quad \text{and} \quad \Gamma(q,\epsilon = 0) \propto q^z$$  \hspace{1cm} (15b)

with $z$ the dynamic exponent. For $q = Q$, as in ferromagnets $z = 5/2$, whereas for antiferromagnets and MnSi, where the relevant parameter is $q = |Q - \tau|$, $z = 3/2$.

![Figure 13](image3.png)

**FIG. 13.** (Color online) Plot of the correlation length $\xi_{111}$ determined at $\vec{\tau}_{111}$ versus the reduced temperature $\epsilon$ on a log-log scale. The continuous line is the best power-law fit $\xi = 12\,\epsilon^{-0.5}\,\text{Å}$. The dotted line shows the extrapolated values from the high-temperature TAS work of Ishikawa et al. (Ref. 5).
At the hydrodynamic limit, \( q = 0 \) and \( \kappa > 0 \), the dynamics is governed by the correlated volumes through the power laws

\[
\begin{align*}
  t_0(q = 0) &\propto \xi^2 \quad \text{and} \\
  \Gamma(q = 0) &\propto \kappa^2.
\end{align*}
\]

(16a)

(16b)

The previous extensive study of spin fluctuations in MnSi with TAS (Ref. 5) showed that the linewidth is equally well described by two universal scaling functions over an extremely large temperature scale, from \( \sim 30 \) K up to the room temperature:

\[
\begin{align*}
  \Gamma &\sim \Gamma_0 Q^3 \left[ 1 + (\kappa/Q)^2 \right] \\
  \sim A_0 Q^{3/2} \left[ 1 + (\kappa/Q)^2 \right]
\end{align*}
\]

(17a)

(17b)

with \( \kappa^2 = 0.0325 \, \text{Å}^{-2}, \quad \Gamma_0 = 50 \, \text{meVÅ}^3, \quad \text{and} \quad A_0 = 19.6 \, \text{meVÅ}^{3/2} \). Equation (17b) is derived from the Moriya-Kawabata theory for weak itinerant ferromagnets,\(^{35}\) whereas Eq. (17b) has the form expected for dynamic scaling. The dotted line going through the data at \( T_C + 2.3 \) K in Fig. 8 corresponds to the calculated values from Eq. (17b) and is in excellent agreement with our experimental results. At high temperatures, the momentum transfer \( Q \) is the relevant parameter and \( z = 5/2 \). Close to \( T_C \), however, magnetic correlations build up at \( \tau \) and the relevant parameter crosses over to \( q = |Q - \tau| \), which is used in this paper. Consequently, also the dynamic critical exponent should cross over from \( z = 5/2 \) to \( 3/2 \).

If the transition were of second order, an analysis along the lines of dynamic scaling would imply critical slowing down. In this case, \( \Gamma_{111}(q = 0) \) should decrease continuously to zero at \( T_C \) following the divergence of \( \xi_{111} \). In contrast, \( \Gamma_{111}(q = 0) \) remains finite and strictly the same as \( \Gamma_{110}(q = 0) \). Moreover, Figs. 7 and 12 show that, close to \( T_C \), both \( \Gamma_{111} \) and \( \Gamma_{110} \) are roughly proportional to \( \kappa_{110} \), not to the “critical” \( \kappa_{111} \). Consequently, we do not observe the critical slowing down and rapidly changing dynamic behavior expected for second-order phase transitions. This is underlined by Fig. 14.

The ratio between all \( \Gamma \) and the calculated \( \kappa_{110} \) levels off to a broad plateau between \( T_C \) and \( T_C' \), pointing toward \( z \sim 1 \).

Figure 15 shows the interdependence of the reduced dimensionless quantities \( \Gamma / \Gamma(T_C) \) and \( \kappa_{110}/q \). The dotted line shows the extrapolated values from the previous high-temperature TAS data [Eq. (17b)]. The red dashed line is the Resibois-Piette function for antiferromagnets and the (green) continuous line is a guide to the eyes through the experimental data for \( T_C \lesssim T \lesssim T_C' \).

\[\begin{align*}
\kappa_{110}/q &\sim (\text{antiferromagnetic Resibois-Piette function}) \\
&\sim (\text{continuous line in Fig. 15})
\end{align*}\]

VII. DISCUSSION

These high-resolution neutron scattering data confirm the first-order nature of the helical transition in MnSi seen by specific heat and ultrasonic attenuation measurements.\(^{7,23}\) In favor of the first-order phase transition are the following:

(a) the sharpness of the transition (Fig. 1), even though the helical Bragg peaks are not resolution limited;

(b) the coexistence of high- and low-temperature phases between \( T_C \) and \( T_C + 0.2 \) K. At \( \tilde{\epsilon}_{111} \), the NSE spectra are the superposition of a fluctuating and elastic part (Figs. 4 and 5) and the static structure factor is best described by the superposition of a Lorentzian (fluctuating) and Gaussian (elastic) contributions (Fig. 10);

(c) the absence of critical slowing down at \( T_C \). The slow change of the dynamics scales with the nondiverging correlation length \( \xi_{110} \).

Fluctuations are present above \( T_C \) and \( \xi_{111} \) can indeed be approximated by a power law [Eq. (13) and Fig. 13]. For this reason, it will always be possible to bend a selection of experimental findings into the second-order phase transition.
scheme by introducing crossovers, as it was recently done by Grigoriev et al.\textsuperscript{37} However, second-order phase transitions are global transformations involving all parameters of the system, and this is not the case in MnSi.

We will now proceed to the discussion of the fluctuating phase between $T_C$ and $T'_C$. Figure 16 recapitulates the most important findings of this work and includes the specific heat measured by Stishov et al.\textsuperscript{23} The first-order helical transition $T_C$ is marked by the sharp peak in the specific heat [Fig. 16(d)] and the Bragg peak [Fig. 16(a)]. On the other hand, the helical transition has no effect on $\eta$, the degree of single-domain chirality. $\eta$ is the fraction of left-handed chiral correlated magnetic moments and can be associated to a characteristic correlation length as suggested by a mean-field model\textsuperscript{9}

$$\eta = \frac{2Qr}{(Q^2 + r^2 + 1/\xi^2)}, \quad (18)$$

which, for $Q = r$, as it is the case for the present results, becomes

$$\eta = 1 - \frac{1/\xi^2}{2r^2 + 1/\xi^2}.$$ 

From $\xi_{111}$, we calculate the dotted line of Fig. 16(b), which is significantly different from the measured $\eta$. The assumption of unpinned chiral fluctuations put forward by Grigoriev et al.\textsuperscript{9,37} is therefore not sufficient to explain the behavior of MnSi above $T_C$.

In spite of this inconsistency, Eq. (18) bears the correct physics: when $\eta \to 1$, the disordered paramagnetic phase fades away, time reversal symmetry is completely broken and, for this reason, some characteristic correlation length must diverge. This is obviously not $\xi$, which is only about half of the pitch of the helix at $T'_C$. If the correlation length between magnetic moments is not the relevant parameter, the answer must be found not at the microscopic but at the mesoscopic scale. The hint is given by recent theoretical approaches,\textsuperscript{18,21} which reveal that chiral objects, such as skyrmions are highly stable and energetically favorable at short distances. These mesoscopic soliton-like objects form by thermal fluctuations at high temperatures and diffuse in the paramagnetic surroundings. Their stability explains the slow decrease of $\eta$ and its finite value well above $T_C$. The number of these objects increases with decreasing temperature until they completely fill the space. When this happens, the associated "renormalized" correlation length diverges and $\eta = 1$.

We suggest that $T'_C$ is the temperature where these skyrmionic objects condensate. Their natural size levels off at about half of the helix pitch, i.e., the same as $\xi_{110}$ between $T_C$ and $T'_C$. Consequently, the mean distance between two skyrmions in the condensed phase is about the helix pitch leading to the homogeneous scattering on the sphere with radius $r$, in spite of the significantly shorter-ranged magnetic correlations. In addition, this closed-packed phase has reduced degrees of freedom, which modify the dynamics, and lead to the low dynamic exponent $z \sim 1$ and to the slow temperature dependence between $T_C$ and $T'_C$ discussed in the previous sections and illustrated by Fig. 16(c).

$T'_C$ is seen in the specific heat [Fig. 16(d)], thermal expansion, sound velocity, sound absorption, or resistivity.\textsuperscript{8} The condensation of the skyrmionic chiral objects is therefore a major transformation with some characteristics of a phase transition.
In summary, we combined high-resolution neutron spin echo spectroscopy and spherical polarimetry to obtain a consistent picture of MnSi above $T_C$. The results evidence a first-order transition between the helical phase and a completely (single-domain) chiral and fluctuating new state of matter, which we identify as a skyrmion liquid. This phase would be the magnetic equivalent of the blue phases in liquid crystals. Through our findings the phase diagram of MnSi becomes similar to that of cholesteric liquid crystals, emphasizing the parallel between magnetic and structural ground states.

ACKNOWLEDGMENTS

C.P. thanks U. Rössler and E.L.-B. thanks P. J. Brown for fruitful discussions. The authors acknowledge the support of the ILL technical teams, in particular, E. Bourgeat-Lami, C. Gomez, and E. Thaveron. Special thanks go to Thomas Krist for the compact solid-state polarizer, which enabled the polarimetric NSE measurements. This project was partly supported by the European Commission under the 6th Framework Programme through the Key Action: Strengthening the European Research Area, Research Infrastructures, under Contract No. RI3-CT-2003-505925.