Coasts may be briefly characterized as follows:

1. Hard (granite etc), medium hard (chalk, sandstone, limestone etc) and soft or loose (shingle, sand, clay). The soft and medium hard coasts give rise to difficulties.

2. Young, middle aged and old (Figure 1). Hard coasts keep their young appearance (fjords), medium hard coasts develop spits, tomboli, cuspate forelands etc in their middle age, and later on become ‘old’ cliff coasts. Soft coasts turn old in a few centuries but this does not mean that an equilibrium is established.

3. Shores of emergence and those of submergence. Owing to the general rise of the sea level relative to land levels by some 300 ft (100 m) or more, mainly as a result of the melting, due to climatic changes, of much polar ice during the holocene period, most coasts are of the submergence type. (The melting of the ice now existing would raise the sea level about 120 ft
Coasts, estuaries and tidal hydraulics

(36 m). Coasts of emergence show the eroded foreshores and ancient cliffs, or other former shore lines, above the sea level.

4 Coasts showing accretion and erosion. Coasts recede because of wave and current erosion; the eroded material (shingle, sand, clay) generally causes accretion in the neighbourhood.

5 Hill land coasts. These have cliffs, the hardest parts of which form the capes, while the softer parts are modelled into coastal curves, which are ‘suspended’ between capes. ‘Curves’ are formed either by erosion, silting up of bays, or by the horizontal growth of a spit (Figure 2). If the curve is not wholly regular there must be a special reason for it. Sometimes erosion is too strong to form curves and the coast then may develop the appearance of the coast of Figure 3. Near such coasts there will be deep foreshores which could provide good harbour sites although the intense wave action may prove adverse.

Spits and hooks are built up from the eroded material which waves tend to make into coastal curves; but these remain incomplete where there is not enough shingle or sand (e.g. German Bight), or they form anything else but a spit when there is no lee cape (e.g. the cape of Skagen, Denmark).

A cuspat e foreland like Dungeness is an alluvial cape. Dungeness has the ripple form; it is a huge horizontal ripple obeying the general law of ripples. It is moving slowly eastward because of wave action (not current action) from the west. The shingle is eroded from the west bank and is carried around the top of the ripple to the east bank where it remains. The top of the ripple is the ‘alluvial cape’. The lines of growth of shingle ridges on Dungeness show this. A tombola is a bar connecting an off shore island with the mainland (Figure 1). Cuspat e forelands, spits, hooks, tomboli etc are made up of eroded shore material.

6 Lowland coasts (sand) are shallow coasts and may stretch monotonously over long distances (e.g. the east coast of North America, the coast of Guinea, the south east coast of the North Sea). Some small hills may have resulted in weak capes on such a coast and huge coastal curves may be ‘suspended’ between them. Other streamlined forms may also be present.

Generally the slope of the sand beach or foreshore is so small that off shore bars have formed with shallow basins behind them. Such off shore bars are formed principally in a vertical direction by wave action, Figure 4, but as soon as they have been formed horizontal growths such as spits come into existence. An off shore bar often bears dunes. A low secondary bar may have formed because of wave action in the basin and behind this bar fresh water may have accumulated, which may have caused fen land areas to come into existence. The secondary bar is the fertile silt area which shuts off the low fen district from the sea. The tidal (salt) basins may have
partly silted up and in this way a lagoon coast may have formed. Because the tidal basin behind the off shore bar is filled and emptied by the tide, the off shore bar often has openings at regular distances. Such a bar is transformed into a string of sand islands (e.g. Frisian islands).

The coast between Cap Blanc Nez (near Calais) and Denmark is formed essentially of an off shore bar. In Flanders, that is south of the Scheldt, the original tidal flats behind this bar have since Roman times been wholly filled with sand and clay; but in western Holland, where the Rhine and Maas provide fresh water, the flats could develop into huge fen districts. The tidal flats on the northern part of this coast are called wadden (cf 'to wade').

**ESTUARIES**

TYPES OF ESTUARIES AND BARS

Estuaries are generally 'sunken' valleys in which marine and river sand and mud have deposited. In these deposits the rivers and tides have scoured channels and creeks. Sometimes, in alluvial plains or in deltaic regions, an estuary has formed due to some low lying peat land becoming a tidal basin, or because some river mouth has become choked and a new mouth has developed. Such estuaries may follow the cycle, young→mature→old, as a result of silt movement along the coast or along the river.

The tidal rise and the area of the tidal basin are of primary importance for the estuary, because the currents which keep the channels in the estuary deep and wide are caused by the filling and emptying of that basin as the tides move in and out. The 'tidal basin' is not, however, synonymous with tidal capacity because the tidal basin is the whole content of the estuary, whereas the tidal capacity is only that part of the estuary contained by the lines indicating the heights of slack water, Figure 5. The magnitude of tidal streams through a cross section of the estuary can thus be calculated.

When the estuary has the form of a wide and short basin (e.g. the Mersey basin), the tidal capacity will be almost as much as the total body of water contained in the basin between high water (h.w.) and low water (l.w.), because in such basins slack water generally occurs almost at h.w. and l.w. When there are tidal streams of about two or three knots at their maximum, which is generally the case because scouring and silting tend to establish that condition, the slack water will occur one or one and a half hours after h.w. and l.w.

When $P$ is the discharge of the river per tidal cycle and $f$ and $e$ are the flood and ebb discharges in the cross section considered, we have the simple relations:

\[
Q = e + f \quad \text{(1)}
\]

\[
P = e - f \quad \text{(2)}
\]

\[
e = 0.5 (Q + P) \quad \text{(3)}
\]

\[
f = 0.5 (Q - P) \quad \text{(4)}
\]

in which $Q$ is the total flow per cycle through the cross section.
As a result of the tidal fill and ebb, sand movements occur. We may introduce the term ‘sand stream’ here. In meandering non-tidal rivers, see p 1053, the sand stream tends to be straight, brushing the concave bends (Figure 6). The bulk of the sand moves near the bottom, the motive power being the current and the turbulence of the water. In bends there is a centrifugal movement at the top part and a centripetal movement near the bottom.

Generally two sand streams occur in estuaries and deltas, one coming down the river from the interior, the other travelling along the coast and often entering the estuary. The latter, called the coastal or littoral drift, can be mainly caused by waves. It may be much larger than the river sand stream. Both sand streams may meet in the estuary, or in front of its mouth. Of course, the sand streams are not continuous steady flows of sand; they are resultants of intricate movements over a long period. Ebb and flood move the sand to and fro in the estuary, and so do waves; but the important thing is that there are resultant sand streams either landward, or seaward, or across the mouth of the estuary. The resultant sand streams may not have the same direction as the resulting water streams near the surface. Often they are opposed, or at different angles, to the main water streams.

Fine silt also may move differently, following the currents which depend on the relative densities of fresh and salt water and on the mixing of the two waters. Like salt, marine silt may move far inland. Where marine salt can go, fine marine silt can also go, and is likely to do so.

When there is any sand movement in a river mouth or estuary, either a terrestrial delta or a submarine delta will have formed. The river solids often create a delta inside the spit or offshore bar of the estuary (e.g. the Rhine). In quiet seas the delta may extend beyond the general coastline; in rough tidal seas a submarine delta is more likely. Though there are many estuaries on the coast between Calais and Jutland, no river, discharging at this coast, has carried enough material since the last ice period to build up a terrestrial delta in the ordinary sense of the word. The many submarine deltas of that coast consist of marine sands. The same can be said of the English rivers and coasts.

The simplest form of a sand bar is as indicated in Figure 7. When a river, carrying sand, flows into fresh water, the primitive form of such a bar is self evident. The cross section suddenly becomes very wide and therefore shallow. But when the river flows into the sea an additional factor affects the result because the fresh river water flows over the heavier salt water (see Figure 19). A primitive bar may develop into a delta or into a submarine delta. When there is coastal drift the form of the bar or delta will be asymmetrical. A tidal wave running along the coast also makes the delta asymmetrical.
In tidal waters with sand bottoms the channels can be divided into flood channels and ebb channels: a flood channel is open to the flood and has a bar at the ebb end, an ebb channel is open to the ebb and has a bar at the flood end (Figure 8). Ebb channels and flood channels carrying sand will not follow the same course. This peculiar behaviour is the reason why shipping channels in estuaries often have one or more bars on which dredging must go on. Ebb channels have a general tendency to take a different course from flood channels and vice versa (Figure 8). It is only when special works effect coincidence of these channels that a shipping channel without bars is formed. The reason why ebb channels and flood channels tend to evade each other is the action of sand streams which have a seaward direction in an ebb channel and a landward direction in a flood channel. Both make small deltas or bars at their ends; these deltas come into conflict.

When the estuary is wide and relatively short there are several flood channels and only one or two ebb channels (Figure 9). When the estuary is long and not too narrow the ideal form is like a poplar tree (Figure 10), whereas on a lagoon coast the creeks take a form resembling an apple tree (Figure 11).

The ideal "poplar" type very seldom occurs. When it does occur, as in the estuary of the Scheldt, the "trunk", or ebb channel, provides a good fairway for ships. The shores of the estuary are responsible for this ideal state; they have been fixed at the right places. In all other instances the
'trunk' is nearly always broken more than once (bars occurring in the main ebb channel). We may call this the 'wild type': with this type of estuary bars occur at both ends of the channels. If the sea bar is higher than the inland bar, we may still call the channel an ebb channel, but sometimes both bars are equally high. A clear picture of an estuary is obtained by showing ebb channels in blue and flood channels in red, schematizing the channels while doing so and increasing the strength of the colour towards the bar.

Cutting off of tidal meanders sometimes occurs in a natural way in an estuary, but generally the initial stage of the cut remains a common flood channel.

Wild types may change their channels by meandering, but more often the depth of their bars, so that shipping has to follow different courses from time to time, Figure 12.

The erosive action of the flow of water at bends is the main cause of changes in the ebb and flood channels, a phenomenon we shall call bend action; it is the result of the centrifugal force of the water. Changes may also be the result of excessive sand transportation causing bars to be heightened so that shipping has to follow other channels.

There are sometimes secondary ebb channels, originating near a bar at the end of a flood channel, and then shifting after some years due to bend action, as indicated in Figure 13. Such secondary ebb channels should not be trusted. When new they may be fairly good shipping channels but their life is short, as ebb channels and flood channels tend to follow different courses. During successive stages the secondary ebb channel will show a movement from $E_1$ to $E_6$ (Figure 13) and after this a new cycle will start over again. The bend from $E_1$ into $E_2$, $E_3$ ... becomes more and more sharp, thus causing more and more bend action.
In the main, of estuary er than the sometimes obtained by th erising the turn towards the tidal way in an flood area and determines the left or right curve.

The action is caused by the cent!ifugal force of water flowing in a curve. The largest body of water goes with the flood to the largest fill area and determines the left or right curve.

In the northern hemisphere streams tend to the right shore because of the rotation of the earth, in the southern hemisphere to the left shore; this is of practical importance where the streams are more than about a mile wide.

The wind may displace a river or channel slowly in its most active direction due to wave action on the shore.

COAST AND ESTUARY RESEARCH

Oceanographic research has been going on for many years, but coastal waters and estuaries have not received much attention from research workers although the economic interests are great. They include the saving of dredging expenses, the opening up of harbours and river mouths, the avoidance of land losses by erosion, the gaining of new agricultural land or industrial sites, and a saving on shore defences.

Four different lines of research are required: 1 geological and historical research, 2 research on the site to ascertain the currents and sand streams, 3 mathematical research and 4 research in hydraulic laboratories.

GEOLOGICAL AND HISTORICAL RESEARCH

The general geology of our coasts and estuaries should be known; much can be learned from peat analysis with the technique devised by GODWIN at Cambridge. Borings should be made in the water covered areas and the study of all available historical data should not be neglected. Among the many questions to which answers are needed are the following. How much does the coast recede in a century and what are the fluctuations in this recession? What quantity of material is added annually to the coastal drift because of coastal recession or river discharge, neither clay layers nor mere chalk producing much coastal drift? Does the coastal drift protect the shore? In what direction do the shingle and sand travel? How much is being lost into the deeper parts of the sea? Is there any cycle in the periodic changes of the channels of an estuary? Does the estuary deepen or does it silt up as a whole, and at what secular rate?

Sediment petrology is a branch of geology which studies the sand grains heavier than bromide. Clay is examined with Röntgen rays. The origin and deposits of these materials can thus be established as well as the course of the sand and mud streams. Diatoms and foraminiferae may also give some useful information. There are distinct salt, brackish and fresh water diatoms. Geologists often want undisturbed boring samples. Borings should reach to the rock bottom, or to a depth of about 120 ft (36 m), which is the depth dredgers can reach.

RESEARCH ON CURRENTS AND SAND STREAMS

Because shore processes are slow the average rate of change can only be decided where exact data are available for a long time. Where such information is lacking, concrete poles should be placed now along receding coasts in order to be able to measure their future annual recession. These poles should be placed every mile or half mile and taken as fixed points on the national triangulation net. The height of the beach should
also be measured annually, and more often (daily or weekly) when the
height fluctuations of the beach are wanted. Those fluctuations may be
up to three feet or more.

The foreshore should be sounded periodically and bottom charts
prepared, showing the different materials (rock, clay, sand, shingle etc).
These charts may show the places where silting and scouring occur; the size
of the grains of sand must be determined as this gives an indication of the
strength of the bottom currents. The engineer in charge of estuaries or
shores should have complete records of the nature of the bottom of the
whole area in his charge.

The currents should be measured from the surface to the bottom under
different conditions of wind, tide and river discharge. The amount of sand
transported by the water can be measured at the same time by using special
instruments. The coastal belt in which these investigations are made should
extend two or three miles, or even more, from the shore.

Different kinds of instruments can be used but it is not easy to design
reliable marine instruments. The instruments necessary are an echo sounder,
a current meter, a bottom sampler, a sand grain meter, salinity meters etc.

There are two main types of sand catchers, one measuring the sand
content of the water, the other measuring the sand transported per minute.
For sand content measurement the open tube is preferred by many; it is
placed with its axis in the direction of the current, Figure 15. By means
of a small weight sliding down the wire suspending the instrument two
valves are released which shut simultaneously, actuated by a strong rubber
attachment. The content of the tube may be five litres.

The sand transported can be measured in a vessel having a small
opening at the front, through which the current flows without any deflection.
This can be obtained by means of suction behind a collar. The idea is that
as the flow expands inside the instrument it drops its sand and silt, Figure 16.

Some oceanographic instruments (e.g. the Petterson drill) can be
recommended.

The volume of sand streams, measured by means of sample takers or
sand transport meters, can be checked by comparing the volume of material
moved, as taken from the charts. Volumetric comparison of old and recent
sounding charts is most useful. If the places where scour has occurred are
shown in blue and the silted parts in yellow a good picture is obtained. The
scouring and silting quantities must balance each other after geological
subsidence has been taken into account. Hydrographic charts show
principally shallow spots and relatively few deep figures. Engineers need
more detail than hydrographers, especially near shores and on sand banks.
For volumetric comparison of the channels use should be made of cross
sections sounded with an echo sounder. Charts based on lead soundings
and on echo soundings may differ; the echo sounder generally gives more detailed results. Liquid mud bottoms and also sand bottoms, which commonly have huge bed dunes, show considerable differences in depth when sounded by echo and by lead.

It is important to know at what distance the four or five fathom (7 or 9 m) depth line lies from the shore. If this line is moving close inshore the coast will recede after a few years.

Off shore waves or tidal fluctuations can be measured by putting the oscillators of an echo sounder upside down on the bottom of the foreshore and connecting these with insulated copper wires to the recording instrument on the shore.

Wind velocities and directions are usually recorded at inland stations but they are not much recorded on coasts. Land breaks the force of the wind so coasts influence rainfall and sunshine to a marked degree; even low coasts have an effect when there are dunes, houses or trees. Meteorological charts for areas near the coast are generally insufficiently detailed for planning purposes or for agricultural needs.

The influence of wind on the water causes waves, currents and abnormal water levels. ‘Wind effect’ is the raising or lowering of the mean sea level because of the direct drag of the wind upon the surface of the water. A ‘storm surge’ is an exceedingly long wave produced by a depression or by wind elsewhere. It has a propagation of its own and the tidal wave is superimposed upon it. In the Wash and in the Thames estuary the tidal high and low water may be about 10 ft (3 m) above predicted levels (11 ft has been recorded above l.w. prediction at Southend), and on the Dutch and German North Sea coast the effect may be slightly higher. The influence of barometric pressure is included in this storm surge. Shallow waters show high wind effects, deep waters small ones.

The height of the wrack of floating weeds etc left on an embankment or shore should be measured after each storm. In the Thames, the wave can surge about 7 ft (2·1 m) higher than the storm h.w. level, but on many coasts it can be much higher.

It is important that the tide gauge records should be kept to the exact time, because the slope of the surface level between two stations is largely dependent on time differences (see p 1082 et seq). Electric clocks are best for tide gauges. One basic level only should be used for all gauges, and the heights of the water level at the recording gauges should be frequently checked with non-automatic ones placed near them. Moreover, in order to learn the variation of the mean sea level, there should be a few unalterable, totally stable, mean sea level recorders, which should be quite foolproof against any human attempt to alter or correct them.

An empirical formula for the influence of wind on wave height and wave surge on a shore can be obtained by laboratory research.

If the grade of the shore is 2 in 7 the depth of the water is \( d \) and the force of the wind at 6 m height is \( S \), the height \( Z \) in metres (1 m = 3·3 ft) to which a wave surges above the mean water level is, according to laboratory tests made by THIJSSE in Delft

\[
Z = 5 \left( \frac{d}{2} \right)^{1/3} S^{1/2}
\]

This is for the case where the direction of the wind is at right angles to the shore and the ‘fetch’ of the wind is very great. When the angle \( \alpha \) between the wind and the shore is different, or where there is a berm at the height of the storm level, the surges above this level are reduced according to the following scale.
The wave surge for shore slopes at other gradients varies as the tan of the angle of slope. If this grade is diminished from 2 in 7 (tan $\beta=0.286$) to 1 in 5 (tan $\beta=0.200$), then the wave surge is diminished by about 30 per cent.

In estuaries the tidal currents generally are stronger than on the coasts, whereas the waves are less powerful. These facts indicate the characteristic differences between estuary coasts and sea coasts.

The h.w. water level at the upper end of the estuary (Figure 17) may not reach the heights of h.w. attained nearer to the sea. This we will call the flood tide depression. It results from either too large a tidal capacity or too shallow and small a bottleneck in the estuary, or both. On the south eastern shores of the North Sea such flood tide depressions occur south of Antwerp, east of Rotterdam, south of Emden etc and also formerly in the Zuider Zee. Such areas involve danger when work or dredging is in progress in the bottleneck, because the tides will reach higher h.w.’s in the flood tide depression area. Such estuaries should be studied with great care. The Zuider Zee flood tide depression vanished when the enclosure dam was made. The h.w.’s came up to 3 ft higher, velocities increased by 20 per cent.

One method of dealing with tidal creeks, tidal rivers, and tidal tributaries is to dam them off, a lock being added for shipping. Such dams often cause higher floods and to prevent this occurring basins with low embankments are sometimes provided into which the sea flood may spill. Wide tidal rivers need large basins to lower the storm floods. This method is not very satisfactory because such a basin is not habitable and raising the embankments is often the better method.

When studying coasts, rivers, and estuaries, sand movement is often found to be the most important factor. Erosion causes an increase in the sand stream, silting means a decrease. Scouring also means that sand deposits elsewhere, often where it is undesirable. Strong currents cause damage to the shore and also much sand displacement resulting in unstable channels and bars; against these, dredging may be of little avail. Small currents of less than half a knot at 3 ft (1 m) above the bottom may allow the fine silt to settle. Medium currents of one half to one knot at 3 ft height may give stable conditions and an estuary in which dredging is required only at long intervals.

In estuaries where the currents are strong there is an excessive amount of sand movement, and the sand flows up the flood channels and down the ebb channels as indicated in Figure 18. When there are flood and ebb channels there are many circular sand streams in the estuary. Excessive sand movements of this nature indicate that Nature, not man, is the master; but shore defence and estuary training can reduce scour and erosion and thus reduce the sand movements. Circular sand streams have bad results because in that way bars are formed. Sometimes when such a bar is dredged the dredgings are dumped in the circular sand stream, thus making the dredging of little avail. (Actually the movement of a single sand grain is not circular but is much more complex because of
the ebb and flood streams; however, we may call these sand streams 'circular' to indicate that the same sand may return to the same spot over and over again.)

There are also the non-circular sand streams mentioned on p 1074 the magnitude of which can be learned by comparing the amount of material moved, as found from old and recent sounding charts. These non-circular sand and silt movements over a long period sometimes make the landward end of an estuary silt up while its seaward end deepens; sometimes the whole estuary may silt up when the coastal drift or the river itself provides much material. It is of great importance to know these slow geological processes.

Clay settles more quickly in salt water than in fresh water, because of coagulation (ionization); when water from a silt laden river flows into the sea this factor may be of great importance. Temperature has a noticeable effect upon the settling of silt, the settling being more rapid in warm than in cold water.

The difference in specific gravity of the fresh river water and the salt sea water may cause peculiar bottom currents which generally move sea sand in a landward direction (Figure 19). In deep river mouths of depth 30-40 ft (9-12 m) these currents can be strong and they may tend to cause a bar inside the river mouth which has to be continuously dredged.

Bars are of particular interest for research engineers but theory and practice have not yet been sufficiently coordinated to deal with them properly. Bars may grow higher even though strong bottom currents exist above them, silting being a question of the sand stream losing part of its sand during part of the tide. The growth of a ripple in a vertical direction may be akin to the growth of a bar, but there are also other factors.

In horticultural and agricultural districts the salinity of the estuary water may be of great importance. The limit for fine fruit is 300 mg of chlorine per litre; for cows, horses etc about 1,000 mg per litre.

**MATHEMATICAL RESEARCH**

The data gathered by means of site observations have to be analysed. It is remarkable how many hydraulic problems can be made clear and solved to a high degree of accuracy by mathematics and statistics. Tidal flow and tidal curves in new channels can be calculated accurately in this way, and sand movements to some degree. The height of embankments and the frequency of storm floods and abnormally low water levels, the mixing of salt and fresh water and many other problems can be approximately solved by statistical methods.

Frequency curves often assume the form of asymmetrical probability curves (Figure 20); when these are drawn on semi-logarithmic paper they produce approximately straight lines, but when the data are plotted on probability paper straight lines are seldom obtained. Data collected during different climatic conditions, as those of summer and winter, should never be
combined, because the graphs of the five winter months differ widely from those of the five summer months.

After much discussion it has been agreed in Holland that extrapolating such frequency curves to a not too far distant future can best be done by the straight lines on logarithmic paper. This method gives a mean between the two best known probability formulae, one giving an upward bend the other a downward bend on logarithmic paper.

Figure 21 shows the frequency curve of the storm flood heights at the Hook of Holland, which is characteristic of all frequency curves of storm floods along the Dutch coast. The strength of the wind at most places also has a frequency curve which is straight on logarithmic paper. These straight lines may generally be extrapolated to a frequency up to say 1/100 (once in a century). It has been officially proposed in Holland to build the main protecting embankments to a height which can endure storms, plus storm waves, which may occur once in 333 years (thrice in a thousand years). Generally this is from 18 to 22 ft (5.5 to 6.7 m) above mean sea level.

Literature—Many articles have been written about the mathematics of practical hydraulics, but modern theory seems to be progressing too rapidly at the present time to allow a general book being written about hydro-mechanics. What we chiefly lack is an exact knowledge of the laws of sand movement in tidal waters.

Laboratory Research

This kind of research has become a special branch of hydraulic science and is dealt with briefly in the chapters on Mechanics of Fluids and Canals, Channels and Rivers.

Tidal Action

Engineers dealing with coasts and estuaries should know the principles of tides, but they may find it difficult to master the mathematical details. The principles of tides can best be learned by studying an elementary book on alternating electrical currents. The details should be tackled by a mathematician or an electrical engineer well versed in telegraph or radio problems.
General analogy between tides and alternating currents:

<table>
<thead>
<tr>
<th>Electrical current</th>
<th>Tides</th>
</tr>
</thead>
<tbody>
<tr>
<td>direct current</td>
<td>stream in ordinary river</td>
</tr>
<tr>
<td>alternating current</td>
<td>streams in tidal channel</td>
</tr>
<tr>
<td>mixed current</td>
<td>streams in tidal inlet with river discharge</td>
</tr>
<tr>
<td>conductivity</td>
<td>conductivity $= \frac{xbh^{3/2}}{2}$ (Figure 22)</td>
</tr>
<tr>
<td>resistance</td>
<td>resistance $= \frac{1}{cbh^{3/2}}$</td>
</tr>
<tr>
<td>voltage</td>
<td>head</td>
</tr>
<tr>
<td>electromagnetic force</td>
<td>slope, gradient</td>
</tr>
<tr>
<td>capacitance</td>
<td>tidal capacity of basin</td>
</tr>
<tr>
<td>condenser</td>
<td>open harbour, tidal basin</td>
</tr>
<tr>
<td>self induction</td>
<td>inertia</td>
</tr>
<tr>
<td>angle of lag $\phi$</td>
<td>angle of lag $\phi$</td>
</tr>
<tr>
<td>conductor with varying capacitance</td>
<td>tidal channel or tidal river</td>
</tr>
<tr>
<td>Ohm's law</td>
<td>Chézy's law: $Q = cbh^{3/2}$</td>
</tr>
<tr>
<td>First law of Kirchhoff</td>
<td>$Q_1 = Q_2 + Q_3$ (at a knot of channels)</td>
</tr>
<tr>
<td>Second law of Kirchhoff</td>
<td>$M_1 = M_0 + M_2$ (around island)</td>
</tr>
<tr>
<td>$e = ir \cos \phi$</td>
<td>$Q = fbbh^{3/2} \sqrt{(M \cos \phi/l)}$</td>
</tr>
<tr>
<td>Telegraph equation</td>
<td>Lorentz equation</td>
</tr>
</tbody>
</table>

In this analogy $b$ is the breadth of part of cross section, say 30 ft; $b_1$ the total breadth of channel, $h_1$ the average depth of channel (the channel has to be considered as having a rectangular cross section); $Q$ the total flow through cross section (ebb + flood per cycle); $a$ the slope of water level; $c$ the constant of Chézy; $M$ the motive area = area between tidal graphs of two successive stations (Figure 23); $l$ the distance between these stations; $\phi$ the angle of lag, generally about 0.9 in tidal channels as well as in electric nets.

Figure 24 can be found in all elementary books dealing with electrical currents. It gives the relationship between the vertical and the horizontal tide. The slopes cause the stream currents, the latter lagging $\phi$ behind the former because of inertia.

A tidal net, containing many channels, receives its impulses from the sea. The boundary conditions are some miles outside the inlet mouths because these mouths influence the tide in the sea. It is difficult to measure the actual vertical sea tides, but they can be found either by calculation, starting from the tides in the mouth or bottleneck, or by using special instruments laid down for periods of sixteen days on the bottom of the (shallow) sea.

The direction of the tidal wave in the sea is of great importance because the main channel will be shaped in the direction from where the tidal wave comes.

Tidal channels parallel to the coast may have small currents because they form a 'Wheatstone bridge' with only a small motive area (Figure 23). All components of the tides in any new net of channels can be calculated, the horizontal tide (currents) as well as the vertical tide. With the well known tide predictors the tides of any new net of tidal channels can be
predicted easily for any future date, when the components are calculated or known. The tides which occur when the river discharge is low, normal, high or very high can also be calculated for the proposed net of branches of the tidal delta.

The direct wind influence can be calculated too, but for deep, narrow channels this influence is small. The surge (indirect wind influence) may be very large. For shallow wide areas the following formula holds good:

\[ e = \frac{a V^2 L \cos \phi}{H} \] ..........(6)

In equation 6 \( e \) is the wind effect (extra direct raising of the sea level), in cm; \( V \) the velocity of the wind in metres per second; \( L \) the fetch, in km; \( H \) the depth of channel, in m; \( a \) the constant, about 0.032; \( \phi \) the angle between wind and channel.

When the wind effect or storm surge in the sea is of importance the tides in the future net have to be calculated also for high sea levels and low sea levels.

Figure 25. Dual scheme of electrical imitation of tidal river (quadratic law of resistance)

Tides can be imitated with copper wires, condensers, resistances etc though there is one marked difference between electrical and water currents: in electricity we have the basic formula (Ohm's law) \( e=ir \) with water (Chezy's law) \( e=i^2 r \) ..........(7)

In equation 7 \( e \) = electromotive force, or slope \( a \); \( i \) = current or flow of water per sec; \( r \) = resistance.

LORENTZ of Leiden University, when having to calculate the future tides outside the Zuider Zee dam in 1918, did not use the quadratic (hydraulic) law but the linear one, by taking a new constant \( k=ci_0 \); therefore \( e=ir \) became \( e=ki \) and so the telegraph equations could be used. This linear method can be imitated electrically and all components of the tides can be measured electrically or made visible with a cathode ray tube. The more exact quadratic law can also be imitated electrically by using special rectifiers or special valves. The accuracy of such an imitation is great, but when using 'quadratic' metal rectifiers a dual scheme must be used. This means that voltage becomes current and vice versa, capacity becomes self induction and vice versa and so on (Figure 25). With valves the non-dual scheme can be carried out.

The propagation of tides can be considered as 'natural', or as advancing and cast back waves, the propagation velocity of which is proportional to \( \sqrt{gh} \). Both views are right, but with the first the propagation of the visible wave is not proportional to \( \sqrt{gh} \).

Conductances in the different cross sections vary in a 'wild' estuary, especially when man has used groynes instead of good smooth streamlines. For a steady well regulated or quiet section of a natural channel, the relation

\[ F = \frac{Q}{bh^{1/4}} \] ..........(8)
should be more or less a constant. That is, the conductance and the total flow (ebb + flood per tide) should become larger, both in the same degree, when going towards the sea.

For two cross sections, distance \( l \) apart, the following formula gives the difference in conductances:

\[
b_1 h_{1}^{3/2} - b_2 h_{2}^{3/2} = \frac{2AB\cos \phi}{F}
\]

where \( A \) is the amplitude, \( B \) the fill breadth of tidal river, and \( \cos \phi \) is about 0.9.

When for navigational purposes depth \( h \) is made a constant, we obtain the flare formula of Chatley:

\[
b_1 - b_2 = \frac{2000AB^2}{Q} \text{ ft per km}
\]

A 'flare' is often not advisable, however, when currents due to differences in specific gravity and sand streams have to be taken into consideration.

The 'left tendency' of tidal channels is caused by a tide in the sea coming from the left (e.g. the mouths of the tidal waters along the south eastern shores of the North Sea). The theory of electricity (or of tides) can easily explain this (Figure 26), because the motive areas will be greater in the left hand channels than in the right hand channels. The co-tidal lines and the amplitudes of the tide define the cross sectional areas of the channels.

Harmonic analysis is the empirical fixation of the amplitude and phase of the component sinusoids in tidal graphs. Instruments, called harmonic analysers, resembling a planimeter, can be used without much trouble; for learning the tidal components used for actual tide predicting, however, one of the methods developed by tide experts must be followed (Doodson and Warburg).

A tide predictor is a machine in which the component sinusoids are running each in its own phase: one of the famous tide predictors can be seen in the Tidal Institute, Birkenhead, England. This Institute will also undertake the harmonic analysis and prediction of existing tides at any place.

Horizontal tides (streams) can be predicted as well as the vertical tides for any date in the future when the component sinusoids are known, but the wind and other meteorological influences are not taken into account.

Near shallow coasts these influences are great.

Harmonic analysis and tidal calculation differ. The first is the analysis of existing tidal curves and prediction of them when no hydraulic changes occur in the channels; the other uses the fundamental law of Euler and calculates new tides in new channels.

Because of the quadratic relation between friction and current the higher harmonics \( M_4, M_6, M_8 \) etc are produced more and more when the tidal wave travels landward, i.e. the front of the wave becomes steeper. These harmonics are called shallow water harmonics. They change in amplitude and phase when dredging is going on, which is when the resistance changes.
Coasts, estuaries and tidal hydraulics

A bore is a breaking tidal wave which only occurs where the tidal amplitude is large and the depth is shallow; it vanishes when dredging increases the depth.

A ‘Wheatstone bridge’ channel, Figure 27 (the Dutch Wan tide, wan meaning abnormal, queer) is a tidal channel in which only weak tidal streams occur; generally it is a channel more or less parallel to the coast. The vertical tides remain normal in such a channel.

Double the number of flood tides, ebbs, and slack waters may occur, a so-called horizontal $M^4$ tide; but the vertical tide remains a normal $M^2$ tide, with two high waters and two low waters. Vertical $M^4$ tides are responsible for double h.w.’s and double l.w.’s. They may disappear when resistance is slackened by dredging. The double h.w. at Helder has vanished largely since the Zuider Zee was shut off in 1932.

At the meeting line of two flood streams between an island and the coast (this line is also called Wan tide in Holland) (Figures 14, 27) there are also an irregular tidal flow and a regular vertical tide.

**CURRENTS**

When measured with good instruments the current velocities are generally highest near the surface, diminishing towards the bed according to the law

$$v = ah^{1/2}$$

in which $v$ is the velocity at height $h$ above bottom, $q$ is a figure (5 to 7), $a$ is the velocity at $h=1$ m above the bottom (Figure 28).

This is for homogeneous water, without wind effect. In the North Sea $q \sim 5$; in rivers we find $q$ higher, approximating to 7 or 8. There are other formulae but equation 11 is the most simple and its graph lies about in the middle of the graphs of other formulae sometimes used.

In deep channels there is relatively more scouring because $a$ is dependent on $\sqrt{h}$.

The formula for stream verticals which is used most nowadays is a logarithmic one. The writer does not quite agree with this use, not because the velocities differ so much from those of the parabolic formula quoted above, but because the parabolic formula is more simple and it gives better results as regards the sand movements. The discrepancy of the logarithmic formula is too great near the bottom, where for $h=0$ the velocity becomes $-\infty$, whereas it should be 0.

Much research is being done to try to express the sand movements, caused by currents, in some mathematical formula. Agreement seems to be reached about the line of sand content in some vertical to be an exponential function.
Currents

When starting from the formula

$$v = ah^{1/4}$$

we find

$$N_z = N_a \exp \left( - \frac{C \sqrt{g}}{s} t (z - a) \right)$$

where $s$ is a constant, dependent on $q$, with a value of about 1.62 to 1.65; $C$ is the constant of the Chezy formula; $c_1$ is the terminal velocity of 'mean bottom sand grain' falling through water; $g$ is the acceleration due to gravity; $H$ is the depth of water; $i$ is the slope; $h$ is the height above bottom; $z = h/H$; $N_z$ is the sand content at relative height $z$, and $N_a$ is the sand content at relative height $a$.

Equation 12 is for continuous currents; $c_1$ is affected by the temperature of the water.

When checked with actual measurements made in the Mississippi and in the Dutch waters (tidal or non-tidal) equation 12 has proved better than the formula based on logarithmic stream verticals (equation 11).

Generally it is found that the total sand content in a vertical varies with $v^3$ or $v^4$, which means that the total sand transport varies with $v^4$ or $v^5$. If a spring tide current is twice as strong as a neap current the former will transport sixteen to thirty two times more sand. Tidal channels therefore are kept wide and deep by the scour of spring tides, more than by the scour of the normal tides. Neap tides have little scouring power.

In tidal streams, where silting and scouring change even during the tide, we should not lose ourselves in too much detail. The graph of sand content in a scouring river is markedly different from the graph of a silting one, Figure 29.

A sand-laden stream will not pick up more sand than it can carry. This is the reason why bars will not scour. A stream not carrying sand, e.g. a stream coming through a weir or barrage, is able to pick up its full load. Scour may therefore take place downstream of a patch of rocky bottom, thus originating a sand stream. Narrows (e.g. the Straits of Dover) may show such a clean rocky bottom with no sand movement above it. Its huge stream is undercharged.

Nevertheless in such regions there may be long and high sand banks lying on the hard bottom in the general direction of the ebb and flood currents. Because they offer little resistance to these currents they have remained in their places during the past centuries. They resemble the desert formation called Lybian dunes, Figure 30, 31.

When the sand grains are the right size and the currents have the right velocity a sand bottom will produce huge bed dunes, perpendicular to the general current direction. These submerged dunes may be 20, 30 or even...
60 ft (6 m to 18 m) high in the southern North Sea and about 3 ft (1 m) in a river of say 15 ft (4.5 m) depth. Generally the height is about 20 per cent of the free depth. The form of these huge ripples depends on the supremacy of either the ebb or the flood. They give an indication in which direction the sand is moving (Figure 32). Regular bed dunes can only occur where much sand is available and do not occur when rock, or a clay bottom, is partly exposed to the currents.

Where only a small quantity of sand is lying upon a rock or clay bottom this sand collects into 'barchan' dunes where the current is continuous in one direction, and into long sand banks, resembling Lybian sand dunes, where there are alternating currents.

In estuaries, ebb channels usually make the best navigable waterways, but in the outer part of a delta a flood channel may be the best entrance when the ebb channel has a high bar there. The aim of the engineer is to make the ebb and flood channels combine in such a way that a deep fairway results. Here Nature opposes because of sand movements in directions from and towards the sea. The way to attain good results is by protecting the banks, constructing training walls, or dredging, to forestall bend erosion and excessive sand transportation. The lower Scheldt is a fairly good example of what can be attained by good fixation of the shores. With the Scheldt the sinuous ebb channel or shipping channel is kept in fairly good condition by its defended shores. The flood channels spring forth at every bend of the ebb channel; they serve a local function of filling part of the estuary.

The Ems estuary was originally also of the ideal poplar type but the Germans decided to make a straight shipping channel and therefore chose the line of the flood channels, Figure 33. It is questionable whether they
chose rightly for there is no defended shore to help that channel. Nowadays dredging and training walls can force almost any solution, though construction and dredging are costly. It will be interesting to see whether the ‘trunk’ or ebb channel can be straight, and the ‘branches’ or flood channels curved.

When a non-tidal river branches off from the main river at a blunt angle the sand will go mainly into that branch because the weak bottom currents (carrying the bulk of the sand) can be deflected more easily than the stronger top currents which flow straight on. The sand may partly settle at A (Figure 34) but the rest flows in the new direction. This angle effect provides a means of diverting part of the river sand into places where it is required. The layout of the dividing points of branching rivers or channels should be constructed with care when they carry sand.

With tidal channels the same principle is at work. The bar is likely to be at the end of a flood channel which may be almost at right angles to the ebb channel. On such a bar the flood channel at flood, as well as the ebb channel at ebb, deposit sand, because the flood in the flood channel is near the end of its fill area and therefore weak in volume and the ebb branches off almost at a right angle towards the flood channel.

Tidal sand streams can be controlled as follows:

1 by making the fill area larger or smaller. If the flow into the fill area becomes smaller the sand stream will be much more so and this may mean less dredging than when the currents were too strong

2 by making good alignments and good dividing points with the aid of spurs and shore defences

3 by dredging; the new depths attract the currents while those in the undredged concurring (parallel) channels slacken.

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Figure 34. Influence of a symmetrical and asymmetrical bifurcation on sand movement A is point where sand may partly settle

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Figure 35. a and b two different ways of training an estuary; b is most economical E ebb channel, F1, F2 flood channels
The wider and larger the tidal channels, the less man can influence them; if a channel is narrow and deep it is more manageable. Large sea shore currents are extremely difficult to influence. We must accept them as they are, but we should not neglect to study them as well as their results.

Example—In the estuary indicated in Figure 35a, there are two flood channels $F_1$ and $F_2$. The latter has been diminishing and the former has been increasing, so that it might be expected that $F_1$ would become the main shipping entrance. To accelerate this, it is proposed that $F_1$ be dredged and that a flank embankment $h$ be constructed along the outer bend of $F_1$, that several long groynes be made across $F_2$, and that a groyne $f$ would serve to make $E$ flow into $F$ without an intervening bar.

This scheme is largely fictitious but serves well as an example for comparison with an alternative scheme (Figure 35b), which has the advantage that a parallel embankment on the high sand bank between $F_1$ and $F_2$ would be much cheaper than the groynes $a$, $b$, $c$, $d$, $e$ and $f$, because parallel works are easy to construct and the sand bank is high.

Secondly, the action of groyne $f$ (Figure 35a) projecting far outside the normal lines would be contrary to the principle of a stream line. A large deep hole would be scoured out, a very bad river portion would result, and $E$ and $F_1$ would not run into each other smoothly.

Thirdly, the parallel embankment $h$ should be connected with the shore at the upper end of that embankment, because the tidal area behind it should be filled and emptied from the sea end. The parallel embankment would be expensive, being made in rather deep water. It would have to be protected over the whole length against attack by the currents. It would, therefore, be cheaper to make a parallel embankment on the higher parts of the tidal sands and to construct small groynes of say 300 ft (90 m) length and at 500 ft (150 m) distances apart projecting from the embankment.

The main trouble here lies near the cape at $C$ where sand may deposit easily. The estuary should not be too wide there, and the channels $F_1$ and $E$ so situated that they join up. Channel $E$ has already in the past moved too far seaward towards $C$ because of bend action, so either channel $E$ or $F_1$, or both, have to be deflected to such an extent that they will coalesce.

There is an old belief that estuaries must be wide in order to have deep channels. This is far from correct. Wide estuaries have large fill basins and therefore large channels, but too much width means also too much liberty for the ebb and flood channels to diverge from each other. Moreover the need is not to have excessive currents and sand displacements, but moderate currents with no sand or mud displacement.

We should not try to obstruct any tidal channel which runs in vast tidal sands because the currents would seek a new channel round the dam, forming an island of it. Such structures attract currents and cause scouring by inducing turbulence in the water. If tidal channels have to be obstructed the dam must be connected with the shore and its seaward end must be far out over the top of the next sand bank.

Though we may expect to be able to calculate sand streams in tidal waters with a moderate degree of exactness in the not too far future there are some baffling problems, especially in connection with the formation of bars in tidal areas and the formation of bed dunes. We should try to learn by calculation why some estuaries or coastal foreshores are eroding, while others show accretion; and we should consider whether we can influence the ebb currents or flood currents so that the former may create a larger sand stream than the latter. The mouth of the Scheldt and the lower half of its estuary has deepened more than 3 ft (1 m) in a century (calculated over the whole area of the mouth) and most other Dutch inlets have also increased their mean depth in this period. The exact cause is not yet known, but it is a geological fact that most coasts are losing sand. This sand goes to the outer sides of the submarine deltas.
The energy of the wind acting on the water is partly stored in the waves. When these break on the shore this energy is largely spent in destroying the coast or in displacing material.

There are three different coastal zones to be considered: those acted on by stream currents, waves, and wind. They are not sharply separated (Figure 36a). The wave zone of a coast is most attacked when an open sea front is concerned; in estuaries the stream currents may be the most destructive.

When a coast has tidal basins the situation of the three zones becomes as indicated in Figure 36b. At regular intervals the streams will have broken through the off shore bar, and dune islands may have formed between the breaches.

Waves create strong bottom currents and much turbulence when they break, Figure 37: wave action alone can create spits etc as can be seen in lakes. Wave turbulence ‘lubricates’ sand movement by water currents. Wind blowing towards the land causes a surface current in that direction and a bottom current in the opposite direction outside the plunge line. This bottom current, especially during storms, may carry much sand seawards. In calm weather some of this sand is carried back by the movement of the breaking waves. Sand which has been transported during the storm into the deep layers at some distance from the shore does not return; generally the shores lose much material and the gains are small.

The submarine sand shore requires a certain slope, say 1 in 100, to be in equilibrium. Coastal retrogression will occur when the slope is steeper; such a coast is called a ‘poor’ coast. When the waves throw a bank of sand on the shore the coast becomes ‘rich’, temporarily.

Waves may create sand ridges of about 3 to 6 ft (1 to 2 m) high, lying parallel to the coast in the breaking zone. These ridges are pushed up the beach when the weather is calm, Figure 38.
Coastal inlets with sand movement have a submarine delta outside the entrance or bottle neck, Figure 39. Such a delta does not grow above a certain level, say about L.W., because wave action opposes further accumulation. A marine delta of this kind may protect the lee shore, because waves break on the sands of the delta and they carry some sand from it on to that shore, making it richer. The littoral drift passes over and along the outer side of the submarine delta. Because of this, and because of the protection which the delta provides, the ‘head’ of the leeward island or coast of such a bottle neck formation may protrude outside the general coastline. The other shore of the inlet shows a ‘tail’ or common spit.

When a lagoon is silting up the streams in the bottle neck decrease, because the tidal fill diminishes; hence the size of the submarine delta also decreases and the protection this delta provides against wave action decreases. When the lagoon has silted up completely the submarine delta will have vanished and the coastline will have become a smooth line of sand. Heads and tails will then have disappeared.

Homogeneous sand shores always show smooth lines because action and reaction is everywhere the same over long distances. Some danger of losing land may result when man alters this smoothness by making defence works, harbour entrances etc. The size of the channels in a submarine delta, as illustrated in Figure 39, depends on the motive areas (gradient of tidal levels, see Figure 26). When the tidal wave comes from the left the size of the channels diminishes from left to right.

**SHORE PROTECTION**

**GENERAL**

Shore protection probably started with planting willows (fresh water) or other plants. Protection with wooden boards or stones may have followed soon after, but it is said that the Chinese, who in early times excelled in making embankments and river improvements, neglected the underwater part of their defences. This is still one of the main faults of many coast defence works.

In medieval Europe the building of embankments seems to have first started on a small scale in England before the Norman invasions (Dobbie states that Romney Marsh was diked before A.D. 772).

In Holland most of the alluvial land was reclaimed by embankments (dikes) before 1200; but after that year much land was lost again because the level of the land had sunk due to settlement of the soil resulting from better drainage. From 1200 to 1930 more land was lost to the sea in Holland than has been reclaimed from it.
Shore protection

The embankments of the Low Countries were originally protected by heavy wooden structures and by mattresses of willow boughs below L.W. These costly wooden structures were eaten up by the pile worm after about 1730, which caused much anxiety throughout the country. Stone defence, based on the principle of grading material (e.g., fine, coarse, coarser, very coarse) was found to be the solution. By this principle sand can be protected by small gravel, and small gravel by coarse gravel, debris, or broken stones, and the latter by stones heavy enough to resist wave attack.

The pores must be as small as possible and be made smaller and smaller in a downward direction. No sand may pass through the pores of the layer of shells or gravel; no shell or gravel may pass through the pores of the coarse gravel; no coarse gravel may pass through the pores of the bigger stones; etc. This is the principle of grading. Mussels and other small shells should be allowed to cement the stones together.

An example of a defective revetment where this principle has not been observed is shown in Figure 40. The defects are:

1. Sand will be washed away through the pores of bricks, rubble, and basalt. There should be a layer of tough clay covered with krammat (straw) underneath the layer of bricks.
2. Unless there are groynes, or the beach is in equilibrium, the toe of the revetment is not safe; there is no grading to prevent the washing away of sand through the large pores of the toe.

Therefore the method should be slightly changed. Sand is protected by a layer of good clay, this clay is protected by a layer of straw, krammat, and above this the layers of rubble (or gravel) and heavier stones can be placed. Straw is not a permanent material, however, as it will rot. The clay must, therefore, be protected with small sized material as well. The wave currents seeking to penetrate the pores must not be able to reach the layer of clay.

Figure 40. Example of revetment with weak toe

When underwater protection of a sandy bottom is needed, the use of willow mattresses is the ancient well tried method. By using reed (with the leaves still on) as the central layer between the willow layers, the zinkstukken (willow mattresses) become less penetrable to currents. However, willow mattresses are not completely impenetrable to strong currents. It might be necessary to have a layer of gravel or rubble underneath to protect the sand bottom. Asphalt sheets are impenetrable, but they cannot yet be made in as large sizes as the willow mattresses. Moreover, they cannot float as willow mattresses can. Asphalt sheeting under and above water is still in an experimental stage. Pumping air inside the sheets to make them float might be a solution; the air being released to sink the mattress.

A general rule is to use local material as extensively as possible. Heavy clay, dredged from the sea bottom in the neighbourhood, may serve as ballast for the mattresses, but this clay may dissolve after some time by molecular action. Also certain stones may crack and split up after some years and such stones and clay should not be used.

The art of making coastal defence as economical as possible is difficult because of the variety of shores and material. Often much rock is wasted by lack of a mattress foundation, which should prevent scouring while the
work advances. A sand bottom should be well covered with a mattress or with good layers of fine and coarse gravel before the coarser material of the training wall, which causes a strong current in front of it, is brought into place.

The construction of dams on a rock bottom was carried out with success at Scapa Flow during the last war. Crates of steel mesh, 6 ft wide, were filled with rip-rap and placed with the aid of a cable spanning the fierce tidal streams from island to island.

When it is desired to construct a dam across a gap with an erodible bottom, a rock apron (or mattress) strong enough to resist excessive erosion should first be laid. In the breaches of Walcheren (1945) 71 ships, up to 3,000 ton weight, were scuttled in the gaps. The use of such large units is the latest development in closing tidal gaps. Using steel mesh sausages filled with rip-rap, placed with their axes in the direction of the streams, is also a good method where rip-rap is available. In the gaps of the Zuider Zee dam heavy barite stones were used.

As erosive action is proportional to about the fifth power of the velocity, gaps cannot be closed economically at spring tides. At Walcheren, with a tidal rise of 10 to 15 ft (3 to 4·5 m) the work of closing the gaps was carried on during neap tides only.22

STREAMLINE PRINCIPLES

One of the main methods of coastal defence is to build artificial capes which can be placed at regular or at irregular distances; for the latter, existing strong points are used. The aim is to divert the streams from the shore i.e. to protect the land. Vierlingh (1570) laid down the principle that streams should be gently deflected: 'he who exerts force on water, will have to meet the force of the water.'

This very simple, self evident, rule of action and reaction is the principle of streamlines. No one would think of fixing an angle section on the wings of a plane with one leg at right angles to the wind, but in hydraulics we sometimes meet with such obstacles. Single groynes create much turbulence and very irregular cross sections with extraordinarily large local disturbances, and they will attract the channel instead of pushing it from the shore, Figure 41. Moreover they are costly, because the force of the stream makes frequent repairs necessary.

Fargue25 in the second half of the nineteenth century formulated his well known rules for correcting rivers; they were rules bearing on streamlines and their objects were to make the river carry its water, sand and ice rather than to protect the shores of the river, though this was included. On shores of estuaries and coasts, the streamline principle should also be taken into account, especially when the shore itself is streamlined by nature.

Where a series of groynes is built, Figures 42, 43, scour will occur on either side if the series ends abruptly. Sometimes a salient point e.g. a harbour pier, is specially required and a large deep hollow will be formed just in front of it.
Types of groynes and other shore defences

The top of the wing of an aeroplane has a lifting function as well as the under surface. In the same way the inner bend of a river can be streamlined with a parallel embankment (revetment) in such a way that it attracts, or keeps, the current so that good navigable depths may be obtained even near the shore of the inner bend. This is, as seen from a theoretical viewpoint, totally different from the irregular depths found along shores defended by groynes.

When the current in a branch of an estuary is not strong enough to cause scour, yet is sufficiently strong to prevent silt from settling, the streamline principle can be neglected to a large extent. These channels make good sites for harbours and industries because extra wide river sections can be made that may remain stable.

The alignment of tidal channels should be in accordance with their breadths as flood and ebb should be led through the same parts of the channels (Figure 44).

A good type of a half trained, half natural estuary is the Lower Scheldt. As has been explained already, the reason why the Lower Scheldt has a good fairway is that the shores offer the right resistance at the right places. If the shores of the Scheldt estuary had not been protected, or had been protected in other positions, the Scheldt would have no more navigable depth than the East Scheldt, north of Walcheren, and would be ‘wild’. Streamlining was not, however, the object; the aim was to fix the bends.

TYPES OF GROYNES AND OTHER SHORE DEFENCES

There are so many different coasts and so many ways of constructing groynes and revetments that it is not possible to give one solution only. Experiments with the materials at hand have been made on many coasts and have resulted in some method being devised which is economical and successful. These experiments still go on however, a sign that the art of finding the most economical way of defending a certain coast is not easy.

Three main types of coastal defence can be discerned:
1 revetment type
2 groyne type (artificial cape type)
3 small groyne type (using the coastal drift as a means of defence).

Revetment type

The whole shore surface is protected from a low level up to a certain height above high water (Figure 45). This is a very costly method. The streamline principle can be followed, so that the stream shows little turbulence near the
Coasts, estuaries and tidal hydraulics

Figure 45. Revetment type of protection

shore, but nevertheless the cost of upkeep is often enormous. The defence works near Den Helder in Holland, shown in Figure 45, are the most costly shore defence works in the world; mattresses and stones have had to be added at frequent intervals for more than 150 years. Instead of using expensive Belgian stone an experiment is now being made to use local diluvial clay, dredged nearby. The revetment type of protection should extend further than the lowest part of the channel, when the current is the cause of coast recession. For wave eroded coasts less depth may be sufficient.

When there is a stable beach, or when there are saltings, only the part above the beach or saltings need be protected. But great care should be taken that such a revetment is not undermined. Figure 40 shows a stone revetment the 'toe' of which is not well cared for. This toe does not show the principle of grading so that sand or clay may be washed out. Often such a high beach or salting has to be protected by groynes, or if possible with plants.

A row of wooden stakes or faggots at the toe may be of some slight use to allow the beach or salting to be lowered a little by the waves without causing damage to the revetment, but they will not stand much loss of beach height.

Waves act fiercely on a revetment as they arrive unbroken. The upper layer of stones should be heavy enough and well placed and keyed, so that only small amounts of water may penetrate into the revetment. Mussels must be allowed to grow on them. Some engineers prefer wooden poles sticking about 3 ft (1 m) high out of the revetment in order to break the force of the waves. Others object to this construction because they consider that the poles are vibrated by the wave action and loosen the revetment.

Several experiments have been made using grout for closing the pores, but a rigid closed surface has the disadvantage that large holes may form underneath it. Even on old, well settled embankments, large concrete slabs or a rigid closed cover of concrete are hardly advisable. Asphalt in the pores allows more settling, but the engineer should beware of making a non-flexible, closed surface where the foundation and footing are not very stable. Bitumen filling can, however, be recommended in the case of many old stone revetments.

Bitumen slabs can be made of 13 to 20 per cent bitumen, 70 per cent sand and the rest small gravel. The slabs can be made in situ or placed with a crane. They have the advantage over willow mattresses that they do not rot above L.W., and that they are watertight. They may be useful in places where stone and willows are not available, but they have the disadvantage of being rather small, with many seams. Experience with bitumen slabs is still limited, especially for use under water, but they may be increasingly used in future. Plants seem to be activated by asphalt so that they may grow through the slabs; the bottom must therefore be made sterile before the slabs are laid. Reinforced asphalt slabs can be handled by crane but the difficulties are considerable.
Types of groynes and other shore defences

Small wave action may be opposed with small means; concrete tiles or bricks of baked clay, or even loose debris may suffice, and grass and weeds should be encouraged to grow between them. Willows, reeds or rushes may be planted to protect the revetment; willows need fresh water, reeds and rushes may grow in slightly brackish water. Saltings or foreshores can be encouraged to silt up to a higher level, see p 1102.

Straw thatching (krammat) and wood thatching have their uses for temporary defence. Krammat is also used as a temporary protection for a clay layer under a stone revetment.

Artificial cape type of groyne
Groynes of the artificial cape type have to be of solid construction and have to be stronger than natural capes. The most important feature of such a groyne is its head. The stones on it must be heavy enough to prevent their being rolled away by the waves and, to prevent the stones settling into the sandy bottom, willow mattresses are needed, or else the principle of grading should be used. The underwater part of the head must be frequently examined and the sea bottom around it must also be sounded regularly.

The length of the groyne, Figure 46, must be longer than \( d/a \), when \( d \) is the depth to be expected in the deep hole in front of the groyne and \( a \) the slope of the sand along the groyne.

If the groyne is made too short, Nature will take material from the shore until it is satisfied, Figure 47. Especially with single groynes the depth \( d \) will become greater and greater and the shore will, therefore, recede more and more.

The ‘body’ of the groyne connecting the head with the shore is of less importance than the head. Its object is to prevent a gully forming behind the ‘cape’. In the older types the body was usually of stone (Figure 48) and much attention had to be paid in making this solid enough to prevent waves destroying it. When the beach lost sand, as was often the case, the stone groyne was left as a high unnatural ridge on the beach and, having lost its side support, toppled over or had to be lowered. Often a side berm had to be made on both sides to obtain a new streamlined cross section. Figure 48 shows only one berm; when the right hand beach lowers still further another berm will have to be constructed and when the beach lowers still further the whole construction will have to be made anew. Bitumen can be used to fill the gaps of the upper layer of stones, when stones are used.
It has been proposed—and there are already some groynes constructed in this way—that the head should be joined to the shore by sheet piles (Figure 49). In some cases the heads of the steel sheet piles have been worn away by the blowing and washing sand, so concrete sheet piles, with a good concrete slab over their tops, are preferable. When a sand beach loses much sand the sheet piles can be driven deeper with a water jet: thus the top of the groyne need not become too high above the beach.

![Figure 49. Groyne (new type) using concrete sheet piles as connection to shore](image)

Small groyne

The small groyne, or beach groyne, resembles a fence and is made of wood or concrete, Figure 50. Its object is to retain the shingle or sand of the upper part of the littoral drift. When using wood, the danger of pile worm must be considered; wooden groynes cannot reach to great depths. Most engineers would prefer permeable groynes passing some littoral drift. One of the functions of small groynes is to break the waves.

Another method of using coastal drift of sand as a means of coast protection is to pump this sand back to where it came from. An experiment has been carried out with this method on the Dutch island of Goeree. Considering the costs the results have been fairly satisfactory, as far as experience goes.

Willow mattresses are of great value in protecting the shore below water level. They consist of a lower grid of fascines consisting of bundles of willow boughs, diameter about 4 in (10 cm), spaced 3 ft (1 m) apart, with an upper grid of the same construction. Between the grids two or three layers of willow boughs are pressed down and bound with ropes. Sometimes a layer of reed (preferably with leaves) is put in the middle instead of a layer of willow boughs; the purpose is to prevent bottom scour under the mattress as far as possible. Instead of willow boughs, other local material can be used such as millet stalks, papyrus, blackthorn etc. The total thickness of a mattress is about 2 ft (0·6 m).

Other methods may be developed for protecting the underwater part of a shore or groyne, for instance, by petrifying sand with some chemical solution.
Types of groynes and other shore defences

Examples—There are three main points in making solid groynes, embankments, revetments, training walls and piers which must be considered carefully:

1. the top layer must consist of stones heavy enough to lie steady despite the impact of waves, and they must be well keyed, or grouted with a bitumen mixture.

2. the grading towards the bottom must be so gradual that no sand, gravel, shingle or larger stones can be washed out.

3. the "toe" must be sufficiently low down and adequately protected against scouring.

These points are illustrated in the following examples:

Figure 51. Unsafe stone training dam on sandy bottom

Figure 52. Action of cross currents on wall of insufficient height

Figure 51 shows the cross section of a training dam laid on a sandy bottom. Where there is a littoral current there is severe scour in front of the groyne or training dam while it is being constructed. This is called 'head action' and is the cause of an unnecessary deep foundation of the training dam. The amount of stone may be two or three times the calculated amount, unless the bed is protected by a stone apron before the training dam is constructed. The principle of grading is not wholly neglected in Figure 51. Still, the sand from the bottom will be washed out by wave currents or by stream currents particularly at A and B and the stones will topple down. Even the central part of the foundation near C is not safe against being washed out. When a training dam with such large pores is made upon a sand bottom, a mattress should be laid well in advance to prevent scouring by head action and to prevent later scouring because of wave and other currents through the pores.

Figure 53. Cheap groyne for a shore with small cross currents and small waves

Figure 54. Cheap groyne for a shore with small cross currents and slight wave action. Height up to h.w. or higher

When there are cross currents at h.w. and the spur or training dam is not made to that height, the water will wash over the structure and cause a deep scour immediately behind it; the training dam will slide into the scour hole. To prevent this the structure should be raised up to or above h.w. mark (Figure 52).

Figure 53 shows a cross section of a cheap groyne often made in Holland. During slack tide, sand is dumped or washed into place and after that this sand is covered quickly with a mattress before the tidal current sets in. These groynes will stand when there is not much wave action and not much cross current, but where cross flow occurs the sand might be washed away from under the mattress.

Because willow boughs will rot above l.w., they should be used only slightly above this level. In order to prevent cross currents flowing over a l.w. groyne a mound of stones can be built upon the l.w. groyne, as in Figure 54, but such a mound is not watertight. The currents will pass through its pores and the sand may be washed away from under the mattress. This could be prevented by a special layer of gravel or shell as shown in Figure 55.
Coasts, estuaries and tidal hydraulics

For dams parallel to the currents, or nearly so, the sections shown in Figures 53, 54 might be good enough. These sections, which are comparatively cheap to build, can be used for groynes or training dams which are likely to be shrouded with silt after a few years.

Figure 56 shows the Mustapha breakwater at Algiers which had a reinforced concrete section upwards of 42-6 ft (13 m) depth, but it had a weak foundation. The stones in the top layer were too small and the grading was poor with little regard to the size of the fine sand underneath it. The washing away of this foundation must have been one of the causes of the collapse of the breakwater in 1934.

The harbour piers of Ymuiden (Figure 57) are protected against the waves by means of large concrete blocks. Though these blocks have large pores through which the wave currents wash freely, there is a fairly efficient layer of small rip-rap as a foundation protecting the sand underneath. Though the grading was far from correct no serious damage has occurred, but blocks have had to be added because they sank into the sandy bottom, a sign that sand was being washed away from under the layer of rip-rap.

Vertical sea walls like the one shown in Figure 58 (Scheveningen) are built to protect the higher part of the shores against storm waves. These vertical walls have to withstand earth pressure from the back and therefore should be made stable. They also have to withstand the huge forces of the storm waves. They must not be undermined by the waves, and they must, therefore, have a foundation well below the lowest level of the beach, or they must have a wide stone revetment or 'toe' in front of them. In addition, large groynes are usually necessary to protect the beach and the foundation of the sea wall.

Figure 59 shows a cheaper method of protecting the higher part of the shore by avoiding the vertical walls. The cross section must be sufficiently streamlined.
There is no earth pressure and the waves do not exert such tremendous forces on the construction, so the concrete slab which has to withstand the attack of the storm may be fairly thin, but the toe should be well cared for lest it becomes undermined. There is always the danger that large holes may form beneath the concrete slabs; the sand should, therefore, be very well tamped before the concrete slabs are poured. The toe of the protection illustrated in Figure 59 is well below the beach level, and the beach itself is protected by large groynes. The waves on this coast (the Belgian coast) are not very large.

Figure 60 shows a mixture of steep and other slopes; the cross section has no simple streamlines. The slope of the sand stands almost vertical at places and the wall protecting this vertical sand is only a thin slab. It is no wonder that the waves proved too strong for this structure. The toe is not extended to a low level, but the beach is protected by long and strong groynes.

The question whether to use natural stone or concrete for the revetment is an important one in countries where good natural stone is expensive.

Concrete slabs, poured in situ or placed by cranes, do not seem to have a great future, as holes may be expected underneath them and the slabs may break. Factory made concrete blocks with hexagonal or square forms are being used more and more for five main reasons:

1. They are often cheaper than good stones.
2. They need no keying, as the blocks can be put very close together.
3. The underlayer, therefore, can be fine gravel, shell, or light debris.
4. They can be placed by almost inexperienced labour in a third of the time; this reduces the cost greatly.
5. They can be made with top surfaces of varying height, so that the waves will break on them, and friction may diminish the uprush of the waves by about 10 per cent.
6. The sides of the concrete blocks can be made in such a way that any block is anchored by the adjacent blocks.

The concrete must be resistant to sea water and have a crushing strength of 7,000 lb/sq in (500 kg/sq cm). The water absorption should be under 8 per cent and the density 144 lb/cu ft (2.3 kg/cu dm). These figures can be obtained by vibrating or tamping methods.

Blocks for moderate wave attack can be about 3 ft × 3 ft × 1.5 ft (1 m × 1 m × 0.5 m) with a hole in the centre for handling. The joints between the concrete blocks can be filled with asphalt. There are also two different types of interlocking concrete block revetment in Holland, both protected by patents.

There must be a good layer of debris or gravel underneath any revetment in which these blocks are embedded.

The newest development is in the more extensive use of asphalt to the exclusion of stone. In Harlingen (Holland) a breakwater was constructed in 1949, the cross section of which is shown in Figure 61. The sand for the core was pumped, the length of the breakwater is 2,952 ft (900 m), the height of the top above mean sea level is 23 ft (7 m), the slopes are 1 : 4 on the sea side and 2 : 5 on the harbour side. The thickness of the bitumen-sand slab is 10 in (0.25 m) and on the most exposed part 16 in (0.40 m). Above mean sea level the bitumen-sand mixture...
was poured *in situ*, below that level cranes or other devices put pre-fabricated asphalt slabs into place. The method is definitely cheaper than stone construction, especially when stone has to be brought from a considerable distance. The cost of this first breakwater was 2,000,000 guilders (£200,000 roughly) for 900 m.

![Figure 61: Breakwater at Harlingen](image)

**LAND RECLAMATION**

Material provided by cliffs receding by erosion may make possible the gaining of much fertile alluvial land. There are three ways of gaining new land:

1. land accretion by using natural means
2. pumping dredgings into a swamp or lake
3. pumping a lake or sea shore dry.

*Land accretion by natural means*

Land accretion can be stimulated in several ways but generally only a small percentage of the total amount of suspended material in the coastal water is retained. The principle of all methods is to make silt settle by producing still water conditions by stopping currents and wave action as far as possible.

*Use of plants—Local plants are easy to obtain and may give sure results when their habits are known sufficiently. Proof of satisfactory growth under varying conditions is needed and it may be necessary to carry out trials in different places over many years. *Spartina Townsendii* is the best pioneer plant for temperate regions. It will grow in salt, brackish and fresh water but the results are best in brackish water. In fresh water rushes or other plants may give better results. Reed is an economic product; there are hundreds of species and it may be possible to select or develop a kind which may grow at a low level. *Spartina* eats up much of the nitrate in the soil so should only be used as a pioneer; it cannot withstand a severe winter.*

Where plants do not thrive because of too much turbulence in the water, planting in rows in the direction of the strongest currents or waves can be tried.

In quiet water the rows can be planted perpendicular to the main current or small waves, and these rows of plants, called living dams, will provide shelter between them and allow the silt to settle.

*Silt trenches—If there is too much wave action along a coast for plants to grow, the age-old method is to dig small trenches (1 ft × 1 ft) which form a grid pattern of about 10 ft × 200 ft (3 m × 60 m). The silt settles in these trenches and by redigging them once a year or more often the small areas are heightened to a level where plants can grow. The method gives a fine homogeneous soil. Thousands of acres have been gained in this way along the coast between the Zuider Zee and the Weser.*

*Small dams—Dams or embankments are expensive; even when very small ones are proposed preliminary experiments should be made over a long period. Gaining new land in the quickest and most economical way is an almost lost art in which Vierlingh, dikemaster to William the Silent,*
exceeded. His method was to use local material and but little stone. He said that 'with small bricks you can build a castle,' meaning that with small means we can gain much new land, provided we put our whole intelligence and art in it.

In Germany (Schleswig) and Holland (Groningen and Friesland) large sums are being spent to make shelter by means of willow-filled dams or breakwaters about 6 ft (2 m) high and one to two ft (0·5 m) wide, giving a grid pattern with areas of 1,300 ft × 1,300 ft (400 m × 400 m). Ice often destroys the hearting of these small breakwaters and the soil it gives is rather heterogenous. Economy is out of the question in many places.

High dams or causeways—Sometimes a railroad or a highway is made across an estuary and this causeway creates quietness in the water. Land accretion on both sides may occur, but generally on one side only. The North Frisian islands (Germany) have been connected by means of large dams with the continent. In 1878 the Dutch island of Ameland was connected with the shore, a distance of about 5 miles (8 km), the object being to gain land, but the dam breached soon afterwards, because it was not high enough. The storm piled the water at the western side up to a great height and at the eastern side the water was totally blown away, so that the western water washed over the dam. The top of a dam of this type should be made well above the storm floods plus wave heights, and a road can then be made upon it.

Further gains resulting from land reclamation (Figure 62)—When 10 per cent at the land end of the fill basin of an estuary is reclaimed the streams in the rest of the estuary diminish; about 10 per cent at the mouth, and much more near the land end. If there is silt and sand in the water the cross sections of the estuary will therefore diminish and the shores will show natural accretion, because the size of the channel is a function of the fill basin. The action of silting in an estuary is progressive. This action, also called the 'method of pinching an estuary from behind,' is quite natural, but it can be accelerated by man, either by planting plants or by pumping parts of the estuary dry.

Narrow rivers and rather narrow ship channels are to be preferred to wide ones. Wide waters show wild, unstable features; the waves are bad for inland shipping; the embankments have to be made extra high because of big waves; and the salt penetrates far into the country because salt and fresh water mix, especially in wide estuaries. There is another advantage in making wide estuaries narrow, namely, the gaining of fertile marine soil.

Gains resulting from channel improvements—When in a network of tidal channels some channel is improved for navigational purposes, another has its currents slackened, mostly to such an extent that it will partly silt up.

Gains resulting from dredging—When the main channel of an estuary is deepened, the breadth of the estuary will decrease in a natural way when there is any sand and silt suspended in the water.
Reclamation by using dredging spoil

Dredging spoil is often used to heighten a low shore in order to create a new town district or harbour terrain. In Germany it was a custom before the war to pump all dredging spoil ashore in order to make either new agricultural land or new building sites. This is called ‘making work with work’. On the river Scheldt about 5,200,000 cu yd (4,000,000 cu m) are dumped annually in the estuary itself. It seems to be a cheap way but some or perhaps much of this sand is added to the circular sand movements. Therefore the ‘cheap’ way may in reality be expensive considering that the dredging may go on endlessly when dumping nearby.

Reclamation by pumping out lakes (Figure 63)

This is often the most economic way of gaining new land. Land accretion is slow and generally requires more capital expenditure and interest charges than the new land can bear. The method becomes costly especially when artificial constructions are necessary to make the silt settle. Formerly labour was less expensive than it is now and much land could be gained by making silt trenches or by using one of the other means mentioned on p 1102, but now that machines have become abundant and more economic, pumps can be used. Often when the methods of land accretion are used, the new polder takes the shape of a segment needing a long expensive embankment to protect it (for a relatively short time only). The pumping method, as used in the Zuider Zee, is much quicker and often requires less capital expenditure per 1,000 acres.

The question of the degree of fertility of the soil then arises. Another problem is whether the existing foreshore or sea bottom, if infertile, can be made fertile. Here agricultural experts are needed. Perhaps there is a layer of clay at some depth which can be brought up with a special machine; such machines exist already for layers at a depth up to 10 ft (3 m). Perhaps there is clay in the neighbourhood which can be transported, and so on. The new soil should not be too clayey. An amount of 20 per cent of silt in the top layer (grains smaller than 20 µ) is often considered to be the best soil, but a committee of experts in Holland recently came to the conclusion that for the upper layer of 2 ft (0·6 m) a content of silt of only 12 per cent was as good. One of the main factors in fertility is to regulate the height of the ground water with extreme care, and to keep this water fresh.

The necessary amount of clay can be shipped while the water is still in the newly formed lakes. Another good method is to make the enclosure some years in advance and leave a breach in it so as to attract the marine silt and make it settle in the new polder during these years. Later on, when sufficient silt has settled, the breach is closed. When 12-20 per cent of silt is sufficient for a layer of 2 ft (0·6 m), a layer of fine silt, 4-6 in (10-15 cm) thick suffices. A layer of 8 in (20 cm) would not harm but a thick layer of clay would harm. However, most clay contains 50 per cent or 70 per cent of sand.

Now that artificial manure is used extensively, sandy soils become more valuable, but the disadvantage of too sandy soil is that it may be blown away. Grass, bulbs and woods can be grown easily on sandy soils.

The planning of large pumped polders can be much better than the planning of the small segment formed polders. The roads, villages, canals, schools, churches etc can, and should, be made before the population moves into the polder. Land reclamation on a large scale is usually a government job.

Land has a private economic value (selling value) and a public economic value. In a well populated country the latter is much higher than the former because the land supports not only the owner but the whole community as
well. It is the public economic value of land which must be taken into consideration when planning a new polder to be added to the country.

**Land reclamation by making sand dikes (Figure 64)**

Near the sea, blown sand can be caught by means of rows of fir boughs or reeds, height about 3 ft (1 m). In the course of a few years high dunes can be made in this way with little cost. Sand dikes have been made in Holland for several centuries, and much new silt land has grown behind them. The method is simple and inexpensive provided that the situation of the sand dike is well chosen. The new sand dikes have to be fixed with marram grass and other dune vegetation. Here the botanist's advice should be sought.

Figure 64. Brushwood hedges for sand dunes

Rabbits and holiday makers are the worst destroyers of dune vegetation. Literature about land gaining is rather old, which shows that this fine art is being neglected. Perhaps the best book about land gaining is still VIERLINGH's *Tractaet of Dyckagie*, written about 1570.

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