Lithium Dynamics in LiMn$_2$O$_4$ Probed Directly by Two-Dimensional $^7$Li NMR

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LiMn$_2$O$_4$ has been studied using magic-angle-spinning nuclear magnetic resonance (MAS NMR). 1D MAS NMR shows three Li resonances assigned to different crystallographic sites. At low temperatures an extra peak appears, indicating charge ordering of Mn$^{3+}$ and Mn$^{4+}$. Direct observation of the lithium dynamics was possible using rotor-synchronized 2D exchange NMR. A millisecond time scale exchange of lithium starts around 285 K between the 8a and the 16c site. At 380 K lithium even starts to hop between more than two sites. The activation energies and Li jump rates are derived and are in agreement with those determined macroscopically.

To characterize sample preparation procedures, Koizumi et al. [14] reported the magnetic properties of LiMn$_2$O$_4$ using $^7$Li-NMR. Mustarelli et al. [15] used NMR and XRD to study the structure of LiMn$_2$O$_4$.

In the study presented here, $^7$Li MAS NMR spectra were recorded using a Bruker DMX-300 spectrometer operated at a frequency of 116 MHz. A 2.5 mm MAS probe spinning at 28 kHz was employed. The temperature was stabilized within 0.5 K using a nitrogen gas flow. Temperature calibration was performed using the $^{207}$Pb resonance of Pb(NO$_3$)$_2$ [16]. Two-dimensional exchange NMR spectra were recorded using a hardware rotor synchronization of the exchange time (also called mixing time) and by employing the whole-echo acquisition technique described in [17]. The exchange of Li between sites with different chemical shifts, i.e., crystallographically different sites, can be observed directly as cross peaks in these spectra. The evolution of the cross peak intensity as a function of time provides direct information on the rate of the exchange process. Furthermore, the temperature dependence has been analyzed using an Arrhenius plot for the jump rate versus $T$.

The materials, obtained from the company SEDEMA (Tertre, Belgium), were characterized by x-ray and neutron diffraction and were of single phase having the spinel structure (space group Fd3m) with $a = 8.24$ Å. It is well known that the LiMn$_2$O$_4$ compound shows a Jahn-Teller distortion and a charge ordering at $T = 280$ K [1]. In the investigated compound Li[Mn$_{1.96}$Li$_{0.04}$]O$_4$, where the atoms in front of, between, and after the brackets are on, respectively, 8a/16c, 16d, and 32e sites, no Jahn-Teller distortion was found with temperature dependent neutron powder diffraction experiments [18]. This could be expected since the random distribution of Li over the 16d positions prevents such a transition to an ordered state.

In Fig. 1 the $^7$Li MAS NMR spectra of Li[Mn$_{1.96}$Li$_{0.04}$]O$_4$ are shown as a function of temperature. The
strongest MAS NMR spinning sideband manifold in the spectrum is assigned to lithium on 8a sites, which is the lithium site with the highest occupancy as was observed in neutron diffraction [4]. The two smaller peaks belong to lithium located at the 16d sites and the interstitial 16c sites [4]. All subspectra shift to smaller ppm values, i.e., smaller hyperfine fields as the temperature increases. This was analyzed in Refs. [12] and [13] as the effect of the paramagnetic susceptibility changing proportional to $T^{-1}$. The width of the spectrum is caused by the anisotropic polarization of the paramagnetic manganese magnetic moments [15]. The width expressed in ppm was checked to be field independent, which indicates negligible quadrupole interaction. Therefore the spectrum has the shape of a central transition.

At high temperatures, i.e., 475 K, the lines start to coalesce due to motional averaging, indicating the onset of Li exchange between the different sites at a rate comparable to the distance in Hz between the different resonances. This is in agreement with the result reported by Lee et al. [13] indicating the same rapid exchange effect. At low temperatures, i.e., 285 K, a fourth peak appears, and additionally line broadening (+35%) of all resonances becomes clearly visible in the 1D spectrum (Fig. 1). This peak may be caused by charge ordering of Mn$^{3+}$ and Mn$^{4+}$ as has been reported by Rodríguez-Carvajal [1]. Such a charge ordering leads to Li surroundings with different Mn$^{3+}$ and Mn$^{4+}$ coordinations instead of Mn ions with all the same time-averaged +3.55 valence.

Figure 2a, in which the 2D spectrum of Li[Mn$_{1.96}$Li$_{0.04}$]O$_4$ at a temperature of 285 K is plotted, shows the absence of exchange between different sites for a mixing time of $t_{\text{mix}} = 5$ ms. It also demonstrates the good performance of the rotor-synchronized-pulse sequence which causes strong signals to be found on the diagonal and cross peaks between side bands of the same site to be suppressed. Furthermore, it indicates that spin diffusion is completely absent due to the fast MAS used in these experiments. As the temperature is increased, the 2D plot (Fig. 2b) shows the onset of cross peaks for the same $t_{\text{mix}}$. A gradual conversion of the diagonal peaks towards a more circular shape corresponds to Li atoms remaining at the same site, but experiencing a slight change in the environment, which is caused by other nearby Li atoms changing position. Note that intense cross peaks are observed between Li signals from Li on the 8a and 16c sites. This means that large fractions of the Li hop from highly occupied 8a sites to the lower occupied interstitial 16c sites. The signal is assigned to the 16c site rather than to the 16d site, since the shortest diffusion path from 8a to 8a sites leads from 8a to 16c to 8a in an almost straight line. The result directly indicates that Li occupies the interstitial 16c site for a finite amount of time. Increasing the mixing time results in increased cross peaks intensity.
as can be seen in Fig. 3 where the cross peak intensity relative to the intensity of the largest peak as a function of the mixing time has been plotted. Full saturation of the cross peaks has not been achieved at this temperature as this would require a mixing time which is longer than the $T_1$ relaxation time ($T_1 = 10$ ms).

The data allow the extraction of two types of information. First is the direct determination of a time scale on which the Li hops from one site to another, and second is the temperature dependence of the exchange which yields an Arrhenius analysis of the activation energy of the hopping process.

Since there is mainly hopping between two sites at the time scale probed by the experiment a two-site Markov hopping process can be used to describe the data. The curves of Fig. 3 have been fitted with the function $I(t_m) = \frac{I_0}{\tau_1 + \tau_2}[1 - e^{-(\tau_1 + \tau_2)\tau_m}]$, where $\frac{1}{\tau_1}$ and $\frac{1}{\tau_2}$ are the jump rates for Li ions hopping from 8a to 16c sites and from 16c to 8a sites, respectively. Within the model the temperature dependent ratio between $\tau_1$ and $\tau_2$ can be derived from the ratio of the integrated peak intensities in the 1D NMR spectra: $\frac{\tau_1}{\tau_2}$ = intensity 8a/ intensity 16c. The results of the fits are presented in Table I. From the jump rate a self-diffusion coefficient can be calculated using the formula $D = \frac{1}{l^2} \frac{I}{\tau}$, where $l$ is the distance over which the Li-ions jump and $\frac{1}{\tau}$ is the average jump rate. This case $l = 1.78$ Å which leads to self-diffusion coefficients given in Table I. Note that these self-diffusion coefficients are derived by studying the movement of a single atom in an equilibrium distribution of Li in the crystals. As is explained by, e.g., Crank [19], differences between self-diffusion coefficients and chemical diffusion coefficients can be very large because the applied electric field, used to measure the chemical diffusion coefficients, can create large (local) gradients in the Li concentration, which are not present when measuring self-diffusion coefficients.

There must be a difference between the activation energies for jumping from 8a to 16c and vice versa since the sites are not equally occupied. This difference has been calculated using the temperature dependent ratio of Li-ions on 8a and 16c sites (Table I) and the Boltzmann equation, yielding a value of $700 \pm 70$ K. In Fig. 4 the derived jump rates $\frac{1}{\tau}$ have been plotted versus $\frac{1}{T}$ on a semilog scale. The activation energies for jumping from a 8a to a 16c site and vice versa are obtained from the exponents of exponential fits of the curves, and the difference of 700 K between them. The exponents of the fit are 6800 and 6100 K which corresponds in both cases, within the error bars, to an activation energy of $0.5 \pm 0.1$ eV. In Fig. 5 the activation energy and energy difference between the 8a and 16c sites are illustrated. Using conductivity measurements Massarotti et al. [20] found a value 0.4 eV for the activation energy of the Li-ion conduction process, which is in good agreement with the value found in this study using a microscopic method. We can, therefore, conclude that this microscopically determined activation energy is the main barrier for the macroscopic Li-ion transport, i.e., that the hopping on the 8a $\rightarrow$ 16c diffusion path observed in the microscopic NMR measurements corresponds to the main lithium conduction process.

As can be seen in Fig. 2c new cross peaks appear in the spectra at 380 K for a mixing time of $t_{mix} = 10$ ms. The occurrence of these new peaks indicates that secondary hopping processes are becoming prominent, i.e., there is the sites.

![Graph of Fig. 3](image)

**FIG. 3.** The intensity of 8a-16c cross peaks as a function of mixing time ($t_m$) for the temperatures (K) indicated in the figure.

**TABLE I.** The ratio $\frac{\tau_1}{\tau_2}$, determined using the 1D NMR spectral intensities, jump rates, and self-diffusion coefficients derived by fitting curves of Fig. 3.

<table>
<thead>
<tr>
<th>$T$ (K)</th>
<th>$\frac{\tau_1}{\tau_2}$</th>
<th>$\frac{1}{\tau_1}$ (s$^{-1}$)</th>
<th>$\frac{1}{\tau_2}$ (s$^{-1}$)</th>
<th>$D$ ($10^{-16}$ cm$^2$ s$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>285</td>
<td>0.97 ± 0.04</td>
<td>1.2 ± 0.1</td>
<td>1.2 ± 0.1</td>
<td>3.4 ± 0.7</td>
</tr>
<tr>
<td>345</td>
<td>0.75 ± 0.04</td>
<td>0.9 ± 0.1</td>
<td>0.9 ± 0.1</td>
<td>2.5 ± 0.5</td>
</tr>
<tr>
<td>355</td>
<td>0.60 ± 0.04</td>
<td>0.7 ± 0.1</td>
<td>0.7 ± 0.1</td>
<td>2.0 ± 0.4</td>
</tr>
<tr>
<td>380</td>
<td>0.43 ± 0.04</td>
<td>0.5 ± 0.1</td>
<td>0.5 ± 0.1</td>
<td>1.6 ± 0.3</td>
</tr>
<tr>
<td>400</td>
<td>0.33 ± 0.04</td>
<td>0.4 ± 0.1</td>
<td>0.4 ± 0.1</td>
<td>1.3 ± 0.2</td>
</tr>
</tbody>
</table>

![Graph of Fig. 4](image)

**FIG. 4.** Semilog plot of the derived jump rates versus $\frac{1}{T}$. Using $\frac{1}{\tau} = \frac{1}{\tau} \exp(-\frac{E}{kT})$ the activation energies $E$ are calculated to be $E = 0.5 \pm 0.1$ eV.
sufficient mobility to make more than one jump during $t_m$. This directly results in cross peaks between 8a spinning side bands following $8a \rightarrow 16c \rightarrow 8a$ hopping, since different 8a sites have a different orientation of the anisotropy tensor with respect to the applied field. The cross peak indicated by an arrow in Fig. 2c shows that hopping between the 8a and the 16d site also becomes an important process. The two-site model then has to be replaced by a three-site model. However, since our $t_m$ could not be extended to sufficiently long times, it was not possible to accurately determine the three-site model parameters.

To our knowledge, this is the first time that the microscopic mobility of Li ions has been observed directly in Li[Mn$_{1.96}$Li$_{0.04}$]O$_4$ using a powerful 2D NMR technique. Temperature dependent experiments indicate an onset of lithium exchange on a ms time scale between two sites at 285 K and between more than two sites at 380 K. Line broadening and a fourth spinning-side-band manifold, which are probably caused by charge ordering of Mn$^{4+}$ and Mn$^{3+}$, disappears at the same temperature as the lithium exchange starts, indicating that the charge ordering and lithium-ion dynamics are correlated. Enhanced screening of the ions in the crystal may lower the barriers for Li mobility, which is the subject of further research. The equilibrium occupation of the 8a and 16c sites and the exponential time dependence of the cross peaks yields the $8a \rightarrow 16c$ and $16c \rightarrow 8a$ activation energies. These activation energies of 0.5 ± 0.1 eV are in good agreement with values found in literature [20] from macroscopic methods. This indicates that the diffusion path found here is the primary Li conduction process.

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